

MASTER

DIPROTON RESONANCES IN THE MASS REGION 2100 TO 2800 MeV

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Meeting on Exotic Resonances
Hiroshima, Japan
September 1-2, 1978



UIC-AUA-USDOE

ARGONNE NATIONAL LABORATORY, ARGONNE, ILLINOIS

Operated under Contract W-31-109-Eng-38 for the
U. S. DEPARTMENT OF ENERGY

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Abstract

A striking energy dependence has been observed in the difference between the p-p total cross sections for parallel and antiparallel longitudinal spin states, $\Delta\sigma_L = \sigma^{\text{Tot}}(\uparrow\downarrow) - \sigma^{\text{Tot}}(\uparrow\uparrow)$. The structure appears around $p_{\text{lab}} = 1.5 \text{ GeV}/c$ where $\Delta\sigma_L = -16.7 \text{ mb}$ and is seen in $\sigma^{\text{Tot}}(\uparrow\downarrow)$ rather than $\sigma^{\text{Tot}}(\uparrow\uparrow)$. The experiments were performed at Argonne National Laboratory using a standard transmission technique.

From the dispersion analysis of a forward p-p scattering amplitude using the data on $\Delta\sigma_L$, Grein and Kroll have shown that the Argand plot of the amplitude has a clear resonance-like behavior around proton-incident momentum of 1.5 GeV/c. At the same energy range, the p-p polarization at fixed $-t$ also shows a remarkable energy dependence. In addition, we have observed a prominent energy dependence for C_{LL} , the spin correlation parameter for elastic $p\bar{p}$ scattering with beam and target both longitudinally polarized. The possibility of a resonance was further pursued by studying Legendre expansion coefficients of p-p differential cross section and polarization data. The analysis showed a partial wave,

*Work supported by the U.S. Department of Energy.

3F_3 consistent with having a resonant behavior. Based on a phase-shift analysis, Hoshizaki also showed that 3F_3 seems to resonate. This resonant state would have the quantum number $J^P = 3^-$, mass ~ 2260 MeV, width ~ 200 MeV and elasticity 20-30%. This exotic state may be described by the MIT bag model.

We also speculate several more diproton resonances in the mass region 2100 to 2800 MeV.

Introduction

We would like to start out by discussing the proton-proton total cross-section data at the intermediate-energy region. As shown in Fig. 1, up to 1.2-GeV/c incident proton momentum, the total cross section, which mainly consists of the elastic process, falls and then rises due to the inelastic-channel opening. The cross section flattens above 1.5 GeV/c. We observe no structures that may suggest the possible existence of a resonance.

However, we have observed totally unexpected structures in the total cross section when both the incident protons and target protons were longitudinally polarized. The most remarkable structure appears around $p_{lab} = 1.5$ GeV/c.

We mainly discuss the existence of at least one diproton resonance and its properties, and speculate three more such candidates. Such a resonance opens a new era in the nucleon-nucleon system and also is crucially important for further development of the quark models that require six quarks in a bag.¹⁻³

First, we describe experimental observables in terms of the helicity amplitudes, and then in terms of singlet and triplet partial-wave amplitudes. There are three s-channel helicity amplitudes at $\theta_{\text{c.m.}} = 0$:

$$\phi_1 = \langle ++ | ++ \rangle,$$

$$\phi_2 = \langle -- | ++ \rangle, \text{ and}$$

$$\phi_3 = \langle +- | +- \rangle.$$

These amplitudes are related to total cross section as follows:

i) Spin averaged total cross section

$$\sigma^{\text{Tot}} = (2\pi/k) \text{Im} \{ \phi_1(0) + \phi_3(0) \} = (1/2) \{ \sigma^{\text{Tot}}(\vec{\leftrightarrow}) + \sigma^{\text{Tot}}(\vec{\rightarrow}) \} \quad (1)$$

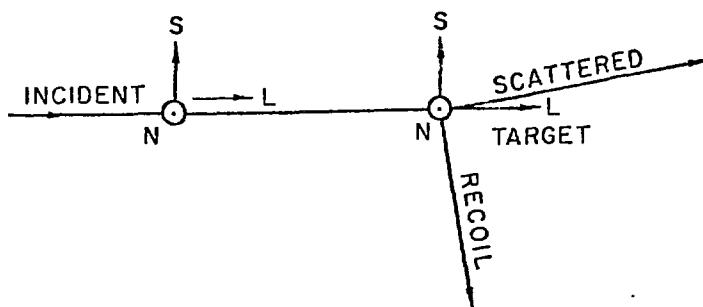
ii) Difference between total cross sections for parallel and antiparallel spin states (longitudinal)

$$\Delta\sigma_L = (4\pi/k) \text{Im} \{ \phi_1(0) - \phi_3(0) \} = \{ \sigma^{\text{Tot}}(\vec{\leftrightarrow}) - \sigma^{\text{Tot}}(\vec{\rightarrow}) \} \quad (2)$$

iii) Difference between total cross sections for parallel and antiparallel spin states (transverse)

$$\Delta\sigma_T = -(4\pi/k) \text{Im} \phi_2(0) = \sigma^{\text{Tot}}(\uparrow\downarrow) - \sigma^{\text{Tot}}(\uparrow\uparrow) \quad (3)$$

Argonne ZGS facilities provide various spin directions of incident beam and target. Spin directions are illustrated below. To express observables in elastic scattering, we adopt the notation (Beam, Target; Scattered, Recoil); $(0, N; 0, 0)$ for polarization, $(N, N; 0, 0)$ and $(L, L; 0, 0)$ for spin correlation parameters, etc. A typical experimental setup for $\Delta\sigma_L$ is shown in Fig. 2 (a). The measurements were done in standard transmission experiment.



N: NORMAL TO THE SCATTERING PLANE

L: LONGITUDINAL DIRECTION

S = N x L IN THE SCATTERING PLANE

$\Delta\sigma_L$ and $\Delta\sigma_T$ Measurements

We show the results of $\Delta\sigma_L$ measurements from 1.0 to 6.0 GeV/c (Fig. 3a).⁴⁻⁶ There is a sharp peak near 1.2 GeV/c and a dip near 1.5 GeV/c. From Eq. 2, a structure in $\phi_1(0)$ and $\phi_3(0)$ should appear as a peak and dip, respectively, in $\Delta\sigma_L$. Figure 3b shows $\sigma^{\text{Tot}}(\frac{1}{2})$ and $\sigma^{\text{Tot}}(\frac{3}{2})$ as obtained from Eqs. 1 and 2. There is a clear bump in $\sigma^{\text{Tot}}(\frac{1}{2})$. We observe the third structure in $\sigma^{\text{Tot}}(\frac{1}{2})$ near 2.0 GeV/c although that is not as remarkable as the one appearing in $\Delta\sigma_T$.

In Fig. 4, preliminary results of several $\Delta\sigma_L$ measurements up to 12 GeV/c are shown. (Several momentum points between 3 and 6 GeV/c have been measured, but they are not shown in the Figure.)

To study the behavior in terms of the partial scattering amplitudes, the data on $(k^2/4\pi)\Delta\sigma_L$ together with $(k^2/4\pi)\Delta\sigma_T$ are plotted in Fig. 5 as a function of the center-of-mass energy,⁷ where k is the c.m. momentum. If the dip in $\Delta\sigma_L$ is considered to be due to a resonance, the mass is about 2260 MeV with a width of about 200 MeV. The 1.2-GeV/c peak is seen in $\Delta\sigma_L$ and possibly in $\Delta\sigma_T$ data. The 2.0-GeV/c peak is clearly visible in $\Delta\sigma_T$.

Using the data on $\Delta\sigma_L$, Grein and Kroll have calculated the real part of $[\phi_1(0) - \phi_3(0)]$ by applying dispersion relations.⁸ In the Argand plot of the $[\phi_1(0) - \phi_3(0)]$ amplitude, we observe a clear resonance-like behavior around the incident proton momentum of 1.5 GeV/c (mass \approx 2260 MeV) and possibly at 1.2 GeV/c (mass \approx 2100 MeV) as shown in Fig. 6.

When the helicity amplitudes are decomposed into partial waves,⁹

$$\text{Im}\phi_1(0) = \frac{1}{k} \sum_J \text{Im} \left\{ (2J+1)R_J + (J+1)R_{J+1,J} + JR_{J-1,J} + 2[J(J+1)]^{\frac{1}{2}}R^J \right\}, \quad (4)$$

$$\text{Im}\phi_2(0) = \frac{1}{k} \sum_J \text{Im} \left\{ -(2J+1)R_J + (J+1)R_{J+1,J} + JR_{J-1,J} + 2[J(J+1)]^{\frac{1}{2}}R^J \right\}, \quad (5)$$

and

$$\text{Im}\phi_3(0) = \frac{1}{k} \sum_J \text{Im} \left\{ (2J+1)R_{JJ} + JR_{J+1,J} + (J+1)R_{J-1,J} - 2[J(J+1)]^{\frac{1}{2}}R^J \right\}, \quad (6)$$

where R_J is the spin-singlet partial-wave amplitudes with $J = L = \text{even}$, R_{JJ} and $R_{J\pm 1,J}$ are spin-triplet waves with $J = L = \text{odd}$ and $J = L \mp 1 = \text{even}$, respectively, and R^J is the mixing term. The partial wave characteristics to $\phi_1(0)$ is R_J and to $\phi_3(0)$ is R_{JJ} ; the peak in Fig. 3a is due to one of the singlets $^1S_0, ^1D_2, \dots$, and the dip is due to one of the triplets $^3P_1, ^3F_3, \dots$.

Structure in σ_{el}^{Tot} and Polarization

So far, such a behavior is discussed only at $|t|=0$, and the properties of the possible resonance (e.g., spin and parity) are not determined. One needs to study the angular distributions of the observables in pp scattering. Let us see if we observe a similar structure in other channels. Figure 7 shows the elastic total cross section, $\sigma_{el}^{Tot 10,11}$. There is also a structure in the plot of polarization against incident momentum at fixed $|t|$, as shown in Fig. 8.¹² We note that the structure in polarization has nothing to do with the peak in $\Delta\sigma_L$ at 1.2 GeV/c , because the polarization does not include singlet terms.

Legendre Coefficient Analysis

We pursue the possibility of the existence of such a resonance and investigate the nature of the possible resonance by studying differential cross-section and polarization data in pp elastic scattering around 1.5 GeV/c . Our interest then is to investigate if an R_{JJ} partial wave has the behavior of a Breit-Wigner formula. The effect of resonances can be studied through the energy dependence of the Legendre expansion coefficients obtained from the differential cross-section and polarization data.^{11,12} We report the results of such an analysis using data at 1.0 - 2.0 GeV/c .⁹ The analysis was carried out by looking at the energy dependence of the coefficients a_n and b_n in the expansions:

$$d\sigma/d\Omega = \chi^2 \sum_{n=0}^N a_n P_n(\cos\theta) \quad (7)$$

$$Pd\sigma/d\Omega = \chi^2 \sum_{n=2}^N b_n P_n^{(1)}(\cos\theta) \quad (8)$$

These coefficients are related to various partial waves, and we show only relevant relations here.

The coefficients a_n , obtained by fitting differential cross-section data to Eq. 7, mainly tell us that the highest significant value of J is four; a_8 and higher coefficients are nearly zero, and we ignore those terms with $J > 4$ and $L > 4$. Figure 9 shows the coefficients b_n obtained by fitting the product of differential cross-section and polarization data, plotted against incident momentum and energy. All coefficients up to and including b_6 have a remarkable energy dependence around $p_{\text{lab}} \approx 1.5 \text{ GeV/c}$. We need to know if such a rapid change is due to one or two resonant partial waves while the other amplitudes vary slowly with energy; our particular attention is on the R_{jj} partial waves, 3P_1 and 3F_3 . We determine how the behavior compares with the Breit-Wigner formula,

$$A_{\text{res}} = (\epsilon + i) (\Gamma_{\text{el}}/\Gamma) / (\epsilon^2 + 1), \text{ where } \epsilon = 2(E_0 - E)/\Gamma \quad (9)$$

The energy dependence of this formula is illustrated in Fig. 9.

In general, the coefficient with higher order is easier to interpret because fewer terms are involved. The coefficient b_6 is related to the partial-wave amplitude by

$$b_6 = 1.8 (\text{Im}^3F_3 \text{Re}^3F_4 - \text{Re}^3F_3 \text{Im}^3F_4) + \dots, \quad (10)$$

where residual terms (...) include neither 3F_3 nor 3P_1 . A rise in b_6 with respect to energy is consistent with 3F_3 following the Breit-Wigner formula while other amplitudes vary slowly with energy; the value of the first term in Eq. 10 is the same both before and after resonance, say at 2110 and 2410 MeV, respectively, and the difference in b_6 at these energies is due to the second term, which has $-\text{Re}A_{\text{res}}$ changing from minus to plus ($\text{Im}^3F_4 > 0$ by unitarity). We note that 3P_1 , another

possible resonance candidate in R_{JJ} , is absent in b_6 . Other coefficients are also consistent with the interpretation.

$C_{LL} = (L,L;0,0)$ Measurements

Simultaneously with $\Delta\sigma_L$ measurements, we have measured the spin-spin correlation parameter $C_{LL}(\theta_{c.m.}) = (L,L;0,0)$ in p-p elastic scattering for $70^\circ \leq \theta_{c.m.} \leq 110^\circ$ at $p_{lab} = 1.0$ to 3.0 GeV/c.¹³ A typical experimental setup is shown in Fig. 2(b).

The differential cross section for a particular spin direction of beam and target, $I^{\pm\pm}$, is given by

$$I^{\pm\pm}(\theta_{c.m.}) = I_0(\theta_{c.m.}) [1 + (\pm P_B)(\pm P_T)C_{LL}(\theta_{c.m.})], \quad (11)$$

where P_B and P_T are the beam and target polarization respectively, and $(+)$ $(-)$ refers to the spin state parallel (antiparallel) to the L direction (beam direction); $I_0(\theta_{c.m.})$ is the spin-averaged differential cross section. The parameter $C_{LL}(\theta_{c.m.})$ is then found to be

$$C_{LL}(\theta_{c.m.}) = \frac{1}{P_B P_T} \frac{(I^{++} + I^{--}) - (I^{+-} + I^{-+})}{(I^{++} + I^{--}) + (I^{+-} + I^{-+})}. \quad (12)$$

Figure 10 shows the angular dependence observed for the parameter C_{LL} at various incident-beam momenta. The errors shown are purely statistical, which dominate over systematic errors. The values of C_{LL} are all positive over the range covered, and are consistent with a symmetry about $\theta_{c.m.} = 90^\circ$ as expected for scattering of identical particles. Figure 10 also shows the predicted curves from existing phase-shift solutions.¹⁴

The values of C_{LL} at $\theta_{c.m.} = 90^\circ$ are plotted with respect to the incident momenta as shown in Fig. 11. We observe a sharp dip near $p_{lab} =$

1.2 GeV/c, rapid decrease near 1.5 GeV/c, and additional structure near $p_{lab} = 2.0$ GeV/c. A way to study these structures is to define C_{LL} in terms of partial wave amplitudes. Using the s-channel helicity amplitudes $\phi_1 = \langle ++|\phi|++\rangle$, $\phi_2 = \langle --|\phi|++\rangle$, $\phi_3 = \langle +-|\phi|+-\rangle$, $\phi_4 = \langle +-|\phi|-+\rangle$, and $\phi_5 = \langle ++|\phi|+-\rangle$, we have

$$C_{LL} (d\sigma/d\Omega) = \frac{1}{2} \left[-|\phi_1|^2 - |\phi_2|^2 + |\phi_3|^2 + |\phi_4|^2 \right], \quad (13)$$

where $d\sigma/d\Omega = \frac{1}{2} \left[|\phi_1|^2 + |\phi_2|^2 + |\phi_3|^2 + |\phi_4|^2 + 4|\phi_5|^2 \right]$ is the spin-averaged differential cross section.

The amplitudes ϕ_1 through ϕ_5 are then expanded in terms of partial wave amplitudes. The spin-singlet partial waves, 1S_0 , 1D_2 , 1G_4 ..., appear in ϕ_1 and ϕ_2 with opposite signs, and the spin-triplet partial waves with $L = J = \text{odd}$, 3P_1 , 3F_3 ..., appear in ϕ_3 and ϕ_4 with opposite signs.

Figure 12a shows the quantity $on k^2 C_{LL} (d\sigma/d\Omega)$ at $\theta_{c.m.} = 90^\circ$ plotted with respect to the incident momenta.¹⁵ This quantity is dimensionless and allows us to study the contributions of partial waves more directly.

First we examine if the rapid decrease observed in Figs. 11 and 12a near $p_{lab} = 1.5$ GeV/c is consistent with the partial wave 3F_3 having a resonant behavior.⁹ Eq. 13 can be expressed in terms of 3F_3 and interfering partial waves as

$$[k^2 C_{LL} (d\sigma/d\Omega)]_{90^\circ} = [0.77 |^3F_3|^2 + a(\text{Re } ^3F_3) + b(\text{Im } ^3F_3) + \dots], \quad (14)$$

where a (b) is the real (imaginary) part of the sum of other partial waves and the values can be estimated from the results of a phase-shift analysis.¹⁴ By substituting these values and the 3F_3 resonance at mass = 2260 MeV with a width = 200 MeV and elasticity = 0.2 into Eq. 14, we find the same amount of rapid decrease as shown in Fig. 12a.

Next, we discuss the structure around $p_{\text{lab}} = 2 \text{ GeV}/c$ in Fig. 12a. From the resonant-like structure in $(k^2/4\pi)\Delta\sigma_T$ as shown in Fig. 5, we expect it is due to a singlet spin state.^{6,7} The contribution of spin singlet waves to Eq. 13 is

$$k^2 C_{LL} (\text{d}\sigma/\text{d}\Omega) = -|{}^1S_0 + 5{}^1D_2 P_2(\cos\theta) + 9{}^1G_4 P_4(\cos\theta) + \dots|^2 + \dots, \quad (15)$$

in which the contribution of 1G_4 vanishes at $\theta \approx 70^\circ$, where $P_4 = 0$.

The structure around 2 GeV/c is absent in Fig. 12(b), where the values of $k^2 C_{LL} \text{d}\sigma/\text{d}\Omega$ at $\theta_{\text{c.m.}} = 70^\circ$ are plotted as a function of beam momentum. Thus we may conclude that 1G_4 wave is responsible for the structure.¹⁶

Next, we discuss the sharp dip observed at 1.17 GeV/c as shown in Figs. 12a and 12b. We consider this due to a spin-singlet wave, because structures also appear as a peak both in $\Delta\sigma_L$ and $\Delta\sigma_T$.^{6,7} In particular, we suspect they are due to the 1D_2 wave, because it is the only wave that couples to the s wave $N\Delta$ state, which is responsible for the rapid increase of pp total cross section near 1.2 GeV/c. We also point out that a resonance-like bump was observed in the cross-section of $pp \rightarrow \pi d$ in the same energy range,¹⁷ which is usually interpreted in terms of the final-state interaction between one of the nucleons and π , forming $\Delta(1236)$ in the intermediate state.

The dip structure in Figs. 12a and 12b may come from the resonant-like behavior of the 1D_2 state.^{14,18,19}

We conclude that the measurement of the spin-spin correlation parameter C_{LL} in pp elastic scattering near $\theta_{c.m.} = 90^\circ$ has revealed rich structure in $p_{lab} = 1.0 - 3.0$ GeV/c, which is consistent with the presence of 3F_3 , and possibly 1G_4 and 1D_2 resonances.

$$C_{NN} = (N, N; 0, 0) \text{ Measurements at } \theta_{c.m.} = 90^\circ$$

The measurement of the spin-spin correlation parameter C_{NN} in pp elastic scattering at $\theta_{c.m.} = 90^\circ$ also reveal a strong energy dependence. A plot of $k^2 C_{NN} (\partial\sigma/\partial\Omega)$ in the momentum region 1 to 6 GeV/c is shown in Fig. 13.^{20,21} We find that the energy dependence is consistent with the existence of 1D_2 and 3F_3 resonances.

Real Part of Scattering Amplitude at $|t| = 0$

The real part of scattering amplitude in the forward region in pp elastic scattering has been experimentally determined.²² A plot of Re/Im at $|t| = 0$ is shown in Fig. 14. The real part changes from positive to negative as energy increases and becomes zero at around 1.5 GeV/c. The behavior is consistent with the existence of 1D_2 and 3F_3 resonances.¹⁴

Any Other Structure?

Do we observe any structure above a mass of 2500 MeV? Measurements of $\Delta\sigma_L$ and $\Delta\sigma_T$ are yet to be made at small-momentum interval. But we observe a remarkable energy dependence in $C_{NN} = (N, N; 0, 0)$ data at all angles²³ and also at $\theta_{c.m.} = 90^\circ$.²¹ As shown in Fig. 10 $C_{LL} = (L, L; 0, 0)$ data are all positive at large angle up to 3.0 GeV/c, but we observe negative values as large as -35% at 6 GeV/c.²⁴

Theoretical Models Without Resonances

There are several attempts to explain the structure in $\Delta\sigma_L$ data by Deck models,²⁵ by opening of inelastic channels, etc.^{26,27} So far, none of the models explained the structure at 1.5 GeV/c.

Conclusion

A summary of diproton resonances is given in Table I. The name, B^2 , of resonances was adopted during the Tokyo conference.

Table I

Diproton Resonances

Name	$B^2(2.14)$	$B^2(2.22)$	$B^2(2.43)$
Mass, GeV	2.14 - 2.17	2.20 - 2.26	2.43 - 2.50
I	1	1	1
Width, MeV	50-100	100-150	~ 150
Elasticity	~ 0.1	~ 0.2	
pp State	1D_2	3F_3	1S_0 or 1G_4
Remarks	$\Delta\sigma_L, \Delta\sigma_T, C_{LL}$ Arndt et al. Hoshizaki	$\Delta\sigma_L, P, C_{LL}$ Hidaka et al. Hoshizaki	$\Delta\sigma_T, C_{LL}$ Hoshizaki

We are aware that the structure in $\Delta\sigma_L$ around 1.5 GeV/c consists of both singlet and triplet spin states. As shown in Fig. 5, $\Delta\sigma_T$ data contain only singlet structures. Then we expect to see only the triplet structure in $(\Delta\sigma_T - \Delta\sigma_L)$ as shown in Fig. 15. In this case the mass of $B^2(2.22)$ would be somewhat higher.

Present Status of $\Delta\sigma_L$ Measurements in the pn System

We are currently measuring the parameter $\Delta\sigma_L$ in pn scattering covering the momentum region of 1.0 to 3.0 GeV/c. We can investigate possible structures in $l = 0$ state. The results will be available within several weeks.

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FIGURE CAPTIONS

Fig. 1 PP Total Cross Section

Fig. 2a Beam Line for the $\Delta\sigma_L$ Measurement

Fig. 2b Experimental Setup for the $C_{LL} = (L, L; 0, 0)$ Measurement

Fig. 3a Total Cross-Section Difference $\Delta\sigma_L = \sigma^{\text{Tot}}(\vec{\gamma}) - \sigma^{\text{Tot}}(\vec{\gamma})$

Fig. 3b Total Cross Sections for Pure Initial Spin States. The dotted curves are only to guide the eye.

Fig. 4 Total Cross Section Difference, $\Delta\sigma_L$, up to 12 GeV/c

Fig. 5 $(k^2/4\pi) \Delta\sigma_L$ Together With $(k^2/4\pi) \Delta\sigma_T$

Fig. 6 Argand Plot of the $[\phi_1(0) - \phi_3(0)]$

Fig. 7 Elastic Total Cross Section

Fig. 8 Polarization at $0.1 < |t| < 0.2$

Fig. 9 Results of Legendre Coefficient Analysis

Fig. 10 $C_{LL} = (L, L; 0, 0)$ Data at 1.0 to 2.5 GeV/c

Fig. 11 $C_{LL} = (L, L; 0, 0)$ at $\theta_{\text{c.m.}} = 90^\circ$

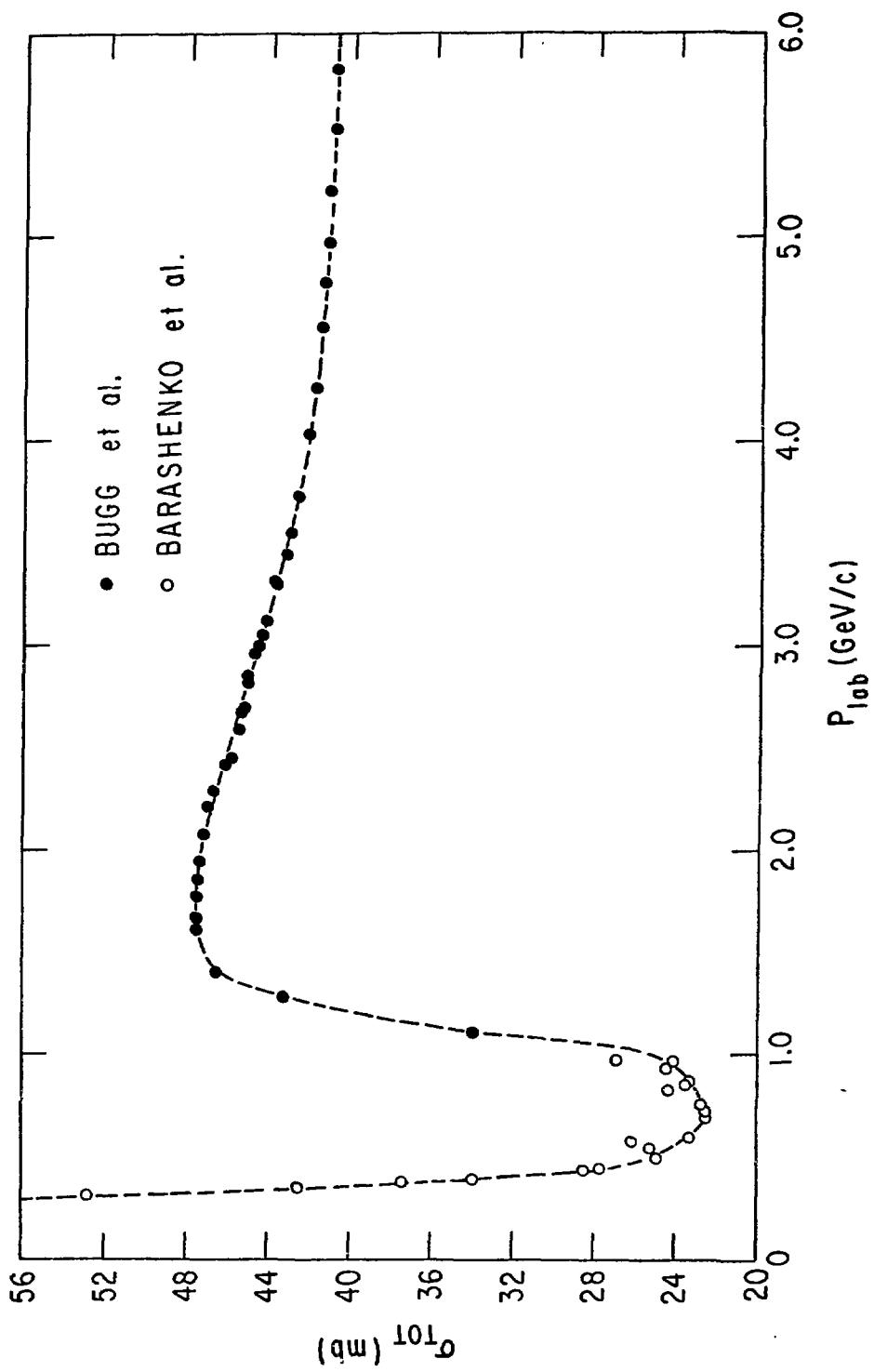
Fig. 12a $k^2 C_{LL} (\text{d}\sigma/\text{d}\Omega)$ at $\theta_{\text{c.m.}} \approx 90^\circ$ vs. p_{lab} . The dashed curve is only to guide the eye. The solid curve is the contribution of the F_3 resonance over a smooth background.

Fig. 12b $k^2 C_{LL} (\text{d}\sigma/\text{d}\Omega)$ at $\theta_{\text{c.m.}} \approx 74^\circ$ vs. p_{lab} . The dashed curve is only to guide the eye.

Fig. 13 $k^2 C_{NN} (\text{d}\sigma/\text{d}\Omega)$ at $\theta_{\text{c.m.}} = 90^\circ$.

Fig. 14 Re/Im at $|t| = 0$.

Fig. 15 $(k^2/4\pi)(\Delta\sigma_T - \Delta\sigma_L)$



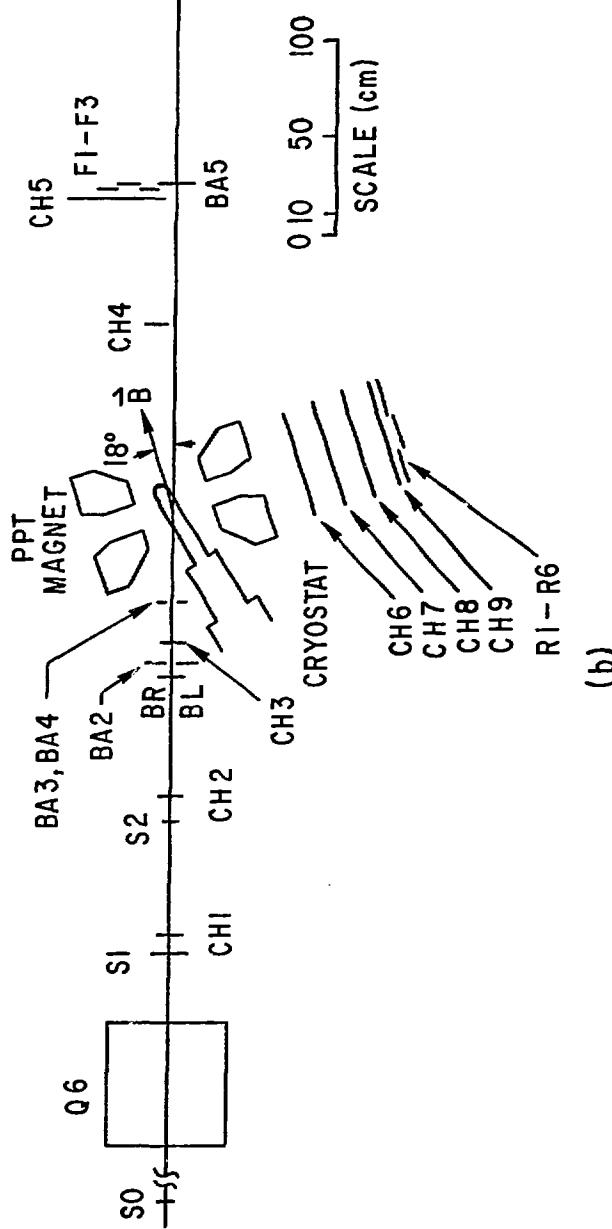
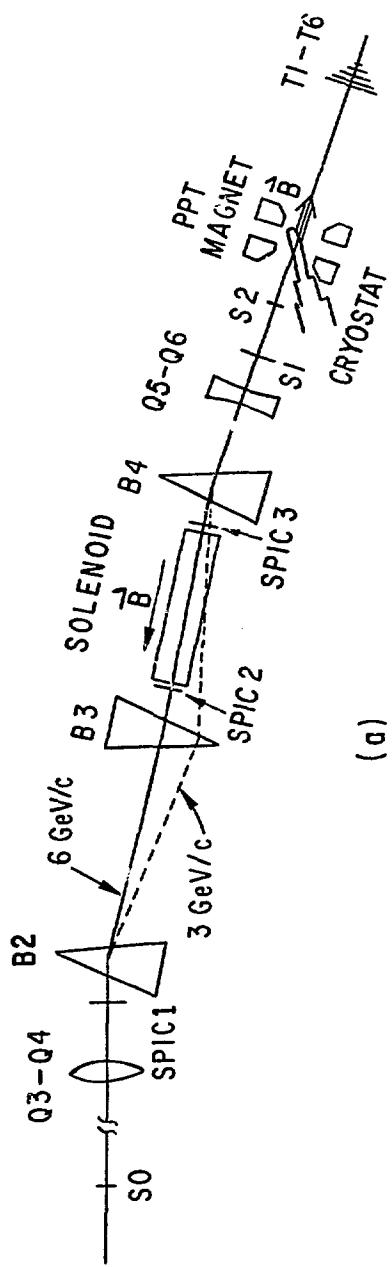


Fig. 2

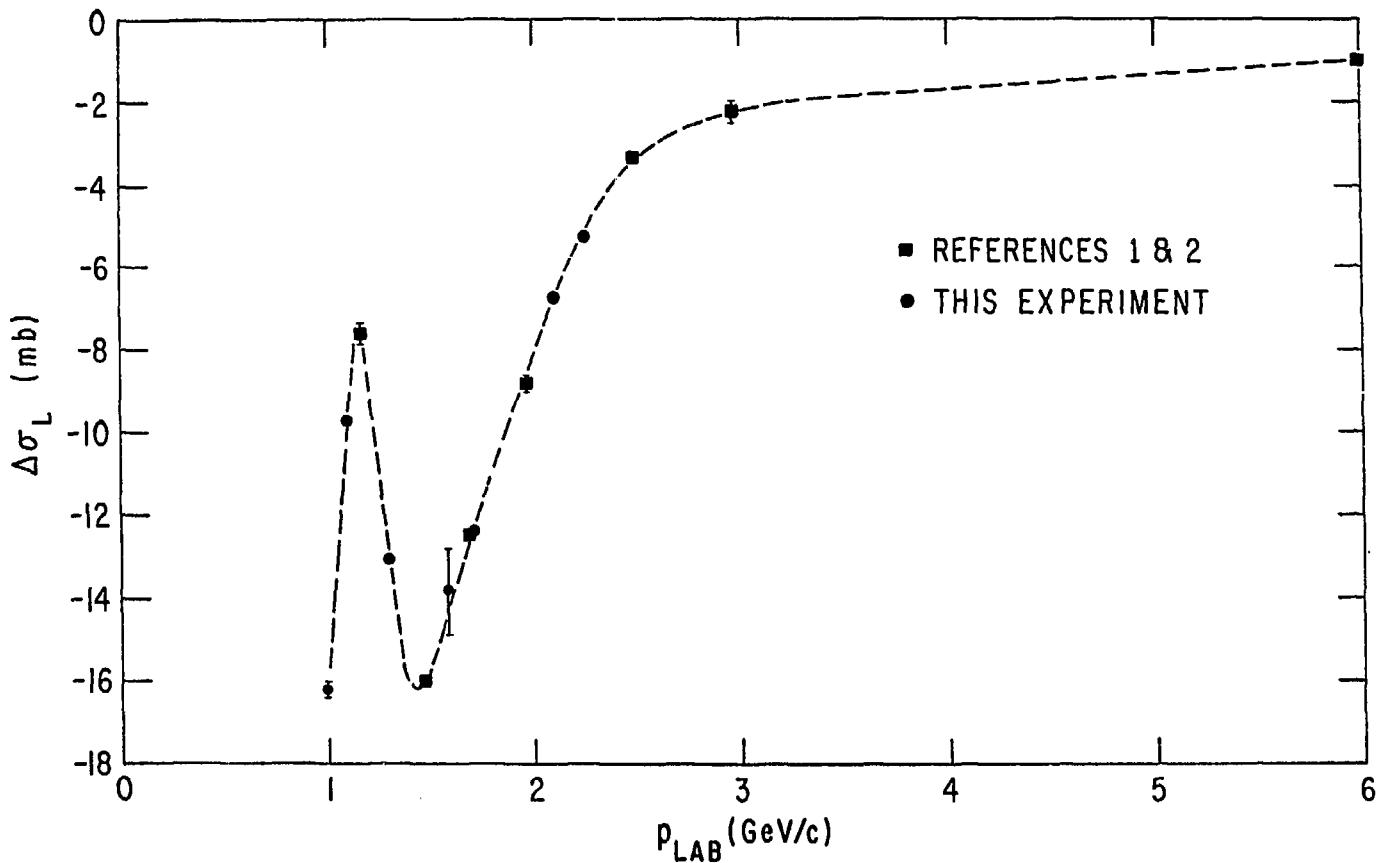


Fig. 3a

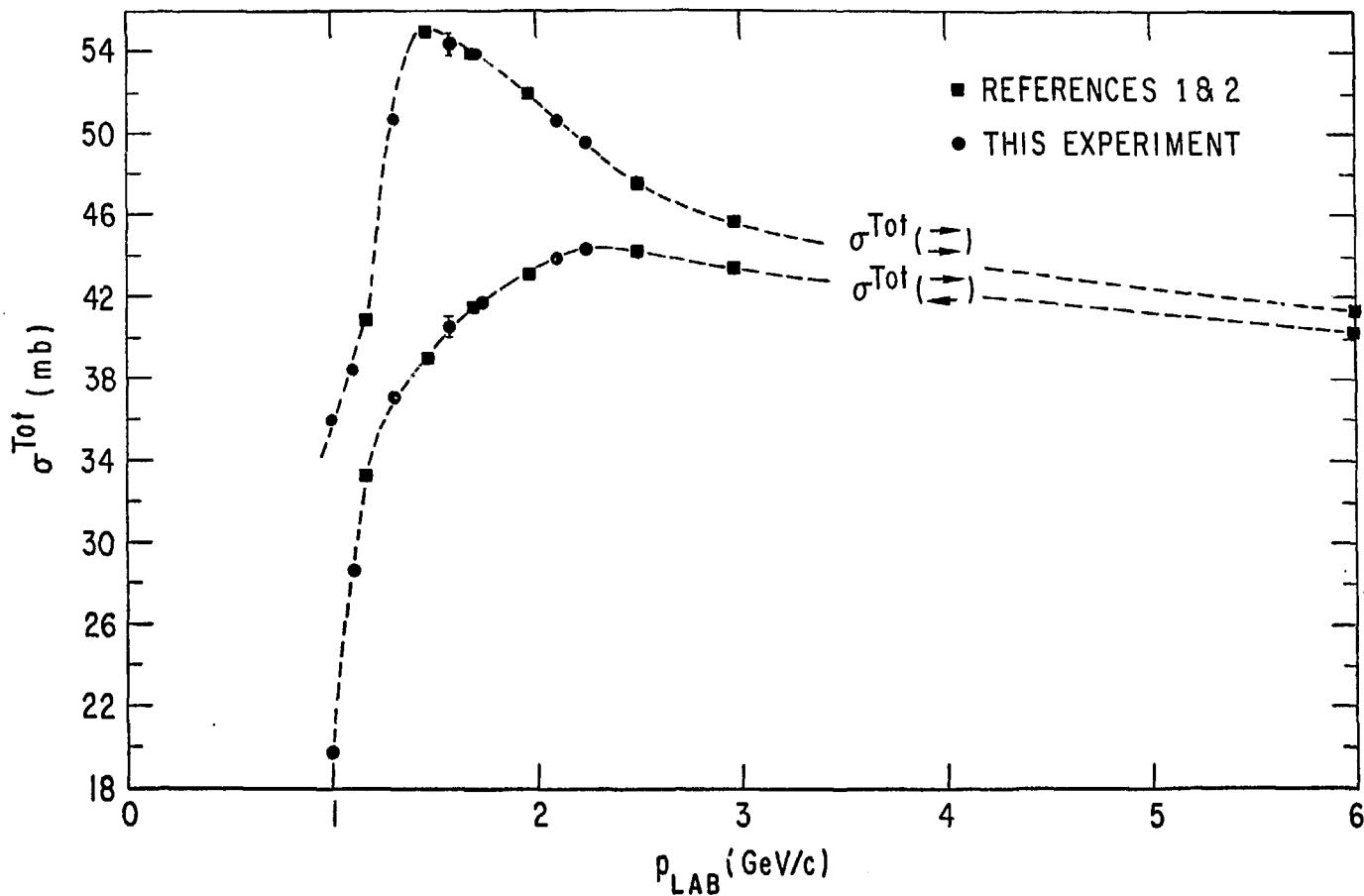


Fig. 3b

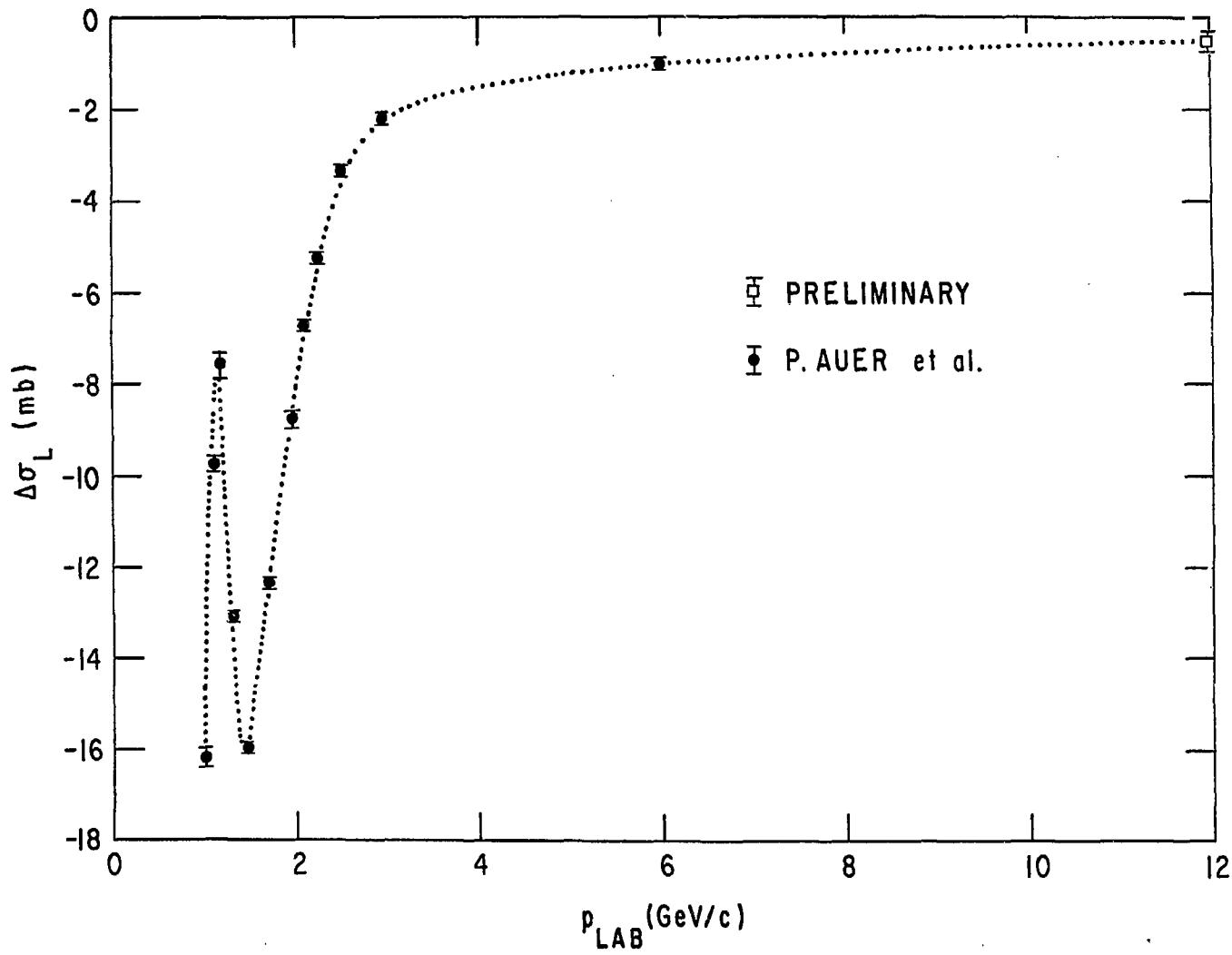


Fig. 4

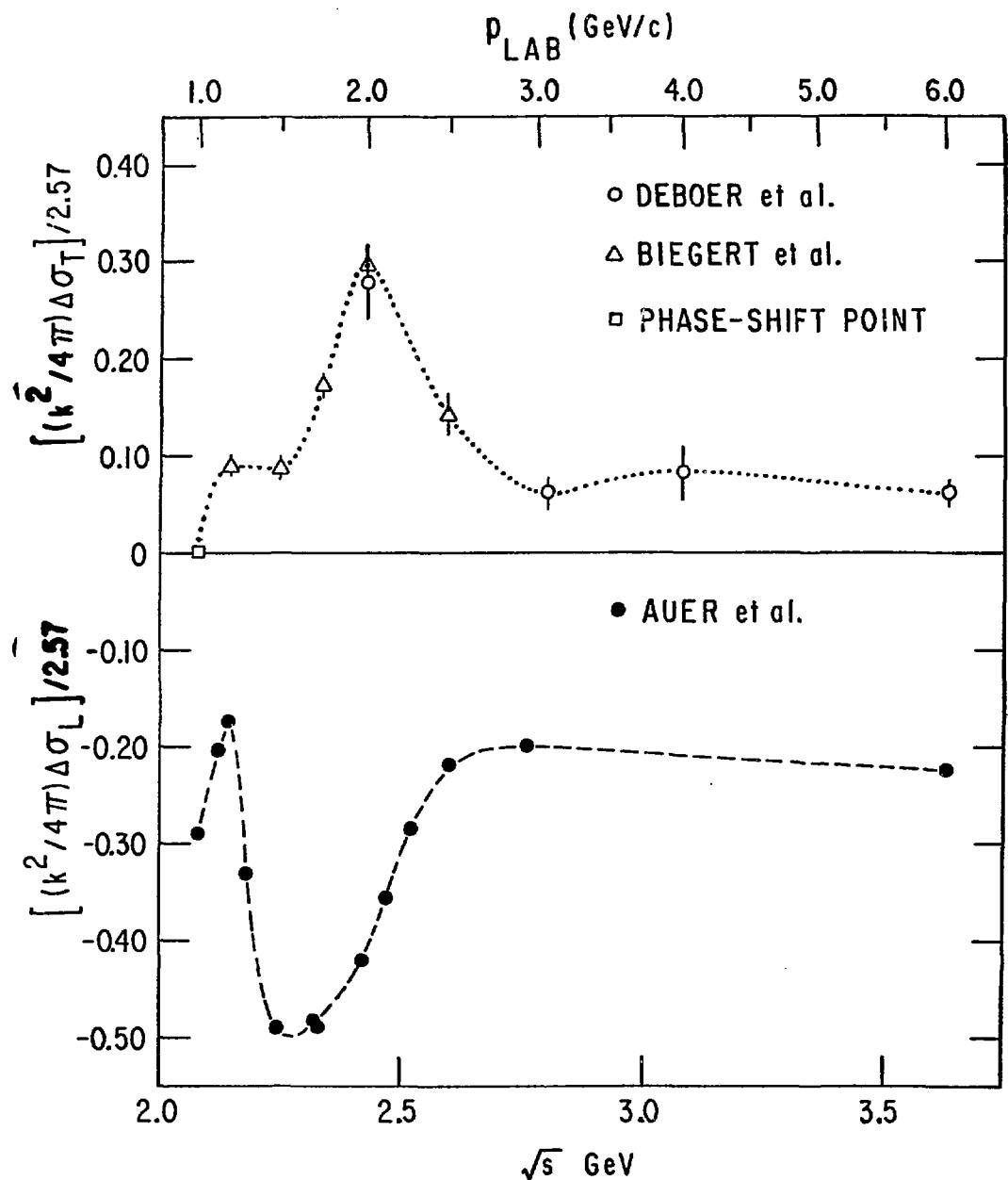


Fig. 5

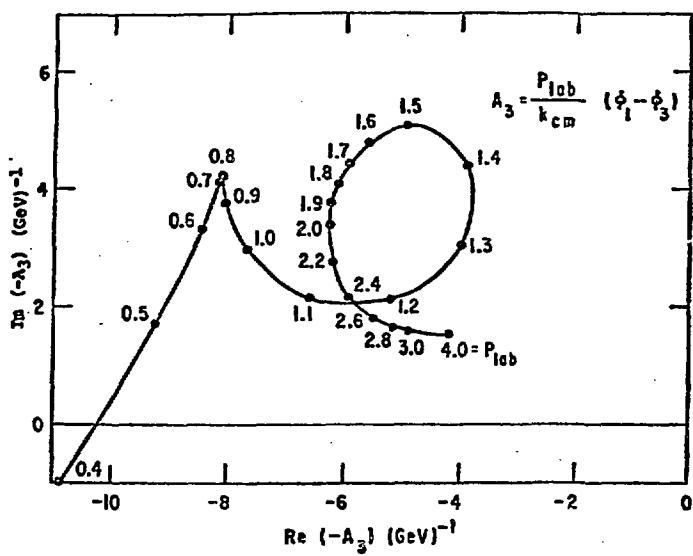


Fig. 6

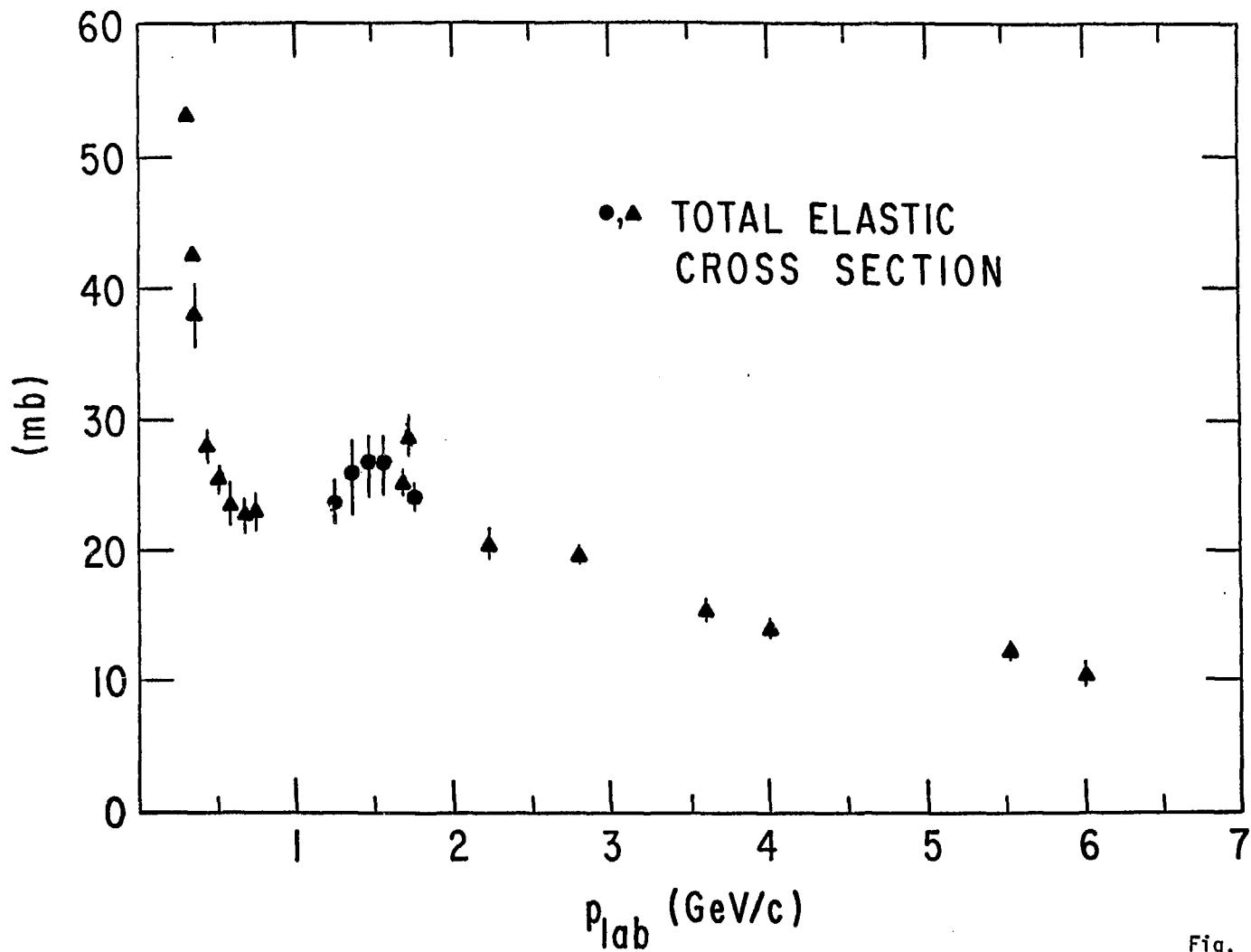


Fig. 7

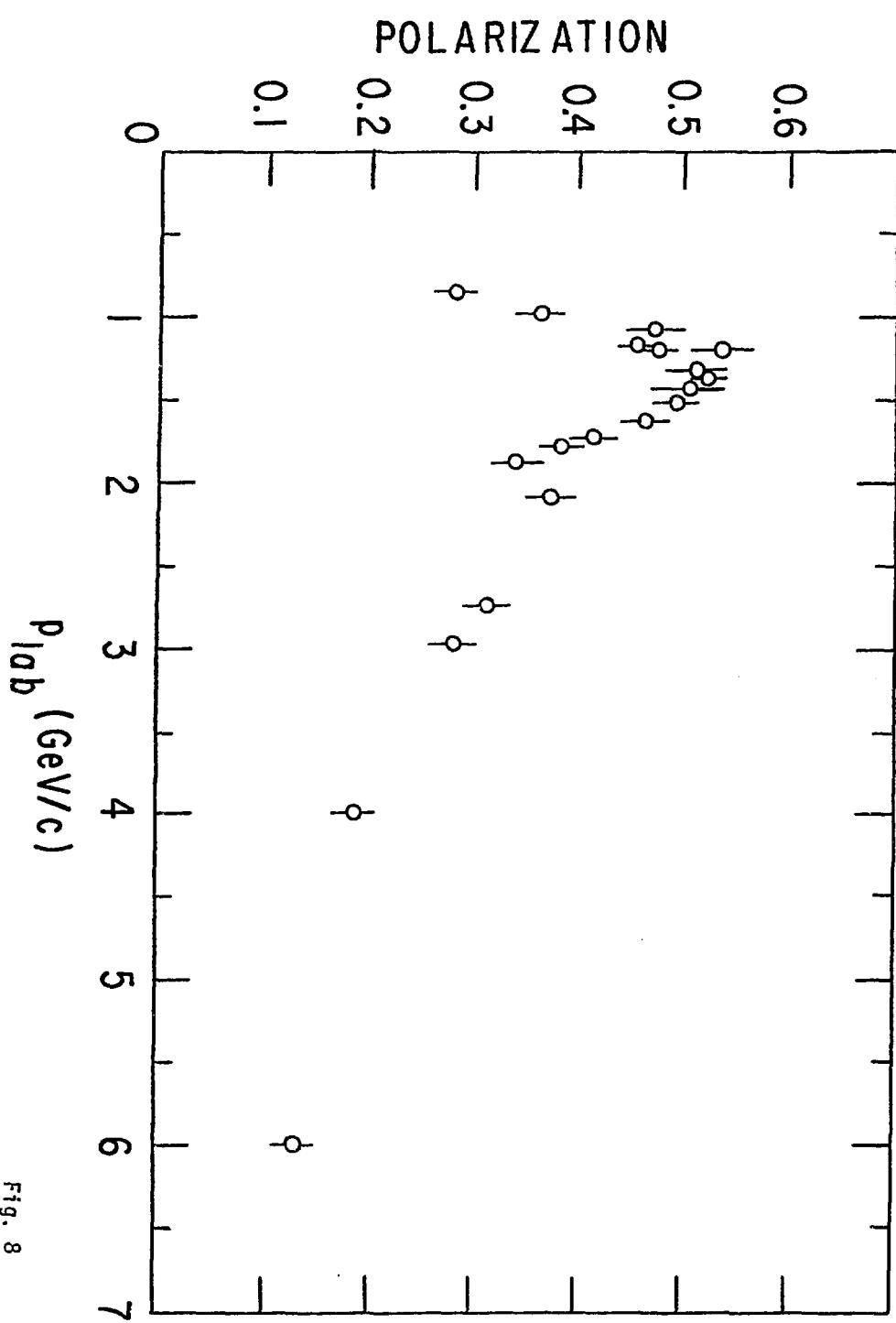


Fig. 8

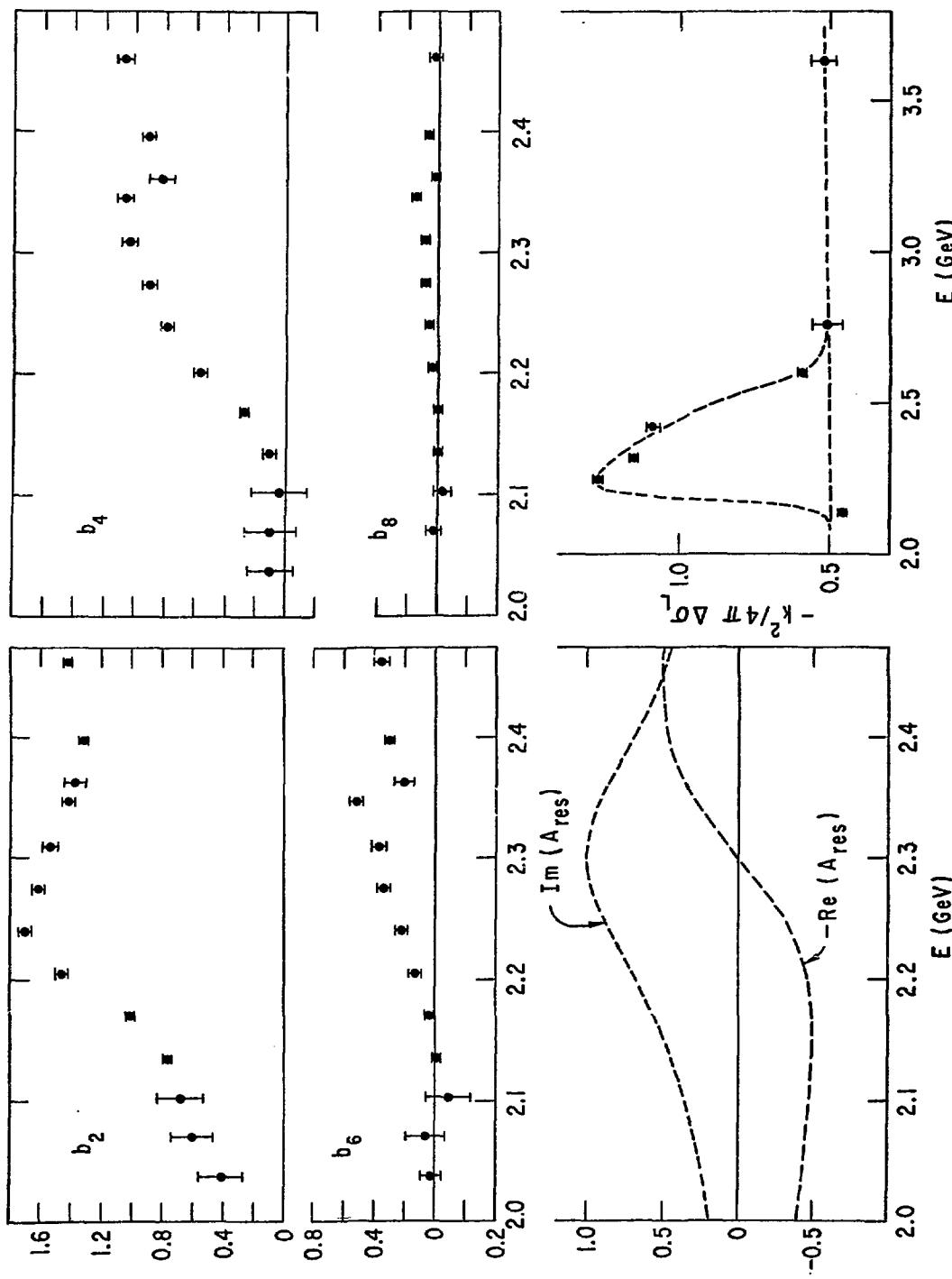


Fig. 9

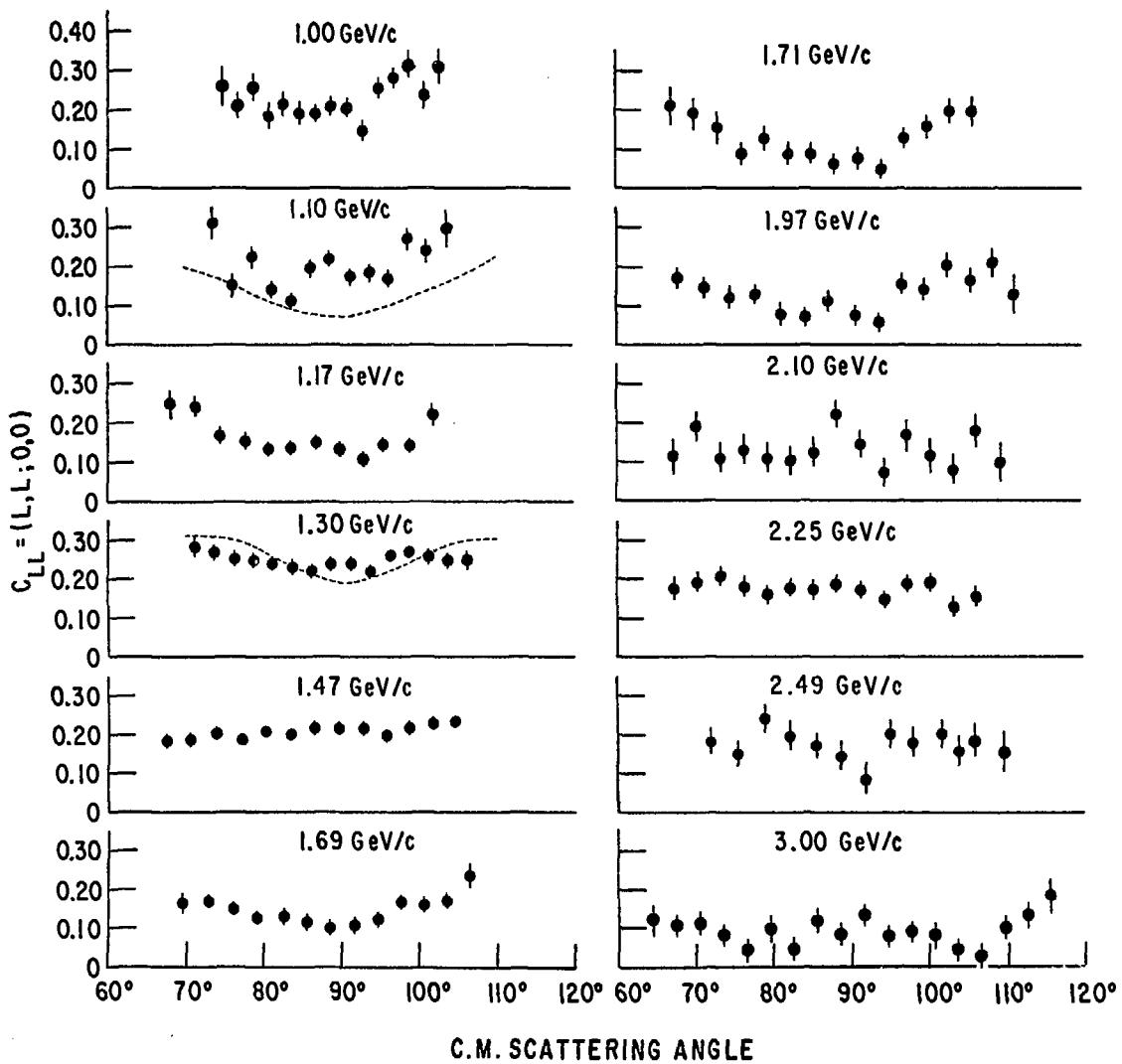


Fig. 10

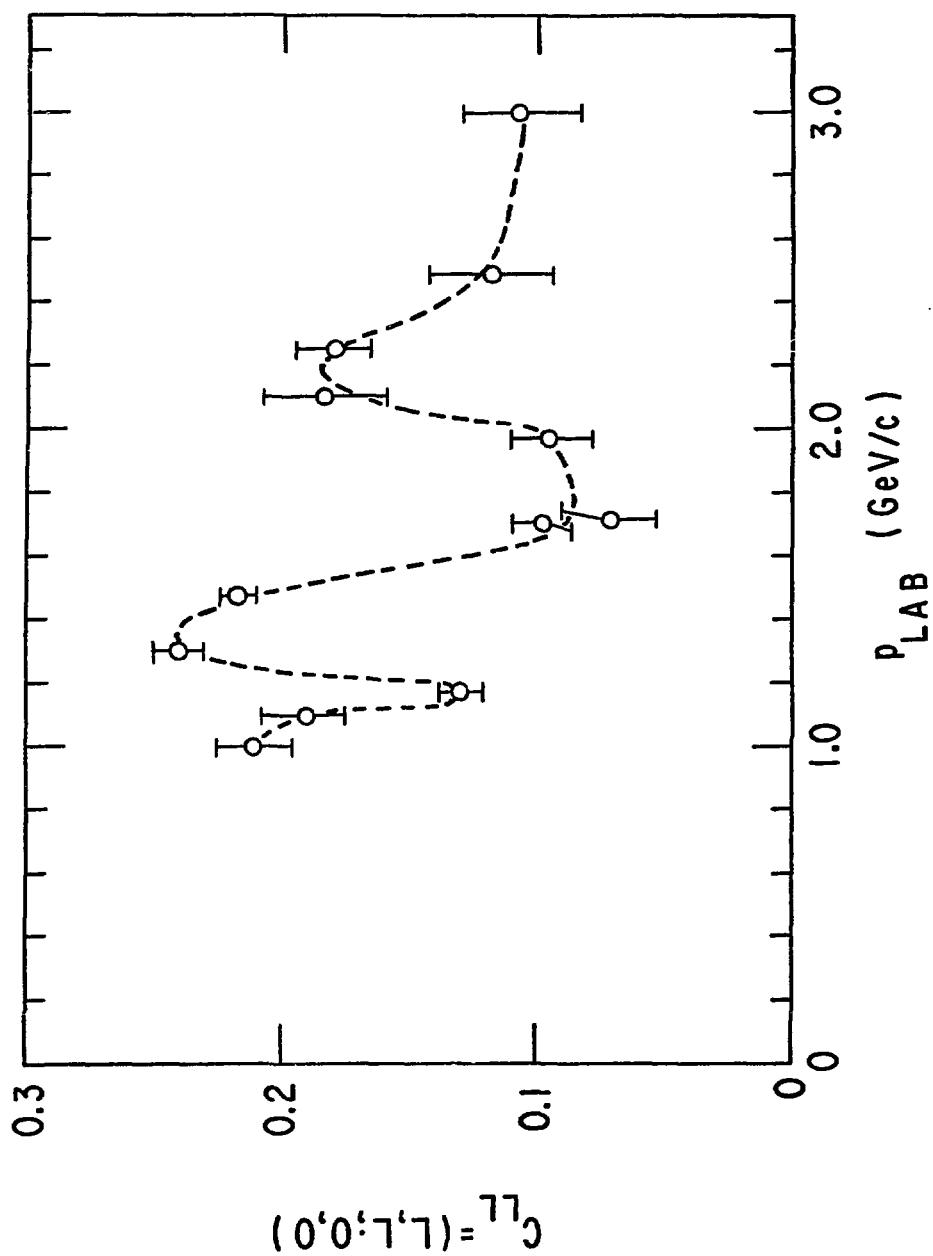


Fig. 11

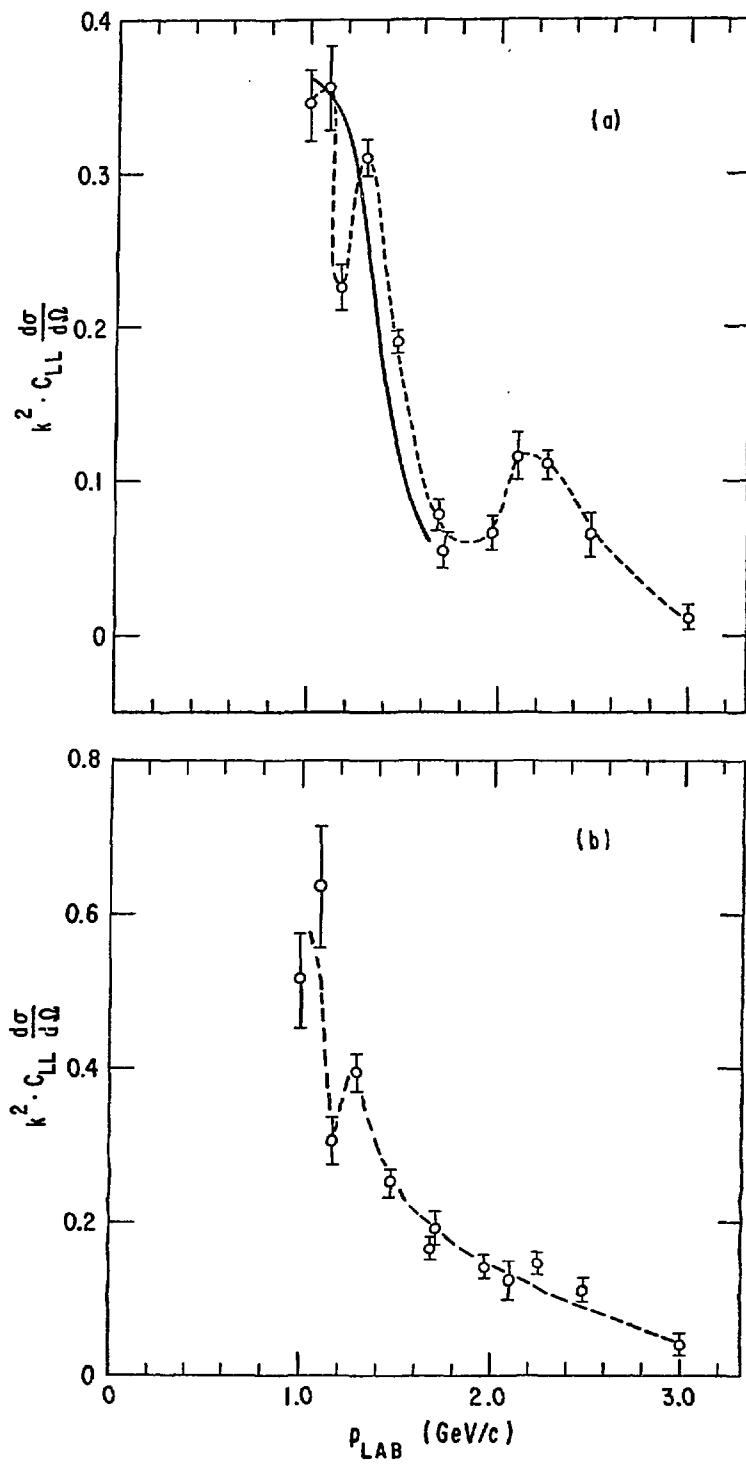


Fig. 12

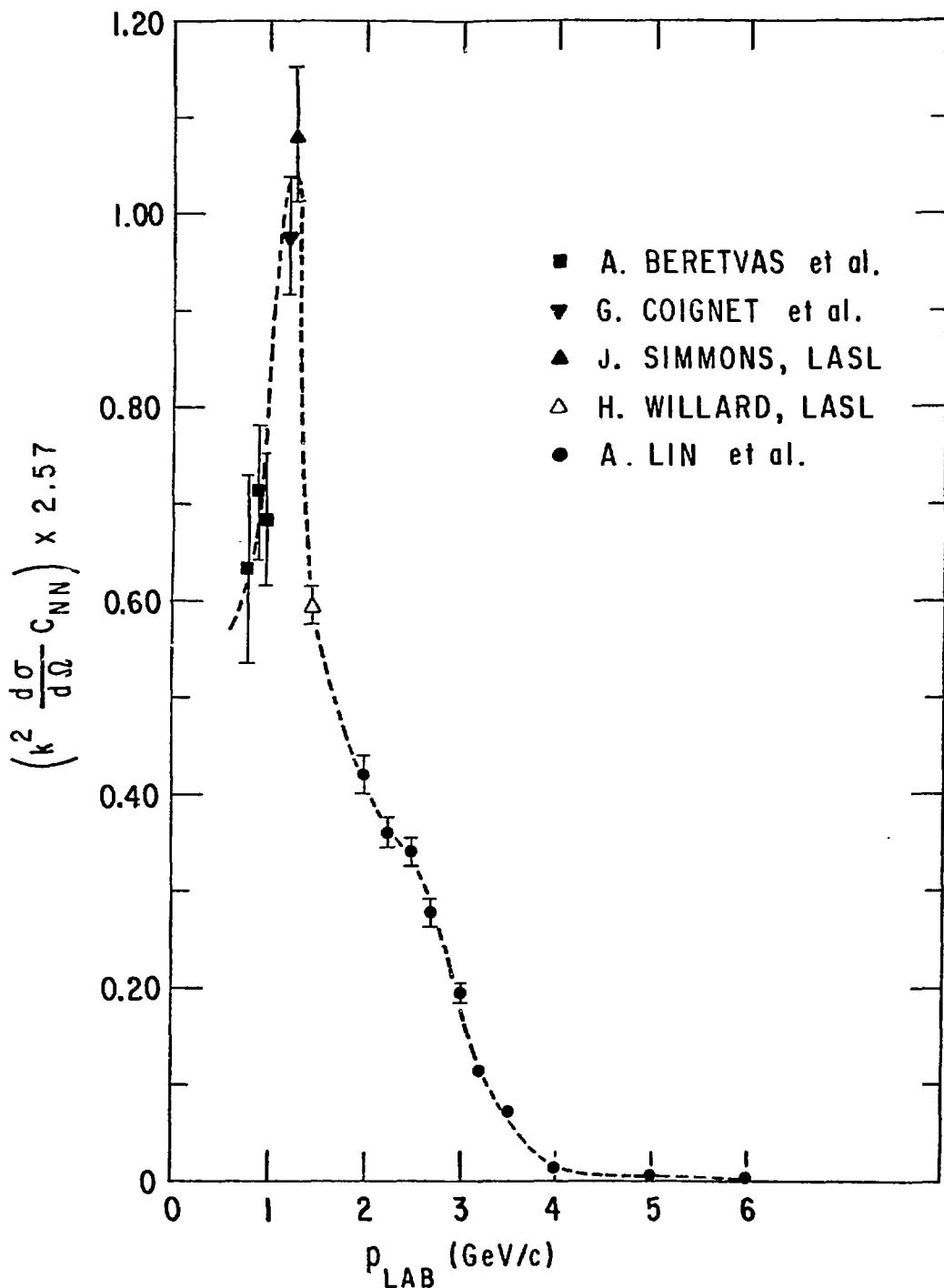


Fig. 13

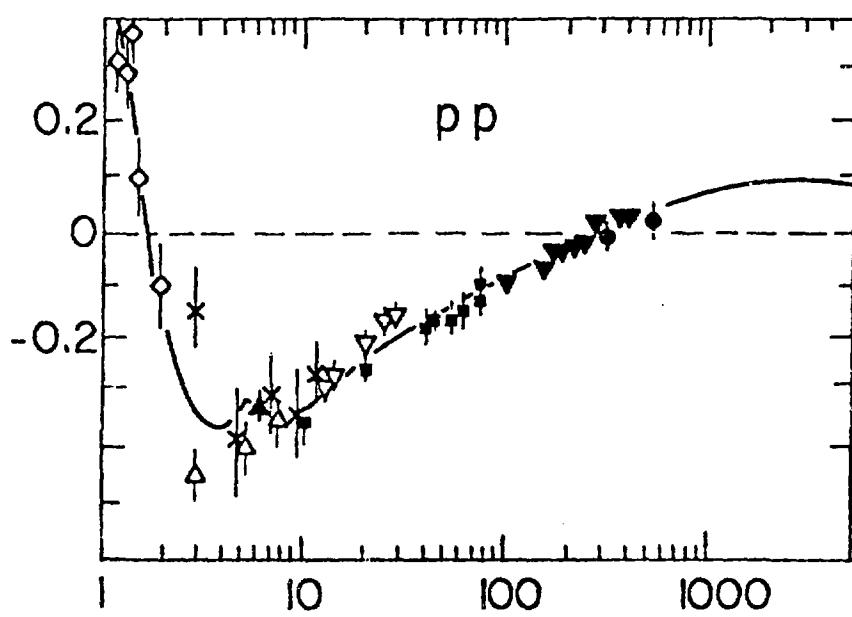


Fig. 14

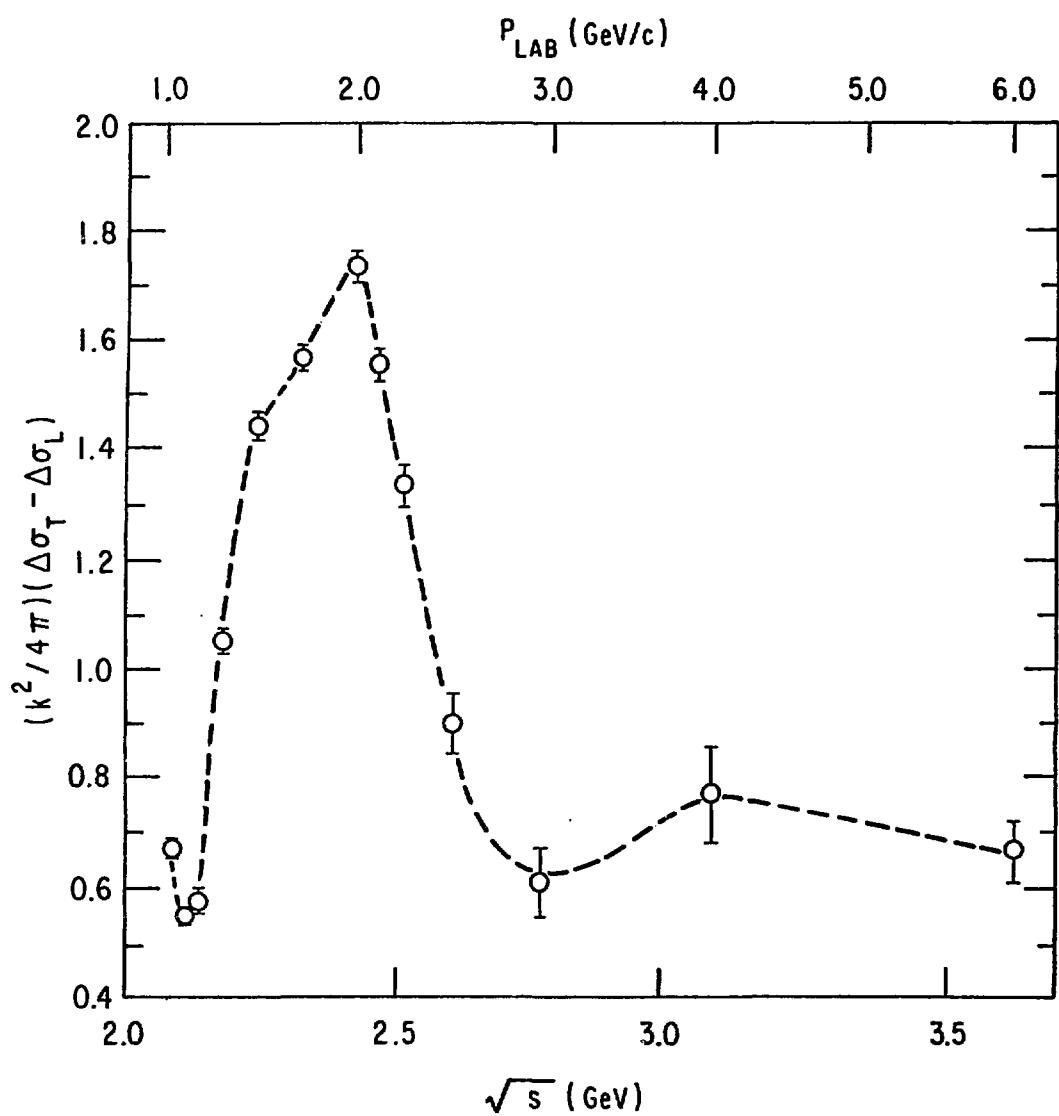


Fig. 15