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**Studies of a Flexible Heliac
Configuration**

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Fusion Energy Division

STUDIES OF A FLEXIBLE HELIAC CONFIGURATION

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ABSTRACT

This paper documents a detailed study of the Flexible Heliac configuration. The remarkable flexibility of this device — which allows variation of the rotational transform, shear, and magnetic well depth over a relatively wide range — is described. Engineering considerations of error fields, finite cross-section conductors, and plasma coil clearances are also discussed.

I. INTRODUCTION

The Flexible Heliac^{1,2} (Fig. 1) consists of a toroidally directed central conductor, with a close-fitting $\ell = 1$ winding wrapped around it, and a set of toroidal field (TF) coils whose centers describe a helix that is concentric with the $\ell = 1$ winding; a set of outboard vertical field (VF) coils is also required for horizontal positioning. This coil set produces “bean-shaped” flux surfaces that follow the helical motion of the TF coils about the central conductors. A typical set of flux surfaces for the 4-field-period reference configuration described in this paper is shown in Fig. 2. It is the $\ell = 1$ winding that distinguishes the Flexible Heliac from the standard Heliac³ and leads to the great flexibility in the device.

The Heliac has been found to have very favorable stability properties in the infinite-aspect-ratio, helically symmetric limit.⁴ At finite aspect ratio, however, the high values of rotational transform per field period (τ/M) inherent to the Heliac can lead to equilibrium problems: the beating of the pressure-induced, toroidal Shafranov shift with the helical harmonics may produce resonant or nearly resonant harmonics that can distort or destroy the flux surfaces.⁵ Such resonant effects

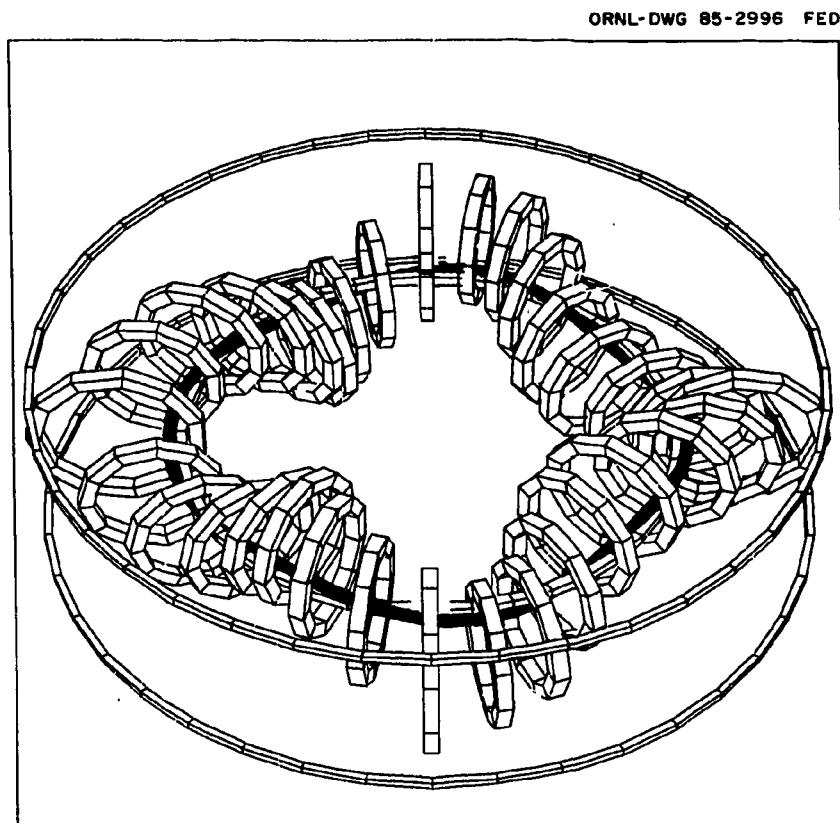


Fig. 1. Coil set for 4-field-period Flexible Heliac.

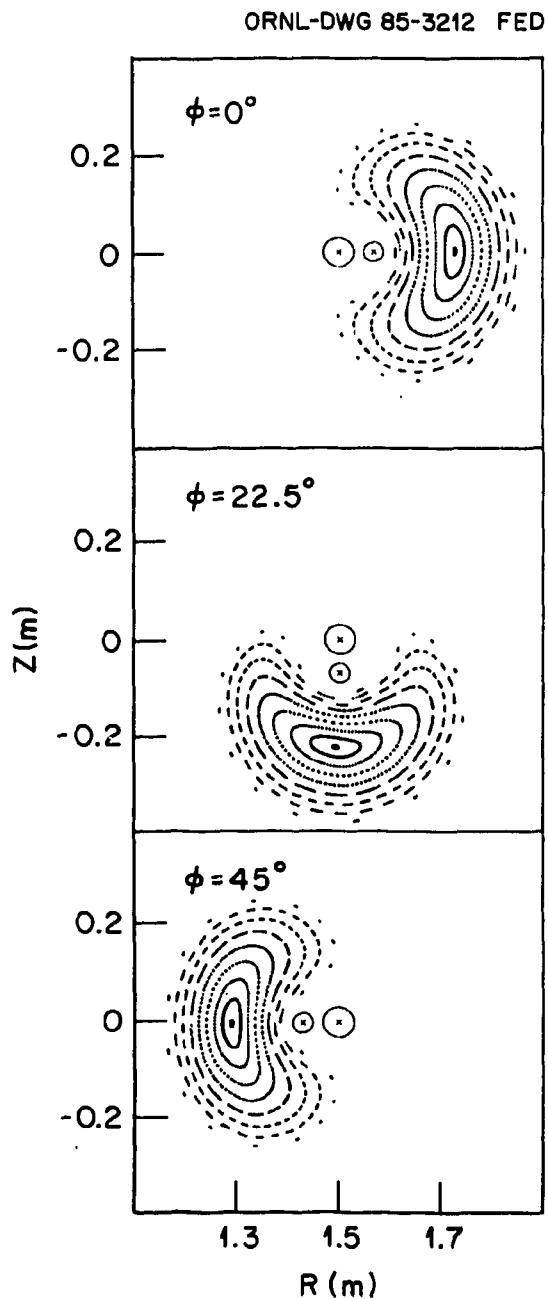


Fig. 2. Typical flux surfaces at four toroidal angles for the reference configuration.

are particularly pronounced when the plasma contains, or has nearby, low-order resonant surfaces.⁶ It is thus very important for a Heliac experiment to have sufficient control over the rotational transform and shear to avoid the low-order resonances. Conversely, it will also be interesting to examine plasma properties in the vicinity of low-order resonances in the hope of improving theoretical understanding.

There are some theoretical indications that the magnetic well depth may play an important role in determining the growth and magnitude of the equilibrium-induced resonant harmonics.⁷ It is thus also desirable to be able to vary the magnetic well depth.

The Flexible Heliac satisfies these requirements for independent variation of the rotational transform, shear, and magnetic well depth. The concept has already undergone a basic test in low-temperature plasma experiments on the prototype SHEILA device,⁸ which showed that the $\ell = 1$ winding can be effectively used to control the rotational transform so as to avoid the most dangerous low-order resonances. The reference configuration described here was chosen for study because it permits variation of the rotational transform over a wide range ($0.15 \lesssim \tau/M \lesssim 0.8$); at fixed values of τ , the shear and magnetic well depth may also be varied to a more limited extent. This particular configuration has been used as a basis for the design of the TJ-II Flexible Heliac,⁹ which is proposed to be constructed in Madrid (Spain). Similar features are being incorporated in the H-1 device under construction in Canberra (Australia).⁸

The parameter scans and external constraints that led to the choice of the reference configuration are briefly described in Sec. II. The physics properties of the reference case are explored in detail in Sec. III. Practical studies of error fields, the effects of finite cross-section conductors, and plasma coil clearances are described in Sec. IV. A summary is given in Sec. V.

II. CONFIGURATION SCANS

As discussed in Sec. I, one of the chief theoretical concerns in the Heliac relates to the possibility that equilibrium flux surfaces may be destroyed at finite beta.⁵ This flux surface destruction arises from resonant or nearly resonant magnetic perturbations, which are generated by the nonlinear beatings of the toroidal and helical shifts (and by subsequent higher order beatings).

Since the helical curvature is intrinsic to the Heliac, the only way to reduce the magnitude of nonlinearly driven resonant fields (and thus the improve the equilibrium beta limit) is to reduce the toroidal shift. At relatively tight aspect ratios ($\lesssim 10$), this can be done by increasing the number of field periods and/or the aspect ratio.¹⁰ Thus, from an equilibrium viewpoint it is clear that a large aspect ratio and a large number of field periods are desirable. However, cost constraints (which must be kept in mind for a practical design) act in the opposite direction and favor a small aspect ratio and number of field periods; a compromise is thus necessary. The chosen reference configuration has four field periods and a major radius of 1.5 m,

which permits plasmas with an average radius of up to 25 cm and betas of at least 8%. Increasing the number of field periods and the coil aspect ratio proportionally improves the equilibrium properties linearly, but of course this leads to a reduction in the plasma minor radius (for fixed R). Similarly, increasing only the number of field periods improves the equilibrium properties but reduces the minor radius. Another problem with increasing the number of field periods beyond four is that access for heating and diagnostics is seriously reduced.

The swing radius of the TF coils sets the optimum ϵ range for the Heliac. Holding all other parameters fixed while increasing the TF coil swing radius decreases ϵ/M , and, conversely, reducing the swing radius raises ϵ/M . The chosen swing radius, $r_S = 28$ cm, leads to optimum plasma volumes near $\epsilon/M \sim 0.4$, although varying the relative currents in the circular and helical hardcore windings allows wide variations of ϵ/M about this “optimum” value. A lower bound on the swing radius of the helical hardcore (r_{hc}) is imposed by the cross-sectional areas of the two central conductors, which are necessary to carry the required currents. For the reference value of $r_{hc} = 7$ cm, each conductor can carry up to 300 kA. This assumes that the helical conductor is tightly wrapped on the central conductor and that each has a 3.5-cm radius. Increasing the swing radius of the helical conductor improves the efficiency with which the required helical fields are generated. However, there is at best limited clearance between the $\ell = 1$ (helical hardcore) winding and the plasma, and some form of limiter may be necessary to protect the winding for some of the variations that can be achieved with the reference configuration. Increasing the $\ell = 1$ winding swing radius further would reduce the plasma-coil clearance and limit the plasma minor radius even more.

The effects of varying the radii of the TF coils while holding all other parameters fixed are shown in Fig. 3. For coil radii less than 40 cm, the plasma-coil clearances at the tips of the plasma “bean” are insufficient, while for radii much greater than 40 cm there is a slow decrease in plasma radius.

The configuration properties are weakly dependent on the number of TF coils per field period. Increasing the number of TF coils yields a slow improvement in flux surface quality and plasma minor radius (Fig. 4) and also leads to deeper magnetic wells (Fig. 5). Eight coils per field period were chosen as a compromise between physics properties, plasma access, and engineering feasibility.

To summarize, the parameters for the reference configuration were selected on the basis of systematic single-parameter scans about an $R = 1.5$ m, 4-field-period case. The chosen configuration consists of 32 TF coils that are helically displaced by 28 cm from the hardcore winding, with the winding law $\theta = 4\phi$. The hardcore itself is composed of a circular coil of 1.5 m radius and a helical $\ell = 1$ winding that follows the same winding law as the TF coils, but with a smaller, 7-cm swing radius. The nominal toroidal field is taken to be 1 T, which is consistent with requirements for electron cyclotron resonance heating (ECRH) at 28 GHz (fundamental) and 56 GHz (second harmonic). The two outboard VF coils located at $R = 2.25$ m and

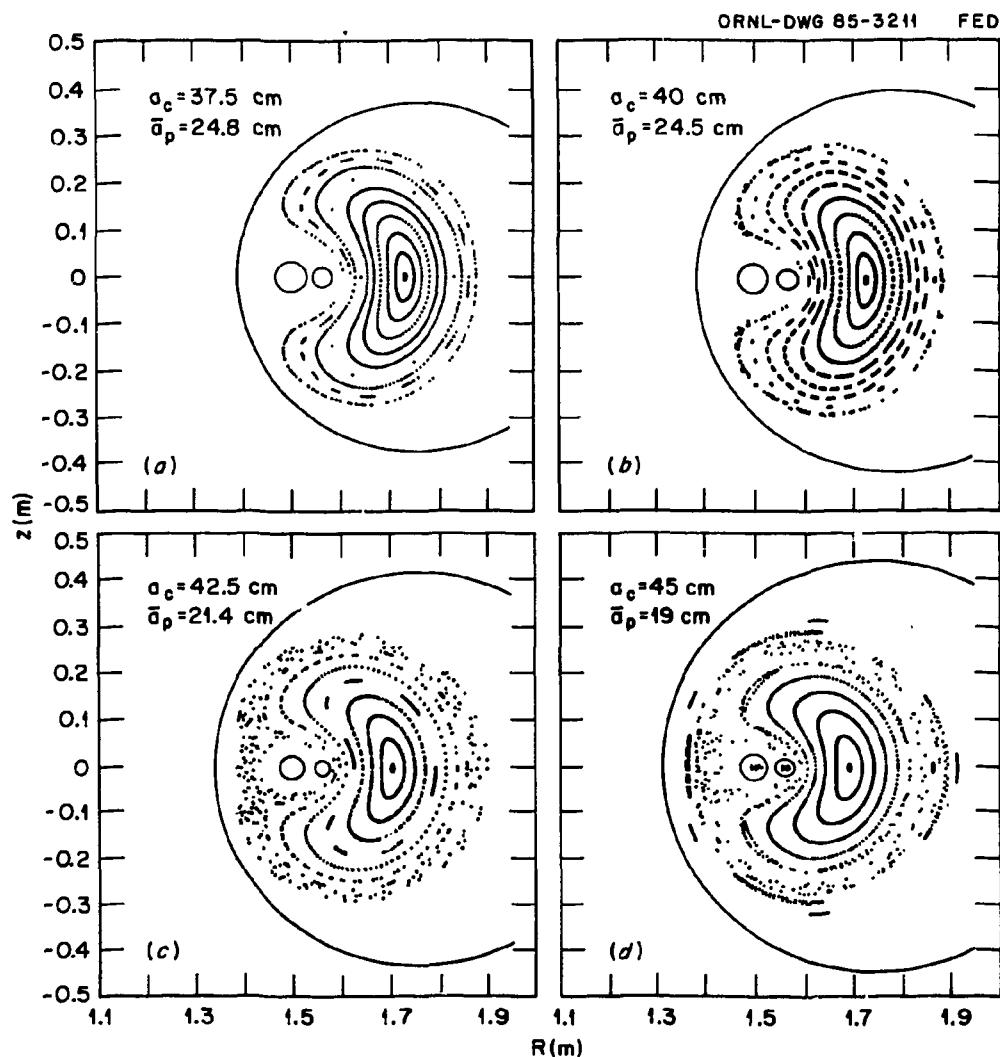


Fig. 3. Effect of varying the TF coil radius (a_c) on the average plasma radius (\bar{r}_p).

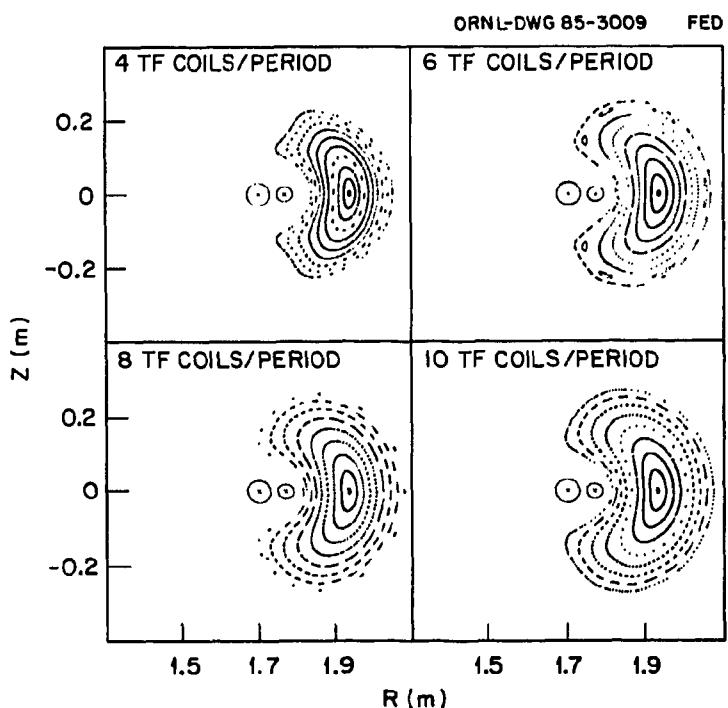


Fig. 4. Effect of increasing the number of TF coils per field period on flux surface quality.

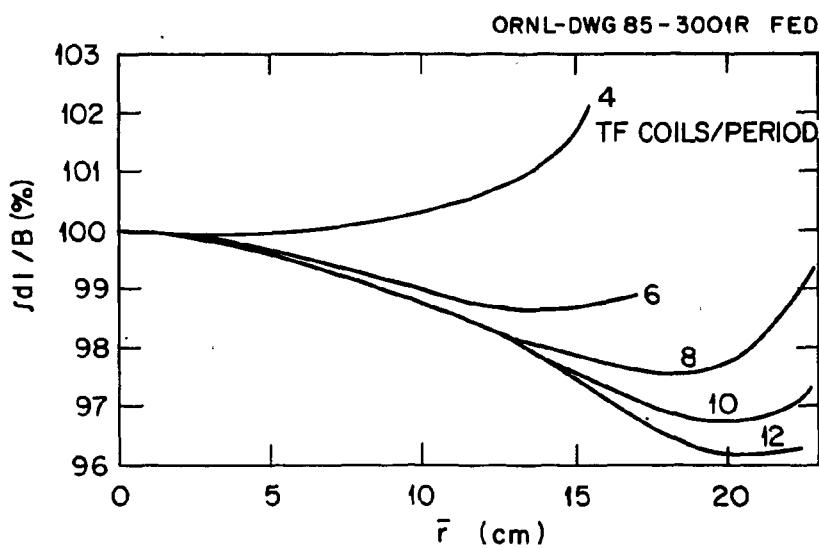


Fig. 5. Effect of increasing the number of TF coils per field period on the magnetic well depth.

$z = \pm 0.4$ m are required to position the plasma and contribute vertical fields of $\sim 5\%$ of the toroidal field strength. The parameters for the reference configuration are summarized in Table I.

TABLE I
Reference Configuration Parameters

Winding law	$\theta = 4\phi$
Major radius	1.5 m
TF coil radius	0.4 m
TF coil swing radius	0.28 m
$\ell = 1$ winding swing radius	0.07 m
VF coil location	$R = 2.25$ m, $Z = \pm 0.4$ m
Maximum central coil current	300 kA
Nominal TF coil current	234 kA
VF coil current range	60–100 kA

III. PHYSICS PROPERTIES

The physics properties of the configuration detailed in Sec. II (and Table I) are described.

Figure 6 illustrates the remarkable flexibility that is achievable in the reference configuration. It shows contours of constant central rotational transform per field period (ε_0/M) as a function of the central conductor current (I_{cc}) and helical conductor current (I_{hc}). The value of ε_0 can be varied by a factor of ~ 5 between a lower limit of ~ 0.15 and an upper limit of ~ 0.8 . The central conductor currents shown in Fig. 6 (< 300 kA) are practical with current densities of 10 kA/cm².

Figure 7 shows a variety of flux surface plots for various ε/M , and Fig. 8 shows a selection of ε profiles. All of the reference configuration ε profiles have the low shear characteristic of helical-axis devices. The increasing bean shaping that occurs at higher ε_0/M (Fig. 7) leads to deeper magnetic wells. This is illustrated for three ε_0/M values in Fig. 9. It is also possible to vary the magnetic well depth at fixed ε_0/M by altering the mix of helical and central conductor currents. Figure 10 shows flux surfaces for $\varepsilon_0/M = 0.36$ and 0.62 . As the total central conductor current is increased with ε/M held fixed, the helical swing radius of the magnetic axis

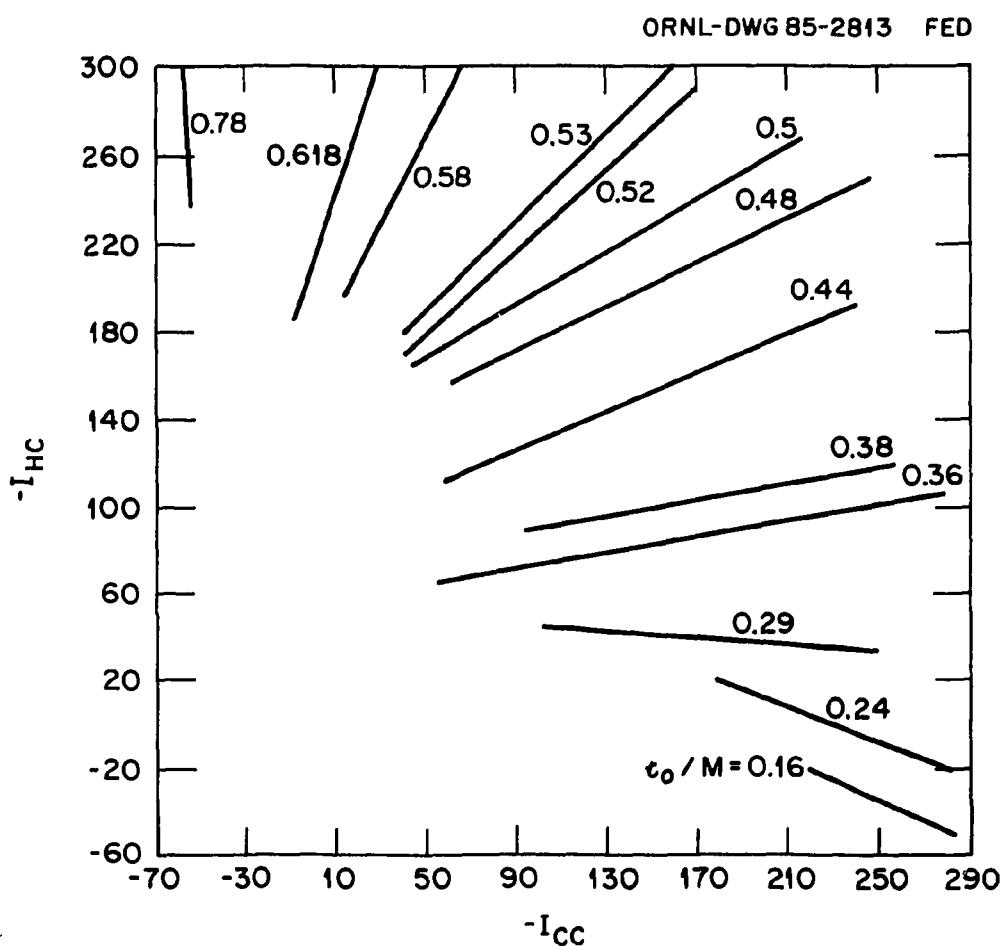
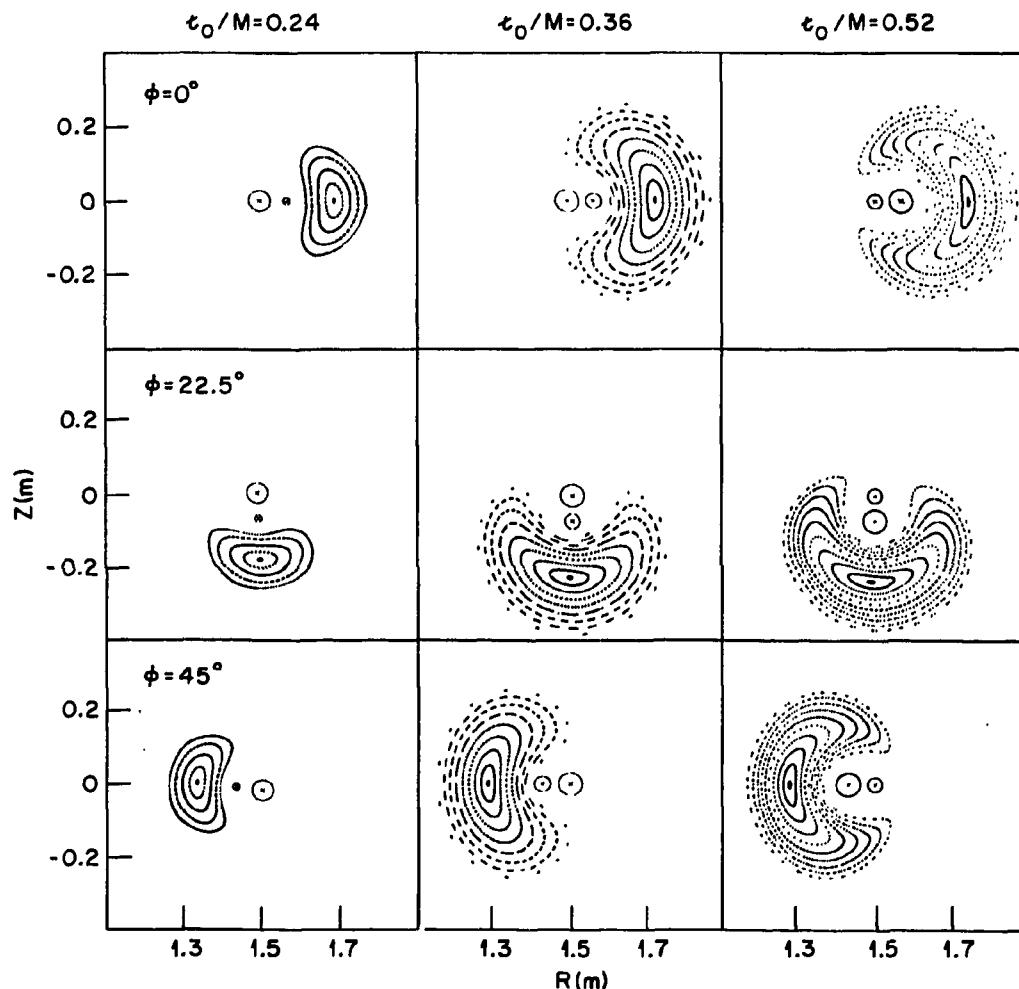


Fig. 6. Contours of constant ϵ_0/M as a function of central conductor (I_{cc}) and helical conductor (I_{hc}) currents.

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Fig. 7. Flux surfaces for several t_0/M .

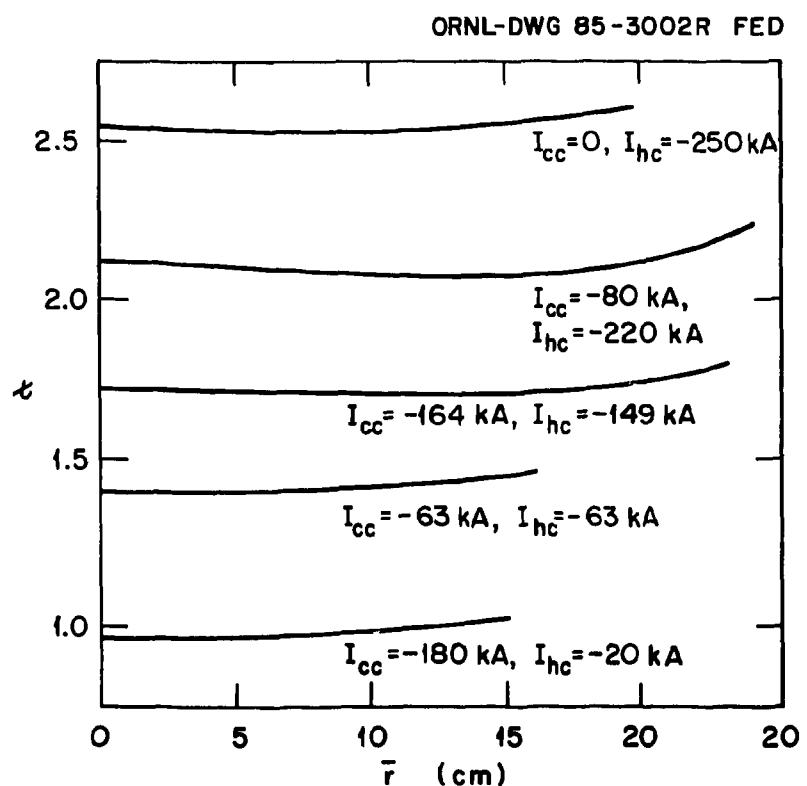


Fig. 8. Typical τ profiles for various central conductor currents.

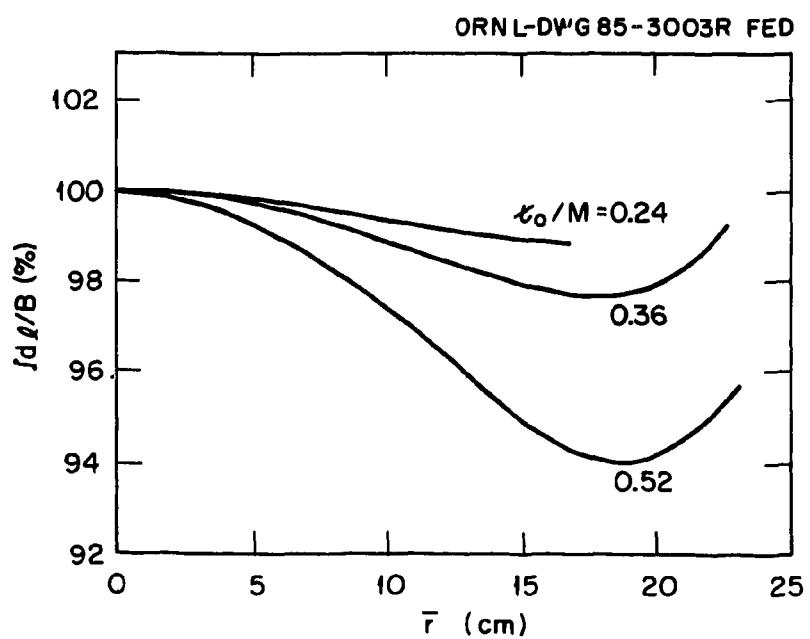


Fig. 9. Increase in magnetic well depth as τ_0/M increases.

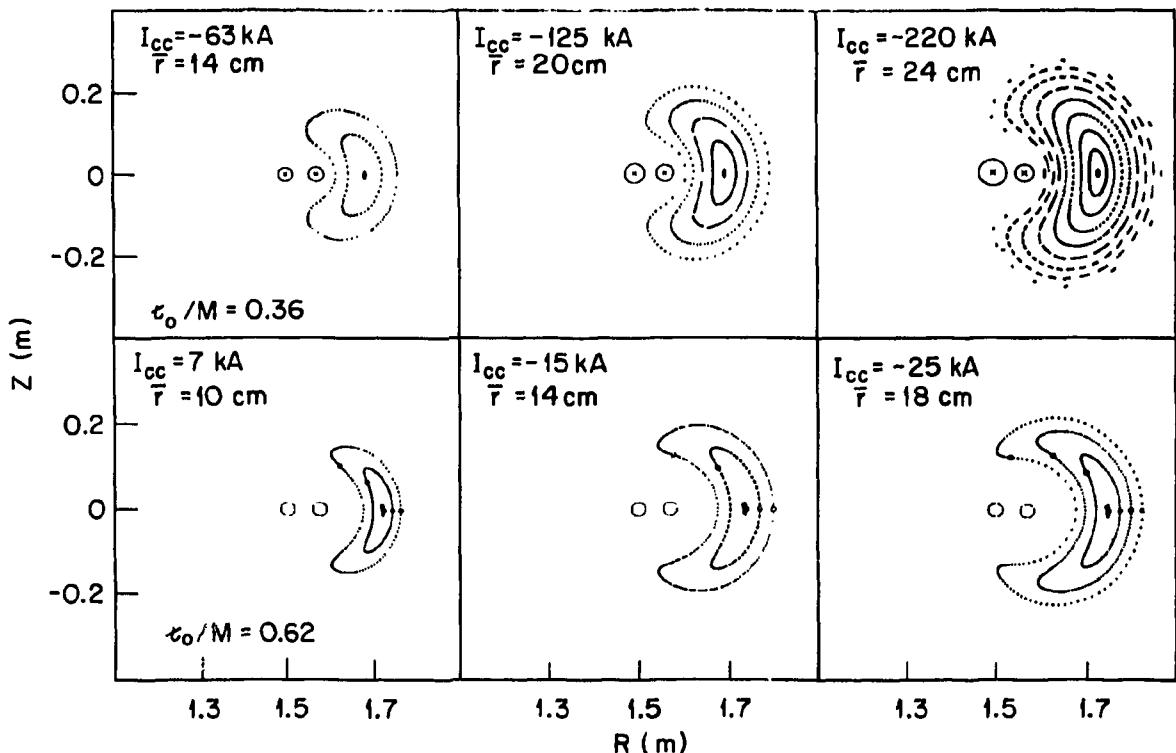


Fig. 10. Flux surfaces at $\epsilon_0/M = 0.36$ (upper row) and 0.62 (lower row), showing increase in plasma volume at fixed ϵ_0/M as the central conductor current is increased.

increases, and there is a corresponding increase in average plasma minor radius. As the magnetic axis moves away from the hardcore, the surface indentation (and thus the magnetic well depth) at a given average radius also decreases. This is shown for the $\epsilon_0/M = 0.36$ case in Fig. 11, where well depths for a range of hardcore currents are plotted. The higher current cases have shallower wells at a given average radius and at the highest currents actually have destabilizing curvature ($V'' > 0$) near the plasma edge.

Figure 12 shows how the average radius of the last closed flux surface varies in the I_{hc} - I_{cc} plane of Fig. 6. A comparison of Figs. 6 and 12 shows that for a given ϵ_0/M , the average plasma radius increases as the total central conductor current is increased. The major resonances ($\epsilon_0/M = 1/3, 1/2, \dots$) also play a role in determining the average radius. As the transform is raised toward the resonance, the outer surfaces begin to break up, and the average plasma radius is reduced. However, the resonances can be approached very closely from above without affecting the average radius, since the shear is positive for most of the accessible configurations.

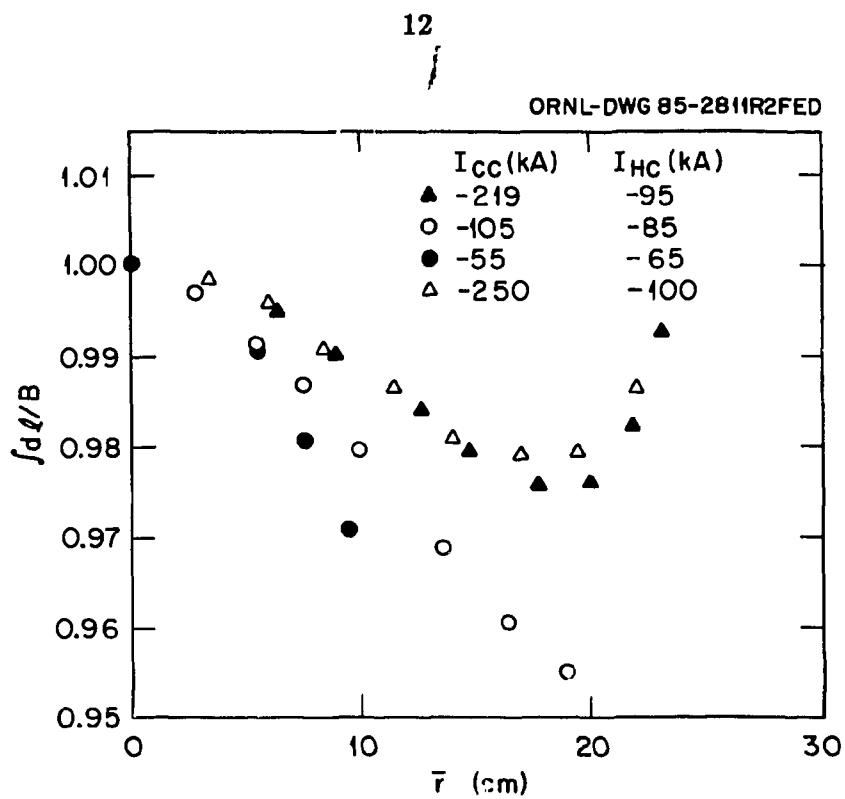


Fig. 11. Decrease in magnetic well depth as $(I_{cc} + I_{hc})$ is raised for the $\tau_0/M = 0.36$ case of Fig. 10.

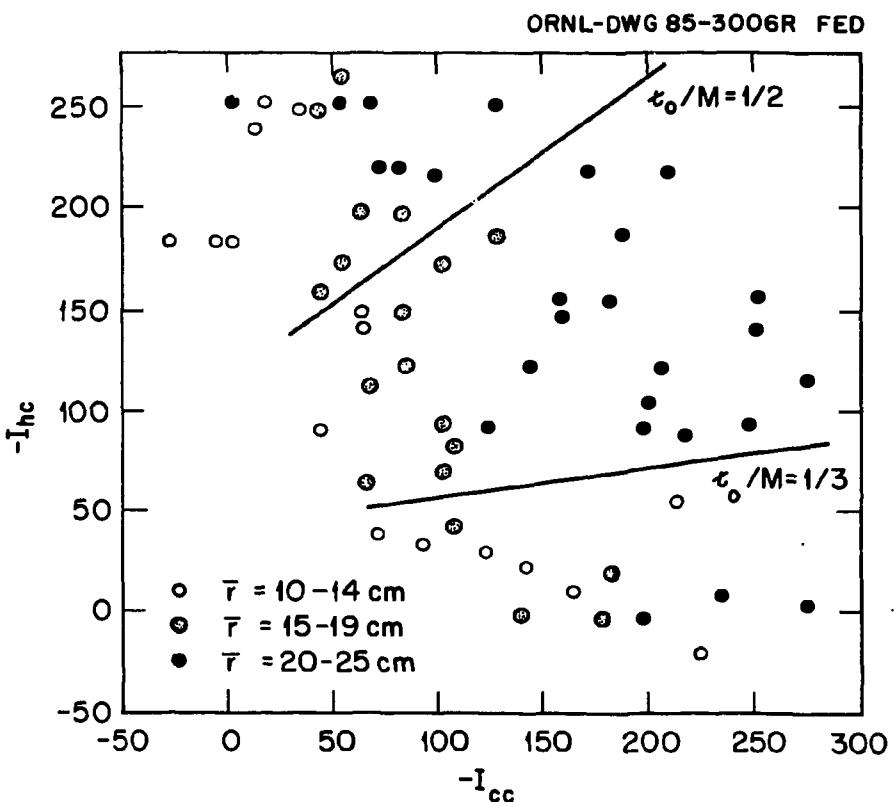


Fig. 12. Average plasma radii in the I_{cc} - I_{hc} plane.

At fixed ν_0/M , it is possible to control the shear to some degree by changing the hardcore currents. At high ν_0/M (≥ 0.5) the shear tends to be lower and even slightly negative in some cases. Neither of these effects on the shear is particularly large; more importantly, they are not independent of the transform and well. A far greater degree of variation in the shear can be achieved by independently powering the inner and outer turns of the $\ell = 1$ winding. This allows the effective swing radius of the $\ell = 1$ winding to be varied between 5.25 cm and 8.75 cm for currents $I_{hc} < 150$ kA. Figure 13 shows the effect of shifting the centroid of the current over this range; significant (by Heliac standards) positive and negative shear can be achieved.

Another degree of freedom in the configuration can be achieved by modulating the currents in the TF coils according to their toroidal location:

$$I_{TF} = I_0(1 + C_F \cos 4\phi) . \quad (1)$$

This modulation directly affects the $m = 0, n = 4$ harmonic of the magnetic field and, by beating with the helical $m = 1, n = 4$ harmonic, can also affect the $m = 1, n = 0$ harmonic. Thus, in second order, the toroidal shift, which is proportional to the magnitude of $B_{1,0}^2$, can be reduced (or increased by this current

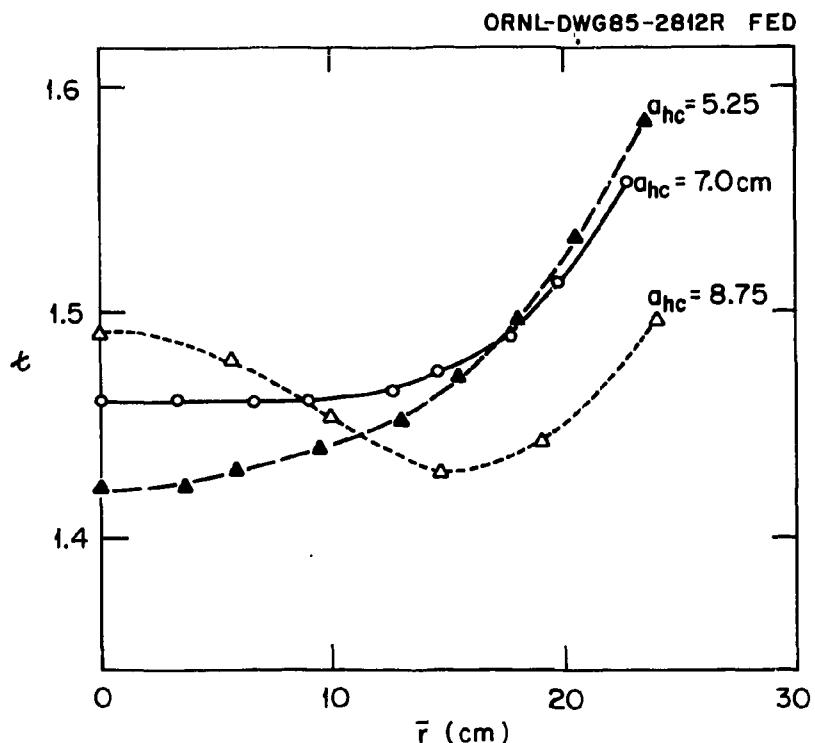


Fig. 13. Effect of shifting the centroid of the $\ell = 1$ winding current (a_{hc}) on the shear.

modulation. At the reference aspect ratio, however, the toroidicity is dominated by the $1/R$ dependence, and the effects of current toroidicity modulation alter $B_{1,0}^2$ by only $\sim 10\%$.⁸ A more important consequence of modulating the TF coil currents is the effect on the field ripple and thus the orbit losses. Figure 14 shows how the field ripple is altered by modulating the TF coil current between the limits $+17\%$ and -20% . It can be seen that the $C_F = 17\%$ modulation substantially reduces the field ripple near the magnetic axis. The flux surfaces corresponding to the range of current modulations of Fig. 14 are shown in Fig. 15. The requirement for conservation of the toroidal flux within a given surface causes the flux surface areas to be larger at $\phi = 0^\circ$ than at $\phi = 45^\circ$ when $C_F = 0$. This results from the underlying $1/R$ dependence of the toroidal field; applying a modulation $C_F = 15\%$ approximately compensates for the $1/R$ dependence, and the flux surface areas at these two cross sections are then nearly equal.

Many of the properties of the Flexible Heliac can be understood by studying a simple analytical model.¹ In the helically symmetric limit, the helical flux function¹¹⁻¹³ is

$$\psi = \frac{B_0 r^2}{R_0 2} - \frac{\mu_0 I}{2\pi} \ln r - r \left[a_1 I'_1 \left(\frac{r}{R_0} \right) + b_1 K'_1 \left(\frac{r}{R_0} \right) \right] \cos \left(\theta - \frac{z}{R_0} \right), \quad (2)$$

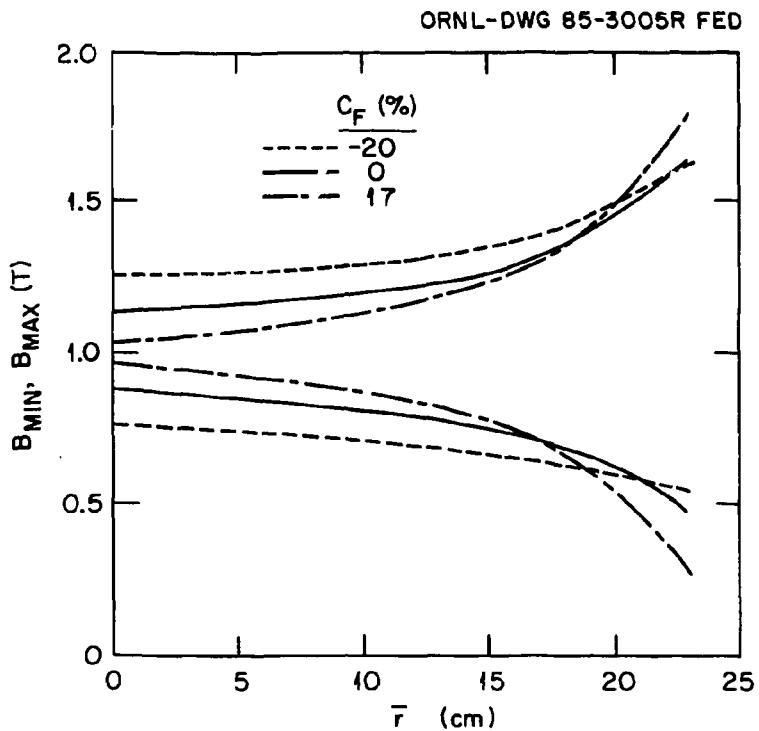


Fig. 14. Effect of changing the modulation (C_F) of the TF coil currents on the variation of $|\vec{B}|$ on a flux surface (labeled by average radius, \bar{r}).

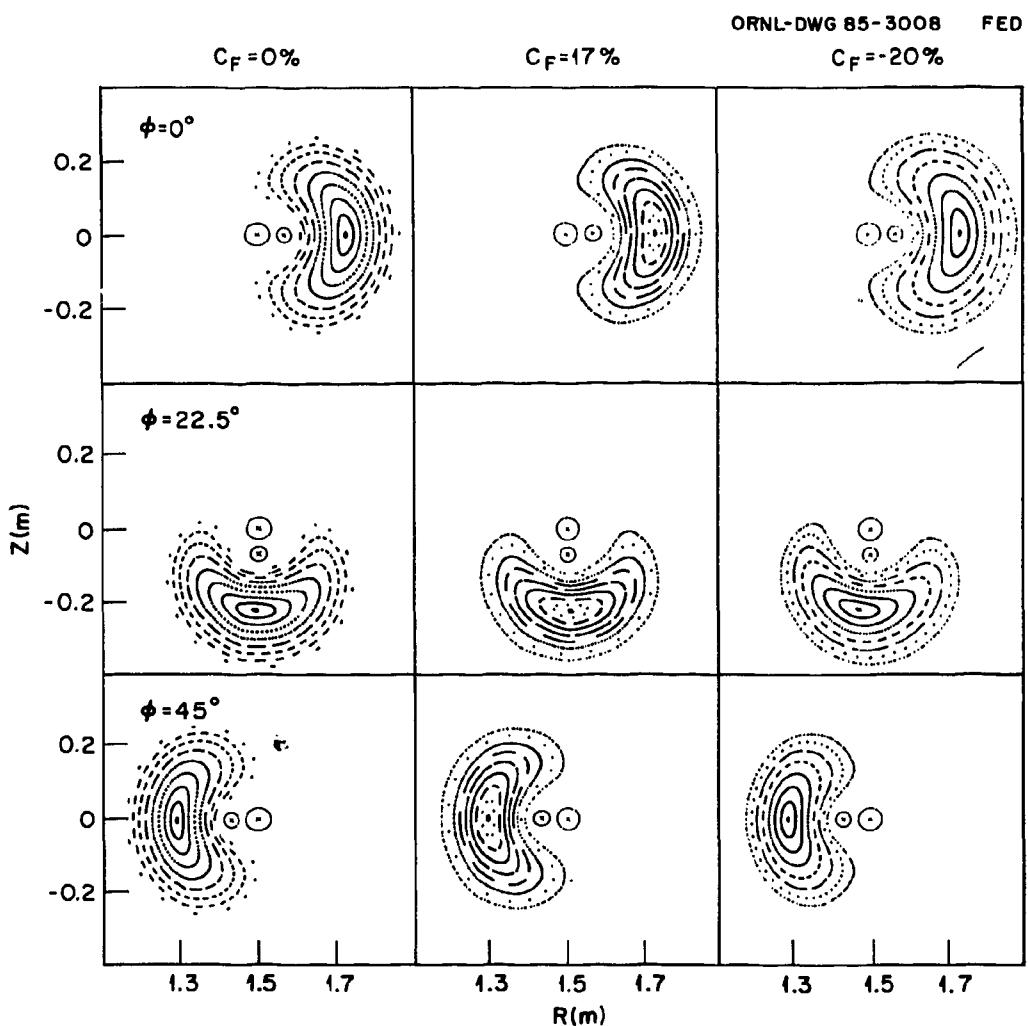


Fig. 15. Effect of TF coil current modulation on the flux surface shape.

where only the dominant helical terms are retained. The first term represents the uniform toroidal field, and the second term results from the average poloidal field generated by the hardcore windings. The Bessel function terms are related to the helical fields generated by the $\ell = 1$ hardcore winding (K_1 term) and the helical displacements of the TF coils (I_1 term). (This model has already been used in Ref. 1 to study some of the properties of the Flexible Heliac, and the formulas developed there are quoted and used without further proof.) The location of the magnetic axis $r = r_A$ is given by

$$\frac{r_A}{R_0} - \frac{\mu_0 I}{2\pi R_0 B_0} \frac{R_0}{r_A} = \frac{R_0}{r_A} \left(\frac{r_A^2}{R_0^2} + 1 \right) \left[\frac{a_1}{B_0} I_1 \left(\frac{r_A}{R_0} \right) + \frac{b_1}{B_0} K_1 \left(\frac{r_A}{R_0} \right) \right] \quad (3)$$

and the central transform by¹¹

$$\frac{\tau_0}{M} = 1 - \frac{2e}{1 + e^2} \frac{1}{(1 + r_A^2/R_0^2)^{1/2}}, \quad (4)$$

where the ellipticity of surfaces is given by

$$e = \left\{ \frac{\partial^2 \psi}{\partial r^2} / \left[\frac{1}{r_A^2} \frac{\partial^2 \psi}{\partial \theta^2} \left(1 + \frac{r_A^2}{R_0^2} \right) \right] \right\}^{1/2}. \quad (5)$$

Using these formulas, we can construct a contour plot equivalent to Fig. 6; Fig. 16 shows contours of constant τ_0/M as functions of b_1/B_0 and $\mu_0 I/(2\pi R_0 B_0)$ for $a_1/B_0 = 0.25$. Each constant τ_0/M contour is a parabola that turns over at increasingly high current (I) as τ_0/M is increased. In the 3-D analogue, the flux surfaces are broken at the extreme ends of the τ_0/M contours by physical interference with the coils. Thus the radiating contours in Fig. 6 are, in fact, short segments of a series of parabolas. The analytic model also reproduces the property that the magnetic axis shifts further out as the total central conductor current is raised at constant τ_0/M . Figure 17 demonstrates this for the case $\tau_0/M = 0.35$.

IV. ENGINEERING CONSIDERATIONS

In this section, aspects of the physics studies that are related to engineering considerations are briefly discussed. In particular, studies of error fields, finite cross-section conductors, and plasma-coil clearances are described.

The low shear inherent to the Heliac accentuates the effects of resonant or nearly resonant error fields. Even with no errors present, the regions near the major resonances ($\tau_0/M = 1/4, 1/3, 1/2, \dots$) are inaccessible. Errors that break the four-fold symmetry are the most dangerous, since they introduce a whole new class of low-order resonances (Fig. 18). For the reference configuration, the most dangerous of these error-induced resonances are $\tau = 3/2$ and $5/2$. The even lower order resonances $\tau = 1/1$ and $2/1$ are already inaccessible resonances ($\tau = 4/4$ and $4/2$) in the error-free case, which has the four-fold symmetry.

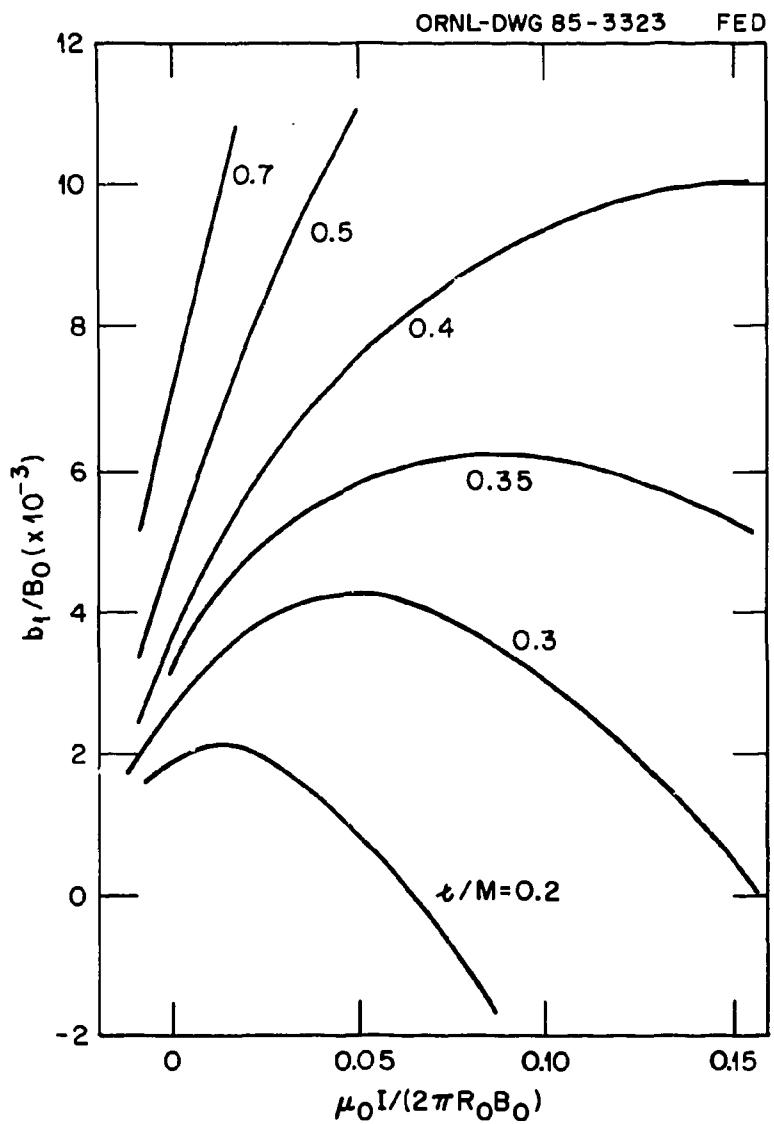


Fig. 16. Contours of ε_0/M from the analytical model.

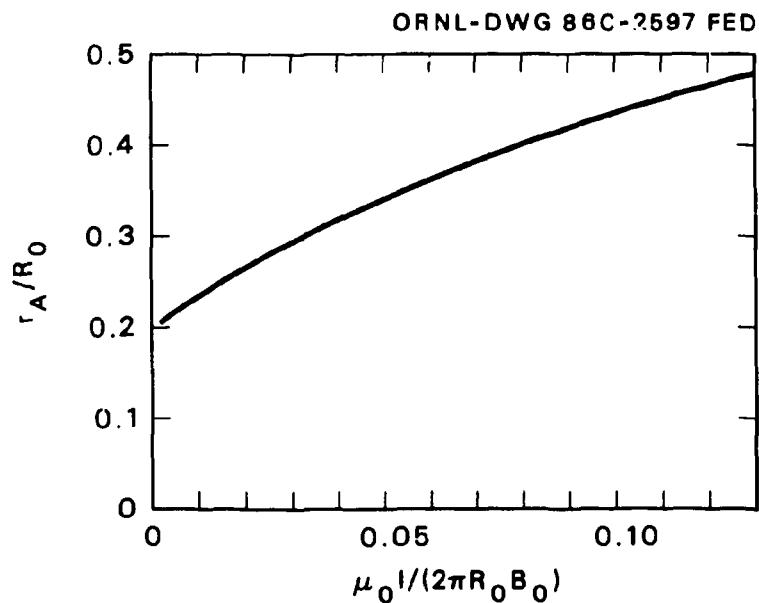


Fig. 17. Location of the magnetic axis (r_A) as the total current (I) is varied in the analytical model.

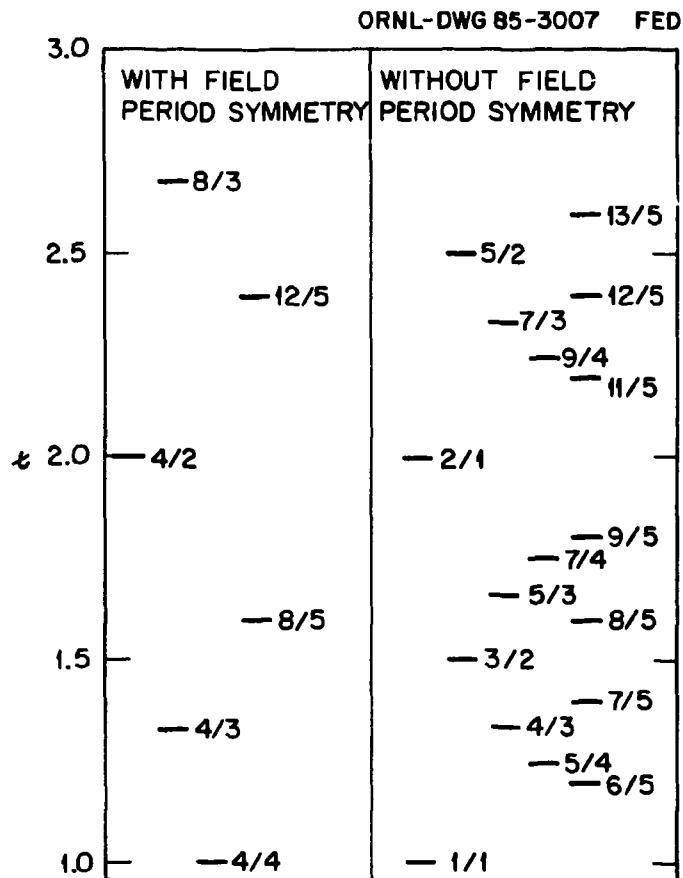


Fig. 18. Potential resonances with and without 4-field-period symmetry.

Figure 19 shows the effect of a horizontal offset of the central conductor structure relative to the TF coils; the unperturbed case has $\varepsilon_0 = 1.46$, and the ε profile crosses the $\varepsilon = 3/2$ resonance. For an offset of 2.5 mm, the $m = 2$ islands induced by the error fields are clearly visible. Other errors, such as gross tilts of the hardcore structure or distortions in the winding law of the $\ell = 1$ winding or TF coils, result in similar error tolerances.

The flexibility allows the resonance ($\varepsilon = 3/2$) to be removed from the plasma by small changes in the hardcore currents. For a horizontal offset of 2.5 mm, changing the hardcore current by $\sim 10\%$ removes the $\varepsilon = 3/2$ resonance and the associated error field problem (Fig. 20).

The effects of the error fields diminish rapidly for higher order resonances, because for higher poloidal mode numbers (m), the range of the error field (whose magnitude is $\propto x^{-m}$, where x is the distance from the source) decreases, and the island width associated with a given radial field perturbation ($\propto m^{-1/2}$) decreases.

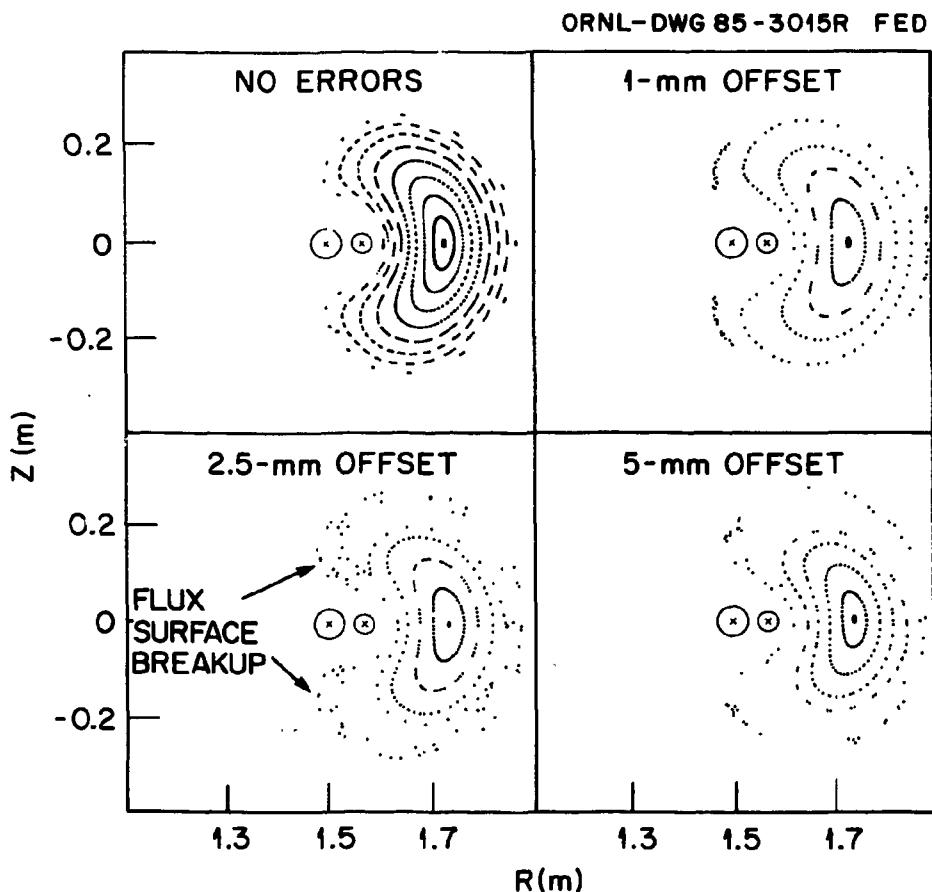


Fig. 19. Effect of various horizontal offsets of the central conductors relative to the TF coils ($\varepsilon_0 = 1.46$).

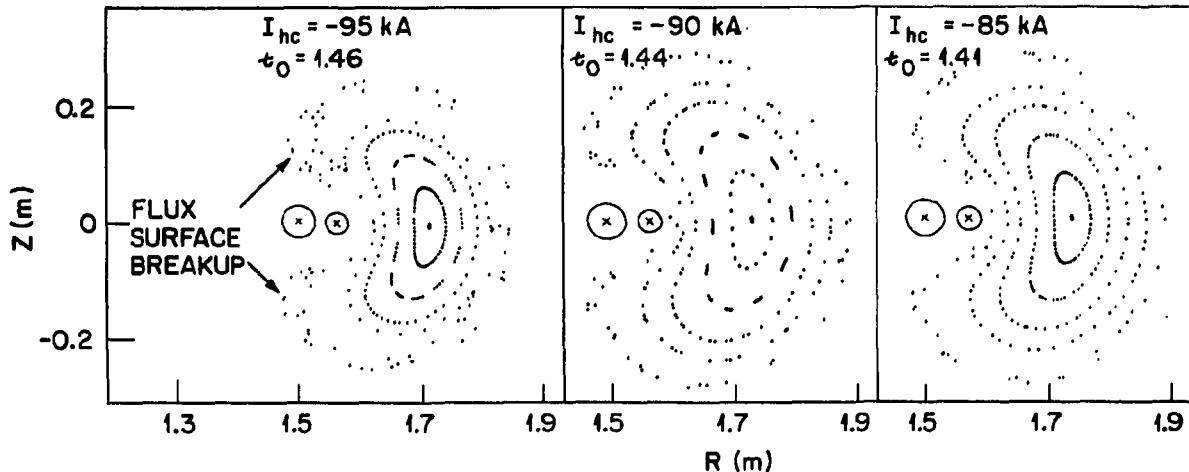


Fig. 20. Effect of lowering t_0 to avoid having the $\tau = 3/2$ resonance in the plasma. The severe flux surface destruction caused by a 2.5-mm offset (Fig. 19 and left-hand flux surfaces in Fig. 20) can be avoided.

Figure 21 shows that, for a configuration containing the $\tau = 5/3$ resonance, a 2.5-mm offset of the hardcore has little effect on the flux surface quality; for the next order lower resonance, $\tau = 3/2$, this error is sufficient to destroy a large portion of the flux surfaces (Fig. 19). It should be noted, however, that the offset of the hardcore is more effective at generating $m = 2$ than $m = 3$ errors. There is a factor of ~ 2 reduction in island size in going from the $\tau = 3/2$ to the $\tau = 5/3$ resonance that can be directly attributed to the change in poloidal mode number. It becomes increasingly difficult to envisage physically feasible errors that would drive significant error fields of higher poloidal mode number.

The Flexible Heliac is remarkably robust with respect to errors that preserve the 4-field-period symmetry. For example, a possible support structure concept for the central conductor is a post three-fourths of the way through each field period (at this point the plasma is above the central conductor and access is possible). Even an average 3-cm "squaring" of the central conductor structure between these four 3/4-field-period fixed points leads only to a distortion of the plasma, with no significant loss of volume (Fig. 22). Such a squaring error is far beyond that likely to be caused by the magnetic forces.

The main conclusion of the error field studies is thus that errors that break the field period symmetry are the most troublesome. A tolerance of < 1 mm is set by such errors, and even then, configurations with the $\tau = 5/2$ and $3/2$ resonances may be inaccessible. The configuration is very tolerant of errors that preserve the four-fold symmetry; this suggests that the support structures, etc., should all have this symmetry.

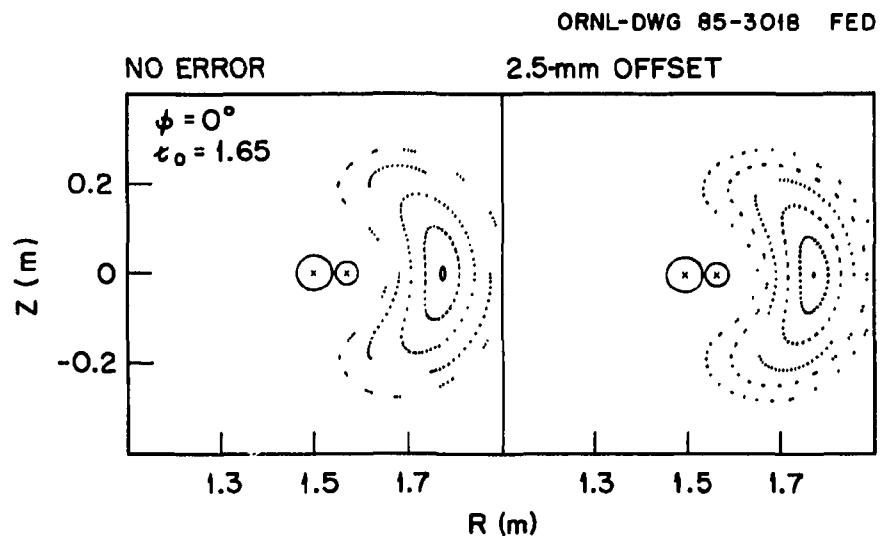


Fig. 21. For the $\epsilon = 5/3$ resonance, a 2.5-mm offset error causes no noticeable flux surface destruction.

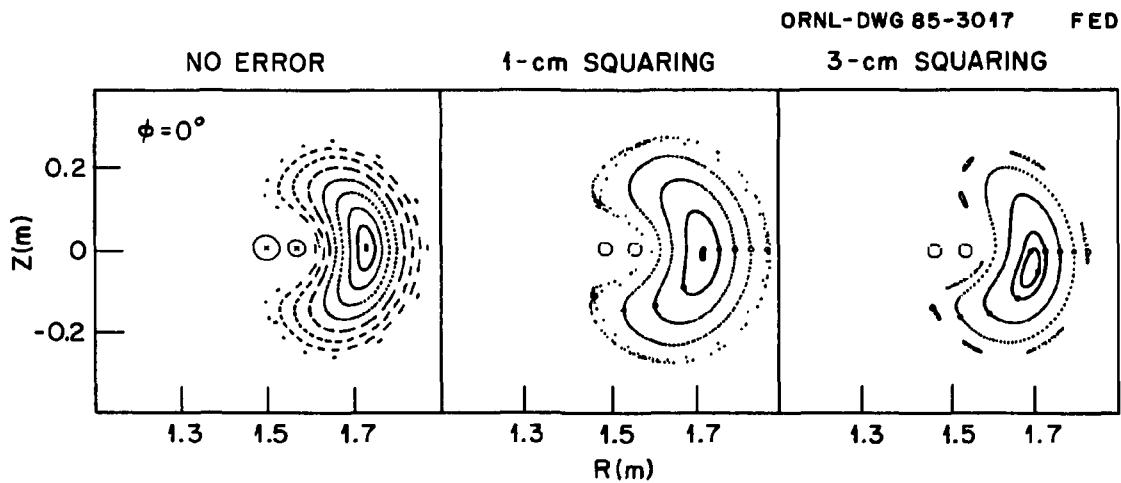


Fig. 22. Effect of squaring the central conductor structure about the fixed points $67.5^\circ + M \times 90^\circ$ ($M = 0, \dots, 3$). The squaring is measured by the average deviation from circularity.

These results change very little when the effects of the finite cross section of the conductors are included. The finite-size coils are simulated by using increasingly large numbers of filaments uniformly distributed throughout the cross section of the coil. The effects of the finite cross-section central conductor (Fig. 23), $\ell = 1$ winding (Fig. 24), and TF coils (Fig. 25) have been checked for several cases. The impact of using finite coil sizes can be seen to be very small; comparison of sensitive quantities such as the magnetic well confirms this conclusion.

Finally, we consider the clearance between the plasma, the $\ell = 1$ winding, and the TF coils. Figure 26 shows the distance from each magnetic surface (labeled by its average radius) to the center of the $\ell = 1$ winding for several values of τ/M . The reference value for the cross-sectional radius of the $\ell = 1$ winding is 3.5 cm, so surfaces that are $\lesssim 3.5$ cm from the helical winding center must be eliminated with a material limiter. It can be seen that each 1 cm of increased separation between the plasma and the $\ell = 1$ winding requires approximately a 2-cm reduction in average radius. Also, it can be seen that the high- τ/M (> 0.5) configurations have considerably improved clearances.

There are several ways to improve the clearance between the plasma and the $\ell = 1$ winding. As discussed in Sec. III, if the hardcore current is increased at constant τ_0/M , the plasma shifts away from the central conductor structure, and there is an accompanying increase in plasma volume. This is illustrated in Fig. 27 for the $\tau_0/M = 0.36$ case. Another method of increasing the separation is to use a “poloidally spread” helical winding (Fig. 28). For the case illustrated, there is a 2.5-cm increase in clearance for flux surfaces having the same average radius. There is, however, a trade-off here, because poloidally spreading the $\ell = 1$ winding makes it less effective at generating the helical fields, and thus higher currents are required.

The other clearance of concern is that between the plasma and the TF coils. Figure 29 compares the plasma clearance to the TF coils and $\ell = 1$ winding for three values of τ_0 . In this case the clearances are to the edges of the coils and not the centers. It can be seen that for the high- τ case ($\tau \gtrsim 2$), neither of the clearances is a particular problem, and for lower transform values the clearance to the edge of the $\ell = 1$ winding is always more restrictive. A potential method of increasing the TF coil clearance still further is to use square TF coils; this is illustrated in Fig. 30 for an $\tau_0/M = 0.3$ case.

V. SUMMARY

The Flexible Heliac reference configuration was determined by systematic parameter scans about a 4-field-period, $R = 1.5$ m case, the gross size of the device being set by considerations of economics and plasma minor radius.

The selected configuration allows the rotational transform to be varied by at least a factor of 5 ($0.15 \lesssim \tau_0/M \lesssim 0.8$). This flexibility, which greatly exceeds that of the standard Heliac, results from the addition of the $\ell = 1$ winding to the hardcore structure. At fixed τ_0/M , the magnetic well depth and plasma volume can be altered to a more limited extent by varying the mix of hardcore currents;

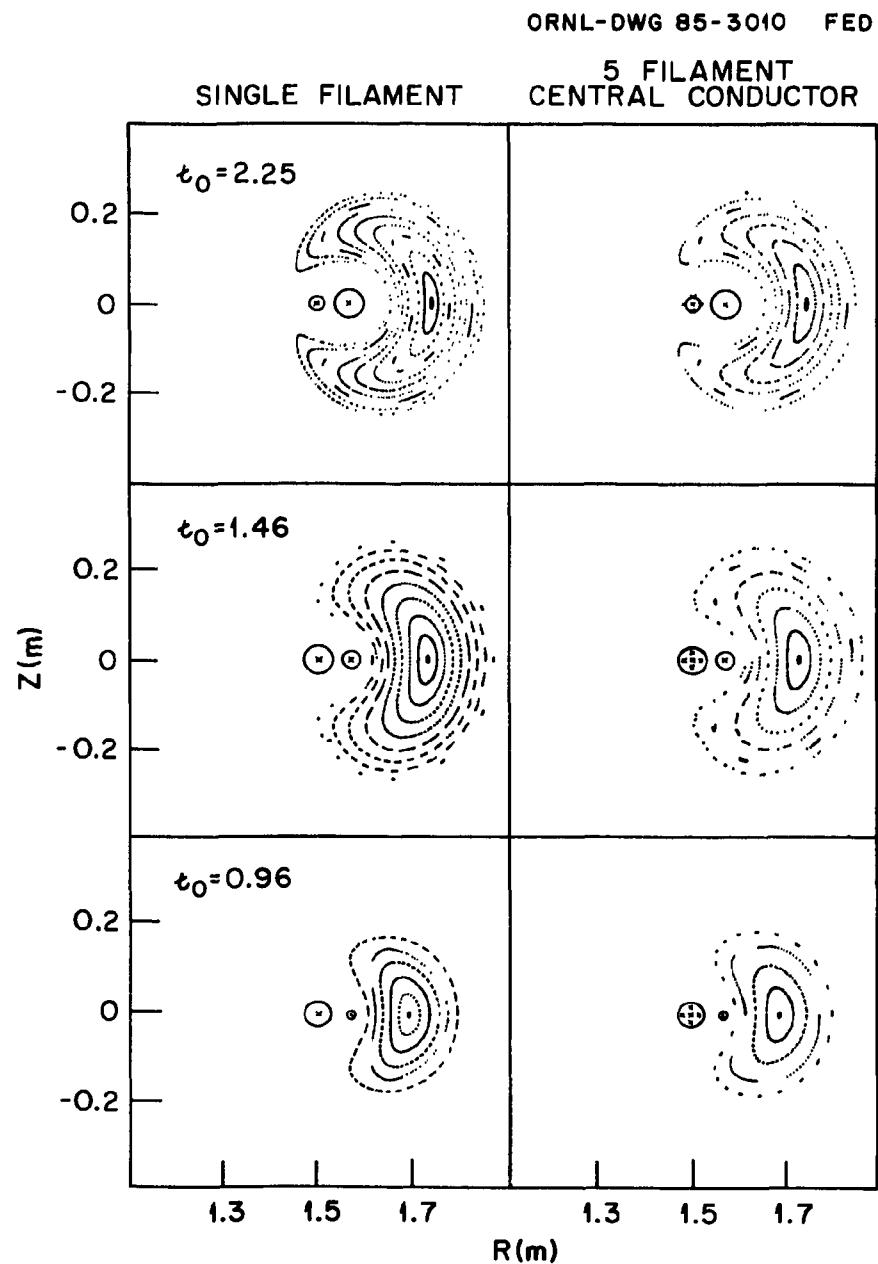


Fig. 23. Inclusion of a finite cross-section central conductor has no effect on the flux surfaces.

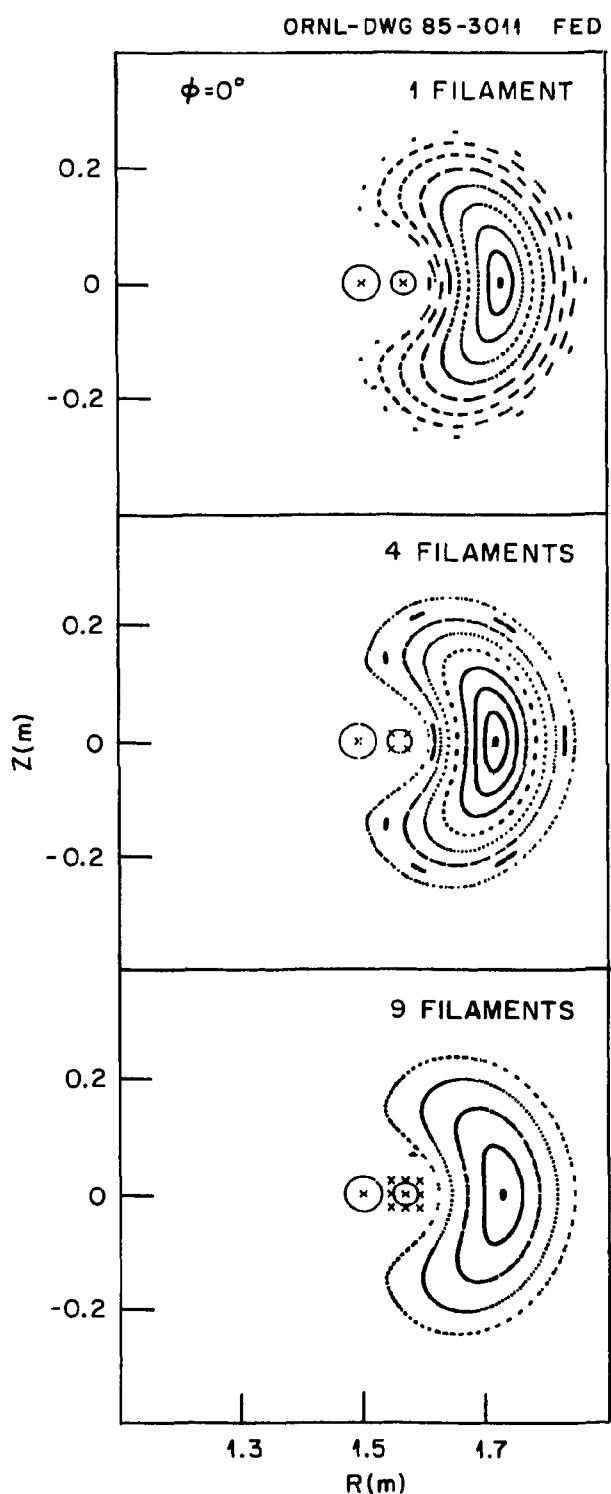


Fig. 24. A finite cross-section $\ell = 1$ winding produces no significant changes in the flux surface quality.

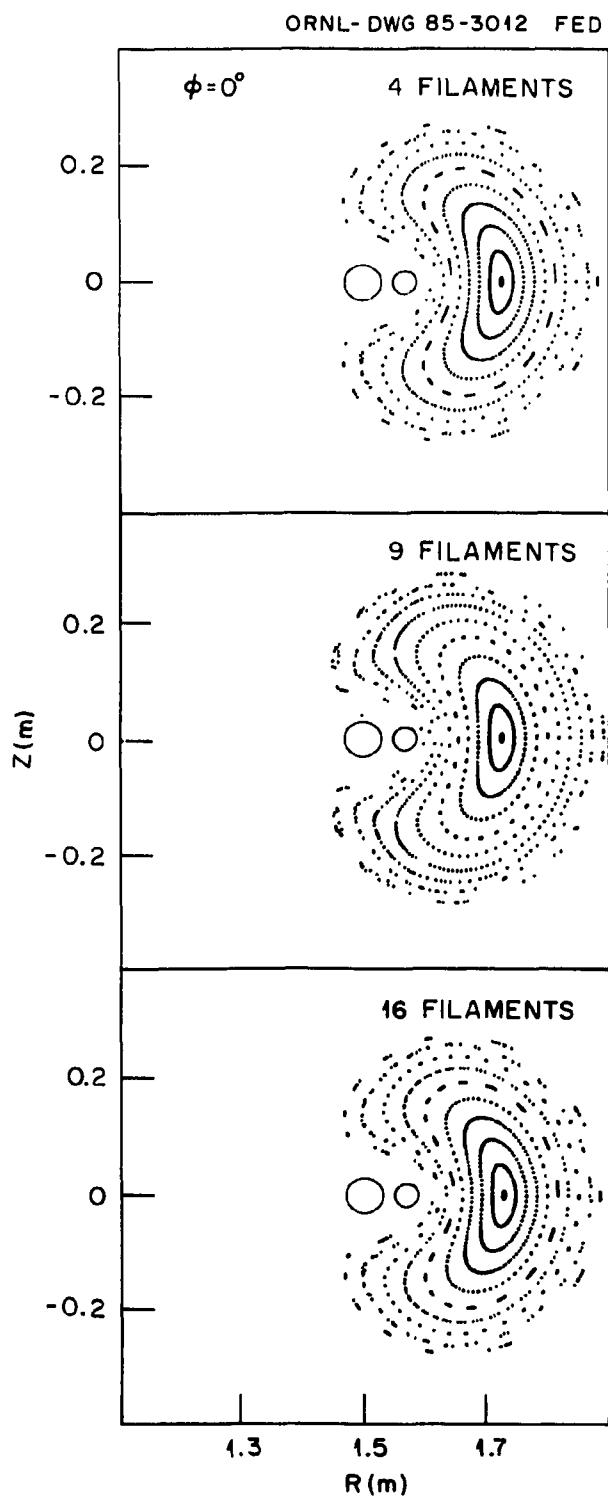


Fig. 25. Finite cross-section TF coils have very little effect on the flux surface quality.

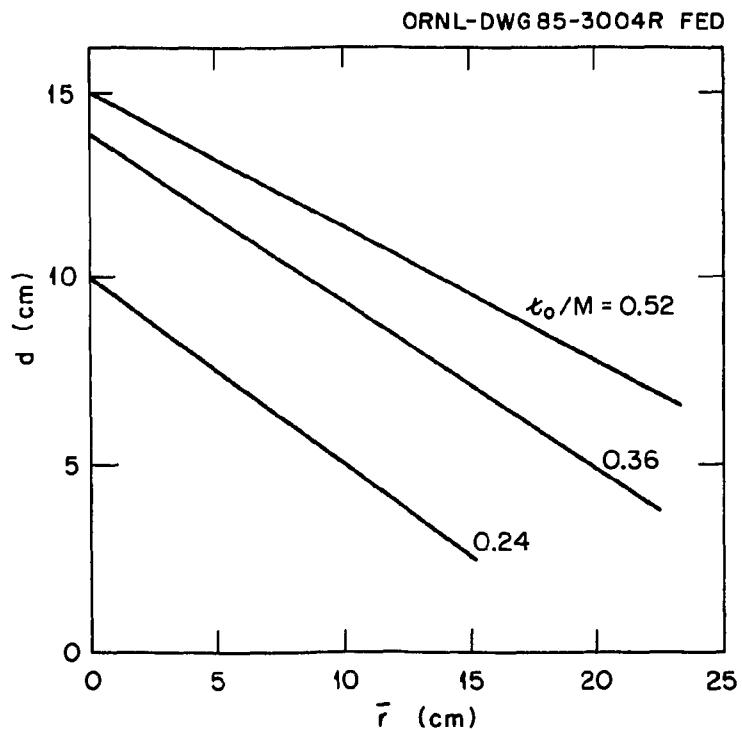


Fig. 26. Clearance to the center of the $\ell = 1$ winding as a function of average radius for various values of x_0/M .

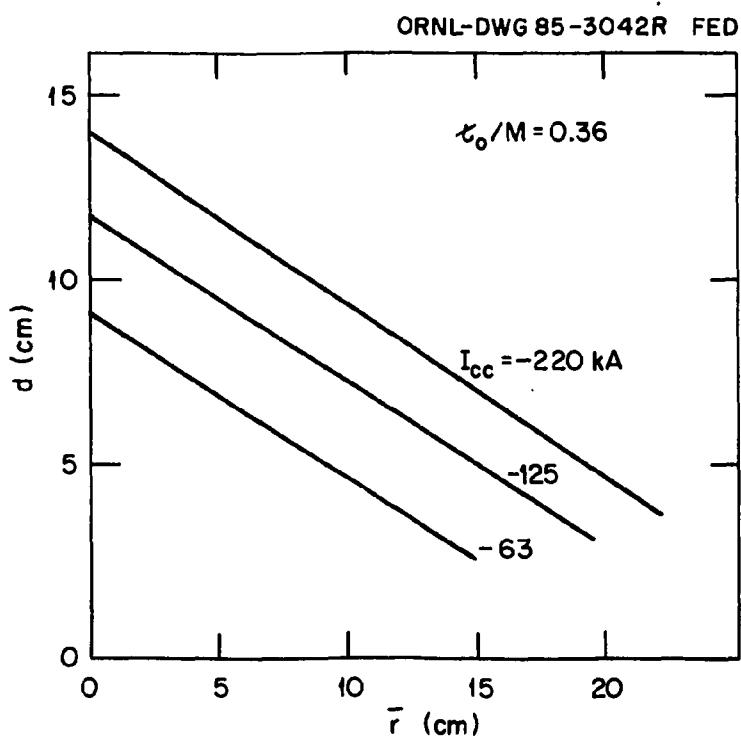


Fig. 27. Effect of increasing the central conductor currents at fixed x_0/M . The clearance to the center of the $\ell = 1$ winding can be increased.

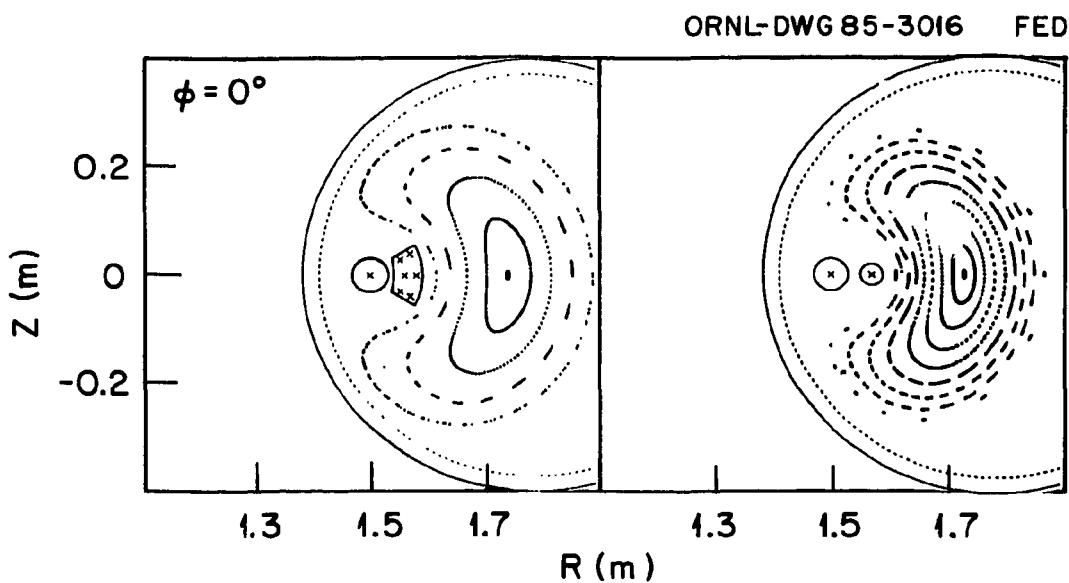


Fig. 28. Plasma clearance with a poloidally spread $\ell = 1$ winding (left) and with the circular cross-section $\ell = 1$ winding (right).

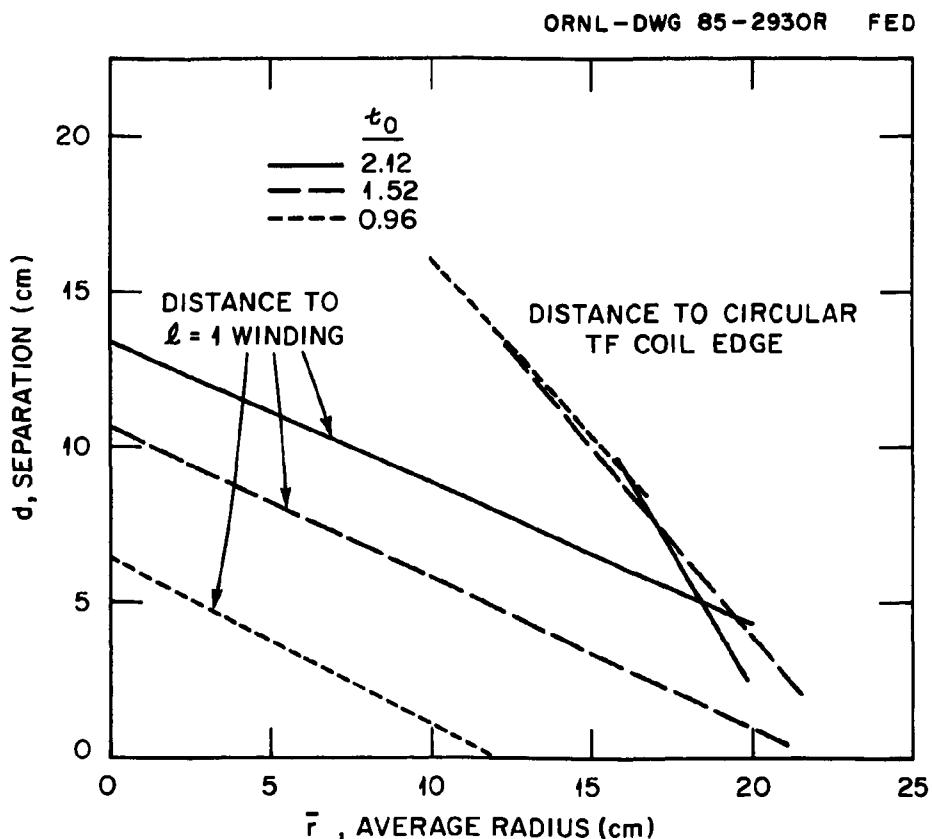


Fig. 29. Clearance between the edge of the $\ell = 1$ winding and the plasma and between the TF coils and the plasma.

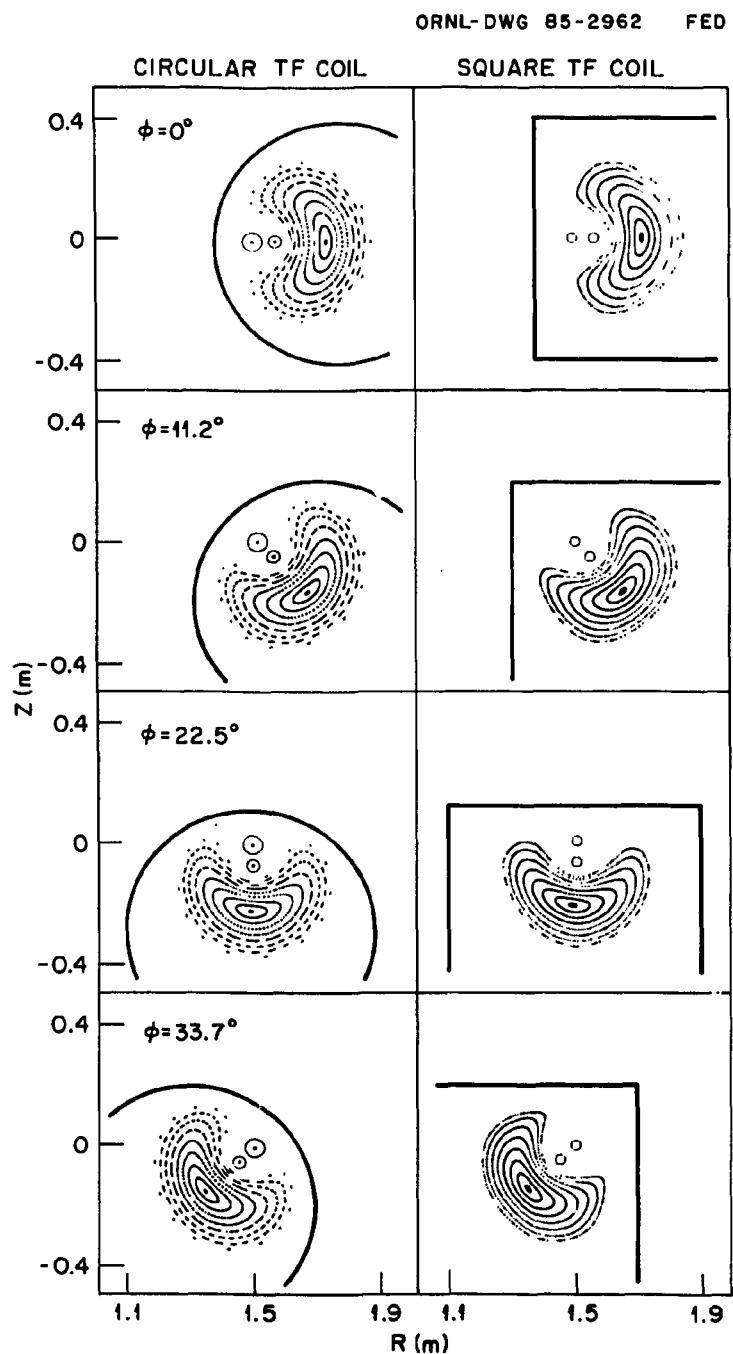


Fig. 30. Clearance between the plasma and the TF coils can be improved by using square TF coils.

plasmas with average minor radii up to 25 cm can be produced. A relatively large variation in the shear can be achieved by independently powering the inner and outer turns of the $\ell = 1$ winding, which permits the effective current center of the helical current to be shifted between 5.25 and 8.75 cm (for $I_{hc} \lesssim 150$ kA).

Error field studies have shown that perturbations that break the four-fold symmetry are most serious since they excite low-order resonances. The effects of including the finite cross section of the conductors are small, even when sensitive quantities such as the magnetic well are compared.

The most important of the plasma coil clearances is that between the $\ell = 1$ winding and the plasma. This problem is particularly pronounced at low ϵ . It appears likely that some form of material limiter will be necessary to protect the $\ell = 1$ winding in these cases. The clearance to the $\ell = 1$ winding can be increased at a given ϵ by using higher hardcore currents. Poloidally spreading the $\ell = 1$ winding also improves this clearance.

In summary, the flexibility of the reference configuration allows the study of rotational transform values between those of conventional stellarators (~ 0.1 /field period) and the very high values (~ 0.8 /field period) that can only be achieved in helical-axis devices. The fine control over the transform, shear, and magnetic well afforded by this configuration should permit the study of the effects of resonances and improve theoretical understanding. By finely tuning the profiles to avoid equilibrium problems, it should be possible to gain access to high-beta stable regimes.

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