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Photonic Encryption: Modeling and Functional Analysis of All-Optical Logic

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Photonic Encryption: Modeling and Functional Analysis of All Optical Logic

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Abstract

With the build-out of large transport networks utilizing optical technologies, more and more capacity is being made available. Innovations in Dense Wave Division Multiplexing (DWDM) and the elimination of optical-electrical-optical conversions have brought on advances in communication speeds as we move into 10 Gigabit Ethernet and above. Of course, there is a need to encrypt data on these optical links as the data traverses public and private network backbones. Unfortunately, as the communications infrastructure becomes increasingly optical, advances in encryption (done electronically) have failed to keep up. This project examines the use of optical logic for implementing encryption in the photonic domain to achieve the requisite encryption rates.

This paper documents the innovations and advances of work first detailed in "Photonic Encryption using All Optical Logic," [1]. A discussion of underlying concepts can be found in SAND2003-4474. In order to realize photonic encryption designs, technology developed for electrical logic circuits must be translated to the photonic regime. This paper examines S-SEED devices and how discrete logic elements can be interconnected and cascaded to form an optical circuit. Because there is no known software that can model these devices at a circuit level, the functionality of S-SEED devices in an optical circuit was modeled in PSpice. PSpice allows modeling of the macro characteristics of the devices in context of a logic element as opposed to device level computational modeling. By representing light intensity as voltage, "black box" models are generated that accurately represent the intensity response and logic levels in both technologies. By modeling the behavior at the systems level, one can incorporate systems design tools and a simulation environment to aid in the overall functional design. Each black box model takes certain parameters (reflectance, intensity, input response), and models the optical ripple and time delay characteristics. These "black box" models are interconnected and cascaded in an encrypting/scrambling algorithm based on a study of candidate encryption algorithms. Demonstration circuits show how these logic elements can be used to form NAND, NOR, and XOR functions. This paper also presents functional analysis of a serial, low gate count demonstration algorithm suitable for scrambling/encryption using S-SEED devices.

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1. Introduction

As existing transport networks evolve into intelligent all-optical networks, end-to-end connections are beginning to look like virtual fibers. The elimination of optical-electrical-optical (OEO) conversions within network equipment allows for a vast increase in network capacity due to enabling technologies such as dense wavelength division multiplexing (DWDM). This is an important trend for Sandia and the DOE complex due to the increasing need to interconnect high performance computing and visualization platforms, often in a "network protocol agnostic" fashion. However, as signaling and switching technologies progress towards an all-optical architecture, network encryption technology, which remains in the electrical domain, fails to keep pace. Because network encryption is paramount to the Sandia/DOE mission, the lack of encryption mechanisms for all-optical networks seriously limits our ability to utilize these exciting new technologies and to reach bit rates currently not viable under electronic methods.

Over the past five years, Sandia has been developing all-optical devices that perform Boolean logic functions on optical inputs and produce optical outputs without intermediate electrical conversion. These all-optical logic gates are built upon two distinct technologies – self electro-optic effect devices (SEED) and gain competition technologies. These devices form logical building blocks suitable for a designing a photonic encryptor. However, optical logic gates are just now maturing into a state of discrete operation and have yet to be demonstrated in monolithic arrangements and present a few limitations (e.g., limited cascade depth, fanout, etc.) when applied in an encryption algorithm.

We are developing a technically feasible design for a photonic encryptor that is based on a simple, but useful encryption algorithm that can be built within the limitations of the SEED and/or gain competition devices. The encryptor will be able to process an optical data stream with known characteristics and will exhibit scaling properties to bit-rates unreachable through traditional OEO methods. By designing a set of Boolean logic elements with all optical logic, we can use them in conjunction with low gate count encrypting/scrambling algorithms to demonstrate an all-optical encryptor. Because there is no known software that can model these devices at a circuit level, we have modeled the functionality of the SEED and gain competition devices in an optical circuit in PSpice. PSpice allows us to model macro characteristics of the devices in context of a logic element as opposed to device level computational modeling.

This project has examined cryptographic algorithms in detail and determined innovative implementation approaches that can be implemented within the constraints of current optical logic gate technology. In addition, novel encryption approaches that utilize other photonic properties (e.g., dispersion, polarization, etc.) that may be modulated by these devices are also being explored.

2. Photonic Encryptor Usage

Figure 1 shows the photonic encryptor designed under this project, and how it fits into a generalized photonic network architecture.

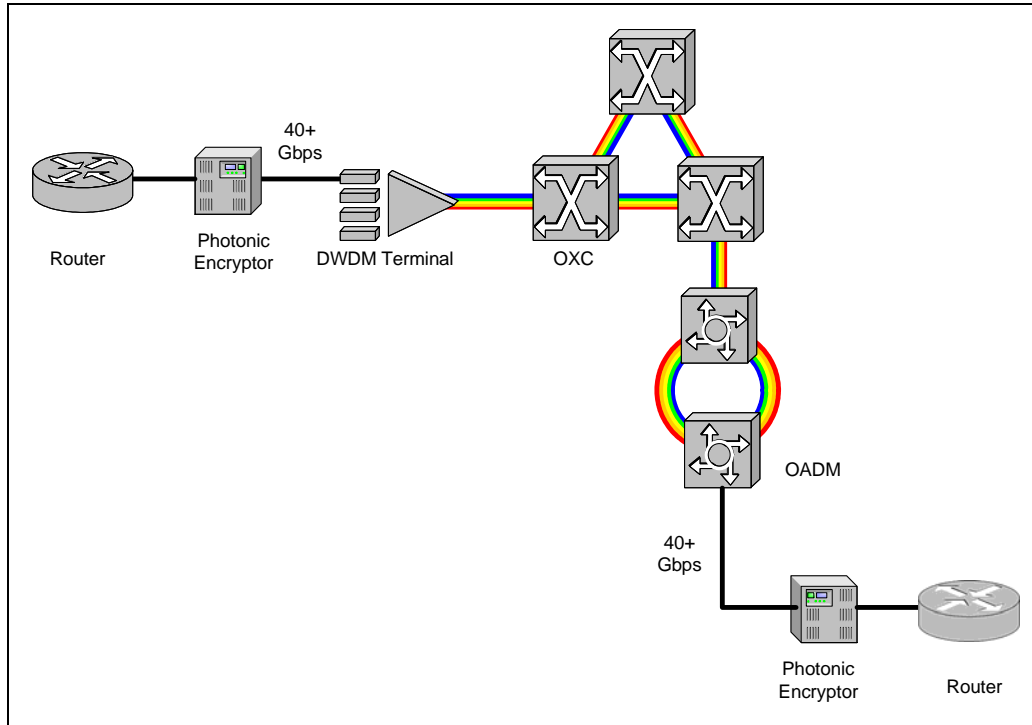


Figure 1: Photonic encryptor placement in all-optical network

In general, a photonic network may consist of the following components:

Dense Wave Division Multiplexer (DWDM)

This device takes multiple inputs with known wavelengths and framing protocols, wavelength-converts the inputs, and multiplexes the converted wavelengths onto a single fiber. These devices are typically connected to each other via a single, point-to-point connection.

Optical Add-Drop Multiplexer (OADM)

This device takes a single input with known wavelength and framing protocol, wavelength-converts it, and multiplexes the converted wavelength onto a single fiber that carries other wavelengths. In the de-multiplexing direction, this device isolates a single wavelength from a collection of wavelengths and converts it to a specified wavelength on the output interface. These devices are typically connected to each other in a ring topology.

Optical Crossconnect (OXC)

An OXC is an all-optical switch. As such, it isolates a wavelength on its input port, wavelength-converts it, and multiplexes it onto the output port. These devices can be interconnected in an arbitrary mesh.

The photonic encryptor designed in this project operates on a single wavelength with known framing protocol, as shown in Figure 1. Therefore, it is meant to connect to the input/output of a DWDM terminal or an OADM. Although techniques for broadband (multi-wavelength) encryption were considered, they were rejected for the following reasons:

Asynchronous key stream and data stream. In general, the data channels on each wavelength in a WDM network are not synchronized with each other. Therefore, a single key stream that would encrypt all wavelengths at once would be asynchronous with the data on all of the wavelengths. This is a departure from conventional cryptographic techniques, in which the key stream is synchronous with the data stream, and could present cryptanalytic challenges that this project is not prepared to accept.

Possibility for sub-rate encryption. Encryption of an arbitrarily formatted data stream with unknown bit rate could lead to a situation where the bit rate of the data stream is faster than the bit rate of the key stream. This results in re-use of key stream, which is taboo from a cryptanalytic perspective. This situation is likely for broadband encryption, as devices that can switch or operate on multiple wavelengths (e.g., micro-mirrors) are typically too slow to switch at the rates required for encryption of 40+ gigabits per second.

Wavelength constraints of photonic logic. Although other devices (e.g., micromirrors, chaotic mode-locked lasers, etc.) were considered, the speed requirements for this project called for the use of photonic logic. However, these devices operate at fixed wavelengths (usually 850 nm).

For the reasons listed above, the encryptor is designed to operate on a single wavelength with known protocol. Furthermore, the encryptor is designed to transparently pass an optical path [2]. However, the optical framing protocol that is encrypted might have overhead information (e.g., for OA&M purposes) that must bypass encryption. If so, then techniques such as those developed for optical label swapping can be used to suppress encrypted headers and substitute plaintext header information [3]. Other techniques for processing optical headers are also possible [4].

Although the single wavelength with known protocol restriction may appear to limit the encryptor's usefulness in photonic networks, it is actually a realistic configuration that would have interesting application in high speed communications. One can easily envision subscribing to a carrier's wavelength service, where the framing protocol and rate are known, but are beyond the capabilities of today's electrical domain encryption devices. By implementing photonic encryption at the point of presence, bulk encryption can be realized. Furthermore, it is expected that the techniques developed for photonic encryption will facilitate scaling of encryption data rates more readily than today's electronic implementations.

3.

PSpice Modeling

3.1. PSpice Model

Our PSpice Model is similar to the Advice model presented by Lentine [5]. Like Lentine, a fifth order polynomial has been used to characterize the optical absorption of the p.i.n diode as a function of reverse bias voltage. However, Lentine chose to characterize the device as a three terminal device, with the diode terminals (cathode and anode) being two terminals and the third being the optical input. The PSpice model presented here characterizes the SEED as a four terminal device, two electrical and two optical. From the standpoint of the simulator, all terminals are electrical. The optical inputs and outputs are simply ideal electrical terminals where 1 V electrical potential is equivalent to 1 mW optical power at the device.

3.2. Diode Electrical Model

The PSpice model is shown in Figure 2. The basic p.i.n. photodiode is modeled by a capacitor and parallel current source, G1. A lookup table is used to model the current versus voltage characteristic of the device (see Table 1). These values were taken from measured data. As can be seen in Figure 3, the piece wise linear model does a fair job of modeling the complex curve.

The diode model also contains a series resistor and series inductor whose values were derived experimentally. [6]

3.3. Responsivity Curves

The photoelectric currents are generated by each of the four beams that shine on the device. A and B are logic inputs, C is the clock input and P is the preset input. The gain for each is light input is modeled by a linear fit where the responsivity in the discharged state (approximately -0.5 V reverse biased) is .45 A/W and in the charged state (approximately +1.5 V reverse biased) is .35 A/W. The resulting line is shown in Figure 4 and the linear fit equation is

$$R_{es} = .425 = .05V_r.$$

3.4. Reflectivity Curve

The reflectivity varies with the diode reverse bias voltage and can be represented quite accurately by a fifth order polynomial. This curve has been fitted to digitized data from an actual device in Figure 5. The data is given in Table 2. The equation is given by

$$R = 5.72 + 2.06X + .28X^2 - .665X^3 + .042X^4 + .057X^5.$$

3.5. Gate Operation

The data is read out using a clock beam, C. The output light, Z, is determined by multiplying the incoming light level by the reflectivity value, R.

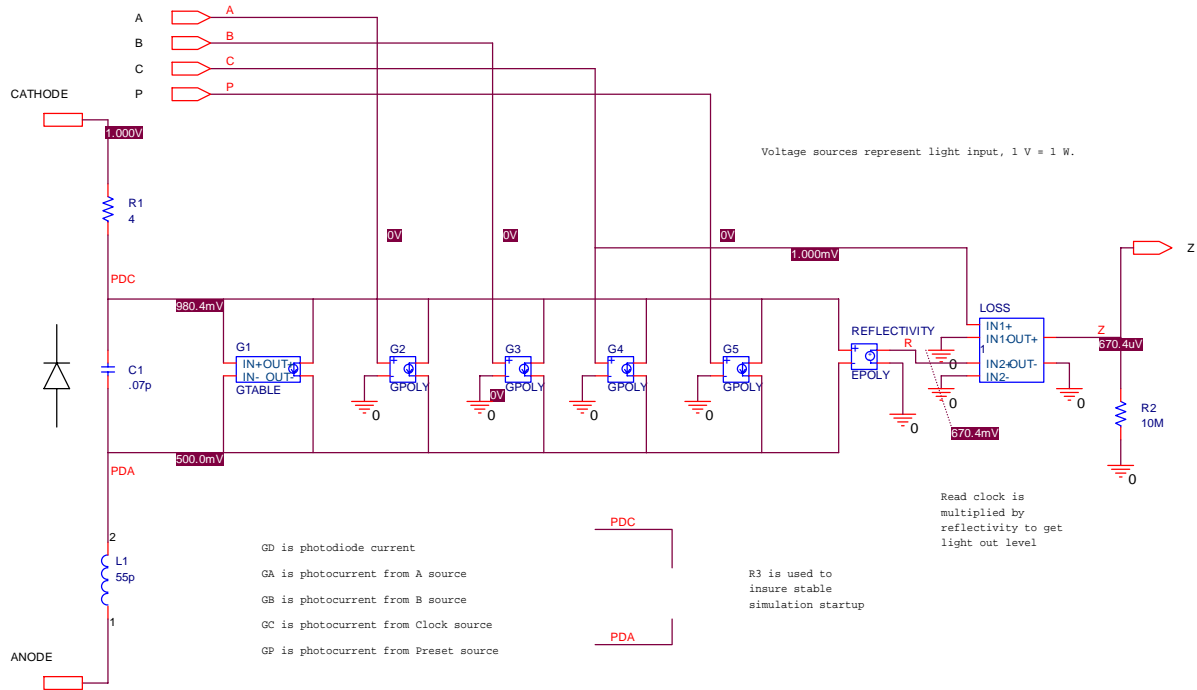


Figure 2: Schematic of SEED Model

Table 1. Measured SEED current versus voltage for input to model.

Reverse Voltage (V)	Reverse Current (mA)
-0.8254	0
-0.8254	0.80851
-0.824	1.617
-0.80952	2.2979
-0.79365	3.3191
-0.78	3.7021
-0.75603	4.0851
-0.74016	4.4255
-0.71828	4.7234
-0.71428	4.9362
-0.66667	5.1489
-0.63492	5.234
-0.60317	5.2766
-0.53968	5.3191
-0.47619	5.3191
-0.44444	5.2766
-0.39682	5.234
-0.25397	5.1489
-0.031745	4.9362
0.19048	4.766
0.44445	4.5106
0.66667	4.3404
0.90476	4.1702
1.1429	4.0426

1.3651	3.9574
1.6825	3.9149
1.9841	3.8723

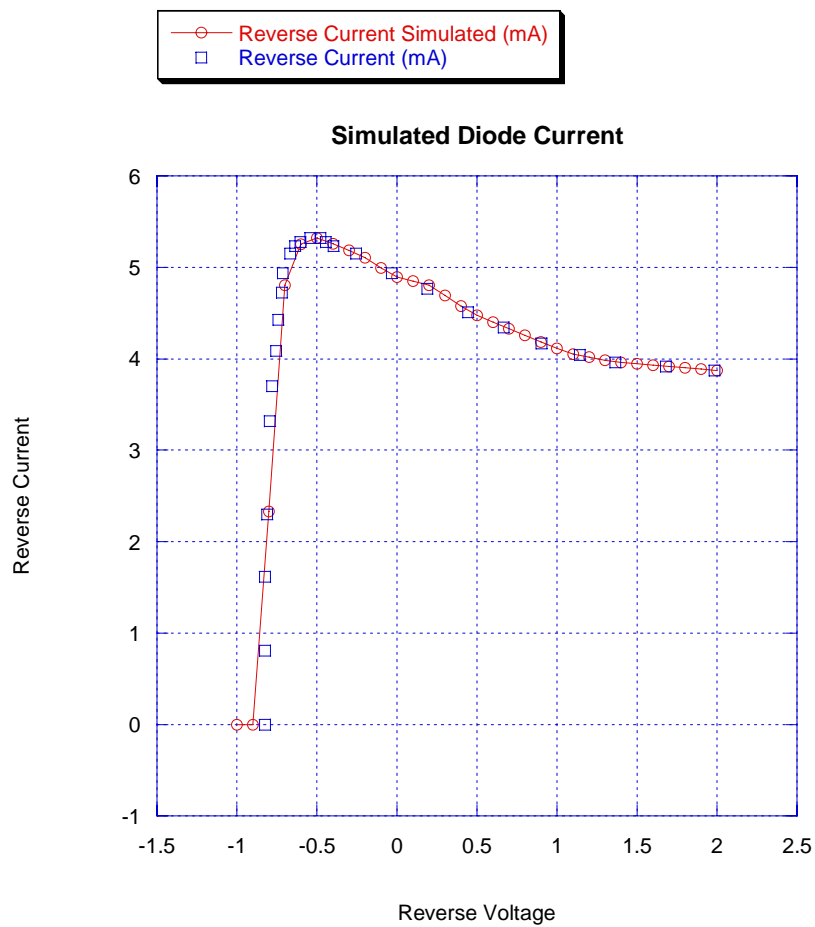


Figure 3: Simulated vs. measured p.i.n. diode current.

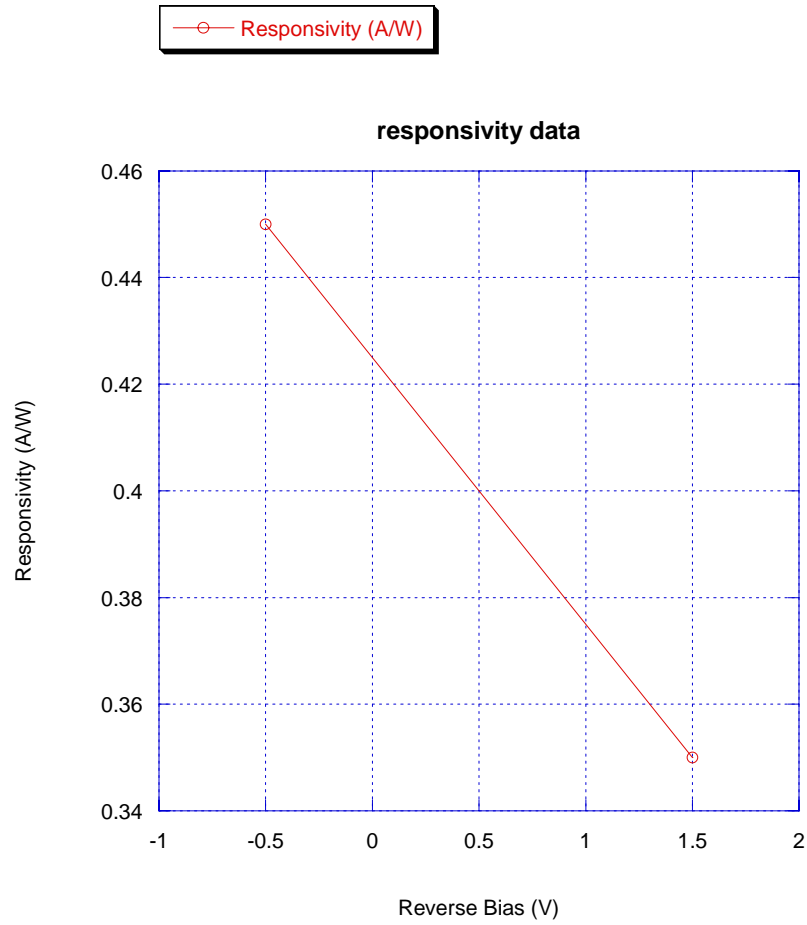


Figure 4: Responsivity curve.

Table 2. Measured reflectivity versus reverse voltage data.

Reverse Voltage (V)	Reflectivity (a.u.)
-1.00000	4.5714
-0.88889	4.5714
-0.82540	4.6032
-0.69841	4.6667
-0.60317	4.7302
-0.49206	4.8571
-0.39682	4.9841
-0.31746	5.1111
-0.25397	5.2381
-0.15873	5.3651
0.015874	5.7460
0.15873	6.0317
0.20635	6.1587

0.28572	6.3492
0.39683	6.5714
0.50794	6.7619
0.60318	6.9524
0.68254	7.0794
0.76191	7.2063
0.87302	7.3333
0.98413	7.4603
1.1111	7.5873
1.2222	7.6825
1.3492	7.7778
1.4762	7.8413
1.6667	7.9365
1.8889	8.0635
2.0000	8.1270

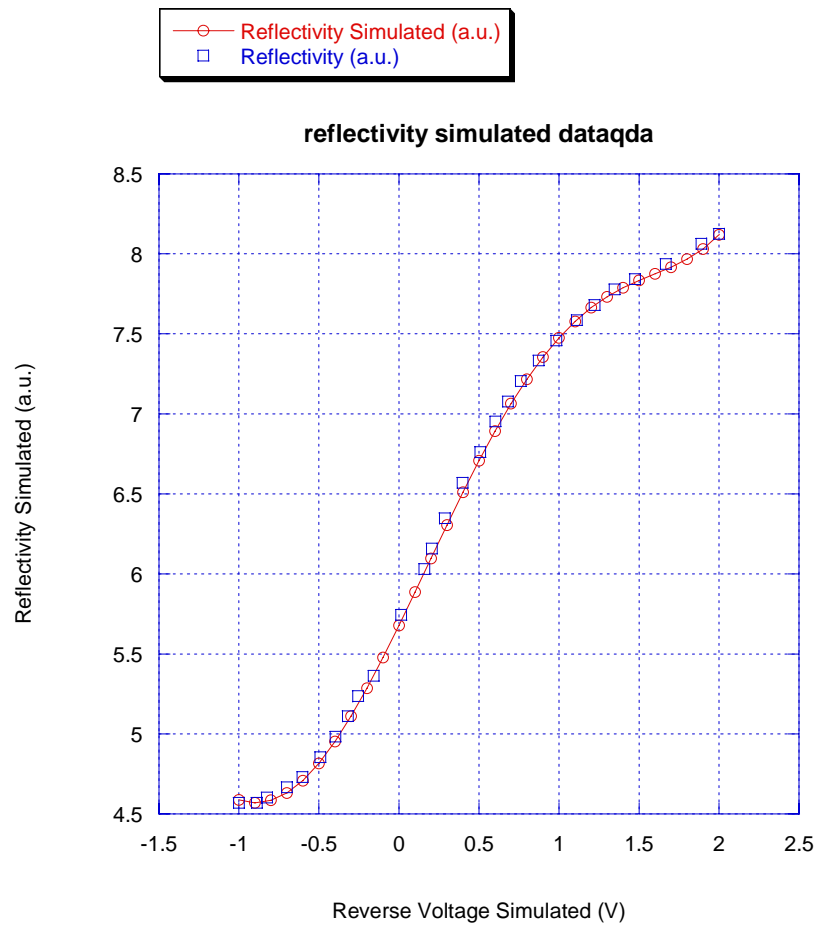


Figure 5: Reflectivity simulated data vs. measured.

4. S-SEED Switching Behavior

The switching characteristic of the S-SEED device was reported in a progress report [6]. The rise time of the S-SEED was 7ps with a settling time of over 75ps. The actual device is shown in Figure 6. The rise time was measured in Figure 7.

4.1. S-SEED Circuit

The circuit consists of two series SEED diodes (p.i.n. diodes are the two circular devices at the bottom of the picture) connected in parallel with a capacitor (the rectangular device at the top center of the picture) which was sized to provide transient current during switching. The two terminals were connected to a 1 V dc power supply. The PSpice schematic is shown in Figure 8.

4.2. Measurement Setup

The measured circuit has a train of light pulses, Pu1 and Pu2, which are shining on D1 and D2 respectively, at a 76 MHz rate. Pu1 and Pu2 are created from a common pump laser. Pu2 passes through a 1.8 meter delay line and arrives at the target delayed by 6 ns with respect to Pu1. Both pulses are vertically polarized by passing through a beam splitter. In operation, Pu1 discharges D1 and Pu2 discharges D2 6 ns later. In this way, the state of the logic gate is toggled continuously. The same beam splitter is used to create a horizontally polarized read signal, Pr1, which is itself delayed with respect to Pu1. The read signal is much smaller in intensity than either of the pulses so that it does not upset the state of the logic during the test. The read pulse is only applied to D2. The timing of these pulses is shown schematically in Figure 9.

4.3. Simulation Setup

The simulated circuit operates as follows. A 1 ps wide pulse, Pu2, is incident on D2 and discharges D2. The voltage across D2 approaches 0 V and, at the same time, the voltage on D1 approaches 1 V. A second 1 ps wide pulse, Pu1, is incident on D1 and discharges D1, thus switching the state of the circuit. The period between pulses is 200 ps. A constant read signal is applied to D2. The reflected output power of the circuit, POUT, is divided by the input power, Pr2, and scaled (by a factor of 10) resulting in a reflection coefficient measurement. The resultant waveforms are shown in Figure 10 and 11.

The output waveform has considerable ringing due to the series inductance in the device interconnect. By adjusting some of the model parameters, we can improve the device performance. For instance, if the series inductance is reduced from 55pH to 5pH, then the settling time improves from 100 ps to less than 10 ps. This also improves the rise time from over 5 ps to around 2 ps. There are two areas to target when reducing the series inductance in this experiment. First, the leads from the power supply probes can be shortened. Second, the interconnect between the two SEED devices can also be shortened. Building the circuit with an airbridge interconnect and widening the traces could lower the inductance.

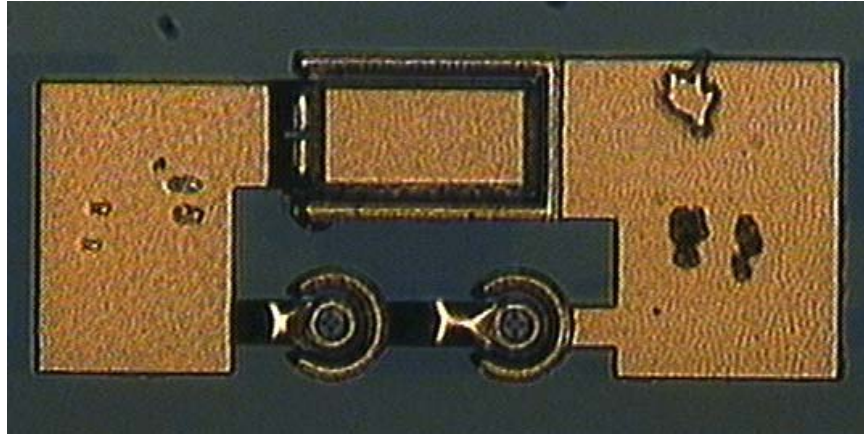


Figure 6: S-SEED photo.

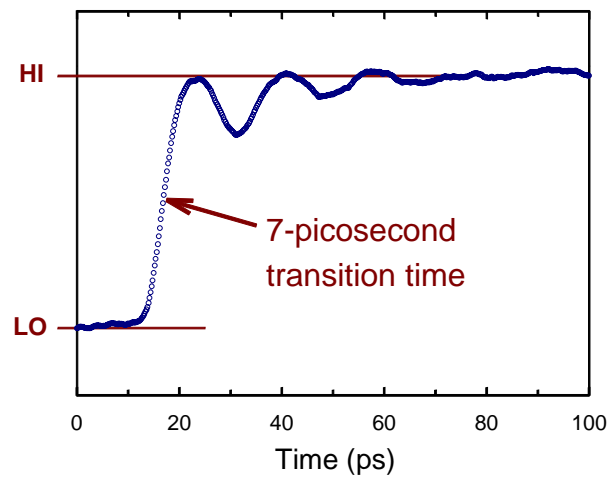
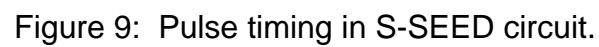


Figure 7: S-SEED switching characteristic.



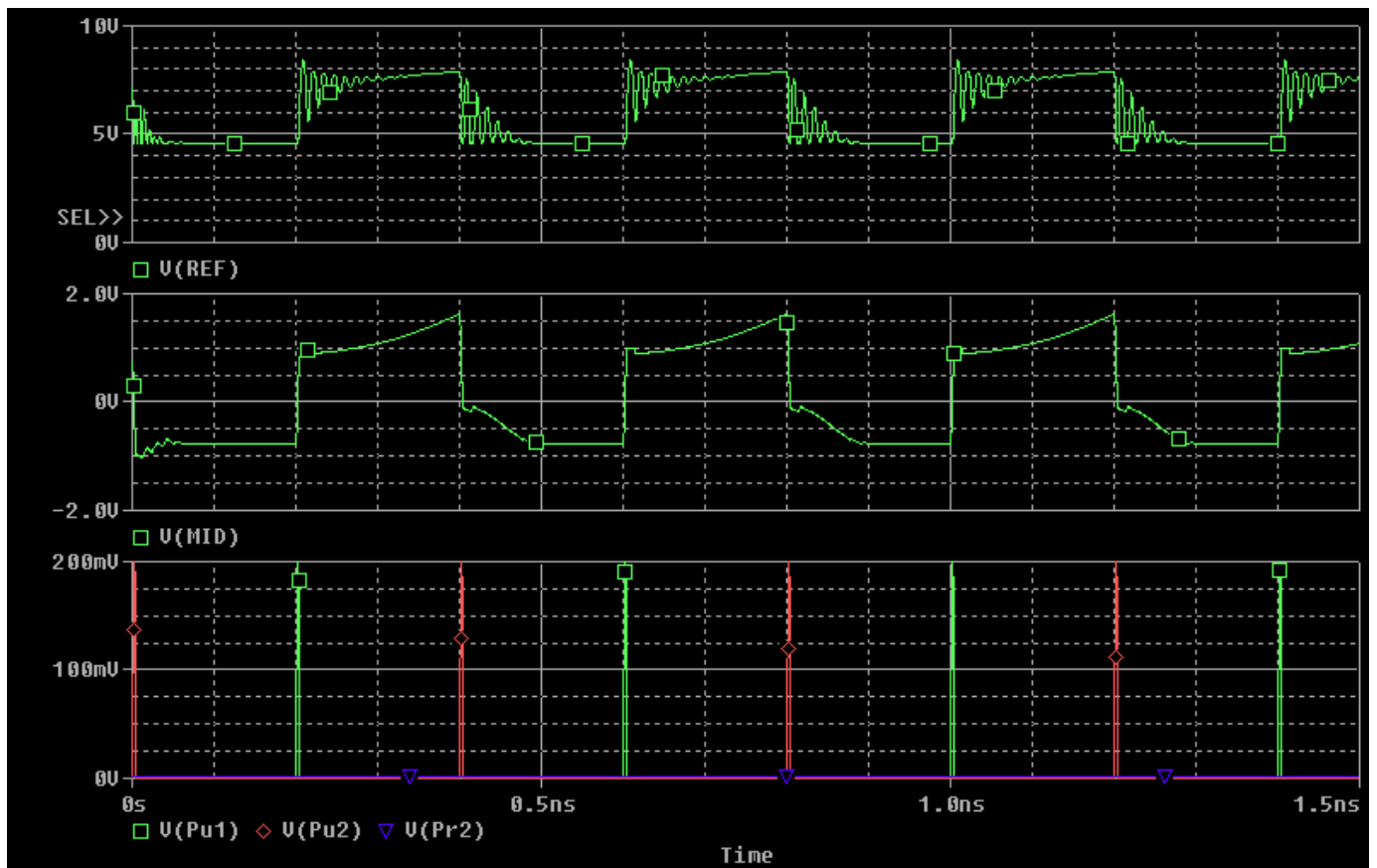


Figure 10: Switching speed simulation waveforms.

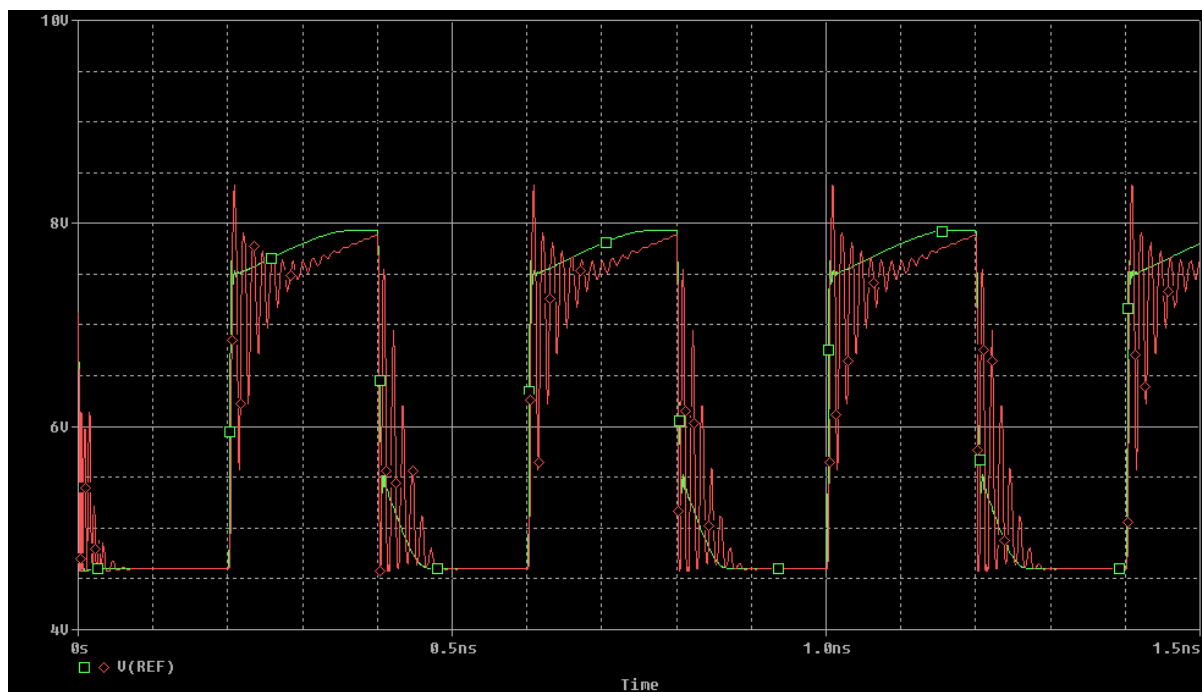


Figure 11: Effect of reducing series inductance.

5. Characterization of the Optical Gate

Each digital logic gate will have a transfer characteristic and switching characteristic that describes the output waveform in terms of the input. In the case of the optical SEED logic gate it is more difficult to measure because the input and output signals are pulses of light. A series of simulations were used to measure the switching and transfer characteristics.

The simulation consists of an OR gate configuration (similar to Figure 18) with a single data input. The schematic is shown in Figure 12. The Preset input is used to discharge D1 (charging D2) and raising the voltage on MID. The data input, D, is pulsed to a maximum value which switches the gate and the magnitude of the output pulse is measured at POUT and POUTB during the clock pulse. The DB input (invert of D) has a maximum value that is $.5625 * D_{max}$. This value represents the extinction ratio of the optical gate. The reflection of the clock input, C, is a function of the diode bias voltage ranging from a minimum of $.45 * C$ to $.8 * C$. Since D is the true logic value, DB should be relatively dimmer by the extinction ratio.

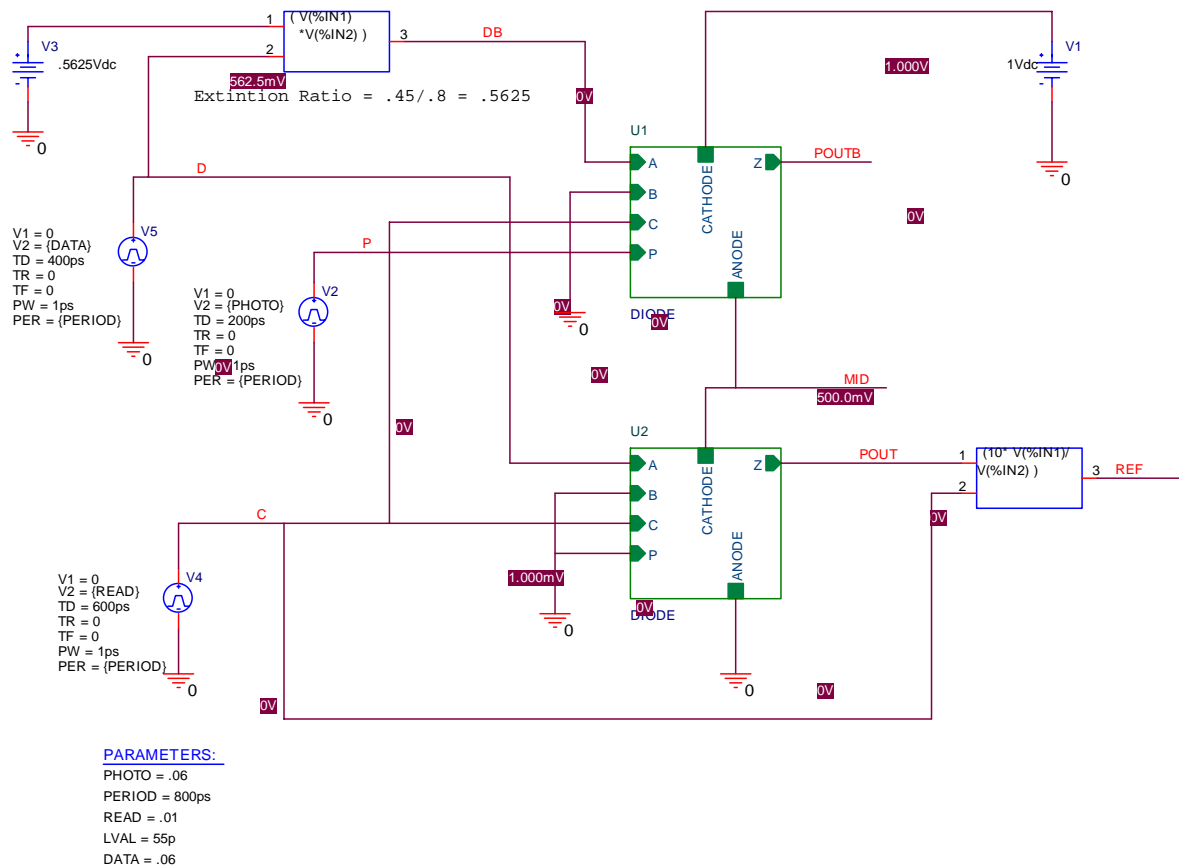


Figure 12: SEED Logic gate transfer characteristic schematic.

The circuit in Figure 12 was used to characterize the switching of the optical logic gate. The P input was used to alternatively switch logic states. The voltage on the electrical output MID varied from a high of 1.75V to a low of -0.75V. Depending on the amplitude of the input pulse, the signal exhibited overshoot. The input pulse was varied from 20uW to 70 uW and the rise/fall time of the pulse was measured. These values are given in Table 3. The goal was to find a pulse height that would generate just enough current to charge the alternate capacitor (of the diode) without having too much current and overcharging the capacitor. The result was that the 60 uW pulse appeared to have the fastest switching time without

excessive overshoot exhibited with larger pulses. All pulses were 1ps in width. The switching characteristic of the MID node for 60 uW pulses is shown in Figure 13. This was the chosen pulse magnitude for future circuit design.

Table 3. Optical gate switching speed.

Pulse Height (uW)	Rise Time (pS)	Fall Time (pS)
20	no switch	no switch
30	no switch	no switch
40	100	100
50	33	32
60	23	23
70	20	20

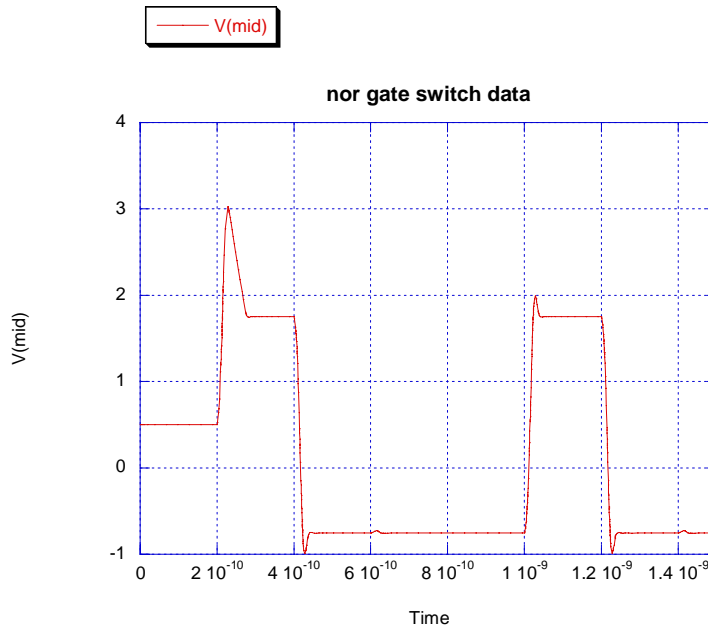


Figure 13: NOR gate switching with 60 uW pulses.

An actual logic input switches the gate differently than a preset pulse because the pulses are generated by previous logic gate for which the inverted and non-inverted outputs do not turn off completely. The low output is only 45% of the clock input while the high output is 80% of the clock input. An extinction ratio of about 56% is the result. Therefore, another series of simulations were performed to characterize the switching of the gates logic state by real optical inputs.

For a 60 uW pulse height on data and clocking inputs, we simulated the amount of preset needed to effectively “set” the state of the SEED device. We swept the preset pulse energy from 10 uW to 90 uW. Again, the switching characteristic for the MID node was examined with the goal of having enough current

to charge the capacitor yet not overcharge it. The resulting data in Figure 14 shows the least amount of overshoot on $v(\text{mid})$ that effectively “presets” the state of the device was 32uW.

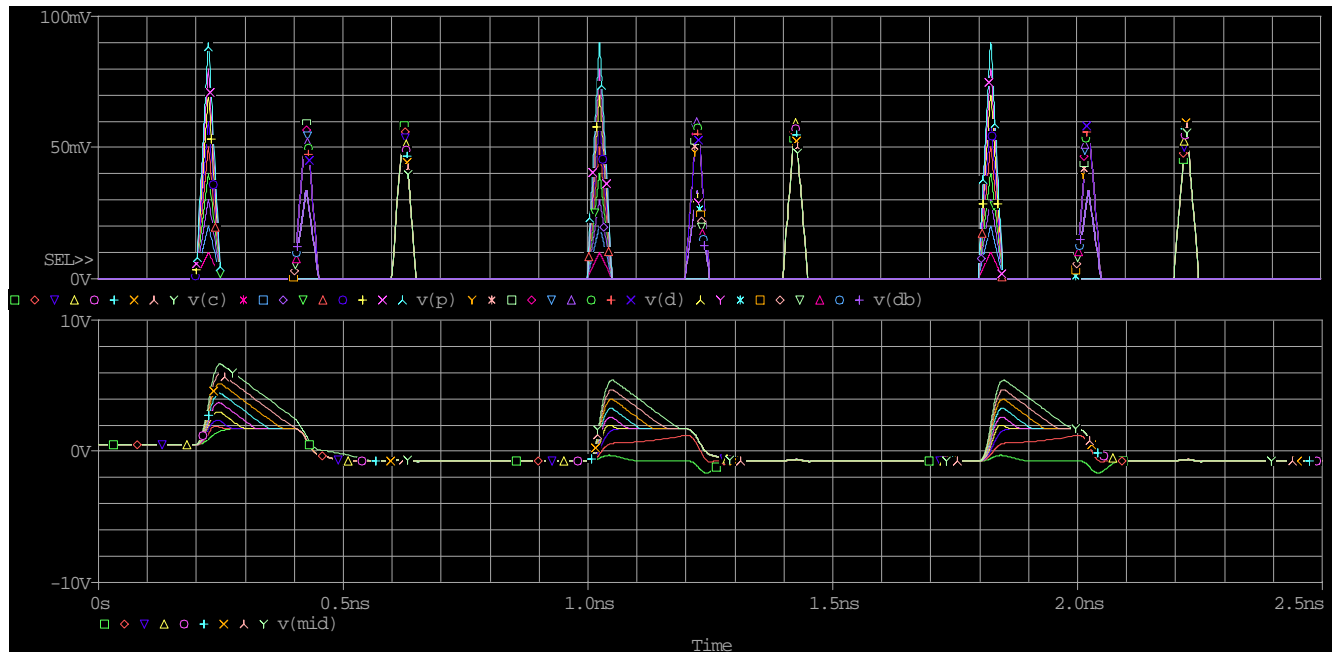


Figure 14: Switch point simulations

A preset height of 40 uW was used in future designs. Now that we determined how much preset was required to set the state of the device, we varied how much clock power was needed to read the state and effectively set the state of the next cascaded device. We used 40 uW of preset and swept input power from 50 uW to 90 uW. The constraint was that the amount of output power had to be at least 32 uW. The result in Figure 15 showed that at least 75uW of clock power is needed to adequately cascade into the next stage and “set” the next gate. Future design and simulations will use minimum preset, data, clock powers of 40 uW, 32 uW, and 80 uW.

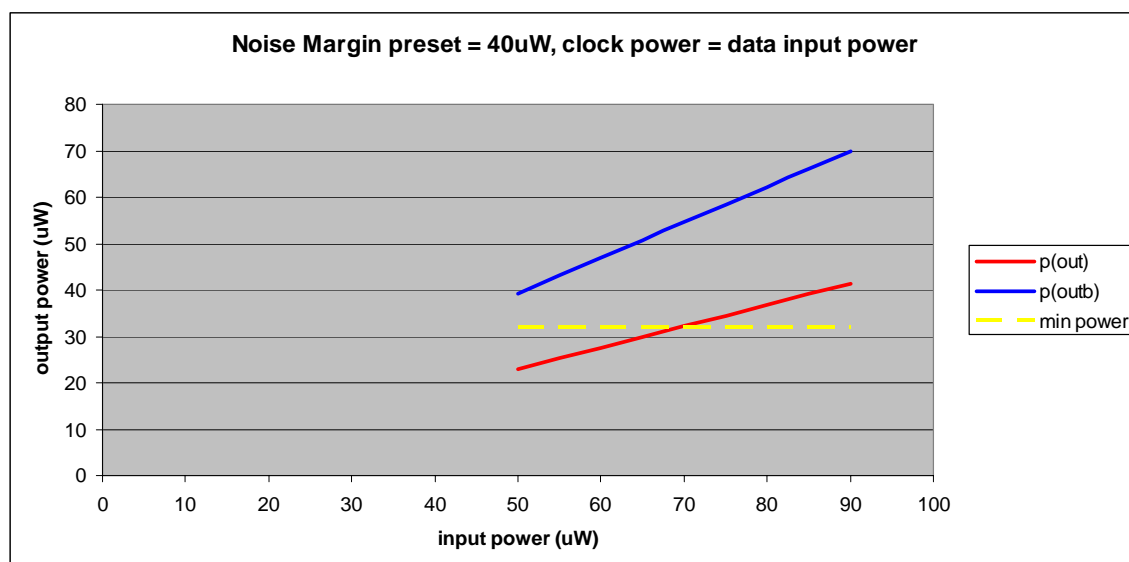


Figure 15: Simulation rules for input/output power.

Extinction Ratio = $.45/.8 = .5625$

PARAMETERS:
 PHOTO = .08
 PERIOD = 300ps
 READ = .08
 LVAL = 55p
 DATA = .08
 FALL = 15ps
 RISE = 15ps
 PW = 1ps

The timing diagram displays three digital signals over a 5ns period. The vertical axis represents voltage in Volts (V), ranging from -4V to 12V. The horizontal axis represents time in nanoseconds (ns), ranging from 0s to 5.0ns. The signals are:

- V(MID2)+5 (Red line with diamond markers):** A square wave oscillating between approximately 3.5V and 7.5V.
- V(MID3)+10 (Blue line with inverted triangle markers):** A square wave oscillating between approximately 8.5V and 11.5V.
- V(MID1) (Green line with square markers):** A square wave oscillating between approximately -1.5V and 2.5V.

The signals exhibit complex timing relationships, including phase shifts and varying duty cycles, which are typical for digital logic analysis.

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6. Optical Logic Gate Simulation

A simple two input optical gate was designed and modeled from the S-SEED device models. The schematic of an OR gate and an AND gate are shown in Figure 18 and Figure 19 respectively. The two diodes are connected in series with a 1 V power supply in reverse bias. Inputs A, B, AB, BB, C and P and outputs Q and QB are optical inputs and outputs simulated by PSpice as voltages where 1 V = 1 μ W optical power. Inputs AB and BB are inverted versions of the inputs A and B. MID is the electrical node connecting diodes D1 and D2.

The optical logic gate operation is based on a three phase clocking scheme shown in Figure 20. The following describes the operation of the OR gate. In the first phase, the logic of the gate (OR) is set using the P input. The P input will discharge D1 and charge D2. The voltage on node *MID* will rise toward VCC. In the second phase, the logic inputs (A, B, AB, BB) are applied to the two diodes. Unless both AB and BB are ON, the gate will not switch from the initial state set in phase 1. This performs the logic function. In phase three, the C input is applied to both diodes, and the light reflecting from the Q (charged diode) indicates the resulting of the logic function. The clock input is equal on both diodes and will not switch the state of the gate by itself. The simulated output of this logic gate is shown in Figure 21.

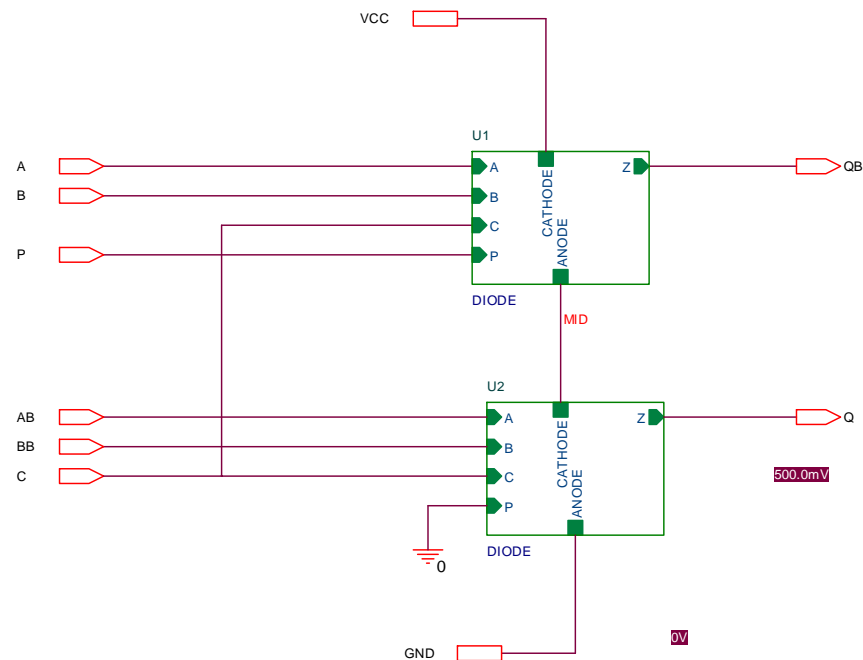


Figure 18: Two input optical OR gate.

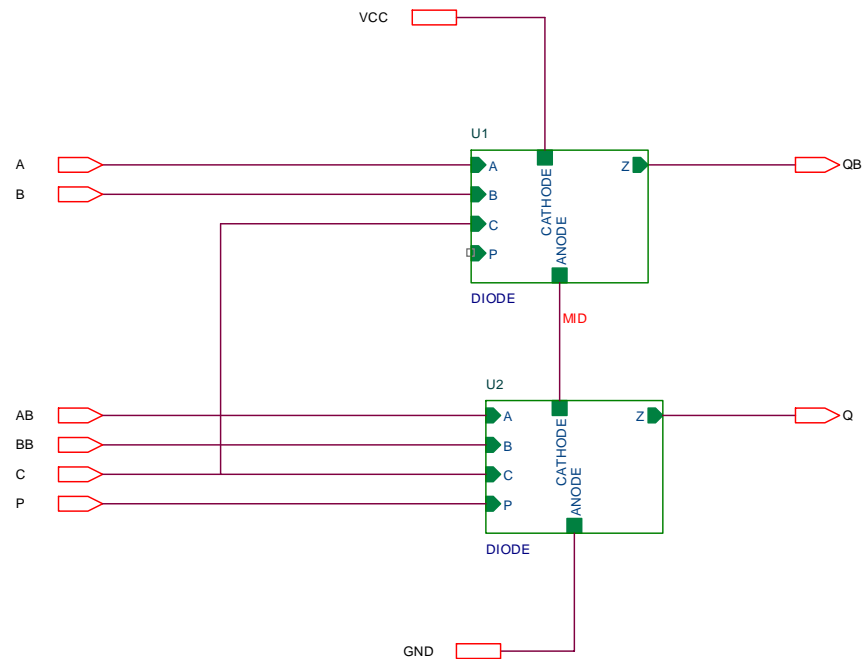


Figure 19: Two input optical AND gate.

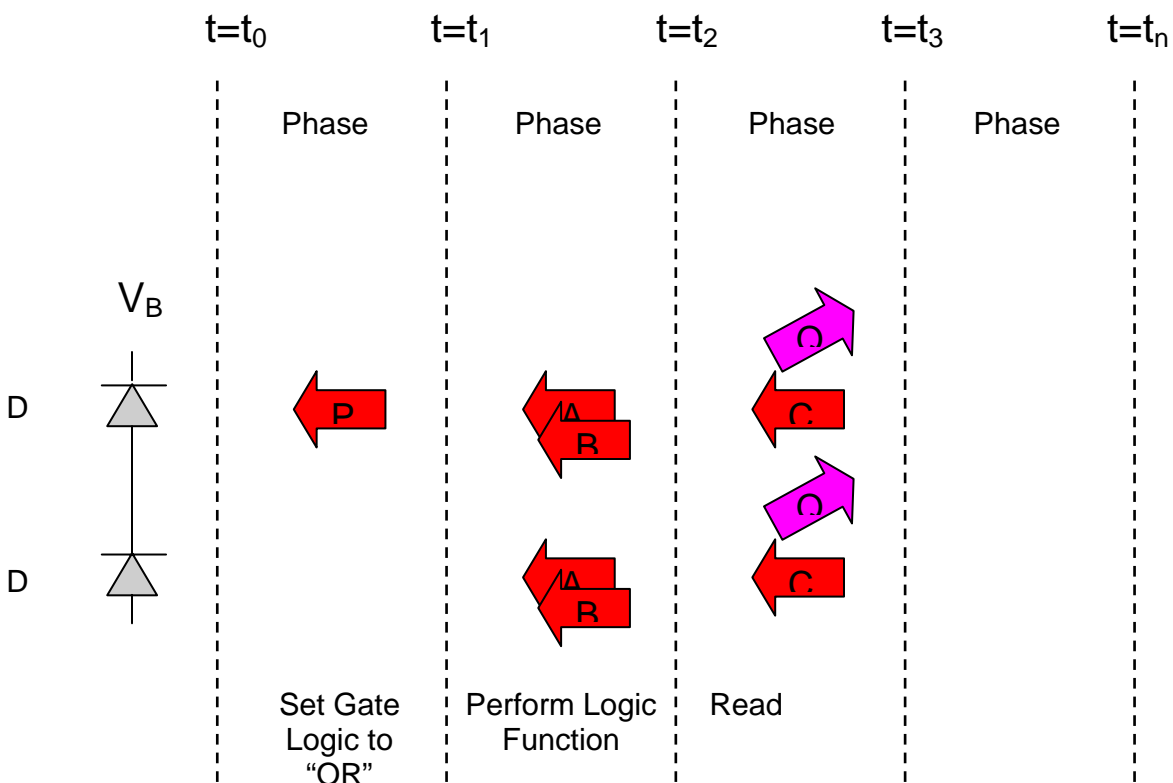


Figure 20: Three phase logic diagram.

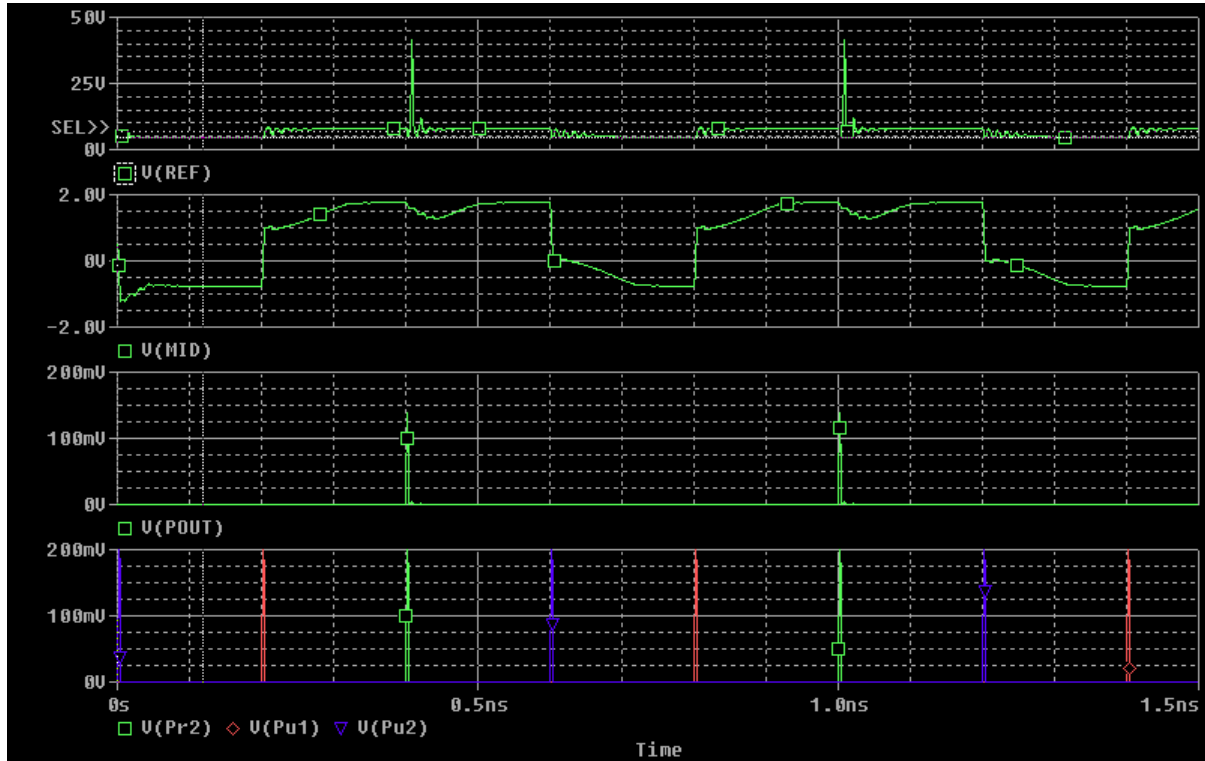


Figure 21: Simulated photonic logic gate operation.

In order to demonstrate AND, OR, and XOR gate functionality, we built a two bit counter that delivers differential logic HI and logic LO. Figure 22 shows the functional block takes input from a piece-wise linear voltage source that describes pulse widths and heights. These inputs are then multiplied by a two bit pattern to generate 00, 01, 10, or 11 in appropriate time scale.

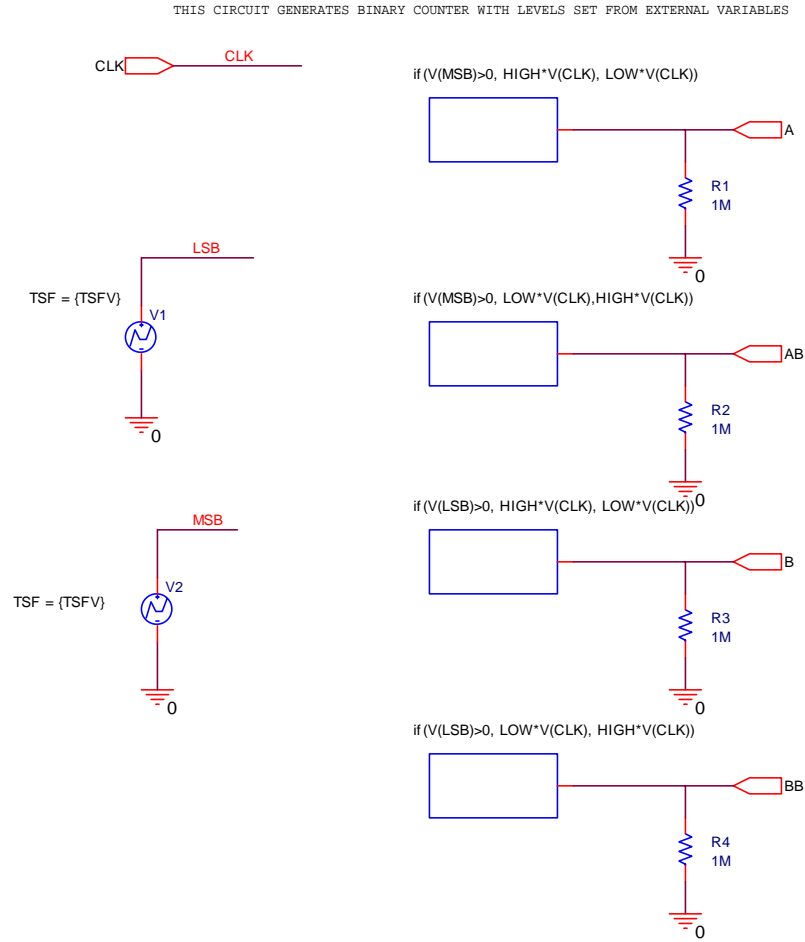


Figure 22: Two bit counter functional block

With this two-bit counter functional block, we demonstrated functional operation on AND, OR, and XOR gates in the figures 23, 24, 25, 26, 27, and 28.

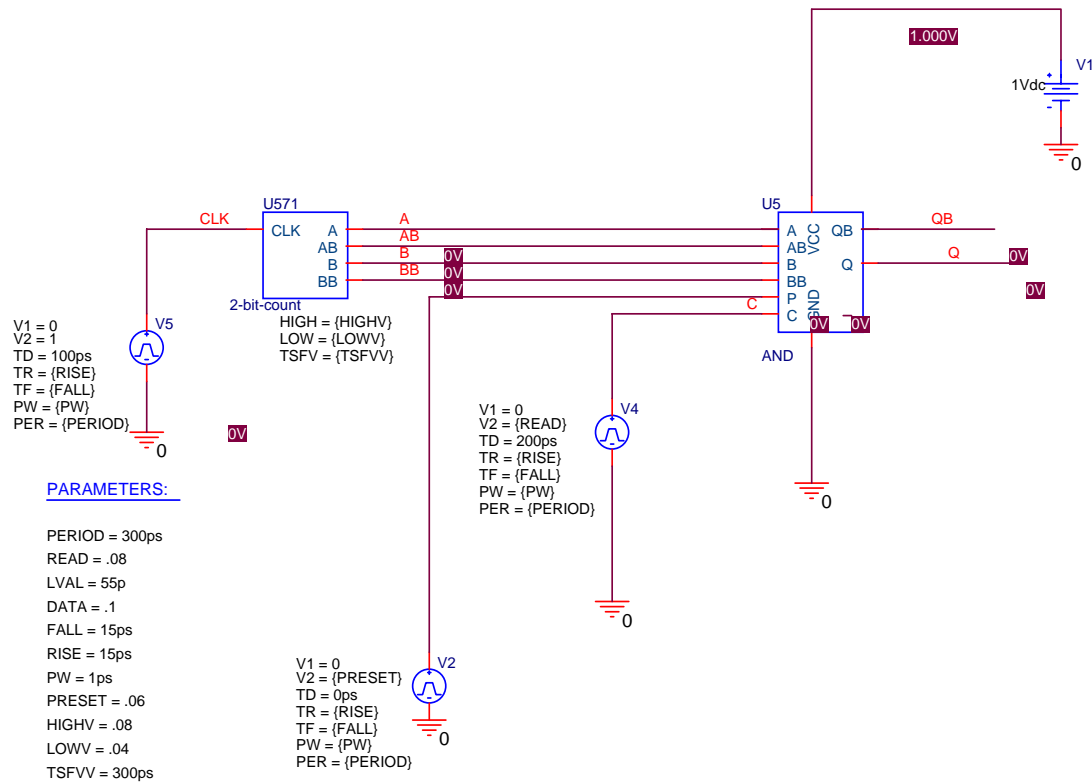


Figure 23: AND demonstration circuit

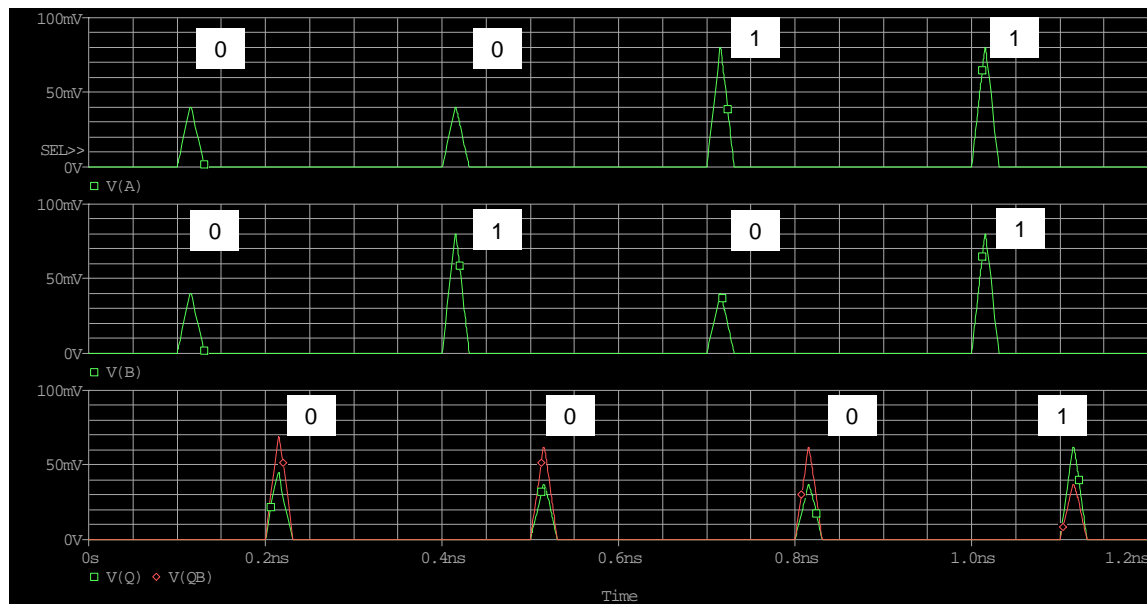


Figure 24: AND demonstration results

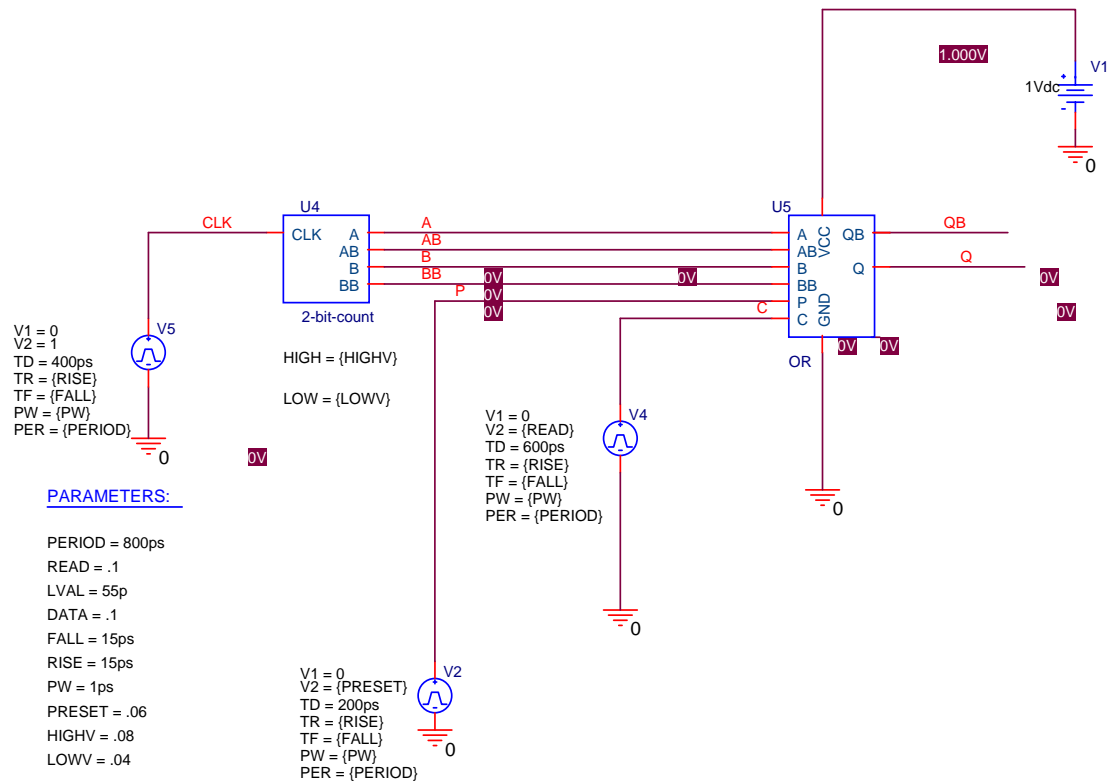


Figure 25: OR demonstration circuit

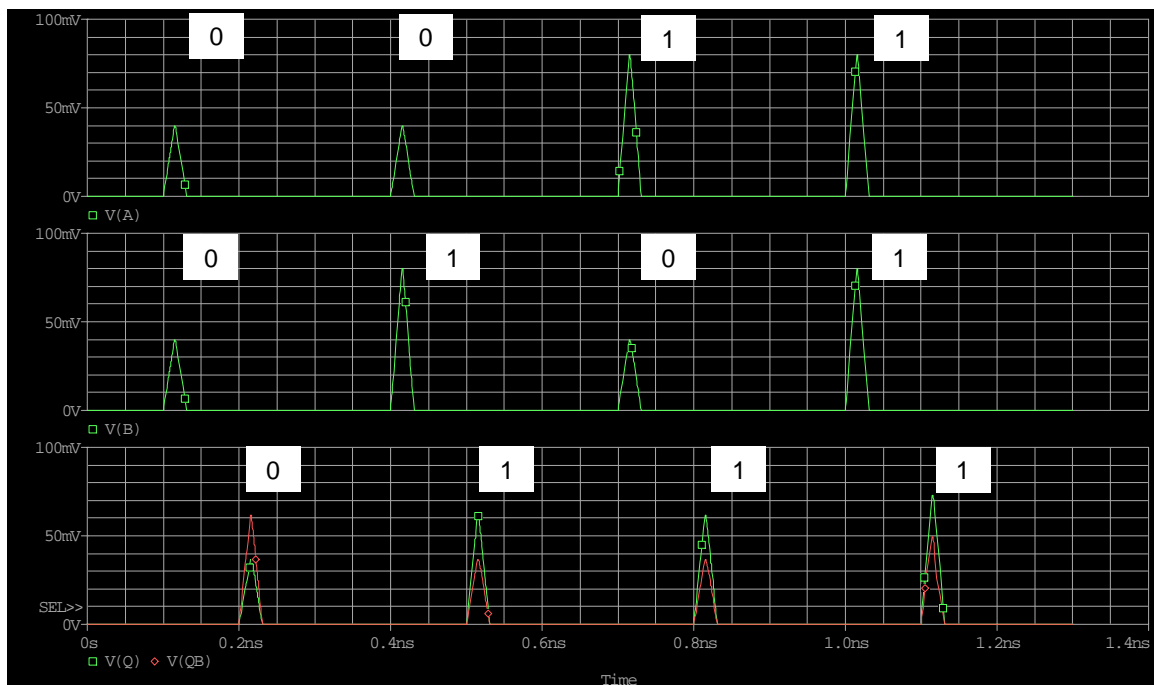


Figure 26 OR demonstration results

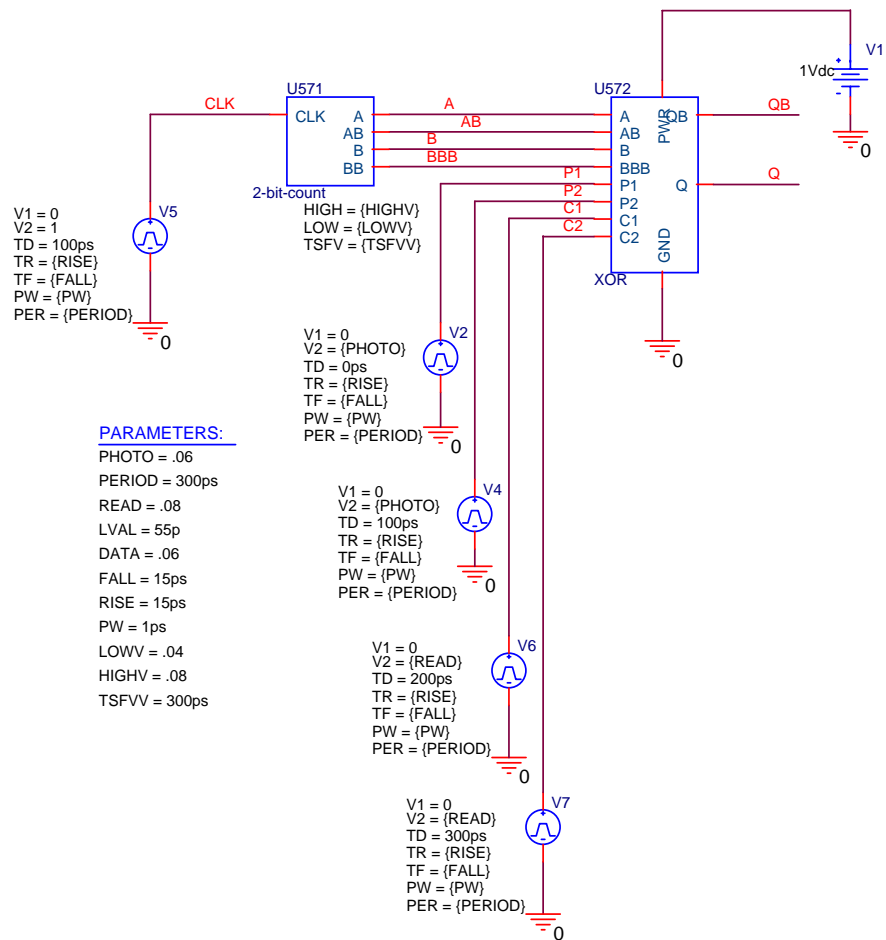


Figure 27: XOR demonstration circuit

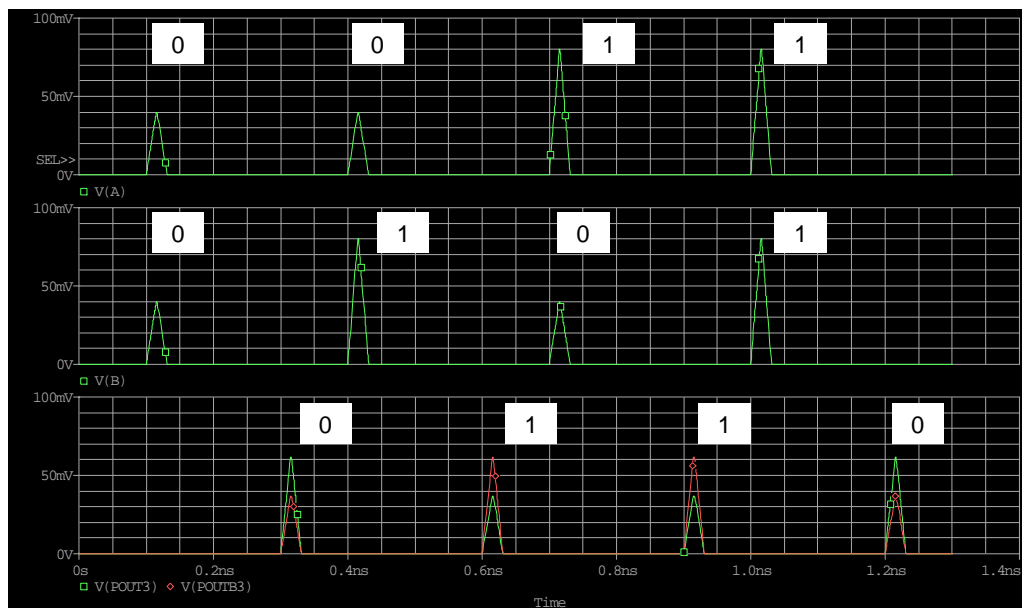


Figure 28: XOR demonstration results

7. Stream Cipher for Optical Communications Systems

7.1. Why a new stream cipher?

We examined existing ciphers, but found nothing that looked buildable within our design constraints. Existing block ciphers like AES and DES require thousands of gates to implement. The best stream ciphers contain long, stuttering, shift-registers, clocked in an irregular pattern. This style of logic seems very doubtful when contrasted with our current capabilities. While we eventually hope to implement arbitrary computation capabilities, this will be a ways down the development road. The new proposal has the important advantage of buildable. Moreover, it can be built up a little at a time, and adding additional stages should be easy.

7.1.1. The Optical Cipher Concept

The new design sends the plaintext message as a bit stream through a series of very simple ciphering boxes. The security of the system comes from using a large number of boxes. A smaller number of boxes can be used as a data scrambler.

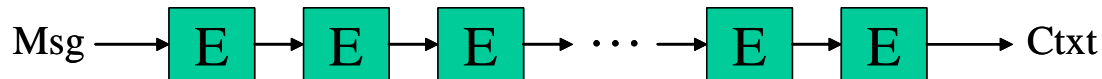


Figure 29: Optical Cipher

In the individual ciphering stages shown in Figure 29, the E-boxes perform very simple operations on the data stream. A simple logic function is computed using a few bits from the data stream, and the single-bit result is Xored into the upstream data.

The inside of an E-box is shown in Figure 30:

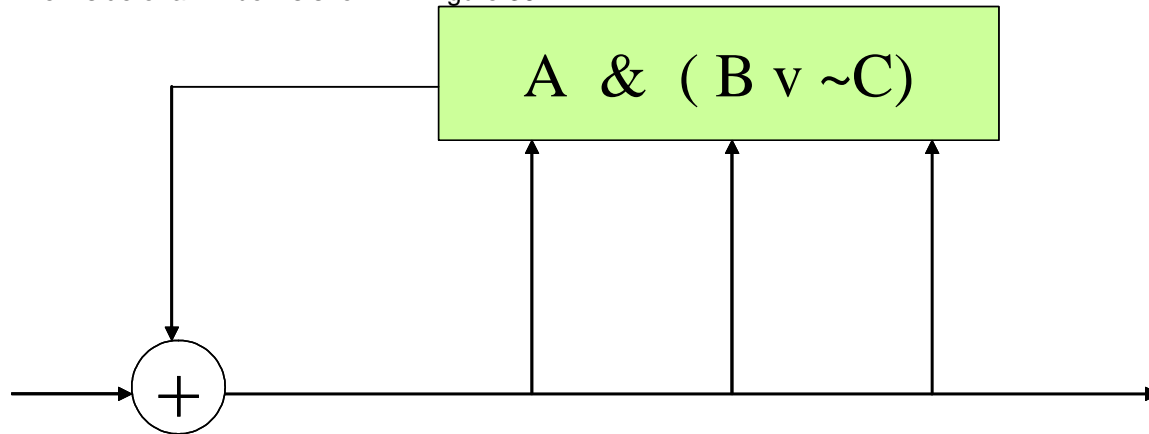


Figure 30: E-box internals.

In Figure 30, the logic function is

$$F(A,B,C) = A \text{ or } (B \text{ and not } C).$$

We will probably use a few different kinds of logic functions. In order for this to be decodable, the bits used as input to the logic function must be older than the bit to be modified, so the taps are taken from the ciphertext side.

Decryption is very similar, but not identical. There is a series of D-boxes, applied to the ciphertext. Each D-box similar to Figure 31 undoes the effect of one E-box. The D-boxes are used in the reverse order of the E-boxes.

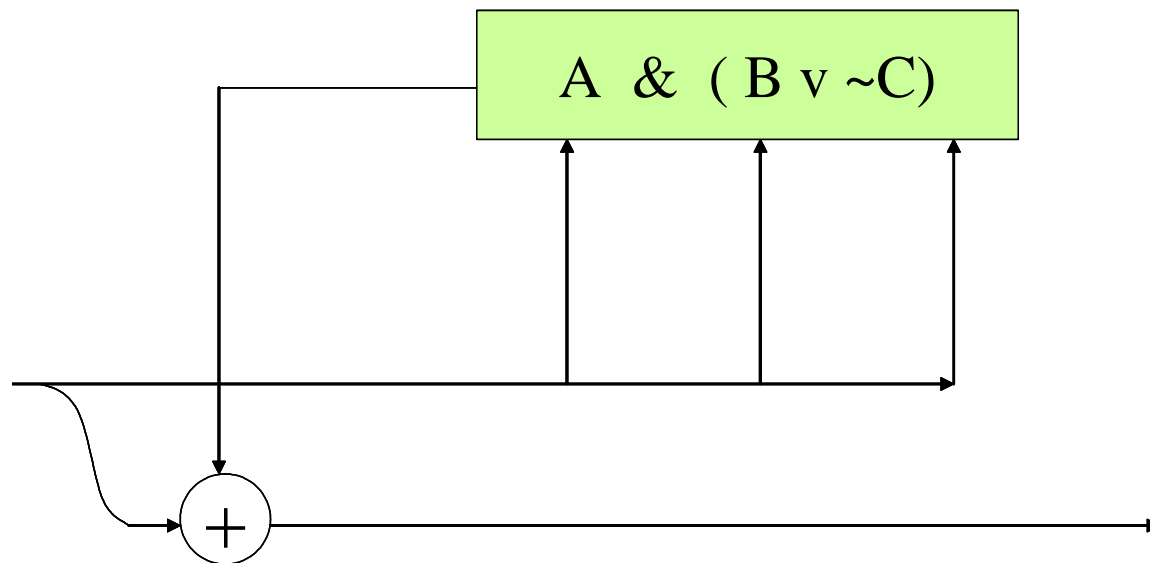


Figure 31: D-box internals.

7.1.2. Circuit Variations

There are several variations possible on the basic theme. We could use D-boxes in the Encryption chain (and match them with E-boxes in the Decryption chain). This loses the Finite-Error-Propagation property. We could also use a more complex arrangement of E-boxes, with some E-boxes wrapped around others, or with interleaved inputs. As long as the inputs to E-boxes only affect newer data stream bits, the resulting output can be decoded. However, the decoding becomes more complicated. This option complicates the device construction with no obvious improvement, so we didn't pursue it.

7.2. Keying

Keying is done by making small changes to the logic function. The inner logic function is fixed, but the inputs and outputs can be modified in simple ways. The E-boxes in the transmitter and the D-boxes in the receiver must use the same keying information.

There are lots of possible keying options as seen in Figure 32.

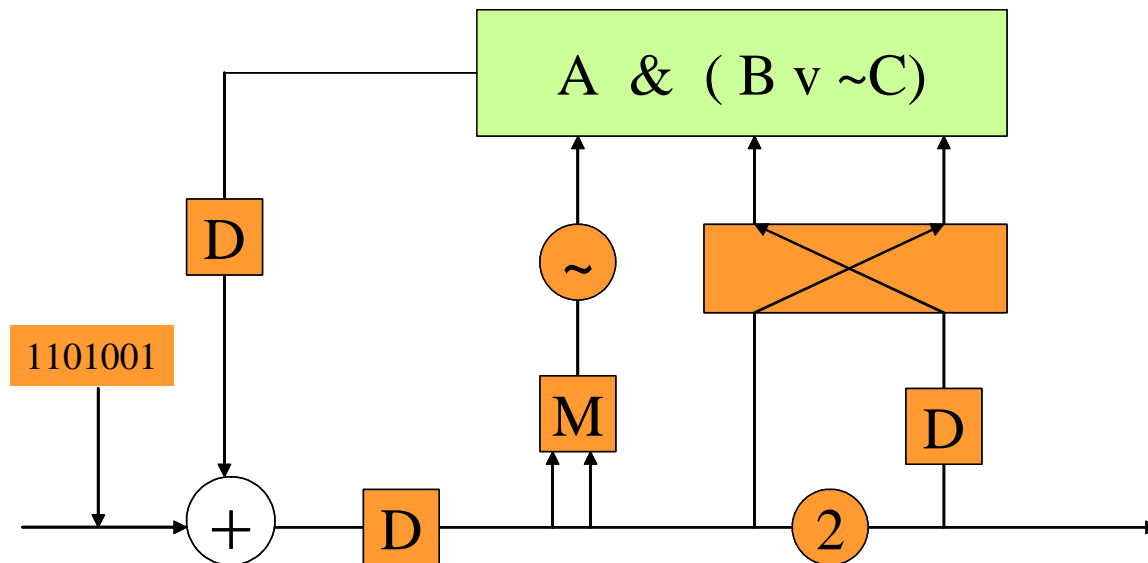


Figure 32: E-box with keying options.

In Figure 32:

D represents a delay of a few bit times;

~ is a Not gate;

Mux selects one of two inputs;

X exchanges two inputs of the logic function;

2 exchanges two bits in the data stream;

1101001 represents a random initialization vector.

In the final system, only a couple of these options will be used.

Keying is accomplished by turning these various kinds of boxes On or Off. In the Off state, they simply pass data through; in the On state, they do their particular modification. There are a few other keying ideas we considered and dropped.

These include:

- (a) using key to select from among two or more F functions; this was discarded because it means there's always unused logic;
- (b) using key to vary the data path of the encryption stream, so the E-boxes can be used in various orders. This is simply hard to build.

7.3. Keying Notes

There is an external user-supplied key. This key should be at least 64 bits for a respectable cipher, but could be smaller for a data scrambler. The key is processed by a control computer, using a hash function like SHA-1, to create (more) internal keying bits. For real encryption, there must be at least 128 internal keying bits. These bits are supplied to control the various keying options of the E-box inputs. The key can be supplied, and changed, at electrical speeds. A given key will be used for at least a second; during key switchover, a period of nano or microseconds, the output of the encryption device will be suppressed. Each module can use only about 4 or 5 keying bits, so we'll need a minimum of 25 E-boxes for encryption. More is probably better, so we might use as many as 50 E-boxes.

7.4. Finite Error Propagation

The design has the property that a transmission error will cause only a finite amount of damage to the downstream decryption. After the error has passed through the decryptor, the effects will circulate in the internal state for a while and then be damped out.

7.5. Simulator

We've written a simulator for the Encryptor. The simulator can encrypt or decrypt a data stream. The current version of the simulator can use up to 1000 E-boxes, in a fairly complicated pattern. It contains several methods of measuring the apparent randomness of a data stream. The simulator has been used in a number of experiments to try out various design details.

7.5.1. Logic Function Effectiveness

The position of the F-function within an E-box can be taken by various different logic functions. In the pictures above, we've used the function $F(A,B,C) = A \vee (B \& \sim C)$, but many other functions are possible. We are interested in evaluating the cryptographic effectiveness of different logic functions, and comparing this to the construction difficulty ("cost") of the functions. Cryptographic strength is hard to measure. We use a simple proxy measurement, suitable at this stage of our design: Statistical randomness. (Later on, as we fix more details of the design, we'll do the more difficult measurements of crypto strength.) Statistical randomness is evaluated by taking a simple input signal such as a stream of all 0s, and looking at the distribution of various patterns in the output stream.

In a typical experiment, a stream of 1,024,000 consecutive 0 bits is supplied as the input. The output is sampled with a sliding 8-bit window, and a histogram of the 256 possible output values is created. A random output will have about 4000 instances of each possible value. The difference from random is evaluated by looking at the standard deviation of the values. A sample run is shown below. This run uses 75 modules.

```
[r@fermat r]$ optenc2a 75 x x x
optical encryptor simulation
```

```
3719 4149 4106 3997 3945 3992 4070 3962
3957 4106 3937 4020 4201 3836 4147 3907
3980 4035 4193 4114 3964 4113 3830 4189
4030 3947 3791 3948 4083 4107 3808 4020
4029 4020 4151 3999 4241 4154 4325 3944
3905 4152 3930 3915 4048 4031 3882 4205
4012 3951 3756 4094 3843 3968 4087 3890
4024 4020 4050 4031 3847 3994 3966 3934
4027 3991 4009 3916 4059 4040 3822 3817
4242 4176 4053 4253 4110 4125 4024 3811
4081 3839 4135 3890 3904 4071 3947 3886
4006 4033 4175 3936 4030 3801 4377 3939
3913 4086 4176 3942 3991 3646 3937 4083
3765 4187 3933 4209 3999 4198 3844 3940
4119 4085 4036 3771 3866 3935 4033 3818
4123 3829 3951 4196 4050 3929 3881 4076
4149 3954 3831 4035 4118 3965 3967 4092
4058 4201 4140 3999 3776 3903 4043 3921
4069 4115 4202 4155 4093 3732 4249 3898
3933 3903 4020 4029 3961 3974 4033 3880
3989 3905 3948 3640 4177 4152 3910 3891
4015 3873 4045 3918 3991 4080 3949 4111
3987 4167 3881 3926 4109 4174 4110 3894
4180 3787 3751 3820 4105 4153 4013 4023
4076 3875 4074 4143 4200 4099 3857 4147
3942 4181 3772 3894 3726 3924 3911 4102
3813 3749 4194 3911 3984 3892 4124 4174
4148 3774 4108 4068 3937 3770 3881 4097
4038 4131 4123 4062 4132 4020 3713 3930
```

```

3797 3918 3943 4089 3923 3978 3863 4038
4050 4100 4116 3872 3849 4097 3868 4083
4027 4159 3995 3755 4136 3821 4076 4006
max = 4377 min = 3640 max-min = 737
sum = 1024000 avg = 4000.000000
sumsq = 4100429126 sigma2 = 17301.273438 sqrt = 131.534305
75 modules

```

The standard deviation in this example is 131.5. In a uniform random distribution, it will be roughly the square root of the bin average. For these runs, the bin average is 4000, and the SD should be around 63. This particular example isn't random enough.

The experiments have shown how the statistics improve as the number of modules is increased. Here's an early experiment to illustrate this. In this experiment, the bin average was 125, and the SD should be around 11. As the number of modules increases, there's a fairly steady decline of the SD, until it levels out around the expected value.

Table 4: Randomization Results

Module Count	Standard Deviation
10	79.16
20	64.06
30	56.00
40	40.06
50	32.45
60	24.59
70	13.80 <=transition to "random enough"
80	13.38
90	10.30
100	9.97
110	11.61
120	11.36
200	12.30
500	11.08

One important lesson learned with the simulator is that it's important to vary the delays used for the input taps in the E-boxes. In our recent experiments, the delays used are mostly 1-8 bits. But in half the E-boxes, one of the inputs is delayed 15-25 bits; and in 20% of the E-boxes, another input is delayed 35-45 bits. These delays made a big improvement in the measured statistical randomness.

The simulator has also been very useful in evaluating the effectiveness of different choices of the logic functions.

7.5.2. Effectiveness of Various Logic Functions

The results of experiments so far are summarized in the table below. The module count is the (approximate) number of E-boxes with the particular logic function, required to completely randomize the input stream (as measured by the standard deviation of the byte-histogram). This indicates the relative effectiveness of the different logic functions.

At least twice as many modules are required for encryption as are needed for simple randomization.

Table 5: Module Count Requirements

Logic Function	Module Count	Comment
A & (B V C)	*125+	Mixed complements.

AB V CD	*200+	All inputs complemented.
Maj3	25	Alternately 1,2 inputs complemented
Maj5	20	3 inputs complemented
1of3	15	1 input complemented
6:1 mix of A(BvC), Maj3	70-105	

* The top two experiments were run before the delay improvements were added, so these functions aren't as bad as the table indicates.

The experiment suggests that mixing several types of F-function is a good thing to do, but it complicates the construction.

Maj3(A,B,C) is the majority vote of the three inputs. Maj5 is similar, with five inputs. These two functions are relatively simple to build with threshold logic. The most effective mixing function is the 1of3 function. This function is true when exactly one of its three inputs is true. Conceptually, it's a little bit like the exclusive-or function, but it's not possible to define it as a combination of simpler Xor functions.

7.6. Authentication

Any cryptographic message that might be subject to tampering, or even plain transmission errors, must be authenticated. Stream ciphers are no exception. For our system, we will periodically insert a 32-bit CRC into the data stream to be encrypted. The receiver will validate the CRC as part of the decryption step, and flag or drop any bad messages.

8. Conclusion

This document detailed the PSpice modeling efforts for S-SEED logic and demonstrated encapsulated models of XOR, NAND, and NOR functions. Future tasks include simulating feedback loops and more complex logic circuits. A stream cipher for photonic encryption has also been devised and its statistical randomness has been simulated in C language.

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