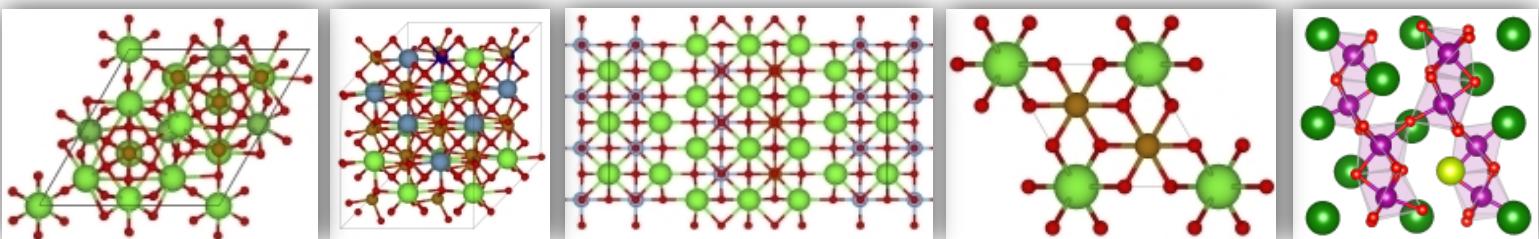




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Machine learning driven discovery and modeling of materials for hydrogen storage and generation



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Experiments

Machine Learning

first principles/DFT

data infrastructure

Introduction:

Methodology and applications

- Graph neural networks for modeling & discovering hydrogen energy materials

Part I, H₂ generation:

Accelerated screening of oxides for high-T clean energy applications

- graph neural networks / direct vacancy property predictions / high-throughput screening

Part II, H₂ storage:

Modeling of (super)-hydrides for hydrogen storage and beyond

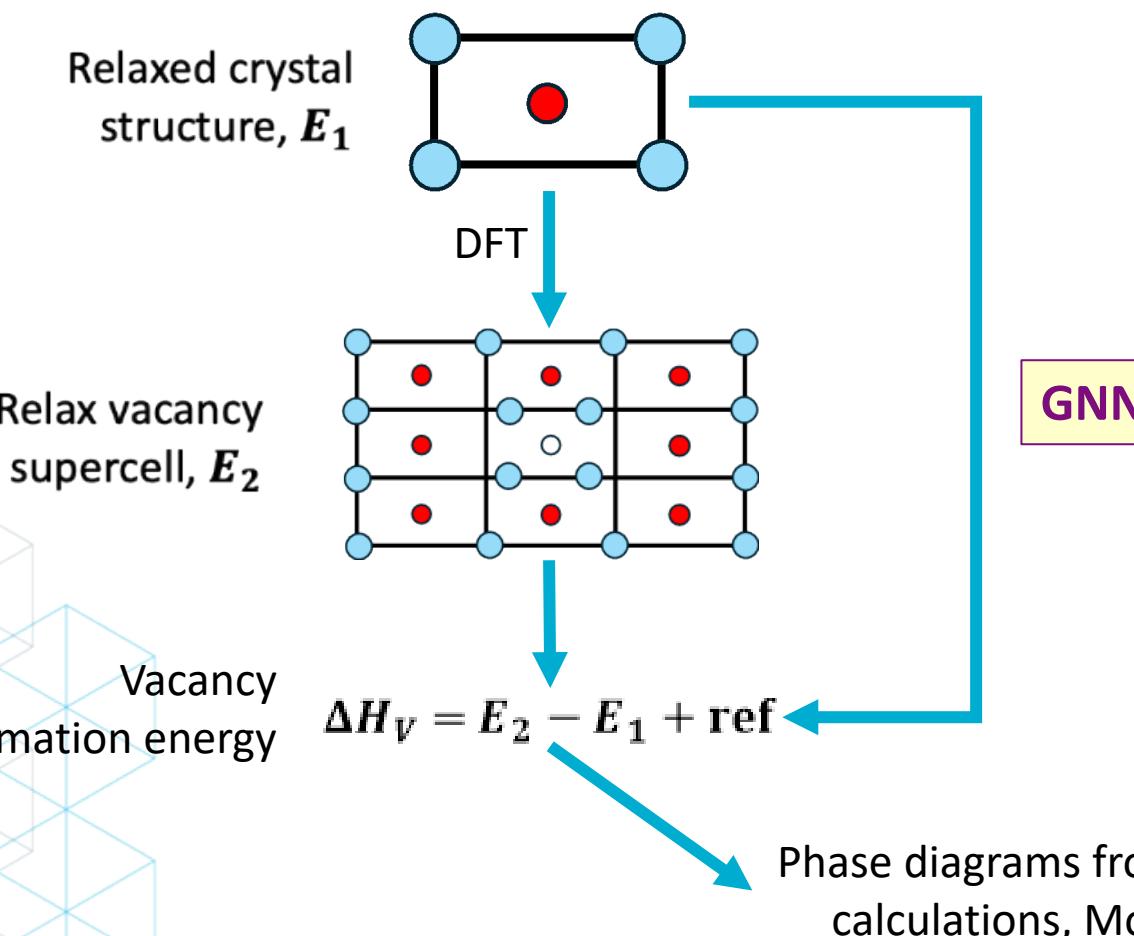
- graph neural networks / screening + statistical sampling / metal-hydrogen phase diagrams

Central methodology theme: Use graph neural networks (GNNs) as a surrogate model for expensive DFT relaxations in *the limit of low data*

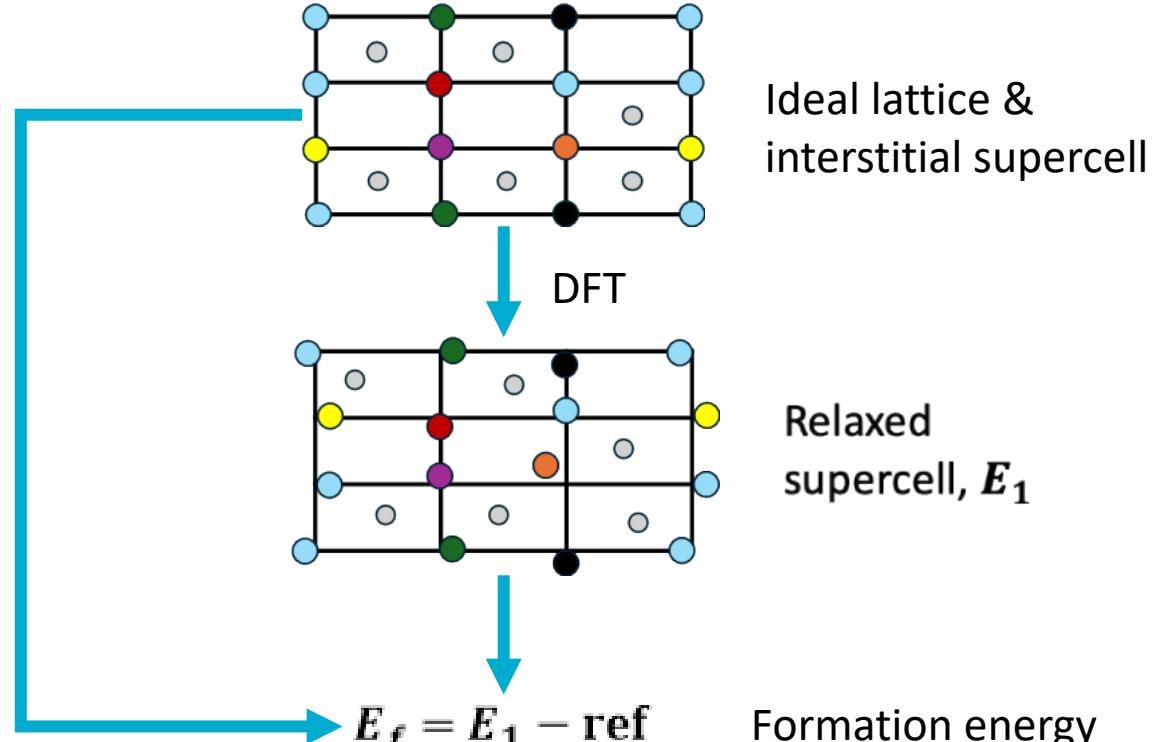


- **Goal:** Predict DFT-relaxed energy of a defected crystal structure from an unrelaxed representation
- For the *most* accurate quantum chemical methods (beyond DFT), we will be data limited for the foreseeable future

Example 1: Vacancy defects



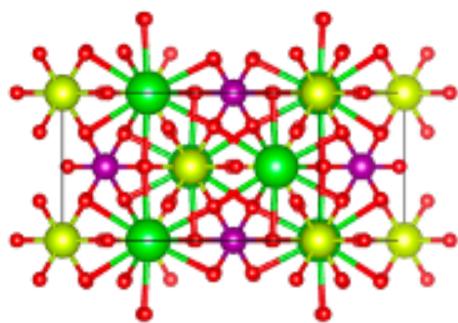
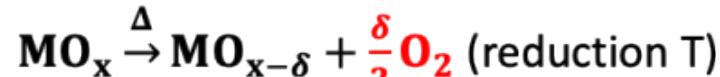
Example 2: Interstitial lattice defects in an alloy



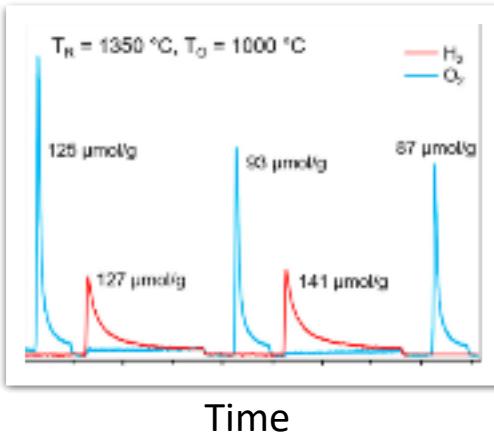
Central application theme: **Experimental and/or 1st principles calculation trial-and-error discovery of new & improved hydrogen materials solutions is too costly**



Application #1: (High entropy) metal oxides for solar thermochemical (STCH) H₂ generation



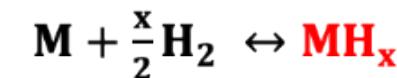
Production Rates



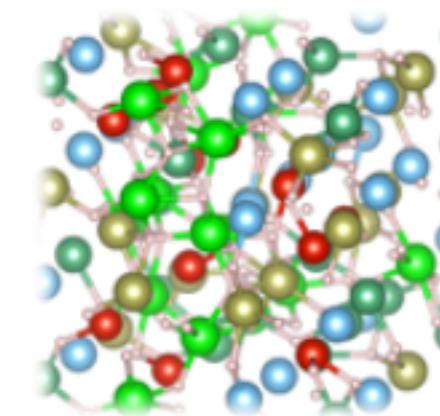
Experiments: Measure H₂ / O₂ production rates

1st principles: Compute ΔH of oxygen vacancy formation

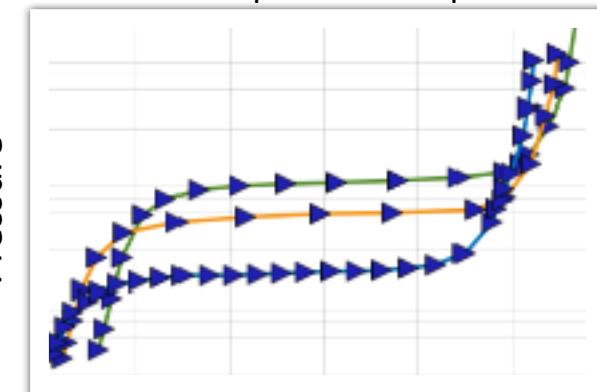
Application #2: Metal (super)-hydrides from (high entropy) alloys



Pressure-Composition-Temperature



Pressure



Experiments: Measure PCT curves (ΔH , ΔS , and capacity)

1st principles: Low-sample estimation of ΔH

Months to synthesize and fully characterize and test a material

Months to predict even *just a proxy* for performance for a small # of materials

Part I:

Accelerated screening of oxides for high temperature, clean energy applications^[1]



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Key concepts:

- Graph neural networks to directly predict *relaxed vacancy properties* from the host structure
- High-throughput screening of vacancy formation enthalpies
- New oxides for water-splitting, fuel cells, CO₂ conversion, and thermochemical energy storage



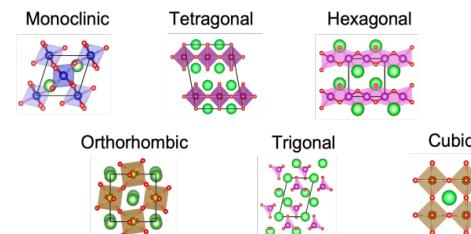
Discovering oxides for clean energy, and specifically solar thermochemical water splitting (STCH) materials



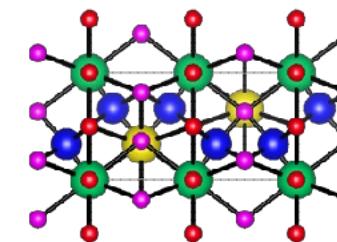
1. **Application:** motivation for H_2 production via solar thermochemical water-splitting (STCH)



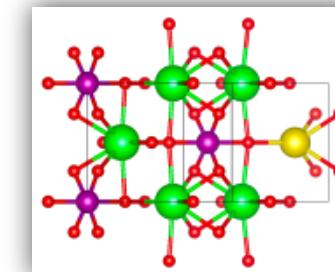
2. **Challenge:** expense of experiments and quantum mechanical based methods



3. **Solution:** surrogate modeling with defect graph neural networks



4. **Screening & validation:** (re)discovery of water-splitting metal oxides



Application: why focus on (green) hydrogen production *without* renewable electrons?



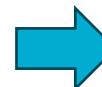
(1) Why H₂?

2022 US Energy demand:

~35% electricity

~20% fuels (cars)

~45% fuels (other)



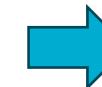
(2) The mismatch problem

2022 Renewable additions:

~90% electricity

~10% fuels (H₂, biofuels, ...)

<https://www.eia.gov/energyexplained/us-energy-facts/>



(3) Why produce H₂ without electrolysis?

"renewables ... are growing quickly enough to meet almost all [growing electricity demand], suggesting we are close to a tipping point for power sector emissions"

As of early 2023, newly added renewable electricity capacity is still just **shy of meeting increasing electricity demand alone...**

(4) High-temperature, concentrating solar power (CSP) is proposed for a variety of decarbonization technologies



2010 LCOE : \$0.38/kWh → 2022 LCOE: \$0.12/kWh

- Thermal batteries
- Thermochemical energy storage
- CO₂ conversion
- H₂ production via solar thermochemical water-splitting (STCH)

➤ **STCH:** A potential pathway to green H₂ relying only on renewable heat, *not* renewable electrons

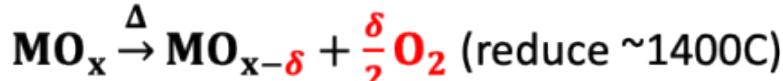
CSP in the cinema: In the dystopian sci-fi classic *Blade Runner 2049*, the world apparently went all in on CSP but failed 😞



Challenge: Experiments and calculations to find the best metal-oxides for STCH are difficult and time-consuming

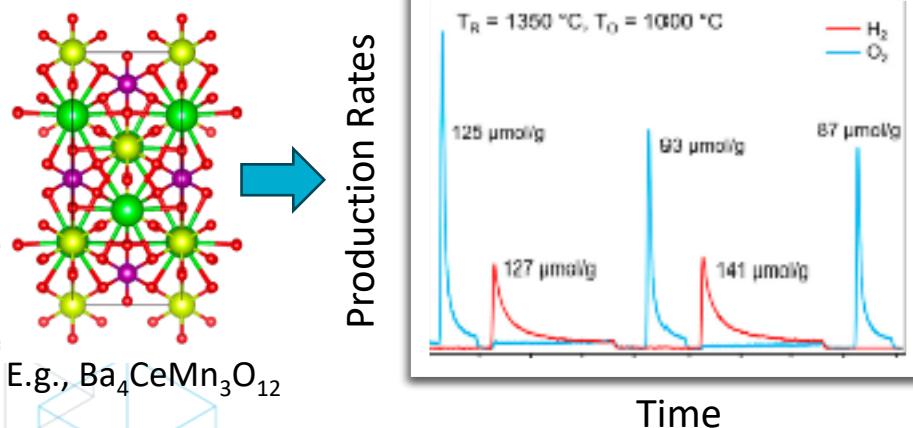


(1) STCH mechanism & experiments



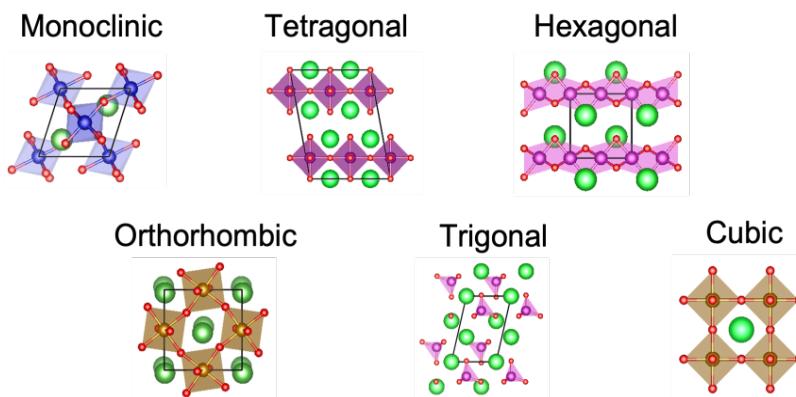
STCH efficacy first and foremost depends on *oxygen vacancy thermodynamics*

Experimentally measure H₂ & O₂ production:



Months to synthesize and fully characterize and test a single material

(2) Density functional theory (DFT)-based calculations of oxygen vacancy formation enthalpy (ΔH_{V_0})



Full search space		Training			
Li	Be				
Na	Mg				
K	Ca	Sc	Ti	V	Cr
Rb	Sr	Y	Zr	Nb	Mo
Cs	Ba	La	Hf	Ta	W
Fr	Ra	Ac	Re	Os	Ir
			Nd	Pm	Sm
			Eu	Gd	Tb
			Dy	Ho	Er
			Tm	Yb	

Calculated oxide space:

14 cations

~200 compounds

~1500 vacancy relaxations

~1 years' work

Screening oxide space (Materials Project):

~30+ cations

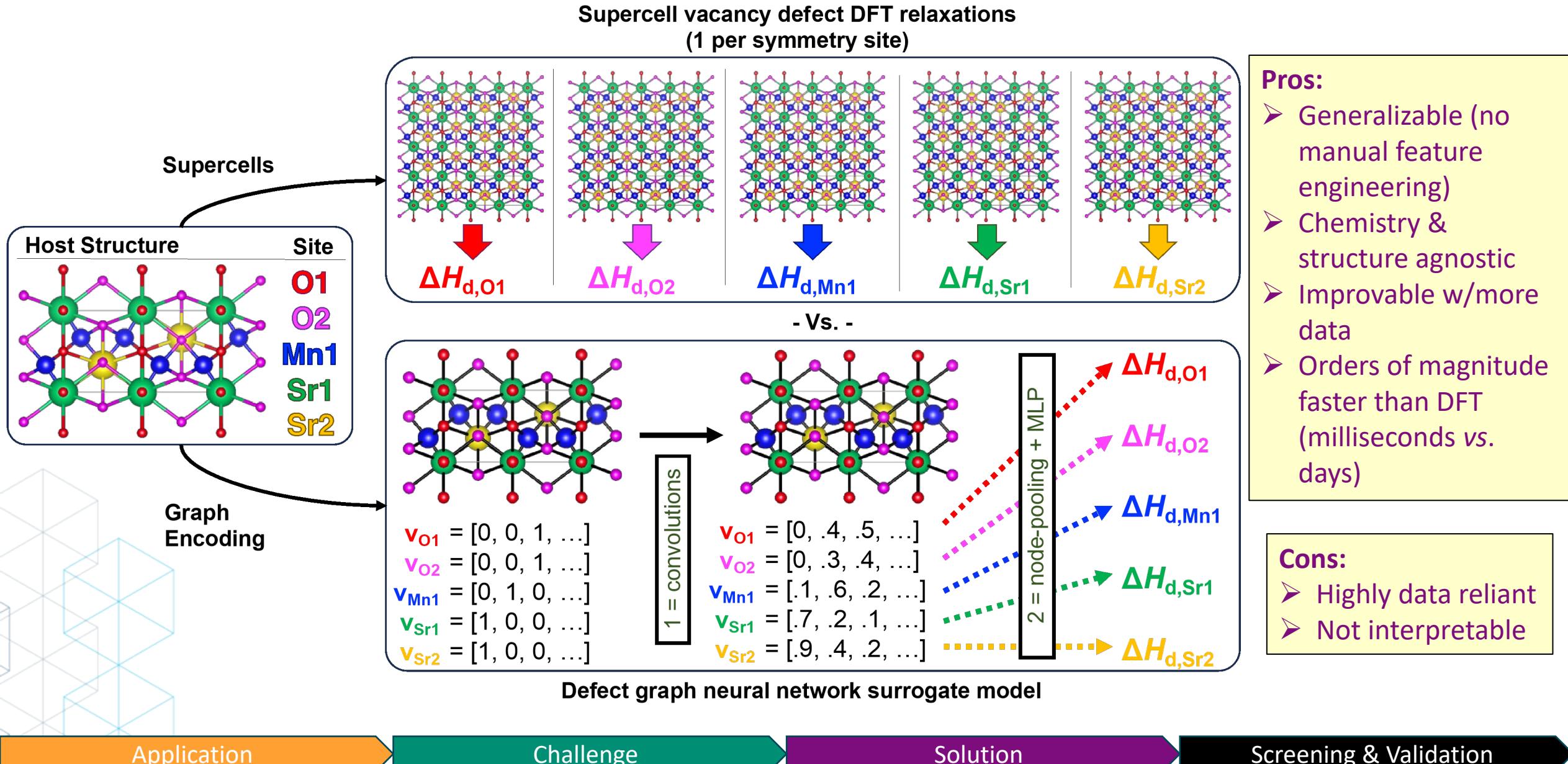
~10,000s+ compounds

~1Ms+ vacancy relaxations



100s+ years' work...

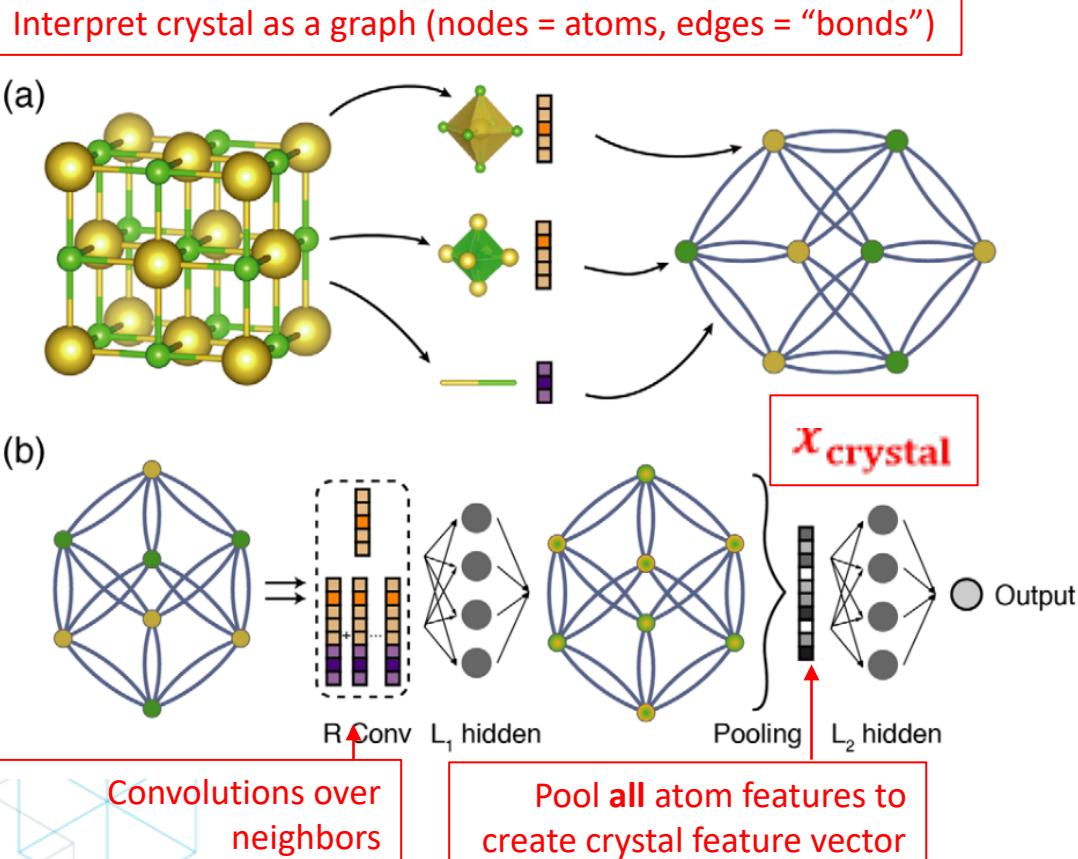
Solution: A generalizable, defect graph neural network (dGNN) model predicts vacancy formation energies many orders of magnitude faster than DFT



Automated feature extraction of graph neural networks (GNNs) enables efficient, generalized modeling of vacancy formation enthalpy



Automated feature extraction with GNNs^[1]



Deriving a "defect GNN" approach^[2]

Predict using only host structure, \mathbf{X}_h , and defect atom index, i'

$$\text{DFT: } \Delta H_d = E_{\text{DFT}}(\mathbf{X}_d) - E_{\text{DFT}}(\mathbf{X}_h) + \text{ref}$$

$$\text{ML: } \Delta \hat{H}_d = f_{\text{GNN}}(\mathbf{X}_h, i'; \theta)$$

➤ Example graph: v_1  e_{12}  v_2

➤ Encode the graph (step $t = 0$):

$$\mathbf{v}_1^{t=0} = \{r_0, \chi_0, \dots, s_1\}$$

Accuracy boosting, site-specific inputs (i.e. oxidation state)

➤ Convolutions ($t = 1 \dots T$)

$$\mathbf{v}_i^{(t+1)} = g \left(\mathbf{v}_i^{(t)} + \sum_j \sigma \left(\mathbf{z}_{ij}^{(t)} \mathbf{W}_1^{(t)} + \mathbf{b}_1^{(t)} \right) \odot g \left(\mathbf{z}_{ij}^{(t)} \mathbf{W}_2^{(t)} + \mathbf{b}_2^{(t)} \right) \right)$$

➤ Property prediction (node pooling):

$$\mathbf{x}_{\text{defect}} = \sigma(\mathbf{v}_{i'}^T \oplus \mathbf{v}_g \cdot \mathbf{W} + \mathbf{b})$$

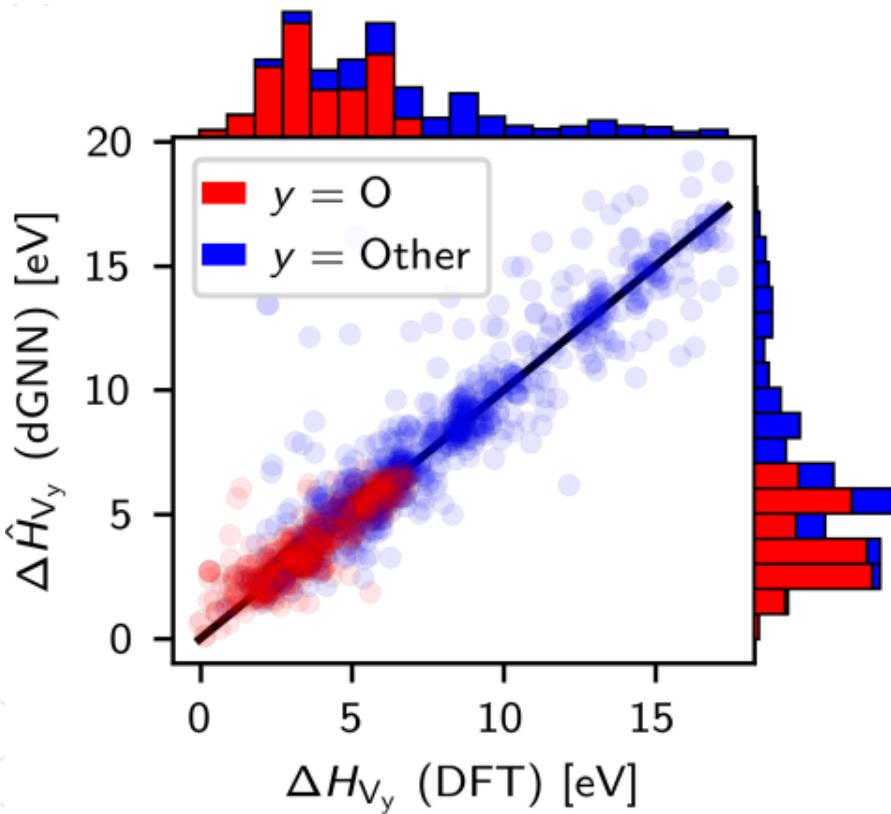
$$\Delta \hat{H}_d = \mathbf{x}_{\text{defect}} \cdot \mathbf{W} + b$$

➤ Node pooling at i'
➤ Can add host's global properties, $\mathbf{v}_g = \{\text{band gap}, \dots\}$

Screening & Validation: Improved performance of dGNN with architecture improvements and additional/more diverse training data



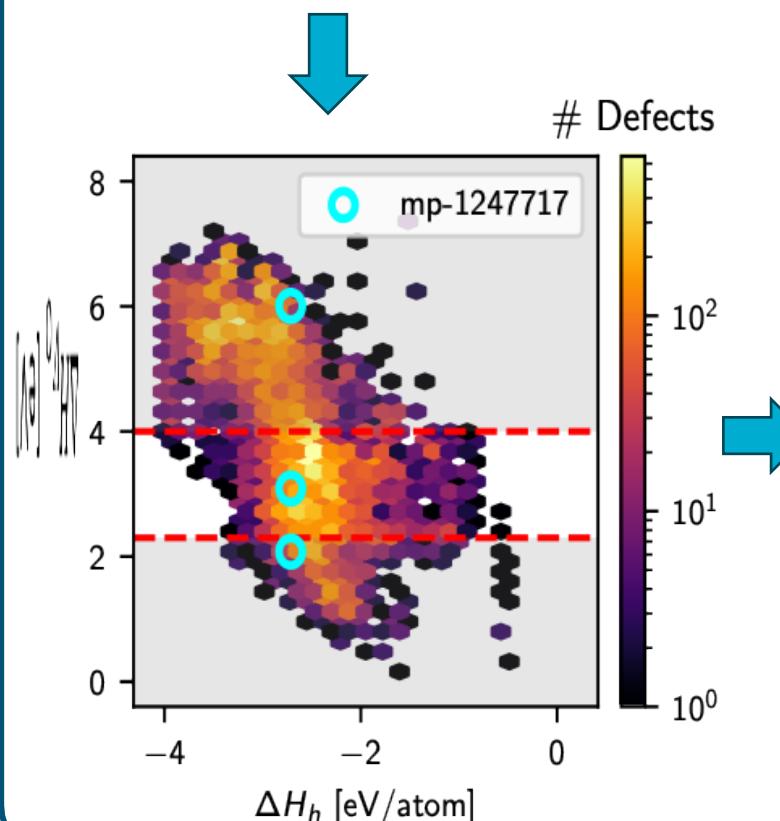
(1) dGNN validation



- Accurate and continually improving oxygen and cation vacancy predictions

(2) Materials screening, down-selection, and experimental validation

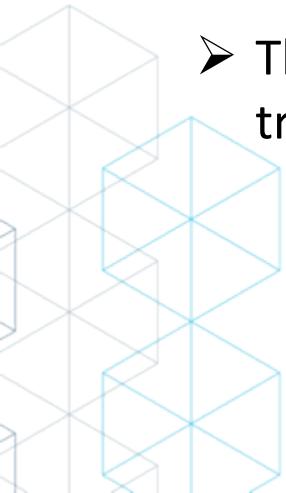
- Screen Materials Project oxide space for:
 - Target defect stability: $\Delta H_{V_O} \in [2.3, 4.0]$ eV
 - Target host oxide stability



- RedisCOVERS known water-splitters (e.g., $\text{Ba}_4\text{CeMn}_3\text{O}_{12}$, ...)
- Newly predicted, earth-abundant BaFe_2O_4 and $\text{BaFe}_{2-x}\text{Al}_x\text{O}_4$ are *experimentally validated*
- Many additional new materials to be tested (e.g., $\text{Sr}_3\text{PrMn}_2\text{O}_8$, ...)



- Accelerated materials discovery made capable by leveraging and adapting state-of-the-art machine learning techniques (GNNs) for defect predictions
DFT screening = *100s of years* ☹ → dGNN screening = *instantaneous* ☺
- (Re)Discovery of water-splitting oxides made possible (experimental papers coming soon)
- This approach is applicable to wide range of materials/applications (hydrides, nitrides, transition metal dichalcogenides, etc.), so long as we can generate the training data...





Part II: Modeling of (super)-hydrides for hydrogen storage and beyond^[1-3]

Key concepts:

- Graph neural networks on ideal lattices
- High-throughput screening of random alloy/interstitial configurations
- Predictions of thermodynamic properties from first-principles
- Direct calculation of metal-hydrogen phase diagrams

^[1] Witman, M. et al. *JPCL*, **2024** (15) 5

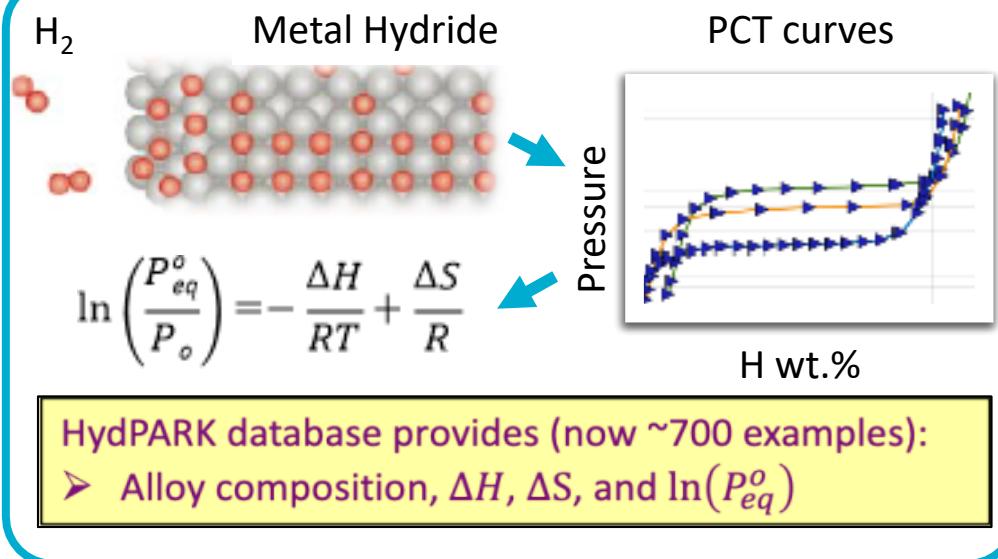
^[2] Way, L. et al. *In prep*

^[3] Guan, P. et al. *In prep*

Explainable machine learning models predict metal hydride thermodynamics



(1) $\ln(P_{eq}^o/P_o)$ target property



(2) Featurization for compositional ML model

Magpie features¹ \rightarrow (mean, stddev., etc) on elemental properties and their at.%

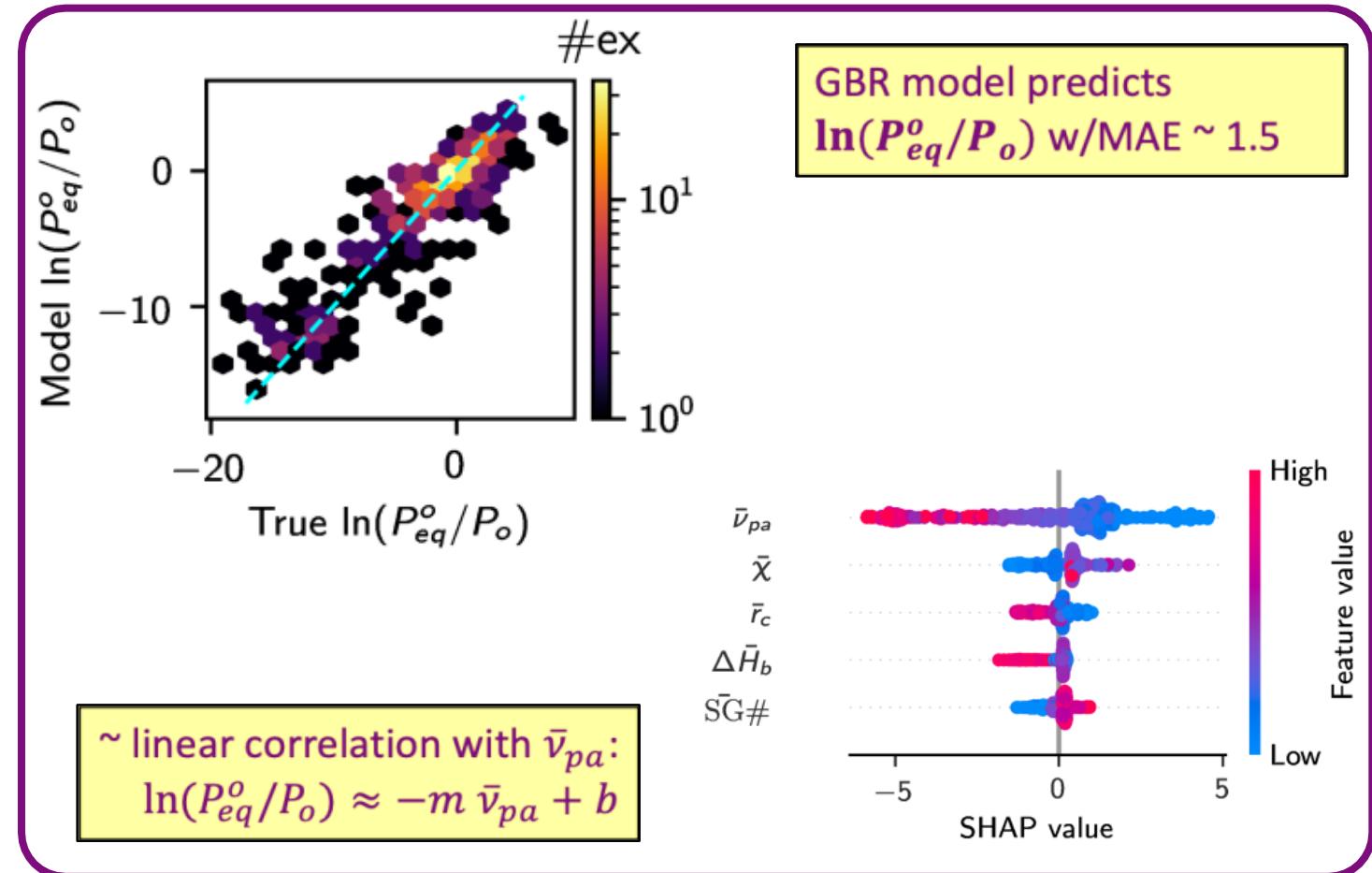
$$\text{TiFe}_{0.92}\text{Nb}_{0.08} \rightarrow \mathbf{x} = \{\bar{v}_{pa}, \bar{r}_{cov}, \bar{\chi}, \dots\} \in \mathbb{R}^{145}$$

$$\bar{v}_{pa} = \sum_i f_i v_i$$

$v_i \equiv$ ground state vol. per atom

$f_i \equiv$ composition frac. of element i

(3) Gradient boosting regression (GBR) model validation and explainability^[2-4]



^[1] Ward, L et al. *Comp. Mat. Sci.* **2018**, 152, 60-69

^[2] Witman, M. et al. *J. Phys. Chem. Lett.*, 11 (1), **2020**

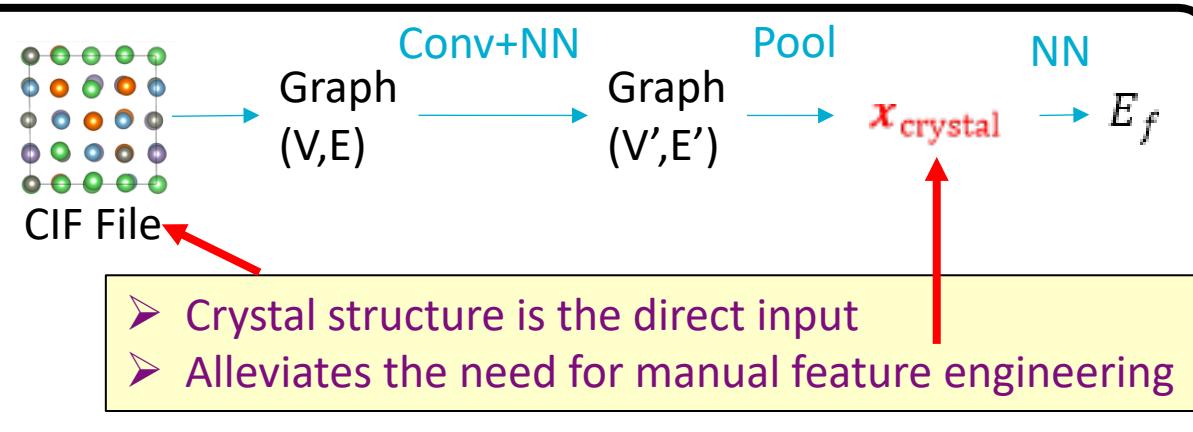
^[3] Witman, M. et al. *Chem. Mater.*, 30 (11), **2021**

^[4] Witman, M. et al. *J. Mater. Chem. A.*, 11 (29), **2023**

Graph neural networks (GNNs) on ideal lattice materials provide an attractive platform for high-throughput configurational screening in high entropy systems



GNNs 101: Property prediction from crystal structure input^[1]



Model inputs cannot rely on DFT-relaxed configuration

- A model that predicts \hat{E}_f from \mathbf{X}_{DFT} not useful because you would already have $E_{f,\text{DFT}}$:

$$\hat{E}_f = f_{\text{GNN}}(\mathbf{X}_{\text{DFT}}; \theta)$$

- Derive model inputs (crystal graph) from ideal lattice :

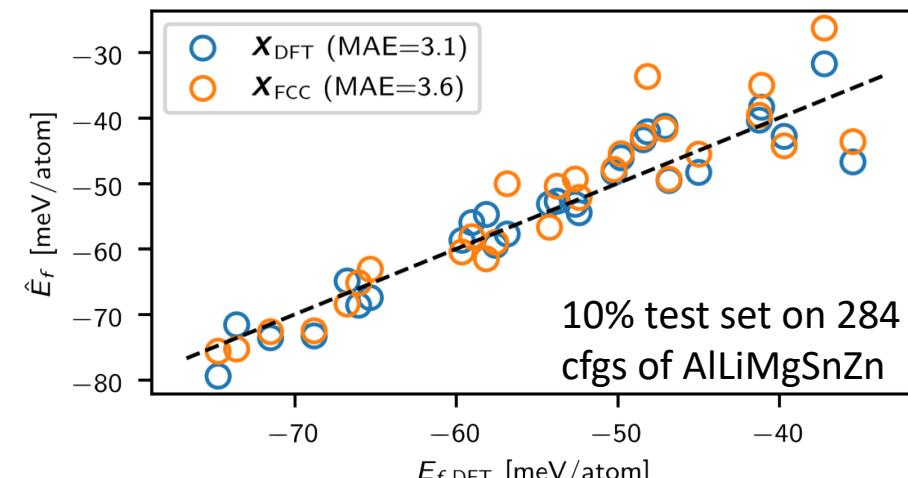
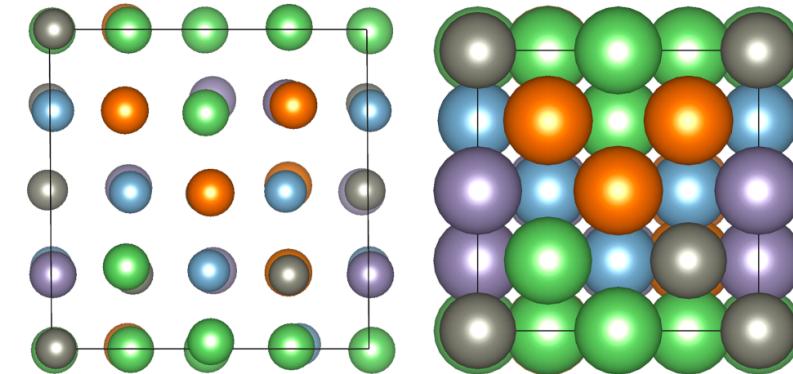
$$\hat{E}_f = f_{\text{GNN}}(\mathbf{X}_{\text{FCC}}; \theta)$$

\mathbf{X}_{FCC} is trivial-to-generate, so model can be run on millions of random HEA configurations

Negligible loss in performance using ideal representation^[2]

$$\mathbf{X}_{\text{DFT}} \begin{cases} a = 8.46 \\ b = 8.54 \\ c = 8.60 \end{cases} \begin{cases} \alpha = 91.42 \\ \beta = 90.81 \\ \gamma = 90.38 \end{cases}$$

$$\mathbf{X}_{\text{FCC}} \begin{cases} a_0 = 2 \\ a = b = c = 2a_0 \\ \alpha = \beta = \gamma = 90 \end{cases}$$



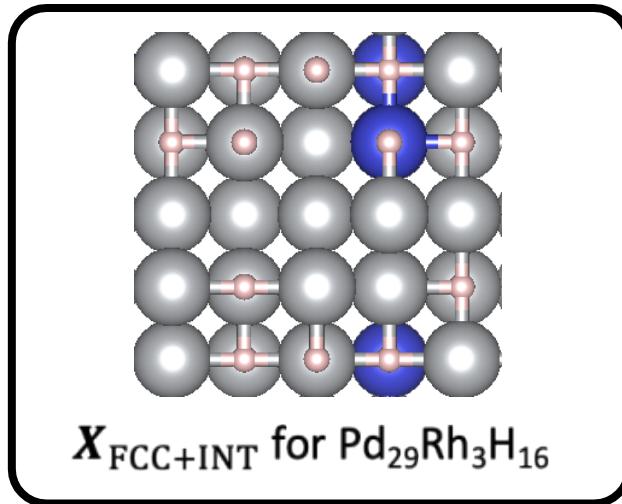
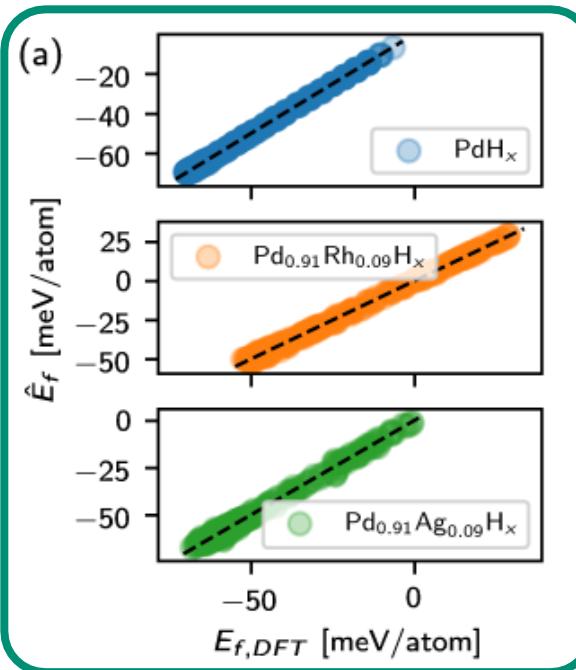
[1] Xie and Grossman. *P.R.L.* 120 (14), 2018

[2] Witman, M. et al. *J. Phys. Chem. Lett.*, 2024 (15) 5

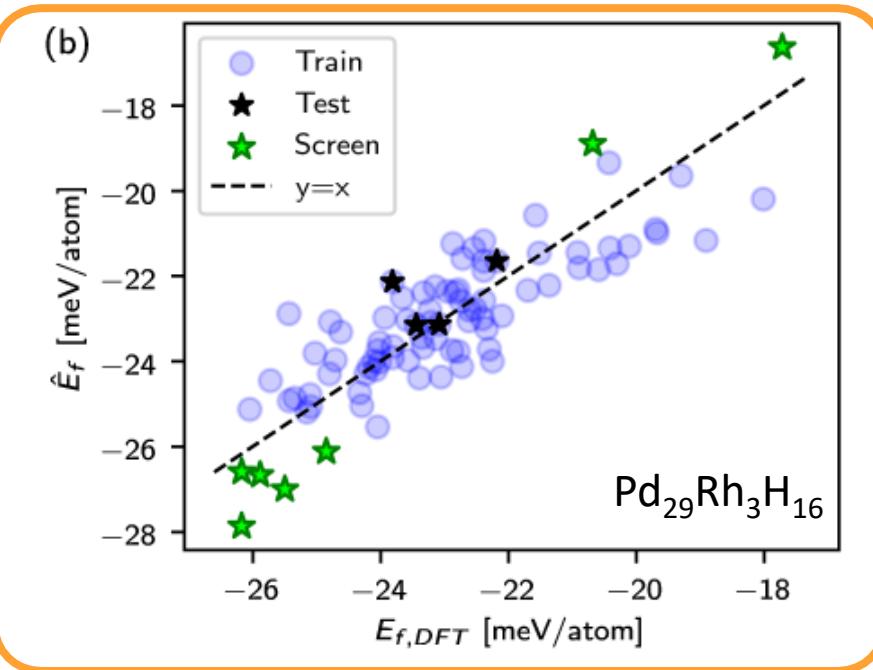
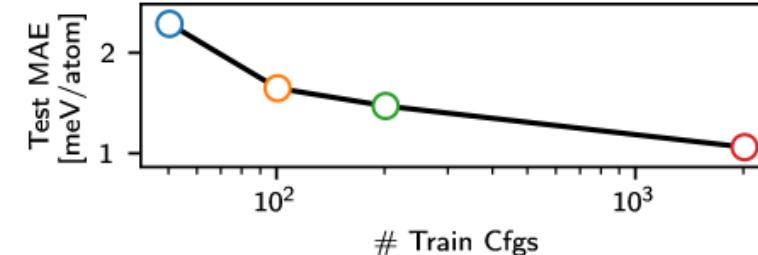
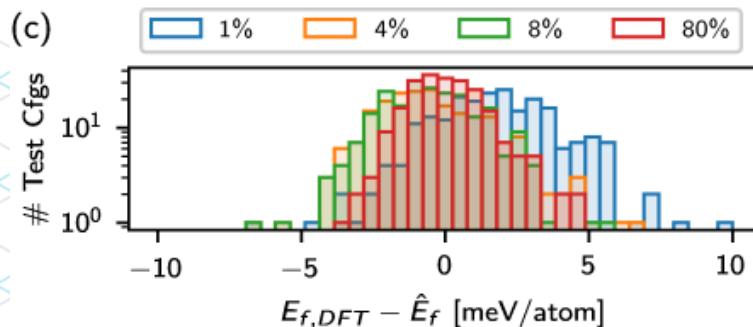
Approach is equally applicable to metal hydrides (random alloy + interstitial occupation)



Ideal FCC hydride representation

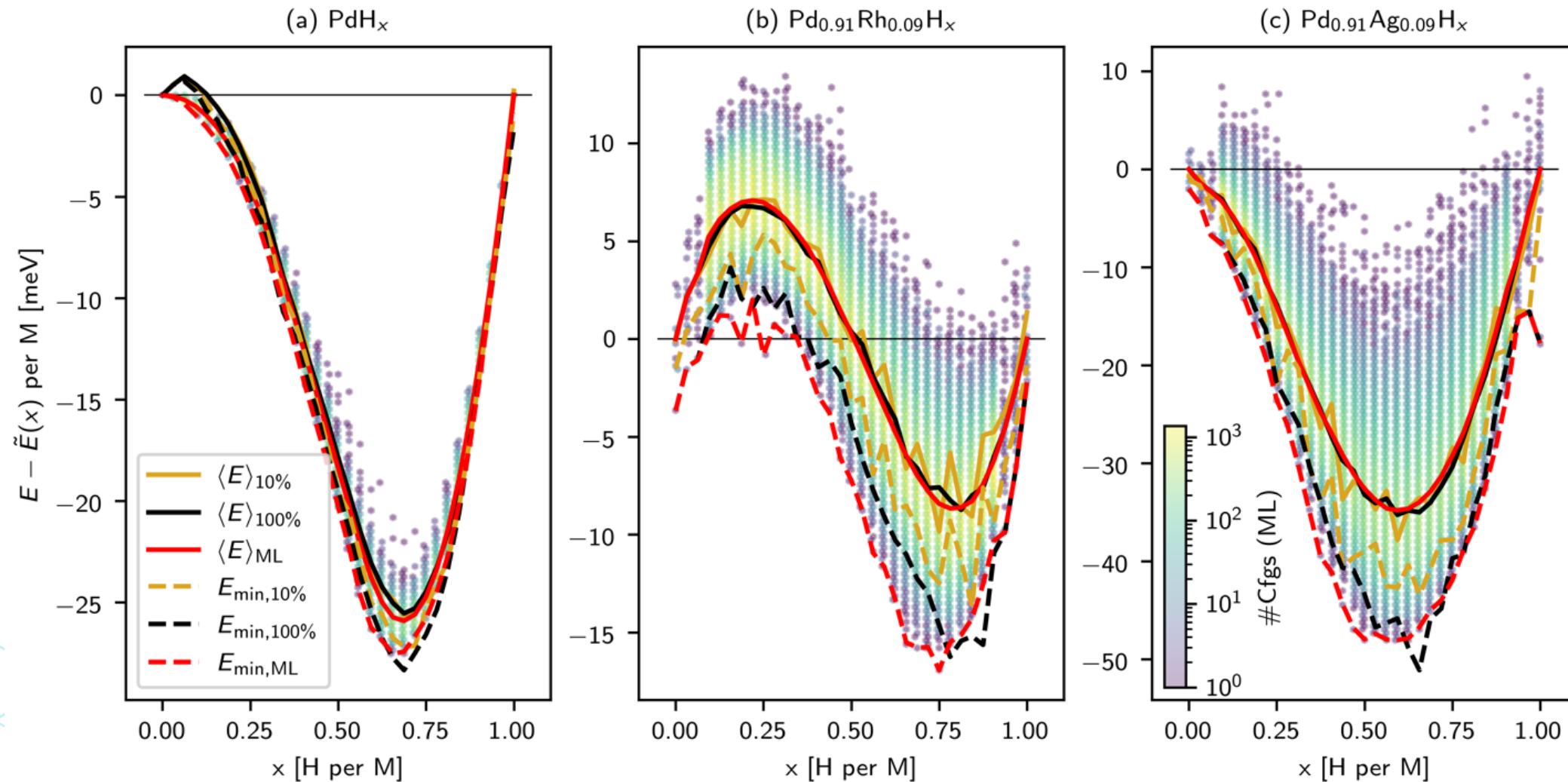
 $\sim 1 \text{ meV test MAE for } \text{Pd}_{29}\{\text{Rh,Ag}\}_3\text{H}_x$ 

Accurate screening outside train distribution

No outlier test set residuals and small MAE despite *small amount of training data*

Models are data-efficient: similar test MAE between 200 vs 2000 train configurations

High-throughput configurational sampling with GNN model identifies lower energy configurations than the brute-force DFT



- ~3,000 DFT cfgs per alloy system needed for $\bar{E}(x)$ convergence (10% of not sufficient)
- ML can screen O(Million) of cfgs, and finds lower energy than anything in training (especially PdRh)

Calculation of PCT curves (metal-hydrogen phase diagram from first principles calculations)



Mean field theory and Boltzmann weighted PCT calculation

Thermodynamic formalism/assumptions:

$$S(x) = k[(1-x) \ln(1-x) + x \ln(x)]$$

$$G(x) = E(x) - TS(x)$$

Energy calculation:

$$\text{MFT: } E(x) = \bar{E}(x)$$

$$\text{Boltzmann: } E(x) = \frac{\sum_i E_i e^{-E_i/kT}}{\sum_i e^{-E_i/kT}}$$

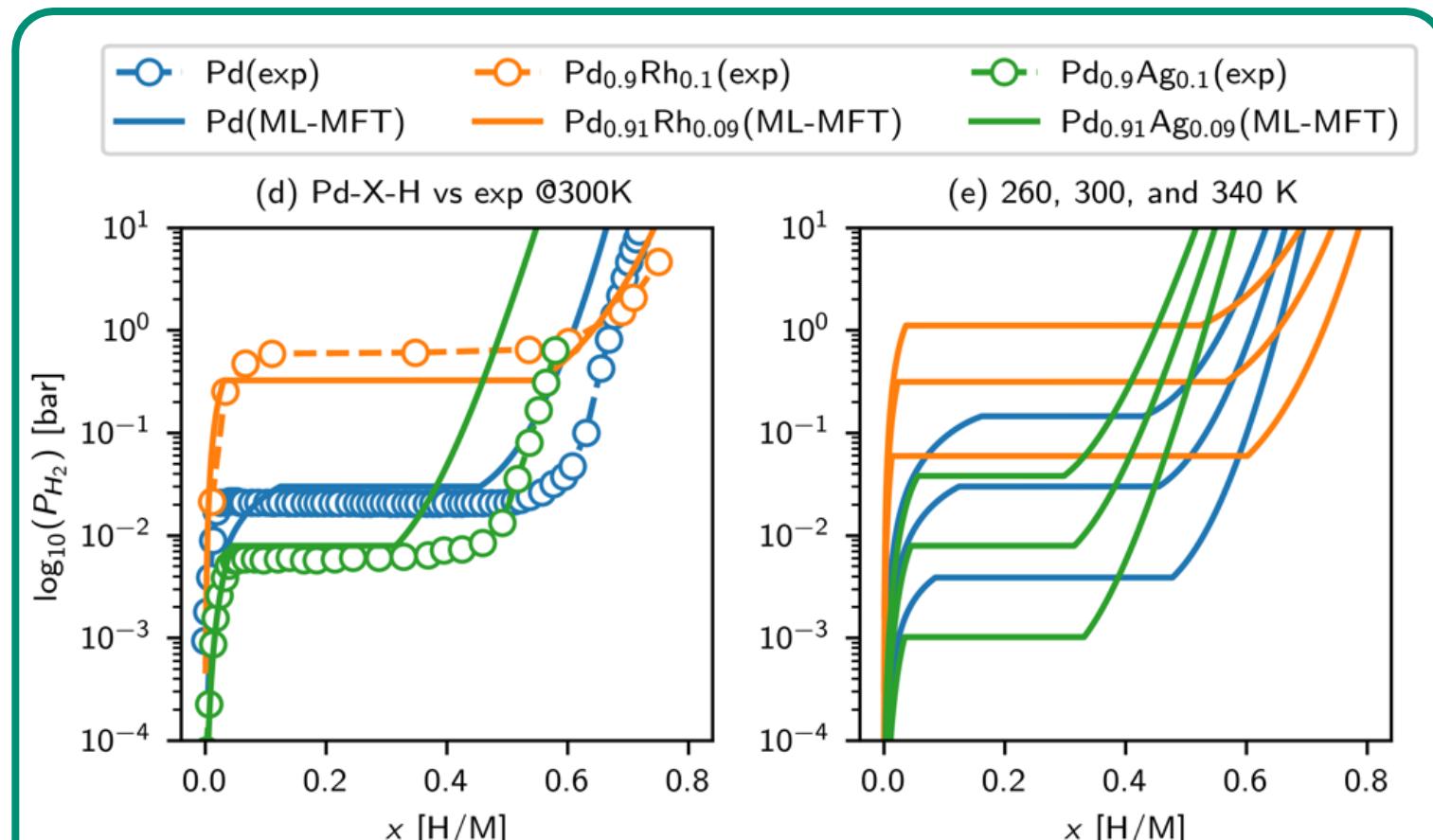
PCT:

➤ fit $G(x)$ to polynomial

➤ Differentiate w.r.t $x \rightarrow \mu$

$$p = p_0 e^{\mu/kT}$$

Comparison of computed vs experimental PCT



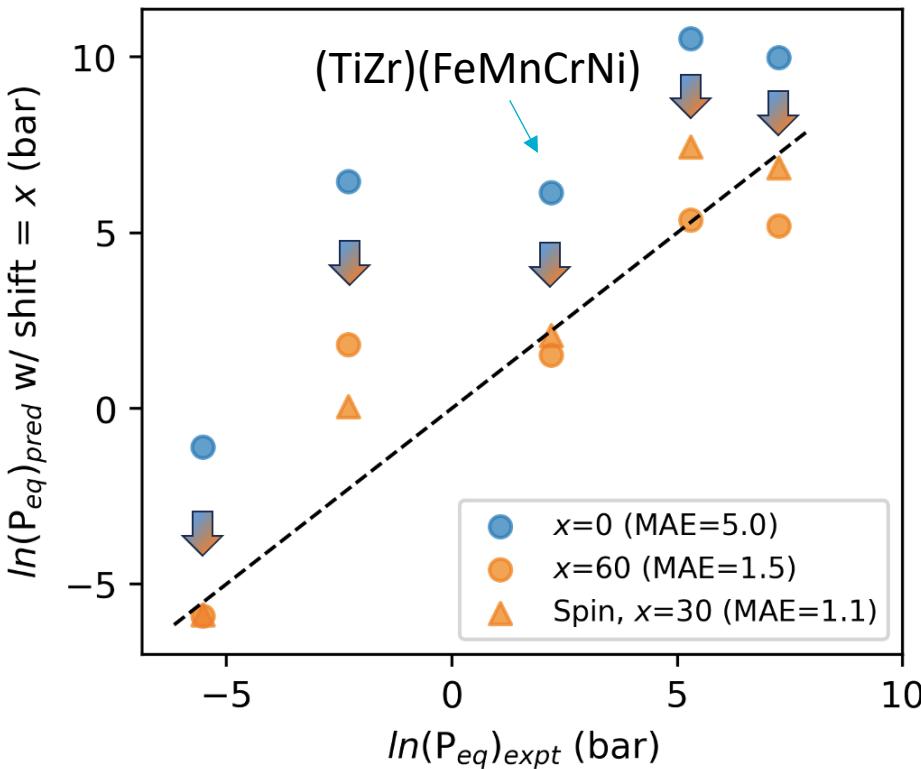
➤ Correctly rank plateau pressure, plateau widths, & H/M saturation between alloy systems

➤ Compute phase envelope

Next steps: Predicting hydrogen phase equilibria in more compositionally complex (super)hydrides



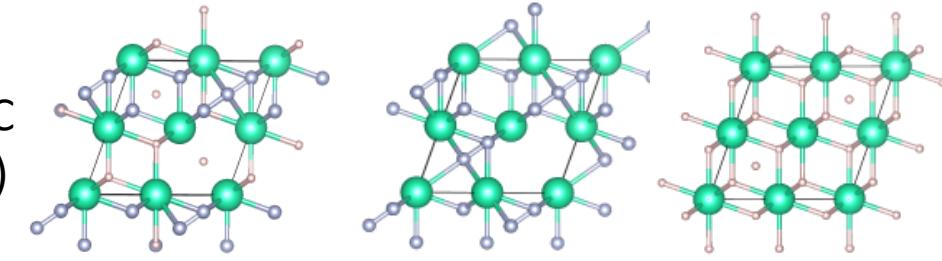
Predicted $\ln(P_{eq}^o/P_o)$ vs. experiment for compositionally complex AB2 alloys^[1]



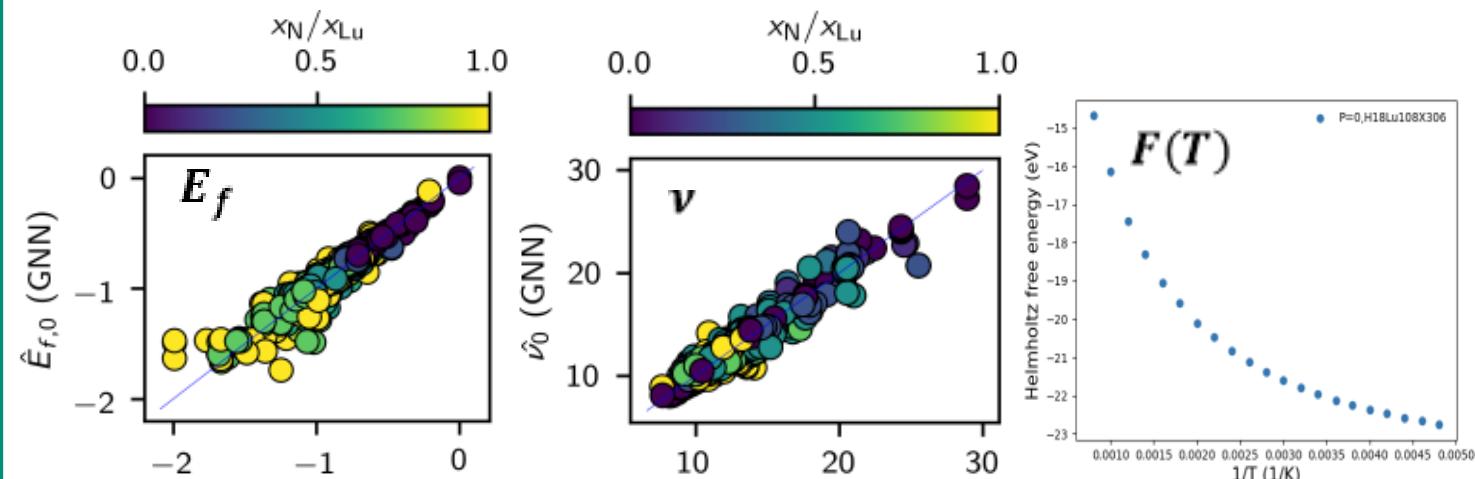
- DFT corrections needed
- Useful for discovering low stability hydrides (high-pressure compression materials)

Multi-interstitial (super)hydrides: $\text{Lu}(\text{N},\text{H})_{3-x}$ ^[2]

1. DFT relaxations of FCC $\text{Lu}(\text{N},\text{H})_{3-x}$ (~1,000 calc's)



2. Validate energy and volume configurational dependence



3. (μ_N, μ_H) phase diagrams from MC in progress

^[1] Way, L. et al. *In prep*

^[2] Guan, P. et al. *In prep*



- GNNs make screening of configurational energy landscape in compositionally complex materials tractable
 $\text{DFT screening} = 100s \text{ of years } \frown \rightarrow \text{dGNN screening} = \text{instantaneous } \smile$
- When coupled to first-principles calculations or simulations, GNNs can power predictions of phase diagrams needed to more wholistically evaluate hydrogen storage performance
- This approach will be particularly useful for predicting/modeling phase equilibria of (super)hydrides under extreme environments (hydrogen pressures) where experimental data is scarce and difficult to obtain



Thank you for your attention!

Questions/comments/collaborations?

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