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Formal Report (Summary)

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**Beam Stability and Nonlinear  
Dynamics Symposium**  
(December 3 - 5, 1996)

**Summary Report**

**BY**

**Zohreh Parsa**

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# Beam Stability and Nonlinear Dynamics

(December 3 - 5, 1996)

## SYMPOSIUM SUMMARY REPORT

By

Zohreh Parsa

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# Beam Stability and Nonlinear Dynamics

(December 3 - 5, 1996)

## Symposium Summary Report

By

Zohreh Parsa

A "Beam Stability and Nonlinear Dynamics" Symposium was held October 3 - 5, 1996 at the Institute for Theoretical Physics (ITP) in Santa Barbara. This was one of the 3 symposia hosted by the ITP and supported by its sponsor, the National Science Foundation, as part of our "New Ideas for Particle Accelerators" program. The symposia was organized and chaired by Dr. Zohreh Parsa of ITP/ Brookhaven National Laboratory. [A 4 member program advisory committee was selected Three who participated included: Z. Parsa, G. Guignard, J. Irwin].

The purpose of this symposium was to deal with some of the fundamental theoretical problems of accelerator physics by bringing together leaders from accelerator physics communities, mathematics, and other fields of physics. The focus was on nonlinear dynamics and beam stability. The symposium began with some defining talks on relevant mathematical topics such as single-particle Hamiltonian dynamics, chaos, and new ideas in symplectic integrators. The physics topics included single-particle and many-particle dynamics. These topics concern circular accelerators in which particles circulate for a very large number of turns as well as linear accelerators where space charge and wakefields induced in accelerating cavities play a strong role.

A major question is to determine the best model for numerical simulations in order to accurately reproduce behavior of beams in real accelerators and to predict long-term or long distance stability. Comparison with experiment is recognized as an important tool in improving models.

\*This work was performed under the auspices of the U.S. Department of Energy under Contract No. DE-AC02-76CH00016 and NSF-PHY-94-07194.

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Straight-forward tracking using linear elements and thin-lens multipoles to preserve symplecticity is the basic tool for studying single-particle dynamics and stability in large circular accelerators such as the Large Hadron Collider (LHC), which was recently approved for construction at CERN. Ideas have been aimed at improving the computation time and/ or in improving analysis of the results. Symplectification of Taylor maps was an important topic that was presented since truncation of expansion maps leads to maps that are not symplectic. The concept of jolt factorization makes it possible to obtain a symplectic truncated expansion. But if the nonlinearity is too large, as is usually the case near the onset of unstable motion, map predictions fail. This raises the difficult question of the applicability of a complete-turn map to a large accelerator. The expansion of such maps is laborious for phase-space dimensions larger than four. Another related development is the use of Taylor's models with additional functions which bound the initial function from above and below. Application of this concept to maps led to the development of an arithmetic, which applies to both the polynomial and the remainders, termed Remainder Differential Algebra. This should provide information on the accuracy of the map description. Symplecticity is ensured if we use the Hamiltonian formalism and action-angle variables. In this approach, the map over one turn or a fraction of turn can be computed by solving algebraic equations related to canonical transformations which are in implicit form. This is done for the non-periodic solutions of the generating function equation by using Newton iterations and approximation in Fourier series and B-spline functions.

Interesting results of numerous trackings and analyses (including those developed during our ITP workshop) were presented for the LHC. Different methods for estimating the dynamic aperture were tested, first using the Henon map. Early indicators such as the Lyapunov criterion, frequency map analysis, and variation of tunes have been used with tracking over an increasing number of turns. A new conjecture combining the result of the KAM theorem with the Nkhoroshev estimate predicts that the dynamic aperture depends on the inverse logarithm of the number of turns. There is remarkable agreement between the predictions of the early indicators and the result of

the conjecture extrapolated to a very large number of revolutions. This gives an increased confidence in the numerical predictions, to within 10 or 20% of the actual value as supported by measurements on existing accelerators.

Particular examples of stability analysis were presented, such as a Hamiltonian system with a quartic potential and the three-body problem in celestial mechanics. Linearization around a periodic solution in the first case and around a Lagrangian fixed point in the second, provides a monodromic matrix which give information on the stability. For the three-body problem, developments to second order allows us to solve the equation of motion near resonance. Also presented was the idea to apply to accelerator dynamics the wavelet analysis of Hamiltonian systems.

Among the other subjects treated were spin dynamics, nonlinear aberration correction including space charge aberrations, collective effects in the LHC, sawtooth instability, and Landau damping in the presence of strong nonlinearity. There were other presentations concerning plasma physics effects relevant to accelerators. And the peculiar effect of beam echos that has recently been observed for the first time in an existing accelerator with echo times as long as one to two minutes. Numerical tools for studying multibunch instability in linear accelerators with strong wakefields were presented, together with a statistical method of analysis of wakefield effects on emittance growth, based on beamline response coefficients.

The conference ended with a unique discussion session in which participants presented and clarified their views on outstanding problems and topics presented at the symposium. This international forum has provided new and valuable input for future developments in this field.

#### **Summary of New Things in Nonlinear Beam dynamics:**

- Recent development of the Remainder Differential Algebra for Taylor's maps.
- Suggestion of using wavelets for solving our nonlinear problems since they apply to Hamiltonian systems with perturbations.
- First or recent measurements on echos in accelerator beams, initially described for plasmas.

- New conjecture for very-long-time dynamic aperture and evidence of convergence of this estimate with early indicators.
- Statistical analysis of strong Wakefield effects on the emittance growth in high frequency linac.

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ITP Conference on  
**Particle Beam Stability and Nonlinear Dynamics**  
December 3-5, 1996  
*Coordinator, Zohreh Parsa*  
**SCHEDULE**

**Tuesday, December 3, 1996:**

| Time:            | Speaker:                | Title:  |
|------------------|-------------------------|---|
| <u>Convener:</u> | <b>Z. Parsa</b>         |   |
| 8:00 am          | Registration            | ITP Front Lobby   |
| 8:40             | Welcome                 | J. Hartle, ITP Director   |
|                  | Intro. & Welcome        | Z. Parsa, BNL   |
| 9:00             | J. Meiss, U Colorado    | Single-Particle Hamiltonian Dynamics  |
| 9:45             | Refreshment Break       | ITP Center Patio  |
| <u>Convener:</u> | <b>G. Guignard</b>      |   |
| 10:15            | J. Marsden, Cal Tech    | Symplectic Geometry, Maps, Integrators  |
| 11:00            | M. Berz, Michigan State | From Taylor Series to Taylor Models & Remainder Differential Algebra with Interval Arithmetic |
| 11:45            | A. Dragt, UM            | Factorization of Taylor Maps  |
| 12:25 pm         | Lunch Break             | ITP Center Patio  |
| <u>Convener:</u> | <b>J. Hagel</b>         |   |
| 2:00             | J. Irwin, SLAC          | One-Turn Map Generators Aberration Sources, Consequences, and Corrective Actions              |
| 2:40             | E. Todesco, INFN        | Long-Term Orbit Stability Predictions (Lyapunov estimates, Normal Forms)                      |
| 3:25             | Refreshment Break       | ITP Center Patio  |
| <u>Convener:</u> | <b>W. Lysenko</b>       |   |
| 4:00             | J. Laskar, BDL          | Frequency Map Analysis - Theory & Experiments   |
| 4:45             | R. Warnock, SLAC        | The Effect of Resonances on Long-Term Stability & Symplectic Full Turn Maps                   |
| 5:30             | Wine & Cheese           | ITP Center Patio  |
| 6:15             | Conference Dinner       | ITP Center Patio  |

Wednesday, December 4, 1996

| Time:   | Speaker:                           | Title:  |
|---------|------------------------------------|---|
|         | <u>Convener:</u> <b>D. Robin</b>   |   |
| 8:30 am | V. Balandin, DESY                  | Nonlinear Spin Dynamics   |
| 9:10    | F. Schmidt, CERN                   | Dynamic Aperture - Simulation and Experiment                              |
| 9:55    | Refreshment Break                  | ITP Center Patio  |
|         | <u>Convener:</u> <b>J. Ellison</b> |   |
| 10:25   | F. Ruggiero, CERN                  | Longitudinal Beam Echoes & Diffusion Rates                                |
| 11:05   | R. Siemann, SLAC                   | Sawtooth Instability & Over-Shoot Phenomena                               |
| 11:45   | H. Yoshida, NAO                    | Instability of Periodic Orbit and Non-Integrability of Hamiltonian System |
| 12:25pm | Lunch Break                        | ITP Center Patio  |
|         | <u>Convener:</u> <b>J. Krommes</b> |   |
| 1:40    | P. Zenkevitch, ITEP                | Neutralized Beams: Landau Damping in Systems with Strong Nonlinearity     |
| 2:20    | G. Guignard, CERN                  | Stability of Beams in a High Frequency Linac with Strong Wakefields       |
| 3:05    | Refreshment Break                  | ITP Center Patio  |
|         | <u>Convener:</u> <b>E. Lessner</b> |   |
| 3:35    | M. Zeitlin, IPME                   | Wavelet Analysis of Hamiltonian System and its Perturbations              |
| 4:20    | S. Andrianov, St. Petersburg       | Nonlinear Aberration Correction   |
| 4:55    | S. Heifets, SLAC                   | Search of the Mechanism of the Saw-Tooth Instability                      |
| 5:30    | Reception                          | ITP Center Patio  |

**Thursday, December 5, 1996**

| Time:    | Speaker:   | Title:  |
|----------|--|---|
|          | <b><u>Convener:</u></b> <b>A. Chao</b>   |   |
| 8:30     | F. Ruggiero, CERN  | Collective Effects in LHC   |
| 9:05     | J. Hagel, Univ Maderia   | Galaxy Dynamics: Resonance Analysis in Celestial Mechanics  |
| 9:50     | Refreshment Break  | ITP Center Patio  |
|          | <b><u>Convener:</u></b> <b>M. Berz</b>   |   |
| 10:20    | A. Pankin, INR   | Nonlinear Structure Near Boundary of Marginal Stability   |
| 10:40    | G. Stupakov  | Nonlinear Dynamics of Single Bunch Instability in Accelerators                                      |
| 11:10    | V. Zadorozhny, IC  | The Dynamic 2-D Electron Beams of the Plasma Lense  |
| 11:30    | TBA  | Map Measurements  |
| 11:45    | G. Guinard   | Statistical Analysis of Emittance Growth  |
| 12:20 pm | Lunch Break  | ITP Center Patio  |
|          | <b><u>Convener:</u></b> <b>R. Siemann</b>  |   |
| 1:50     | Round Table Discussions on Outstanding Issues in Beam Instabilities and Nonlinear Accelerator Dynamics | Z. Parsa, A. Dragt, G. Guignard, J. Laskar, J. Meiss, E. Todesco, & other speakers and participants |
| 3:00     | Z. Parsa, BNL  | Summary and Closing Talk  |

**Conference Ends**

TBA = To be announced

\* = late contributions

BNL = Brookhaven National Laboratory

FNAL = Fermi National Laboratory

LANL = Los Alamos National Laboratory

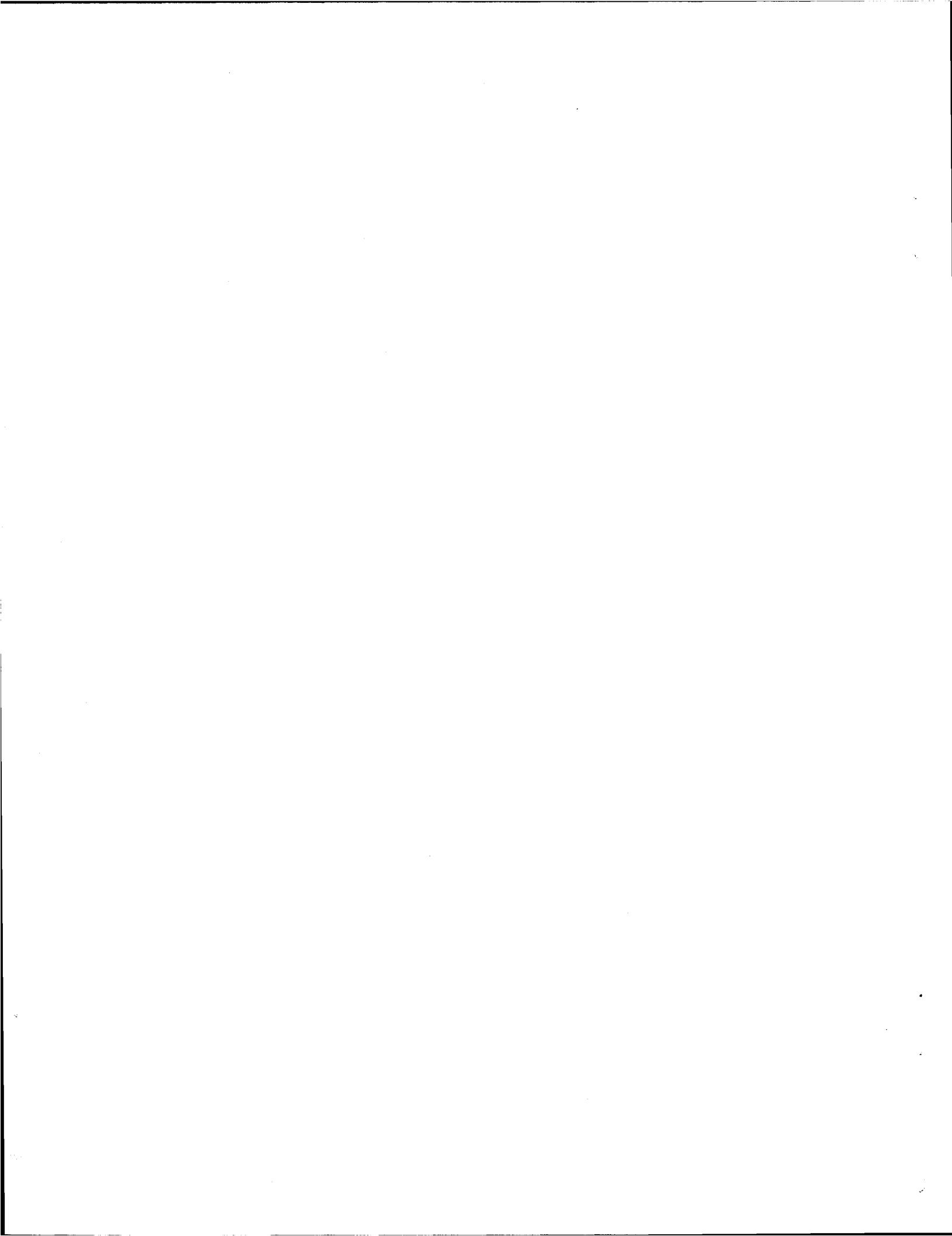
SLAC = Stanford Linear Accelerator Center

DOE = Department of Energy

NSF = National Science Foundation

UCLA = Univ. California Los Angeles

UCSB = Univ. California Santa Barbara



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