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## Planning Tools and Techniques for Product Evaluation and Disassembly \*

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### ABSTRACT

This paper describes the development and implementation of a computerized model to support production planning in a specialized type of remanufacturing facility, the Pantex Plant operated for the U. S. Department of Energy. The model integrates two different production processes (nuclear weapon dismantlement and stockpile evaluation) which use common facilities and personnel, and reflects the interactions of scheduling constraints, material flow constraints and resource availability. These two processes reflect characteristics of flow-shop and job-shop operations in a single facility. Operational results from using the model are also discussed.

**KEYWORDS:** Production planning, scheduling, optimization

### INTRODUCTION

The Pantex Plant in Texas is a U.S. Department of Energy (DOE) facility that is responsible for product evaluation and disassembly of a very specialized type of product -- nuclear weapons. Despite the very specialized nature of the items being evaluated and dismantled, the structure of the problem at Pantex is similar to that faced in more general remanufacturing environments. Pantex is engaged in a mixture of tasks that share common production facilities, personnel and storage areas. Some of these tasks are flow-shop activities -- the dismantlement of many similar units which require processing through the same sequence of steps. Others are job-shop activities -- evaluation of single units which must be partially disassembled, tested and then reassem-

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bled, each involving a relatively unique series of operations. Effective production planning tools to help allocate and schedule shared resources are of great value in such an environment. The tools and techniques described in this paper have been developed for direct application to the Pantex Plant, but they should also have broader applicability to other remanufacturing operations, as well as to agile manufacturing facilities.

Sandia National Laboratories has developed a computerized manufacturing optimization model called the *Pantex Process Model (PPM)*. The PPM has the ability to:

- ☐ simultaneously plan two fundamentally different types of production processes utilizing common facilities and personnel;
- ☐ optimize total production output;
- ☐ allocate technicians efficiently; and
- ☐ expedite recovery planning and option evaluation after a production disruption.

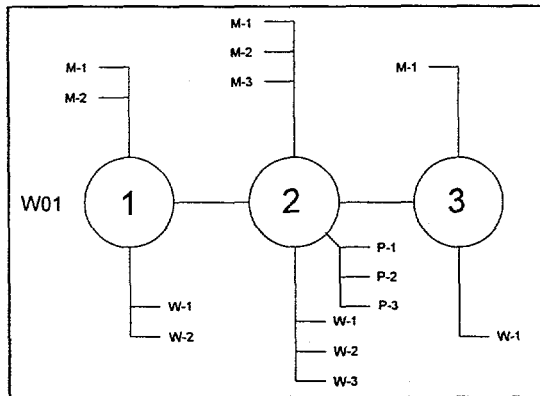
Simultaneous planning of flow shop and job shop activities using common resources is a key characteristic of the PPM. In a flow shop, many individual production units follow the same prespecified sequence of operations, and the focus of production planning is on overall throughput, line balancing, bottleneck identification, etc. In a job-shop environment, individual items are made to order, with varying sequences of operations and varying times for each operation. Morton and Pentico (1993) provide a thorough description of the differences in approaching production planning and scheduling for flow shops and job shops.

## **PROBLEM DEFINITION**

The basic perspective of the PPM is to maximize throughput, given limited resources and required milestones for certain operations. The workstations are combinations of facility types and personnel, and the work performed is mostly manual, being either dismantlement (the disassembly of weapons) or evaluation tasks (work done in support of stockpile surety). Total production is in the thousands, the workstations number about 80, and the number of production technicians is in the hundreds.

Production planning is complex, for a number of reasons. One problem is that the disassembly and evaluation activities are fundamentally different. Disassembly requires performance of a specific sequence of operations, and can be described using a network flow diagram like the one illustrated in Figure 1. At any given time, several different types of weapons are being dismantled, each being at a different stage in its series of operations. Evaluations require a unique sequence of operations on individual units (i.e., job-shop operation), and each unit typically has scheduling constraints (i.e., earliest available start times and latest allowable completion times). Evaluation tasks are significantly more complex and often involve situations where facilities are being "used" by partially disassembled units, but technicians are not involved. Both types of operations use common facilities and personnel.

More complexity arises from the extremely demanding and complicated safety and security rules. For example, technicians must receive extensive training before being certified for a particular task. The combination of several hundred technicians and nearly one hundred unique certifications presents a daunting assignment problem. Adding to this challenge is the fact that certifications must be used or they are lost, as determined by another set of complex rules.



*Figure 1: Example flow diagram of disassembly operations used by the PPM, where W01 = weapon system 1, W-1 = waste stream 1, M-1 = input material 1, P-1 = part 1, and the three nodes (numbered circles) indicate specific operations or processes.*

A "two-person" rule must also be observed. At least two technicians (each with the same certification) must be present during an operation.

Compliance with ALARA guidelines must also be addressed. Strict guidelines must be followed to ensure that personnel receive radiation doses as low as reasonably attainable (ALARA), and if the maximum dose is reached by a technician, he/she is unavailable (for a specified period of time) for production activities, regardless of his/her certification status.

Facility allocation is complicated by safety and security considerations. There are fifteen

types of facilities, with multiple sub-types, each governed by a set of rules, including fissile and explosive material limits, as well as environmental and physical requirements. Furthermore, a hierarchy exists among these facilities, so that an operation which is normally performed in a facility of type A can also be performed in a facility of type B, but the converse is not necessarily true.

An additional complicating factor is limited storage capacity. Storage facilities are used both to stage incoming weapons (to be evaluated or dismantled) and to store parts removed from the weapons (either temporarily or permanently). Because of tight storage (or staging) capacity, the arrival, staging, and shipment of weapons and the storage/staging and shipment of parts must be closely monitored and controlled to support a production plan and schedule. As might be expected, the storage facilities, like the production facilities, are governed by complex safety and security rules.

## PROBLEM FORMULATION

The overall production planning problem can be formulated as a very large mixed integer programming (MIP) problem, in which the objective is to maximize disposal throughput (numbers of weapons dismantled, of various types) over a one-year planning horizon. The constraints include completion of required evaluation activities and resource availability limits (facilities, technicians and storage). We will explain the construction of the constraints on

technician use and allocation quite thoroughly, but give only a brief summary of the facility and storage use constraints.

For the dismantlement activities, the basic time unit is one month. The actual disposal output in each month,  $V_{st}$ , is defined in terms of the units processed through particular operations, since the operations are weapon-specific. Each operation requires a facility and technicians with the correct certification. The model focuses on the flow of units through the system, and the consumption of resources is measured in facility-hours and person-hours.

If we let  $s(i)$  be the weapon system to which operation  $i$  belongs, we can write the consumption of technician person-hours by disposals for a particular certification  $c$ , in month  $t$ , as follows:

$$\sum_{i \in I_c} u_i z_i V_{s(i)t} \quad (1)$$

where  $I_c$  is the set of operations,  $i$ , for which certification  $c$  is valid;  $u_i$  is the number of machine hours required to perform operation  $i$ ; and  $z_i$  is number of technicians required for operation  $i$ .

Technician person-hours are also consumed by evaluation activities, so to form the full constraint for the resource represented by technicians with a specific certification, we need to add to the quantity in (1) the amount consumed by the evaluations. In contrast to the disposal activities, where many units flow through the same sequence of operations, the evaluation of a specific weapon unit requires a set of tasks that may be unique, so it is important to track the individual units through the specific tasks that are performed on it. For example, a lab test involves partial disassembly of the weapon, assembly of a test bed, conduct of the test, disassembly of the test bed, and rebuild of the weapon. These steps must be done in sequence, and within each step, more detailed tasks exist, some of which may be performed in parallel. "Due dates" are common for the intermediate tasks (e.g., for completion of the test bed), and meeting these dates has high priority. Also, tasks have priorities, such as disassembly of the test bed following the test. Lower priority tasks can be "fit in" around the higher priority ones on a resource-available basis.

These evaluation activities share technicians and facilities with disposals, but the required level of detail in terms of timing is much finer than for disposals. Individual tasks must be tracked, and these tasks require anywhere from a few hours to several days. Consequently, short time periods,  $t'$ , are defined, and these are "rolled up" to gain resource utilizations that mesh with the disposal activities. We will use  $t$  to denote months in the planning horizon ( $t = 1, 2, \dots, 12$ ), and  $t'$  to represent the smaller periods used for tracking evaluation activities, and define  $\beta(t')$  to be the length of period  $t'$  (e.g., hours) and  $T(t)$  to be the set of periods,  $t'$ , contained in month  $t$ . Then, a set of constraint equations can be written to ensure that sufficient technician resources (with a specific certification) are available to support all planned activities (disposals and evaluations) in each month.

$$\sum_j \sum_{l=t'}^{t+d_j-1} g_{jk} v_{jl} = \Gamma_{kt'} \quad \forall \quad k, t' \quad (2)$$

$$\sum_{i \in I_c} u_i z_i V_{s(i)t} + \sum_{t' \in T(t)} \Gamma_{k_{ct'}} \beta(t') - \sum_e x_{ect} - D_{ct} = 0 \quad \forall \quad c, t \quad (3)$$

where  $d_j$  is the duration of task  $j$ ;  $g_{jk}$  is the number of units of resource  $k$  required for task  $j$  (e.g., number of technicians);  $\Gamma_{kt'}$  is the total units of resource  $k$  required during period  $t'$ ;  $v_{jl}$  is equal to 1 if task  $j$  ends in period  $l$  and 0 otherwise;  $x_{ect}$  is the person-hours of employee  $e$  allocated to using certification  $c$  in month  $t$ ; and  $D_{ct}$  is the exposure limit for certification  $c$  in month  $t$ .

Constraint (2) is used to define the allocation of resources to tasks and ensures that sufficient person-hours of resources are allocated to support both disposal and resource index which corresponds to certification  $c$  in (3) helps remove the possibility that the users at Pantex wondering why the function as penalty terms, so the solution created for the PPM which really is infeasible.

*Have the Professors reviewed these equations to type? Summary?*

Constraint (3) then defines the allocation of person-hours to certifications) are designated the "technician hours" leaving the objective function setup is

For the evaluation tasks, we must ensure that precedence relationships are maintained. Constraints (4) and (5). Constraint (4) ensures that each task must end in one (and only one) period. The limits on the summation,  $e_j$  and  $\tau_j$ , in (5) are determined prior to the optimization, based on due dates and precedence relations among the tasks.

$$\sum_{t'=e_j}^{\tau_j} v_{jt'} = 1 \quad \forall \quad j \quad (4)$$

$$\sum_{t'=e_j}^{\tau_j} (t' - d_j) v_{jt'} - \sum_{t'=e_j}^{\tau_j} t' v_{lt'} \geq 0 \quad \forall \quad j, l \in P_j \quad (5)$$

where  $e_j$  is earliest time at which task  $j$  can end, based on the earliest possible start time for the evaluation activity of which  $j$  is a part, and the precedence relationships among the tasks;  $\tau_j$  is the latest time for completion of task  $j$ , based on required due dates and precedence relationships among the tasks; and  $P_j$  is the set of all tasks which immediately precede task  $j$ .

Technician-hours (reflected by the  $x_{ect}$  variables) are allocated based on the availability of individual technicians, maximum allowable radiation exposure, and crew-size requirements for specific operations. If  $S_{et}$  is the hours available for technician  $e$  in month  $t$ , one set of constraints is:

$$\sum_{c \in C_{et}} x_{ect} \leq S_{et} \quad \forall \quad e, t \quad (5)$$

The radiation exposure constraints, which ensure that no technician is allocated to tasks in such a way as to violate the acceptable exposure level, are written as follows:

$$\sum_t \sum_i r_i x_{ec(i)t} \leq U \quad \forall \quad e \quad (6)$$

where  $c(i)$  is the certification required for operation  $i$ , and  $U$  is the maximum radiation exposure allowed over a year.

The crew size requirements imply, for example, that if a particular operation requires two technicians, and a total of 180 technician-hours in a given month, we want to allocate two technicians for 90 hours each, not one technician for 160 hours and a second for 20 hours. To make sure that the total allocation of person-hours is spread across sufficient technicians to allow staffing of the operations, we limit each of the individual allocation terms, as follows:

$$x_{ect} - \sum_{i \in I_c} u_i V_{s(i)t} \leq 0 \quad \forall \quad e, c, t \quad (7)$$

The consumption of facility resources (facility-hours) is represented in a similar way to technicians, but with greater detail in some respects and less in others. The overall set of constraints is as follows:

$$\sum_{i \in Y_f} d_i W_{ift} \leq F_{ft} + E_{ft} \quad \forall \quad f, t \quad (8)$$

$$V_{st} = \sum_f W_{ift} \quad \forall \quad t, i \in I_s, s \quad (9)$$

where  $W_{ift}$  is the number of units processed through operation  $i$  in facility type  $f$  during month  $t$ ;  $Y_f$  is set of operations,  $i$ , which can be performed in facility type  $f$ ;  $d_i$  is the facility-hours required to perform operation  $i$ ;  $F_{ft}$  is the facility-hours of facility type  $f$  available in month  $t$ ; and  $E_{ft}$  is the excess facility-hours of type  $f$  consumed in month  $t$ .

Note that the variable definitions refer to facilities of a particular type, since there may be several individual facilities that are identical, and the PPM is only concerned with consumption of facility-hours in a facility of that type, without identifying exactly which facility is involved. The  $E_{ft}$  terms are similar to the  $D_{ct}$  values in the technician constraints, and must also be added to the objective function as penalty terms on overuse of facility-hours.



In constraint (9), the throughput of system  $s$  in any month  $t$  is connected to the variables which account for the number of units processed through operation  $i$  using facility  $f$  during month  $t$  ( $W_{ift}$ ). If we denote  $I_s$  as the set of operations required for dismantling weapon  $s$ , and sum over the facility types,  $f$ , we count the total units processed through operation  $i$  in month  $t$ . By having a "copy" of constraint (9) for each  $i$  in  $I_s$ , we ensure that all required operations are performed on each unit dismantled.

There is a hierarchy in facility types, and each operation  $i$  will have a minimum required facility, but can also be assigned to any higher capability facility. Thus, in general, for each  $i$  there will be several  $f$  values which are feasible assignments. Normally, we will want the solution to assign each operation (as much as possible) to the lowest available facility in the hierarchy. This is accomplished by adding to the objective function a set of usage penalties for assigning an operation to a higher-than-necessary facility type. Such assignments are then feasible, and will be done as necessary to use available facility-hours most effectively, but will be penalized in the objective function.

There may also be bounds on volume throughput. These produce constraint set (10):

$$V_{\min_{st}} \leq V_{st} \leq V_{\max_{st}} \quad \forall \quad s, t \quad (10)$$

where  $V_{\min_{st}}$  is the minimum required volume of system  $s$  in month  $t$  and  $V_{\max_{st}}$  is the maximum allowable volume for system  $s$  in month  $t$ .

In addition to representing the operations necessary for dismantlement, the PPM also tracks inventory balances and inbound/outbound shipment schedules. This integration of storage management within the PPM ensures that the disposal plan developed is internally consistent with the inbound and outbound shipment plans and the on-site storage constraints and logistics.

For units of system  $s$ , stored on-site awaiting dismantlement, an inventory balance equation can be written as follows:

$$Q_{st} = Q_{s,t-1} + A_{st} - V_{st} + \alpha_1 Z_s \quad \forall \quad s, t \quad (11)$$

where  $Q_{st}$  is the units of system  $s$  in storage at the end of month  $t$ ;  $A_{st}$  is the units of system  $s$  which arrive during month  $t$ ;  $Z_s$  is the additional units of system  $s$  that would have to be in inventory (or scheduled to arrive across the planning horizon) to support the disposal plan; and  $\alpha_1$  is 1 for month 1 in the planning horizon and 0 otherwise.

The values of  $A_{st}$  are assumed to be specified exogenously. The use of the  $Z_s$  variables in (11) allows the PPM to find a "solution" to any set of input data, even if the inbound shipment schedule is too small to support the level of system dismantlement demanded by the minimum values,  $V_{\min_{st}}$ , specified in equation (10). On output, if one of the  $Z_s$  variables is nonzero, it means there is a

shortfall in the number of units of system  $s$  available (either from initial inventory or the inbound arrival schedule) to support the dismantlement schedule that the model has developed.

An analogous set of constraints is defined to maintain the inventory balance for parts stored on-site after dismantlement:

$$R_{pt} = R_{p,t-1} + \left( \sum_s \sum_{i \in I_s} n_{ip} V_{st} \right) - G_{pt} + \alpha_1 L_p \quad \forall \quad p, t \quad (12)$$

where  $R_{pt}$  is the units of part  $p$  in storage at the end of month  $t$ ;  $n_{ip}$ , the units (pieces, kg, etc.) of part  $p$  removed (from weapon system  $s$ ) in operation  $i$ ;  $G_{pt}$  is the units of part  $p$  which are shipped off-site during month  $t$ ;  $L_p$  is the number of "pseudo-parts" of part  $p$  shipped in month  $t$  to meet shipment requirements; and  $\alpha_1$  is 1 for month 1 in the planning horizon and 0 otherwise.

The values of  $G_{pt}$  are assumed to be exogenous input to the model. The  $L_p$  variables act for parts the same way the  $Z_s$  variables act for incoming systems, to indicate the shortfall in parts generation (e.g., due to a lower-than-needed) dismantlement schedule, to support the planned parts shipments in the input dataset.

The on-site storage representation also connects the numbers of weapons and parts stored to the amount of space consumed for various configurations of the available storage facilities. If we index the configurations by  $j$ , then we can create two variables:  $\xi_{sj}$ , which is 1 if system  $s$  is to be stored in configuration  $j$  and 0 otherwise; and  $\eta_{pj}$ , which is 1 if part  $p$  is to be stored in configuration  $j$  and 0 otherwise.

The requirement for space in configuration  $j$  in month  $t$  is then represented by the following set of equations:

$$\sum_s \xi_{sj} \left( \frac{1}{cs_{sj}} \right) Q_{st} + \sum_p \eta_{pj} \left( \frac{1}{cs_{pj}} \right) R_{pt} = M_{jt} \quad \forall \quad m, t \quad (13)$$

where:  $cs_{sj}$  is the capacity of a magazine in configuration  $j$  for systems of type  $s$ ;  $cp_{pj}$  is the capacity of a magazine in configuration  $j$  for parts of type  $p$ ; and  $M_{jt}$  is the number of magazines which must be in configuration  $j$  during month  $t$  (i.e., sufficient to handle the inventory at the end of month  $t$ ).

Finally, the configurations are limited by the actual physical facilities available. If we let  $J_m$  represent the set of configurations possible for a magazine type,  $m$ , then these constraints can be written as follows:

$$\sum_{j \in J_m} M_{jt} \leq N_{mt} + B_{mt} \quad \forall \quad m, t \quad (14)$$

where:  $N_{mt}$  is the number of magazines of type  $m$  available in month  $t$  and  $B_{mt}$  is the "pseudo storage capacity" variable reflecting a shortfall in storage capacity of type  $m$  in month  $t$ .

The  $B_{mt}$  variables are introduced to represent possible storage capacity shortages, without having the model report "no feasible solution." The values of  $N_{mt}$  are input as data, and can be varied from month to month to reflect special considerations like repairs, etc.

The overall PPM objective function includes terms to represent the throughput (being maximized), as well as terms to reflect the added "penalty terms" for the excess technician hours, excess facility hours, pseudo-disposals and pseudo-shipments, and storage facility shortages that have been added to the model to prevent conditions of "no feasible solution" from the model, as well as the facility usage penalties. The resulting objective function is:

$$\begin{aligned} \max \sum_t \sum_s \lambda_s V_{st} - \gamma \sum_t \sum_c D_{ct} - \delta \sum_t \sum_f E_{ft} - \pi \sum_s Z_s \\ - \nu \sum_p L_p - \omega \sum_m \sum_t B_{mt} - \sum_i \sum_c \mu_{if} \sum_t W_{ift} \end{aligned} \quad (15)$$

This objective maximizes the system's (weighted) throughput, where the  $\lambda_s$  values reflect the possibility of different importance (weights) being placed on dismantlement of different systems. The second through sixth terms are penalty terms, with multipliers that must be set large enough to ensure that the model will not violate one of those constraints to increase throughput. Consequently, the sums from these five terms should normally be zero; otherwise, we actually have an infeasible solution.

The last term in (15) is the usage penalty for performing operations in higher-than-necessary facility types. The value of the multiplier  $\mu_{if}$  is the per-unit penalty for performing operation  $i$  in facility type  $f$ . For the minimum required facility for operation  $i$ , this value is zero. For facility types of higher capability,  $\mu_{if}$  should be positive, with larger values associated with facilities of greater capability. However, on the whole, the  $\mu_{if}$  values should be small, relative to the system weight coefficients in the first term of (15). In practice, the  $\mu_{if}$  values are determined automatically within the model, based on the other input data.

The overall problem (P) is then:

**Maximize (15)**

**Subject to: (2)-(14).**

## THE SOLUTION

To solve problem P in a manageable fashion, a modular structure is employed, as shown in Figure 2. This modularity facilitates modification of the model to meet new or changing requirements. It also allows substitution of other components, such as alternate GIS software, data base management system, or optimization software.

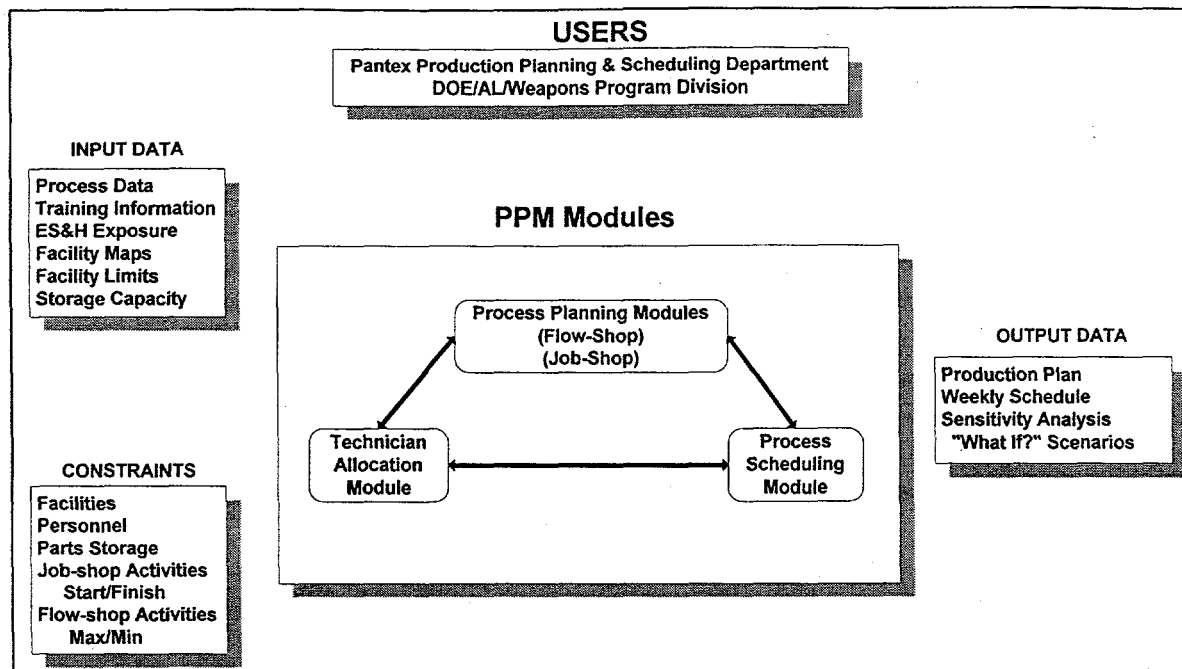


Figure 2: Structure of the PPM

The PPM has modules for planning disposal (DPM) and evaluation (EPM) activities as well as a technician allocation module (TAM) and a process scheduleability module (PSM). The following paragraphs describe how each of these modules functions, and how they are interconnected.

**DPM** – The DPM is a large-scale linear programming model that seeks to maximize the total number of units disassembled over a one-year planning horizon, subject to constraints on facility availability, technician availability, available space for storage/staging of both incoming units and outgoing parts/subassemblies, and mandated program requirements for specific weapon systems. Its output is an optimal disposal plan, on a monthly basis, for a one-year planning period. Because the DPM is a linear programming model, the solution also yields valuable sensitivity analysis information, such as shadow prices that indicate how much the total throughput be increased if additional hours of a given resource were made available. The binding constraints in the DPM solution identify the choke points in the process, and allow the users at Pantex to determine whether the number of disposals is being limited by facility availability, technician availability, storage/staging availability, etc.

The user interface for the DPM allows the staff at Pantex to focus on providing input data in a form they are familiar with, and getting output that is as graphical as possible to facilitate understanding and communication with other parts of the Pantex operation. The interface also allows them to quickly change selected inputs and rerun the model, to respond effectively to “what if” questions from DOE, or to change the disposal plan to reflect the influences of unanticipated disruptions in the over process, from whatever source they arise.

**EPM** – The EPM creates a plan for conducting a set of prespecified stockpile evaluation activities over the course of a one-year planning period. Typically, each of these activities involves an earliest possible start time, a due date for completion, and a specified set of operations that must be performed in a particular order. Each operation requires a certain facility type, and technicians with particular certifications. The overall facility pool and set of available technicians are shared with the disposal activities. The solution to this problem is based on techniques for multiproject, constrained resource, project scheduling (see, for example, Bell and Han, 1991). The output of the EPM is a proposed plan, on a week-by-week basis, for conducting the required evaluation activities, and a specification of what resources must be allocated to those activities in each week.

The essential idea embedded in the solution procedure for the EPM is to level the resource demands subject to the time window constraints on the tasks and the precedence requirements. In general, for situations of realistic size, this is a very complicated problem, so a heuristic is employed.

It is clear that the DPM and EPM are closely connected, because they are used to plan activities that compete for a common set of resources (facilities and technicians). For facilities, the modules interact directly to ensure that the available facility-hours of each facility type are efficiently allocated between disposals and evaluations. For technicians, the interaction is more complex, because both the DPM and the EPM are seeking available technician-hours for particular certifications, and individual technicians often hold multiple certifications. Thus, the interaction between the planning modules for technicians requires a third module.

**TAM** – The Technician Allocation Module determines allocations of technician-hours in each month of the one-year planning horizon to demands for person-hours of various certifications, arising from the DPM and EPM. The model takes the form of a network optimization for each month, with linking constraints across the months of the year to prevent overexposure of any individual technician to radiation. Figure 4 illustrates the network structure of the model, in which the “supplies” (available hours for a specific technician with given certifications) are allocated to meet the “demands” (required technician-hours, by certification, within a given month). A “pseudo-source” is included to identify any infeasibilities which must be resolved by iteration with the DPM and EPM. The resulting network problem can be solved very efficiently, using specialized algorithms (see, for example, Bertsekas, 1991).

In a typical application, the DPM and EPM are run first, using “infinite” technician resources, to generate a desired level of technician-hours in each certification. Then the TAM is run to determine how many hours in each certification is actually supportable by existing technicians. These values are then fed back to the DPM and EPM, resulting in new plans. The iteration among the DPM, EPM and TAM continues until consistent results are achieved.

**PSM** – When a consistent plan (involving disposals, evaluations and technician allocations) has been developed, the PSM is invoked to check for scheduleability: that a given plan can be converted into actual assignments of specific people and facilities to specific tasks. Typically the time frame employed is 2-4 weeks. This is the time when detailed requirements and special

regulations are taken into account to ensure the feasibility of the planned activities. If infeasibilities are uncovered at this level, it is necessary to return to the planning modules and revise the overall plan.

## ILLUSTRATIVE EXAMPLE

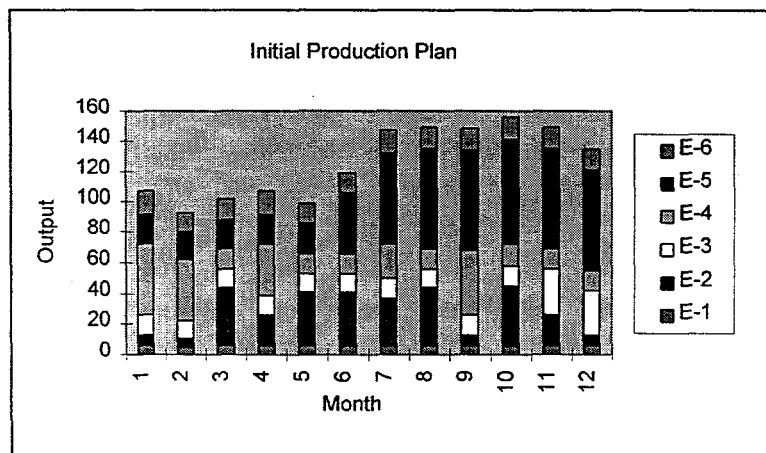
This section presents an example of how the PPM can be used to plan production. Because there are sensitivities about the specifics of problems pertaining to the Pantex plant, the example is built around a hypothetical small aircraft engine remanufacturing plant that rebuilds high-performance engines for stunt planes. The size and complexity of the engines mandates special assembly jigs, testing devices and highly trained technicians. Moreover, as part of a quality control/quality assurance program, randomly selected engines are returned to the plant each year to undergo evaluations, some more extensive than others, to ensure that no fatigue-related problems are developing. In terms of the Pantex plant, the remanufacture of engines is like dismantlement and the two evaluation programs are functionally equivalent. The facilities are assembly jigs and testing devices instead of rooms with certain characteristics.

The parameters of the example problem are as follows. Six types of engines are being built, with a production goal of about 1000 engines per year, total. Complementing this is a test program involving slightly more than 250 engines. To support this activity, some 70 assembly jigs are used and a dozen or so testing devices, plus about 200 technicians. The jigs break down into about 20 types, and the testing devices divide into six types. Some of these are unique. In total, the number of workstations is about 80. Each technician holds up to 5 certifications, related to different aspects of manufacturing or testing. The most common number of certifications held is 2. For any given task, at least two and sometimes three people are required.

Our initial production solution focuses on capacity planning, seeking to determine what level of output is possible if the facility resources are the only constraint (jigs, test stands, and storage). In this case, the upper limits on production are set to high values while the minimums are set to expected demand. The problem involves 6 engines, 4-5 operations per engine (25 total), 1-5 facility

options for each operation, and 8 certifications. The overall math programming problem involves about 2300 rows and 3600 variables for the 12-month planning horizon.

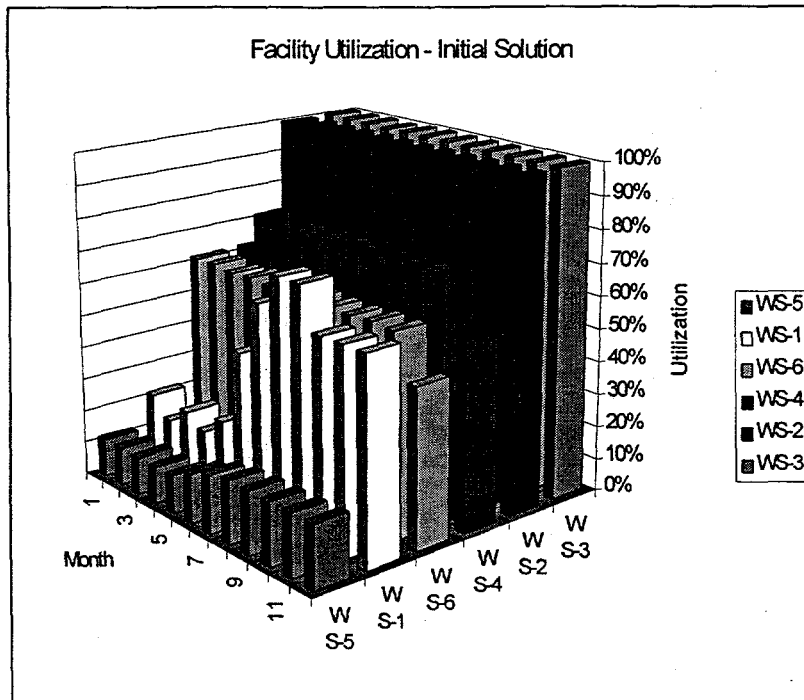
This results in a total potential output of 1,510 engines, 50% in excess of the target value. Figure 3 shows this is a production rate of 100-160 engines per month. Engine type 5 tends to predominate, with the quantities of engine types



**Figure 3: Initial Production Solution**

2 and 4 varying month to month.

If the current marketplace can absorb this level of output, or if new markets can be tapped, this suggests where to focus training efforts to create qualified technicians sufficient to support this level of output.

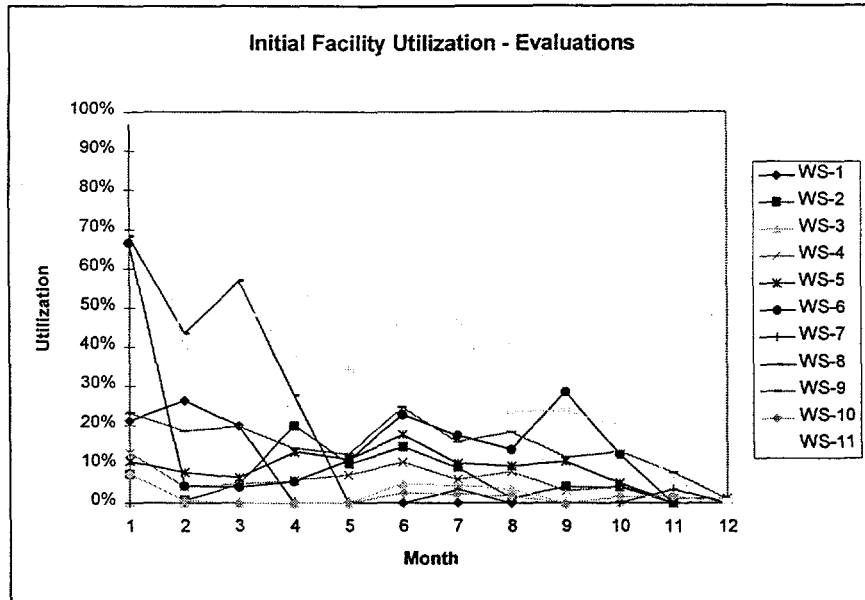


**Figure 4: Facility Utilization - Initial Solution**

deploy the resources.

The evaluation plan calls for roughly 250 engines to be tested. Unlike the production analysis, however, no potential market expansion warrants consideration of greater output. The question is whether the evaluations planned can be accommodated with the facilities available. (The problem being solved involves 368 jobs, all with earliest allowable start times and latest allowable finish times, 1000 tasks, and 42 resources - 11 facilities and 31 certifications. The plan is developed across 252 days constituting a single work year. On 233 occasions, resource demands are in excess of supply and the timings of tasks and jobs needed to be adjusted.)

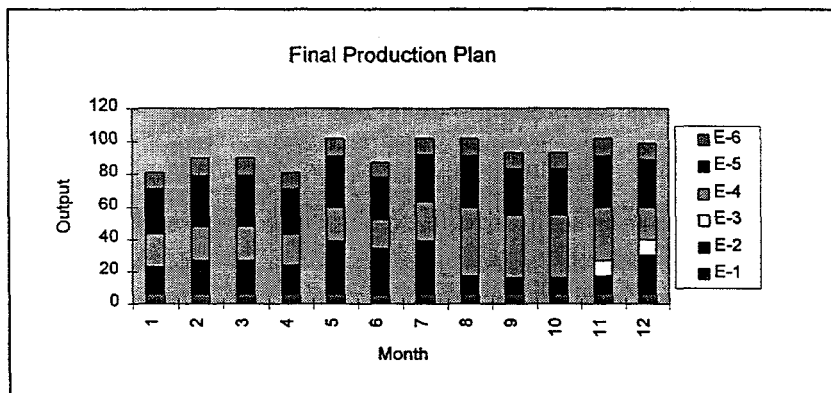
The analysis also tells us whether the right balance of facility capacity exists. As Figure 4 shows, a poor balance currently exists. Workstations of types WS-2 and WS-3 are in full use for this facility driven solution. (It's not critical here to identify exactly what type of workstations these are.) Those two facility types are the bottlenecks to greater output. The other four workstation types are only partly utilized, and could be reconfigured for redeployment or converted into WS-2's or WS-3's. Either strategy would produce a more balanced production situation and better



**Figure 5: Initial Facility Utilization - Evaluations**

not an automatic, or even achievable outcome, necessarily. Moreover, many of these facilities are set aside for evaluation use and are not easily diverted to other activities. The main message in Figure 5 may be that redeployment of some of these resources would be a healthy change. Potentially, more production could be achieved.

The model suggests that the evaluation plan can be achieved. Figure 5 shows that facility utilization rates stay below 65% except for WS-11. Also, the evaluation plan seems to be front-loaded with more activity occurring in the beginning of the year. While it might be better if these rates were higher, there are earliest allowable start times on most jobs, as well latest allowable finish times on certain tasks within those jobs, so level resource requirements is



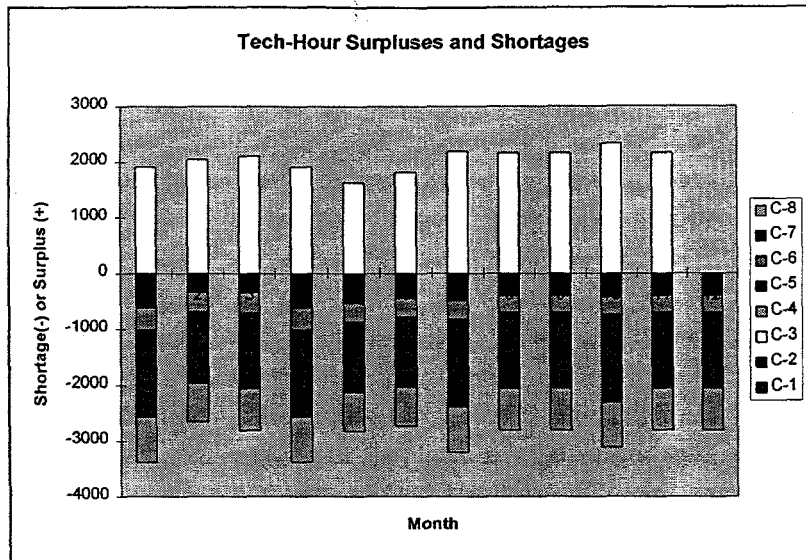
**Figure 6: Final Production Plan**

This is because very few technicians have the certifications required to produce all but those two engines.

When the availability of technicians is taken into account, the total potential output drops to 939 engines, just shy of the 1,000 target. The output rate ranges between 80 and 100 engines per month as shown in Figure 6. There is less production of every engine, especially E-5. In fact, only engines E-2 and E-4 are being produced at levels above minimum requirements.

Figure 7 gives guidance about the training needed to rectify this situation. People are needed with certifications C-5 through C-8 and some of these can be obtained by retraining people who hold C-3 certifications.



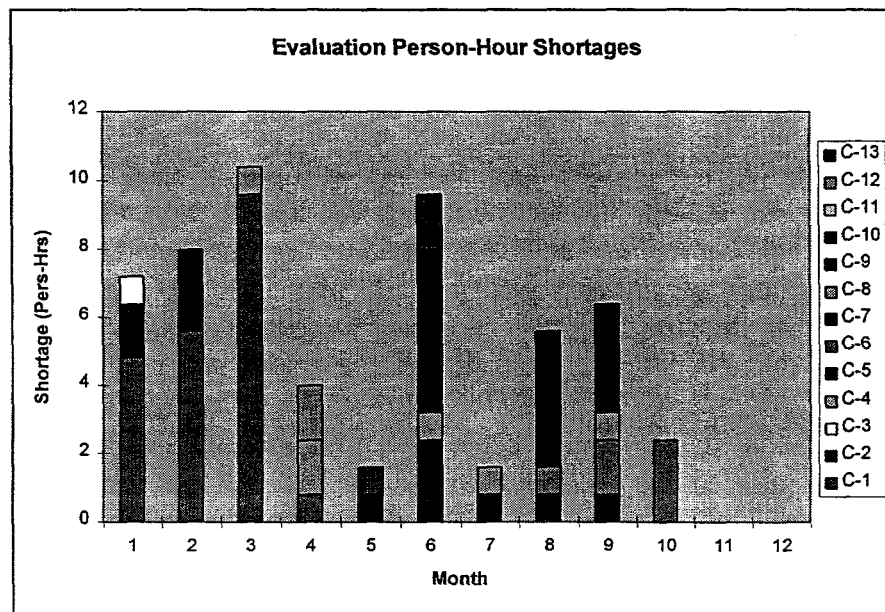


**Figure 7: Cert-Hour Surpluses and Shortages - Production**

will have to be revised with lower minimums for E-3 and E-4 until a feasible solution is achieved. (Note that as this is done, the output of other engines may increase, absorbing some of the pool of technicians perceived to be available for training in the current situation.)

The labor situation for the evaluation activities is more hopeful. As Figure 8 shows, only a few shortages exist, and none are significant in magnitude.

During the early months, certification C-1 is in short supply. In later months it is C-5. In no event are the shortfalls here as significant as they are for the production plan.



**Figure 8: Certification Shortfalls for Evaluations**

It reflects the interactions among scheduling constraints, material flow constraints, and resource

The technician allocation analysis (whose results are not shown here) indicates that sufficient technicians are available to receive the required training. (The technician allocation problem involves slightly more than 140 technicians, who hold slightly more than 230 certifications total, in response to demands for 40 certifications. For 19 of these certifications, shortages are identified.) Of course, if the training does not take place, or not enough people are trained, then the production plan

## CONCLUSIONS AND FUTURE WORK

This paper has presented an overview of the Pantex Process Model, a computerized production planning tool developed for the Pantex Plant, a U.S. Department of Energy facility, so that more effective and efficient production planning can be achieved. It is specifically geared for situations where resources are shared among multiple products and processes.

availability for situations where both flow-shop and job-shop operations are occurring simultaneously.

The PPM can help achieve substantial productivity increases. The Pantex Production Planning and Scheduling Department expects to achieve significant improvement in the following areas:

- *total production output* – the PPM allows Pantex to achieve *optimal* production output, as opposed to settling for the first *workable* plan and schedule that they find.
- *time required for planning and scheduling* – use of the PPM cuts the response time for re-scheduling production activities after a disruption and for replying to “what-if” questions from days to hours, while increasing the confidence in the answers achieved.
- *allocation of technicians* – optimal assignment of the technicians requires juggling thousands of variables, which is an impossible task to do well without computer support. The PPM optimally assigns technicians, as well as provides guidance on future training requirements.
- *allocation of facilities* – the PPM is used to assign specific facilities for specific tasks in an optimal manner, taking into account maintenance activities.
- *identification of potential choke points* – for production planning and risk management purposes, it is important to understand which processes control production output. The PPM identifies such choke points (including the geographic location) and presents valuable sensitivity analysis information, which allows the users at Pantex to determine whether the output is being limited by facility availability, technician availability, storage/staging availability, etc

We have also successfully demonstrated that the integration of a geographic information system with the PPM can provide direct facility impact information related to an on-site inspection, as well as how the potential impact could be minimized through intelligent routing of the inspectors in conjunction with the option analysis capabilities of the PPM.

Future work will focus on development of a training program planner, GIS capabilities, including the routing of inspectors, and an on-line scheduler. The first of these will provide plant management with an ability to more effectively determine who should receive what skills in support of future needs. The example problem illustrates the value of redeploying resources but stops short of suggesting how such decisions should be made. Such assignment problems are difficult, especially in cases where the training time frames are long and the skill requirements are complex and time varying. Such is the case at Pantex.

The GIS interface, coupled with routing analysis capabilities, will make it possible to measure the impact of uncleared visitors (such as on-site inspections in support of treaty verification, etc.). It also offers the intriguing possibility of analyzing trade-offs and minimizing potential impacts on normal operations.

The on-line scheduler will function in real time, tied to production data from the shop floor, and be capable of suggesting workflow strategies that maximize both efficiency and effectiveness at

the plant level. For places like Pantex, where safety is of great concern, this is not simply a matter of maximizing plant utilization, but achieving a balance among a number of competing objectives, only one of which is maximizing plant output.

## ACKNOWLEDGMENT

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