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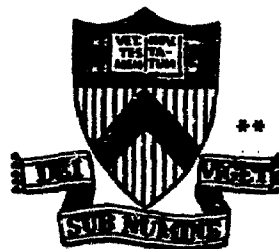
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OF FUSION PLASMAS IN CONTEMPORARY  
BEAM-DRIVEN TOKAMAKS

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**PLASMA PHYSICS  
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# FOKKER-PLANCK/TRANSPORT ANALYSES OF FUSION PLASMAS

## IN CONTEMPORARY BEAM-DRIVEN TOKAMAKS

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**ABSTRACT.** The properties of deuterium plasmas in experimental tokamaks heated and fueled by intense neutral-beam injection are evaluated with a Fokker-Planck/radial transport code coupled with a Monte Carlo neutrals treatment. Illustrative results are presented for the Poloidal Divertor Experiment at PPPL as a function of beam power and plasma recycling coefficient,  $R_c$ . When  $P_{beam} = 8$  MW at  $E_b = 60$  keV, and  $R_c = 0.2$ , then  $\langle n_{hot}/n_e \rangle \sim 0.5$ ,  $[2/3 \langle E_{ion} \rangle] = 22$  keV  $\sim 6 \langle T_e \rangle$ , and the D-D neutron intensity is  $10^{16}$  n/sec.

## 1. INTRODUCTION

In several large tokamak experiments now in operation or under construction, the injected neutral beam power will far exceed the ohmic heating power. By controlling the warm-ion density by gettering or by a magnetic divertor, it is possible to operate in three different reactor-plasma regimes [1]: (1) The energetic-ion regime, where the average ion energy greatly exceeds the electron energy, the plasma recycling coefficient  $R_c \ll 1$ ,  $n_{hot}/n_e \gg 0.3$ , and the dominant fusion production is by reactions between the energetic ions; (2) The TCT regime, where  $n_{hot}/n_e \approx 0.1$ , and the dominant fusion production is by beam-target reactions; (3) The beam-driven thermonuclear regime, where  $n_{hot}/n_e \ll 0.1$ , and the dominant fusion production is by thermonuclear reactions.

For smaller tokamaks with injected powers in the 2 to 12 MW range at 40 to 60 keV, the energetic-ion regime provides the largest neutron intensity [1]. A specific example of the "energetic-ion" regime is the CIT (counterstreaming-ion torus), which is established by beam injection parallel and antiparallel to the magnetic axis [2]. The transition region between the CIT and TCT regimes is perhaps more accessible, and also results in intense fusion-neutron production. In either case the injected beams serve simultaneously to fuel the plasma, to heat electrons and warm ions, and to produce most of the fusion power.

In order to predict and interpret accurately the plasma characteristics and fusion output of intensely beam-driven tokamak plasmas, the time evolution of the velocity-space distribution functions of the energetic species must be calculated using the complete nonlinear Fokker-Planck operator. This paper describes computational studies that make use of the Fokker-Planck/Transport code (FPT) developed at the National Magnetic Fusion Energy Computer Center at Livermore [3]. This code has been integrated with a Monte Carlo neutrals transport treatment [4], a self-consistent beam deposition code [5], and an impurity radiation model [6]. Illustrative results are presented for the Poloidal Divertor Experiment (PDx) now nearing completion at PPPL.

## 2. COMPUTATIONAL MODEL

The FPT Code utilizes an arbitrary number of Maxwellian plasma species which are described by their individual densities  $n_a(\rho, t)$  and by a common temperature profile  $T_i(\rho, t)$ , where  $\rho$  is the average radius of a flux surface. The electrons are described by a separately computed temperature profile  $T_e(\rho, t)$ . An arbitrary number of energetic ion species are represented by distributive functions of the form  $f_h(v, \theta, \rho, t)$ , where  $v$  is speed and  $\theta$  is pitch angle.

Neutral beam deposition is computed self-consistently using a Monte Carlo Code [5] that follows fast neutrals from injectors of specified dimensions and focal properties. The injected energetic ions form a hot-ion velocity distribution determined separately for each radial position. The evolution of  $f_h(v)$  is described by

$$\frac{\partial f_h}{\partial t} = \left( \frac{\partial f_h}{\partial t} \right)_c + \text{beam source} + \text{losses} \quad (1)$$

The collision operator  $(\partial f_h / \partial t)_c$  is that of Rosenbluth, et al [7], where the "Rosenbluth Potentials"  $\phi_h$  and  $\eta_h$  take into account Coulomb collisions among all charged species. The loss terms include charge exchange, fusion burn-up, and transfer to the warm-ion population. The hot ions are assumed to be perfectly confined until they decelerate to an energy  $\epsilon_{\min} = 3/2 T_e$ .

The transport of neutrals in the plasma is determined by a Monte Carlo code [4]. The sources of neutrals include charge-exchange trapping of the injected beams, recycling from the wall, and gas puffing. A Maxwellian warm-ion population is formed from: (i) deceleration of hot ions, (ii) charge-exchange of hot ions, (iii) ionization of warm neutrals formed during neutral-beam trapping, (iv) ionization of neutrals recycled from the wall. The transport equations for the warm ions and electrons are

$$\frac{\partial n_a}{\partial t} = - \frac{1}{\rho} \cdot \frac{\partial}{\partial \rho} (\rho \Gamma_a) + S_{1a} + L_{1a} \quad (2)$$

$$\frac{\partial}{\partial t} (3/2 n_a T_e) = - \frac{1}{\rho} \cdot \frac{\partial}{\partial \rho} (\rho Q_e) + S_2 + L_2 \quad (3)$$

$$\frac{\partial}{\partial t} (3/2 \frac{e}{2} n_a T_i) = - \frac{1}{\rho} \cdot \frac{\partial}{\partial \rho} (\rho Q_i) + S_3 + L_3 \quad (4)$$

where the transport fluxes are written as linear combinations of the density and temperature gradients and the toroidal electric field. The source (S) and loss (L) terms include phenomena such as beam heating, ion-electron energy transfer, Ohmic heating, radiation loss, ionization and charge exchange. The radiation loss term, which is due to a fixed density of impurity ions, is determined by numerical fits to the curves of Refs. [6]. Although a sophisticated neoclassical transport model may be implemented, the present study uses a simpler model based on empirical transport coefficients:

$$\Gamma_a = D_a \partial n_a / \partial \rho \quad (5)$$

$$Q_e = 5/2 T_e \frac{e}{2} Z_a \Gamma_a + K_e n_a \partial T_e / \partial \rho \quad (6)$$

$$Q_i = 5/2 T_i \int_a T_a + K_i \int_a n_a \partial T_i / \partial r \quad (7)$$

The magnitudes and dependences for  $D$ ,  $K_i$ , and  $K_e$  are taken to be the same as those observed in present-day tokamak plasmas, such as TFR [8] and PLT [9], namely,  $D = 1 \times 10^3 [1 + 9(r/a)^2]$  cm<sup>2</sup>/s,  $K_e = (5 \times 10^{17}/n_e)$  cm<sup>2</sup>/s,  $K_i = 1 \times 10^4$  cm<sup>2</sup>/s. The parabolic  $D(r)$  turns out to be roughly equivalent to  $D(r) = n_e^{-1}$ . These transport coefficients are all independent of temperature. At the limiter radius ( $r = a$ ), we fix  $n_h = 0$ ,  $n_e = 3.5 \times 10^{12}$  cm<sup>-3</sup>, and  $T_e = T_i = 0.3$  keV. Neutrals are reflected from the wall with 20 eV energy. For all cases reported herein, an iron impurity with a uniform fixed density of  $3 \times 10^{10}$  cm<sup>-3</sup> is specified.

Fusion reaction rates are accurately computed via a five-fold velocity-space integral of the fusion cross-section over the reacting distribution functions [10]. Steady-state solutions for all plasma parameters and the fusion-neutron production rate are presented in the following sections.

#### 4. EFFECT OF RECYCLING COEFFICIENT

The numerical model has been applied to circular plasmas in the PDX device [11] whose principal parameters are given in Table 1. In PDX the recycling coefficient  $R_c$  of the plasma can in principal be controlled by the poloidal magnetic divertor. ( $R_c$  is defined as the ratio of the rate of cold neutral inflow to the rate of warm-ion outflow.) Figure 1 shows how several important parameters vary with  $R_c$  when the D<sup>+</sup> injection power of 8 MW at 60 keV is held constant. Steady-state solutions are shown. As  $R_c$  increases from 0 to 1.0, the relative hot-ion density decreases by a factor of 3, and  $\langle E_{ion} \rangle$ , the average energy of all hot and warm ions, decreases by a factor of 2.4. The fusion power multiplication,  $Q_p$ , and neutron intensity decrease by a factor of 3.6. [Here  $Q_p = (\text{fusion power/injected power})$ , and does not include ohmic heating ( $\sim 0.5$  MW).] Additional influx of gas into the plasma from the beam lines would cause a further decrease in  $Q_p$  for a given  $R_c$ .

Table 2 gives parameters for the case of  $R_c = 0.2$ , where 54% of the fusion power production is due to reactions between the energetic ions, and 40% is due to beam-target reactions. Figure 2 shows the ion velo-

Table 1. Reference PDX Parameters.

Major radius	1.40 m
Plasma radius	0.42 m
Field at plasma	2.5 T
Plasma current	500 kA
Neutral-beam energy	40 to 60 keV
Neutral-beam power	2 to 12 MW (D <sup>+</sup> )
	85% at full energy
	15% at half energy
Beam pulse length	1.0 s
Injection angles	50% co-injection
(this study)	50% counter-inj.

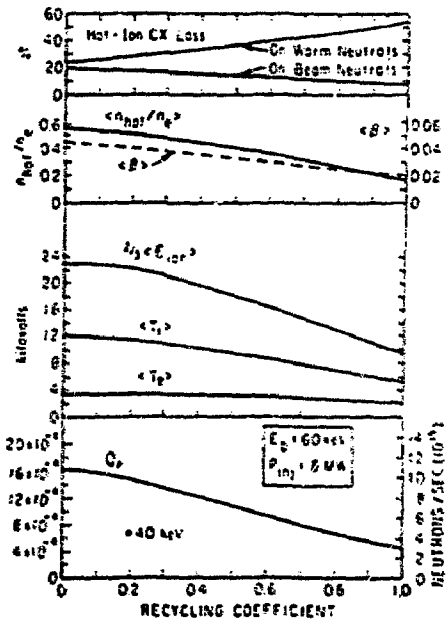


Fig. 1. Variation of spatially-averaged plasma parameters and fusion power gain  $Q_p$  with plasma recycling coefficient, for  $E_b = 60$  keV and  $P_{beam} = 8$  MW. (78-3357)

city distribution. Note that Coulomb collisions between ions injected in the same beam cause dispersion to velocities well above the injection velocity.

The accessibility of this CIT/TCT operation requires (1) that  $R_c \ll 1$ , (2) that the fast ions slow down classically, and (3) that the energetic ions remain close to their magnetic surfaces of birth while slowing down, a time that is of the order of 1.5 times the particle confinement time  $\tau_p$ . Charge-exchange loss, however, reduces the average hot-ion lifetime.

### 5. RADIAL PROFILES

Figure 3 shows the radial profiles of various plasma parameters for the cases  $R_c = 0.01$  and  $0.99$ . For  $R_c = 0.01$ , the neutral population at  $r < 30$  cm originates mainly from charge-exchange trapping of the neutral beams, while for  $R_c = 0.99$ , the neutral population is 2 to 3 times larger, and originates mainly by inward diffusion from the plasma boundary. Surprisingly,  $n_0$  is nearly the same for the two cases: for  $R_c = 0.01$ , the hot-ion lifetime is much longer, and these ions are assumed not to undergo radial diffusion; the much larger warm-ion population for  $R_c = 0.99$  undergoes relatively rapid diffusion. The average ion energy for  $R_c = 0.01$  is about twice that for  $R_c = 0.99$ , and results in several times higher  $Q_p$  (see Fig. 1). The fairly steep density profile but relatively shallow  $T_e$  profile are characteristic of plasmas with divertors operating in the "unload" mode.

### 6. VARIATION WITH BEAM POWER

Figure 4 shows the variation of species temperatures and neutron intensity,  $F_n$ , with beam power, when  $R_c = 0.20$ . It is found that  $Q_p$  is nearly proportional to  $\langle T_e \rangle$ , which increases more rapidly at lower values of  $P_{beam}$ . Thus  $F_n$  increases as  $P_{beam}^{1/2}$  at lower powers, but only linearly with  $P_{beam}$  at higher powers. These large neutron production rates are achieved with very small energy, namely 1 to  $1.5 \times 10^{12}$  cm<sup>-3</sup>s, but with very large average ion energy  $E_i \sim 25$  to 35 keV. (Here  $\tau_{ee}$  is the ratio of the total electron energy to the sum of the rates of electron energy loss by diffusion and radiation; diffusion is dominant.) At higher  $P_{beam}$  the predicted beta-values are near the largest that

Table 2. Illustrative Energetic-Ion Regime.

Beam energy	60 keV ( $0^\circ$ )
Beam power	8 MW
Recycling coef.	0.20
$n_e(0)$	$8.0 \times 10^{13}$ cm <sup>-3</sup>
$\langle n_{hot}/n_e \rangle$	0.51
$\langle Z_{eff} \rangle$	1.7 (iron)
$T_e(0)$	5.1 keV
$T_i(0)$	13.9 keV
$2/3 \times \bar{E}_{ion}(0)$	24.6 keV
$n_e(0)\tau_{ee}$	$3.9 \times 10^{12}$ cm <sup>-3</sup> s
Hot-ion lifetime	75 ms $\sim 1.2 \tau_{Ei}$
$\langle \beta \rangle$	0.041
<u>Neutron Production (D-D)</u>	
$Q_p$	$1.46 \times 10^{-3}$
Thermonuclear	$6.1 \times 10^{14}$ n/s
Beam-Target (TCT)	$4.0 \times 10^{15}$ n/s
Energetic-Ion	$5.4 \times 10^{15}$ n/s
Total intensity	$1.0 \times 10^{16}$ n/s

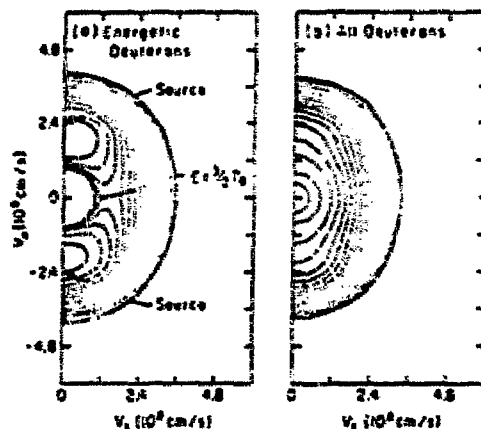


Fig. 2. Steady-state ion velocity distribution in PDX for co- and counter-injection at  $E_b = 60$  keV, with  $P_{beam} = 8$  MW and  $R_c = 0.2$ . Energetic ions enter warm Maxwellian at  $E = 3/2 T_e$ . (70-3369)

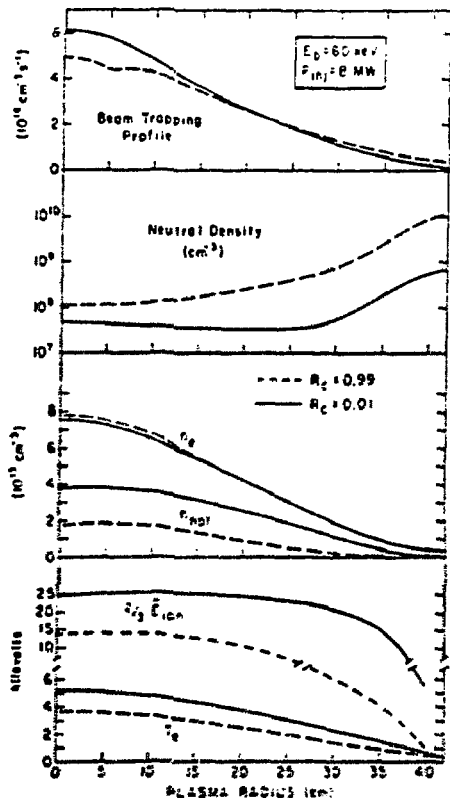


Fig. 3. Radial variation of steady-state plasma parameters for recycling coef.  $R_c = 0.01$  (solid line) and  $R_c = 0.99$  (dashed line). (76-3355)

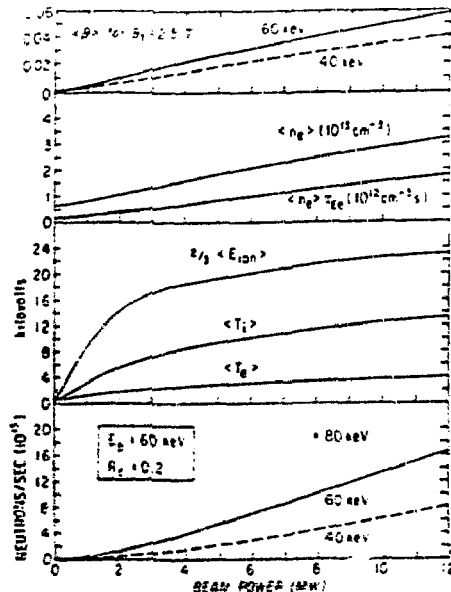


Fig. 4. Variation of spatially-averaged plasma parameters and fusion neutron intensity with beam power, for  $E_b = 60$  keV and recycling coef. = 0.2.  $\langle E_{ion} \rangle$  is average energy of all hot and warm ions. Dashed lines are for  $E_b = 40$  keV. (78-3356)

can in theory be sustained in a circular PDX plasma. About 85% of the plasma pressure is due to the ions, and 60% is due to the energetic ions alone. The reduced fusion production rate at  $E_b = 40$  keV is due to a smaller beam-target reaction rate and increased charge-exchange loss.

If the bulk plasma temperature could be attained by some means other than by reacting beam injection,  $F_n$  would be a factor of 10 to 30 lower. Furthermore, the property  $\langle T_i \rangle = 3\langle T_e \rangle$  is dependent to a great extent on beam fueling. If  $\langle T_i \rangle$  and  $\langle T_e \rangle$  were comparable, as expected to be the case with other heating methods, then  $F_n$  (and  $Q_0$ ) would be of the order of 1/100 of the values obtained in beam-driven energetic-ion operation. Finally, we note that parallel-antiparallel injection is not essential for producing large neutron intensities. For example, if approximately half the beams are injected tangentially and half perpendicularly, it is found that the fusion-neutron production is reduced by at most a factor of 1.5. With no opposing counter-injection, it should be possible for the co-injected beams to drive the plasma current [12], with relatively little penalty in neutron production.

## 7. SUMMARY

Plasmas with average ion energy exceeding 25 keV can be attained in medium-sized tokamak devices (i.e.,  $B_{Ta} \sim 1$  T-m) with intense neutral-beam injection, provided that plasma recycling is minimized by a magnetic divertor or getter assembly, and that essentially all fueling is performed by the beams. The energetic-ion density is then of the order  $0.5 n_e$ , and the warm-ion temperature is 2 to 3  $T_e$ . In PDX-sized plasmas with 4 to 10 MW of beam injection at  $E_b = 40$  to 60 keV, D-D fusion-neutron intensities in the range  $10^{15}$  to  $10^{16}$  n/s are attainable in this energetic-ion mode of operation. The electron energy confinement time need satisfy only  $\tau_{Ee} > \tau_{Ee} \sim 1$  to  $2 \times 10^{12}$  cm<sup>3</sup>s.

Initial beam-injection experiments in PLT at the 1-MW level [13] have demonstrated several features of the hot-ion/warm-electron plasmas that our analysis predicts for PDX. When  $n_e(0) < 5 \times 10^{13}$  cm<sup>-3</sup> with 1 MW of 38-keV D<sup>0</sup> injection, it is reported that  $n_{hot}/n_e \geq 0.2$  at the center of the plasma,  $T_i > T_e$  and  $\bar{E}_i(0) \approx 8$  keV. With co-injection alone, or co- and counter-injection together, the fast-ion slowing-down rate appears to be classical ( $\tau_s \sim 0.5 \tau_D$ ), with little radial drift of the fast ions [13, 14], thus justifying critical basic assumptions of the present analysis. The largest fusion-neutron intensity is obtained at lower densities, where gas influx and recycling are minimized, and up to 30% of the neutron production is due to reactions between energetic ions [14]. However, neutron intensities of the order of those calculated in this paper will be attainable only by eliminating gas influx entirely, and by minimizing recycling with an effective magnetic divertor or large-area getter pumping system.

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