

ORNL Fusion Power Demonstration Study: The Concept of the Cassette Blanket

Richard W. Werner

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OAK RIDGE NATIONAL LABORATORY

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FUSION ENERGY DIVISION

ORNL FUSION POWER DEMONSTRATION STUDY:
THE CONCEPT OF THE CASSETTE BLANKET

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ABSTRACT

The cassette blanket introduces four major improvements in fusion reactor blanket design. These are:

- 1) the cassette itself which by design furnishes the key unit for simplification of blanket replacement and maintenance and also isolates the lithium moderator from the plasma by enveloping it in the coolant;
- 2) the concept of blanket zoning, which uses to advantage the fact that radiation damage to structure decreases exponentially with distance. With the use of cassettes in series, only the front fraction of the blanket, the first cassette, need be changed due to damage over the life of the plant;
- 3) the rectangular blanket concept, which recognizes that blankets must envelop the plasma but need not conform to plasma shape. With this rectangular geometry, cassettes may be installed or removed by simple linear motion between magnet coils;
- 4) internal tritium recovery, which uses a favorable temperature gradient and "MHD-frozen" lithium to diffuse tritium out of the cassette.

Supporting calculations and illustrative cases are provided for these four areas using two coolants: helium and HITEC, a eutectic mixture of inorganic salts (potassium nitrate, sodium nitrate, and sodium nitrite).

1. SUMMARY

1.1 THE NEW CONCEPTS

This report describes a number of new ideas in fusion reactor blanket design centering on one principal concept — that of the cassette module. The design incorporates a number of innovative features and has been developed in an attempt to satisfy all criteria of assembly, disassembly, integrity, tritium breeding, use of existing materials technology, and integration with plasma physics, based on today's understanding of the problem. The design introduces and combines in a beneficial way four major new features: the cassette, the concept of blanket zoning, the rectangular blanket concept, and internal tritium recovery.

1.1.1 The Cassette

The cassette itself is an elementary, simple structure which is designed to furnish the key unit for simplification of blanket replacement and maintenance. It also isolates the lithium moderator from the plasma by enveloping it in the coolant.

1.1.2 Blanket Zoning

The concept of blanket zoning uses to advantage the fact that radiation damage to structure decreases exponentially with distance. With the use of cassettes in series, only the front fraction of the blanket, the first cassette, will need to be changed due to radiation damage over the life of the plant.

1.1.3 Rectangular Blanket

The rectangular blanket concept recognizes that blankets must envelop the plasma but need not conform to plasma shape. With this geometry, cassettes may be installed or removed by simple linear motion between toroidal and poloidal coils.

1.1.4 Internal Tritium Recovery

Internal tritium recovery uses a favorable temperature gradient and "MHD-frozen" lithium to diffuse tritium out of the cassette.¹

1.1.5 The Blanket Assembly

The combination of these four major design ideas produces a blanket assembly which eases the total design problem, is relatively simple, and can be serviced and maintained with a minimum of difficulty. The basic cassette module, the assembly of cassettes in a sector of a reactor, and the cross section of a completed reactor with cassettes in place are fully discussed and illustrated in the following sections.

1.2 THE CASSETTE CONCEPT IN THE FUSION PROGRAM

The concept of the cassette blanket came about as a result of the Oak Ridge National Laboratory (ORNL) Fusion Power Demonstration Study, the purpose of which was to develop a plan for demonstrating in this century the commercial feasibility of fusion power based on the tokamak concept.² A major part of the plan involves highlighting and discussing key engineering problems to focus attention on them and to ensure that they receive the necessary technological support. In order for fusion to enter the marketplace at the earliest possible time, the physics and the technology for fusion must proceed concurrently and with equal vigor. It would be a serious blunder if failing to recognize the compression of time and acceleration of progress now occurring in plasma physics, we found ourselves not in a state of technological readiness when scientific feasibility was unequivocally demonstrated.

2. THE USE OF CASSETTES IN A FUSION REACTOR BLANKET

2.1 A TYPICAL CASSETTE UNIT

We have found that a typical cassette has the general characteristics given in Table 1. Figure 1 illustrates the general design features of a cassette blanket module. The cassette's assembly of individual coolant tubes completely encapsulates the lithium moderator, providing good isolation from the plasma. Figure 2 illustrates a method for producing the coolant tubes by fusing together scalloped sheets. The benefits of this method are:

- the welds need not be completely leaktight, because a leak will produce only cross flow between adjacent tubes;
- the welds are isolated from both the plasma and the lithium; and
- the welds are on the neutral axis (zero stress) for tube bending.

The balance of the tube uses 20% cold worked material. A method of fusing the two sheets is illustrated in Fig. 3.

The cassette may be relatively slender to facilitate assembly and disassembly. Its thickness is determined by the desired decrease in radiation damage from front to back, usually about 25 cm for a damage reduction of five to ten, and by the temperature profile within the module. The module is ~ 4 m long and <1 m wide. The module assembly includes supply and return headers for the coolant and a noncirculating lithium moderator complete with an expansion plenum to accommodate the volumetric change of the lithium during the operating cycle. This bellows-type expansion plenum also acts as a pressure transducer or stress transducer that senses pressure changes in the event of a leak between coolant and moderator. The cassette also incorporates a method for tritium recovery.

2.2 STRUCTURAL AND THERMAL-HYDRAULIC CHARACTERISTICS OF CASSETTES

We have examined in reasonable depth the structural and thermal-hydraulic characteristics

of an individual cassette for two coolants: helium and the commercial inorganic salt HITEC. Although more detailed calculations will eventually be in order, we have found that there is an ample thermal-hydraulic-structural operating regime when helium is the coolant. Using the constraints of 1% of the thermal power for pumping and allowing a 32,000-psi cyclic stress for 316 stainless steel at temperatures less than 500°C, we have found the required coolant tube diameters for helium to be between 2 and 5 mm in order to accommodate wall loadings of 2-4.5 MW/m². This high wall load capability with helium is a very encouraging result. The structural limits on the salt HITEC as a coolant are less severe than those for helium. However, the salt has inescapable problems of thermal and radiation stability, melting point, start-up, and freezing on shutdown. It is our opinion that helium is the preferred coolant. Also, with helium encapsulating the lithium in a cassette, there is a much lower probability of venting lithium to the plasma.

2.3 THE CASSETTE BLANKET

2.3.1 Fusion Reactor Blankets in General

The blanket of a fusion reactor is a complicated, multifunctional unit enveloping the reacting plasma. In a deuterium-tritium (D-T) system it must

- 1) moderate the 14-MeV neutrons to thermal energy levels,
- 2) breed the required tritium fuel via neutron reactions with lithium or lithium compounds,
- 3) provide for thermal energy transfer to an external turbogenerator so that useful electrical power is produced, and
- 4) envelop the plasma and yet allow flux penetration so that current may be induced in the plasma.

These tasks must be accomplished in a relatively flimsy structure — the flimsiness is

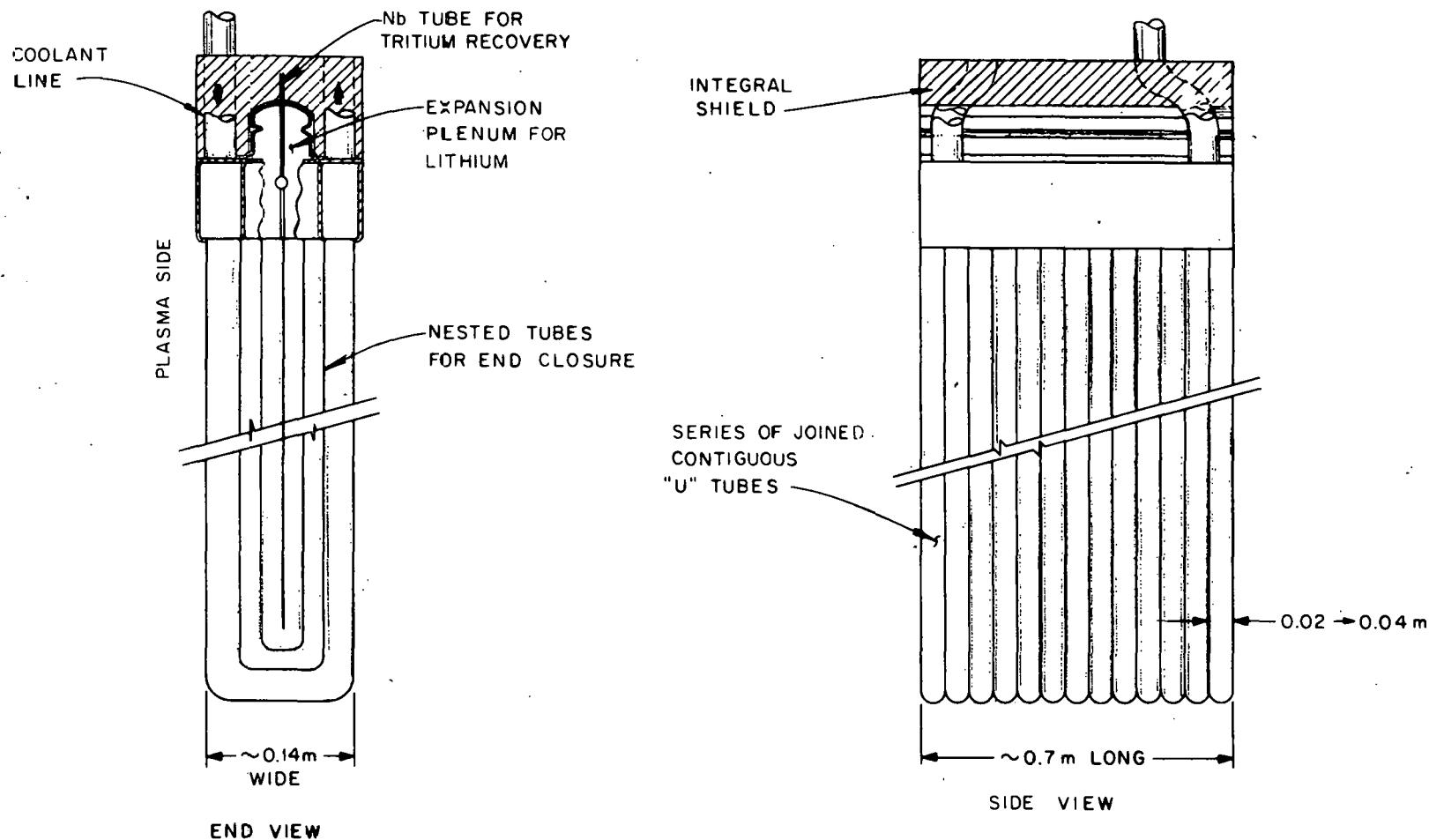


Fig. 1. General design features of a cassette blanket module.

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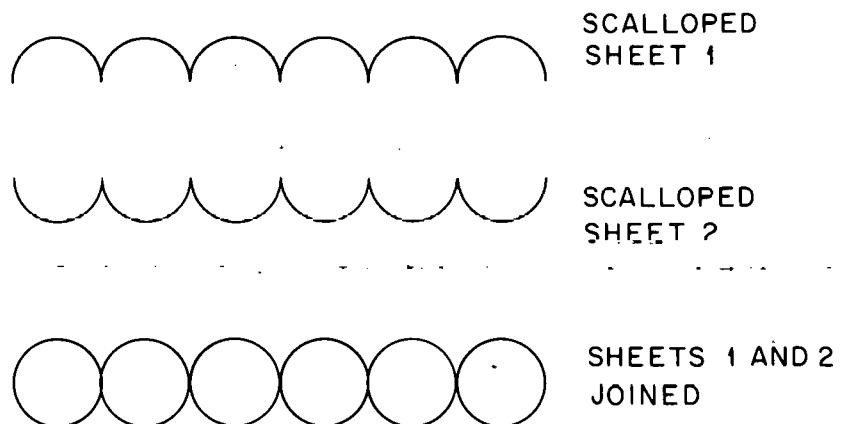


Fig. 2. Scalloped sheets joined to form coolant tubes for cassette.

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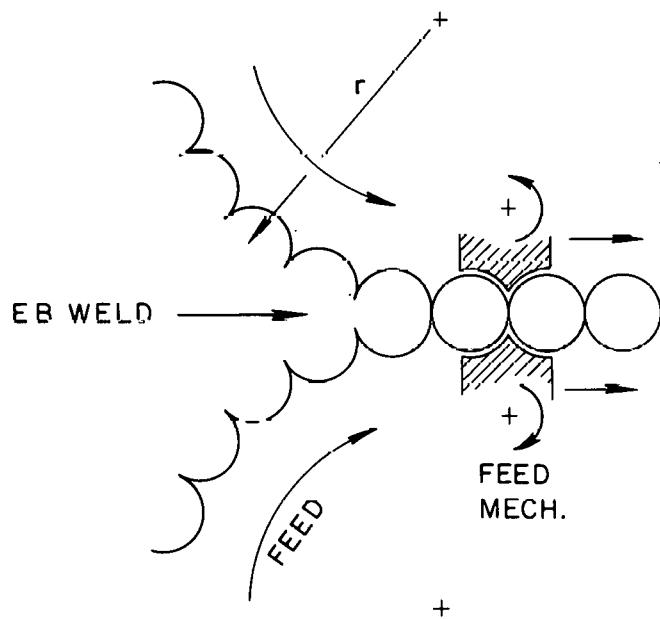


Fig. 3. Curved scalloped sheets are fed to a convergent line where joining is accomplished by electron beam welding.

Table 1. Cassette characteristics

Structural material	316 stainless steel, 20% cold worked
Coolant	Helium at 60 atm
Coolant temperature	$T_{in} \approx 350$ K; $T_{out} \approx 750$ K
Maximum material temperature in high radiation zone	700 K
Wall loading capability	≈ 4.5 MW/m ²
Probable lifetime	≈ 2 years
Moderator	Noncirculating lithium sealed in place
Tritium recovery	Niobium or vanadium window
Cassette thickness	≈ 0.14 m
Cassette length	≈ 4.0 m
Cassette width	≈ 1 m
Coolant disconnect location	Outside shield
Removal method	Linear motion
Tritium partial pressure	$\approx 10^{-6}$ torr
HeLi leak detection	Pressure sensor in plenum
Fail-safe feature	Helium-encapsulated lithium
Cost	Appears reasonable; not calculated
Changing time	Appears short; not analyzed
In situ repairs	Not necessary; cassette would be replaced
Compatibility with plasma	Wall of front cassette may be treated with low Z coating
Resistance to magnetic field forces	Not calculated

necessary to ensure adequate tritium breeding. The ratio of reacting volume to structural volume is about 20:1 ideally and 15:1 practically. Because of its thermodynamic function as an energy store, the blanket is quite hot — 400-500°C is representative. (It is, after all, the heat source of a power plant.) Because of its proximity to the plasma, it is subjected to the ravages of radiation and other fusion environmental effects: atomic displacements, helium-induced swelling, sputtering, spalling, cyclic fatigue, and thermal stress. Consequently, its life expectancy may be less than that of the total plant. It must be designed in small units because it has to be assembled in some reasonable way and also because if it were a single homogeneous unit, flux penetration to the plasma would be impaired. It is disagreeably inaccessible, situated immediately next to the plasma and surrounded by such things as shields, poloidal coils, vertical field coils, toroidal coils,

injectors, coolant piping, divertors, structure, instrumentation, and miscellany. Yet access is necessary because the blanket — at least the first 12-25 cm — is likely to be the shortest-lived reactor component and must be replaced periodically. A 5-year lifetime projection is probably optimistic. Furthermore, some number of faults in the blanket modules would seem almost inevitable during their life span, and it is highly probable that replacement of single blanket modules rather than in situ repair would have to be planned. The blanket must be economical to fabricate and maintain. Of utmost importance is that it must be as fault-free and as fail-safe as possible. Simplicity must be strived for both in method of manufacture and in the use of contemporary structural materials. Above all, there must exist a credible method of blanket module assembly, disassembly, and maintenance under (more than likely) remote operating conditions.

2.3.2 The Idea of Zoning

In the cassette design approach, we take advantage of the fact that radiation damage decreases as a function of depth into the blanket. For a reference design, a spatial distribution of damage characterized by atomic displacement rate and helium generation rate is illustrated in Fig. 4.³ It may be observed from Fig. 4 that in a distance of about 25 cm, the atomic displacement rate decreases by a factor of five and the helium generation rate decreases by a factor of seven. We define this region, which represents volumetrically about 25% of the total blanket, as the first blanket zone (FBZ). The FBZ is that part of the blanket which would be changed routinely when radiation effects dictated or when surface effects such as sputtering erosion required it. All other things being equal, the second blanket zone, i.e., the remaining 75% of the blanket, would last 5-10 times longer, or about the ~30-year life of the plant. This zoning approach to blanket maintenance is markedly superior to the more common approach of a main blanket and a separable first wall. There is little to be gained by changing a thin first wall and leaving behind other material that also has had significant damage.

The coolant circuit for the FBZ may be one which is completely independent of the remainder of the blanket, or the outlet duct may feed to the second blanket zone. Piping connections for coolant in either case would be outside the shield where access is relatively simple. There is no lithium flow. The cassette within the zone may be a single or a double unit, as shown in Fig. 5. The choice of unit is dictated by temperature profiles and temperature limits on structural materials of the total cassette, by adequate temperatures at the niobium capillaries to assure tritium recovery, by the level of wall loading, and also by requirements for assembly and ease of replacement.

2.3.3 Details of the Rectangular Blanket

Tokamak plasmas were initially developed or created in toroidal shells with circular cross

sections, a logical design geometry at that time. As understanding of plasmas has increased, the drive towards optimum system physics has dictated the plasma shape to improve and enhance the performance of the plasma. Plasma shape is now frequently elliptical or elongated, with the major axis in the vertical plane, and is no longer dictated by the surrounding walls.

It should follow that freed from the constraint of shaping the plasmas, the shape of the blanket would be dictated by engineering requirements, including fabricability, ease of maintenance, economy, and dependability, but particularly assembly and disassembly. The rectangular blanket using cassette modules is a step in this direction.

The cassette modules which make up the blanket are designed as long, relatively thin, box-like volumes. The walls of these volumes are a series of U-shaped tubes containing the coolant which completely envelops the lithium-moderating fluid contained within. The cassettes are removed and replaced by remote means with linear motions, passing the cassettes between the coils and other obstructions. Figure 6 is a schematic illustration of one subassembly of cassette modules occupying the space between adjacent toroidal field (TF) coils. The number of subassemblies is equal to the number of TF coils. Each subassembly may be divided radially into three "slices." Figure 7 shows how cassettes are positioned for removal through the middle region so as to clear the TF coils.

Figure 8 shows the cross section of a completed tokamak reactor equipped with the cassette blanket. It can be seen that a simple linear motion will permit the removal of any of the innermost cassettes through the vertical field (VF) coils without interference. The individual cassettes slip out between the VF coils without disturbing them.

2.4 COMMENTS ON INTERNAL TRITIUM RECOVERY

The lithium volume contained in the U-shaped envelope of the cassette module has roughly centered within it an independent, nonstructural

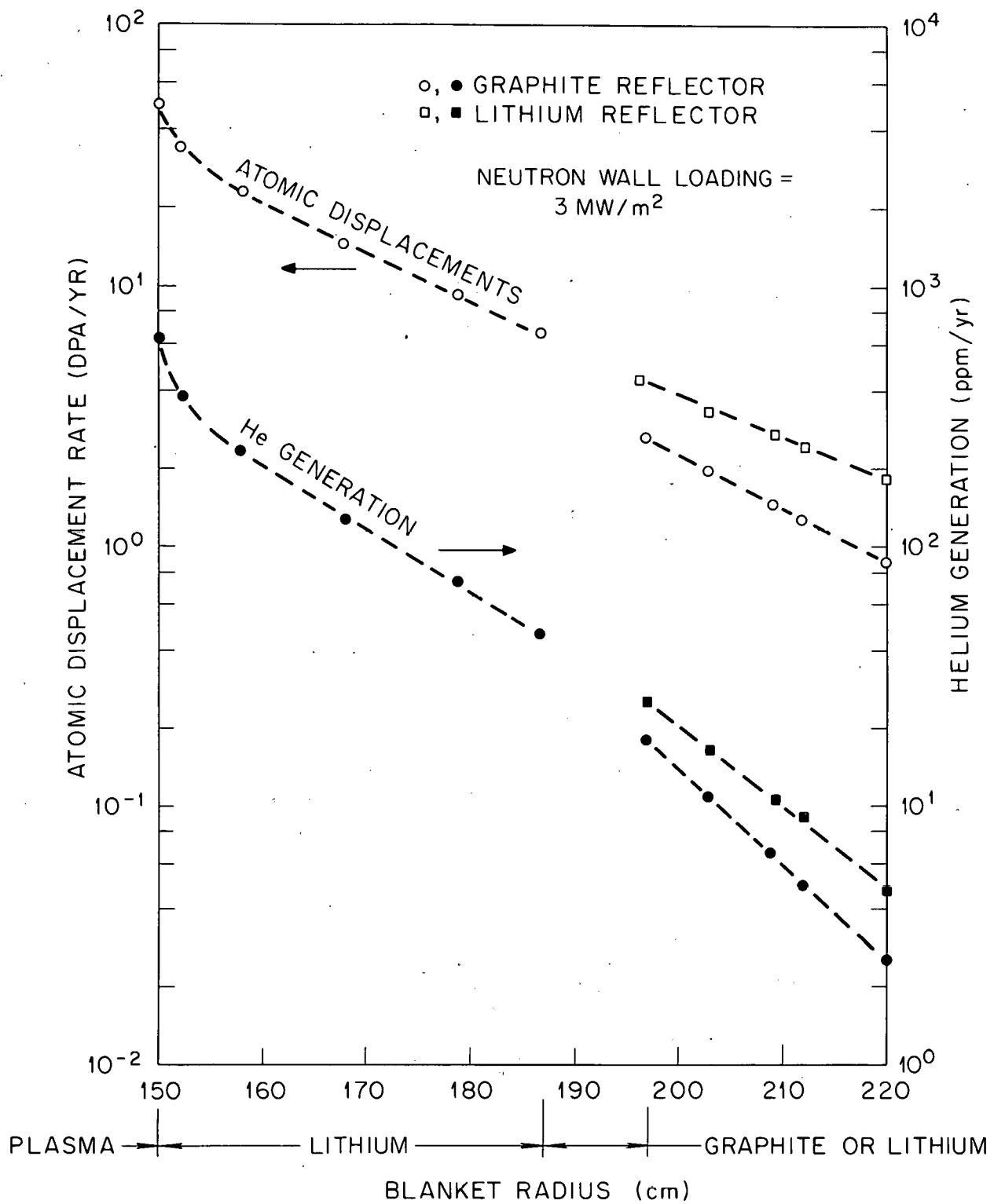


Fig. 4. Radiation damage vs blanket thickness.

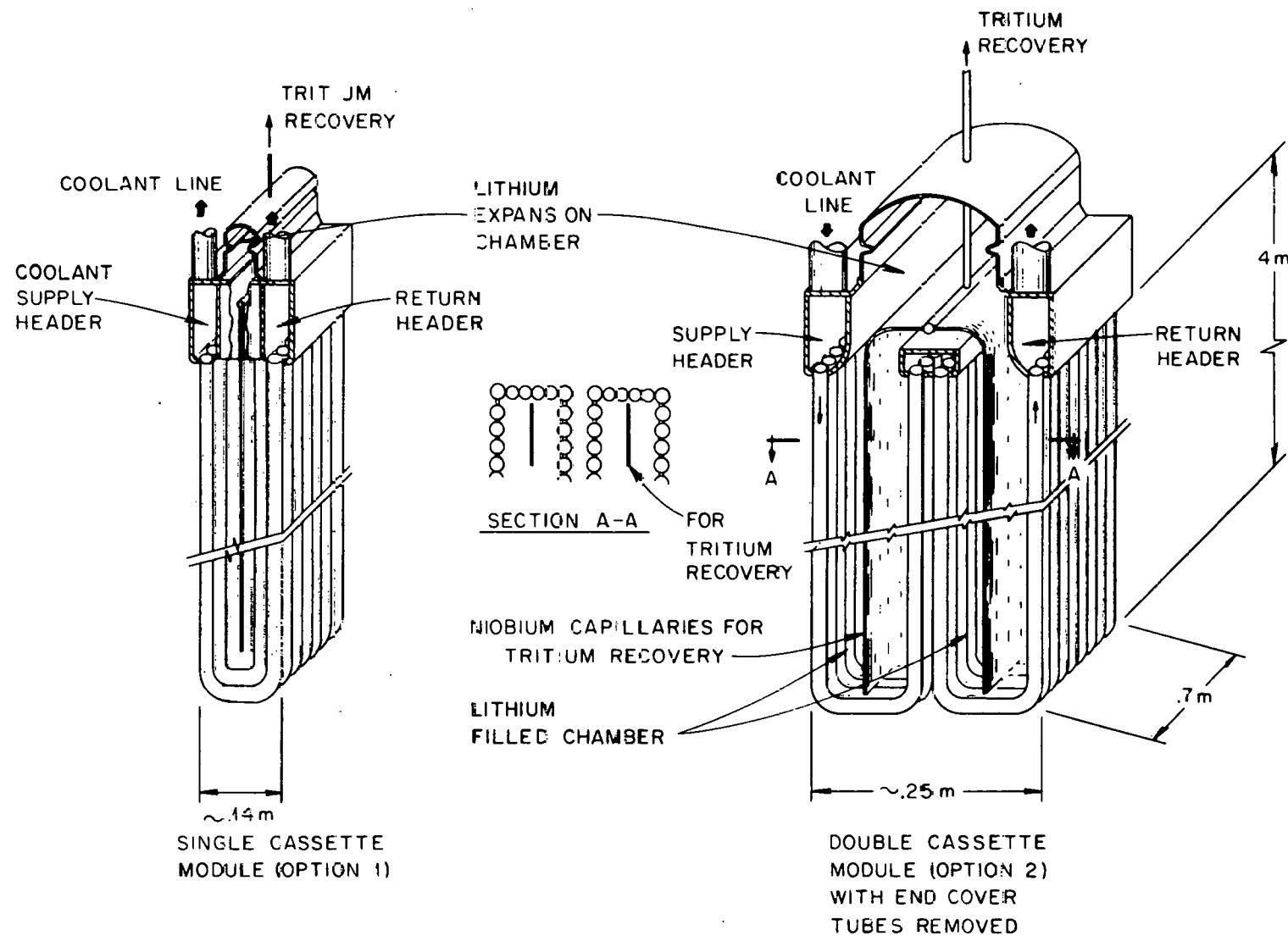


Fig. 5. The cassette module for a fusion reactor blanket.

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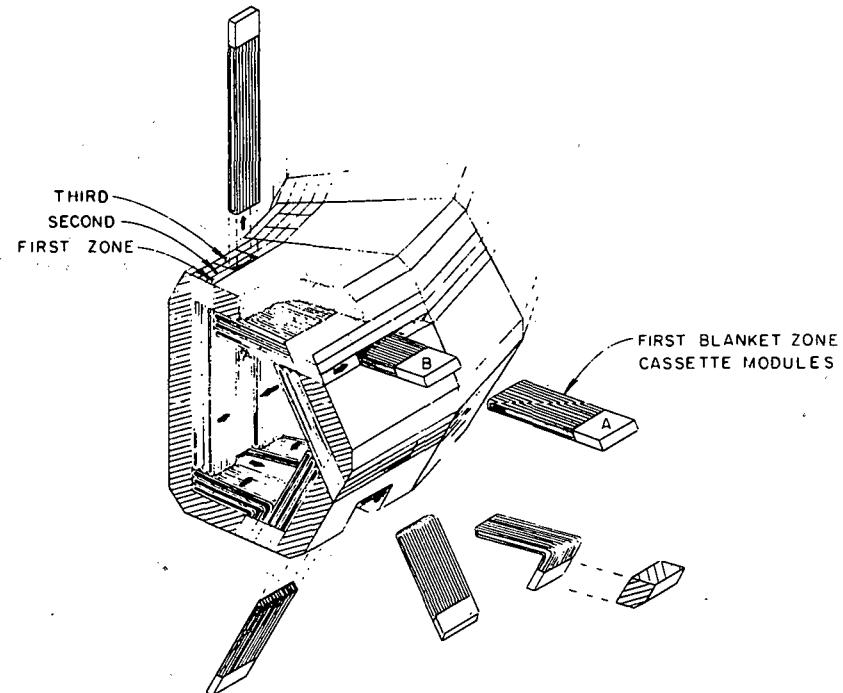
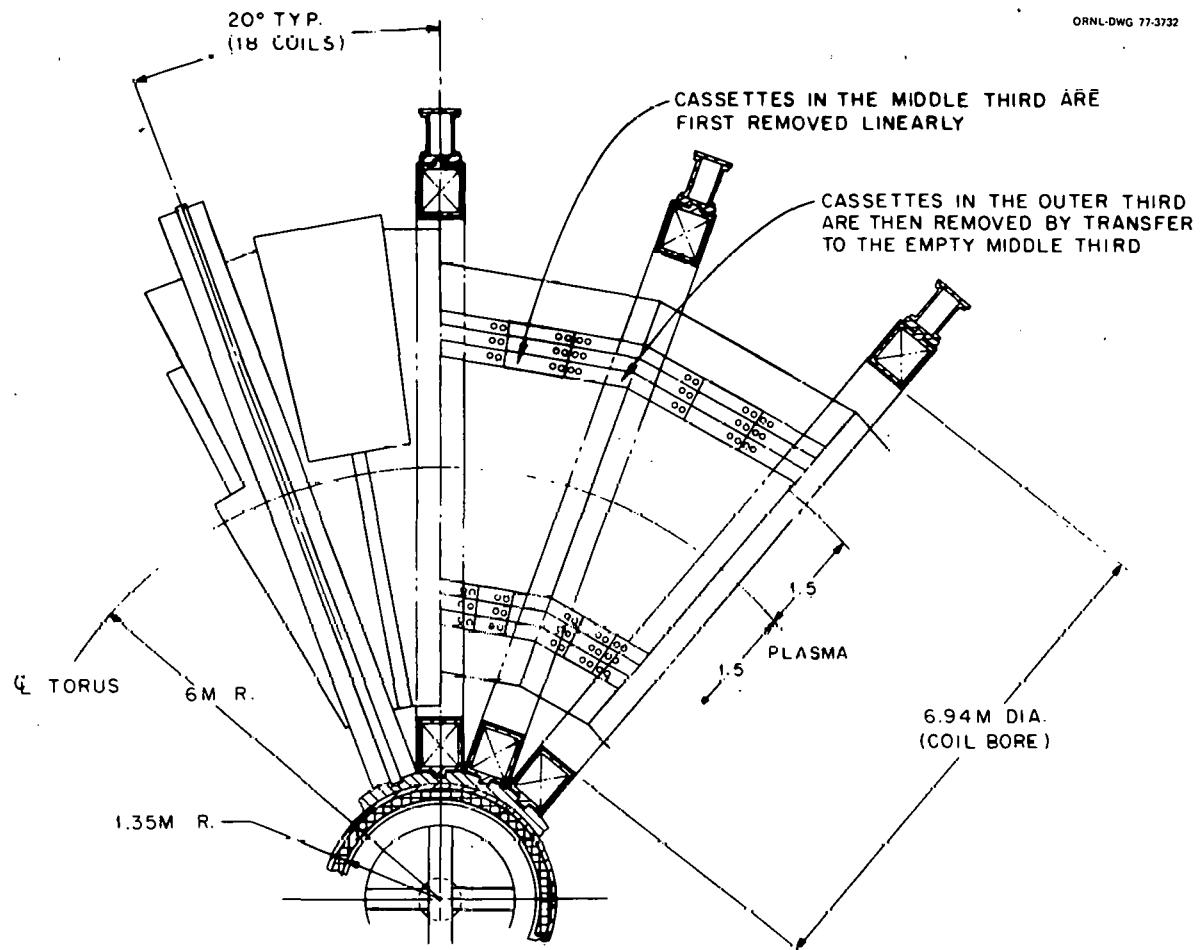


Fig. 6. The zoning approach to blanket design using replaceable cassettes. The figure illustrates the removal of cassettes in the first zone damaged by radiation. With this arrangement, there would be a five-step sequence to remove the middle cassettes (A) of the first zone. The outer cassettes (B) would then be moved to the free space and the sequence repeated.



barrier wall that serves a dual role: (1) it acts as an adiabatic, energy-isolating surface between the half of the coolant tubes facing the plasma and the other half of the U-shaped tubes facing the secondary blanket zone, and (2) it is a means of tritium recovery. This barrier wall is made of capillary tubes of niobium or vanadium. Tritium is recovered by diffusion in the lithium and permeation through the niobium. The location of the barrier wall (see Fig. 5) is determined by heat transfer considerations, by the desired flux attenuation, by the gradient in temperature within the lithium, and by the diffusion of tritium in lithium that is assumed to have zero fluid circulation due to magnetic field effects.

Because the magnetohydrodynamic (MHD) effects strongly inhibit the convective mixing of the lithium, the temperature profile in this

fluid contained within the module is determined by conduction heat transfer. Thus, we are able to determine appropriate values of t_1 and t_2 , the distances between coolant tubes and the adiabatic surface. To determine an acceptable value of t , we specify that the temperature at the coolant tubes must be low enough to satisfy radiation damage requirements, while the temperature at the adiabatic surface must be high enough so that the tritium will diffuse and permeate through the niobium at an appropriate rate. Once within the niobium tube, the tritium is removed by vacuum pumping or gas flow. Fortunately, the required temperature profiles occur at a total distance ($t_1 + t_2$) that is also appropriate to radiation damage attenuation of 5-10 so that tritium recovery in a cassette is consistent with the need to change only the innermost of the cassettes.

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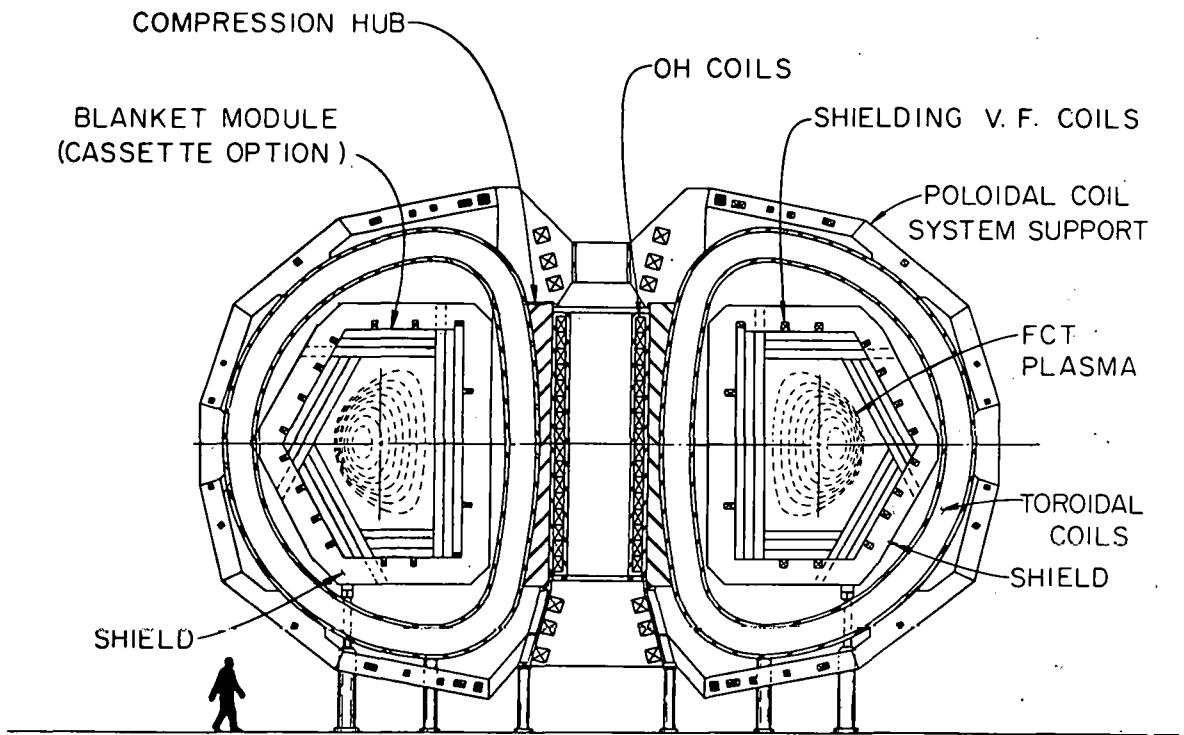


Fig. 8. Tokamak reactor cross section incorporating cassettes.

3. DESIGN CONSIDERATIONS

3.1 GENERAL STRUCTURAL DESIGN CRITERIA

In the development of a blanket for a demonstration reactor or for the following commercial machines, there are certain criteria that we must try to satisfy. In addition to the previous statement that in a D-T system we must breed tritium in the blanket and are therefore inexorably committed to lithium or lithium compounds as the principal blanket constituent, we must be guided by the following items.⁴

- 1) Low pressure systems or pressure safe systems.
- 2) Pumping power which is acceptably low compared to thermal power.
- 3) Conservative limits on structural material, stress, corrosion effects, and temperature.
- 4) Convenient and efficient blanket module shape and coolant path flow geometry.
- 5) Simple connectors for remote assembly and disassembly.
- 6) Small ducting volume, small number of joints and welds, etc.
- 7) Ease of tritium removal.
- 8) Economy.
- 9) The use of current technology materials.
- 10) Capability of withstanding cyclic thermal stress.
- 11) Compatibility with the plasma.
- 12) Acceptable replacement frequency.
- 13) High power density.
- 14) High wall loading.

3.2 STRUCTURAL MATERIAL SELECTION

High power density and high wall loading are likely to be two of the most important economic criteria, simply because capital costs for a reactor are inversely proportional to the power density and wall loading over some operating regime. Countering the requirement for capital cost economy is the fact that the useful life of the first wall and the immediate region of the blanket next to the plasma is inversely proportional to wall loading; therefore, the operating

(replacement) costs could be high. We must strive toward a good balance between capital cost and operating cost while achieving high plant availability. Thus, either the first wall and the first 15-25 cm of the blanket must be replaceable quickly, simply, and inexpensively, or the structural material must have a long life expectancy despite damaging radiation and other hostile conditions.

The cassette module could meet the first option as a "throwaway" blanket if it is carefully designed. Also, a material may be selected and a temperature range used for the cassettes which will minimize radiation damage and therefore lengthen life.

The choice of material and temperature is made difficult by the fact that data are so limited that a simple choice or a highly confident one is not possible. We choose as a primary guide the data in a paper by Bloom et al.⁵ on austenitic type 316 stainless steel and the data in a survey paper on candidate materials for fusion by J. L. Scott.⁶ These data suggest that 20% cold worked 316 stainless steel at a temperature of $<530^{\circ}\text{C}$ may have a useful wall lifetime of $\sim 8 \text{ MW-yr/m}^2$ if $\sim 5\%$ swelling is permitted. Also, with a tensile ductility of $\sim 2\%$ at 575°C a useful wall lifetime of $\sim 10 \text{ MW-yr/m}^2$ is estimated, and if the material temperature can be kept as low as $350\text{--}380^{\circ}\text{C}$ (see Fig. 9) a ductility greater than 2% appears to be retained even with increasing fluence, with the percentage of swelling limiting life. (There are a number of assumptions in these statements and the reader is encouraged to read the references cited.) We use a maximum 5% swelling and a minimum 2% ductility at conservative temperatures of $\sim 400\text{--}500^{\circ}\text{C}$ (in the coolant tube facing the plasma, where radiation damage is greatest, the temperature is held at $\sim 400^{\circ}\text{C}$; in the other half of the tube, where damage may be a factor of five lower, the temperature may reach $\sim 500^{\circ}\text{C}$). The useful wall life in terms of neutron wall loading may then be $8\text{--}10 \text{ MW-yr/m}^2$.

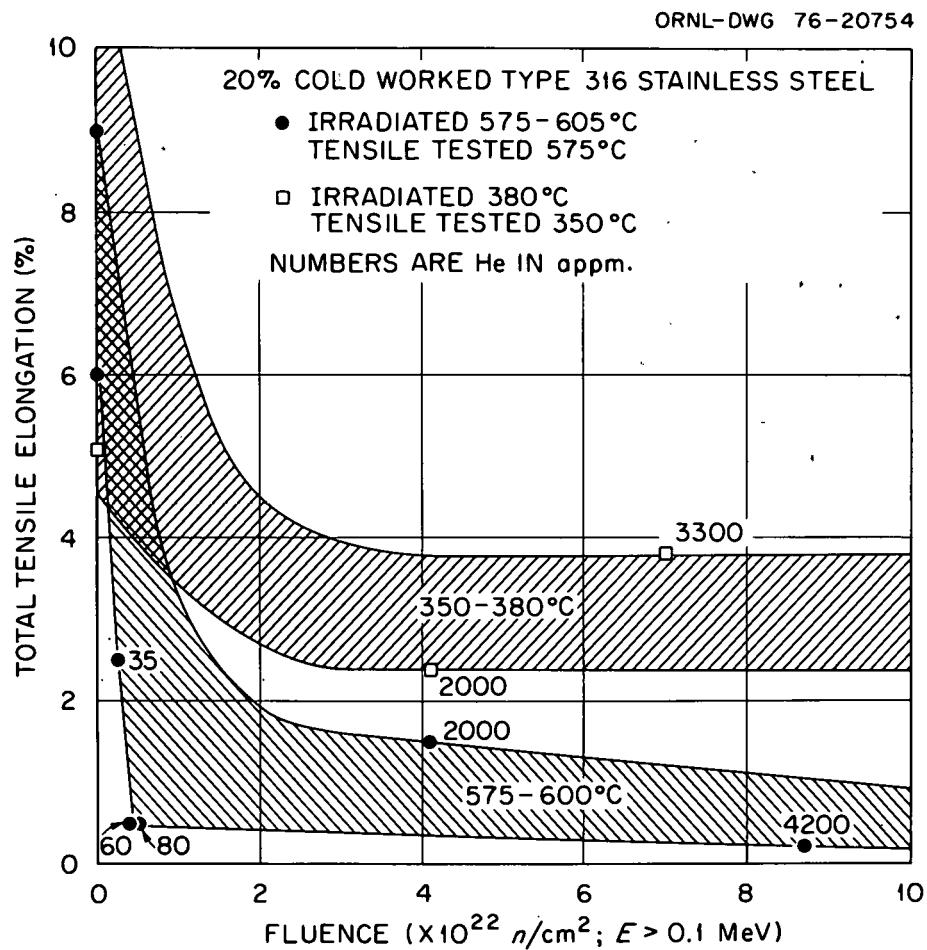


Fig. 9. Fluence-dependence of total elongation in cold worked type 316 stainless steel irradiated in the High Flux Isotope Reactor. Trend curves were drawn based on the data of R. L. Fish et al. ("Swelling and Tensile Property Evaluation of High-Fluence EBR-II Thimbles," p. 149 in *Effects of Radiation on Substructure and Mechanical Alloys of Metals and Alloys*, ASTM-STP 529, American Society for Testing and Metals, Philadelphia, Pennsylvania, 1973).

Looking to the future, there is a modified 316 stainless steel (with 0.25 Ti added) that promises to be better than the standard 316 stainless steel. Other compositional variations are also possible; thus, improvements in life expectancy may be expected for the stainless steels. Clearly, much more information is needed — not only on stainless steels, but also on other materials. Stainless steel has two rather severe limitations: poor thermal conductivity, which can result in thermal stresses dominating a blanket design, and a relatively low allowable operating temperature, which limits thermodynamic efficiency. Nevertheless, for a demonstration reactor or an early commercial reactor, we use for our blanket/first wall cold worked 316 stainless steel. This material is chosen over annealed 304 and 316 stainless steel despite the fact that there are more data for the annealed steels because

- 1) 316 stainless steel is stronger than 304,
- 2) cold worked 316 swells less than annealed 316, and
- 3) cold worked 316 has better ductility than the annealed 316.

Limited radiation data have been collected for 316 stainless steel, and it has the advantage of being a contemporary material.

One of the design constraints will be to maintain temperatures of 400°C at the first wall, where the damage rate is highest. Because damage decreases exponentially with radial distance into the neutron-moderating blanket, temperatures will be allowed to increase with radial distance.

Figures 9, 10, and 11 (taken from Ref. 2) provide some data on the properties of cold worked type 316 stainless steel. Radiation data are taken from tests made in the High Flux Isotope Reactor (HFIR).

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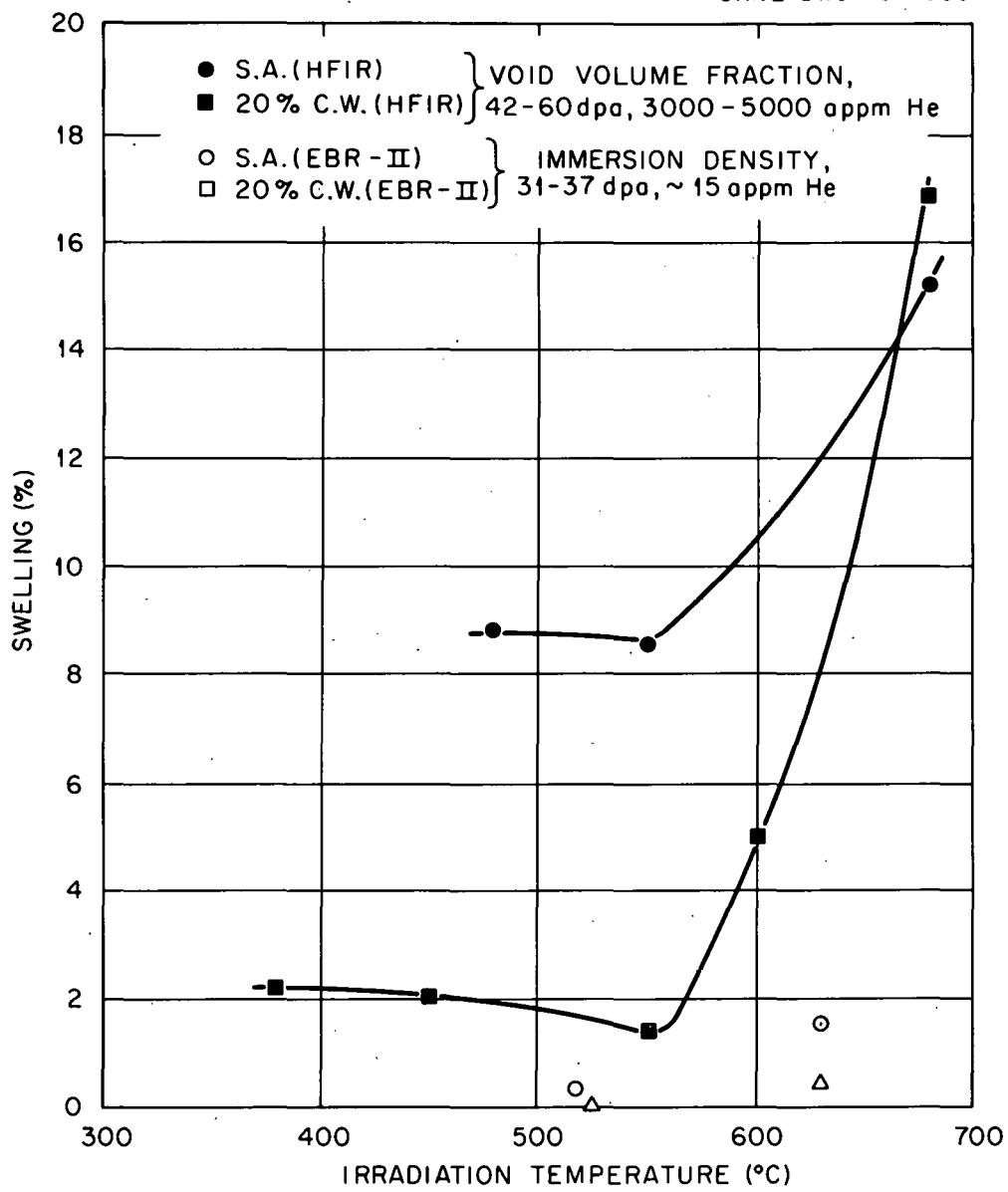


Fig. 10. Swelling of cold worked and annealed type 316 stainless steel in HFIR to .40-.60 dpa and 3000-4300 appm He.

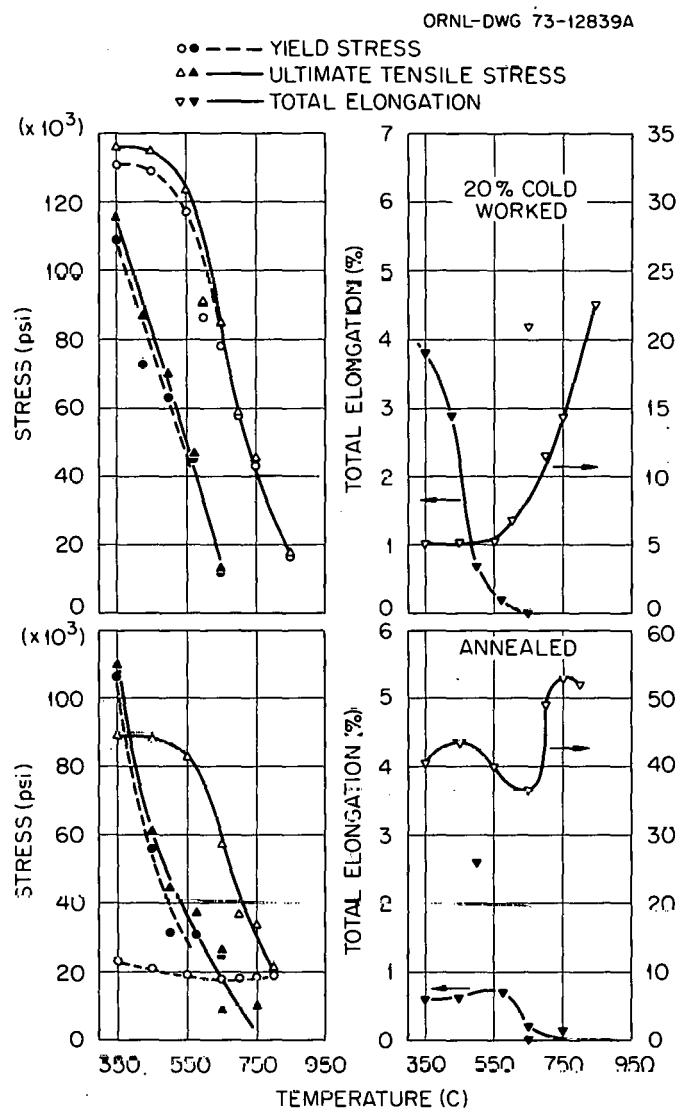


Fig. 11. Tensile properties of type 316 stainless steel after irradiation in HFIR to 40-60 dpa and 3000-4300 appm He. Data are plotted at test temperatures; irradiation temperatures were slightly higher than test temperatures for each test point. The open points are for unirradiated samples, and the closed points are for irradiated samples.

4. THERMAL-HYDRAULIC ANALYSIS

4.1 THE COOLANTS

No clear-cut optimum choice of coolant for fusion reactor blankets can be made at this time. However, based on the excellent survey work of H. E. McCoy on coolants,⁷ at least two candidates warrant further study.

- 1) The salt candidates — HITEC, sodium hydroxide, and chlorides — appear to have promise for operation based on the guidelines of low pressure and good heat transfer characteristics. The sodium-potassium-nitrate-nitrite salt mixture HITEC has been used commercially and limited property data are available. HITEC is a eutectic mixture of water-soluble inorganic salts: potassium nitrate, 53%; sodium nitrite, 40%; and sodium nitrate, 7%.⁸ Much further experimental work is needed on this class of salts in the areas of corrosion and stability before a final assessment can be made of their potential usefulness for fusion applications.
- 2) In terms of stability and compatibility, helium is the coolant with the most potential, but it must be shown that helium can remove the heat from the first wall without imposing intolerable thermal stresses.

Helium and HITEC are particularly interesting as coolants because they are at almost opposite poles — one inert but operating at high pressure, the other reactive and more fragile but able to operate at low pressure.

4.2 THE HEAT TRANSFER MODEL

For our calculations, we consider the front leg of a cassette blanket, using a single tube of diameter d and length L as shown in Fig. 12.

The tube is heated by the alpha energy source on the plasma side (q_{inc}) and by the neutron heating of the lithium moderator (q_{NL}) of thickness t on the back side. Additional heating is generated in the tube wall (q_{NT}) and in the coolant (q_{NC}).

The energy balance model assumes that we create an adiabatic surface A so that the heat transfer calculations for the front leg of the coolant tube can be separated from those for the back leg. The adiabatic surface is created using the series of evacuated small-diameter tubes made of niobium or vanadium used for tritium recovery (discussed in Sect. 6). Establishing the proper temperature for these tubes so that tritium recovery can be accomplished is also a necessary part of the heat transfer calculations.

Calculations are done in two successive steps. The first step, for the front leg of the tube, establishes the bulk of the requirements such as acceptable tube diameters, flow rates, pumping power, preliminary stress analysis, etc. The second step, for the back leg, satisfies the total energy balance of the cassette by calculating the value of t_2 . We focus here on the first step.

The total energy deposition in the front leg of the tube is

$$Q_{TOT} = q_{inc}(L \cdot d_0 \cdot t) + P_{NT}[L\pi \cdot 0.25(d_0^2 - d_i^2)] + P_{NC}(L\pi \cdot 0.25d_i^2), \quad (1)$$

where P_{NL} , P_{NT} , and P_{NC} are the local power density in the lithium, tube wall, and coolant, respectively.

From attenuation data and neutronic runs on a representative lithium/stainless steel blanket, we have established that for the internal heat generation in the lithium,⁹

$$P_{(y)NL} = 4.62 \exp\left(\frac{-y}{0.385}\right) \text{ MW/m}^3 \quad (2)$$

when the wall loading is 1.0 MW/m².

Furthermore, to a close approximation, the internal heat generation in the coolant tube material (stainless steel) is

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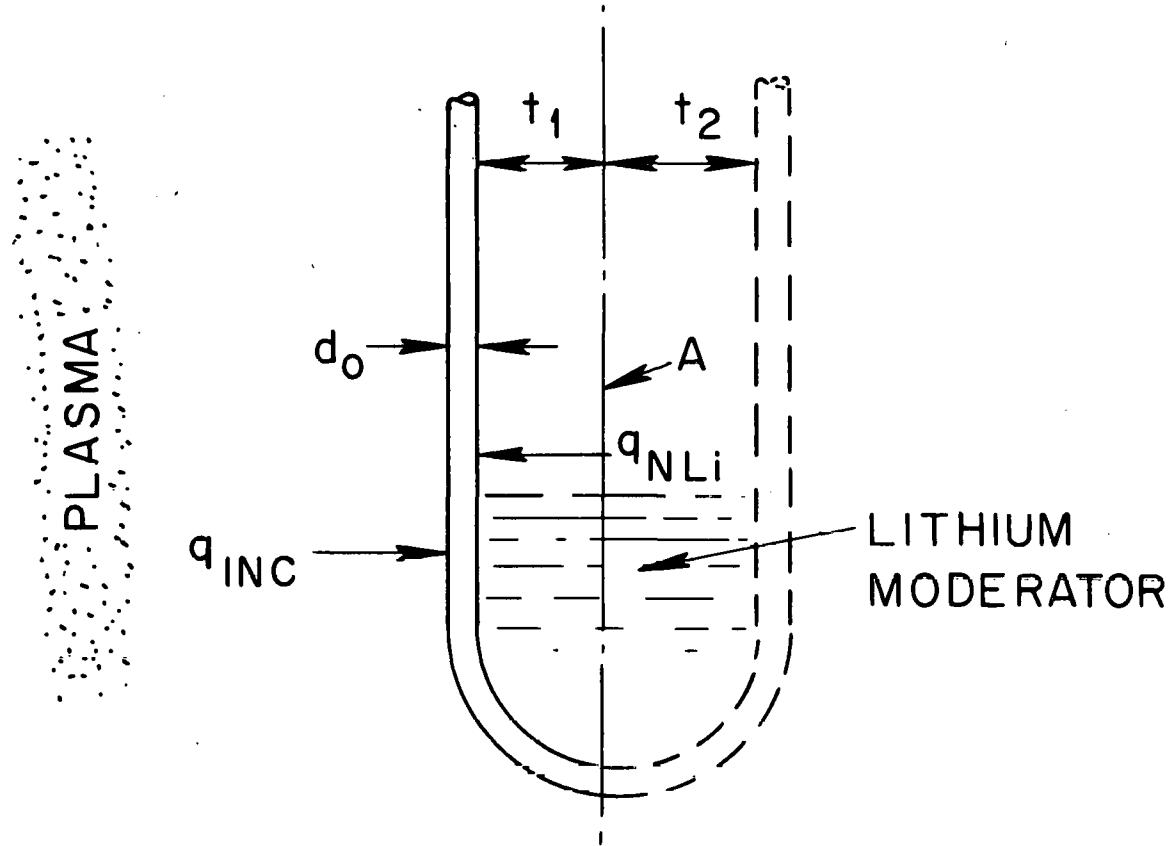


Fig. 12. Tube from front leg of cassette blanket used for heat transfer calculations.

$$P_{(y)NT} = 13.1 \exp \left(\frac{-y}{0.385} \right). \quad (3)$$

For helium the internal heat generation is

$$P_{(y)NC} = 0; \quad (4a)$$

for the salt,

$$P_{(y)NC} = 9.24 \exp \left(\frac{-y}{0.385} \right). \quad (4b)$$

The q_{inc} is functionally related to the neutron wall loading W_L by the ratio of neutron to alpha energy and by the use of a divertor and its efficiency. With a D-T reactor, the functional relationship comes from

$$D + T \rightarrow 14.1 \text{ MeV}(n) + 3.5 \text{ MeV}(\alpha), \quad (5)$$

so that without a divertor the alpha energy in one form or another must end up on the wall; that is,

$$q_{inc} = \frac{3.5}{14.1} W_L = 0.25 W_L. \quad (6)$$

The value of W_L for reactors of interest at this time ranges from 1.0 to $\sim 4 \text{ MW/m}^2$. With the use of a completely effective divertor, the least value of q_{inc} would be caused by radiation (bremsstrahlung). As a parameter the range of q_{inc} may be

$$0.1 \text{ MW/m}^2 < q_{inc} < 1.0 \text{ MW/m}^2.$$

We use 1.5 MW/m^2 as a maximum value instead of 1.0 MW/m^2 to allow for both flux peaking due to asymmetry and values somewhat higher than 4.0 MW/m^2 for W_L . We will assume for this analysis that there is no divertor which is the most critical, most difficult case for both heat transfer and problems of stress.

For numerous reasons, the wall loading parameter W_L is quite important — it strongly influences economics, radiation damage, etc. Therefore, we will use W_L as a control parameter

and write other quantities in terms of it as suggested by Fig. 13.

There is some advantage in setting $q_{NL} \leq q_{inc}$. We do not want the cassette to be too thick nor can we allow the temperature of the lithium at the adiabatic surface A to be too high. If the lithium becomes too hot, convection currents could be set up that could overcome the MHD effects which freeze the lithium. This could cause hot lithium to be dumped on the relatively cool wall of the coolant tube, introducing possible cyclic fatigue problems. Figure 14 shows two cases, $q_{NL} = 1/2 q_{inc}$ and $q_{NL} = q_{inc}$. We choose the first case for our discussion. Using the inequality of the first case, we establish the value of t , the thickness of the lithium that will be required to furnish the necessary heat input q_{NL} .

We do not know at this point what values of tube diameter are appropriate. This is another of the principal parameters. We use d_o , the outside diameter, as the reference. It is likely that the range of d_o will be

$$0.005 \text{ m} \leq d_o \leq 0.04 \text{ m}.$$

The value of δ , the tube wall thickness, is a function of d_o determined by both heat transfer and stress. Generally,

$$\delta \approx 0.05 d_o. \quad (7)$$

The value of d_i , the inside diameter, is then explicitly determined by

$$d_i = 0.9 d_o. \quad (8)$$

There are two precautions to note. The value of δ may be smaller than is commercially feasible for the smaller diameter tubes; it is also possible that δ will be larger than necessary. At any rate, when we converge on what is a reasonable solution or set of solutions for heat transfer and stress, we may wish to refine δ .

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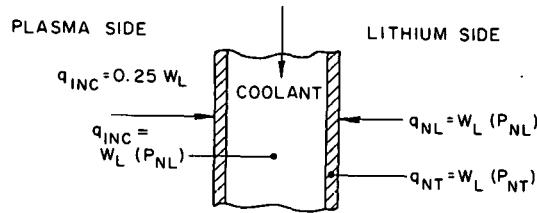
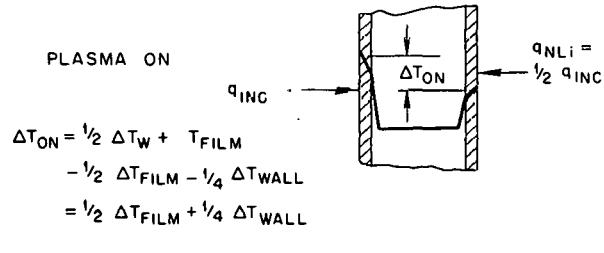
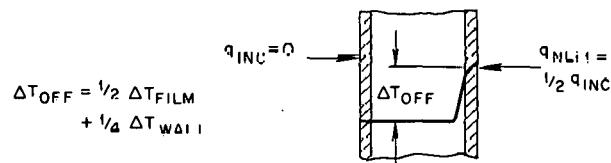
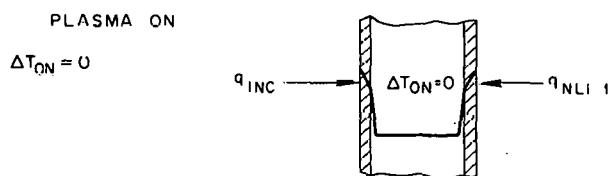


Fig. 13. Heating parameters in terms of the wall loading parameter w_L .

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CASE 1

PLASMA OFF

CASE 2

PLASMA OFF

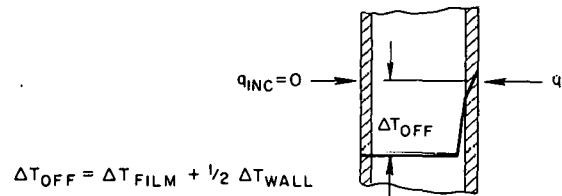


Fig. 14. Temperatures for $q_{NL} = 1/2 q_{inc}$ (Case 1) and $q_{NL} = q_{inc}$ (Case 2).

The value of t , the thickness of lithium needed to produce the appropriate q_{NL} , will be large enough so that Eq. (2) must be integrated,

$$q_{NL} = \int_{y_0}^{y_1} 4.62 \exp\left(\frac{-y}{0.385}\right) dy ,$$

$$q_{NL} = \frac{y_1}{y_0} 1.78 \exp\left(\frac{-y}{0.385}\right) \text{ MW/m}^2 .$$

When we include in the equation the wall loading factor, W_L , the tube length, L , and its diameter, d_0 , we have the energy input to the coolant from the lithium. For a tube width this may be written as

$$q_{NL} = \left(\frac{y_1}{y_0} 1.78 \exp\left(\frac{-y}{0.385}\right) \right) W_L \cdot L \cdot d_0 . \quad (9)$$

For the heat generation in the tube wall for tube diameters that are relatively small, it is sufficiently accurate to write the energy contribution to the coolant as

$$q_{NT} = \left[13.1 \exp\left(\frac{-y_c}{0.385}\right) \right] \left(\frac{0.19 d_0^2}{4} \right) \pi \cdot L \cdot W_L , \quad (10)$$

where

y_c = distance to center line of coolant tube.

For the heat generation in the HITEC salt coolant for relatively small tube diameters, the contribution of coolant energy to total energy input when $d_i = 0.9 d_0$ is

$$q_{NC} = \left[9.24 \exp\left(\frac{-y}{0.385}\right) \right] \left(\frac{0.81 d_0^2}{4} \right) \pi W_L \cdot L . \quad (11)$$

We assume a unit length of 1 m for the tube length, L .

The properties of helium¹⁰ and HITEC⁸ which we will require are shown in Appendix 1. The reference density ρ for the helium used in our calculations is 0.14 kg/m³ at 350 K and 1 atm. We use the perfect gas law to determine ρ for other pressures and temperatures and a mean density $\bar{\rho}$ determined at the first quarter-length of the U-shaped tube.

Generally in the cassette blanket, the overall length L of the tube will be ~ 8 m. At the point where $L = 4$ m (at the bend), there is a radiation damage constraint on the tube wall temperature, $T_{wmax} \lesssim 400^\circ\text{C}$ (~ 700 K). The combined value of film drop, ΔT_{film} , and the temperature drop across the wall, ΔT_{wall} , is yet to be determined, but we will guess initially that the greatest value is ~ 100 K. Therefore, T_{BM} must not exceed ~ 600 K.

For the helium coolant, a reasonable inlet temperature to the blanket, T_{BIN} , is 350 K with a helium/water external heat exchanger driving a steam cycle. The outlet temperature is taken as 750 K. Figure 15 helps to clarify the energy balance assumptions.

The pressure of the helium is assumed to be a parameter. It is likely that the range of pressure will be

$$20 \text{ atm} < p < 80 \text{ atm} .$$

For any calculation where the front leg is ~ 4 m and we input as a parameter the change in temperature ΔT per meter for the coolant, the mean density of the helium is

$$\bar{\rho} = \left[\rho_{350 \text{ K}} \times \frac{350 \text{ K}}{(350 \text{ K} + 2\Delta T)} \right] \times \rho_{atm} .$$

With the heat loading as specified in Fig. 15, the maximum ΔT per meter of length for the front leg could be 75 K/m.

For the salt, a bulk fluid inlet temperature T_{BIN} is specified by the melting point plus some margin of safety,

$$T_{BIN} \geq T_{mp} + 50^\circ\text{C}$$

$$\geq 142^\circ\text{C} + 50^\circ\text{C} \geq 415 \text{ K} .$$

The outlet temperature is limited by dissociation and thermal instability to ~ 700 K. The maximum temperature T_{BM} at the midpoint of the tube for the salt is therefore

$$T_{BM} = (700 \text{ K} - 415 \text{ K}) \times \frac{1.5}{2} + 415 \text{ K} \approx 630 \text{ K} .$$

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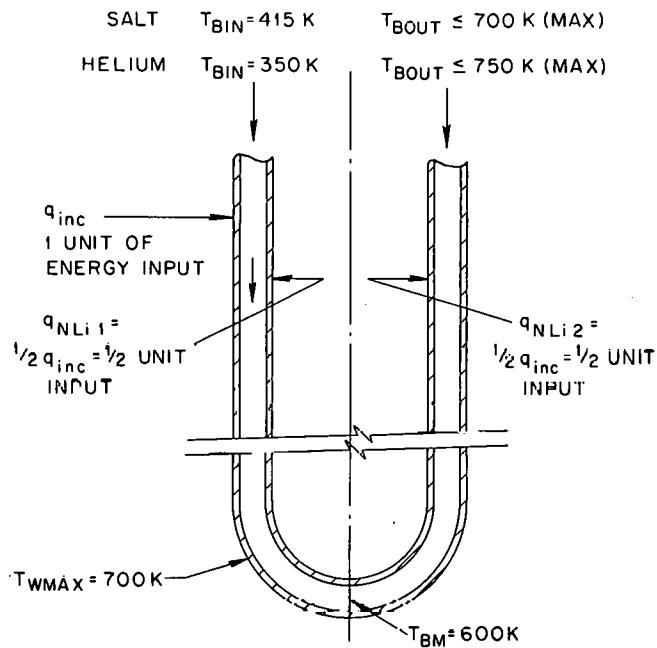


Fig. 15. Assumptions for the energy balance in a cassette coolant tube.

4.3 SOME ILLUSTRATIVE DATA

The heat transfer calculations are given in Appendix 2 and output data for different wall loadings and tube diameters are given in Appendix 3 for illustration. The data given are for helium at 60 atm with $\Delta T = 20^\circ\text{C}/\text{m}$ and for the salt at 7 atm with $\Delta T = 10^\circ\text{C}/\text{m}$. Other pressures and temperature changes would also be appropriate and better cases could possibly be cited; however, for the values chosen there is adequate design space for both helium and the salt as coolants.

We may now use the acceptable values in this compilation to determine their acceptability from a structural stress standpoint.

As a high pressure coolant, helium will be more limited by stress than salt. In this case, we use as our starting point the higher wall loadings and an acceptable fraction of thermal

power for pumping power. The pumping power must be limited to $\sim 1\%$ of the thermal power because of

- 1) plant efficiency (assumed $\sim 32\%$) and
- 2) allowance for additional coolant tube lengths outside the blanket – approximately a factor of two.

Thus, in terms of electrical power,

$$\%PP_{elec} = \frac{1\%}{0.32} \times 2 = 6.25\% .$$

This is a reasonable value, although a lower value would be better for a commercial machine. It could be perhaps twice as high for demonstration purposes. Figure 16 shows that with these 1% and 2% constraints on pumping power, tube diameters in the range $3 \text{ cm} \leq d_o \leq 5 \text{ cm}$ will be required for wall loadings greater than 2 MW/m^2 for helium.

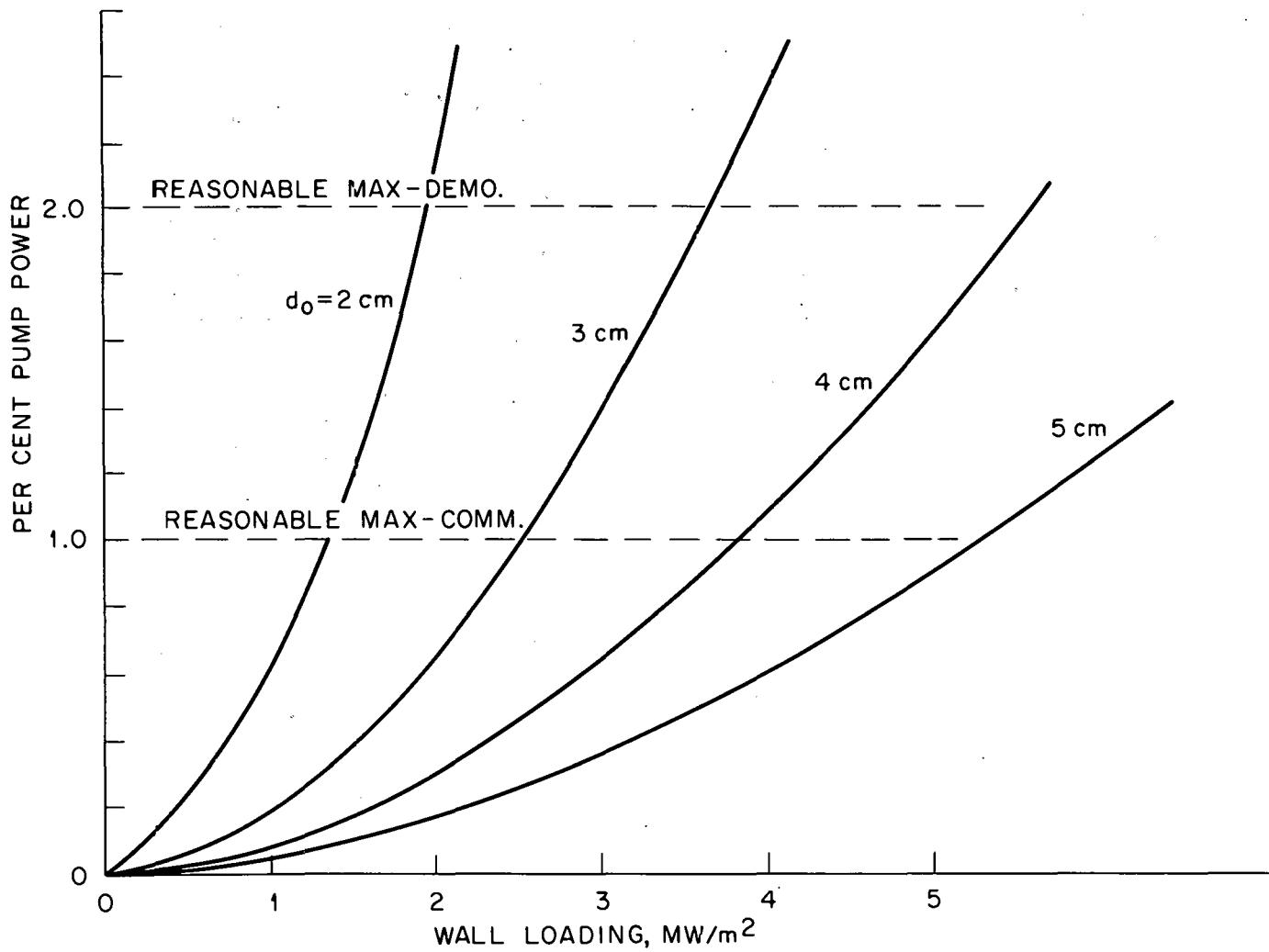


Fig. 16. Pumping power vs wall loading for various tube diameters using helium at 60 atm.
Temperature rise of coolant = 20°C/m.

5. THE STRUCTURAL MODEL

5.1 GENERAL COMMENTS ON STRESS ANALYSIS

The three stresses to be calculated are

- 1) the diametral stress, σ_B , dealing with tube bending due to unequal heating from front to back;
- 2) local thermal stresses in the tube wall, σ_T ; and
- 3) pressure stresses from the coolant flow, σ_H and σ_L .

The stresses that arise in assemblies such as the cassette module are complicated by uncertainty about geometry and fabrication. The cassette is a relatively simple structure, but the stresses are cyclic because the tokamak is the reference case and the state of stress may be influenced by time in a radiation field or in a region where surface effects such as sputtering may exist. A proper analysis should include a three-dimensional survey (plus time). It would probably be even more appropriate to build and test a model. However, a one-dimensional analysis seems in order for general shakedown purposes and to see where operating regimes are likely to be. The design should stand up under one-dimensional analysis before more detailed study is in order.

5.2 DEFORMATION AND BENDING STRESS IN NONUNIFORMLY HEATED TUBES

During a burn cycle, the q_{inc} from radiant or alpha energy is buffered or balanced by the q_{NL} from the neutron-heated lithium. During the burn cycle, if $q_{inc} \neq q_{NL}$ tube deformation takes place because of the temperature difference across the tube diameter. If the tube were unrestrained, it would bow in an arc.

After the burn the q_{inc} disappears, but due to the heat capacity of the lithium q_{NL} is effectively undiminished in the first few seconds so that there is a new temperature gradient from front to back of the tube, as illustrated in Fig. 14, and the tube bows differently, either with a new radius r or in a different direction.

To assess the bending stress, we consider a unit length of tubing of diameter d , subjected to heating from one side so that there is some differential growth,

$$\Delta s = \alpha \Delta T . \quad (12)$$

The tube develops a radius of curvature r . We wish to determine r as a function of d , the tube diameter, and Δs , the differential growth due to the differential temperature. We know that for arcs $s = r\theta$ and here

$$r = \frac{s + \Delta s}{\theta} ,$$

$$r = \frac{1.0 + \alpha \Delta T}{\theta} . \quad (13)$$

The α term is the coefficient of thermal expansion of the material. The tube diameter d is a parameter which allows r to be calculated. The tube wall thickness δ is taken to be a function of d so that hoop stress and longitudinal stress are constant, i.e.,

$$\delta = 0.05 d .$$

The ΔT represents how much hotter one side of the tube is than the other (the diametral difference). For Case 1 (shown in Fig. 14),

$$\Delta T = \frac{1}{2} \Delta T_{film} + \frac{1}{4} \Delta T_{wall} .$$

From Fig. 17

$$\tan \frac{\theta}{2} = \frac{\alpha \Delta T_s}{2d}$$

$$\frac{\theta}{2} = \tan^{-1} \frac{\alpha \Delta T_s}{2d}$$

$$\theta_{\text{radians}} = 2 \tan^{-1} \frac{\alpha \Delta T_s}{2d_0} \frac{\pi}{180} \quad (14)$$

The radius of curvature of the tube due to non-uniform heating is

$$r = \frac{1.0 + \alpha \Delta T}{\theta} \quad (15)$$

We require b , the displacement of the tube, to determine the stress. From Fig. 18,

$$\cos \phi = \frac{a}{r} = \frac{r - b}{r} \quad (16)$$

Almost certainly, in an operational situation the tube cannot be allowed to deform, and if it is constrained to remain straight, stresses will be generated because of the nonuniform heating. These stresses may be calculated assuming the tube is a cantilevered beam with an end coupling, as shown in Fig. 19. Then having determined b , the deflection of the beam, we may determine the stress as follows. The equation for the deflection is

$$b = \frac{1}{2} \frac{ML^2}{EI} \quad (17)$$

the moment is

$$M = \frac{2EIb}{L^2} \quad (18)$$

and the bending stress is

$$\sigma_B = \frac{Mc}{I} = \frac{2Ebc}{L^2} \quad (19)$$

To this stress we must add the local thermal stress across the tube wall, σ_T , the hoop stress, σ_H , and the longitudinal stress, σ_L . The thermal stress across the thickness of the tube δ is

$$\sigma_T = \frac{E\alpha \Delta T_{\text{wall}}}{2(1 - \nu)} \quad (20)$$

where the temperature drop across the wall, ΔT_{wall} , is

$$\Delta T_{\text{wall}} = \frac{2a_{\text{inc}}}{k\pi} \quad (21)$$

The hoop stress and the longitudinal stress are

$$\sigma_H = \frac{P' R}{t} \quad (22)$$

and

$$\sigma_L = \frac{P' R}{2t} \quad (23)$$

5.2.1 The Stress Levels

We may now calculate the principal stresses σ_z , σ_R , and σ_θ . Figure 20 and the data in Table 2 indicate the makeup of these principal stresses. The illustrative values shown in the figure are for a wall loading of 3 MW/m², a tube diameter of 4 cm, a temperature rise in the helium coolant of 20°C/m, and a pressure of 60 atm. Table 2 is a compilation of stresses on the plasma side of the tube. The stresses on the lithium side are somewhat less.

5.2.2 Cyclic Stress Intensities

These stresses are to be evaluated under cyclic behavior. This is the significance of the last column in Table 2, where

$$S_{1-2} = \sigma_z - \sigma_R$$

$$S_{2-3} = \sigma_R - \sigma_\theta$$

$$S_{3-1} = \sigma_\theta - \sigma_z$$

A portion of the American Society of Mechanical Engineers (ASME) design code is included in Appendix 4 to explain the stress analysis.

The stress intensity with which we will be concerned is the largest of the stress differences. By the ASME boiler code,¹¹ we are

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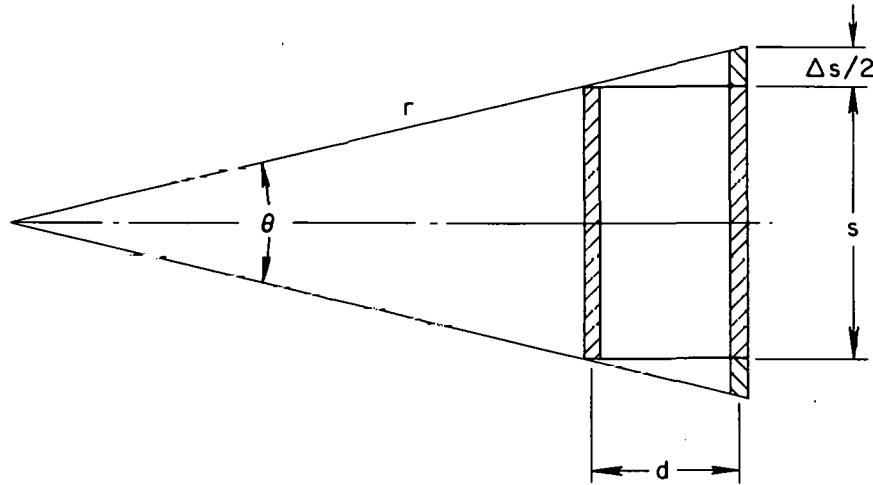


Fig. 17. Radius of curvature r determined as function of tube diameter d and differential growth Δs .

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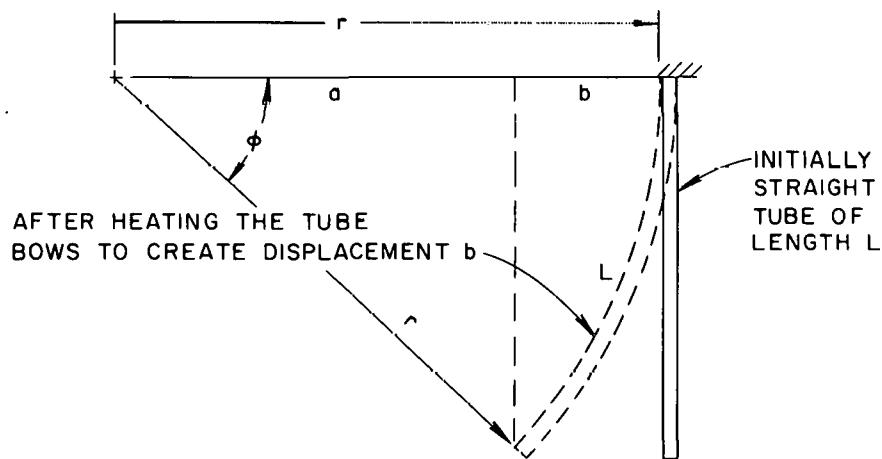


Fig. 18. Calculation of the deflection, b , of a tube subjected to nonuniform heating.

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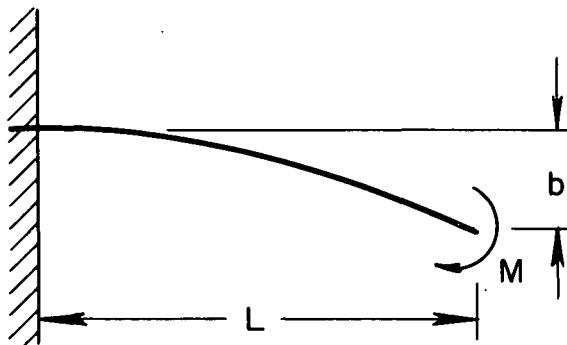


Fig. 19. Tube deflection, b , created by nonuniform heating.

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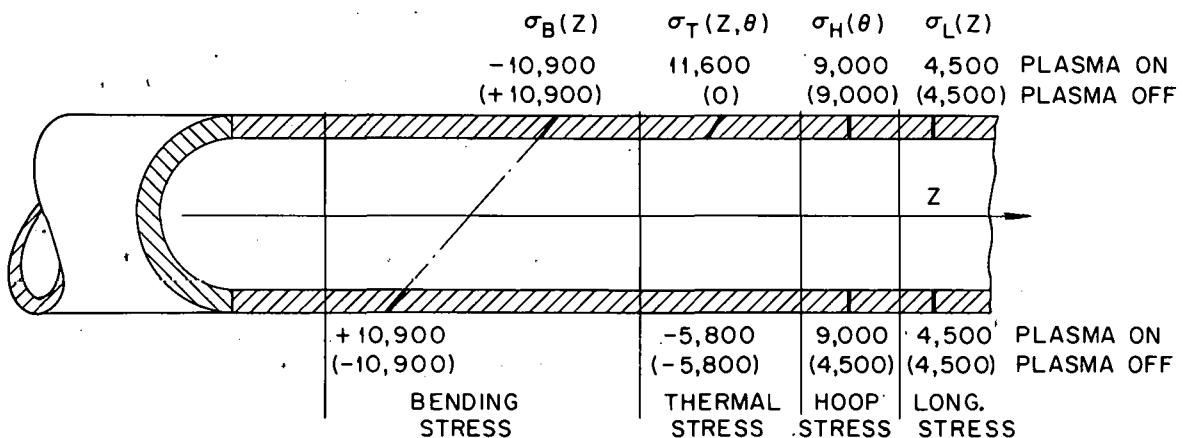
PLASMA SIDELITHIUM SIDE

Fig. 20. Components of stress in a tube subjected to a wall loading of 3 MW/m^2 with $q_{NL} = 1/2 q_{inc}$ for helium coolant at 60 atm..

Table 2. Principal stresses on the plasma side of the tube

	σ_z	σ_θ	σ_R	Maximum S_{ij}
Plasma on	$\sigma_B = -10,900$	$\sigma_r = -11,600$	0	33,400
	$\sigma_T = -11,600$	$\sigma_H = +9,000$		
	$\sigma_L = -4,500$			
	$\Sigma_z = -18,000$	$\Sigma_\theta = -2,600$		
Plasma off	$\sigma_B = +10,900$	$\sigma_r = +11,600$		
	$\sigma_T = 0$	$\sigma_H = +9,000$		
	$\sigma_L = +4,500$			
	$+15,400$	$20,600$		
	Range = 15,400	Range = 20,600		
	$+ 18,000$	$+ 2,600$		
	$- 33,400$	$- 23,200$		

allowed an alternating stress that is half the maximum stress difference,

$$S_{alt} = 0.5(S_{ij})_{MAX} \quad (24)$$

= 16,700 psi for the illustrative case.

For any one reactor design we may estimate the number of cycles per year and assign a desired number of years of life to establish the total number of cycles to which a part will be subjected. For instance, we may decide that a reasonable life span is 5 years, based on radiation damage. For tokamaks it is hoped that the burn time will be around 1000 sec, so the number of cycles will be $\sim 1.5 \times 10^5$ maximum. For this value the allowable stress would be 35,000 psi when E , the modulus of elasticity, is 26×10^6 psi. Correcting for $E = 24 \times 10^6$ psi at 500°C, the value of S_A is $\sim 32,000$. [This value is obtained from the ASME boiler code (see Appendix 4).] This S_A , when compared to the value of 16,700 psi in our case, provides a safety margin of ~ 2 .

A set of data on stresses for helium at 60 atm is plotted in Fig. 21 as a function of wall loading for various tube diameters. Pumping power limits of 1 and 2% and the limit on alternating stress (32,000 psi) are also shown. Within these boundaries, it can be seen that there is a reasonable operating regime for helium at high wall loadings. (The reader may refer to Fig. 16 for an illustration of pumping power vs wall loading for selected tube diameters.)

5.3 STRESSES IN THE TUBE AS A UNIT

The preceding calculations have indicated the stress levels that would arise if a simple straight tube subjected to heating from one side only was constrained to remain straight. The constraint against bending was not specified, but is built in between the front and back portions of the U-shaped tube as a result of the tube bend of radius R in the assembly. The following example and the additional analyses in

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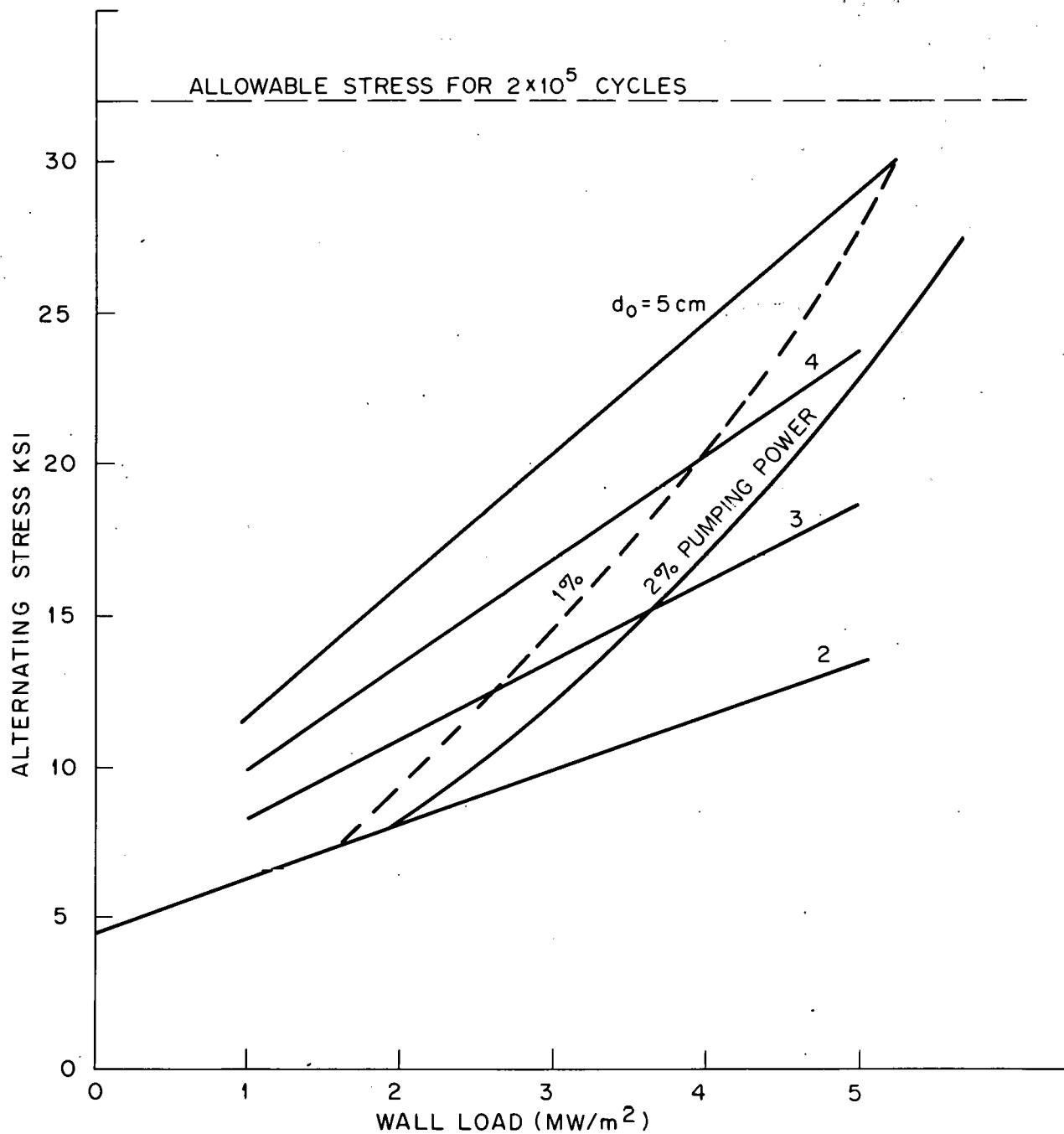


Fig. 21. Alternating stress vs wall loading for various tube diameters using helium coolant at 60 atm. The acceptable operating range is bounded by allowable stress and allowable pumping power.

Appendix 5 take this constraint into account. The form and the equations for the analyses were provided by John Mayhall of Oak Ridge National Laboratory.

By proper combination we may reduce Mayhall's 5×5 matrix (derived in Appendix 5) to one that is 2×2 , as we are primarily interested in determining the moment, M , and the shear, V , contained in the stress equation

$$\sigma_{\max} = \frac{M + Vl}{\pi r^2 t} \quad (25)$$

After substituting the influence coefficients the equations are:

$$\begin{aligned} \left(\frac{l}{EI} + \frac{\pi R}{2EI} \right) M + \left[\frac{l^2}{2EI} - \frac{R^2}{EI} \left(\frac{\pi}{2} - 1 \right) \right] V \\ = \frac{l\alpha\Delta T}{2r} - \frac{\pi R}{2r} \alpha\Delta T, \end{aligned} \quad (26)$$

$$\begin{aligned} \left[\frac{l^2}{2EI} + \frac{R^2}{EI} \left(\frac{\pi}{2} - 1 \right) \right] M + \left[\frac{l^3}{3EI} - \frac{R^3}{EI} \left(\frac{3\pi}{4} - 2 \right) \right] V \\ = \frac{2r}{\alpha\Delta T} \left[1 - \cos \left(\frac{l\alpha\Delta T}{2r} \frac{180}{\pi} \right) \right] \\ - \frac{\alpha(T_H + T_C)R}{2} \end{aligned} \quad (27)$$

We will assume from our previous calculations that

$$l = 4.0 \text{ m}$$

$$R = 0.07 \text{ m}$$

$$r = 0.015 \text{ m}$$

$$t = 0.0015 \text{ m}$$

$$\Delta T = 51^\circ\text{C}$$

$$\alpha = 18 \times 10^{-6} \text{ m/m}$$

$$E = 24 \times 10^6 \text{ psi}.$$

The resulting stress is 12,400 psi or $8.55 \times 10^7 \text{ Pa}$. With intermediate supports the effective length, l , may be decreased and these stresses diminished. However, the stress is acceptable as it stands.

6. TRITIUM PROCESSING

6.1 HEATING OF THE LITHIUM

For any one set of conditions of incident energy, heat transfer, etc., we establish t_1 and t_2 , the distances from the coolant tubes to the adiabatic surface A (see Fig. 12). The values of t may be determined from Eq. (9), which is rewritten here as

$$q_{NL} = \left[\frac{y_1}{y_0} 1.78 \times 10^6 \exp\left(\frac{-y}{0.385}\right) \right] W_L . \quad (28)$$

We need the relationship between q_{inc} and W_L . For the assumptions previously made, we know that $q_{NL} = 0.5 q_{inc}$ and $q_{inc} = 0.25 W_L$. Also from the figure, y_0 is first zero and then equal to t_1 . Thus, in two steps we may determine that $t_1 = 0.03 \text{ m}$ and $t_2 = 0.045 \text{ m}$.

It is interesting to note that with 0.03-m-diam coolant tubes (which satisfy pumping power and cyclic stress requirements for helium as a coolant), the thickness of the cassette is 0.14 m, allowing $\sim 0.0005 \text{ m}$ for the thickness of the adiabatic niobium tube surface. This is a desirable thickness in terms of both damage attenuation and ease of changing. With this size, the innermost cassette may be changed as a single unit, two units could be changed, or a double cassette could be changed.

From Appendix 6, we have the temperature distribution within the lithium of thickness L (when $x < L$)

$$t_x - t_1 = \frac{Q_0}{k\mu^2} (e^{-\mu x} - \mu x e^{-\mu L} + 1) . \quad (29)$$

We take as an example the Demonstration Power Reactor (Demo) model, which has the parameters

$Q_0 = 4.62 \text{ MW/m}^3$ when wall load is 1 MW/m^2 ,

$\mu = 1/0.385 = 2.597 \text{ m}^{-1}$,

$L = 0.03 \text{ m}$,

$k = 60 \text{ W/m}^\circ\text{C}$ for lithium at an average temperature of 700°C ,

and an assumed wall loading of 3 MW/m^2 . Then

$$\begin{aligned} t_L - t_1 &= \frac{4.62 \times 10^6 \times 3}{60 \times 2.597^2} \left(-e^{-0.03 \cdot 2.597} \right. \\ &\quad \left. - 2.597 \times 0.03 \times e^{-0.03 \cdot 2.597} + 1 \right) \\ &= 3.425 \times 10^4 (2.88 \times 10^{-3}) ; \\ t_L - t_1 &= 98.7^\circ\text{C} \approx 100^\circ\text{C} . \end{aligned}$$

This is a fairly modest temperature rise, considering that the wall loading of 3 MW/m^2 is substantial. We may wish to consider some asymmetry in the flux distribution and assume that a peak flux of 4.5 MW/m^2 is possible. Figure 22 shows a plot of the temperature gradient in the lithium as a function of increasing L . Notice that the lithium temperature at L rises rather abruptly as the thickness of the zone increases. For instance, had we wished the thickness to be 0.06 m instead of 0.03 m , the temperature gradient would have been about 500°C . This would increase the rate of tritium diffusion through the niobium but could be troublesome since, as the gradient increases, the probability of convective mixing in the lithium increases. That is, if the MHD forces prohibit the convective mixing until the convective forces overcome the MHD forces, it is possible that the convective mixing could become cyclic, periodically dumping hot lithium on the 316 stainless steel coolant tube. This would introduce a new cyclic fatigue problem. Therefore, it appears better to keep this temperature gradient fairly low.

6.2 TRITIUM PRODUCTION AND RECOVERY

Tritium is produced in the lithium by the following reactions:



and



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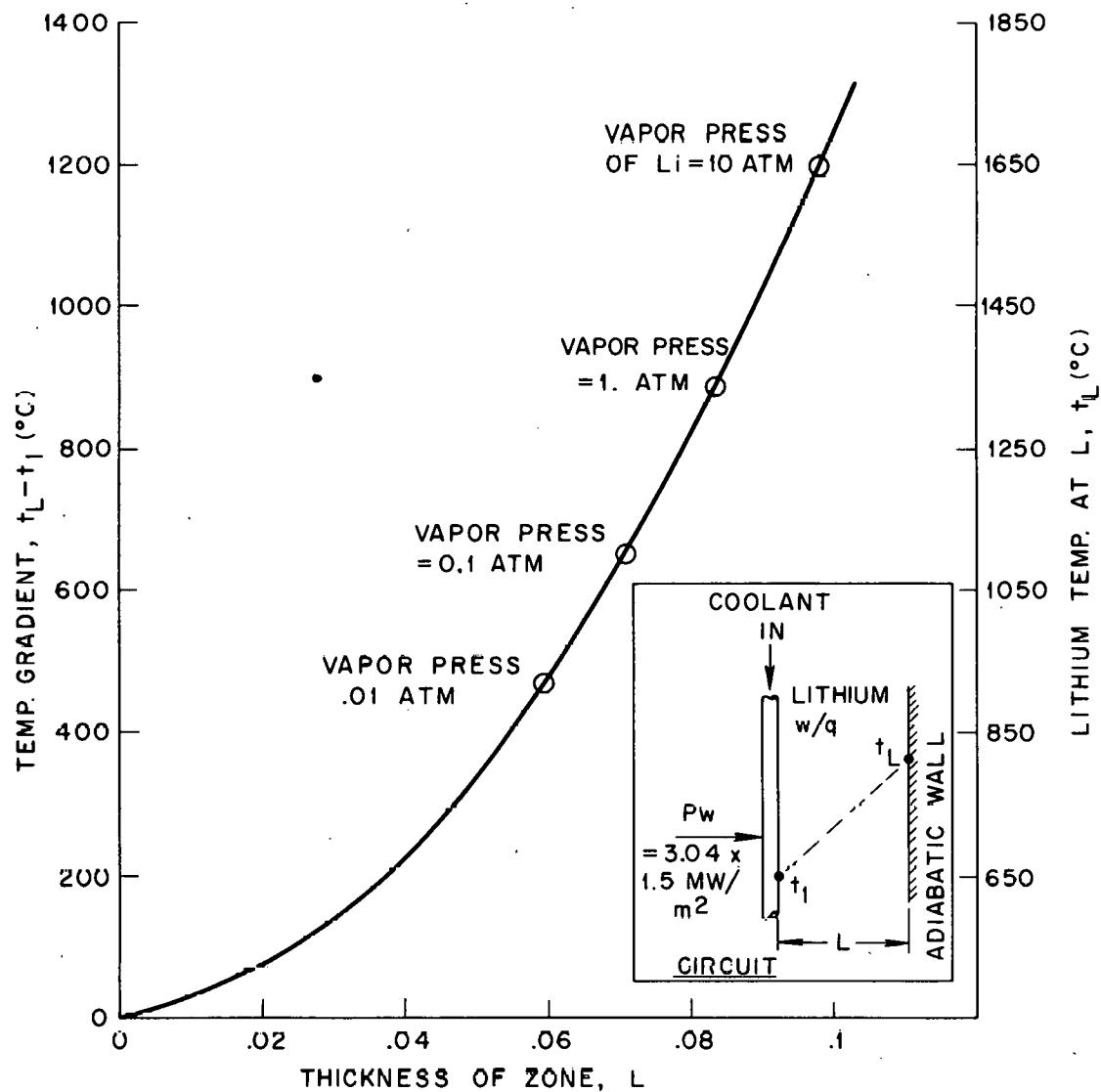


Fig. 22. Temperature gradient in lithium with internal heat generation due to a neutron wall load of $3 \text{ MW/m}^2 \times 1.5$ to account for the peak flux.

For the D-T reaction, the energy production is equal to 17.6 MeV from the fusion reaction itself plus some quantity of additional energy generated as a consequence of exothermic reactions in the blanket (such as that of a neutron with ^{6}Li). The total energy is conservatively ~ 20 MeV per source neutron. Given this total energy production for each D-T reaction, the tritium consumption T_{con} can be calculated from

$$T_{\text{con}} = \frac{P}{E} \times \frac{M}{N_0} \times 6.25 \times 10^{12} \text{ g/sec} \quad , \quad (32)$$

where

P = thermal power (watts)

E = energy production (megaelectron volts per fusion reaction)

M = mass of tritium ion (grams per gram molecule)

N_0 = Avogadro's number (6.025×10^{23} molecules per gram molecule)

and 1 watt = 6.25×10^{12} MeV/sec. Thus for each thermal megawatt, the tritium consumption is

$$T_{\text{con}} = \frac{1 \times 10^6}{20} \times \frac{3}{6.025 \times 10^{23}} \times 6.25 \times 10^{12} \\ = 1.55 \times 10^{-6} \text{ g/MW-sec} \quad (33)$$

For convenience, at standard temperature and pressure (STP) in the diffusion calculations which follow Eq. (33) is rewritten as

$$T'_{\text{con}} = 1.155 \times 10^{-2} \text{ cm}^3(\text{STP})/\text{MW-sec} \quad (34)$$

The rate of permeation of tritium through the adiabatic tube surface may be determined by the Richardson equation,

$$F = \frac{CA}{d\sqrt{3}} \left(P_1^{1/2} - P_2^{1/2} \right) \exp \left(- \frac{Q}{RT} \right) \quad , \quad (35)$$

where

F = permeation rate (cm^3/hr at STP)

C = permeation constant for system
[cm^3 (STP) $\text{mm}/\text{hr cm}^2 \text{ atm}^{1/2}$]

A = available area for diffusion (cm^2)

d = thickness of tube wall (mm)

P_1 = partial pressure of tritium on lithium side of tube (atm)

P_2 = partial pressure of tritium on heat-pipe side of tube (atm)

T = gas temperature (degrees Kelvin)

R = universal gas constant (1.9864 cal/mole K)

Q = activation energy of diffusion (cal/mole)

and $\sqrt{3}$ takes into account the mass difference between n and hydrogen. The activation energy Q and the permeation constant C are given for selected materials in Table 3. We are particularly interested in niobium and in type 316 stainless steel; the first has high permeation, which could be used in tritium recovery, and the second has low permeation, which could be used to ensure that the tritium does not go where it is not wanted. For convenience, the permeation equation

Table 3. Activation energies for diffusion and permeation constants

Metal	Q (cal/mole)	C $\text{cm}^3(\text{STP})\text{-mm}$ $\text{hr}^{-1}\text{cm}^2\text{-atm}^{1/2}$
Hastelloy N	13800	190
Hastelloy B	16675	1810
Nickel	13400	1000
Iron	9100	144
Type 304 stainless steel	16100	850
Type 316 stainless steel	16075	1526
Type 321 stainless steel	16075	1526
Type 430 stainless steel	11200	360
Ph15-7Mo stainless steel	20000	7800
Haynes 25	15100	327
Molybdenum	20100	950
Tungsten	20340	1840
Niobium	3430	1040
Platinum	18600	1840
Palladium	4500	6100

may be written with time in seconds and pressure in torr as

$$F_{ST} = \frac{CA}{d\sqrt{3}} \left(P_1^{1/2} - P_2^{1/2} \right) \exp \left(-\frac{Q}{RT} \right) \times 10^{-5} \text{ cm}^{-3}/\text{sec} \quad (36)$$

6.2.1 An Example: Partial Pressure Requirements

We may equate the consumed tritium with the tritium diffused through the adiabatic wall by combining Eqs. (34) and (36). This allows us to determine either the required surface area of the niobium or the partial pressure that will result with a given area. For a square meter of cassette, we have

$$1.155 \times 10^{-2} \times W_L = \frac{CA}{d\sqrt{3}} \left(P_1^{1/2} - P_2^{1/2} \right) \exp \left(-\frac{Q}{RT} \right) \times 10^{-5} \quad (37)$$

We assume the following parameters:

$$\begin{aligned} W_L &= 4 \text{ MW/m}^2 \\ P_2 &= 0 \\ T &\approx 723 \text{ K} \\ C &= 1040 \\ Q &= 3430 \\ d &= 0.25 \text{ mm} \end{aligned}$$

and a surface area A for each cassette of mm^2 per square meter. With a typical cassette thickness of $\sim 0.14 \text{ m}$, it is likely that at least four or five cassettes will be required for proper overall neutron moderation. In this case, A will be not less than $4\pi \text{ mm}^2$ per square meter of blanket facing the plasma. Thus,

$$P_1^{1/2} = \frac{1.155 \times 10^3 \times W_L \times d\sqrt{3}}{CA \exp \left(-\frac{Q}{RT} \right)}$$

$$= \frac{1.155 \times 10^3 \times 4 \times 0.25 \sqrt{3}}{1040 \cdot 4\pi \times 10^4 \times 0.107}$$

$$P_1^{1/2} = 1.43 \times 10^{-4};$$

$$P_1 = 2 \times 10^{-8} \text{ torr}$$

Evidently, there is no problem in attaining either adequate temperatures or adequate area, as evidenced by the low requirement of only 2×10^{-8} torr for the tritium driving pressure force. The problem is that the downstream pressure must be finite rather than the zero that we assumed. We may more correctly assume that the differential pressure relationship should be

$$P_1^{1/2} - P_2^{1/2} = 1.43 \times 10^{-4} \quad (38)$$

If we consider tritium holdup as a limiting criterion, then for a holdup of $\sim 10 \text{ kg}$ in the total blanket the value of $P_1 \approx 10^{-6}$ torr. Thus

$$-P_2^{1/2} = 1.43 \times 10^{-4} - 1 \times 10^{-3}$$

and

$$P_2 = 7.34 \times 10^{-7} \text{ torr} \approx 1 \times 10^{-6} \text{ torr}$$

6.2.2 Removing the Tritium to an External Region

This 10^{-6} torr is probably not a reasonable pressure to achieve when pumping on a long tube ($\sim 4 \text{ m}$) of small diameter ($\sim 0.005 \text{ m}$) with a closed end. If this vacuum pumping should prove to be a problem, a continuous tube with a flow of some carrier gas could be substituted. The carrier gas could have entrained in it lithium vapor or the vapor of some salt at low partial pressure. The vapor would scavenge the inner surface of the niobium tube wall, cleaning off contaminants and assuring good permeation, and would also react with the tritium for its transport and removal. The effective pressure P_2 would be very low.

7. CONCLUSIONS AND RECOMMENDATIONS

7.1 HELIUM AND HITEC AS COOLANTS

It is difficult to make direct comparisons between helium and the salt HITEC as coolants for reactor blankets. However, the following considerations are noted.

The use of helium produces higher stresses than those produced using HITEC but there does appear to be adequate design space for the helium. While the necessary pumping power is trivial for HITEC, for helium it must always be a consideration. Thus, with helium we are always committed to high pressures and substantial pumping power; these are its two major deficiencies.

HITEC's melting point of 142°C poses substantial problems in the initial charging of the system and in the formulation of procedures to follow in case of unplanned blanket cooldown. HITEC cannot be used at temperatures much above 700 K, and its thermal stability is a matter of concern. Its radiation stability must also be verified. HITEC is a strong oxidizer and reacts exothermically with lithium; also, with its high energy capture, it degrades the ability of the lithium to breed tritium.

In the area of mechanical considerations, a method of remote disconnection for helium lines is far simpler than it would be for HITEC lines. If a leak which vented to the plasma occurred in the blanket cassette, there would be no quick way to turn off the HITEC — a gravity head alone could cause the fluid to flow for a substantial time, perhaps hours — while a faulty helium line could be evacuated and the flow stopped very quickly (provided that a cassette can be equipped with a pressure transducer capable of isolating the leak or detecting a leak rate). Also, the problems of cleanup following a helium leak must clearly be significantly less than those following a leak of HITEC.

All things considered, my personal conviction is that helium is the better choice. I believe, however, that HITEC and that class of fluids offer excellent heat transfer properties

at low pressure — a significant advantage — and should be studied further to answer and resolve some of the questions posed here.

7.2 FURTHER ANALYSIS AND MODEL TESTING

In the design of fusion reactors, we are not yet cognizant of the total problem; however, we are making good progress at present. Blanket designs, for instance, are beginning to yield to the pressures of studies which include all influencing parameters instead of ignoring important issues. We are approaching designs that with some refinement will satisfy the total criteria of assembly, disassembly, integrity, breeding, technology, and physics; models of these designs should be fabricated and tested.

The cassette represents one of these designs. It is recommended that more rigorous analyses be accomplished, particularly in the area of mechanics of materials. These should be both analytical and practical. The initial model testing could be done on single modules or portions of modules, but eventually should proceed to the scale testing of a representative sector of a reactor and should include testing in a simulated fusion environment. These activities could be pursued in concert with other ongoing studies, such as the Large Coil Program at ORNL. The data obtained in this way would then be ready to integrate into the overall plan for commercial feasibility indicated by the ORNL Fusion Power Demonstration Study.

7.3 THE CASSETTE AND THE VACUUM BUILDING

The cassette blanket concept fits in well with another concept introduced in the ORNL Fusion Power Demonstration Study² — that of housing the entire reactor in a vacuum building.¹² The vacuum building approach liberates the blanket from the requirements of absolute vacuum integrity during and after assembly; the building envelops the total blanket in a

vacuum. Complex mechanical seals or welds, almost precluding disassembly and replacement, are no longer required.

Not only the cassette blanket design but also blanket designs in general should benefit from the vacuum building approach. We may be able to use existing facilities which are large enough to accommodate a reactor, such as the facility at Plum Brook, Ohio (described in Ref. 12).

7.4 A FINAL CAVEAT: THE NEED FOR A FAIL-SAFE BLANKET

There are serious considerations in the design of fusion reactor blankets which have

only been alluded to in this report. One of these considerations is the need for an assessment of the consequences of a lithium or coolant leak that vents to the plasma. Such a leak could be catastrophic. A pinhole leak no larger than the period at the end of this sentence, with only a static head driving force, would extinguish the plasma in milliseconds and unfortunately continue to vent for hours. The cassette design with helium as the coolant circumvents this problem by encapsulating the lithium with helium. More work is required in evaluation of this area, but the cassette design appears to present a workable, fail-safe blanket.

REFERENCES

1. W. Wells (Oak Ridge National Laboratory), personal communication, August 25, 1976.
2. D. Steiner et al., *ORNL Fusion Power Demonstration Study: Interim Report*, ORNL/TM-5813, Oak Ridge National Laboratory, Oak Ridge, Tennessee (March 1977).
3. R. T. Santoro (Oak Ridge National Laboratory), personal communication, January 24, 1977.
4. M. A. Hoffman et al., *Review of Heat Transfer Problems Associated with Magnetically Confined Fusion Reactor Concepts*, UCRL-78036, Lawrence Livermore Laboratory, Livermore, California (April 1976).
5. E. E. Bloom et al., "Temperature and Fluence Limits for a Type 316 Stainless Steel CTR First Wall," *Trans. Am. Nucl. Soc.* 22, 178-179.
6. J. L. Scott, "Blanket Structure," Sect. 5 in *ORNL Fusion Power Demonstration Study: Interim Report*, ORNL/TM-5813, Oak Ridge National Laboratory, Oak Ridge, Tennessee (March 1977).
7. H. E. McCoy, "Blanket Coolant," Sect. 6 in *ORNL Fusion Power Demonstration Study: Interim Report*, ORNL/TM-5813, Oak Ridge National Laboratory, Oak Ridge, Tennessee (March 1977).
8. *HITEC Heat Transfer Salt: Properties, Uses, Storage, and Handling*, Industrial Chemicals Department, E. I. DuPont de Nemours & Co., Aiken, South Carolina.
9. R. T. Santoro (Oak Ridge National Laboratory), personal communication, December 1976.
10. E. R. Eckert and R. M. Drake, *Analysis of Heat and Mass Transfer*, McGraw-Hill Book Co., New York, 1972.
11. *ASME Boiler and Pressure Vessel Code, Section III. Nuclear Power Plant Components*, Subsections NA: General Requirements and NB: Class 1 Components, American Society of Mechanical Engineers, New York, 1974.
12. R. W. Werner, *ORNL Fusion Power Demonstration Study: Arguments for a Vacuum Building in Which to Enclose a Fusion Reactor*, ORNL/TM-5664, Oak Ridge National Laboratory, Oak Ridge, Tennessee (December 1976).

APPENDIX 1
PROPERTIES OF HELIUM AND HITEC

Table A1.1. Properties of HITEC at 400°C

Melting point, mp	142°C
Specific heat, C_p	1.54×10^3 W·sec/kg·K
Density, ρ	1.68×10^3 kg/m ³
Viscosity, μ	3×10^{-3} kg/m·sec
Thermal conductivity, k	0.6 W/m·K

Table A1.2. Property values of helium at atmospheric pressure

Temperature (K)	Density, ρ (kg/m ³)	Specific heat, C_p (Wsec/kg K)	Viscosity (dynamic), μ (kg/msec)	Viscosity (kinematic), ν (m ² /sec)	Thermal conductivity, k (W/mk)	Thermal diffusivity, $\alpha = k/C_p \rho$ (m ² /sec)	Prandtl number, Pr ($\mu C_p / k$)
3		5.200×10^3	8.42×10^{-7}		0.0106		
33	1.4657	5.200	50.2	3.42×10^{-4}	0.0353	0.04625×10^{-4}	0.74
144	3.3799	5.200	125.5	37.11	0.0928	0.5275	0.70
200	0.2435	5.200	156.6	61.38	0.1177	0.9288	0.694
255	0.1908	5.200	181.7	95.50	0.1357	1.3675	0.70
366	0.13280	5.200	230.5	173.6	0.1691	2.419	0.71
477	0.10204	5.200	275.0	269.3	0.197	3.716	0.72
589	0.08282	5.200	311.3	375.8	0.225	5.215	0.72
700	0.07032	5.200	347.5	491.2	0.251	6.661	0.72
800	0.06023	5.200	381.7	634.4	0.275	8.774	0.72
900	0.05286	5.200	413.6	781.3	0.298	10.831	0.72

APPENDIX 2
CALCULATIONAL PROCEDURE FOR
HEAT TRANSFER

We specify as input parameters the following:

$$\begin{aligned} d_0 &= 0.005 \text{ m}, 0.04 \text{ m}, 0.005 \text{ m steps} \\ W_L &= 5 \times 10^5 \text{ W/m}^2, 5 \times 10^6 \text{ W/m}^2, 5 \times 10^5 \text{ W/m}^2 \\ &\text{steps} \\ P(\text{pressure}) &= 10 \text{ atm}, 60 \text{ atm}, 10 \text{ atm steps for} \\ &\text{helium} \\ &= 7 \text{ atm (constant) for salt} \\ q_{inc} &= 0.25 \times W_L (\text{W/m}^2) \\ q_{NL} &= 0.5 q_{inc} (\text{W/m}^2) \\ d_i &= 0.9 d_0 (\text{m}) \\ \Delta T &= 10 \text{ K/m}, 60 \text{ K/m}, 10 \text{ K/m steps.} \end{aligned}$$

The following output data are determined.

1) Heat into the coolant, Q , per meter of tube length

$$\begin{aligned} Q_{\text{TOTAL}} &= W_L d_0 (q_{inc} + q_{NL}) + W_L (Q_{NT} + Q_{NC}) \\ &= W_L d_0 (0.25 + 0.125) + W_L \left[13.1 \exp \left(\frac{-y_c}{0.385} \right) \right. \\ &\quad \times \frac{0.19 \pi d_0^2}{4} \left. \right] + W_L \left[9.24 \exp \left(\frac{-y_c}{0.385} \right) \right. \\ &\quad \times \frac{0.81 \pi d_0^2}{4} \left. \right], \end{aligned}$$

$$Q_{\text{TOTAL}} = W_L d_0 \left[0.375 + (1.955 d_0 + 5.87 d_0^2) \exp \left(\frac{-y_c}{0.385} \right) \right]$$

For salt,

$$Q_{\text{TOTAL}} = W_L d_0 \left[0.375 + 7.83 d_0 \exp \left(\frac{-y_c}{0.385} \right) \right] \quad (A2.1a)$$

For helium,

$$Q_{\text{TOTAL}} = W_L d_0 \left[0.375 + 1.955 d_0 \exp \left(\frac{-y_c}{0.385} \right) \right] \quad (A2.1b)$$

2) The mass flow rate \dot{m} , in kilograms per second, for helium,

$$\dot{m}_H = \frac{Q}{C_p \Delta T} = \frac{Q}{5.2 \times 10^3 \times \Delta T}, \quad (A2.2a)$$

and for salt,

$$\dot{m}_S = \frac{Q}{1.54 \times 10^3 \times \Delta T} \quad (A2.2b)$$

3) The flow velocity, V , in meters per second, for helium,

$$V_H = \frac{\dot{m}}{\rho A} = 4 \frac{\dot{m}}{\pi} \cdot 0.81 d_0^2 \bar{\rho} P, \quad (A2.2b)$$

where

$$\bar{\rho} = (0.14 \cdot 350) / (350 + 20 T)$$

and P is atmospheric pressure, and for salt,

$$V_S = 4 \frac{\dot{m}}{\pi} \cdot 0.81 d_0^2 \rho_S \quad (A2.3b)$$

4) The Reynolds number, N_R ,

$$N_R = \frac{d_i V \cdot \rho}{\mu}$$

For helium,

$$N_{RH} = \frac{0.9 d_0 V_H \bar{\rho} P}{2.75 \times 10^{-7}} \quad (A2.4a)$$

for salt,

$$N_{RS} = \frac{0.9 d_0 V_S \rho_S}{3 \times 10^{-3}} \quad (A2.4b)$$

5) The friction factor, f , which for smooth tubes is proportional to the Stanton number (Ref. 1), N_S ,

$$f = 1.5 N_S.$$

The Stanton number for smooth tubes may be written as

$$N_S = \alpha (N_p)^{-2/3} (N_R)^{-0.2}$$

where $\alpha = 0.023$; thus

$$f = 0.0345 (N_p)^{-2/3} (N_R)^{-0.2}$$

The value of N_p is 0.72 for helium and 7.7 for the salt; therefore, for helium

$$f_H = 0.043 (N_R)^{-0.2} \quad (A2.5a)$$

and for salt

$$f_S = 0.011 (N_R)^{-0.2} . \quad (A2.5b)$$

6) The pressure drop, ΔP , in newtons per square meter,

$$\Delta P = \frac{2 f \dot{m}^2 L}{\rho d} \left(\frac{\pi d_i^2}{4} \right)^{-2} ,$$

where $\rho = \bar{\rho}$ for helium and $\rho = \rho_S$ for salt. In terms of d_0 ,

$$\Delta P_{II} = \frac{2 f \dot{m}^2 L}{\rho} \frac{1}{d} \left(\frac{0.81 \pi d_0^2}{4} \right)^{-2} \quad (A2.6a)$$

and

$$\Delta P_S = \frac{2 f_S \dot{m}^2 L}{\rho_S} \frac{1}{d} \left(\frac{0.81 \pi d_0^2}{4} \right)^{-2} . \quad (A2.6b)$$

The pressure drop may be expressed in pounds per square inch as

$$\Delta P_{psi} = \Delta P / 6.894 \times 10^3 . \quad (A2.7)$$

7) The pumping power, PP , in watts,

$$PP = \Delta P \cdot G.$$

$$\text{For helium, } PP = (\Delta P \dot{m}) / (\bar{\rho} \cdot P); \quad (A2.8a)$$

$$\text{For the salt, } PP = (\Delta P \dot{m}) / \rho_S . \quad (A2.8b)$$

8) The percentage of thermal power used for pumping power, % PP ,

$$\% PP = \frac{PP}{Q} \times 100\% . \quad (A2.9)$$

9) The Nusselt number, Nu . For helium, where the Prandtl number Pr for a constant heat rate is $0.5 < Pr < 1.0$,

$$Nu_H = 0.222 \cdot Pr^{0.6} Re^{0.8}; \quad (A2.10a)$$

for the salt, where $Pr = 7.7$,

$$Nu_S = 0.0155 \cdot Re^{0.83} Pr^{0.5} = 0.043 Re^{0.83}. \quad (A2.10b)$$

10) The film coefficient, h ,

$$h = Nu \cdot \frac{k}{0.9 d_0} . \quad (A2.11)$$

11) The film drop, ΔT_{film} , in degrees Celsius,

$$T_{film} = T_{wi} - T_{BM} = \frac{q_{inc} \cdot 2}{h \pi} . \quad (A2.12)$$

12) The temperature drop across the wall, ΔT_{wall} , in degrees Celsius,

$$\Delta T_{wall} = \frac{q_{inc} \cdot 2 \cdot 0.05 d_0}{K \pi} . \quad (A2.13)$$

REFERENCE

- 1 G. R. Hopkins and G. Melese-D'Hospital, "Helium Cooling for Fusion Reactors," Nucl. Eng. Des. 26, 215-230 (1974).

APPENDIX 3
OUTPUT DATA FOR HELIUM AND HITEC
AT DIFFERENT WALL LOADINGS AND TUBE DIAMETERS

Tables A3.1 through A3.5 present data for helium at 60 atm and $\Delta T = 20^\circ\text{C}/\text{m}$ with different wall loadings ($1\text{-}5 \text{ MW}/\text{m}^2$) and tube diameters ($0.005\text{-}0.05 \text{ m}$). Tables A3.6 through A3.10 present data for HITEC at 7 atm and $\Delta T = 10^\circ\text{C}/\text{m}$ for wall loadings of $1\text{-}5 \text{ MW}/\text{m}^2$ and tube diameters of $0.005\text{-}0.05 \text{ m}$. The data are for the following parameters:

- 1) heat into the coolant, Q
- 2) mass flow rate, m
- 3) flow velocity, V

- 4) Reynolds number, N_R
- 5) pressure drop, ΔP (in newtons per meter and in pounds per square inch)
- 6) pumping power, PP
- 7) percentage of thermal power used for pumping power, $\%PP$
- 8) Nusselt number, Nu
- 9) film coefficient, \bar{h}
- 10) film drop, ΔT_{film}
- 11) temperature drop across the wall, ΔT_{wall}

Table A3.1. Output data for helium at 60 atm, $\Delta T = 20^\circ\text{C}$, and wall loading of 1 MW/m²

d_o (m)	Q (W)	\dot{m} (kg/sec)	V (m/sec)	N_R	ΔP (N/m ²)	ΔP (psi)	PP (W)	%PP	Nu	\bar{h}	ΔT (°C)	
											Film	Wall
0.005	1,923	0.0184	154	2.1×10^5	2.65×10^5	38.5	52	33.8	329	1.31×10^4	12.1	2.1
0.010	3,945	0.0379	79	2.16×10^5	3.46×10^4	5.0	175	4.43	335	6.7×10^3	23.7	4.2
0.015	6,064	0.0583	54	2.2×10^5	1.07×10^4	1.56	83	1.37	342	4.56×10^3	34.8	6.3
0.020	8,282	0.0796	41.5	2.27×10^5	4.7×10^3	0.687	50	0.604	348	3.48×10^3	45.6	8.4
0.025	10,597	0.101	33.9	2.32×10^5	2.52×10^3	0.366	34	0.322	355	2.84×10^3	55.9	10.4
0.030	13,010	0.125	28.9	2.4×10^5	1.52×10^3	0.221	25.3	0.194	362	2.4×10^3	66	12.5
0.035	15,520	0.149	25.4	2.43×10^5	1.0×10^3	0.145	19.8	0.127	368	2.1×10^3	75.6	14.6
0.040	18,129	0.174	22.7	2.5×10^5	6.9×10^2	0.101	16.1	0.088	374	1.87×10^3	85	16.7
0.045	20,835	0.20	20.6	2.5×10^5	5.08×10^2	0.073	13.5	0.065	381	1.7×10^3	94	18.8
0.050	23,639	0.227	19.0	2.6×10^5	3.84×10^2	0.0558	11.6	0.05	388	1.55×10^3	102	21

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Table A3.2. Output data for helium at 60 atm, $\Delta T = 20^\circ\text{C}$, and wall loading of 2 MW/m²

d_o (m)	Q (W)	\dot{m} (kg/sec)	V (m/sec)	N_R	ΔP (N/m ²)	ΔP (psi)	PP (W)	%PP	Nu	\bar{h}	ΔT (°C)	
											Film	Wall
0.005	3,848	0.037	308	4.2×10^5	9.25×10^5	134	4539	118	572	2.3×10^4	13.9	4.2
0.010	7,891	0.076	158	4.3×10^5	1.2×10^5	17.5	1217	15.4	584	1.16×10^4	27.2	8.4
0.015	12,130	0.116	108	4.4×10^5	3.74×10^4	5.43	579	4.77	595	7.94×10^3	40	12.5
0.020	16,564	0.159	83	4.5×10^5	1.64×10^4	2.4	348	2.1	607	6.07×10^3	52.4	16.7
0.025	21,194	0.203	68	4.6×10^5	8.8×10^3	1.27	238	1.12	618	4.94×10^3	64.3	21
0.030	26,020	0.25	58	4.7×10^5	5.3×10^3	0.77	176	0.67	630	4.2×10^3	75.7	25.1
0.035	31,041	0.298	51	4.8×10^5	3.48×10^3	0.505	137	0.44	641	3.66×10^3	87	29.3
0.040	36,257	0.348	45.4	5.0×10^5	2.42×10^3	0.35	112	0.309	652	3.26×10^3	97.5	33.5
0.045	41,670	0.4	41.2	5.1×10^5	1.77×10^3	0.256	94.1	0.225	663	2.95×10^3	107.8	37.7
0.050	47,277	0.45	38	5.2×10^5	1.34×10^3	0.194	81	0.17	675	2.7×10^3	118	42

Table A3.3. Output data for helium at 60 atm, $\Delta T = 20^\circ\text{C}$,
and wall loading of 3 MW/m²

d_o (m)	Q (W)	\dot{m} (kg/sec)	V (m/sec)	N_R	ΔP (N/m ²)	ΔP (psi)	PP (W)	%PP	Nu	\bar{h}	ΔT (°C)	
										Film	Wall	
0.005	5,771	0.055	462	6.3×10^5	1.9×10^6	278	1.41×10^4	244	792	3.17×10^4	15	6.3
0.010	11,837	0.113	237	6.5×10^5	2.5×10^5	36.4	3.8×10^3	32	808	1.6×10^4	29.5	12.5
0.015	18,195	0.175	162	6.6×10^5	7.7×10^4	11.3	1.8×10^3	9.9	824	1.1×10^4	43.4	18.8
0.020	24,846	0.238	124	6.8×10^5	3.42×10^4	4.96	1.08×10^3	4.36	839	8.4×10^3	56.8	25
0.025	31,791	0.305	102	6.9×10^5	1.82×10^4	2.65	740	2.33	855	6.8×10^3	69.7	31.4
0.030	39,029	0.375	87	7.1×10^5	1.1×10^4	1.59	548	1.4	871	5.8×10^3	82	37.7
0.035	46,561	0.447	76.2	7.3×10^5	7.2×10^3	1.04	428	0.92	887	5.06×10^3	94	44
0.040	54,386	0.523	68	7.5×10^5	5.03×10^3	0.73	349	0.64	902	4.5×10^3	106	50.2
0.045	62,504	0.6	62	7.6×10^5	3.67×10^3	0.54	292	0.468	918	4.1×10^3	117	56.5
0.050	70,916	0.68	57	7.8×10^5	2.78×10^3	0.4	251	0.354	933	3.7×10^3	128	63

Table A3.4. Output data for helium at 60 atm, $\Delta T = 20^\circ\text{C}$,
and wall loading of 4 MW/m²

d_o (m)	Q (W)	\dot{m} (kg/sec)	V (m/sec)	N_R	ΔP (N/m ²)	ΔP (psi)	PP (W)	%PP	Nu	\bar{h}	ΔT (°C)	
										Film	Wall	
0.005	7,695	0.074	617	8.4×10^5	3.2×10^6	467	31,600	410	996	4×10^4	16	8.4
0.010	15,782	0.151	316	8.6×10^5	4.2×10^5	61	8,479	54	1017	2×10^4	31.2	16.7
0.015	24,260	0.233	216	8.8×10^5	1.3×10^5	19	4,036	16.6	1037	1.4×10^4	46	25.1
0.020	33,128	0.318	166	9×10^5	5.74×10^4	8.3	2,427	7.3	1057	1.05×10^4	60.2	33.5
0.025	42,388	0.407	136	9.3×10^5	3.06×10^4	4.44	1,658	3.91	1077	8.6×10^3	73.8	42
0.030	52,039	0.50	116	9.5×10^5	1.85×10^4	2.68	1,227	2.35	1097	7.3×10^3	87	50.2
0.035	62,081	0.596	101	9.7×10^5	1.2×10^4	1.75	960	1.54	1116	6.4×10^3	99.7	58.6
0.040	72,515	0.697	91	9.9×10^5	8.4×10^3	1.22	781	1.07	1136	5.7×10^3	112	67
0.045	83,339	0.80	82.5	1×10^6	6.1×10^3	0.894	655	0.786	1156	5.2×10^3	124	75
0.050	94,555	0.91	75.8	1×10^6	4.6×10^3	0.676	562	0.595	1175	4.7×10^3	135	84

Table A3.5. Output data for helium at 60 atm, $\Delta T = 20^\circ\text{C}$, and
wall loading of 5 MW/m^2

d_o (m)	Q (W)	\dot{m} (kg/sec)	V (m/sec)	N_R	ΔP (N/m ²)	ΔP (psi)	PP (W)	%PP	Nu	\bar{h}	ΔT (°C)
											Film Wall
0.005	9,619	0.092	771	1×10^6	4.8×10^6	698	5.9×10^4	6.4	1191	4.7×10^4	16.7 10.4
0.010	19,728	0.189	395	1.1×10^6	6.3×10^5	91.3	1.58×10^4	80.2	1216	2.4×10^3	32.7 21
0.015	30,325	0.29	270	1.1×10^6	1.95×10^5	28.2	7.5×10^3	24.3	1240	1.65×10^4	48.1 31.4
0.020	41,410	0.398	207	1.1×10^6	8.6×10^4	12.4	4.5×10^3	10.9	1264	1.26×10^4	63 42
0.025	52,985	0.51	170	1.16×10^6	4.6×10^4	6.6	3.09×10^3	5.84	1287	1.03×10^4	77 52
0.030	65,049	0.62	145	1.2×10^6		4	2.3×10^3	3.52	1311	8.7×10^3	91 63
0.035	77,600	0.746	127	1.2×10^6	1.81×10^4	2.62	1.8×10^3	2.3	1335	7.6×10^3	104 73.2
0.040	90,643	0.87	113	1.24×10^6	1.25×10^4	1.83	1.46×10^3	1.61	1358	6.8×10^3	117 84
0.045	104,170	1.0	103	1.3×10^6	9.2×10^3	1.33	1.22×10^3	1.17	1382	6.1×10^3	129 94
0.050	118,190	1.13	95	1.3×10^6	6.97×10^3	1.01	1.05×10^3	0.89	1405	5.6×10^3	141 105

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Table A3.6. Output data for salt at 7 atm, $\Delta T = 10^\circ\text{C/m}$,
and wall loading of 1 MW/m^2

d_o (m)	Q (W)	\dot{m} (kg/sec)	V (m/sec)	N_R	ΔP (N/m ²)	ΔP (psi)	PP (W)	%PP	Nu	\bar{h}	ΔT (°C)
											Film Wall
0.005	2,070	0.1345	5.0	12,581	28,293	4.1	2.26	0.110	103	14,589	11 2.1
0.010	4,533	0.2944	2.75	13,380	4,161	0.6	0.73	0.016	113	7,862	20 4.2
0.015	7,386	0.48	1.99	15,079	1,431	0.2	0.4	0.005	123	5,615	28.3 6.3
0.020	10,632	0.69	1.61	16,278	692	0.1	0.284	0.0027	133	4,487	35.5 8.4
0.025	14,269	0.925	1.39	17,477	403	0.058	0.222	0.0016	143	3,808	42 10.5
0.030	18,298	1.188	1.23	18,577	263	0.038	0.186	0.001	153	3,353	47.4 12.6
0.035	22,718	1.475	1.12	19,376	185	0.027	0.16	0.0007	153	3,026	52.5 14.6
0.040	27,530	1.78	1.04	21,075	138	0.020	0.146	0.0005	163	2,780	57.2 16.6
0.045	32,734	2.125	0.932	22,274	107	0.0155	0.135	0.0004	173	2,587	61.5 18.8
0.050	38,329	2.48	0.93	23,474	85.7	0.012	0.127	0.0003	183	2,432	65.4 21

Table A3.7. Output data for salt at 7 atm, $\Delta T = 10^\circ\text{C}/\text{m}$,
and wall loading of $2 \text{ MW}/\text{m}^2$

d_o (m)	Q (W)	\dot{m} (kg/sec)	V (m/sec)	N_R	ΔP (N/m ²)	ΔP (psi)	PP (W)	%PP	Nu	\bar{h}	ΔT (°C)
										Film	Wall
0.005	4,141	0.268	10	25,363	98,525	14.3	15.77	0.38	194	25,936	12.3
0.010	9,066	0.588	5.5	27,761	14,490	2.1	5.1	0.056	209	13,977	22.7
0.015	14,773	0.96	3.98	30,159	4,983	0.72	2.84	0.02	224	9,981	32
0.020	21,264	1.38	3.3	32,557	2,412	0.35	1.98	0.009	240	7,977	40
0.025	28,538	1.85	2.7	34,955	1,404	0.20	1.55	0.0054	254	6,770	47
0.030	36,596	2.37	2.47	37,354	915	0.132	1.29	0.003	268	5,960	53.4
0.035	45,436	2.95	2.25	39,752	645	0.093	1.13	0.0025	282	5,380	59
0.040	55,061	3.57	2.09	42,151	480	0.07	1.02	0.0019	296	4,942	64.4
0.045	65,468	4.25	1.96	44,549	372	0.054	0.942	0.0014	310	4,599	69.2
0.050	76,659	4.98	1.86	46,948	298	0.043	0.88	0.0012	324	4,323	73.6

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Table A3.8. Output data for salt at 7 atm, $\Delta T = 10^\circ\text{C}/\text{m}$, and
wall loading of $3 \text{ MW}/\text{m}^2$

d_o (m)	Q (W)	\dot{m} (kg/sec)	V (m/sec)	N_R	ΔP (N/m ²)	ΔP (psi)	PP (W)	%PP	Nu	\bar{h}	ΔT (°C)
										Film	Wall
0.005	6,212	0.4	15.1	38,045	204,414	29.6	49	0.79	272	36,312	13.1
0.010	13,599	0.88	8.26	41,642	30,063	4.36	15.8	0.116	293	19,570	24.4
0.015	22,160	1.44	5.98	45,239	10,340	1.5	8.86	0.04	314	13,975	34.2
0.020	31,896	2.07	4.35	48,836	5,006	0.726	6.17	0.02	335	11,168	42.7
0.025	42,808	2.78	4.16	52,433	2,913	0.423	4.82	0.011	355	9,477	50.4
0.030	54,894	3.56	3.7	56,031	1,899	0.275	4.03	0.007	375	8,345	57.2
0.035	68,155	4.42	3.38	59,628	1,338	0.194	3.52	0.005	395	7,532	63.4
0.040	82,591	5.36	3.13	63,226	996	0.144	3.18	0.004	415	6,919	69
0.045	98,202	6.37	2.94	66,824	772	0.112	2.93	0.003	434	6,439	74.1
0.050	114,989	7.46	2.79	70,422	619	0.09	2.75	0.0024	454	6,053	78.9

Table A3.9. Output data for salt at 7 atm, $\Delta T = 10^\circ\text{C}/\text{m}$,
and wall loading of $4 \text{ MW}/\text{m}^2$

d_o (m)	Q (W)	\dot{m} (kg/sec)	V (m/sec)	N_R	ΔP	ΔP	PP (W)	%PP	Nu	\bar{h}	$\Delta T (\text{ }^\circ\text{C})$	
					(N/m ²)	(psi)					Film	Wall
0.005	8,283	0.537	20.1	50,727	340,000	49.7	109.8	1.32	346	46,105	13.8	8.4
0.010	18,132	1.17	11	55,523	50,457	7.32	35.36	0.19	372	24,848	25.6	16.7
0.015	29,547	1.92	7.97	60,319	17,354	2.52	19.8	0.067	400	17,744	36	25.1
0.020	42,529	2.75	6.46	65,115	8,432	1.22	13.8	0.032	425	14,180	45	33.5
0.025	57,077	3.7	5.5	69,911	4,839	0.71	10.8	0.02	451	12,034	53	41.1
0.030	73,192	4.75	4.94	74,708	3,138	0.46	9.02	0.0123	472	10,596	60.1	50.2
0.035	90,873	5.9	4.5	79,505	2,245	0.32	7.88	0.0087	502	9,563	66.5	58.6
0.040	110,122	7.15	4.18	84,302	1,671	0.24	7.1	0.0065	527	8,785	72.4	67
0.045	130,937	8.5	3.9	89,100	1,237	0.188	6.5	0.005	551	8,176	77.8	75.4
0.050	153,319	9.9	3.72	93,897	1,039	0.15	6.15	0.004	576	7,686	82.8	83.7

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Table A3.10. Output data for salt at 7 atm, $\Delta T = 10^\circ\text{C}/\text{m}$,
and wall loading of $5 \text{ MW}/\text{m}^2$

d_o (m)	Q (W)	\dot{m} (kg/sec)	V (m/sec)	N_R	ΔP	ΔP	PP (W)	%PP	Nu	\bar{h}	$\Delta T (\text{ }^\circ\text{C})$	
					(N/m ²)	(psi)					Film	Wall
0.005	10,353	0.6*	25.1	63,409	500,000	74.4	205	1.98	415	55,487	14.3	10.5
0.010	22,665	1.4*	13.7	69,404	75,398	10.9	66	0.29	443	29,903	26.6	20.9
0.015	36,934	2.4	9.97	75,398	25,933	3.76	37	0.10	480	21,354	37.3	31.4
0.020	53,161	3.45	8.07	81,394	12,555	1.82	25.8	0.048	512	17,066	46.6	41.8
0.025	71,346	4.63	6.93	87,389	7,305	1.05	20.1	0.028	543	14,482	55	52.3
0.030	91,490	5.94	6.17	93,385	4,764	0.69	16.8	0.0184	574	12,752	62.4	62.8
0.035	113,592	7.37	5.63	99,381	3,355	0.486	14.7	0.013	604	11,509	69.1	73.3
0.040	137,652	8.9	5.2	105,377	2,498	0.362	13.2	0.0047	634	10,573	75.2	83.7
0.045	163,671	10.6	4.9	111,374	1,938	0.28	12.2	0.0075	664	9,840	80.9	94.2
0.050	191,649	12.4	4.65	117,371	1,553	0.22	11.5	0.006	693	9,250	86	105

APPENDIX 4
SELECTIONS FROM THE ASME BOILER CODE
ON ALTERNATING STRESSES

The following material provides information on stress and stress analysis which is useful in analyzing the requirements for fusion reactors.

ASME BOILER AND PRESSURE VESSEL CODE
An American National Standard

SECTION III—DIVISION 1
Rules for Construction of
Nuclear Power Plant Components

SUBSECTION NB
Class 1 Components

1974 EDITION

July 1, 1974



ASME BOILER AND PRESSURE VESSEL COMMITTEE
SUBCOMMITTEE ON NUCLEAR POWER

THE AMERICAN SOCIETY OF MECHANICAL ENGINEERS
UNITED ENGINEERING CENTER
345 EAST FORTY-SEVENTH STREET, NEW YORK, N.Y. 10017

NB-3216.1-NB-3221.4

SECTION III, DIVISION 1 -- SUBSECTION NB

(a) Principal Stresses—Consider the values of the three principal stresses at the point versus time for the complete stress cycle taking into account both the gross and local structural discontinuities and the thermal effects which vary during the cycle. These are designated as σ_1 , σ_2 , and σ_3 for later identification.

(b) Stress Differences—Determine the stress differences $S_{12} = \sigma_1 - \sigma_2$, $S_{23} = \sigma_2 - \sigma_3$, $S_{31} = \sigma_3 - \sigma_1$ versus time for the complete cycle. In what follows, the symbol S_{ij} is used to represent any one of these three stress differences.

(c) Alternating Stress Intensity—Determine the extremes of the range through which each stress difference (S_{ij}) fluctuates and find the absolute magnitude of this range for each S_{ij} . Call this magnitude S_{rij} and let $S_{alt,ij} = 0.5S_{rij}$. The alternating stress intensity, S_{alt} , is the largest of the $S_{alt,ij}$'s.

NB-3216.2 Varying Principal Stress Direction. For any case in which the directions of the principal stresses at the point being considered do change during the stress cycle, it is necessary to use the more general procedure of (a) through (e) below.

(a) Consider the values of the six stress components, σ_{ii} , $\sigma_{ii'}$, $\sigma_{ii''}$, τ_{li} , $\tau_{li'}$, $\tau_{li''}$, versus time for the complete stress cycle, taking into account both the gross and local structural discontinuities and the thermal effects which vary during the cycle.

(b) Choose a point in time when the conditions are one of the extremes for the cycle (either maximum or minimum, algebraically) and identify the stress components at this time by the subscript i . In most cases it will be possible to choose at least one time during the cycle when the conditions are known to be extreme. In some cases it may be necessary to try different points in time to find the one which results in the largest value of alternating stress intensity.

(c) Subtract each of the six stress components, σ_{ii} , $\sigma_{ii'}$, from the corresponding stress components, σ_{ii} , $\sigma_{ii'}$, etc., at each point in time during cycle and call the resulting components, σ'_{ii} , $\sigma'_{ii'}$, etc.

(d) At each point in time during the cycle, calculate the principal stresses, σ'_1 , σ'_2 , σ'_3 , derived from the six stress components, σ'_{ii} , $\sigma'_{ii'}$, etc. Note that the directions of the principal stresses may change during the cycle but each principal stress retains its identity as it rotates.

(e) Determine the stress differences $S'_{12} = \sigma'_1 - \sigma'_2$, $S'_{23} = \sigma'_2 - \sigma'_3$, $S'_{31} = \sigma'_3 - \sigma'_1$, versus time for the complete cycle and find the largest absolute magnitude of any stress difference at any time. The alternating stress intensity, S_{alt} , is one-half of this magnitude.

- (2) Local primary membrane stress, P_L (NB-3213.10);
- (3) Primary bending stress, P_b (NB-3213.7 and NB-3213.8);
- (4) Expansion stress, P_e (NB-3213.20);
- (5) Secondary stress, Q (NB-3213.9);
- (6) Peak stress, F (NB-3213.11). NB-3217 provides guidance for this step.

(c) For each category, calculate the algebraic sum of the σ 's which result from the different types of loadings and similarly for the other five stress components. Certain combinations of the categories must also be considered.

(d) Translate the stress components for the t , l , and r directions into principal stresses, σ_1 , σ_2 , and σ_3 . In many pressure component calculations, the t , l , and r directions may be so chosen that the shearing stress components are zero and σ_1 , σ_2 , and σ_3 are identical to σ_t , σ_l , and σ_r .

(e) Calculate the stress differences S_{12} , S_{23} , and S_{31} from the relations

$$\begin{aligned} S_{12} &= \sigma_1 - \sigma_2 \\ S_{23} &= \sigma_2 - \sigma_3 \\ S_{31} &= \sigma_3 - \sigma_1 \end{aligned}$$

The stress intensity, S , is the largest absolute value of S_{12} , S_{23} , and S_{31} .

Note: Membrane stress intensity is derived from the stress components averaged across the thickness of the section. The averaging shall be performed at the component level, in step (b) or (c) above.

NB-3216 Derivation of Stress Differences

If the specified operation of the component does not meet the conditions of NB-3222.4(d), the ability of the component to withstand the specified cyclic operation without fatigue failure shall be determined as provided in NB-3222.4(e). The determination shall be made on the basis of the stresses at a point of the component and the allowable stress cycles shall be adequate for the specified operation at every point. Only the stress differences due to operational cycles as specified in the Design Specification need be considered.

NB-3216.1 Constant Principal Stress Direction. For any case in which the directions of the principal stresses at the point being considered do not change during the cycle, the steps stipulated in the following subparagraphs shall be taken to determine the alternating stress intensity.

- (1) General primary membrane stress, P_m (NB-3213.8):

¹See Tables NB-3217-1 and NB-3217-2 and Note 1 of Figure NB-3221-1.

ASME BOILER AND PRESSURE VESSEL CODE
An American National Standard

SECTION III—DIVISION 1
Rules for Construction of
Nuclear Power Plant Components

SUBSECTION NA
General Requirements
(Includes All Appendices)

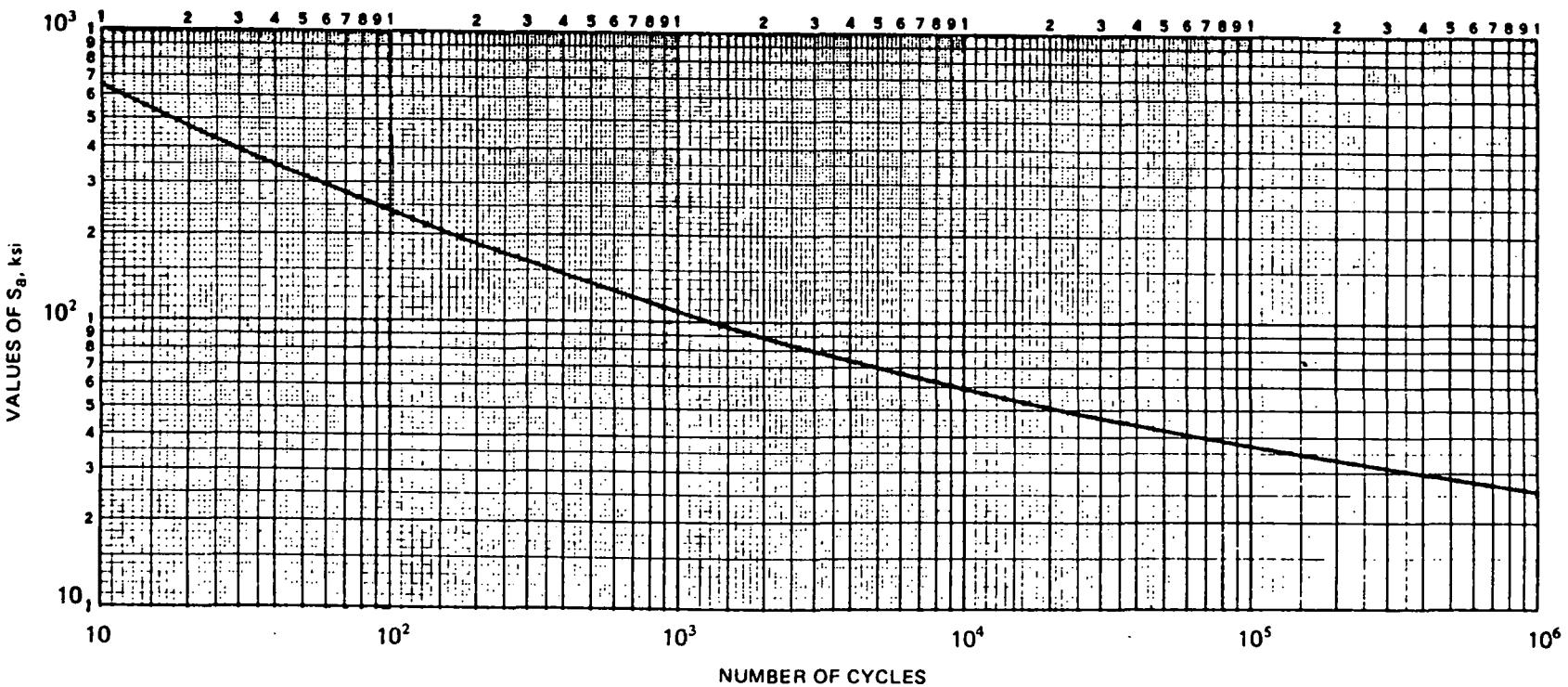
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345 EAST FORTY-SEVENTH STREET, NEW YORK, N.Y. 10017



NOTE:

FIG. I-9.2 DESIGN FATIGUE CURVE FOR AUSTENITIC STEELS, NICKEL-CHROMIUM-IRON ALLOY, NICKEL-IRON-CHROMIUM ALLOY AND NICKEL-COPPER ALLOY

Fig. 1-9.2

APPENDIX 5
STRESSES AT THE BEND OF A
U-SHAPED TUBE

To find the stresses in the U-shaped tube shown in Fig. A5.1, we may consider only half the tube because of symmetry. The conditions shown in Fig. A5.1 (tube free at one end and subjected to nonuniform heating) will result in the tube deformation shown in Fig. A5.2.

The compatibility equations are

$$\beta - \theta_c = aM + bV \quad , \quad (A5.1)$$

$$\theta_c - \beta_2 = eM - fV \quad , \quad (A5.2)$$

$$\delta_1 = bM + cV \quad , \quad (A5.3)$$

$$\delta_2 = fM - gV \quad , \quad (A5.4)$$

and

$$\Delta_1 - \Delta_2 = \delta_1 + \delta_2 \quad , \quad (A5.5)$$

where a , b , c , e , f , and g are influence coefficients and V , M , δ_1 , δ_2 , and θ_c are unknowns. We can calculate the influence coefficients and β_1 , β_2 , Δ_1 , and Δ_2 given the assumption that the tube will bend like a beam and the plane section will remain plane. From Fig. A5.3, we can deduce

$$\frac{\rho}{\rho d\theta} = \frac{r}{\rho d\theta \frac{\Delta T \alpha}{2}} \quad ,$$

where α = coefficient of expansion of tube material. Thus,

$$\rho = \frac{2r}{\alpha \Delta T} \quad ,$$

$$\beta_1 = \ell/\rho \quad ,$$

and

$$\Delta_1 = \rho(1 - \cos \beta_1) \quad .$$

For the circular tube illustrated in Fig. A5.4,

$$e' = \frac{2r}{\alpha \Delta T} \quad ,$$

$$\beta_2 = \frac{\pi R}{2r} \alpha \Delta T \quad ,$$

and

$$\Delta_2 = \alpha \frac{(T_H + T_C)}{2} \quad .$$

We calculate the influence coefficients as

$$a = \frac{\ell}{EI} \quad , \quad b = \frac{\ell^2}{2EI} \quad , \quad c = \frac{\ell^3}{3EI} \quad , \quad e = \frac{\pi R}{2EI} \quad ,$$

$$f = \frac{R^2}{EI} \left(\frac{\pi}{2} - 1 \right) \quad , \quad g = \frac{R^3}{EI} \left(\frac{3\pi}{4} - 2 \right) \quad ,$$

where E is the modulus at average material temperature and $I = \pi r^3 t$.

Therefore,

$$\frac{\ell \alpha \Delta T}{2r} - \theta_c = \frac{\ell}{EI} M + \frac{\ell^2}{2EI} V \quad (A5.6)$$

$$- \frac{\pi}{2} \left(1 - \frac{\alpha \Delta T \cdot R}{2r} \right) + \theta_c = \frac{\pi R}{2EI} M - \frac{R^2}{EI} \left(\frac{\pi}{2} - 1 \right) V \quad ,$$

$$\delta_1 = \frac{\ell^2}{2EI} M + \frac{\ell^3}{3EI} V \quad , \quad (A5.7)$$

$$\delta_2 = \frac{R^2}{EI} \left(\frac{\pi}{2} - 1 \right) M - \frac{R^3}{EI} \left(\frac{3}{4} \pi - 2 \right) V \quad , \quad (A5.8)$$

and

$$\frac{2r}{\alpha \Delta T} \left[1 - \cos \left(\frac{\ell \alpha \Delta T}{2r} \right) \right] - \alpha \frac{(T_H + T_C) R}{2} = \delta_1 + \delta_2 \quad . \quad (A5.9)$$

We may solve Eqs. (A5.6) through (A5.9) simultaneously and parametrically. We are able to vary R , t , ℓ , r , ΔT within the system constraints to see what happens to stress.

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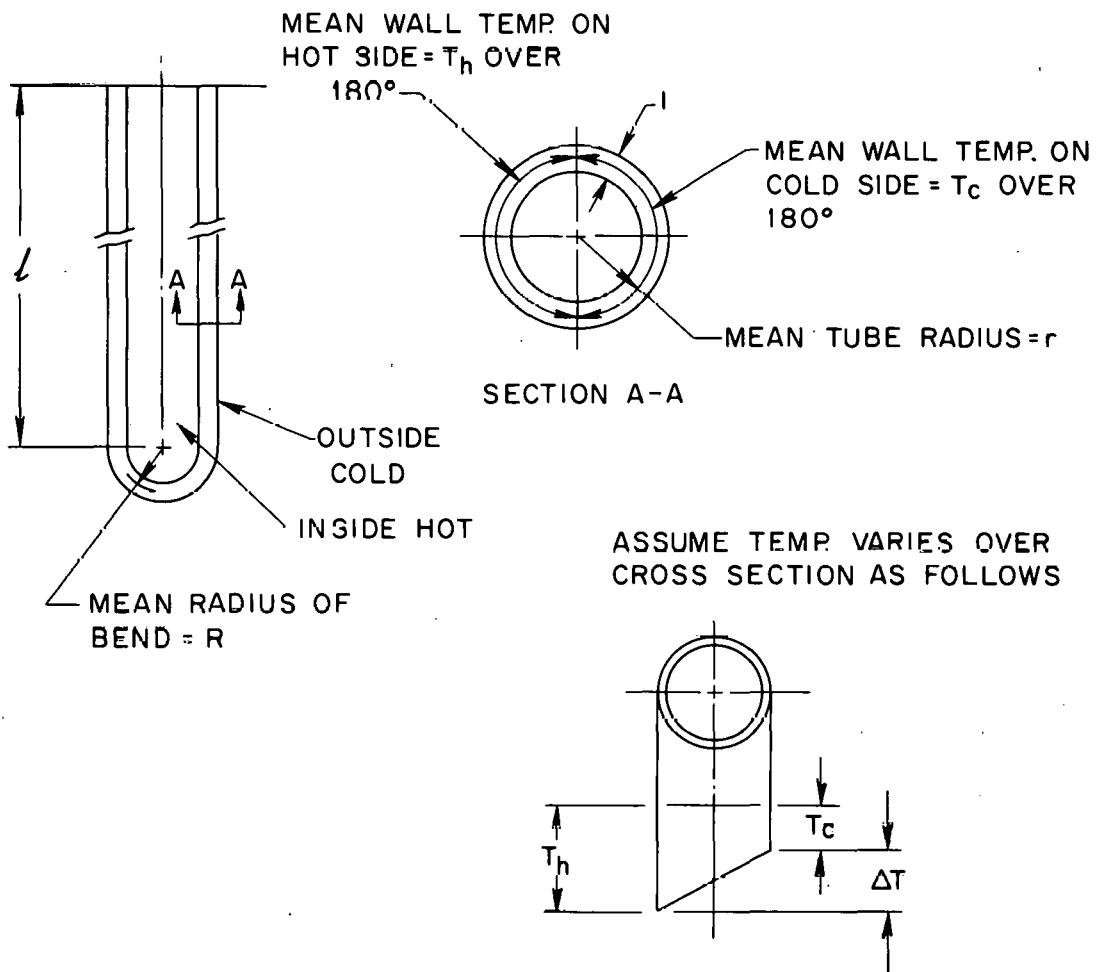


Fig. A5.1. Stresses in a U-shaped tube.

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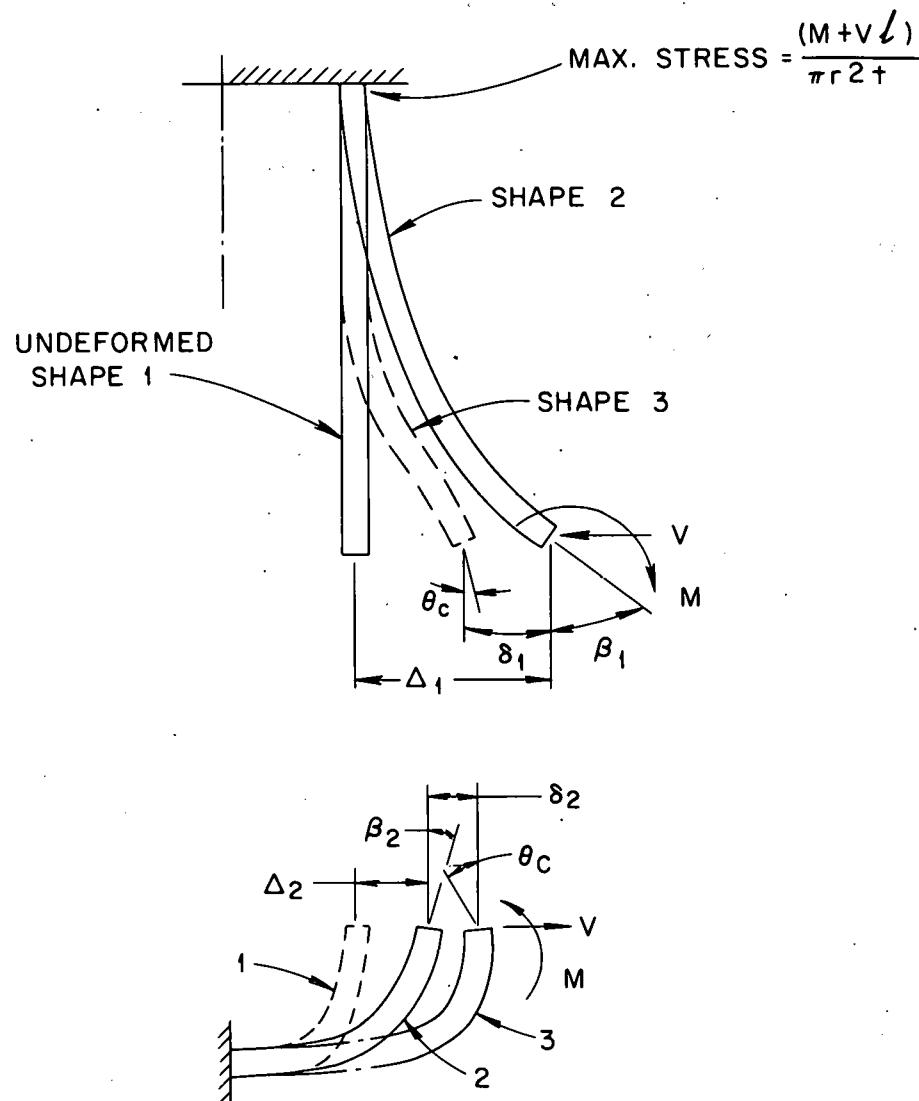


Fig. A5.2. Deformation of U-shaped tube. Shape 2 is the shape the tube would assume if it were free on the end and heated as shown. Shape 3 is the final shape of the tube. V is the internal shear force and M is the moment induced in the tube.

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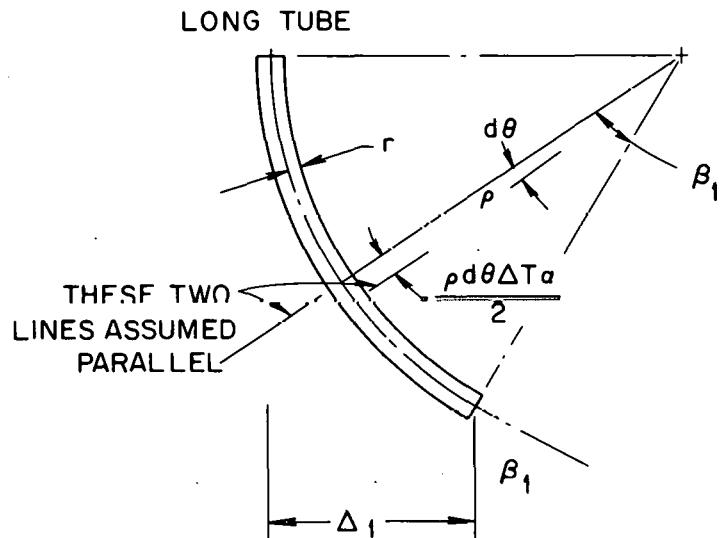


Fig. A5.3. Deformation in a long tube.

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CIRCULAR TUBE

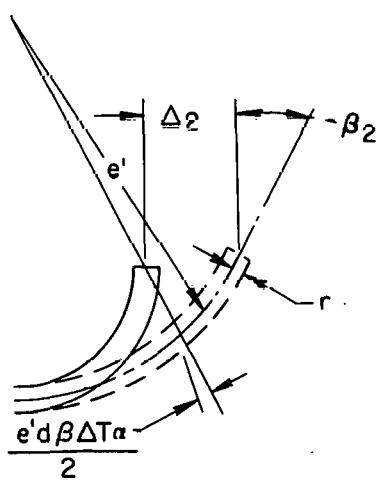


Fig. A5.4. Deformation in a circular tube.

APPENDIX 6
EQUATION FOR TEMPERATURE PROFILES
IN THE LITHIUM

For steady-state temperatures in a one-dimensional system with internal heat sources,

$$t_2 = \frac{-Q_0 e^{-\mu L}}{k\mu^2} + C_1 L + C_2 \quad , \quad (A6.7)$$

$$\frac{d^2t}{dx^2} + \frac{\dot{q}}{k} = 0 \quad , \quad (A6.1) \quad \text{where}$$

For a fusion reactor blanket the internal heat deposition is exponential so that

$$C_1 = \frac{-Q_0 e^{-\mu L}}{k\mu} \quad . \quad (A6.8)$$

$$\frac{d^2t}{dx^2} = \frac{-Q_0 e^{-\mu x}}{k} \quad , \quad (A6.2)$$

where

$$\dot{q} = Q_0 e^{-\mu x} \quad , \quad (A6.3)$$

$$\frac{dt}{dx} = \frac{Q_0 e^{-\mu x}}{k\mu} + C_1 \quad , \quad (A6.4)$$

$$t = \frac{-Q_0 e^{-\mu x}}{k\mu^2} + C_1 x + C_2 \quad . \quad (A6.5)$$

In establishing the temperatures in the lithium in the cassette units, we use the boundary conditions shown in Fig. A6.1 and the following definitions:

$t = t_1$ at $x = 0$,

$t = t_2$ at $x = L$,

$dt/dx = 0$ at $x = L$.

From these conditions we may calculate t_1 and t_2 ,

$$t_1 = \frac{-Q_0}{k\mu^2} + C_2 \quad (A6.6)$$

and

Subtracting Eq. (A6.6) from Eq. (A6.7) yields

$$t_2 - t_1 = \frac{-Q_0 e^{-\mu L}}{k\mu^2} + C_1 L + \frac{Q_0}{k\mu^2} \quad . \quad (A6.9)$$

Substituting the value of C_1 [from Eq. (A6.8)] into Eq. (A6.9), we obtain

$$t_2 - t_1 = \frac{-Q_0 e^{-\mu L}}{k\mu^2} + \left(\frac{-Q_0 e^{-\mu L}}{k\mu} L \right) + \frac{Q_0}{k\mu^2} \quad .$$

Thus, the temperature at L is

$$t_L - t_1 = \frac{Q_0}{k\mu^2} \left(-e^{-\mu L} - \mu L e^{-\mu L} + 1 \right) \quad , \quad (A6.10)$$

and for the temperature distribution within the region of thickness L (when $x < L$) we have

$$t - t_1 = \frac{Q_0}{k\mu^2} \left(e^{-\mu x} - \mu x e^{-\mu L} + 1 \right) \quad . \quad (A6.11)$$

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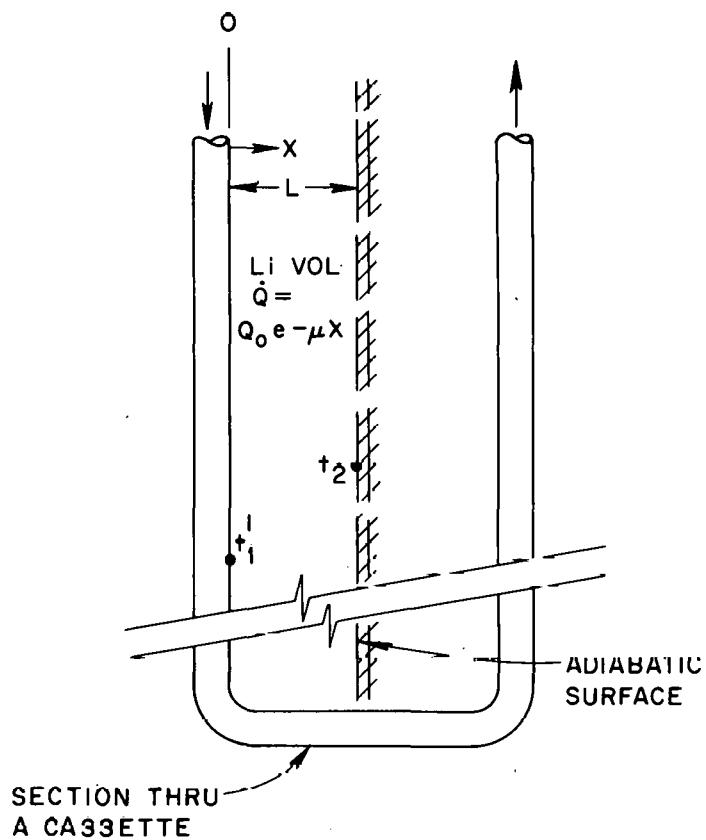


Fig. A6.1. Boundary conditions for calculating temperatures in lithium.

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