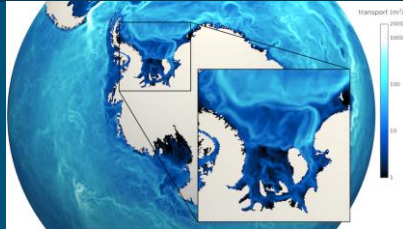
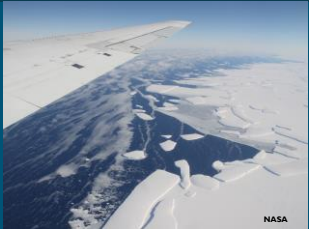
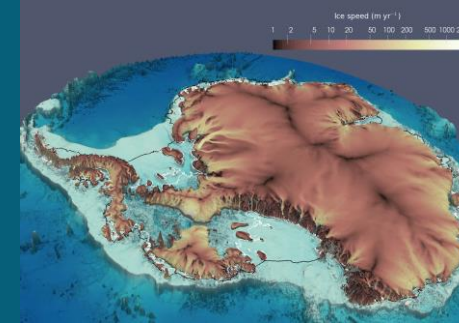


# Performance-portable extensions to ice-sheet modeling in MALI



March 2<sup>nd</sup>, 2023

PRESENTED BY

Jerry Watkins, Max Carlson, Irina Tezaur, Mauro Perego, Jonathan Hu

SIAM Conference on Computational Science and Engineering

# Outline



- 1) Motivation - Why are we interested in performance portability in ice-sheet modeling?
- 2) MALI software
- 3) Current Performance Results
- 4) Future Performance Goals
- 5) Conclusions



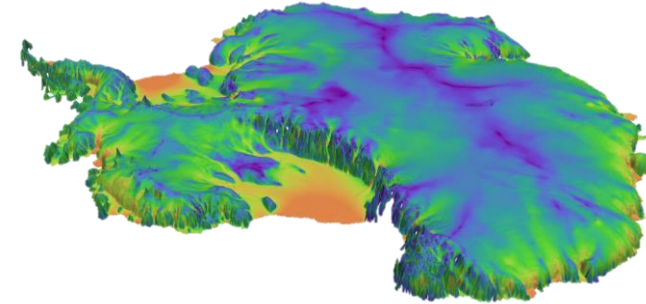
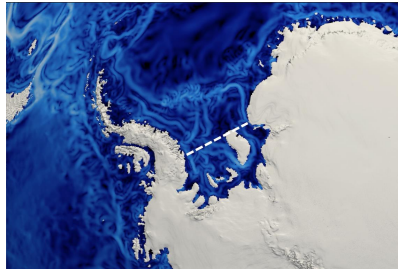
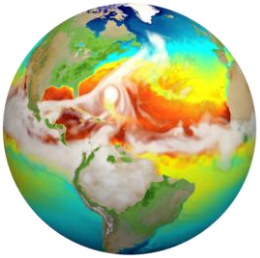
# Motivation

Why are we interested in performance portability in ice-sheet modeling?



## High-fidelity simulations of the DOE E3SM's ice sheet model, MALI, on exascale systems

- As part of **DOE's Earth System Model** - provide actionable predictions of 21<sup>st</sup> century sea-level change (including uncertainty bounds)



OLCF Summit  
NVIDIA V100 GPU



ALCF Aurora  
Intel Xe GPU



OLCF Frontier  
AMD Instinct GPU



NERSC Perlmutter  
NVIDIA A100 GPU

GPUs in open-science are here, need efficient access to computational power

# Performance portability for exascale computing



## Challenges:

- Diverse set of HPC vendors and architectures
  - Intel, AMD, NVIDIA, IBM, ARM-based
  - CPUs with vector processing; GPUs
- Software life cycle is much longer than hardware

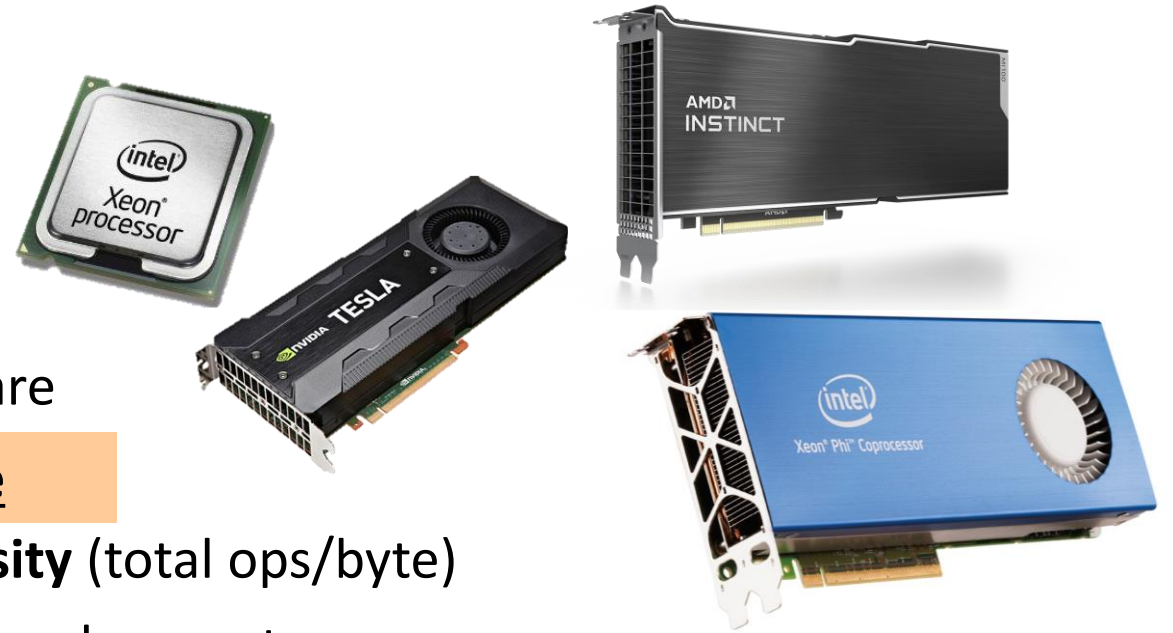
## Different architectures, trend remains the same

- Need algorithms with **higher arithmetic intensity** (total ops/byte)
- Need fundamental **abstractions** during code development

**Performance portability:** A reasonable level of performance is achieved across a wide variety of computing architectures with the same source code.

## Approaches:

- **Libraries** – High-level abstractions with specified input/output (e.g. BLAS)
- **Task-based** – Data-centric abstractions for mapping tasks to resources (e.g. Legion)
- **MPI+X** – Algorithmic-level abstractions for distributed (MPI) and shared (X) memory parallelism (e.g. **Directives:** OpenMP, OpenACC; **Frameworks:** Kokkos, RAJA, OCCA)





# MALI software

What software tools are we using?

# MALI (MPAS-Albany Land Ice) software



## MPAS:

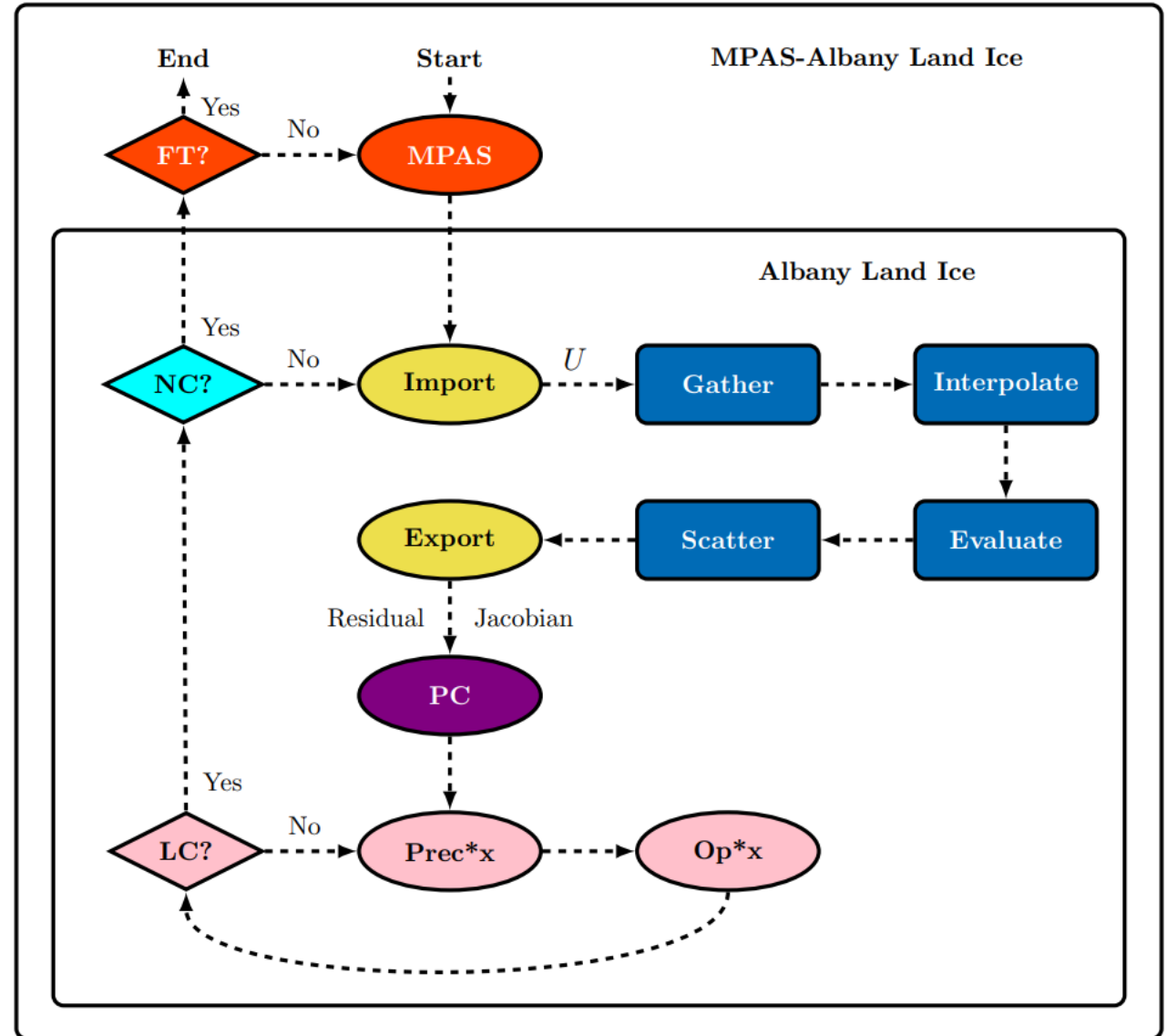
- Thickness/Temperature evolution

## Albany Land Ice:

- **First-order Stokes velocity solver**

## Trilinos:

- Mesh tools (*STK*)
- Discretization tools (*Intrepid2*)
- Nonlinear/Linear solver (*NOX/Belos*)
- Distributed memory linear algebra (*Tpetra*)
- Multigrid Preconditioner (***MueLu***)
- Field DAG (***Phalanx***)
- Automatic differentiation (***Sacado***)
- Shared memory parallelism (***Kokkos***)
- Many more...





# First Order (FO) Stokes/Blatter-Pattyn Model



Ice behaves like a **very viscous non-Newtonian shear-thinning fluid** (like lava flow) and is modeled **quasi-statically** using **nonlinear incompressible Stokes equations**.

$$\begin{cases} -\nabla \cdot \boldsymbol{\tau} + \nabla p = \rho \mathbf{g} \\ \nabla \cdot \mathbf{u} = 0 \end{cases}, \quad \text{in } \Omega$$

Stokes( $\mathbf{u}, p$ ) in  $\Omega \in \mathbb{R}^3$

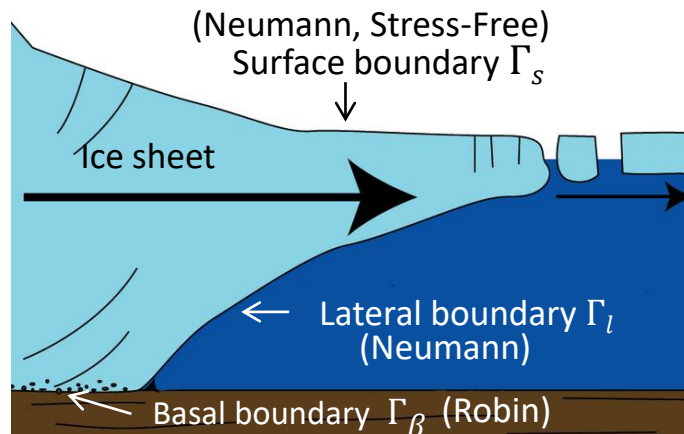


FO Stokes( $u, v$ ) in  $\Omega \in \mathbb{R}^3$

$$\begin{aligned} -\nabla \cdot (2\mu \dot{\epsilon}_1) &= -\rho g \frac{\partial s}{\partial x} \\ -\nabla \cdot (2\mu \dot{\epsilon}_2) &= -\rho g \frac{\partial s}{\partial y} \end{aligned}, \quad \text{in } \Omega$$

- Fluid velocity vector:  $\mathbf{u} = (u_1, u_2, u_3)$
- Strain rate tensor:  $\epsilon_{ij} = \frac{1}{2} \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right)$
- Isotropic ice pressure:  $p$
- Glen's Law Viscosity\*:  $\mu = \frac{1}{2} A(T)^{-\frac{1}{n}} \left( \frac{1}{2} \sum_{ij} \epsilon_{ij}^2 \right)^{\left( \frac{1}{2n} - \frac{1}{2} \right)}$
- Flow factor:  $A(T) = A_0 e^{-\frac{Q}{RT}}$
- Deviatoric stress tensor:  $\boldsymbol{\tau} = 2\mu \boldsymbol{\epsilon}$

**Hydrostatic approximation + scaling argument** based on the fact that ice sheets are thin and normals are almost vertical



## Discussion:

- Nice “**elliptic**” approximation to full Stokes.
- 3D model for two unknowns ( $u, v$ ) with nonlinear  $\mu$ .
- Valid for both **Greenland** and **Antarctica** and used in **continental scale** simulations.



# 9 MueLu/Belos – preconditioned iterative solver

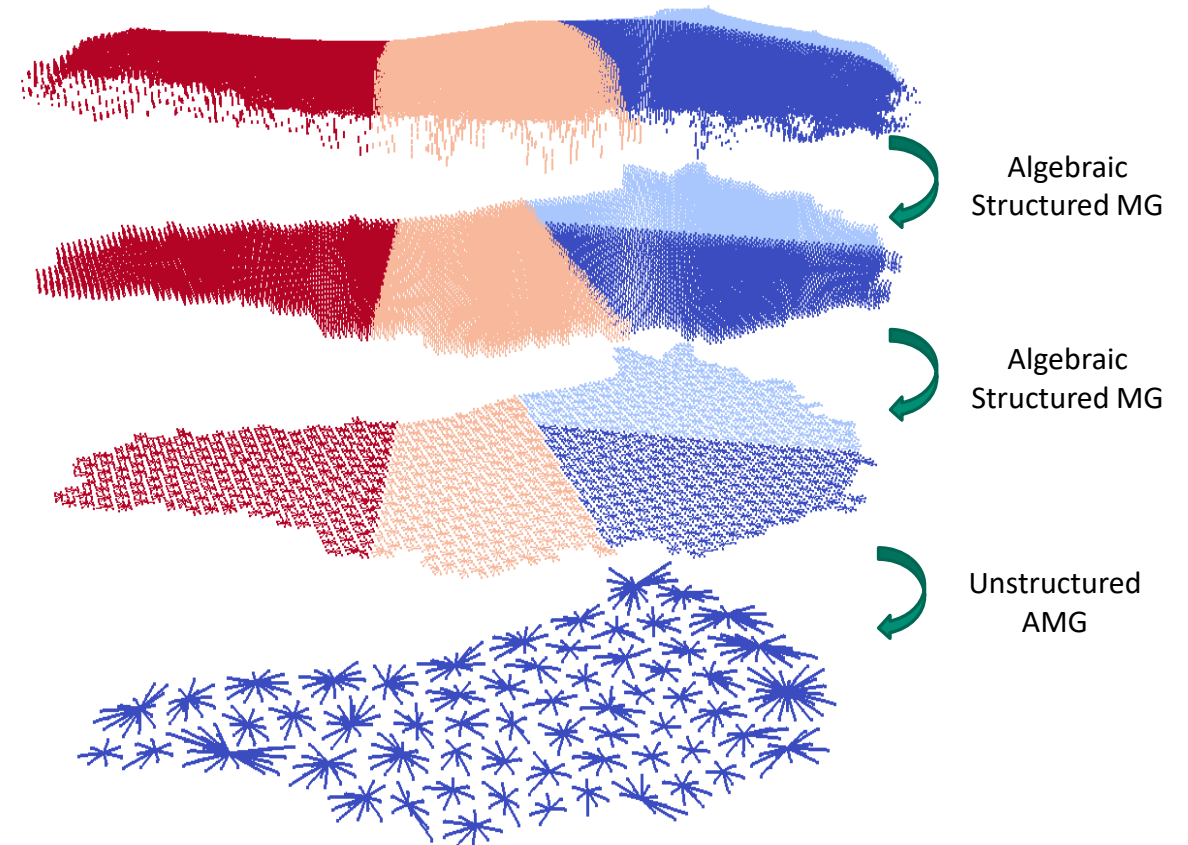
**Problem:** Ice sheet meshes are thin with high aspect ratios

**Solution:** Matrix dependent semi-coarsening algebraic multigrid (MDSC-AMG)

- First, matrix-dependent **structured** multigrid to coarsen vertically
- Second, smoothed aggregation **AMG** on single layer
- Implemented in Trilinos – MueLu

**Solver:** Preconditioned Newton-Krylov

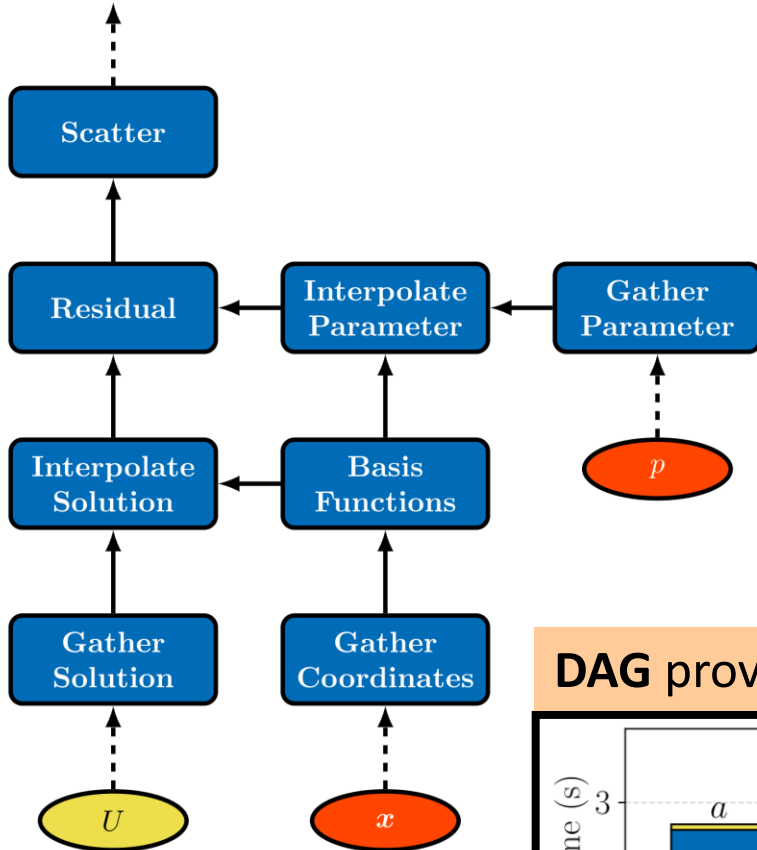
- MDSC-AMG is used as preconditioner for GMRES
- Performance portability through Trilinos/MueLu (multigrid) + Trilinos/Belos (GMRES)



# Phalanx – directed acyclic graph (DAG)



## DAG Example



## Advantages:

- Increased flexibility, extensibility, usability
- Arbitrary data type support
- Potential for task parallelism

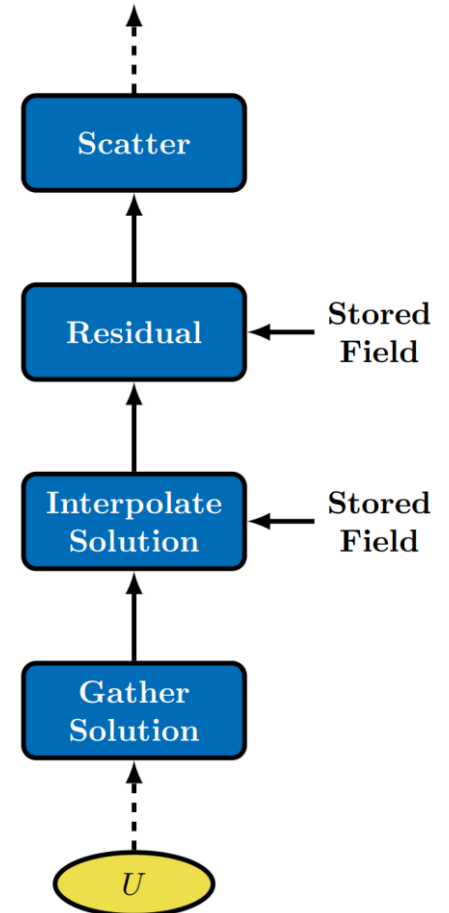
## Disadvantage:

- Performance loss through fragmentation

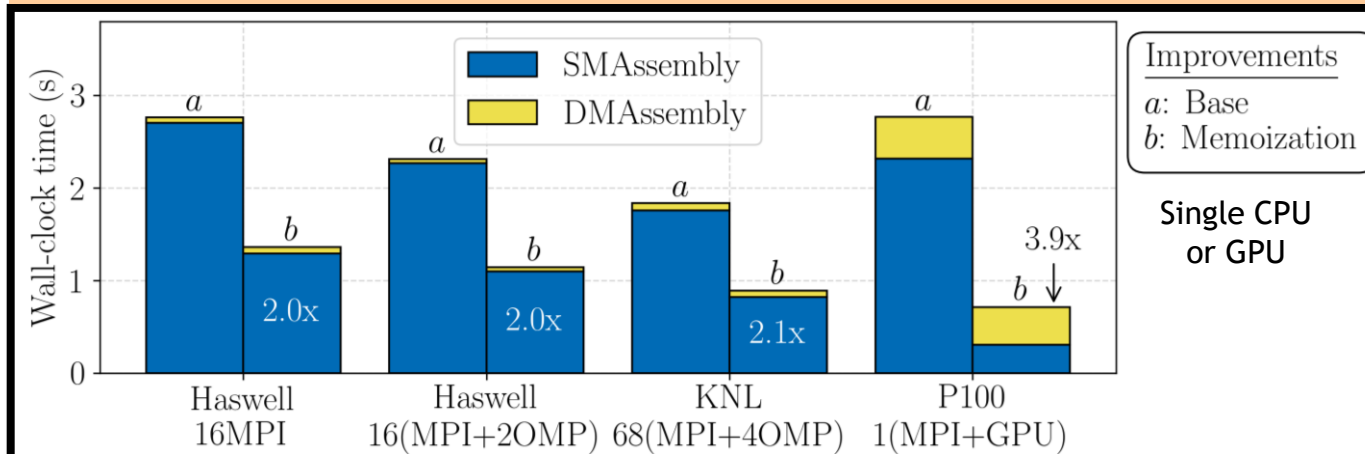
## Extension:

- Performance gain through memoization

## DAG Example (memoization)



**DAG provides flexibility; Memoization improves performance**

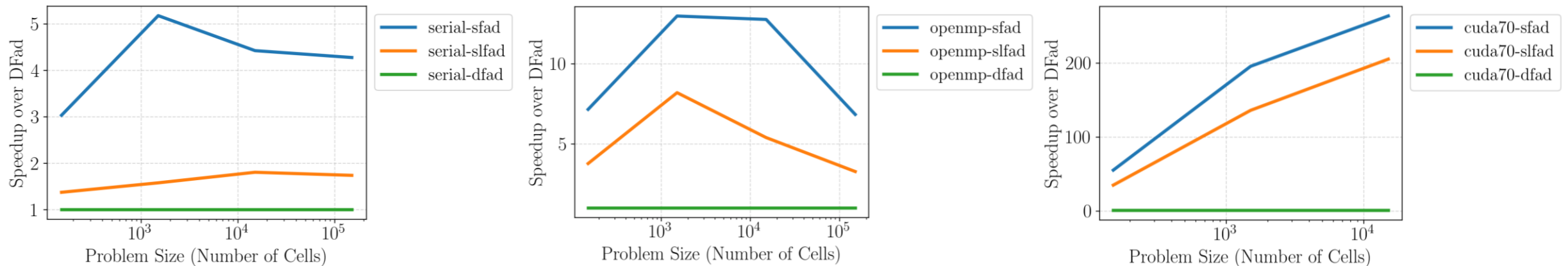


# Sacado – automatic differentiation (AD)



- AD provides **exact** derivatives - no Jacobian derivation or hand-coding required
- Allows for **advanced analysis** capabilities – easily construct any derivative, hessian
  - Ex: Optimization, sensitivity analysis
- Sacado **data types** are used for derivative components via class **templates**
  - DFad (most flexible) – size set at run-time
  - SLFad (flexible/efficient) – max size set at compile-time
  - SFad (most efficient) – size set at compile-time

**AD** capability allows for advanced analysis while maintaining performance portability

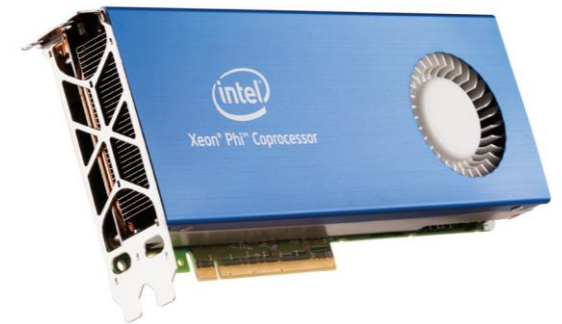


**Fad Type Comparison:** Tetrahedral elements (4 nodes), 2 equations, ND =  $4 \times 2 = 8$

# Kokkos – performance portability



- **Kokkos** is a C++ library that provides **performance portability** across multiple **shared memory** computing architectures
- Abstract **data layouts** and **hardware features** for optimal performance on **current** and **future** architectures
- Allows researchers to focus on **application** or **algorithmic development** instead of **architecture specific programming**



With Kokkos, you write an algorithm once for multiple hardware architectures.



# Phalanx Evaluator – templated Phalanx node

Residual



A Phalanx node (**evaluator**) is constructed as a C++ class

- Each evaluator is templated on an **evaluation type** (e.g. residual, Jacobian)
- The evaluation type is used to determine the **data type** (e.g. double, Sacado data types)
- Kokkos **RangePolicy** is used to parallelize over **cells** over an **Execution Space** (e.g. Serial, OpenMP, CUDA)
- Inline functors are used as kernels
- MDField data layouts
  - Serial/OpenMP – **LayoutRight** (row-major)
  - CUDA – **LayoutLeft** (col-major)

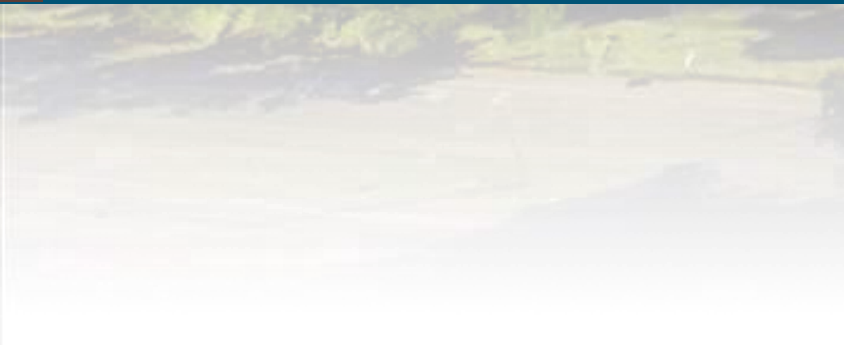
```
template<typename EvalT, typename Traits>
void StokesForesid<EvalT, Traits>::
evaluateFields(typename Traits::EvalData workset) {
    Kokkos::parallel_for(
        Kokkos::RangePolicy<ExeSpace>(0,workset.numCells),
        *this);
}

template<typename EvalT, typename Traits>
KOKKOS_INLINE_FUNCTION
void StokesForesid<EvalT, Traits>::
operator() (const int& cell) const{
    for (int node=0; node<numNodes; ++node){
        Residual(cell,node,0)=0.;
    }
    for (int node=0; node < numNodes; ++node) {
        for (int qp=0; qp < numQPs; ++qp) {
            Residual(cell,node,0) +=
                Ugrad(cell,qp,0,0)*wGradBF(cell,node,qp,0) +
                Ugrad(cell,qp,0,1)*wGradBF(cell,node,qp,1) +
                force(cell,qp,0)*wBF(cell,node,qp);
        }
    }
}
```

Template parameters are used to get hardware specific features.



# Current Performance Results



How well does MALI perform?

# Performance Overview



## Major improvements to finite element assembly time

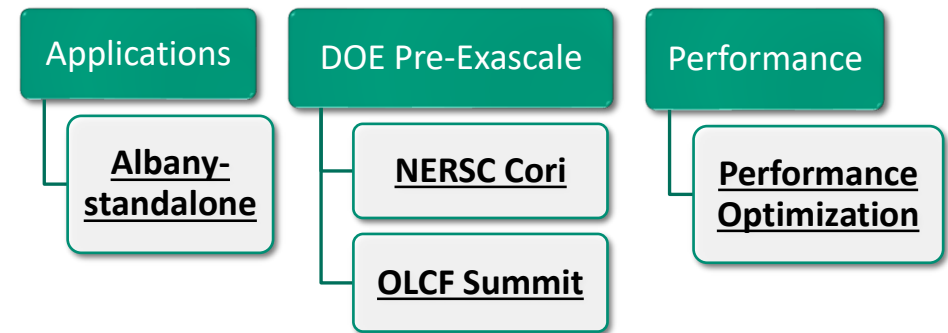
- **Memoization** to avoid unnecessary data movement and computation
- **Tpetra::FECrsMatrix** refactor to reduce memory footprint and data movement
- **Boundary condition** refactor to reduce memory footprint and data movement

## Solver portability on Cori and Summit

- **MueLu SemiCoarsen** refactor using Kokkos
- **Ifpack2 portable smoothers** tuned to GPU hardware

## Automated performance testing/tuning

- **Changepoint detection** for performance monitoring
- **Bayesian optimization** for performance tuning



Watkins, J., Carlson, M., Shan, K., Tezaur, I., Perego, M., Bertagna, L., Kao, C. *et al.*

“Performance portable ice-sheet modeling with MALI.” (Submitted, IJHPCA) <https://arxiv.org/abs/2204.04321>

# Major improvements to finite element assembly

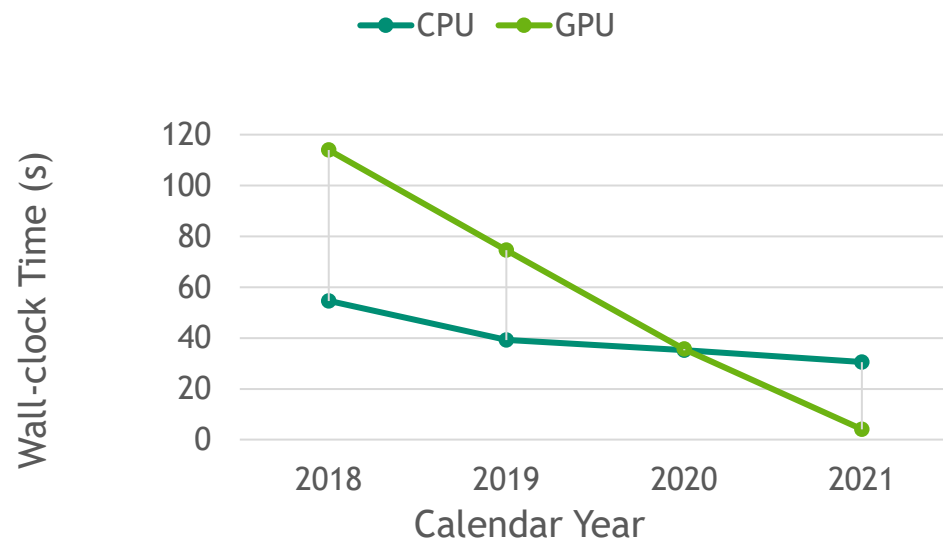


## Improvements (GIS [1-7km])

- ~**2x** CPU speedup over original
- ~**27x** GPU speedup over original

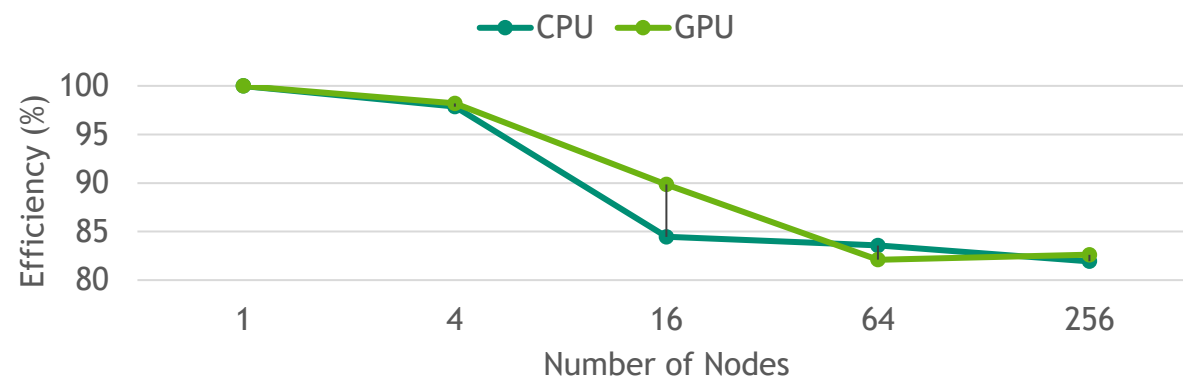
## Wall-clock time (GIS [1-7km])

- ~**11x** GPU speedup over CPU (node)

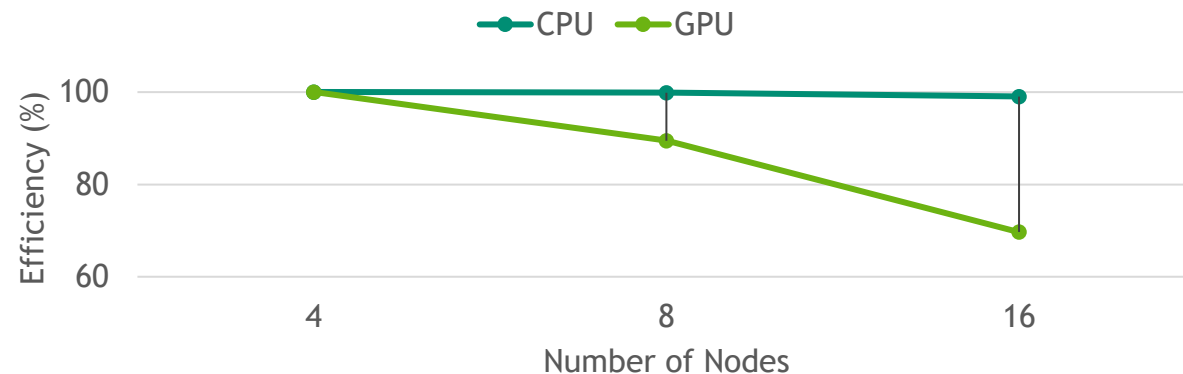


## Scalability (AIS [16,1km], TW [1-10km])

- Weak Efficiency: ~**82%** CPU/GPU



- Strong Efficiency: ~**99%** CPU, ~**70%** GPU





# Solver portability on Cori and Summit



## Setup:

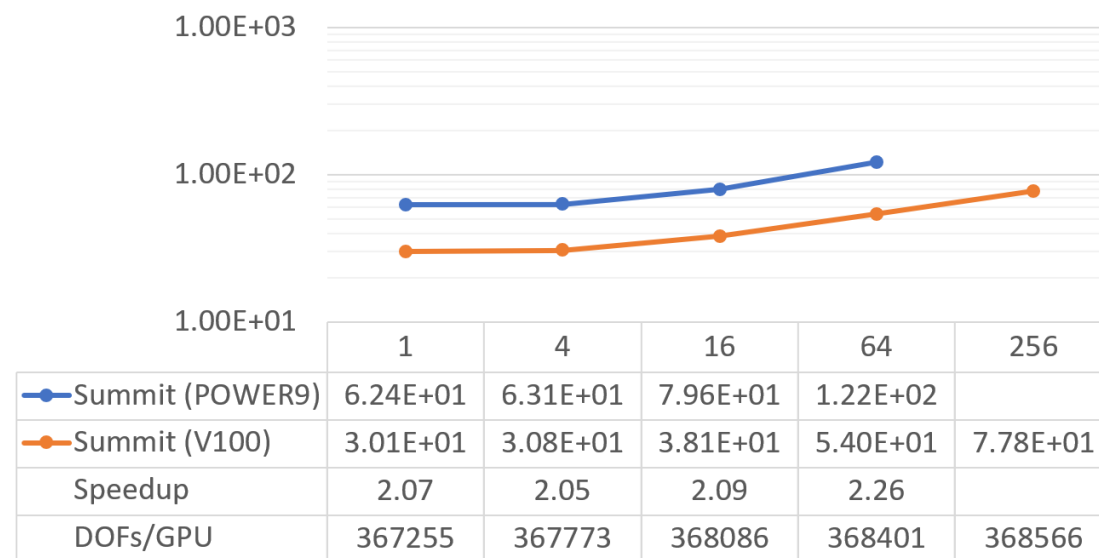
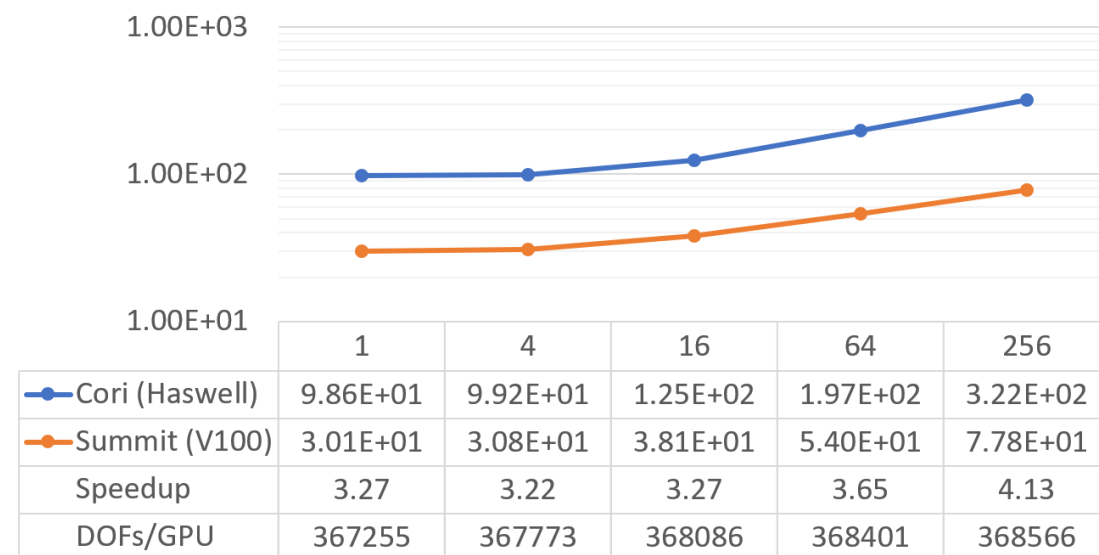
- Same input file for all cases
  - Performance portable point smoothers
  - No architecture specific tuning

## Results:

- Performance degrades at higher resolutions
  - (645->1798 total linear iterations)
  - GPU scaling slightly better
- Speedup on GPU
  - 3.2-4.1x speedup Summit over Cori
  - 2.1-2.3x speedup V100 over POWER9

Speedup achieved over MPI-only simulations without architecture specific tuning

Solver Weak Scaling  
Wall-clock time (s) vs. Nodes

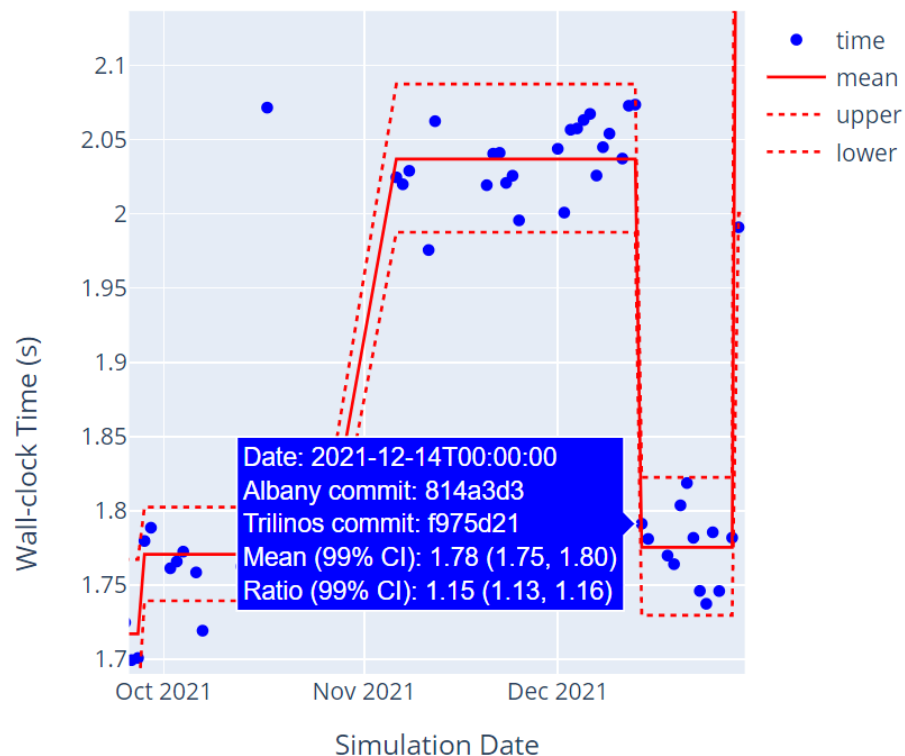


# Automated performance testing/tuning



## Changepoint Detection

- Autodetects performance regressions/improvements

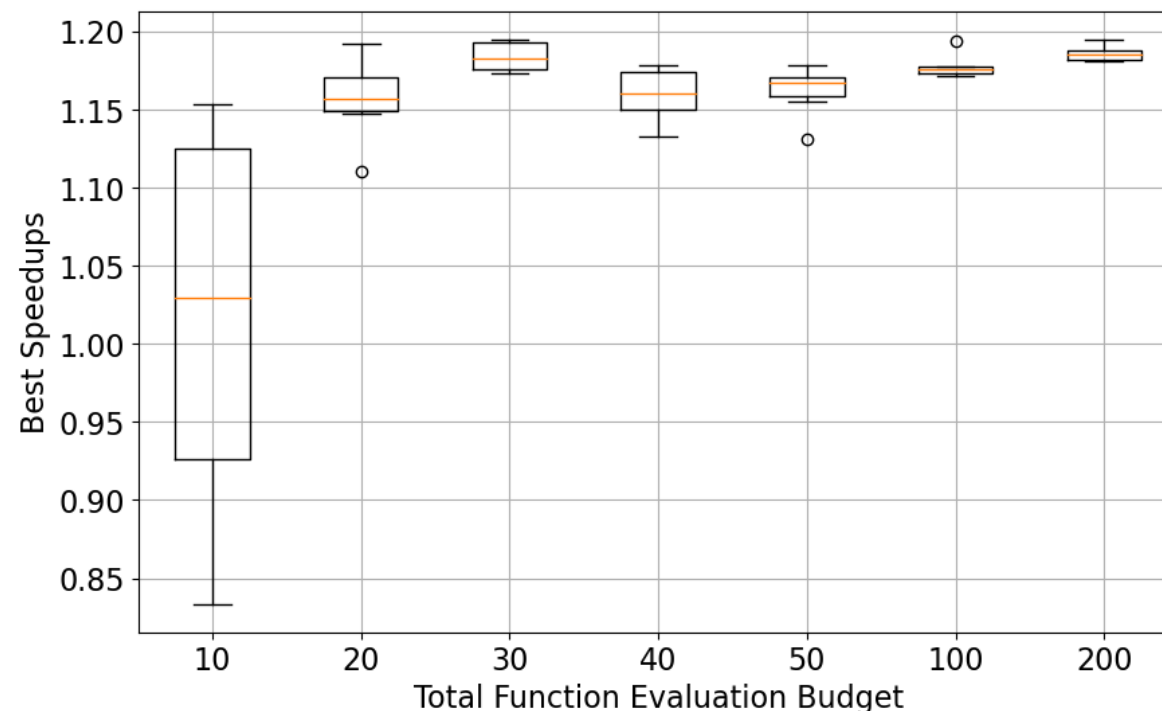


**Example:** Kokkos regression/improvement

Carlson, M., Watkins, J., Tezaur, I. "Automatic performance tuning for MPAS-Albany Land Ice." (Submitted, JCAM)

## Bayesian Optimization

- Autotunes performance **parameters**



**Example:** Optimizing multigrid parameters using GPTune



# Future Performance Goals

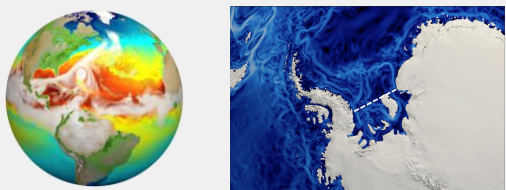
What are next steps for MALI performance?

# Future Performance Overview

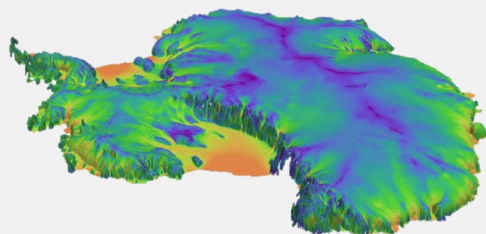


## Applications

### E3SM + MALI



### MALI-standalone

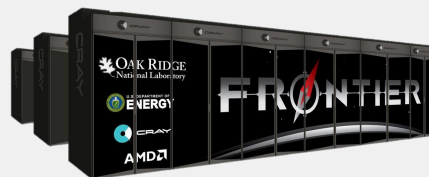


## DOE Exascale

### NERSC Perlmutter



### OLCF Frontier

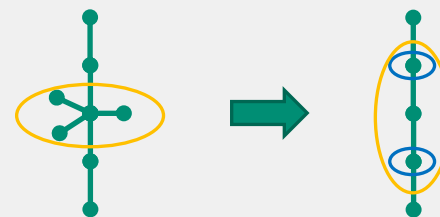


### ALCF Aurora

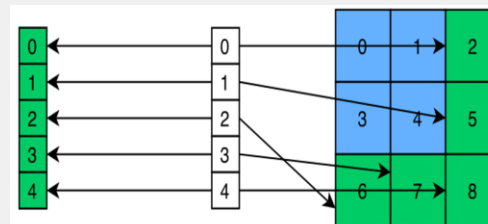


## Performance

### Algorithmic improvements



### Performance Optimization



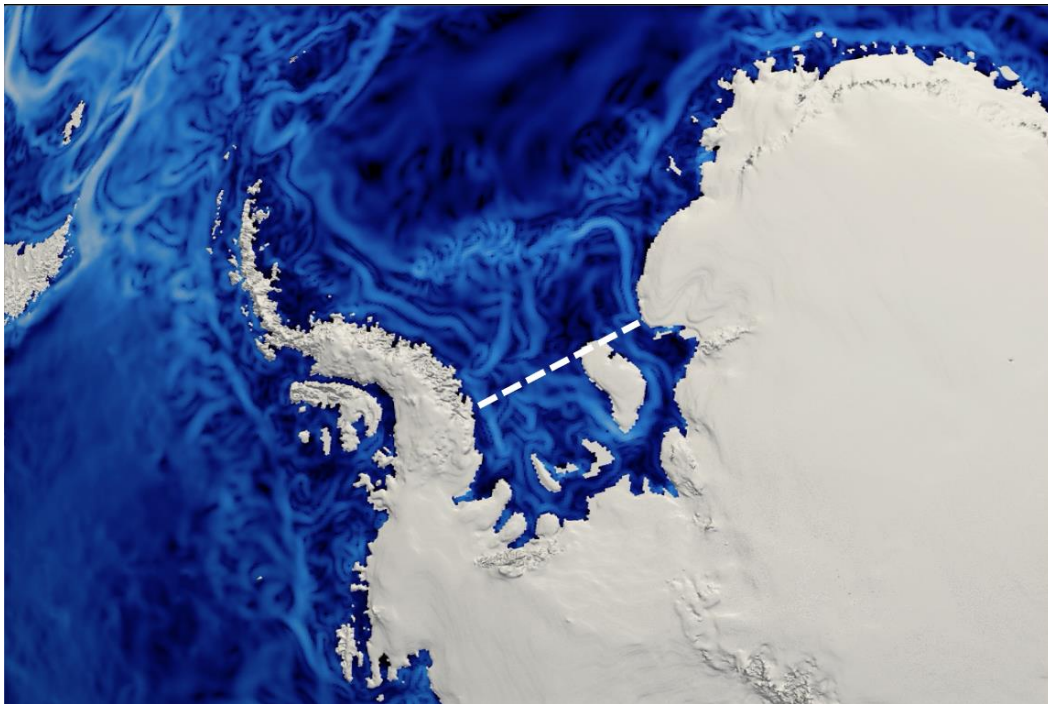
FAST MATH

RAPIDS



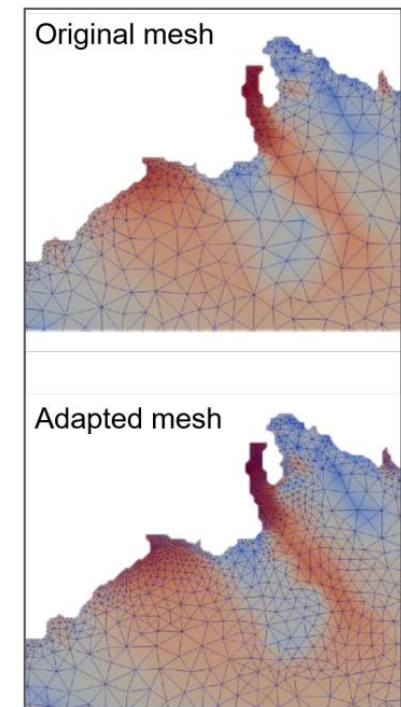
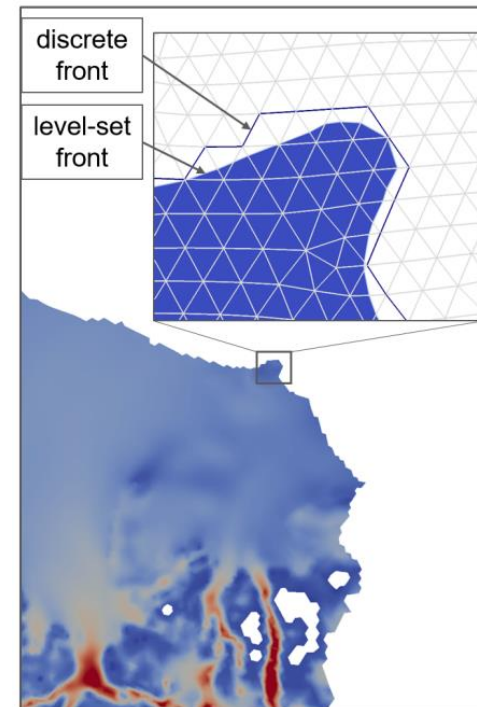
## E3SM+MALI

- Dynamic ocean/ice-sheet interface
  - Quantify performance characteristics
  - Quantify load balancing
  - Establish benchmarks



## MALI-standalone

- Level sets, mesh adaptivity, initialization
  - Quantify performance characteristics
  - Quantify load balancing
  - Establish benchmarks



# DOE Exascale

## NERSC Perlmutter (NVIDIA GPU)

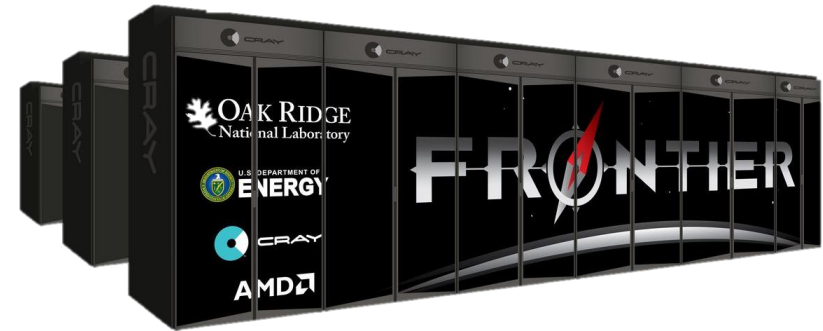
- Automated MALL testing
- Performance optimization
  - AMD EPYC & NVIDIA A100
- Establish benchmarks

## OLCF Frontier (AMD GPU)

- All TPLs have support
- Unified Virtual Memory (UVM) optional
- Start testing on Crusher

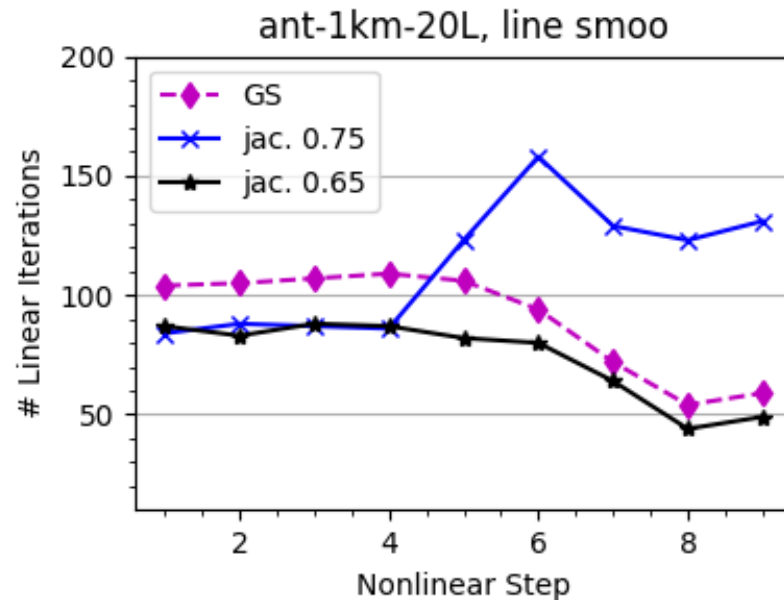
## ALCF Aurora (Intel GPU)

- Kokkos/SYCL
- Identify what's needed in Trilinos



## Algorithmic Improvements

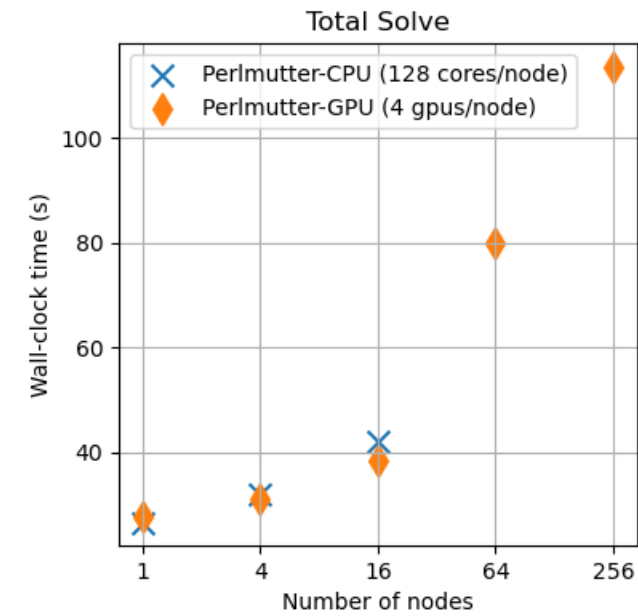
- Improve convergence of linear solver on GPUs
  - Damped block Jacobi for fine grid smoother



**Example:** AIS 1km Block Gauss-Seidel & Jacobi (Jonathan Hu)

## Performance Optimizations

- Scalability study on Perlmutter
  - Benchmarks for forward solve/initialization
  - Fix CUDA-Aware MPI
  - OpenMP build for CPU

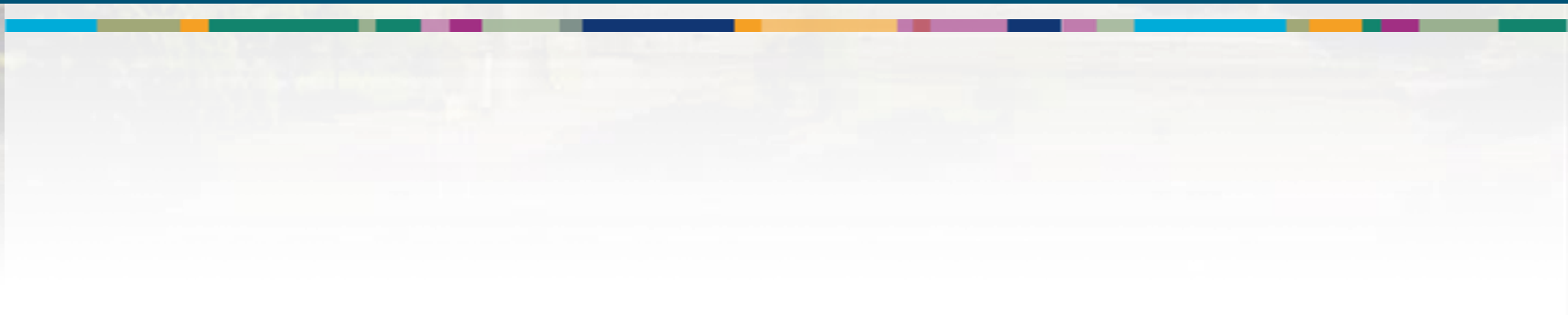
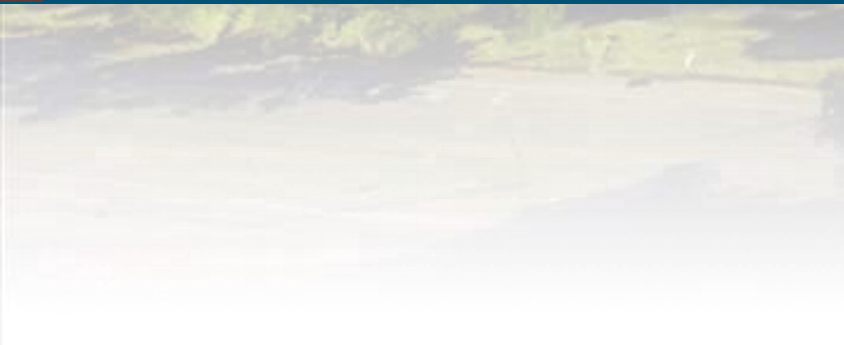


**Example:** Issues with AIS weak scalability on Perlmutter (Max Carlson)





# Conclusions





# Conclusions



- **HPC software/hardware is changing rapidly** which poses a significant challenge for open-science
- Multiple **performance portable** features exist in the **MALI** software stack to meet this challenge
- **Performance & portability** for exascale is a **work in progress**
  - **1.9x** speedup of V100 node over POWER9 node in total solve time
  - CPU scales better than GPU using best solvers (**65.1% vs. 41.2%** weak scaling efficiency)
- Maintaining **performance** and **portability** is crucial for an active code base
  - **Changepoint detection** adds level of confidence to performance regressions/improvements
  - **Bayesian optimization** adds level of confidence to optimal parameters for given system

Watkins, J., Carlson, M., Shan, K., Tezaur, I., Perego, M., Bertagna, L., Kao, C. *et al.*

“Performance portable ice-sheet modeling with MALI.” (Submitted, IJHPCA) <https://arxiv.org/abs/2204.04321>

# Funding/Acknowledgements



Support for this work was provided by Scientific Discovery through Advanced Computing (**SciDAC**) projects funded by the U.S. Department of Energy, Office of Science (**OS**), Advanced Scientific Computing Research (**ASCR**) and Biological and Environmental Research (**BER**).

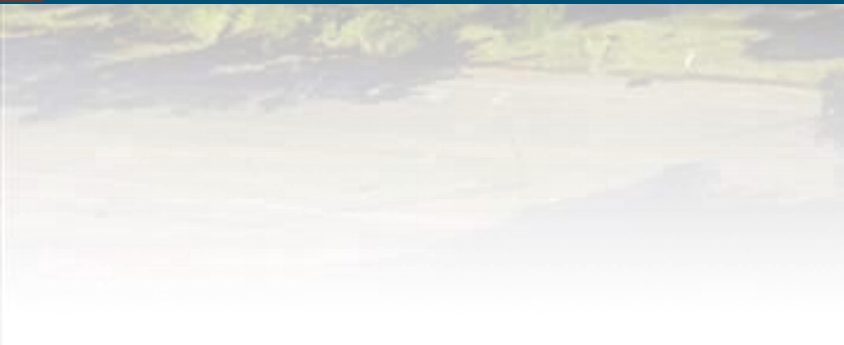


Computing resources provided by the National Energy Research Scientific Computing Center (**NERSC**) and Oak Ridge Leadership Computing Facility (**OLCF**).





Backup





# Weak Scalability Study



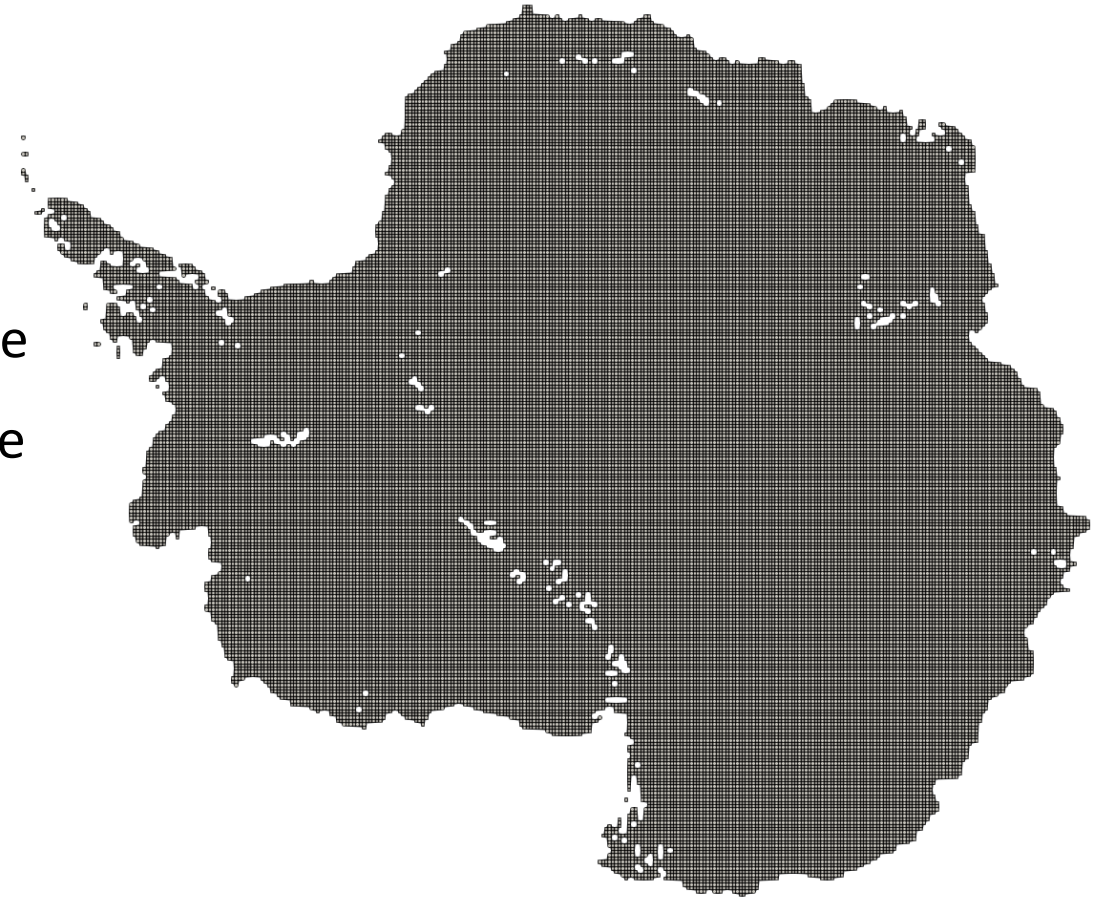
## Architectures:

- NERSC Cori-Haswell (**HSW**): 32 cores/node
- NERSC Cori-KNL (**KNL**): 68 cores/node
- OLCF Summit-POWER9-only (**PWR9**): 44 cores/node
- OLCF Summit-POWER9-V100 (**V100**): 44 cores/node + 6 GPU/node

## Benchmark:

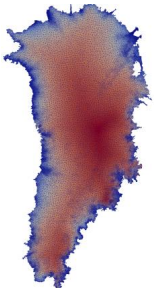
- First-order Stokes, hexahedral elements
- 16 to 1km structured Antarctica meshes, 20 layers
- 1 to 256 compute nodes

Benchmark used to assess performance



**Mesh Example:** 16km, structured Antarctica mesh (2.20E6 DOF - 20 layer, 2 equations)

# Autotuned performance portable smoothers



Random search used to improve performance of multigrid smoothers on GPU

## Smoother parameters:

- Limited to three levels, two smoothers
- Good parameter ranges provided by Trilinos/MueLu team

```
type: RELAXATION
ParameterList:
  'relaxation: type': MT Gauss-Seidel
  'relaxation: sweeps': positive integer
  'relaxation: damping factor': positive real number

type: RELAXATION
ParameterList:
  'relaxation: type': Two-stage Gauss-Seidel
  'relaxation: sweeps': positive integer
  'relaxation: inner damping factor': positive real number

type: CHEBYSHEV
ParameterList:
  'chebyshev: degree': positive integer
  'chebyshev: ratio eigenvalue': positive real number
  'chebyshev: eigenvalue max iterations': positive integer
```

## Results:

- Applied to four cases (Greenland, 3-20km)
  - Different architectures (blake: 8 CPU nodes/weaver: GPU)
  - Different equations (vel: FOSTokes/ent: Enthalpy)
- 100 iterations, random search
- Timer: Preconditioner + Linear Solve

Cases	Manual Tuning (sec.)	Autotuning (sec.)	Speedup
blake_vel	3.533972	2.658731	1.33x
blake_ent	3.07725	2.036044	1.51x
weaver_vel	19.13084	16.30672	1.17x
weaver_ent	19.76345	15.00014	1.32x

Cases	#Passed Runs	#Failed Runs	%Failure
blake_vel	70	30	30%
blake_ent	37	63	63%
weaver_vel	71	29	29%
weaver_ent	26	74	74%

Autotuning framework: Carolyn Kao



# Performance on Cori and Summit



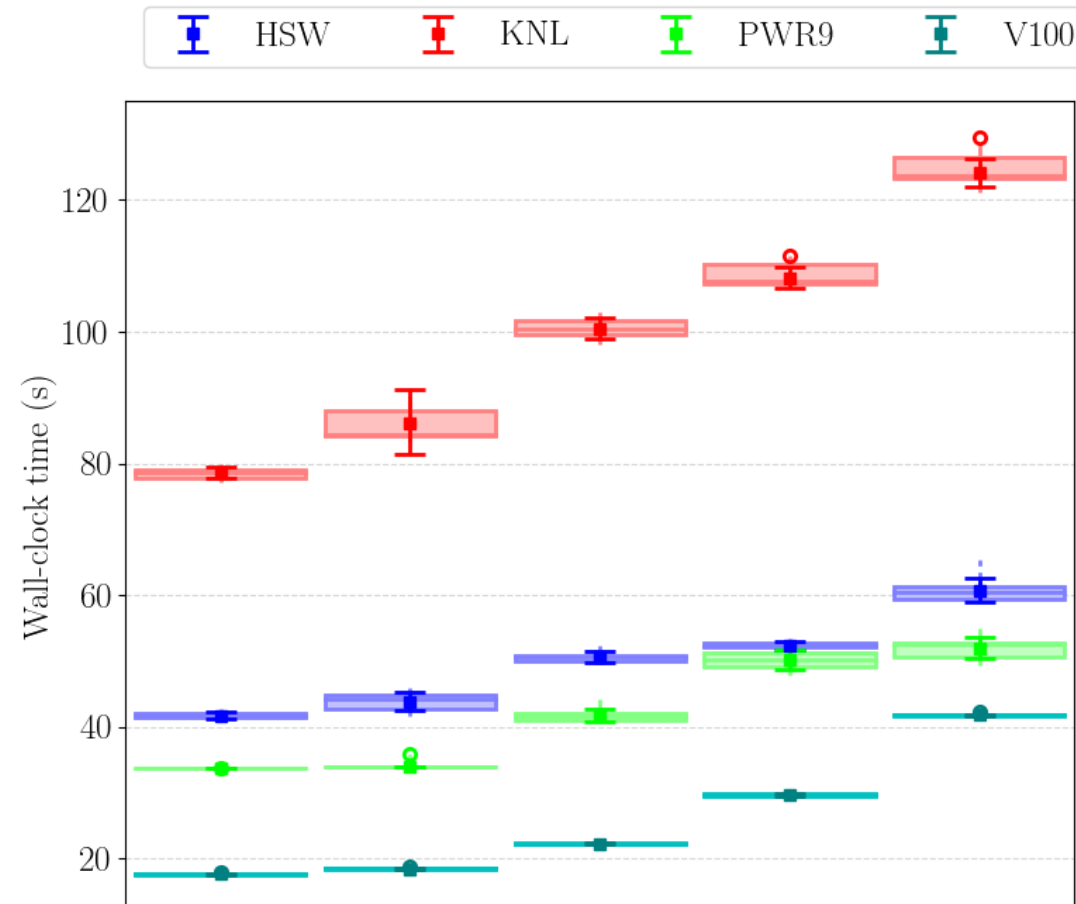
## Setup:

- Tuned input files
  - CPU block preconditioner
  - Autotuned GPU point smoothers
- Multiple samples for confidence

## Results:

- CPU scales better than GPU
  - 16->18 avg. linear iterations on CPU
  - 88->194 avg. linear iterations on GPU
- Speedup on GPU
  - 1.9->1.2 speedup V100 over POWER9
  - Speedup degrades at higher resolutions

Speedup over MPI-only simulations;  
Tuned CPU model scales better



Resolution	16km	8km	4km	2km	1km
# Nodes	1	4	16	64	256
V100 Speedup	1.92	1.85	1.88	1.70	1.24
99% CI	(1.91, 1.92)	(1.84, 1.86)	(1.84, 1.92)	(1.65, 1.74)	(1.21, 1.28)

# Areas to improve

## Weak Scaling Efficiency:

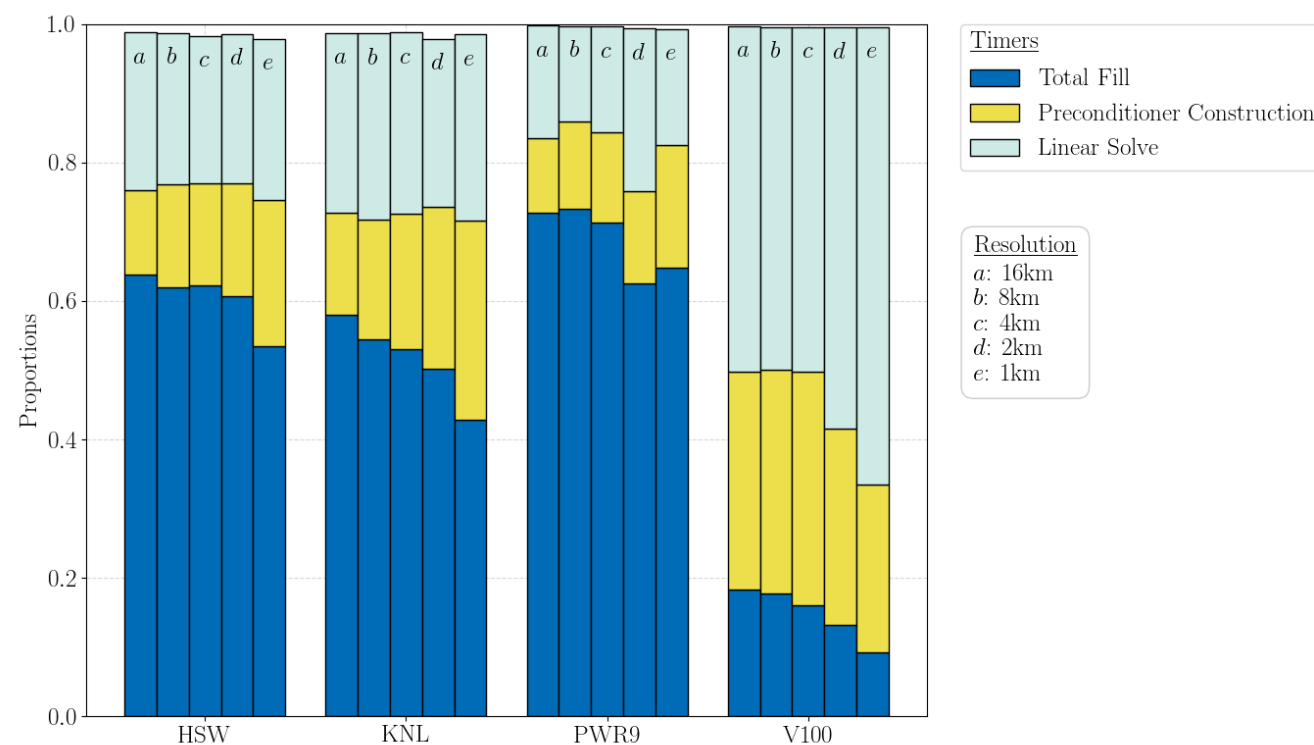
- Higher is better
- Areas of improvement
  - CPU/GPU preconditioner construction
  - GPU linear solve (better precondition.)

## Proportions of total solve time:

- Improve assembly on CPU
  - 40-60% of total solve time
- Improve GPU linear solver
  - 80-90% of total solve time

Focus on improving GPU solver

	Total Solve	Total Fill	Preconditioner Construction	Linear Solve
HSW	68.9% (67.0, 70.9)	82.2% (81.5, 82.9)	41.2% (38.2, 44.5)	67.5% (66.2, 68.8)
KNL	63.5% (62.3, 64.6)	85.3% (84.5, 86.0)	33.0% (30.8, 35.5)	61.1% (60.6, 61.6)
PWR9	65.1% (63.3, 66.9)	73.1% (70.0, 76.4)	39.5% (39.0, 40.0)	63.0% (62.9, 63.1)
V100	42.2% (42.0, 42.4)	82.9% (80.5, 85.4)	55.2% (54.7, 55.8)	31.9% (31.6, 32.2)

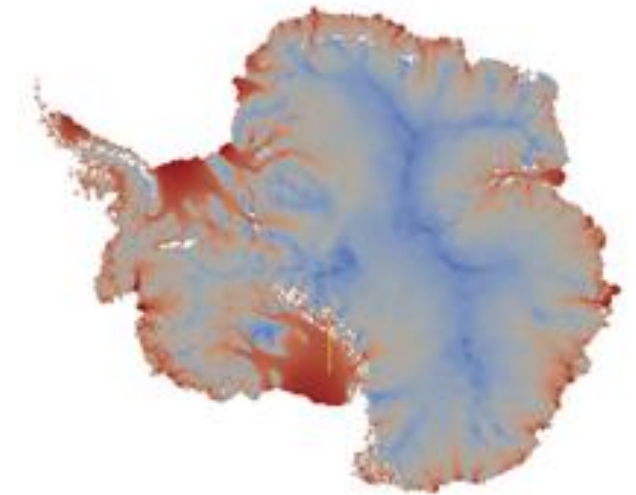
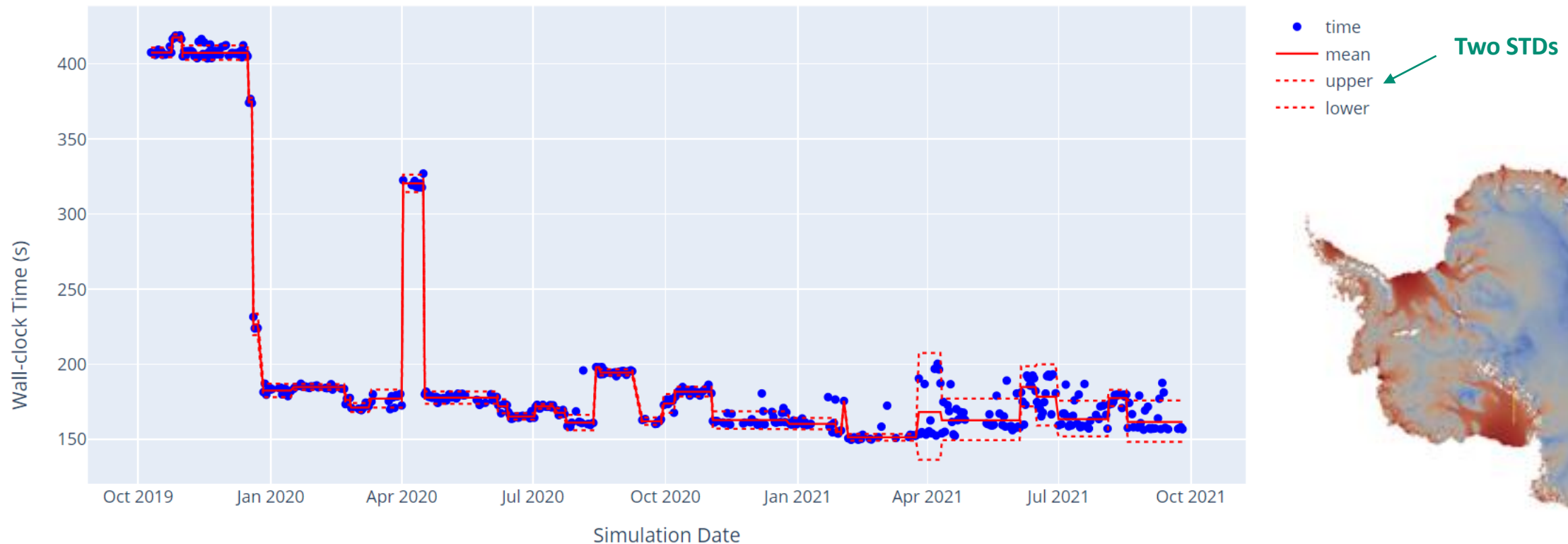


# Changepoint detection for performance testing



**Maintaining/improving performance and portability in the presence of active development is essential**

- **Changepoint detection:** process of finding abrupt variations in time series data
- Manual testing and analysis is increasingly infeasible



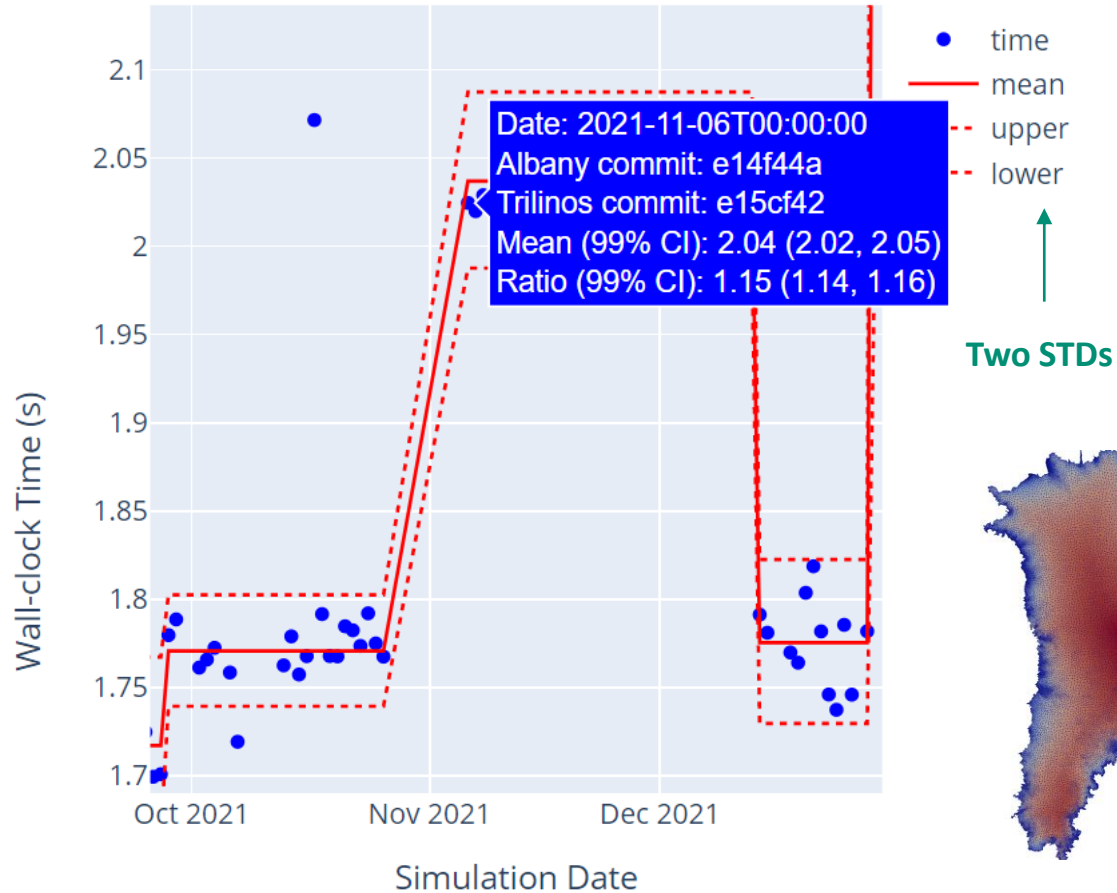
**Total Time** for a 2-to-20 km resolution Antarctica mesh, executed nightly in Albany Land Ice  
**Changepoint Detection:** Kyle Shan

# Detecting performance regressions/improvements

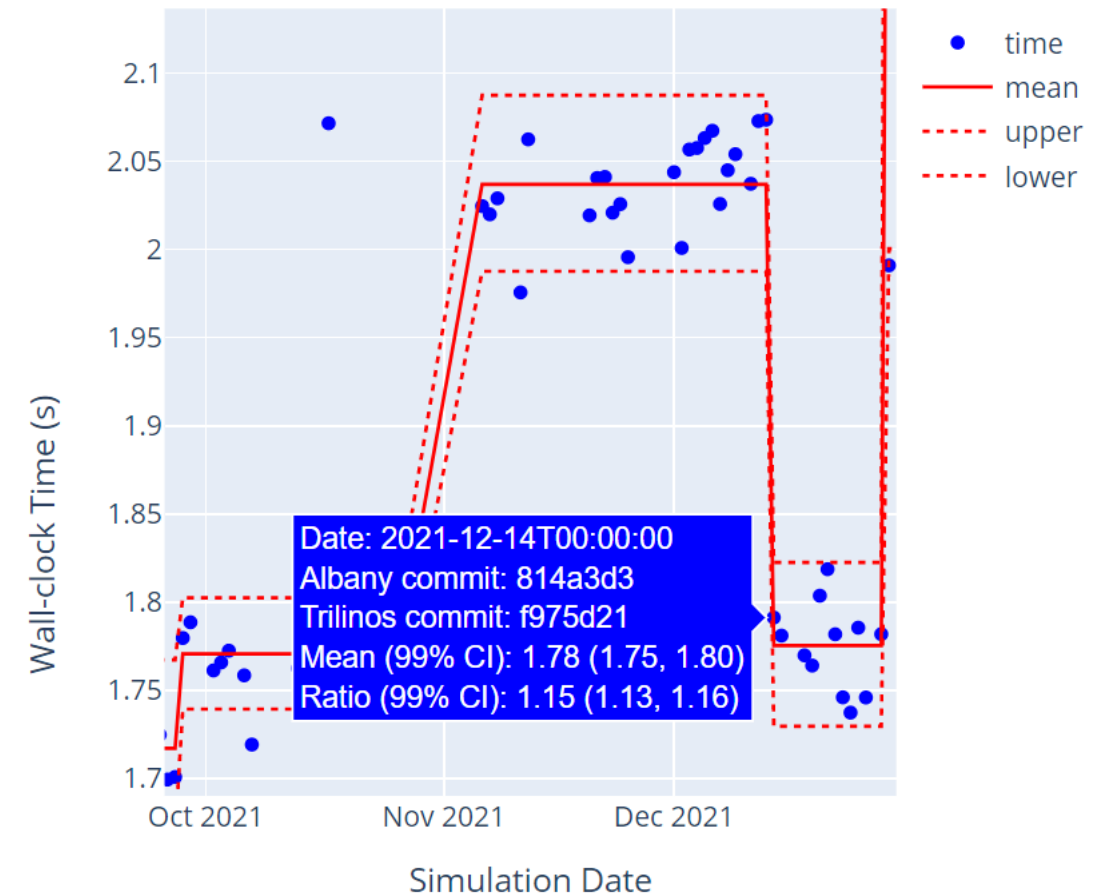


Example: Transition to Kokkos 3.5.0 caused a performance regression but was soon fixed

## Regression



## Improvement

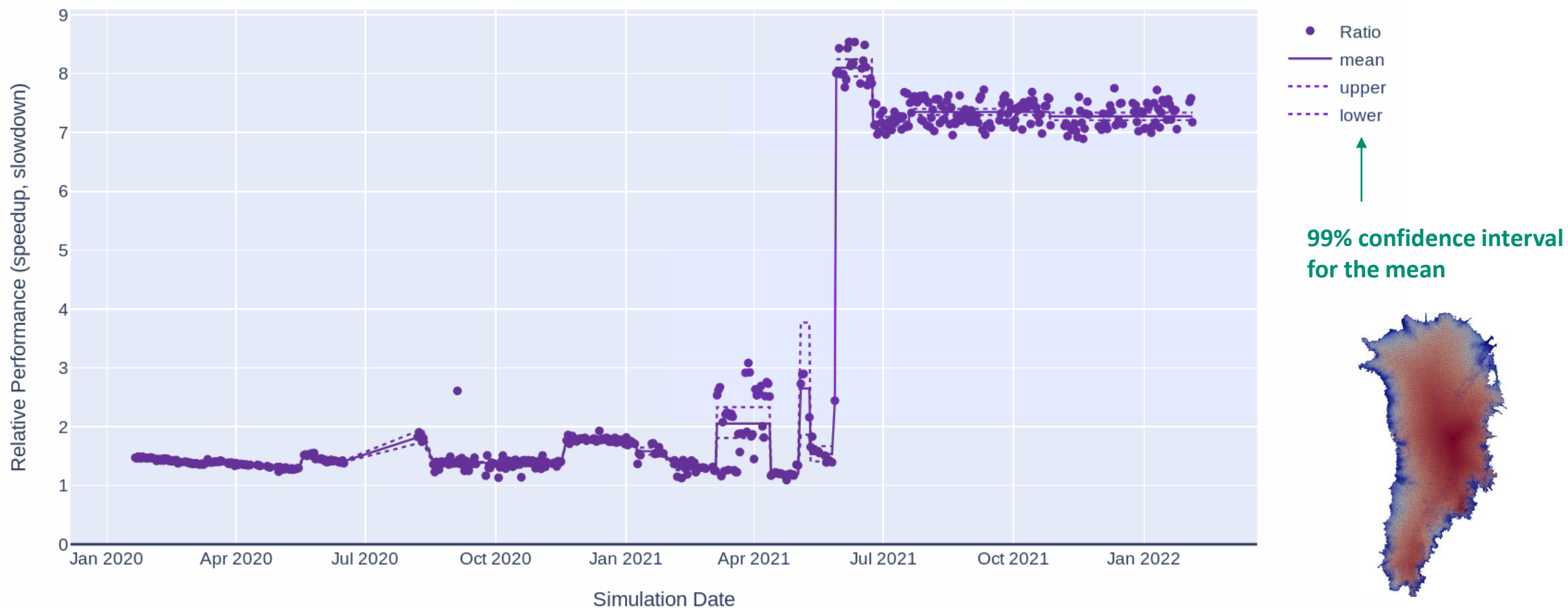


**Total Fill** time for a 1-to-7 km resolution Greenland mesh, executed nightly in Albany Land Ice

# Algorithmic performance comparisons



Example: Memoization comparison (w. & w.o.) shows that relative performance has increased



Speedup of **Total Fill** time from **memoization** for a 1-to-7 km resolution Greenland mesh, executed nightly in Albany Land Ice