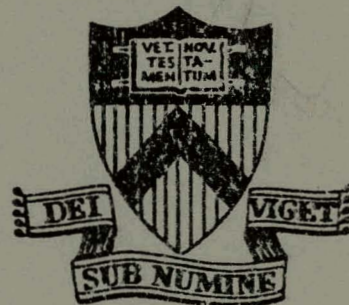# ANOMALOUS SLOWING OF A PERPENDICULARLY-INJECTED ION BEAM IN BOTH QUASILINEAR AND TRAPPING REGIMES

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Ion Beam in Both Quasilinear and Trapping Regimes

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Anomalous Slowing of a Perpendicularly-Injected

Ion Beam in Both Quasilinear and Trapping Regimes*

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ABSTRACT

The anomalous slowing of an ion beam injected perpendicularly to the confining magnetic field of a low β plasma is experimentally verified in the nonlinear stages of the excited lower-hybrid instability. Furthermore, a transition of the main nonlinear mechanism from the quasilinear to the particle trapping regime is demonstrated by varying beam parameters.

The ion distribution resulting from neutral and/or ion beam injection perpendicular to the confining magnetic field is theoretically predicted to destabilize microinstabilities,[1-3] and the injected beam is expected to lose its momentum anomalously fast as a result of wave-particle interaction.[4] We wish to present the first experimental verification, to our knowledge, of the anomalous slowing and the velocity space diffusion of a perpendicularly injected ion beam due to the nonlinear interaction of the beam with the excited lower-hybrid instability.

Two major nonlinear wave-particle interactions have been separately invoked as the saturation mechanism of beam-driven plasma instabilities, i.e., particle trapping in a coherent wave trough[5,6] or quasilinear velocity-space diffusion in a broad spectrum of waves.[7,8] Another novel contribution of the present experiment is that a transition of the nonlinear mechanism from the quasilinear to the particle trapping regime is observed together with time-resolved measurements of the beam's velocity-space modification.

The experiments were performed in the Princeton Q-1 device, using the machine layout in which the lower-hybrid wave, excited by spiral ion beam injection, had been identified by the wave's dispersion $(\omega, \vec{k})$.[3] To follow the nonlinear evolution of the instability, a pulsed ion beam is used in the present experiment; the beam follows a helical path $(r_{helix} \simeq 5\rho_i$, ρ_i = target ion Larmor radius) and creates a double-humped ion velocity distribution $[f(v_\perp)]$ in a cylindrical shell of the target

plasma column ($r_{column} \simeq 3 r_{helix}$). A flute-type ($k_z \simeq 0$) lower instability destabilizes when the average beam density throughout the column reaches a threshold value and propagates with the same azimuthal velocity as the beam. The mode is a standing wave in both the parallel and radial directions. Before reaching the nonlinear stage, the instability grows in time with the growth-rate predicted by linear warm-plasma theory.

Figure 1 shows the growth and saturation of the lower-hybrid instability for different beam densities but constant beam energy and temperature. In Fig. 1(a) the instability monotonically approaches a constant saturation level in a few growth times (~ 100 μsec), which is consistent with the quasilinear diffusion time estimate for the measured wave amplitude, $e\tilde{\phi}_{max}/T_0 \simeq 0.08$. The amplitude overshoots in Figs. 1(b) and (c), with higher beam densities and growth rates, are not consistent with a slowly developing stochastic process; they represent the beginning of a trapping cycle and indicate some coherence in the interaction. The maximum amplitude of the overshoot $\tilde{\phi}_{max}$ is often 2-3 times the steady-state level, up to $e\tilde{\phi}_{max}/T_0 \sim 1$. The potential fluctuation $\tilde{\phi}$ is measured with calibrated Langmuir and capacity-coupled probes.[3]

In Fig. 1(d), where spectral measurements show two modes of high growth rate, wave-wave interactions become an important nonlinear effect. After the overshoot of the fastest growing wave, the second wave ($\gamma_2 < \gamma_1$) can suddenly detrap ions from the main wave, and the reappearance of random-phase interactions allows a quasi-linear-like plateau to be formed.[9] These results are in good agreement with particle simulation results for one dimensional beam plasma systems.[10]

The coherence of a wave is determined by its autocorrelation time [$\tau_{ac} \simeq 1/\Delta\omega$ or more strictly defined by the phase velocity spread, $\tau_{ac} = (k \cdot \delta v_p)^{-1}$], which has to be compared to the linear growth time ($\tau_g = \gamma^{-1}$), bounce frequency for a trapped particle [$\tau_b = 2\pi/\omega_b = 2\pi(M_i/e\phi k^2)^{1/2}$], and the beam's velocity-space diffusion time {$\tau_d \simeq (\delta v_p)^3/[2(e/M)^2 \sum k\tilde{\phi}_k^2]$}. The requirements for quasilinear theory to be valid are $\gamma << \omega_r$ and $\tau_{ac} < \tau_g < \tau_d$, while trapping becomes important when $\tau_b < \tau_g \lesssim \tau_{ac}$. These time scales are shown vs. wave amplitude in Fig. 2 for the present beam-plasma parameters. Roughly speaking, if $\tau_g > \tau_{ac}$ the growth and saturation of the instability will proceed as described by quasi-linear theory on the time scale, $\tau_n \simeq \tau_d \propto \tilde{\phi}_{max}^{-2}$. For $\tau_g \lesssim \tau_{ac}$, quasilinear theory is invalid, and eventually the wave saturates by trapping and slowing the beam; the time scale for the non-linearity is then $\tau_n \simeq \tau_b \propto \phi_{max}^{-0.5}$. The solid lines in Fig. 2 indicate the valid nonlinearity time scales. The open-circles are the measured nonlinear growth times which are defined here as the time interval from the cessation of linear growth to saturation; the data clearly shows the expected transition.

In the experiment, with the injection of a low-density warm beam, the maximum wave growth is predominantly determined by inverse Landau damping ($\gamma \propto f_b'(\omega/k)_{MAX} \propto n_b/n_t$, $\gamma < \Delta\omega$), and the quasilinear effect dominates wave nonlinearity [Fig. 1(a)]. With higher beam density, the growth rate of the wave with phase velocity $\omega/k \simeq u_b[1 - 1/2(n_b/2n_o)^{1/3}]$ becomes large mainly due to reactive coupling to satisfy $\gamma > \Delta\omega$. In the latter case, particle trapping causes wave saturation after the amplitude reaches the value to fulfill $(2e\tilde{\phi}/m)^{1/2} \simeq u_b - \omega/k$, [Fig. 1(c,d)]. These characteristics are in agreement with those of O'Neil and Malmberg[11] who define a beam thermalization parameter

$S = (v_b/u_b)(2n_o/n_b)^{1/3}$ where v_b is the beam's velocity spread; if $S < 1$ reactive coupling dominates while for $S > 1$ resonant effects prevail. The present experiments were performed in the transition region $S \simeq 0.2 \rightarrow 5$.

To strengthen the association of the overshoot with trapping, the fall time (τ_f) is plotted as a function of $\tilde{\phi}_{max}$ in Fig. 2, in good agreement with the trapping relation $\tau_b \propto \tilde{\phi}^{-1/2}$. The appearance of a strong bounce frequency modulation is usually observed only for one bounce cycle after the initial growth; a coherent trapping oscillation tends to be suppressed due to the fact that the trapped beam ions in different spiral steps oscillate with different phases in the potential trough of this flute-type $(k_z = 0)$ wave. After the overshoot, we note, the wave frequency shifts to a slightly lower value $(\Delta\omega/\omega_{LH} < 0.1)$ and the spectral width increases.

An ion energy analyzer (size 2 mm) is used to directly observe the nonlinear modification of the beam distribution using Boxcar sampling techniques with a resolution time of 2 ~ 4 μsec. Because the instability propagates perpendicularly, it has no effect on the parallel component of the beam velocity. The time evolution of the perpendicular velocity distribution is shown in Fig. 3. In this case the instability overshoot is weak and the time scale for the nonlinear modification of the distribution, $\tau_n \simeq 15$ μsec , agrees with the time estimate from quasilinear diffusion for $e\tilde{\phi}_{max}/T_0 \simeq 0.2$ which falls in the transition region, $\tau_n \simeq \tau_d \simeq \tau_b$. The beam distribution actually becomes monotonically decreasing before setting down to a level plateau, an effect also observed in particle simulations.[10] For lower beam densities (the quasilinear regime), accurate $f_b(v_\perp)$ measurements could not be made because of the sensitivity of the energy analyzer.

Figure 4 gives an example of the evolution when the overshoot is stronger $(e\phi_{max}/T_0 \simeq 0.3)$ and a bounce back of the instability amplitude occurs. The distribution remains peaked until $\tilde{\phi}$ reaches a maximum and then rapidly flattens. As the amplitude reaches a minimum, the peak reappears and slides to lower energy as the wave regrows. Although, this process occurs on a little longer time scale than trapping, it represents the partially reversible coherent oscillation of beam ions in wave troughs. (Whole process occurs in less than the beam transit -time.)

The quasilinear theory for a two-dimensional ring or loss-cone distribution[4,12] also suggests the occurrence of an overshoot, although the predicted amplitude dependence is $\tau_f \propto \tilde{\phi}^{-2}$ instead of $\tau_f \propto \tilde{\phi}^{-1/2}$ as observed here. In addition, the present geometry is effectively one-dimensional because both beam and wave propagate along the same azimuthal path.[3]

As the instability grows and diffuses the beam in velocity space, it also diffuses the beam radially inward; as the beam ions slow in perpendicular velocity, their Larmor radii are reduced. This effect is observed as a flattened radial beam density profile after instability saturation. Wave heating of the target plasma was too small to be detected due to the reasons stated in the earlier communication.[3]

The anomalous beam slowing $(\nu_{eff}/\nu_{classical} \simeq 10^2 \sim 10^3)$ observed in the present experiment has a strong impact on perpendicular neutral beam injection in Tokamak or Mirror fusion devices. In the preheating stage this anomalous effect may be useful, but it will have deleterious results on the ripple injection scheme,[13] or on the deutron injection burning stage because of the rapid

loss of fusable ions. In future fusion devices, high-energy charges fusion-reaction products (H, T, H_e^3, H_e^4) may also destabilize the lower hybrid wave. These ions may be poorly confined because of their large banana orbits, and in this case, anomalously fast perpendicular momentum loss would be beneficial as it would improve the confinement of these particles.

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*Work supported by U.S. Energy Research and Development Administration, Contract EY-76-C-02-3073.

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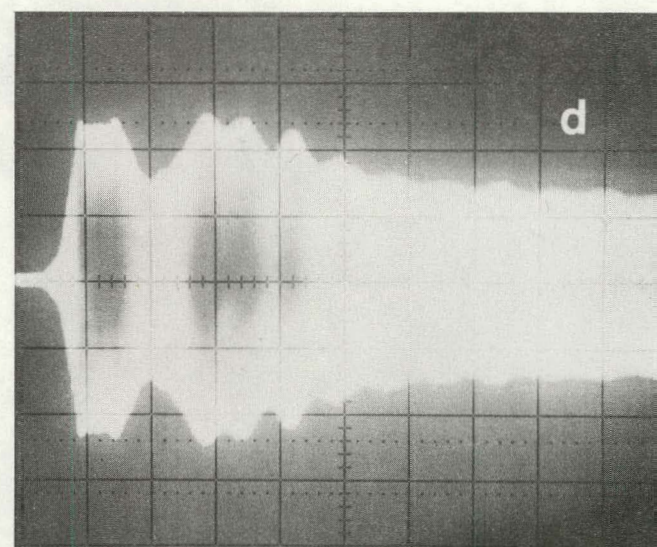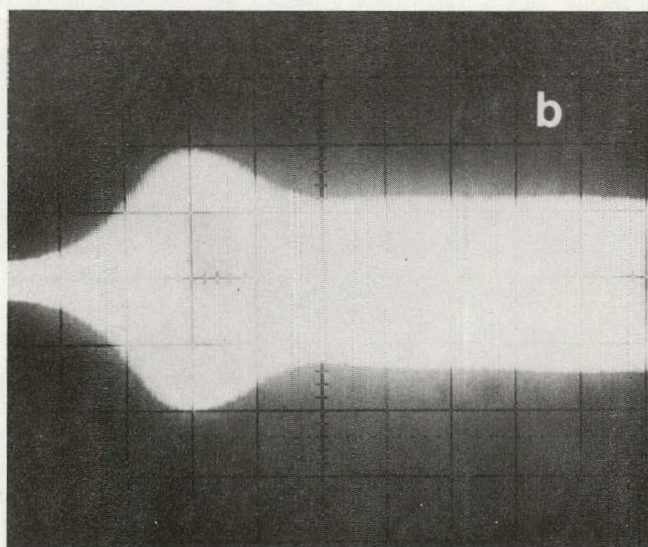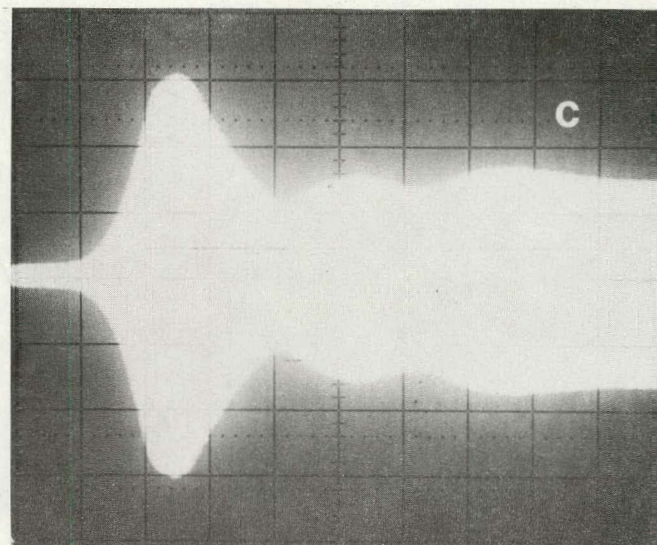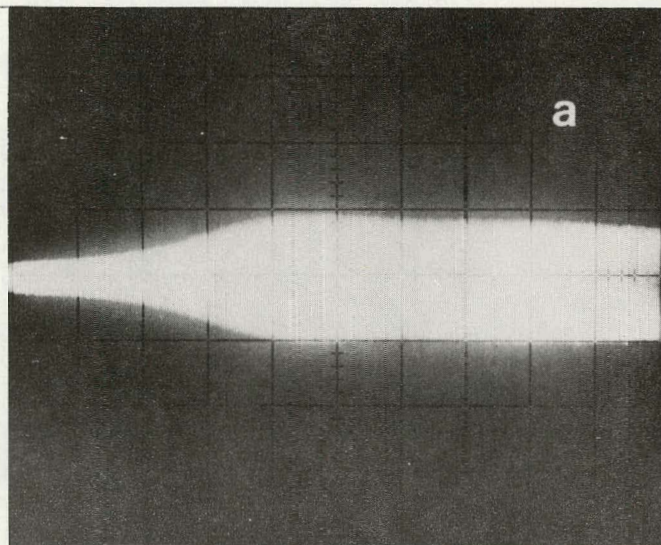
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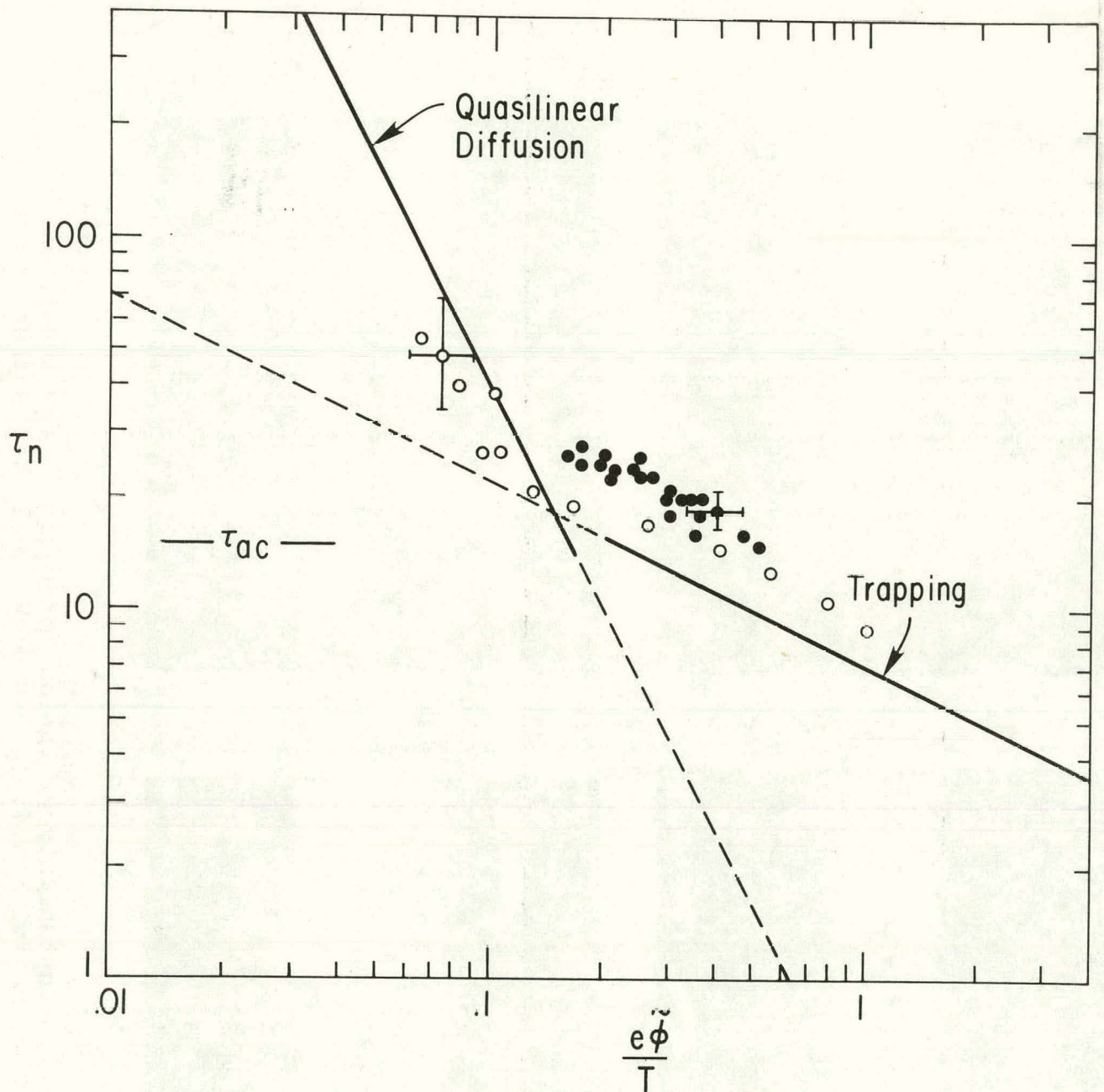[14] L. P. Mai and W. Horton, Jr., Phys. Fluids 18, 356 (1975).

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Fig. 1. Instability evolution for various beam densities.
$n_0 = 10^9 cm^{-3}$, $u_{b\perp}/v_0 = 5.4$, $T_b = 0.5$ eV. All time scales are
20 µsec/div. (a) $\bar{n}_b/n_0 = 0.18\%$, $e\tilde{\phi}/T_0 = (0.1)/div$; (b) 0.27%,
(0.1); (c) 0.45%, (0.2); (d) 2.4% (0.4).

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Fig. 2. Quasilinear diffusion and trapping times vs wave
potential amplitude. All times normalized to $\tau_p = 2\pi/\omega_{pi}$ ($\simeq 1$
μsec). $\tau_{ci} \simeq 5\tau_{pi}$, $\tau_{ac} \simeq 15\tau_{pi}$. Open circles (o) are the non-
linear growth-times and closed circles (●) are from fall times
after the overshoot.
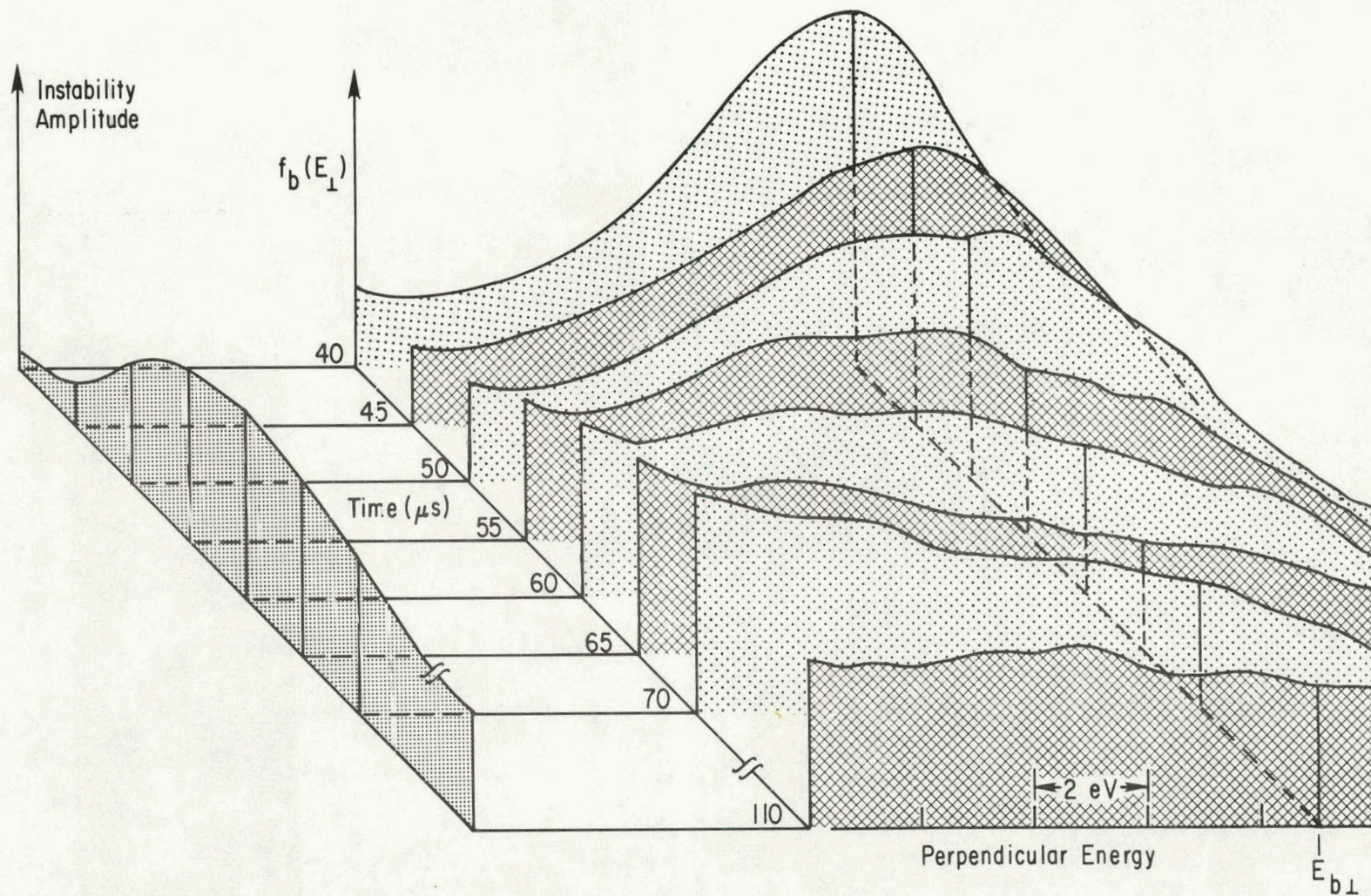
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Fig. 3.   Beam perpendicular energy distribution and wave
amplitude vs time.   The target ion distribution is not shown
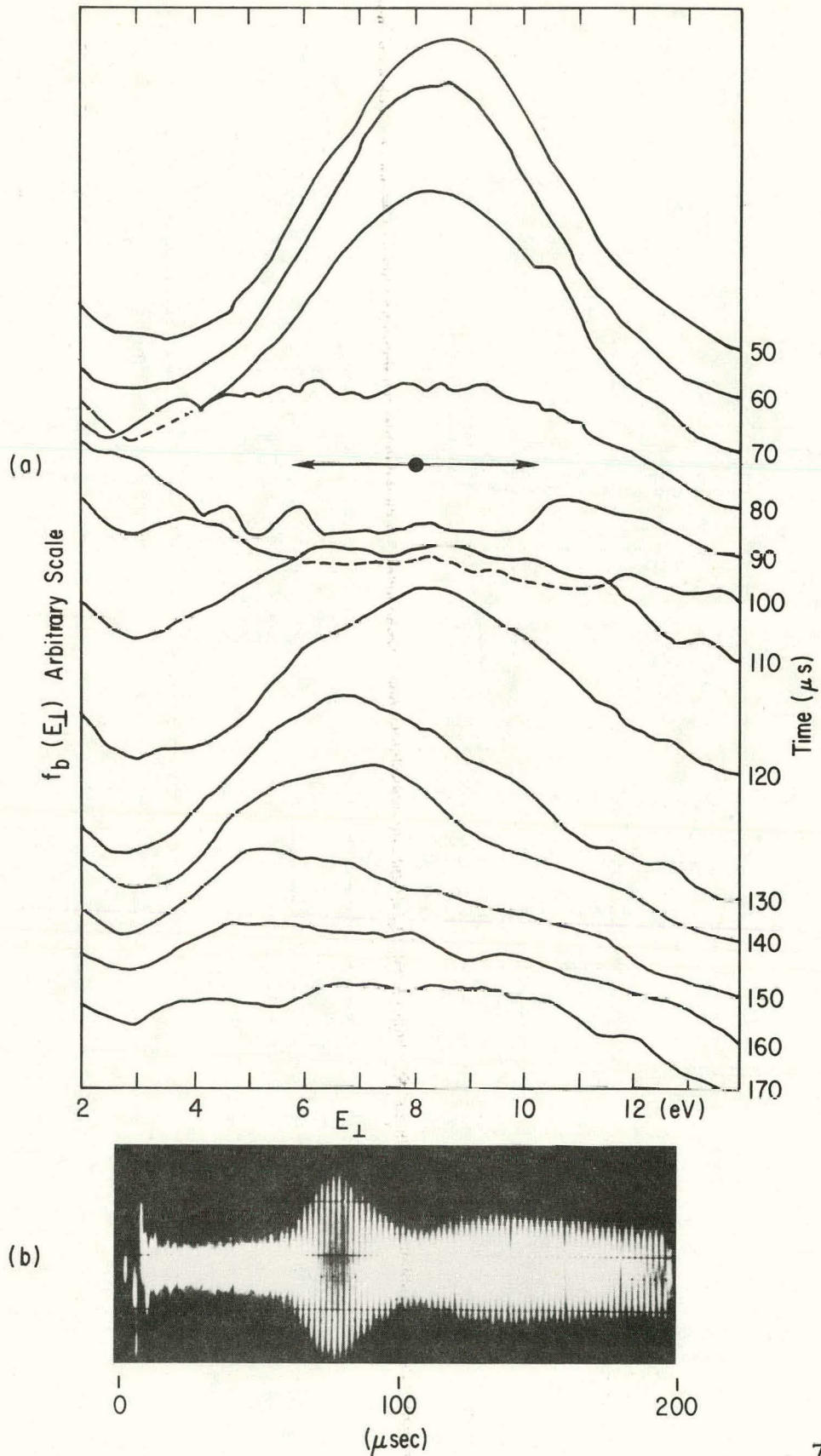for clarity. $e\phi_{max}/T_o \simeq 0.2 \pm 50\%$.

Fig. 4. Beam perpendicular energy distribution (a) and wave
amplitude (b) vs time for $e\phi_{max}/T_o \simeq 0.3 \pm 50\%$ and a large ini-
tial overshoot. $(1/2)m\,u_{b\perp}^2 = 8$ eV. The arrow shows rough ener-
gy scale of the trapping width around $(1/2)m\,(\omega/k_\perp)^2$ at $t \simeq 80$
μsec.

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