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RE-34, AN IBM-704 REACTOR SHIELDING PROGRAM

by

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HISTORY AND ACKNOWLEDGMENTS

The problem which this program solves was originally proposed in 1955 by J. W. Butler and M. Grotenhuis. At this time the Laboratory did not have a computing machine with a sufficiently large memory to adequately solve the problem; consequently, when the IBM-704 was installed in November of 1957 the problem was reviewed and the program described in this report prepared.

J. Heestand assisted the authors by checking the machine program, while J. W. Butler and M. Grotenhuis, in addition to being very patient, contributed advice and assistance throughout the development of the program.

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ABSTRACT

An IBM-704 shielding program is described which solves, by a finite difference method, the multigroup diffusion equation system in slab, cylindrical, or spherical geometry, with a prescribed source distribution given for the highest energy group. A wide choice of boundary conditions has been made available at the outer boundaries and either continuity of flux and current or the "black boundary" condition may be specified at each regional interface.

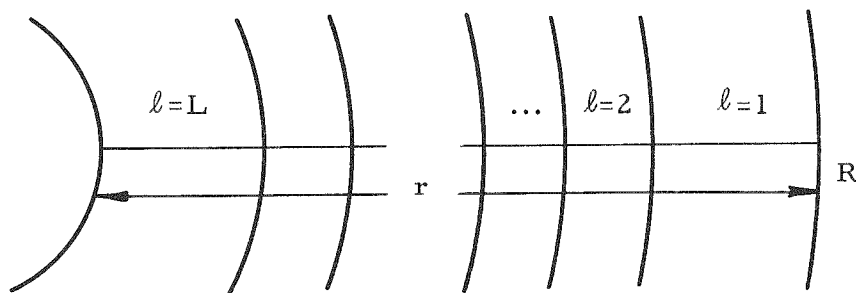
The machine time required to process an average problem is approximately 1-2 minutes. This includes reading in the program deck.

I. INTRODUCTION

The purpose of this report is to present the IBM-704 program for solving the one-dimensional multigroup diffusion equation system of reactor shielding problems.

The problem originator specifies certain problem parameters, such as the outer boundary, energy group divisions, geometrical and material properties of each region, and the source distribution for the highest energy group which enable the program to solve the diffusion equation system printing the flux distributions, the integrals of the fluxes, neutron leakages and balance checks for each region, as well as the value of the current at the outer boundary and at any regional interface where a "black" sheet has been inserted.

The outer edge of the reactor shield is designated as R and the reactor or the reactor shield whichever is being considered is divided into L regions, ($1 \leq L \leq 100$), numbered from R inward to the inner boundary which may be at the center of the reactor or at the beginning of any shield region.



Each region, ℓ , is divided into H_ℓ sub-intervals of equal thickness, Δ_ℓ . The lattice points in each region, designated by integers, are numbered from the outer edge of the region inward, h_ℓ , ($0 \leq h_\ell \leq H_\ell$). It is at these points that the source for the highest energy group is specified, the fluxes and lower energy group sources are computed, and numerical integration is performed, $\left(\sum_{\ell=1}^L H_\ell + L \leq 1000 \right)$.

The neutron energy spectrum is divided into a set of J energy groups, ($J \geq 1$). In the numerical solution of the problem the set of J diffusion equations of the form

$$\nabla (D \nabla \phi) - \sigma \phi + S = 0,$$

is replaced by a set of J coupled difference equations, where

$$D \text{ is the diffusion coefficient } \left(= \frac{1}{3\sigma_{tr}} \right),$$

$$\sigma \text{ is the removal cross section } (= \sigma_{\text{elastic}} + \sigma_{\text{capture}} + DB^2),^*$$

ϕ is the neutron flux,

and S is the source term prescribed as input data point by point for $j = 1$, and computed for the lower energy groups, $j \neq 1$, as $S_j = s_{j-1} \sigma_{j-1} \phi_{j-1}$,

where s_{j-1} is the transfer fraction for the $j-1$ st energy group.

Before describing the boundary conditions available it will be helpful to distinguish the inner and outer edges from the interior regional boundaries. This has been done by referring to only the inner and outer boundaries of the problem as boundaries and applying the term interfaces to the interior boundaries.

At the inner edge of the problem, (the point of minimum r value), any of three boundary conditions may be employed. The derivative of the flux may be set equal to zero, the flux value, k , may be specified, or if $r \neq 0$, the "black boundary" condition, $-\frac{1}{\phi} \frac{d\phi}{dr} = \frac{1}{d}$, may be imposed.

*This is not the usual removal cross section as defined for shielding work.

At each interface the problem originator has two choices; he may elect the standard boundary condition of continuity of flux and current or a "black boundary" condition may be chosen. The "black boundary" condition may be written as

$$-\frac{1}{\phi} \frac{d\phi}{dr} = \frac{1}{d} \text{ for the inner region,}$$

and

$$\frac{1}{\phi} \frac{d\phi}{dr} = \frac{1}{d} \text{ for the outer region.}$$

At the outer boundary, ($r = R$), the flux may be set equal to zero, the derivative of the flux may be set equal to zero, or the "black boundary" condition may be applied.

These boundary conditions are specified and applied at each boundary and on both sides of each interface. Obviously, if an interface is a "black boundary" to one of its adjacent regions, it is a "black boundary" to the other, or if the continuity condition is used for one adjacent region it must be used for the other.

The input data may be divided into three categories - the general problem parameters, the point-by-point source distribution for the highest energy group, and the group-region parameters. Included in the general problem parameters are such items as the problem number, the geometry (N), J , L , R , and the interval size ($\Delta\ell$), and number of intervals (H_ℓ), included in each region. The group-region parameters for each region and each energy group consist of the boundary condition indicators for both the outer (d_0), and the inner (d_I) boundaries of the region, D , σ , and s . A more detailed description of the input is provided in Section III.

No description of the IBM-704 computer will be attempted here, instead the reader is referred to the IBM-704 Data Processing System Reference Manual, IBM Form A22-6500-0.

II. DESCRIPTION OF NUMERICAL METHOD

We are to solve the diffusion equation $D\nabla^2\Phi - \sigma\Phi + Q = 0$ for three different reactor shapes: slab ($N = 1$), cylinder ($N = 2$), and sphere ($N = 3$).

$$\Phi = \phi(r) \psi(\theta_1, \dots, \theta_{N-1}), \text{ where } \nabla^2\Phi = (\nabla^2\phi)\psi + \phi \cdot (\nabla^2\psi), \text{ and } \nabla^2\psi = -\mathcal{L}\psi$$

The \mathcal{L} corresponds to neutron leakage out of the reactor in directions parallel to the surfaces $r = \text{constant}$. If we consider it as a form of absorption, add it to σ , and factor out ψ ; the diffusion equation becomes an ordinary differential equation $D\nabla^2\phi - \Sigma\phi + S = 0$ in r , with $\nabla^2 = \frac{1}{r^{N-1}} \frac{d}{dr} r^{N-1} \frac{d}{dr}$ and

$\Sigma = \sigma + D\mathcal{L}$. The range of r is from b_0 to b_L with $0 \leq b_0 < b_L$. The boundary conditions are of the form $A_0 = A_1\phi(b_0) + A_2\phi'(b_0)$ and $0 = \phi(b_L) + d\phi'(b_L)$.

We use the following difference approximation to the differential operators (see ANL-5437, Sec. V, note (6)):

$$\begin{aligned} \left[\frac{d\phi}{dr} \right]_{r_n} &= \frac{1}{2\Delta r} \left[\left(1 + \frac{1}{2n}\right)^{N-1} \phi_{n+1} + \left(\left(1 - \frac{1}{2n}\right)^{N-1} - \left(1 + \frac{1}{2n}\right)^{N-1} \right) \phi_n - \left(1 - \frac{1}{2n}\right)^{N-1} \phi_{n-1} \right] \\ \left[\nabla^2\phi \right]_{r_n} &= \frac{1}{(\Delta r)^2} \left[\left(1 + \frac{1}{2n}\right)^{N-1} \phi_{n+1} - \left(\left(1 + \frac{1}{2n}\right)^{N-1} + \left(1 - \frac{1}{2n}\right)^{N-1} \right) \phi_n + \left(1 - \frac{1}{2n}\right)^{N-1} \phi_{n-1} \right] \text{ if } r_n \neq 0 \\ &= \frac{N}{(\Delta r)^2} \left[\phi_{-1} - 2\phi_0 + \phi_1 \right] \text{ if } r_n = 0 \end{aligned}$$

where

$$n = n_{\ell, h\ell} = r_n / \Delta r \text{ need not be integral.}$$

The differential system to be solved is given by

$$\begin{aligned} (b_1) \quad D_\ell \nabla^2 \phi(r) - \Sigma_\ell \phi(r) + S(r) &= 0 & b_{\ell-1} < r < b_\ell \\ & & 1 \leq \ell \leq L \\ (b_2) \quad D_\ell \left[\frac{d\phi}{dr} \right]_{b_{\ell-}} &= D_{\ell+1} \left[\frac{d\phi}{dr} \right]_{b_\ell+} & 1 \leq \ell < L \\ & & 1 \leq \ell < L \\ (b_3) \quad \phi(b_{\ell-}) &= \phi(b_{\ell+}) \\ (b_4) \quad \phi(b_L) + d\phi'(b_L) &= 0 \\ (b_5) \quad A_1 \phi(b_0) + A_2 \phi'(b_0) &= A_0 \end{aligned}$$

We replace this system by the following difference system

$$(c_1) \frac{D_\ell}{(\Delta_\ell r)^2} \left[p_\ell(h_\ell) \phi_\ell(h_\ell + 1) - (p_\ell(h_\ell) + q_\ell(h_\ell)) \phi_\ell(h_\ell) + q_\ell(h_\ell) \phi_\ell(h_\ell - 1) \right] \\ - \Sigma_\ell \phi_\ell(h_\ell) + S_\ell(h_\ell) = 0 \quad 0 < h_\ell < H_\ell, \quad 1 \leq \ell \leq L$$

$$(c_2) \frac{D_\ell}{\Delta_\ell r} \left[p_\ell(H_\ell) \phi_\ell(H_\ell + 1) + (q_\ell(H_\ell) - p_\ell(H_\ell)) \phi_\ell(H_\ell) - q_\ell(H_\ell) \phi_\ell(H_\ell - 1) \right] =$$

$$\frac{D_{\ell+1}}{\Delta_{\ell+1} r} \left[p_{\ell+1}(0) \phi_{\ell+1}(1) + (q_{\ell+1}(0) - p_{\ell+1}(0)) \phi_{\ell+1}(0) - q_{\ell+1}(0) \phi_{\ell+1}(-1) \right]$$

$$(c_3) \phi_\ell(H_\ell) = \phi_{\ell+1}(0)$$

$$(c_4^*) (d + \Delta_L r) \phi_L(H_L) - d \phi_L(H_L - 1) = 0$$

$$(c_5) a_0 \phi_1(0) + a_1 \phi_1(1) = a_2,$$

where functions of n_{ℓ, h_ℓ} are written as $f_{n_{\ell, h_\ell}} = f_\ell(h_\ell)$, and the derivative $\phi'(b_L)$ in the extrapolated end-point condition (C_4^*) is approximated by $(\phi_L(H_L) - \phi_L(H_L - 1))/\Delta_L r$. The quantities p and q are defined by

$$p_\ell(h_\ell) = \left(1 + \frac{1}{2n_{\ell, h_\ell}} \right)^{N-1} \quad \text{and} \quad q_\ell(h_\ell) = \left(1 - \frac{1}{2n_{\ell, h_\ell}} \right)^{N-1}$$

The fictitious fluxes $\phi_\ell(-1)$ and $\phi_\ell(H_\ell + 1)$ are defined outside of the ℓ^{th} region R_ℓ by using (c_1) to extend across the boundary.

We now use (c_1) on (c_2) to eliminate these extensions. Then let $\lambda_\ell = (\Delta_\ell r)^2/D_\ell$ and $k_\ell(h_\ell) = p_\ell(h_\ell) + q_\ell(h_\ell) + \lambda_\ell \Sigma_\ell$, and (c) becomes:

$$(d_1) p_\ell(h_\ell) \phi_\ell(h_\ell + 1) - k_\ell(h_\ell) \phi_\ell(h_\ell) + q_\ell(h_\ell) \phi_\ell(h_\ell - 1) + \lambda_\ell S_\ell(h_\ell) = 0 \\ 0 < h_\ell < H_\ell, \quad 1 \leq \ell \leq L$$

$$(d_2) \Delta_\ell r \cdot \lambda_{\ell+1} [-2q_\ell(H_\ell) \phi_\ell(H_\ell - 1) + (k_\ell(H_\ell) + q_\ell(H_\ell) - p_\ell(H_\ell)) \phi_\ell(H_\ell) \\ - \lambda_\ell S_\ell(H_\ell)] = \Delta_{\ell+1} r \cdot \lambda_\ell [(q_{\ell+1}(0) - p_{\ell+1}(0) - k_{\ell+1}(0)) \phi_{\ell+1}(0) \\ + 2p_{\ell+1}(0) \phi_{\ell+1}(1) + \lambda_{\ell+1} S_{\ell+1}(0)]$$

$$(d_3) \phi_\ell(H_\ell) = \phi_{\ell+1}(0)$$

$$(d_4^*) (d + \Delta_L r) \phi_L(H_L) - d \phi_L(H_L - 1) = 0$$

$$(d_5) a_0 \phi_1(0) + a_1 \phi_1(1) = a_2$$

Omission of the boundary condition (d₅) gives a system which has a unique solution for each assigned value of $\phi_L(H_L)$. The difference X of any two such solutions is a solution of the following system:

$$(e_1) \quad p_\ell(h_\ell)X_\ell(h_\ell + 1) - k_\ell(h_\ell)X_\ell(h_\ell) + q_\ell(h_\ell)X_\ell(h_\ell - 1) = 0$$

$$0 < h_\ell < H_\ell, \quad 1 \leq \ell \leq L$$

$$(e_2) \quad \Delta_\ell r \cdot \lambda_{\ell+1} \left[-2q_\ell(H_\ell)X_\ell(H_\ell - 1) + (k_\ell(H_\ell) + q_\ell(H_\ell) - p_\ell(H_\ell))X_\ell(H_\ell) \right] = \\ \Delta_{\ell+1} r \cdot \lambda_\ell \left[(q_{\ell+1}(0) - p_{\ell+1}(0) - k_{\ell+1}(0))X_{\ell+1}(0) + 2p_{\ell+1}(0)X_{\ell+1}(1) \right]$$

$$1 \leq \ell < L$$

$$(e_3) \quad X_\ell(H_\ell) = X_{\ell+1}(0)$$

$$(e_4^*) \quad (d + \Delta_L r)X_L(H_L) - dX_L(H_L - 1) = 0$$

In order to keep the quantities of the problem in range, it is simpler to solve for certain auxiliary functions.

Set $u_\ell(h) = X_\ell(h+1)/X_\ell(h)$. Then from (e₁) we get

$$p_\ell(h_\ell) \frac{X_\ell(h_\ell + 1)}{X_\ell(h_\ell)} - k_\ell(h_\ell) + q_\ell(h_\ell) \frac{X_\ell(h_\ell - 1)}{X_\ell(h_\ell)} = 0$$

or

$$u_\ell(h_\ell - 1) = q_\ell(h_\ell) / (k_\ell(h_\ell) - p_\ell(h_\ell)u_\ell(h_\ell))$$

From (e₂) we get

$$\Delta_\ell r \cdot \lambda_{\ell+1} \left[-2q_\ell(H_\ell)/u_\ell(H_\ell - 1) + k_\ell(H_\ell) + q_\ell(H_\ell) - p_\ell(H_\ell) \right] = \\ \Delta_{\ell+1} r \cdot \lambda_\ell \left[q_{\ell+1}(0) - p_{\ell+1}(0) - k_{\ell+1}(0) + 2p_{\ell+1}(0)u_{\ell+1}(0) \right];$$

and from (e₄), $u_L(H_L - 1) = d/(d + \Delta_L r)$. So u is determined by the system

$$(f_1) \quad u_\ell(h_\ell - 1) = q_\ell(h_\ell) / (k_\ell(h_\ell) - p_\ell(h_\ell)u_\ell(h_\ell)) \quad \begin{matrix} 0 < h_\ell < H_\ell \\ 1 \leq \ell \leq L \end{matrix}$$

$$(f_2) \quad u_\ell(H_\ell - 1) = 2q_\ell(H_\ell) / \left[k_\ell(H_\ell) + q_\ell(H_\ell) - p_\ell(H_\ell) \right. \\ \left. + \frac{\Delta_{\ell+1} r \cdot \lambda_\ell}{\Delta_\ell r \cdot \lambda_{\ell+1}} (k_{\ell+1}(0) + p_{\ell+1}(0) - q_{\ell+1}(0) - 2p_{\ell+1}(0)u_{\ell+1}(0)) \right] \quad 1 \leq \ell < L$$

$$(f_3^*) \quad u_L(H_L - 1) = d/(d + \Delta_L r).$$

$$\text{Now set } v_\ell(h_\ell - 1) = \phi_\ell(h_\ell) - u_\ell(h_\ell - 1)\phi_\ell(h_\ell - 1).$$

To express it in terms of $u_\ell(h_\ell - 1)$, $v_\ell(h_\ell)$, and $S_\ell(h_\ell)$ we proceed as follows:

$$\begin{aligned}
v_\ell(h_\ell - 1) &= \frac{1}{X_\ell(h_\ell - 1)} (X_\ell(h_\ell - 1) \phi_\ell(h_\ell) - X_\ell(h_\ell) \phi_\ell(h_\ell - 1)) \\
&= \frac{1}{X_\ell(h_\ell - 1)} \left((k_\ell(h_\ell) X_\ell(h_\ell) - p_\ell(h_\ell) X_\ell(h_\ell + 1)) \phi_\ell(h_\ell) \right. \\
&\quad \left. - X_\ell(h_\ell) (k_\ell(h_\ell) \phi_\ell(h_\ell) - p_\ell(h_\ell) \phi_\ell(h_\ell + 1) - \lambda_\ell S_\ell(h_\ell)) \right) / q_\ell(h_\ell)
\end{aligned}$$

(where we have solved (e_1) and (d_1) for $X_\ell(h_\ell - 1)$ and $\phi_\ell(h_\ell - 1)$ to insert in the first equality)

$$\begin{aligned}
v_\ell(h_\ell - 1) &= \frac{1}{X_\ell(h_\ell - 1)} \left(p_\ell(h_\ell) (X_\ell(h_\ell) \phi_\ell(h_\ell + 1) - X_\ell(h_\ell + 1) \phi_\ell(h_\ell)) \right. \\
&\quad \left. + \lambda_\ell X_\ell(h_\ell) S_\ell(h_\ell) \right) / q_\ell(h_\ell) \\
&= u_\ell(h_\ell - 1) (p_\ell(h_\ell) v_\ell(h_\ell) + \lambda_\ell S_\ell(h_\ell)) / q_\ell(h_\ell).
\end{aligned}$$

To carry v inwards across an interface, we follow the same procedure, using (e_2) and (d_2) instead of (e_1) and (d_1) :

$$\begin{aligned}
v_\ell(H_\ell - 1) &= \frac{1}{X_\ell(H_\ell - 1)} (X_\ell(H_\ell - 1) \phi_\ell(H_\ell) - X_\ell(H_\ell) \phi_\ell(H_\ell - 1)) \\
&= \frac{1}{X_\ell(H_\ell - 1)} \left(\left[k_\ell(H_\ell) + q_\ell(H_\ell) - p_\ell(H_\ell) + \frac{\Delta_{\ell+1} r \cdot \lambda_\ell}{\Delta_\ell r \cdot \lambda_{\ell+1}} (p_{\ell+1}(0) \right. \right. \\
&\quad \left. \left. + k_{\ell+1}(0) - q_{\ell+1}(0)) \right] X_{\ell+1}(0) \phi_\ell(H_\ell) - X_\ell(H_\ell) \left[k_\ell(H_\ell) + q_\ell(H_\ell) \right. \right. \\
&\quad \left. \left. - p_\ell(H_\ell) + \frac{\Delta_{\ell+1} r \cdot \lambda_\ell}{\Delta_\ell r \cdot \lambda_{\ell+1}} (p_{\ell+1}(0) + k_{\ell+1}(0) - q_{\ell+1}(0)) \right] \phi_{\ell+1}(0) \right. \\
&\quad \left. - \frac{\Delta_{\ell+1} r \cdot \lambda_\ell}{\Delta_\ell r \cdot \lambda_{\ell+1}} 2 p_{\ell+1}(0) X_{\ell+1}(1) \phi_\ell(H_\ell) - X_\ell(H_\ell) \left[-\lambda_\ell S_\ell(H_\ell) \right. \right. \\
&\quad \left. \left. - \frac{\Delta_{\ell+1} r \cdot \lambda_\ell}{\Delta_\ell r \cdot \lambda_{\ell+1}} (-2 p_{\ell+1}(0) \phi_{\ell+1}(1) - \lambda_{\ell+1} S_{\ell+1}(0)) \right] \right) / 2 q_\ell(H_\ell) \\
&= \frac{1}{X_\ell(H_\ell - 1)} \left(p_{\ell+1}(0) \frac{\Delta_{\ell+1} r \cdot \lambda_\ell}{\Delta_\ell r \cdot \lambda_{\ell+1}} \left[X_{\ell+1}(0) \phi_{\ell+1}(1) - X_{\ell+1}(1) \phi_{\ell+1}(0) \right] \right. \\
&\quad \left. + X_{\ell+1}(0) \left[\frac{\lambda_\ell}{2} S_\ell(H_\ell) + \frac{\Delta_{\ell+1} r \cdot \lambda_\ell}{\Delta_\ell r \cdot \lambda_{\ell+1}} \frac{\lambda_{\ell+1}}{2} S_{\ell+1}(0) \right] \right) / q_\ell(H_\ell) \\
&= \frac{u_\ell(H_\ell - 1)}{q_\ell(H_\ell)} \left(p_{\ell+1}(0) \frac{\Delta_{\ell+1} r \cdot \lambda_\ell}{\Delta_\ell r \cdot \lambda_{\ell+1}} v_{\ell+1}(0) + \frac{\lambda_\ell}{2} S_\ell(H_\ell) + \right. \\
&\quad \left. \frac{\Delta_{\ell+1} r \cdot \lambda_\ell}{2 \Delta_\ell r} S_{\ell+1}(0) \right) \quad \text{for } 1 \leq \ell < L
\end{aligned}$$

(where we have used (d_3) and (e_3)).

At the extrapolated end-point $v_L(H_L-1) =$

$$\frac{1}{X_L(H_L-1)} (X_L(H_L-1)\phi_L(H_L) - X_L(H_L)\phi_L(H_L-1)) = 0 \text{ because both}$$

X and ϕ obey the same homogeneous linear condition on their values at H_L-1 and H_L .

So v is determined by the system:

$$(g_1) v_\ell(h_\ell-1) = u_\ell(h_\ell-1) (p_\ell(h_\ell)v_\ell(h_\ell) + \lambda_\ell S_\ell(h_\ell)) / q_\ell(h_\ell)$$

$$0 < h_\ell < H_\ell, \quad 1 \leq \ell \leq L$$

$$(g_2) v_\ell(H_\ell-1) = \frac{u_\ell(H_\ell-1)\lambda_\ell}{2q_\ell(H_\ell)} \left(p_{\ell+1}(0) \frac{2\Delta_{\ell+1}^r}{\Delta_\ell^r \cdot \lambda_{\ell+1}} v_{\ell+1}(0) + S_\ell(H_\ell) \right. \\ \left. + \frac{\Delta_{\ell+1}^r}{\Delta_\ell^r} S_{\ell+1}(0) \right) \quad 1 \leq \ell \leq L$$

$$(g_3^*) v_L(H_L-1) = 0$$

After u and v have been found from the systems (f) and (g), then ϕ is found by means of the following system:

$$(h_1) \phi_\ell(h_\ell+1) = v_\ell(h_\ell) + u_\ell(h_\ell) \phi_\ell(h_\ell), \quad 0 \leq h_\ell < H_\ell, \quad 1 \leq \ell \leq L$$

$$(h_2) \phi_1(0) = (a_2 - a_1 v_1(0)) / (a_1 u_1(0) + a_0),$$

where (h_1) is obtained by solving for $\phi_\ell(h_\ell+1)$ in the definition of v , and (h_2) by solving for $\phi_1(0)$ in (h_1) (evaluated at $h_1=0$) and (c_5) , considered as a set of simultaneous linear equations in $\phi_1(0)$ and $\phi_1(1)$.

Instead of approximating the derivative $\phi'(b_L)$ by the two-point formula $(\phi_L(H_L) - \phi_L(H_L-1)) / \Delta_L^r$ for the extrapolated end-point condition (c_4^*) , it would be more consistent with the rest of the calculation to use the three-point formula

$$\left[\frac{d\phi}{dr} \right]_{b_L} = \frac{1}{2\Delta_L^r} (p_L(H_L)\phi_L(H_L+1) + (q_L(H_L) - p_L(H_L))\phi_L(H_L) - q_L(H_L)\phi_L(H_L-1)).$$

If (d_1) , evaluated at $\ell=L$ and $h_\ell = H_L$, is used to eliminate the fictitious flux $\phi_L(H_L+1)$, we get

$$\left[\frac{d\phi}{dr} \right]_{b_L} = \frac{1}{2\Delta_L^r} ((k_L(H_L) + q_L(H_L) - p_L(H_L))\phi_L(H_L) - 2q_L(H_L)\phi_L(H_L-1) - \lambda_L S_L(H_L)).$$

The corresponding expression for X is

$$\left[\frac{dX}{dr} \right]_{b_L} = \frac{1}{2\Delta_L r} \left((k_L(H_L) + q_L(H_L) - p_L(H_L)) X_L(H_L) - 2q_L(H_L) X_L(H_L - 1) \right).$$

Now the general boundary condition

$$(b_4) B_0 \phi(b_L) + B_1 \phi'(b_L) = 0$$

is expressed in difference form as

$$(c_4) \left(2\Delta_L r B_0 + B_1 (k_L(H_L) + q_L(H_L) - p_L(H_L)) \right) \phi_L(H_L) - 2B_1 q_L(H_L) \phi_L(H_L - 1) = \lambda_L B_1 S_L(H_L).$$

For X it is

$$(e_4) \left(2\Delta_L r B_0 + B_1 (k_L(H_L) + q_L(H_L) - p_L(H_L)) \right) X_L(H_L) - 2B_1 q_L(H_L) X_L(H_L - 1) = 0.$$

Then the initial value for u is given by

$$(f_3) u_L(H_L - 1) = 2B_1 q_L(H_L) / \left(2\Delta_L r B_0 + (k_L(H_L) + q_L(H_L) - p_L(H_L)) B_1 \right),$$

and that for v by

$$(g_3) v_L(H_L - 1) = \lambda_L B_1 S_L(H_L) / \left(2\Delta_L r B_0 + (k_L(H_L) + q_L(H_L) - p_L(H_L)) B_1 \right).$$

To check the computations we integrate the diffusion equation over each region R_ℓ .

$$\int_{R_\ell} (D_\ell \nabla \phi - \Sigma_\ell \phi + S) \frac{N\pi^{\frac{N}{2}}}{\Gamma\left(\frac{N}{2} + 1\right)} r^{N-1} dr = 0$$

i.e.

$$0 = \left[\frac{N\pi^{\frac{N}{2}} D_\ell}{\Gamma\left(\frac{N}{2} + 1\right)} r^{N-1} \frac{d}{dr} \phi \right]_{b_{\ell-1}}^{b_\ell} - \Sigma_\ell \frac{N\pi^{\frac{N}{2}}}{\Gamma\left(\frac{N}{2} + 1\right)} \int_{b_{\ell-1}}^{b_\ell} \phi \cdot r^{N-1} dr + \frac{N\pi^{\frac{N}{2}}}{\Gamma\left(\frac{N}{2} + 1\right)} \int_{b_{\ell-1}}^{b_\ell} S \cdot r^{N-1} dr$$

or

$$(i_1) E_\ell - E'_\ell - \Sigma_\ell \frac{N\pi^{\frac{N}{2}}}{\Gamma\left(\frac{N}{2} + 1\right)} \int_{b_{\ell-1}}^{b_\ell} \phi \cdot r dr + \frac{N\pi^{\frac{N}{2}}}{\Gamma\left(\frac{N}{2} + 1\right)} \int_{b_{\ell-1}}^{b_\ell} S \cdot r^{N-1} dr = 0$$

where E_ℓ and E'_ℓ are the leakages radially outward thru the inner and outer interfaces (respectively) of R_ℓ . All integrals are computed trapezoidally, and the E 's are given a difference approximation which makes (i₁) an algebraic identity as follows:

$$\int_{b_{\ell-1}}^{b_\ell} \nabla^2 \phi \cdot r^{N-1} dr = \frac{\Delta_\ell r}{2} (r^{N-1} \nabla^2 \phi)_{n_\ell(0)} + (r^{N-1} \nabla^2 \phi)_{n_\ell(1)} \Delta_\ell r + \dots$$

$$\dots + \Delta_\ell r (r^{N-1} \nabla^2 \phi)_{n_\ell(H_\ell-1)} + \frac{\Delta_\ell r}{2} (r^{N-1} \nabla^2 \phi)_{n_\ell(H_\ell)}.$$

But $(r^{N-1} \nabla^2 \phi)_{n_\ell(h)} = (n_\ell(h) \Delta_\ell r)^{N-1} \frac{1}{(\Delta_\ell r)^2} \left[p_\ell(h) \phi_\ell(h+1) - (p_\ell(h) + q_\ell(h)) \phi_\ell(h) \right.$

$$\left. + q_\ell(h) \phi_\ell(h-1) \right]$$

$$= (\Delta_\ell r)^{N-3} \left[\left(n_\ell(h) + \frac{1}{2} \right)^{N-1} \left(\phi_\ell(h+1) - \phi_\ell(h) \right) \right.$$

$$\left. - \left(n_\ell(h) - \frac{1}{2} \right)^{N-1} \left(\phi_\ell(h) - \phi_\ell(h-1) \right) \right]$$

$$= (\Delta_\ell r)^{N-3} \left[\left(n_\ell(h) + \frac{1}{2} \right)^{N-1} \left(\phi_\ell(h+1) - \phi_\ell(h) \right) \right]_{h-1}^h$$

Therefore

$$\sum_{h=1}^{H_\ell-1} (r^{N-1} \nabla^2 \phi)_{n_\ell(h)} \Delta_\ell r = - (\Delta_\ell r)^{N-2} \left(n_\ell(0) + \frac{1}{2} \right)^{N-1} (\phi_\ell(1) - \phi_\ell(0))$$

$$+ (\Delta_\ell r)^{N-2} \left(n_\ell(H_\ell) - \frac{1}{2} \right)^{N-1} (\phi_\ell(H_\ell) - \phi_\ell(H_\ell-1)),$$

and

$$\int_{b_{\ell-1}}^{b_\ell} \nabla^2 \phi r^{N-1} dr = \left[\frac{\Delta_\ell r}{2} (r^{N-1} \nabla^2 \phi)_{n_\ell(0)} - (\Delta_\ell r)^{N-2} \left(n_\ell(0) + \frac{1}{2} \right)^{N-1} (\phi_\ell(1) - \phi_\ell(0)) \right]$$

$$+ \left[\frac{1}{2} (\Delta_\ell r)^{N-2} \left(n_\ell(H_\ell) - \frac{1}{2} \right)^{N-1} (\phi_\ell(H_\ell) - \phi_\ell(H_\ell-1)) \right.$$

$$\left. + \frac{1}{2} (\Delta_\ell r)^{N-2} \left(n_\ell(H_\ell) + \frac{1}{2} \right)^{N-1} (\phi_\ell(H_\ell+1) - \phi_\ell(H_\ell)) \right].$$

$$\begin{aligned}
\text{So } E'_\ell &= -D_\ell \frac{N\pi^{\frac{N}{2}}}{\Gamma(\frac{N}{2}+1)} \frac{1}{2\Delta_\ell r} \left[(\Delta_\ell r)^{N-1} \left(n_\ell(H_\ell) - \frac{1}{2} \right)^{N-1} \left(\phi_\ell(H_\ell) - \phi_\ell(H_\ell - 1) \right) \right. \\
&\quad \left. + (\Delta_\ell r)^{N-1} \left(n_\ell(H_\ell) + \frac{1}{2} \right)^{N-1} \left(\phi_\ell(H_\ell + 1) - \phi_\ell(H_\ell) \right) \right] \\
&= -D_\ell \frac{N\pi^{\frac{N}{2}}}{\Gamma(\frac{N}{2}+1)} r_\ell(H_\ell)^{N-1} \left[q_\ell(H_\ell) \left(\phi_\ell(H_\ell) - \phi_\ell(H_\ell - 1) \right) + p_\ell(H_\ell) \left(\phi_\ell(H_\ell + 1) - \phi_\ell(H_\ell) \right) \right] \frac{1}{2\Delta_\ell r} \\
&= -D_\ell \frac{N\pi^{\frac{N}{2}}}{\Gamma(\frac{N}{2}+1)} r_\ell(H_\ell)^{N-1} \left[\left(k_\ell(H_\ell) + q_\ell(H_\ell) - p_\ell(H_\ell) \right) \phi_\ell(H_\ell) - 2q_\ell(H_\ell) \phi_\ell(H_\ell - 1) - \lambda_\ell S_\ell(H_\ell) \right] \frac{1}{2\Delta_\ell r} \quad (\text{by } (d_1)) .
\end{aligned}$$

Similarly, if $b_0 > 0$, then

$$\begin{aligned}
E_\ell &= -D_\ell \frac{N\pi^{\frac{N}{2}}}{\Gamma(\frac{N}{2}+1)} r_\ell(0)^{N-1} \left[\left(q_\ell(0) - p_\ell(0) - k_\ell(0) \right) \phi_\ell(0) + 2p_\ell(0) \phi_\ell(1) \right. \\
&\quad \left. + \lambda_\ell S_\ell(0) \right] \frac{1}{2\Delta_\ell r}
\end{aligned}$$

On the other hand, if $b_0 = 0$, then we must use the formula

$$\begin{aligned}
\left[\nabla^2 \phi \right]_0 &= \frac{N}{(\Delta_1 r)^2} \left[\phi_1(-1) - 2\phi_1(0) + \phi_1(1) \right] \\
&= \frac{2N}{(\Delta_1 r)^2} \left[\phi_1(1) - \phi_1(0) \right] \quad \left(\text{since } \phi_1(-1) = \phi_1(+1) \right) .
\end{aligned}$$

Therefore

$$\begin{aligned}
E_1 &= D_1 \frac{N\pi^{\frac{N}{2}}}{\Gamma(\frac{N}{2}+1)} \left[\frac{\Delta_1 r}{2} (r^{N-1} \nabla^2 \phi)_{r=0} - \frac{(\Delta_1 r)^{N-2}}{2^{N-1}} (\phi_1(1) - \phi_1(0)) \right] \\
&= D_1 \frac{N\pi^{\frac{N}{2}}}{\Gamma(\frac{N}{2}+1)} \left[0 + \frac{(\Delta_1 r)^{N-2}}{2^{N-1}} (\phi_1(0) - \phi_1(1)) \right] \\
&= D_1 \frac{N\pi^{\frac{N}{2}}}{\Gamma(\frac{N}{2}+1)} \frac{(\Delta_1 r)^{N-2}}{2^{N-1}} (\phi_1(0) - \phi_1(1)) .
\end{aligned}$$

III. PREPARATION OF INPUT DATA

This program has been designed to accept the problem input from the standard SHARE symbolic coding form, (IBM Form 12-6809-1), and will be described in that format here. The input sheet for a sample problem has been included in Appendix A. SHARE subroutine NY INP1 is used.

In the listing that follows the quantities are listed either with or without a decimal point. If a decimal point is included it indicates the quantity specified must either contain its decimal point or be written in the standard floating point notation as a fraction and E followed by the base 10 exponent. For example, π may be written 3.14159 or .314159E1 or 31.4159E-1. In addition, when quantities are listed successively on a card, (or line), a comma must be used to separate items. The last item on the card, (or line), must not be followed by a comma.

<u>LOCATION</u>	<u>OPERATION</u>	<u>ADDRESS, TAG, DECREMENT</u>
1000	DEC	XX.YYYYY, J, L, N, R., P Here, XX.YYYYY is the problem number, XX = the problem originator's code number and YYYYY = the chronological problem identification. J = the number of energy groups included in the problem. L = the number of regions into which the problem is divided. N = the geometry of the problem, N=1 for a slab, N=2 for a cylinder, and N=3 for a sphere. R is the outer edge, (cm.), of the problem. P is the total number of intervals.

$$P = \sum_{\ell=1}^L H_{\ell}$$

DEC $\Delta_L, \Delta_{L-1}, \Delta_{L-2}, \dots, \Delta_1.$

The Δ_{ℓ} value is the size of the interval spacing, (cm.), in region ℓ .

These values are given from the innermost region, $\ell=L$, to the outermost, $\ell=1$.

<u>LOCATION</u>	<u>OPERATION</u>	<u>ADDRESS, TAG, DECREMENT</u>
1106	DEC	$H_L, H_{L-1}, H_{L-2}, \dots, H_1$
		The H_ℓ value is the number of intervals into which region ℓ is subdivided for the solution. These are given from the innermost region, ($\ell = L$), outward through region 1, the outermost region.
1206	DEC	$S_{L,H}, S_{L,H-1}, \dots, S_{L,1}, S_{L,0}, S_{L-1,H},$ $\dots, S_{\ell,h}, \dots, S_{2,0}, S_{1,H}, S_{1,H-1}, \dots, S_{1,0}$
		These are the lattice point source values to be used as the source value in the diffusion equation for the highest energy group, $j = 1$.
	TRA	3,4
		This card always follows the specified general problem parameters and point source values.

Next, in ascending energy group order, the group-region parameters must be listed for each region from innermost, $\ell = L$, to outermost, $\ell = 1$. These are, in the SHARE coding form format:

<u>LOCATION</u>	<u>OPERATION</u>	<u>ADDRESS, TAG, DECREMENT</u>
2999	DEC	$k., d_0(L), D(L), \sigma(L), s(L), d_I(L).$

These are the parameters for region L . k is the value to be used as the value of the flux at the inner edge of the region if the boundary condition, inner edge $\phi = k$, was chosen. Otherwise, it is irrelevant and may be given as zero. d_0 is the boundary condition at the outer edge of the region and here the choice of interface boundary conditions is indicated. $d_0 > 0$ indicates d_0 is the extrapolation distance, (cm.), to be used for the "black boundary" condition. $d_0 < 0$, usually given as -1, is used if the flux and current are to be continuous across the interface. D (cm.) is

<u>LOCATION</u>	<u>OPERATION</u>	<u>ADDRESS, TAG, DECREMENT</u>
		<p>the diffusion coefficient, σ (cm.⁻¹), the removal cross section, s, the transfer fraction, and d_I, the boundary condition at the inner boundary of the problem. If $d_I > 0$, then d_I represents the extrapolation distance of the "black boundary" condition and r at this boundary must be greater than zero. If $d_I=0$ the flux at this boundary is set equal to the value of k specified, or if $d_I < 0$, the derivative of the flux is set to zero.</p> <p>For regions $\ell=L-1, L-2, \dots, 2$ the group-region input can be described generally as:</p>
3ccc	DEC	$d_0(\ell), D(\ell), \sigma(\ell), s(\ell), d_I(\ell).$
ccc=000+5(L- ℓ)		<p>These parameters are as described for region L, except that since d_0 and d_I apply only to interior regions they can never equal zero and hence, no value of k is permitted. If d_0 or $d_I > 0$ their values are taken as the appropriate extrapolation distance value, d, (cm.), for the "black boundary" while if d_0 or $d_I < 0$, usually given as -1, the continuity of flux and current is preserved across the interface.</p> <p>For region $\ell = 1$ the only change comes in the specification of d_0 since this is the boundary condition indicator for the outer edge, $r=R$. Here, the value of $d_0 > 0$ corresponds to the "black boundary" extrapolation distance, d, (cm.), as before, $d_0=0$ indicates the flux is to go to zero at $r=R$, and $d_0 < 0$, usually given as -1, requires the cell condition, that is, the derivative of the flux equal zero at $r=R$. Obviously, in the case of a one region problem the description of the $\ell = L$ group-region parameters must be altered to permit d_0 to specify the $r=R$ boundary condition rather than the interface condition.</p>

<u>LOCATION</u>	<u>OPERATION</u>	<u>ADDRESS, TAG, DECREMENT</u>
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The group-region parameters for all regions
for energy group 1 are followed by

TRA	3,4
-----	-----

After this the group-region parameters for the next group are
enumerated in the same manner, until the group-region parameters have
been given for all J energy groups.

IV. OPERATING INSTRUCTIONS

This program requires an IBM 704 equipped with the 8K memory and input and output may be on or off-line determined by sense switch settings. No tapes are required although both an input and output tape may be used.

The standard 72-72 board is used in the card reader, the SHARE 2 board in the on-line printer. If tapes are available, tape 2 may be used as a BCD output unit, tape 3 for the BCD input unit. Sense switch 1 is down if card rather than tape input is to be used and sense switches 3 and 5 are down if on-line rather than tape output is desired.

A. Operating Procedure:

1. Mount tapes, if required, set tape selector switches and ready tape units.
2. Ready the printer.
3. Ready the binary program deck followed by problem input, if on cards, in card reader.
4. Clear and load cards.
5. STOP 6662₈. Problems are completed.

B. Program Stops (Octal):

- 4653 Illegal operation code specified on input data card.
- 5171 Out-of-range input data.
- 5452 Illegal punch in problem input card.
- 7766 "Black boundary" condition requested at inner edge and $r=0$.

C. Off-line Printing:

Tape 2, the output, should be printed on single space, off-line. An end of file follows each problem so that the paper may be restored, if desired.

V. OUTPUT INFORMATION

All of the input information is printed as well as the problem solution so that the problem originator will have a complete record of the problem for later reference and checking, if desired.

The problem solution provides a listing for each energy group, $j = 1, 2, \dots, J$, of the radius and flux value at each lattice point from $r = R - \Delta_L H_L - \Delta_{L-1} H_{L-1} - \dots - \Delta_1 H_1$, in steps of Δ_ℓ through each region to $r = R$.

The integral of the flux, the leakage, and the value of the neutron balance check equation for each region is given, as is the value of the current at the outer boundary, ($r = R$). In addition, if a "black boundary" condition was imposed at an interface the value of the current at this interface is computed and printed. If the current was not computed a zero is printed in that position.

An output listing for a sample problem is included as Appendix B. SHARE subroutine NY OUT1 is used.

APPENDIX A

Sample Problem Input

Share Symbolic Coding Form

Problem		RE 34		TEST		PROBLEM		Page		Of		
Coder		M. BUTLER				Date		2-12-58		1		
H	Location	6	7	8	Op	Address, Tag, Decrement	12	10	11	Comments	72	73
	1000				DEC	99, 91234, 3, 3, 2, 30, 30						RE34T000
					DEC	1, 1, 1						RE34T001
	1106				DEC	10, 5, 15						RE34T002
	1206				DEC	1, 95, 93, 90, 85, 83, 8, 79, 77, 75, 73						RE34T003
					DEC	7, 6, 5, 4, 3, 2, 15, 14, 13, 12, 11, 1						RE34T004
					DEC	08, 05, 03, 02, 01, 005, 001, 0005, 0003, 0002						RE34T005
					TRA	3, 4						RE34T006
	2999				DEC	0, -1, .06, .21, .2386952, -1.						RE34T007
	3005				DEC	-1, .025, .18, .3888889, -1.						RE34T008
	3010				DEC	0, 10, .24, .125, -1.						RE34T009
					TRA	3, 4						RE34T010
	2999				DEC	0, -1, .08, .19, .0263158, -1.						RE34T011
	3005				DEC	-1, .03, .16, .0625, -1.						RE34T012
	3010				DEC	0, .12, .22, .03636364, -1.						RE34T013
					TRA	3, 4						RE34T014
	2999				DEC	0, -1, .04, .33, 0, -1.						RE34T015
	3005				DEC	-1, .06, .30, 0, -1.						RE34T016
	3010				DEC	0, .08, .36, 0, -1.						RE34T017
					TRA	3, 4						RE34T018

APPENDIX B

Sample Problem Output

R.E. 34 PROBLEM 99.91234

J= 3 L= 3 N= 2 R= 30.000 P= 30

MESH SPACING
1.000000 1.000000 1.000000

POINTS PER REGION 5 15

POINT-WISE SOURCES

1.0000E-00	9.5000E-01	9.1000E-01	9.0000E-01	8.5000E-01	8.3000E-01	8.0000E-01	7.9000E-01	7.7000E-01	7.5000E-01
7.3000E-01	7.0000E-01	6.0000E-01	5.0000E-01	4.0000E-01	3.0000E-01	2.0000E-01	1.5000E-01	1.4000E-01	1.3000E-01
1.2000E-01	1.1000E-01	10.0000E-02	8.0000E-02	5.0000E-02	3.0000E-02	2.0000E-02	10.0000E-03	5.0000E-03	10.0000E-04
5.0000E-04	3.0000E-04	2.0000E-04							

GROUP-REGION PARAMETERS

K=	D OUT	DIFF. COEF.	SIGMA	TRANSFER	D IN
-1.0000E 00	6.0000E-02	2.1000E-01	2.3810E-01	-1.0000E 00	
-1.0000E 00	2.5000E-02	1.8000E-01	3.8889E-01	-1.0000E 00	
0.	10.0000E-02	2.4000E-01	1.2500E-01	-1.0000E 00	

RADIUS	FLUX	FLUX INTEGRAL	LEAKAGE	CURRENT	BAL	CK	J=
0.	4.6214E 00						1
1.000	4.4985E 00						
2.000	4.3986E 00						
3.000	4.2548E 00						

4.000	4.0593E 00				
5.000	3.9436E 00				
6.000	3.8208E 00				
7.000	3.7536E 00				
8.000	3.6680E 00				
9.000	3.5969E 00				
10.000	3.6176E 00	1.2002E 03	-1.0076E 00	0.	1.9073E-06
10.000	3.6176E 00				
11.000	3.2986E 00				
12.000	2.7680E 00				
13.000	2.2124E 00				
14.000	1.6294E 00				
15.000	8.2801E-01	9.1340E 02	4.2268E 00	0.	3.8147E-06
15.000	8.2801E-01				
16.000	6.2975E-01				
17.000	5.5155E-01				
18.000	5.0084E-01				
19.000	4.5483E-01				
20.000	4.0300E-01				
21.000	3.2168E-01				

22.000	2.1683E-01								
23.000	1.3657E-01								
24.000	8.6896E-02								
25.000	4.7627E-02								
26.000	2.3921E-02								
27.000	8.3812E-03								
28.000	3.3373E-03								
29.000	1.4272E-03								
30.000	0.	4.4174E 02	4.5304E-02	2.4034E-04	-0.				

GROUP-REGION PARAMETERS

K=	0.								
D OUT	DIFF. COEF.	SIGMA	TRANSFER	D IN					
-1.0000E 00	8.0000E-02	1.9000E-01	2.6316E-02	-1.0000E 00					
-1.0000E 00	3.0000E-02	1.6000E-01	6.2500E-02	-1.0000E 00					
0.	1.2000E-01	2.2000E-01	3.6364E-02	-1.0000E 00					

RADIUS	FLUX	FLUX INTEGRAL	LEAKAGE	CURRENT	BAL	CK
0.	1.1882E 00					
1.000	1.1716E 00					
2.000	1.1467E 00					
3.000	1.1112E 00					

4.000	1.0687E 00				
5.000	1.0368E 00				
6.000	1.0084E 00				
7.000	9.9090E-01				
8.000	9.8264E-01				
9.000	1.0142E 00				
10.000	1.1946E 00	3.2802E 02	-2.3093E 00	0.	.4.7684E-07
10.000	1.1946E 00				
11.000	1.3756E 00				
12.000	1.1964E 00				
13.000	9.5645E-01				
14.000	6.7546E-01				
15.000	2.2117E-01	3.7077E 02	2.3054E 00	0.	4.7684E-07
15.000	2.2117E-01				
16.000	1.1994E-01				
17.000	8.5389E-02				
18.000	7.0943E-02				
19.000	6.1999E-02				
20.000	5.3472E-02				
21.000	4.2711E-02				

5.000	1.5706E-02			
6.000	1.5293E-02			
7.000	1.5048E-02			
8.000	1.5101E-02			
9.000	1.6800E-02			
10.000	2.9523E-02	5.4210E 00	-1.4880E-01	0. 2.9802E-08
10.000	2.9523E-02			
11.000	4.2599E-02			
12.000	3.8977E-02			
13.000	3.1316E-02			
14.000	2.1499E-02			
15.000	7.4552E-03	1.1611E 01	7.5600E-02	0. 1.4901E-07
15.000	7.4552E-03			
16.000	3.2831E-03			
17.000	2.0602E-03			
18.000	1.6181E-03			
19.000	1.3823E-03			
20.000	1.1784E-03			
21.000	9.4131E-04			
22.000	6.8087E-04			

23.000	4.5709E-04			
24.000	2.9239E-04			
25.000	1.7277E-04			
26.000	9.3293E-05			
27.000	4.3974E-05			
28.000	1.9172E-05			
29.000	7.2512E-06			
30.000	0.	1.7805E 00	1.0752E-04	5.7043E-07 2.2352E-08

APPENDIX C

SHARE Assembly Program Listing

				R. E. 34 REACTOR SHIELDING PROGRAM M. BUTLER + J. HEESTAND	2289
		04573	ORG 2427		RE34SR00
		04573	INP1 LIB		RE34LIB3
		00613	ORG 395		RE34SR02
		00613	OUT1 LIB		RE34LIB4
		06654	ORG 3500		RE340000
		06654	P HED		RE340001
		04573	INP1 SYN I\$INP1		RE340002
		00613	OUT1 SYN O\$OUT1		RE340003
06654	0	76600	0 00361	WPR	RE340004
06655	0	76000	0 00165	SWT 5	RE340005
06656	0	02000	0 10153	TRA TAPE	RE340006
06657	0	76000	0 00361	SPR 1	RE340007
06660	0	07400	4 04573	IO TSX INP1,4	RE340008
06661	0	00000	0 01750	1000,0,0	RE340009
06662	0	42000	0 04622	HPR INP1+23	RE340010
06663	0	50000	0 04402	CLA 2306 1 GOES TO J	RE340011
06664	0	60100	0 17527	STO 8023	RE340012
06665	0	50000	0 01752	CLA 1002 SET UP PRINT ORDER FOR PROBLEM PARAMETERS,MESH SPACINGS	RE340013
06666	0	76700	0 00022	ALS 18	RE340014
06667	0	40000	0 10147	ADD PD1	RE340015
06670	0	60100	0 06711	STO I0+25	RE340016
06671	0	50000	0 01752	CLA 1002 SET UP PRINT ORDER FOR POINTS PER REGION	RE340017
06672	0	76700	0 00022	ALS 18	RE340018
06673	0	40000	0 10150	ADD PD2	RE340019
06674	0	60100	0 06713	STO I0+27	RE340020
06675	0	50000	0 01752	CLA 1002 SET UP PRINT ORDER FOR GROUP 1 SOURCES	RE340021
06676	0	40000	0 01755	ADD 1005	RE340022
06677	0	76700	0 00022	ALS 18	RE340023
06700	0	40000	0 10151	ADD PD3	RE340024
06701	0	60100	0 06715	STO I0+29	RE340025
06702	0	50000	0 01752	CLA 1002 SET UP PRINT ORDER FOR GROUP-REGION PARAMETERS	RE340026
06703	0	76700	0 00002	ALS 2	RE340027
06704	0	40000	0 01752	ADD 1002	RE340028
06705	0	76700	0 00022	ALS 18	RE340029
06706	0	40000	0 10152	ADD PD4	RE340030
06707	0	60100	0 06755	STO I1+20	RE340031
06710	0	07400	4 10022	TSX P1,4 PRINT PROBLEM PARAMETERS, MESH SPACINGS	RE340032
06711	0	01755	0 01750	1000,0,1005	RE340033
06712	0	07400	4 10046	TSX P2,4 PRINT POINTS PER REGION	RE340034

06713	0	02121	0	02122		1106,0,1105	RE340035
06714	0	07400	4	10055		TSX P3,4 PRINT GROUP ONE SOURCES	RE340036
06715	0	02265	0	02266		1206,0,1205	RE340037
06716	0	50000	0	04407		CLA 2311 2 GOES TO ALPHA N	RE340038
06717	0	60100	0	17500		STO 8000	RE340039
06720	0	50000	0	04403		CLA 2307	RE340040
06721	0	34000	0	01753		CAS 1003	RE340041
06722	0	02000	0	06731		TRA I1 SLAB	RE340042
06723	0	02000	0	07177		TRA CYL CYLINDER	RE340043
06724	0	40200	0	01753		SUB 1003	RE340044
06725	0	40000	0	04402		ADD 2306	RE340045
06726	-0	10000	0	07233		TNZ I10 N GREATER THAN 3	RE340046
06727	0	50000	0	04567		CLA 2423 SPHFRE	RE340047
06730	0	60100	0	17500		STO 8000	RE340048
06731	0	50000	0	01752	I1	CLA 1002	RE340049
06732	0	76000	0	00006		COM	RE340050
06733	0	40000	0	04402		ADD 2306	RE340051
06734	0	73400	1	00000		PAX 0,1 BAR L GOES TO A REGISTER	RE340052
06735	0	50000	0	01755		CLA 1005	RE340053
06736	0	40000	0	01752		ADD 1002	RE340054
06737	0	76000	0	00006		COM	RE340055
06740	0	40000	0	04402		ADD 2306	RE340056
06741	0	73400	2	00000		PAX 0,2 BAR P+L GOES TO B REGISTER	RE340057
06742	0	50000	0	01752		CLA 1002	RE340058
06743	0	76700	0	00002		ALS 2	RE340059
06744	0	40000	0	01752		ADD 1002	RE340060
06745	0	76000	0	00006		COM	RE340061
06746	0	40000	0	04402		ADD 2306	RE340062
06747	0	73400	4	00000		PAX 0,4 BAR 5L GOES TO C REGISTER	RE340063
06750	-0	63400	4	17520		SXD 8016,4 SAVE C REGISTER	RE340064
06751	0	07400	4	04573		TSX INP1,4 READ IN GROUP-REGION PARAMETERS	RE340065
06752	0	00000	0	05667		2999,0,0	RE340066
06753	0	42000	0	04622		HPR INP1+23	RE340067
06754	0	07400	4	10065		TSX P4,4 PRINT GROUP-REGION PARAMETERS	RE340068
06755	0	05667	0	05667		2999,0,2999	RE340069
06756	0	07400	4	10112		TSX P5,4 PRINT J AND FORMAT	RE340070
06757	0	17527	0	17527		8023,0,8023	RE340071
06760	-0	53400	4	17520		LXD 8016,4 REPLACE C REGISTER	RE340072
06761	0	50000	0	17501	I2	CLA 8001	RE340073
06762	0	60100	0	17520		STO 8016 G1 OF L-1 GOES TO TEMP 1	RE340074

06763 0 50000 1 02121
 06764 0 60100 0 17505
 06765 0 56000 1 01755
 06766 0 26000 1 01755
 06767 0 24000 4 05664
 06770 -0 60000 0 17501
 06771 0 26000 0 04405
 06772 0 60100 0 17502
 06773 0 56000 0 17501
 06774 0 26000 4 05665
 06775 0 60100 0 17501
 06776 0 50000 4 05663
 06777 0 24000 1 01755
 07000 -0 60000 0 17504
 07001 0 50000 0 04406
 07002 0 60100 0 17511
 07003 -0 63400 4 17521
 07004 0 50000 0 01753
 07005 0 40200 0 04402
 07006 0 73400 4 00000
 07007 0 10000 0 07023
 07010 0 50200 1 01755
 07011 0 24000 0 01754
 07012 0 26000 0 04405
 07013 0 30000 0 04406
 07014 0 60100 0 17511
 07015 0 60100 0 17522
 07016 -2 00001 4 07023
 07017 0 56000 0 17511
 07020 0 26000 0 17522
 07021 0 60100 0 17511
 07022 0 02000 0 07016
 07023 0 56000 0 17501
 07024 0 26000 0 04405
 07025 0 30000 0 17511
 07026 0 60100 0 17513
 07027 -0 53400 4 17521
 07030 -0 75400 1 00000
 07031 0 77100 0 00022
 07032 0 40000 0 01752

I3

CLA 1105,1
 STO 8005 H SUB L GOES TO H
 LDQ 1005,1 COMPUTE G2
 FMP 1005,1 DELTA SQUARED
 FDH 2996,4 DIVIDED BY D
 STQ 8001
 FMP 2309 TIMES 1/2
 STO 8002
 LDQ 8001 COMPUTE G1
 FMP 2997,4
 STO 8001
 CLA 2995,4 COMPUTE G4
 FDH 1005,1
 STQ 8004
 CLA 2310 1 GOFS TO QL,0
 STO 8009
 SXD 8017,4
 CLA 1003 CALCULATION OF QL,0
 SUB 2306
 PAX 0,4 N-1 GOES TO C REG
 TZE 13
 CLS 1005,1 -DELTA
 FDH 1004 DIVIDED BY R
 FMP 2309 TIMES 1/2
 FAD 2310 PLUS 1
 STO 8009
 STO 8018
 TNX 13,4,1
 LDQ 8009
 FMP 8018
 STO 8009
 TRA 12+29
 LDQ 8001 CALCULATION OF F1
 FMP 2309
 FAD 8009
 STO 8011
 LXD 8017,4
 PXD 0,1
 ARS 18
 ADD 1002

RE340075
 RE340076
 RE340077
 RE340078
 RE340079
 RE340080
 RE340081
 RE340082
 RE340083
 RE340084
 RE340085
 RE340086
 RE340087
 RE340088
 RE340089
 RE340090
 RE340091
 RE340092
 RE340093
 RE340094
 RE340095
 RE340096
 RE340097
 RE340098
 RE340099
 RE340100
 RE340101
 RE340102
 RE340103
 RE340104
 RE340105
 RE340106
 RE340107
 RE340108
 RE340109
 RE340110
 RE340111
 RE340112
 RE340113
 RE340114

07033	0	76700	0	00030	ALS 24		RE340115
07034	0	10000	0	07211	TZE I4 GO TO I4 IF REGION 1		RE340116
07035	0	50000	1	01755	CLA 1005,1 COMPUTE G3		RE340117
07036	0	24000	1	01756	FDH 1006,1		RE340118
07037	0	26000	4	05671	FMP 3001,4		RE340119
07040	0	24000	4	05664	FDH 2996,4		RE340120
07041	-0	60000	0	17503	STQ 8003		RE340121
07042	0	50000	4	05674	CLA 3004,4		RE340122
07043	0	12000	0	07216	TPL I6 GO TO I6 IF DI, L-1 ZERO OR POSITIVE		RE340123
07044	0	56000	0	17520	I5 LDQ 8016 COMPUTE U L,1		RE340124
07045	0	26000	0	04405	FMP 2309		RE340125
07046	0	30000	0	17514	FAD 8012	PLUS F2	RE340126
07047	0	76500	0	00043	LRS 35		RE340127
07050	0	26000	0	17503	FMP 8003		RE340128
07051	0	30000	0	17513	FAD 8011		RE340129
07052	0	60100	0	17521	STO 8017		RE340130
07053	0	50000	0	17511	CLA 8009		RE340131
07054	0	24000	0	17521	FDH 8017		RE340132
07055	-0	60000	2	13556	STQ 5998,2		RE340133
07056	0	50000	1	01756	CLA 1006,1 COMPUTE V L,1		RE340134
07057	0	24000	1	01755	FDH 1005,1		RE340135
07060	0	26000	2	02266	FMP 1206,2		RE340136
07061	0	30000	2	02265	FAD 1205,2		RE340137
07062	0	76500	0	00043	LRS 35		RE340138
07063	0	26000	0	17502	FMP 8002		RE340139
07064	0	60100	0	17521	STO 8017		RE340140
07065	0	56000	0	17515	LDQ 8013		RE340141
07066	0	26000	0	17503	FMP 8003		RE340142
07067	0	30000	0	17521	FAD 8017		RE340143
07070	0	76500	0	00043	LRS 35		RE340144
07071	0	26000	2	13556	FMP 5998,2		RE340145
07072	0	24000	0	17511	FDH 8009		RE340146
07073	-0	60000	2	15526	STQ 6998,2		RE340147
07074	1	00001	2	07075	I8 TXI I8+1,2,1 B REGISTER PLUS 1 GOES TO B REGISTER		RE340148
07075	0	50000	1	01755	CLA 1005,1		RE340149
07076	0	24000	0	04407	FDH 2311		RE340150
07077	0	50000	0	01754	CLA 1004 R-DELTA R GOES TO R		RE340151
07100	0	30700	1	01755	FSB 1005,1		RE340152
07101	0	60100	0	01754	STO 1004		RE340153
07102	0	04000	0	07104	TLQ I8+8		RE340154

07103 0 02000 0 07305
 07104 0 50000 0 04406
 07105 0 60100 0 17511
 07106 0 60100 0 17512
 07107 -0 63400 4 17521
 07110 0 50000 0 01753
 07111 0 40200 0 04402
 07112 0 73400 4 00000
 07113 0 10000 0 07137
 07114 0 50200 1 01755
 07115 0 24000 0 01754
 07116 0 26000 0 04405
 07117 0 60100 0 17520
 07120 0 30000 0 04406
 07121 0 60100 0 17511
 07122 0 60100 0 17522
 07123 0 50000 0 04406
 07124 0 30200 0 17520
 07125 0 60100 0 17512
 07126 0 60100 0 17520
 07127 -2 00001 4 07137
 07130 0 56000 0 17511
 07131 0 26000 0 17522
 07132 0 60100 0 17511
 07133 0 56000 0 17512
 07134 0 26000 0 17520
 07135 0 60100 0 17512
 07136 0 02000 0 07127
 07137 -0 53400 4 17521
 07140 0 50000 0 04406
 07141 0 30200 2 13557
 07142 0 76500 0 00043
 07143 0 26000 0 17512
 07144 0 60100 0 17514
 07145 0 56000 2 15527
 07146 0 26000 0 17512
 07147 0 60100 0 17515
 07150 0 50000 0 17505
 07151 0 40200 0 04402
 07152 0 60100 0 17505

TRA 016 R EQUAL ZERO
 CLA 2310 COMPUTE P L,H AND Q L,H
 STO 8009
 STO 8010
 SXD 8017,4
 CLA 1003
 SUB 2306
 PAX 0,4
 TZE 18+35
 CLS 1005,1
 FDH 1004
 FMP 2309
 STO 8016
 FAD 2310
 STO 8009
 STO 8018
 CLA 2310
 FSB 8016
 STO 8010
 STO 8016
 TNX 18+35,4,1
 LDQ 8009
 FMP 8018
 STO 8009
 LDQ 8010
 FMP 8016
 STO 8010
 TRA 18+27
 LXD 8017,4
 CLA 2310 COMPUTE F2
 FSB 5999,2
 LRS 35
 FMP 8010
 STO 8012
 LDQ 6999,2
 FMP 8010
 STO 8013
 CLA 8005 H-1 GOES TO H
 SUB 2306
 STO 8005

COMPUTE F3

RE340155
 RE340156
 RE340157
 RE340158
 RE340159
 RE340160
 RE340161
 RE340162
 RE340163
 RE340164
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 RE340192
 RE340193
 RE340194

07153	0	10000	0	07201	TZE 19		RE340195
07154	0	50000	0	17511	CLA 8009 COMPUTE U L, H+1		RE340196
07155	0	30000	0	17501	FAD 8001		RE340197
07156	0	30000	0	17514	FAD 8012		RE340198
07157	0	60100	0	17520	STO 8016		RE340199
07160	0	50000	0	17511	CLA 8009		RE340200
07161	0	24000	0	17520	FDH 8016		RE340201
07162	-0	60000	2	13556	STQ 5998,2		RE340202
07163	0	50000	2	13556	CLA 5998,2	COMPUTE V L,H+1	RE340203
07164	0	24000	0	17511	FDH 8009		RE340204
07165	-0	60000	0	17520	STQ 8016		RE340205
07166	0	50000	0	17502	CLA 8002		RE340206
07167	0	30000	0	17502	FAD 8002		RE340207
07170	0	76500	0	00043	LRS 35		RE340208
07171	0	26000	2	02265	FMP 1205,2		RE340209
07172	0	30000	0	17515	FAD 8013		RE340210
07173	0	76500	0	00043	LRS 35		RE340211
07174	0	26000	0	17520	FMP 8016		RE340212
07175	0	60100	2	15526	STO 6998,2		RE340213
07176	0	02000	0	07074	TRA 18		RE340214
07177	0	50000	0	04566	CLA 2422		RE340215
07200	0	02000	0	06730	TRA 11-1		RE340216
07201	-0	75400	1	00000	19 PXD 0,1 TEST FOR LAST REGION		RE340217
07202	0	77100	0	00022	ARS 18		RE340218
07203	0	40000	0	04402	ADD 2306		RE340219
07204	0	76700	0	00030	ALS 24		RE340220
07205	0	10000	0	07305	TZE 016		RE340221
07206	1	00005	4	07207	TXI 19+6,4,5 C REG PLUS 5 GOES TO C REG		RE340222
07207	1	00001	2	07210	TXI 19+7,2,1 B REG PLUS 1 GOES TO B REG		RE340223
07210	1	00001	1	06761	TXI 12,1,1 A REG PLUS 1 GOES TO A REG		RE340224
07211	0	50000	4	05663	14 CLA 2995,4 IS D O OF REGION 1 POSITIVE		RE340225
07212	0	12000	0	07216	TPL 16		RE340226
07213	0	50000	0	17511	CLA 8009		RE340227
07214	0	24000	0	17513	FDH 8011		RE340228
07215	0	02000	0	07225	TRA 17-1		RE340229
07216	0	56000	0	17504	16 LDQ 8004 COMPUTE U L,1		RE340230
07217	0	26000	0	17513	FMP 8011		RE340231
07220	0	30000	0	04406	FAD 2310		RE340232
07221	0	60100	0	17520	STO 8016		RE340233
07222	0	56000	0	17511	LDQ 8009		RE340234

07223	0	26000	0	17504	FMP 8004		RE340235
07224	0	24000	0	17520	FDH 8016		RE340236
07225	-0	60000	2	13556	STQ 5998,2		RE340237
07226	0	26000	0	17502	I7 FMP 8002		RE340238
07227	0	24000	0	17511	FDH 8009		RE340239
07230	0	26000	2	02265	FMP 1205,2		RE340240
07231	0	60100	2	15526	STO 6998,2		RE340241
07232	0	02000	0	07074	TRA 18		RE340242
07233	0	50000	0	04404	I10 CLA 2308 3 GOES TO TEMP 1		RE340243
07234	0	60100	0	17520	STO 8016	ALPHA N CALCULATION	RE340244
07235	0	53400	4	04404	LXA 2308,4	3 GOES TO C REGISTER	RE340245
07236	0	56000	0	04566	LDQ 2422 2 PI GOES TO MQ		RE340246
07237	0	26000	4	04571	FMP 2425,4 TIMES ALPHA N-2		RE340247
07240	0	24000	4	04412	FDH 2314,4 DIVIDED BY N-2		RE340248
07241	-0	60000	4	04573	STQ 2427,4 GOES TO ALPHA N		RE340249
07242	-0	60000	0	17500	STQ 8000		RE340250
07243	0	50000	0	17520	CLA 8016		RE340251
07244	0	40000	0	04402	ADD 2306		RE340252
07245	0	60100	0	17520	STO 8016		RE340253
07246	0	40200	0	01753	SUB 1003 IS THIS N OF PROBLEM		RE340254
07247	0	10000	0	06731	TZE I1 YES		RE340255
07250	2	00001	4	07236	TIX I10+3,4,1 NO		RE340256
07251	0	00000	0	07251	HTR I10+14 N GREATER THAN 6		RE340257
07252	0	50000	0	04406	00 CLA 2310 COMPUTE P L,H		RE340258
07253	0	60100	0	17512	STO 8010		RE340259
07254	-0	63400	4	17521	SXD 8017,4		RE340260
07255	0	50000	0	01753	CLA 1003		RE340261
07256	0	40200	0	04402	SUB 2306		RE340262
07257	0	73400	4	00000	PAX 0,4		RE340263
07260	0	10000	0	07274	TZE 00+18		RE340264
07261	0	50000	1	01755	CLA 1005,1		RE340265
07262	0	24000	0	01754	FDH 1004		RE340266
07263	0	26000	0	04405	FMP 2309		RE340267
07264	0	30000	0	04406	FAD 2310		RE340268
07265	0	60100	0	17512	STO 8010		RE340269
07266	0	60100	0	17522	STO 8018		RE340270
07267	-2	00001	4	07274	TNX 00+18,4,1		RE340271
07270	0	56000	0	17512	LDQ 8010		RE340272
07271	0	26000	0	17522	FMP 8018		RE340273
07272	0	60100	0	17512	STO 8010		RE340274

07273	0	02000	0	07267	TRA 00+13		RE340275
07274	-0	53400	4	17521	LXD 8017,4 COMPUTE F2		RE340276
07275	0	50000	0	04406	CLA 2310		RE340277
07276	0	30200	2	13557	FSB 5999,2		RE340278
07277	0	76500	0	00043	LRS 35		RE340279
07300	0	26000	0	17512	FMP 8010		RE340280
07301	0	60100	0	17514	STO 8012		RE340281
07302	0	56000	0	17512	LDQ 8010 COMPUTE F3		RE340282
07303	0	26000	2	15527	FMP 6999,2		RE340283
07304	0	60100	0	17515	STO 8013		RE340284
07305	-0	75400	0	00000T	PXD 0,0 ZERO TO INTEGRALS	016	RE340285
07306	0	60100	0	17506	STO 8006		RE340286
07307	0	60100	0	17525	STO 8021		RE340287
07310	0	50000	1	02121	CLA 1105,1 H L GOES TO H		RE340288
07311	0	60100	0	17505	STO 8005		RE340289
07312	0	56000	1	01755	LDQ 1005,1 COMPUTE G2		RE340290
07313	0	26000	1	01755	FMP 1005,1		RE340291
07314	0	24000	4	05664	FDH 2996,4		RE340292
07315	0	26000	0	04405	FMP 2309		RE340293
07316	0	60100	0	17502	STO 8002		RE340294
07317	0	76500	0	00043	LRS 35 COMPUTE G1/2		RE340295
07320	0	26000	4	05665	FMP 2997,4		RE340296
07321	0	60100	0	17501	STO 8001		RE340297
07322	-3	77776	1	07741	TXL 03,1,32766	IS THIS INNERMOST REGION	RE340298
07323	0	50000	4	05667	CLA 2999,4 YES, IS DI EQUAL ZERO	01	RE340299
07324	-0	10000	0	07723	TNZ 02		RE340300
07325	0	50000	0	05667	CLA 2999 K GOES TO FLUX L,H		RE340301
07326	0	60100	0	17507	STO 8007		RE340302
07327	0	50000	0	17507	CLA 8007	COMPUTE F4, F5	RE340303
07330	0	60100	0	17517	STO 8015		RE340304
07331	0	50000	2	02265	CLA 1205,2		RE340305
07332	0	60100	0	17516	STO 8014		RE340306
07333	-0	63400	4	17521	SXD 8017,4	SAVE C INDEX	RE340307
07334	0	50000	0	01753	CLA 1003		RE340308
07335	0	40200	0	04402	SUB 2306		RE340309
07336	0	73400	4	00000	PAX 0,4		RE340310
07337	0	10000	0	07347	TZE 06+16		RE340311
07340	0	56000	0	01754	LDQ 1004		RE340312
07341	0	26000	0	17517	FMP 8015		RE340313
07342	0	60100	0	17517	STO 8015		RE340314

07343 0 56000 0 01754
 07344 0 26000 0 17516
 07345 0 60100 0 17516
 07346 2 00001 4 07340
 07347 -0 53400 4 17521
 07350 0 50000 0 01754
 07351 0 30200 1 01755
 07352 0 60100 0 17522
 07353 0 76100 0 00000
 07354 0 76100 0 00000
 07355 0 50000 0 17505
 07356 0 10000 0 07361
 07357 0 40200 1 02121
 07360 -0 10000 0 07367
 07361 0 56000 0 17517
 07362 0 26000 0 04405
 07363 0 60100 0 17517
 07364 0 56000 0 17516
 07365 0 26000 0 04405
 07366 0 60100 0 17516
 07367 0 50000 0 17517
 07370 0 30000 0 17506
 07371 0 60100 0 17506
 07372 0 50000 0 17516
 07373 0 30000 0 17525
 07374 0 60100 0 17525
 07375 0 50000 0 17505
 07376 0 40200 1 02121
 07377 0 40000 0 04402
 07400 -0 10000 0 07435
 07401 -3 77776 1 07667
 07402 0 50000 0 01753
 07403 0 40200 0 04402
 07404 0 10000 0 07667
 07405 0 50000 1 01755
 07406 0 24000 0 04407
 07407 0 50000 0 17522
 07410 0 04000 0 07667
 07411 0 50000 0 17510
 07412 0 30200 0 17507

LDQ 1004
 FMP 8014
 STO 8014
 TIX 06+9,4,1
 LXD 8017,4
 CLA 1004
 FSB 1005,1
 STO 8018
 NOP
 NOP
 CLA 8005 ACCUMULATE INTEGRALS
 TZE 06+26 IS THIS INNER EDGE OF REGION
 SUB 1105,1
 TNZ 06+32 IS THIS OUTER EDGE OF REGION
 LDQ 8015
 FMP 2309
 STO 8015
 LDQ 8014
 FMP 2309
 STO 8014
 CLA 8015
 FAD 8006
 STO 8006
 CLA 8014
 FAD 8021
 STO 8021
 CLA 8005
 SUB 1105,1
 ADD 2306
 TNZ 07+1
 TXL 012,1,32766
 CLA 1003
 SUB 2306
 TZE 012
 CLA 1005,1
 FDH 2311
 CLA 8018
 TLQ 012
 CLA 8008 FOR R OF 0, COMPUTE EI FOR INNERMOST REGION
 FSB 8007

RE340315
 RE340316
 RE340317
 RE340318
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07413	0	24000	0	04407	FDH 2311		RE340355
07414	0	26000	0	17500	FMP 8000		RE340356
07415	0	76500	0	00043	LRS 35		RE340357
07416	0	26000	4	05664	FMP 2996,4		RE340358
07417	0	60100	0	17523	STO 8019		RE340359
07420	0	50000	1	01755	CLA 1005,1		RE340360
07421	0	24000	0	04407	FDH 2311		RE340361
07422	-0	60000	0	17520	STQ 8016		RE340362
07423	-0	63400	4	17521	SXD 8017,4		RE340363
07424	0	50000	0	01753	CLA 1003		RE340364
07425	0	40200	0	04403	SUB 2307		RE340365
07426	0	73400	4	00000	PAX 0,4		RE340366
07427	0	10000	0	07434	TZE 07		RE340367
07430	0	56000	0	17523	LDQ 8019 DELTA/2 TIMES E0		RE340368
07431	0	26000	0	17520	FMP 8016		RE340369
07432	0	60100	0	17523	STO 8019		RE340370
07433	2	00001	4	07426	TIX 06+63,4,1		RE340371
07434	-0	53400	4	17521	LXD 8017,4		RE340372
07435	0	50000	2	02265	CLA 1205,2 S L,H GOES TO S+		RE340373
07436	0	60100	0	04415	STO 2317		RE340374
07437	0	56000	0	17507	LDQ 8007 COMPUTE POINT SOURCE FOR NEXT GROUP		RE340375
07440	0	26000	4	05665	FMP 2997,4		RE340376
07441	0	76500	0	00043	LRS 35		RE340377
07442	0	26000	4	05666	FMP 2998,4		RE340378
07443	0	60100	2	02265	STO 1205,2		RE340379
07444	0	50000	0	17505	CLA 8005 IS H ZERO		RE340380
07445	0	10000	0	07473	TZE 08		RE340381
07446	0	40200	0	04402	SUB 2306 H-1 GOES TO H		RE340382
07447	0	60100	0	17505	STO 8005		RE340383
07450	1	77777	2	07451	TXI 09,2,32767	B REG-1 GOES TO B REG	RE340384
07451	-0	63400	4	17520	SXD 8016,4		RE340385
07452	0	50000	0	01754	CLA 1004		RE340386
07453	0	60100	0	17521	STO 8017		RE340387
07454	0	50000	0	17507	CLA 8007		RE340388
07455	0	60100	0	17522	STO 8018		RE340389
07456	0	07400	4	10137	TSX P6,4 PRINT R, FLUX		RE340390
07457	0	17522	0	17521	8017,0,8018		RE340391
07460	-0	53400	4	17520	LXD 8016,4		RE340392
07461	0	50000	0	17507	CLA 8007 FLUX GOES TO FLUX +		RE340393
07462	0	60100	0	17510	STO 8008		RE340394

07463	0	50000	0	01754	CLA 1004 R PLUS DELTA R GOES TO R	RE340395
07464	0	30000	1	01755	FAD 1005,1	RE340396
07465	0	60100	0	01754	STO 1004	RE340397
07466	0	56000	0	17510	LDQ 8008	RE340398
07467	0	26000	2	13556	FMP 5998,2 COMPUTE FLUX	RE340399
07470	0	30000	2	15526	FAD 6998,2	RE340400
07471	0	60100	0	17507	STO 8007	RE340401
07472	0	02000	0	07327	TRA 06	RE340402
07473	0	50000	0	17523	CLA 8019 EO GOES TO EI	RE340403
07474	0	60100	0	17524	STO 8020	RE340404
07475	0	50000	0	04406	CLA 2310 COMPUTE Q L,0	RE340405
07476	0	60100	0	17511	STO 8009	RE340406
07477	-0	63400	4	17521	SXD 8017,4	RE340407
07500	0	50000	0	01753	CLA 1003	RE340408
07501	0	40200	0	04402	SUB 2306	RE340409
07502	0	73400	4	00000	PAX 0,4	RE340410
07503	0	10000	0	07516	TZE 08+19	RE340411
07504	0	50200	1	01755	CLS 1005,1	RE340412
07505	0	24000	0	01754	FDH 1004	RE340413
07506	0	26000	0	04405	FMP 2309	RE340414
07507	0	30000	0	04406	FAD 2310	RE340415
07510	0	60100	0	17511	STO 8009	RE340416
07511	0	60100	0	17522	STO 8018	RE340417
07512	-2	00001	4	07517	TNX 08+20,4,1	RE340418
07513	0	56000	0	17511	LDQ 8009	RE340419
07514	0	26000	0	17522	FMP 8018	RE340420
07515	0	60100	0	17511	STO 8009	RE340421
07516	0	02000	0	07512	TRA 08+15	RE340422
07517	-0	53400	4	17521	LXD 8017,4	RE340423
07520	0	56000	0	04415	LDQ 2317 COMPUTE EO	RE340424
07521	0	26000	0	17502	FMP 8002	RE340425
07522	0	60100	0	17522	STO 8018	RE340426
07523	0	50000	0	17511	CLA 8009	RE340427
07524	0	30000	0	17501	FAD 8001	RE340428
07525	0	76500	0	00043	LRS 35	RE340429
07526	0	26000	0	17507	FMP 8007	RE340430
07527	0	60100	0	17521	STO 8017	RE340431
07530	0	56000	0	17511	LDQ 8009	RE340432
07531	0	26000	0	17510	FMP 8008	RE340433
07532	0	30200	0	17521	FSR 8017	RE340434

07533	0	30000	0	17522	FAD 8018		RE 340435
07534	0	24000	1	01755	FDH 1005,1		RE 340436
07535	0	26000	4	05664	FMP 2996,4		RE 340437
07536	0	76500	0	00043	LRS 35		RE 340438
07537	0	26000	0	17500	FMP 8000		RE 340439
07540	0	60100	0	17523	STO 8019		RE 340440
07541	-0	63400	4	17521	SXD 8017,4		RE 340441
07542	0	50000	0	01753	CLA 1003		RE 340442
07543	0	40200	0	04402	SUR 2306		RE 340443
07544	0	73400	4	00000	PAX 0,4		RE 340444
07545	0	10000	0	07552	TZE 08+47		RE 340445
07546	0	56000	0	17523	LDQ 8019		RE 340446
07547	0	26000	0	01754	FMP 1004		RE 340447
07550	0	60100	0	17523	STO 8019		RE 340448
07551	2	00001	4	07546	TIX 08+43,4,1		RE 340449
07552	-0	53400	4	17521	LXD 8017,4		RE 340450
07553	0	56000	0	17525	LDQ 8021 ALPHA N TIMES THE SOURCE INTEGRAL		RE 340451
07554	0	26000	0	17500	FMP 8000		RE 340452
07555	0	76500	0	00043	LRS 35		RE 340453
07556	0	26000	1	01755	FMP 1005,1 TIMES DELTA R		RE 340454
07557	0	60100	0	17525	STO 8021		RE 340455
07560	0	56000	0	17506	LDQ 8006 ALPHA N TIMES THE FLUX INTEGRAL		RE 340456
07561	0	26000	0	17500	FMP 8000		RE 340457
07562	0	76500	0	00043	LRS 35		RE 340458
07563	0	26000	1	01755	FMP 1005,1 TIMES DELTA R		RE 340459
07564	0	60100	0	17506	STO 8006		RE 340460
07565	0	76500	0	00043	LRS 35 COMPUTE BALANCE CHECK		RE 340461
07566	0	26000	4	05665	FMP 2997,4		RE 340462
07567	0	76000	0	00002	CHS		RE 340463
07570	0	30000	0	17524	FAD 8020		RE 340464
07571	0	30200	0	17523	FSR 8019		RE 340465
07572	0	30000	0	17525	FAD 8021		RE 340466
07573	0	60100	0	17526	STO 8022		RE 340467
07574	-0	75400	1	00000	PXD 0,1	IS L EQUAL TO 1	RE 340468
07575	0	77100	0	00022	ARS 18		RE 340469
07576	0	40000	0	01752	ADD 1002		RE 340470
07577	0	76700	0	00030	ALS 24		RE 340471
07600	0	10000	0	07603	TZE 010		RE 340472
07601	0	50000	4	05663	CLA 2995,4 IS DO POSITIVE		RE 340473
07602	-0	12000	0	07664	TMI 015		RE 340474

07603	0	56000	0	17502	010	LDQ 8002 COMPUTE CURRENT		RE340475
07604	0	26000	0	04415		FMP 2317		RE340476
07605	0	60100	0	17520		STO 8016		RE340477
07606	0	56000	0	17511		LDQ 8009		RE340478
07607	0	26000	0	17510		FMP 8008		RE340479
07610	0	60100	0	17521		STO 8017		RE340480
07611	0	50200	0	17511		CLS 8009		RE340481
07612	0	30200	0	17501		FSB 8001		RE340482
07613	0	76500	0	00043		LRS 35		RE340483
07614	0	26000	0	17507		FMP 8007		RE340484
07615	0	30000	0	17520		FAD 8016		RE340485
07616	0	30000	0	17521		FAD 8017		RE340486
07617	0	24000	1	01755		FDH 1005,1		RE340487
07620	0	26000	4	05664		FMP 2996,4		RE340488
07621	0	60100	0	17530		STO 8024		RE340489
07622	-0	63400	4	17521	011	SXD 8017,4 PRINT R, FLUX, INTEGRAL FLUX, LEAKAGE, CURRENT, B.C.		RE340490
07623	0	50000	0	01754		CLA 1004		RE340491
07624	0	60100	0	17531		STO 8025		RE340492
07625	0	50000	0	17507		CLA 8007		RE340493
07626	0	60100	0	17532		STO 8026		RE340494
07627	0	50000	0	17506		CLA 8006		RE340495
07630	0	60100	0	17533		STO 8027		RE340496
07631	0	50000	0	17523		CLA 8019		RE340497
07632	0	60100	0	17534		STO 8028		RE340498
07633	0	50000	0	17530		CLA 8024		RE340499
07634	0	60100	0	17535		STO 8029		RE340500
07635	0	50000	0	17526		CLA 8022		RE340501
07636	0	60100	0	17536		STO 8030		RE340502
07637	0	07400	4	10143		ISX P7,4		RE340503
07640	0	17536	0	17531		8025,0,8030		RE340504
07641	-0	53400	4	17521		LXD 8017,4		RE340505
07642	-0	75400	1	00000	013	PXD 0,1 IS L EQUAL 1		RE340506
07643	0	77100	0	00022		ARS 18		RE340507
07644	0	40000	0	01752		ADD 1002		RE340508
07645	0	76700	0	00030		ALS 24		RE340509
07646	0	10000	0	07654		TZE 014		RE340510
07647	0	50000	0	17507		CLA 8007 FLUX GOES TO FLUX +		RE340511
07650	0	60100	0	17510		STO 8008		RE340512
07651	1	77777	1	07652		TXI 013+8,1,32767	A REG-1 GOES TO A REG	RE340513
07652	1	77777	2	07653		TXI 013+9,2,32767	B REG-1 GOES TO B REG	RE340514

07653	1	77773	4	07252		TXI 00,4,32763			RE340515
07654	0	50000	0	17527	014	CLA 8023 IS THIS LAST GROUP	C REG-5 GOES TO C REG		RE340516
07655	0	40200	0	01751		SUB 1001			RE340517
07656	0	10000	0	07663		TZE OMEGA			RE340518
07657	0	50000	0	17527		CLA 8023			RE340519
07660	0	40000	0	04402		ADD 2306			RE340520
07661	0	60100	0	17527		STO 8023			RE340521
07662	0	02000	0	06731		TRA 11			RE340522
07663	0	02000	0	06654	OMEGA	TRA 10-4			RE340523
07664	-0	75400	0	00000T	015	PXD 0,0			RE340524
07665	0	60100	0	17530		STO 8024			RE340525
07666	0	02000	0	07622		TRA 011			RE340526
07667	0	56000	0	04415	012	LDQ 2317 R NOT 0, COMPUTE EI FOR INNERMOST REGION			RE340527
07670	0	26000	0	17502		FMP 8002			RE340528
07671	0	60100	0	17520		STO 8016			RE340529
07672	0	56000	0	17507		LDQ 8007			RE340530
07673	0	26000	0	17512		FMP 8010			RE340531
07674	0	60100	0	17521		STO 8017			RE340532
07675	0	50000	0	17512		CLA 8010			RE340533
07676	0	30000	0	17501		FAD 8001			RE340534
07677	0	76500	0	00043		LRS 35			RE340535
07700	0	26000	0	17510		FMP 8008			RE340536
07701	0	30200	0	17520		FSB 8016			RE340537
07702	0	30200	0	17521		FSB 8017			RE340538
07703	0	24000	1	01755		FDH 1005,1			RE340539
07704	0	26000	4	05664		FMP 2996,4			RE340540
07705	0	76500	0	00043		LRS 35			RE340541
07706	0	26000	0	17500		FMP 8000			RE340542
07707	0	60100	0	17523		STO 8019			RE340543
07710	-0	63400	4	17521		SXD 8017,4			RE340544
07711	0	50000	0	01753		CLA 1003			RE340545
07712	0	40200	0	04402		SUB 2306			RE340546
07713	0	73400	4	00000		PAX 0,4			RE340547
07714	0	10000	0	07721		TZE 012+26			RE340548
07715	0	56000	0	17523		LDQ 8019			RE340549
07716	0	26000	0	01754		FMP 1004			RE340550
07717	0	60100	0	17523		STO 8019			RE340551
07720	2	00001	4	07715		TIK 012+22,4,1			RE340552
07721	-0	53400	4	17521		LXD 8017,4			RE340553
07722	0	02000	0	07434		TRA 07			RE340554

07723	0	12000	0	07765	02	TPL CHECK		RE340555
07724	0	50000	1	01755		CLA 1005,1 IS R EQUAL ZERO		RE340556
07725	0	24000	0	04407		FDH 2311		RE340557
07726	0	50000	0	01754		CLA 1004		RE340558
07727	0	04000	0	07731		TLQ 02+6		RE340559
07730	0	02000	0	07775		TRA 05		RE340560
07731	0	50000	0	17514		CLA 8012 COMPUTE FLUX AT INNER EDGE		RE340561
07732	0	30000	0	17501		FAD 8001		RE340562
07733	0	60100	0	17520		STQ 8016		RE340563
07734	0	56000	0	17502		LDQ 8002		RE340564
07735	0	26000	2	02265		FMP 1205,2		RE340565
07736	0	30000	0	17515		FAD 8013		RE340566
07737	0	24000	0	17520		FDH 8016		RE340567
07740	0	02000	0	07326		TRA 06-1		RE340568
07741	0	50000	4	05656	03	CLA 2990,4		RE340569
07742	0	12000	0	07746		TPL 04		RE340570
07743	0	50000	0	17510		CLA 8008 FLUX AT ZERO, I+1 GOES TO FLUX AT H+1		RE340571
07744	0	60100	0	17507		STQ 8007 CONTINUITY CONDITION FLUX AT INTERFACE		RE340572
07745	0	02000	0	07327		TRA 06		RE340573
07746	0	50000	4	05667	04	CLA 2999,4		RE340574
07747	0	10000	0	07772		IZE CHECK+5		RE340575
07750	0	50000	1	01755		CLA 1005,1 BLACK BOUNDARY CONDITION		RE340576
07751	0	24000	4	05667		FDH 2999,4 FLUX AT INTERFACE		RE340577
07752	-0	60000	0	17520		STQ 8016		RE340578
07753	0	50000	0	17520		CLA 8016		RE340579
07754	0	30000	0	17501		FAD 8001		RE340580
07755	0	30000	0	17514		FAD 8012		RE340581
07756	0	60100	0	17520		STQ 8016		RE340582
07757	0	56000	0	17502		LDQ 8002		RE340583
07760	0	26000	2	02265		FMP 1205,2		RE340584
07761	0	30000	0	17515		FAD 8013		RE340585
07762	0	24000	0	17520		FDH 8016		RE340586
07763	-0	60000	0	17507		STQ 8007		RE340587
07764	0	02000	0	07327		TRA 06		RE340588
07765	0	50000	1	01755	CHECK	CLA 1005,1 IS R EQUAL ZERO		RE340589
07766	0	24000	0	04407		FDH 2311		RE340590
07767	0	50000	0	01754		CLA 1004		RE340591
07770	0	04000	0	07746		TLQ 04		RE340592
07771	0	00000	0	07771		HTR CHECK+4		RE340593
07772	-0	75400	0	00000T		PXD 0,0		RE340594

07773	0	60100	0	17507	STO 8007		RE340595
07774	0	02000	0	07327	TRA 06		RE340596
07775	-0	63400	4	17521	05 SXD 8017.4 COMPUTE FLUX AT R EQUAL ZERO		RE340597
07776	0	50000	0	01753	CLA 1003 FOR DERIVATIVE OF FLUX EQUAL ZERO		RE340598
07777	0	76000	0	00006	COM	BOUNDARY CONDITION	RE340599
10000	0	40000	0	04402	ADD 2306		RE340600
10001	0	73400	4	00000	PAX 0.4		RE340601
10002	0	50000	0	04406	CLA 2310		RE340602
10003	0	30200	2	13557	FSB 5999.2		RE340603
10004	0	76500	0	00043	LRS 35		RE340604
10005	0	26000	4	04405	FMP 2309.4		RE340605
10006	0	30000	0	17501	FAD 8001		RE340606
10007	0	60100	0	17520	STO 8016		RE340607
10010	0	56000	2	15527	LDQ 6999.2		RE340608
10011	0	26000	4	04405	FMP 2309.4		RE340609
10012	0	60100	0	17522	STO 8018		RE340610
10013	0	56000	2	02265	LDQ 1205.2		RE340611
10014	0	26000	0	17502	FMP 8002		RE340612
10015	0	30000	0	17522	FAD 8018		RE340613
10016	0	24000	0	17520	FDH 8016		RE340614
10017	-0	60000	0	17507	STQ 8007		RE340615
10020	-0	53400	4	17521	LXD 8017.4		RE340616
10021	0	02000	0	07327	TRA 06		RE340617
10022	0	02000	0	00613	P1 TRA OUT1		RE340618
10023	010730513325				BCD 17HR.E. 34 PROBLEM F8.5//6H	J= 13.6H L= 13.6H N= 11.6	RE340619
10024	336003046060						
10025	475146224325						
10026	446076103305						
10027	616106306060						
10030	604113603103						
10031	730630606060						
10032	431360310373						
10033	063060606045						
10034	136031017306						
10035	306060605113				BCD 9H R= F9.3.6H	D= 14//13HMESH SPACING/(10F12.6)	RE340620
10036	602611330373						
10037	063060606047						
10040	136031046161						
10041	010330442562						
10042	306060624721						

10043	233145276174						
10044	010026010233						
10045	063460606060						
10046	0 02000 0 00613	P2	TRA OUT1				RE340621
10047	616101113047		BCD 6//19HPOINTS PER REGION/(10112)				RE340622
10050	463145636260						
10051	604725516060						
10052	512527314645						
10053	617401003101						
10054	023460606060						
10055	0 02000 0 00613	P3	TRA OUT1				RE340623
10056	616101113047		BCD 7//19HPOINT-WISE SOURCES/(1P10E12.4)				RE340624
10057	463145634066						
10060	316225606062						
10061	466451232562						
10062	617401470100						
10063	250102330434						
10064	606060606060						
10065	0 02000 0 00613	P4	TRA OUT1				RE340625
10066	616102043027		BCD //24HGROUP-REGION PARAMETERS/4H K= 1PE12.4/58H		D OUT		RE340626
10067	514664474051						
10070	252721464560						
10071	604721512144						
10072	256325516261						
10073	043060421360						
10074	014725010233						
10075	046105103060						
10076	606060602460						
10077	466463606060						
10100	602421262633		BCD	DIFF. COEF.	SIGMA	TRANSFER	D IN /(1P5E12.4)
10101	602346252633						RE340627
10102	606060623127						
10103	442160606060						
10104	606063512145						
10105	622625516060						
10106	606060602460						
10107	314560617401						
10110	470525010233						
10111	043460606060						
10112	0 02000 0 00613	P5	TRA OUT1				RE340628

10113	616101001030	BCD	//108H	RADIUS	FLUX	FLUX INTEGRAL	LEAKAGE	CURRRE340629
10114	606051212431							
10115	646260606060							
10116	606060264364							
10117	676060606026							
10120	436467603145							
10121	632577512143							
10122	606043252142							
10123	212775606060							
10124	606073645151							
10125	254563606060	BCD	ENT	BAL	CK		J= 13/	RE340630
10126	602271436060							
10127	234260606060							
10130	606060606060							
10131	606060606060							
10132	606060606060							
10133	606060606060							
10134	606060606060							
10135	606060411360							
10136	310361606060							
10137	0 02000 0 00613	P6		TRA OUT1				RE340631
10140	260100330373			BCD 3F10.3,1PE12.4				RE340632
10141	014775010233							
10142	046060606060							
10143	0 02000 0 00613	P7		TRA OUT1				RE340633
10144	260100330373			BCD 3F10.3,1P5E12.4				RE340634
10145	014705250102							
10146	330460606060							
10147	0 01755 0 01750	PD1		1000.0,1005				RE340635
10150	0 02121 0 02122	PD2		1106.0,1105				RE340636
10151	0 02265 0 02266	PD3		1206.0,1205				RE340637
10152	0 05667 0 05667	PD4		2999.0,2999				RE340638
10153	0 77000 0 00202	TAPE	WEF 2	WRITE END OF FILE TAPE 2				RE340639
10154	0 02000 0 06660			TRA IO				RE340640
04402	+000000000001	2306	DEC	1,2,3,.5,1.0,2.0,3.0,4.0,5.0,6.0,7.0				RE340641
04403	+000000000002							
04404	+000000000003							
04405	+200400000000							
04406	+201400000000							
04407	+202400000000							

04410 +2026000000000
04411 +2034000000000
04412 +2035000000000
04413 +2036000000000
04414 +2037000000000
04565 +2024000000000
04566 +203622077324
04567 +204622077324

06660

2421 DEC 2.0.6.2831853.12.5663706

END IO

RE340642

RE340643