

## Neural-ODE Surrogates for Fuel Degradation Processes in Nuclear Waste Repository Simulations

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Sandia ML DL Workshop  
Sept. 2024

SAND2024-#####

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# Acknowledgements and Disclaimers

- Acknowledgements:

- Funding by the Department of Energy (DOE), Office of Nuclear Energy, Spent Fuel and Waste Science and Technology

- Disclaimer:

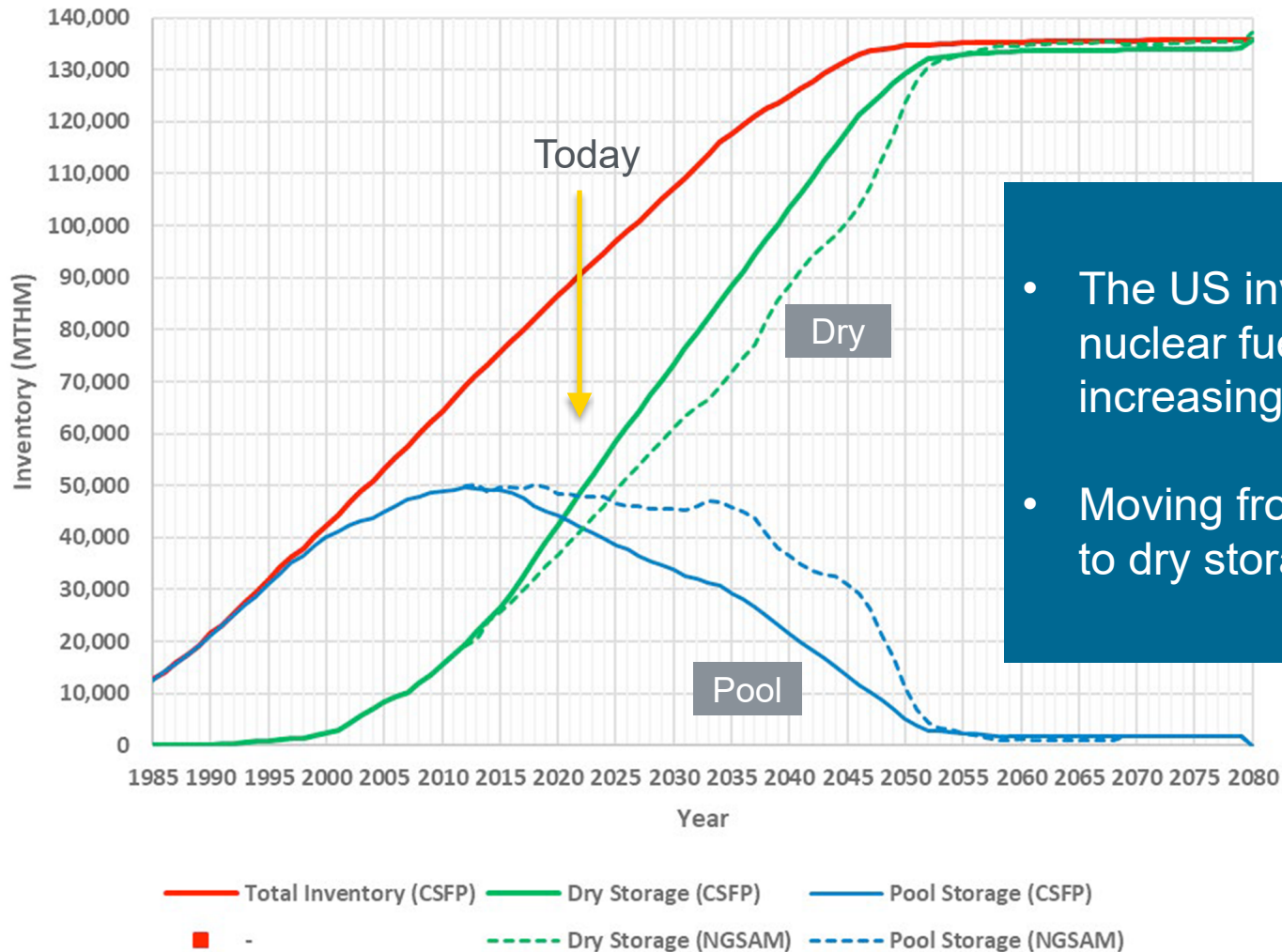
- This presentation describes objective technical results and analysis. Any subjective views or opinions that might be expressed in the presentation do not necessarily represent the views of the U.S. Department of Energy or the United States Government.

- Computational Modeling of Spent Nuclear Fuel
- Training Data
- Neural-ODE Surrogates
  - Methods
  - Logistic Decay Toy Problem
  - Application to Spent Nuclear Fuel
- Conclusions and Future Work

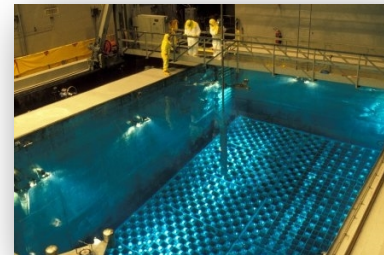
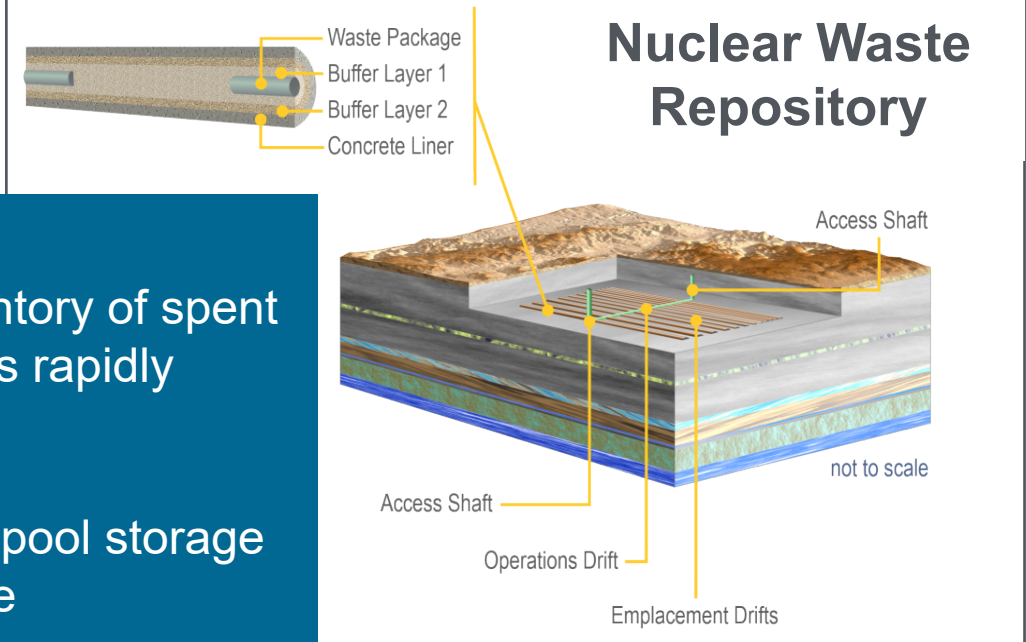
# Computational Modeling of Spent Nuclear Fuel

# More Spent Nuclear Fuel in Dry Storage

## Storage Projections (2 models)

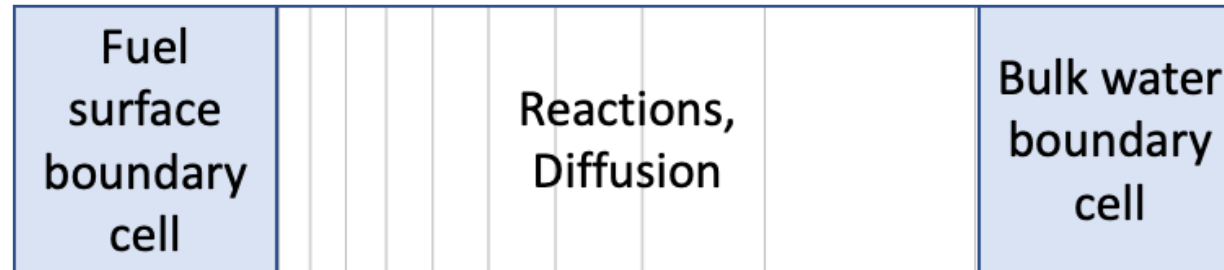
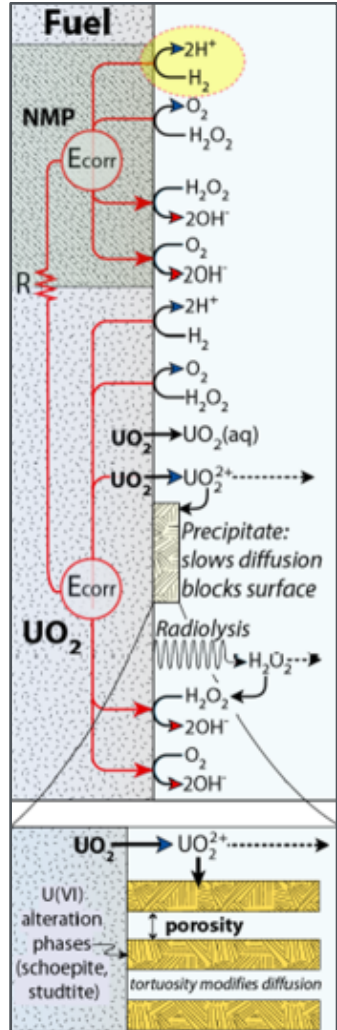


- The US inventory of spent nuclear fuel is rapidly increasing
- Moving from pool storage to dry storage



[1] Adapted from Freeze et al. (2021, Figure 2-3)

# Fuel Matrix Degradation Model (FMDM)



- 1-dimensional reactive transport model of a waste package
- Needed for each breached package in the repository at each time point
- Computationally intensive to calculate  $\text{UO}_2$  degradation rates
- Surrogate models map inputs to outputs with less computational cost

# Training Data



# Sampling Input Parameters

Parameter	Distribution	Min.	Max.
Init. Temp. (K)	Uniform	300	600
Burnup (Gwd/MTU)	Uniform	40	80
Delay Time (years)	Log-uniform	$10^2$	$10^4$
Env. $\text{CO}_3^{2-}$ (mol/m <sup>3</sup> )	Log-uniform	$10^{-3}$	$2 \times 10^{-2}$
Env. $\text{O}_2$ (mol/m <sup>3</sup> )	Log-uniform	$10^{-7}$	$10^{-5}$
Env. $\text{Fe}^{2+}$ (mol/m <sup>3</sup> )	Log-uniform	$10^{-3}$	$10^{-2}$
Env. $\text{H}_2$ (mol/m <sup>3</sup> )	Log-uniform	$10^{-5}$	$2 \times 10^{-2}$

- Process model input parameters sampled from expected ranges in reservoir simulations to generate training data time-trajectories
- Ranges that span multiple orders of magnitude sampled with log-uniform distribution
- Parameters are externally-imposed

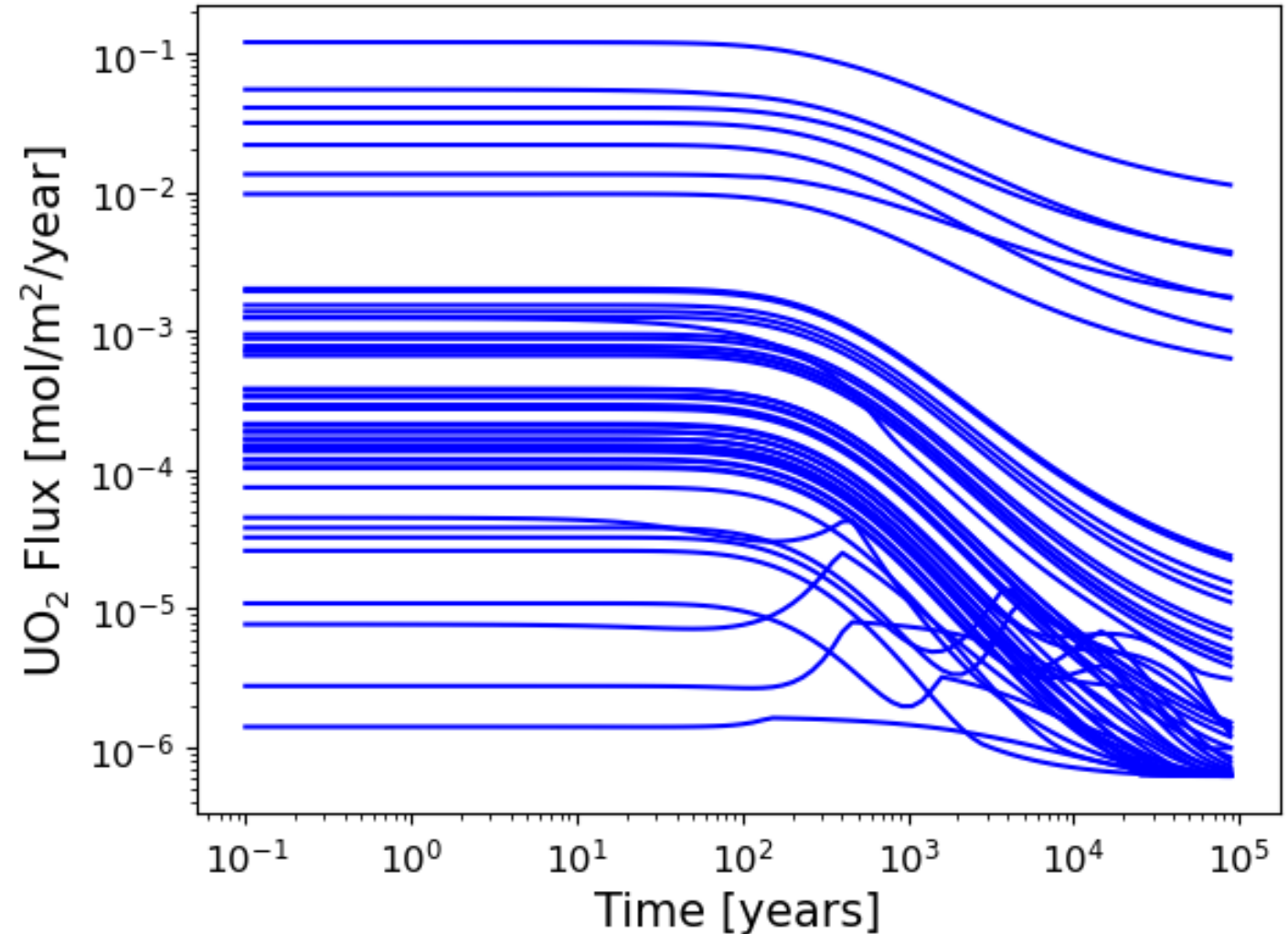


# Surrogate Inputs and Outputs

- Environmental  $\text{CO}_3^{2-}$  and  $\text{H}_2$
- Temperature
- Dose rate (function of time and burnup)



$\text{UO}_2$  Degradation  
(Surface Flux)



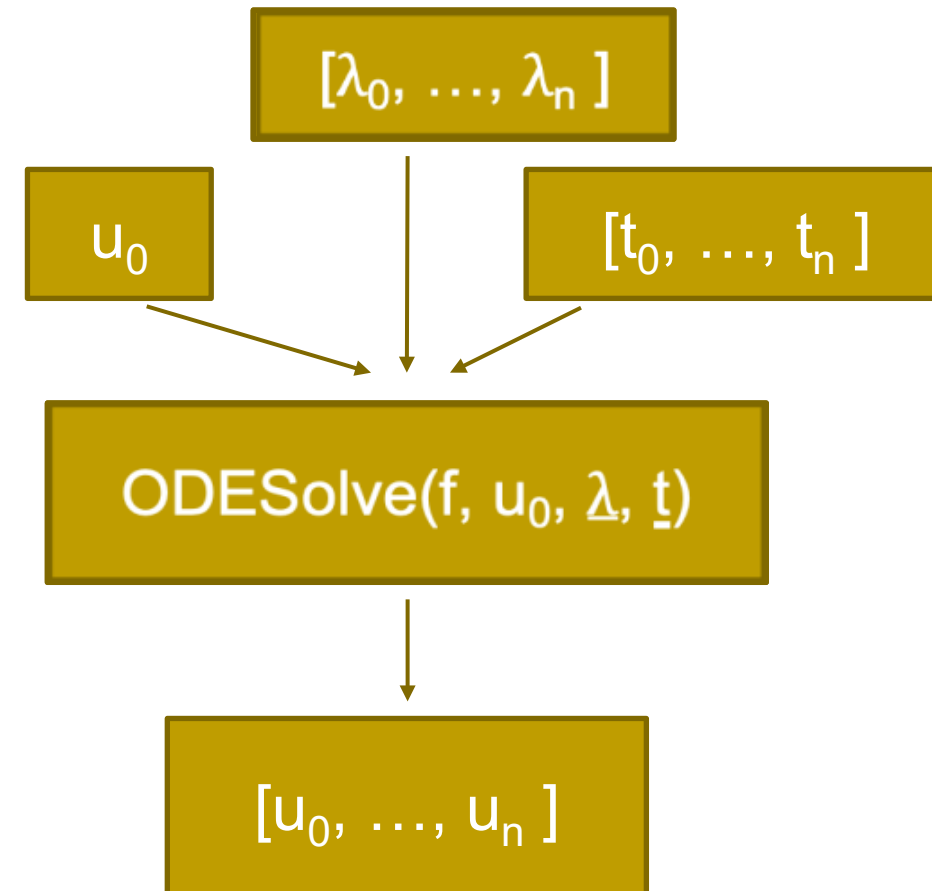
# Neural ODEs

## Methods

# Neural ODEs Background

$$\frac{du}{dt} = f(u, \lambda) = \text{NN}$$

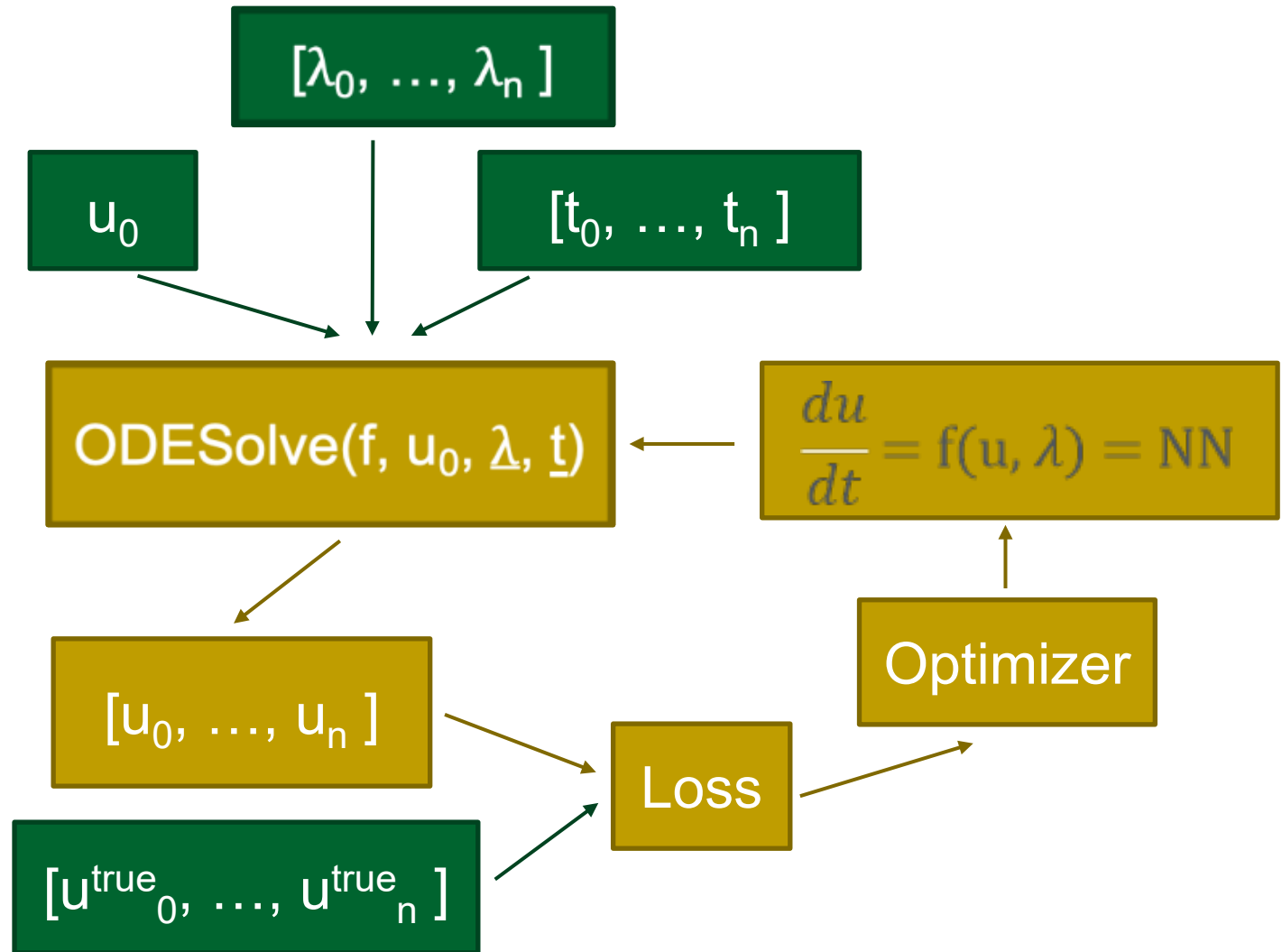
- Neural ODEs approximate the derivative of the system state as a Neural Network
- Predict with ODE Solver



[3] “Neural Ordinary Differential Equations”, Chen et al.

# Training Process and Hyperparameters

- Select random points from a trajectory to serve as batch initial conditions
- Hyperparameters to tune:
  - Learning rate
  - Number of layers
  - Number of neurons per layer
  - Number of batches (batch\_size)
  - Number of time steps to predict/integrate during training (batch\_time)
  - Amount of training data
  - Number of time points to use from training data
  - Choice of numerical ODE solver

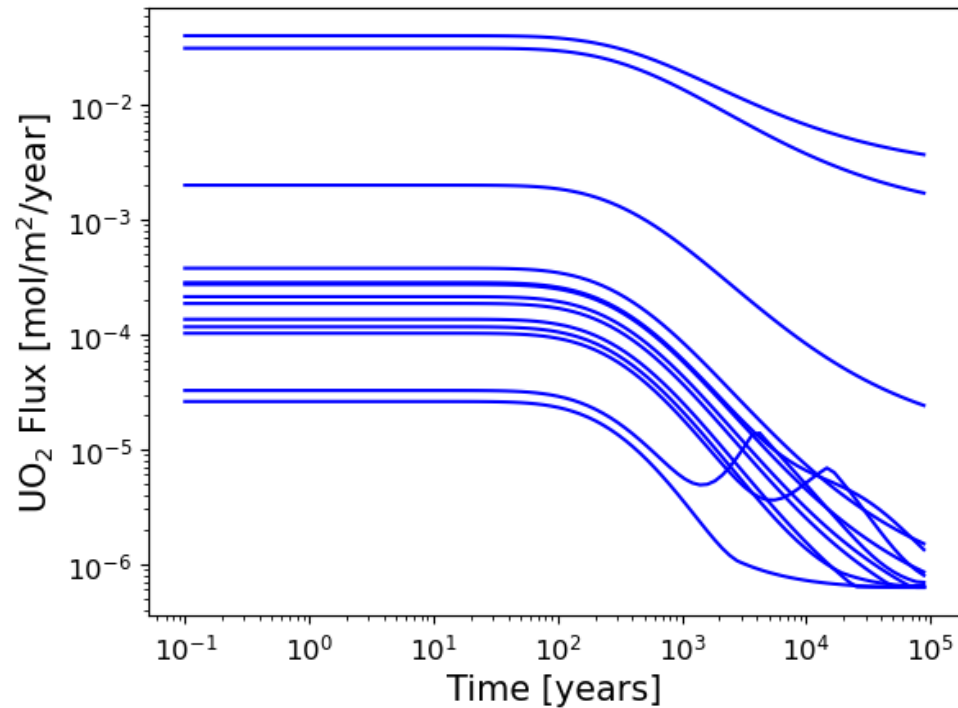


# Neural ODEs

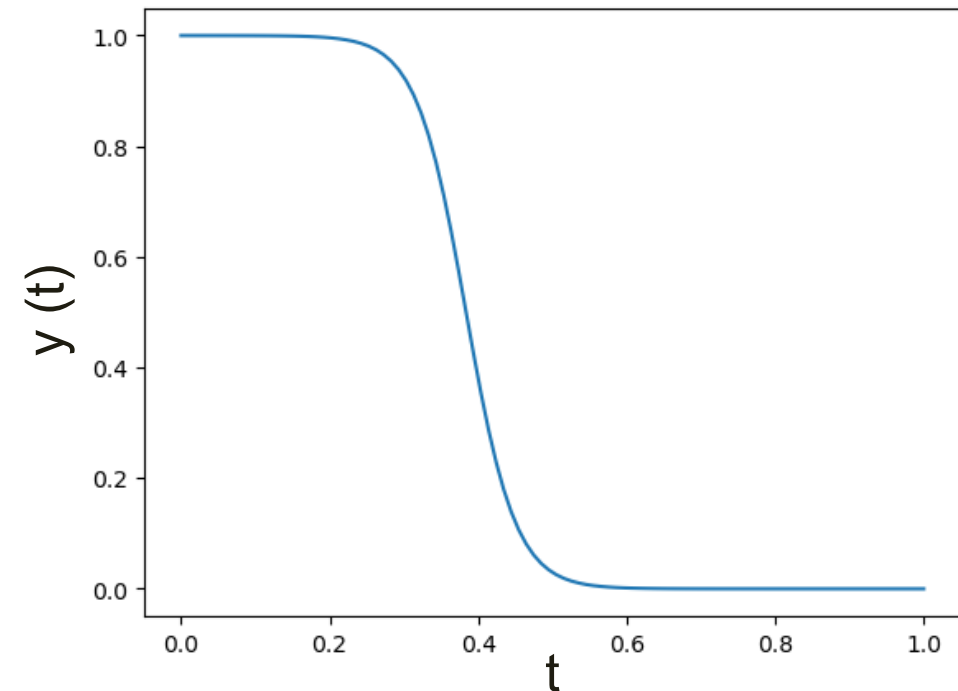
## Logistic Decay Toy Problem

# Simplify Problem-Solving with Logistic Decay ODE

- Logistic Decay ODE with precise initial conditions mimics plateau-and-decay shape of  $\text{UO}_2$  flux trajectories but has known dynamics and no parameter dependence



**$\text{UO}_2$  Flux**

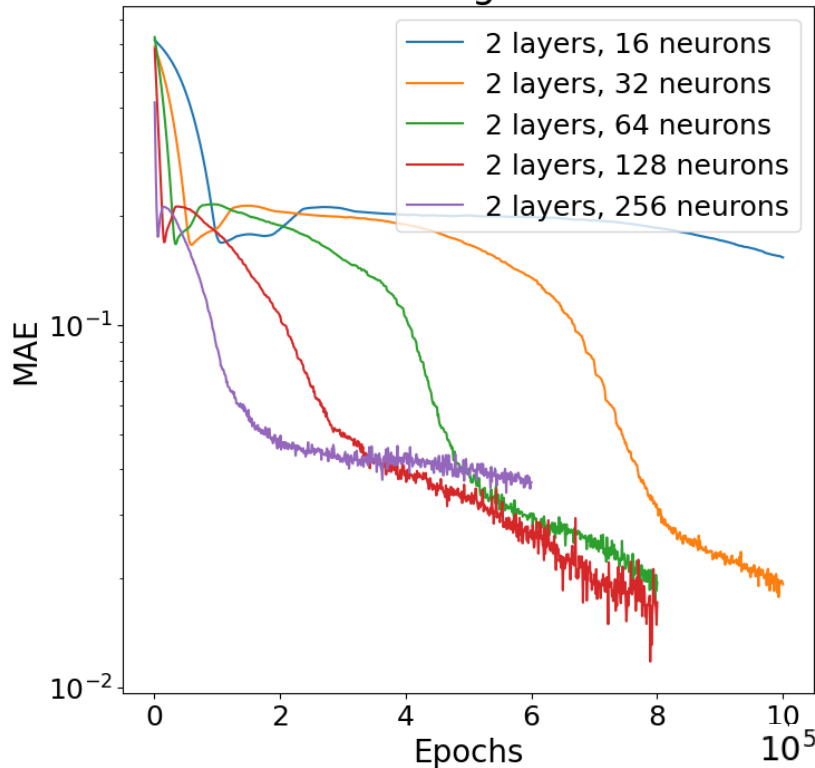


$$\frac{dy}{dt} = -30y(1 - y),$$
$$y(0) = 0.99999$$

# Experiments with Logistic Decay

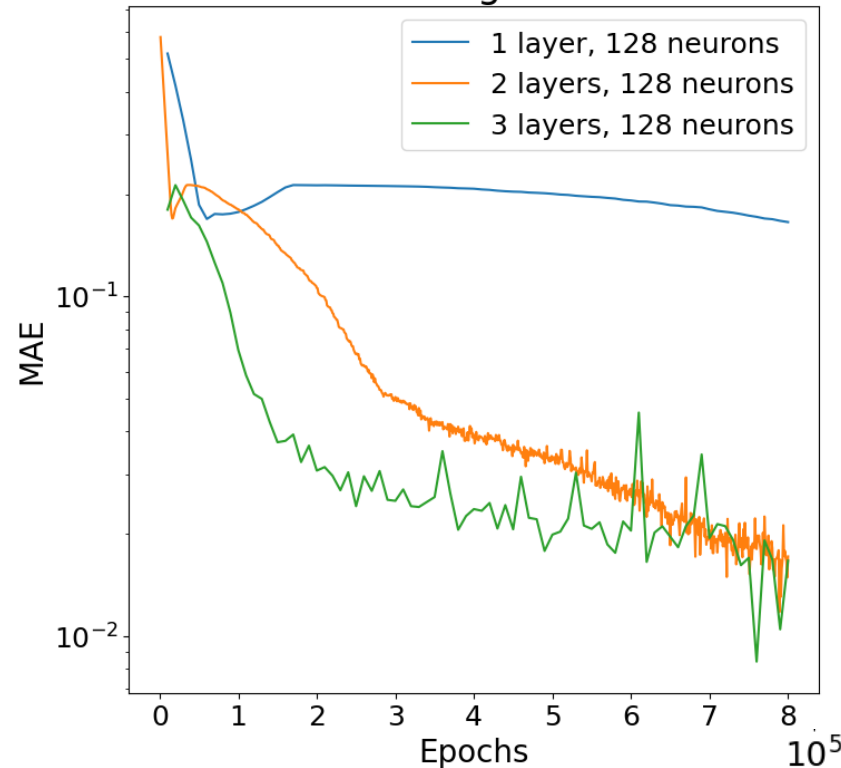
- Dopri5 has best balance of speed and accuracy in torchdiffeq.odeint solvers (with NRMSE =  $9.4490\text{e-}05$  when solving the true RHS of the ODE)
- Precision of the problem requires a learning rate of  $1\text{e-}6$
- Lowest training loss with 2 layers, 128 neurons, batch\_time 20, and batch\_size 80

Training Loss



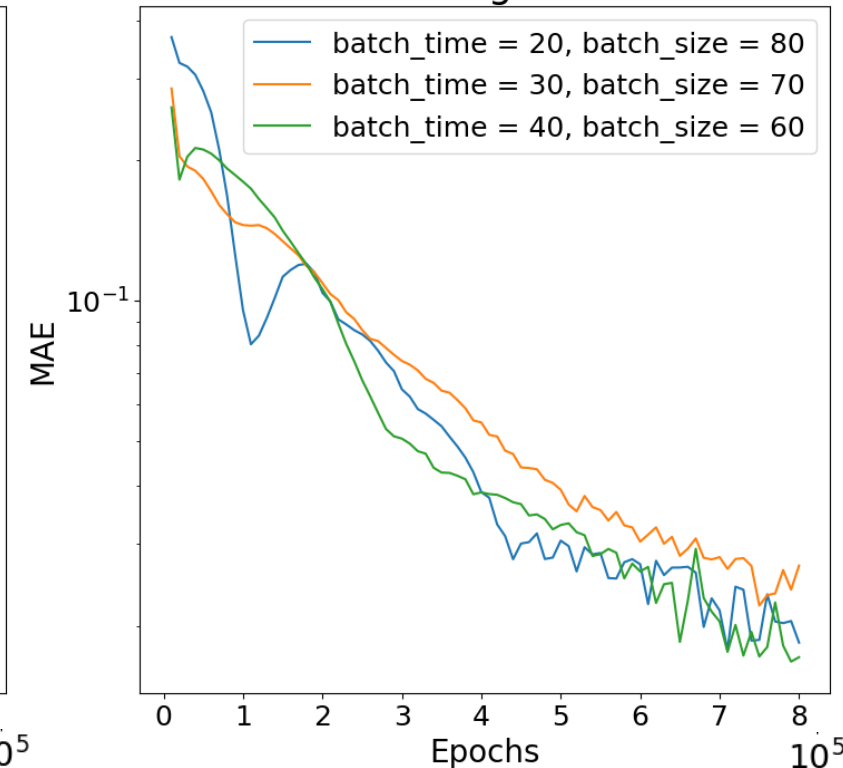
batch\_time = 40, batch\_size = 60

Training Loss



batch\_time = 40, batch\_size = 60

Training Loss

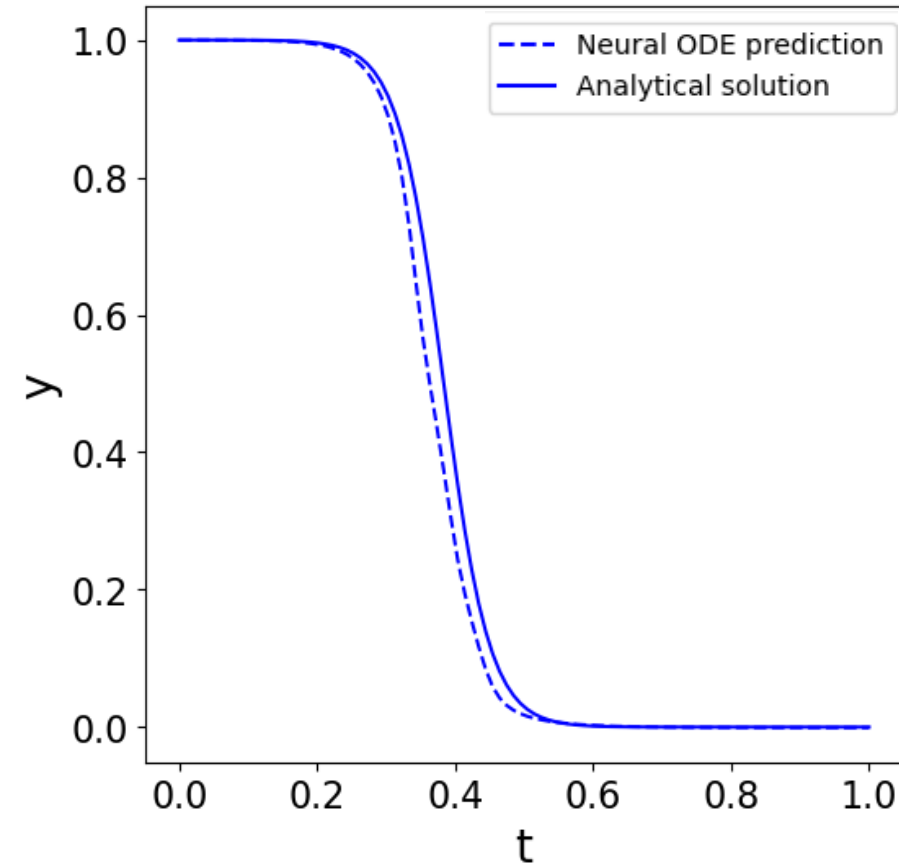


2 layers, 128 neurons/layer



# Logistic Decay Results

- Neural ODEs have difficulty learning a trajectory with an initial plateau
- Very sensitive to initial conditions
- For the best set of hyperparameters, training NRMSE = 0.08323 after 1.2M epochs

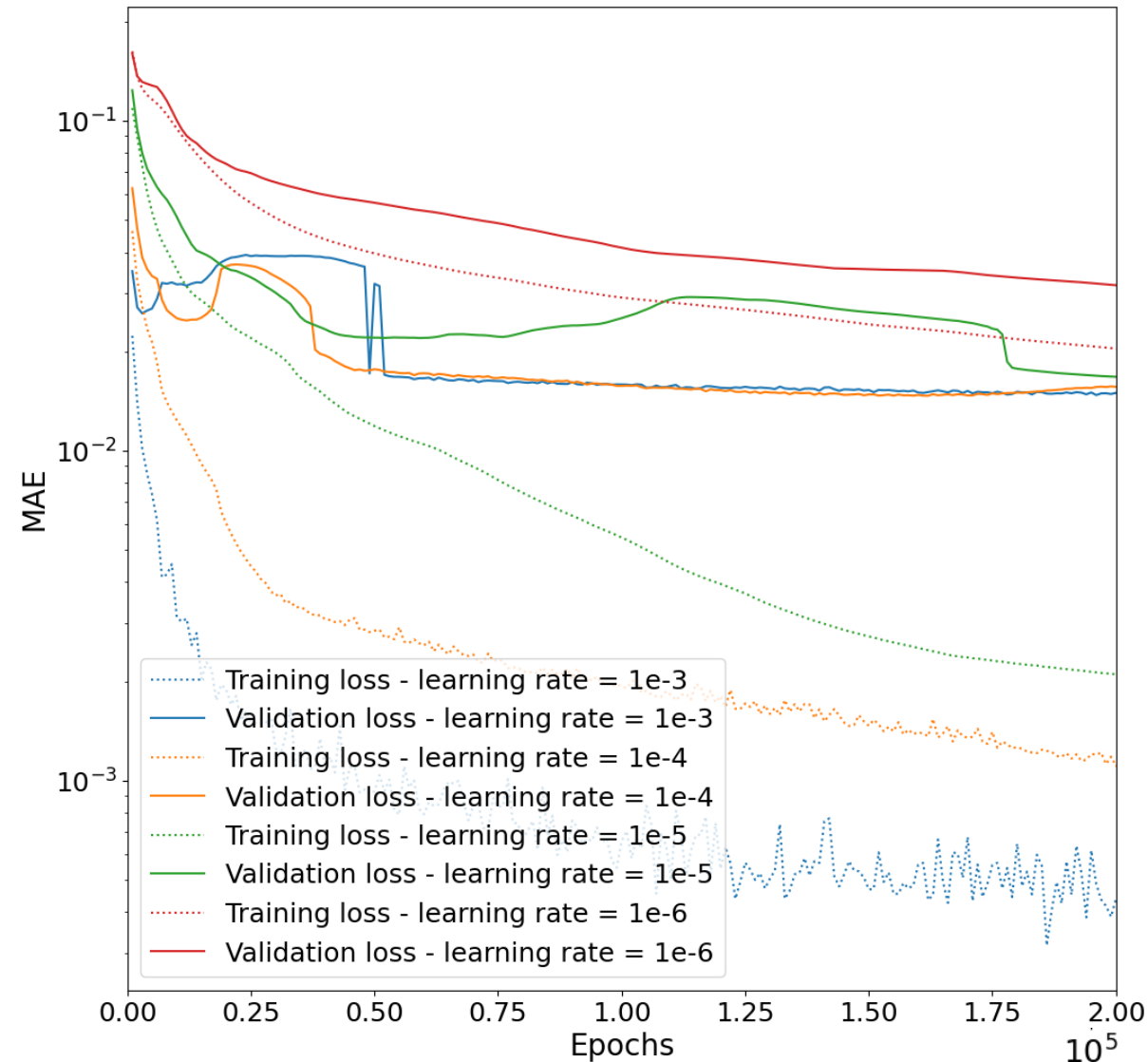


# Neural ODEs

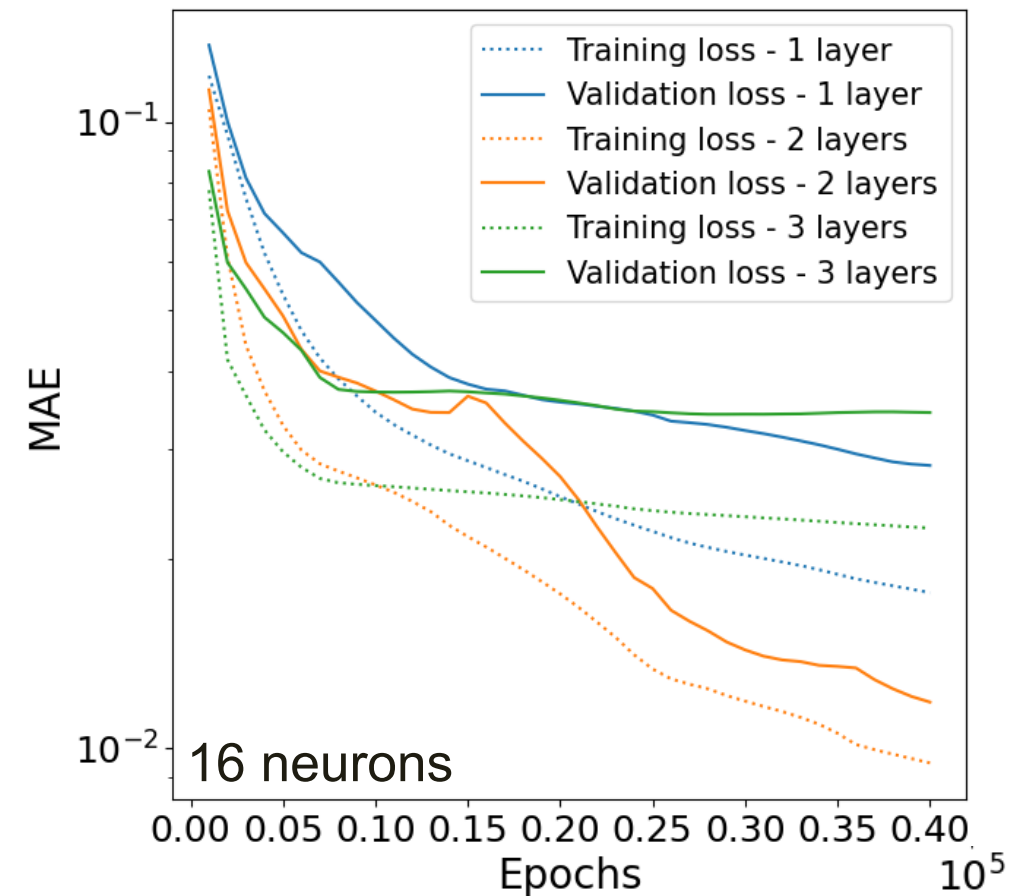
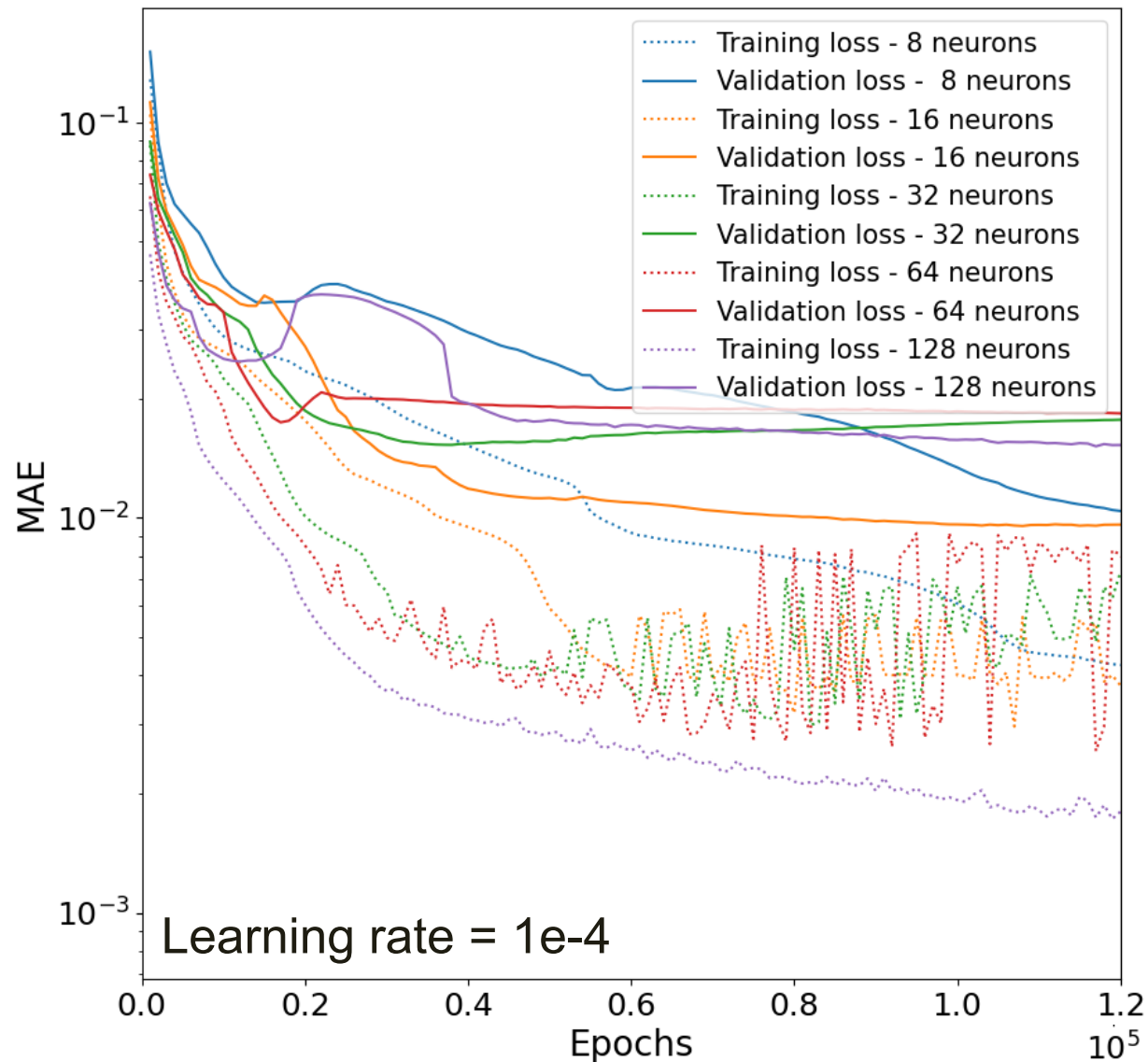
## FMD Application

# Hyperparameter Tuning: Learning Rate

- For preliminary tests, we use
  - torchdiffeq.dopri5 solver
  - 100 trajectories (80 training/ 20 validation)
  - 100 time steps
  - Batch\_time = 20
  - Batch\_size = 80
  - 2 layers, 128 neurons
- A learning rate of  $1e-4$  is a good balance of speed, accuracy, and stability

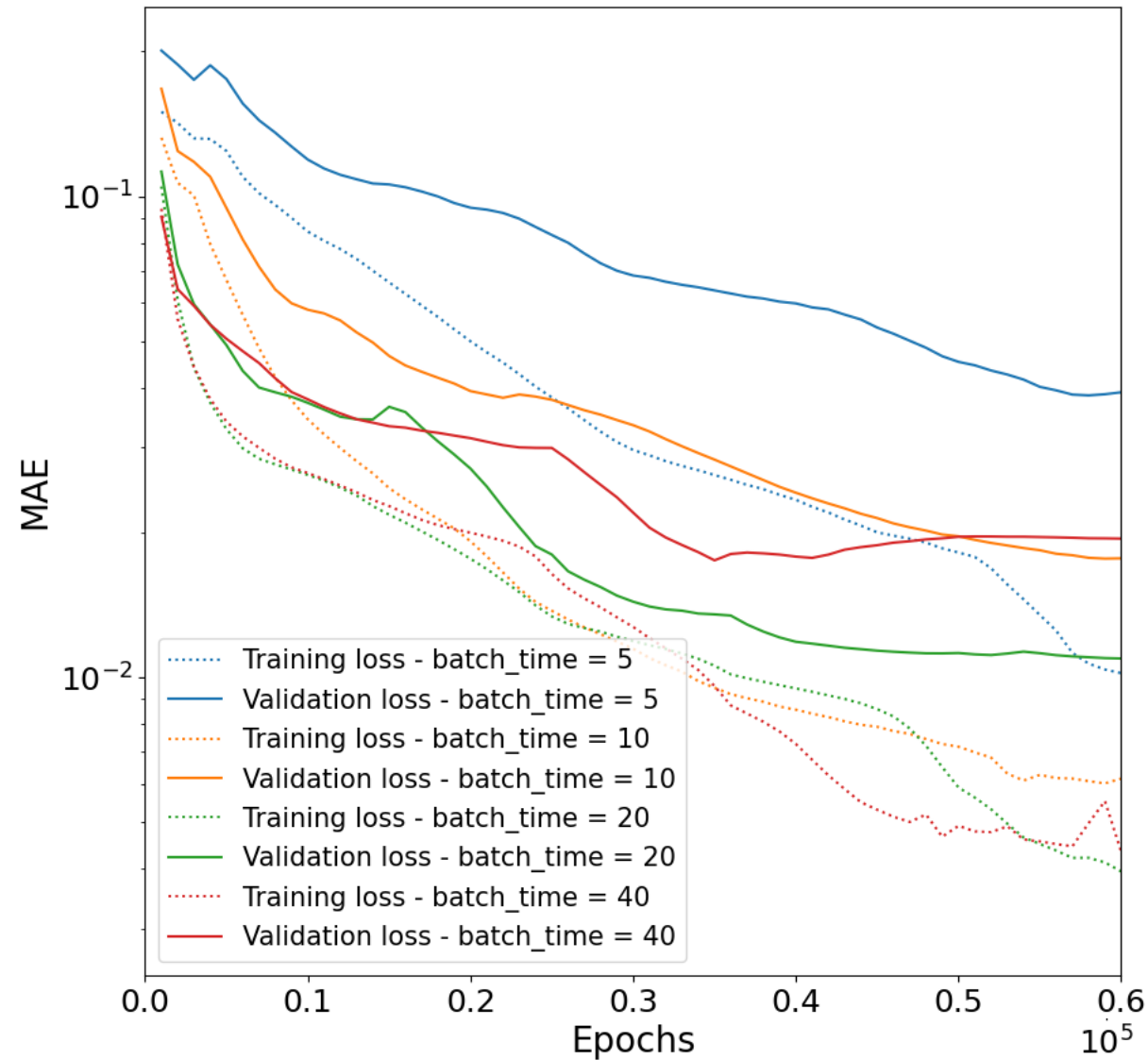


# Hyperparameter Tuning: Neurons and Layers



- An architecture of 16 neurons and 2 layers has the lowest validation loss

# Hyperparameter Tuning: batch\_time

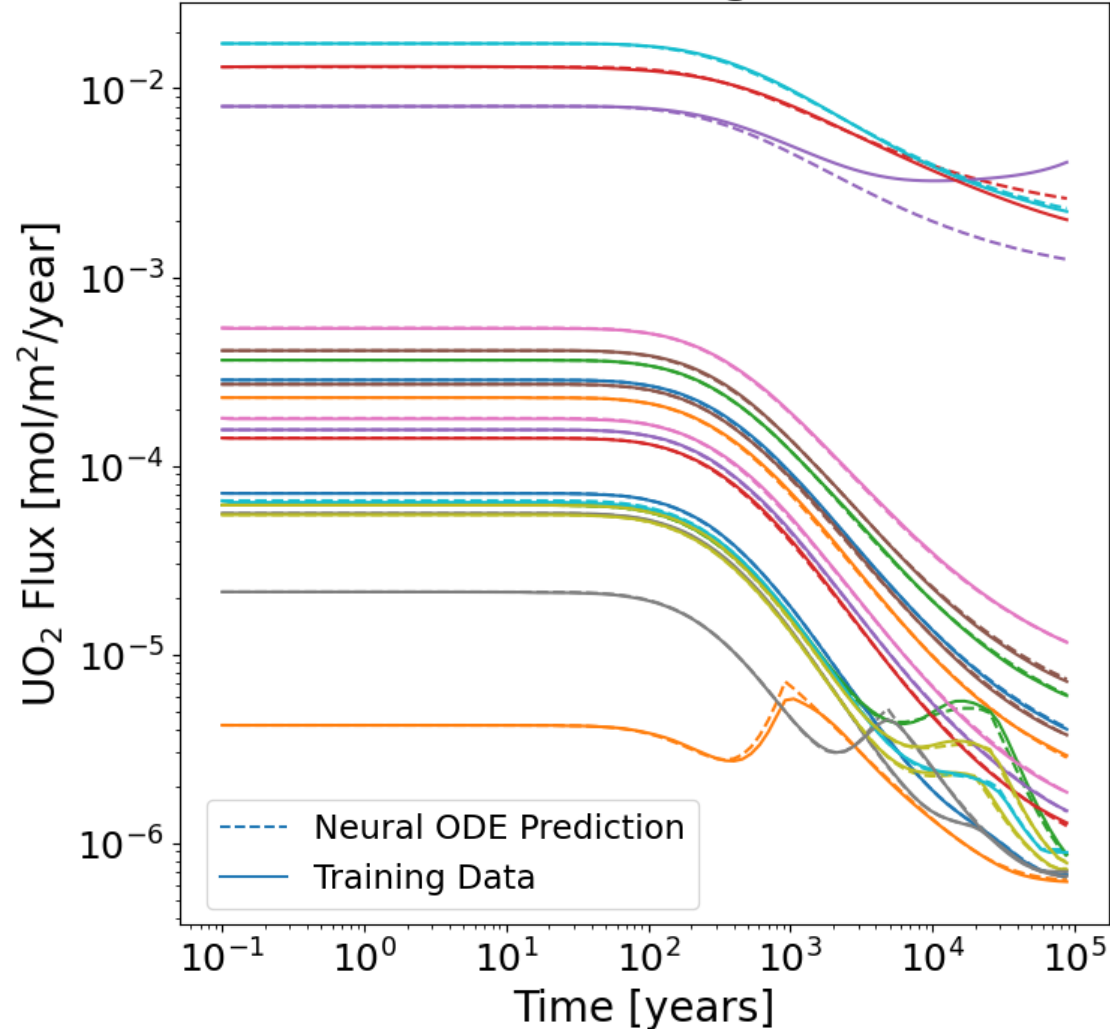


- Batch\_time = 20 yields the lowest validation loss

Note: For each batch\_time, batch\_size = # time steps –

# Prediction of FMD Validation Data from Initial Flux

20 Random Training Predictions

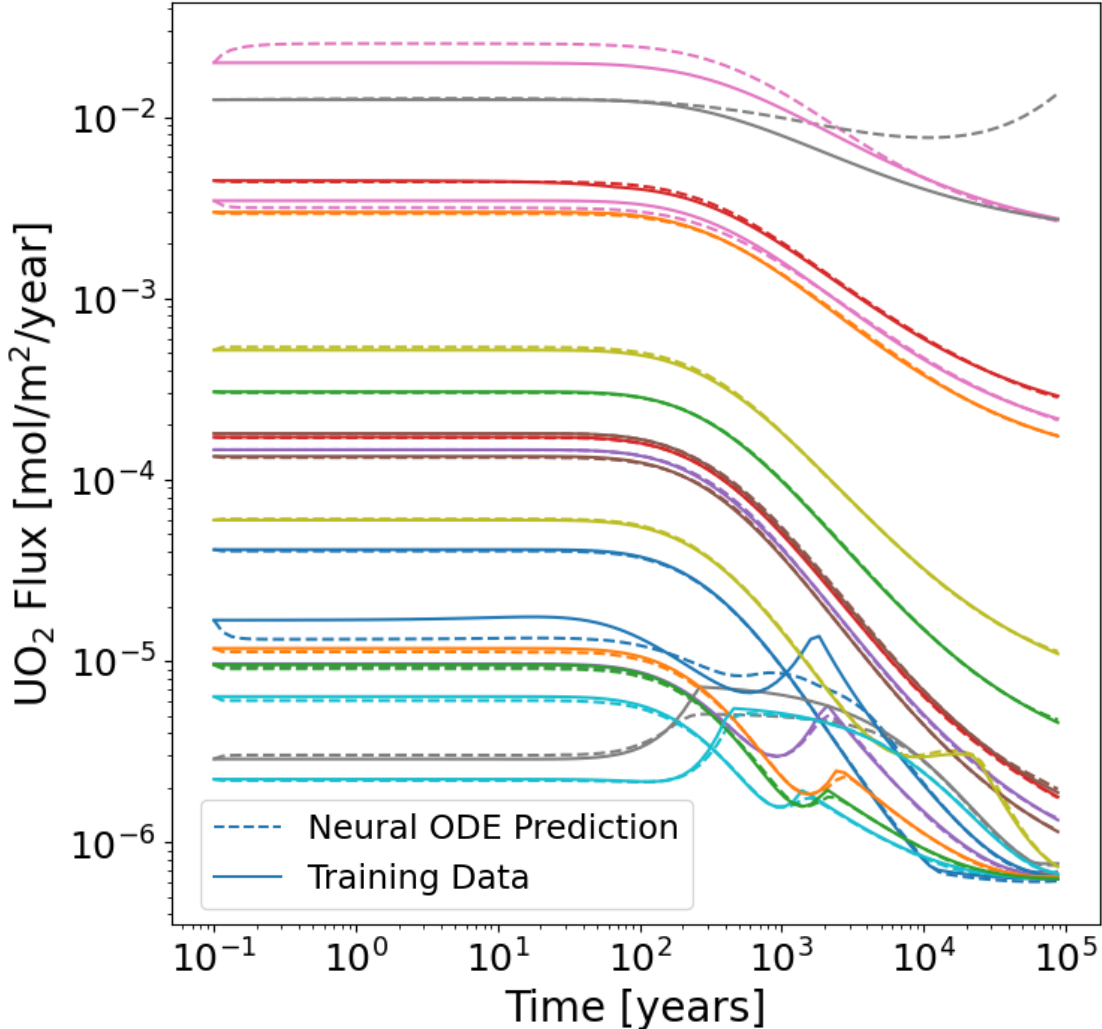


MAE = 0.0072875

NRMSE =

0.066859

Validation Predictions



MAE = 0.0095912

NRMSE = 0.230

# Conclusions and Future Work



# Conclusions and Ongoing Work

- Choosing an accurate ODE solver and a large enough batch\_time are crucial for learning the timing of the slope transition.
- Training requires over 100,000 epochs and may involve local minima in the loss.
- Neural ODEs have shown the ability to learn the dynamics of the FMDM data and predict a time trajectory from its initial condition, and therefore, have potential as a surrogate.
- Ongoing Work
  - Further Hyperparameter tuning of
    - Number of trajectories of training data
    - Number of time steps in training data
    - Choice of numerical solver
  - Cross-validation for hyperparameter tuning
  - Evaluation on testing data

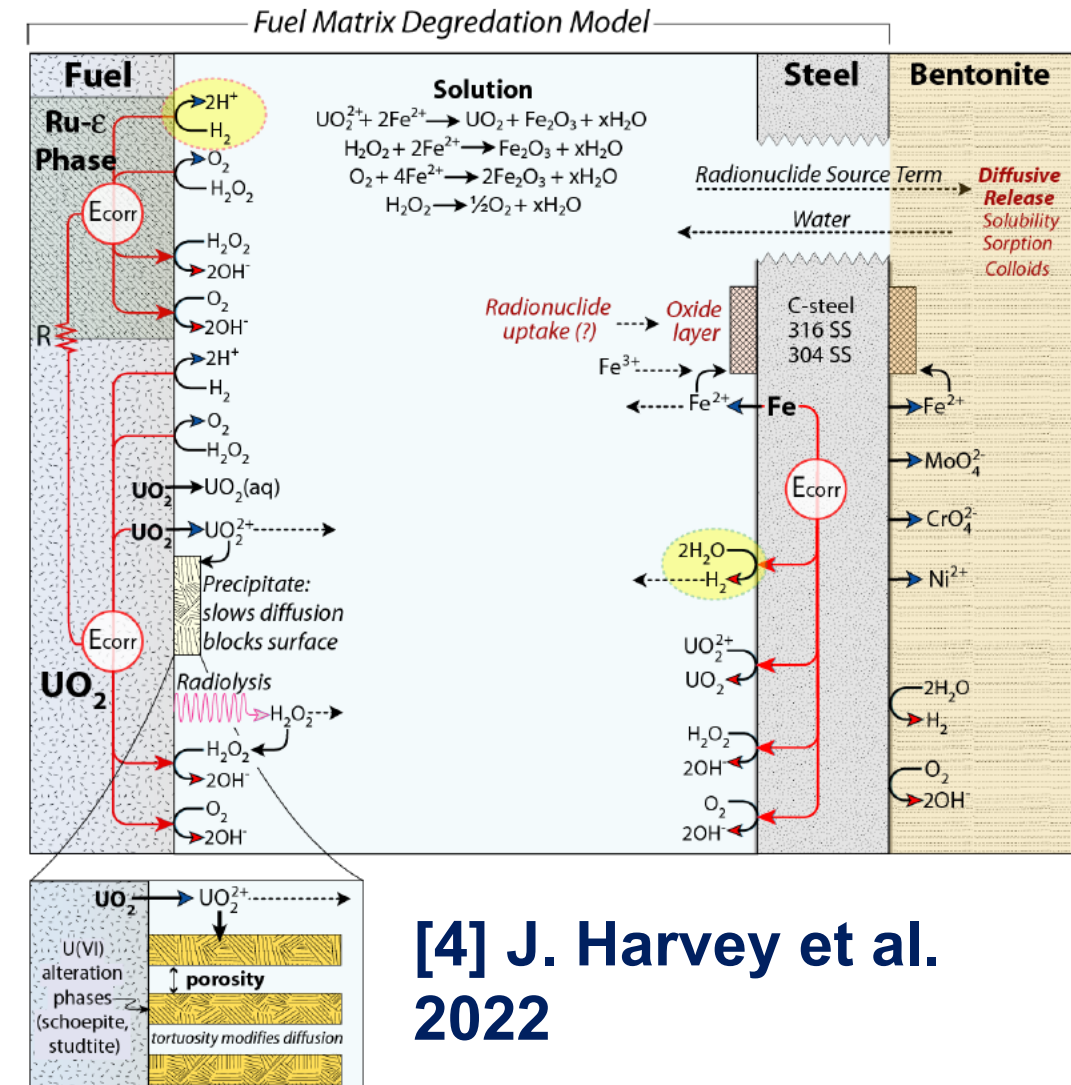
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2. J. Jerden, K. Frey, and W. Ebert, “A Multiphase Interfacial Model for the Dissolution of Spent Nuclear Fuel,” Journal of Nuclear Materials, 462, 135, <https://doi.org/10.1016/j.jnucmat.2015.03.036> (2015)
3. Chen, Ricky T. Q., Yulia Rubanova, Jesse Bettencourt, and David K. Duvenaud, “Neural Ordinary Differential Equations.” Advances in Neural Information Processing Systems 31 (2018).
4. J. Harvey et al.: Development of an Efficient Version of the Fuel Matrix Degradation Model, IHLRWM 22 (2022)

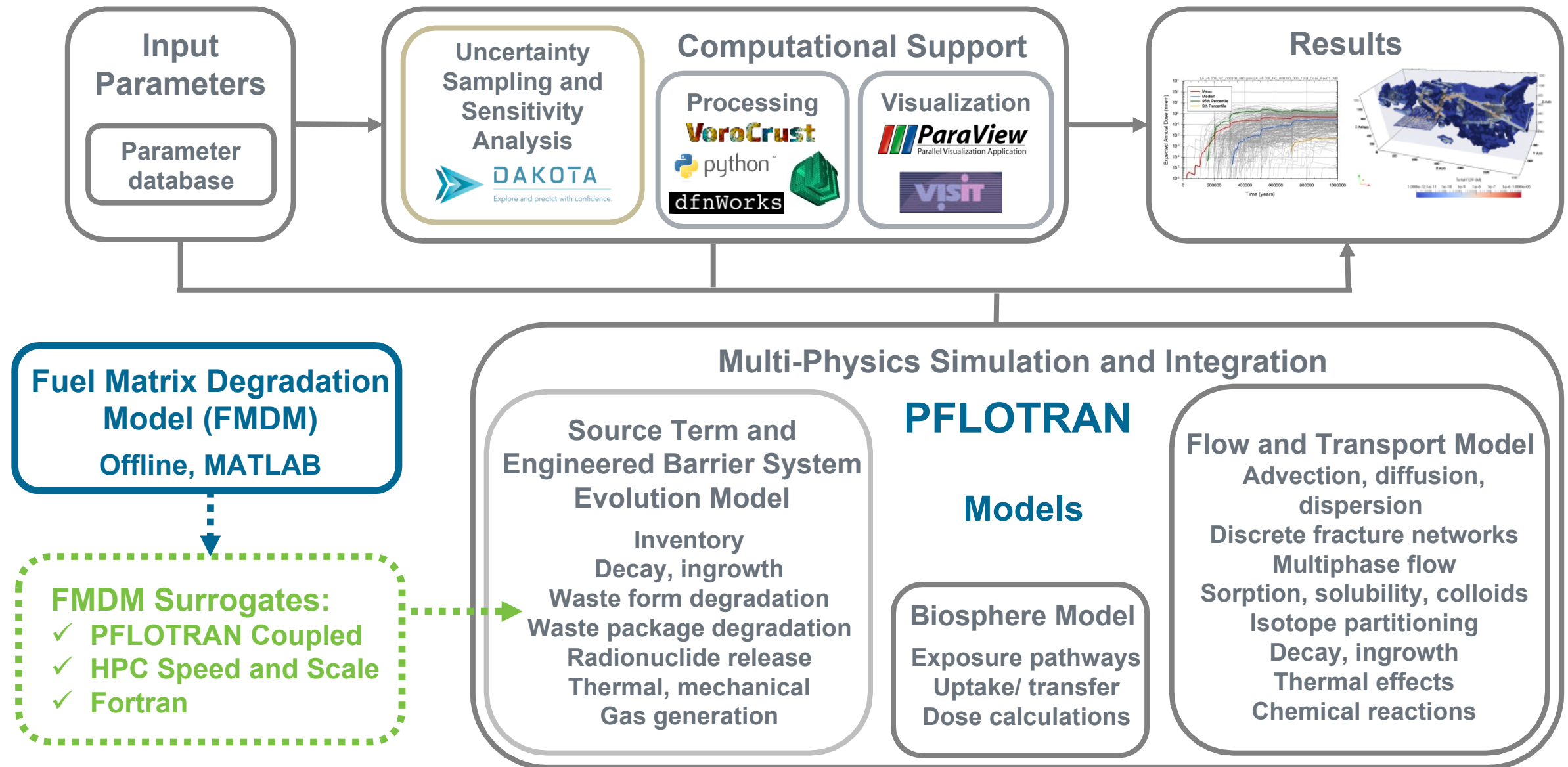
# Additional Materials

# The Fuel Matrix Degradation (FMD) process model computes the degradation rate of spent nuclear fuel

- 1D reactive-transport model (diffusion only)
- Chemical (slow) and oxidative (fast) dissolution of  $\text{UO}_2$  matrix
- Hydrogen peroxide production via alpha-radiolysis
- Precipitation and dissolution of U(VI) (i.e., schoepite) corrosion layer at the fuel surface
- Arrhenius temperature dependence
- Complexation of uranium with carbonates
- Hydrogen as an oxidation sink (focused on fuel interface)
- Logarithmic spatial discretization for enhanced accuracy near the solid interfaces

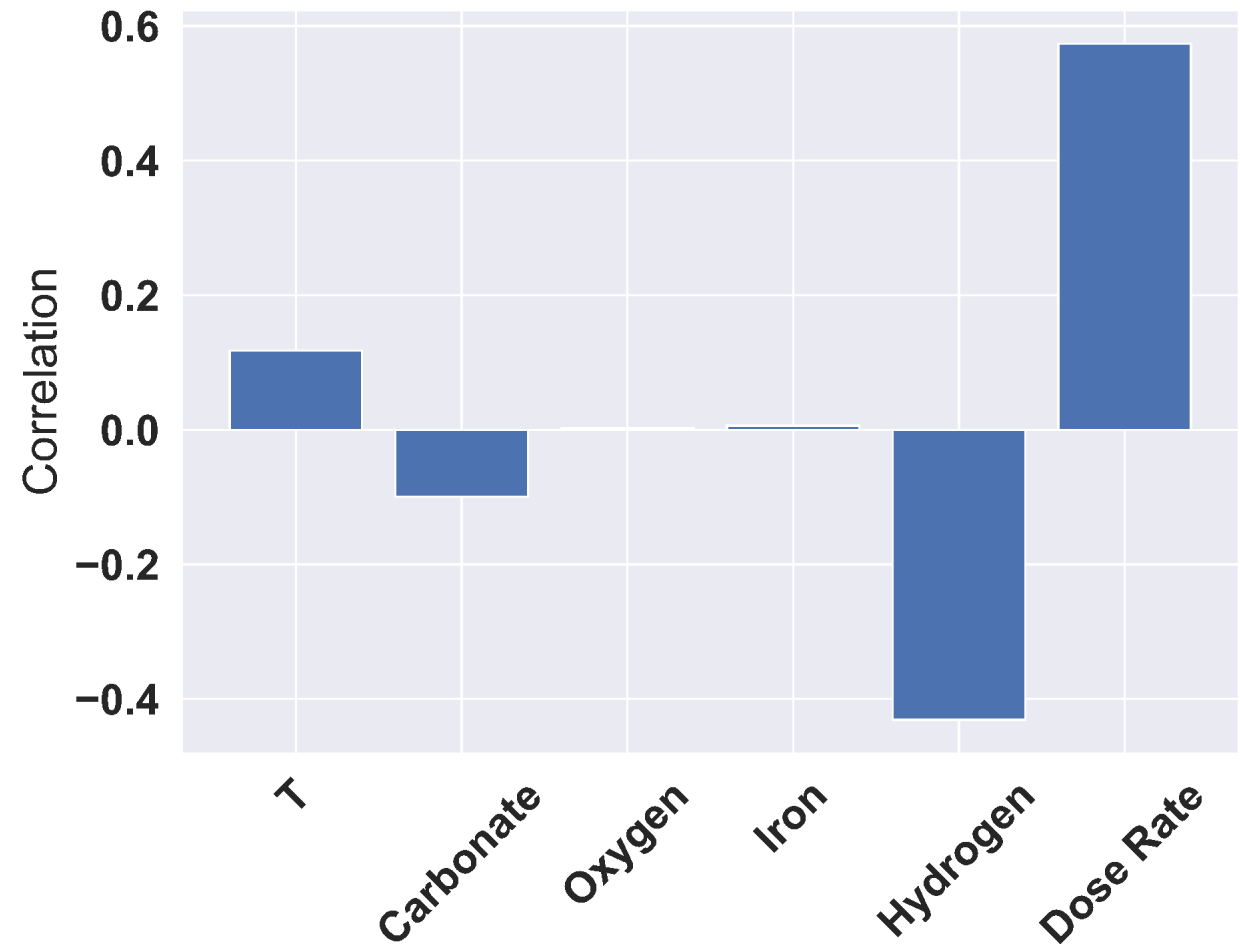


# 27 Surrogate FMD models can alleviate cost of UO<sub>2</sub> flux computation in probabilistic repository assessments



# Model inputs that do not impact the fuel degradation rate much can be dropped

- Correlation between fuel degradation rate and  $O_2$ ,  $Fe^{2+}$  is very small



# Data conditioning improves the quality of the training data

- Remove FMD process model runs that are physically unrealistic
  - Runs that do not finish
  - Runs that stagnate at late time
  - Runs with Corrosion Layer Thicknesses that exceed physical domain size
  - Runs with  $\text{UO}_2$  (aq) over 2 times the solubility concentration
- Log-transform data
- Scale between -1 and 1



# A variety of metrics evaluate different elements of the surrogate model accuracy

- (Normalized Root) Mean Squared Error
  - Good metric for engineering purposes

$$mse = \frac{1}{N} \sum_{i=1}^N (y_{pred,i} - y_{true,i})^2$$

- Mean Absolute Percentage Error
  - Highlights errors in small values

$$nrmse = \sqrt{\frac{1}{N} \sum_{i=1}^N (y_{pred,i} - y_{true,i})^2}$$
$$mape = \frac{1}{N} \sum_{i=1}^N \left| \frac{y_{pred,i} - y_{true,i}}{\frac{1}{N} \sum_{i=1}^N y_{true,i}} \right| \times 100$$

- Mean Absolute Error
  - Not as sensitive to outliers

$$mae = \frac{1}{N} \sum_{i=1}^N |y_{pred,i} - y_{true,i}|$$