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# Experimental and Kinetic modeling of soot formation in counterflow non-premixed flames of surrogate fuel components: n-dodecane and iso-dodecane

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## Abstract

Normal dodecane (n-C12) and iso-dodecane (i-C12) are often used as components for surrogate mixtures of aviation and diesel fuels. Although studies have been performed to understand the combustion and spray behavior of dodecane isomers, the soot formation from the combustion of n- and i-C12 in non-premixed flames is not well studied. In this work, soot volume fraction (SVF) profiles of n- and i-C12 were measured across a wide range of strain rates and mixture conditions in a counterflow burner facility at the University of Connecticut. Neat and binary mixtures of n- and i-C12 were investigated to study the influence of alkane branching on soot formation. A soot model was developed and validated in this study by extending the detailed kinetic model developed at the Lawrence Livermore National Laboratory (LLNL) for the formation of polycyclic aromatic hydrocarbons (PAHs) to simulate soot formation and growth based on the discrete sectional method. Additional gas phase reactions forming pyrene and ring enlargement reactions were added to the existing PAH model. The LLNL kinetic model was validated with SVF data obtained in this work for n-C12 and i-C12 flames along with data available in literature for ethylene, iso-butene, n-heptane and iso-octane. The soot precursor reactions added in this work were found to play a critical role in simulating the experimentally observed non-linear trend of the peak SVF with increased branched alkanes. Reaction path analysis was conducted to illustrate the fuel structure effects on soot formation pathways in n- and i-C12 mixtures. In view of the satisfactory agreement between modeling results and experimental data, as well as capturing the non-linear variation in peak SVF with the alkane branching for the first time, further investigation within the framework of the soot model is discussed and critical insights are provided into the reaction pathways which require further attention.

*Keywords:* counterflow non-premixed flame; soot; dodecane isomers; surrogate fuel components; kinetic modeling

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## Information for Colloquium Chairs and Cochairs, Editors, and Reviewers

### 1) Novelty and Significance Statement

Normal dodecane (n-C12) and iso-dodecane (i-C12) are commonly used as diesel and jet fuel surrogates. Although soot formation from n-C12 has been studied previously in the literature, soot studies of its highly branched isomer, i-C12, and blends of large n-alkanes and iso-alkanes have been meager. This is the first experimental study to measure soot volume fraction (SVF) in counterflow (CF) flames of n-C12, i-C12, and their blends with an aim to better understand the effects of alkane branching on soot formation and provide new soot measurements for model validation. A new soot model is also proposed and comprehensively validated for the first time across a wide range of CF flames involving commonly used surrogates for real complex fuels. Using the validated model, this study provides critical insight into reactions playing a key role in simulating the experimentally observed non-linearity in peak SVF as alkane branching in the fuel blend increases.

### 2) Author Contributions

*The authors should be identified by their initials and each author's contributions to the manuscript should be indicated by 2-3 words such as, for example, "designed research," "performed research," "analyzed data," "wrote the paper," etc.*

- **T.C.** Data curation; formal analysis; investigation; validation; writing – original draft; writing – review & editing.
- **C.S.** Validation; data analysis; supervision; writing – review & editing
- **X.X.** Investigation; formal analysis; data curation; writing – original draft.
- **G.K.** Validation; data analysis; supervision
- **W.J.P.** Writing – review & editing.
- **S.W.W.** Funding acquisition; project administration; supervision; writing – review & editing.
- **C.J.S.** Conceptualization; funding acquisition; project administration; supervision; writing – review & editing.

### 3) Authors' Preference and Justification for Mode of Presentation at the Symposium

The authors strongly prefer **OPP** presentation at the Symposium, for the following reasons:

- This paper is deemed to have the potential of adding value to the community through a room-audience-level discussion.
- This OPP can focus on outcomes and results without requiring the inclusion of extensive background information.
- We approach the subject that is different to other related work and contextual information is not deemed essential.

## 1. Introduction

2 Soot particles resulting from the incomplete  
3 combustion of hydrocarbons can lead to significant  
4 health hazards as well as global warming [1]. Efforts  
5 to mitigate these adverse effects have often taken the  
6 form of increasingly stringent emissions standards to  
7 reduce soot particulate matter. These stringent  
8 standards have made it progressively more  
9 challenging to achieve permissible levels of engine  
10 out soot using existing devices, fuels, and approaches.

11 Low-lifecycle carbon and low-sooting fuels such  
12 as renewable diesel and synthetic paraffinic kerosene  
13 are widely viewed as viable fuels to help mitigate  
14 adverse effects stemming from combustion  
15 applications. However, one impediment to utilizing  
16 combustion with low engine out soot is the inability  
17 to design and optimize combustors using predictive  
18 simulations of surrogate mixtures for sustainable  
19 fuels. Although kinetic models have been developed  
20 to simulate soot formation and growth at engine  
21 conditions, many studies have focused on ethylene  
22 ( $C_2H_4$ ) as a fuel since it is a significant intermediate  
23 formed during combustion [2-5]. Far fewer studies  
24 have focused on soot formation during the  
25 combustion of heavier fuel components and surrogate  
26 mixtures for complex fuels.

27 For instance, literature studies of reference  
28 compounds such as n-heptane (n-C7), iso-octane (i-  
29 C8), and toluene provide critical insights into the soot  
30 formation of larger linear alkanes, branched alkanes,  
31 and aromatics. These reference compounds are also  
32 template species for larger, less volatile components  
33 found in aviation and diesel fuels. While there are  
34 many ways to study the fundamentals of soot  
35 formation and growth for fuels, such as using sprays  
36 [6] and premixed flames [7], the literature most  
37 relevant to this work pertains to non-premixed flames.  
38 A very recent example of a single-component fuel  
39 includes the study of Zheng et al. [8] and Nobili et al.  
40 [9] which investigated soot formation from n-C7 in  
41 counterflow (CF) non-premixed flames by  
42 performing both experiments and numerical  
43 simulations. Also using co-flow non-premixed  
44 flames, Kashif et al. [10, 11] and Consalvi et al. [12]  
45 studied sooting tendencies of n-C7 and i-C8 binary  
46 mixtures. These binary mixture studies agree well  
47 with the broader literature which indicates that highly  
48 branched alkanes typically produce more soot than  
49 linear alkanes. Using CF non-premixed flames, Choi  
50 et al. [13] investigated soot formation in binary  
51 mixtures of n-C7, i-C8, and toluene. The authors  
52 observed a synergistic effect on the formation of  
53 polycyclic aromatic hydrocarbons (PAHs) as a  
54 function of toluene ratio in the n-C7/toluene and i-  
55 C8/toluene flames. Systematic investigations of  
56 toluene primary reference mixtures on PAH/soot  
57 formation have only been done recently by Park et al.  
58 [14] and Kruse et al. [15] by performing both

59 experiments and kinetic modeling studies. For CF  
60 flame of n-C7/i-C8, soot volume fraction (SVF)  
61 increases non-linearly as i-C8 branching increases.  
62 However, for n-C7/toluene and i-C8/toluene flames,  
63 Park et al. [14] observed that, although PAHs show a  
64 synergistic behavior, SVF increases monotonically as  
65 toluene content in the mixture increases.

66 Measurements of and models for soot formation  
67 from surrogate components of diesel and jet fuels,  
68 such as n-dodecane and iso-dodecane, are sparser. n-  
69 Dodecane (n-C12) is commonly used as a diesel and  
70 jet fuel surrogate component to represent the linear  
71 paraffins in complex fuels. In addition to being a  
72 surrogate component for complex fuels, iso-dodecane  
73 (i-C12; 2,2,4,6,6-pentamethylheptane) is also a  
74 primary reference compound for cetane  
75 measurements. Skeen and Yasutomi [6] studied soot  
76 growth for n-C12 in a high-pressure constant-volume  
77 spray chamber and observed that under high-pressure  
78 pyrolyzing conditions, the maximum rate of soot  
79 formation increases linearly with ambient  
80 temperature. Furthermore, a critical temperature of  
81 1550 K was observed above which the total soot mass  
82 did not increase with ambient temperature. Using a  
83 coflow non-premixed burner, Mitra et al. [16] studied  
84 the growth of PAHs and young soot from n-C12. The  
85 authors observed a rapid increase in PAHs when  
86 young soot transitions to a mature one. Wang et al.  
87 [17] proposed a reduced PAH mechanism for n-C12.  
88 The proposed PAH model was validated with ignition  
89 delays and species concentration profiles from shock  
90 tubes and jet stirred reactors (JSR). To the authors'  
91 knowledge, soot formation studies of n-C12 and i-C12  
92 have not been previously performed in a CF non-  
93 premixed flame.

94 In this study, new soot volume fraction  
95 measurements from soot formation in non-premixed  
96 flames of neat n-C12 and i-C12 were acquired using  
97 the University of Connecticut CF burner facility.  
98 Binary mixtures of n-C12 and i-C12 were also studied  
99 to better understand how large linear and branched  
100 alkanes directly relevant to sustainable aviation fuels  
101 influence soot formation in non-premixed CF flames.  
102 This is the first study to present SVF data from CF  
103 soot formation flames of n-C12, i-C12, and their  
104 binary mixtures. In addition, the LLNL model for  
105 PAHs [18] was updated and paired with a new soot  
106 model based on the discrete sectional method [19,20]  
107 proposed in this work.

108 The developed soot model was then validated with  
109 SVF data obtained in this work for n-/i-C12 flames.  
110 Additional validations considered literature  
111 measurements of SVF and soot precursors. Validation  
112 efforts in this work invoked a wide range of CF soot  
113 formation flames, including common surrogate fuel  
114 components, such as n-C7 and i-C8, and their blends.  
115 The use of n-C7 and i-C8 as additional validation  
116 cases establishes support for the current  
117 implementation of soot formation and growth rate

1 rules since n-C7 and i-C8 have similar molecular  
2 features and intermediate species to the heavier n-C12  
3 and i-C12 components. In addition, the reaction path  
4 analysis provides a basis for the discussion of fuel  
5 molecular structure effects on soot formation  
6 pathways in CF non-premixed flames of n-C12 and i-  
7 C12.

8

## 9 2. Experimental specification

10 Two aerodynamically-converging opposing  
11 nozzles of 10 mm exit diameter with a separation  
12 distance of 11 mm were placed opposed to each other.  
13 Both fuel and oxidizer streams were diluted with  
14 nitrogen before flowing into the bottom and top  
15 nozzles, respectively. A shroud of nitrogen gas was  
16 used to isolate the resulting flame from the ambient  
17 air. The flow system and the CF burner were  
18 maintained at a temperature of  $473 \pm 2$  K to prevent  
19 condensation of pre-vaporized fuel. The laser-induced  
20 incandescence (LII) technique was combined with the  
21 light extinction (LE) method to measure the soot  
22 volume fraction profiles in CF sooting flames. In the  
23 LE measurements, a continuous He-Ne laser beam  
24 with a wavelength of 632.8 nm was used and a  
25 refractive index (m) of 1.57-0.56i was adopted for the  
26 current study, which is widely used in literature, as  
27 discussed in [21]. For the current experiments, the  
28 standard deviation of the LE measurements is less  
29 than 5% based on three consecutive runs, while the  
30 standard deviation of the LII measurements is less  
31 than 18% based on 40 LII images. To study how the  
32 alkane branching effect influences soot formation in  
33 non-premixed CF flames, several binary mixtures of  
34 i-C12 and n-C12 at liquid volume ratios of 25/75,  
35 50/50, 75/25, 90/10, and 95/5 were considered. The  
36 mixture compositions and corresponding notations  
37 are summarized in Table 1. Further details of the  
38 experimental specifications and test conditions are  
39 provided in the SM (Discussion 1).

40

41 Table 1: Test conditions for i-C12 (2,2,4,6,6-  
42 pentamethyheptane) and n- C12 blends studied.

$X_F$	$X_{O_2}$	$Z_{st}$	$K$ (s <sup>-1</sup> )
0.138	0.50	0.237	200-500
0.117	0.45	0.238	
0.100	0.40	0.236	200

43  $X_F$ : fuel mole fraction in the fuel stream;  $X_{O_2}$ : oxygen mole  
44 fraction in the oxidizer stream;  $Z_{st}$ : stoichiometric mixture  
45 fraction < 0.5 (soot formation flame);  $K$ : global strain rate

## 46 3. Kinetic model development and numerical 47 simulation

48 The current work extends the detailed kinetic  
49 model developed at LLNL for the formation of PAHs  
50 [18] to soot formation and growth. The developed  
51 soot model is based on the discrete sectional method.  
52 Following a similar methodology as Saggese et al.

53 [19], heavy PAHs and soot particles are discretized  
54 into 20 sections of lumped species, i.e., BIN<sub>n</sub> with  
55  $n=1-20$ , with carbon atoms ranging from 20 in BIN1  
56 to  $10^7$  in BIN20. For all BIN<sub>n</sub>, only one  
57 hydrogenation level is considered which greatly  
58 reduces the number of species and reactions in the  
59 model. The primary soot reaction classes and their  
60 related references for the kinetic parameters used in  
61 this study are summarized in Table 2.

62

63 Table 2: Main soot reaction classes.

Soot reaction classes	References
<b>1. HACA</b> H abstraction from BIN(M) C <sub>2</sub> H <sub>2</sub> addition to BIN(R)	C <sub>6</sub> H <sub>5</sub> +H/CH <sub>3</sub> from [22] C <sub>6</sub> H <sub>5</sub> +OH from [23] C <sub>6</sub> H <sub>5</sub> +C <sub>2</sub> H <sub>2</sub> from [24]
<b>2. Soot inception</b> PAH(R/M)+PAH(R/M) BIN <sub>i</sub> (i<5) + BIN <sub>j</sub> (j<5)	BIN+BIN from [20] C <sub>6</sub> H <sub>5</sub> +C <sub>6</sub> H <sub>5</sub> from [27] C <sub>6</sub> H <sub>5</sub> +C <sub>6</sub> H <sub>6</sub> from [28]
<b>3. Surface growth</b> RSR + BIN (R/M) PAH (R) + BIN (R/M) BIN <sub>i</sub> (i<5) + BIN <sub>j</sub> (j>5)	BIN+BIN from [20] C <sub>3</sub> H <sub>3</sub> +C <sub>6</sub> H <sub>5</sub> from [25] C <sub>3</sub> H <sub>3</sub> +C <sub>6</sub> H <sub>6</sub> from [26] C <sub>6</sub> H <sub>5</sub> +C <sub>6</sub> H <sub>5</sub> from [27] C <sub>6</sub> H <sub>5</sub> +C <sub>6</sub> H <sub>6</sub> from [28]
<b>4. Particle coalescence and aggregation</b> BIN <sub>i</sub> (i>5) + BIN <sub>j</sub> (j>5)	BIN+BIN from [20]

64 R=radical; M=molecule; RSR=Resonance stabilized  
65 radicals: C<sub>3</sub>H<sub>3</sub>, i-C<sub>4</sub>H<sub>9</sub>, i-C<sub>4</sub>H<sub>3</sub>, C<sub>5</sub>H<sub>5</sub>, C<sub>3</sub>H<sub>5</sub>-A, C<sub>7</sub>H<sub>7</sub>, C<sub>9</sub>H<sub>7</sub>;  
66 PAH=polycyclic aromatic hydrocarbons: A1-A4.

67

68 It is well known that the H-atom abstraction  
69 (H+BIN<sub>n</sub>), acetylene addition to BIN radicals  
70 (C<sub>2</sub>H<sub>2</sub>+BIN<sub>n</sub>J) (i.e., HACA) reaction class plays a  
71 critical role in soot inception and growth [19,20]. In  
72 the LLNL model, rate parameters for HACA are  
73 based on theoretical studies [22-24] using benzene  
74 (C<sub>6</sub>H<sub>6</sub>) and phenyl radicals (C<sub>6</sub>H<sub>5</sub>) as reference  
75 aromatics. To consider the effect of the size of the soot  
76 particle on rate parameters of C<sub>2</sub>H<sub>2</sub> addition to BIN  
77 radicals, the A-factors have been scaled according to  
78 the size of the particle [22]. In addition to C<sub>2</sub>H<sub>2</sub>, odd  
79 carbon numbered resonance stabilized radicals  
80 (RSRs) are also known to play critical role in soot  
81 formation and growth [14]. Reactions involving  
82 propargyl (C<sub>3</sub>H<sub>3</sub>) radicals were found to be highly  
83 sensitive to SVF in the sensitivity analysis performed  
84 in this study (Fig. SM1). In the proposed model, rate  
85 constants for RSR+BIN<sub>n</sub>J reactions are based on a  
86 recent theoretical study by Mebel and coworkers [25]  
87 involving C<sub>6</sub>H<sub>5</sub> and C<sub>3</sub>H<sub>3</sub>. To consider the change in  
88 collision frequency with the increasing diameter of  
89 soot particles and aggregates, the A-factors have been

1 scaled for surface growth reactions according to the  
2 methodology proposed by Pejpichestakul et al. [4].  
3 Reactions of PAH addition to BIN radicals also  
4 contribute significantly to soot inception and growth  
5 [19,20]. In this study, rate constants for surface  
6 growth reactions involving light PAH radicals up to  
7 pyrene (A4) are based on theoretical studies involving  
8 self-reaction of phenyl radicals (i.e.,  $C_6H_5 + C_6H_5$ )  
9 [27]. Rate constants for surface growth involving  
10 heavy PAHs, i.e., BIN1-4 and soot particles (BIN5-  
11 12)/aggregates (BIN13-20) are based on Ref. 20. Rate  
12 constants for soot reaction class 4 i.e., particle  
13 coalescence and aggregation which involves  
14 interactions only between soot particles and soot  
15 aggregates are also based on Ref. 20. Interactions only  
16 between heavy PAHs (BIN1-4) result in the first soot  
17 particle i.e., BIN5 called soot inception (soot reaction  
18 class 2). Rate constants for interactions between  
19 heavy PAHs (BIN1-4) are also based on Ref. 20. Soot  
20 inception reaction class also includes interactions  
21 between light PAHs leading to form BIN1 and/or  
22 BIN2. Rate constants for interactions between light  
23 PAHs are based on analogy to reactions:  $C_6H_5 + C_6H_5$   
24 from [27] and  $C_6H_5 + C_6H_6$  from [28].

25 The existing PAH model from LLNL [18] was  
26 updated by adding new lumped reactions involving  
27  $C_9H_7$  and  $C_7H_7$  radicals to form pyrene ( $C_{16}H_{10}$ , A4)  
28 based on the study by Park et al. [14]. New ring  
29 enlargement reactions involving phenanthrene (A3)  
30 and pyrene (A4) radicals were added to form BIN1.  
31 The newly added reactions play a critical and sensitive  
32 role in CF of i-C12 and i-C8 flames studied in this  
33 work.

34 Simulations of SVF were performed using the  
35 unsteady counterflow non-premixed flame code  
36 developed at LLNL [29], with constant Lewis number  
37 approximations for each species. Applying a constant  
38 Lewis number approximation reduces the wall time of  
39 simulations by as much as a factor of 10 compared to  
40 using mixture-averaged transport approach for CF  
41 flames calculations involving large surrogate  
42 components, such as n-C12 and i-C12. Effects of  
43 thermophoresis and particle diffusivity coefficients  
44 computed through a Stokes–Cunningham correlation  
45 on simulations of SVF are provided in Figs. SM2-3.  
46 Thermophoresis typically shifts the SVF peak towards  
47 the fuel side, while utilizing Stokes–Cunningham  
48 diffusivity coefficients changes the shape of the SVF  
49 profile as well as increasing peak SVF. Reaction path  
50 analysis was performed with CHEMKIN Pro [30] to  
51 facilitate discussion of fuel molecular structure effects  
52 on SVF.

## 53 4. Results and Discussion

### 54 4.1. Experimental results and model validation 55 studies

56 A selection of the experimental results along with  
57 the corresponding simulations of SVF from the CF

58 flame of neat n-C12, i-C12, and their binary mixtures  
59 are shown in panels a) and b) of Fig. 1. Additional  
60 SVF measurements and validations from this work are  
61 provided in the SM (Fig. SM4). As expected, it can be  
62 seen that the peak SVF along the centerline and the  
63 overall soot loading increase with higher  
64 concentrations of i-C12 in the fuel blend.  
65 Furthermore, it can be observed that as  $K$  increases,  
66 peak SVF decreases as expected due to the reduction  
67 in characteristic residence time within the flame.  
68 These observations are consistent with literature  
69 studies comparing soot formation for linear and  
70 branched alkanes [14,15]. A more thorough  
71 discussion of fuel molecular structure effects on SVF  
72 is provided in Section 4.2. It can also be observed  
73 from Fig. 1(a) that peak SVF values increase non-  
74 linearly as a function of i-C12 content in the fuel  
75 blend. In particular, when the i-C12 concentration is  
76 greater than 90% in the blend, peak SVF exhibits a  
77 stronger non-linear increase. This non-linearity in  
78 peak SVF data has already been reported by Park et  
79 al. [14] for CF non-premixed flames of i-C8 and n-C7  
80 blends, as shown in Fig. 1c. Simulations using the  
81 LLNL model can capture the non-linear increase of  
82 peak SVF with iC12 content reasonably well across  
83 the wide range of strain rates considered in this study.  
84 The LLNL model also captures the non-linear trend in  
85 peak SVF for n-C7/i-C8 blends reported by Park et al.  
86 [14], as seen in Fig 1c. The simulation is also able to  
87 qualitatively capture the strain rate dependence with  
88 peak SVF.

89 Figure 1b compares the spatially resolved SVF  
90 profiles along the centerline of flame. The x axis is the  
91 distance from the fuel nozzle normalized to the  
92 location of the peak SVF in i-C12. The peak values of  
93 each SVF curve were observed to occur at  
94 approximately 3.96 mm from the fuel nozzle,  
95 suggesting that the location of peak LII signal is  
96 independent of i-C12/n-C12 blending ratio when  
97 keeping  $Z_{st}$  constant. Furthermore, the overall  
98 thickness of the SVF profiles appears similar for all  
99 fuel blends, as  $K$  is kept constant. It can be observed  
100 from Fig. 1b that the simulated SVF profile matches  
101 well with the data.

102 Regarding quantitative agreement, the simulations  
103 tend to overpredict SVF of C12 mixtures by a factor  
104 of 5 for all conditions studied in this work. In addition  
105 to the validations against SVF data obtained in this  
106 study for n-i-C12, the LLNL model was also  
107 validated with literature data for CF flames of n-C7  
108 and i-C8, which are common surrogate fuel  
109 components and have similar molecular structures to  
110 n-C12 and i-C12, respectively. From validation  
111 studies shown in Figs. 1c and SM5-6, it can be  
112 observed that simulations predict peak SVF for CF  
113 flames of n-C7 and i-C8 within a factor of 3. The  
114 LLNL model was also validated with the SVF data  
115 available in literature for  $C_2H_4$  counterflow flames,  
116 which have been commonly used in the literature to

1 validate soot models. These validations for C<sub>2</sub>H<sub>4</sub> 2 mixtures are provided in the SM (Fig. SM7) and the 3 LLNL model underpredicts the SVF data for C<sub>2</sub>H<sub>4</sub> 4 flames by as much as a factor of 4.

5 While evaluating the LLNL model for quantitative 6 agreement of SVF, it is notable that there exists a 7 systematic uncertainty in SVF measurements using 8 the LE technique. This uncertainty is of a factor 3 9 stemming from the assignment of the refractive index 10 value used to convert raw signals to SVF while 11 calibrating the LII signals against LE measurements 12 [3,15,21,31,32]. It has also been discussed in the 13 literature that the choice of diagnostic wavelength 14 potentially introduces additional systematic bias into 15 SVF measurements [31]. As addressed in Section 3, 16 decisions regarding the exclusion of thermophoretic 17 effects and estimation of particle diffusivity 18 coefficients can also influence the simulated SVF of 19 CF flames. Therefore, in this work quantitative 20 agreement of simulations with SVF measurements 21 within a factor of 5 was considered reasonably 22 accurate.

23 To the best of authors' knowledge, this is the first 24 study to capture both the experimentally observed 25 non-linear trend and the absolute value of peak SVF 26 for n-alkane and highly branched alkane flames 27 reasonably well. For example, although Park et al. 28 [14] in their study used the soot model from Wang et 29 al. [33] to simulate the non-linear trend in peak SVF 30 for n-C7/i-C8 mixtures, their model comparisons only 31 showed normalized SVF data. Furthermore, although 32 the latest soot model published by Nobili et al. [20] 33 can capture peak SVF for n-C7/i-C8 mixtures in CF 34 flames within a factor of 3, it is not able to capture the 35 non-linear trend in peak SVF reported by Park et al. 36 [14]. Comparisons illustrating this point are provided 37 in the SM (Fig. SM8).

38 In addition to SVF validations, the LLNL model 39 was validated with measurements of smaller 40 intermediate species including PAHs under similar 41 flame conditions. Validations of the LLNL model for 42 species from CF flames of n-C7, i-C8, C<sub>2</sub>H<sub>4</sub>, and iso- 43 butene (i-C4) are provided in the SM (Figs. SM9-13). 44 iso-Butene was included since it is one of the primary 45 intermediates in both i-C8 and i-C12 flames. To the 46 best of our knowledge, there is no speciation data 47 available for CF flames of n-C12 and i-C12 which 48 could further validate modeled pathways to soot 49 formation. The LLNL model can simulate the mole 50 fraction of small gas phase species reasonably well for 51 all CF flames studied in this work (within a factor of 52 2), while overpredicting the mole fraction of C<sub>6</sub>H<sub>6</sub>. 53 However, other aromatics such as toluene, styrene, 54 naphthalene, phenanthrene etc. are captured 55 reasonably well (within a factor of 3) for all flames. 56 Taken together, these comprehensive validations 57 demonstrate an effort to evaluate and improve the 58 LLNL model using a wide range of CF flame

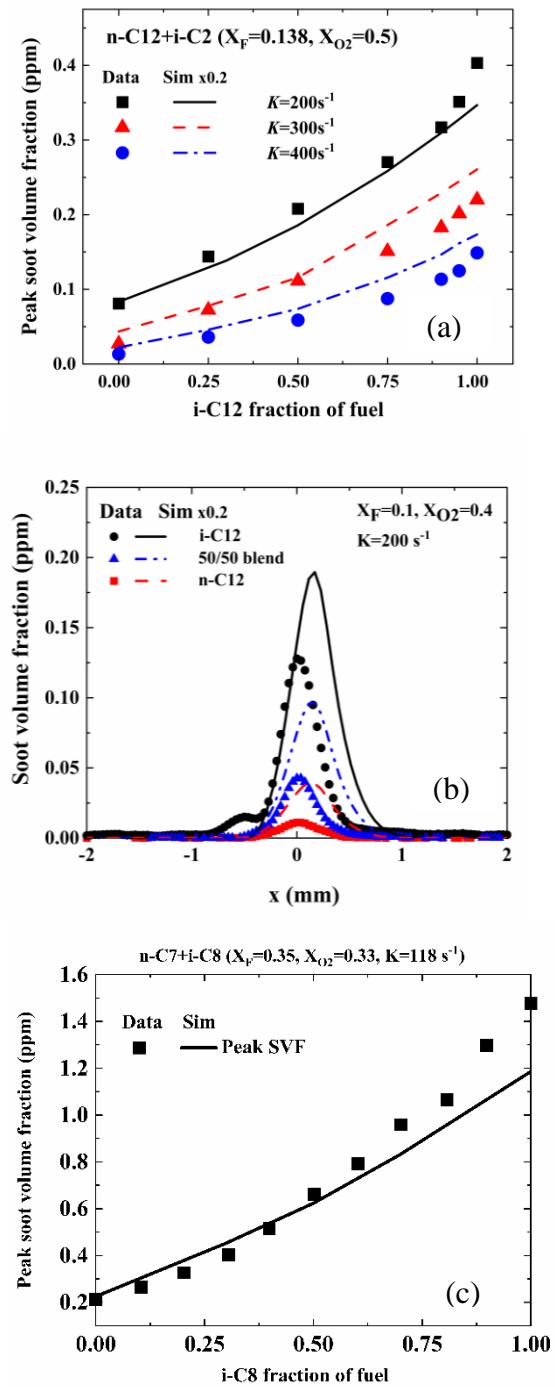


Figure 1. Comparison of SVF measurements and simulations for: a) i-C12 and n-C12 flames vs i-C12 liquid volume fraction in the fuel blend; b) i-C12 and n-C12 flames along the centerline; c) i-C8 and n-C7 flames vs i-C8 fraction in the fuel blend.

1 conditions and mixtures, including common surrogate  
2 components sharing structural similarities.

3

#### 4.2 Chemical kinetic analysis and discussion of 5 alkane branching influence on SVF

6 Rate of production analysis (ROPA) using  
7 CHEMKIN Pro [30] was performed to identify the  
8 differences in reaction pathways for PAH formation  
9 in CF flames of n-/i-C12 mixtures. Fig. 2 shows the  
10 simplified ROPA for benzene (C<sub>6</sub>H<sub>6</sub>, A1),  
11 naphthalene (C<sub>10</sub>H<sub>8</sub>, A2), phenanthrene (C<sub>14</sub>H<sub>10</sub>, A3)  
12 and pyrene (C<sub>16</sub>H<sub>10</sub>, A4). A detailed ROPA for A1-A4  
13 is provided in the SM (Figs. SM14-15). To identify  
14 possible reasons for the non-linear increase in SVF as  
15 i-C12 content increases, the evolution of critical  
16 intermediates (C1-C9) along with PAH/soot  
17 precursors were investigated. Additional simulations  
18 were run to identify reactions which play a critical  
19 role in simulating the experimentally observed non-  
20 linear trend in SVF.

21 The ROPA shows that primary pathways for A1-  
22 A4 formation remain similar for both n-C12 and i-  
23 C12. Benzene (A1) is primarily formed via ring  
24 expansion reactions preceded by addition of methyl  
25 radicals to cyclopentadienyl radical in both flames.  
26 Once formed, benzene undergoes H-atom abstraction  
27 to form phenyl radicals which react with allyl radical  
28 (C<sub>3</sub>H<sub>5</sub>-A) to form indenyl (C<sub>9</sub>H<sub>8</sub>) which undergoes  
29 ring enlargement reactions via H-atom abstraction and  
30 addition of methyl radicals to form naphthalene  
31 (C<sub>10</sub>H<sub>8</sub>, A2). Phenyl radicals also react with other  
32 intermediate species (CH<sub>3</sub>, C<sub>2</sub>H<sub>4</sub>, C<sub>2</sub>H<sub>2</sub>, C<sub>4</sub>H<sub>6</sub>) to form  
33 naphthalene (A2). A2 is also formed through another  
34 major pathway involving propargyl (C<sub>3</sub>H<sub>3</sub>) and  
35 fulvenallenyl (C<sub>7</sub>H<sub>5</sub>) radicals which is primarily  
36 formed via reactions involving only C<sub>2</sub>H<sub>2</sub> and C<sub>3</sub>H<sub>3</sub>.  
37 From Fig. SM16(a) it can be observed that while the  
38 mole fraction of C<sub>2</sub>H<sub>2</sub> reduces as alkane branching  
39 increases, the mole fraction of C<sub>3</sub>H<sub>3</sub> increases. Similar  
40 conclusion was also made by Park et al. [14] in their  
41 study on CF flames of n-C7 and i-C8. The increased  
42 mole fraction of C<sub>3</sub>H<sub>3</sub> with alkane branching leads to  
43 a higher percentage of A2 formed via fulvenallenyl  
44 and propargyl pathway in i-C12 flame. Similar to A2,  
45 phenanthrene (A3) is also formed via similar ring  
46 enlargement and ring closure reactions involving  
47 benzene, naphthalene and intermediate species such  
48 as CH<sub>3</sub>, C<sub>2</sub>H<sub>2</sub>, C<sub>3</sub>H<sub>3</sub>, C<sub>5</sub>H<sub>5</sub>. A3 thus formed undergoes  
49 H-atom abstraction and subsequent C<sub>2</sub>H<sub>2</sub> addition  
50 (HACA) to form pyrene (A4). Pyrene is also formed  
51 via newly added pathways involving two RSRs,  
52 indenyl (C<sub>9</sub>H<sub>7</sub>) and benzyl (C<sub>7</sub>H<sub>7</sub>) radicals [14] (R1:  
53 C<sub>9</sub>H<sub>7</sub>+C<sub>9</sub>H<sub>7</sub>=>A4+C<sub>2</sub>H<sub>2</sub>+H<sub>2</sub>; R2: C<sub>9</sub>H<sub>7</sub>+C<sub>7</sub>H<sub>7</sub>=>A4+  
54 2H<sub>2</sub>). As i-C12 content increases, the percentage of  
55 A4 formed via R1 and R2 increases. Among PAHs,  
56 only A4 shows significant non-linearity as branching  
57 increases (Fig. SM16(b)). Park et al. [14] also  
58 observed in their experiments that larger PAHs such

59 as pyrene exhibit a non-linear increase with i-C8  
60 blending ratio. From Fig. SM16(a), it is observed that  
61 mole fractions of indenyl and benzyl radicals increase  
62 non-linearly with i-C12 blending ratio which possibly  
63 explains the non-linear increase in mole fraction of  
64 A4. Additional simulations were performed by  
65 removing R1 and R2 to further confirm the role of  
66 C<sub>7</sub>H<sub>7</sub> and C<sub>9</sub>H<sub>7</sub> in A4 formation as alkane branching  
67 increases (Figs. SM17-18). It has been observed from  
68 these simulations that without R1 and R2 in the LLNL  
69 model, the model is no longer able to simulate the  
70 non-linear evolution of pyrene as alkane branching  
71 increases. Furthermore, it has been observed that  
72 without R1 and R2 in the model, the rate of increase  
73 in A4 with alkane branching reduces significantly and  
74 is lower than smaller PAHs which would contradict  
75 experimental observations made by Park et al. [14]. In  
76 addition, from Fig. 3 it can be observed that without  
77 R1 and R2 in the LLNL model, simulations fail to  
78 capture the non-linearity observed during experiments  
79 in the evolution of peak SVF with alkane branching.  
80 Newly added ring enlargement reactions involving A3  
81 and A4 were also found to be important in predicting  
82 the non-linearity accurately. From Fig. 3 it can be  
83 observed that removing all the newly added gas phase  
84 PAH reactions from the model leads to significant  
85 reduction in simulated peak SVF for i-C12 flame and  
86 changes the peak SVF profile to be almost linear with  
87 alkane branching. It is to be noted that there is no  
88 significant effect of newly added gas phase PAH  
89 reactions on simulated SVF for n-C12 flame. Similar  
90 observations were also made for CF flame of n-C7, i-  
91 C8 and their blends. Given the importance of the  
92 additional soot precursor reactions in capturing the  
93 non-linear trends in peak SVF, further experimental  
94 and theoretical studies of these reactions and their  
95 related potential energy surfaces are necessary.

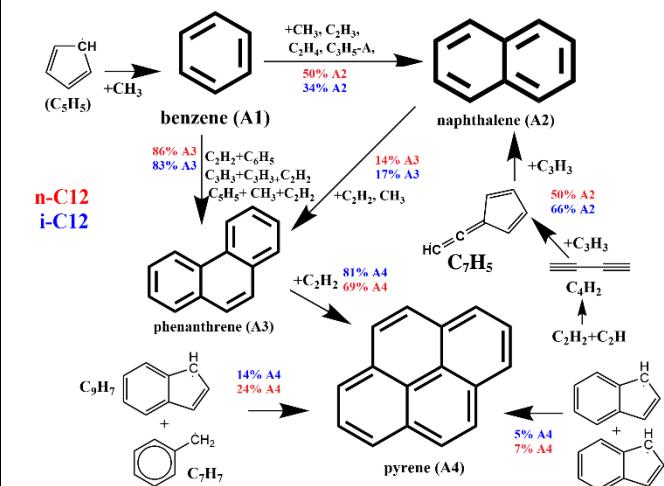


Figure 2. Reaction path analysis for A1-A4 in CF flames of  
neat n-C12 and i-C12 at 1300 K (X<sub>F</sub>=0.138, X<sub>O2</sub>=0.5, K=200 s<sup>-1</sup>).

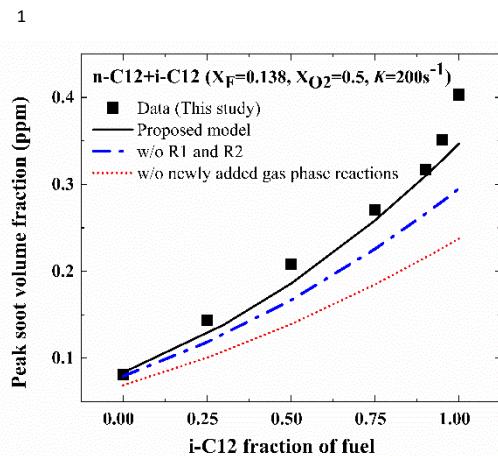


Figure 3. Simulations of peak SVF with and without additional soot precursor reactions, see main text for details.

## 2 5. Conclusion

3 Soot formation from the combustion of n-C12 and  
 4 i-C12 was studied in counterflow non-premixed  
 5 flames. This work is the first experimental study to  
 6 measure SVF in CF flames of n-C12 and i-C12 which  
 7 are commonly used as diesel and aviation surrogate  
 8 fuel components. Soot volume fractions were  
 9 measured for several global strain rates and fuel  
 10 loadings for a fixed stoichiometric mixture fraction.  
 11 The role of linear and branched fuel structures on the  
 12 formation of soot was investigated using several  
 13 binary mixtures of n-C12 and i-C12. As expected, the  
 14 measurements show that peak SVF for n-C12, i-C12,  
 15 and their binary mixtures decrease with increasing  
 16 global strain rate. This work demonstrates that peak  
 17 SVF increases non-linearly with i-C12 content,  
 18 agreeing with the observations of Park et al. [14] for  
 19 n-C7 and i-C8 which share similar structural features.  
 20 To simulate these measurements, the PAH model  
 21 previously developed at LLNL was extended to model  
 22 soot formation. New reactions involving indenyl,  
 23 benzyl, propargyl, and methyl radicals forming  
 24 pyrene and heavier PAHs were added to the PAH  
 25 submodel. These reactions were observed to play a  
 26 critical role in CF flames of highly branched alkanes  
 27 such as i-C12 and i-C8. The LLNL soot model  
 28 coupled with the updated PAH model was validated  
 29 with the data obtained in this work for CF flames of  
 30 n- and i-C12.  
 31 Additional experimental data available from  
 32 literature was used to comprehensively validate the  
 33 model for CF flames of n-C7, i-C8, C<sub>2</sub>H<sub>4</sub>, and iso-  
 34 butene mixtures. Comparisons show that the LLNL  
 35 model can capture the data qualitatively well across a  
 36 wide range of strain rates and mixture conditions.

37 Regarding quantitative agreement, the simulated SVF  
 38 is typically within a factor of 5. Given the systematic  
 39 uncertainty of a factor of 3 associated with SVF  
 40 measurements, simulations of SVF within a factor of  
 41 5 can be considered reasonably accurate. More  
 42 importantly, the current LLNL model with the newly  
 43 added soot precursor reactions is able to capture, for  
 44 the first time, the non-linear variation in peak SVF  
 45 with the alkane branching. Furthermore, using the  
 46 validated model developed in this work, this study  
 47 provides important insights into the reaction pathways  
 48 which require further investigation to bridge  
 49 quantitative gaps that remain in accurately predicting  
 50 soot formation for surrogate fuel components of  
 51 aviation and diesel fuels.

52

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61

## 62 Supplementary materials

63 Experimental data, kinetic model with  
 64 thermodynamic and transport files, additional model  
 65 validation studies and discussion.

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