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# Technical basis for fatigue crack growth rules in gaseous hydrogen (B31.12 CC220 and BPVC VIII-3 CC2938-2)

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# Background

- ASME BPVC uses a basic Paris Law (power law) formulation to characterize fatigue crack growth rate:

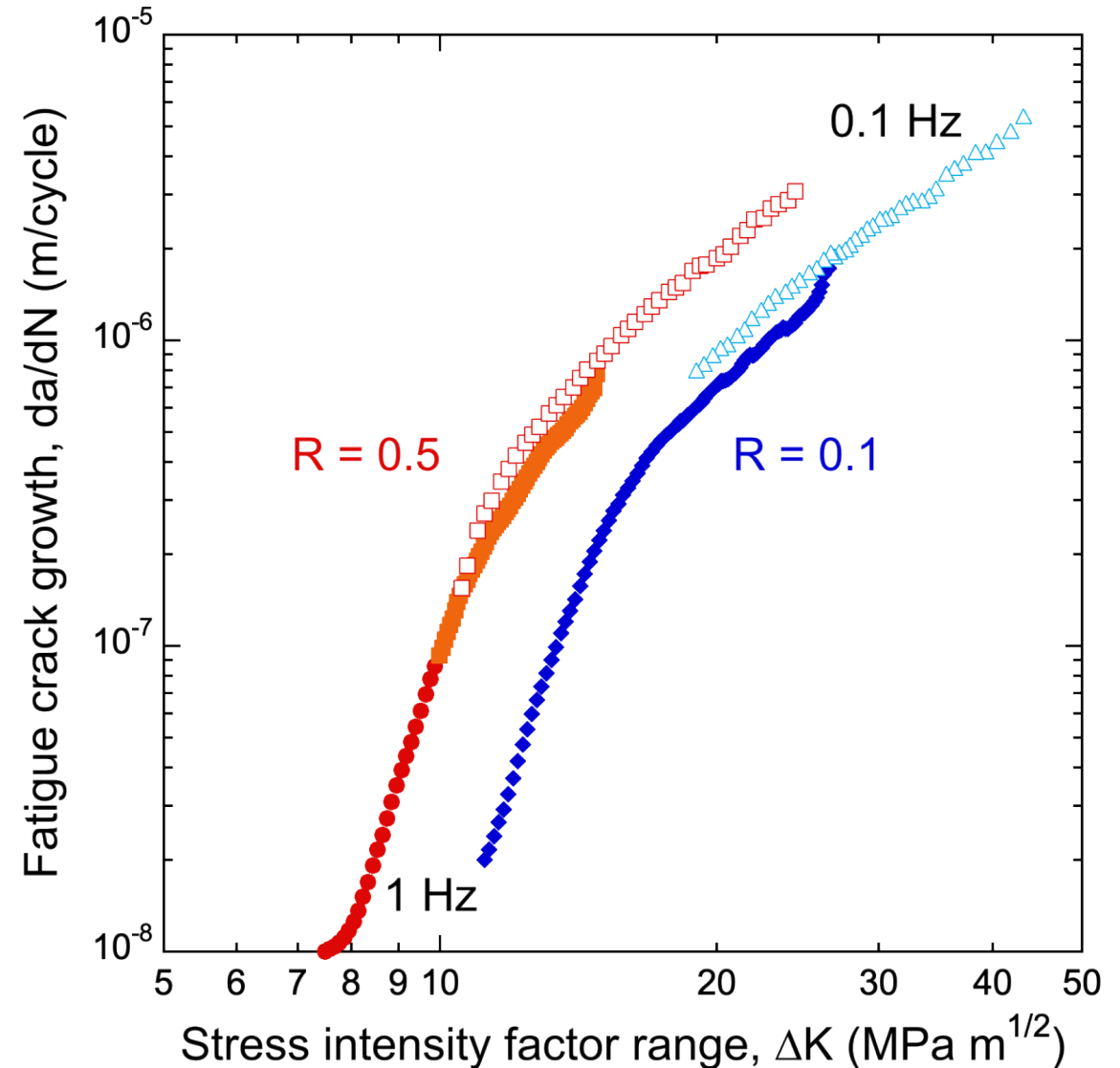
*Basic Paris Law form*

$$\frac{da}{dN} = C \underbrace{f(R_k)}_{\text{stress ratio dependence}} \underbrace{\Delta K^m}_{\text{power law}}$$

*constant*

# Background

- In high-pressure gaseous hydrogen, a single power law formulation is insufficient to capture the observed fatigue crack growth behavior over relevant range of  $\Delta K$
- Additionally, a relatively large dependence on stress ratio ( $R$ ) is observed



# Background

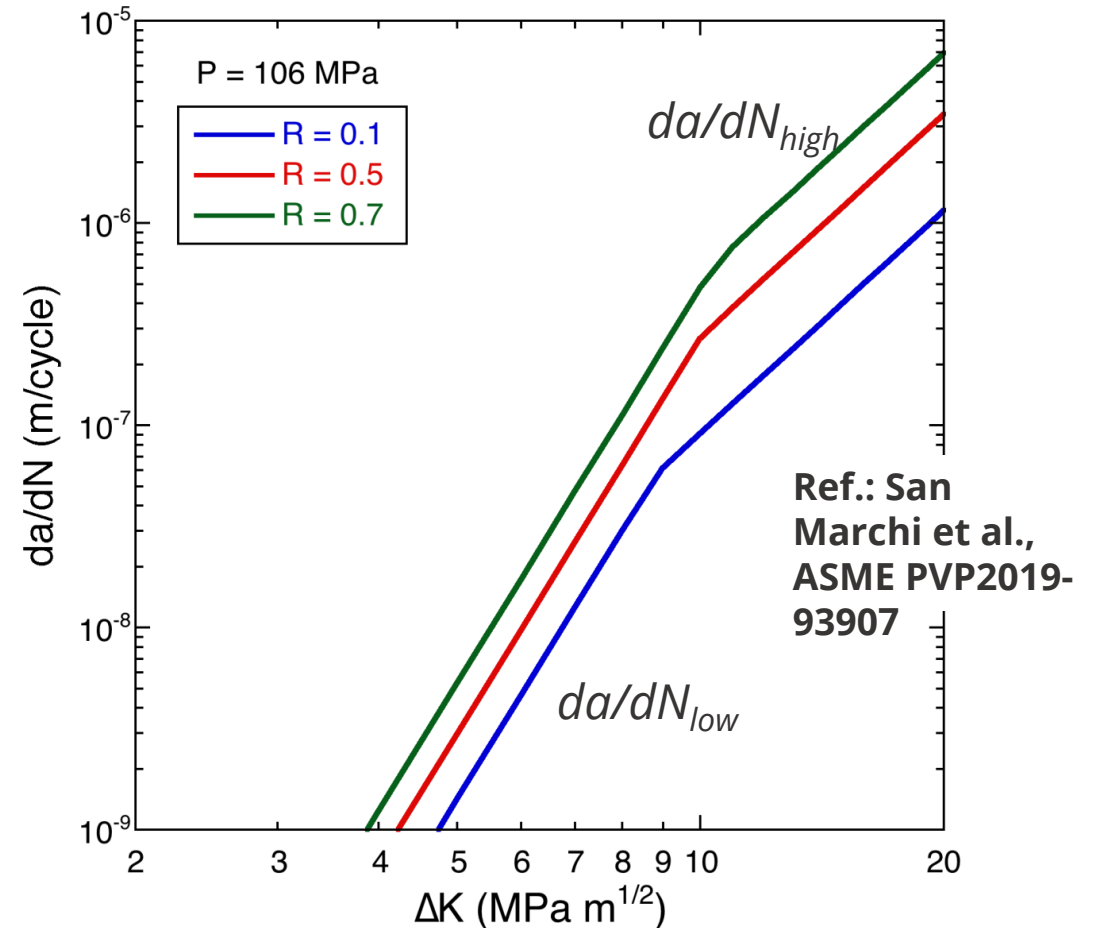
- BPVC VIII-3 Code Case 2938 adopted a two-part power-law formulation to capture observed rate

$$\frac{da}{dN} = C \underbrace{\left[ \frac{1+C_H R}{1-R} \right]}_{\text{stress ratio dependence}} \underbrace{\Delta K^m}_{\text{power law}}$$

constant
stress ratio dependence
power law

	$da/dN_{low}$	$da/dN_{high}$
$C$ (m/cycle)	$3.5 \times 10^{-14}$	$1.5 \times 10^{-11}$
$C_H$	0.4286	2.00
$m$	6.5	3.66

$\Delta K$  units: MPa  
m<sup>1/2</sup>



- Specifically developed for
- Pressure of 106 MPa
  - Quenched and tempered, pressure vessel steels



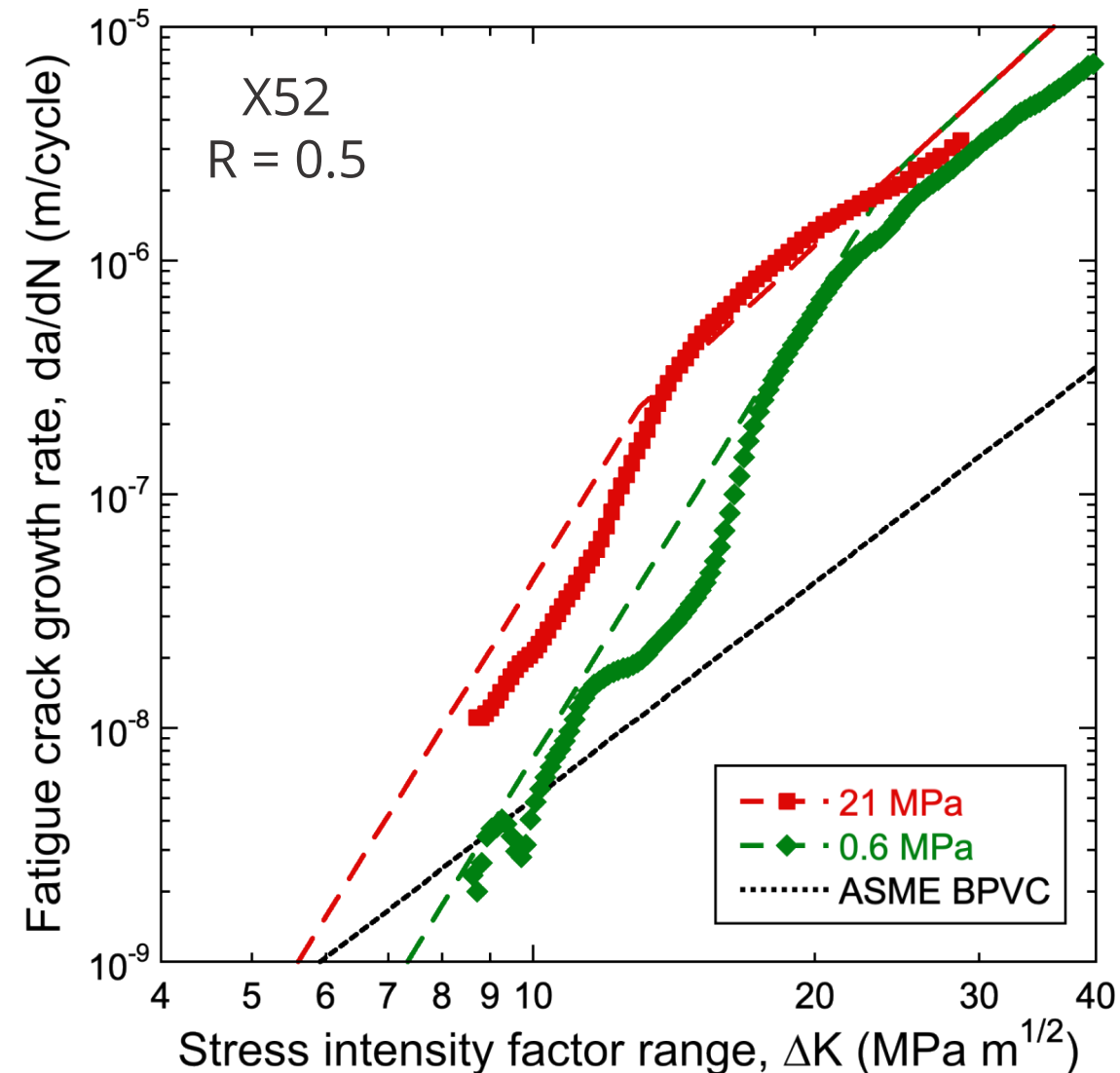
# Background and Motivation

Two important observations from extensive testing in gaseous hydrogen

1. Line pipe steels show similar behavior as PV steels
2. Pressure affects lower domain of crack growth but not upper domain

Motivation: can formulation be adapted to capture:

1. other steels and
2. pressure effects?





# Formulation of Fatigue Design Curves (FDCs) for steels in hydrogen service

Proposed generic form to include pressure dependence:

$$\frac{da}{dN} = C \underbrace{f(R_k) \Delta K^m}_{\text{basic ASME form}} f(P)$$

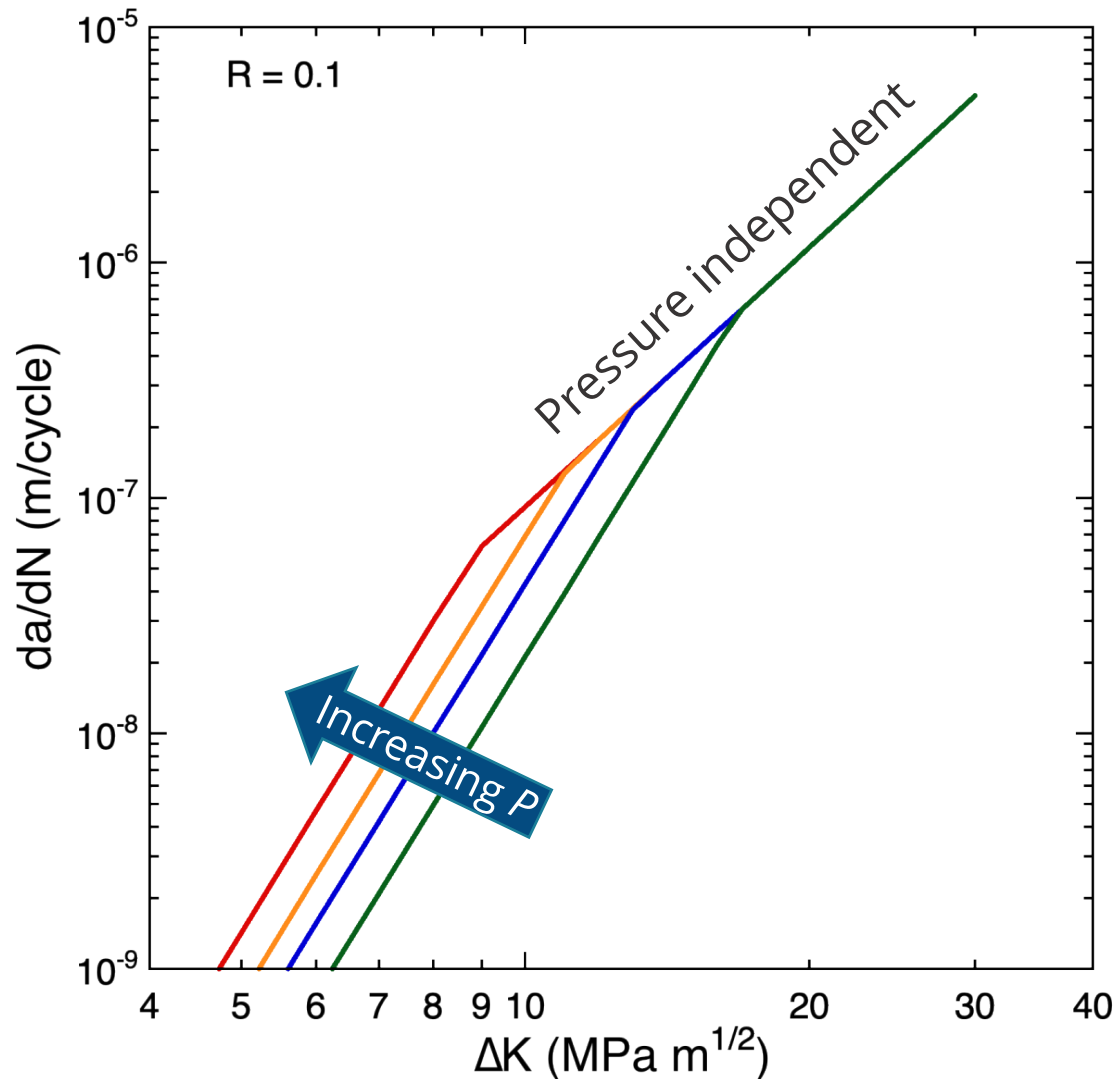
**Pressure term**

	$da/dN_{low}$	$da/dN_{high}$
$C$ (m/cycle)	$3.5 \times 10^{-14}$	$1.5 \times 10^{-11}$
$C_H$	0.4286	2.00
$m$	6.5	3.66
$f(P)$	$g(P)$	1

$$f(R_k) = \left[ \frac{1 + C_H R}{1 - R} \right] \quad \text{from BPVC VIII.3 CC 2938}$$

$$g(P) = \left( \frac{f}{f_{ref}} \right)^{1/2} \quad \text{Phenomenological form based on thermodynamics}$$

# Idealized framework to capture pressure effect



Low  $\Delta K$ : *pressure dependent*

$$\frac{da}{dN} = C \left[ \frac{1+C_H R}{1-R} \right] \Delta K^m g(P)$$

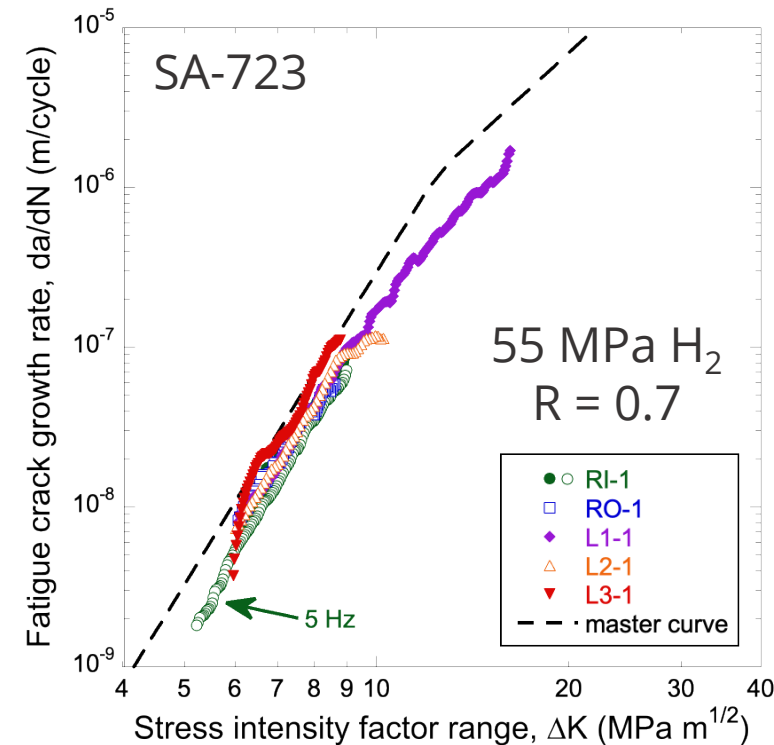
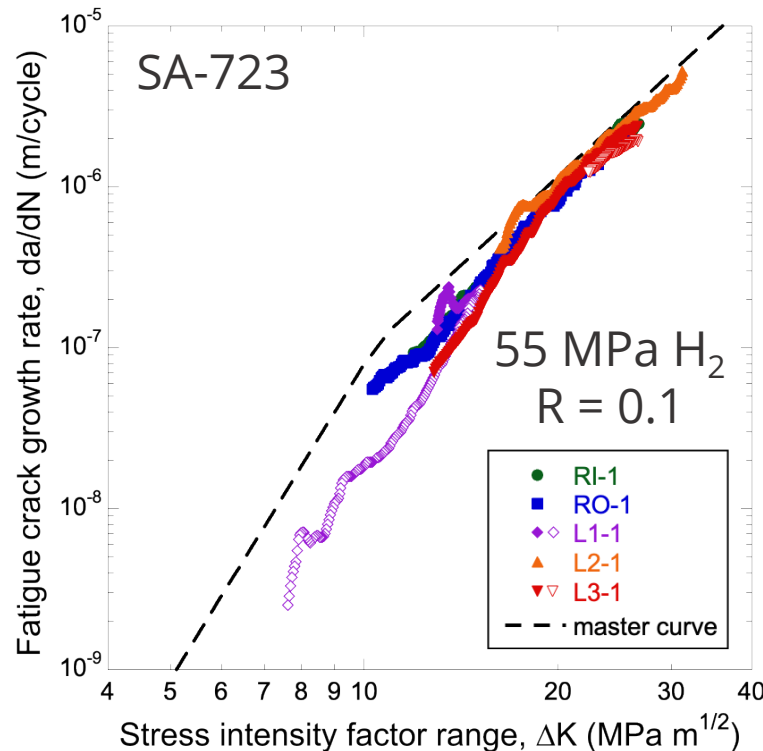
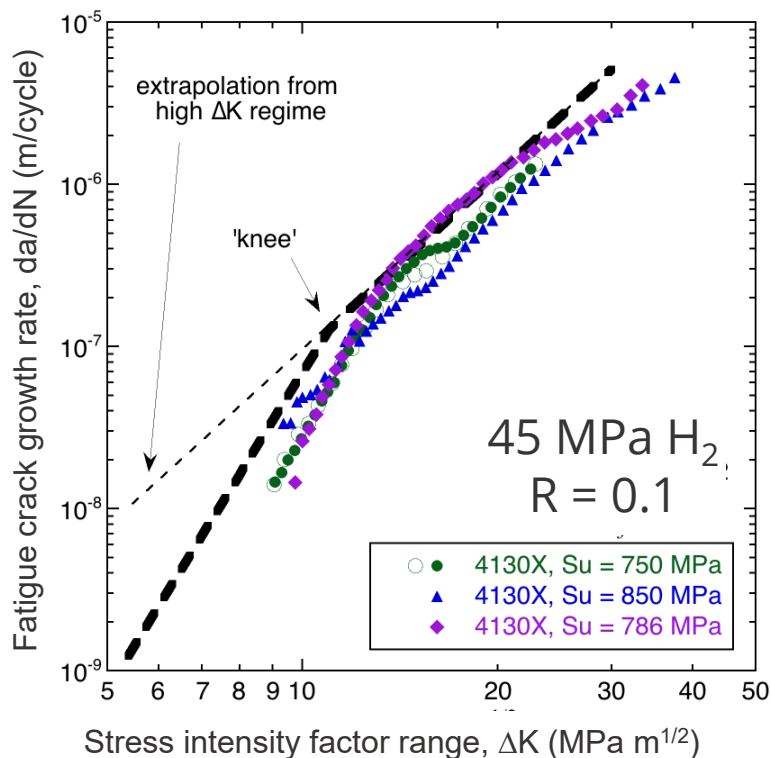
High  $\Delta K$ : *pressure independent*

$$\frac{da}{dN} = C \left[ \frac{1+C_H R}{1-R} \right] \Delta K^m$$



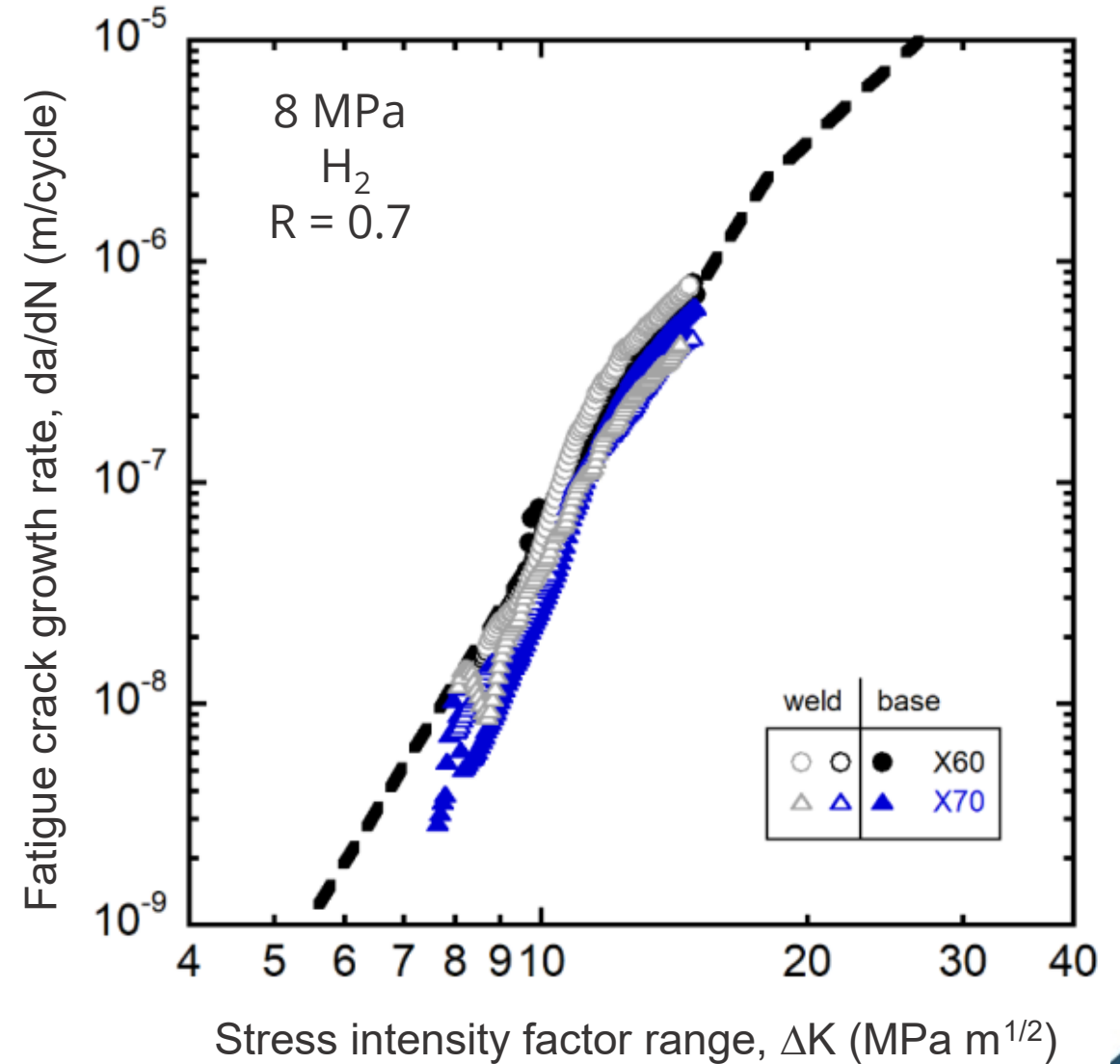
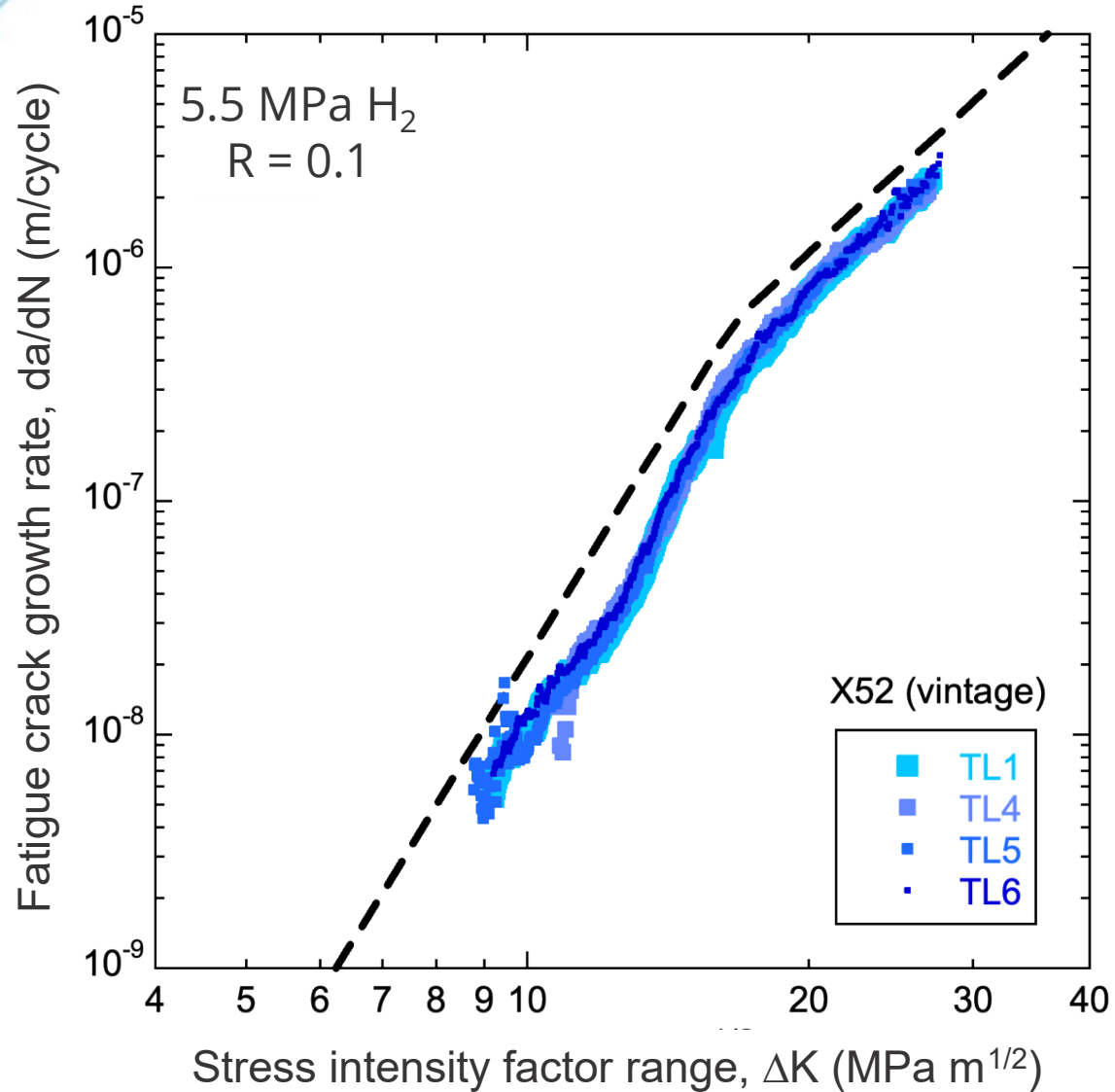
# Fatigue crack growth for PV steels

- Note capturing the transition region (*i.e.*, 'below' the knee) is important for design in the low  $\Delta K$  regime
- SA-723 designations (RI, RO, L) represent different positions and orientations



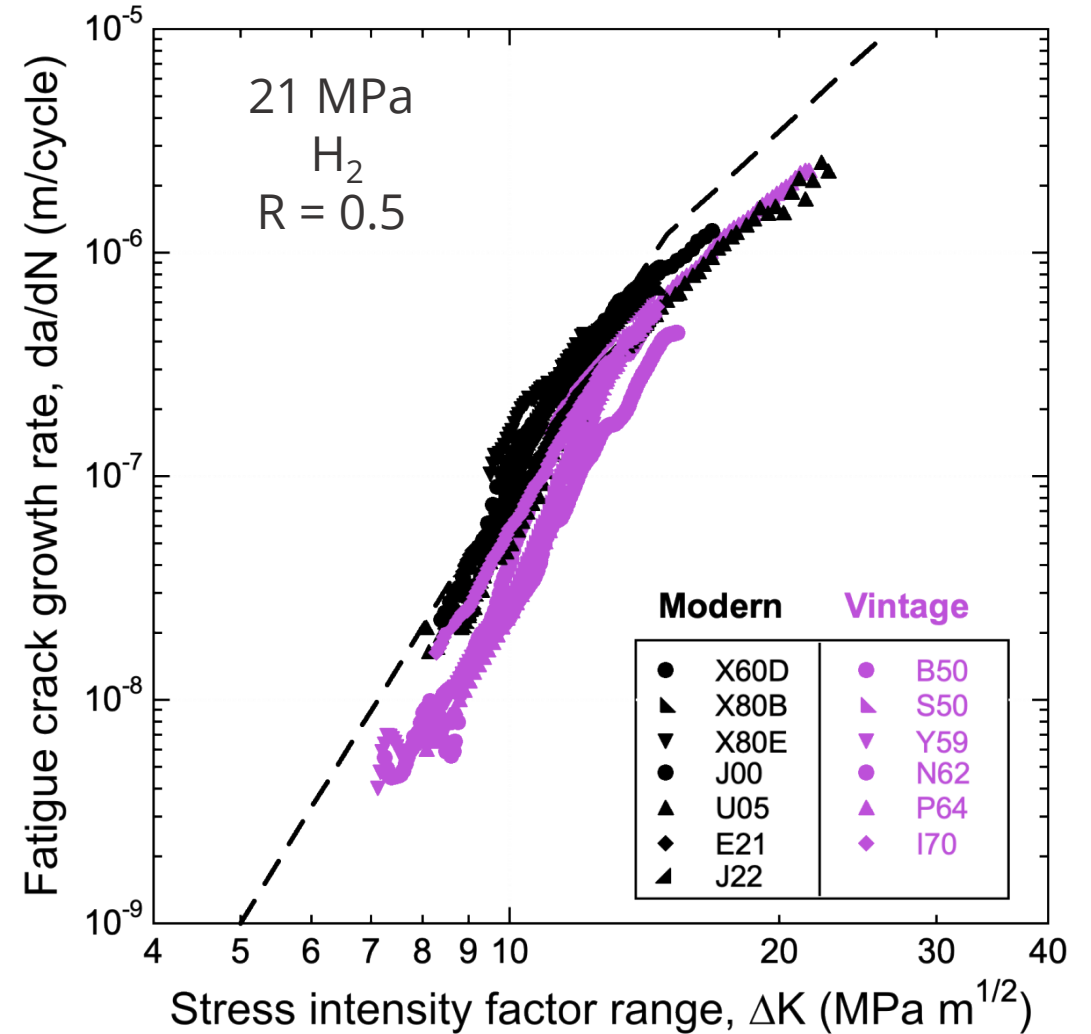
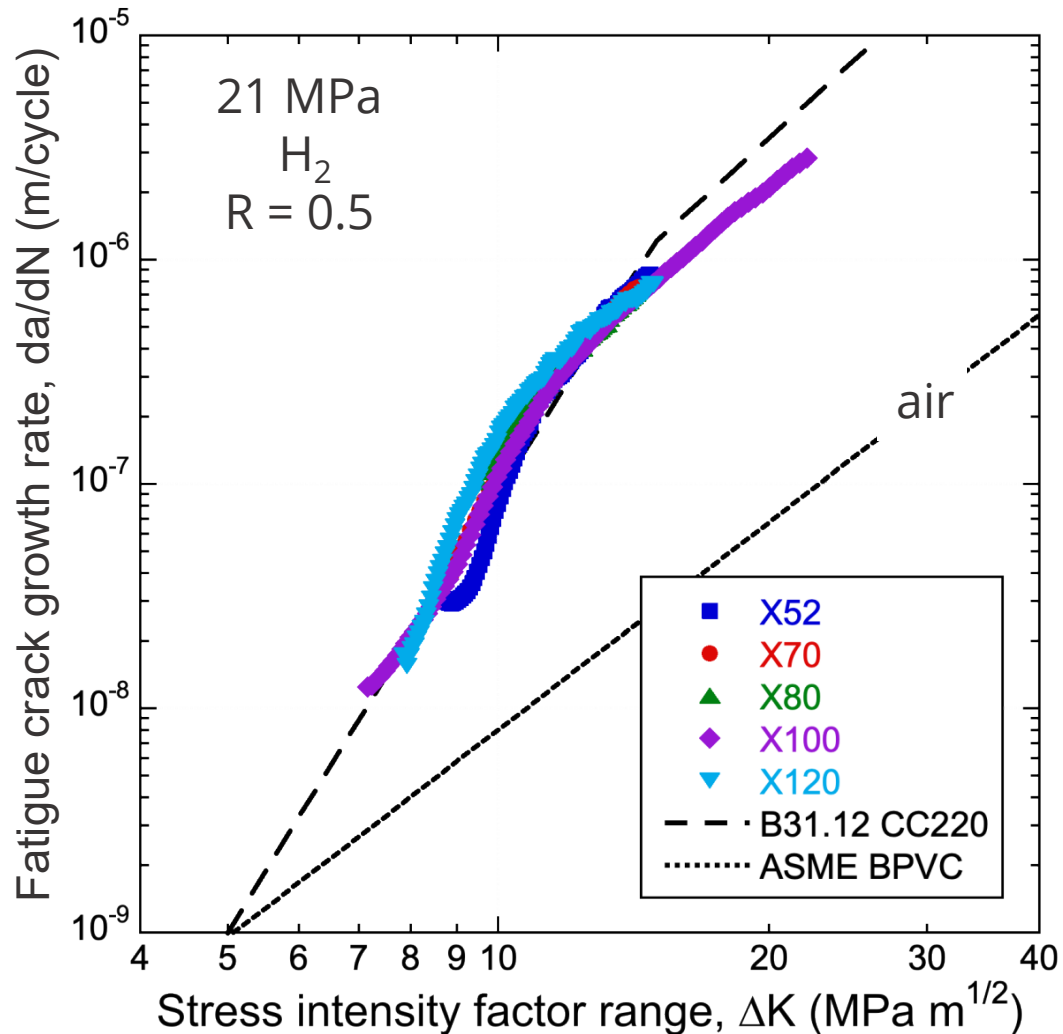


# Fatigue crack growth of line pipe steels: low pressure



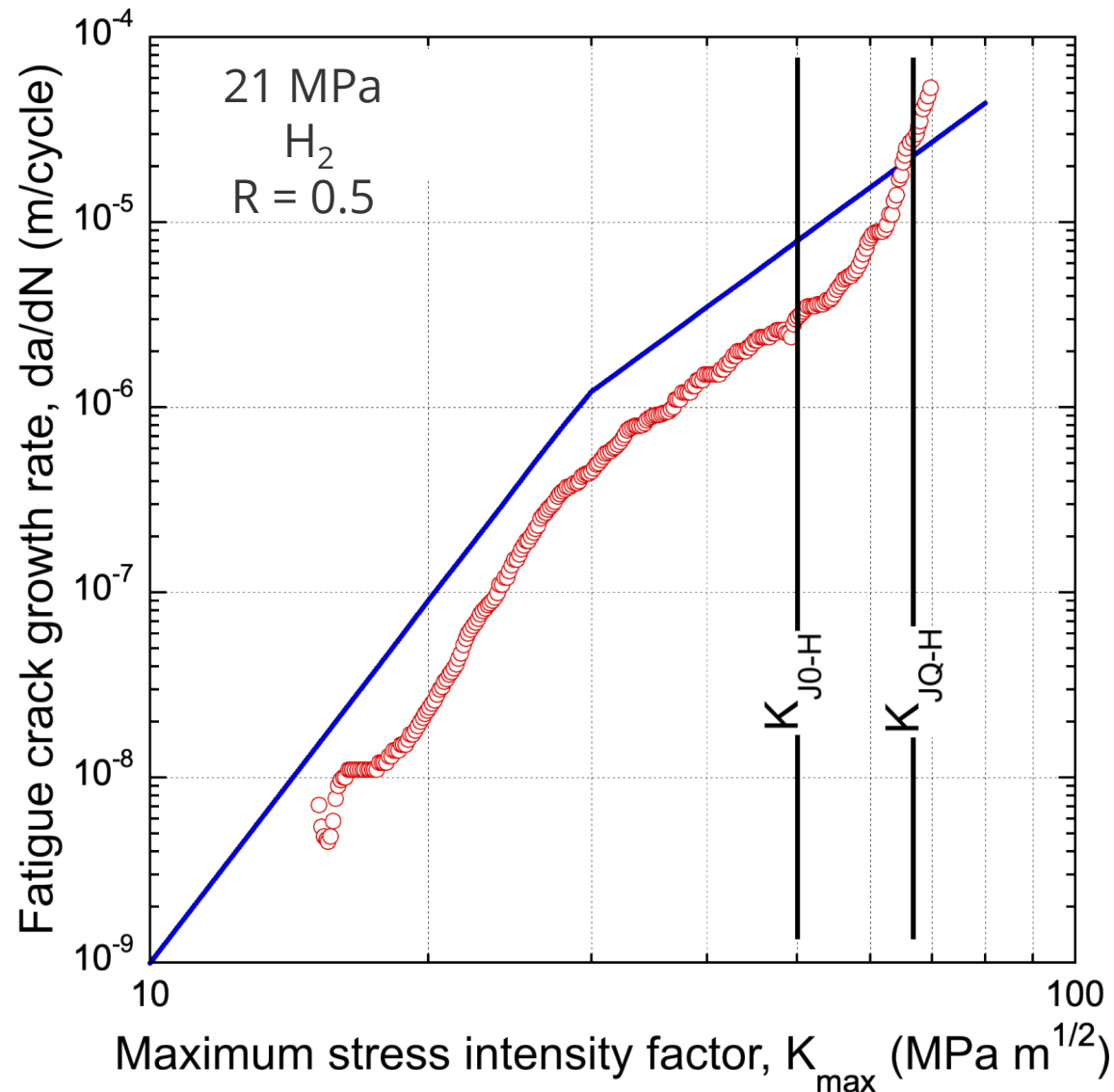


# Both vintage and modern linepipe steels are bounded by proposed fatigue design curves, regardless of strength



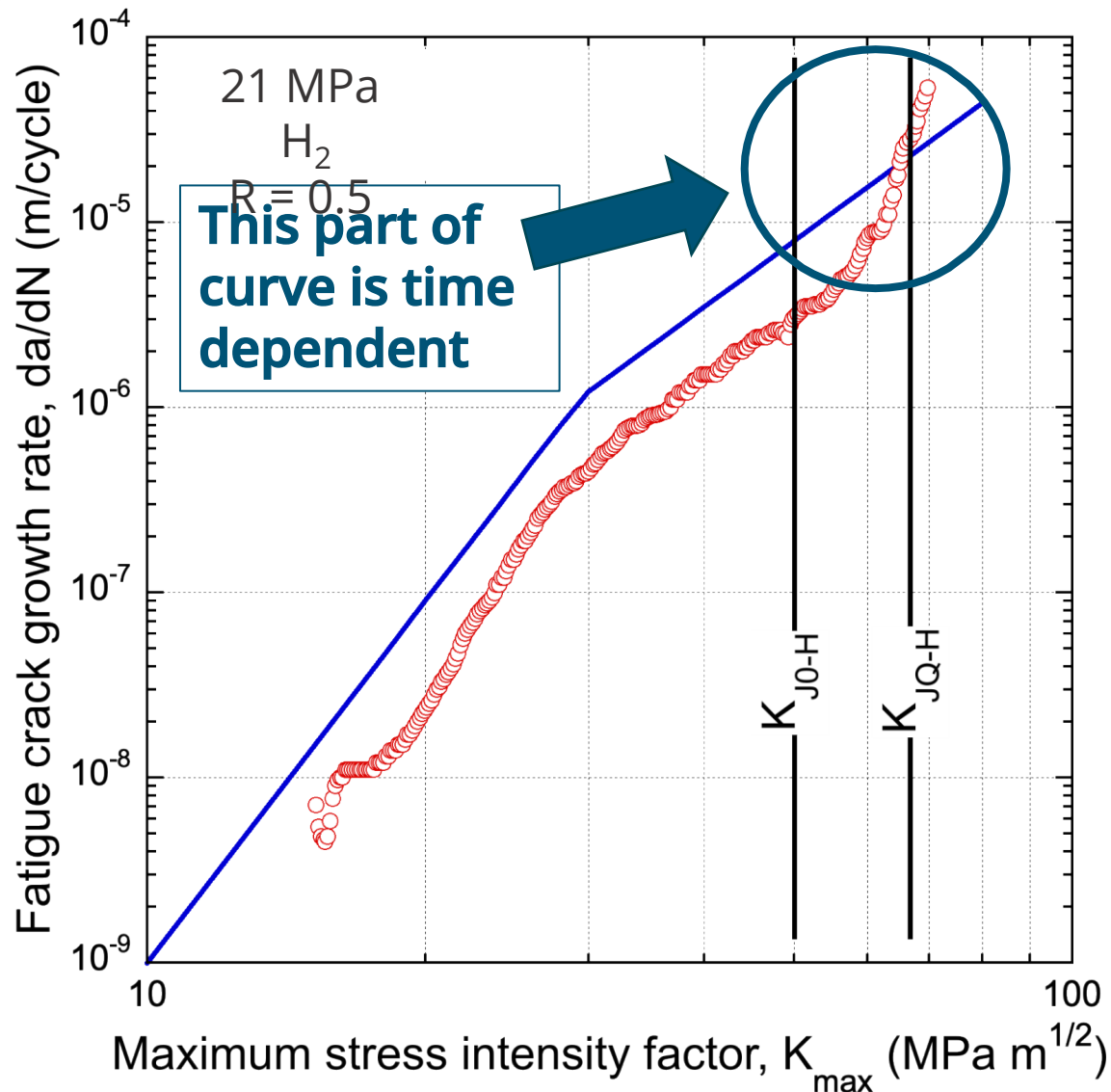


## Application of fatigue curves is limited by fracture resistance



- Fatigue crack growth curves cannot be extrapolated to any stress intensity factor ( $K$ )
- Practical application of fatigue curves is limited to  $40 MPa m^{1/2}$ , perhaps lower in some cases

## Application of fatigue curves is limited by fracture resistance



- Fatigue crack growth curves cannot be extrapolated to any stress intensity factor (K)
- Practical application of fatigue curves is limited to  $40 \text{ MPa m}^{1/2}$ , perhaps lower in some cases
- Also important to recognize that  $K_{max} > K_{J0-H}$  is time dependent
  - Meaning this portion of the curve is frequency dependent

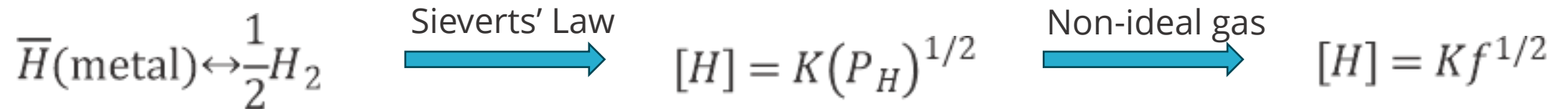


# Pressure dependence based on thermodynamics

- Consider the hydrogen effect as proportional to the equilibrium hydrogen concentration

$$\frac{da}{dN} \propto [H]$$

- Concentration is proportional to square root of fugacity



- Use high-pressure condition (106 MPa) as reference pressure (fugacity)

$$\frac{da}{dN}^{low} = \underbrace{C \left[ \frac{1 + C_H R}{1 - R} \right] \Delta K^m}_{\text{Specifically for } f_{ref}} \underbrace{\left( \frac{f}{f_{ref}} \right)^{1/2}}_{= g(P)}$$



# Use thermodynamics to determine pressure relationship: $g(P)$

**Abel-Noble EOS**  
**Pure gas**

$$\frac{f}{P_H} = \exp\left(\frac{P_H b}{RT}\right)$$

**Regular solution model**  
**Mixed gas**

$$\frac{f}{P_H} = \exp\left(\frac{P_t b}{RT}\right)$$

**Reference pressure**

$$\frac{f_{ref}}{P^*} = \exp\left(\frac{P^* b}{RT}\right)$$

$$g(P) = \left(\frac{f}{f_{ref}}\right)^{1/2}$$

**Combining on Abel-Noble EOS  
and regular solution model**

$$g(P) = \left[ \left(\frac{P_H}{P^*}\right) \exp\left(\frac{b}{RT}(P_t - P^*)\right) \right]^{1/2}$$

$P^*$  Reference pressure:  
= 106 MPa (15,374 psi)

$P_t$  Total pressure

$P_H$  Hydrogen partial pressure

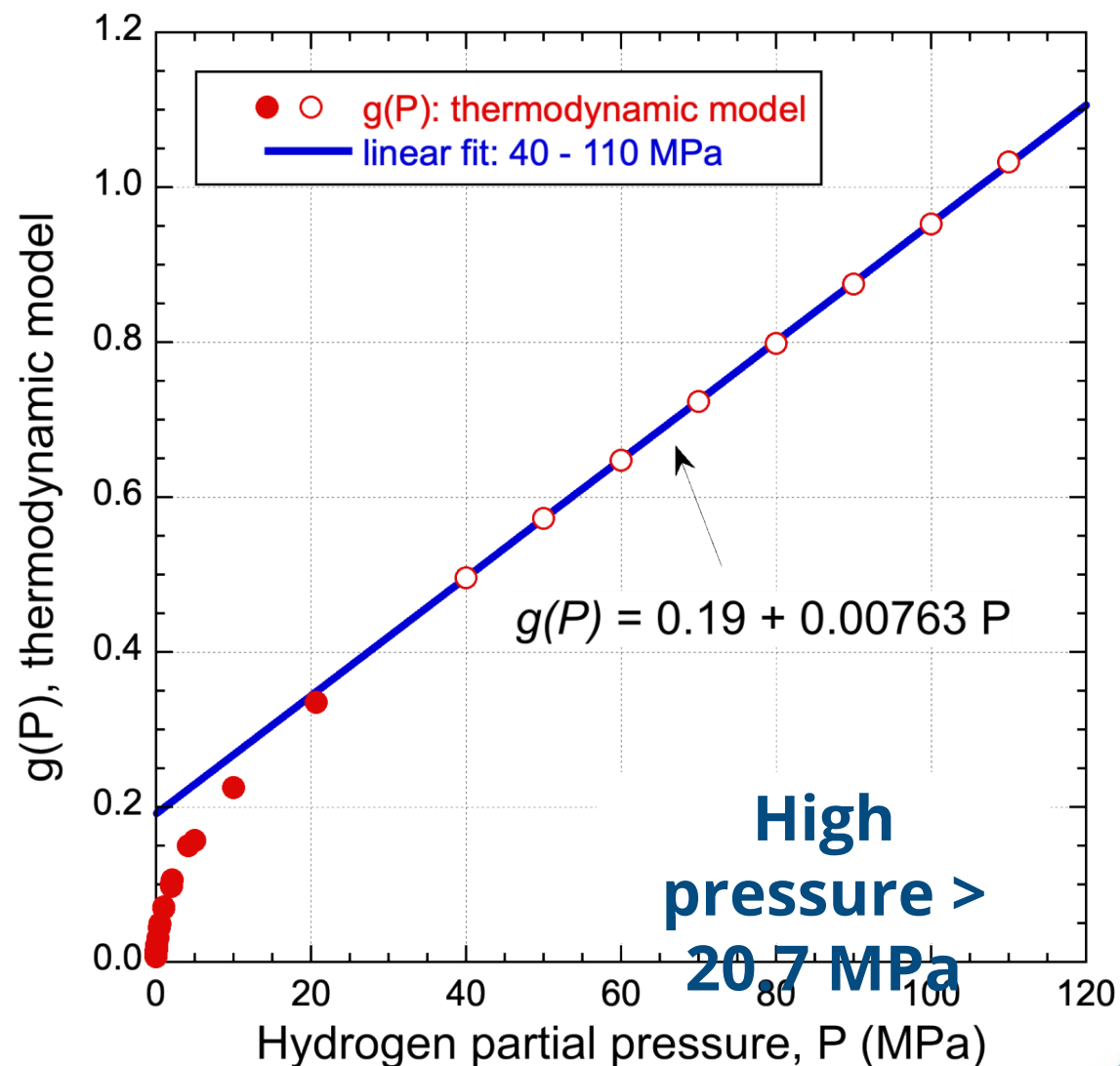
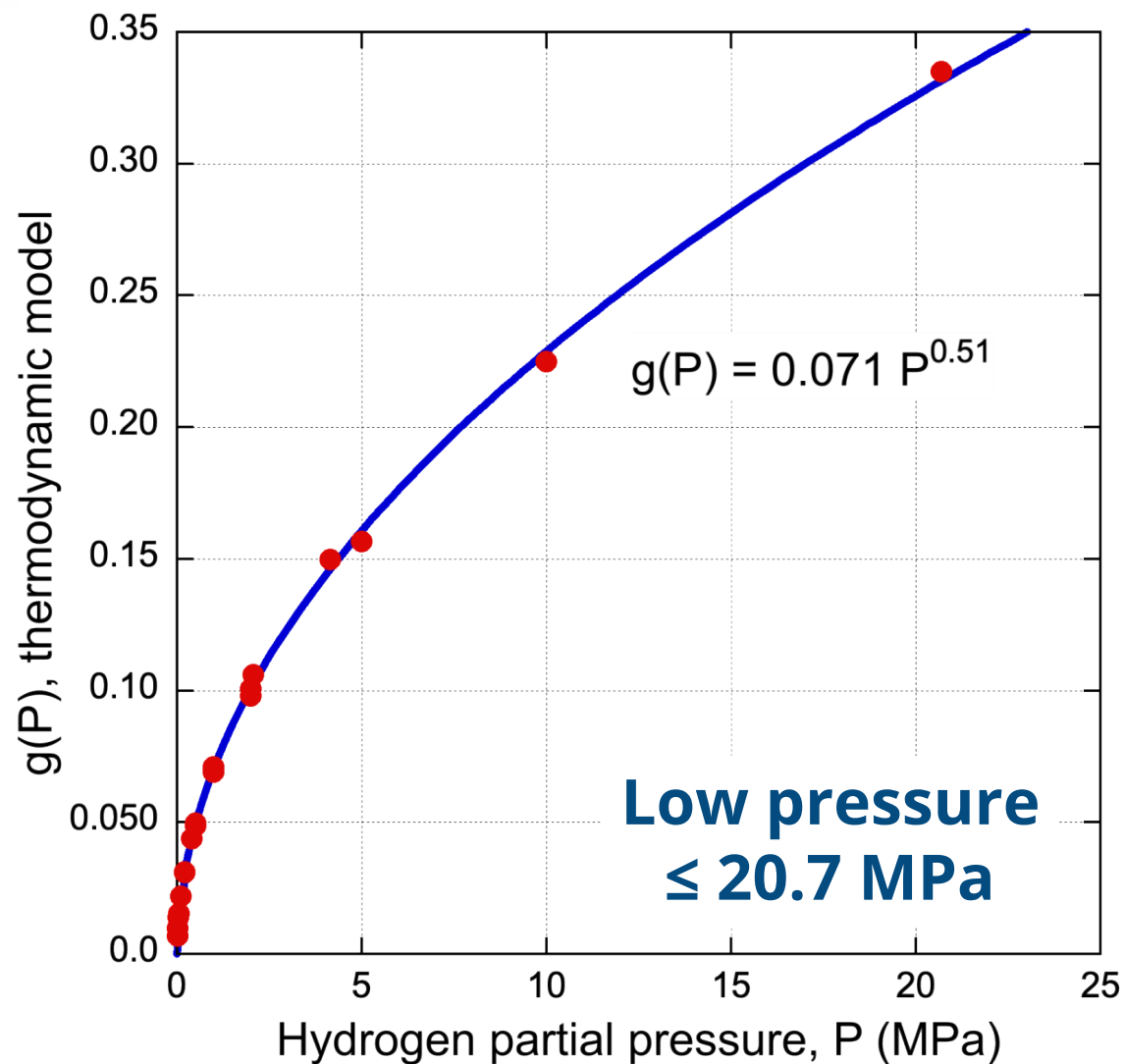
References of EOS and mixed gas:

(1) San Marchi et al, IJHE 32 (2007)

(2) ASME PVP2021-62045



# Fit $g(P)$ in low pressure and high pressure regime separately







# Formulation of Fatigue Design Curves (FDCs) for steels in hydrogen service

	$da/dN_{low}$	$da/dN_{high}$
$C$ (m/cycle)	$3.5 \times 10^{-14}$	$1.5 \times 10^{-11}$
$C_H$	0.4286	2.00
$m$	6.5	3.66
$f(P \leq 20.7 \text{ MPa})$	$0.071 P^{0.51}$	1
$f(P > 20.7 \text{ MPa})$	$0.19 + 0.00763 P$	

Low  $\Delta K$ :  
*pressure dependent*

$$\frac{da}{dN} = C \left[ \frac{1+C_H R}{1-R} \right] \Delta K^m g(P)$$

High  $\Delta K$ :  
*pressure independent*


$$\frac{da}{dN} = C \left[ \frac{1+C_H R}{1-R} \right] \Delta K^m$$





# Formulation of Fatigue Design Curves (FDCs) for steels in hydrogen service

	$da/dN_{low}$	$da/dN_{high}$
$C$ (m/cycle)	$3.5 \times 10^{-14}$	$1.5 \times 10^{-11}$
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$f(P \leq 20.7 \text{ MPa})$	$0.071 P^{0.51}$	1
$f(P > 20.7 \text{ MPa})$	$0.19 + 0.00763 P$	

  $= g(P) = \left[ \left( \frac{P_H}{P^*} \right) \exp \left( \frac{b}{RT} (P_t - P^*) \right) \right]^{1/2}$

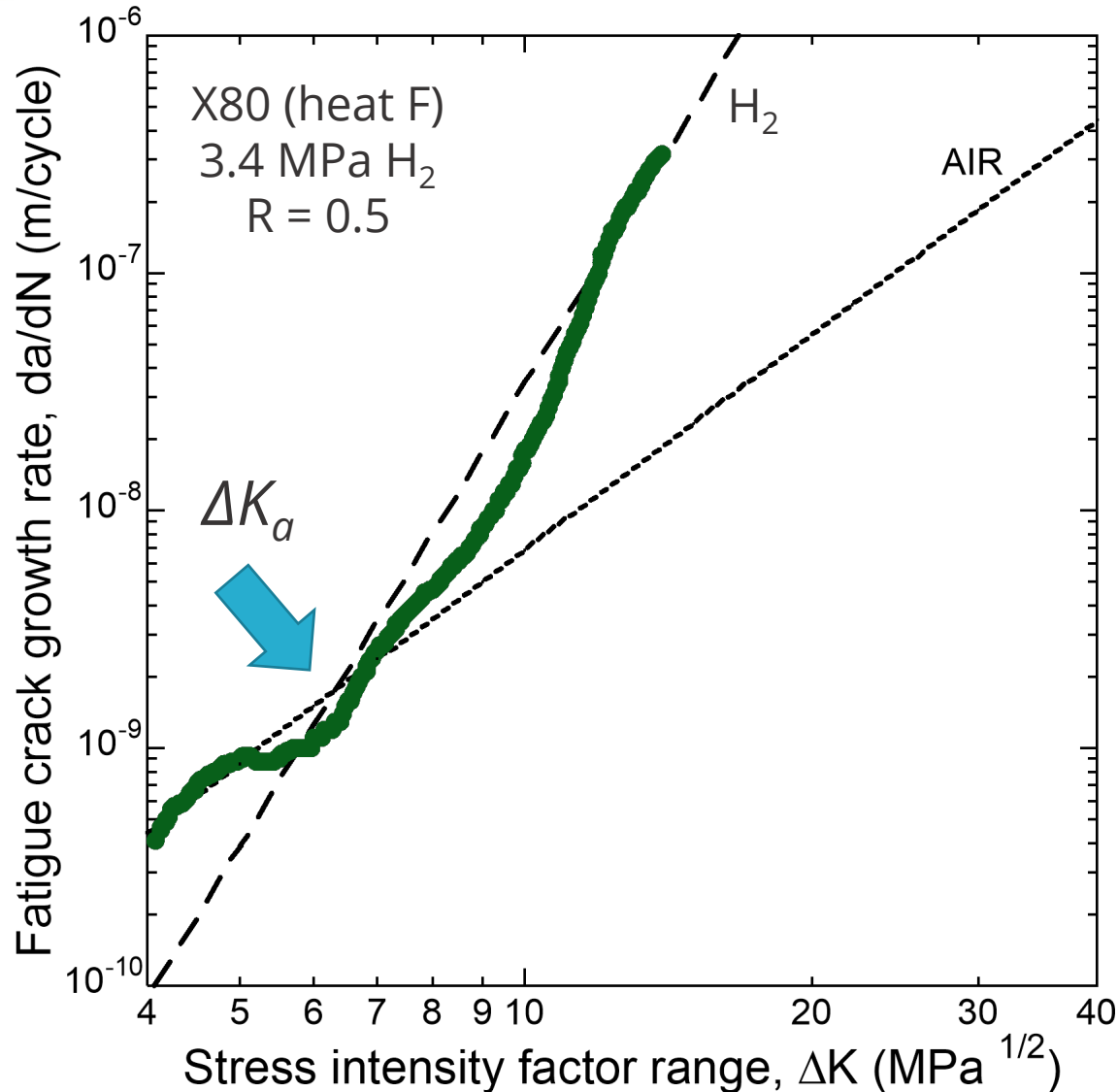
Low  $\Delta K$ :  
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High  $\Delta K$ :  
*pressure independent*

$$\frac{da}{dN} = C \left[ \frac{1+C_H R}{1-R} \right] \Delta K^m$$

## One more thing...



- At low stress intensity (and low pressure) fatigue design curves extrapolate to crack growth rates less than air
- However, experimental observations show that material response can transition to the behavior in air

***Fatigue design curves should not be extrapolated below the air curve***



# Three regimes of fatigue crack growth must be considered for hydrogen service

$$\Delta K < \Delta K_a$$

$$da/dN = da/dN_{air}$$

$$da/dN_{air} = 3.8 \times 10^{-12} \left( \frac{2.88}{2.88 - R_k} \right)^{3.07} \Delta K^{3.07}$$

steels  
 $S_y \leq 620$   
MPa

$$\Delta K_a < \Delta K < \Delta K_c$$

$$da/dN = da/dN_{low}$$

$$da/dN_{low} = 3.5 \times 10^{-14} \left( \frac{1 + 0.43R_k}{1 - R_k} \right) \Delta K^{6.5} \underbrace{[0.071P^{0.51}]}$$

$g(P \leq 20.7 \text{ MPa})$

$$\Delta K > \Delta K_c$$

$$da/dN = da/dN_{high}$$

$$da/dN_{high} = 1.5 \times 10^{-11} \left( \frac{1 + 2R_k}{1 - R_k} \right) \Delta K^{3.66}$$

←  $f(P) = 1$

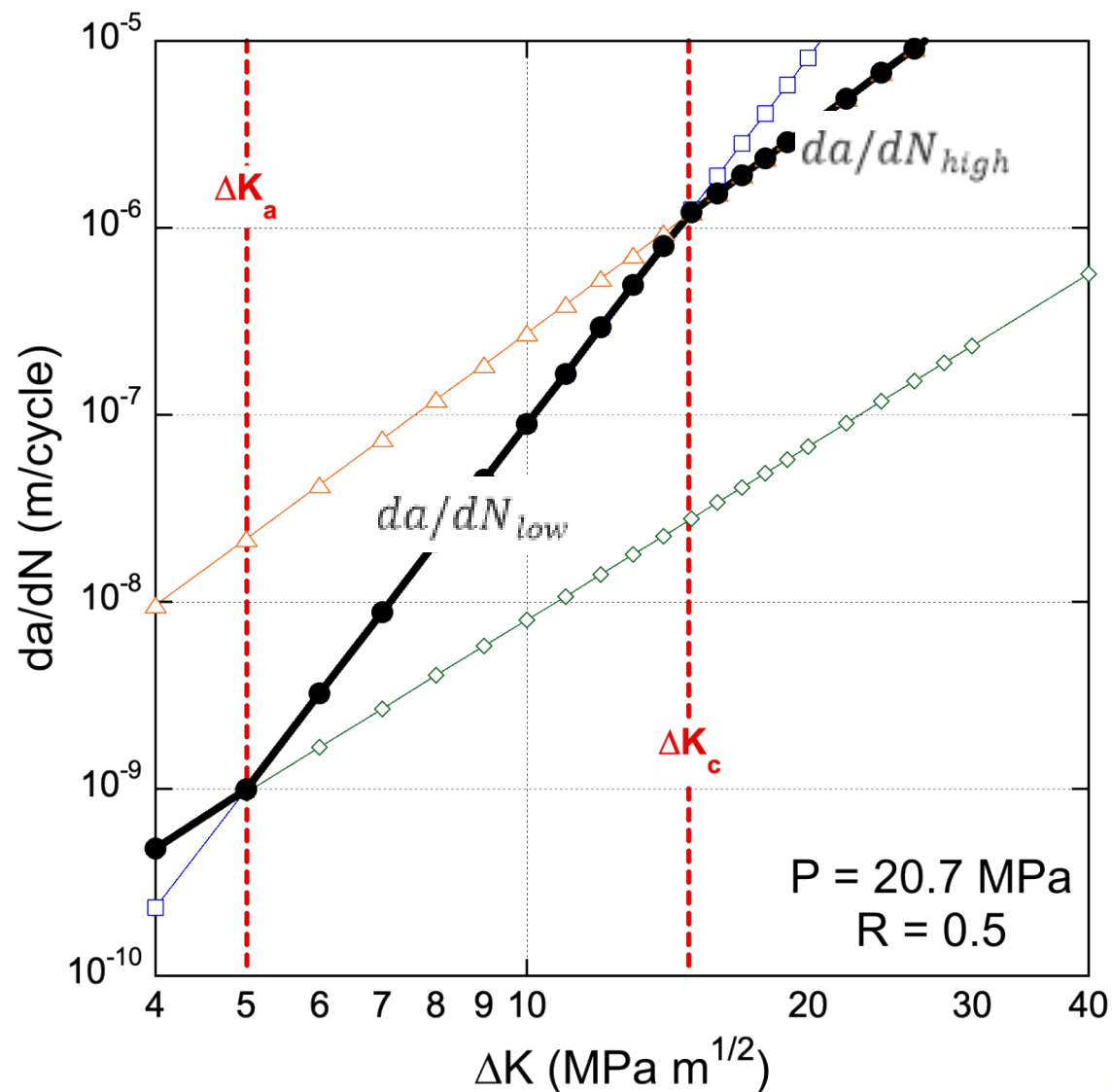
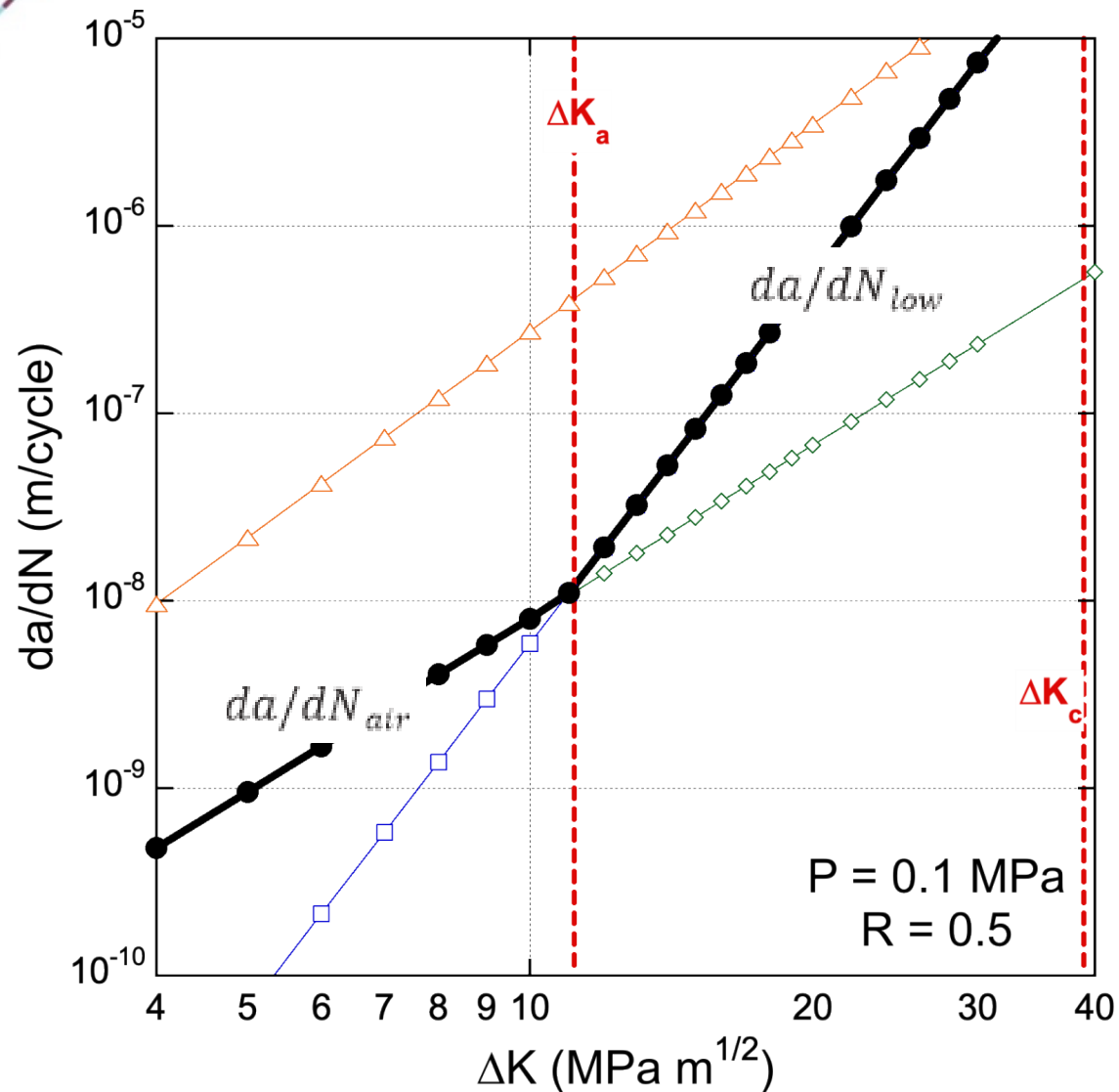
$$\Delta K_a \rightarrow da/dN_{air} = da/dN_{low}$$

$$\Delta K_c \rightarrow da/dN_{low} = da/dN_{high}$$

UNITS:	$\Delta K$	(MPa m <sup>1/2</sup> )
	$da/dN$	(m/cycle)
	$P$	(MPa)



# Example Fatigue Design Curves: unique for each combination of P and R





# Summary of fatigue design curves

For carbon steels and low alloy steels,  $S_y \leq 915$  MPa

$$\Delta K < \Delta K_a$$

$$da/dN = da/dN_{air}$$

Material	$da/dN_{air}$ [m/cycle]†	$R_k$
Carbon and low alloy steels $S_y \leq 620$ MPa	$3.8 \times 10^{-12} \left( \frac{2.88}{2.88 - R_k} \right)^{3.07} \Delta K^{3.07}$	$0 \leq R_k < 1$
High strength low alloys steels $S_y > 620$ MPa	$3.64 \times 10^{-12} (1 + 3.53 R_k) \Delta K^{3.26}$	$R_k \geq 0$

† relationships from the ASME BPVC



# Summary of fatigue design curves

For carbon steels and low alloy steels,  $S_y \leq 915$  MPa

$$\Delta K_a < \Delta K < \Delta K_c$$

$$da/dN = da/dN_{low} [\text{m/cycle}] = 3.5 \times 10^{-14} \left( \frac{1+0.43R_k}{1-R_k} \right) \Delta K^{6.5} [g(P)]$$

P range [MPa]	$g(P)$ [MPa]	Material	$\Delta K_a$ [MPa m <sup>1/2</sup> ]
0.1 to 20.7	$0.071 P^{0.51}$	Carbon and low alloy steels, $S_y \leq 620$ MPa	$(8.6 - 3.0R_k + 7.9R_k^2 - 9.4R_k^3) P^{-0.15}$
		High strength low alloys steels, $S_y > 620$ MPa	$(9.6 + 2.7R_k + 0R_k^2 - 7.8R_k^3) P^{-0.16}$
20.7 to 110 †	$0.19 + 0.00763 P$	Carbon and low alloy steels, $S_y \leq 620$ MPa	$(10.6 - 3.7R_k + 9.8R_k^2 - 11.7R_k^3) P^{-0.21}$
		High strength low alloys steels, $S_y > 620$ MPa	$(11.9 + 3.4R_k + 0R_k^2 - 9.6R_k^3) P^{-0.22}$

† relationships fit to pressure range of 40 to 110 MPa



# Summary of fatigue design curves

For carbon steels and low alloy steels,  $S_y \leq 915$  MPa

$$\Delta K > \Delta K_c$$

Note:  $da/dN$  pressure independent

$$da/dN = da/dN_{high} \text{ [m/cycle]} = 1.5 \times 10^{-11} \left( \frac{1+2R_k}{1-R_k} \right) \Delta K^{3.66}$$

P range [MPa]	$\Delta K_c$ [MPa m <sup>1/2</sup> ]
0.1 to 20.7	$(21.66 + 10R_k - 3.7R_k^2) P^{-0.18}$
20.7 to 110 †	$(27.4 + 12.7R_k - 4.8R_k^2) P^{-0.25}$

Transition is pressure dependent because  $da/dN_{low}$  depends on pressure

$\Delta K_c$  is defined by  
 $da/dN_{low} = da/dN_{high}$

† relationships fit to pressure range of 40 to 110 MPa



# Summary

- Measured fatigue crack growth of steels in gaseous hydrogen can be bounded by a two-part 'Paris Law' (simple power law)
  - And consideration for fatigue in air
- Fatigue Design Curves (FDCs) have a wide range of applicability for pressure vessel steels and line pipe steels in gaseous hydrogen service
  - FDCs are pressure dependent
    - 0.1 MPa to 110 MPa
  - FDCs account for dependence on stress ratio  $R$ 
    - 0.1 to 0.7 (potentially 0.9 and higher)
  - FDCs are relatively simple Paris Law (power law) relationships





# Thank You for your attention

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## **Additional resources:**



<https://h-mat.org/>

<https://www.sandia.gov/matlsTechRef/>

<https://granta-mi.sandia.gov/>

## *Hydrogen Effects on Materials Laboratory (HEML) team*



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