

27
5/28/80
Pass
2404TIS

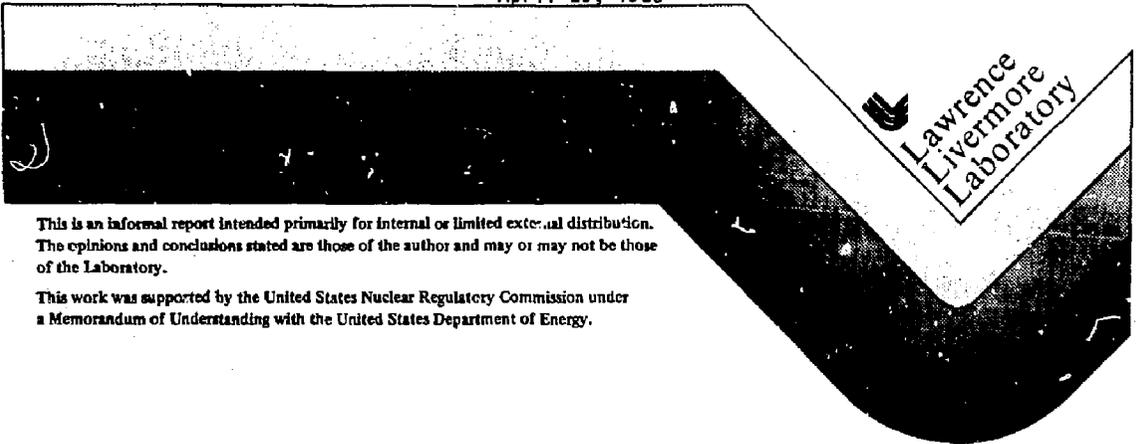
UCID- 18660

MASTER

ADVANCED THREE-DIMENSIONAL THERMAL MODELING OF A
BASELINE SPENT FUEL REPOSITORY

Thomas J. Altenbach
William E. Lowry

April 29, 1980



This is an informal report intended primarily for internal or limited external distribution. The opinions and conclusions stated are those of the author and may or may not be those of the Laboratory.

This work was supported by the United States Nuclear Regulatory Commission under a Memorandum of Understanding with the United States Department of Energy.

DISTRIBUTION OF THIS DOCUMENT IS UNLIMITED

DISCLAIMER

This book was prepared as an account of work sponsored by an agency of the United States Government. Neither the United States Government nor any agency thereof, nor any of their employees, makes any warranty, expressed or implied, or assumes any legal liability or responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or any agency thereof.

DISCLAIMER

This book was prepared as an account of work sponsored by an agency of the United States Government. Neither the United States Government nor any agency thereof, nor any of their employees, makes any warranty, express or implied, or assumes any legal liability or responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or any agency thereof. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or any agency thereof.

TABLE OF CONTENTS

	<u>Page No.</u>
ABSTRACT	v
INTRODUCTION	1
SCOPE OF WORK	2
PRELIMINARY MODEL DESCRIPTION	2
ADVANCED MODEL	3
Baseline Design	5
Geometric Model: Initial and Boundary Conditions	10
Air Gap and Emplacement Room Heat Transfer Characteristics	13
ANALYSIS AND RESULTS	18
Gap/No Gap Comparison	18
Comparison of Ventilated and Unventilated Cases	19
Room Cool-Down Response	22
CONCLUSIONS AND RECOMMENDATIONS	26
ACKNOWLEDGMENTS	29
REFERENCES	30
APPENDIX A: ANALYSIS OF RESULTS FROM THE NO GAP-UNVENTILATED CASE	31
INTRODUCTION	31
SIMPLE 2-D MODEL	34
1-D MODELS	42
CONCLUSIONS	50

ABSTRACT

We have performed a three-dimensional thermal analysis using finite difference techniques to determine the near-field response of a baseline spent fuel repository in a deep geologic salt medium. A baseline design incorporates previous thermal modeling experience and OWI recommendations for areal thermal loading in specifying the waste form properties, package details, and emplacement configuration. The base case in this thermal analysis considers one 10-year old PWR spent fuel assembly emplaced to yield a 36 kw/acre (8.9w/m^2) loading. A unit cell model in an infinite array is used to simplify the problem and provide upper-bound temperatures. Boundary conditions are imposed which allow simulations to 1000 years. Variations studied include a comparison of ventilated and unventilated storage room conditions, emplacement packages with and without air gaps surrounding the canister, and room cool-down scenarios with ventilation following an unventilated state for retrieval purposes. We found that at this low power level ventilating the emplacement room has an immediate cooling influence on the canister and effectively maintains the emplacement room floor near the temperature of the ventilating air.

The annular gap separating the canister and sleeve causes the peak temperature of the canister surface to rise by 10°F (5.6°C) over that from a no gap case assuming perfect thermal contact. It was also shown that the time required for the emplacement room to cool down to 100°F (38°C) from an unventilated state ranged from 2 weeks to 6 months; when ventilation initiated after times of 5 years to 50 years, respectively. As the work was performed for the Nuclear Regulatory Commission, these results provide a significant addition to the regulatory data base for spent fuel performance in a geologic repository. Recommendations are made for future directions of thermal analysis efforts, particularly for an expansion of the unit cell concept to treat asymmetrical boundary conditions.

ADVANCED THREE-DIMENSIONAL THERMAL MODELING OF A BASELINE SPENT FUEL REPOSITORY

INTRODUCTION

The work described in this report was performed at the Lawrence Livermore Laboratory under contract to the U.S. Nuclear Regulatory Commission to provide "Technical Support in the Development of Nuclear Waste Management Criteria." In the Waste Management Program, Task 1 is concerned with the performance of spent fuel emplaced in a geologic repository. An important element of spent fuel performance is the thermal behavior of the spent fuel, package, and nearby geologic medium. This report describes work performed during FY79 in the development of a three-dimensional thermal model of a spent fuel repository, and presents preliminary results from the analysis of a baseline repository in salt.

The purpose of our thermal modeling is to calculate the time-dependent near-field temperatures in the repository. The near field includes the waste form, package, immediately surrounding geologic medium, and the emplacement room. This temperature field is essential for predicting the performance of the waste form and package. This information is used directly as input to other performance models, such as structural response, brine migration, package corrosion, and waste form dissolution.

SCOPE OF WORK

The approach taken in this work was to build upon the preliminary thermal model developed during FY78. Many phases of the original model were improved, such as boundary and initial conditions, the detail of the 3-D mesh, the treatment of annular air gap and storage room heat transfer, and the expansion of graphical output capabilities. An improvement is the capability to study problems of long duration. Not only is the retrievability period of interest, but also the post-closure phase of the repository can be analyzed for times of at least 1000 years after emplacement.

A baseline salt repository for spent fuel was defined based on OWI recommendations and our own experience. The thermal model was applied to this baseline repository and temperature fields were generated for 1000-year problems, using the TRUMP¹ finite difference heat transfer code. The goal of this analysis was to demonstrate the capability of the thermal model to handle a long-term problem with a realistic package.

PRELIMINARY MODEL DESCRIPTION

The preliminary thermal model, described by Altenbach,^{2,3} was developed for a repository consisting of many parallel emplacement rooms, with a single row of canisters emplaced beneath the floor at regular intervals in each room. This basic approach uses a unit cell concept, which considers one canister in the infinite array and the immediately surrounding salt.

The three-dimensional (3-D) unit cell is therefore rectangular in shape, and symmetry is invoked so that only one-fourth of a canister is treated (Figure 1). Then the four vertical faces are all planes of symmetry and have adiabatic boundary conditions. The front and left faces slice through the canister centerline, the right face coincides with the pillar centerplane, and the back face coincides with the midplane between canisters along the room axis. The room floor is located at a depth of 2000 ft. below the surface, and the cell extends a distance of 500 ft. above and below the room. These horizontal boundaries were assumed to be isothermal in the preliminary model.

Other features of the preliminary model are summarized as follows. The heat source was modeled as a cylinder with properties of UO_2 . A canister containing the spent fuel was not modeled. The waste form was assumed to be in perfect thermal contact with the surrounding salt, and heat flowed by conduction away from the source. Heat transfer modes in the room considered radiation from floor to ceiling, convection from floor to ceiling for an unventilated case, and convection from both floor and ceiling to the bulk air for a ventilated case. Heat transfer from the walls was neglected. Initial temperatures in the repository were calculated from an assumed geothermal gradient.

ADVANCED MODEL

In order to have a clearer focus for the development of the advanced thermal model, it was necessary to define a baseline design for a spent fuel package stored in a salt repository. Once developed, the model was then

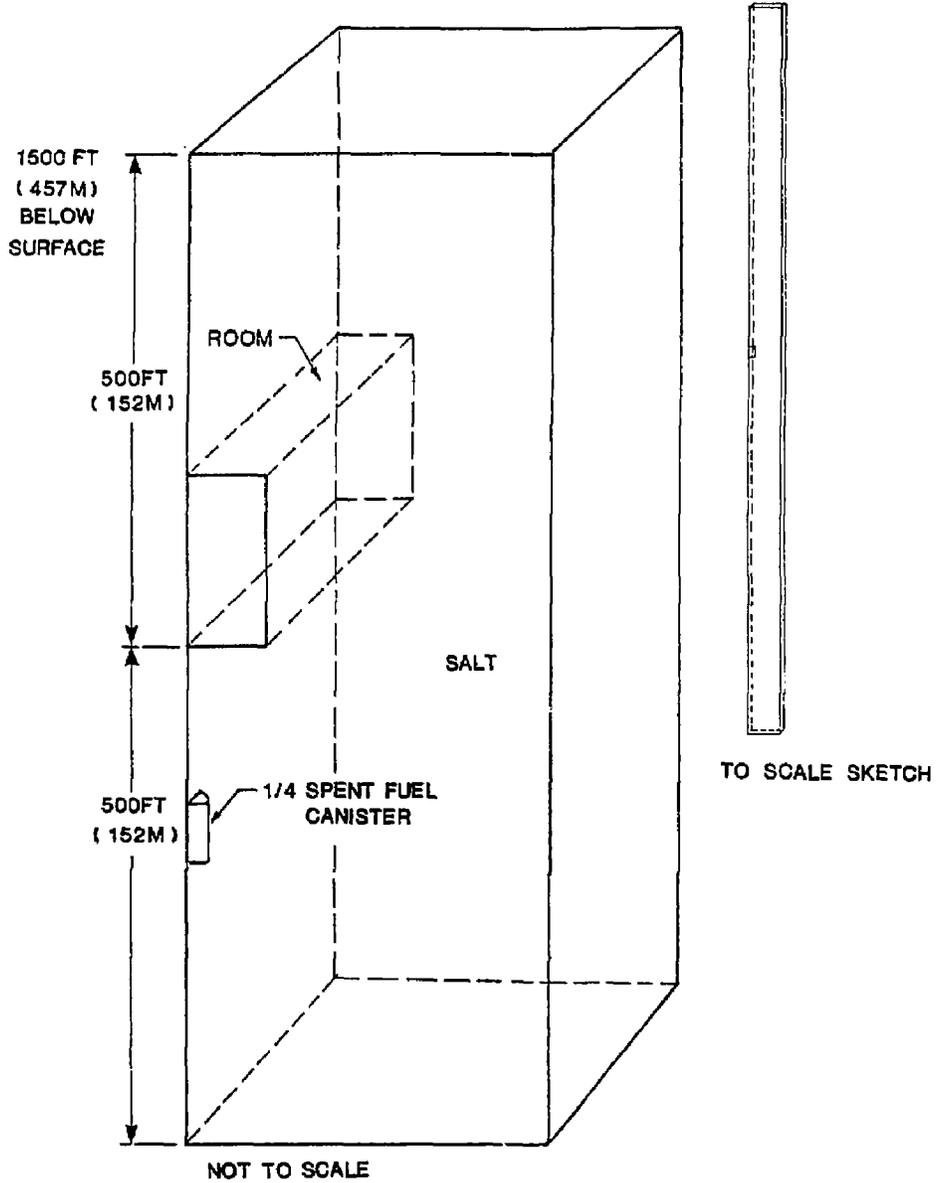


FIGURE 1 THREE-DIMENSIONAL UNIT CELL FOR PRELIMINARY TRUMP MODEL OF A GEOLOGIC SALT REPOSITORY .

applied to the baseline design in a preliminary analysis. This section describes the baseline design and the rationale for selecting various parameters. The design consists of specifications for the waste form, package design, and repository design.

Baseline Design

The waste form for the baseline design consists of one PWR spent fuel assembly, which is placed in its entirety inside of a carbon steel canister. The spent fuel is emplaced in the repository 10 years after reactor shutdown, as recommended by OWI for 25-year retrievable storage of spent fuel in salt.⁴ The uranium content was arbitrarily set at 0.426 MTU per assembly. Calculations with the ORIGEN code set the thermal power level at the time of emplacement at 0.55 KW per canister. Table 1 lists the power of the assembly as it decays with time.

In the context of a nuclear waste repository, the package is defined as everything that is placed inside of the emplacement hole. The main components of the package for a salt repository are the spent fuel assembly, canister, sleeve, and plug. The spent fuel is placed inside of the canister, which is then emplaced in a hole drilled into the floor of a mined room in the repository. The emplacement hole is lined with the carbon steel sleeve. The top is capped with a concrete plug.

TABLE 1

The thermal power of a baseline PWR assembly containing 0.426 MTHM, as it decays with time after reactor shutdown. The calculation was done with the ORIGN code for a reference equilibrium fuel cycle containing 3.3% enriched uranium and achieving a burnup of 33000 MWD/MT.

Time, Yr.	Watts
0 (Reactor Shutdown)	682,000.
10	550.
15	464.
20	412.
25	373.
30	339.
35	309.
40	283.
45	259.
50	237.
60	204.
75	164.
100	121.
150	80.1
200	62.6
300	48.1
400	40.8
500	35.5
700	28.1
1000	21.1
2000	11.8

The canister is designed to withstand credible handling accidents. It is 16 ft. in length with a 12.75 in. outside diameter, and is constructed of Schedule 60 stainless steel. The extra space inside the canister is filled with air.

The canister is emplaced within a carbon steel sleeve of 20 in. outside diameter and 1.5 in. wall thickness (Schedule 120). The purpose of the sleeve is to isolate the canister from thermal and lithostatic stresses and to provide for easy retrievability. Between the canister and sleeve is an air gap of 2.125 in. which allows the retrieval mechanism to slide down and lift the canister from the bottom. For our purposes, the sleeve is assumed to be in intimate contact with the surrounding salt.

A concrete plug is placed on top of the canister inside of the sleeve in order to isolate the canister from the emplacement room above. The plug length is 10 ft. (See Figure 2).

The baseline repository consists of a series of parallel emplacement rooms, 18 ft. wide and 30 ft. high. The high ceiling is needed for retrieval machinery. The rooms are separated by a salt pillar of 45 ft. width. The repository thermal load is set at 36 KW per acre as recommended by OWI.⁵ This fixes the canister pitch at 10.5 ft. The canisters are then emplaced in a row along the center of a room, 10 ft. below the floor. (See Figure 3)

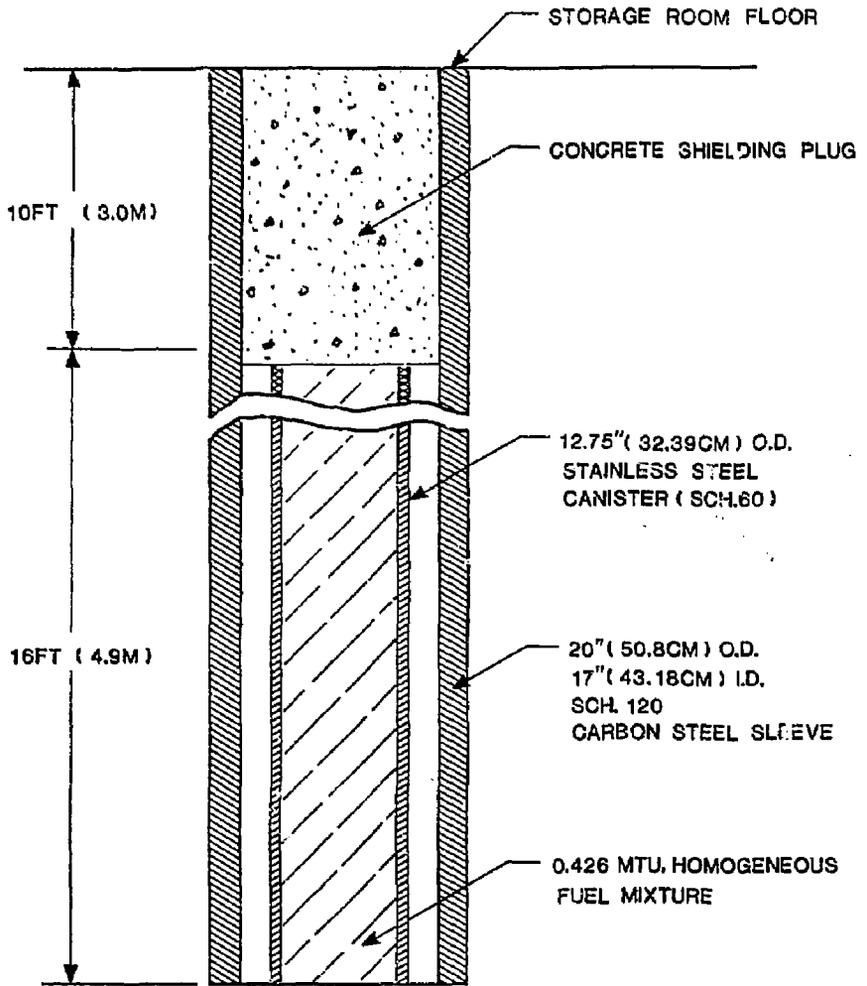


FIGURE 2 EMPLACEMENT PACKAGE DETAILS.

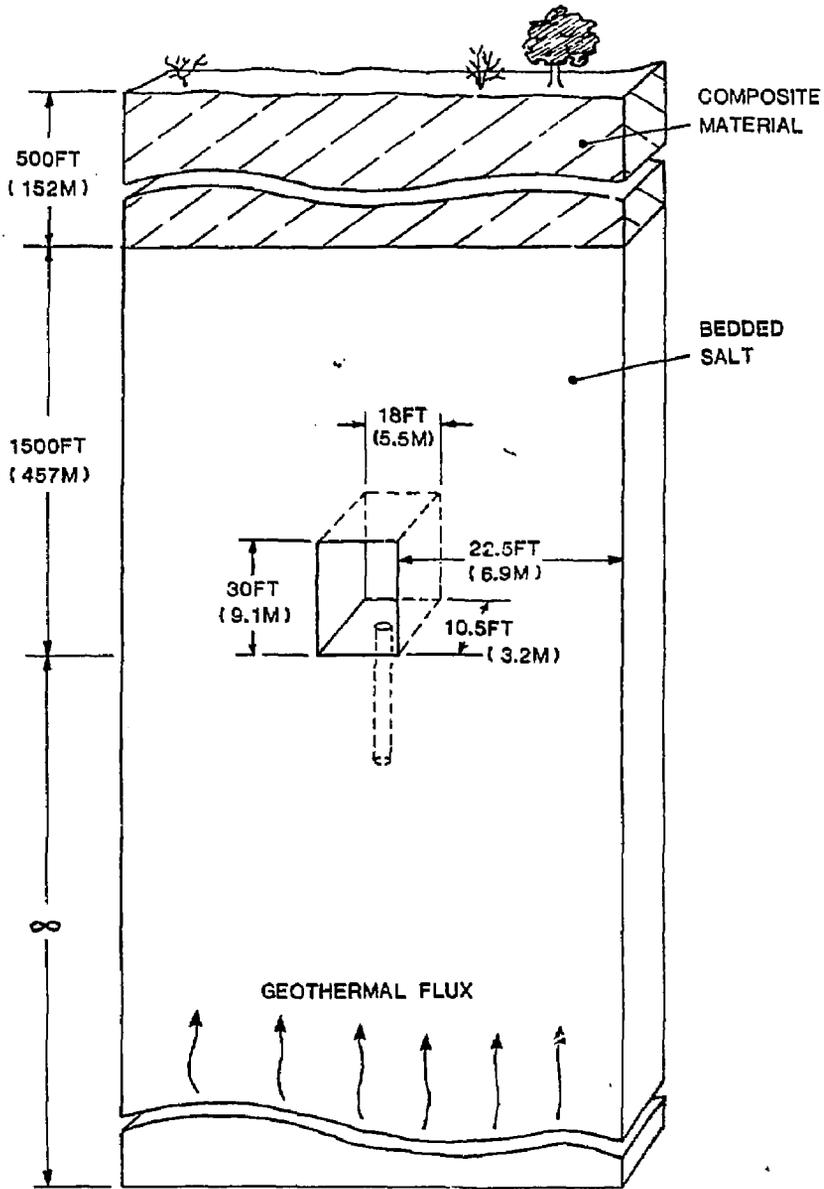


FIGURE 3 UNIT CELL DIMENSIONS USED IN BASELINE THERMAL ANALYSIS.

Geometric Model; Initial and Boundary Conditions

The advanced thermal model builds upon the preliminary model previously described. A unit cell with quarter symmetry is used, having adiabatic vertical boundaries. However, the top and bottom boundaries were extended and the boundary conditions modified in order to handle post-closure problems. It was found, in 50-year runs with a high-level waste source,³ that the horizontal isothermal boundaries caused a general underprediction of temperatures throughout the unit cell. This happens because the boundaries are artificially maintained at a lower temperature than they would eventually achieve from the heating of the unit cell. This effect could be significant for long-term problems.

In order to analyze a 1000-year problem, then, the top boundary of the unit cell was extended upward 1500 ft. to the surface of the earth. Boundary conditions at the surface include:⁶

- Solar heat flux of 73 Btu/ft.²-hr.
- Re-radiation to space (sky temperature of 45°F, earth's surface emissivity of .3).
- Convection to ambient air (air temperature 66°F, convective heat transfer coefficient of 3.1 Btu/hr.ft.²°F).

Perturbations from seasonal variations in these parameters are known to disappear fifty feet from the earth's surface.⁶ Since our concern here is to predict temperature responses near the heat source (as opposed to the far

field, i.e., earth's surface response), measured values were averaged over a one year time span to provide these numbers.

It was found, through simplified one dimensional modeling, that the medium 4500 ft. below the heat source would experience negligible temperature rise in 1000 years. This allowed us to place an isothermal boundary at this point which would essentially simulate a semi-infinite medium.

Initial temperatures throughout the cell were obtained by applying an appropriate geothermal flux ($140 \text{ Btu/ft.}^2\text{-year}$)⁷ to the bottom of the cell and allowing it to reach steady state without either the canister heat source or emplacement room ventilation. The temperature at the lower boundary is then fixed as an isothermal condition, which continues to apply the geothermal flux as long as the thermal "wave" from the heat source does not reach the boundary throughout the period of analysis.

The emplacement medium directly surrounding the canister, up to 1500 ft. above it, and down to the lower cell boundary consists of bedded salt. The remaining 500 ft. up to the surface of the earth is arbitrarily modeled as a homogeneous material with constant thermal properties representing an approximate average of granite, shale, and basalt. Materials used in the analysis, and their thermal properties, are listed in Table 2.

TRUMP is a generalized, multidimensional finite difference heat transfer code, capable of handling both rectangular and curvilinear geometries. It is possible to zone the problem so the near-source detail provides the resolution

TABLE 2

Thermal Properties of Materials Used in Baseline Analysis

Material	Density ₃ (lbm/ft. ³)	Specific Heat (Btu/lbm°F)	Conductivity (Btu/hr. ft.°F)
Air (storage room)	0.060	.240	0.018
304 Stainless Steel ⁸	488.0	.110	9.40
Carbon Steel ⁸ (sleeve)	487.0	.113	25.00
Spent Fuel* (homogenized)	541.0	.090	12.00
Concrete ⁸ (plug)	140.0	.210	0.60
"Composite geomedium**	165.0	.20	1.0
Bedded Salt ⁹ (major geomedium)		.204 (32°F)	3.09 (32°F)
		.217 (212°F)	2.61 (122°F)
		.222 (392°F)	2.23 (212°F)
		.230 (752°F)	1.94 (302°F)
			1.70 (392°F)
			1.53 (482°F)
			1.39 (572°F)
		1.29 (662°F)	
		1.18 (752°F)	

* These figures were obtained by "spreading out" the material properties of a PWR assembly to fill the emplacement canister.

** This material represents approximate material property averages of granite, basalt, and shale.

needed for temperature gradient measurements, while the far field is progressively more coarse, where detail is unnecessary. A side view of the mesh is shown in Figure 4, with details of each level in Figure 5.

Air Gap and Emplacement Room Heat Transfer Characteristics

The baseline design include a 2.125 in. air gap separating the spent fuel canister and the sleeve. Since the convection and radiation heat transfer across such a gap is not readily handled by TRUMP, a methodology was developed to model this phenomenon by means of an "analog conductivity" approach.¹⁰ Vertical enclosed flat plate convection correlations are coupled with gray body radiation exchange properties (emissivities and view factors) in an iterative procedure. The required heat flux is fixed, as well as one gap surface temperature. Then the radiation and convection equations are solved to yield the other gap surface temperature. Knowing the heat flux, the average gap temperature, and the annular gap dimensions, an equivalent conductivity can be determined that represents the thermal conductance of the gap at a given average gap temperature. This process yields a set of temperature/conductivity pairs that are easily used by TRUMP to simulate the convection and radiation heat transfer. The set used in this analysis is given in Table 3.

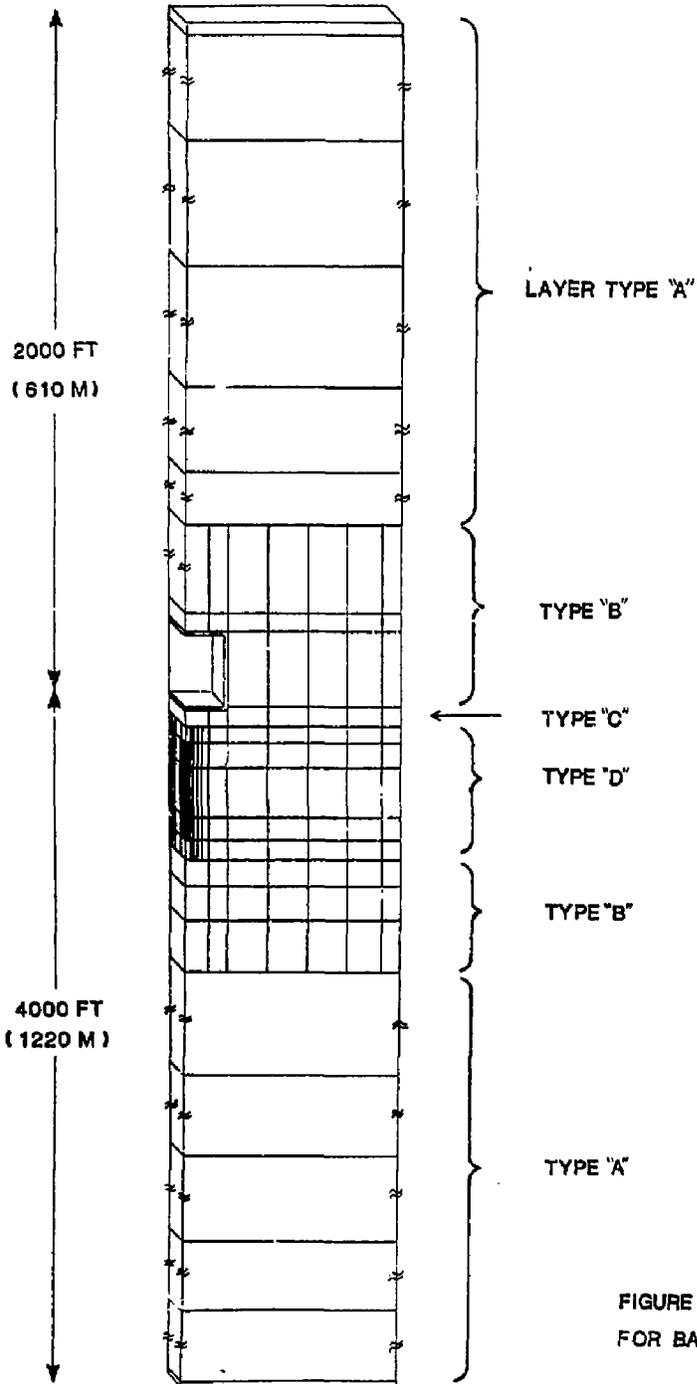
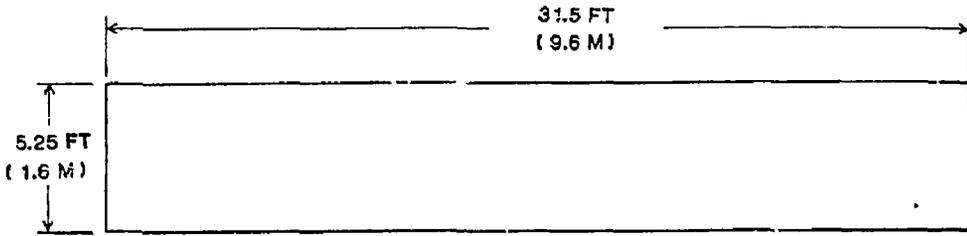
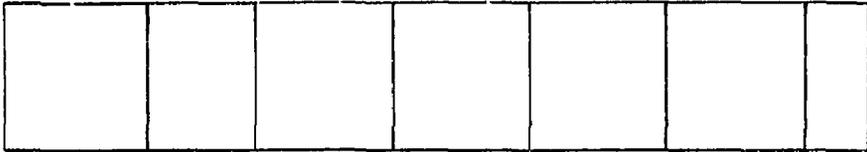


FIGURE 4 TRUMP MESH
FOR BASELINE ANALYSIS



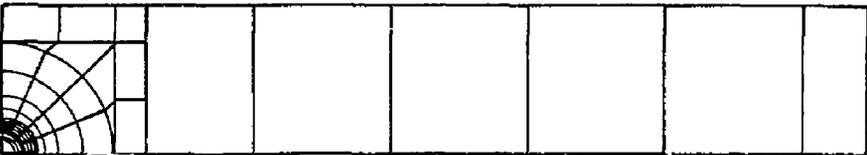
LAYER TYPE "A"



LAYER TYPE "B"



LAYER TYPE "C"



LAYER TYPE "D"

FIGURE 5: LAYER DETAILS FOR BASELINE MESH SHOWN IN FIGURE 4. MASS OF MATERIAL IS CONCENTRATED AT GEOMETRIC CENTER OF EACH NODE.

TABLE 3

Analog conductivity set representing the radiation and free convection heat exchange across the 2.125 inch annular gap of the baseline design. Surface emissivities were set at .75 for both the canister and sleeve surfaces.

Temperature (°F)	Conductivity (Btu/hr-ft.°F)
100.0	.160
151.5	.192
210.9	.238
259.3	.284
367.8	.337
381.2	.431

Emplacement room heat transfer is modeled as either ventilated or non-ventilated. Correlations developed by McAdams¹¹ and summarized by Davis¹² represent the ventilated situation with convection heat transfer coefficients as follows:

$$\begin{aligned} \text{From floor:} \quad h &= .22 (T_f - T_\infty)^{1/3} \\ \text{From ceiling:} \quad h &= .068 (T_c - T_\infty)^{1/4} \\ \text{From walls:} \quad h &= .19 (T_w - T_\infty)^{1/3} \end{aligned}$$

where temperatures are in °F, h is Btu/hr-ft.²-°F, and T_∞ is the bulk temperature of the air flowing through the repository. In this analysis, T_∞ was set at a constant 79°F (26°C).

Convection heat transfer in the non-ventilated case is modeled with a correlation developed for enclosed spaces:¹² $h_s = 0.125 (T_f - T_c)^{1/3}$, where h_s is the coefficient for floor to ceiling convection, and T_f and T_c are those surface temperatures. For our purposes, this heat transfer was modeled as a two-step process of convection from floor to air and from air to ceiling. The convection coefficient for each step is then given by: $h = 2 h_s$. Convection from the walls to the air is included as before.

Time-averaged temperature differences between bulk air and the surfaces are used, and the coefficients can then be considered constant throughout the period of analysis. (For our purposes the system thermal response is relatively insensitive to the magnitudes of convection coefficients). Values for both ventilated and non-ventilated cases are given in Table 4.

Gray body radiation is modeled in the room, with salt surface spectral emissivity of .75.

TABLE 4

Convective heat transfer coefficients applied to the storage room heat transfer.

	Ventilated (Btu/ft. ² hr°F)	Non-Ventilated (Btu/ft. ² hr°F)
Floor	.44	.36
Wall	.38	.18
Ceiling	.11	.36

ANALYSIS AND RESULTS

The advanced model was utilized to study three areas of concern:

- 1) Thermal response of the canister with and without an annular air gap.
- 2) Comparison of ventilated vs. non-ventilated cases.
- 3) Room cool-down responses for retrieval operations.

The analysis focused on the thermal responses of the canister surface, emplacement package components, the near and very near field emplacement medium, and both the air and surfaces of the emplacement room. Graphical results provide time/temperature responses and temperature distributions for selected locations.

Gap/No Gap Comparison

In previous thermal analyses,^{2,3} it has been assumed that the canister is placed in perfect thermal contact with the geomedium. The first study made with the advanced baseline design compared results obtained from modeling the emplacement package with and without an annular gap. The perfect thermal contact case assumed the canister to be placed directly into the salt with zero clearance, while the baseline case was analyzed as described in Figure 2, with a 2.125 in. gap separating canister and sleeve.

The net effect of this particular gap configuration is to raise the canister surface peak temperature 10°F over the perfect thermal contact case.

Figure 6 shows the 1000 year temperature histories for each case. The gap, however, has no influence on the surrounding medium. The emplacement room in both cases is unventilated.

Note that the temperature history for the canister surface in the perfect thermal contact case (Figure 6) is characterized by a quick rise and sharp peak at 30 years after emplacement, followed by a decline to a minimum at 520 years, then a small rise to a broad peak around 620 years and eventual decline. This unusual double-peaked response was thoroughly investigated by using simple 2-D and 1-D models to explain the behavior from the standpoint of the physical heat flows occurring as well as from the theoretical standpoint of superposition. It was concluded that the double-peaked response is due to the shape of the spent fuel decay curve and the thermal properties of salt, as inputs to the calculation. The complete analysis of this case is presented in Appendix A.

Comparison of Ventilated and Unventilated Cases.

Methods of modeling ventilated and unventilated emplacement rooms have been described earlier. The baseline design was studied for both scenarios. Temperature histories plotted in Figure 7 show responses of the canister surface and emplacement room floor in each case. The ventilation air temperature is 79°F, circulating through the room at 10,000 CFM. At such a low power level, this ventilation effectively maintains the room floor at the temperature of the air after the first hundred years. The canister surface experiences almost immediate reduction in temperature from its initial state.

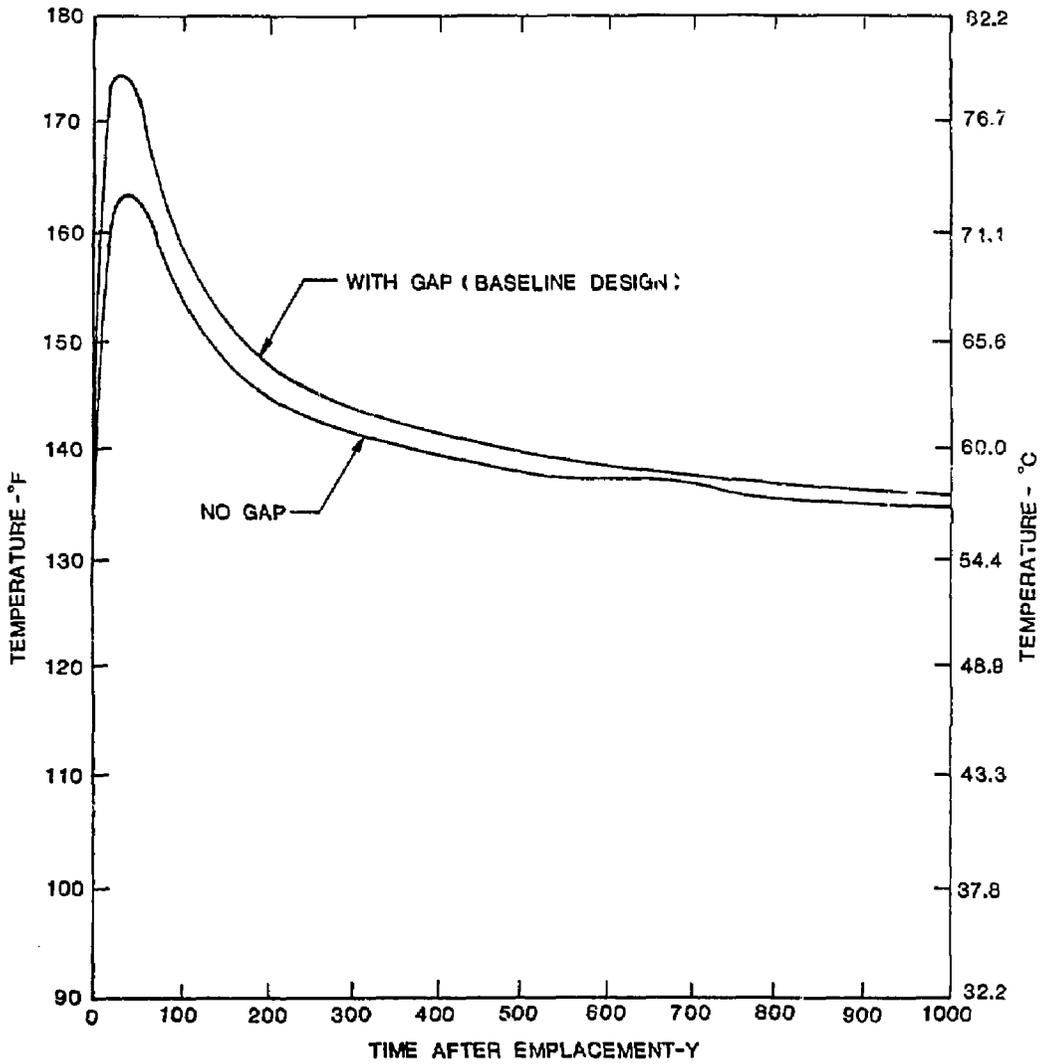


FIGURE 6 1000-YEAR TEMPERATURE HISTORIES OF CANISTER SURFACE WITH AND WITHOUT A 2.125-INCH GAP SEPARATING CANISTER AND SLEEVE.

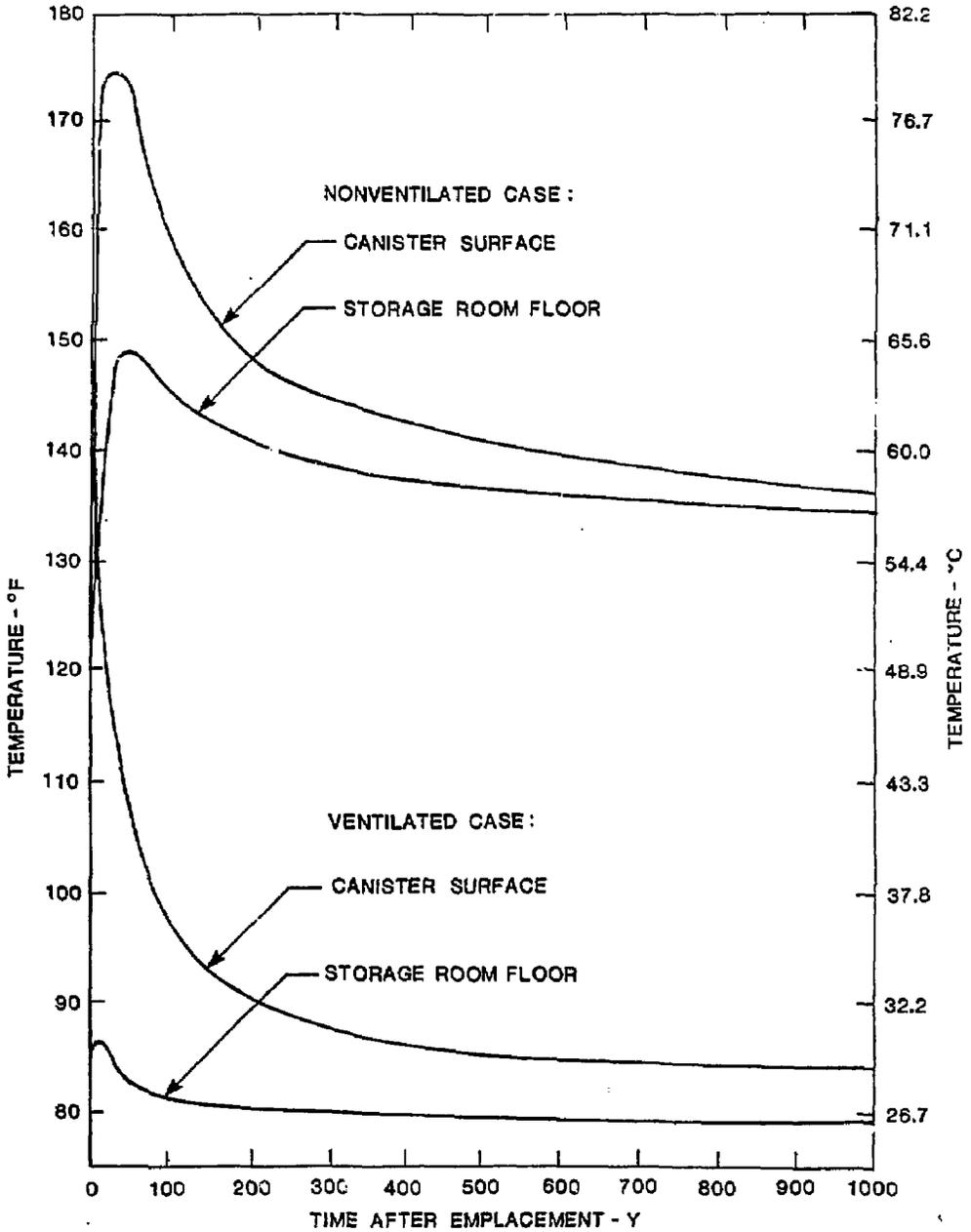


FIGURE 7 CANISTER SURFACE AND STORAGE ROOM FLOOR TEMPERATURE HISTORIES FOR BOTH VENTILATED (WITH 79°F AIR AT 10,000 CFM) AND UNVENTILATED CASES.

Ventilation is also effective at removing a large fraction of the heat generated (Figure 8). After 1 year, 55% of the cumulative heat generated has been removed by ventilation. This fraction increases to 90% after 44 years. After 30 years the rate of heat removal by ventilation exceeds the rate of heat generation, causing a decline in the average temperature of the unit cell. Sensitivity studies are needed to determine the importance of ventilation for higher canister power.

Room Cool-Down Response

A conceivable scenario of repository operations is to close off a section of the repository (no ventilation) after it has been filled with spent fuel. At a later time, if reentry is necessary for any reason, ambient conditions in the storage room would become a critical consideration for personnel and machinery operations. Most probably a ventilation system would be activated to reduce the room temperature to an acceptable level.

TRUMP runs were executed to simulate scenarios of a non-ventilated room, with ventilation by 79°F air initiated at 5, 10 and 50 years. Emplacement room floor temperature histories are shown in Figure 9. In 5- and 10-year scenarios the floor, which is slightly warmer than the walls or the ceiling, cools down to under 100°F in roughly 2 weeks and 7 weeks, respectively. The 50-year case required 6 months to reach 100°F. Figure 10 shows the temperature response of the floor to ventilation for these cases on an expanded, overlaid time scale, for easy comparison of cooling times.

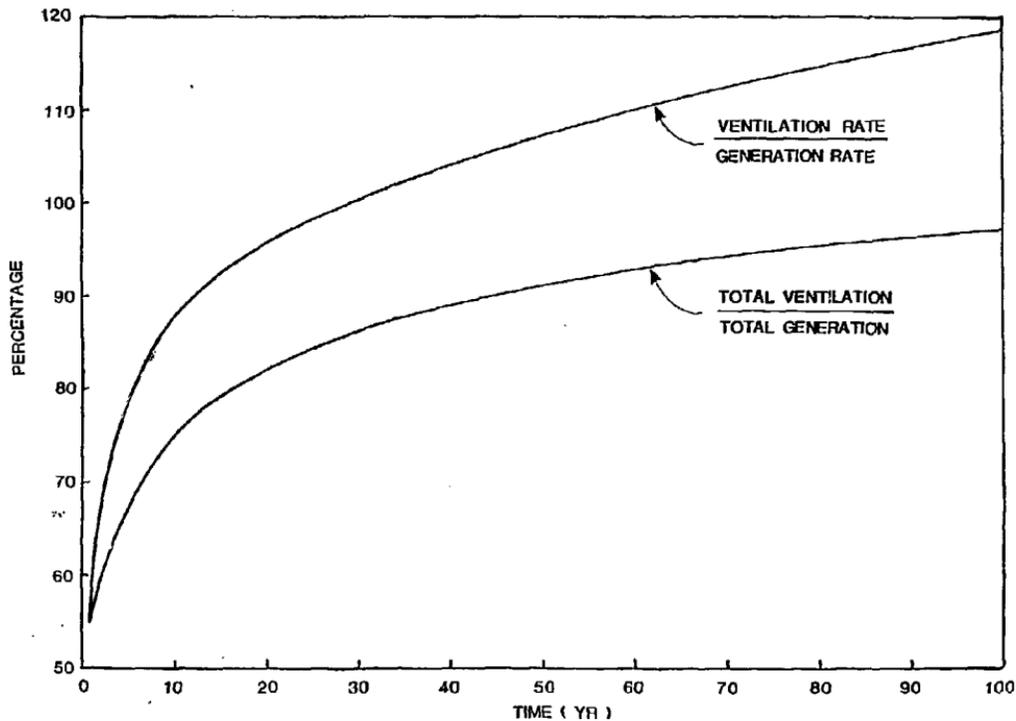


FIGURE 8 A COMPARISON OF VENTILATION HEAT REMOVAL AND THE HEAT GENERATION IN THE BASE CASE

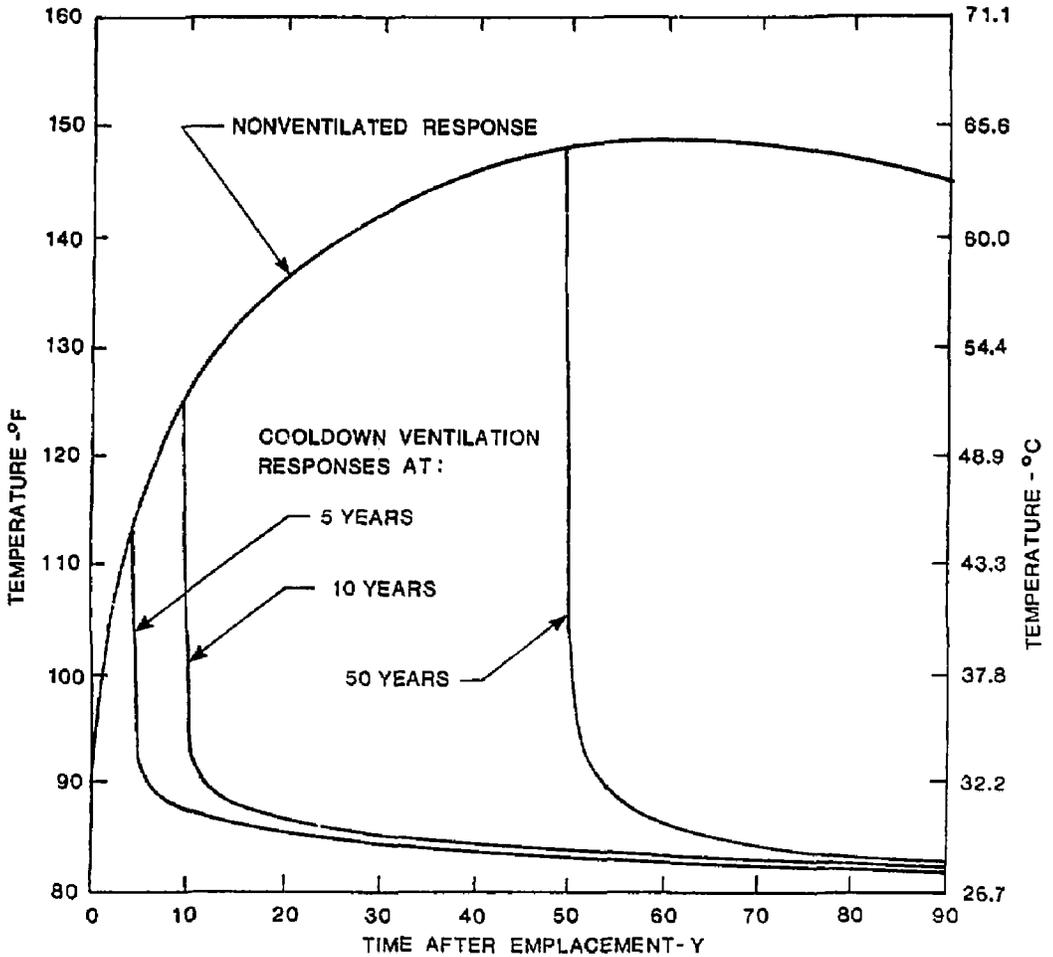


FIGURE 9 STORAGE ROOM FLOOR TEMPERATURE HISTORIES REPRESENTING COOL-DOWN (10,000 CFM OF AIR) FROM AN UNVENTILATED STATE AFTER 5, 10, AND 50 YEARS.

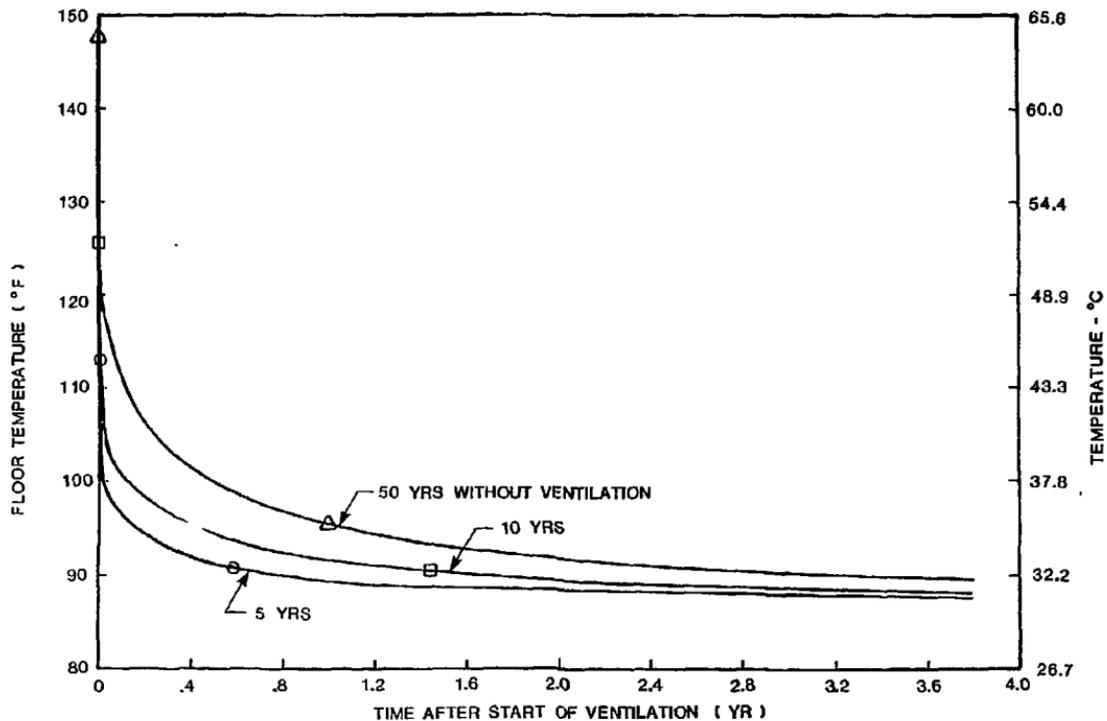


FIGURE 10 TEMPERATURE RESPONSE OF THE FLOOR TO VENTILATION AFTER VARIOUS PERIODS OF NO VENTILATION

CONCLUSIONS AND RECOMMENDATIONS

The advanced 3-D thermal model was utilized to study a low power spent fuel emplacement. Additional detail was included to represent a more complicated emplacement package, and boundary condition refinements allowed for 1000 year simulations. An analog conductivity approach was used to represent the annular air gap separating the canister and sleeve.

Significant conclusions can be drawn from this analysis:

- Annular air gaps surrounding an emplaced spent fuel canister increase the canister surface temperature significantly over that expected from a perfect thermal contact case. Although the maximum temperature difference is only 10°F in this low power situation, special attention should be given to gap design for higher areal power loading levels, and lower emplacement media conductivities than bedded salt.
- Ventilation at low power levels has an immediate cooling effect on the canister and effectively maintains the room surfaces at the temperature of the ventilation air.

- Emplacement room cool-down simulations showed the time required to reduce the floor temperature to 100°F from an unventilated state to be on the order of 2 weeks to 6 months, depending on the time when ventilation is initiated. These time requirements could inhibit immediate retrieval operations.

The unit cell approach to modeling a repository is a gross simplification. For strictly thermal purposes, however, it does provide "worst case" temperature responses and can be used to bound results expected from the real problem. With these limitations in mind, the following recommendations are made for future thermal analysis work:

- 1) A detailed study should assess the accumulative air heating effect of many canisters emplaced below a corridor. This modeling effort used a constant ventilation air temperature, which may hold only for a particular unit cell in a corridor.
- 2) The unit cell method addresses one emplacement in an infinite array of canisters, all generating equal power with identical boundary conditions. Asymmetrical situations such as sequential emplacement hole loading, tunnel excavation occurring adjacent to a loaded and sealed room, and thermal effects on a canister at the edge of the array should be addressed.

- 3) A sensitivity analysis is needed to provide detailed information for storage room cool-down scenarios. Results of this work could dictate specific requirements for retrieval machinery.

ACKNOWLEDGMENTS

The authors would like to acknowledge the assistance provided by Billy W. Davis in the development of the air gap model and by Harris B. Levy in generating the ORIGEN results.

REFERENCES

1. A. L. Edwards, TRUMP: A Computer Program for Transient and Steady-State Temperature Distributions in Multidimensional Systems, Lawrence Livermore Laboratory Report, UCRL-14754, Rev. 3 (September 1972).
2. T. J. Altenbach, Interim Report On Nuclear Waste Depository Thermal Analysis, Lawrence Livermore Laboratory Report, UCID-17865 (July 1978).
3. T. J. Altenbach, Three-Dimensional Thermal Analysis Of A High-Level Waste Repository, Lawrence Livermore Laboratory Report, UCID-17984 (April 1979).
4. R. K. Kibbe, A. L. Boch, Technical Support for GEIS: Radioactive Waste Isolation in Geologic Formations, Repository Reconceptual Design Studies: Salt, Office of Waste Isolation Report Y/OWI/TM-36/8 (April 1978).
5. J. E. Russell, Areal Thermal Loading Recommendations For Nuclear Waste Repositories in Salt, Office of Waste Isolation Report Y/OWI/TM-37, (June 1979).
6. R. K. Kibbe, A. L. Boch, Technical Support for GEIS: Radioactive Waste Isolation in Geologic Formations, Thermal Analyses, Office of Waste Isolation Report Y/OWI/TM-36/19, (April 1978).
7. G. H. Llewellyn, Prediction of Temperature Increases in a Salt Repository Expected from the Storage of Spent Fuel or High-Level Waste, Oak Ridge National Laboratory, Oak Ridge, Tennessee, ORNL/ENG/TM-7 (April 1978).
8. B. V. Karlekar, R. M. Desmond, Engineering Heat Transfer, West Publishing Company, New York, 1977.
9. C. M. Koplik, D. L. Pentz, R. Talbot, Information Base for Waste Repository Design, The Analytic Sciences Corporation, Reading, Mass., Vol. 3, TR-1210-1 (August 1, 1978).
10. H. Cheung, B. W. Davis, W. E. Lowry, Annual Air Space Effects on Nuclear Waste Canister Temperatures in a Deep Geologic Waste Repository, Lawrence Livermore Laboratory, Livermore, California, UCRL-84152.
11. W. H. McAdams, Heat Transmission, McGraw-Hill Book Co., New York, 1954.
12. B. W. Davis, Convection and Thermal Radiation Analytical Models Applicable to a Nuclear Waste Repository Room, Lawrence Livermore Laboratory Report UCID-18103, 1979.
13. L. D. Ramspott, et al., Technical Concept for Test of Geologic Storage of Spent Reactor Fuel in the Climax Granite, Nevada Test Site, Lawrence Livermore Laboratory, UCID 18197, 1979.

APPENDIX A:
ANALYSIS OF RESULTS FROM THE NO GAP - UNVENTILATED CASE

INTRODUCTION

In Figure A1, a temperature history is plotted for a node on the canister surface at the canister midplane, in a case assuming perfect thermal contact between the canister and salt and no ventilation in the storage room. These results show a quick rise and sharp peak at 30 years after emplacement, followed by a decline to a minimum at 520 years, then a small rise to a broad peak around 620 years and eventual decline.

Our base case results are not the first to reveal a double-peaked thermal response in a repository. Figure A2, extracted from Reference 13, shows temperature histories calculated from an analysis of the Spent Fuel Test in the Climax granite at the Nevada Test Site. The 2.5-year curve is also double-peaked. This response is noted in the report, but no explanation is offered.

As the consequence of interest in these results, we have thoroughly investigated the base case thermal response. In order to fully explain the heat transfer occurring in the repository, we have constructed very simple models which allow many runs to be completed quickly. Following is a description of a simple 2-D model with heat input, transfer, and output flows analogous to the 3-D base case. The thermal response will be explained from

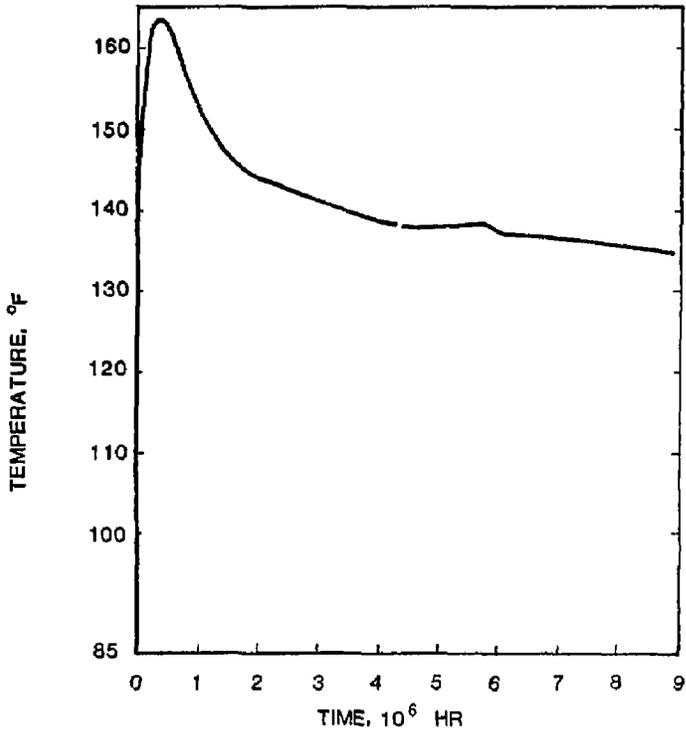


FIGURE A-1 TEMPERATURE HISTORY FOR BASE CASE, UNVENTILATED ROOM, PERFECT THERMAL CONTACT, AT THE CANISTER SURFACE. NOTE DOUBLE PEAK.

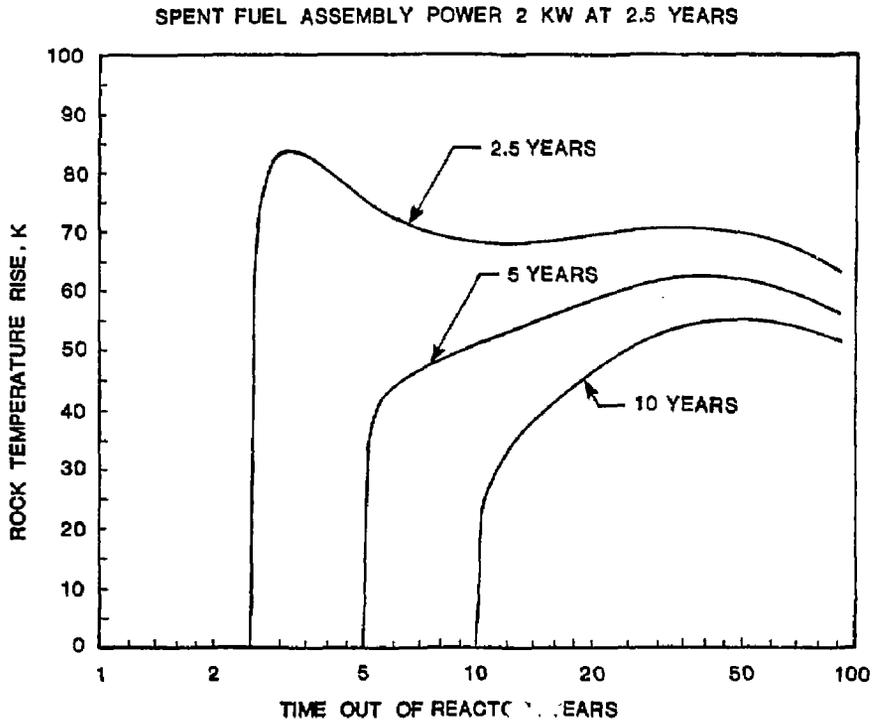


FIGURE A-2. CENTERHOLE ROCK SURFACE TEMPERATURE HISTORY AT THE CANISTER MIDPLANE FOR A HYPOTHETICAL REPOSITORY WITH FUEL ASSEMBLIES ON A 3 M X 15 M SPACING. FUEL STORED AT 2.5, 5 OR 10 YEARS OUT OF REACTOR. (REF. 13)

the standpoint of the physical heat flows occurring, as well as from the numerical/mathematical standpoint of superposition. Also described is an elementary 1-D model, which is used to demonstrate how two and even three peaks are possible in the thermal response from a decreasing heat source.

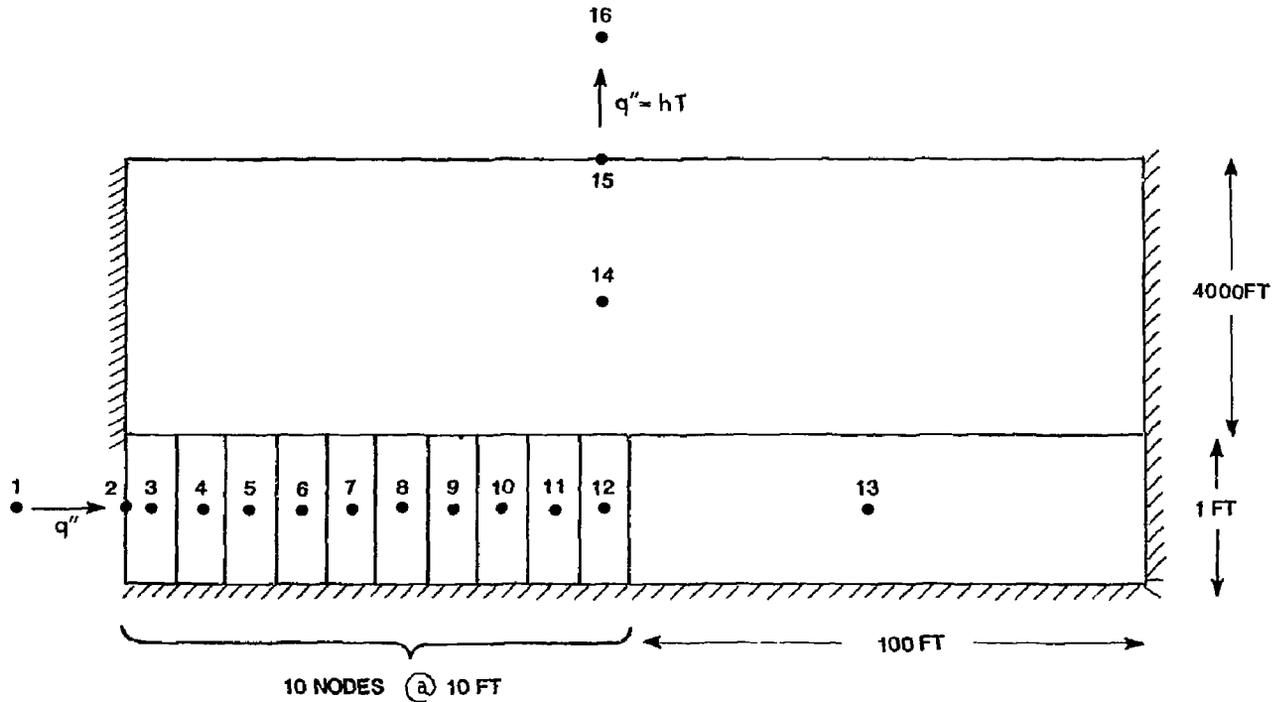
SIMPLE 2-D MODEL

In order to demonstrate the validity of a double-peaked temperature response in the complex 3-D TRUMP model, a very simple 2-D model was set up. The 2-D model contains only 14 nodes (nos. 2-15) which crudely represent the repository. Figure A3 shows the geometry used. A heat flux is applied from a source (node 1) to the lower left surface (node 2). Heat is transferred by conduction through the material and leaves via convection from the top surface to the sink (node 15 to 16). The convection coefficient is constant and the ambient temperature is fixed at zero. All other surfaces are adiabatic.

The specified heat flux varies with time, having a normalized magnitude and the same shape as the spent fuel decay curve as calculated by the ORIGEN code and used in the 3-D model (Figure A4). Thermal properties in the model are constant and represent salt: density = 135 Lb/ft³; heat capacity = 0.21 BTU/lb; conductivity = 2.5 BTU/ft/hr/°F.

This simple model is analogous to the 3-D model in that a heat flux is imposed on the salt, which then transfers heat through a large distance and rejects it from the upper surface. Figure A5 shows the temperature response from this 2-D model, which is similar in shape to our 3-D result. The surface

FIGURE A-3. THIS SKETCH SHOWS THE SIMPLE 2-D MODEL WITH A TIME-DEPENDENT HEAT FLUX APPLIED AT NODE 2 AND HEAT REMOVAL BY CONVECTION AT NODE 15.



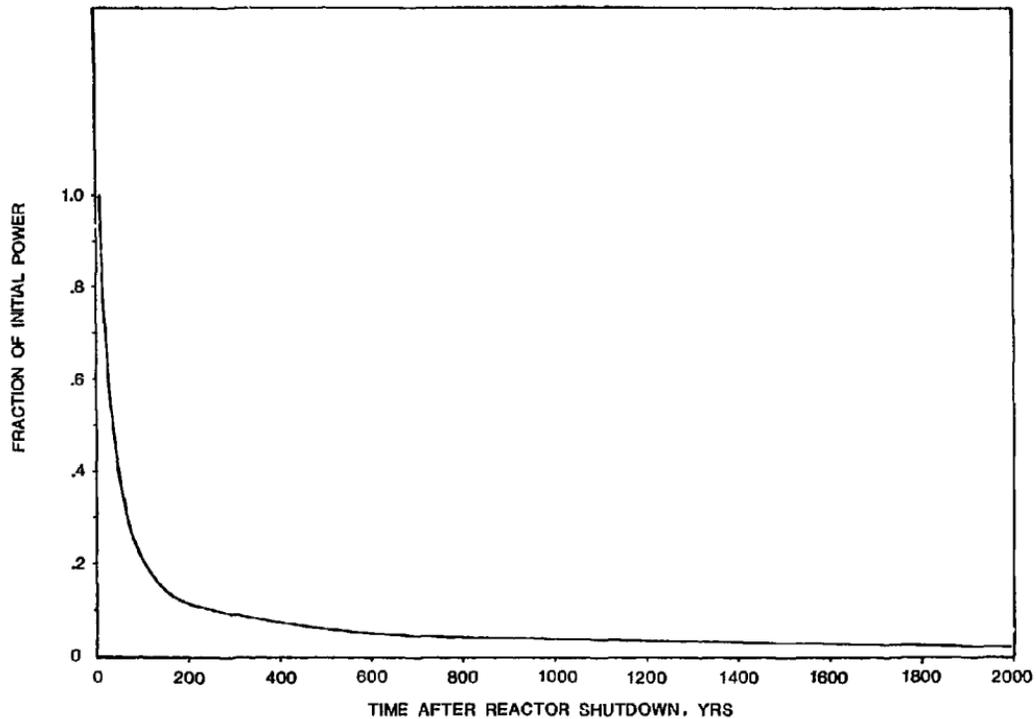


FIGURE A-4. NORMALIZED DECAY CURVE FOR SPENT FUEL RELATIVE TO THERMAL POWER AT 10 YR

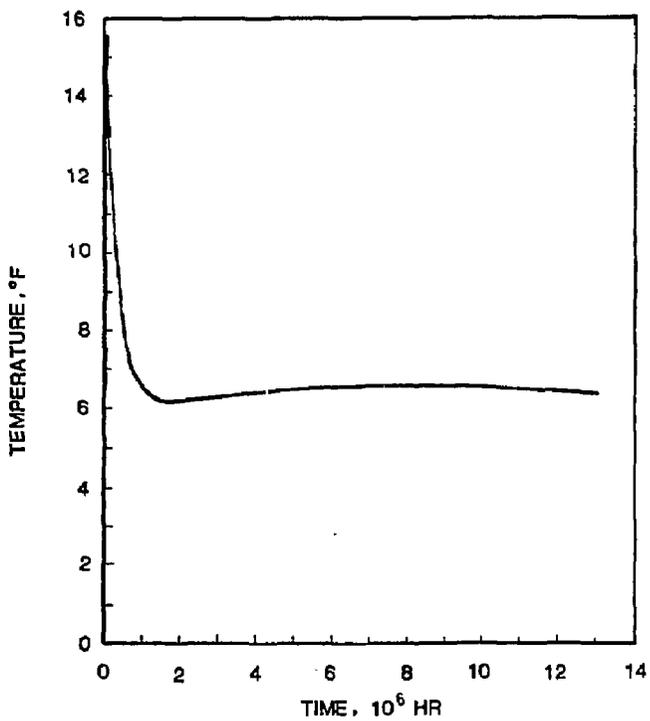


FIGURE A-5. TEMPERATURE HISTORY FOR THE NODE AT THE HEATED SURFACE IN THE 2-D MODEL ALSO HAS TWO PEAKS.

temperature (node 2) is plotted vs. time to 1500 years, again revealing a distinct double peak. Initial temperatures are zero, then they rise, establishing a gradient to conduct away the applied heat flux. The gradient slowly flattens as the heat source decays rapidly, causing the first maximum when the gradient is just able to remove the incoming heat. The temperature then drops as the heat source is decaying faster than the gradient. As the gradient continues to flatten, the source changes from a rapid decay to a very slow decay, eventually inputting as much heat as is being removed. This point is the minimum between peaks.

As the gradient continues to decrease after the time of the temperature minimum, the heat source decays very slowly. The temperature then rises because the source is producing more heat than the flat gradient can conduct away. The second temperature maximum occurs when these two are equal. Eventually the change in the gradient is slow enough so that all decaying heat can again be conducted away, causing the final decline in temperature.

The response in Figure A5 can also be explained by using the principle of superposition to decompose the problem to two simpler problems. The decomposition considers two independent problems. The first uses the normalized spent fuel source exactly as before for the time period of 0 to 140 years after emplacement, at which time the source drops to zero. The temperature response is calculated to 1500 years. The second problem in the decomposition has no thermal source for the first 140 years, then follows the spent fuel decay curve from 140 to 1500 years. Since the two simpler problems are linear, the principle of superposition says that the temperature responses of these two problems can be superposed to give the response for the original problem.

Figure A6 shows the temperature history for node 2 in the first decomposition with 0 to 140 year source. The results during this time are identical to Figure A5. At 140 years, there is a steep drop when the source is removed, followed by a slow decline to 1500 years. Figure A7 shows the temperature history for node 2 in the second decomposition with the 140-1500 year source. The response is zero until 140 years, when the temperature rises rapidly. (The slight dip after the peak is another example of a double-peaked response as explained earlier.) After the initial rise and slight dip, the temperature rises gradually as the source decays slowly.

When Figures A6 and A7 are superposed, the result is Figure A5. From these decomposed problems it is clear that the first peak in Figure 5 is due to the relatively powerful and rapidly decaying source early in time. The second peak is due to the slowly decaying source in later times. The temperature rise from this part of the source curve (Figure A7) is steeper than the decline from the early part of the source curve (Figure A6), yielding a net rise in the superposed results.

The double-peaked nature of the 3-D results (Figure A1) may also be explained using this superposition argument. However, superposition does not hold precisely because the 3-D model is not linear, using thermal properties dependent on temperature. Nevertheless, the 3-D results shows a sharp peak from the rapidly decaying heat source and a broad peak from the relatively constant source of later times.

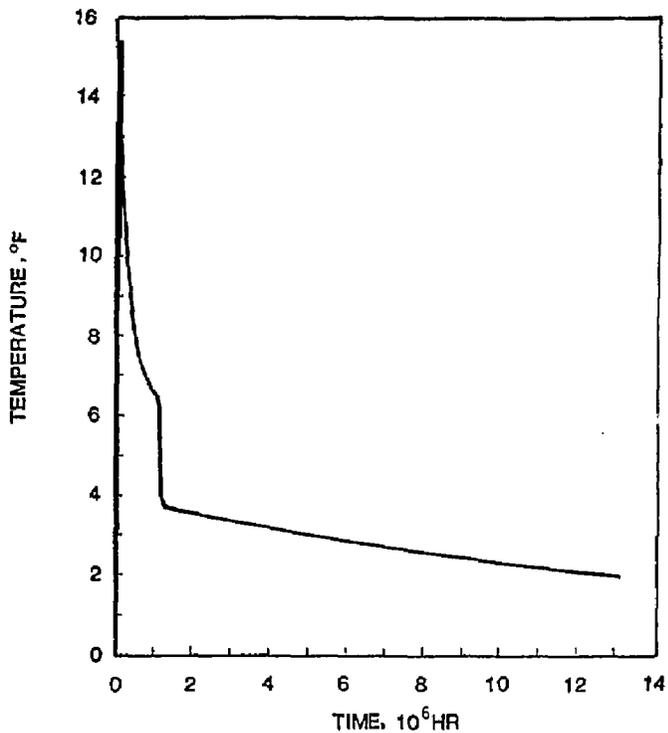


FIGURE A-6. TEMPERATURE HISTORY FOR NODE 2 IN THE FIRST OF THE DECOMPOSED PROBLEMS. THE HEAT SOURCE FOLLOWS THE SPENT FUEL DECAY CURVE FOR 140 YEARS, THEN DROPS TO ZERO.

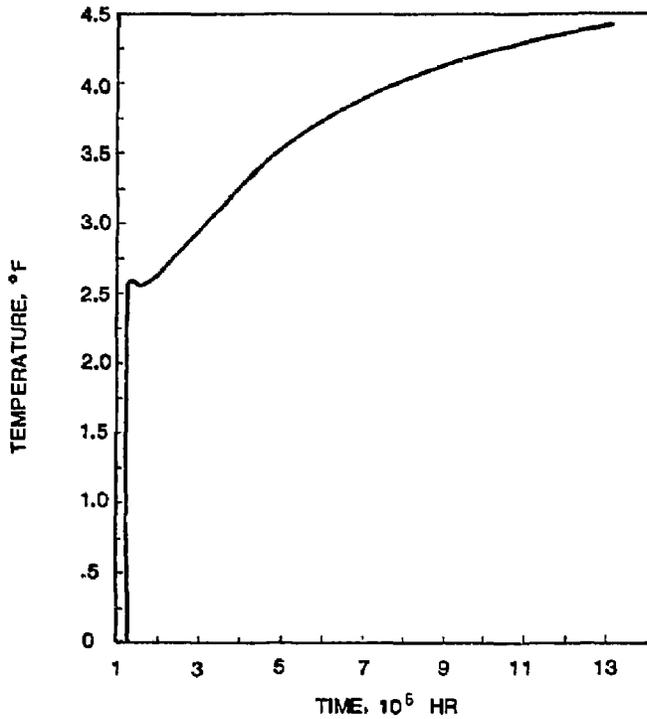


FIGURE A-7. TEMPERATURE HISTORY FOR NODE 2 IN THE SECOND OF THE DECOMPOSED PROBLEMS. THE HEAT SOURCE IS ZERO FOR THE FIRST 140 YRS, THEN FOLLOWS THE SPENT FUEL DECAY CURVE FOR 140-1500 YRS.

1-D MODELS

Two simple one-dimensional models were set up to show that the occurrence of a double-peaked temperature response is primarily controlled by the shape of the heat source decay curve and the thermal properties of the transport medium. The response is not an artifact due to the boundary conditions used in the 3-D and 2-D models. One model uses the spent fuel source in an infinite plane wall medium of reduced conductivity to demonstrate double-peaked response. The second model uses two-piece and three-piece linear approximations to the decay in a finite adiabatic medium with a reduced diffusivity to demonstrate both double- and triple-peaked responses.

An infinite medium is modeled as in Figure A8. The same flux is applied at node 2 as in the 2-D model. The conductivity of the medium was dropped from 2.5 to 0.25 BTU/hr.ft.°F, so it no longer represents salt. Heat is then conducted away from the source toward node 20. However, after 1500 years only a negligible amount of heat reaches node 20, maintaining the infinite medium approximation.

The results are plotted in Figure A9 for the temperature history of node 2. Figure A10 shows temperature profiles out to a distance of 155 ft. from the source for various times. Included are the times of the three extremes and times on either side of each. Note that the thermal gradient is always becoming flatter from early in the problem, even though temperatures out as far as 25 ft. show the familiar double-peak response.

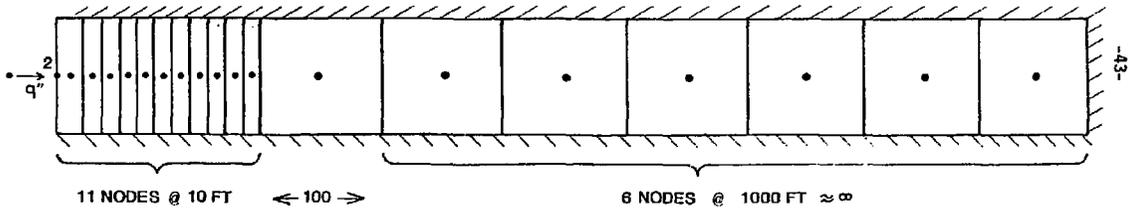


FIGURE A-8 SIMPLE 1-D "INFINITE MEDIUM" MODEL. A NORMALIZED SPENT FUEL HEAT FLUX IS APPLIED AT NODE 2.

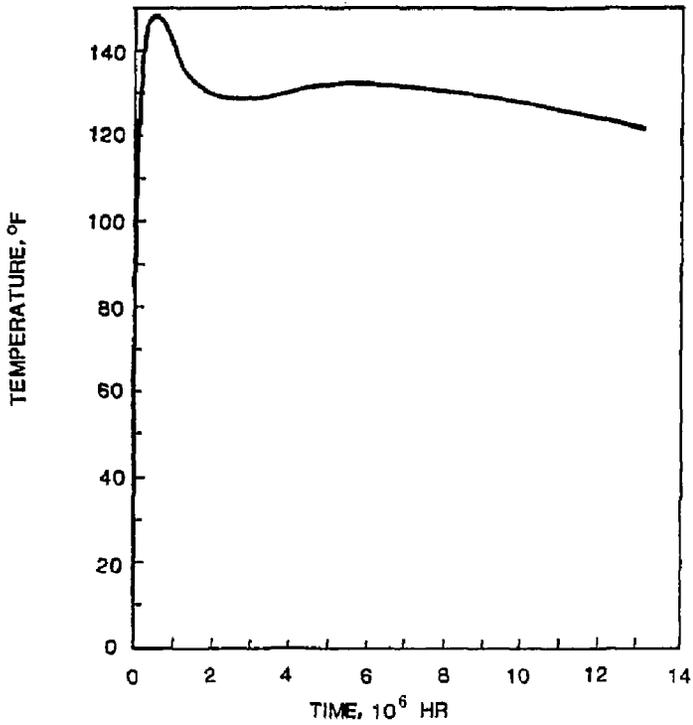


FIGURE A-9. TEMPERATURE HISTORY FOR NODE 2 AT THE HEATED SURFACE OF A 1-D INFINITE PLANE WALL. THE HEAT SOURCE FOLLOWS THE NORMALIZED SPENT FUEL DECAY CURVE.

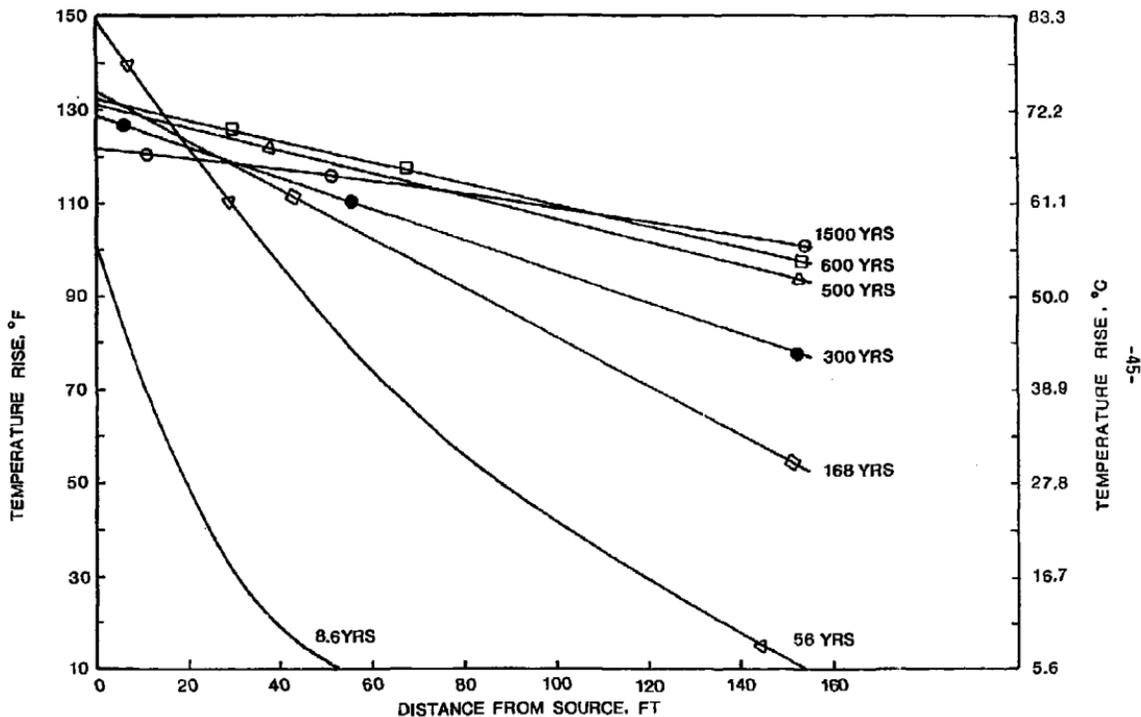


FIGURE A-10. TEMPERATURE RISE VS DISTANCE FROM SOURCE IN AN INFINITE MEDIUM FOR VARIOUS TIMES

Figure A11 shows a 1-D model of a finite plane wall with an adiabatic boundary 100 ft. from the source. Two cases were run with a heat source following a piece-wise linear decay. In the first case the source drops from a relative value of 1.0 at 0 years to 0.1 at 100 years and 0 at 1000 years. The second case uses 3 linear pieces for the source decay: 1.0 at 0 years, to 0.3 at 171 years, to 0.05 at 513 years, to 0 at 1000 years. In this case the material properties were set at a conductivity of 0.5 BTU/hr.ft.^{°F}, specific heat of 2.0 BTU/lb^{°F}, and density of 135 lb/ft³. This provides for a decrease in thermal diffusivity from 0.0882 ft²/hr. for salt to 0.0019 in this problem.

The low diffusivity slows down the heat transfer in the system and provides greater definition of the temperature peaks. Figure A12 shows the temperature history for node 2 in the first case using a two-piece linear source. Each peak can be attributed to its corresponding segment from the heat source decay.

Figure A13 shows the temperature history for node 4 in the second case using a three-piece linear source. In this case the three peaks each correspond to a segment from the heat source. It should be emphasized that the thermal response in these 1-D, 2-D, and 3-D repository problems is primarily governed by the heat source decay and material thermal properties. The existence of temperature maxima (whether 1, 2, 3 ...) is strongly dependent on these parameters. In these 1-D cases, we have artificially input a set of parameters which produce multiple peaks.

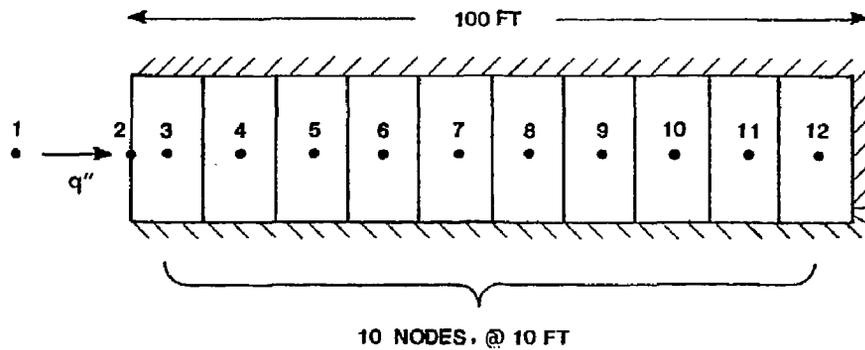


FIGURE A-11. SIMPLE 1-D MODEL WITH AN ADIABATIC BOUNDARY 100 FT FROM THE APPLIED HEAT FLUX .

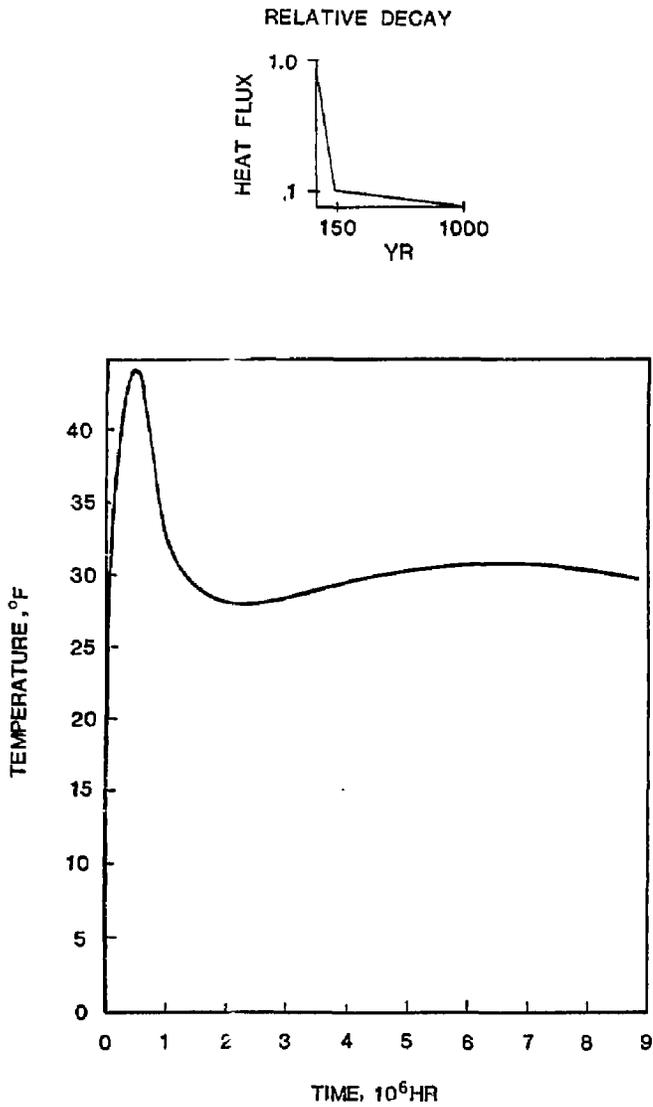


FIGURE A-12. TEMPERATURE HISTORY FOR NODE 2 IN THE 1-D ADIABATIC PLANE WALL PROBLEM USING A 2-PIECE LINEAR HEAT SOURCE SHOWN AT TOP.

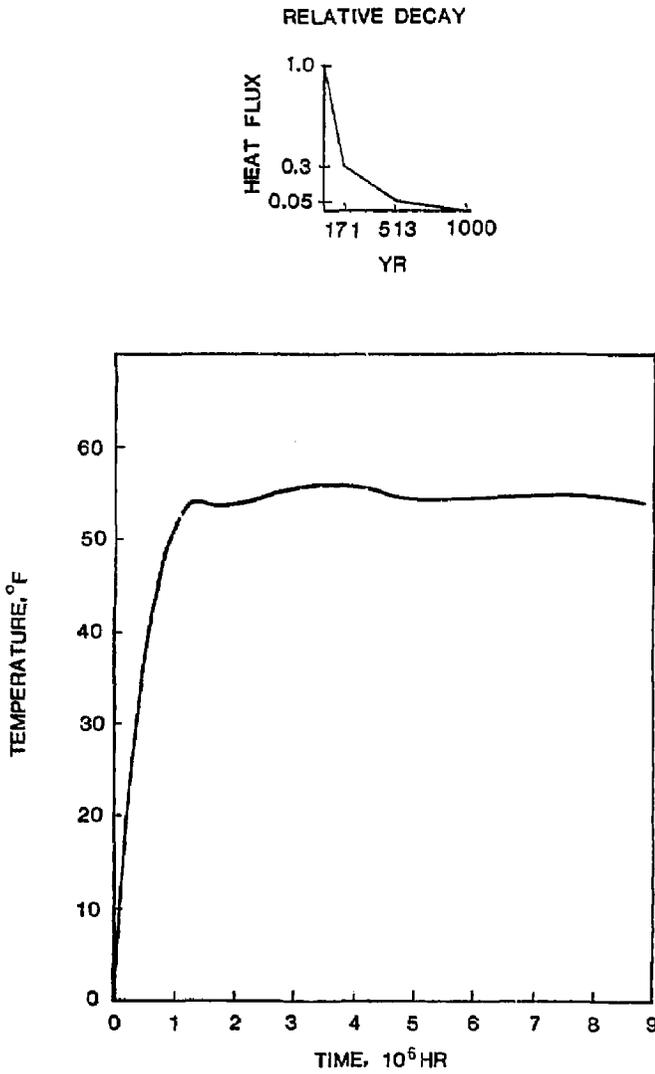


FIGURE A-13. TEMPERATURE HISTORY FOR NODE 4 IN THE 1-D ADIABATIC PLANE WALL PROBLEM USING THE 3-PIECE LINEAR HEAT SOURCE SHOWN AT TOP.

CONCLUSIONS

We have shown that the double-peaked temperature history resulting from the 3-D spent fuel base case (Figure A1) is due to the shape of the spent fuel decay curve and the thermal properties of salt. The second hump is an expected result from the problem, and is not caused by a "glitch" in the TRUMP Code. By using both 2-D and 1-D models we have shown that a multiple-peak response is possible when the power input curve has a slope which changes drastically with time. The thermal diffusivity of the conducting medium must also be low enough so that the thermal gradient is relatively slow to respond to changes in the input heat flux. These conclusions hold in cases with external heat removal, infinite media with no heat removal, and finite adiabatic media.

We have also demonstrated that the principle of superposition may be used for the case of constant material properties to decompose the problem. Two simpler problems were run using complementary parts of the heat source curve. The results of the two superpose exactly to match the original case. This superposition clearly shows how each peak in the thermal response matches a corresponding part of the decay curve.