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TARGET EFFECTS ON PACKAGE RESPONSE:
AN EXPERIMENTAL AND ANALYTICAL EVALUATION*

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ABSTRACT

Sandia National Laboratories has completed an experimental and analytical evaluation to compare the effects of a simple model transportation cask impacting on targets encompassing a range of stiffnesses. The cylindrical shaped unit was impacted into soil, concrete, and "unyielding" targets at velocities varying from 44 ft/s (30 mph) to 110 ft/s (75 mph). The 44 ft/s impact velocity correlates directly to a 30-ft drop height used in regulatory testing.

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1.0 INTRODUCTION

Sandia National Laboratories conducted an evaluation including experimental testing and analytical calculations to compare effects of a simple model transportation cask impacting onto various targets. A cylindrical-shaped unit was impacted into soil, concrete, and "unyielding" targets in a range of velocities. Cask responses at various impact velocities onto soil and concrete targets were compared with a 30-foot drop onto an essentially unyielding surface. The model transportation cask used in this program was a 5200 lb steel cylinder without energy mitigating devices or impact limiters attached.

An analytical evaluation was also performed for impacts onto the unyielding, concrete, and soil targets. These calculations concentrated on trying to account for soil and concrete cracking as the cask unit penetrated into the respective yielding targets. Experimental and analytical results were then compared to better understand the response generated by impacting different targets.

1.1 Scope

An unyielding target is described as a flat, horizontal surface of such character that any increase in its resistance to displacement or deformation upon impact by a package would not significantly increase the damage to the package [1,2]. A specific example of an unyielding target is a steel plate on the upper surface of a concrete block of mass at least ten times that of any

specimen to be dropped onto it. The block should be set on firm soil and the steel plate at least 0.5 inches thick. The target should be as close to cubic or cylindrical in form as possible [2]. The purpose of the unyielding target is to have all of the kinetic energy available from a drop test be absorbed by the package. This total absorption by the package produces maximum decelerations resulting in larger forces. Impacting a concrete or soil target will likely result in energy partitioning where some of the available impact energy is absorbed by the target. Thus, this energy absorption by a yielding target results in less available energy that can be applied to the impacting package. In addition, the unyielding target provides a repeatable and consistent impact surface producing results that can be more easily verified by analytical calculations.

A testing and analytical evaluation was performed to better determine the relationship between an unyielding target and targets in which yielding does occur. Concrete and soil represent the materials chosen for the yielding targets. These materials are typical of hazards found in a transportation environment as opposed to an unyielding target which is highly unlikely to exist for actual accidents. Concrete and soil represent a more realistic impact surface that will absorb some of the available energy of an impacting cask.

A simple-geometry cylindrical unit was used as the projectile impacting the various targets. The unit roughly modeled a half-scale truck cask without any energy mitigating devices attached. This was done to allow concentration of target effects upon impact without having to compensate for any impact limiter response. The simple geometry of the unit provided ease in instrumentation, duplication of data, and analytical modeling.

Both physical testing and computer analyses were performed to help correlate the results and to better understand the phenomenon of target yielding and its effects upon the projectile. In addition, improvements in computer modeling techniques were explored to better represent the yielding targets in analytical calculations.

1.2 Testing and Analysis

Testing was a critical and important component of the evaluation activities. Eleven tests, on five different targets were conducted at impact velocities ranging from 44 ft/s (30 mph) to 110 ft/s (75 mph). The 44 ft/s impact velocity stems from a 30-ft drop height used in regulatory testing. All drops performed on the cylindrical unit were end-on. This produced consistent loads, stresses, and accelerations along the axial direction at any circumferential point. All tests included the use of photometrics to visually analyze and record each drop.

Computer analyses using finite element methods also evaluated cask responses. Because of the cask geometry and orientation of impact, each finite element evaluation simplified to a two-dimensional analysis. From an analytical point of view, modeling a package impact into a rigid surface is quite simple and tends to be conservative since a perfectly unyielding target does not exist for actual experiments. In analyzing an impact into an unyielding target, only the impact projectile has to be modeled. The computer code can produce an impenetrable surface that will not absorb any energy. Thus, in this type of analysis no target geometrical modeling, material properties, or boundary conditions are needed. However, when variables

associated with a yielding target enter into an analysis, the appropriate modeling and calculations can be very different and even misleading.

Depending on the target, factors such as cracking, unit penetration, and target energy absorption in addition to geometry, material properties and boundary conditions come into effect. These additional variables increase the difficulty of the analysis plus producing results that may not be duplicated by testing. With respect to the concrete and soil targets, these factors plus other phenomenon particular to each yielding surface were evaluated.

2.0 TARGETS

In comparing a rigid target to various yielding surfaces, targets common to everyday life were emphasized. This evaluation employed four types of targets in addition to the unyielding:

- concrete airport runway
- concrete highway
- undisturbed desert soil
- uncompacted soil

These yielding targets provided a range of impact stiffnesses and included environments a cask could realistically strike while transporting radioactive materials. Considerable effort was made to provide yielding surfaces representative of an environment which exists in real life. In addition, these targets needed to be reproducible either in construction or

characterization. Each of the targets, all located at Coyote Test Site in Albuquerque, are discussed in detail in the following sections.

2.1 Unyielding Target

The 340-ton steel-faced concrete target used in the test series to represent an unyielding surface is shown in Figure 1. This target, which was constructed in 1975, features a 22-ft diameter, 12-ft deep concrete mass. Integrally fastened to the concrete mass is a 10 x 10 x 0.42 ft steel plate. To aid in fastening the steel plate to the concrete is a network of steel tubes welded to the bottom of the plate (Figure 2). These tubes effectively spread any applied load to the concrete. Since 1975 this target has been used extensively for regulatory 30-ft (9 meter) drops, 1 meter puncture tests and higher velocity impacts for a variety of packages and scale models. This target satisfies the requirements set forth by the International Atomic Energy Agency (IAEA) as an unyielding target for the purpose of this evaluation program.

2.2 Concrete Targets

Special consideration was made to characterize yielding targets familiar in real life. Common concrete structures having specific quality assurance standards that must be met at the time of construction are highways and airport runways. These standards are common throughout the United States.

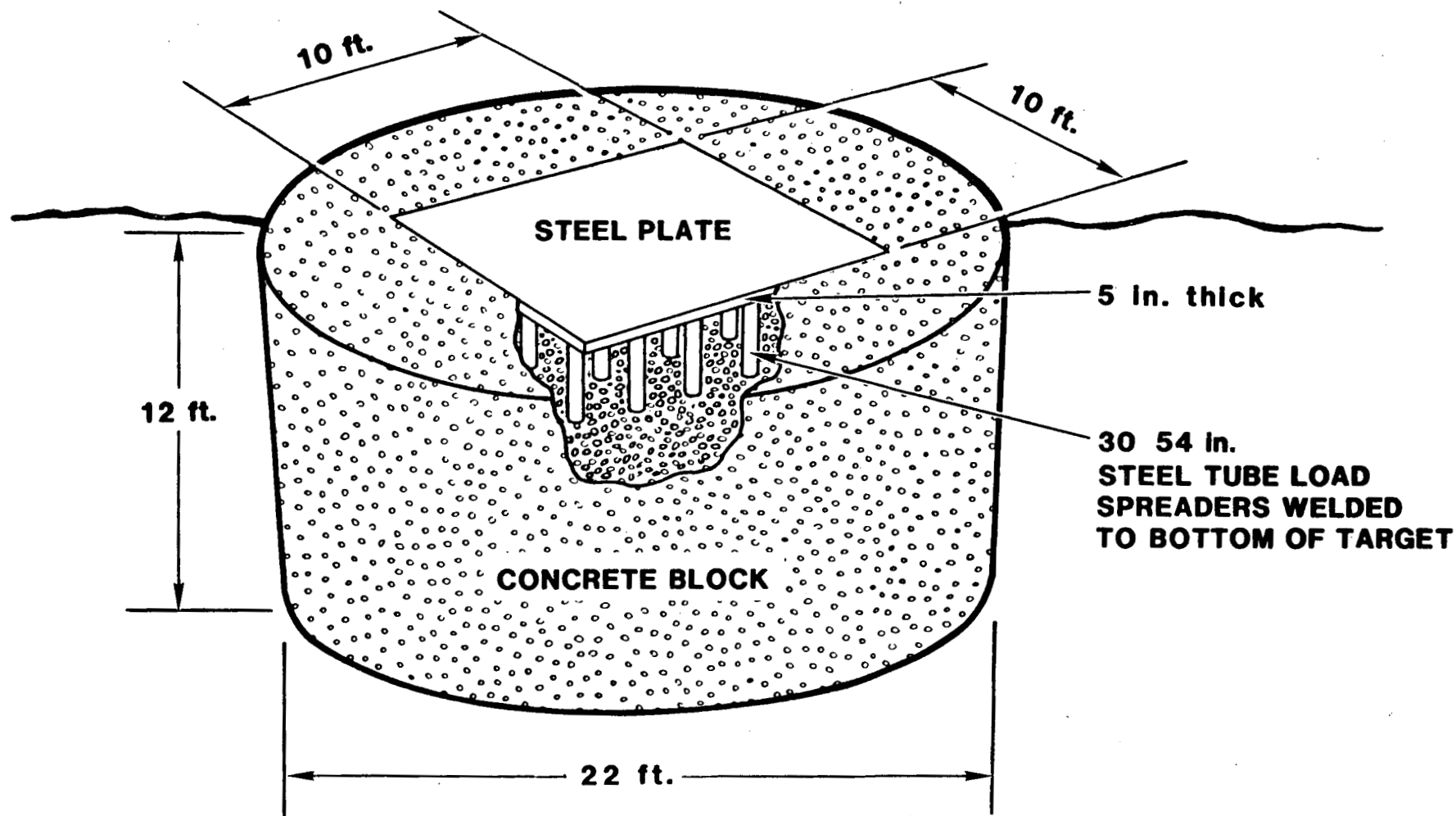


Figure 1 Unyielding Target at Sandia National Laboratories' Coyote Canyon Test Site

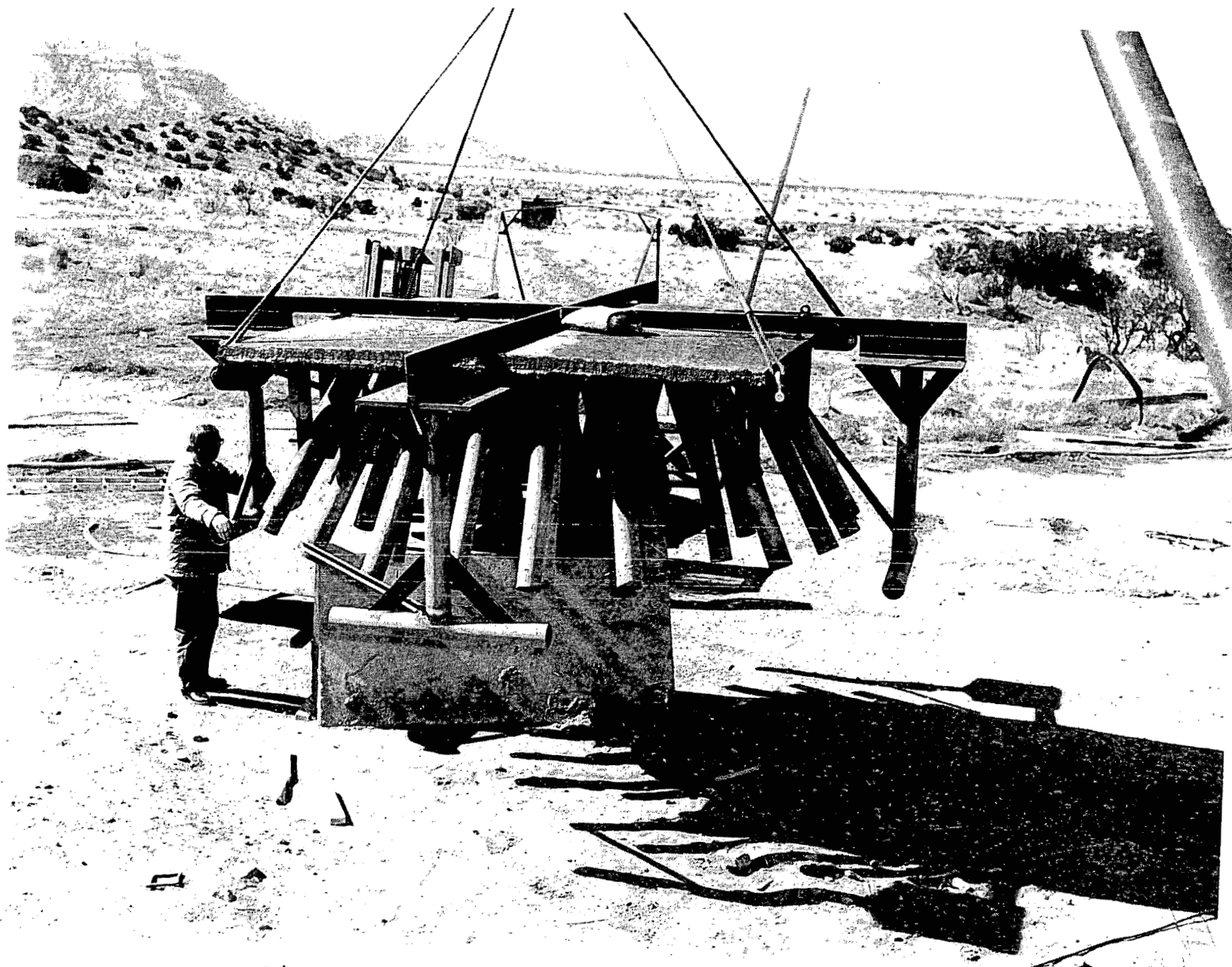


Figure 2 Steel Tube Assembly in Unyielding Target

2.2.1 Runway Concrete Targets

Three 20 x 20 ft concrete slabs shown in Figure 3 were used to represent the runway targets. These slabs were constructed for another program in 1976 (Figure 4) according to U. S. Federal Aviation Agency (FAA) design criteria [3] but they had not been used for testing. The 18 inch deep slab includes a 5 x 5 inch mesh steel reinforcement to provide strength in tension and shear. The compacted soil beneath the concrete underwent a series of plate bearing tests to assure proper soil strength and compaction (Figure 5). The value obtained from the test, k , is in units of pressure over length. The k value can be envisioned as the pressure required to produce a unit deformation of a bearing plate into the pavement foundation. The k value found for this particular soil was within the 500 psi/in. allowed in Reference 3.

Concrete cylinders and cores were also laboratory tested to obtain compressive and flexural strengths. For the concrete cylinder, the standard twenty-eight day compressive strength test resulted in a value of 5060 psi and a flexural stress of 670 psi was also obtained. The drilled cores yielded a compressive strength of 4800 psi. These values are within the FAA allowable limits for a 18-inch thick concrete slab designed to carry a 747 aircraft.

2.2.2 Highway Concrete Targets

Using applicable U. S. Federal Highway design criteria [4], three 10 x 10 ft concrete slabs (Figure 6) were constructed to represent the highway targets. A typical concrete highway cross section does not actually exist.

5000 psi Concrete
3/4 in. Aggregate
5 in.
Square Steel Mesh

Compacted Subsoil

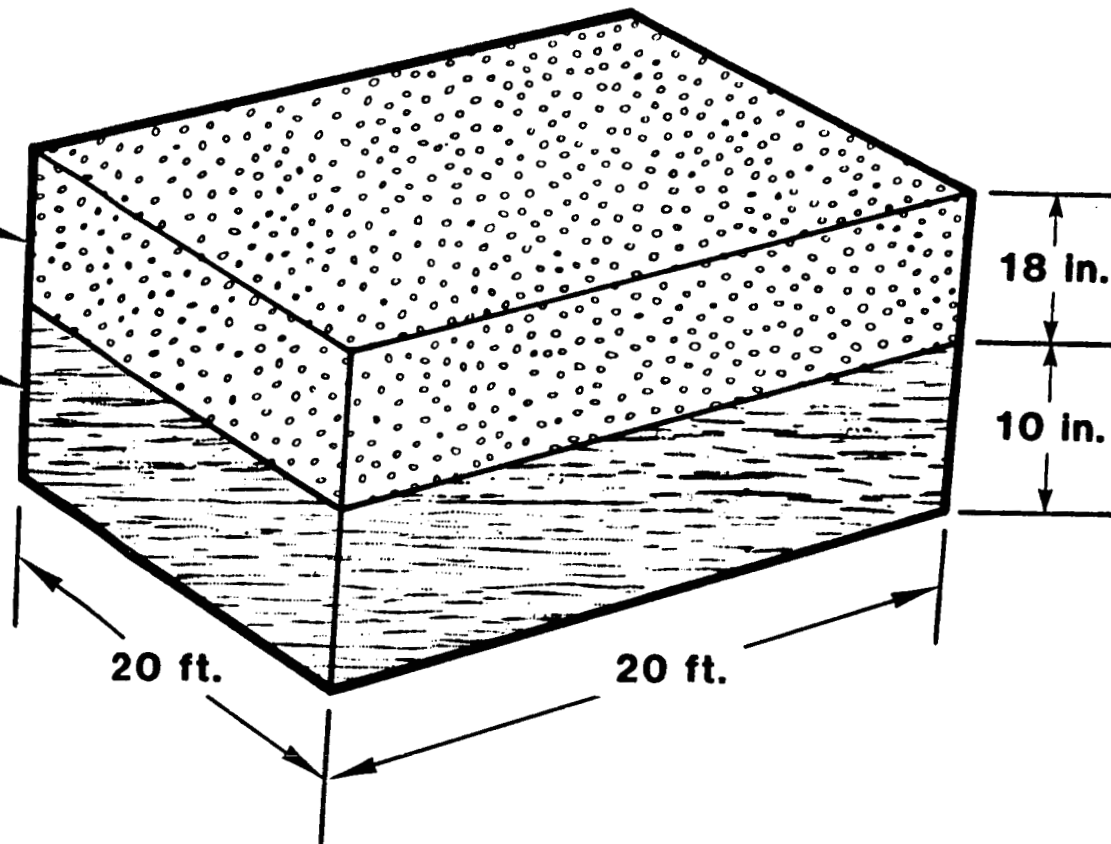


Figure 3 Federal Aviation Agency Runway Cross Section

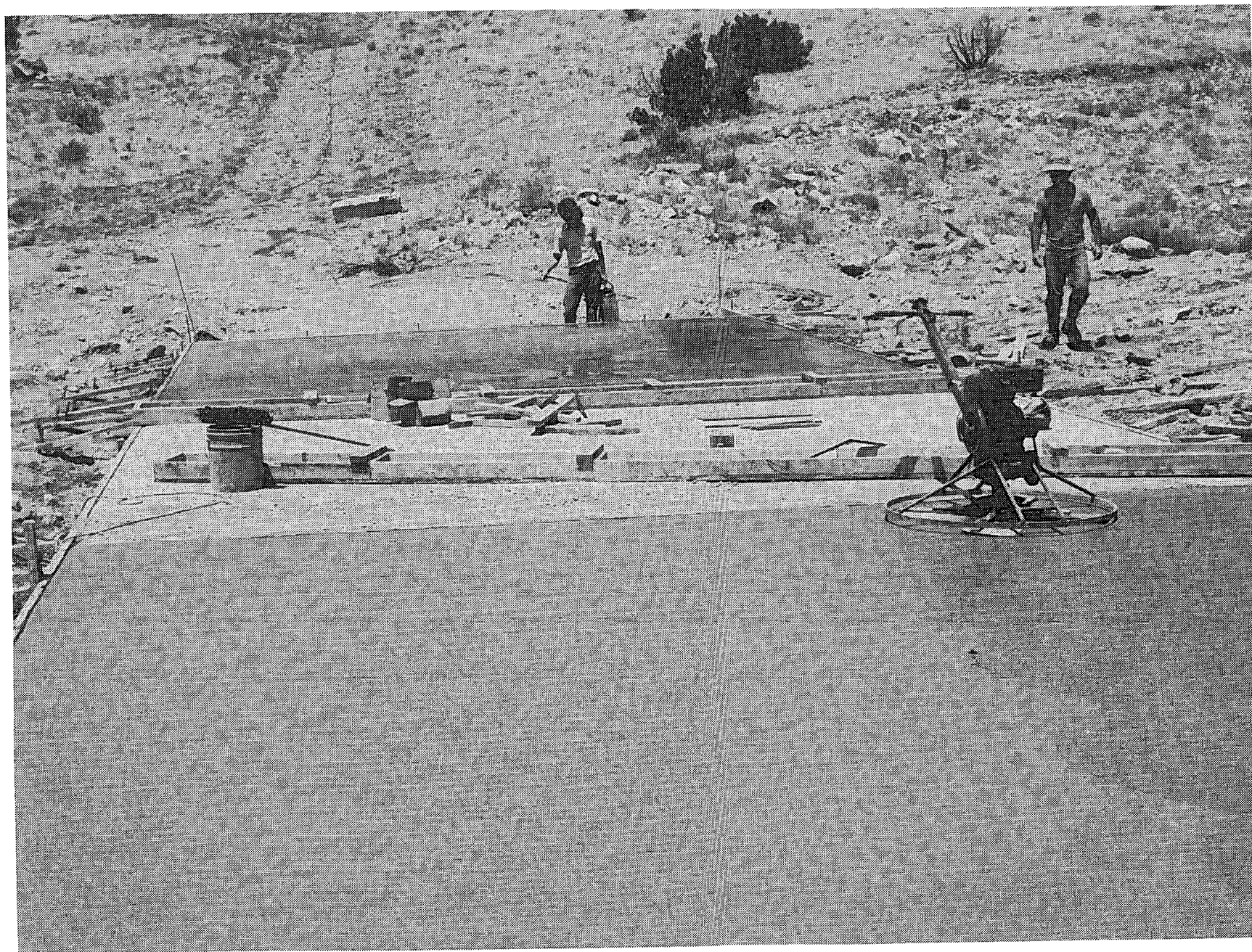


Figure 4 Construction of Concrete Runway Slabs

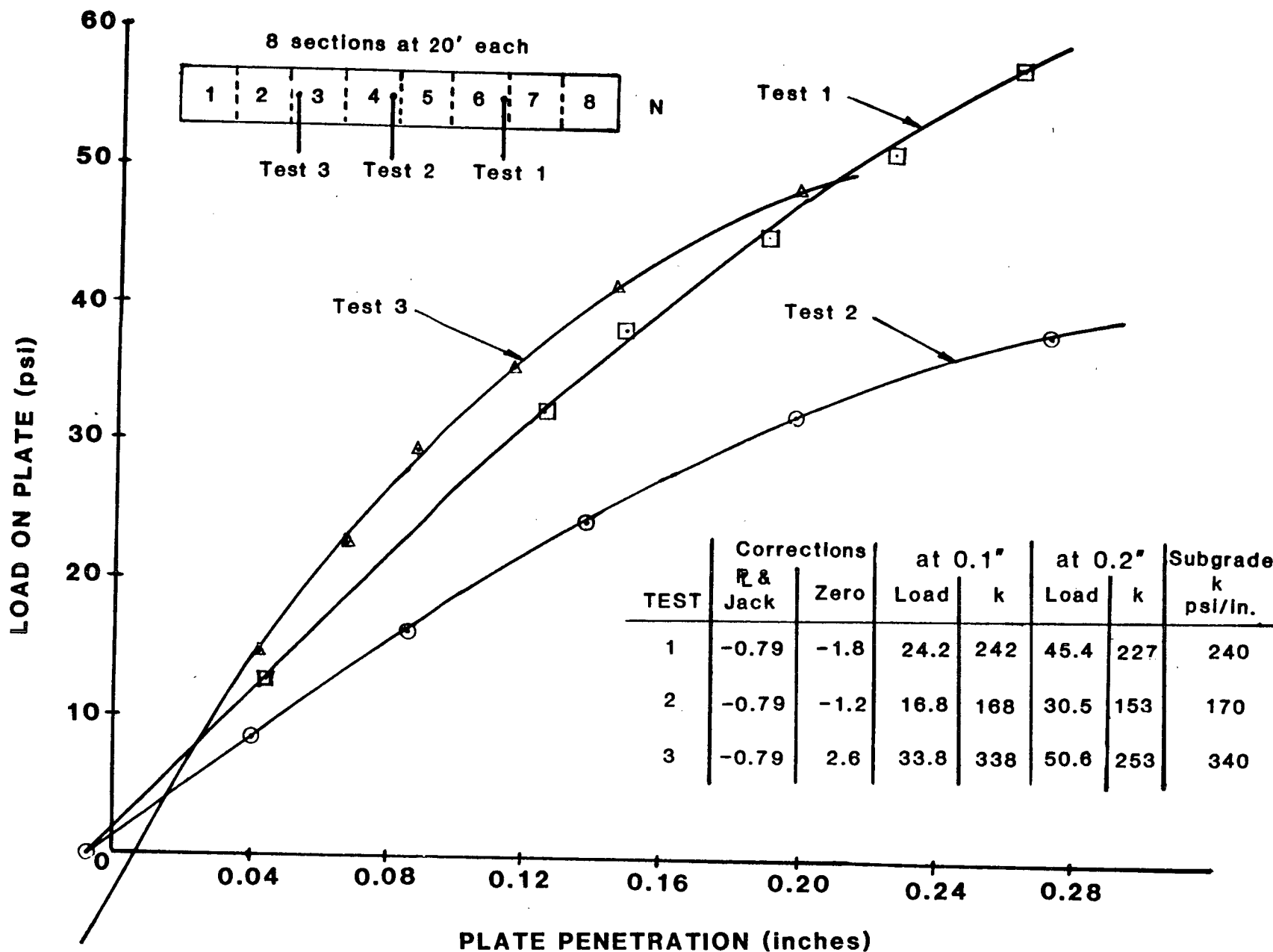


Figure 5 Results of Plate Bearing Tests for Concrete Runway

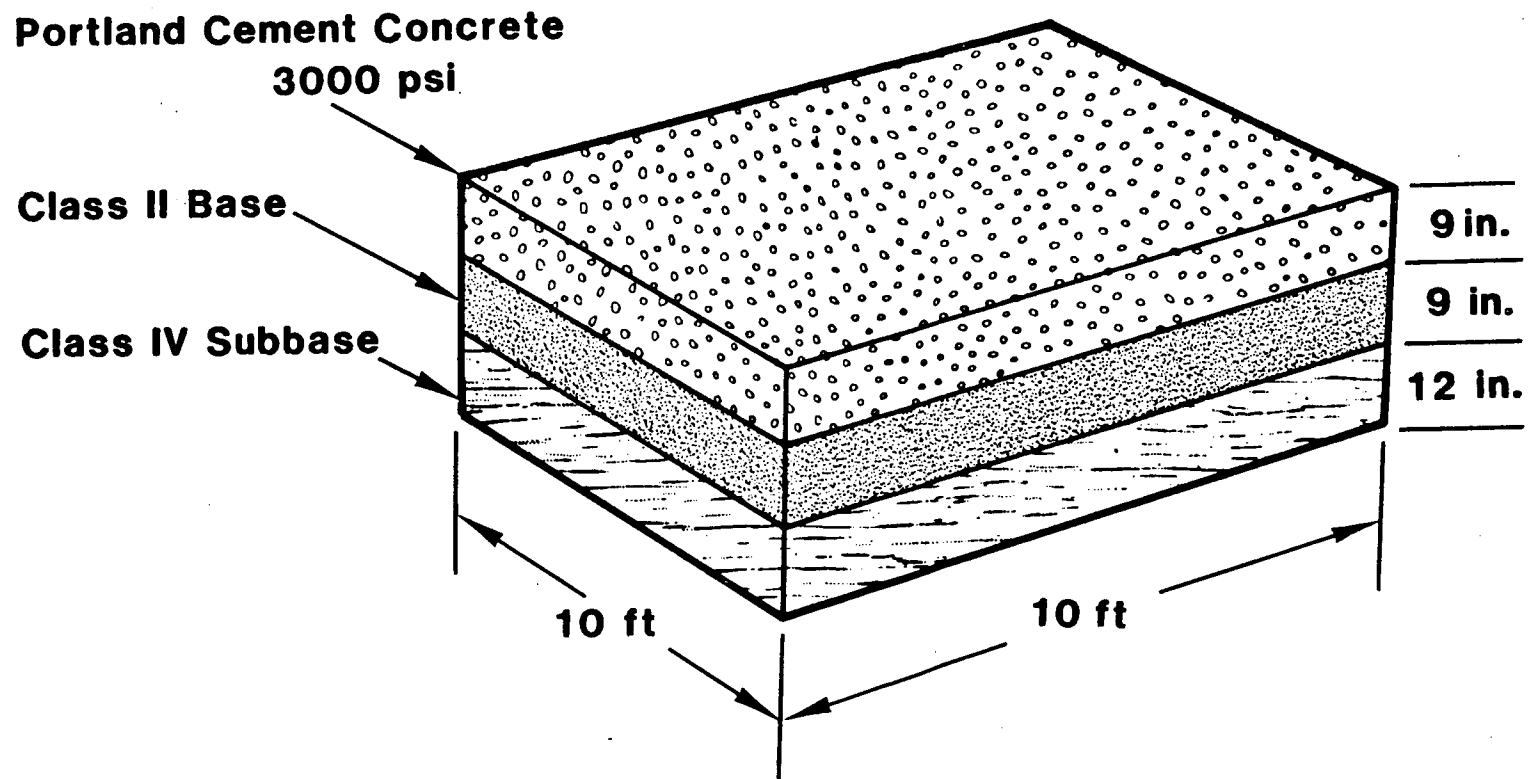


Figure 6 Concrete Highway Cross Section

However given the types of materials and cross sections used in highway design and construction, the selected configuration represents a roadway that is stiffer and more resistant to applied loads than the average interstate highway. This target cross section presents a more severe environment than a concrete bridge abutment which typically is less than 4 inches thick.

Native soil compacted to 95% of its optimum density [5] constituted the Class IV Subbase. Crushed quarry stone also compacted to 95% of its optimum density and satisfying highway [4] specifications represented the Class II base. A 3700 psi minimum compressive strength concrete slab, which is 9 inches thick, made up the roadway surface.

Reinforcing bar was not included in the roadway test sections constructed in 1985 for two reasons. First, recent highway rehabilitation projects in the United States have discovered steel reinforcing bars greatly increase the difficulty in replacing roadway sections. Thus, most highway designs are now omitting reinforcing bars to facilitate roadway maintenance and rehabilitation efforts. The second reason stems from an analytical perspective. Since analytical computer codes do not fully duplicate the response of concrete under large impact loading, the addition of reinforcing bars would further complicate any analyses. Thus, it was decided to avoid a variable that would increase the difficulty of the problem without providing any additional benefits.

2.3 Soil Targets

Determining a suitable soil target presented several problems. Since soil properties and characteristics can change drastically with location,

establishing a section that is universally typical proved to be impractical. Densities for common soils such as sand can range from 75 to 140 pcf [5]. Other variables used to define soils such as specific gravity, moisture content, plasticity index, and compression strength can also vary considerably. In addition, the composition within a given cross section usually varies not only in percentages of different types of soil constituents, but also in location. Since a universal soil definition does not exist, the native soil at the test facility was used for the targets. It is representative of a target category called soil but in reality there are potentially significant differences in the response of packages hitting soils.

The soil target was not altered in any way, instead considerable effort was made to fully characterize all of its properties. A series of laboratory and on-site tests performed by the University of New Mexico Civil Engineering Research Facility (NMERI-CERF) defined the soil properties [6]. The tests include compaction, density, moisture content, sieve analysis, triaxial, unconfined compression, confined compression and consolidation. Table 1 gives a description of the soil properties. Of the tests performed, the triaxial test (Figure 7) was the most valuable for obtaining pertinent material properties. In particular the triaxial test provides the relationship between the principal and shear stresses plus the friction angle which is required to perform the analytical calculations. The information obtained from one triaxial test is shown in Figure 8.

Through the depth of the soil, differences in properties were exhibited, particularly in the first two feet. These differences in properties were characterized in the finite element analysis as six separate layers of

SOIL PROPERTIES AND CHARACTERISTICS ⁺								
Depth cm (inches)	Natural Moisture %	Natural Dry Density g/cm ³ (PcF)	Specific Gravity	ATTERBERG LIMITS		Unconfined Compressive Strength MPa (psi)	Consolidation 0.2MPa Loading %	SOIL TYPE
				Liquid Limit %	Plasticity Index %			
0-30 (0-12)	15.47	-	-	21.0	-	-	-	SM Gravelly Silty Sand
30-61 (12-24)	17.1	1.43 (89.0)	2.63	33.0	14.4	-	24.8	CL-Lean Clay- Some Gravel
61-91 (24-36)	15.1 12.5	1.57 1.64 (97.8) (102.2)	2.65	32.0	14.0	0.119 (17.2)	16.4	SC-Silty Sandy Clay
91-122 (36-48)	14.9 13.3	1.72 1.59 (107.4) (98.6)	2.65	36.0	19.0	0.097 (14.0)	28.3	SC-Silty Sandy Clay
122-152 (48-60)	12.6 11.2	1.67 1.62 (104.0) (101.0)	2.63	29.0	10.0	0.093 (13.5)	17.5	SC-Silty Sandy Clay
152-183 (60-72)	16.9 8.5	1.59 1.62 (99.1) (104)	2.64	30.0	10.0	- -	11.7 -	SC-Silty Sandy Clay SM-Silty Sand

⁺ more than one value indicates the property had a given range for the stated depth

Table 1

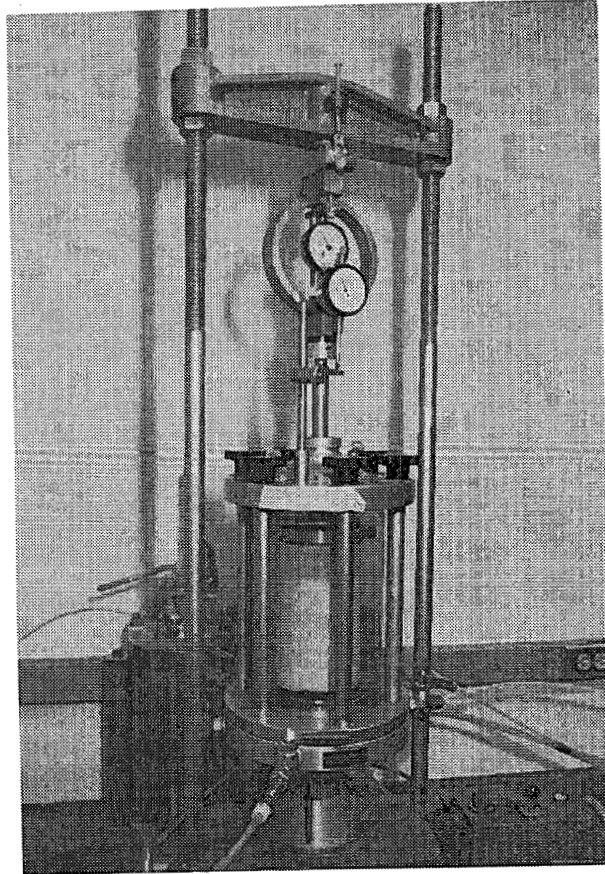


Figure 7 Triaxial Test

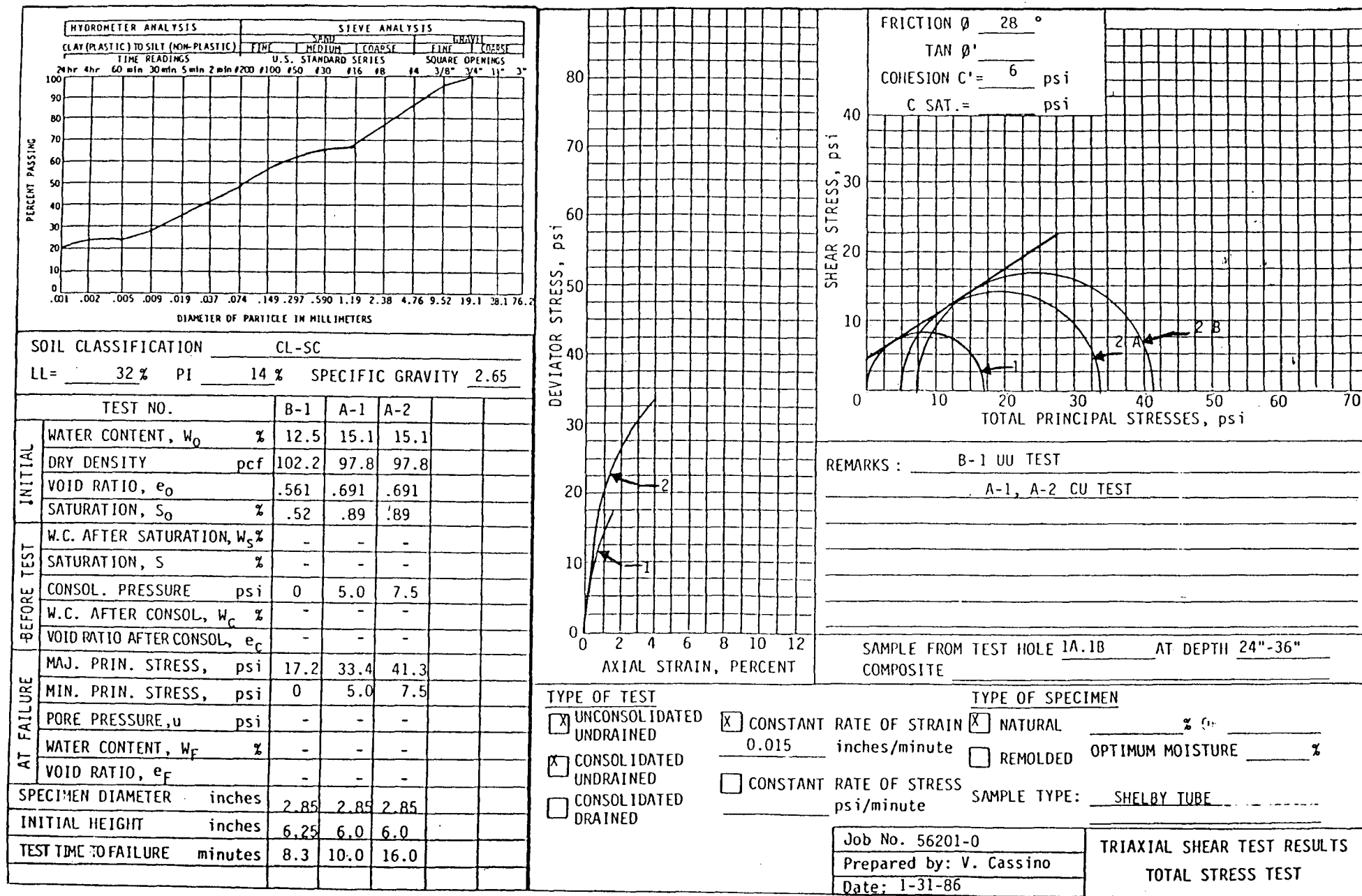


Figure 8 Data Obtained from Triaxial Test

material. This radical variation of properties illustrates the complexity of characterizing soil both experimentally and analytically.

A second soil target was also tested to obtain a comparison between soils having different compaction. The native soil has a compaction that is relatively high thus providing a stiff soil target. To produce a softer soil target, a seven foot hole was excavated and replaced with uniform imported borrow. The soil was placed using a hand held tapper with water added to help the material settle. No heavy compaction equipment was used to bring the relative density to that found in the native desert soil. A dynamic core penetrometer test was performed on both the new soil target and native desert soil for comparisons (Figure 9). This test measures the soil resistance to an applied dynamic load. For the soft soil target, it took an average of 10 to 12 blows by a 12-pound weight falling 12 inches to force a coned-faced rod to penetrate one foot into the soil. By contrast over 80 blows were required to obtain the same one foot penetration into the native desert soil. A comparison of unit penetration into the respective targets are made in the experimental results section 3.2.3.

3.0 EXPERIMENTAL TESTING

The test program consisted of a series of drops onto the different targets to determine package response characteristics caused by the various relative stiffnesses of the impact surfaces. Table 2 is the test matrix showing the variety of impact velocities used for each respective target. The 44 ft/s (30 mph) impact velocity correlates directly to a 30-ft drop height used in regulatory testing. The other impact velocities of 66 ft/s (45 mph),

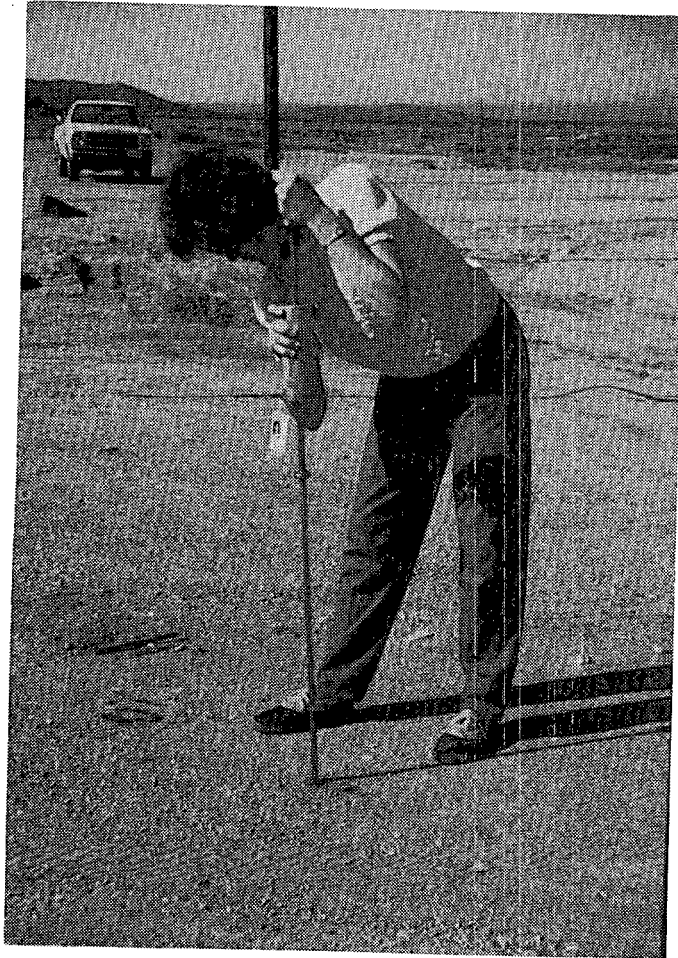


Figure 9 Dynamic Core Penetrometer Test

TEST MATRIX

TARGET	IMPACT VELOCITY (ft/s)			
	44	66	88	110
IN-SITU DESERT SOIL	X	X	X	
UNCOMPACTED IMPORTED BORROW				X
CONCRETE RUNWAY	X	X	X	
CONCRETE HIGHWAY	X	X [*]	X	
UNYIELDING TARGET	X			

• Actual impact velocity 44 ft/s because
of test malfunction, no data at this velocity

88 ft/s (60 mph) and 110 ft/s (75 mph) correspond to free fall drop heights of 68 ft, 120 ft, and 188 ft, respectively. The uncompacted soil target represented the softest environment while the rigid unyielding surface constituted the most severe.

3.1 Test Unit

The test unit was a simple cylindrical-shaped projectile. The unit, constructed out of Grade A36 mild steel, was tested without impact limiters or energy mitigating devices. This was done to better differentiate between the responses obtained from impacting the various targets without having to compensate for any effects provided by the impact limiters. At 6 ft long and 20 inches in diameter, the unit represents a simplified half-scale truck transportation cask (Figure 10). The unit consists of two hollow cylinder sections fastened together with a double set of radial pins. The two cylinders represent an outer cask body and an inner shielding liner respectively. The bottom cap is welded around the unit perimeter to the outer cylinder. Twelve 0.5-inch diameter bolts secure the lid to the test unit. To model cask contents, a stack of steel plates fill the unit bringing the total weight to 5200 lb. These plates are held together by a rod/bolt connection keeping them from moving independently inside the cavity and in turn making the contents act as a solid mass. A total of six test units were used in this program.

Instrumentation on each test unit included eight strain gages and at least four accelerometers, depending on the target (Figure 10). Strain gages, every 90° around the unit, were situated in two levels, 2.75 and 12 inches

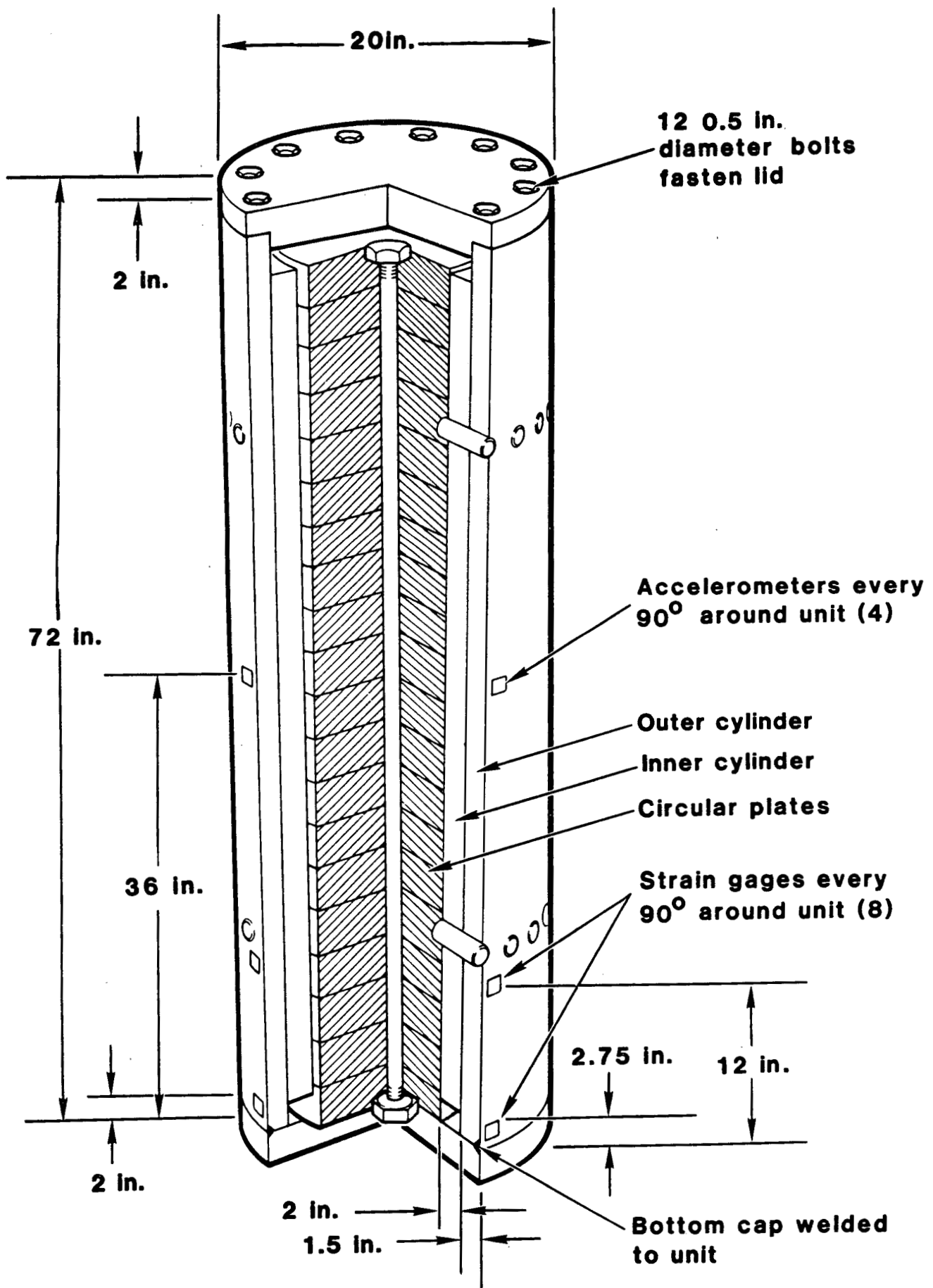


Figure 10 Test Unit Used for Experimental Program

from the bottom. The lower level of strain gages coincides with the gap between the outer cylinder and circular plates. This is where the maximum strains and package deformation was expected. For tests where small or micro-deformation was expected, Micro Measurements CEA-06-125UW-350 [7] strain gages were used. These gages are functional up to 15% strain levels. Micro Measurement EP-08-125AC-350 gages, which can adequately account for strains up to 50% instrumented the test unit for impacts expected to generate large deformations. These gages were installed using techniques recommended by the manufacturer [7]. The strain gage specifications are listed in Appendix A.

A primary set of accelerometers were also placed every 90° around the unit at the midplane. Any additional accelerometers were situated at the 45° point between the primary accelerometers. Every accelerometer was located to measure the same axial acceleration in the direction of impact. Thus, duplication of magnitude was sought by all accelerometers and strain gages.

Two types of accelerometers with different applicable ranges were used to instrument the test unit. Entran Devices EGAXT-23-F-5000 and EGAXT-48-F-10000 [8] are capable of measuring accelerations in the 5000 g and 10,000 g range, respectively. Both types of Entran accelerometers are damped to help avoid the effects of any resonating the system may have during impact that could reduce the validity of the accelerometer response. Endevco 2262 (damped) and 2264 (undamped) [9] are capable of measuring 25,000 g and 50,000 g acceleration levels, respectively. The acceleration specifications are given in Appendix A.

Each projectile unit underwent geometric inspection for length, diameter and circumference before and after each test to monitor deformations. Also, photometrics, ranging in camera speed from real time to 2000 frames/second,

were employed for velocity measurements and event recording. A plan view of the camera setup is shown in Figure 11. Recorded data included test unit strain, acceleration, deformation, impact velocity and penetration into the target. Comparison of this information was made between experimental results and analytical calculations.

The test apparatus consisted of a 75-ft long I-beam attached vertically to a frame (Figure 12). The I-beam helped guide the unit via a sled in addition to keeping the projectile perpendicular as it fell toward the target. The test unit was fastened to the sled by three 0.5-inch diameter explosive bolts (Figure 13). The use of rockets enabled the unit to obtain higher velocities without having to increase the drop height (Figure 14). Upon reaching the lower section of the I-beam, the test unit separated from the guide sled and impacted unrestrained into the target.

3.2 Results

The results obtained from the test series included information ranging from anticipated to unexpected. The unyielding target, as expected, produced the most severe strains, accelerations and deformations. However, the drop tests onto the yielding targets provided some unusual strain gage and accelerometer data. Of the eleven tests performed, five resulted in permanent deformations to the test unit. Differences in radius and length were measured for each test unit. In the cases of permanent deformations, the maximum radial strains occurred between three to four inches from the impact end of the unit. This is because of the added stiffness provided by the bottom cap

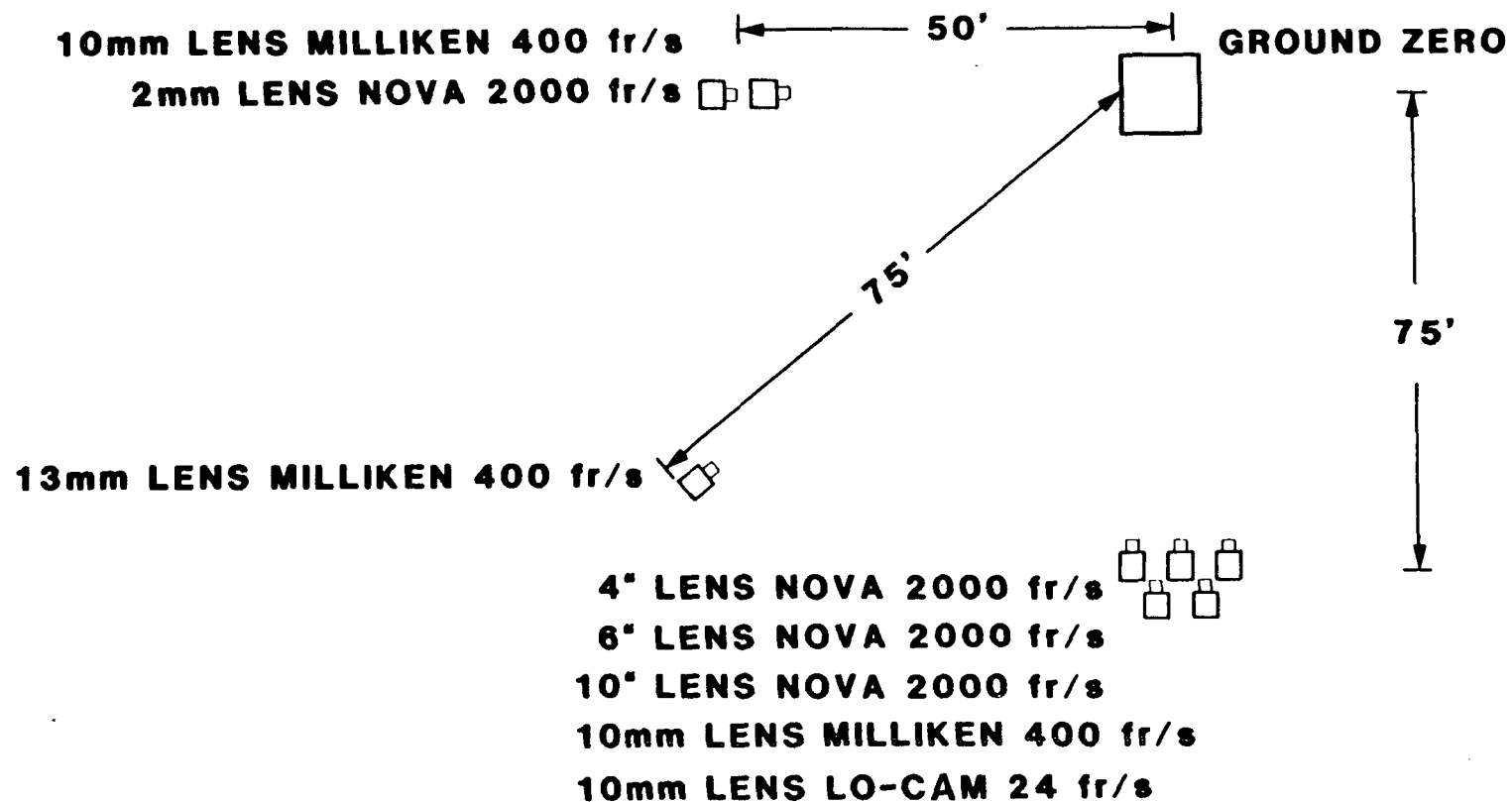
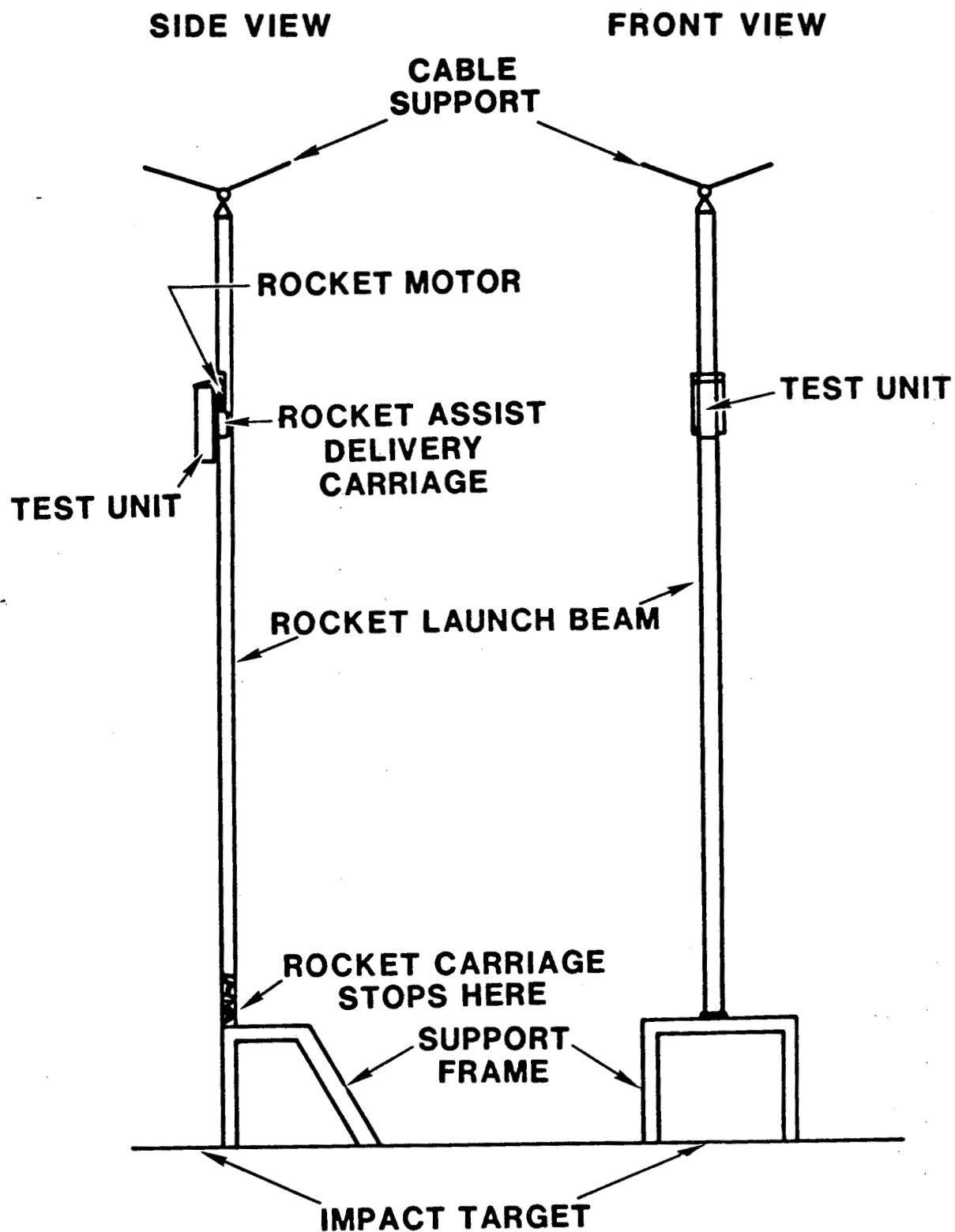


Figure 11 Camera Setup Used for Photometric Coverage



*** THE UNIT AND CARRIAGE WILL BE SEPARATED BY EXPLOSIVE BOLTS**

Figure 12 Test Apparatus

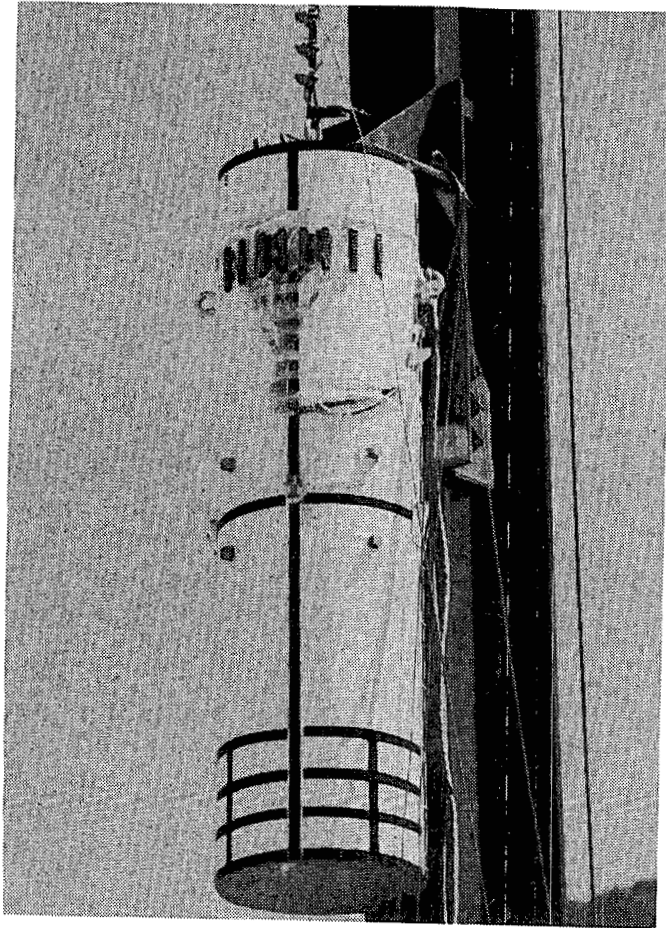


Figure 13 Test Unit Fastened to Sled

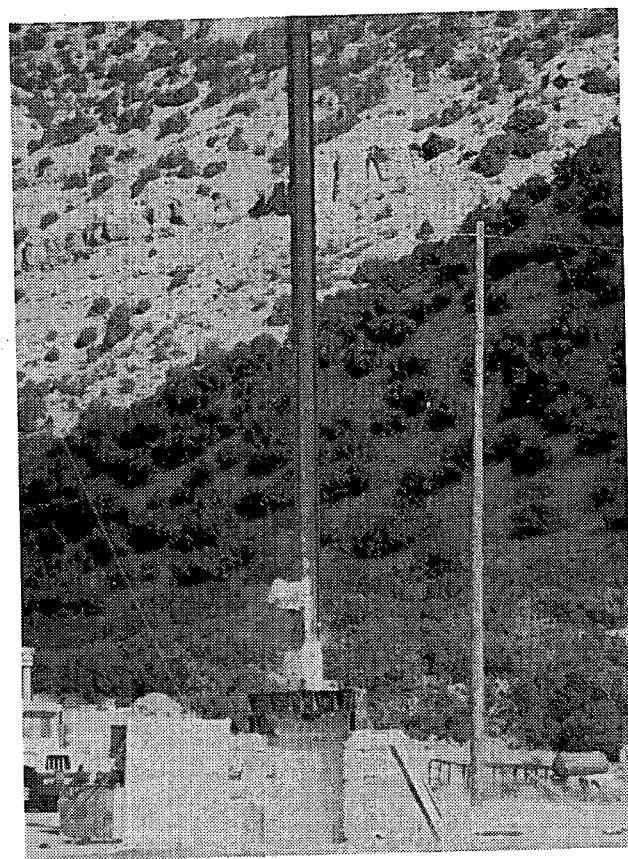
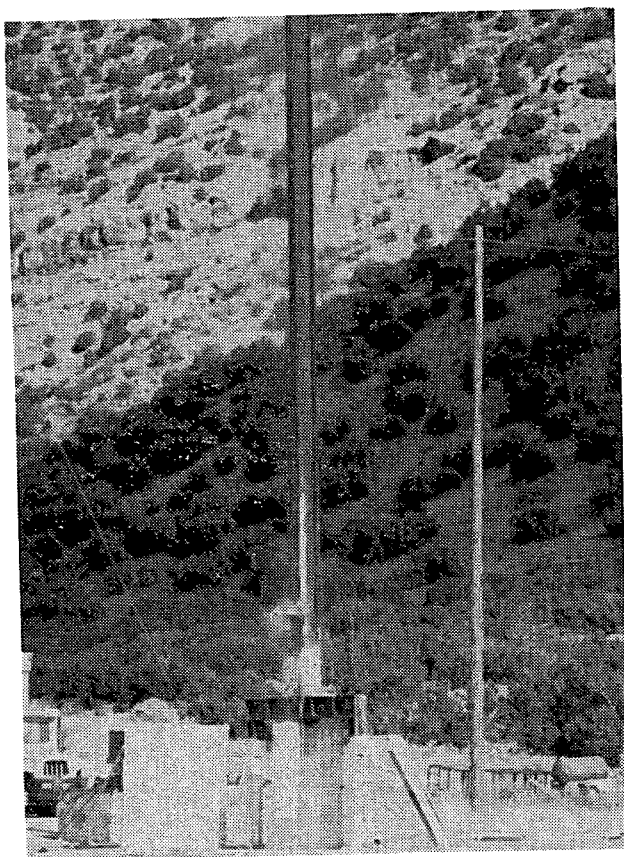
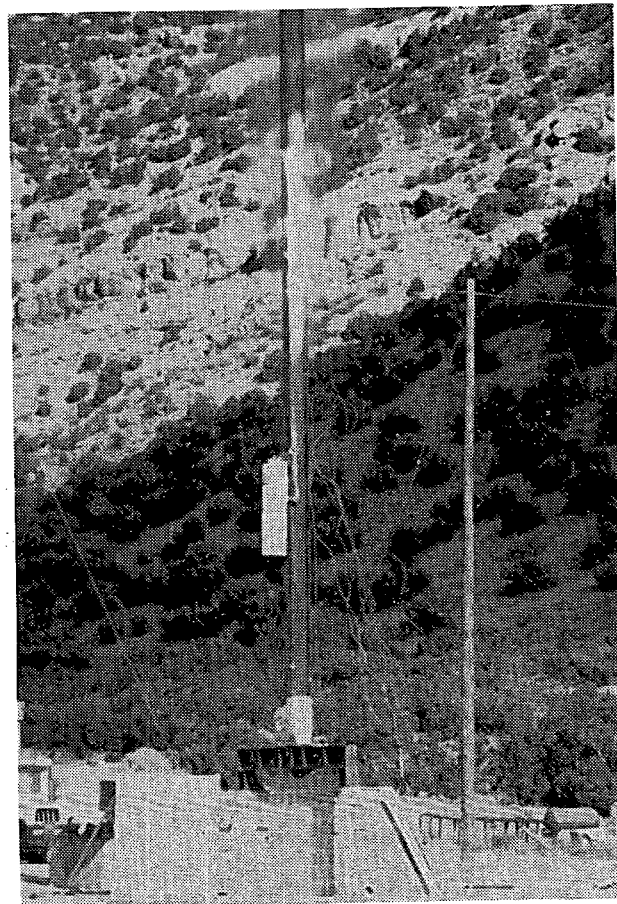
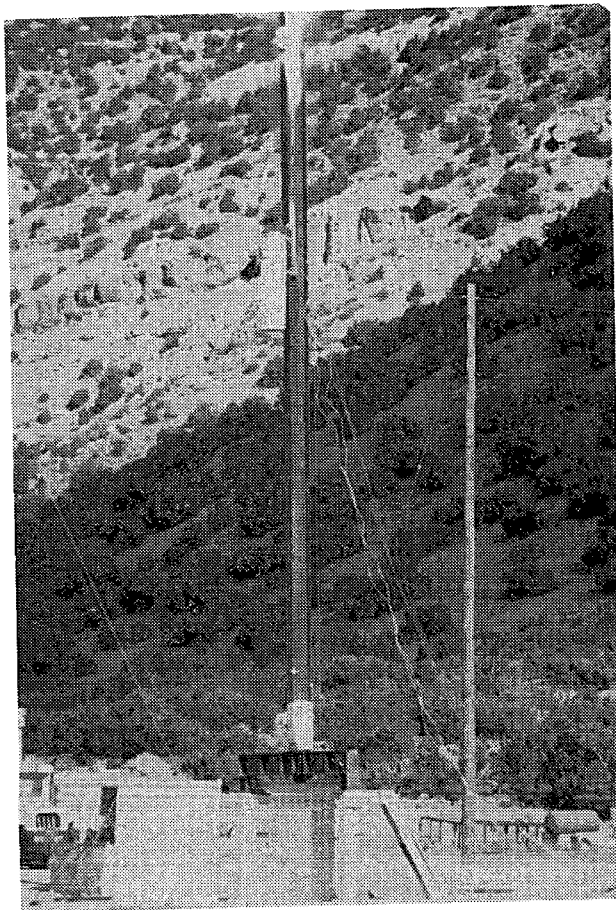


Figure 14 Test Unit Propelled by Rockets Impacting Target

being welded to the unit perimeter. Discussion of these results are detailed in the following sections.

3.2.1 Unyielding Target

The test unit was subjected to a 30-ft drop onto an unyielding target (Figure 15). After striking the target, the unit rebounded approximately six feet. The largest cask deformation experienced during the testing program occurred from this impact into the rigid target. At four inches above the point of impact, the maximum circumferential expansion occurred. The distance from the cask center-of-axis to the outer wall (radial length) increased 0.09 inches from its original 10 inches and the overall 6 ft length was shortened by 0.1 inches. The damage could not be detected visually so mechanical inspection had to be employed to measure the deformations on the order of one-hundredth of an inch. Thus, the maximum plastic deformations of the test units were on the order of 1% or less of its overall dimension.

Of the two types of instrumentation used to monitor cask responses, strain gage measurement provided much more reliable and consistent data. Accelerometer readings are inherently sensitive to the natural frequency of the test unit [10]. The possibility of exciting the natural frequencies of the test unit was increased since impact limiters were not present. This frequency which is activated from impact could cause the instrumentation to resonate ("ring") producing accelerometer readings that could be misleading. In addition, accelerometer response is highly susceptible to frequency playback that may be used during data reduction processes [11]. Every accelerometer was calibrated before and after each test to ensure validity in

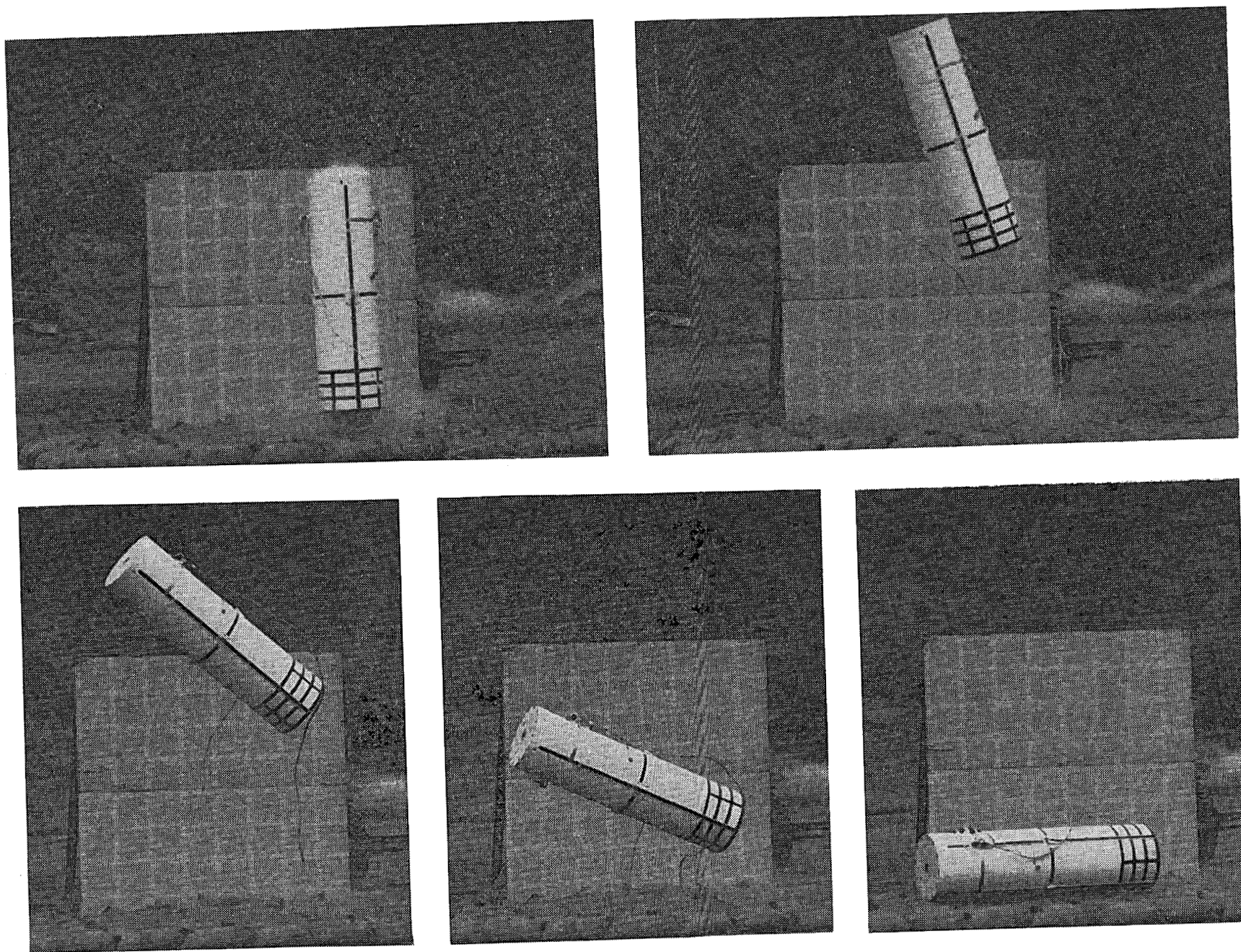


Figure 15 44 ft/s Impact into the Unyielding Target

test data and instrumentation integrity. The calibration tests performed to validate the accelerometers were the drop ball and 1000-g centrifuge. These tests were done in accordance with Sandia National Laboratories' procedures [12].

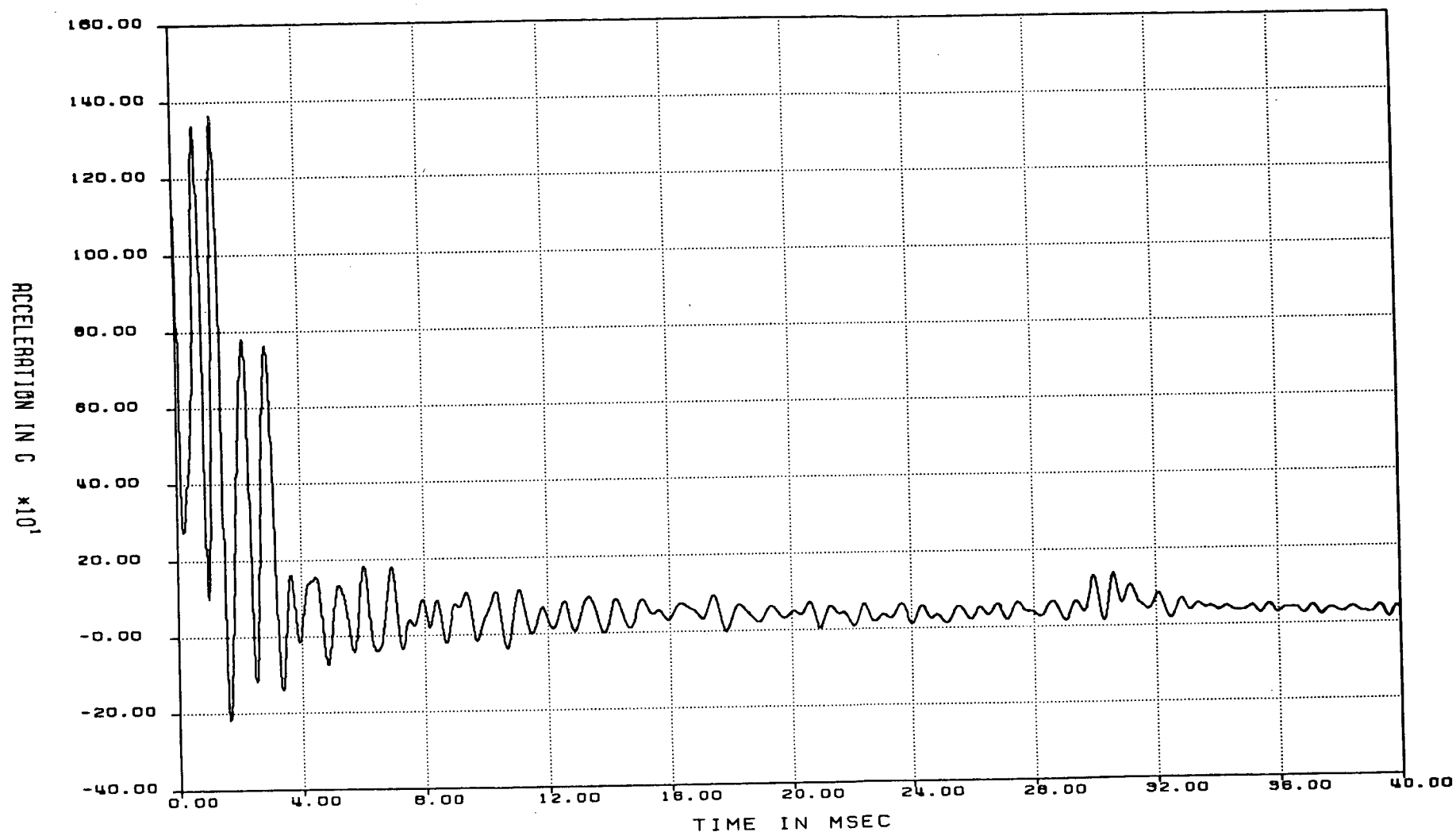
Figure 16 presents accelerometer data obtained from the 44 ft/s impact onto the rigid target. The response shows a maximum acceleration of approximately 1300 g's. The strain gage data (Figure 17) shows how the cask outer wall first compressed then proceeded to bow outward producing tension in the material. Regarding the mechanics behind this deformation mode, the impact forces the test unit into compression but because the load rate is so high the outer wall begins to buckle. This buckling stretches the outer wall thus producing a tensile reading in the strain gages. This particular strain gage was located 12 inches from the bottom of the test unit. A final permanent strain of 3000 μ in./in. (which is greater than the elastic strain limit of approximately 1200 μ in./in.) indicates plastic deformation did occur. This deformation translates to approximately 37,000 to 40,000 psi uniaxial stress at this point. Comparing the acceleration and strain gage data at the time of impact shows as the unit begins to plastically deform, energy absorption is occurring. This absorption is decreasing the response from impact. In other words, as the unit undergoes plastic deformation the magnitude of deceleration decreases. Referring to Figure 17, note that between 1 and 2 milliseconds into the event the strain gage is recording the process of plastic deformation. During the same time frame acceleration levels are decreasing dramatically (Figure 16). This is the justification for the use of impact limiters. As large deformations to impact limiters occur,

DATA FILE: R5601A
CHARGE * R803144
FILTER 10 KHZ
IIR FILTER

SAMPLE RATE 100000.0
START 0.000 MSEC
STOP 40.000 MSEC
CUTOFF= 2000.0 HZ

DIGITIZED: 20 MAR., 1986
ZERO TIME 20:36:32.309000
STATIC RUN LEVEL 0.000
LOWPASS

SYS ID: A3 CEN,AD3
HIGH CAL 5000.0000
LOW CAL 0.0000



CHANNEL ID: A-1

TRACK # 9

TEST ID: TARGET HARDNESS

TEST DATE: 3/14/86

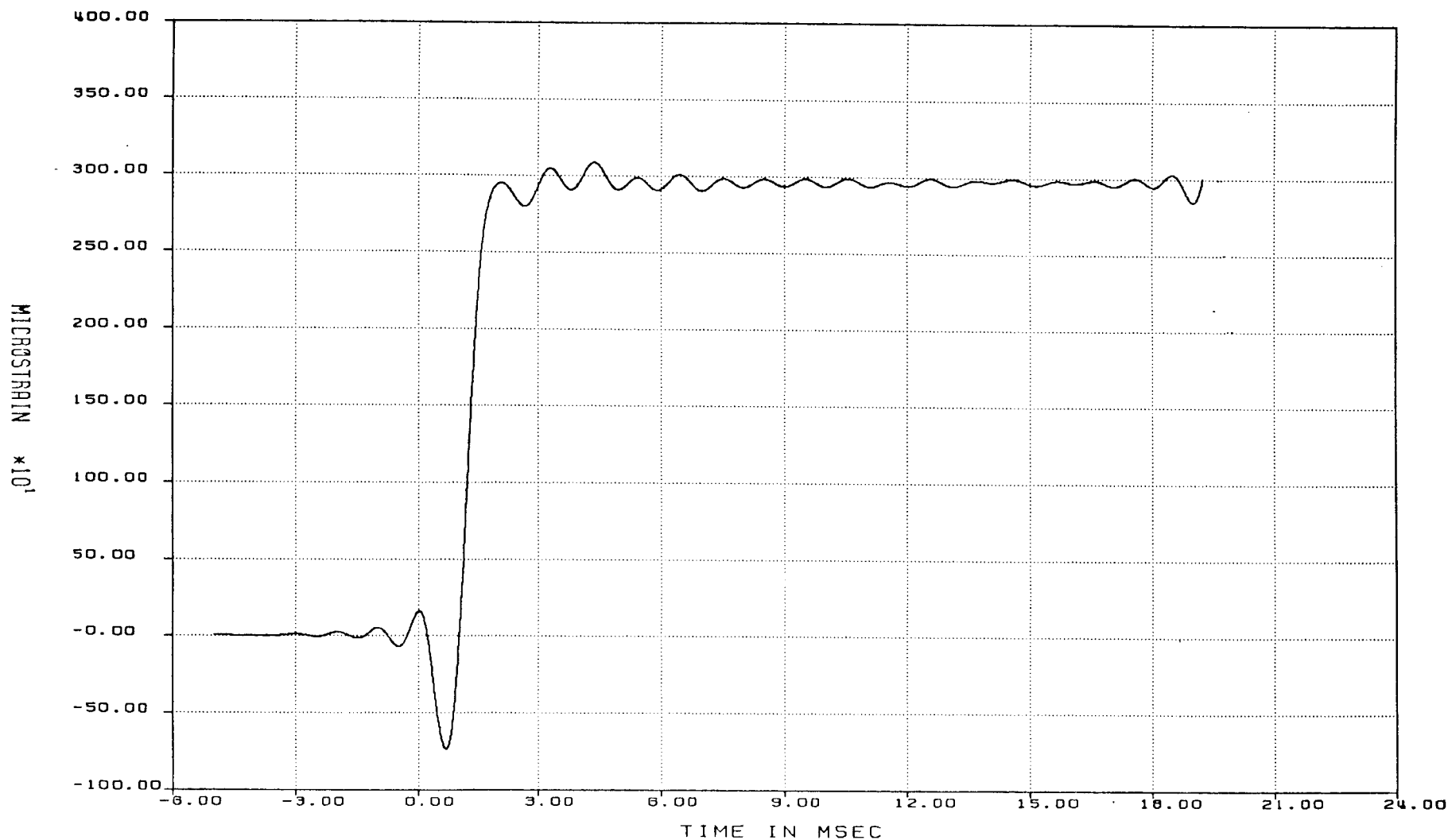
Figure 16 Acceleration Data for 44 ft/s Impact Velocity into Unyielding Target

DATA FILE: R5601A
CHARGE # R803144
FILTER 10 KHZ
IIR FILTER

SAMPLE RATE 100000.0
START -5.000 MSEC
STOP 20.000 MSEC
CUTOFF= 1000.0 HZ

DIGITIZED: 20 MAR., 1986
ZERO TIME 20:36:32.309000
STATIC RUN LEVEL 0.000
LOWPASS

SYS ID: A3 CEN,AD4
HIGH CAL 3000.0000
LOW CAL 0.0000



CHANNEL ID: S-4

TRACK # 4

TEST ID: TARGET HARDNESS

TEST DATE: 3/14/86

Figure 17 Strain Gage Data for 44 ft/s Impact Velocity into Unyielding Target

energy is being absorbed thus reducing the magnitude of accelerations experienced by the impacting package.

3.2.2 Concrete Targets

Impacting the blunt-end object into concrete targets provided a variety of results. In every case where a concrete plug was formed, the shape of the plug was conical in geometry (Figure 18). The 45° shear plane formed from impact matches the failure theory of concrete when subjected to axial compressive loads. This failure is evident when a concrete test cylinder is subjected to an axial compressive load to the point of total fracture. At ultimate strength, or when total fracture occurs, a 45° shear plane will form. This failure mechanism was apparent in every impact test into a concrete target that resulted in a shear plug.

In every concrete target test, accelerometer data produced results disproportionately higher than expected. This was in direct contrast to the strain gage readings which recorded values well within the expected range. An explanation of the unexpected accelerometer readings relates to the rigidity and the abrupt method of failure of the concrete targets. The lack of energy mitigating devices (impact limiters) on the test unit results in an increased susceptibility to resonance as a result of high natural frequency excitations in the package. In other words, the accelerometers react to the high frequency resonance generated at impact rather than the actual deceleration rate of the package. If no soft impact limiters are present to reduce the amount of high frequency oscillations produced during impact, the accelerometers naturally record a higher frequency. If a test unit

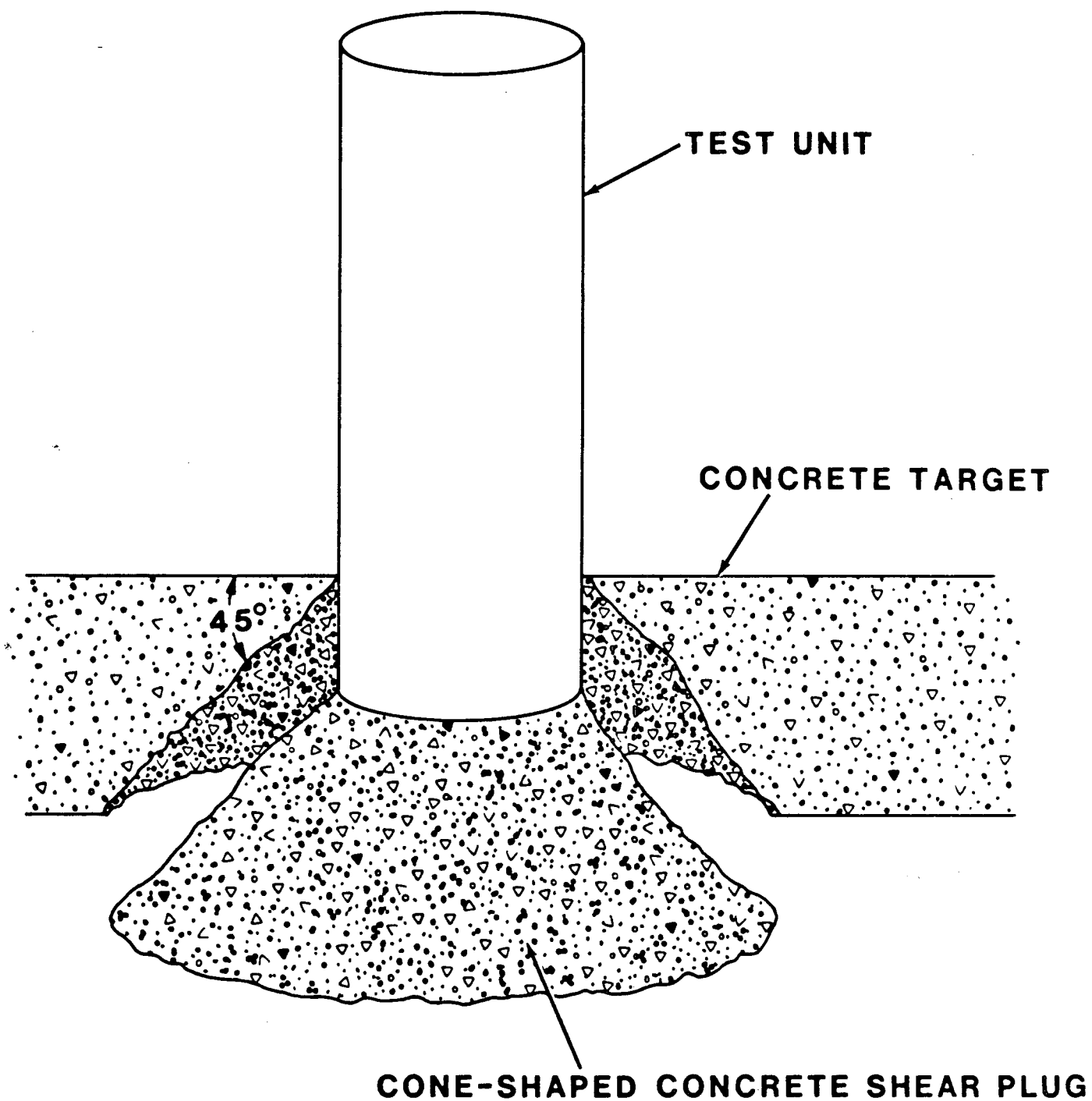


Figure 18 Shear Plug Formed in Concrete Targets

experiences a high frequency that approaches its natural frequency, resonance or "ringing" may result. If the test unit begins to resonate, it will directly effect the accelerometers and produce higher recorded g-loadings. For the test units used in this program, this susceptibility to ringing is increased by impacting onto a concrete target. An acceleration spike occurs at the point of impact producing a stress wave throughout the test unit. Once the concrete shear plug is formed, the resistance to cask motion decreases markedly. At this point the concrete material is providing very little resistance to cask travel. The soil underneath the plug then provides the stiffness needed to stop the test unit motion. With the decrease in resistance to cask travel, there is relatively little consistent support under the test unit to absorb the stress wave. A resonating effect becomes apparent producing a response in the accelerometers. In other words, the large and consistent force against the projectile as it impacted the unyielding target appears to have damped the ringing response of the test unit. Whereas with the concrete targets, the high initial force was quickly relaxed and there was no significant immediate damping of the natural frequency excitation of the test unit.

The following sections summarize the results of each concrete target test.

3.2.2.1 44 ft/s Impact into the Concrete Runway

The 44 ft/s impact into the concrete runway target penetrated approximately 0.25 inches (Figure 19). The impact produced radial cracking in the concrete target from the point of impact. This radial cracking was

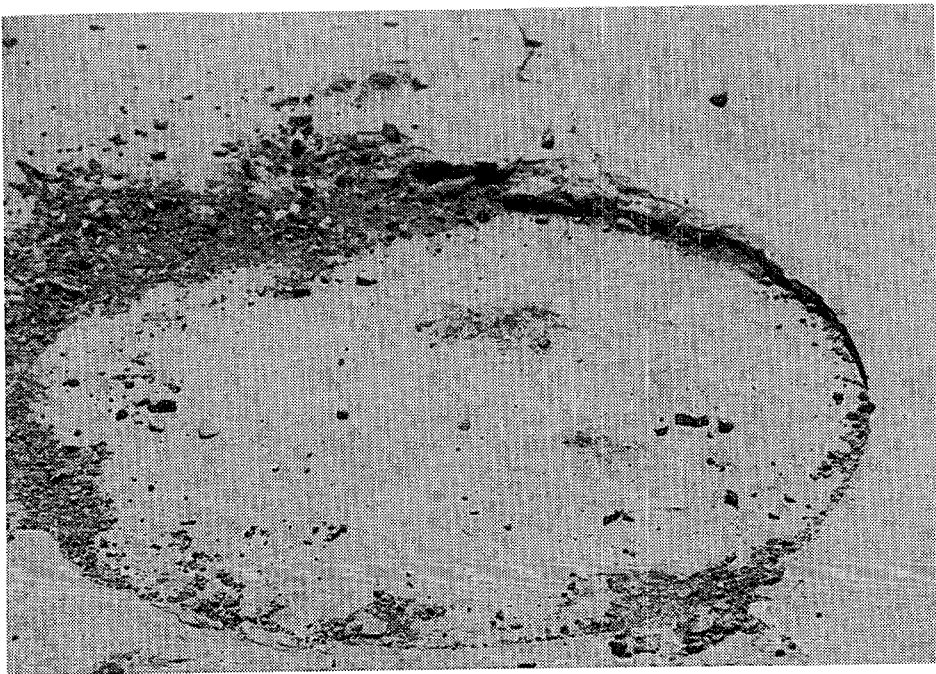


Figure 19 Concrete Runway Surface After an Impact at a Velocity of 44 ft/s

slight, but presented a phenomenon becoming more pronounced in higher velocity impacts. A very slight measurable cask deformation was determined from mechanical inspection. The test unit radial length expanded a maximum of 0.01 inches at 3.0 inches from the cask bottom.

Figures 20 and 21 present the recorded accelerations and strains measured from the drop test. A maximum acceleration of 480 g's resulted in strain levels of approximately 900 μ in./in. in compression. This strain gage, located twelve inches from the bottom, showed residual strain of 400 μ in./in. in tension which indicates a very slight permanent deformation. This correlates with the findings obtained from mechanical inspection.

3.2.2.2 66 ft/s Impact into the Concrete Runway

Impacting the 18-inch thick concrete runway at 66 ft/s resulted in a cask penetration of 4 inches (Figure 22). The radial length increased 0.03 inches, at the point 3.0 inches from the cask bottom. A shear plug (Figure 23) was formed with the top face a perfect imprint of the bottom of the test unit.

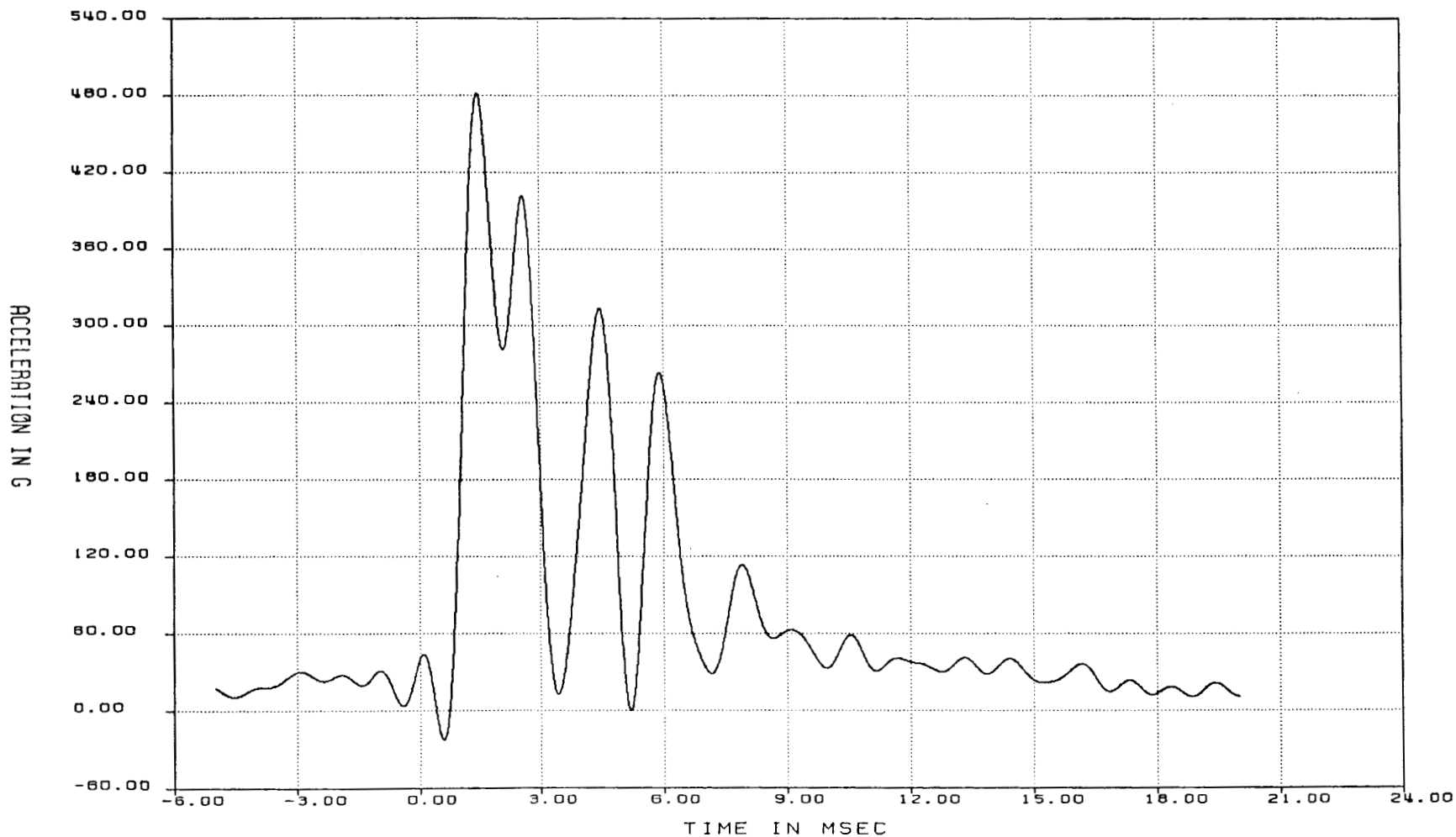
The peak recorded acceleration of 900 g's (Figure 24) and peak strains of 2,300 μ in./in. (Figure 25) are a definite increase in magnitude from the values obtained from the 44 ft/s impact. As with the impact into the unyielding target, the phenomenon of the outer wall compressing upon impact then bowing outward occurred. The material in the outer cylinder reached strains in compression in the order of 1000 μ in./in., then bowed outward producing strains in tension. A residual strain of approximately 500 μ in./in. shows the unit suffered permanent deformation. This strain reading

DATA FILE: R5542A
CHARGE # 8950433
FILTER 10 KHZ
IIR FILTER

SAMPLE RATE 100000.0
START -5.000 MSEC
STOP 20.000 MSEC
CUTOFF= 1000.0 HZ

DIGITIZED: 16 AUG., 1985
ZERO TIME 19:28:19.270000
STATIC RUN LEVEL 0.000
LOWPASS

SYS ID: A3 CEN,AD6
HIGH CAL 5000.0000
LOW CAL 0.0000



CHANNEL ID: A-5

TRACK #13

TEST ID: TARGET HARDNESS # 4

TEST DATE: 8/15/85

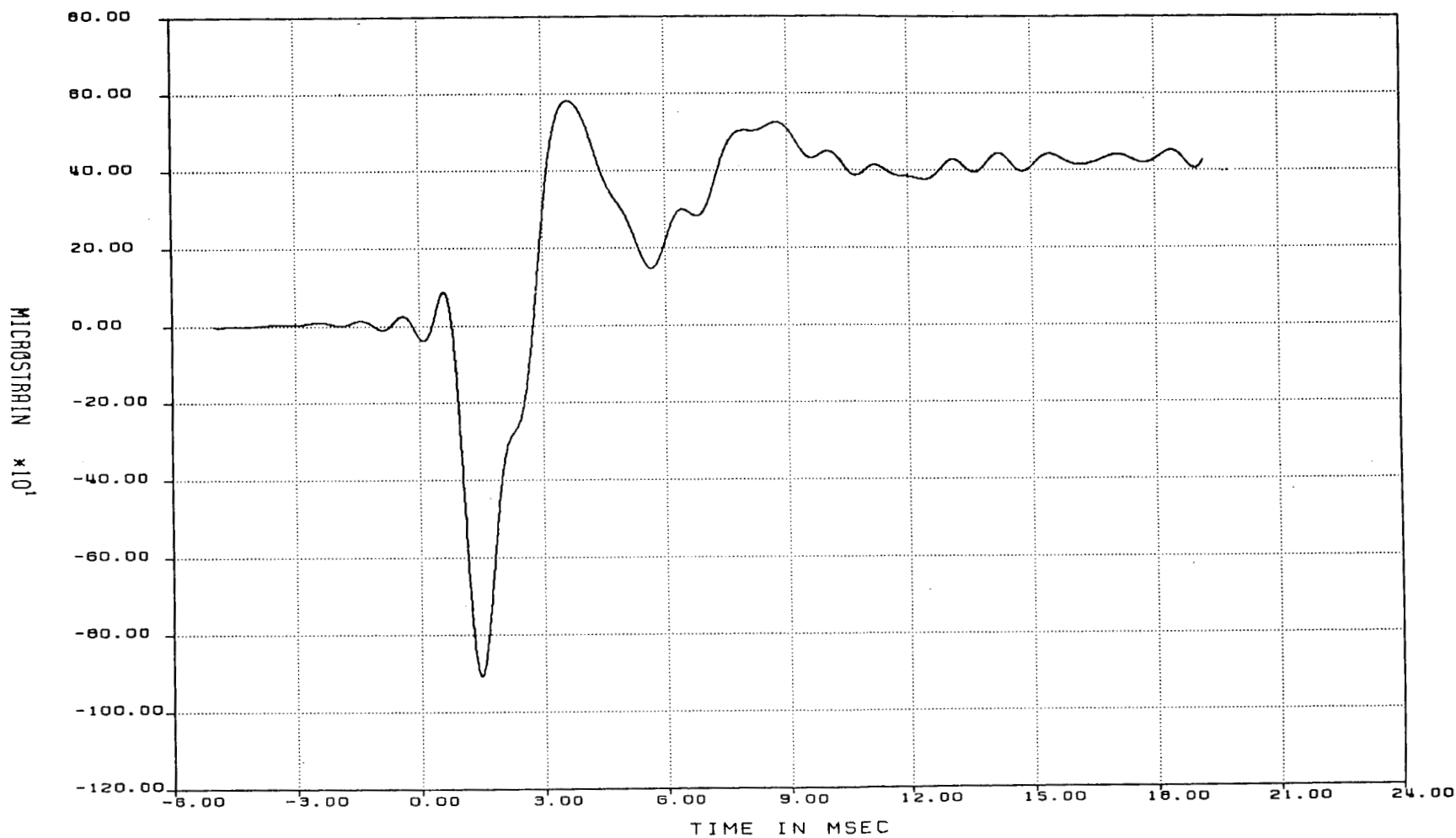
Figure 20 Acceleration Data for 44 ft/s Impact Velocity into Concrete Runway Target

DATA FILE: R5542A
CHARGE # 8950433
FILTER 10 KHZ
IIR FILTER

SAMPLE RATE 100000.0
START -5.000 MSEC
STOP 20.000 MSEC
CUTOFF= 1000.0 HZ

DIGITIZED: 16 AUG., 1985
ZERO TIME 19:28:19.270000
STATIC RUN LEVEL 0.000
LOWPASS

SYS ID: A3 CEN,AD5
HIGH CAL 1000.0000
LOW CAL 0.0000



CHANNEL ID: S-8

TRACK #12

TEST ID: TARGET HARDNESS # 4

TEST DATE: 8/15/85

Figure 21 Strain Gage Data for 44 ft/s Impact Velocity into Concrete Runway Target

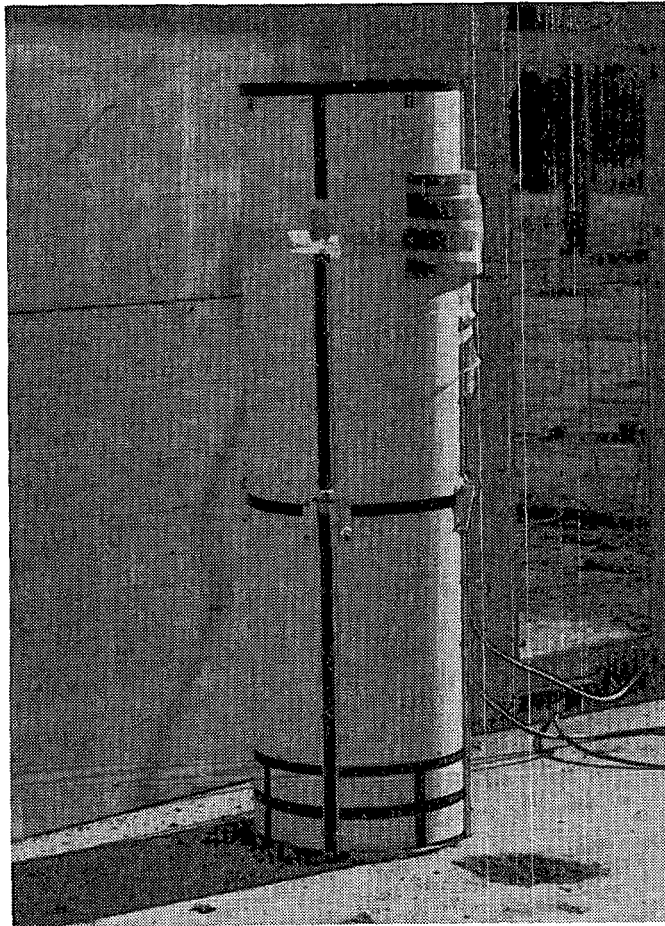


Figure 22 Test Unit's 4-inch Penetration into the Concrete Runway
After Impacting at a Velocity of 66 ft/s



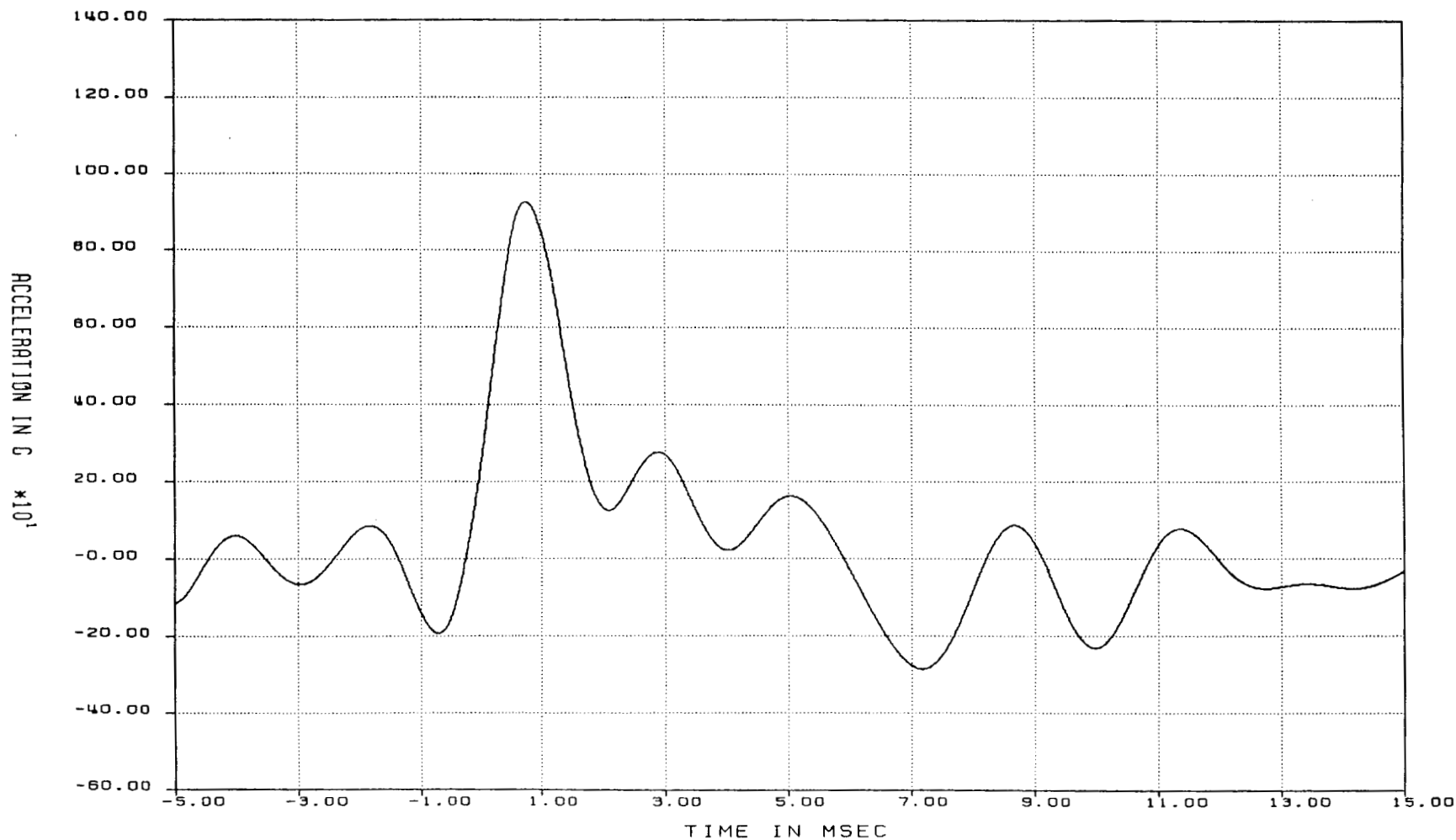
Figure 23 Shear Plug Formed in Concrete Runway After Impacting at a Velocity of 66 ft/s

DATA FILE: R5570A
CHARGE # 8950.433
FILTER 10 KHZ
IIR FILTER

SAMPLE RATE 100000.0
START -5.000 MSEC
STOP 15.000 MSEC
CUTOFF= 500.0 HZ

DIGITIZED: 7 NOV., 1985
ZERO TIME 21:35:28.192000
STATIC RUN LEVEL 0.000
LOWPASS

SYS ID: A3 CEN,AD1
HIGH CAL 5000.0000
LOW CAL 0.0000



CHANNEL ID: A-1

TRACK # 1

TEST ID: TARGET HARDNESS #6

TEST DATE: 11/ 1/85

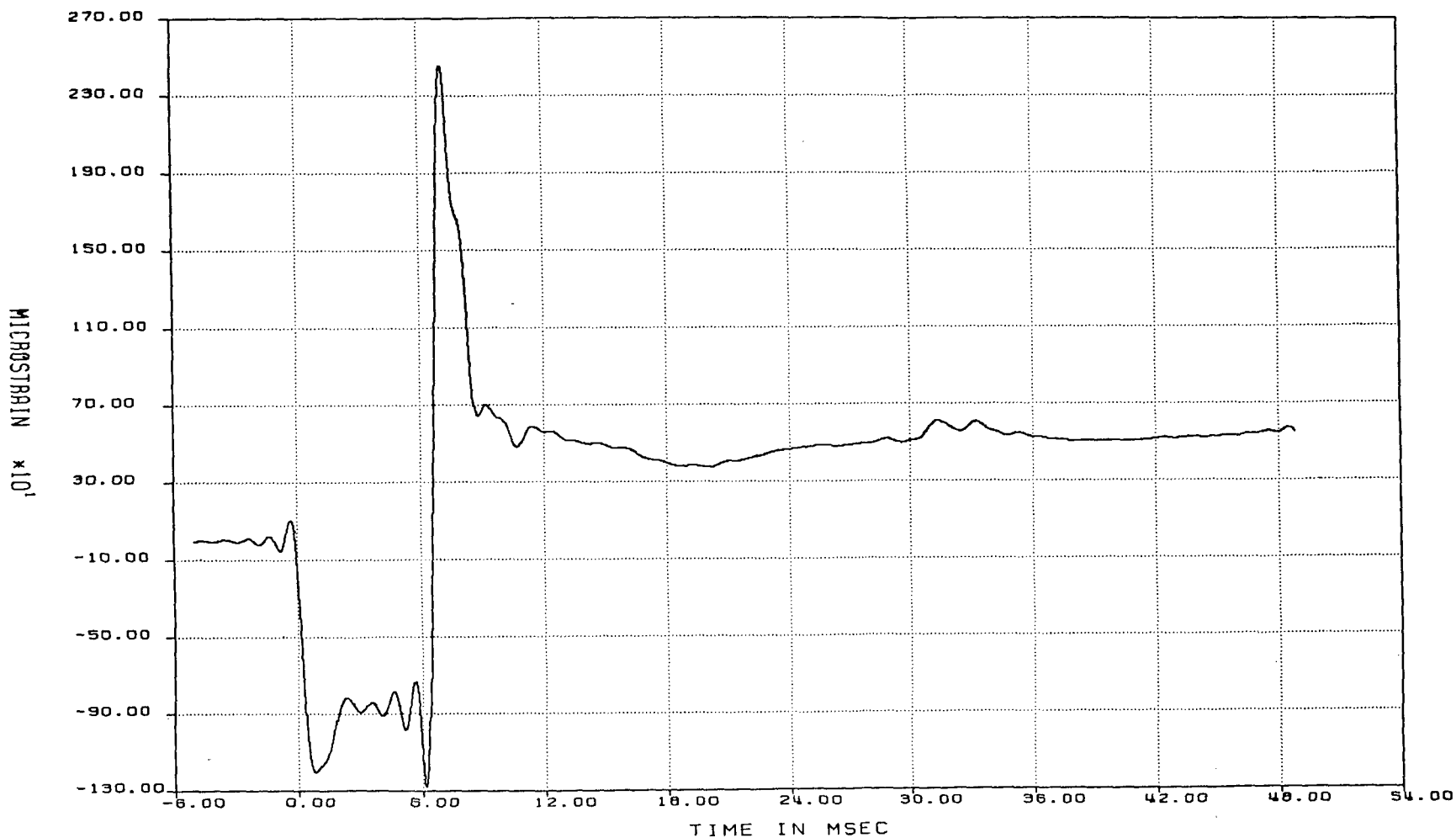
Figure 24 Acceleration Data for 66 ft/s Impact Velocity into Concrete Runway Target

DATA FILE: R5570A
CHARGE # 8950.433
FILTER 10 KHZ
IIR FILTER

SAMPLE RATE 100000.0
START -5.000 MSEC
STOP 50.000 MSEC
CUTOFF= 1000.0 HZ

DIGITIZED: 7 NOV., 1985
ZERO TIME 21:35:28.192000
STATIC RUN LEVEL 0.000
LOWPASS

SYS ID: A3 CEN,AD7
HIGH CAL 2000.0000
LOW CAL 0.0000



CHANNEL ID: S-3

TRACK # 7

TEST ID: TARGET HARDNESS #6

TEST DATE: 11/ 1/85

Figure 25 Strain Gage Data for 66 ft/s Impact Velocity into Concrete Runway Target

again coincides with the permanent deformation found from posttest measurements.

3.2.2.3 88 ft/s Impact into the Concrete Runway

The highest impact velocity of 88 ft/s into the concrete runway target produced a cask penetration of 8 inches (Figures 26 and 27). The unit suffered an increase in radial length of 0.08 inches at 3.5 inches from the cask bottom. The unit's overall axial length shortened 0.08 inches.

Recorded accelerations were in the range of 1000 g's. Figure 28 shows a positive acceleration pulse of 1000 g's and a negative pulse of approximately 900 g's. This negative pulse of such a large magnitude is an anomaly in the data which is not typical of the type of accelerometer readings expected. The negative pulse occurs at approximately six milliseconds into the impact event. A possible explanation of this pulse relates to Figures 29 and 30 where the strain gage levels change drastically at the six milliseconds mark. As discussed previously, this change in magnitude directly effects the measured acceleration levels. A large drop in strain levels correlates to a decreased magnitude in accelerations which in this case have been over compensated by the instrumentation.

Figures 29 and 30 present strain gage data at two different points on the test unit. Figure 29 shows data from a strain gage 2.75 inches from the cask bottom. Data from a strain gage located 90° around the unit and 12 inches from the bottom is shown in Figure 30. Figure 29 shows at the location close to the point of impact the material was strained to 5500 μ in./in. in compression and finally ended up with 4800 μ in./in. in residual compressive

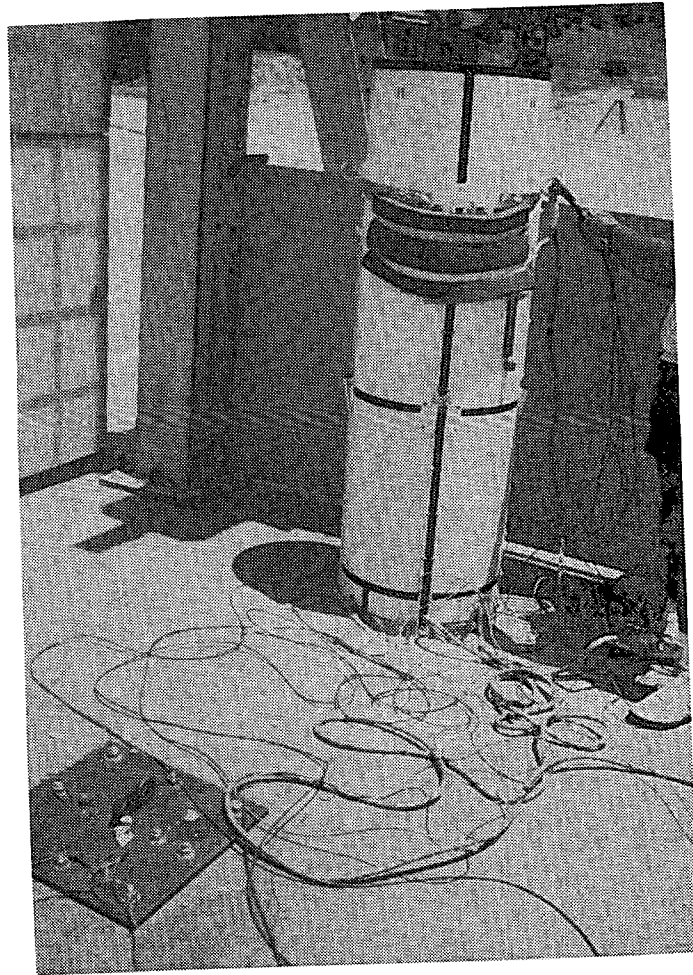


Figure 26 Test Unit's 8-inch Penetration into the Concrete Runway
After Impacting at a Velocity of 88 ft/s

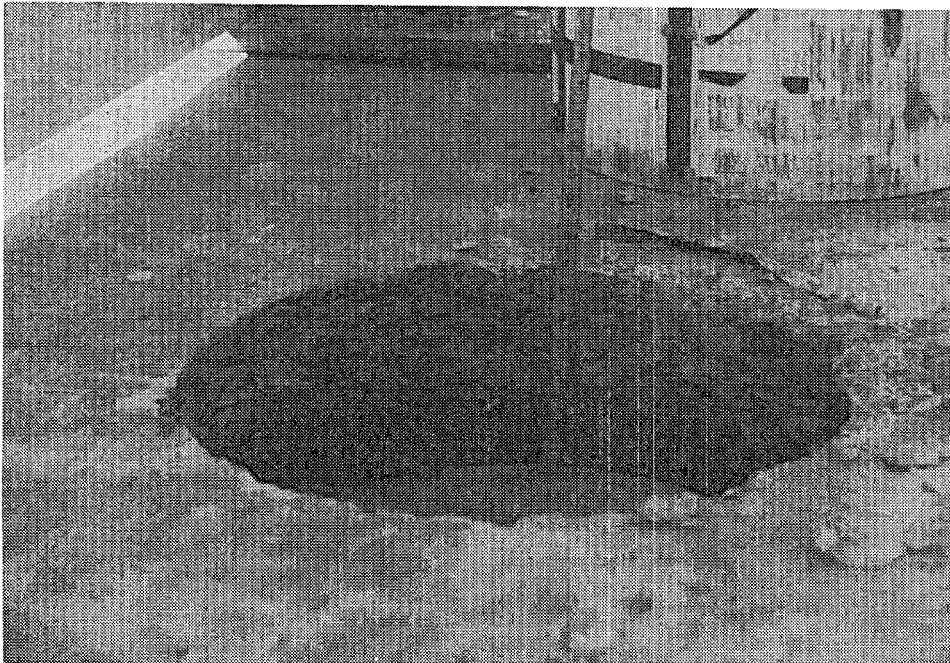


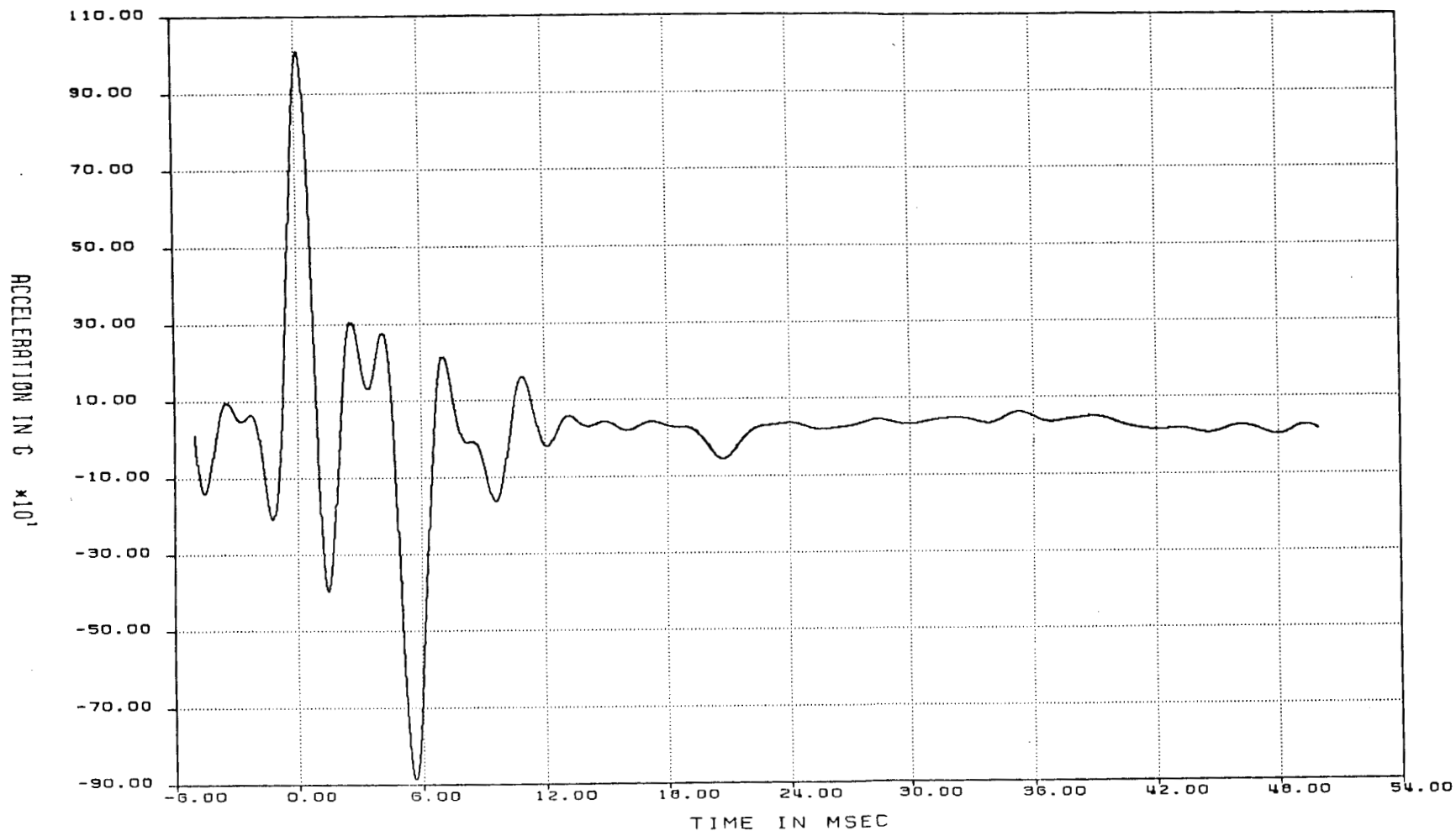
Figure 27 Shear Plug Formed in Concrete Runway
After Impacting at a Velocity of 88 ft/s

DATA FILE: R5640A
CHARGE * R803144
FILTER 10 KHZ
IIR FILTER

SAMPLE RATE 100000.0
START -5.000 MSEC
STOP 50.000 MSEC
CUTOFF= 500.0 HZ

DIGITIZED: 24 JUNE, 1986
ZERO TIME 19:19:29.080580
STATIC RUN LEVEL 0.000
LOWPASS

SYS ID: A3 CEN,AD1
HIGH CAL 10000.000
LOW CAL 0.0000



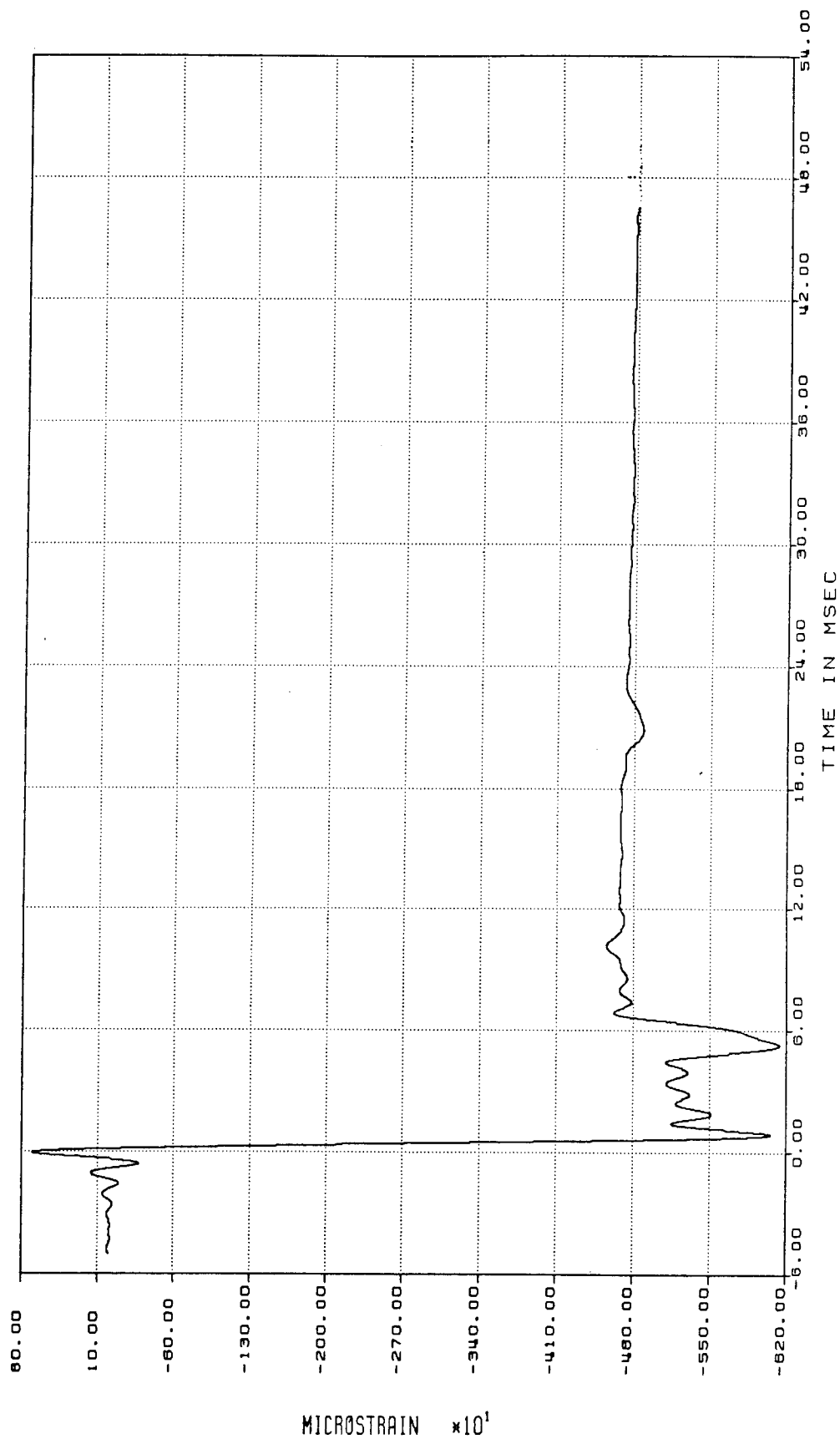
CHANNEL ID: A-1

TRACK # 1

TEST ID: TARGET HARDNESS # 11
Figure 28 Acceleration Data for 88 ft/s Impact Velocity into Concrete Runway Target

TEST DATE: 6/17/86

DATA FILE: R5640A SAMPLE RATE 100000.0 DIGITIZED: 24 JUNE, 1986 SYS ID: A3 CEN.AD3
 CHARGE # R803144 START -5.000 MSEC ZERO TIME 19:19:29.080580 HIGH CAL 3000.0000
 FILTER 10 KHZ STOP 50.000 MSEC STATIC RUN LEVEL 0.000 LOW CAL 0.0000
 IIR FILTER CUTOFF= 1000.0 HZ LOWPASS



CHANNEL ID: S-7 TRACK #11

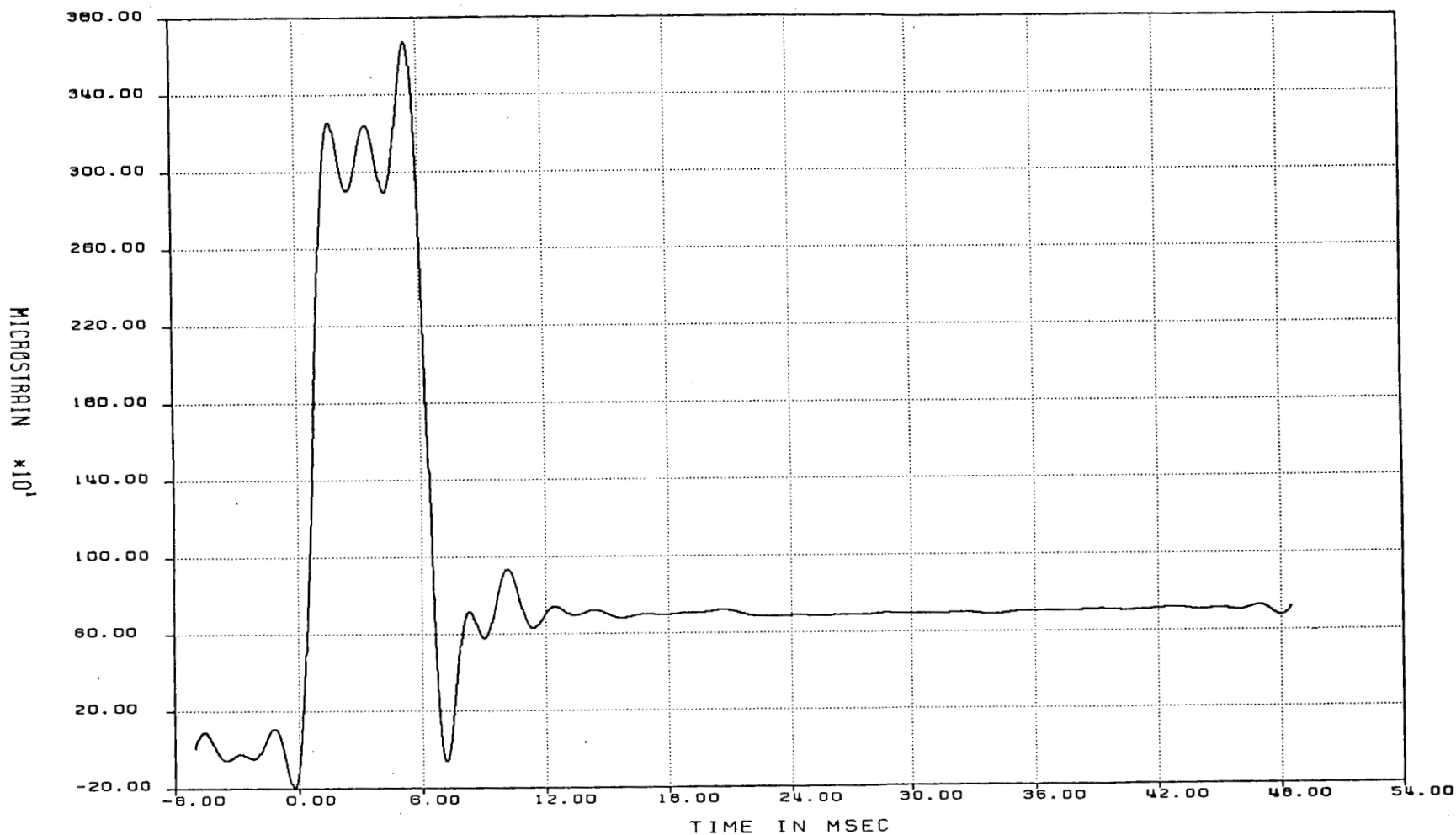
TEST ID: TARGET HARDNESS # 11 TEST DATE: 6/17/86
 Figure 29 Strain Gage Data for 88 ft/s Impact Velocity into Concrete Runway Target

DATA FILE: R5640A
CHARGE # R803144
FILTER 10 KHZ
IIR FILTER

SAMPLE RATE 100000.0
START -5.000 MSEC
STOP 50.000 MSEC
CUTOFF= 500.0 HZ

DIGITIZED: 24 JUNE, 1986
ZERO TIME 19:19:29.080580
STATIC RUN LEVEL 0.000
LOWPASS

SYS ID: A3 CEN,AD6
HIGH CAL 3000.0000
LOW CAL 0.0000



CHANNEL ID: S-2

TRACK # 6

TEST ID: TARGET HARDNESS # 11

TEST DATE: 6/17/86

Figure 30 Strain Gage Data for 88 ft/s Impact Velocity into Concrete Runway Target

strain. Here, the material did not bow outward but compressed axially. About 9 inches above this point on the unit the material did expand outward as indicated by the maximum 3400μ in./in. with a residual strain of approximately 600μ in./in. in tension. These two figures are representative of the phenomenon that exists when a hollow-shaped cylinder, whose head end is highly constrained, is impacted into a target to produce plastic deformation.

3.2.2.4 44 ft/s Impact into Concrete Highway

Impacting into the 9-inch thick concrete highway targets produced extensive radial and concentric cracking (Figure 31) on the impact surface with the formation of a shear plug. As the impact speed increased so did the magnitude of target damage. The target cracking and deflection became more pronounced such that the final deformed shape was concave in appearance. At 44 ft/s impact velocity, the test unit penetrated 4 inches into the target (Figure 32). No permanent cask deformation resulted from the drop test.

A measured acceleration of 350 g's was recorded (Figure 33). The maximum strain of 900μ in./in. in compression produced no residual strain (Figure 34) thus correlating with the mechanical inspection findings of no permanent deformation.

3.2.2.5 66 ft/s Impact into Concrete Highway

This particular test was marred with technical difficulties with respect to the test rockets and instrumentation. The rockets misfired resulting in an impact velocity of approximately 44 ft/s. Inoperable instrumentation produced

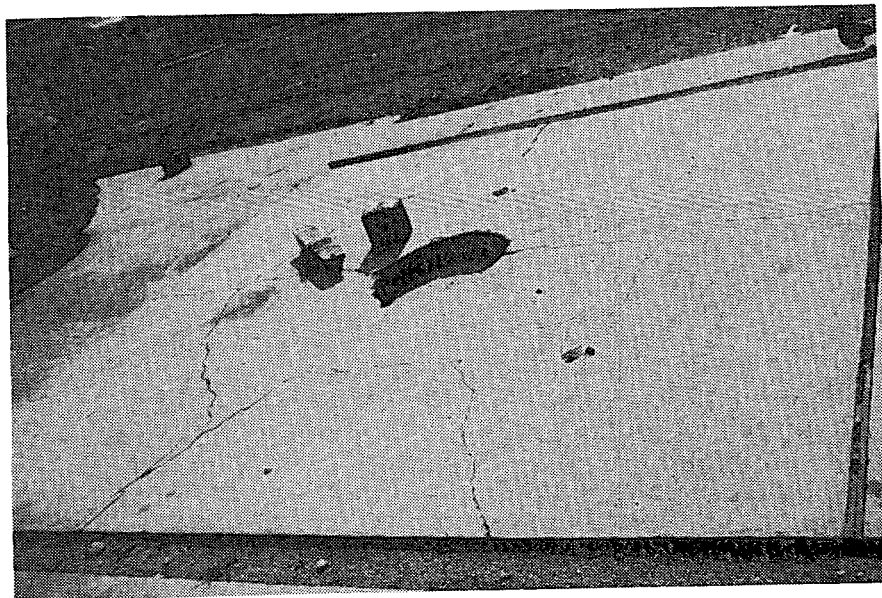


Figure 31 Concrete Highway Damage After
Impacting at a Velocity of 44 ft/s

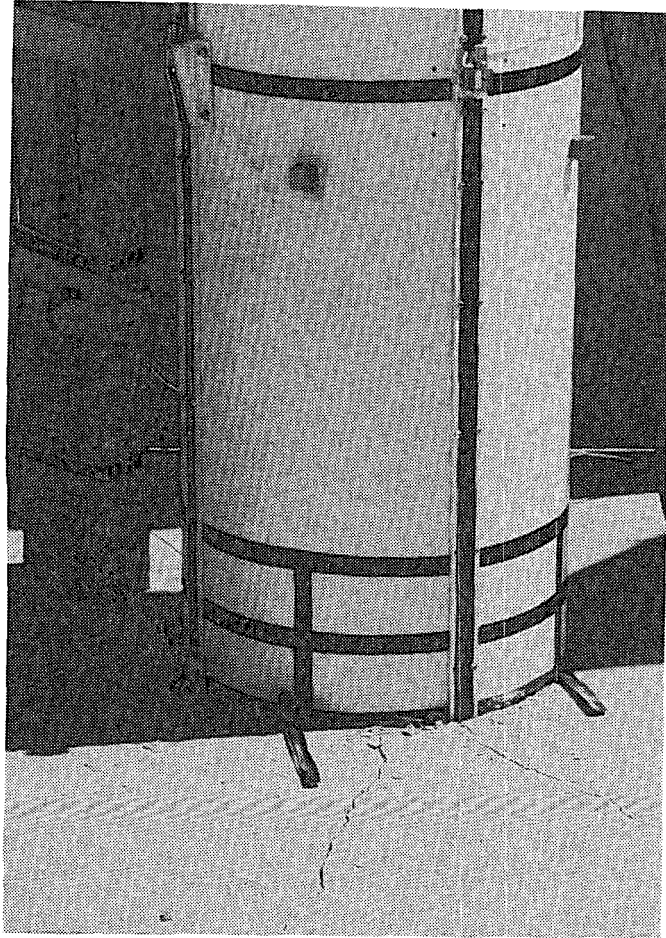


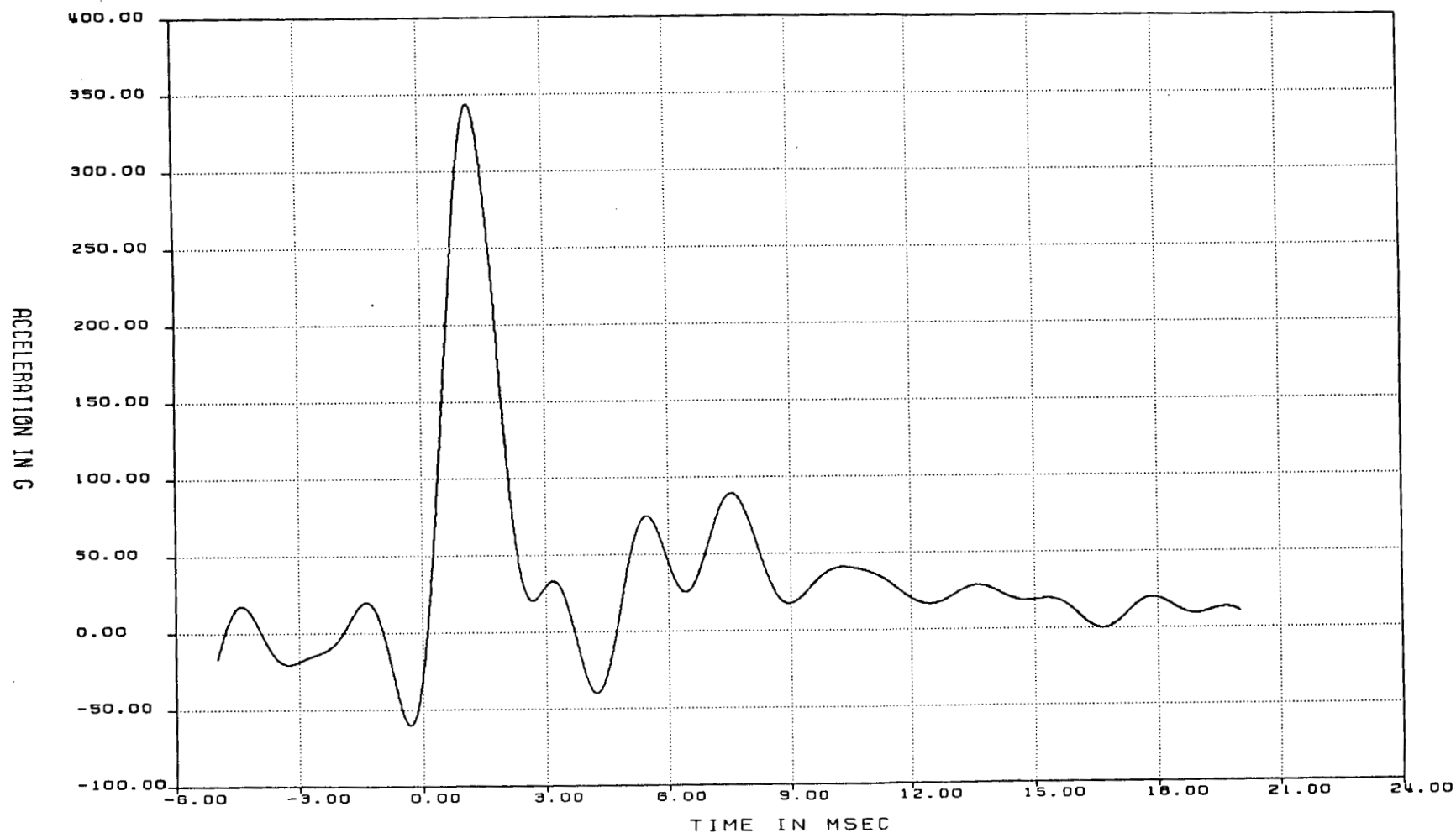
Figure 32 Test Unit's 4-inch Penetration into the Concrete Runway
After Impacting at a Velocity of 44 ft/s

DATA FILE: R5554A
CHARGE # 8950.433
FILTER 10 KHZ
IIR FILTER

SAMPLE RATE 100000.0
START -5.000 MSEC
STOP 20.000 MSEC
CUTOFF= 500.0 HZ

DIGITIZED: 13 SEPT, 1985
ZERO TIME 19:50:41.956000
STATIC RUN LEVEL 0.000
LOWPASS

SYS ID: A3 CEN,AD5
HIGH CAL 500.0000
LOW CAL 0.0000



CHANNEL ID: A-5

TRACK # 5

TEST ID: TARGET HARDNESS EVENT #5

TEST DATE: 9/12/85

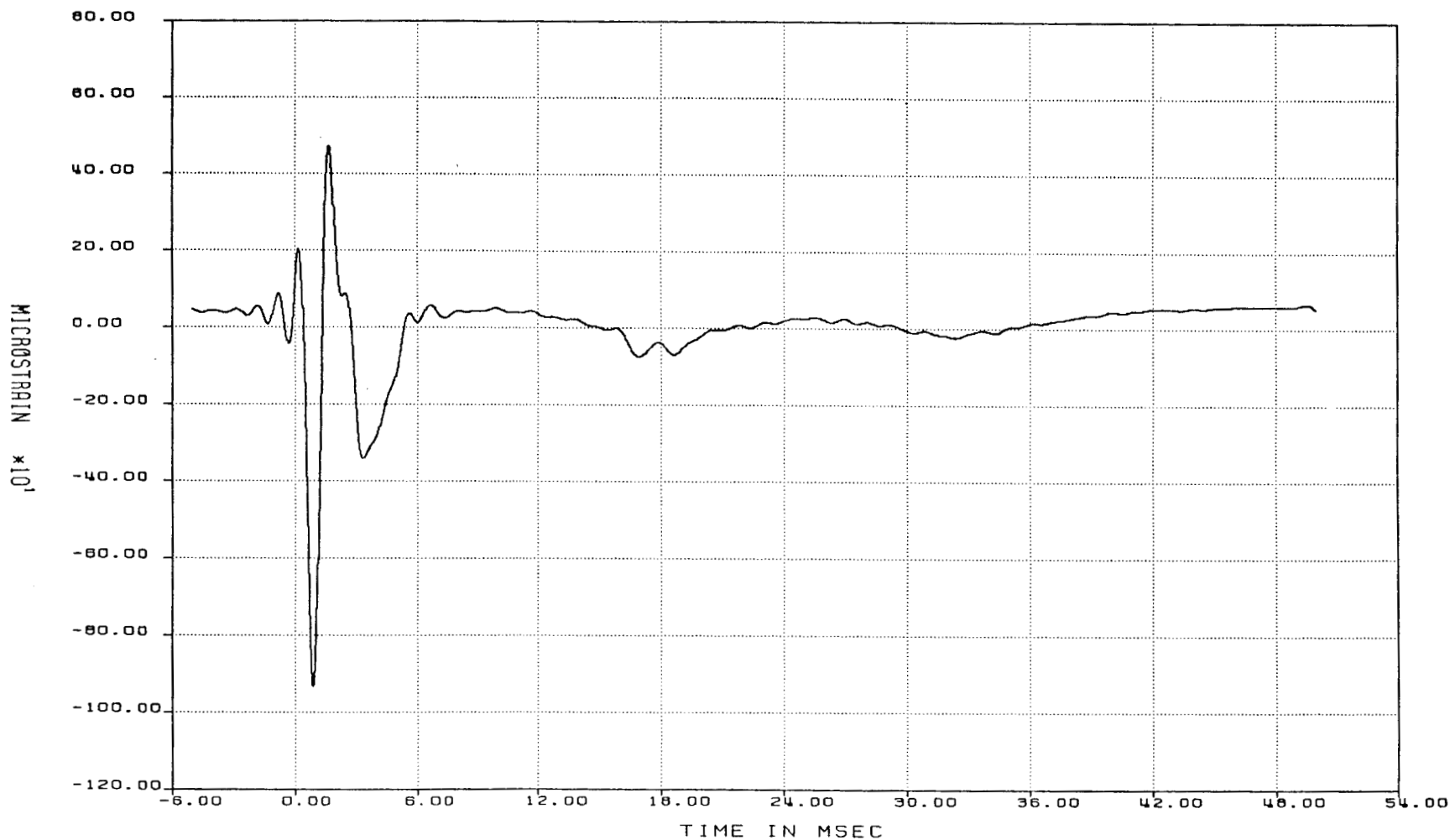
Figure 33 Acceleration Data for 44 ft/s Impact Velocity into Concrete Highway

DATA FILE: R5554A
CHARGE # 8950.433
FILTER 10 KHZ
IIR FILTER

SAMPLE RATE 100000.0
START -5.000 MSEC
STOP 50.000 MSEC
CUTOFF= 1000.0 HZ

DIGITIZED: 13 SEPT, 1985
ZERO TIME 19:50:41.956000
STATIC RUN LEVEL 0.000
LOWPASS

SYS ID: A3 CEN,AD6
HIGH CAL 1000.0000
LOW CAL 0.0000



CHANNEL ID: S-7

TRACK #13

TEST ID: TARGET HARDNESS EVENT #5

TEST DATE: 9/12/85

Figure 34 Strain Gage Data for 44 ft/s Impact Velocity into Concrete Highway Target

no acceleration or strain gage data. However, the cask penetration into the target of 4 inches matched that obtained from the earlier 44 ft/s drop. The target damage between the two tests was identical (Figure 35). Thus, with respect to unit penetration and target damage, reproducible results were obtained impacting a concrete highway target twice at a velocity of 44 ft/s.

3.2.2.6 88 ft/s Impact into Concrete Highway

A penetration of 19 inches resulted from the 88 ft/s impact into the concrete highway (Figure 36). Taking into account a high impact velocity and large unit penetration, the target damage and cracking was identical in geometrical appearance to that found in the two previous concrete highway tests. At 3.5 inches above the bottom of the test unit, the maximum increase in radial length was 0.02 inches.

As with the 88 ft/s impact into the concrete runway, acceleration readings were disproportionately higher than expected (Figure 37), however the magnitude of the highway impact was much greater. At impact the accelerometers recorded 4500 g's. This is the cask response at the point the test unit strikes the target and energy is absorbed into forming the shear plug. Approximately 6 milliseconds later another acceleration load of 7500 g's is recorded. This represents the test unit stopping after the soil underneath locks up. These acceleration magnitudes do not coincide with expected values and in fact are contradictory with respect to measured deformations and recorded strains. Note that the 18-inch thick concrete runway recorded lower acceleration magnitudes (1000 g's) than this 9-inch thick highway slab. This is an anomaly since the stiffer runway should

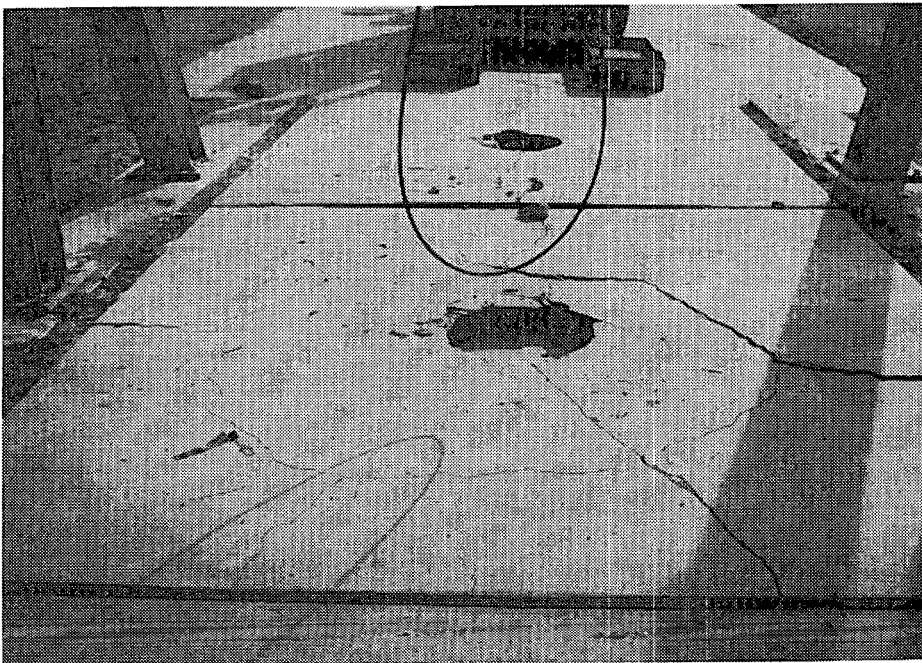


Figure 35 Concrete Highway Damage from Impacting
at a Velocity of 44 ft/s

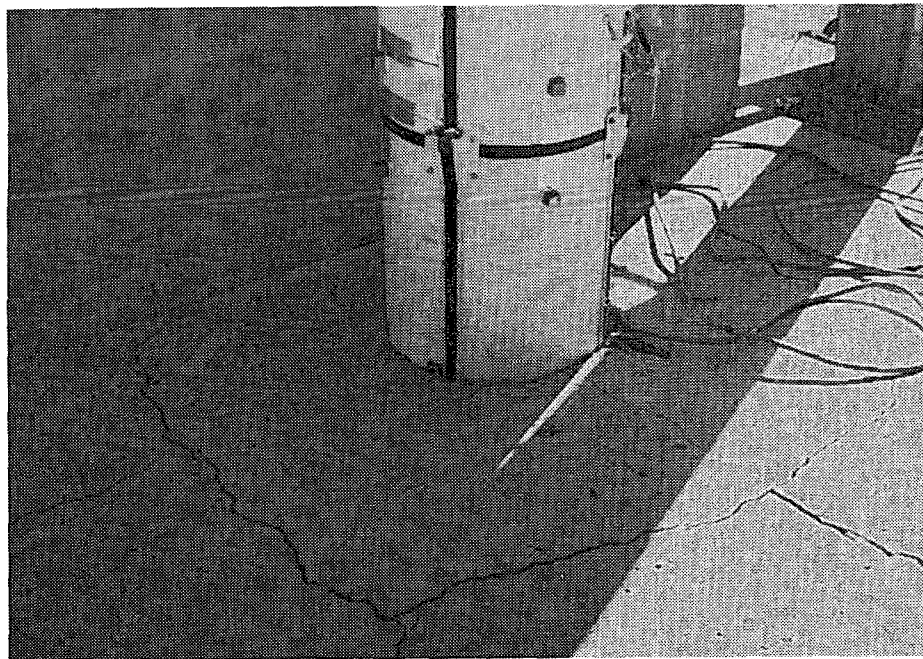


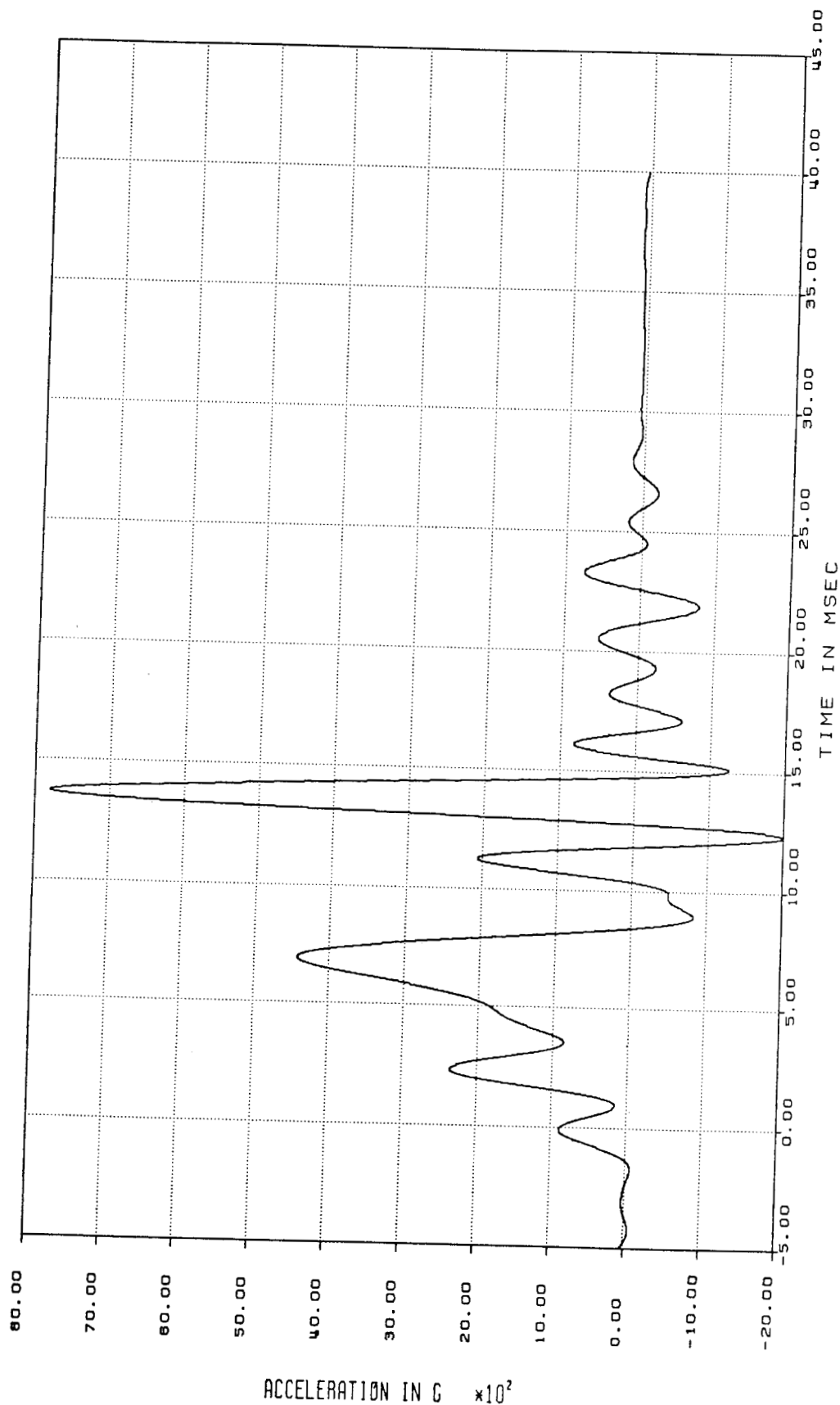
Figure 36 Test Unit's 19-inch Penetration into the Concrete Highway
After Impacting at a Velocity of 88 ft/s

DATA FILE: R5592A
CHARGE # 8950.433
FILTER 10 KHZ
IIR FILTER

SAMPLE RATE 100000.0
START -5.000 MSEC
STOP 40.000 MSEC
CUTOFF= 500.0 HZ

DIGITIZED: 27 JAN., 1986
ZERO TIME 19:51:21.931000
STATIC RUN LEVEL 0.000
LOWPASS

SYS ID: A3 CEN,ADS
HIGH CAL 10000.000
LOW CAL 0.0000



TEST ID: TARGET HARDNESS #7

Figure 37 Acceleration Data for 88 ft/s Impact Velocity into Concrete Highway Target

TEST DATE: 1/24/86

produce higher decelerations. The maximum strain in compression of 1800μ in./in. produced a residual strain of 1300μ in./in. (Figure 38) which correlates well with the 0.02 in. measured axial deformation. This strain gage was located 12 inches from the bottom. Figure 39 shows the recorded data of a strain gage 2.75 inches from the cask's bottom. The unit suffered a maximum compressive strain of 800μ in./in. then experienced 2400μ in./in. in tension. A 600μ in./in. residual strain correlates with the elongation of the cask circumference. Thus, the recorded accelerations are assumed to be directly affected by the frequencies generated by impacting a brittle target. The natural frequencies of the test unit are excited and produce artificially high readings in the accelerometers.

3.2.3 Soil Targets

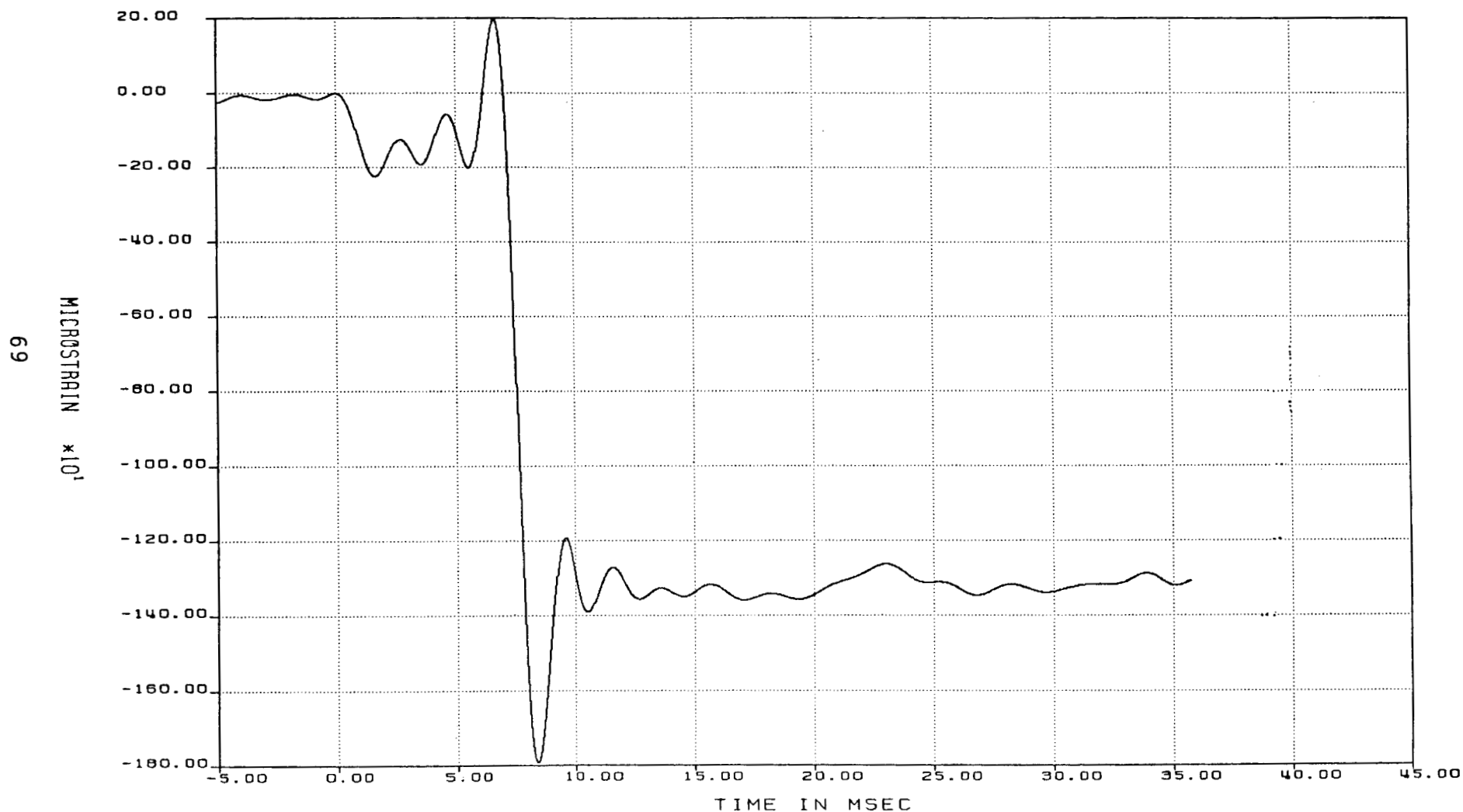
Four drops ranging in velocity from 44 ft/s (30 mph) to 110 ft/s (75 mph) into soil generated results of impacting a relatively soft target. Two types of soil were used as targets. For the velocities of 44 ft/s, 66 ft/s, and 88 ft/s an in-situ undisturbed native desert soil represented the target. Imported borrow, uncompacted for a depth of 7 ft, constituted the target for the 110 ft/s impact. The 7 ft depth was based on analytical calculations to determine final penetration depth of the test unit impacting at a velocity of 110 ft/s. The phenomenon of a dual acceleration spike that occurred in the 88 ft/s concrete highway test becomes more pronounced in the soil tests. The following sections summarizes the series of soil impact tests.

DATA FILE: R5592A
CHARGE # 8950.433
FILTER 10 KHZ
IIR FILTER

SAMPLE RATE 100000.0
START -5.000 MSEC
STOP 40.000 MSEC
CUTOFF= 500.0 HZ

DIGITIZED: 27 JAN., 1986
ZERO TIME 19:51:21.931000
STATIC RUN LEVEL 0.000
LOWPASS

SYS ID: A3 CEN,AD1
HIGH CAL 2000.0000
LOW CAL 0.0000



CHANNEL ID: S-2

TRACK # 8

TEST ID: TARGET HARDNESS #7

TEST DATE: 1/24/86

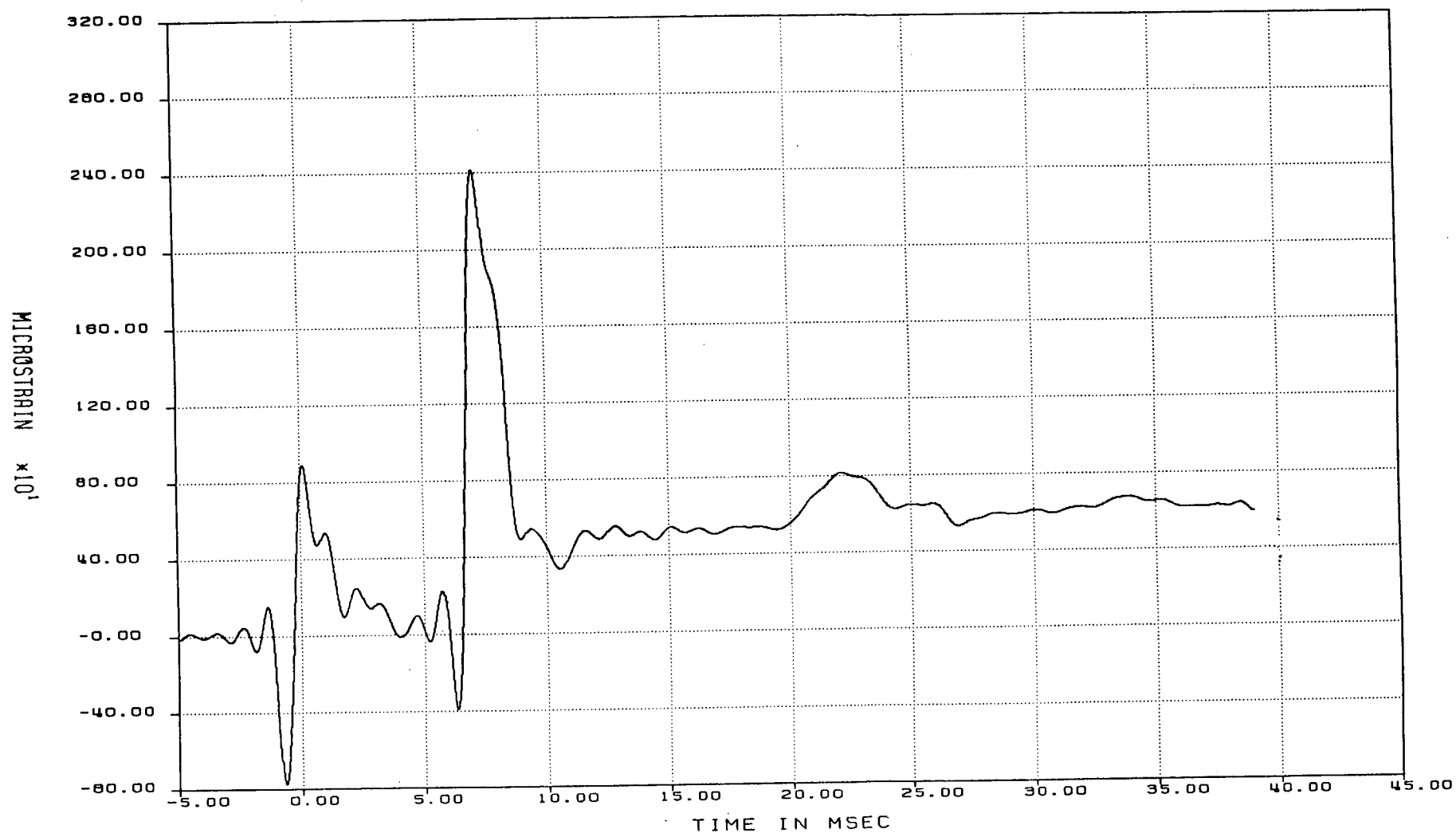
Figure 38 Strain Gage Data for 88 ft/s Impact Velocity into Concrete Highway Target

DATA FILE: R5592A
CHARGE * 8950.433
FILTER 10 KHZ
IIR FILTER

SAMPLE RATE 100000.0
START -5.000 MSEC
STOP 40.000 MSEC
CUTOFF= 1000.0 HZ

DIGITIZED: 27 JAN., 1986
ZERO TIME 19:51:21.931000
STATIC RUN LEVEL 0.000
LOWPASS

SYS ID: A3 CEN,AD6
HIGH CAL 2000.0000
LOW CAL 0.0000



CHANNEL ID: S-7

TRACK #13

TEST ID: TARGET HARDNESS #7

TEST DATE: 1/24/86

Figure 39 Strain Gauge Data for 88 ft/s Impact Velocity into Concrete Highway Target

3.2.3.1 44 ft/s Impact into Desert Soil

The test unit penetrated 19 inches into the soil after impacting the target at 44 ft/s (Figure 40). Maximum acceleration levels reached 100 g's (Figure 41). No permanent deformations on the test unit resulted from the maximum recorded strain level of 180 μ in./ in. which correlates to zero residual strain (Figure 42).

3.2.3.2 66 ft/s Impact into Desert Soil

An impact velocity of 66 ft/s resulted in a 25 inch penetration into the soil (Figure 43). Figure 44 shows the two acceleration spikes approximately 15 milliseconds apart. The strain gage readings also show two spikes 15 milliseconds apart (Figure 45). The first spike represents the time of impact while the second spike signifies the unit coming to rest. Note that between the two spikes the signal basically approaches zero for both strain and accelerometer gages. The second spike represents the cask stopping due to soil lock-up then rebounding. Film studies show that after initial impact, the test unit velocity is relatively constant until the cask stops. Maximum accelerations reached 120 g's while maximum strains on the test unit were approximately 500 μ in./in. with no permanent deformations.

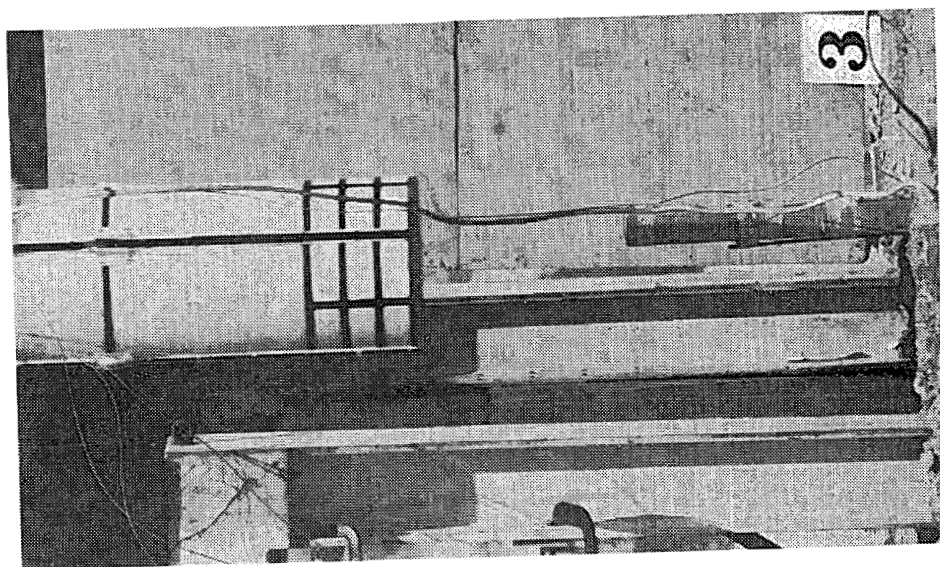
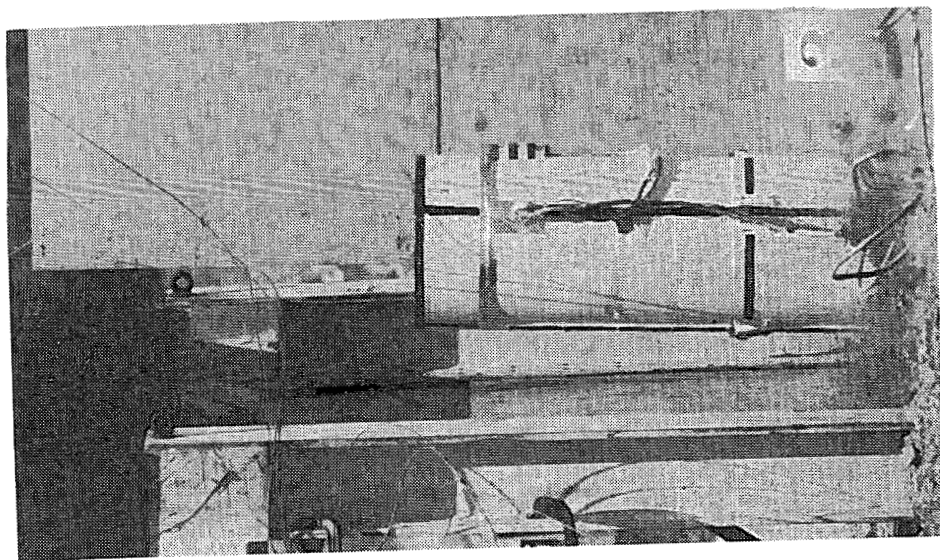
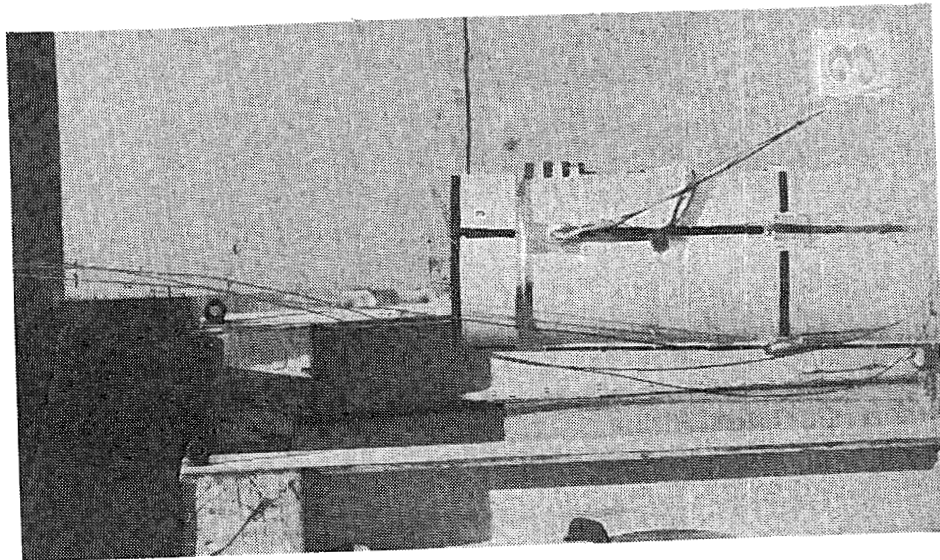


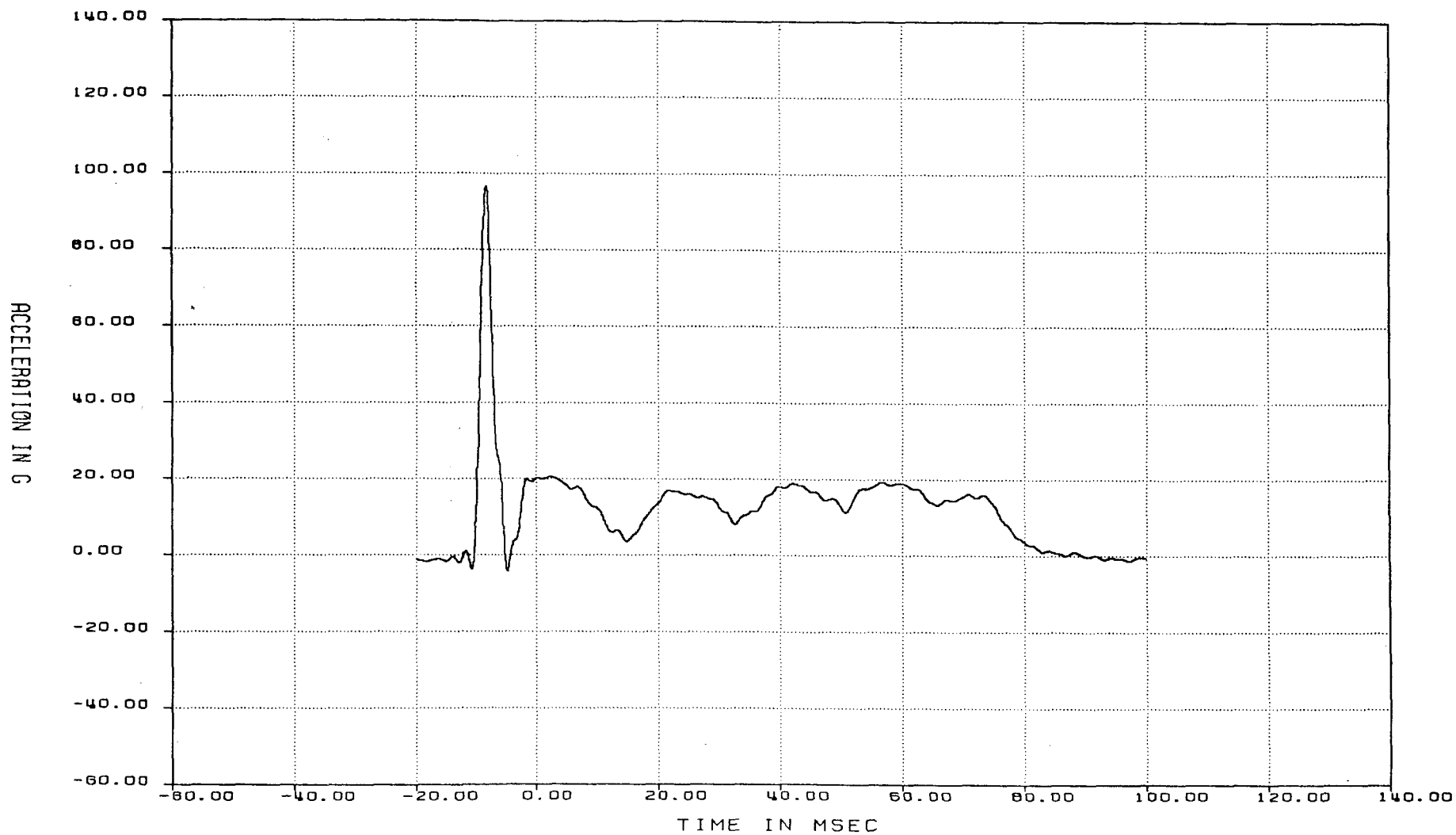
Figure 40 Impacting at a Velocity of 44 ft/s into the Soil Producing a
19-inch Cask Penetration

DATA FILE: R5539A
CHARGE # 8950.433
FILTER 10 KHZ
IIR FILTER

SAMPLE RATE 100000.0
START -20.000 MSEC
STOP 100.000 MSEC
CUTOFF= 500.0 HZ

DIGITIZED: 7 AUG., 1985
ZERO TIME 19:15:51.897000
STATIC RUN LEVEL 0.000
LOWPASS

SYS ID: A3 CEN,AD1
HIGH CAL 500.0000
LOW CAL 0.0000



CHANNEL ID: A-1

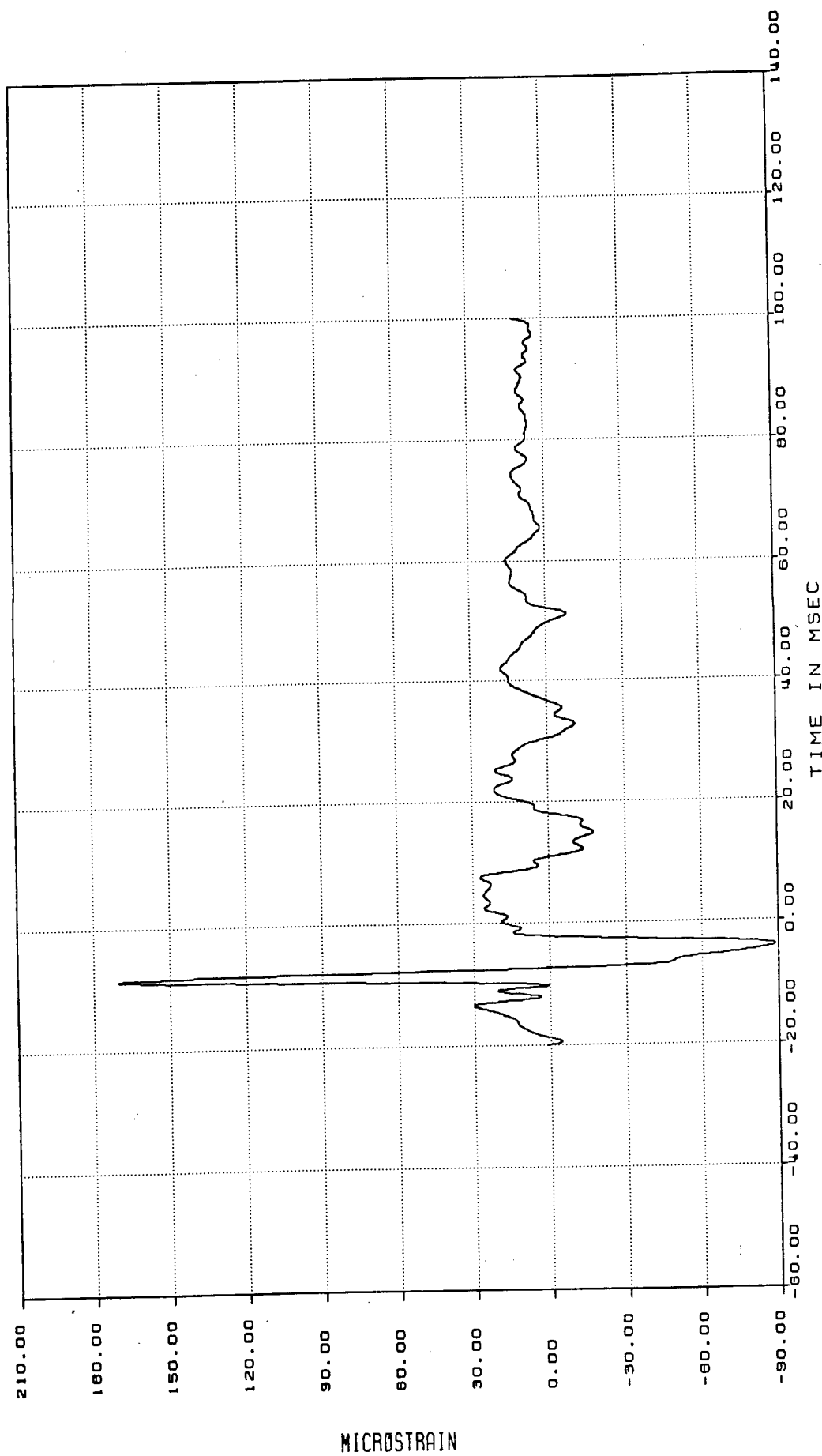
TRACK # 1

TEST ID: TARGET HARDNESS EVENT #3

TEST DATE: 8/ 6/85

Figure 41 Acceleration Data for 44 ft/s Impact Velocity into Soil Target

DATA FILE: R5539A SAMPLE RATE 100000.0 DIGITIZED: 7 AUG., 1985 SYS ID: A3 CEN,AD5
 CHARGE # 8950.433 START -20.000 MSEC ZERO TIME 19:15:51.897000 HIGH CAL 1000.0000
 FILTER 10 KHZ STOP 100.000 MSEC STATIC RUN LEVEL 0.000 LOW CAL 0.0000
 IIR FILTER CUTOFF= 500.0 HZ LOWPASS



CHANNEL ID: S-1 TRACK # 5

TEST ID: TARGET HARDNESS EVENT #3 TEST DATE: 8/ 6/85
 Figure 42 Strain Gage Data for 44 ft/s Impact Velocity into Soil Target

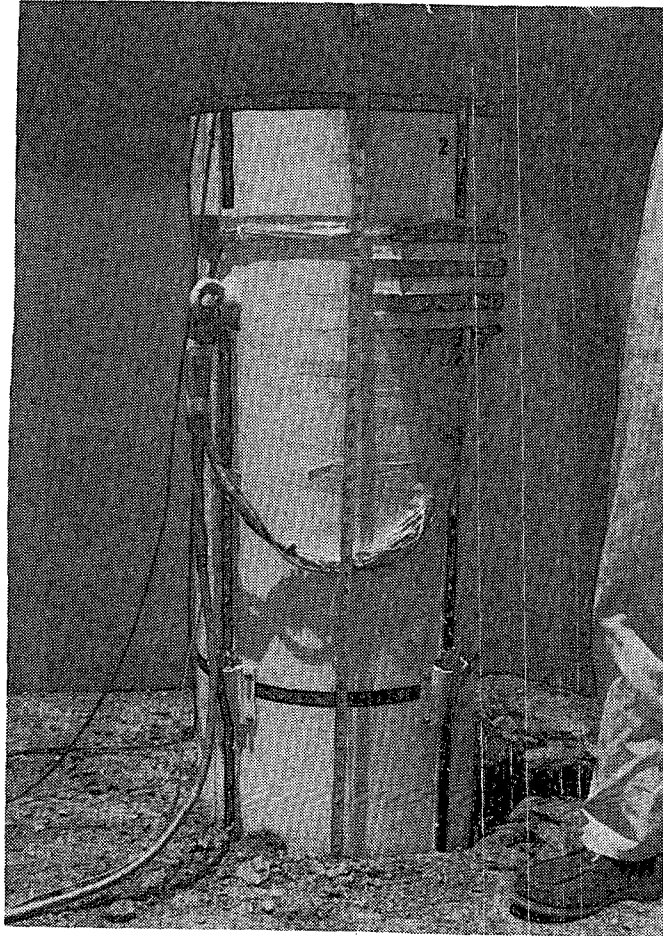


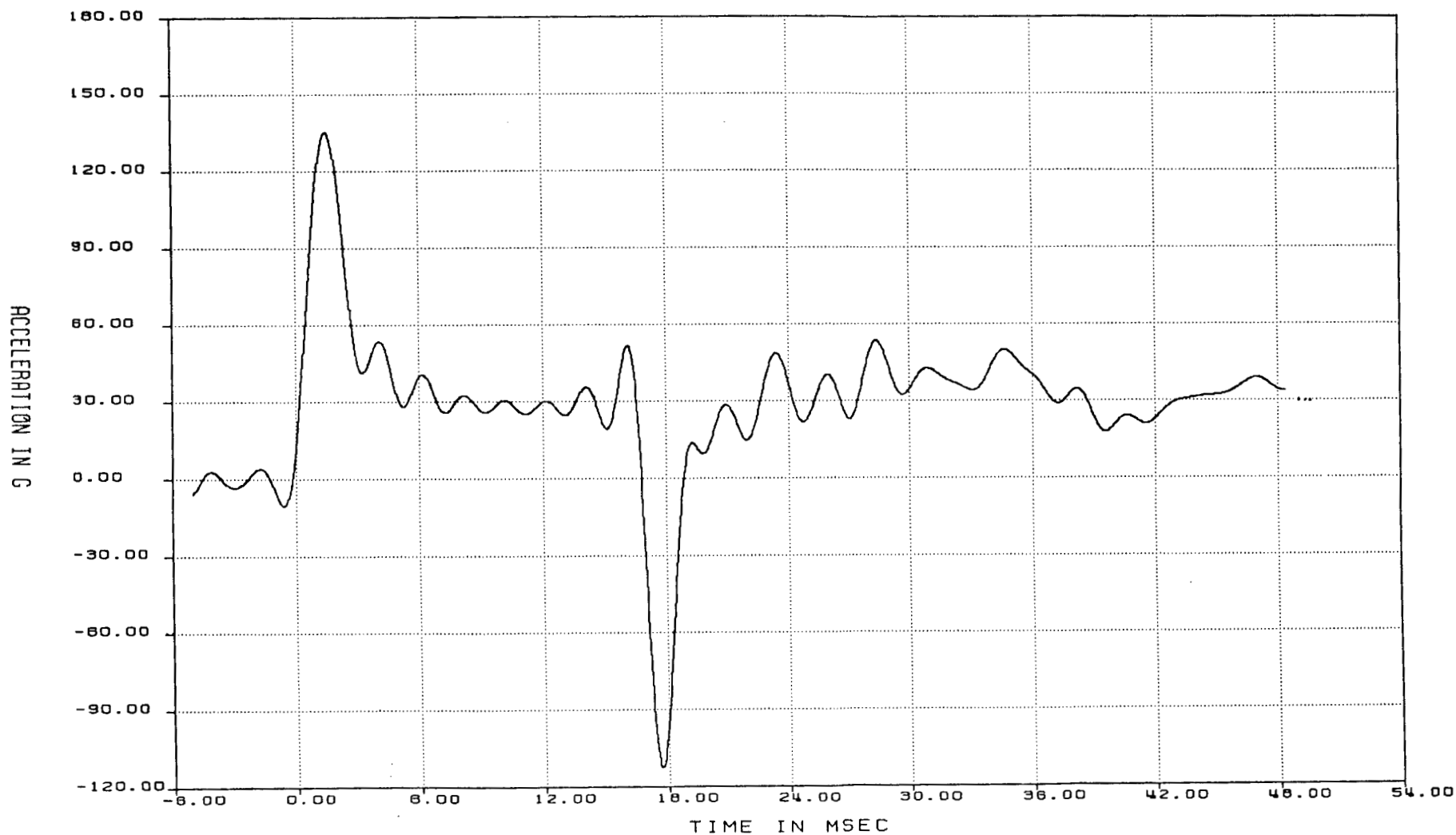
Figure 43 Test Unit's 25-inch Penetration into the Soil
After Impacting at a Velocity of 66 ft/s

DATA FILE: R5533B
CHARGE # 8950433
FILTER 10 KHZ
IIR FILTER

SAMPLE RATE 100000.0
START -5.000 MSEC
STOP 50.000 MSEC
CUTOFF= 500.0 HZ

DIGITIZED: 26 JULY, 1985
ZERO TIME 18:58:43.141000
STATIC RUN LEVEL 0.000
LOWPASS

SYS ID: A3 CEN,AD1
HIGH CAL 500.0000
LOW CAL 0.0000



CHANNEL ID: A-1

TRACK # 1

TEST ID: TARGET HARDNESS # 2

TEST DATE: 7/26/85

Figure 44 Acceleration Data for 66 ft/s Impact Velocity into Soil Target

DATA FILE: R5533B

CHARGE # 8950433

FILTER 10 KHZ

IIR FILTER

SAMPLE RATE 100000.0

START -5.000 MSEC

STOP 25.000 MSEC

CUTOFF= 1000.0 HZ

DIGITIZED: 26 JULY, 1985

ZERO TIME 18:58:43.141000

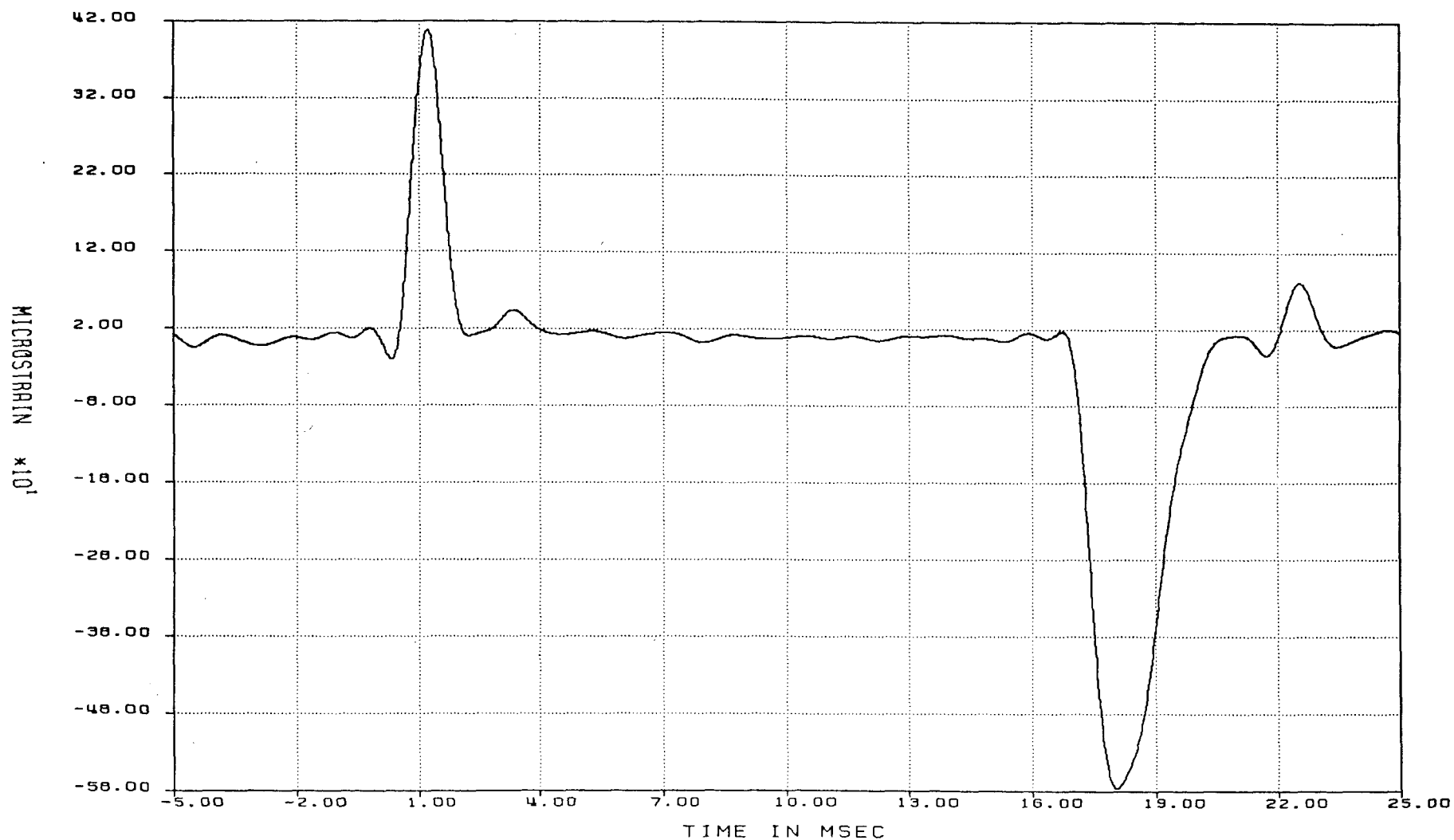
STATIC RUN LEVEL 0.000

LOWPASS

SYS ID: A3 CEN,AD5

HIGH CAL 1000.0000

LOW CAL 0.0000



CHANNEL ID: S-1

TRACK # 5

TEST ID: TARGET HARDNESS # 2

TEST DATE: 7/26/85

Figure 45 Strain Gage Data for 66 ft/s Impact Velocity into Soil Target

3.2.3.3 88 ft/s Impact into Desert Soil

At 88 ft/s impact velocity, the cask came to rest 36 inches into the soil (Figure 46). The impact produced a maximum acceleration of 250 g's (Figure 47). The strain gage on the test unit recorded a double spike with a maximum strain of 900 μ in./in. in compression (Figure 48). No permanent deformations resulted from the impact.

3.2.3.4 110 ft/s Impact into Uncompacted Soil

This particular test was performed to determine the penetration depth sensitivity to soil compaction. Impacting at 110 ft/s into uncompacted soil resulted with a final penetration of 92 inches and completely burying the 72-inch long test unit. This was much farther than the 46-inch penetration calculated analytically prior to the test. As the test unit entered the soil, past the instrumentation cables, the signal to the data collection system was completely severed. Thus, no data was recorded. However, the test unit was inspected for posttest damage and no permanent deformation was found.

3.3 Comparison of Test Results

A comparison of the eleven drop tests is made evaluating the cask responses, deformations, and penetrations. A summary of the test results described in the previous sections are given in Table 3. Of the various

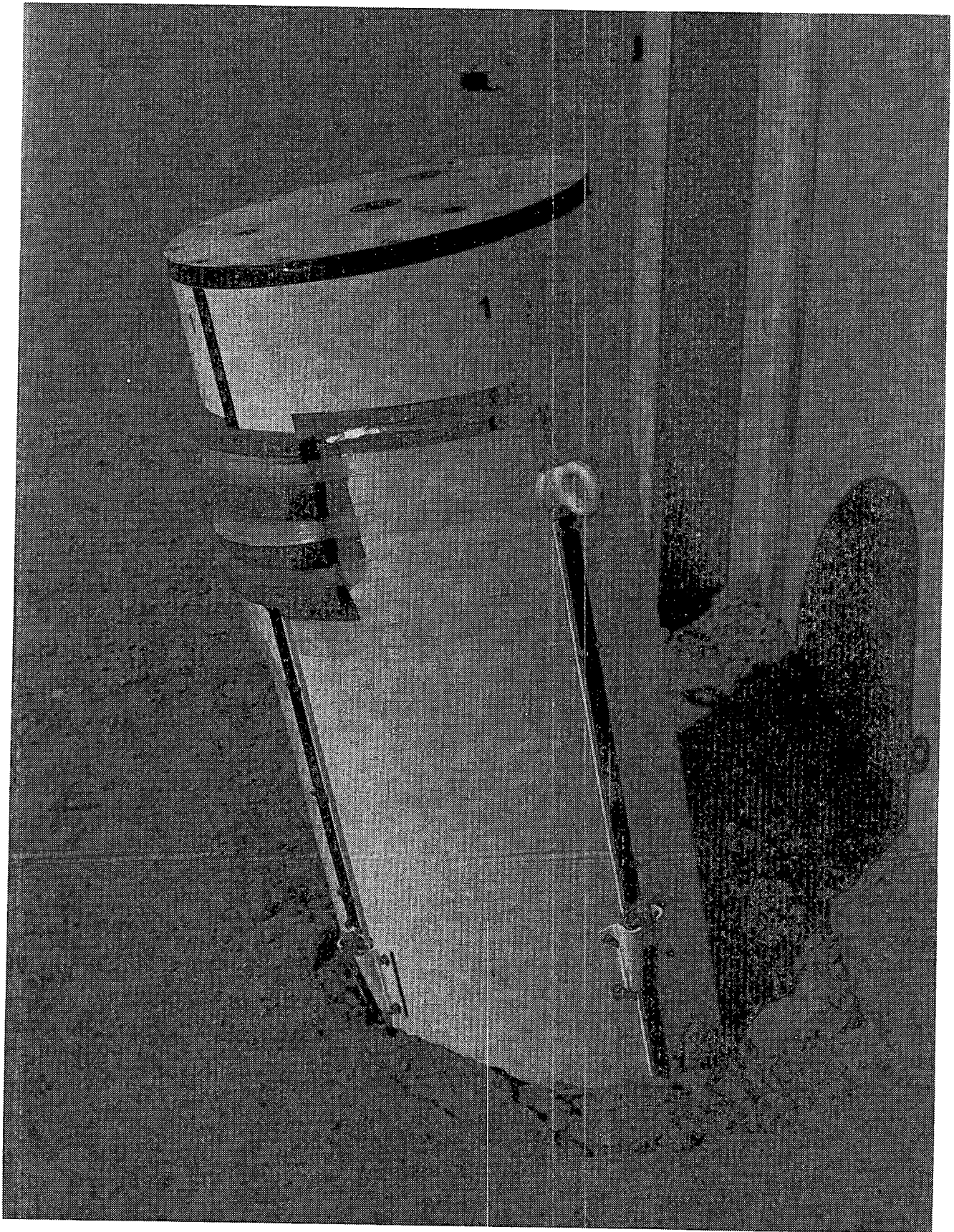


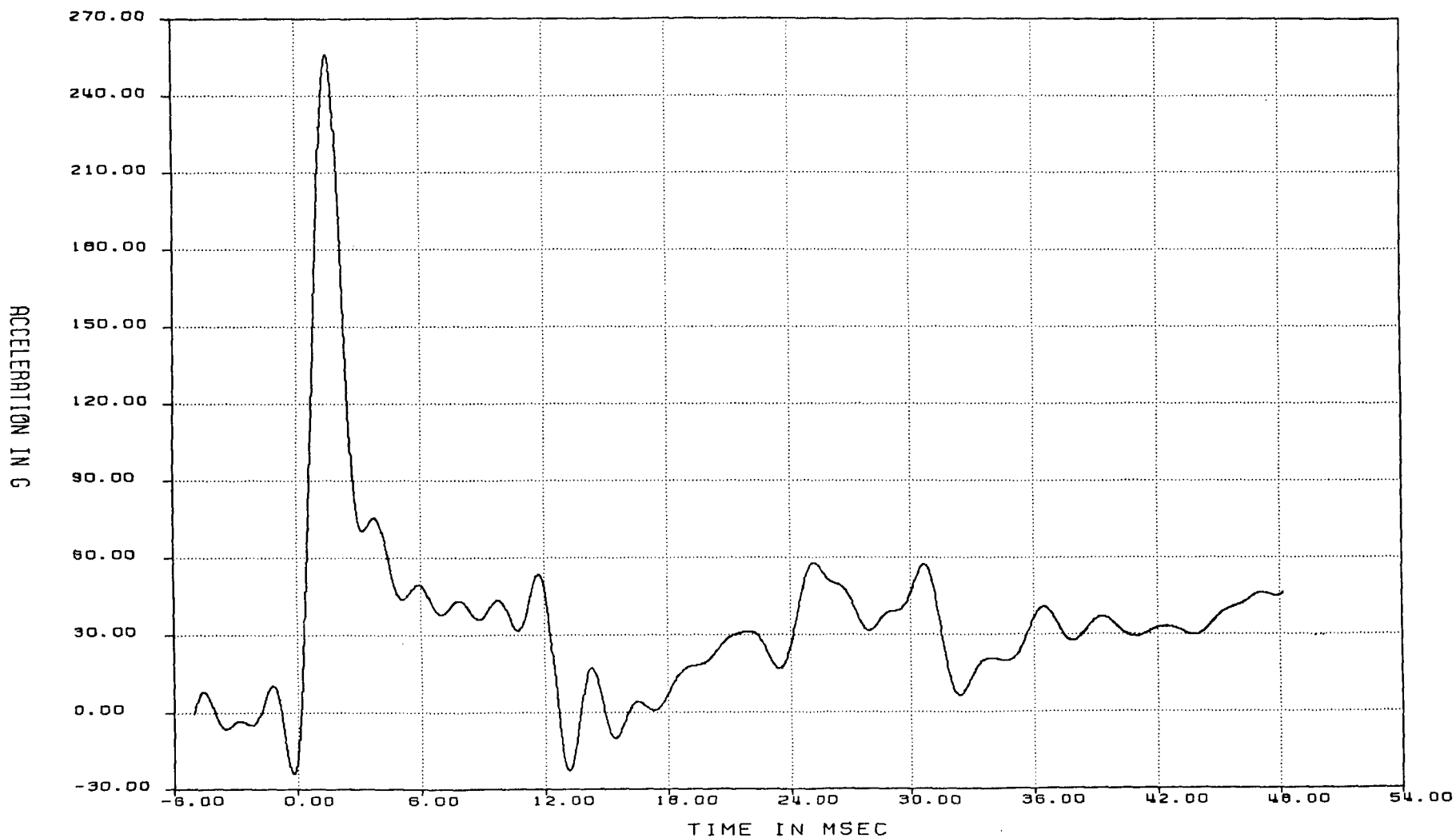
Figure 46 Test Unit's 36-inch Penetration into the Soil
After Impacting at a Velocity of 88 ft/s

DATA FILE: R5532A
CHARGE # 8950433
FILTER 10 KHZ
IIR FILTER

SAMPLE RATE 100000.0
START -5.000 MSEC
STOP 50.000 MSEC
CUTOFF= 500.0 HZ

DIGITIZED: 18 JULY, 1985
ZERO TIME 21: 8:39.928000
STATIC RUN LEVEL 0.000
LOWPASS

SYS ID: A3 CEN,AD1
HIGH CAL 200.0000
LOW CAL 0.0000



CHANNEL ID: A-1

TRACK # 1

TEST ID: TARGET HARDNESS EVENT #1

TEST DATE: 7/17/85

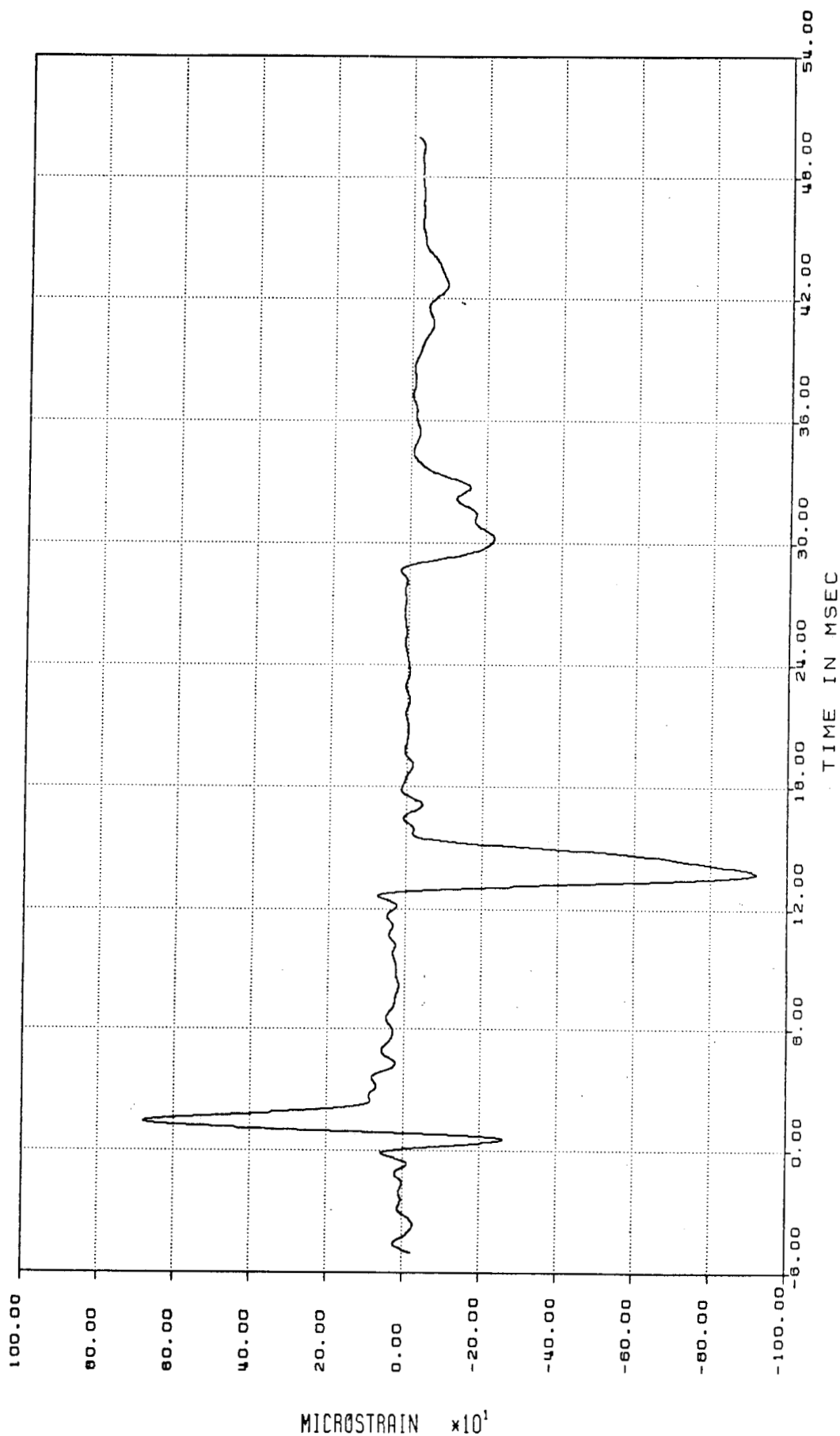
Figure 47 Acceleration Data for 88 ft/s Impact Velocity into Soil Target

DATA FILE: R5532A
CHARGE # 8950433
FILTER 10 KHZ
IIR FILTER

SAMPLE RATE 100000.0
START -5.000 MSEC
STOP 50.000 MSEC
CUTOFF= 1000.0 HZ

DIGITIZED: 18 JULY, 1985
ZERO TIME 21: 8:39.928000
STATIC RUN LEVEL 0.000
LOWPASS

SYS ID: A3 CEN.AD4
HIGH CAL 1000.0000
LOW CAL 0.0000



CHANNEL ID: S-7

TRACK #11

TEST ID: TARGET HARDNESS EVENT #1

TEST DATE: 7/17/85
Figure 48 Strain Gage Data for 88 ft/s Impact Velocity into Soil Target

TARGET HARDNESS TEST RESULTS

TEST		MAXIMUM RECORDED ACCELERATION (g's)	MAXIMUM RECORDED STRAIN (u in/in)		RECORDED PERMANENT STRAIN (u in/in)		PENETRATION (in)	MAXIMUM INCREASE IN RADIAL LENGTH (in)
			axial (comp)	radial (tension)	axial (comp)	radial (tension)		
UNYIELDING TARGET	44 ft/s	1300	-750	3000	0	3000	0	0.09
	44 ft/s	480	-900	600	0	400	0.25	0.01
	66 ft/s	900	-1000	2300	0	500	4	0.03
CONCRETE RUNWAY	88 ft/s	1000	-5500	3000	-4800	600	8	0.08
	44 ft/s	350	0	900	0	0	4	0
	* 44 ft/s	-	-	-	-	-	4	-
CONCRETE HIGHWAY	88 ft/s	7500	-1800	2400	-1300	500	19	0.02
	44 ft/s	100	-90	170	0	0	19	0
	66 ft/s	130	-580	420	0	0	25	0
COMPACTED SOIL	88 ft/s	250	-900	600	0	0	36	0
	+ 110 ft/s	-	-	-	-	-	92	0

* SCHEDULED FOR 66 ft/s HOWEVER ROCKETS DID NOT FIRE AND INSTRUMENTATION WAS NOT OPERATING

+ INSTRUMENTATION WAS LOST FROM EXCESS PENETRATION INTO SOIL

Table 3

columns of information presented, only the acceleration magnitudes deviate from the values expected.

3.3.1 Accelerations

The recorded accelerations are directly related to the frequency generated on impact. Since the test unit has no impact limiters, high frequencies are generated upon impact lasting only a short duration. The test unit can be thought of as a cylindrical bar that is struck on one end. In the case of impacting the unyielding target, most of the energy is absorbed by the projectile with very little taken by the target itself. The frequency response is large, however the test unit is fully supported by the unyielding target until rebound. At this point the acceleration from rebound is slight compared to impact and any resonance of the test unit that may effect the accelerometers is easily determined and can be filtered out.

Impacting into the soil targets produced acceleration histories that were proportional to those obtained in the unyielding target drop. The typical acceleration response consisted of a spike at the point of impact, another spike in the negative direction when the test unit comes to rest and relatively small response in between. The mechanics behind the soil impacts lies in its ability to resist movement of the traveling projectile. At the point the unit impacts the soil, energy is absorbed in producing a shear plane underneath the impact area of the test unit. Once this is accomplished the unit travels into the target, compressing the soil. As the soil compresses, the resistance to load increases until lock-up occurs for a particular velocity and stops the unit. The unit rebounds to produce the second

acceleration and strain gage spike (Figures 44 and 45). The soil acts somewhat as an impact limiter while continually supporting the test unit as it penetrates. This continual support becomes important when comparing with the response for impacting the concrete targets.

The mechanics involved in striking the concrete targets is similar to that of the soil except for two important factors. The phenomenon of two separate responses at impact and at rest, with a minimal readings in between, is still evident. However, the magnitude of the acceleration from initial impact is very large compared to any other response. This is the point where the concrete shear plug is formed which absorbs a substantial amount of available energy. Along with the formation of the concrete shear plug, the soil underneath undergoes establishment of shear planes. This allows the test unit to travel into the target at a relatively small deceleration until the soil locks up to provide enough stiffness to stop the unit.

The response of the test unit at impact is such that the frequency is quite high. The unit absorbs this frequency and excites the accelerometers. After the concrete and soil form their respective shear planes the relative support upon the cask drops dramatically. Even though the unit is compressing the soil, the differential response between initial impact and subsequent travel is very large. The resulting environment is that of the cask suspended in air and being struck by a stiff brittle object at one end. Without any firm support to provide damping, the unit resonates at the produced frequency. Thus, the accelerometers are measuring both the frequency associated with deceleration forces, and frequencies related to the test unit resonating.

This phenomenon was recorded by two accelerometers manufactured by independent sources. The test unit was instrumented with 10,000 g EGAXT-24

Entran [8] and 50,000 g 2264 Endevco [9] units. The Entran units are damped accelerometers that resist impulses due to test hardware resonating. The Endevco are undamped, however, due to their large 50,000 g range are less susceptible to resonating excited by low frequencies. Both of these accelerometers produced data within 5% of each other during the course of testing on this program. The reaction of the accelerometers recording the resonating effect of the test unit suggest this phenomenon was a major portion of the response the unit experienced. Thus, even with the built in factor of the damped Entrans and high range Endevcos used to avoid effects from cask resonating, the accelerometers could not compensate for the applied frequencies. The recorded response on the two types of accelerometers was real, however, the phenomena is directly dependent on the target impacted.

For this particular program, accelerometer data was a tool to be evaluated rather than to provide absolute empirical results. Confidence was generated in the acceleration values obtained in the soil and unyielding target tests. However, with the concrete targets, the accelerometer data is subject to interpretation. Consequently, for impacts into yielding targets, the validity of the acceleration data is dependent on the characteristics of the test unit and the penetration phenomena experienced by the target surface.

3.3.2 Strains and Deformations

Strains and deformations have a relationship in that any residual strains directly coincide with permanent deformations. Table 3 lists five tests in which residual strains were obtained from impacting the various targets. All three concrete runway impact tests along with the 88 ft/s impact into the

concrete highway produced permanent deformations. However, only the 88 ft/s impact into the runway exhibited strains and deformations on the order of that found from the drop onto the unyielding target. Reviewing the strain levels of the respective 88 ft/s into the runway and 44 ft/s into the unyielding target tests show a higher absolute magnitude from the concrete drop. Figure 29 presents the strain gage measurement at 2.75 inches from the cask bottom for the 88 ft/s impact into the runway. The large $-5500 \mu \text{ in./in.}$ strain in compression can be attributed to the stiffness from the geometrical configuration. In this case, the bottom cap welded to the outer cylinder precludes the wall from buckling or deforming outward. This directs all of the applied axial load to be absorbed in compression.

Comparing the two strain gages located twelve inches from the cask bottom, Figures 17 and 30 respectively present data from the unyielding and the 88 ft/s runway impacts. At this cask location, the outer cylinder is allowed to buckle outward producing tensile stresses. These two gages are similar in response for the first six milliseconds. At this time the concrete shear plug has formed decreasing the resistance to cask motion. This is evident by the drop in tensile stress shown in Figure 30. Once the concrete shear plug has formed, cask stresses decrease allowing the material to recover from the applied loading. However, the unyielding target continues the applied load until the impacting system rebounds. Under these conditions, the cask material must deform in order to absorb energy.

The additional deformation with increased impact velocity is approximately equal in proportion to the change in amount of available kinetic energy. For example, from 44 ft/s to 66 ft/s results in 2.25 times the additional amount of kinetic energy. This produces an increase in radial

deformation in the unit from 0.01 inch to 0.03 inch. The resulting factor of 3 is comparatively close to the factor of 2.25 increase in kinetic energy. From 66 ft/s to 88 ft/s the increase in kinetic energy is 1.78 times, versus an additional deformation factor of 2.67 times. Again, the proportional change in deformation with respect to additional kinetic energy is similar. Note that the magnitude of deformation is small and any slight variation in results can greatly alter the ratios. However, in the limited amount of data obtained to compare damaged test units, the correlation between the experimental findings and additional available energy is good.

3.3.3 Unit Penetration

With respect to unit penetration, the relationship between increased kinetic energy and penetration depth depends on the type of target. For soil, the increase in penetration was less than the relative addition in kinetic energy. From 44 ft/s to 66 ft/s the unit traveled an additional distance from 19 inches to 25 inches. This represents an increase of 1.32 times compared to the kinetic energy factor of 2.25. The 36 inch travel into the soil after impacting at 88 ft/s is 1.89 times greater than the penetration found from impacting at 44 ft/s. This is less than half of the kinetic energy factor of 4.0. The closest soil correlation came between the 88 ft/s and 66 ft/s impacts. The experimental penetration ratio is 1.44 compared to the increased energy factor of 1.78. In every case the additional available kinetic energy factor was greater than the proportional increase in penetration depth obtained from impacting the soil targets.

For the concrete roadway and runway the increase in penetration was larger than the kinetic energy factor. Close correlation occurred between the 88 ft/s and 44 ft/s impact into the concrete highway. The 19 inch and 4 inch penetration results in a ratio of 4.75 versus the kinetic energy factor of 4.0. Also, the penetration ratio of 8 inches from the 88 ft/s impact and 4 inches from the 44 ft/s impact into the concrete runway obtains a ratio of 2 compared to the 1.78 kinetic energy factor. However a penetration component of 32 between the 88 ft/s and 44 ft/s impact into the concrete runway far exceeds the 2.0 kinetic energy factor. The same occurs between the 66 ft/s and 44 ft/s impact into the runway resulting in the 16 penetration factor versus the 2.25 kinetic energy component. Hence, unlike the soil tests, in every impact into the concrete surfaces a larger target penetration occurred than suggested by the additional amount of available kinetic energy. This can be explained by the fact a specific amount of finite energy is needed to produce the shear plug formed in the concrete targets. Once this shear plug is formed, the remaining kinetic energy is applied to compressing the soil underneath. The soil targets are less involved with formations of shear planes and primarily resist cask motion when the material compresses. This material compression is dependent on a variety of factors characterized by its properties. These factors influence the penetration depth from dynamic loading. This may imply that the energy to produce soil lock-up is less dependent on impact velocity than the energy needed to produce a shear plug in a brittle material such as concrete.

4.0 ANALYSIS

An important part of the program was the analytical evaluation of the problem presented by impacting the cylindrical-shaped object into a variety of targets. As was done with the experimental phase of the program, analytical results and methods were focused toward comparison against the 30-ft drop onto an unyielding target.

Analytical methods varied with respect to both problem definition and analytical codes used. The 30-ft drop onto an unyielding target provided the most consistent results that closely matched the data obtained from experimental testing. In comparison, the analytical process for the concrete and soil targets was complex and time consuming. As the complexity of the problem increased, so did the difficulty of defining it into practical constraints and also establishing analytical codes that produced meaningful results.

The following sections review the analytical process and tools used. Each analysis is given in terms of the respective target impacted.

4.1 Unyielding Target

DYNA2D [13], an explicit two-dimensional finite element code, was used to analyze the 30-ft drop onto an unyielding target. The problem was defined using a preprocessor, PATRAN-G [14], to construct the geometry required for input into the DYNA2D program.

Because the cask geometry and loading is symmetric about its longitudinal centerline the problem was treated as axisymmetric. This allowed for a two-dimensional analysis. The resulting finite element model consisted of 642 nodes and 568 quadrilateral elements (Figure 49). The unit was modeled as a solid monolithic steel mass. The hole at the lower corner represents the gap formed by the inner sleeve, internal plates and bottom cap. Maximum stresses and deformations were expected to be generated at this point. Regular Grade A36 steel material properties were used for the cask's yield and ultimate strengths. Strain hardening effects were also included in the analysis. To simulate the unyielding target, a stonewall option offered by DYNA2D was enacted. This forces all available energy from the impact to be totally absorbed by the projectile. This option provides a conservative analysis since in real life no such surface exists that will transmit 100% of the available energy to the striking object. However, from past tests at SNL with the same unyielding target used for this work, comparable results between analytical calculations and experimental testing have been favorable.

DYNA2D results show that at approximately one millisecond into the impact event the available kinetic energy has been expended and rebound begins to occur (Figure 50). This correlates well with experimental duration of approximately 1 to 2 milliseconds shown in Figure 17. The velocity of the center of mass with respect to time is shown in Figure 51. Taking the slope of the line determines the analytical acceleration giving a value of 1600 g's. Keeping in mind the conservatism of the analysis, this compares well with the 1300 g's obtained from experimental testing. The radial deformation from the analysis at the point approximately 3.5 inches from the bottom of the unit

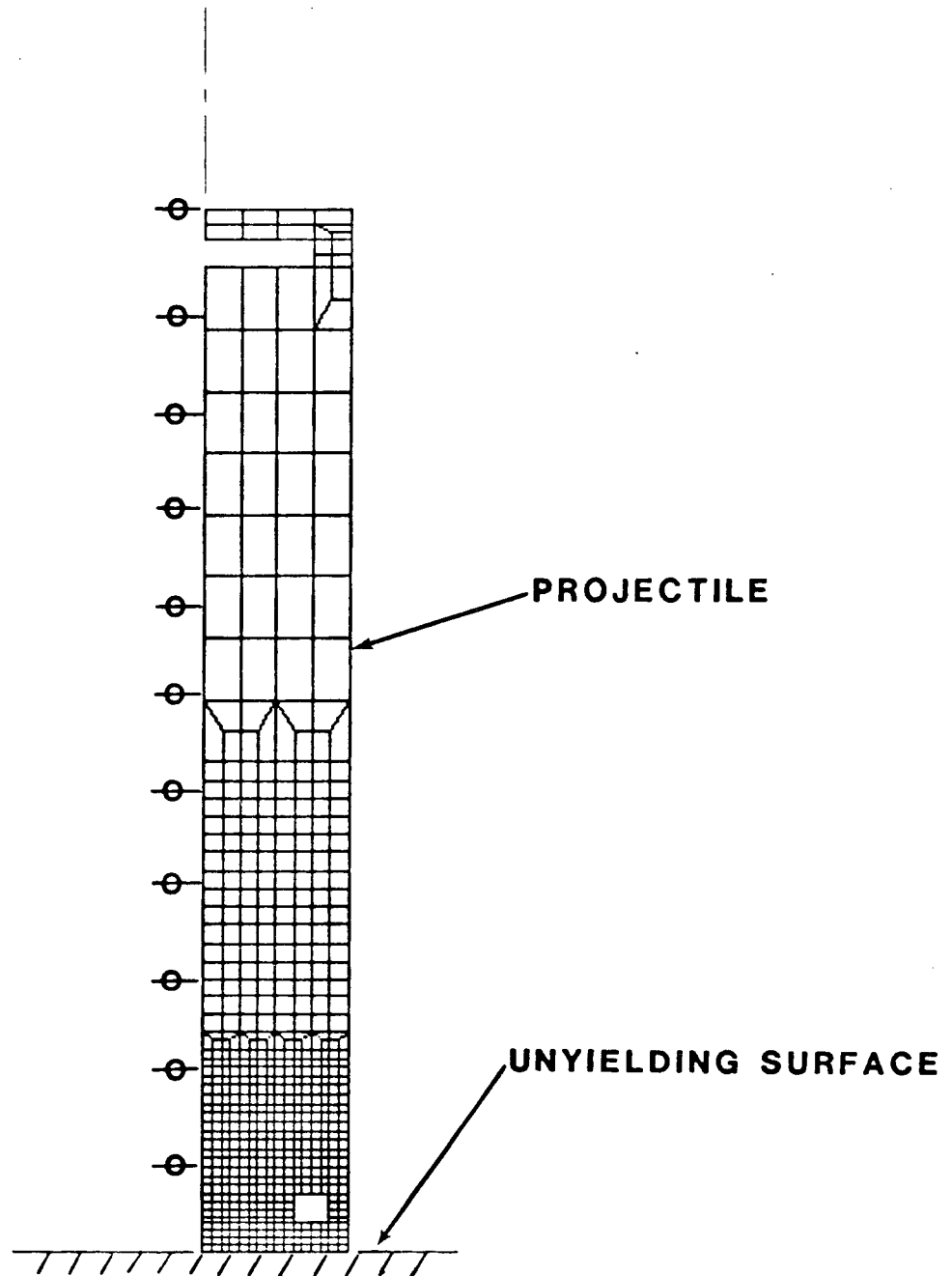


Figure 49 Finite Element Model for Unyielding Target Analysis

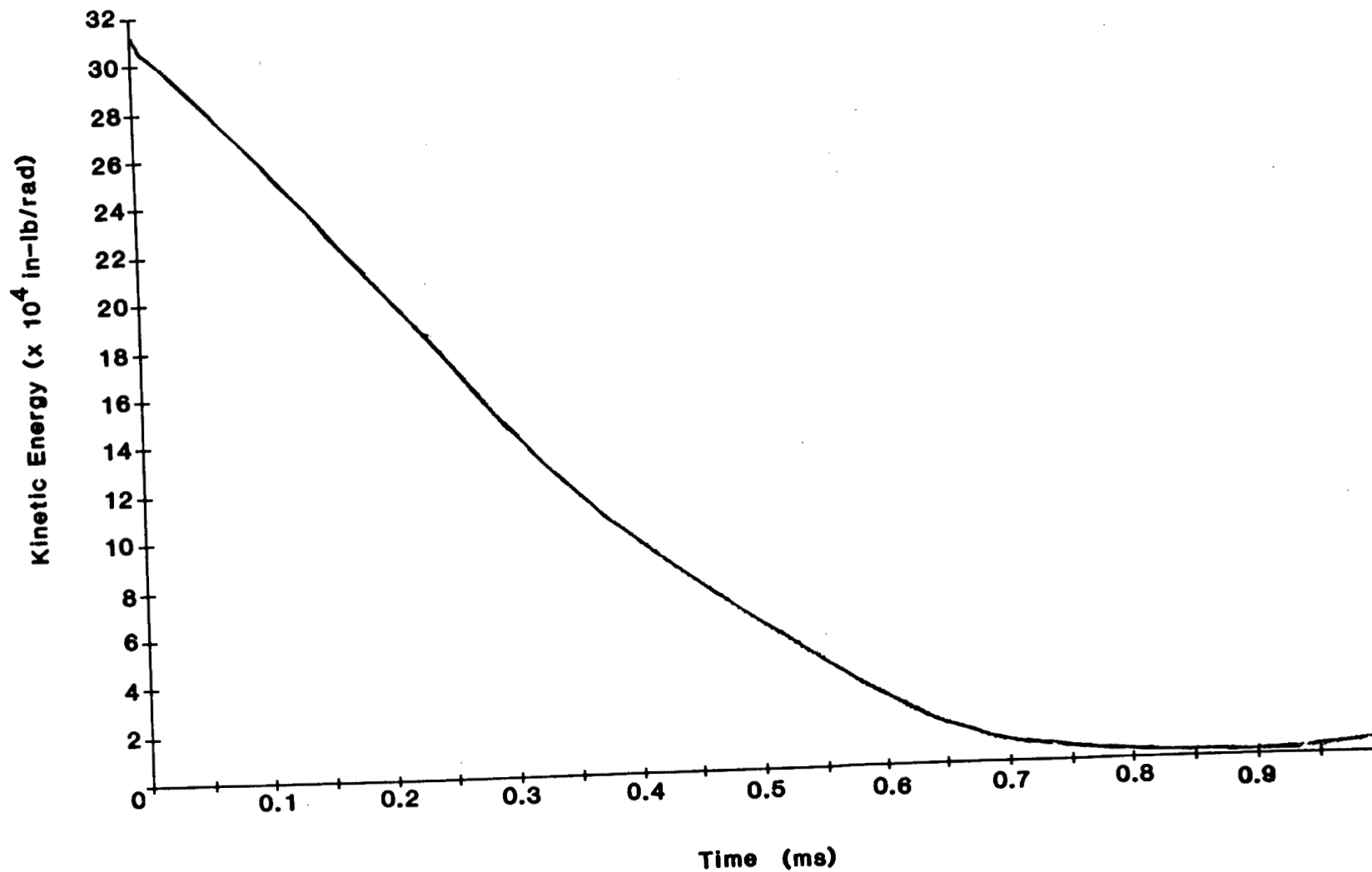


Figure 50 Kinetic Energy vs. Time from Unyielding Target Analysis

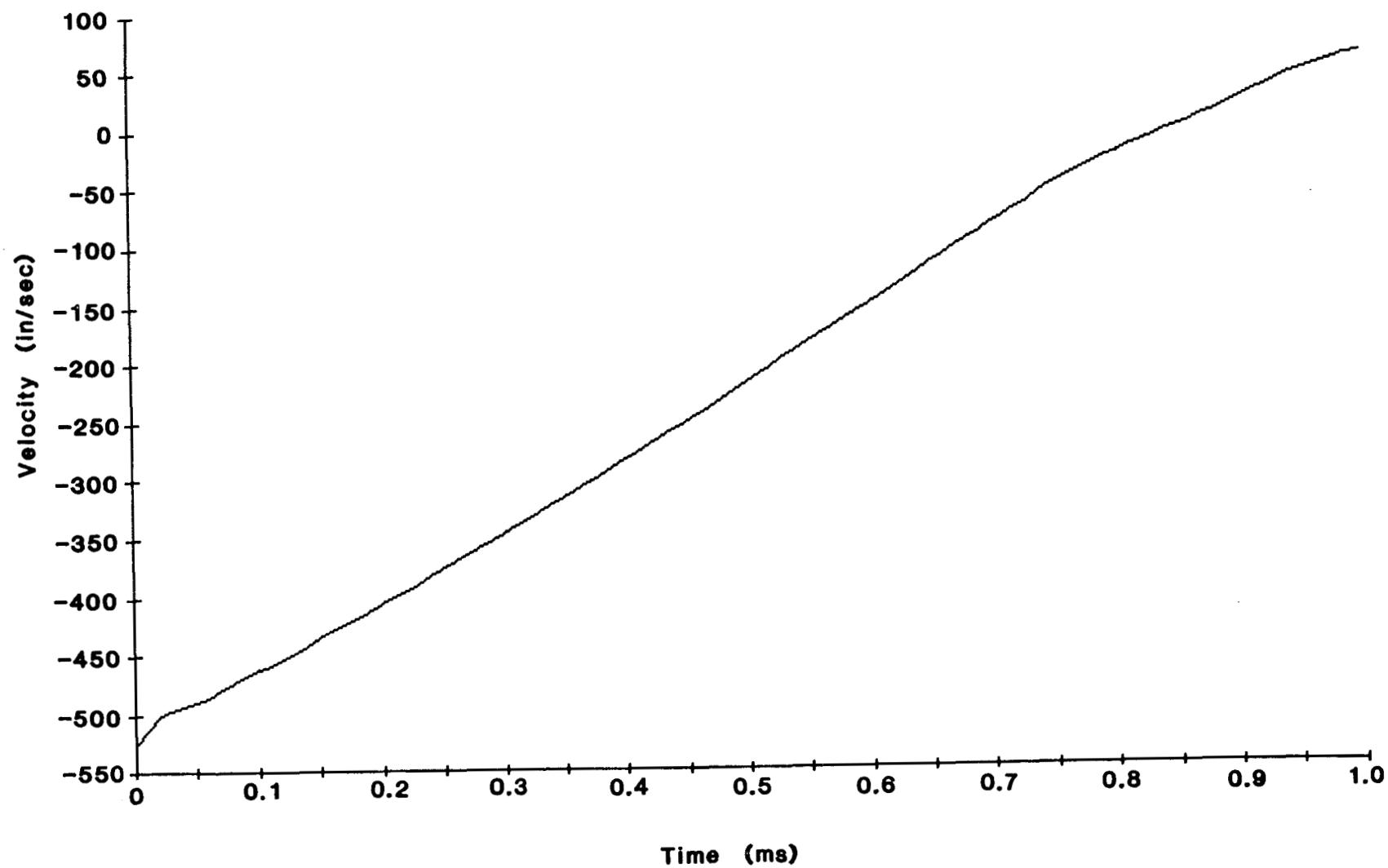


Figure 51 Velocity vs. Time from Unyielding Target Analysis

came to 0.12 inches (Figure 52). This also compares well with the experimentally measured amount of 0.09 inches.

At the point of strain measurement, 12 inches from the bottom, the calculated stress was approximately 38,000 psi (Figure 53). From the experimental strain reading of 3000 μ in./in., this correlates to approximately 37,000 psi stress at the same location.

The analytical results compare favorably with experimental findings. In every case, the conservatism of the analysis produced results that enveloped the data obtained from experimental testing. The analysis was relatively easy to perform and duplicate both in terms of analytical complexity and computer cost.

4.2 Concrete Target

The degree of analytical complexity increases substantially with analyzing the yielding targets. In this program, properly modeling the cask becomes secondary in difficulty to mathematically analyzing the target itself. Two immediate problems arise with respect to this type of analysis. First, determining the material characteristics of concrete and soil under impact loading must be made. Second, and more difficult, is properly accounting for the failure mechanisms associated with each type of material.

In the case of the concrete target, the 45° shear plug formed at impact was taken into account directly in the finite element model (Figure 54). The section below the concrete shear plug is the soil that must be compressed in order to increase resistance and stop the unit. Only the concrete highway targets were evaluated at this time.

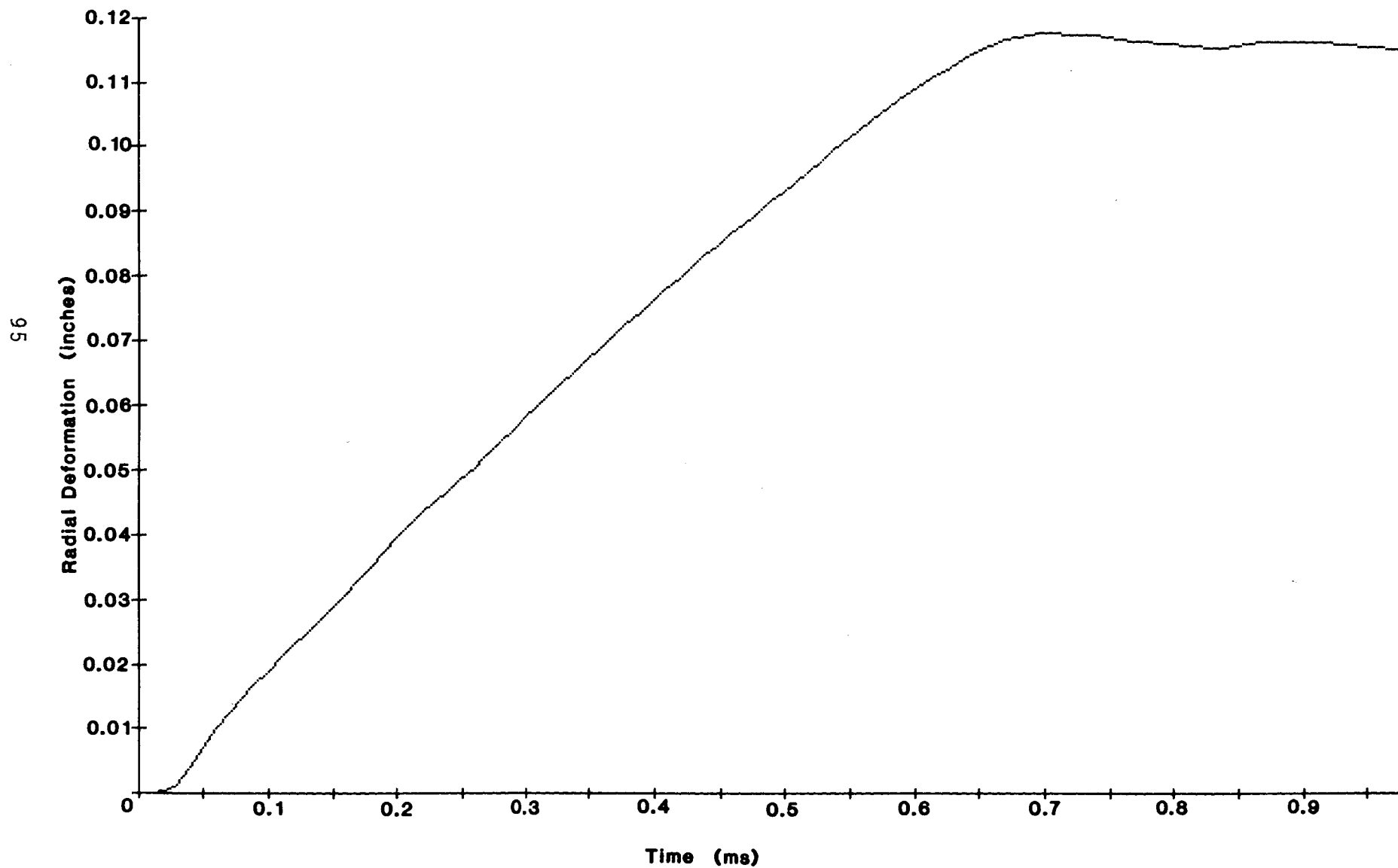
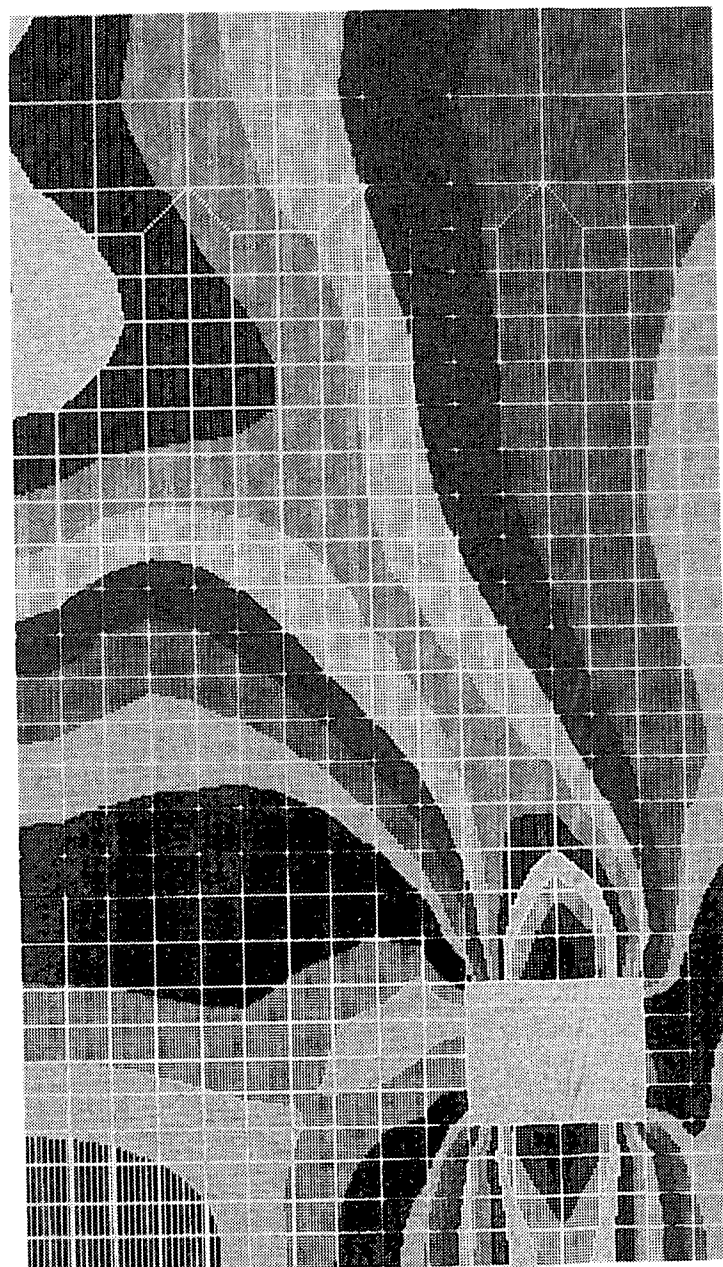
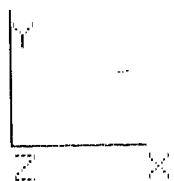


Figure 52 Radial Deformation from Unyielding Target Analysis

44 FT/S IMPACT
 UNYIELDING TARGET
 STRESS CONTOURS



TIME = 0.319104E-03

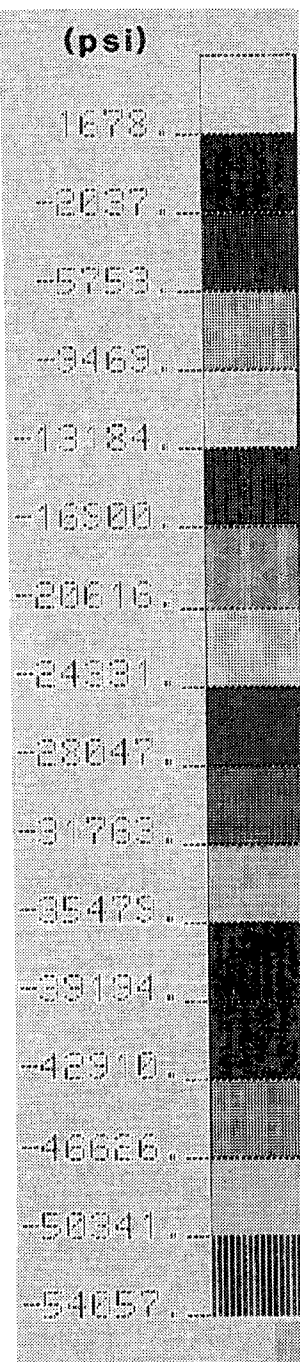


Figure 53 Stresses from Unyielding Target Analysis

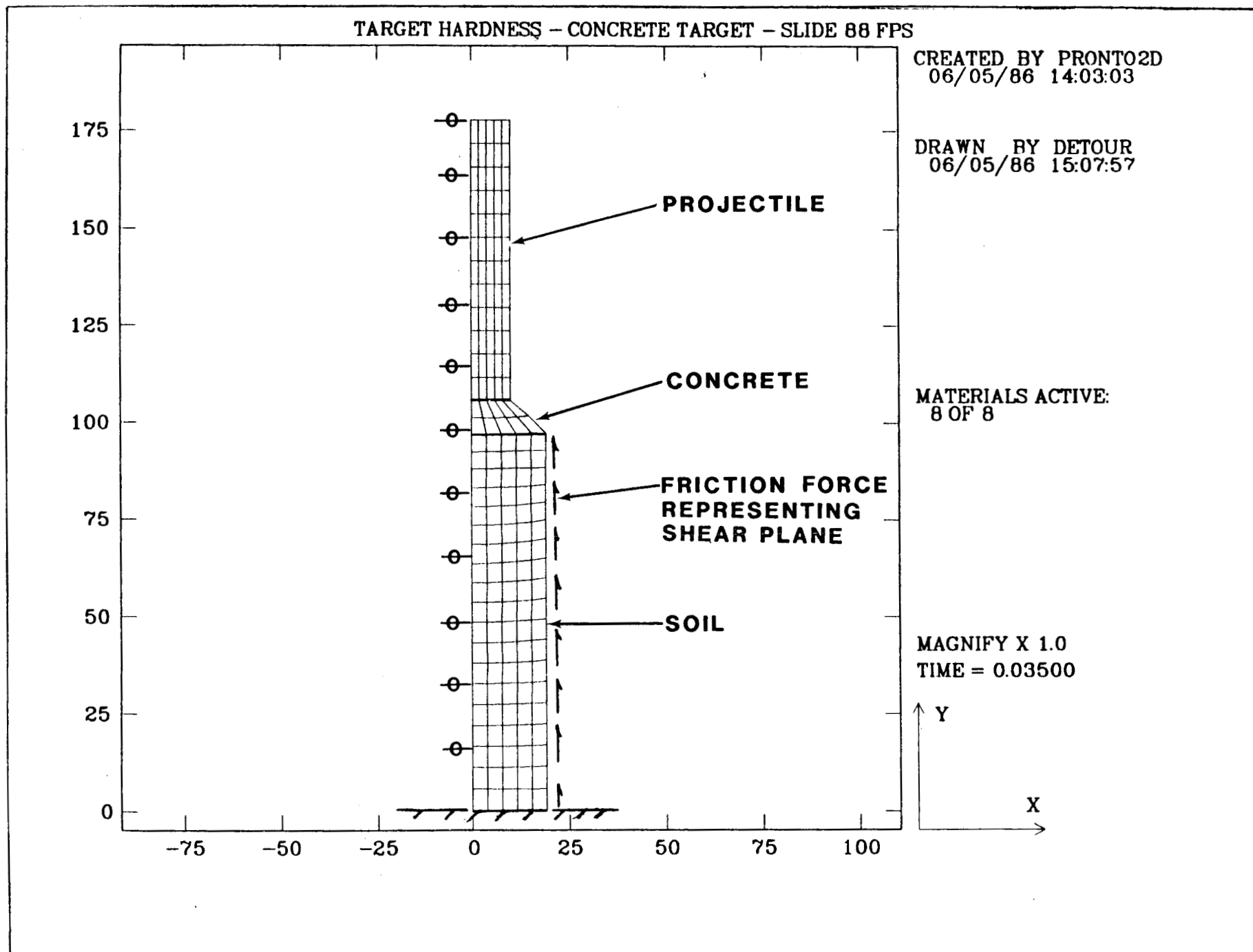


Figure 54 Finite Element Mesh for Concrete Highway Analysis

Because of the geometry of the test unit and the assumption made that the target failure was symmetrical, an axisymmetric two-dimensional analysis was performed using PRONTO [15]. Only the 44 ft/s and 88 ft/s impacts were evaluated. An analytical assumption was made that no significant energy is absorbed by crack generation. The boundary conditions of the target was total vertical constraint at the bottom and a resistance to movement of the outer edge produced by friction.

A plot of velocity vs. time for the 44 ft/s impact reveals an analytical acceleration of approximately 300 g's at the point of impact (Figure 55). This compares well with the 350 g's measured during the experimental test (Figure 33). The maximum calculated penetration of approximately 8.0 inches (Figure 56) is double that produced from impacting experimentally. The particular deviation between predicted and experimental penetration is probably a result of the analytical assumption that no significant energy is absorbed by crack generation.

Reviewing the analytical results of the 88 ft/s impact shows the initial slope of the velocity vs. time curve gives an acceleration of 600 g's (Figure 57). This is quite different than the 7500 g's measured experimentally, which is not surprising considering the lack of confidence in the experimental value. The penetration was calculated to be about 14 inches which is less than the 19 inches the unit actually experienced. (Figure 58). For such a complex failure phenomenon exhibited by the concrete target, these penetration values are comparable.

Reviewing the concrete analysis reveals a complex problem that requires special analytical considerations. Unlike the analysis of impacting an unyielding target where the only concern is modeling the projectile, the

TARGET HARDNESS - CONCRETE TARGET - SLIDE 44 FPS

CREATED BY PRNTO2D
06/05/86 13:54:15

DRAWN BY TPLOT
06/05/86 15:10:20

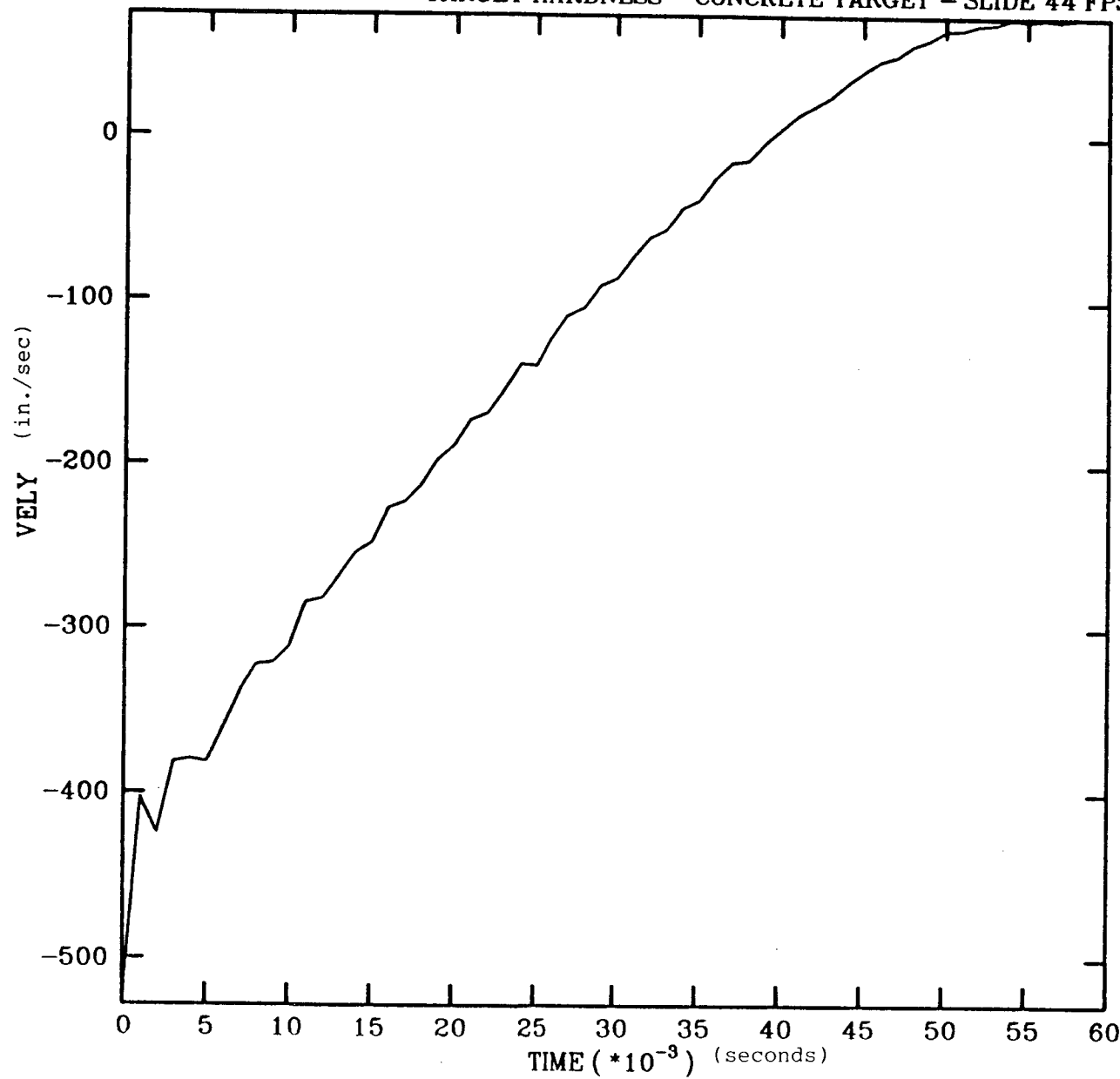


Figure 55 Velocity vs. Time from 44 ft/s Concrete Highway Analysis

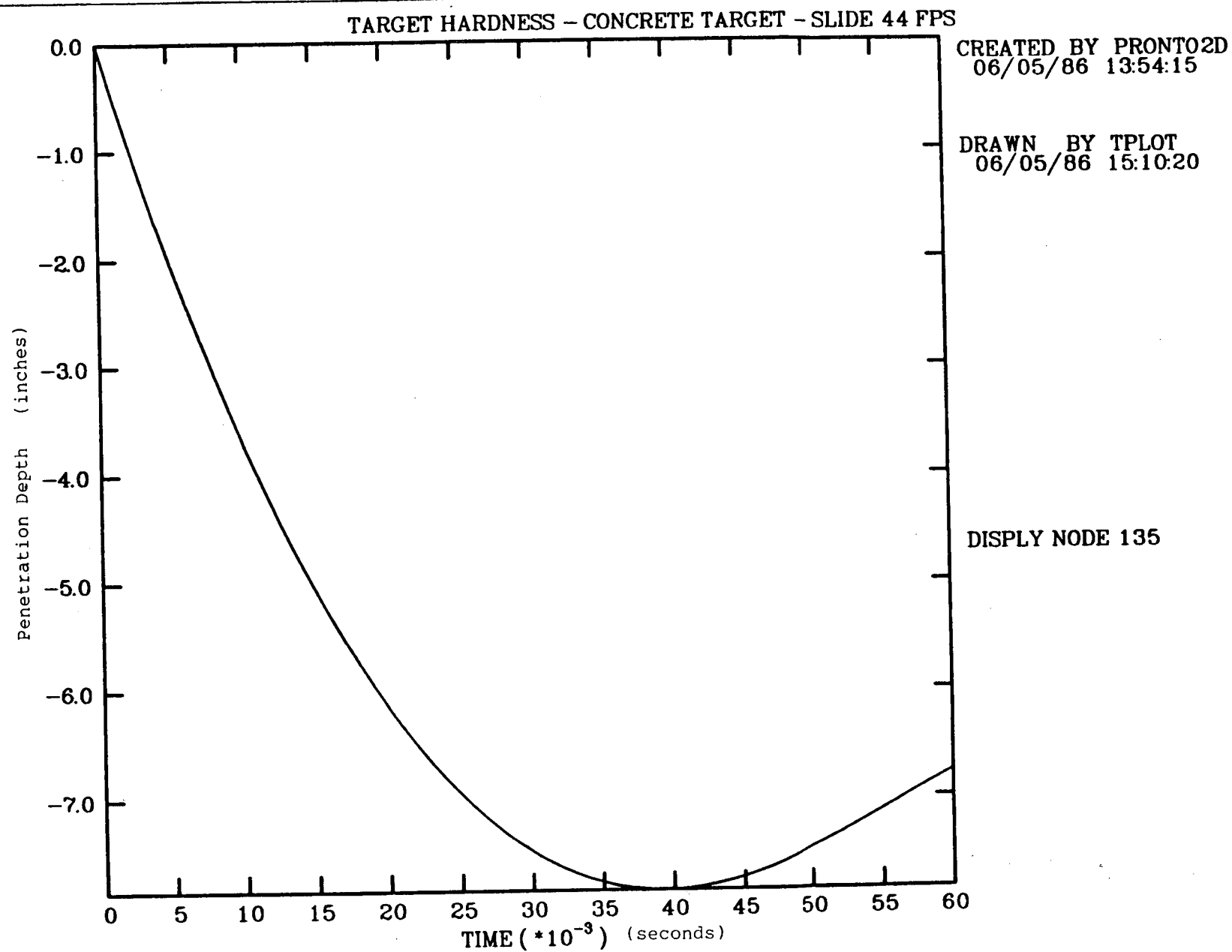


Figure 56 Penetration vs. Time from 44 ft/s Concrete Highway Analysis

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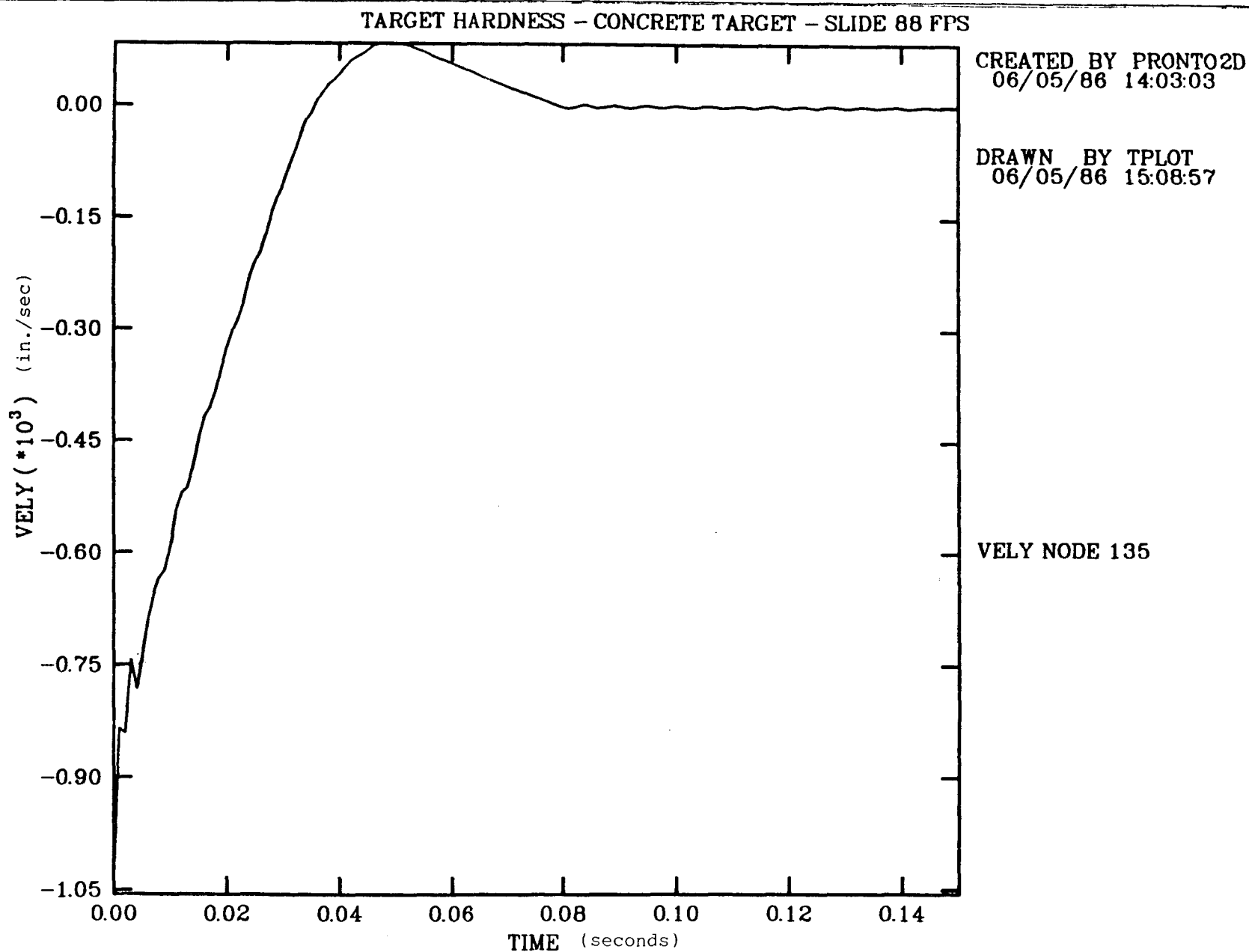


Figure 57 Velocity vs. Time from 88 ft/s Concrete Highway Analysis

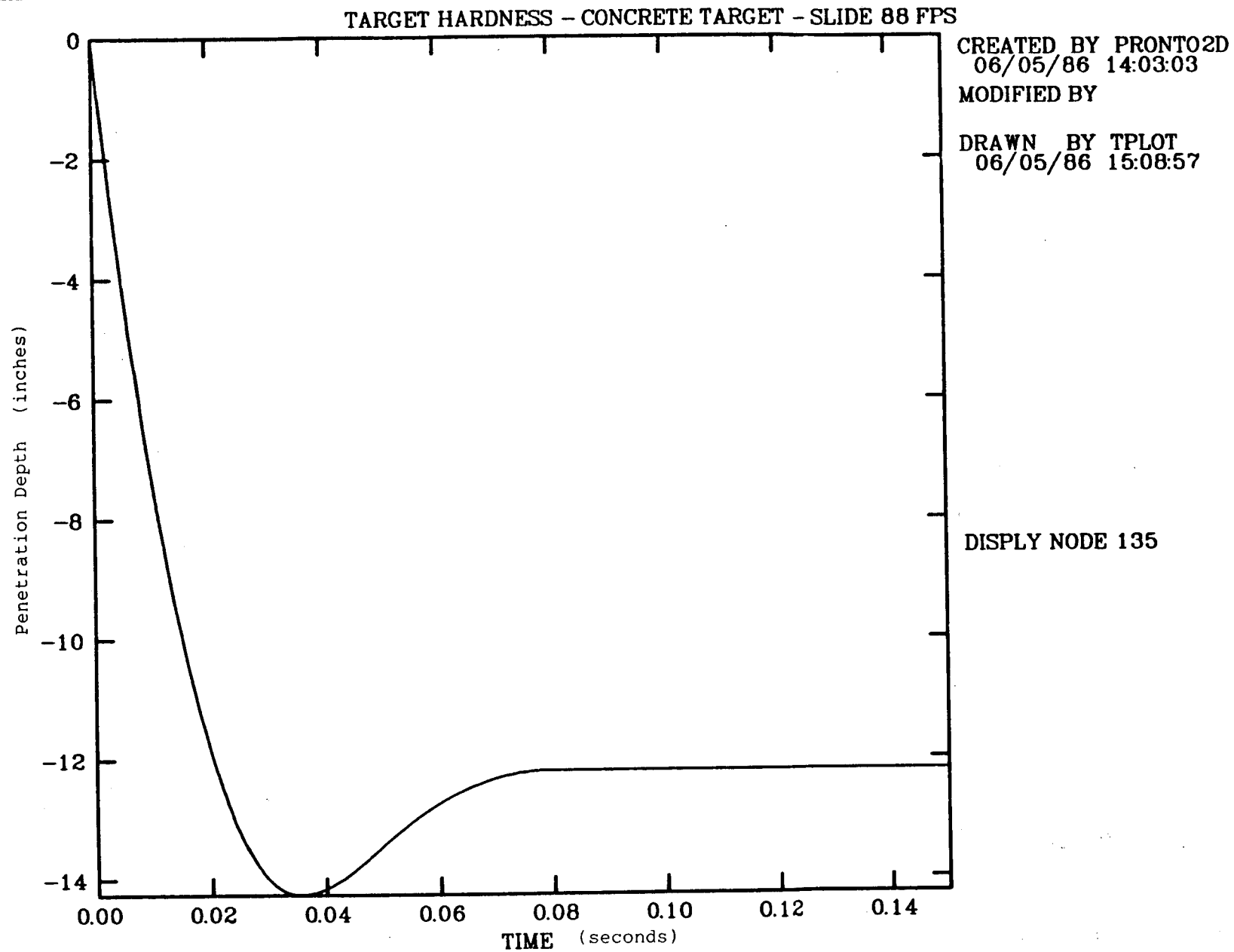


Figure 58 Penetration vs. Time from 88 ft/s Concrete Highway Analysis

concrete analysis had to also include accurately representing the target. This presents inherent problems that must be taken into account. The material properties of both the concrete and soil beneath the concrete had to be determined. In addition, the projectile/impact surface and the concrete/soil interaction had to be formulated. However, the most difficult aspect of modeling the concrete targets is properly accounting for the radial cracking that occurs during impact. In this particular analytical evaluation, radial cracking was ignored. The concrete analysis provided results that were within reasonable proximity to the experimental findings but there were some differences. The relative agreement between experimental and analytical results is particularly encouraging since only the concrete shear plug and soil directly underneath was modeled.

4.3 Soil Target

An initial series of analyses [16] was completed to determine the behavior of a cask dropped onto a soil target. This initial series indicated that penetration depths of 1.0 to 60.0 inches would be expected for drops with an impact velocity of 66 ft/s onto various soil targets. Results from these analyses indicated detailed mechanical properties for the soil would be needed to generate accurate predictions of penetration depths for tests at the cable drop site.

An additional series of analyses has been completed using results from the New Mexico Engineering Research Institute (NMERI) soil tests [6]. Results from the NMERI soil classification tests indicated the material present at the cable drop site at depths greater than 12 inches was a sand-clay mixture (SC).

The top 12 inches of material contained large amounts of gravel (3-inch maximum diameter) and could not be sampled with a Shelby tube. Engineering properties for the soil at depths greater than 12 inches were determined from a series of uniaxial and triaxial compression tests (Table 4).

For these tests, the soil samples were first loaded hydrostatically to a prescribed confining pressure. A confining pressure of 0 psi was used for the uniaxial tests. Next, additional stress was applied to the soil sample in only one direction. Plots of principal stress difference versus axial strain from the triaxial compression tests were used to determine a value for Young's modulus for this soil. For the triaxial compression tests, principal stress difference is equal in magnitude to the additional stress that is applied in only one direction. Young's modulus for this soil was approximately 3000 psi on initial loading. All of the uniaxial and triaxial tests were performed at very low strain rates; consequently, no information on strain rate effects was obtained. A linear pressure volume strain behavior was used in the finite element analyses.

4.3.1 Soil Finite Element Analysis

A finite element series of analyses was completed using the soil model in DYNA2D [13] and PRONTO-2D [15]. This soil constitutive model [17] combines volumetric plasticity with pressure dependent deviatoric plasticity. The following input parameters are required to use this model:

SOIL PROPERTIES⁺

DEPTH (in)	NATURAL DRY DENSITY (pcf)	UNCONFINED COMPRESSIVE STRENGTH (psi)	COHESION (psi)	INTERNAL FRICTION ANGLE (degree)
12 - 24	89.	12.5	3.0	34
24 - 36	100.	17.2	6.0	28
36 - 48	103.	14.0	4.5	28
48 - 60	103.	13.5	4.0	27

⁺ Since soil properties were not uniformly available for a depth of 0 - 12 inches, the properties between 12 - 24 inches were used in calculations

Table 4

- shear modulus, G
- bulk unloading modulus, B
- deviatoric yield function constants
- pressure-volumetric strain data.

The shear and bulk moduli were derived using the experimentally measured Young's modulus and an estimated Poisson's ratio of 0.25. The deviatoric yield function constants were derived from the experimentally measured cohesion and internal friction angle values. The pressure volumetric strain data was generated using the bulk modulus and the following equation

$$\gamma = -\ln(1 - P/B),$$

where

γ = volumetric strain

P = pressure

B = bulk modulus.

The bulk modulus is not expected to remain constant during each drop test but since the experimental pressure-volumetric strain behavior was not reported, there was no way to determine how it would vary as a function of pressure; therefore, a constant bulk modulus was used for each drop test.

Different values were used for the bulk modulus for some of the analyses to determine what effect this change would have on the results. Material properties used in this series of analyses are given in Table 5. Since

MATERIAL PROPERTIES USED IN FINITE ELEMENT ANALYSES

CASK: YOUNG'S MODULUS = 29.0E+6 psi
 POISSON'S RATIO = 0.30
 DENSITY = 8.74E-4 lbs/in.

SOIL: BULK MODULUS = 2000. psi
 SHEAR MODULUS = 1200. psi

COEFFICIENT OF FRICTION AND DEVIATORIC YIELD FUNCTION CONSTANTS

DEPTH (in)	FRICTION COEFF.	DYNA-2D			PRONTO-2D		
		a0	a1	a2	a0	a1	a2
0 - 24	0.675	15.3	6.21	0.630	6.77	1.38	0.00
24 - 36	0.532	39.0	8.03	0.413	10.82	1.11	0.00
36 - 48	0.532	25.8	6.53	0.413	8.81	1.11	0.00
48 - 60	0.509	25.1	6.20	0.381	8.69	1.07	0.00
60+	0.488	24.3	5.85	0.351	8.55	1.03	0.00

Table 5

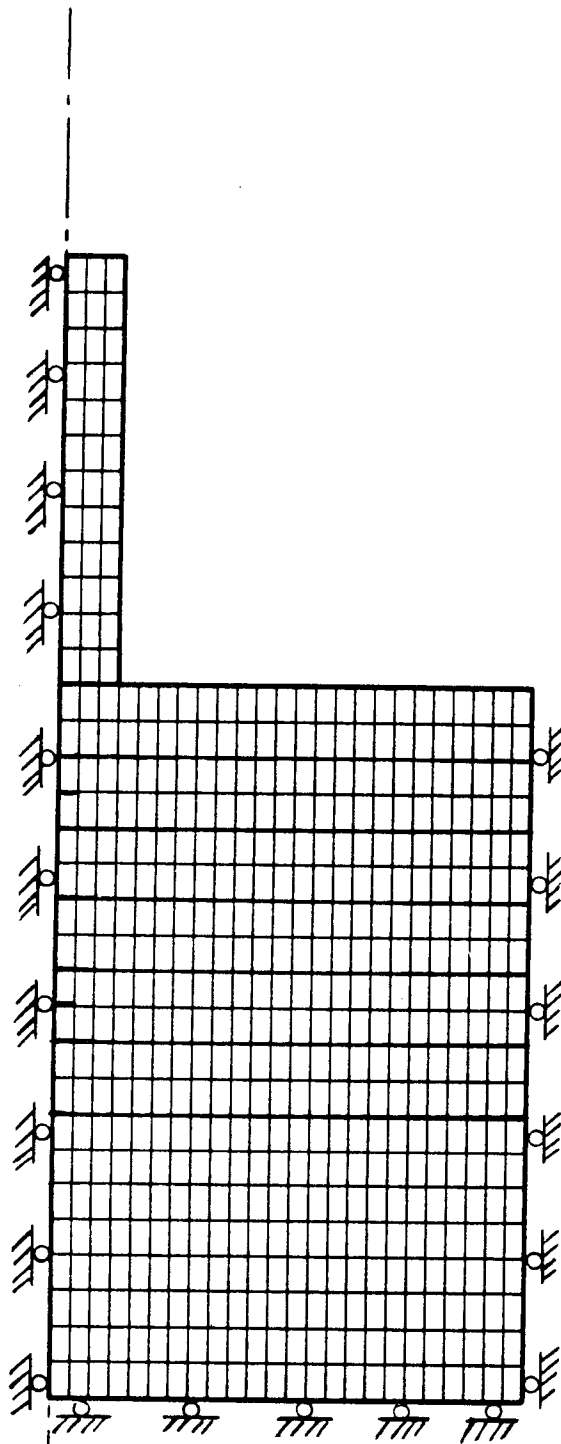
material properties for the top 12 inches of soil were not available, properties for the 12- to 24-inch layer were used for the top 12-inch layer. The deviatoric yield function constants for PRONTO-2D are different than those for DYNA2D because the deviatoric yield function in the soil constitutive model in PRONTO-2D uses effective stress in place of the second invariant of deviatoric stress used in DYNA2D. The deviatoric yield function constants in Table 5 actually represent the same deviatoric yield surface.

Since both the loading and the geometry were axisymmetric, two-dimensional axisymmetric finite element models were used in this series of calculations (Figure 59). Model A was used with the DYNA2D finite element code and Model B was used with the PRONTO-2D finite element code. These two different models were used to take advantage of special features found in each code. The series of analyses completed with DYNA2D and Model A used the mesh rezoning capability for large strains. Since a rezoning capability was not available in PRONTO-2D a different model was required. The series of analyses completed with PRONTO-2D and Model B used slide lines with friction on the right edge to represent the effects of the rest of the soil on the model.

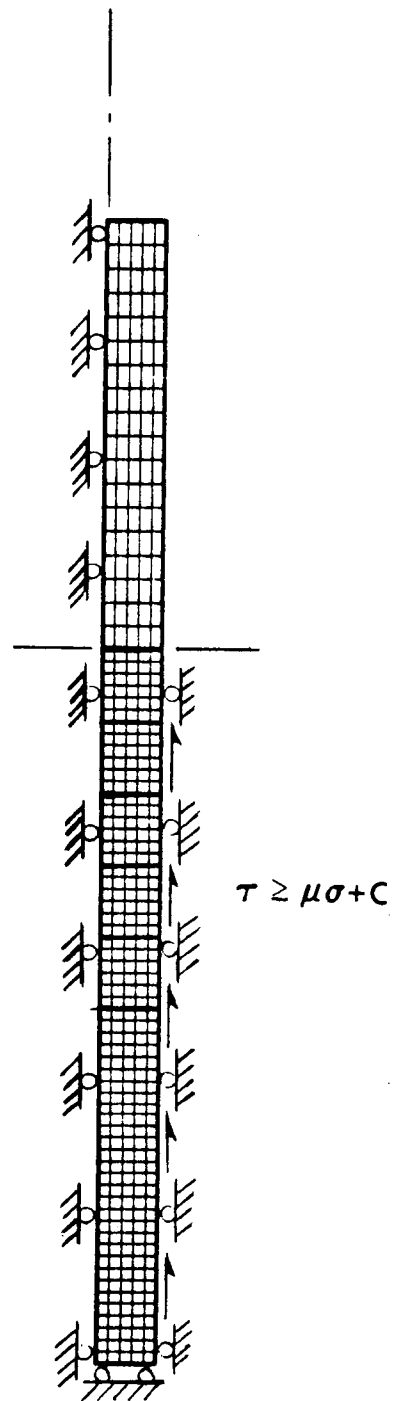
In the second series of analyses with PRONTO-2D and Model B, sliding was expected along the right edge when the magnitude of the shear stress along this edge (τ) exceeded the magnitude of the soil cohesion (C) plus the product of the internal friction coefficient (μ) and the normal stress (σ_n). In equation form, sliding is expected if

$$\tau > C + \mu \sigma_n$$

The internal friction coefficient, μ , is given by the following equation



a) Model A



b) Model B

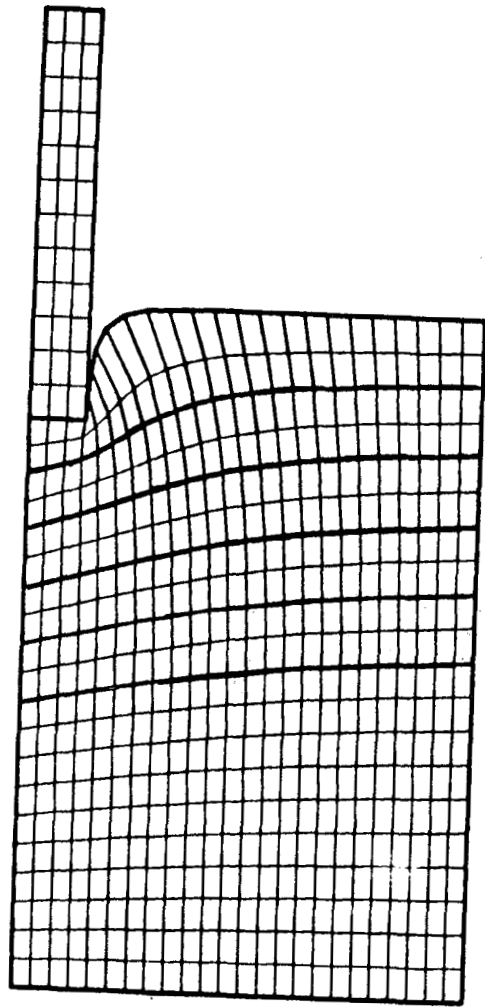
Figure 59 Finite Element Model for Soil Analysis

$$\mu = \tan \phi$$

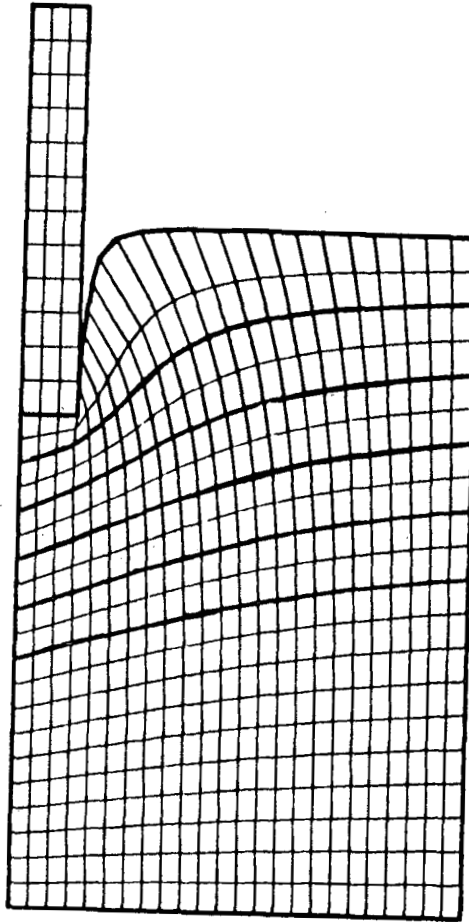
where ϕ is the experimentally measured internal friction angle. Internal friction coefficient values used in this analysis are given in Table 5. For this series of analyses, the small cohesion values were neglected and sliding was allowed along the right edge when the magnitude of the shear stress along this edge exceeded the product of the internal friction coefficient and the normal stress.

4.3.2 Soil Finite Element Results

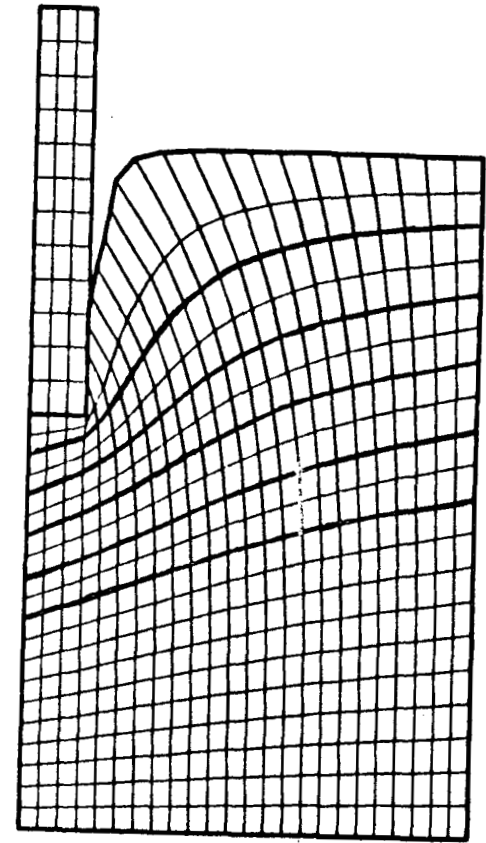
Plots of the deformed finite element meshes are shown in Figures 60 and 61. The top soil layer in the DYNA2D series of calculations was rezoned at several time steps during these analyses. Effects of the slide line friction in the PRONTO-2D series of analyses can be seen in Figure 61. The models in both series of analyses predicted the soil behavior very well. Plots of cask penetration as a function of time are shown in Figure 62. For the series of analyses completed with DYNA2D, estimates of cask acceleration were obtained by dividing the change in cask velocity during a time step by the time step magnitude. For the series of analyses completed with PRONTO-2D, estimates of cask acceleration as a function of time are shown in Figure 63. For the drop with an initial velocity of 88 ft/s, a peak acceleration of 38 g's was predicted by the series of analyses with DYNA2D and a peak acceleration of 50 g's was predicted with PRONTO-2D. A computer analysis was not performed for the 110 ft/s impact into the uncompacted soil.



a) Impact Velocity = 44 fps



b) Impact Velocity = 66 fps



c) Impact Velocity = 88 fps

Figure 60 Deformed Shape of Finite Element Model 'A' at Maximum Cask Penetration

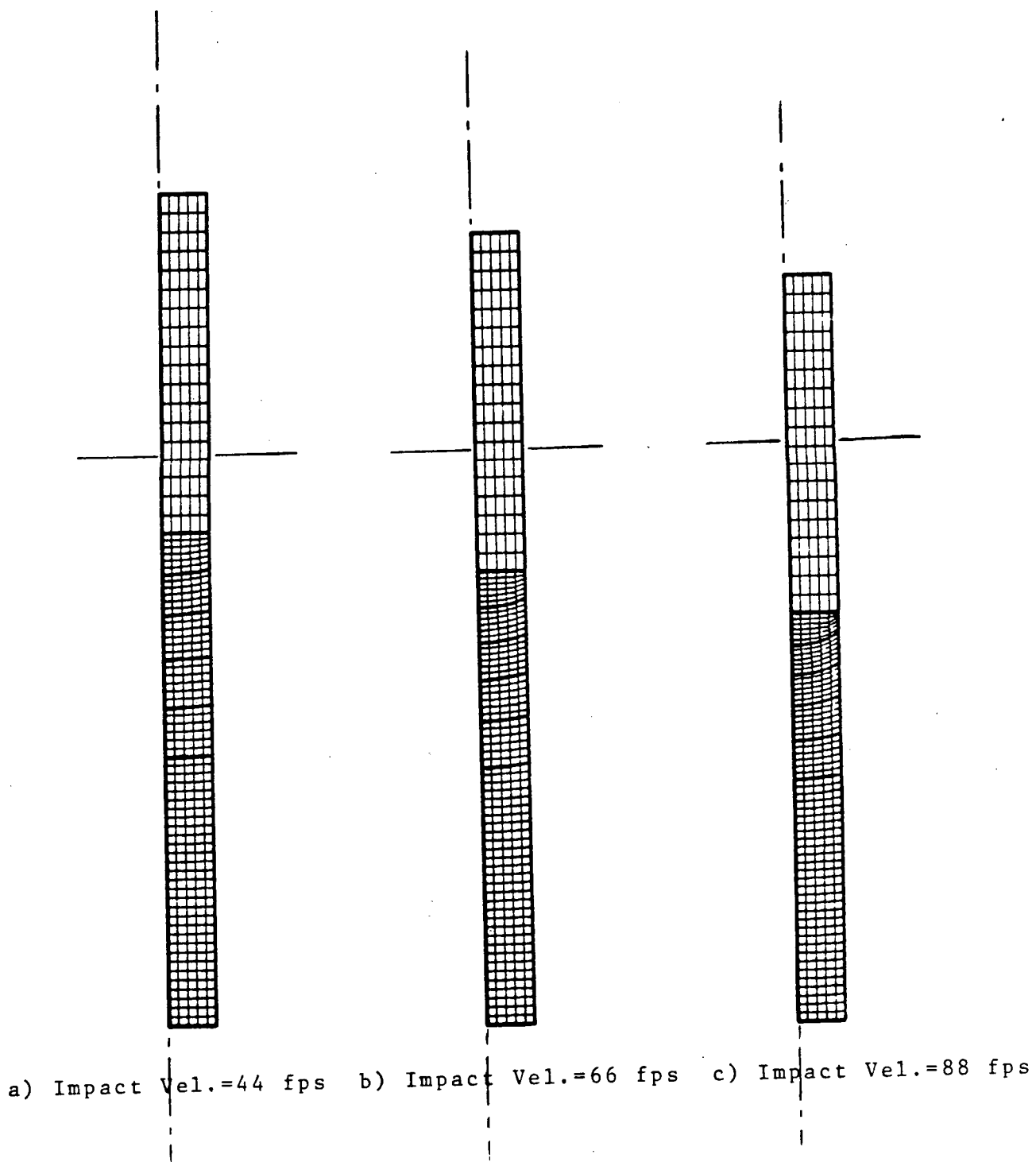
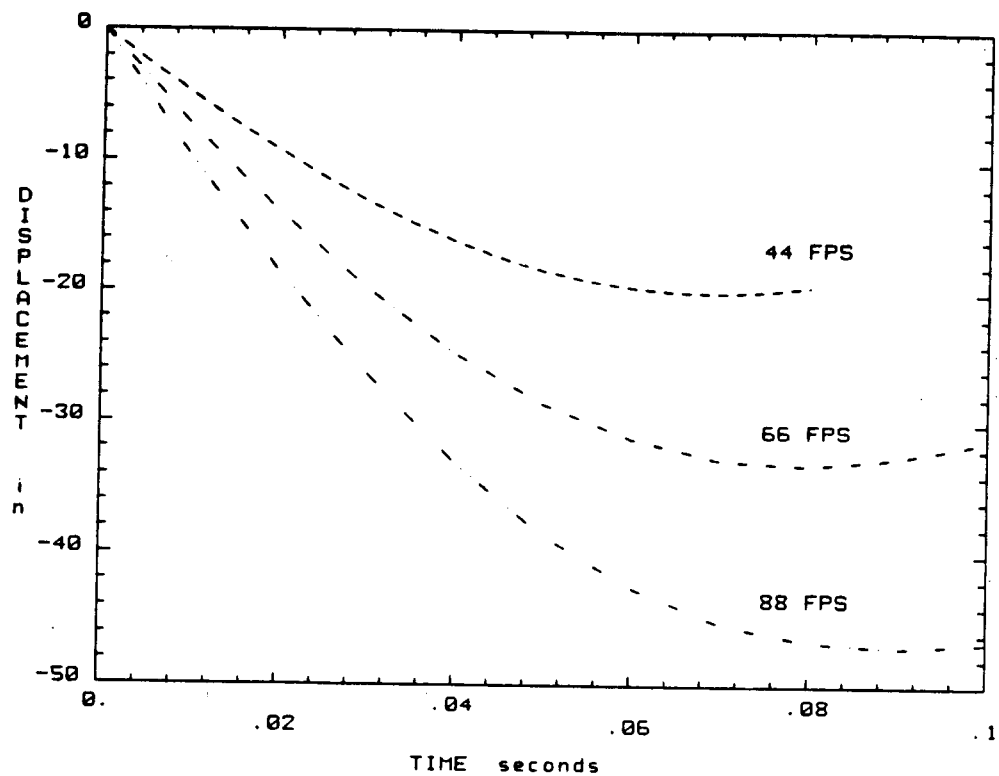
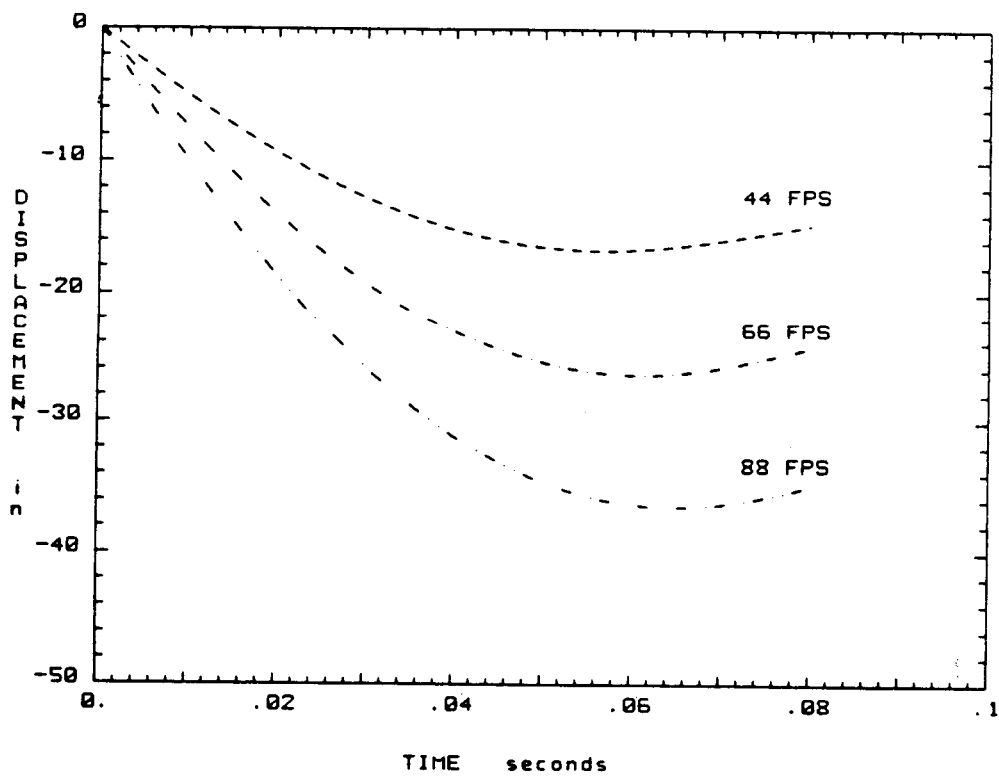


Figure 61 Deformed Shape of Finite Element Model 'B'
at Maximum Cask Penetration

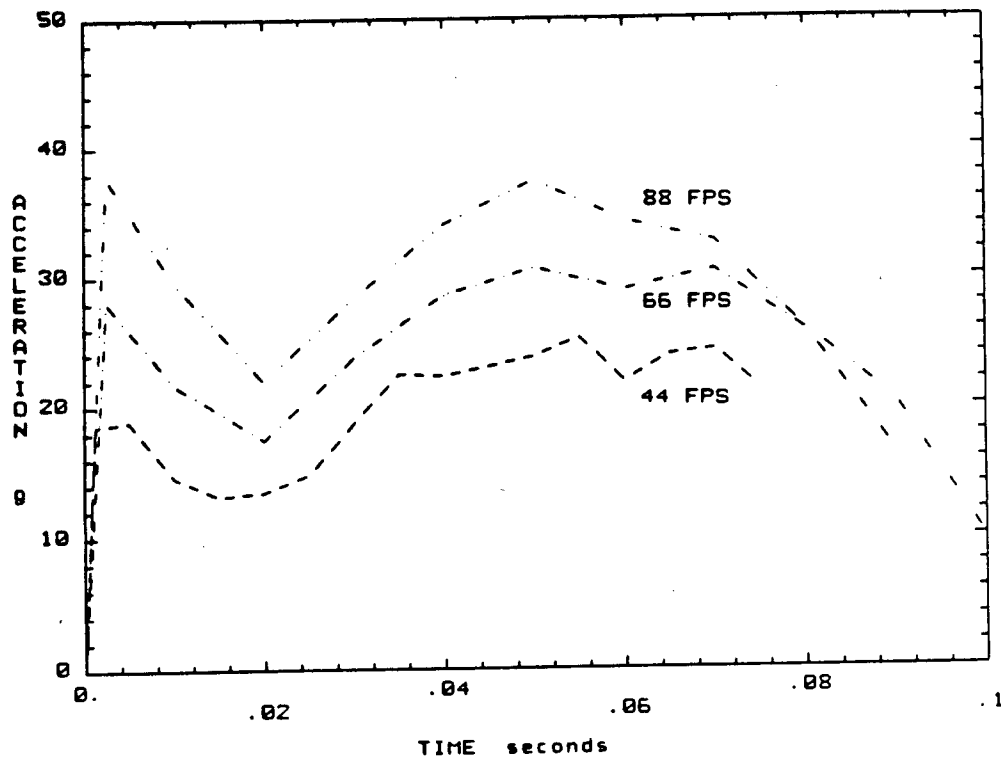


a) Model A and DYNA-2D

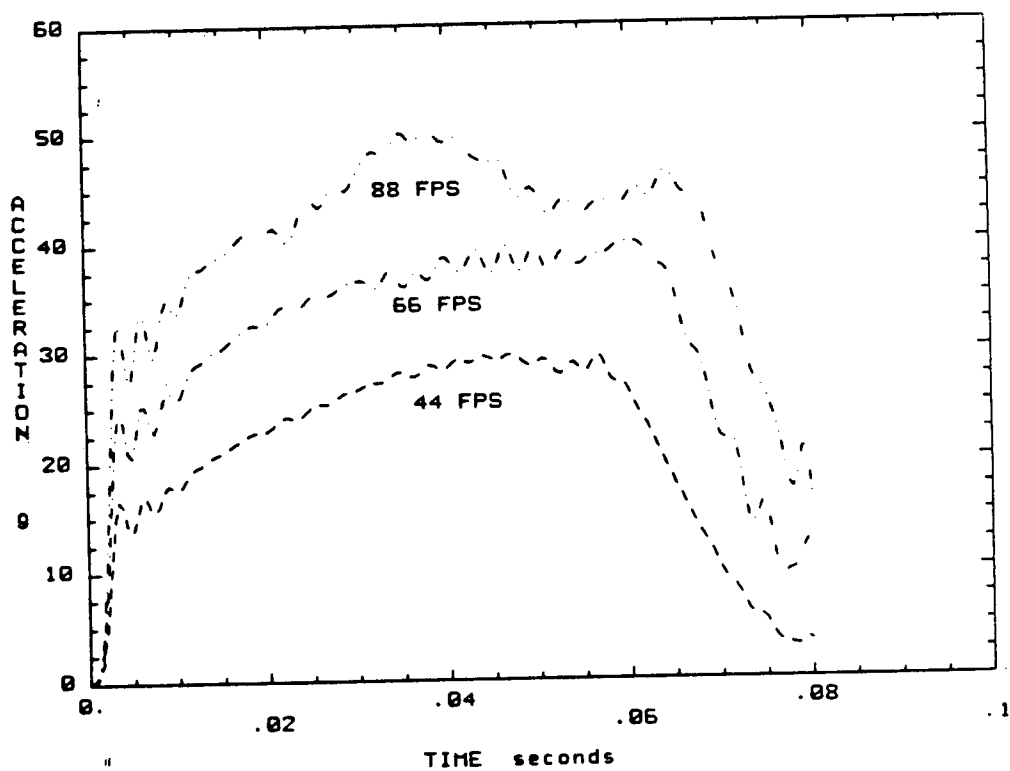


b) Model B and PRONTO-2D

Figure 62 Penetration vs. Time from Soil Analysis



a) Model A and DYNA-2D



b) Model B and PRONTO-2D

Figure 63 Acceleration vs. Time from Soil Analysis

The next series of analyses was completed to determine what effects variations in the volumetric behavior of the soil would give on the results. This series of analyses was completed using PRONTO-2D and Model B, and an impact velocity of 66 ft/s. Results from this series of analyses indicate that when the bulk modulus was increased from 2000 to 4000 psi, the expected penetration depth decreased from 26 to 18 inches (Figure 64). When the bulk modulus was decreased from 2000 to 1000 psi, the expected penetration depth increased from 26 to 38 inches. The results were sensitive to variation in bulk modulus.

A final series of analyses was completed to determine how sensitive the results were to friction coefficient variations. This series of analyses was also completed using PRONTO-2D and Model B and an impact velocity of 66 ft/s. For this analyses, all soil layers were given the same friction coefficient. Results from this series of analyses indicated that selection of friction coefficients of 0.25 and 0.75 would generate penetration depth estimates of 36 and 24 inches, respectively (Figure 65).

4.3.3 Comparison of Experimental and Analytical Results

Penetration depths predicted by the finite element analyses were compared with experimental results in Table 6. This comparison indicated that the finite element analyses completed with PRONTO-2D generated the most accurate estimates of penetration depth. A graphical comparison of penetration depths is shown in Figure 66.

Included in Figure 66 is a curve obtained from an empirical equation used to predict the penetration depth of various penetrators. The relationship was

BULK MODULUS EFFECTS

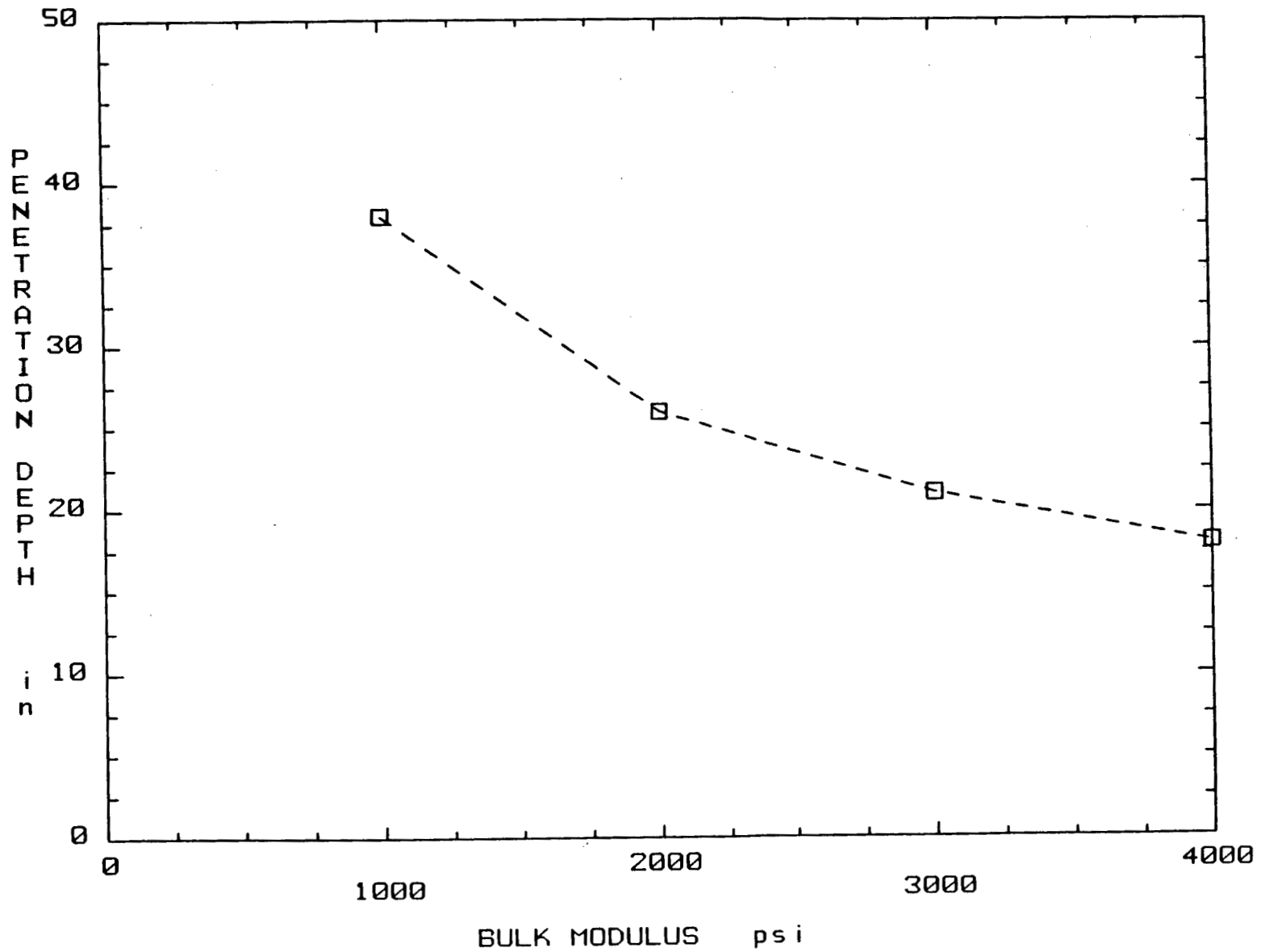


Figure 64 Effect of Variations in Soil Volumetric Behavior - Model B and PRONTO-2D, Impact Velocity at 66 ft/s

FRICITION COEFFICIENT EFFECTS

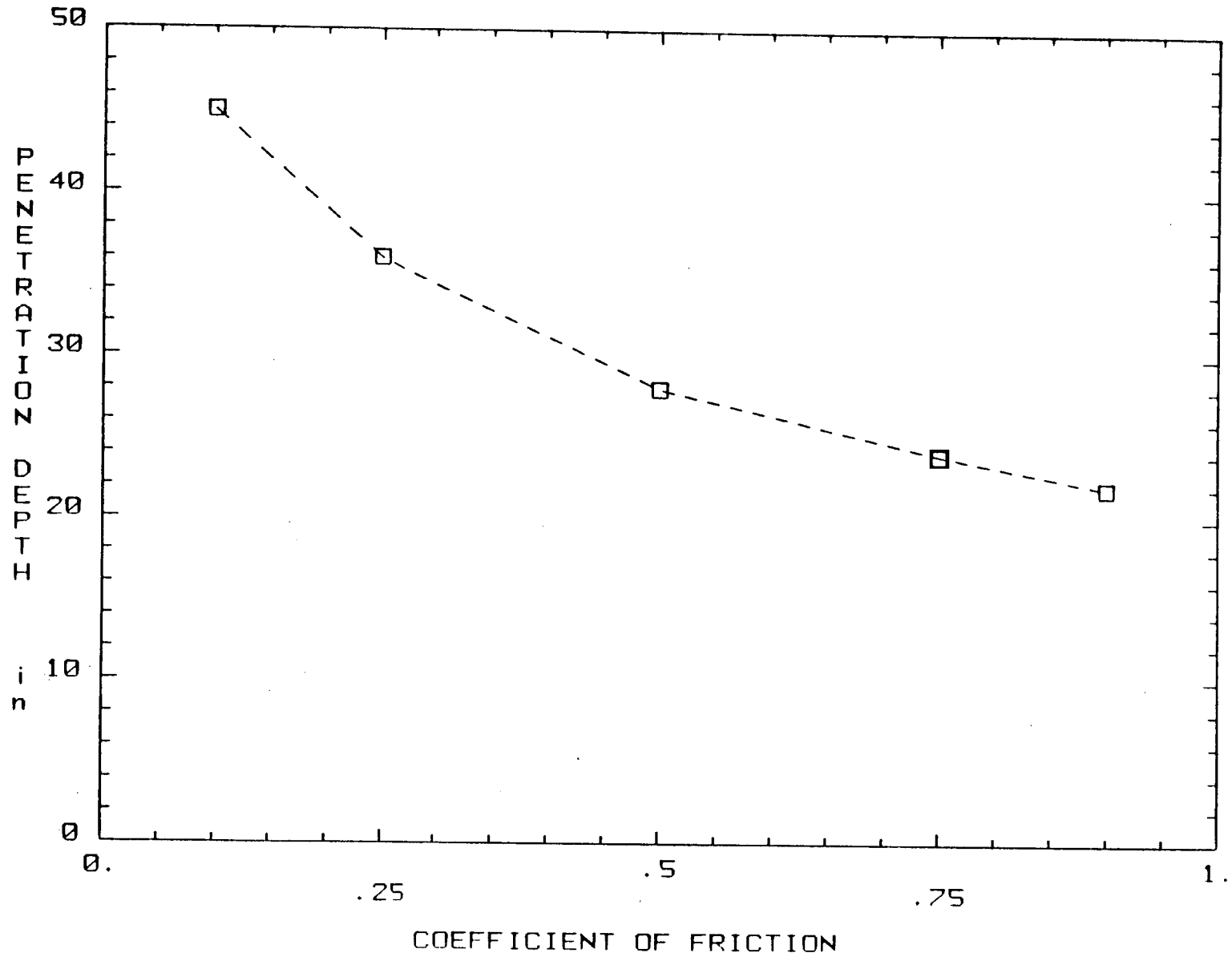


Figure 65 Effect of Variations in Friction Coefficient - Model B and PRONTO-2D, Impact Velocity of 66 ft/s

SOIL PENETRATION DEPTH (inches)			
IMPACT VELOCITY (ft/s)	44	66	88
EXPERIMENTAL	19	25	36
DYNA2D AND MODEL A	20	33	47
PRONTO-2D AND MODEL B	17	26	36

Table 6

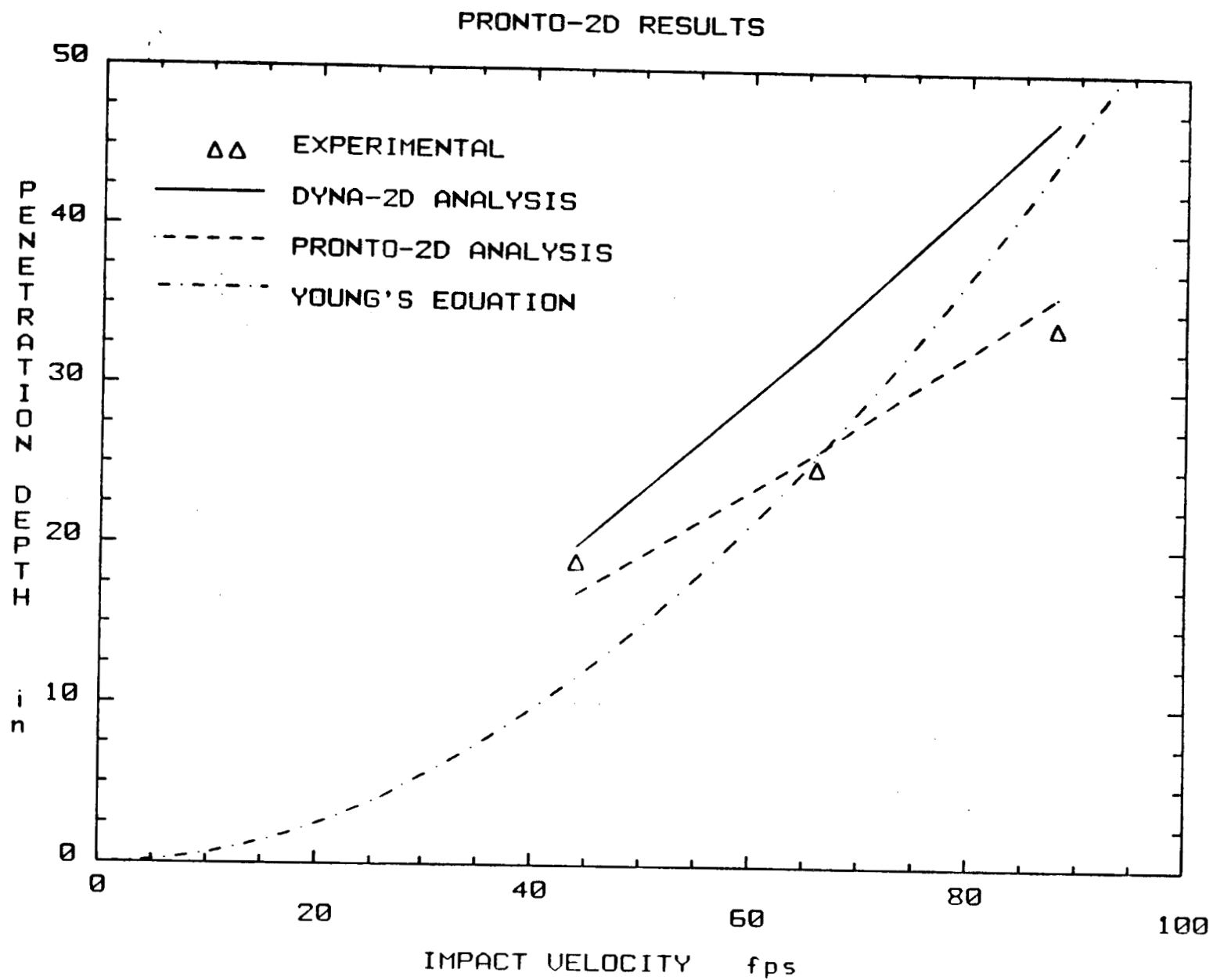


Figure 66 Comparison of Experimental and Analytical
Soil Results of Penetration Depth at 44 ft/s

developed and published by C. W. Young in 1969 [18] and based on experimental results from a series of drop tests completed during the 1960s. For a penetrator with an impact velocity of less than 200 ft/s the equation developed is:

$$D = 0.535N (W/A)^{1/2} \ln (1 + 2 \times 10^{-5} V^2)$$

where

D = depth of penetration, ft

S = soil constant (Table 7)

N = nose performance constant (Table 7)

W = penetration weight, lbs

A = penetration sectional area, in²

V = impact velocity, ft/s

The major difficulty encountered using this equation is the selection of an appropriate soil constant (S). For this analysis, a soil constant of 19.4 generated the best fit of Young's equation to the experimental data (Figure 66). In Table 7 a soil constant between 9 and 14 is suggested for topsoil. Penetration depths would have been seriously underestimated if these values were used.

Cask accelerations predicted by the finite element analyses were compared with the experimental results in Figures 67 to 69. These plots were filtered with a low pass filter with a cut-off frequency of 500 Hz. Both finite element analyses predicted the cask acceleration would remain nearly constant

COEFFICIENTS FOR YOUNG'S EMPIRICAL EQUATION

SOIL TYPE	S	NOSE TYPE	N
Rock	1.0 - 1.1	Flat	0.56
Loose Sand	6.0 - 8.0	Cone ($l/d = 0.3$)	1.32
Topsoil	9.0 - 14.0		
Saturated Clay	33.0 - 60.0		

Table 7

ACCELERATION - 44 FPS - EXPERIMENTAL

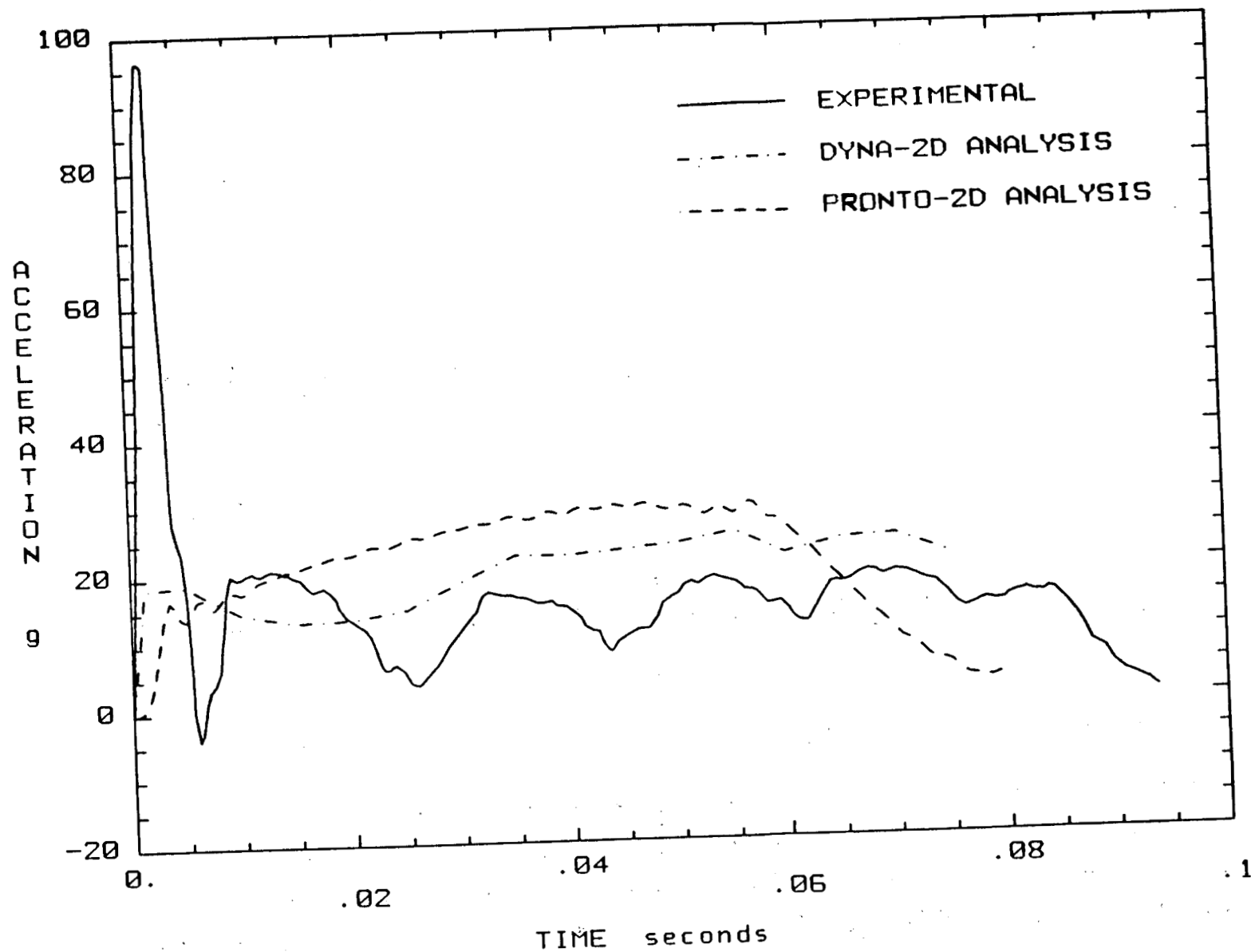


Figure 67 Comparison of Experimental and Analytical
Soil Results - Cask Acceleration - 44 ft/s

EXP 66

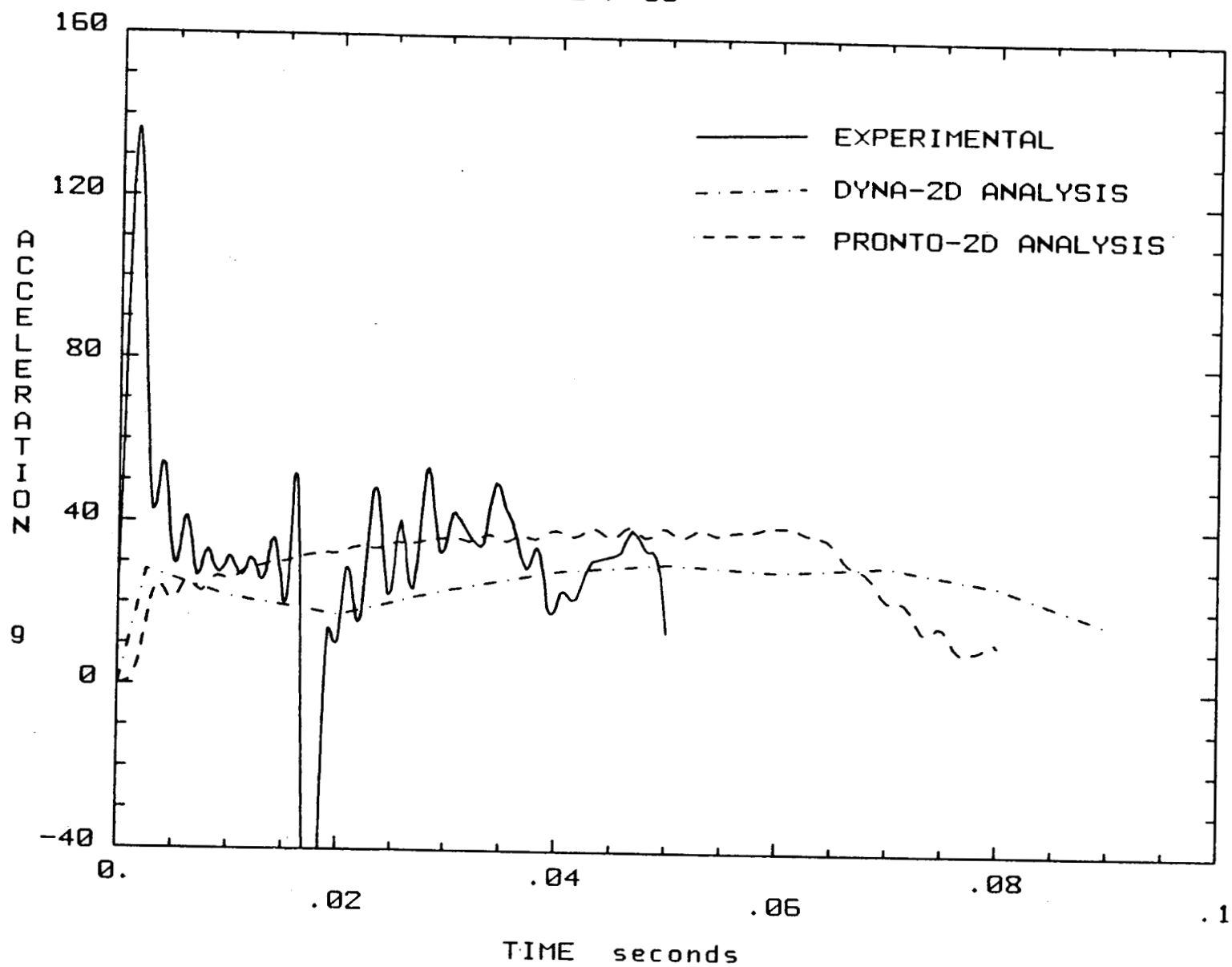


Figure 68 Comparison of Experimental and Analytical
Soil Results of Cask Acceleration at 66 ft/s

EXP 88

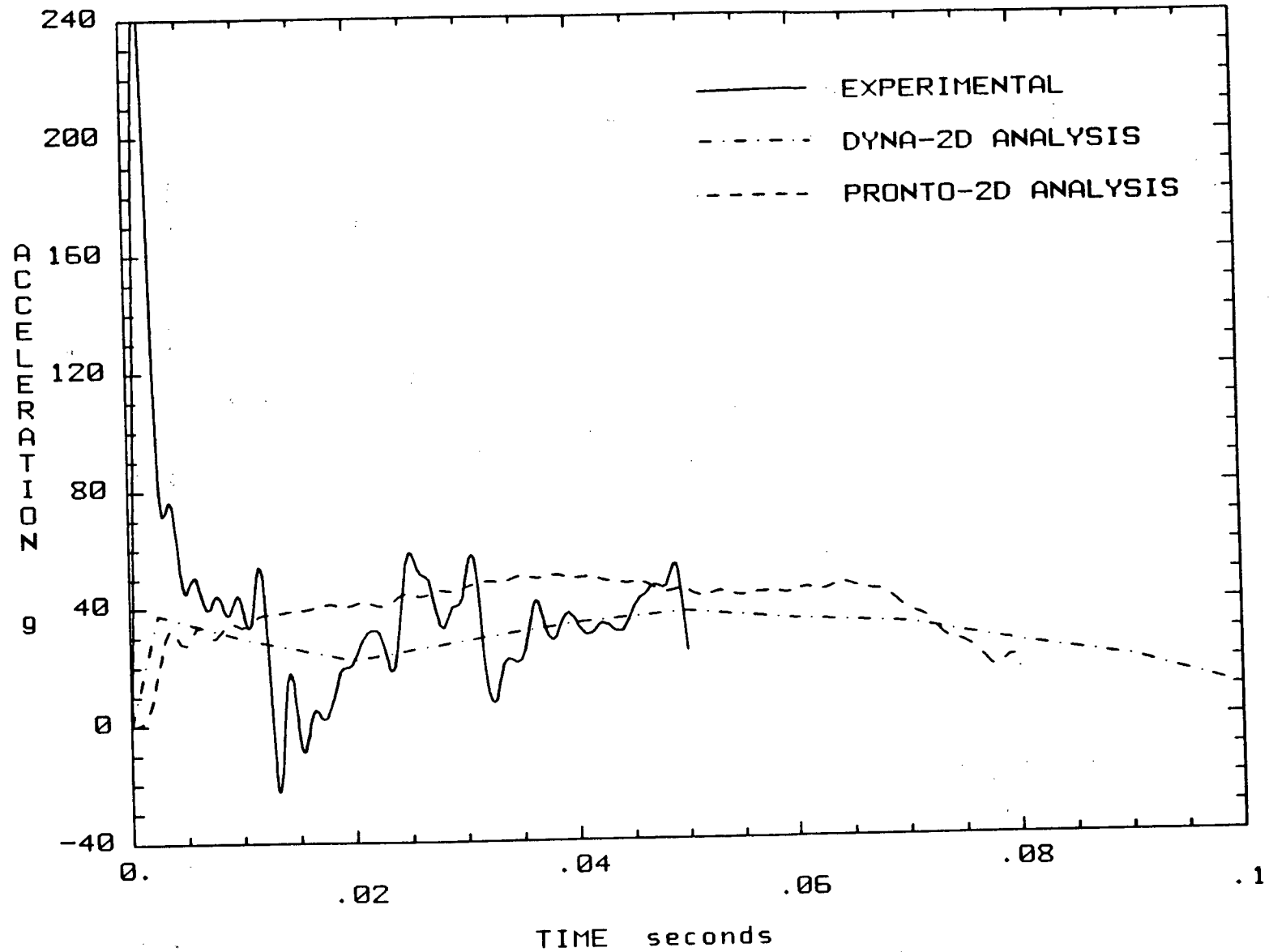


Figure 69 Comparison of Experimental and Analytical
Soil Results of Cask Acceleration at 88 ft/s

during the impact event which correlates with experimental findings. Experimental results indicated the cask acceleration would be significantly higher during the first few milliseconds of the impact event. Both analyses failed to predict the relatively large acceleration that was generated during the first few milliseconds of the impact event. One possible reason for this discrepancy between analytical and experimental results is that the top 12 inches of soil material was not accurately modeled because mechanical properties for this top soil layer were not measured. Also, the acceleration spike from rebound was not reproduced in the analysis. Experimental soil classification tests indicated that the top 12 inches of soil material contained a large amount of gravel and was significantly different than the rest of the soil.

5.0 CONCLUSIONS

Impacting a blunt-end cylindrical object into a series of various targets at a range of velocities produced results ranging from both anticipated to unexpected. The most severe damage to the test unit was from impacting the unyielding target at 44 ft/s. Only the 88 ft/s impact into the concrete runway produced unit responses on the same order of magnitude. However, several observations are made from this testing and analytical program.

The analytical calculations concerning the concrete and soil targets were difficult and cumbersome despite the fact several experimental findings were reproduced. A more detailed analysis may result in a mathematical process and procedure that more accurately predicts projectile and target response, but,

the complexity associated with this type of analysis is far more difficult than the problem of a projectile striking an unyielding target.

In analyzing the effects of impacting an object into an unyielding target, only the actual projectile needs to be modeled. Computer codes mathematically represent an impenetrable surface enabling all of the available energy to be applied to the striking projectile. Analyzing a yielding target entails representing the geometry, materials and boundary conditions of the impacted surface itself. In addition, the complex failure mechanisms of each type of target must also be taken into account.

Overall, the correlation between experimental results and analytical calculations were encouraging (Table 8). The unyielding target results obtained analytically were well matched with those found experimentally. The penetration values with respect to the soil targets were reproduced between experimental and analytical results, however, acceleration levels did not match. This discrepancy in acceleration levels was common in all the yielding targets.

With regard to a yielding target's response upon impact, the phenomenon of a double spike was evident. At the instant of impact the projectile experiences a response producing measurable accelerations and strains. This first spike is evidence of the shear planes that are forming in the concrete and soil targets. Depending on the impact velocity and nature of the target, a second response representing the unit rebounding is likely to occur after the unit comes to a complete stop. However, note that this phenomenon is representative of a blunt-end object without impact limiters. If impact limiters were employed, the phenomenon of the double spike would most likely disappear. Depending on the impact limiters, the softer the material, the

COMPARISON OF EXPERIMENTAL VS ANALYTICAL RESULTS

TEST		ACCELERATIONS (g's)		PENETRATION (inches)	
		Experimental	Analytical	Experimental	Analytical
UNYIELDING TARGET	44 ft/s	1300	1600	0	0
CONCRETE HIGHWAY	44 ft/s	350	300	4	8
	88 ft/s	7500	600	8	14
NATIVE DESERT SOIL	44 ft/s	100	20	19	17
	66 ft/s	130	30	25	26
	88 ft/s	250	40	36	36

Table 8

more closely a yielding target such as concrete would appear to be unyielding. However, that correlation strictly relies on the impact limiters, test unit and target used.

Comparison of the additional available kinetic energy involved by increasing the impact velocity was made with respect to unit damage and penetration depth. A good correlation was obtained between the increased kinetic energy and unit damage. Radial deformation was used to represent the test unit damage. The relationship between damage and increased available energy was within a factor of a half. However, comparison between penetration depth and kinetic energy was not so close. The additional penetration into the soil was less than the ratio of increased available energy. On the other hand, the change in penetration into the concrete targets was greater than the increase kinetic energy ratio. This suggests that a finite amount of energy is required to form the concrete shear plug. Once that has occurred, travel through the concrete target is less restricted. Forming the shear planes in the soil target and then compressing the soil to lock-up becomes more difficult as penetration depth increases. It is quite probable as impact speeds increase far beyond the 88 ft/s impact velocity used in this program, the same phenomenon would occur in the concrete targets.

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Appendix A
Accelerometer and Stain Gage Specifications

MINIATURE ACCELEROMETER, HI-OVERRANGE PROTECTED, PIEZORESISTIVE
FULL BRIDGE, DAMPED, WITH FLANGE MOUNTING.
ENTRAN DEVICES MODEL NO. EGAXT-23-F-5000/CERTIFIED

Accelerometer range +/- 5000 g

Overrange at approximately +/- 7000 g

Overrange in all three axes

Sensitivity .05 Mv/g

Full scale output 250 Mv

Resonate frequency 8.5 KHz

Nonlinearity +/- 1%

Transverse sensitivity 3% max

Damping .7 critical nominal at 75 Deg F flat to 1/2 db

Useful frequency range 30% to 50% resonate frequency at 75 Deg F

Thermal and mechanical conditioning

Input impedance 1000 ohms

Output impedance 450 ohms

Excitation voltage 15 VDC

Case material 300 series stainless steel

Compensated temperature 0 Deg F to 100 Deg F

Operating temperature -40 Deg F to 250 Deg F

Compensation module at 18 inches

Accelerometer to be supplied with 48 inch lead length

Unit to be flange mounted

Supplier to furnish requester with drawings of mounting configuration and manufactures specification for installation and torque values for mounting

Supplier will furnish accelerometers with unique identification numbers, which will be referenced to the supplier furnished certifications

Units to be supplied with E5 type shielded cable

Units to be supplied calibrated at -20 Deg F and 75 Deg F

Shock test units to 10,000 g prior to final calibration

Vibration testing @ 40 g +/- 20 percent of natural frequency 3 sec/sweep for a total time of 15 minutes

Thermal testing @ 250 Deg F for 30 minutes and -40 Deg F for 30 minutes test to be repeated 8 times.

Unit body length to be .500 inches

Units to be supplied with 0-80 unf mounting holes with a center to center spacing of .270.

MINIATURE ACCELEROMETER, HI-OVERRANGE PROTECTED, PIEZORESISTIVE
FULL BRIDGE, DAMPED, WITH FLANGE MOUNTING.
ENTRAN DEVICES MODEL NO. EGAXT-48-F-10000/CERTIFIED

Accelerometer range +/- 10000 g

Overrange at approximately +/- 15000 g

Overrange in all three axes

Sensitivity .025 Mv/g nominal

Full scale output 250 Mv +/- 20 percent

Resonate frequency 12 KHz nominal

Nonlinearity +/- 1% of full scale

Transverse sensitivity +/- 3% max

Response at 75 Deg F flat to +/- .5 db from 20 Hz to 4.5 KHz minimal

Total unit response at 75 Deg F not to exceed +/- .5 db

Thermal and mechanical conditioning

Input impedance 1000 ohms nominal

Output impedance 450 ohms nominal

Excitation voltage 15 VDC

* Case material 300 series stainless steel

Compensated temperature -20 Deg F to 100 Deg F

Operating temperature -40 Deg F to 250 Deg F

Compensation module located at 48 inches

Accelerometer to be supplied with 120 inch lead length

Unit to be flange mounted

Supplier to furnish requester with drawings of mounting configuration and manufactures specification for installation and torque values for mounting

Supplier will furnish accelerometers with unique identification numbers, which will be referenced to the supplier furnished calibrations

Units to be supplied with E5 type shielded cable

Units to be supplied calibrated at -20 Deg F and 74 Deg F

Shock test units to 10,000 g prior to final calibration

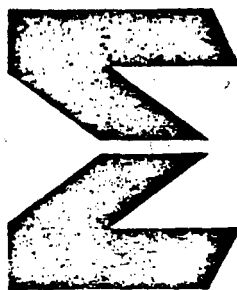
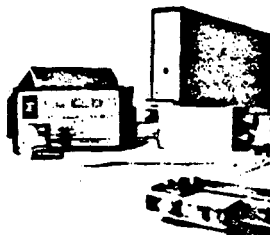
Vibration testing @ 40 g +/- 20 percent of natural frequency 3 sec/ sweep for a total time of 15 minutes

Thermal testing @ 250 Deg F for 30 minutes and -40 Deg F for 30 minutes test to be repeated 8 times

Unit body length to be .500 inches

Units to be supplied with 0-80 unf mounting holes with a center to center spacing of .270

ENDEVCO PRODUCT DATA



MODELS **2262-1000**
2262C-1000

±1000 g
Damped

**PIEZORESISTIVE
ACCELEROMETERS**

The Models 2262-1000 and 2262C-1000 are rugged and damped accelerometers that measure static and dynamic acceleration. Endevco Piezite® Type P-9 piezoresistive elements are employed in a full bridge circuit to obtain a high level, low impedance output at ±1000 g full scale. The Model 2262C is a 6-wire device with a pair of fixed precision resistors in half the bridge, designed especially for shunt calibration.

The units will withstand up to 2.5 times their rated range without damage or calibration shift. The use of subcritical viscous damping extends their useful frequency range and reduces the effect of spurious, high frequency vibrations.

The broad frequency response from steady state to 2000 Hz makes these transducers ideal for measurement of transient type phenomena such as encountered in rocket engine ignitions, package testing, transportation shock, and automotive crash studies.

*SANDIA STN
758710*



SPECIFICATIONS FOR THE MODEL 2262-1000 AND 2262C-1000 ACCELEROMETERS (According to ANSI and ISA Standards)

DYNAMIC

	Model 2262-1000	Model 2262C-1000
RANGE	± 1000 g	± 1000 g
SENSITIVITY	0.5 mV/g, nominal	0.25 mV/g, nominal
MOUNTED NATURAL FREQUENCY (at 75°F)	6000 Hz, nominal	6000 Hz, nominal
FREQUENCY RESPONSE ¹	± 5%, 0 to 2000 Hz, at 75°F; —35%/+ 10%, nominal, at 0°F/200°F and 2000 Hz, reference 75°F.	
DAMPING RATIO	0.7 nominal, at 75°F	
TRANSVERSE SENSITIVITY ²	3% maximum	
THERMAL SENSITIVITY SHIFT	—2%/0/—4% nominal at 0°F/75°F/200°F	
LINEARITY AND HYSTERESIS	± 1% of reading, maximum, to ± 1000 g	

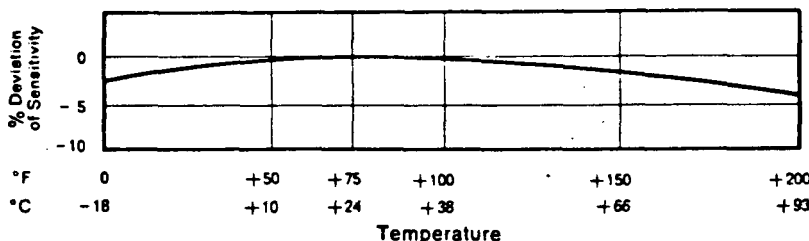
ELECTRICAL

EXCITATION ³	10.0 Vdc	10.0 Vdc
INPUT RESISTANCE (at 75°F)	560Ω nominal	1000Ω nominal
OUTPUT RESISTANCE (at 75°F)	350Ω nominal	1000Ω nominal
INSULATION RESISTANCE ⁴	100 MΩ minimum	100 MΩ minimum
ZERO MEASURAND OUTPUT	± 10 mV, maximum, at 10.0 Vdc and 75°F.	
THERMAL ZERO SHIFT	± 10 mV, maximum, at 0°F and 200°F, reference 75°F (24°C).	

NOTES

- ¹ Response is ±5%, 0 Hz to 250 Hz, over the temperature range of 0°F to 200°F.
- ² Worst case error in any axis perpendicular to sensitive axis. Selection of 1% is available on special order.
- ³ Unit is calibrated at 10.0 Vdc. Lower excitation voltages may be employed, but should be specified at time of order to obtain best thermal compensation. Warmup time to meet all specifications is 1 minute. Endevco® Model 4470 Signal Conditioner is recommended as the excitation source.
- ⁴ Measured with 100 Vdc, maximum, all leads to case. Cable shield common to case.

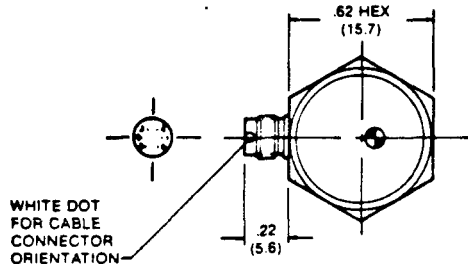
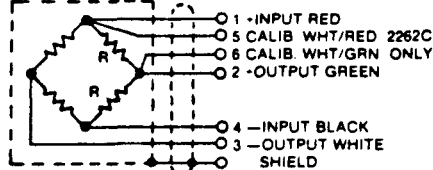
TYPICAL TEMPERATURE RESPONSE



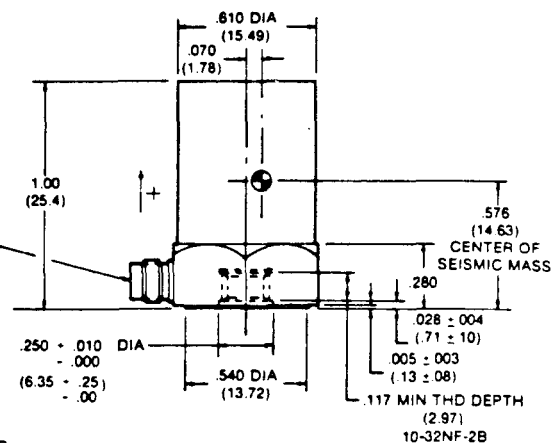
The curve shows the typical deviation of sensitivity with temperature.

SPECIFICATIONS FOR THE MODEL 2262-1000 AND 2262C-1000

WIRING DIAGRAM



CONNECTOR MATES WITH
CABLE ASSEMBLY SUPPLIED



DIMENSIONS IN INCHES AND
(MILLIMETERS)

TOLERANCES: .XX = ±0.03 (.8) IN MODEL 2262C.
.XXX = ±0.010 (.25) R = 1000 Q ±1%

PHYSICAL

WEIGHT

1 oz. (28 grams) nominal

CASE MATERIAL

Stainless Steel

SENSING ELEMENTS

Piezite® Type P-9

MOUNTING

Tapped hole for 10-32 x 1/4 in. stud.
Recommended mounting torque: 18 lbf-in (2Nm)

ELECTRICAL CONNECTIONS

Integral six-pin connector

ACCESSORIES INCLUDED

Model 2981-3 (10-32) or 2981-4 (M5 metric) Mounting Stud.

2262: Model 3022B-30 Cable Assembly, 30 inch, four conductor, shielded,
with accelerometer mating connector.

2262C: Model 3023B-30 Cable Assembly, 30 inch, six conductor, shielded,
with accelerometer mating connector.

ENVIRONMENTAL

ACCELERATION LIMITS (in any direction)

Static: 2500 g
Vibration: 1000 g pk sinusoidal
Shock: 2500 g pk half sine pulse

TEMPERATURE

Compensated: 0°F to 200°F (-18°C to 93°C)

HUMIDITY

Non-Operating: -20°F to 220°F (-29°C to 104°C)

BASE STRAIN SENSITIVITY

Hermetically sealed

0.0002 equivalent g, nominal, per μ strain.

Continued product improvement necessitates that Endevco reserve the right to modify these specifications without notice.

RELIABILITY: Endevco maintains a program of constant surveillance over all products to ensure a high level of reliability. This program includes attention to reliability factors during product design, the support of stringent Quality Control requirements, and compulsory corrective action procedures. These measures, together with conservative specifications, have made the name Endevco synonymous with reliability.

CALIBRATION: Each unit is calibrated at room temperature for sensitivity, input resistance, output resistance, maximum transverse sensitivity, mounted natural frequency, and zero measurement output. Temperature response data taken during initial calibration is available on request. Shock and other calibrations are available on special order. See Calibration Bulletin No. 301.

Estimated calibration errors: 5-1000 Hz, ±1.5%; 1000-10 000 Hz, ±2.5%.

U.S. Patent No. 3,351,880 applies to this transducer.

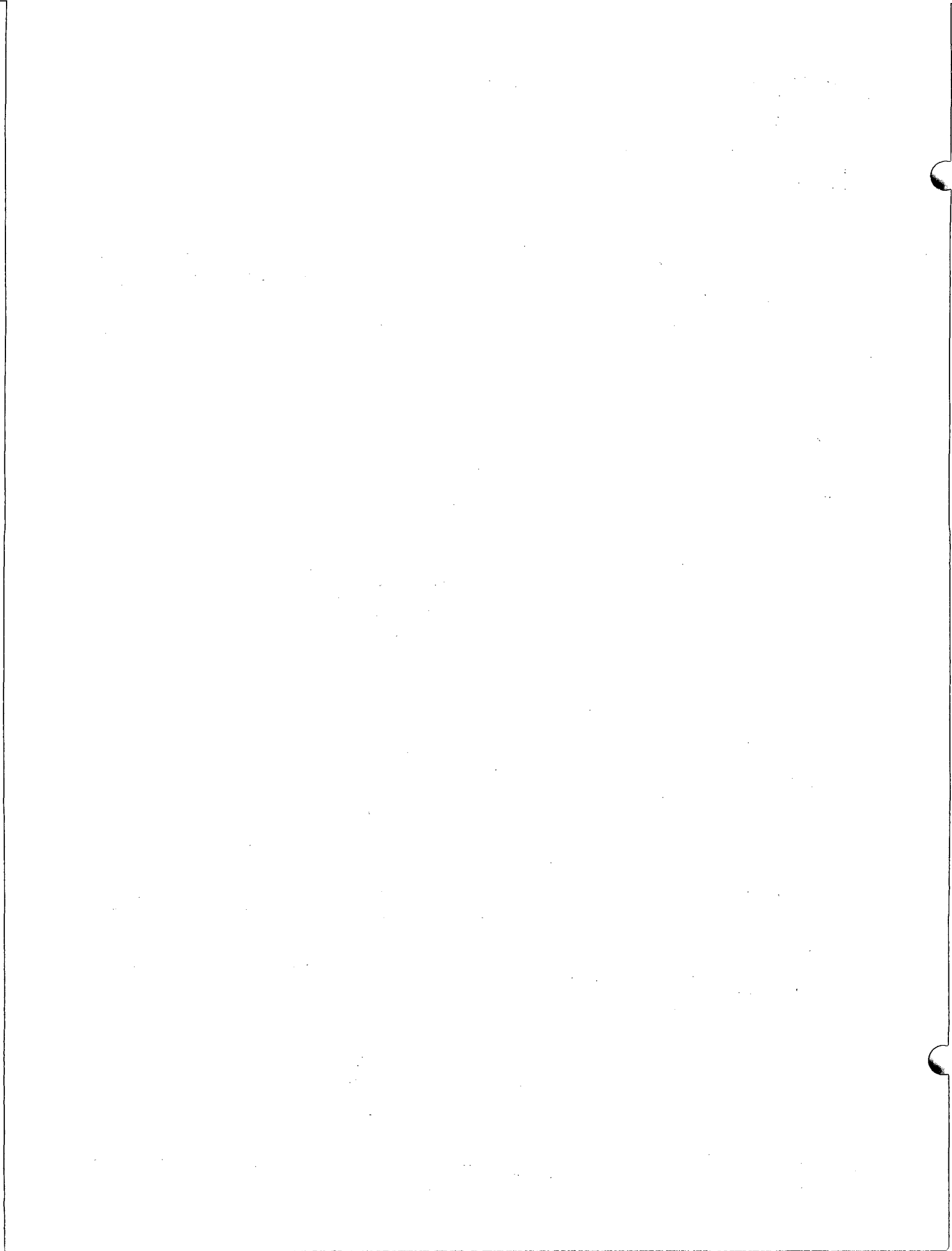


RANCHO VIEJO ROAD · SAN JUAN CAPISTRANO, CA 92675 · TELEPHONE (714) 493-8181

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Appendix B
Analytical Input
for Finite Element Calculations

Finite Element Input
for Unyielding Target Analysis
into DYNA2D Code

UNYIELDING TARGET - REFINED MESH

ND	1	642	568	0	0	0	0				0	
	0	0	0	0	0	1	1	0	0	0	0	0
		0.001		1E-05		1E-05		1E-05		0	9000	0
	1	3		6.42E-04								

STAINLESS STEEL

29E+06

0.3

30000.0

300000.0

0.5

1	1	0.000E+00	0.000E+00	0
2	1	0.000E+00	5.000E-01	0
3	1	0.000E+00	1.000E+00	0
4	1	0.000E+00	1.500E+00	0
5	1	0.000E+00	2.000E+00	0
6	0	6.250E-01	0.000E+00	0
7	0	6.250E-01	5.000E-01	0
8	0	6.250E-01	1.000E+00	0
9	0	6.250E-01	1.500E+00	0
10	0	6.250E-01	2.000E+00	0
11	0	1.250E+00	0.000E+00	0
12	0	1.250E+00	5.000E-01	0
13	0	1.250E+00	1.000E+00	0
14	0	1.250E+00	1.500E+00	0
15	0	1.250E+00	2.000E+00	0
16	0	1.875E+00	0.000E+00	0
17	0	1.875E+00	5.000E-01	0
18	0	1.875E+00	1.000E+00	0
19	0	1.875E+00	1.500E+00	0
20	0	1.875E+00	2.000E+00	0
21	0	2.500E+00	0.000E+00	0
22	0	2.500E+00	5.000E-01	0
23	0	2.500E+00	1.000E+00	0
24	0	2.500E+00	1.500E+00	0
25	0	2.500E+00	2.000E+00	0
26	0	3.125E+00	0.000E+00	0
27	0	3.125E+00	5.000E-01	0
28	0	3.125E+00	1.000E+00	0
29	0	3.125E+00	1.500E+00	0
30	0	3.125E+00	2.000E+00	0
31	0	3.750E+00	0.000E+00	0
32	0	3.750E+00	5.000E-01	0

33	0	3.750E+00	1.000E+00	0
34	0	3.750E+00	1.500E+00	0
35	0	3.750E+00	2.000E+00	0
36	0	4.375E+00	0.000E+00	0
37	0	4.375E+00	5.000E-01	0
38	0	4.375E+00	1.000E+00	0
39	0	4.375E+00	1.500E+00	0
40	0	4.375E+00	2.000E+00	0
41	0	5.000E+00	0.000E+00	0
42	0	5.000E+00	5.000E-01	0
43	0	5.000E+00	1.000E+00	0
44	0	5.000E+00	1.500E+00	0
45	0	5.000E+00	2.000E+00	0
46	0	5.625E+00	0.000E+00	0
47	0	5.625E+00	5.000E-01	0
48	0	5.625E+00	1.000E+00	0
49	0	5.625E+00	1.500E+00	0
50	0	5.625E+00	2.000E+00	0
51	0	6.250E+00	0.000E+00	0
52	0	6.250E+00	5.000E-01	0
53	0	6.250E+00	1.000E+00	0
54	0	6.250E+00	1.500E+00	0
55	0	6.250E+00	2.000E+00	0
56	0	6.875E+00	0.000E+00	0
57	0	6.875E+00	5.000E-01	0
58	0	6.875E+00	1.000E+00	0
59	0	6.875E+00	1.500E+00	0
60	0	6.875E+00	2.000E+00	0
61	0	7.500E+00	0.000E+00	0
62	0	7.500E+00	5.000E-01	0
63	0	7.500E+00	1.000E+00	0
64	0	7.500E+00	1.500E+00	0
65	0	7.500E+00	2.000E+00	0
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67	0	8.125E+00	5.000E-01	0
68	0	8.125E+00	1.000E+00	0
69	0	8.125E+00	1.500E+00	0
70	0	8.125E+00	2.000E+00	0
71	0	8.750E+00	0.000E+00	0
72	0	8.750E+00	5.000E-01	0
73	0	8.750E+00	1.000E+00	0
74	0	8.750E+00	1.500E+00	0
75	0	8.750E+00	2.000E+00	0
76	0	9.375E+00	0.000E+00	0

77	0	9.375E+00	5.000E-01	0
78	0	9.375E+00	1.000E+00	0
79	0	9.375E+00	1.500E+00	0
80	0	9.375E+00	2.000E+00	0
81	0	1.000E+01	0.000E+00	0
82	0	1.000E+01	5.000E-01	0
83	0	1.000E+01	1.000E+00	0
84	0	1.000E+01	1.500E+00	0
85	0	1.000E+01	2.000E+00	0
86	1	0.000E+00	2.500E+00	0
87	1	0.000E+00	3.000E+00	0
88	1	0.000E+00	3.500E+00	0
89	1	0.000E+00	4.000E+00	0
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93	0	6.250E-01	4.000E+00	0
94	0	1.250E+00	2.500E+00	0
95	0	1.250E+00	3.000E+00	0
96	0	1.250E+00	3.500E+00	0
97	0	1.250E+00	4.000E+00	0
98	0	1.875E+00	2.500E+00	0
99	0	1.875E+00	3.000E+00	0
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102	0	2.500E+00	2.500E+00	0
103	0	2.500E+00	3.000E+00	0
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107	0	3.125E+00	3.000E+00	0
108	0	3.125E+00	3.500E+00	0
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110	0	3.750E+00	2.500E+00	0
111	0	3.750E+00	3.000E+00	0
112	0	3.750E+00	3.500E+00	0
113	0	3.750E+00	4.000E+00	0
114	0	4.375E+00	2.500E+00	0
115	0	4.375E+00	3.000E+00	0
116	0	4.375E+00	3.500E+00	0
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122	0	5.625E+00	2.500E+00	0
123	0	5.625E+00	3.000E+00	0
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160	0	9.375E+00	4.625E+00	0
161	0	1.000E+01	4.625E+00	0
162	1	0.000E+00	5.250E+00	0
163	0	6.250E-01	5.250E+00	0
164	0	1.250E+00	5.250E+00	0

165	0	1.875E+00	5.250E+00	0
166	0	2.500E+00	5.250E+00	0
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168	0	3.750E+00	5.250E+00	0
169	0	4.375E+00	5.250E+00	0
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172	0	6.250E+00	5.250E+00	0
173	0	6.875E+00	5.250E+00	0
174	0	7.500E+00	5.250E+00	0
175	0	8.125E+00	5.250E+00	0
176	0	8.750E+00	5.250E+00	0
177	0	9.375E+00	5.250E+00	0
178	0	1.000E+01	5.250E+00	0
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186	0	4.375E+00	5.875E+00	0
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189	0	6.250E+00	5.875E+00	0
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197	0	6.250E-01	6.500E+00	0
198	0	1.250E+00	6.500E+00	0
199	0	1.875E+00	6.500E+00	0
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202	0	3.750E+00	6.500E+00	0
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205	0	5.625E+00	6.500E+00	0
206	0	6.250E+00	6.500E+00	0
207	0	6.875E+00	6.500E+00	0
208	0	7.500E+00	6.500E+00	0

209	0	8.125E+00	6.500E+00	0
210	0	8.750E+00	6.500E+00	0
211	0	9.375E+00	6.500E+00	0
212	0	1.000E+01	6.500E+00	0
213	1	0.000E+00	7.125E+00	0
214	0	6.250E-01	7.125E+00	0
215	0	1.250E+00	7.125E+00	0
216	0	1.875E+00	7.125E+00	0
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219	0	3.750E+00	7.125E+00	0
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222	0	5.625E+00	7.125E+00	0
223	0	6.250E+00	7.125E+00	0
224	0	6.875E+00	7.125E+00	0
225	0	7.500E+00	7.125E+00	0
226	0	8.125E+00	7.125E+00	0
227	0	8.750E+00	7.125E+00	0
228	0	9.375E+00	7.125E+00	0
229	0	1.000E+01	7.125E+00	0
230	1	0.000E+00	7.750E+00	0
231	0	6.250E-01	7.750E+00	0
232	0	1.250E+00	7.750E+00	0
233	0	1.875E+00	7.750E+00	0
234	0	2.500E+00	7.750E+00	0
235	0	3.125E+00	7.750E+00	0
236	0	3.750E+00	7.750E+00	0
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238	0	5.000E+00	7.750E+00	0
239	0	5.625E+00	7.750E+00	0
240	0	6.250E+00	7.750E+00	0
241	0	6.875E+00	7.750E+00	0
242	0	7.500E+00	7.750E+00	0
243	0	8.125E+00	7.750E+00	0
244	0	8.750E+00	7.750E+00	0
245	0	9.375E+00	7.750E+00	0
246	0	1.000E+01	7.750E+00	0
247	1	0.000E+00	8.375E+00	0
248	0	6.250E-01	8.375E+00	0
249	0	1.250E+00	8.375E+00	0
250	0	1.875E+00	8.375E+00	0
251	0	2.500E+00	8.375E+00	0
252	0	3.125E+00	8.375E+00	0

253	0	3.750E+00	8.375E+00	0
254	0	4.375E+00	8.375E+00	0
255	0	5.000E+00	8.375E+00	0
256	0	5.625E+00	8.375E+00	0
257	0	6.250E+00	8.375E+00	0
258	0	6.875E+00	8.375E+00	0
259	0	7.500E+00	8.375E+00	0
260	0	8.125E+00	8.375E+00	0
261	0	8.750E+00	8.375E+00	0
262	0	9.375E+00	8.375E+00	0
263	0	1.000E+01	8.375E+00	0
264	1	0.000E+00	9.000E+00	0
265	0	6.250E-01	9.000E+00	0
266	0	1.250E+00	9.000E+00	0
267	0	1.875E+00	9.000E+00	0
268	0	2.500E+00	9.000E+00	0
269	0	3.125E+00	9.000E+00	0
270	0	3.750E+00	9.000E+00	0
271	0	4.375E+00	9.000E+00	0
272	0	5.000E+00	9.000E+00	0
273	0	5.625E+00	9.000E+00	0
274	0	6.250E+00	9.000E+00	0
275	0	6.875E+00	9.000E+00	0
276	0	7.500E+00	9.000E+00	0
277	0	8.125E+00	9.000E+00	0
278	0	8.750E+00	9.000E+00	0
279	0	9.375E+00	9.000E+00	0
280	0	1.000E+01	9.000E+00	0
281	1	0.000E+00	9.625E+00	0
282	0	6.250E-01	9.625E+00	0
283	0	1.250E+00	9.625E+00	0
284	0	1.875E+00	9.625E+00	0
285	0	2.500E+00	9.625E+00	0
286	0	3.125E+00	9.625E+00	0
287	0	3.750E+00	9.625E+00	0
288	0	4.375E+00	9.625E+00	0
289	0	5.000E+00	9.625E+00	0
290	0	5.625E+00	9.625E+00	0
291	0	6.250E+00	9.625E+00	0
292	0	6.875E+00	9.625E+00	0
293	0	7.500E+00	9.625E+00	0
294	0	8.125E+00	9.625E+00	0
295	0	8.750E+00	9.625E+00	0
296	0	9.375E+00	9.625E+00	0

297	0	1.000E+01	9.625E+00	0
298	1	0.000E+00	1.025E+01	0
299	0	6.250E-01	1.025E+01	0
300	0	1.250E+00	1.025E+01	0
301	0	1.875E+00	1.025E+01	0
302	0	2.500E+00	1.025E+01	0
303	0	3.125E+00	1.025E+01	0
304	0	3.750E+00	1.025E+01	0
305	0	4.375E+00	1.025E+01	0
306	0	5.000E+00	1.025E+01	0
307	0	5.625E+00	1.025E+01	0
308	0	6.250E+00	1.025E+01	0
309	0	6.875E+00	1.025E+01	0
310	0	7.500E+00	1.025E+01	0
311	0	8.125E+00	1.025E+01	0
312	0	8.750E+00	1.025E+01	0
313	0	9.375E+00	1.025E+01	0
314	0	1.000E+01	1.025E+01	0
315	1	0.000E+00	1.088E+01	0
316	0	6.250E-01	1.088E+01	0
317	0	1.250E+00	1.088E+01	0
318	0	1.875E+00	1.088E+01	0
319	0	2.500E+00	1.088E+01	0
320	0	3.125E+00	1.088E+01	0
321	0	3.750E+00	1.088E+01	0
322	0	4.375E+00	1.088E+01	0
323	0	5.000E+00	1.088E+01	0
324	0	5.625E+00	1.088E+01	0
325	0	6.250E+00	1.088E+01	0
326	0	6.875E+00	1.088E+01	0
327	0	7.500E+00	1.088E+01	0
328	0	8.125E+00	1.088E+01	0
329	0	8.750E+00	1.088E+01	0
330	0	9.375E+00	1.088E+01	0
331	0	1.000E+01	1.088E+01	0
332	1	0.000E+00	1.150E+01	0
333	0	6.250E-01	1.150E+01	0
334	0	1.250E+00	1.150E+01	0
335	0	1.875E+00	1.150E+01	0
336	0	2.500E+00	1.150E+01	0
337	0	3.125E+00	1.150E+01	0
338	0	3.750E+00	1.150E+01	0
339	0	4.375E+00	1.150E+01	0
340	0	5.000E+00	1.150E+01	0

341	0	5.625E+00	1.150E+01	0
342	0	6.250E+00	1.150E+01	0
343	0	6.875E+00	1.150E+01	0
344	0	7.500E+00	1.150E+01	0
345	0	8.125E+00	1.150E+01	0
346	0	8.750E+00	1.150E+01	0
347	0	9.375E+00	1.150E+01	0
348	0	1.000E+01	1.150E+01	0
349	1	0.000E+00	1.213E+01	0
350	0	6.250E-01	1.213E+01	0
351	0	1.250E+00	1.213E+01	0
352	0	1.875E+00	1.213E+01	0
353	0	2.500E+00	1.213E+01	0
354	0	3.125E+00	1.213E+01	0
355	0	3.750E+00	1.213E+01	0
356	0	4.375E+00	1.213E+01	0
357	0	5.000E+00	1.213E+01	0
358	0	5.625E+00	1.213E+01	0
359	0	6.250E+00	1.213E+01	0
360	0	6.875E+00	1.213E+01	0
361	0	7.500E+00	1.213E+01	0
362	0	8.125E+00	1.213E+01	0
363	0	8.750E+00	1.213E+01	0
364	0	9.375E+00	1.213E+01	0
365	0	1.000E+01	1.213E+01	0
366	1	0.000E+00	1.275E+01	0
367	0	6.250E-01	1.275E+01	0
368	0	1.250E+00	1.275E+01	0
369	0	1.875E+00	1.275E+01	0
370	0	2.500E+00	1.275E+01	0
371	0	3.125E+00	1.275E+01	0
372	0	3.750E+00	1.275E+01	0
373	0	4.375E+00	1.275E+01	0
374	0	5.000E+00	1.275E+01	0
375	0	5.625E+00	1.275E+01	0
376	0	6.250E+00	1.275E+01	0
377	0	6.875E+00	1.275E+01	0
378	0	7.500E+00	1.275E+01	0
379	0	8.125E+00	1.275E+01	0
380	0	8.750E+00	1.275E+01	0
381	0	9.375E+00	1.275E+01	0
382	0	1.000E+01	1.275E+01	0
383	1	0.000E+00	1.338E+01	0
384	0	6.250E-01	1.338E+01	0

385	0	1.250E+00	1.338E+01	0
386	0	1.875E+00	1.338E+01	0
387	0	2.500E+00	1.338E+01	0
388	0	3.125E+00	1.338E+01	0
389	0	3.750E+00	1.338E+01	0
390	0	4.375E+00	1.338E+01	0
391	0	5.000E+00	1.338E+01	0
392	0	5.625E+00	1.338E+01	0
393	0	6.250E+00	1.338E+01	0
394	0	6.875E+00	1.338E+01	0
395	0	7.500E+00	1.338E+01	0
396	0	8.125E+00	1.338E+01	0
397	0	8.750E+00	1.338E+01	0
398	0	9.375E+00	1.338E+01	0
399	0	1.000E+01	1.338E+01	0
400	1	0.000E+00	1.400E+01	0
401	0	6.250E-01	1.400E+01	0
402	0	1.250E+00	1.400E+01	0
403	0	1.875E+00	1.400E+01	0
404	0	2.500E+00	1.400E+01	0
405	0	3.125E+00	1.400E+01	0
406	0	3.750E+00	1.400E+01	0
407	0	4.375E+00	1.400E+01	0
408	0	5.000E+00	1.400E+01	0
409	0	5.625E+00	1.400E+01	0
410	0	6.250E+00	1.400E+01	0
411	0	6.875E+00	1.400E+01	0
412	0	7.500E+00	1.400E+01	0
413	0	8.125E+00	1.400E+01	0
414	0	8.750E+00	1.400E+01	0
415	0	9.375E+00	1.400E+01	0
416	0	1.000E+01	1.400E+01	0
417	0	6.250E-01	1.463E+01	0
418	0	1.250E+00	1.463E+01	0
419	0	1.875E+00	1.463E+01	0
420	0	3.125E+00	1.463E+01	0
421	0	3.750E+00	1.463E+01	0
422	0	4.375E+00	1.463E+01	0
423	0	5.625E+00	1.463E+01	0
424	0	6.250E+00	1.463E+01	0
425	0	6.875E+00	1.463E+01	0
426	0	8.125E+00	1.463E+01	0
427	0	8.750E+00	1.463E+01	0
428	0	9.375E+00	1.463E+01	0

429	1	0.000E+00	1.525E+01	0
430	0	1.250E+00	1.525E+01	0
431	0	2.500E+00	1.525E+01	0
432	0	3.750E+00	1.525E+01	0
433	0	5.000E+00	1.525E+01	0
434	0	6.250E+00	1.525E+01	0
435	0	7.500E+00	1.525E+01	0
436	0	8.750E+00	1.525E+01	0
437	0	1.000E+01	1.525E+01	0
438	1	0.000E+00	1.650E+01	0
439	0	1.250E+00	1.650E+01	0
440	0	2.500E+00	1.650E+01	0
441	0	3.750E+00	1.650E+01	0
442	0	5.000E+00	1.650E+01	0
443	0	6.250E+00	1.650E+01	0
444	0	7.500E+00	1.650E+01	0
445	0	8.750E+00	1.650E+01	0
446	0	1.000E+01	1.650E+01	0
447	1	0.000E+00	1.775E+01	0
448	0	1.250E+00	1.775E+01	0
449	0	2.500E+00	1.775E+01	0
450	0	3.750E+00	1.775E+01	0
451	0	5.000E+00	1.775E+01	0
452	0	6.250E+00	1.775E+01	0
453	0	7.500E+00	1.775E+01	0
454	0	8.750E+00	1.775E+01	0
455	0	1.000E+01	1.775E+01	0
456	1	0.000E+00	1.900E+01	0
457	0	1.250E+00	1.900E+01	0
458	0	2.500E+00	1.900E+01	0
459	0	3.750E+00	1.900E+01	0
460	0	5.000E+00	1.900E+01	0
461	0	6.250E+00	1.900E+01	0
462	0	7.500E+00	1.900E+01	0
463	0	8.750E+00	1.900E+01	0
464	0	1.000E+01	1.900E+01	0
465	1	0.000E+00	2.025E+01	0
466	0	1.250E+00	2.025E+01	0
467	0	2.500E+00	2.025E+01	0
468	0	3.750E+00	2.025E+01	0
469	0	5.000E+00	2.025E+01	0
470	0	6.250E+00	2.025E+01	0
471	0	7.500E+00	2.025E+01	0
472	0	8.750E+00	2.025E+01	0

473	0	1.000E+01	2.025E+01	0
474	1	0.000E+00	2.150E+01	0
475	0	1.250E+00	2.150E+01	0
476	0	2.500E+00	2.150E+01	0
477	0	3.750E+00	2.150E+01	0
478	0	5.000E+00	2.150E+01	0
479	0	6.250E+00	2.150E+01	0
480	0	7.500E+00	2.150E+01	0
481	0	8.750E+00	2.150E+01	0
482	0	1.000E+01	2.150E+01	0
483	1	0.000E+00	2.275E+01	0
484	0	1.250E+00	2.275E+01	0
485	0	2.500E+00	2.275E+01	0
486	0	3.750E+00	2.275E+01	0
487	0	5.000E+00	2.275E+01	0
488	0	6.250E+00	2.275E+01	0
489	0	7.500E+00	2.275E+01	0
490	0	8.750E+00	2.275E+01	0
491	0	1.000E+01	2.275E+01	0
492	1	0.000E+00	2.400E+01	0
493	0	1.250E+00	2.400E+01	0
494	0	2.500E+00	2.400E+01	0
495	0	3.750E+00	2.400E+01	0
496	0	5.000E+00	2.400E+01	0
497	0	6.250E+00	2.400E+01	0
498	0	7.500E+00	2.400E+01	0
499	0	8.750E+00	2.400E+01	0
500	0	1.000E+01	2.400E+01	0
501	1	0.000E+00	2.525E+01	0
502	0	1.250E+00	2.525E+01	0
503	0	2.500E+00	2.525E+01	0
504	0	3.750E+00	2.525E+01	0
505	0	5.000E+00	2.525E+01	0
506	0	6.250E+00	2.525E+01	0
507	0	7.500E+00	2.525E+01	0
508	0	8.750E+00	2.525E+01	0
509	0	1.000E+01	2.525E+01	0
510	1	0.000E+00	2.650E+01	0
511	0	1.250E+00	2.650E+01	0
512	0	2.500E+00	2.650E+01	0
513	0	3.750E+00	2.650E+01	0
514	0	5.000E+00	2.650E+01	0
515	0	6.250E+00	2.650E+01	0
516	0	7.500E+00	2.650E+01	0

517	0	8.750E+00	2.650E+01	0
518	0	1.000E+01	2.650E+01	0
519	1	0.000E+00	2.775E+01	0
520	0	1.250E+00	2.775E+01	0
521	0	2.500E+00	2.775E+01	0
522	0	3.750E+00	2.775E+01	0
523	0	5.000E+00	2.775E+01	0
524	0	6.250E+00	2.775E+01	0
525	0	7.500E+00	2.775E+01	0
526	0	8.750E+00	2.775E+01	0
527	0	1.000E+01	2.775E+01	0
528	1	0.000E+00	2.900E+01	0
529	0	1.250E+00	2.900E+01	0
530	0	2.500E+00	2.900E+01	0
531	0	3.750E+00	2.900E+01	0
532	0	5.000E+00	2.900E+01	0
533	0	6.250E+00	2.900E+01	0
534	0	7.500E+00	2.900E+01	0
535	0	8.750E+00	2.900E+01	0
536	0	1.000E+01	2.900E+01	0
537	1	0.000E+00	3.025E+01	0
538	0	1.250E+00	3.025E+01	0
539	0	2.500E+00	3.025E+01	0
540	0	3.750E+00	3.025E+01	0
541	0	5.000E+00	3.025E+01	0
542	0	6.250E+00	3.025E+01	0
543	0	7.500E+00	3.025E+01	0
544	0	8.750E+00	3.025E+01	0
545	0	1.000E+01	3.025E+01	0
546	1	0.000E+00	3.150E+01	0
547	0	1.250E+00	3.150E+01	0
548	0	2.500E+00	3.150E+01	0
549	0	3.750E+00	3.150E+01	0
550	0	5.000E+00	3.150E+01	0
551	0	6.250E+00	3.150E+01	0
552	0	7.500E+00	3.150E+01	0
553	0	8.750E+00	3.150E+01	0
554	0	1.000E+01	3.150E+01	0
555	1	0.000E+00	3.275E+01	0
556	0	1.250E+00	3.275E+01	0
557	0	2.500E+00	3.275E+01	0
558	0	3.750E+00	3.275E+01	0
559	0	5.000E+00	3.275E+01	0
560	0	6.250E+00	3.275E+01	0

561	0	7.500E+00	3.275E+01	0
562	0	8.750E+00	3.275E+01	0
563	0	1.000E+01	3.275E+01	0
564	1	0.000E+00	3.400E+01	0
565	0	1.250E+00	3.400E+01	0
566	0	2.500E+00	3.400E+01	0
567	0	3.750E+00	3.400E+01	0
568	0	5.000E+00	3.400E+01	0
569	0	6.250E+00	3.400E+01	0
570	0	7.500E+00	3.400E+01	0
571	0	8.750E+00	3.400E+01	0
572	0	1.000E+01	3.400E+01	0
573	0	1.250E+00	3.613E+01	0
574	0	2.500E+00	3.613E+01	0
575	0	3.750E+00	3.613E+01	0
576	0	6.250E+00	3.613E+01	0
577	0	7.500E+00	3.613E+01	0
578	0	8.750E+00	3.613E+01	0
579	1	0.000E+00	3.825E+01	0
580	0	2.500E+00	3.825E+01	0
581	0	5.000E+00	3.825E+01	0
582	0	7.500E+00	3.825E+01	0
583	0	1.000E+01	3.825E+01	0
584	1	0.000E+00	4.250E+01	0
585	0	2.500E+00	4.250E+01	0
586	0	5.000E+00	4.250E+01	0
587	0	7.500E+00	4.250E+01	0
588	0	1.000E+01	4.250E+01	0
589	1	0.000E+00	4.675E+01	0
590	0	2.500E+00	4.675E+01	0
591	0	5.000E+00	4.675E+01	0
592	0	7.500E+00	4.675E+01	0
593	0	1.000E+01	4.675E+01	0
594	1	0.000E+00	5.100E+01	0
595	0	2.500E+00	5.100E+01	0
596	0	5.000E+00	5.100E+01	0
597	0	7.500E+00	5.100E+01	0
598	0	1.000E+01	5.100E+01	0
599	1	0.000E+00	5.525E+01	0
600	0	2.500E+00	5.525E+01	0
601	0	5.000E+00	5.525E+01	0
602	0	7.500E+00	5.525E+01	0
603	0	1.000E+01	5.525E+01	0
604	1	0.000E+00	5.950E+01	0

561	0	7.500E+00	3.275E+01	0
562	0	8.750E+00	3.275E+01	0
563	0	1.000E+01	3.275E+01	0
564	1	0.000E+00	3.400E+01	0
565	0	1.250E+00	3.400E+01	0
566	0	2.500E+00	3.400E+01	0
567	0	3.750E+00	3.400E+01	0
568	0	5.000E+00	3.400E+01	0
569	0	6.250E+00	3.400E+01	0
570	0	7.500E+00	3.400E+01	0
571	0	8.750E+00	3.400E+01	0
572	0	1.000E+01	3.400E+01	0
573	0	1.250E+00	3.613E+01	0
574	0	2.500E+00	3.613E+01	0
575	0	3.750E+00	3.613E+01	0
576	0	6.250E+00	3.613E+01	0
577	0	7.500E+00	3.613E+01	0
578	0	8.750E+00	3.613E+01	0
579	1	0.000E+00	3.825E+01	0
580	0	2.500E+00	3.825E+01	0
581	0	5.000E+00	3.825E+01	0
582	0	7.500E+00	3.825E+01	0
583	0	1.000E+01	3.825E+01	0
584	1	0.000E+00	4.250E+01	0
585	0	2.500E+00	4.250E+01	0
586	0	5.000E+00	4.250E+01	0
587	0	7.500E+00	4.250E+01	0
588	0	1.000E+01	4.250E+01	0
589	1	0.000E+00	4.675E+01	0
590	0	2.500E+00	4.675E+01	0
591	0	5.000E+00	4.675E+01	0
592	0	7.500E+00	4.675E+01	0
593	0	1.000E+01	4.675E+01	0
594	1	0.000E+00	5.100E+01	0
595	0	2.500E+00	5.100E+01	0
596	0	5.000E+00	5.100E+01	0
597	0	7.500E+00	5.100E+01	0
598	0	1.000E+01	5.100E+01	0
599	1	0.000E+00	5.525E+01	0
600	0	2.500E+00	5.525E+01	0
601	0	5.000E+00	5.525E+01	0
602	0	7.500E+00	5.525E+01	0
603	0	1.000E+01	5.525E+01	0
604	1	0.000E+00	5.950E+01	0

605	0	2.500E+00	5.950E+01	0	
606	0	5.000E+00	5.950E+01	0	
607	0	7.500E+00	5.950E+01	0	
608	0	1.000E+01	5.950E+01	0	
609	1	0.000E+00	6.375E+01	0	
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612	0	7.500E+00	6.375E+01	0	
613	0	1.000E+01	6.375E+01	0	
614	1	0.000E+00	6.800E+01	0	
615	0	2.500E+00	6.800E+01	0	
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618	0	1.000E+01	6.800E+01	0	
619	0	8.750E+00	6.588E+01	0	
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563	626	639	637	625	1		
564	640	641	637	639	1		
565	629	632	633	630	1		
566	632	635	636	633	1		
567	635	637	638	636	1		
568	637	641	642	638	1		
1		0.0	-528.0			1	
642		0.0	-528.0				
17		0.0	0.0			0.0	1.0
1	1						
2	6						
3	11						
4	16						
5	21						
6	26						
7	31						

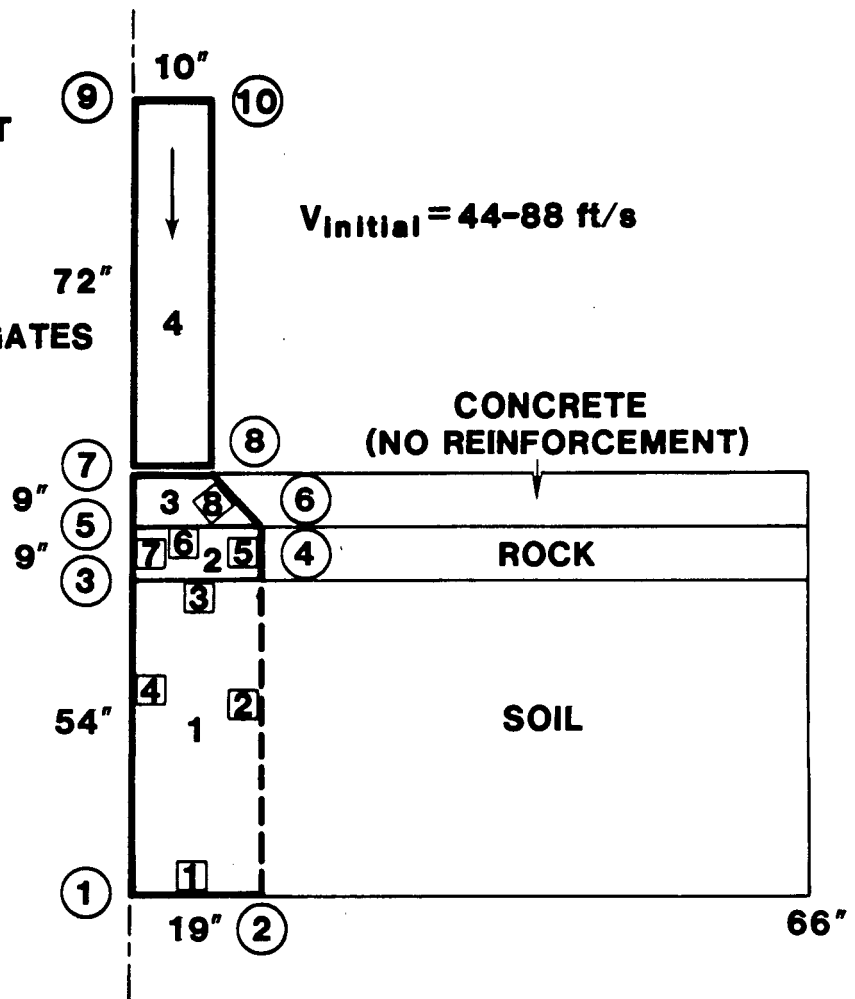
568	637	641	642	638	1	
1		0.0	-528.0			1
642		0.0	-528.0			
17		0.0	0.0		0.0	1.0
1	1					
2	6					
3	11					
4	16					
5	21					
6	26					
7	31					
8	36					
9	41					
10	46					
11	51					
12	56					
13	61					
14	66					
15	71					
16	76					
17	81					

[EOB]

Finite Element Input
for Concrete Highway Target
Analysis into PRONTO-2D Code

ASSUME:

- NO SIGNIFICANT ENERGY IS ABSORBED BY CRACK GENERATION
- CRACK PROPAGATES AT 45° ANGLE
- $\mu_{\text{rock}} \approx \mu_{\text{soil}}$



INITIAL VELOCITY ft/s	44 ft/s	66 ft/s	88 ft/s
MAXIMUM DISPLACEMENT (inches)	16.4	25.2	34.8
MAXIMUM ACCELERATION (g's)	37.2	55.0	71.8
AVERAGE ACCELERATION (g's)	22.0	32.2	41.5
MAXIMUM AVERAGE ACCELERATION	1.69	1.71	1.73

CONCRETE PROPERTIES

E (psi)	2.50×10^6
G (psi)	1.06×10^6 ($2.12 \times 10^6 = 2\mu$)
B (psi)	1.30×10^6
σ_t (psi)	250
σ_c (psi)	3500 (C_o)
ν	0.18
α	20°
μ (tan α)	0.364

$$f(\sigma_{eff}): \quad 2600 a_0$$

$$0.772 a_1$$

p_m	$\ln (1-p_m/B)$
0	0
5000	0.00385
10000	0.00772
20000	0.01550

$$S_o = \frac{C_o}{2 [\mu^2 + 1]^{1/2} + \mu} = \frac{3500}{2 [1.418]} = 1225 \text{ psi cohesion}$$

$$\sigma_1 = 3500, \sigma_2 = \sigma_3 = 0$$

$$J_2 = \frac{1}{6} [(\sigma_1 - \sigma_2)^2 + (\sigma_2 - \sigma_3)^2 + (\sigma_3 - \sigma_1)^2] = \frac{1}{3} \sigma_y = 4.083 \times 10^6$$

$$\sigma_y = 3500 \quad P_m = 1166.7$$

for

$$\sigma_2 = \sigma_3 = \sigma_{\max} = 5000 \text{ psi}$$

$$\sigma_1 = \frac{\sigma_{\max} [\mu^2 + 1]^{1/2} + \mu}{[(\mu^2 + 1)^{1/2} - \mu]} - 2S_o = \frac{-5000(1.428) - 2450}{(0.7002)}$$

$$\sigma_1 = -13,696 \text{ psi}$$

$$J_2 = \frac{1}{6} [8696^2 + 8696^2] = 25.2 \times 10^6$$

$$\sigma_y = 8696 \text{ psi} \quad \text{pm} = 7898.7$$

$$\begin{bmatrix} 1 & 1166.7 \\ 1 & 7898.7 \end{bmatrix} \begin{Bmatrix} a_0 \\ a_1 \end{Bmatrix} = \begin{Bmatrix} 3500 \\ 8696 \end{Bmatrix}$$

$$a_0 = 2500$$

$$a_1 = 0.772$$

$$G = \frac{E}{2(1 + \nu)} = 1.06 \times 10^6 \text{ psi}$$

$$B = \frac{E}{3(1 - 2\nu)} = 1.30 \times 10^6 \text{ psi}$$

Finite Element Input
for Soil Analysis
into PRONTO-2D Code


```

MIN .PROC .120.
USER .MNEILS .}PASSWORD{
CHARGE(8950433)
ACCESS .DN=$PROC .PDN=PROCS .ID=ACCLIB
ACCESS .DN=XPROC .PDN=PROCS .ID=DPFLANA.
ASSIGN .DN=TAPE11 .A=FT11
LIBRARY .DN=* XPROC.
FASTQ
FRONT02.
SAVE .DN=TAPE11 .PDN=PRO66.
EXIT
BFTOV1,FILE=TAPE11.

```

TITLE

TARGET HARDNESS MODEL 1

POINT	1	0.000E+00	0.000E+00
POINT	2	1.000E+01	0.000E+00
POINT	3	0.000E+01	6.000E+01
POINT	4	1.000E+01	6.000E+01
POINT	5	0.000E+01	7.200E+01
POINT	6	1.000E+01	7.200E+01
POINT	7	0.000E+01	8.400E+01
POINT	8	1.000E+01	8.400E+01
POINT	9	0.000E+01	9.600E+01
POINT	10	1.000E+01	9.600E+01
POINT	11	0.000E+00	1.080E+02
POINT	12	1.000E+01	1.080E+02
POINT	13	0.000E+01	1.200E+02
POINT	14	1.000E+01	1.200E+02
POINT	15	0.000E+01	1.920E+02
POINT	16	1.000E+01	1.920E+02
LINE	1	STR 1 2	0 5 1.0000
LINE	2	STR 2 4	0 30 1.0000
LINE	3	STR 4 3	0 5 1.0000
LINE	4	STR 3 1	0 30 1.0000
LINE	5	STR 4 6	0 6 1.0000
LINE	6	STR 6 5	0 5 1.0000
LINE	7	STR 5 3	0 6 1.0000
LINE	8	STR 6 8	0 6 1.0000
LINE	9	STR 8 7	0 5 1.0000
LINE	10	STR 7 5	0 6 1.0000
LINE	11	STR 8 10	0 6 1.0000
LINE	12	STR 10 9	0 5 1.0000
LINE	13	STR 9 7	0 6 1.0000
LINE	14	STR 10 12	0 6 1.0000
LINE	15	STR 12 11	0 5 1.0000
LINE	16	STR 11 9	0 6 1.0000
LINE	17	STR 12 14	0 6 1.0000
LINE	18	STR 14 13	0 5 1.0000
LINE	19	STR 13 11	0 6 1.0000
LINE	20	STR 14 16	0 18 1.0000
LINE	21	STR 16 15	0 5 1.0000
LINE	22	STR 15 13	0 18 1.0000
REGION	1	1 -1 -2	-3 -4
REGION	2	2 -3 -5	-6 -7
REGION	3	3 -6 -8	-9 -10
REGION	4	4 -9 -11	-12 -13
REGION	5	5 -12 -14	-15 -16
REGION	6	6 -15 -17	-18 -19
REGION	7	7 -18 -20	-21 -22
SCHEME	1	M	
SCHEME	2	M	
SCHEME	3	M	
SCHEME	4	M	
SCHEME	5	M	
SCHEME	6	M	
SCHEME	7	M	
BODY	1	2 3 4	5 6 7
LINEBC	1	4 7 10	13 16 19 22
LINEBC	2	1	
SIDEBC	3	2	
SIDEBC	4	5	
SIDEBC	5	8	

SIDEBC	8	11
SIDEBC	7	14
SIDEBC	8	17
EXIT		

TITLE
TARGET HARDNESS - SLIDE 66 FPS - B = 2000 psi
AXISYMMETRIC
TERM TIME.0.040
OUTPUT TIME.0.0002
PLOT TIME.0.0002
PLOT ELEMENT. STRESS. ENERGY. PRESSURE
NO DISPL. X, 1
NO DISPL. Y, 2
INITIAL VEL MAT, 7, 0.0, -792.0
RIGID SURFACE, 3, 10., 0, -1., 0.0.488
RIGID SURFACE, 4, 10., 0, -1., 0.0.509
RIGID SURFACE, 5, 10., 0, -1., 0.0.532
RIGID SURFACE, 6, 10., 0, -1., 0.0.532
RIGID SURFACE, 7, 10., 0, -1., 0.0.675
RIGID SURFACE, 8, 10., 0, -1., 0.0.675
FUNCTION, 10
0.0
0.0513, 100.
0.1054, 200.
0.1625, 300.
0.2231, 400.
0.2877, 500.
0.3567, 600.
END
MATERIAL, 1, SOIL N FOAMS, 1.5-4
TWO MU, 2400.
BULK MODULUS, 2000.
A0, 8.551
A1, 1.027
A2, 0
FUNCTION ID, 10
END
MATERIAL, 2, SOIL N FOAMS, 1.5-4
TWO MU, 2400.
BULK MODULUS, 2000.
A0, 8.686
A1, 1.070
A2, 0
FUNCTION ID, 10
END
MATERIAL, 3, SOIL N FOAMS, 1.5-4
TWO MU, 2400.
BULK MODULUS, 2000.
A0, 8.805
A1, 1.113
A2, 0
FUNCTION ID, 10
END
MATERIAL, 4, SOIL N FOAMS, 1.5-4
TWO MU, 2400.
BULK MODULUS, 2000.
A0, 10.818
A1, 1.113
A2, 0
FUNCTION ID, 10
END
MATERIAL, 5, SOIL N FOAMS, 1.33-4
TWO MU, 2400.
BULK MODULUS, 2000.

A0.6.772
A1.1.375
A2.0
FUNCTION ID.10
END
MATERIAL.6,SOIL N FOAMS,1.33-4
TWO MP.2400.
BULK MODULUS.2000.
A0.6.772
A1.1.375
A2.0
FUNCTION ID.10
END
MATERIAL.7,ELASTIC,6.74-4
YOUNGS MODULUS,29.+6
POISSONS RATIO,0.300
END
EXIT

PLANTS INPUT
BY COMPUTER
FILE 11.11.11

TITLE
TARGET HARDNESS - SLIDE 66 FPS - M = 0.500
AXISYMMETRIC
TERM TIME 0.040
OUTPUT TIME 0.0002
PLOT TIME 0.0002
PLOT ELEMENT STRESS ENERGY PRESSURE
NO DISPL X 1
NO DISPL Y 2
INITIAL VEL MAT 7.0.0.-792.0
RIGID SURFACE 3,10.,0,-1.,0,0.500
RIGID SURFACE 4,10.,0,-1.,0,0.500
RIGID SURFACE 5,10.,0,-1.,0,0.500
RIGID SURFACE 6,10.,0,-1.,0,0.500
RIGID SURFACE 7,10.,0,-1.,0,0.500
RIGID SURFACE 8,10.,0,-1.,0,0.500
FUNCTION,10
0,0
0.0513,100.
0.1054,200.
0.1625,300.
0.2231,400.
0.2877,500.
0.3567,600.
END
MATERIAL,1,SOIL N FOAMS,1.5-4
TWO MU,2400.
BULK MODULUS,2000.
A0,8.551
A1,1.027
A2,0
FUNCTION ID,10
END
MATERIAL,2,SOIL N FOAMS,1.5-4
TWO MU,2400.
BULK MODULUS,2000.
A0,8.686
A1,1.070
A2,0
FUNCTION ID,10
END
MATERIAL,3,SOIL N FOAMS,1.5-4
TWO MU,2400.
BULK MODULUS,2000.
A0,8.805
A1,1.113
A2,0
FUNCTION ID,10
END
MATERIAL,4,SOIL N FOAMS,1.5-4
TWO MU,2400.
BULK MODULUS,2000.
A0,10.818
A1,1.113
A2,0
FUNCTION ID,10
END
MATERIAL,5,SOIL N FOAMS,1.33-4
TWO MU,2400.
BULK MODULUS,2000.

A0,6.772
A1,1.375
A2,0
FUNCTION ID,10
END
MATERIAL,6,SOIL N FOAMS,1 33-4
TWO MU,2400.
BULK MODULUS,2000.
A0,6.772
A1,1.375
A2,0
FUNCTION ID,10
END
MATERIAL,7,ELASTIC,6.74-4
YOUNGS MODULUS,29.+6
POISSONS RATIO,0.300
END
EXIT

Finite Element Input
for Soil Analysis
into DYNA2D Code

MFNEILS.T600.STSCZ. MFNEILS. BOX 440
USER.MFNEILS, {PASSWORD}
CHARGE.8950433.
ACCESS.DN=\$PROC.PDN=PROCS.ID=ACCLIB.
ASSIGN.DN=TAPE10.A=FT10.
QMESH.
RENAM
* QPLOT.DEV=HC1.SITE=R0
*
ACCESS.DN=RSCALE.PDN=RSCALE.
*
DYNA2D.C=RSCALE.
* .DYNA2D.
REWIND.DN=TAPE10.
SAVE.DN=TAPE10.PDN=PEN66.RT=21.
* .SAVE.DN=DUMPFL.PDN=PRST66.RT=21.
*
AUDIT.ID=MKNEILS.
*
EXIT.
REWIND.DN=TAPE10.
SAVE.DN=TAPE10.PDN=PEN66.RT=5.
*
AUDIT.ID=MKNEILS.

.DAT

TARGET HARDNESS - RUN 2 - 60 FPS

ND	6	-2	0	0	0	0	0.00	0.05	0.01
	0	0	0	0	0	1	0	0	0
		050		0010		0010			
	1	5		1.50E-04					

TARGET MATERIAL 60+

1	200E+03	2	000E+03	2	430E+01	5	850E+00	3	510E-01
0	000E+00	0	000E+00	0	513E-01	1	000E+02		
1	625E-01	3	000E+02	3	567E-01	6	000E+02		

2 5 1.50E-04

TARGET MATERIAL 48-60

1	200E+03	2	000E+03	2	510E+01	6	200E+00	3	810E-01
0	000E+00	0	000E+00	0	513E-01	1	000E+02		
1	625E-01	3	000E+02	3	567E-01	6	000E+02		

3 5 1.50E-04

TARGET MATERIAL 36-48

1	200E+03	2	000E+03	2	580E+01	6	530E+00	4	130E-01
0	000E+00	0	000E+00	0	513E-01	1	000E+02		
1	625E-01	3	000E+02	3	567E-01	6	000E+02		

4 5 1.50E-04

TARGET MATERIAL 24-36

1	200E+03	2	000E+03	3	900E+01	8	030E+00	4	130E-01
0	000E+00	0	000E+00	0	513E-01	1	000E+02		
1	625E-01	3	000E+02	3	567E-01	6	000E+02		

5 5 1.33E-04

TARGET MATERIAL 0-24

1	200E+03	2	000E+03	1	530E+01	6	210E+00	6	300E-01
0	000E+00	0	000E+00	0	513E-01	1	000E+02		
1	625E-01	3	000E+02	3	567E-01	6	000E+02		

6 1 6.74E-04

STEEL CASK

2.900E+07
3.000E-01

BCC	1.	1.
BCC	2.	2.
1	0.	0.000
500	0.	0.000
501	0.	-792.
504	0.	-792.
505	0.	0.000
525	0.	0.000

526	0.	-792		
573	0.	-792		
573	0.	0.	0.	10
1	1			
573	573			

OMEN	TARGET	HARDNESS	MODEL 1
OINT	1/	0.0000	0.0000
OINT	2/	80.0000	0.0000
OINT	3/	0.0000	60.0000
OINT	4/	80.0000	60.0000
OINT	5/	0.0000	72.0000
OINT	6/	80.0000	72.0000
OINT	7/	0.0000	84.0000
OINT	8/	80.0000	84.0000
OINT	9/	0.0000	96.0000
OINT	10/	80.0000	96.0000
OINT	11/	0.0000	120.0000
OINT	12/	10.0000	120.0000
OINT	13/	80.0000	120.0000
OINT	14/	0.0000	192.0000
OINT	15/	10.0000	192.0000
INE STR	1/	1	2
INE STR	2/	2	4
INE STR	3/	4	3
INE STR	4/	3	1
INE STR	5/	4	6
INE STR	6/	6	5
INE STR	7/	5	3
INE STR	8/	6	8
INE STR	9/	8	7
INE STR	10/	7	5
INE STR	11/	8	10
INE STR	12/	10	9
INE STR	13/	9	7
INE STR	14/	10	13
INE STR	15/	13	12
INE STR	16/	12	11
INE STR	17/	11	9
INE STR	18/	12	15
INE STR	19/	15	14
INE STR	20/	14	11
IDE	1/	15	16
EGION 1	1/	-1	-2
EGION 2	2/	-3	-5
EGION 3	3/	-6	-8
EGION 4	4/	-9	-11
EGION 5	5/	-12	-14
EGION 6	6/	-16	-18
CHEME	1M		
CHEME	2M		
CHEME	3M		
CHEME	4M		
CHEME	5M		
CHEME	6M		
ODY	/	1	2
ND	4		
EOR{	1	1	2
-L-			