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# Characterizing the dynamic strength of a polymer epoxy using the Richtmyer-Meshkov Instability

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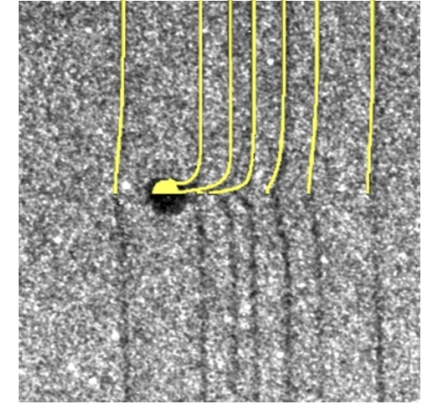
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# The Dynamic Strength of Polymers is not well characterized

- Little work done regarding strength in the shock regime
- Recent particle tracking experiments performed by Bober et al indicated that silicone has a flow strength of 500 to 750 MPa, stronger than some metals
- Epon 828 Epoxy
  - Has been previously investigated in planar impact experiments
  - Can be polymerized with a variety of curing agents
  - Many shock Hugoniot datasets in the literature fail to list curing agent
  - Often assumed that the Equation-of-State (EOS) is the same regardless of curing agent



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Particle Tracking Experiments in Silicone  
[Bober et al (2019)]

EPOXY, Epon 828

Average  $\rho_s = 1.185 \text{ g/cm}^3$

Sound velocities longitudinal 2.63 km/s  
shear 1.16 km/s

Reference 51

$\rho_s$ (g/cm <sup>3</sup> )	$U_s$ (km/s)	$U_p$ (km/s)	P (GPa)	V (cm <sup>3</sup> /g)	$\rho$ (g/cm <sup>3</sup> )	V/V <sub>0</sub>	Exp
1.192	2.263	0.000	0.000	8389	1.192	1.000	ssp x
1.184	3.265	.370	1.430	7489	1.335	.887	iml o
1.184	3.355	.411	1.633	7411	1.349	.877	iml o
1.184	3.421	.494	2.001	7228	1.384	.856	iml o
1.184	3.805	.639	2.879	7028	1.423	.832	iml o

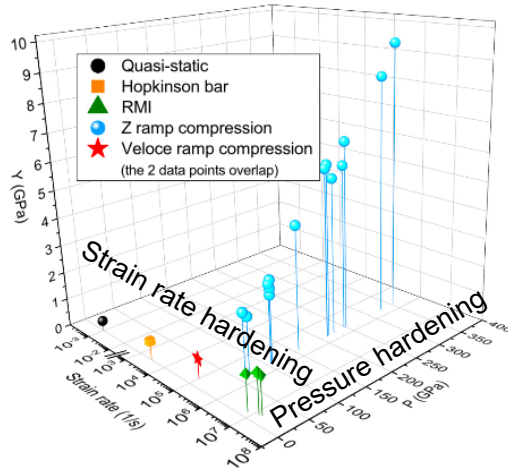
[LASL Marsh Compendium]

# Pressure and Strain Rate Hardening



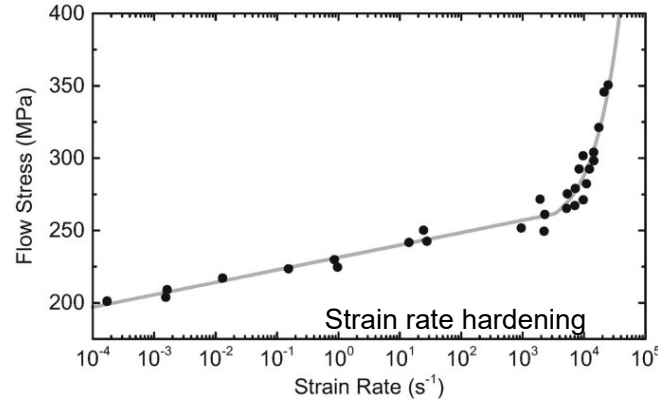
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## Tantalum



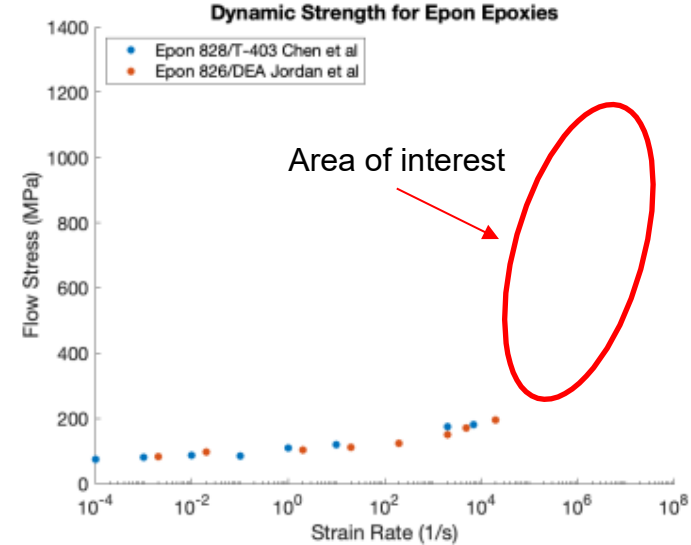
Prime et al (2019)

## Copper



Lea and Walley [High Strain Rate Metal Plasticity]

## Epoxy

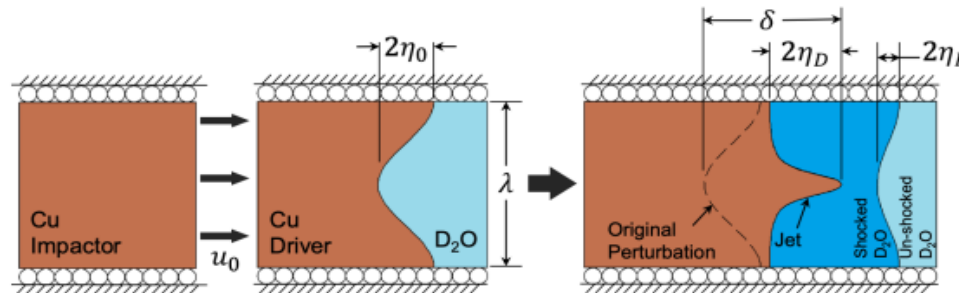


# Tamped Richtmyer-Meshkov Instability (RMI) Experiments

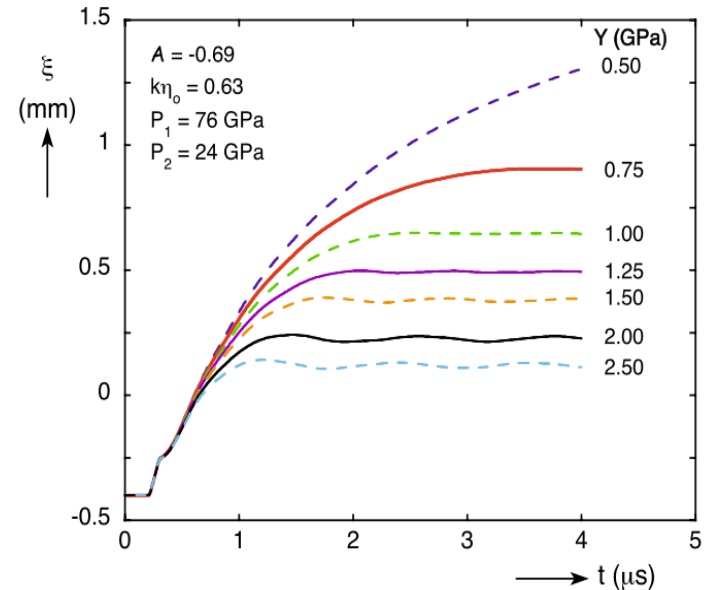


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- Used for constitutive model calibration
- Experimental behavior is compared to simulations to calibrate the material strength
- RMI inversion behavior is affected by
  - Driver strength,  $Y_p$
  - Tamper strength,  $Y_T$
  - Shock stress,  $\sigma$
  - Atwood Number,  $A = \frac{\rho_T - \rho_D}{\rho_T + \rho_D}$
  - Corrugation aspect ratio  $k\eta_0$



Olles et al (2021)



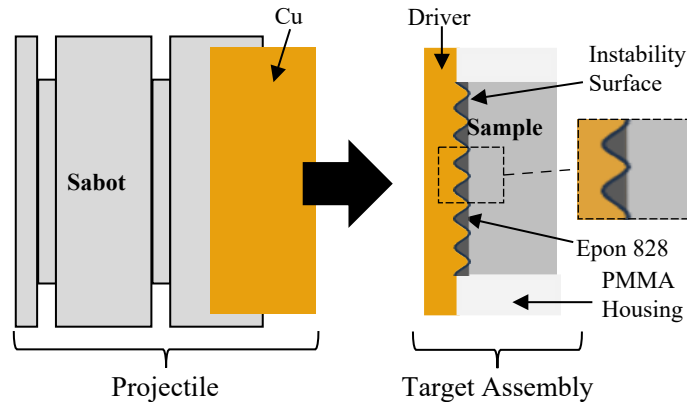
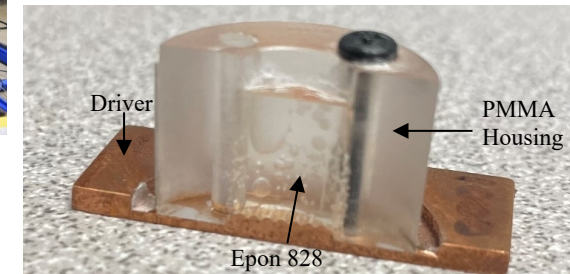
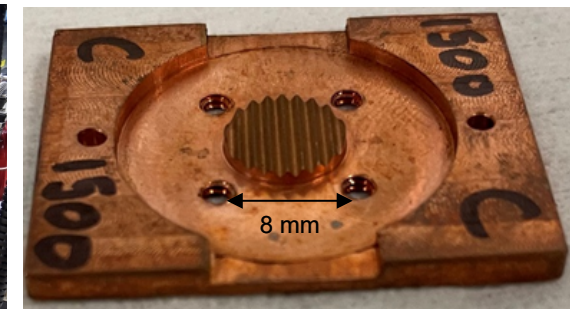
Vogler et al (2021)



# Experimental Details and Setup



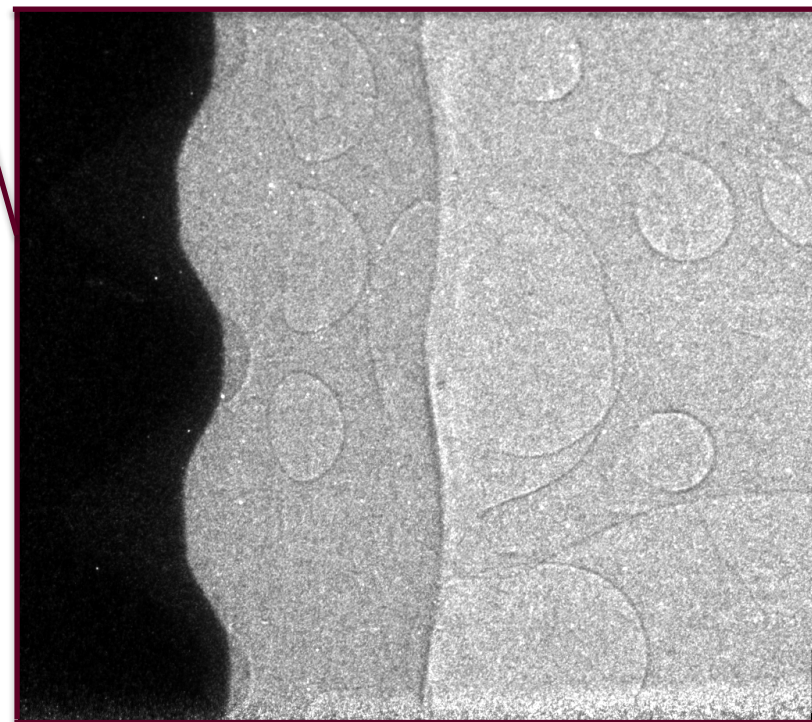
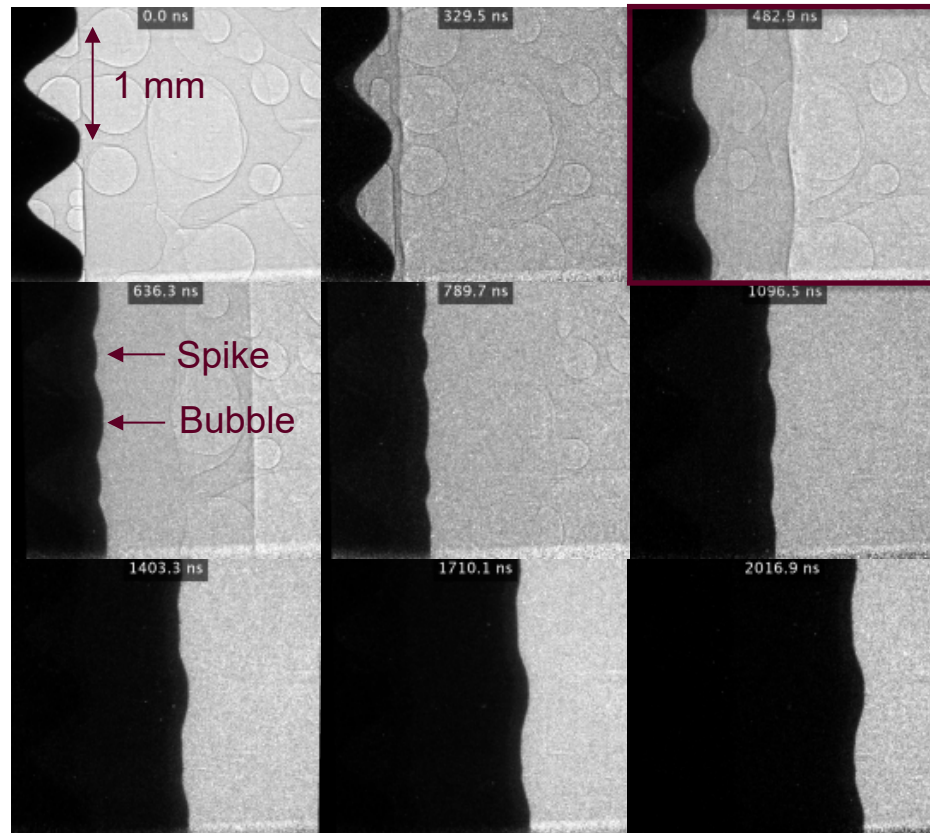
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# Evaluating Radiography Data



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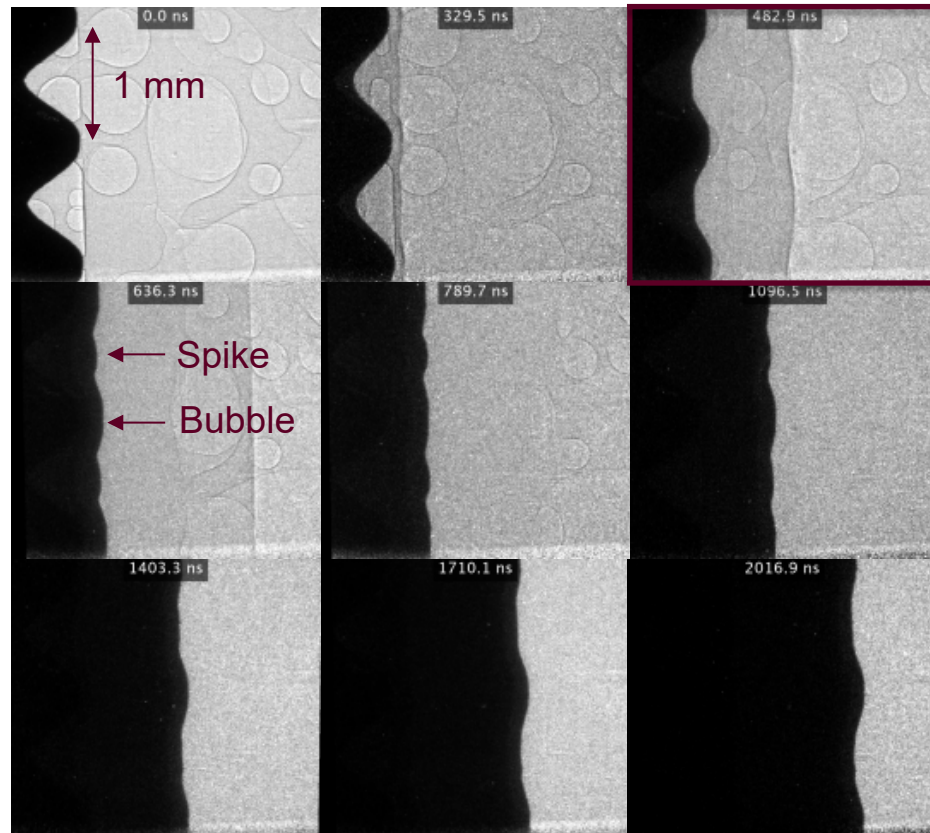
Impacted at 1.2 km/s and 5 GPa



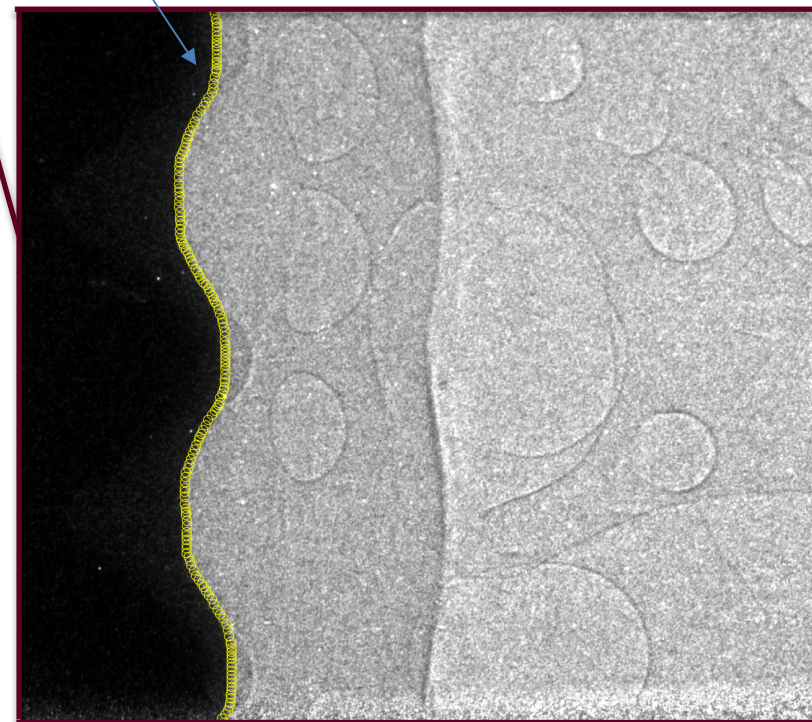
# Evaluating Radiography Data



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Cu – Epon828  
Contact Surface

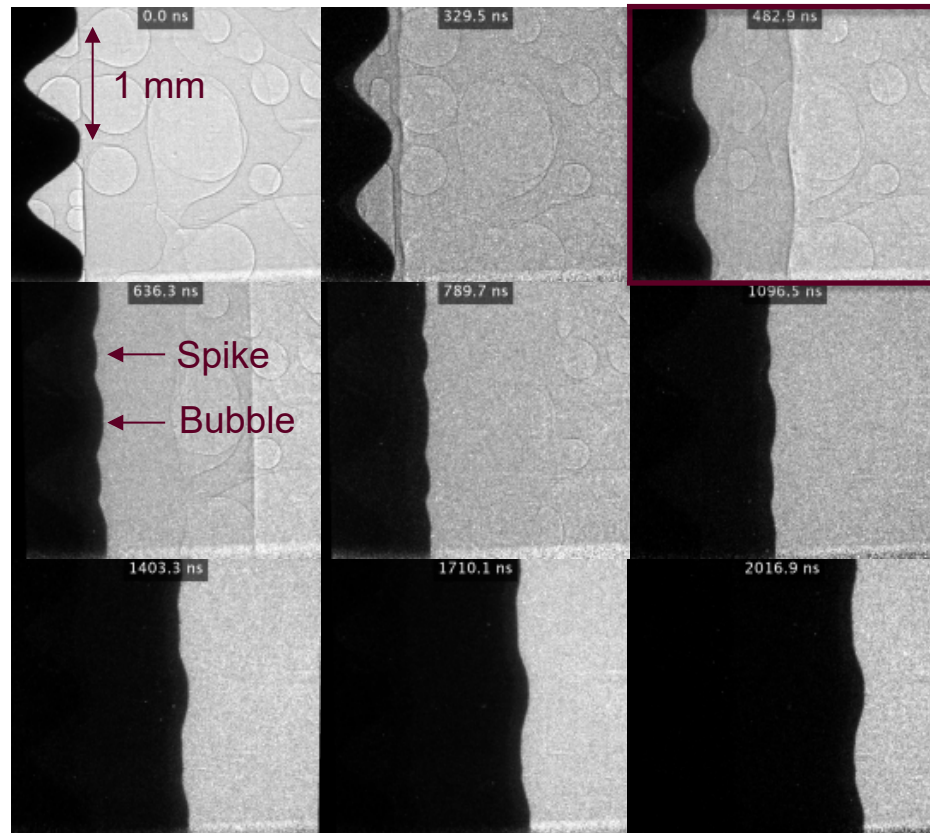


Impacted at 1.2 km/s and 5 GPa

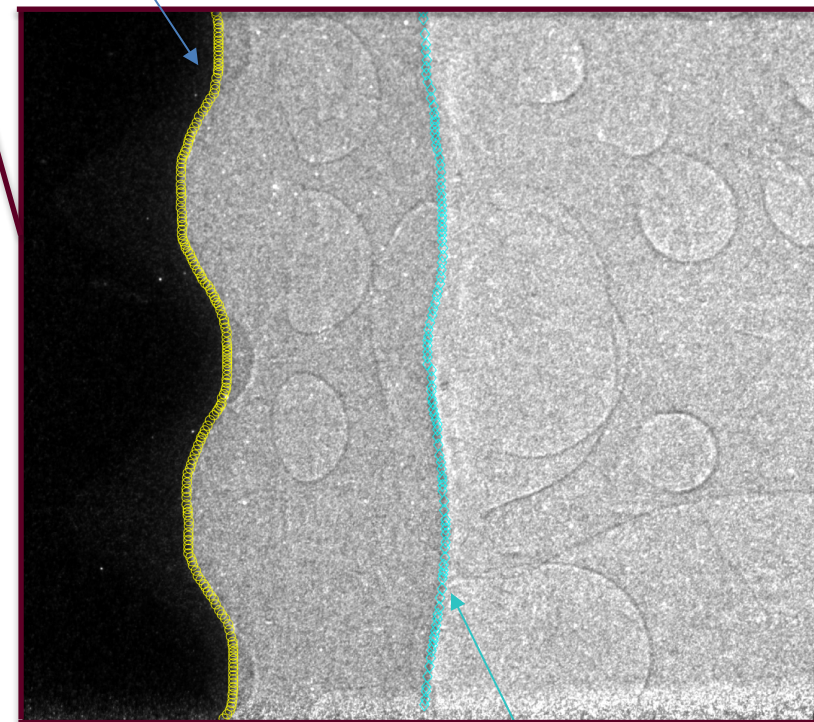
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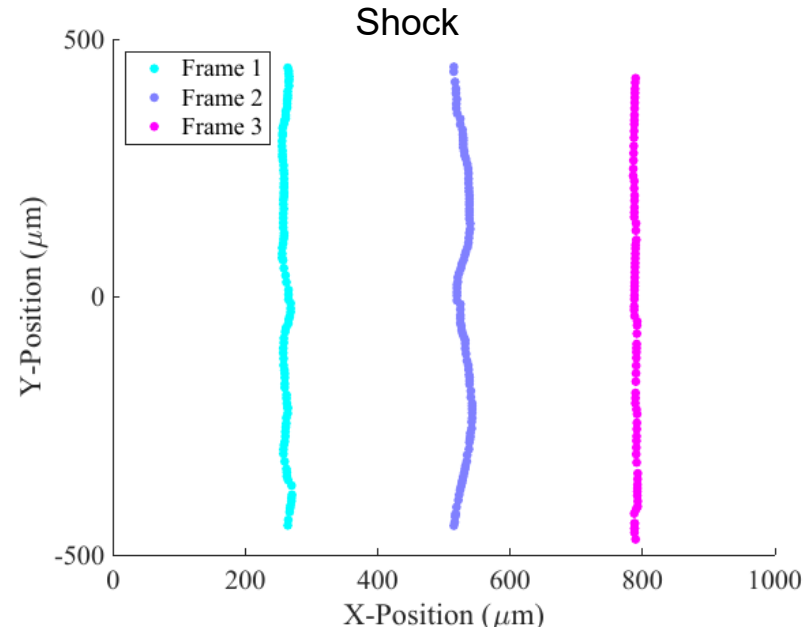
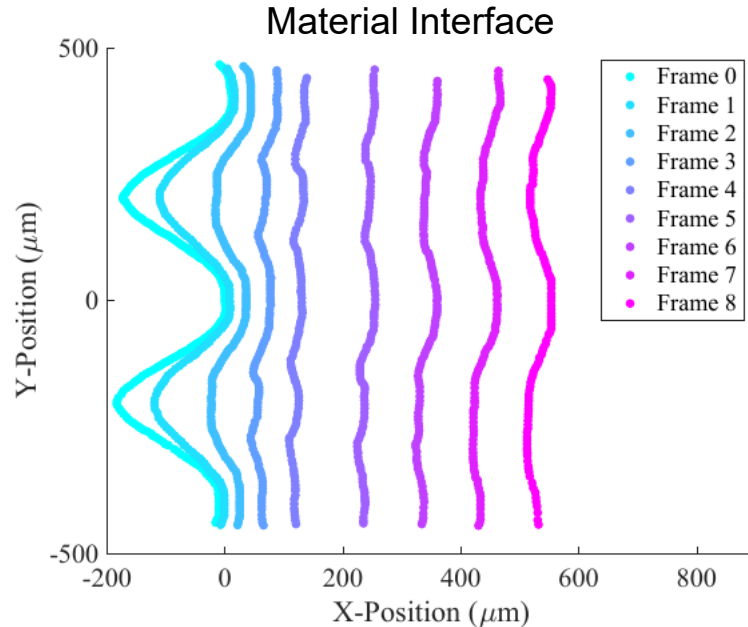


Shockwave

Impacted at 1.2 km/s and 5 GPa

# Extracted Contours

- Contour locations can be used for three evaluations:
  1. Obtaining particle velocities ( $u_p$ )
  2. Obtaining shock velocities ( $U_s$ )
  3. Obtaining shock compressed density
  4. Comparing experiment to simulation in time to find the dynamic strength of a material

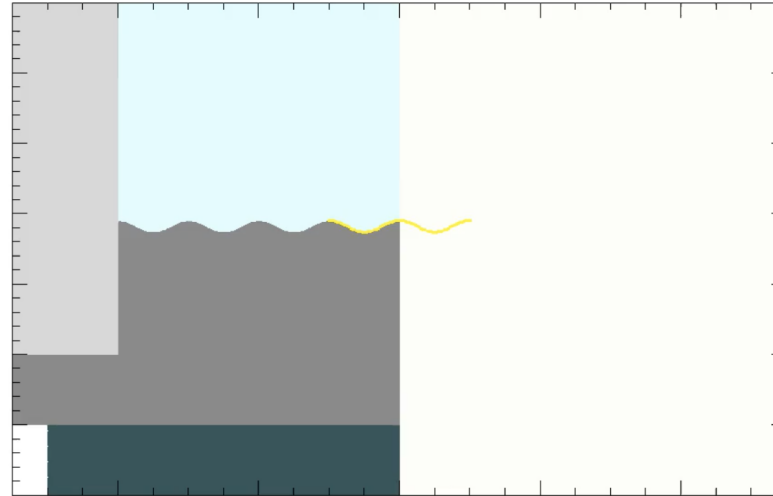


# Relating Experiment to Simulation



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- Two material specific properties that need to be accurately represented
  - Equation-of-State (EOS)
    - Mie-Grüneisen
  - Strength Model
    - Elastic Perfectly-Plastic
- These are typically done using two separate types of experiments

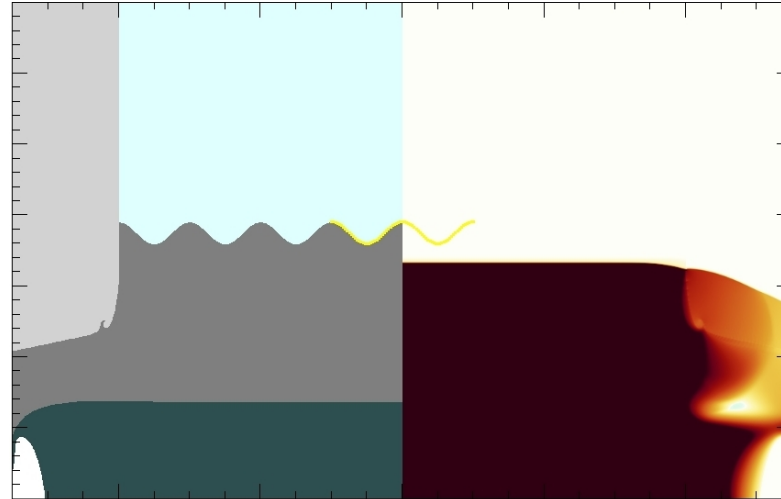


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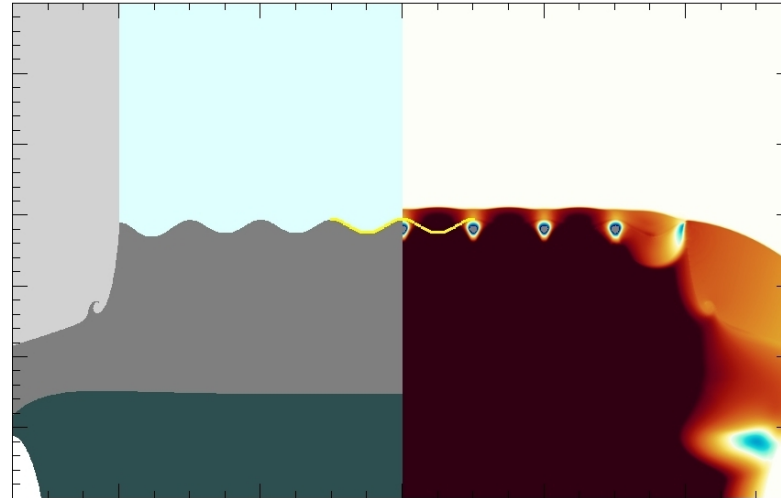


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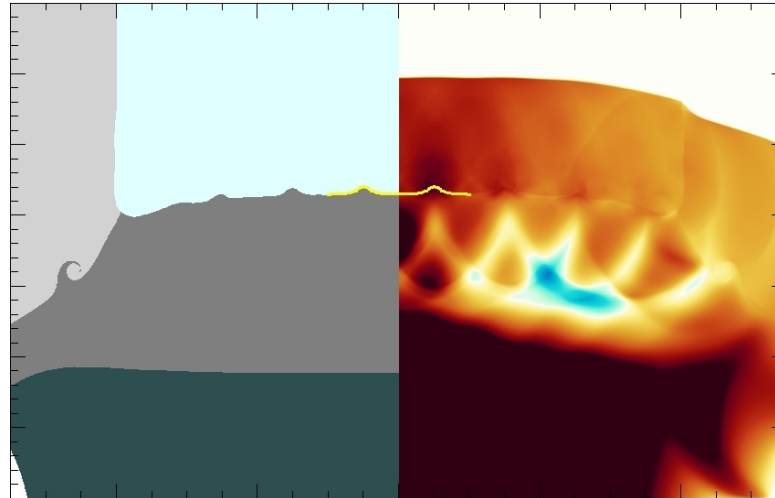


# Relating Experiment to Simulation



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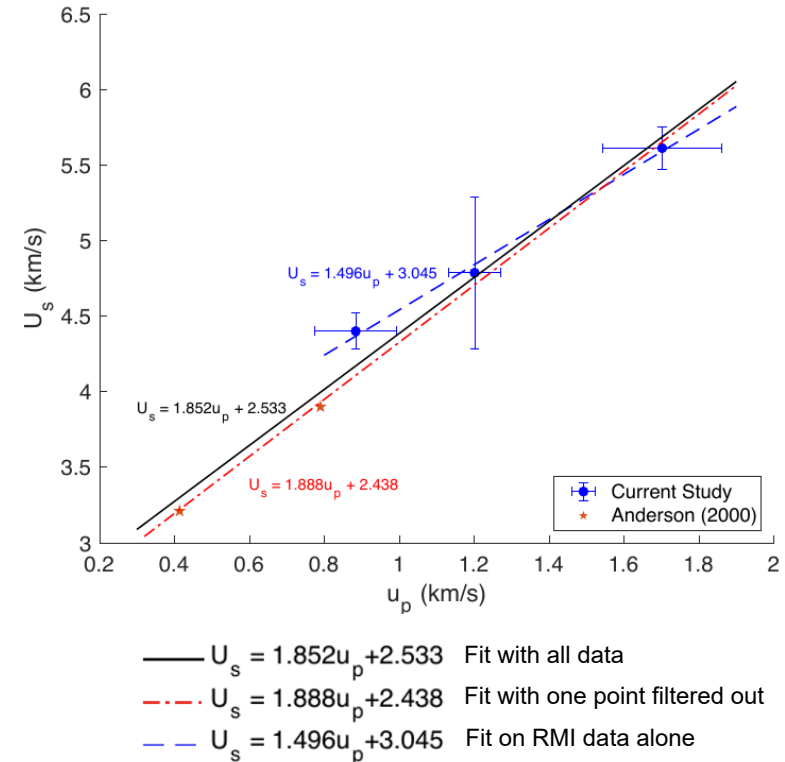
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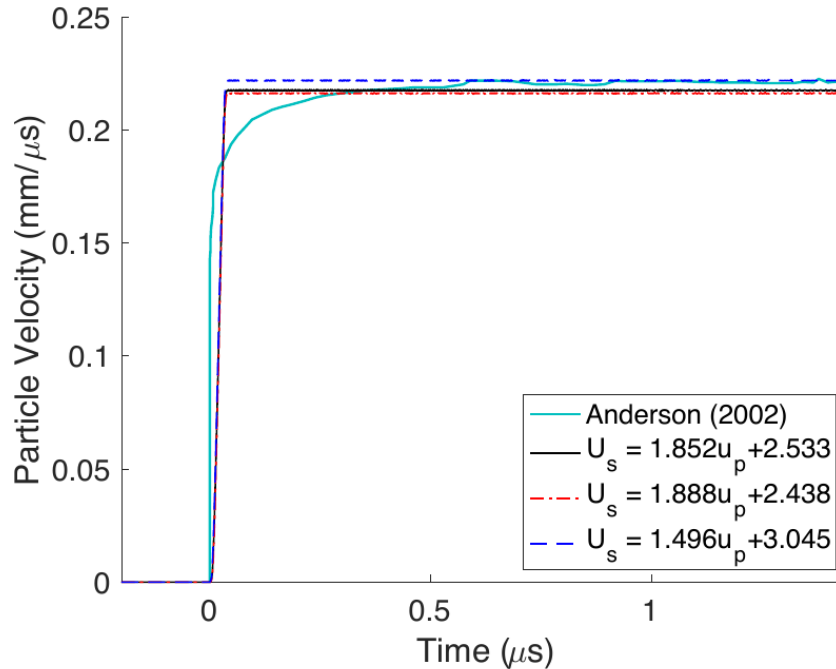
# Calibrating an Equation-of-State (EOS) from $U_s$ - $u_p$ Data



- $U_s$ - $u_p$  data tends to form a linear trend that can be approximated by the equation
  - $U_s = c_0 + su_p$
  - $c_0$  is a sound speed-like quantity in the material
  - $s$  is the slope
- Using prior literature data from Anderson (2000) in addition to the data gathered from this study, three possible  $U_s$ - $u_p$  relationships were determined



# EOS calibrated to RMI datapoints best reproduces Anderson (2002) data



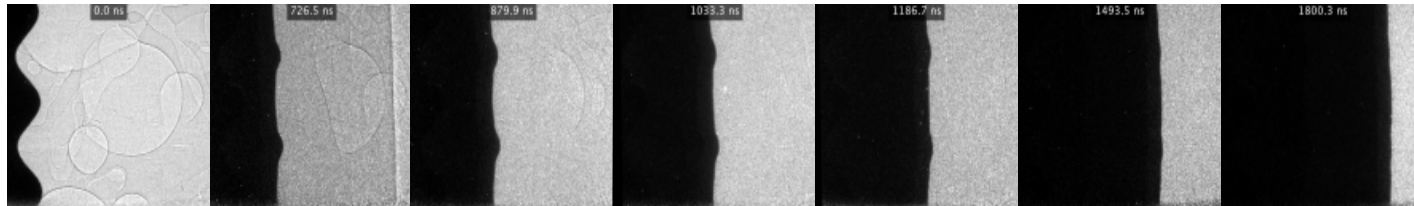
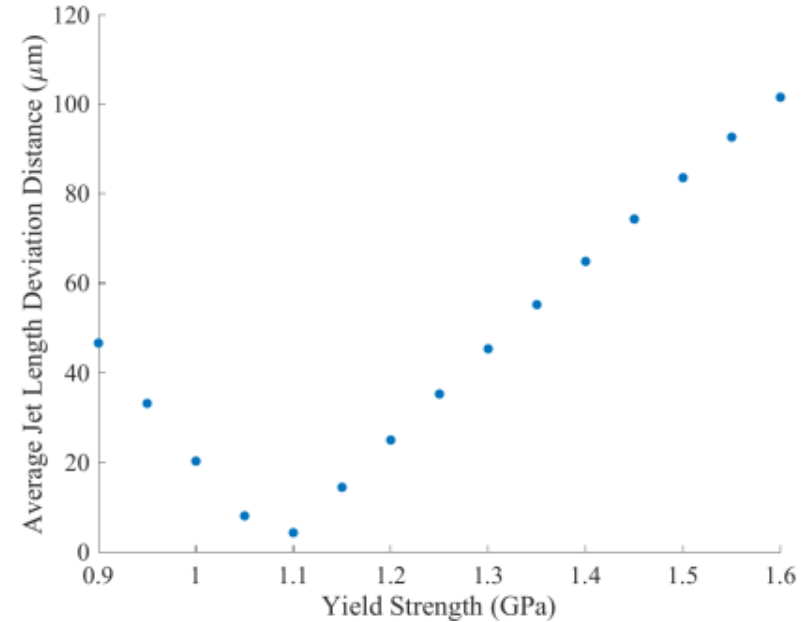
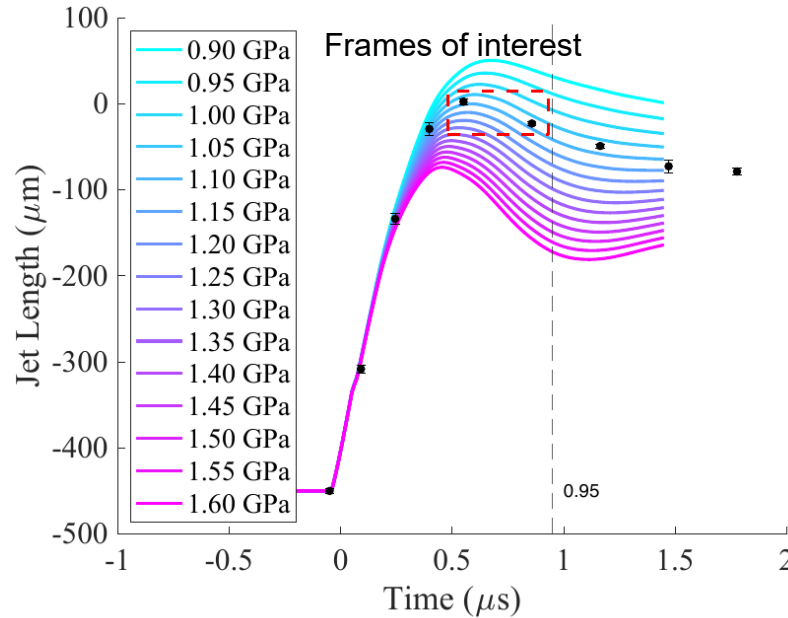
—  $U_s = 1.852u_p + 2.533$  Fit with all data  
- . -  $U_s = 1.888u_p + 2.438$  Fit with one point filtered out  
- -  $U_s = 1.496u_p + 3.045$  Fit on RMI data alone

- Simulation performed under hydrostatic conditions
- Matched the shock behavior with a 0.48% difference between simulation and experiment

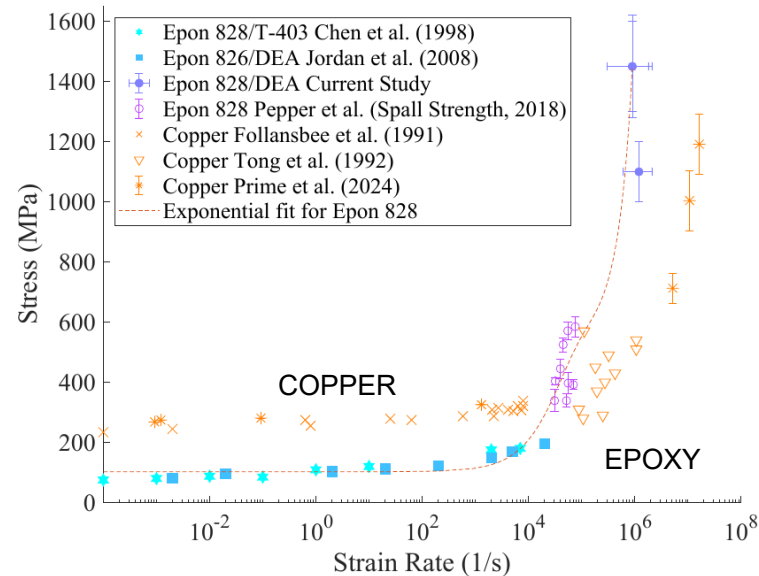
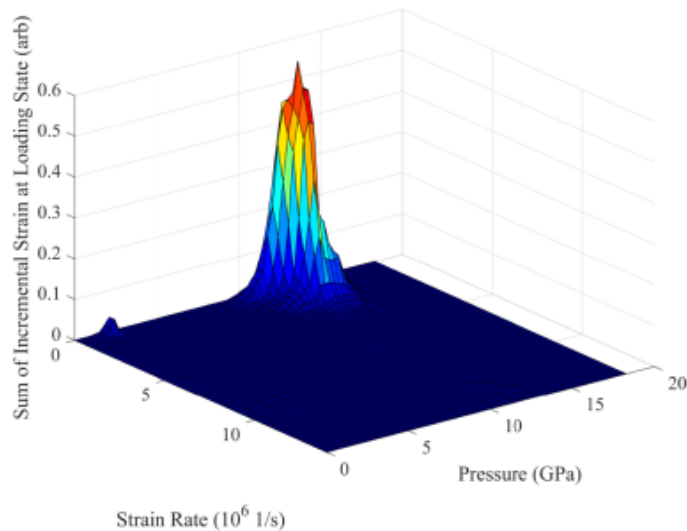
# Calibrating dynamic strength



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# Loading Conditions

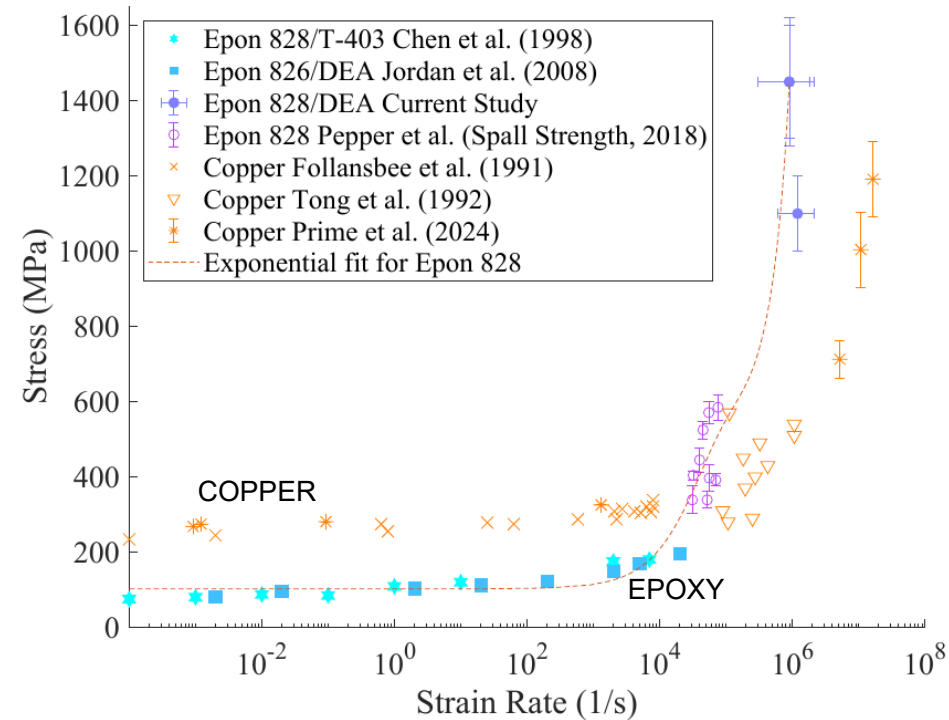


Test ID	Dynamic Strength (GPa)	Temperature (°C)	Pressure (GPa)	Strain Rate (10 <sup>6</sup> 1/s)	Plastic Strain
23-4-013	1.10 ± 0.10	233.7 ± 55.7	5.40 ± 1.20	1.20 <sup>+0.90</sup> <sub>-0.60</sub>	Peak: 0.005 Centroid: 0.269
23-4-007	1.45 ± 0.15	345 ± 55.7	8.40 ± 0.90	0.90 <sup>+1.20</sup> <sub>-0.60</sub>	Peak: 0.00 Centroid: 0.285
23-4-015	1.45 ± 0.17	484.4 ± 13.9	12.6 ± 0.9	0.90 <sup>+0.9</sup> <sub>-0.6</sub>	Peak: 0.00 Centroid: 0.421

# Conclusions



- Epon 828/DEA can exhibit dynamic strengths around 1.5 GPa at strain rates of  $10^6$  1/s which is higher than copper and comparable to high strength metals such as tool steel
- Showed a method for calibrating both the EOS and the dynamic strength off of a single type of experiment
  - This method eliminates the need for two separate types of experiments
- Contributed to the available Hugoniot data for Epon 828/DEA
- Presented a validated EOS in the 4-12 GPa Hugoniot stress range



# Acknowledgements



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Thank you!

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