

# **Optimization of Comminution Circuit Throughput and Product Size Distribution by Simulation and Control**

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Authors: H.J. Walqui – Graduate Student  
T. C. Eisele – Engineer/Scientist  
S. K. Kawatra – Principal Investigator

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### **Submitting Organization**

Department of Chemical Engineering  
Michigan Technological University  
1400 Townsend Drive  
Houghton, MI 49931 - 1295

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## **Abstract**

The goal of this project is to improve energy efficiency of industrial crushing and grinding operations (comminution). Mathematical models of the comminution process are being used to study methods for optimizing the product size distribution, so that the amount of excessively fine material produced can be minimized. The goal is to save energy by reducing the amount of material that is ground below the target size, while simultaneously reducing the quantity of materials wasted as “slimes” that are too fine to be useful. This will be accomplished by: (1) modeling alternative circuit arrangements to determine methods for minimizing overgrinding, and (2) determining whether new technologies, such as high-pressure roll crushing, can be used to alter particle breakage behavior to minimize fines production.

## **Table of Contents**

Introduction	5
Executive Summary	5
Experimental	7
Results and Discussion	10
Conclusions	13
References	13

## **List of Tables and Graphical Materials**

<b>Figure 1: Redesigned flowsheet to reduce circuit instability</b>	<b>6</b>
<b>Figure 2: 2-stage hydrocyclone configurations</b>	<b>9</b>
<b>Figure 3: Comparison of mill performance predicted by the grinding mill model with performance actually observed in the operating plant.</b>	<b>10</b>
<b>Figure 4: Predicted product size distributions for the simulation of an open-circuit mill processing the intermediate size fraction generated by two-stage hydrocycloning.</b>	<b>11</b>
<b>Figure 5: Intermediate and final products in the simulated comminution circuit shown in Figure 1.</b>	<b>12</b>

## **Introduction**

While crushing and grinding (comminution) of various feedstocks is a critical operation in mining, as well as in a range of other industries, it is both energy-intensive and expensive, with tremendous room for improvement. A neglected route in optimizing the comminution process is the minimizing of overgrinding. Since grinding particles to finer than the target size both wastes energy and produces unusable product, such overgrinding must be minimized in order to improve energy efficiency. The objective of this project is therefore to sample and simulate a full-scale iron ore processing plant to determine methods for increasing grinding circuit energy efficiency by minimizing overgrinding.

Plant sampling and analysis has demonstrated that the largest single source of overgrinding in the industrial process is the return of high-density material to the grinding process by hydrocyclones. The particles of high-density iron oxides that are near the cut size are fully liberated and do not require further comminution, but they are returned to the mill rather than being removed as final product. A fundamental redesign of the comminution circuit is therefore needed to deal with these intermediate-size dense particles.

## **Executive Summary**

The goal of a comminution circuit is to grind particles to their liberation size, so that the valuable minerals are completely broken free from the gangue minerals. For the best grinding efficiency, all particles must be ground only to the liberation size, and no finer. To accomplish this, grinding mills are generally operated in closed circuit with a sizing device, such as a screen or a hydrocyclone, so that as soon as particles reach the target size they are removed from the circuit by the sizing device. In most grinding circuits, the hydrocyclone is the preferred sizing device because it can classify very fine particles, and it is rugged and inexpensive to operate. Screens for sizing very fine particles would be theoretically superior to hydrocyclones for this application, but they are much larger and at fine particle sizes they tend to be very high-maintenance items.

When samples were collected from the plant, it was determined that approximately 35% of the hydrocyclone underflow that is returned to the pebble mills is liberated magnetite that does not need to be ground further. Coarsening the separation by the hydrocyclone would prevent this magnetite from being overground, but would also result in an unacceptable amount of locked quartz/magnetite particles leaving the comminution circuit.

A proposed solution to the problem caused by the hydrocyclone “fish-hook” behavior was to first use two stages of hydrocyclones to produce three products: A coarse product that definitely required regrinding, a fine product where all particles were finer than the target size, and an intermediate product where the magnetite particles were at the target cut size and the gangue particles were coarser than the cut size. Once this was done, it was proposed that the intermediate size particles could be passed once through an open-



## Experimental

In order to study the effect of hydrocyclone “fish-hook” behavior on comminution efficiency, and to evaluate potential solutions to the problem, models are needed for both the hydrocyclone, and the associated pebble mill. The hydrocyclone model has already been developed in this project, and a pebble mill model was needed.

The pebble mills modeled had the following characteristics:

–Number of mills in parallel	1
–Mill diameter inside shell (m)	4
–Length/diameter ratio	2.1
–Fraction of critical speed	0.8785
–Mill discharge	Overflow
–Filling of the mill (%)	43
–Reference size for the wear function (mm)	15.875
–Wear coefficient (0=surface, 1=volume)	0
–Wear rate of pebbles (1/h)	3.45

The overall form of the grinding mill model consisted of a breakage function and selection function to describe how the mill breaks down particles, which are then used to predict the mill performance under any given conditions. The breakage function describes the size distribution of the fragments that result from breakage of particles of a particular size. The breakage function used in this model was:

$$B_{ij} = \phi \left( \frac{x_{i-1}}{x_j} \right)^\gamma + (1 - \phi) \left( \frac{x_{i-1}}{x_j} \right)^\beta$$

where  $B_{ij}$  is the fraction of the mass of broken particles from size fraction  $i$  that reports to size fraction  $j$ ,  $x_i$  is the top size limit of size fraction  $i$ , and the breakage function parameters were constants obtained from fitting known data from laboratory and in-plant samples:  $\phi = 0.096$ ;  $\beta = 3.93$ ;  $\gamma = 0.608$ .

The selection function describes the probability that a particle of a specific size will actually be broken in the mill, producing fragments with the size distribution given by the breakage function. The selection function used in this model was:

$$S_i = S_1^E e^{a_1 \ln\left(\frac{d_i}{d_{i(ref)}}\right) + a_2 \left(\ln\left(\frac{d_i}{d_{i(ref)}}\right)\right)^2}$$

where  $S_i$  is the fraction of particles in size fraction  $i$  that are broken,  $d_i$  is the geometric mean particle diameter of size fraction  $i$ ,  $d_{i(ref)}$  is the reference particle size class, and the selection function parameters were constants obtained from fitting known data from laboratory and in-plant samples:  $S_1^E = 0.75$ ;  $a_1 = -1.5$ ;  $a_2 = -0.5$

The breakage function was primarily determined from drop-test data for this ore body. These tests were performed as part of an earlier project and their cost is not included as a part of this DOE project. These tests determined particle fragment size distributions as a function of the size of the parent particle. Given a breakage function, and actual pebble mill operating data from the plant, the selection function could be calculated.

Once the model was developed, work began to use it to simulate the performance of a grinding mill in combination with two-stage hydrocycloning. Previously, plant personnel had operated the full-scale grinding circuit with 2-stage hydrocyclone classification, as shown in Figure 2A. This had been intended to separate out the intermediate-sized particles that contained liberated dense particles, and bypass the grinding mill with this material. While the combination of hydrocyclones was found to be effective in producing this intermediate product, this flowsheet resulted in the intermediate particles simply accumulating in the circuit rather than being removed. This had been found to lead to unmanageably large recirculating loads and therefore proved impractical, but it did provide necessary information for use in subsequent simulations.

Size data was collected for the material in Stream 6, and this size distribution was used as the feed for simulation of open-circuit grinding. The objective of the simulation was to determine whether the intermediate-size particles, which represented a narrow size distribution, could be sufficiently ground by a single pass through an open-circuit mill to eliminate the locked particles. Since the feed to the open-circuit mill was a narrow size distribution, it was expected that the product would also be a relatively narrow size distribution, eliminating the need for the product to be passed through a classifier so that locked particles could be returned to the circuit. This would have the following anticipated benefits:

1. A considerable amount of grinding load would be removed from the closed-circuit mill, which would now be grinding to a coarser size with a much reduced circulating load. This would boost circuit capacity.
2. The liberated magnetite, which would normally be returned multiple times for regrinding by the hydrocyclones, would instead pass through only a single final grinding stage. This would reduce overgrinding of the intermediate-size liberated particles.

The first flowsheet configuration used in the simulations was that shown in Figure 2B, which was a minimal modification to simply grind Stream 6 to prevent it from building up in the circuit.

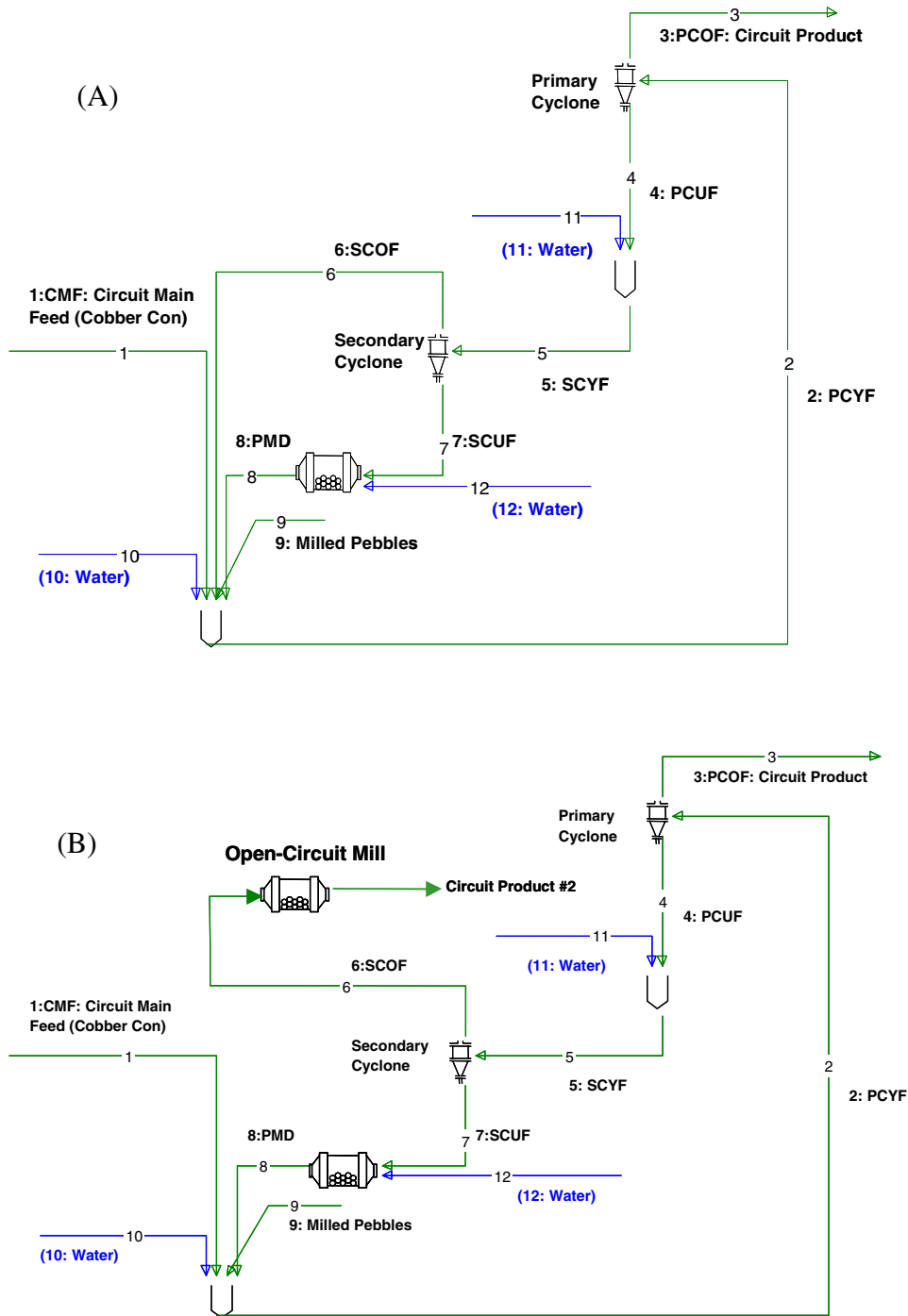


Figure 2: 2-stage hydrocyclone configurations (A) As tested in the plant, and (B) Proposed configuration incorporating open-circuit grinding for the intermediate-sized material in Stream 6.

## Results and Discussion

Once the model parameters had been determined for the mill and for the ore body, the model was validated against actual operating data. The results of this validation are given in Figure 3, where it can be clearly seen that the predicted mill product from the model is an extremely close match for the actual mill product as measured in plant samples. This confirmed that the model was suitable for prediction of mill performance, although it must be kept in mind that if the simulation is run under conditions that are greatly different from the mill operation conditions that the model was developed for, the model predictions are unlikely to match quite as closely to reality as do the results in Figure 3.

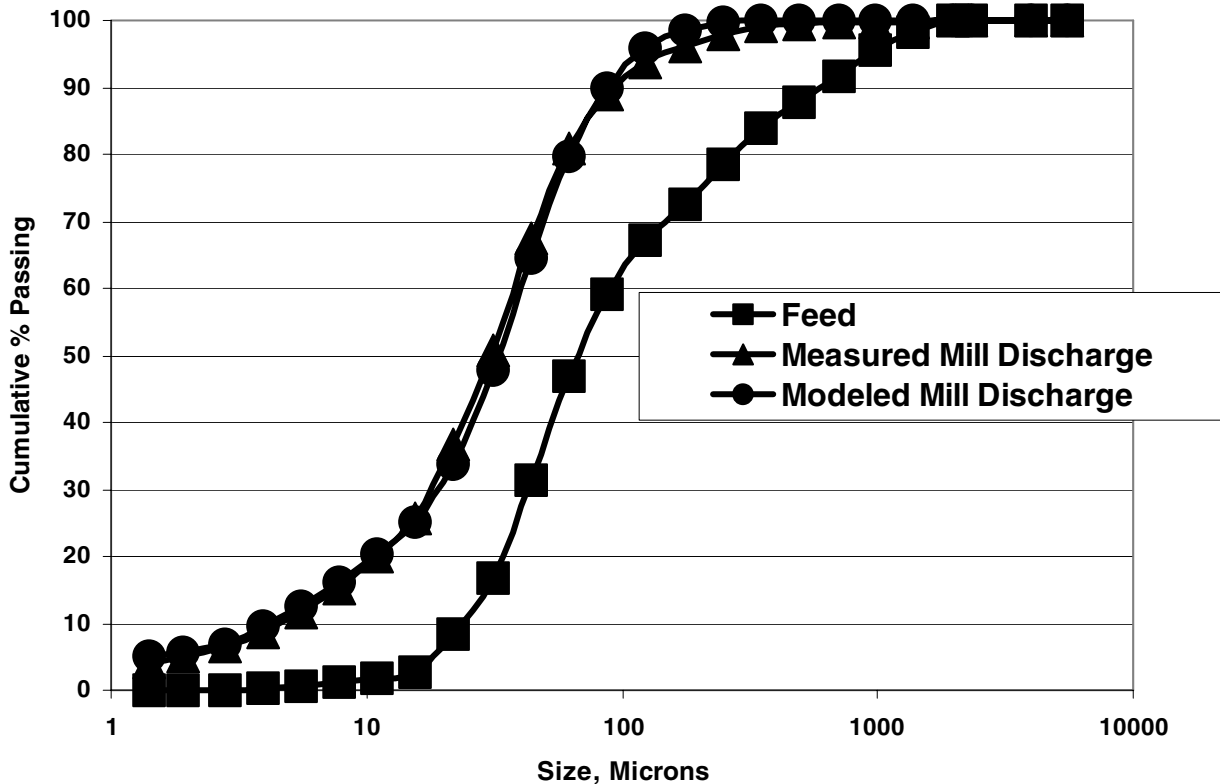


Figure 3: Comparison of mill performance predicted by the grinding mill model with performance actually observed in the operating plant. The match between the measured and the modeled mill discharge size distribution is excellent.

Once the model had been validated, it was used to predict the performance of the grinding mill when grinding material having the size distribution of the ore in Stream 6 of the flowsheet shown in Figure 2A. This “mill feed” was determined to have a narrow size distribution consisting primarily of particles between 10  $\mu\text{m}$  and 100  $\mu\text{m}$ .

Simulations were run with several different size distributions determined on different days in the plant. Representative results of these simulations are shown in Figure 4. From these results, it is clear that the fineness of the mill product is highly sensitive to the

mill feedrate. In order to keep the material from being overground, the open-circuit mill needs to have a feedrate at least six times higher than the normal feedrate for these mills.

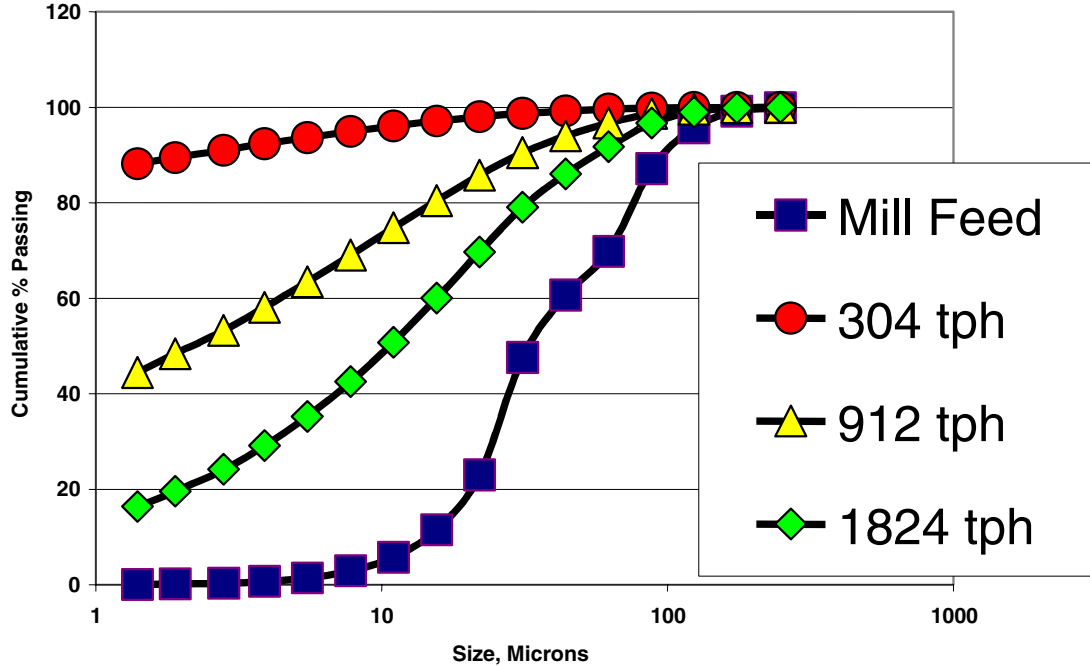


Figure 4: Predicted product size distributions for the simulation of an open-circuit mill processing the intermediate size fraction generated by two-stage hydrocycloning. The product fineness is highly sensitive to the mill feedrate.

When the open-circuit mill simulation was fully integrated into the comminution circuit shown in Figure 2B, it was found that there were instability problems due to excessive water in the open-circuit mill feed, and to a large recirculating load that developed in the closed-circuit mill. This was primarily due to the fact that the open-circuit mill feed was taken from a hydrocyclone overflow, which had a very low solids content and therefore forced the mill to run with an excessively dilute slurry. To eliminate these problems, the circuit was reconfigured as shown in Figure 1, so that both mills would be receiving a high-percent-solids feed from the hydrocyclone underflows that would be ground more efficiently. In this configuration, the coarsest particles are first separated by the larger 26-inch diameter hydrocyclones and sent as feed to the closed-circuit mill. The smaller 15-inch diameter hydrocyclones then produce an intermediate-size fraction that is the feed to the open-circuit mill, and a fine fraction that is removed from the circuit as a finished product.

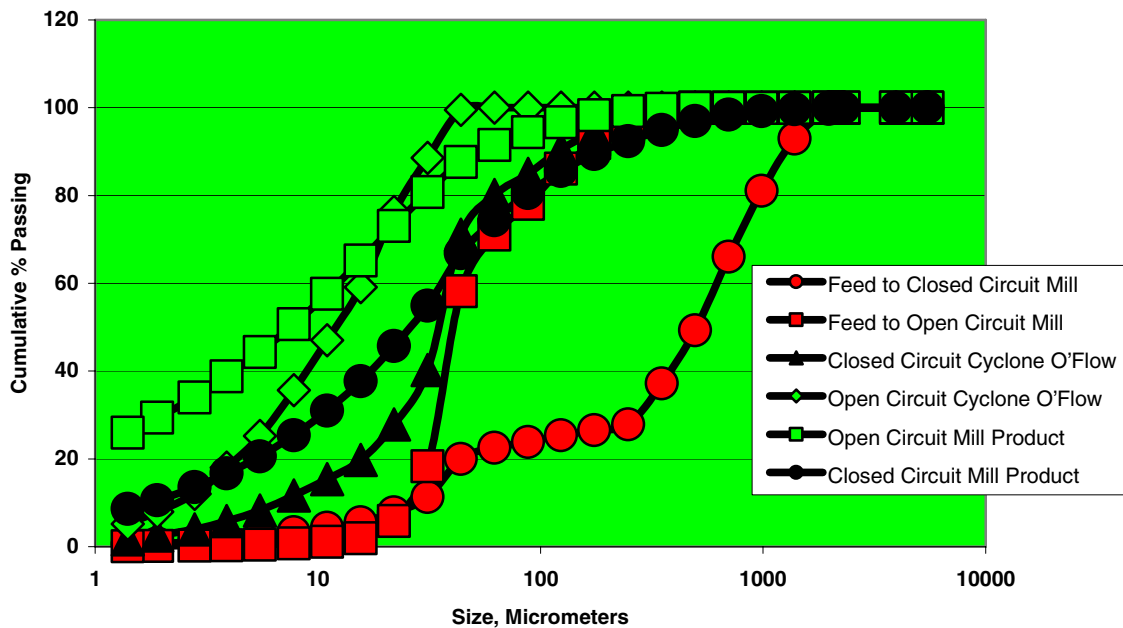


Figure 5: Intermediate and final products in the simulated comminution circuit shown in Figure 1. The “Open Circuit Cyclone Overflow” and “Open Circuit Mill Product” are final products from the grinding circuit.

The two final products from the circuit are the open-circuit cyclone overflow and the open-circuit mill product. The simulation predicts both of these products to have very similar size distributions, indicating that this approach is feasible. The simulated circuit was stable, without excessive circulating loads or water use. Differences in projected energy use for this circuit compared to the existing configuration are currently being evaluated.

As was expected, the feed to the open-circuit mill had a very narrow predicted size distribution, centered on the region where the hydrocyclones have the greatest tendency to return liberated magnetite particles to the mill, causing them to be overground. When this feed was ground by the open-circuit mill, the resulting product had a somewhat broader size distribution than was anticipated. However, it should be noted that the very narrow size distribution of the feed is outside of the region of the data that was originally used to validate the model, and so the predicted size distribution is likely to be inaccurate at the finer sizes. Studies are underway to check the model to determine whether the predicted production of particles in the sizes finer than about 10 micrometers are accurate, or whether the model is overpredicting fines production in this region.

## Conclusions

In order to address the overgrinding caused by the “fish-hook” behavior of the hydrocyclones, it is necessary to remove the intermediate-sized magnetite that the hydrocyclones otherwise preferentially return to the grinding mills.

Open-circuit grinding of a narrow size fraction from the pebble mill feed is a potential solution to overgrinding. The simulation results indicate that either very high flowrates, or a smaller pebble mill, is needed to keep the open-circuit mill from severely overgrinding the feed. Data for very fine particles is not yet available for model validation, and so the model may be overestimating the amount of material produced at the finest particle sizes.

Simulation of the complete circuit determined that a simple adaptation of a previous two-stage hydrocyclone flowsheet did not lead to stable operation. Experimentation with the simulation layout showed that much better results could be obtained with a new configuration where the feed to both mills was a high-percent-solids hydrocyclone underflow product. The resulting circuit exhibited stable operation and produced an open-circuit mill discharge that had very close to the desired size distribution.

Studies are currently underway, using both laboratory data and recent plant data, to determine whether the comminution model is overpredicting the production of very fine particles during open-circuit grinding.

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