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Department of  
Aerospace Engineering

# Characterizing the dynamic strength of a polymer epoxy using the Richtmyer-Meshkov Instability

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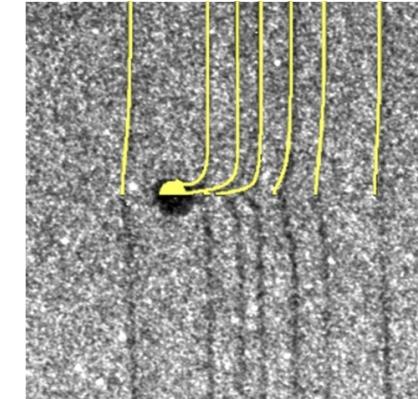
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# The Dynamic Strength of Polymers is not well characterized

- Little work done regarding strength in the shock regime
- Recent particle tracking experiments performed by Bober et al indicated that silicone has a flow strength of 500 to 750 MPa, stronger than some metals
- Epon 828 Epoxy
  - Has been previously investigated in planar impact experiments
  - Can be polymerized with a variety of curing agents
  - Many shock Hugoniot datasets in the literature fail to list curing agent
  - Often assumed that the Equation-of-State (EOS) is the same regardless of curing agent



Particle Tracking Experiments in Silicone  
[Bober et al (2019)]

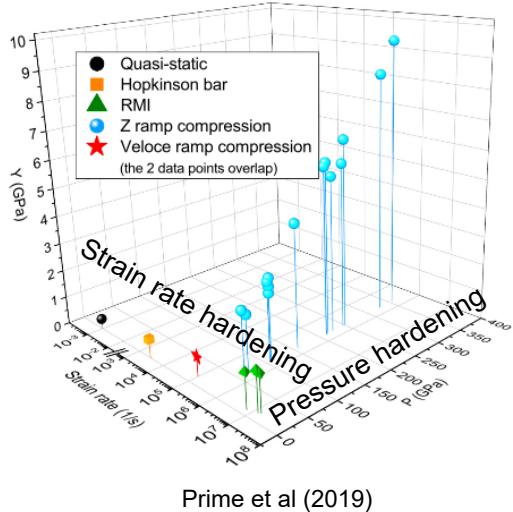
| EPOXY - Epon 828                          |              |           |       |                            |                     |         |     |   |
|---|--------------|-----------|-------|----------------------------|---------------------|---------|-----|---|
| Average $\rho_0 = 1.185 \text{ g/cm}^3$ . |              |           |       |                            |                     |         |     |   |
| Sound velocities                          | longitudinal | 2.63 km/s | shear | 1.16 km/s                  |                     |         |     |   |
| Reference                                 | Si           |           |       |                            |                     |         |     |   |
| $\rho_0$                                  | $U_s$        | $U_p$     | $P$   | $V$                        | $\rho$              | $V/V_0$ | Exp |   |
| ( $\text{g/cm}^3$ )                       | (km/s)       | (km/s)    | (GPa) | ( $\text{cm}^3/\text{g}$ ) | ( $\text{g/cm}^3$ ) |         |     |   |
| 1.182                                     | 2.263        | 0.000     | 0.000 | 8389                       | 1.182               | 1.000   | ssp | x |
| 1.184                                     | 3.285        | .370      | 1.430 | 7469                       | 1.335               | .887    | imI | o |
| 1.184                                     | 3.355        | .411      | 1.633 | 7411                       | 1.349               | .877    | imI | o |
| 1.184                                     | 3.421        | .494      | 2.001 | 7226                       | 1.384               | .856    | imI | o |
| 1.184                                     | 3.805        | .639      | 2.879 | 7028                       | 1.423               | .832    | imI | o |

[LASL Marsh Compendium]

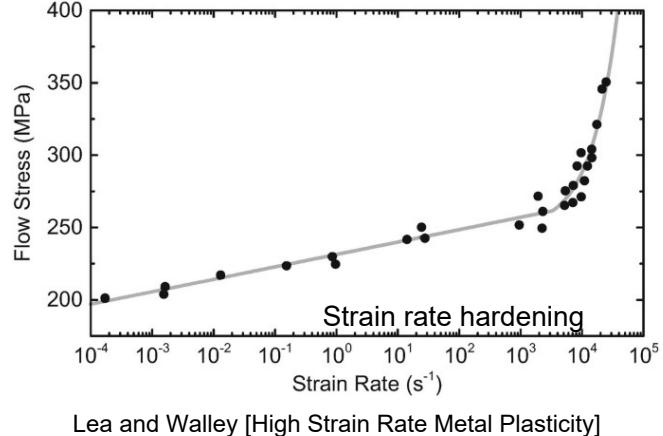
# Pressure and Strain Rate Hardening



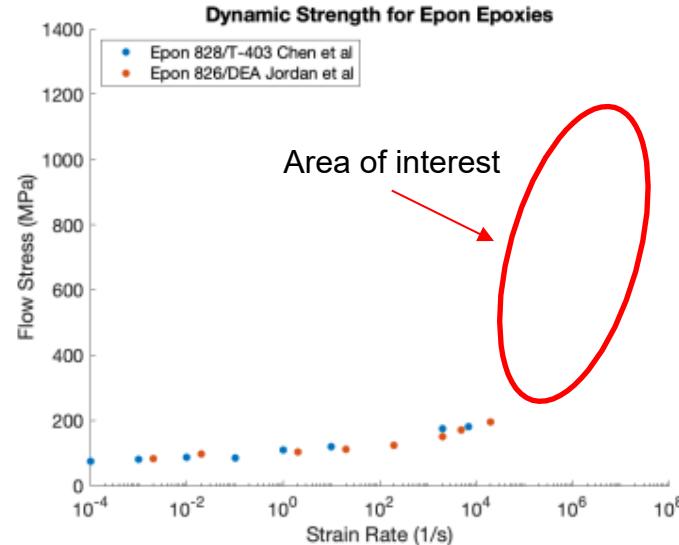
Tantalum



Copper

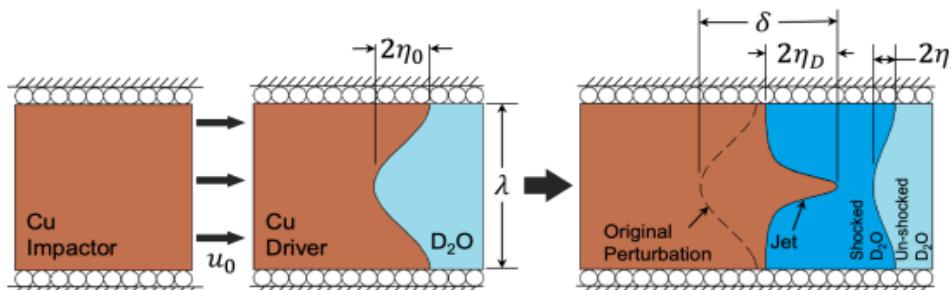


Epoxy

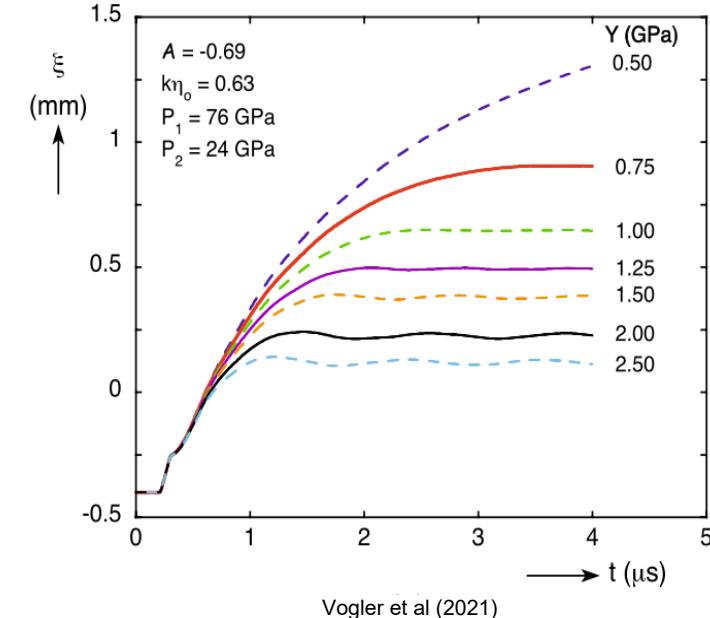


# Tamped Richtmyer-Meshkov Instability (RMI) Experiments

- Used for constitutive model calibration
- Experimental behavior is compared to simulations to calibrate the material strength
- RMI inversion behavior is affected by
  - Driver strength,  $Y_p$
  - Tamper strength,  $Y_T$
  - Shock stress,  $\sigma$
  - Atwood Number,  $A = \frac{\rho_T - \rho_D}{\rho_T + \rho_D}$
  - Corrugation aspect ratio  $k\eta_0$



Olles et al (2021)

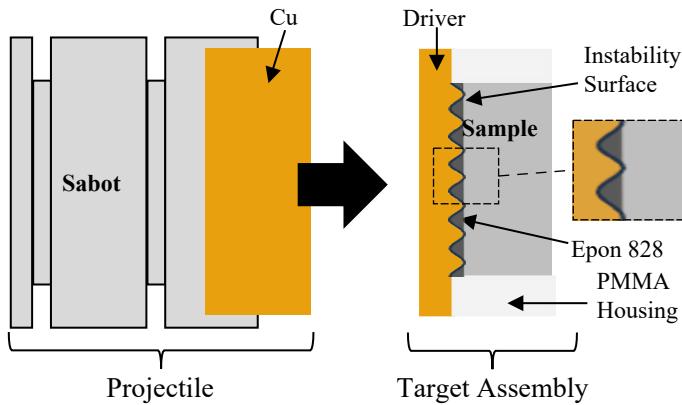
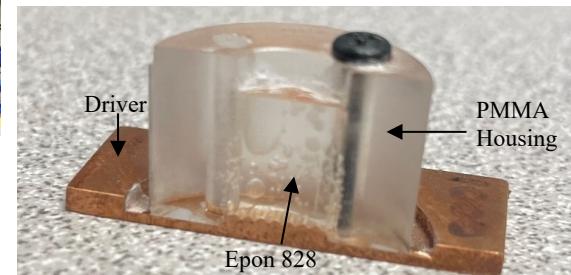
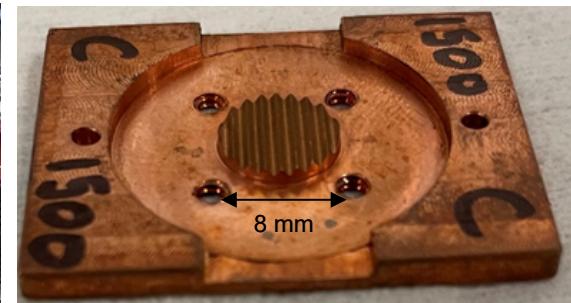


Vogler et al (2021)

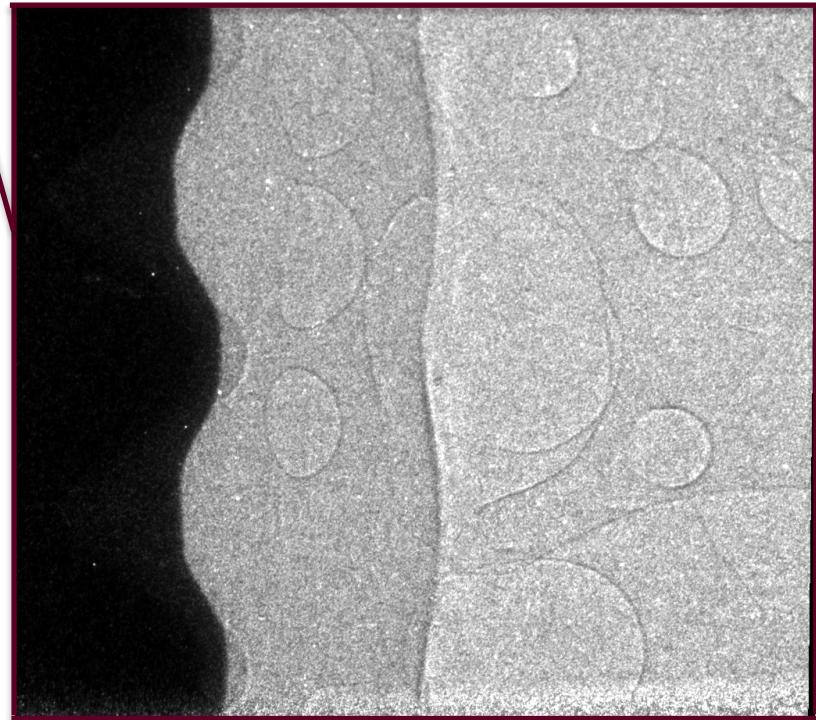
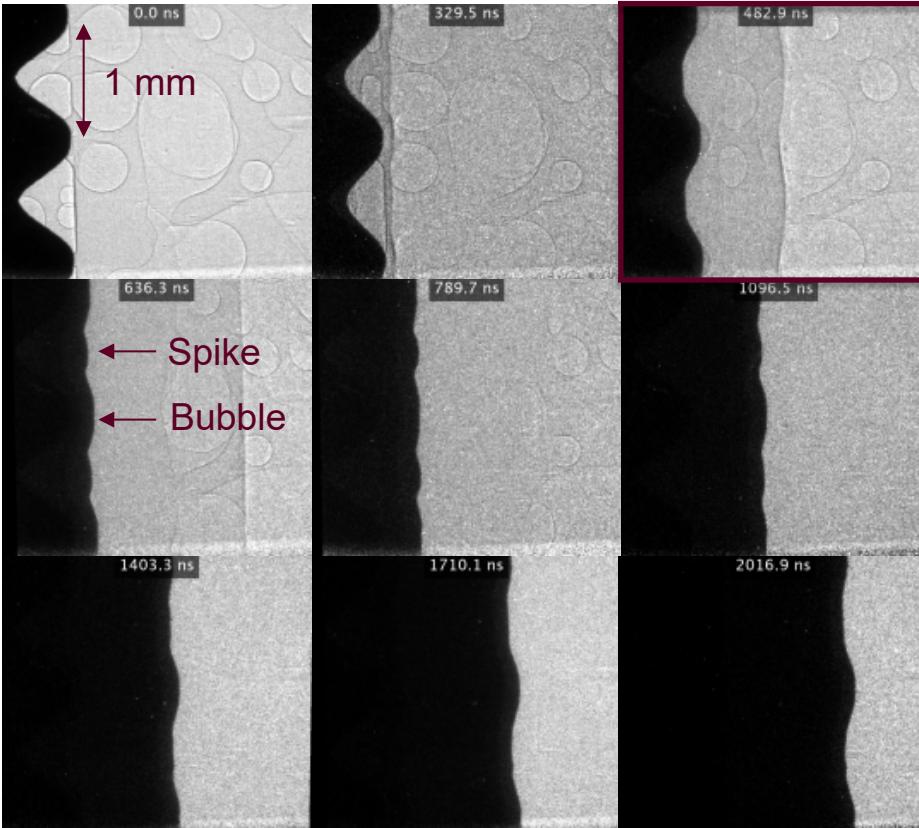
# Experimental Details and Setup



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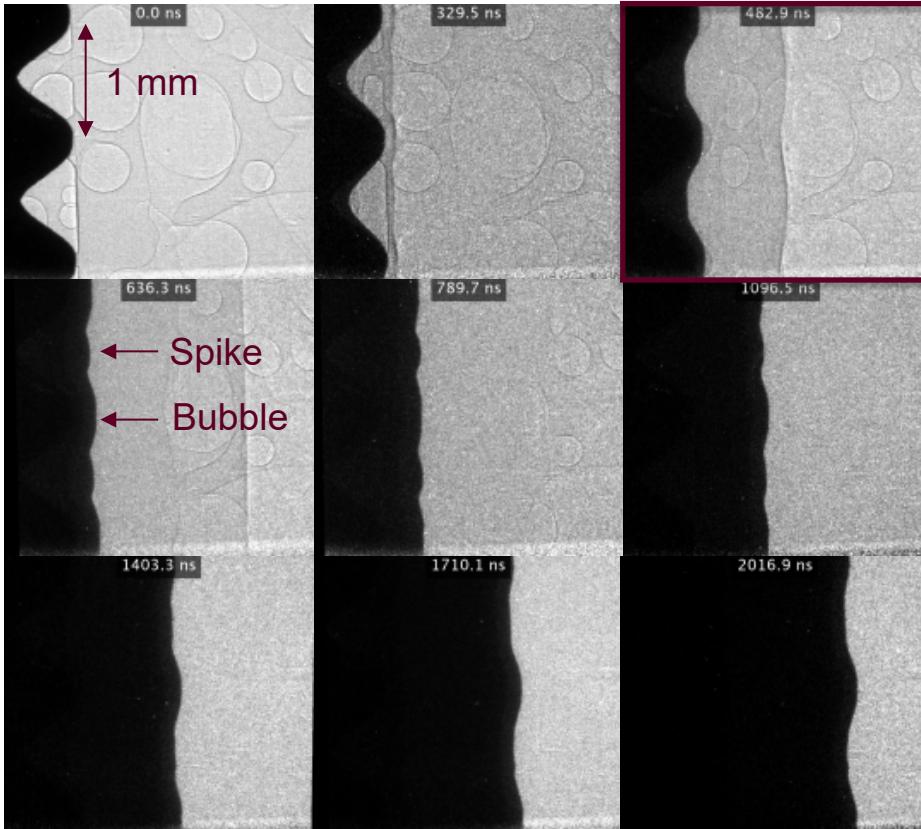


# Evaluating Radiography Data

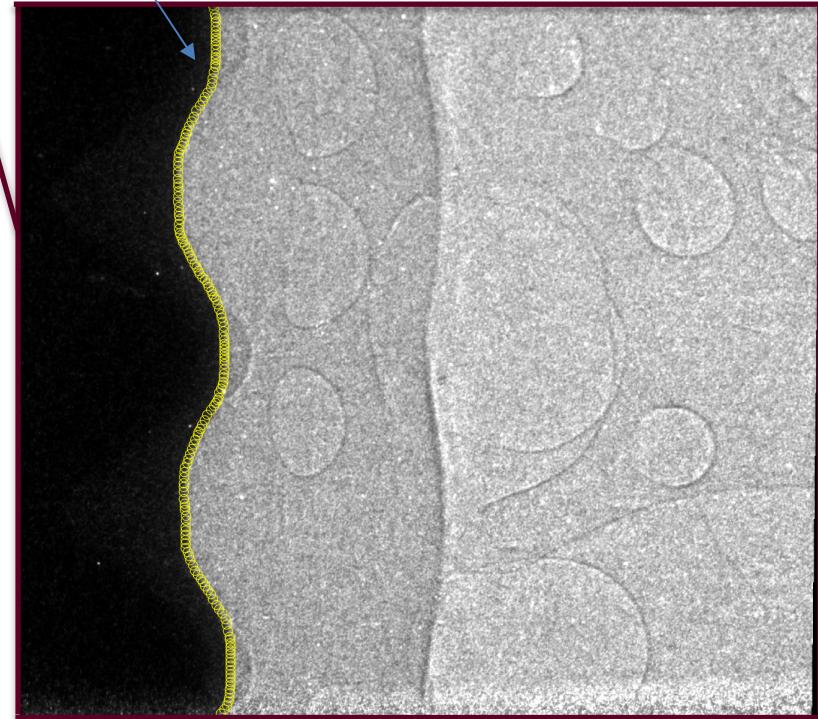


Impacted at 1.2 km/s and 5 GPa

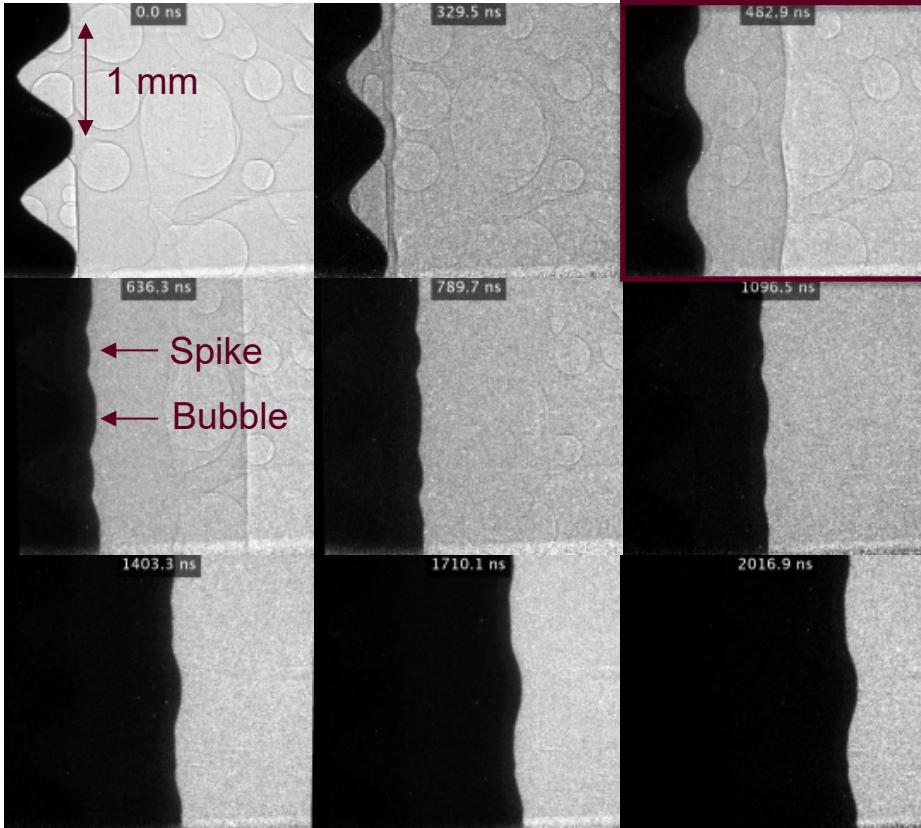
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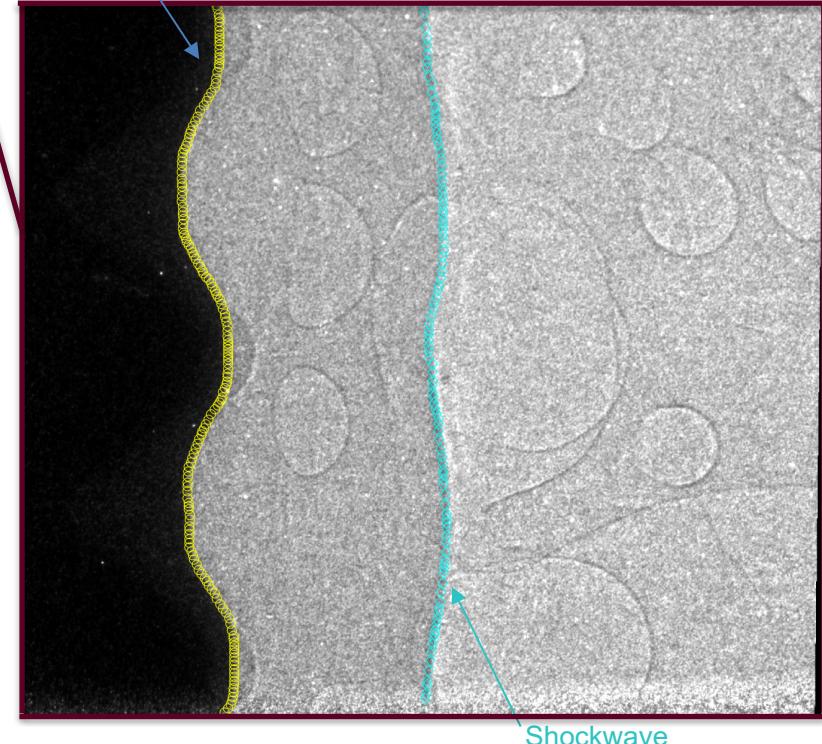
Cu – Epon828  
Contact Surface



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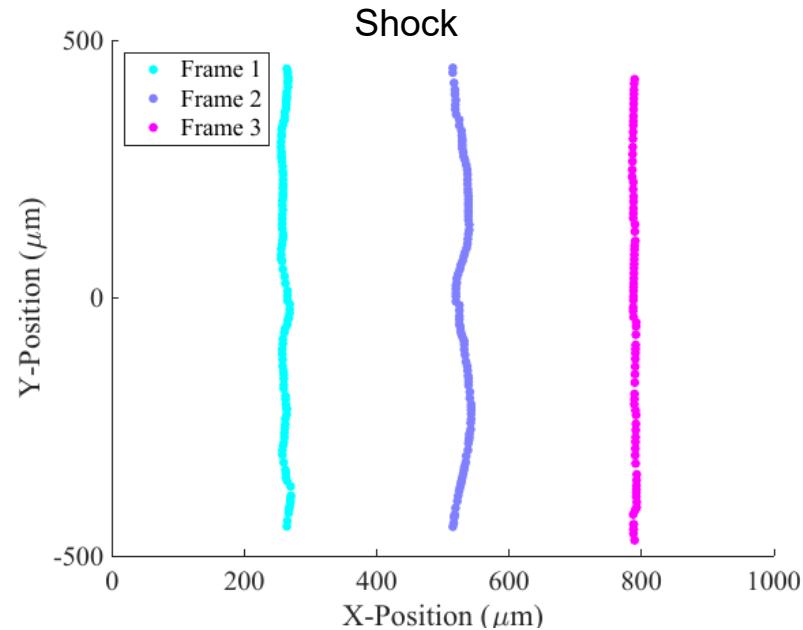
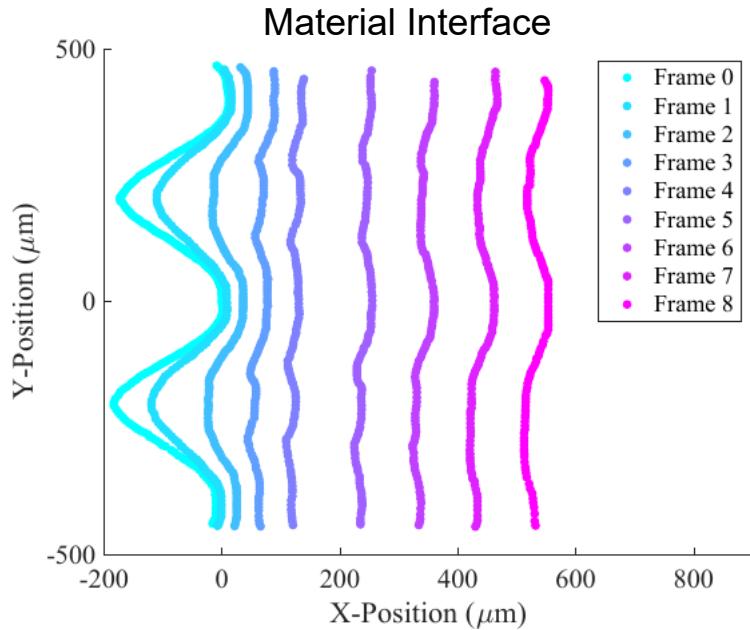


Impacted at 1.2 km/s and 5 GPa

# Extracted Contours

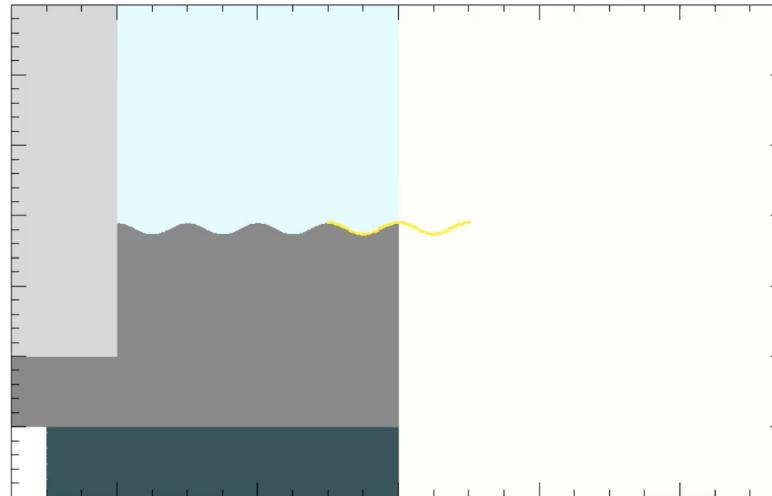
- Contour locations can be used for three evaluations:

1. Obtaining particle velocities ( $u_p$ )
2. Obtaining shock velocities ( $U_s$ )
3. Obtaining shock compressed density
4. Comparing experiment to simulation in time to find the dynamic strength of a material



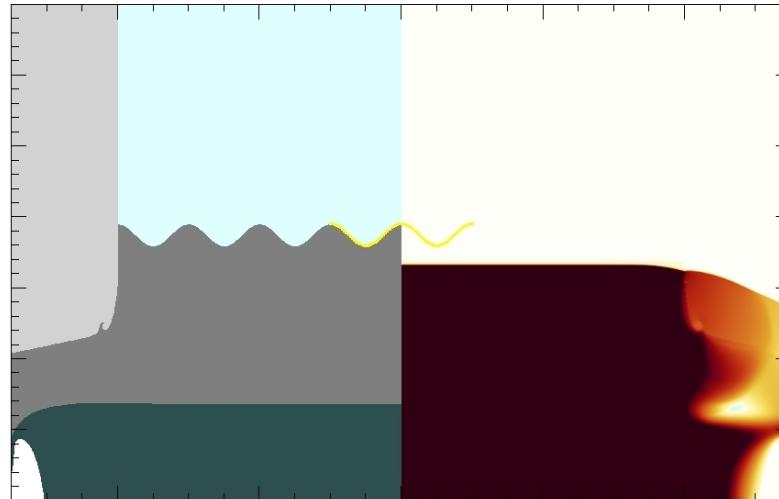
# Relating Experiment to Simulation

- Two material specific properties that need to be accurately represented
  - Equation-of-State (EOS)
    - Mie-Grüneisen
  - Strength Model
    - Elastic Perfectly-Plastic
- These are typically done using two separate types of experiments



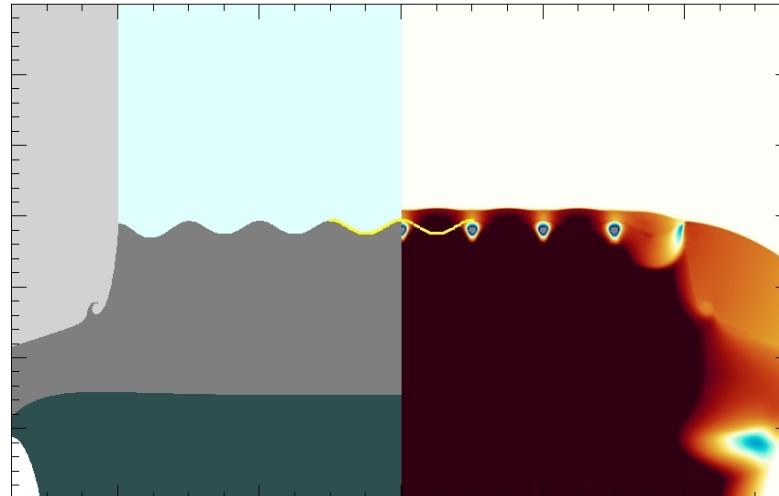
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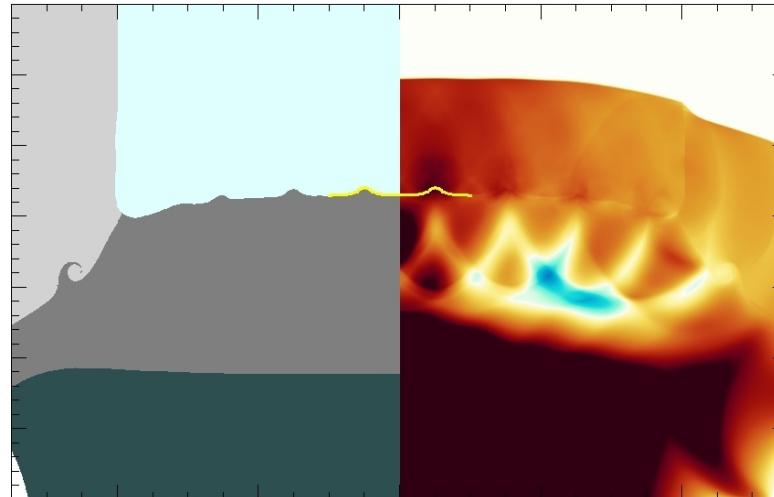
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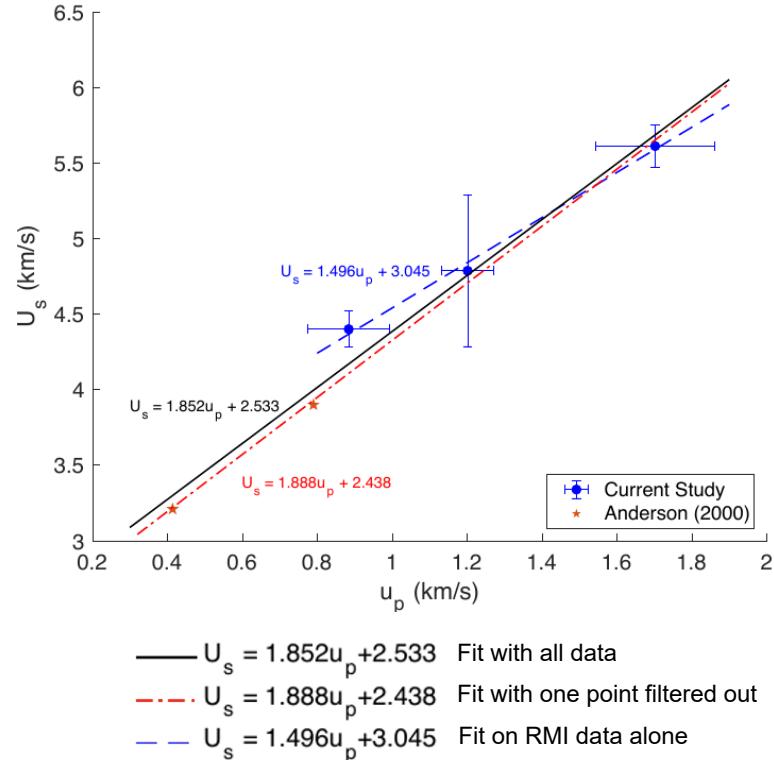
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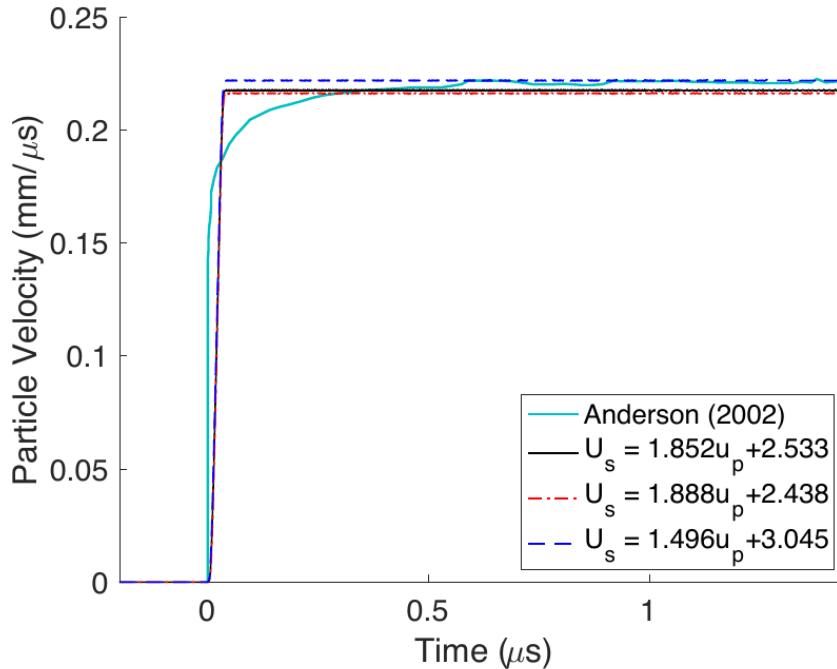


# Calibrating an Equation-of-State (EOS) from $U_s$ - $u_p$ Data

- $U_s$ - $u_p$  data tends to form a linear trend that can be approximated by the equation
  - $U_s = c_0 + su_p$
  - $c_0$  is a sound speed-like quantity in the material
  - $s$  is the slope
- Using prior literature data from Anderson (2000) in addition to the data gathered from this study, three possible  $U_s$ - $u_p$  relationships were determined



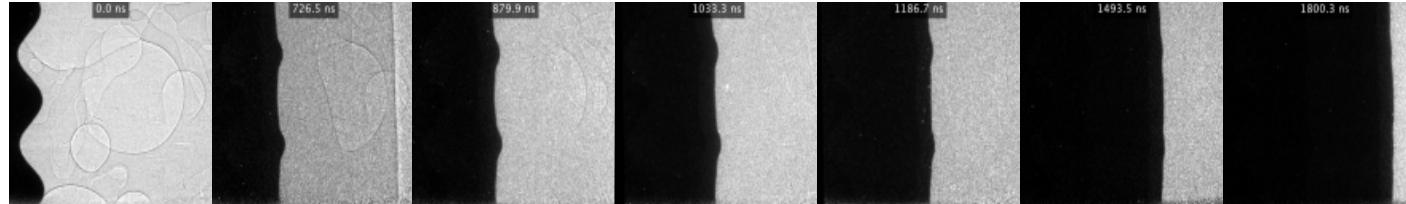
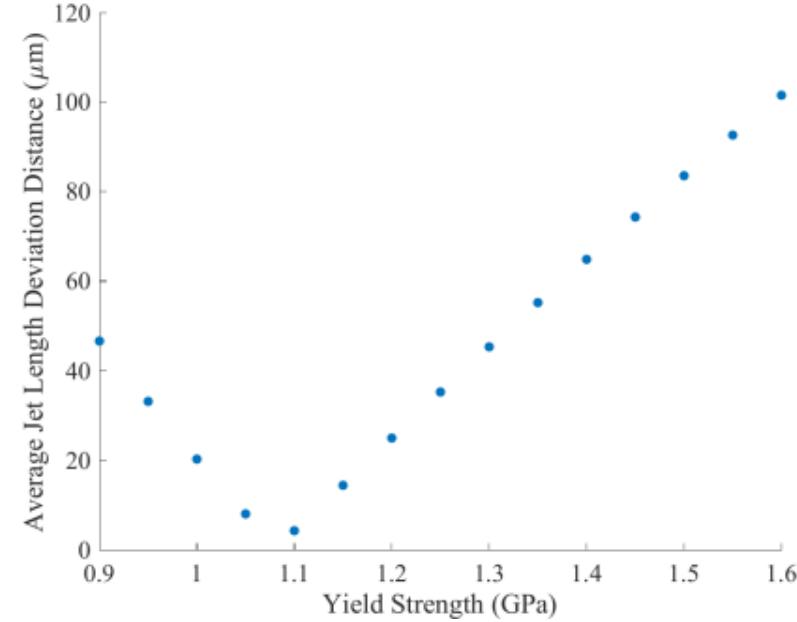
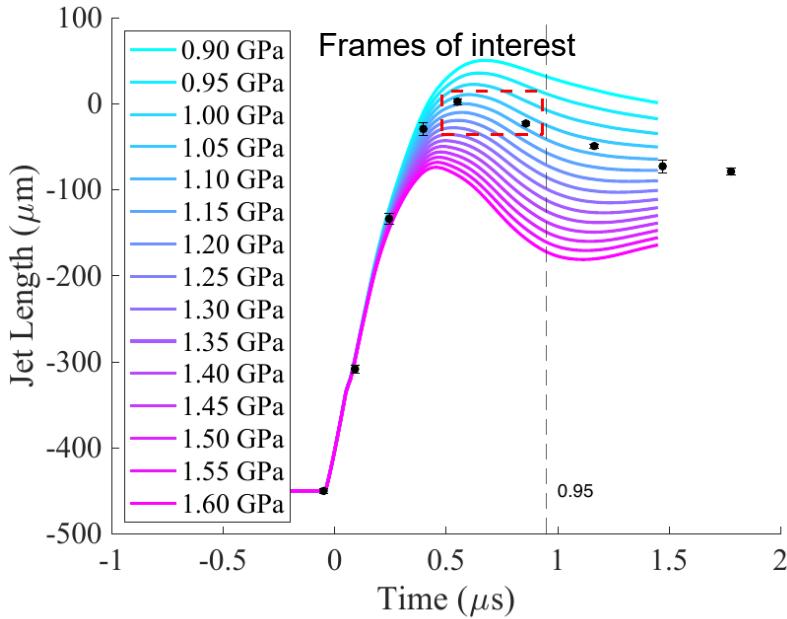
# EOS calibrated to RMI datapoints best reproduces Anderson (2002) data



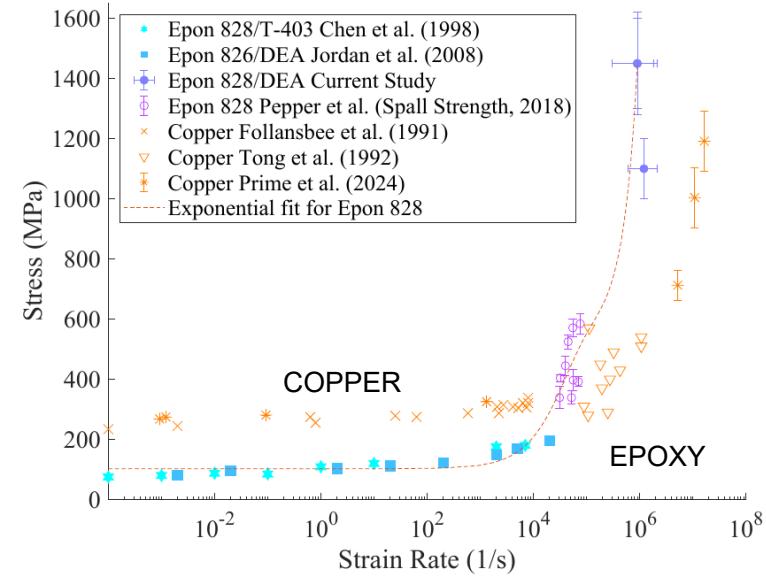
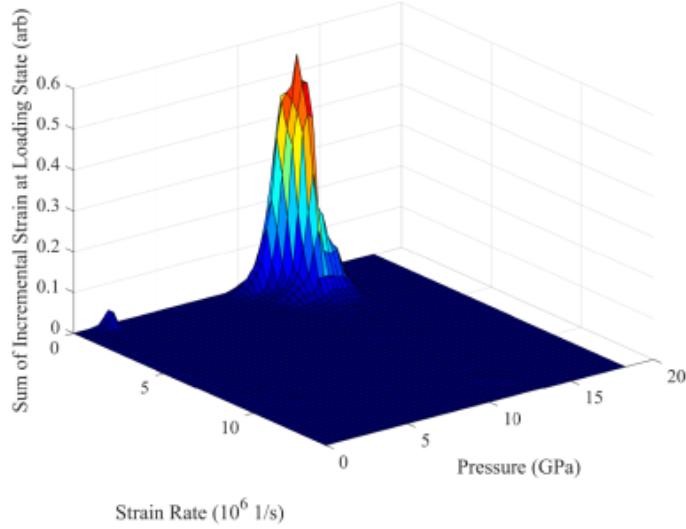
—  $U_s = 1.852u_p + 2.533$  Fit with all data  
- - -  $U_s = 1.888u_p + 2.438$  Fit with one point filtered out  
- - -  $U_s = 1.496u_p + 3.045$  Fit on RMI data alone

- Simulation performed under hydrostatic conditions
- Matched the shock behavior with a 0.48% difference between simulation and experiment

# Calibrating dynamic strength



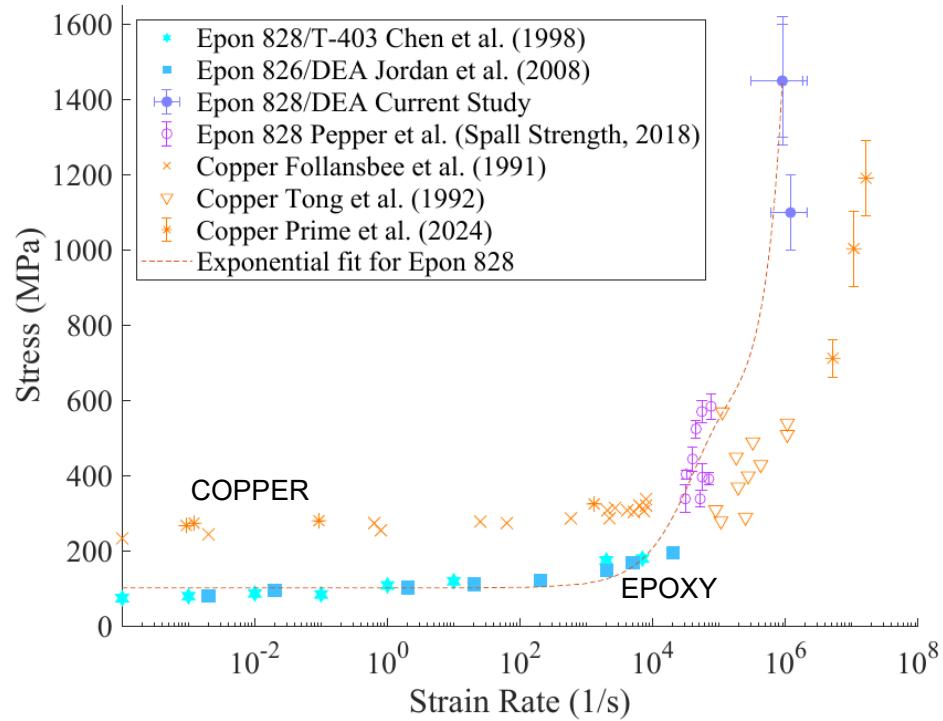
# Loading Conditions



| Test ID  | Dynamic Strength (GPa) | Temperature (°C) | Pressure (GPa)  | Strain Rate ( $10^6$ 1/s) | Plastic Strain                 |
|----------|------------------------|------------------|-----------------|---------------------------|--------------------------------|
| 23-4-013 | $1.10 \pm 0.10$        | $233.7 \pm 55.7$ | $5.40 \pm 1.20$ | $1.20^{+0.90}_{-0.60}$    | Peak: 0.005<br>Centroid: 0.269 |
| 23-4-007 | $1.45 \pm 0.15$        | $345 \pm 55.7$   | $8.40 \pm 0.90$ | $0.90^{+1.20}_{-0.60}$    | Peak: 0.00<br>Centroid: 0.285  |
| 23-4-015 | $1.45 \pm 0.17$        | $484.4 \pm 13.9$ | $12.6 \pm 0.9$  | $0.90^{+0.9}_{-0.6}$      | Peak: 0.00<br>Centroid: 0.421  |

# Conclusions

- Epon 828/DEA can exhibit dynamic strengths around 1.5 GPa at strain rates of  $10^6$  1/s which is higher than copper and comparable to high strength metals such as tool steel
- Showed a method for calibrating both the EOS and the dynamic strength off of a single type of experiment
  - This method eliminates the need for two separate types of experiments
- Contributed to the available Hugoniot data for Epon 828/DEA
- Presented a validated EOS in the 4-12 GPa Hugoniot stress range



# Acknowledgements

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