



# Machine-learned Interatomic Potential Development for H Trapping in ZrC Strengthened W

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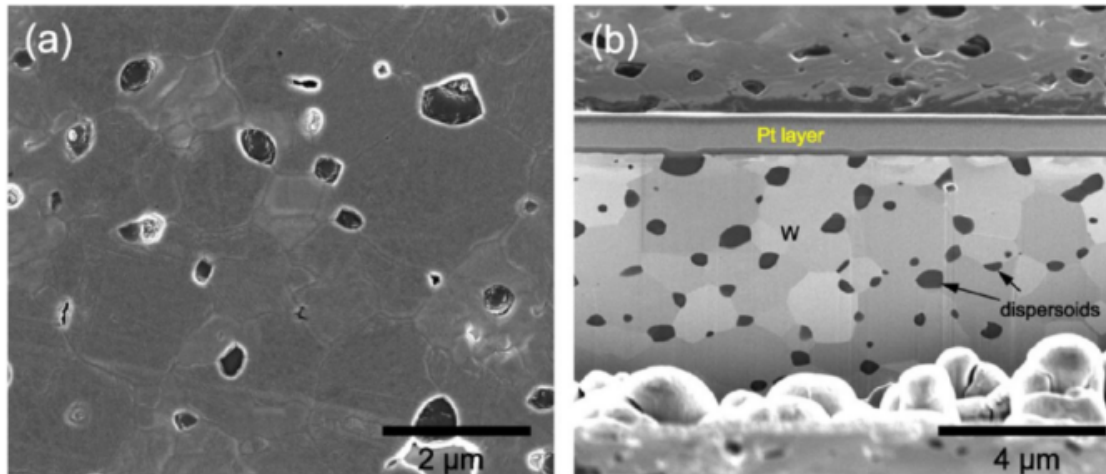


- Application/Needs of the Potential(s)
- Potential Development Workflow (W-ZrC)
  - DFT Training Data
  - Objective functions vs. energy and force errors
- Example of the W-ZrC Potential's Performance: Bicrystal Tensile Tests
- Preliminary W-ZrC-H properties and performance

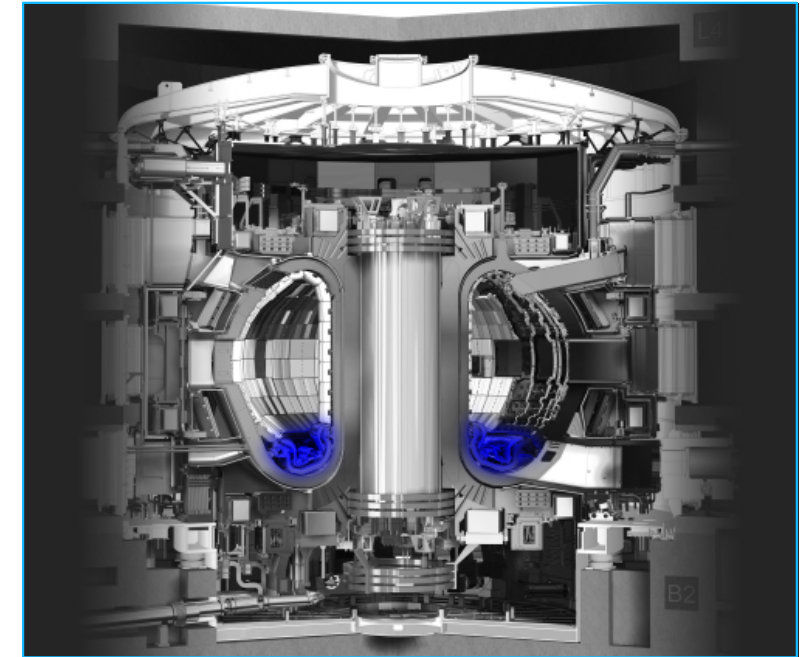
# How can we predict fusion material performance?



- W suffers from a high brittle-to-ductile transition temperature ( $>473\text{ K}$ )<sup>2</sup> and may undergo recrystallization and grain growth above  $1000\text{ K}$ <sup>3</sup>.
- Strengthening W with zirconium carbide (ZrC) can improve mechanical properties, but these mechanisms and effects on hydrogen fuel retention are not well understood.



**SEM of ZrC dispersoid strengthened W<sup>4</sup>**



**The divertor in a fusion reactor will control the waste and withstand the highest heat loads of the machine<sup>1</sup>.**

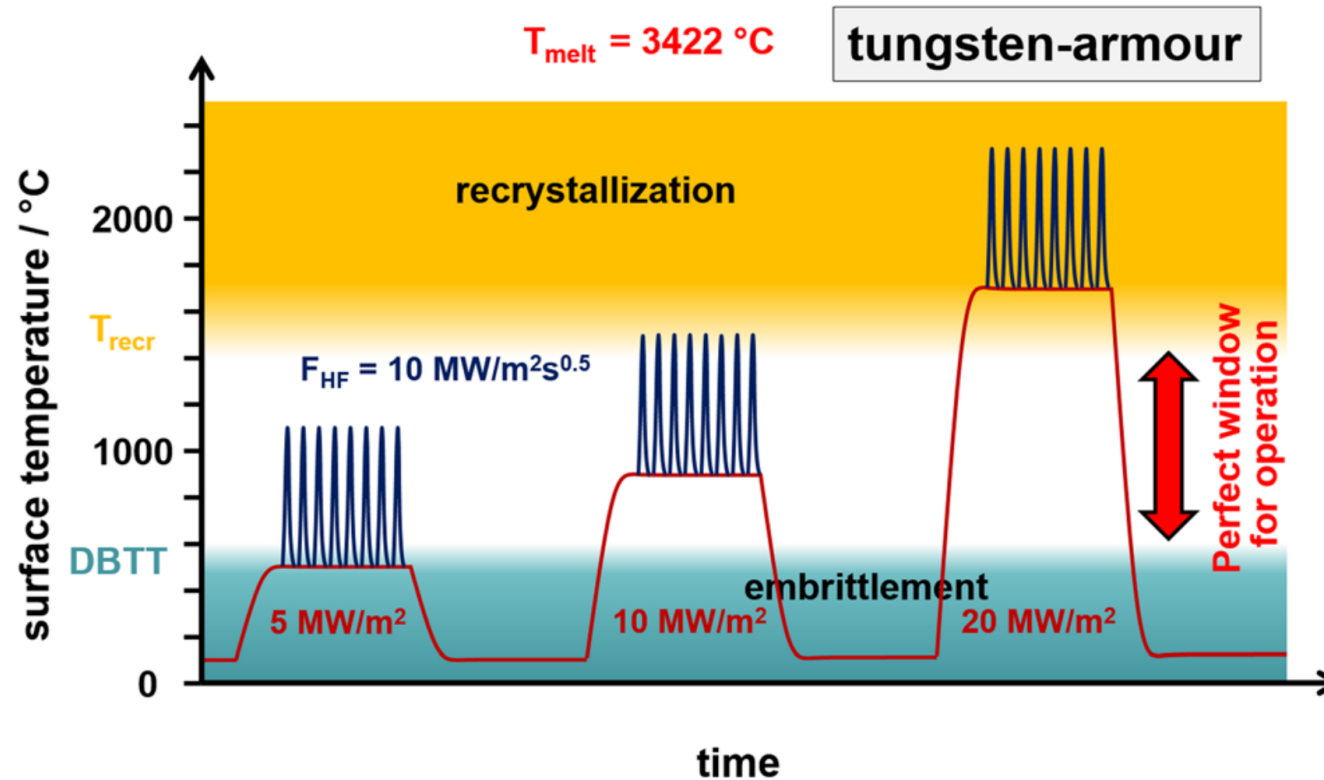
[1] [www.iter.org/mach](http://www.iter.org/mach)

[2] Xie, et al. Sci. Rep. 5, 1-11 (2015)

[3] Lang, et al. J. Nucl. Mater. 545, 152613 (2021)

[4] Kolasinski, et al. Int. J. Refract. Met. Hard Mater. 60 (2016).

The divertor in ITER is expected to reach up to 2573 K under normal operation.



**FIG. 3.** Schematic presentation of the surface temperature of tungsten-armored divertor targets in ITER at three different power density levels (5, 10, and 20 MW m<sup>-2</sup>). Thermal spikes caused by mitigated ELMs with an assumed intensity of 10 MW m<sup>-2</sup> s<sup>0.5</sup> are shown in dark blue.<sup>16</sup> Reproduced with permission from Rieth *et al.*, J. Nucl. Mater. **519**, 334-368 (2019). Copyright 2019 Elsevier.



# The Spectral Neighbor Analysis Potential (SNAP) can map quantum data to a classical interatomic potential.



## Model Form

- Each neighbor position,  $(r, \theta, \phi)$ , is mapped to a point,  $(\theta_0, \phi, \theta)$ , on the unit 3-sphere.
- The basis can be described with bispectrum components,  $B_k^i$ .
- Fitting the linear coefficients,  $\beta_k$ , produces the SNAP potential:

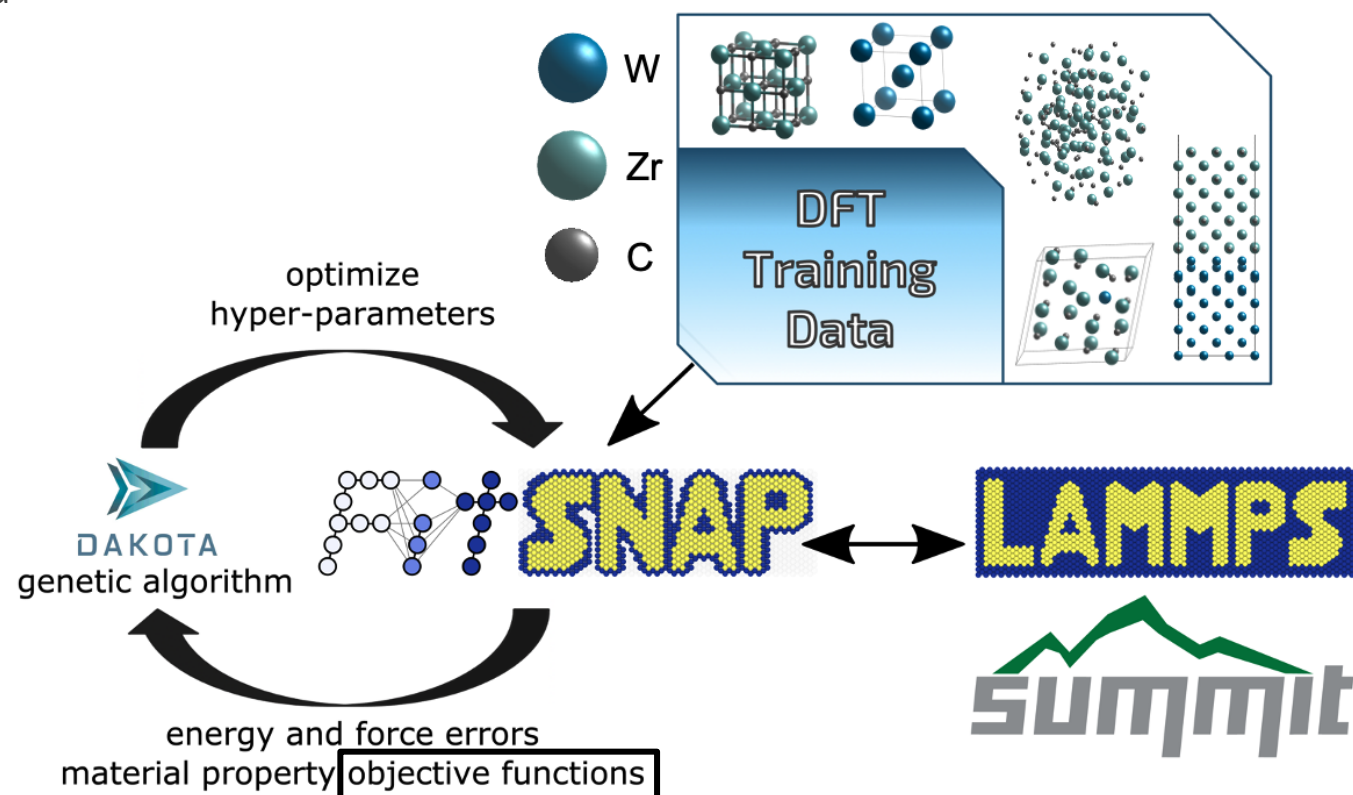
$$E_{SNAP}^i = \beta_0 + \sum_{k=1}^K \beta_k (B_k^i - B_k^i 0)$$

## Linear Regression

$$\min(\|\epsilon \cdot (D\beta - T)\|^2)$$

group weight    descriptor prediction    DFT training

## Work flow

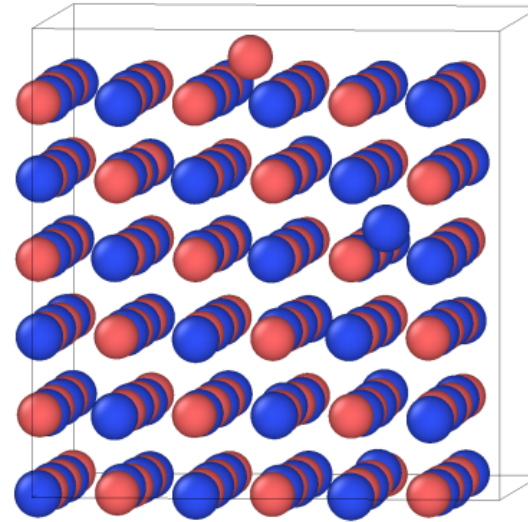


Code available: <https://github.com/FitSNAP/FitSNAP>  
 →(Now with docs! <https://fitsnap.github.io/> )

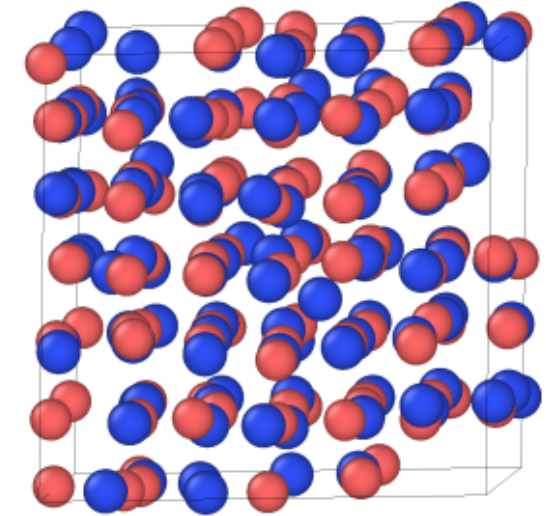
# What is an objection function? Example using Radial Distribution Function



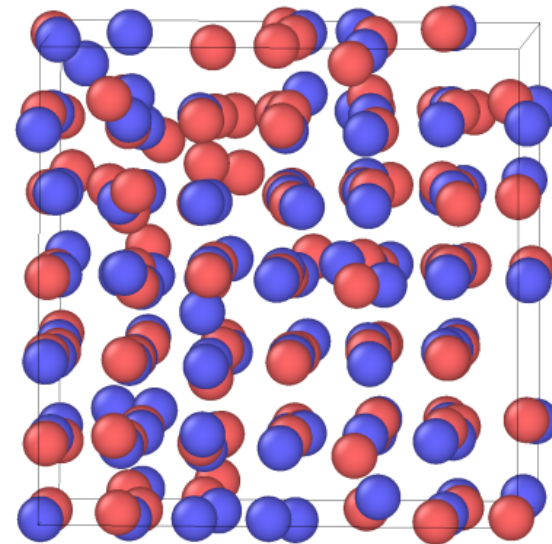
- NPT run @ 2000K
- 3x3x3 supercell with 1U and 1N interstitial
- RDF calculated with 50 bins and 4 Å cutoff
- Objective function takes the absolute value of the difference between SNAP and DFT for each bin
- Throws arbitrary error if atoms cluster



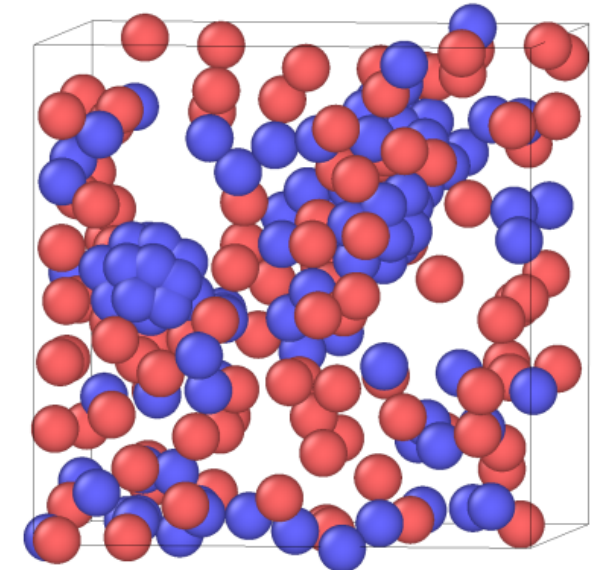
Starting structure



AIMD after 817 fs

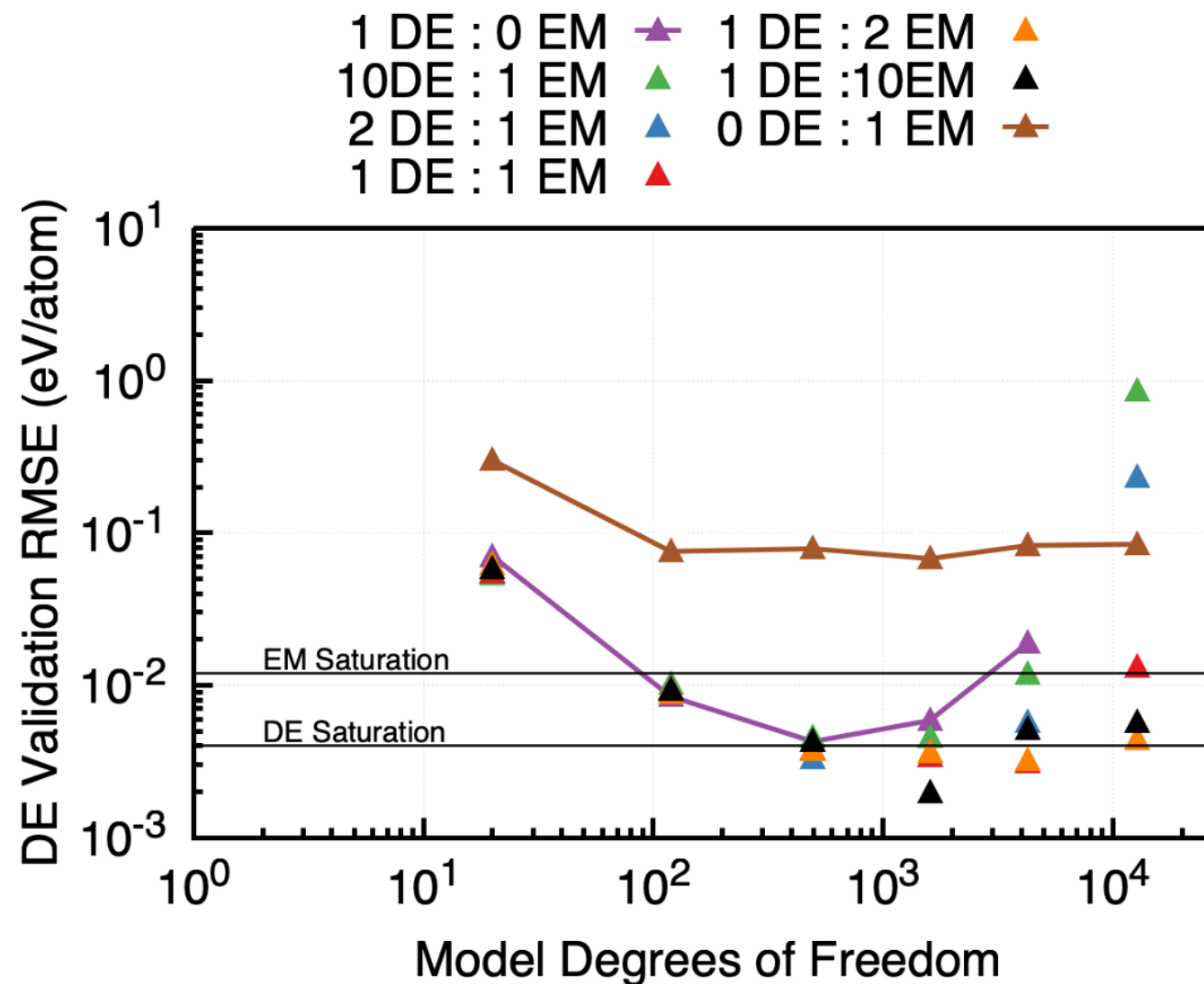


Obj. f. value 5.33



Penalty value 2113

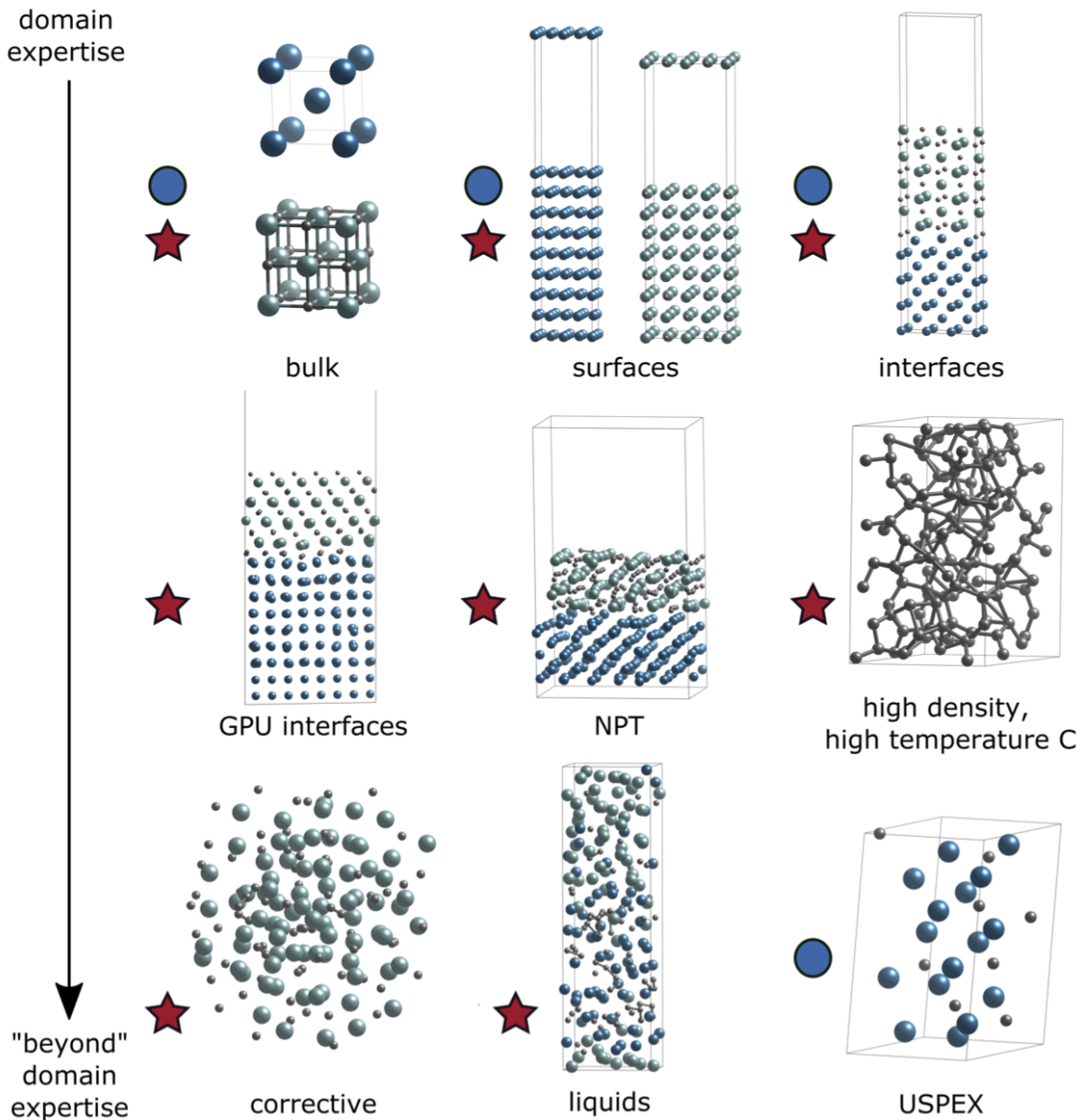
# How to make a transferable potential – “domain expertise” (DE) vs. “entropy maximized” (EM)



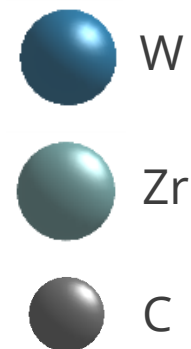
# What is in the training set? (~9,000 structures)



domain  
expertise

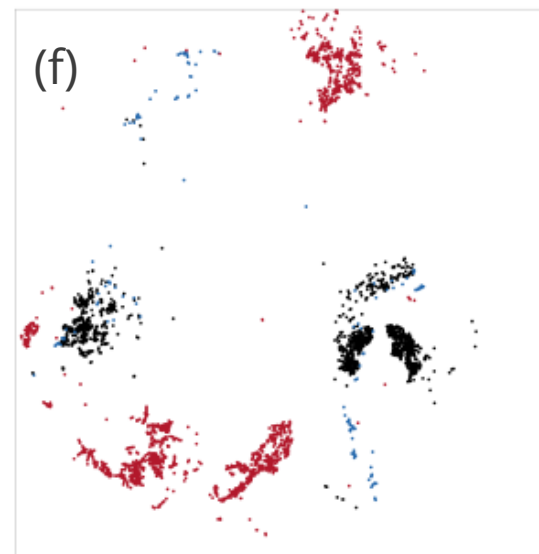
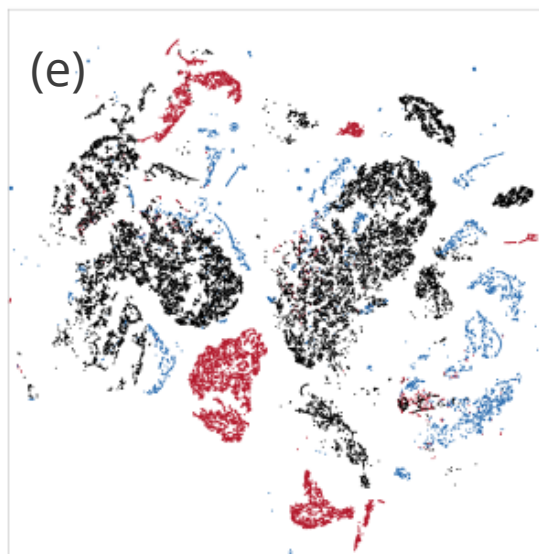
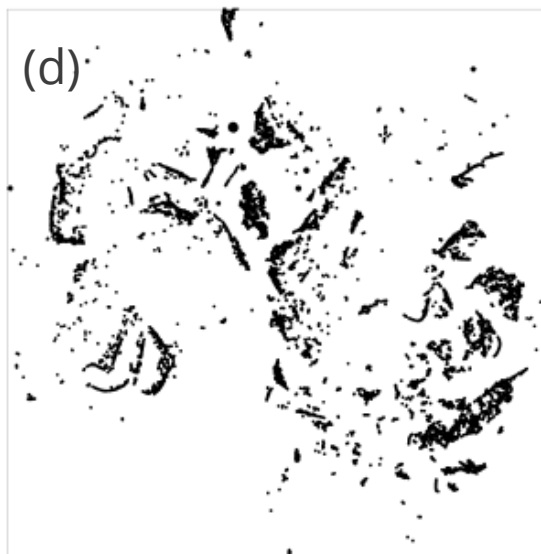
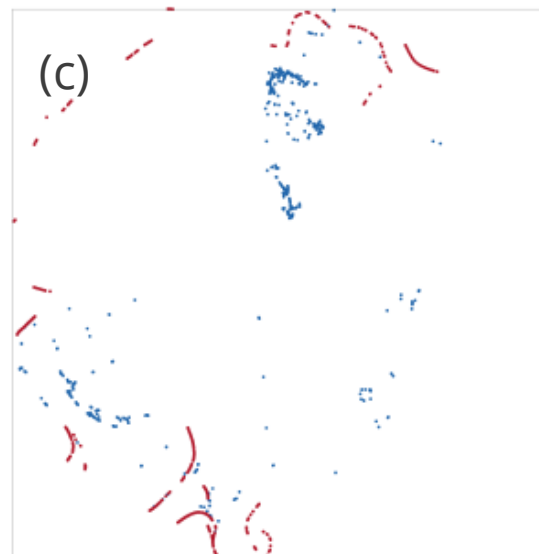
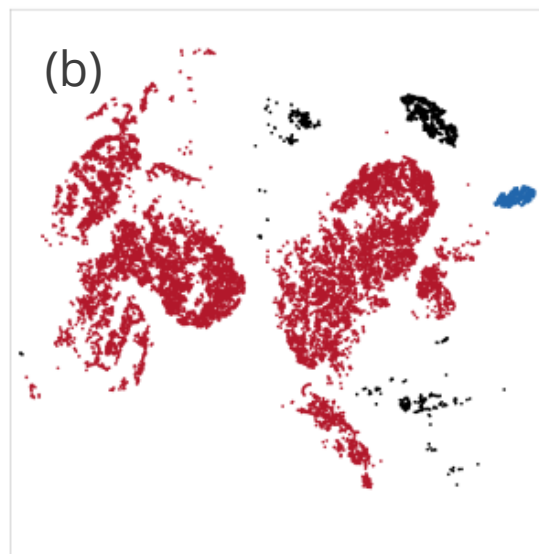
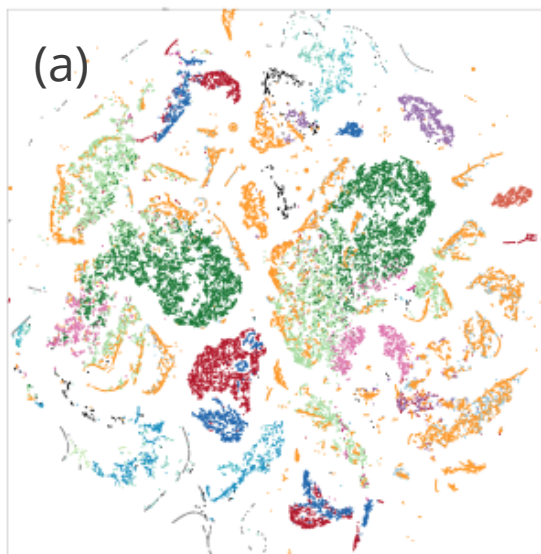


● without temperature (DFT)  
★ with temperature (AIMD)





# How does this configuration data look to SNAP?



## t-SNE visualization of SNAP descriptors in 2D

(a) All data  
\*labels omitted

(b) By constituents

● W ● ZrC ● C

(c) Ground states

● EOS ● unit cells, defects, etc.

(d) AIMD – 300K

(e) AIMD – 1000 – 5000K

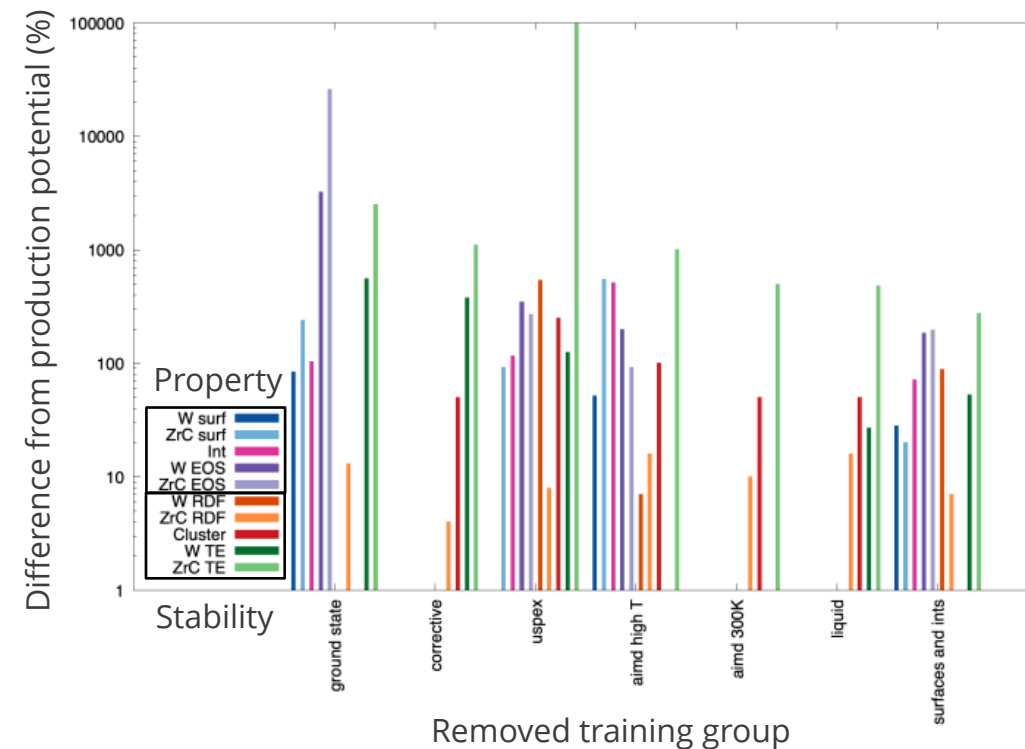
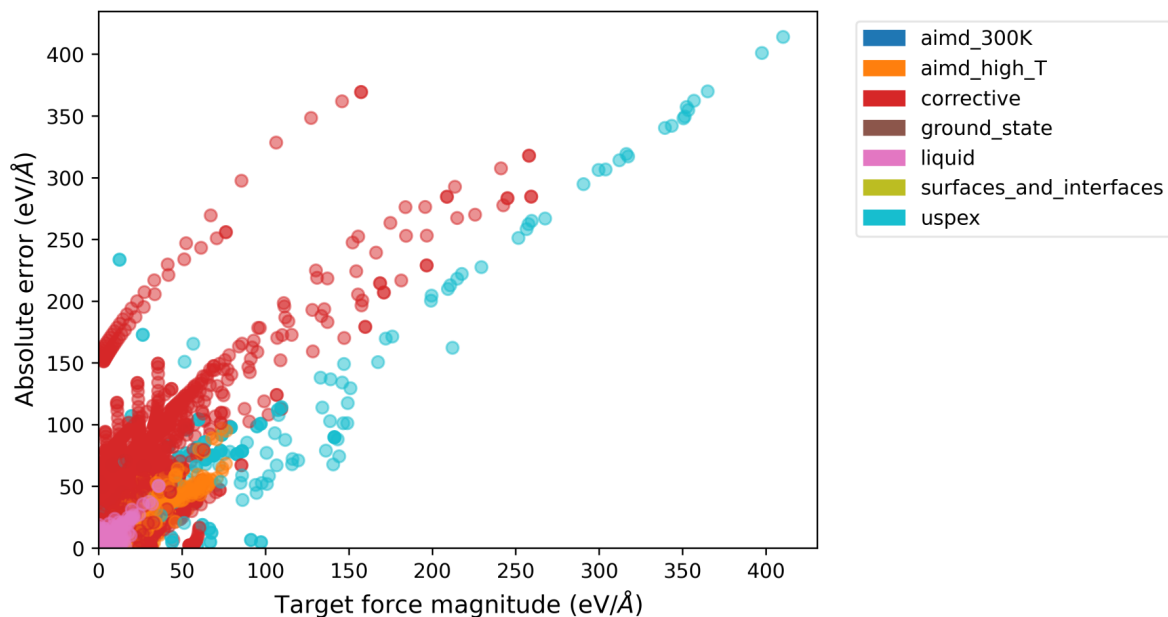
● W/ZrC/C ● >200 atoms ● interfaces

(f) Beyond domain expertise

● liquid ● USPEX ● corrective



# Do low force and energy errors prove a potential is good?



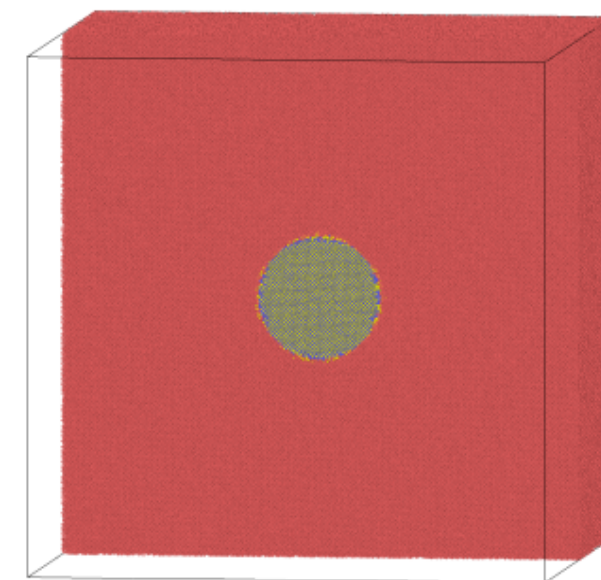
	Production Potential	Drop ground state	Drop corrective	Drop USPEX	Drop AIMD High T	Drop AIMD 300K	Drop Liquid	Drop surfaces and ints
Energy error (eV/atom)	0.43	0.34	0.43	0.25	0.41	0.55	0.44	0.44
Force error (eV/Å)	1.02	0.78	0.95	0.62	1.53	1.22	0.95	1.04

→ No, low force and energy errors may be promising, but provide no information on the accuracy of material properties or dynamics.

# The W-ZrC SNAP agrees well with DFT and can now run 10s of nm/10 million atom structures.



- The W-ZrC SNAP potential yields material properties in good agreement with DFT values for lattice parameter,  $a$  (Å), bulk modulus,  $B$  (GPa), and surface energies,  $E_{surf}$  (eV/Å).
- Using the W-ZrC SNAP potential we can run millions of atom simulations at divertor temperature ranges ( $\sim 373 - 2573$  K<sup>8</sup>).



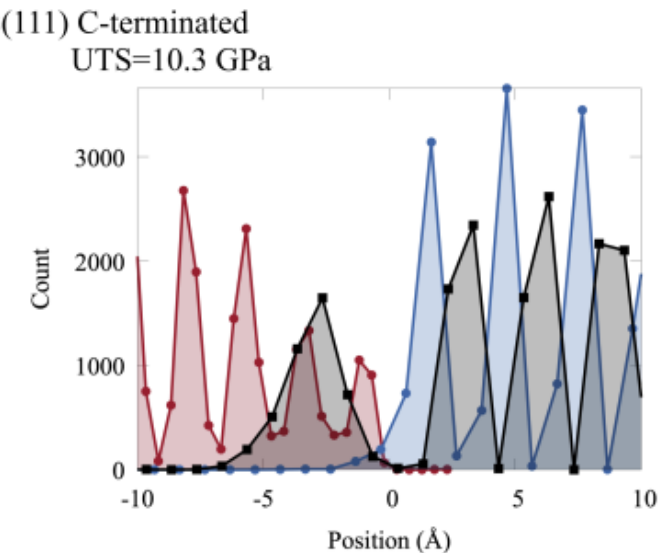
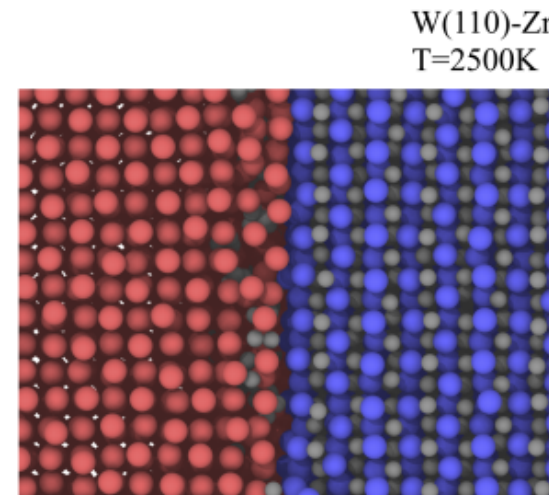
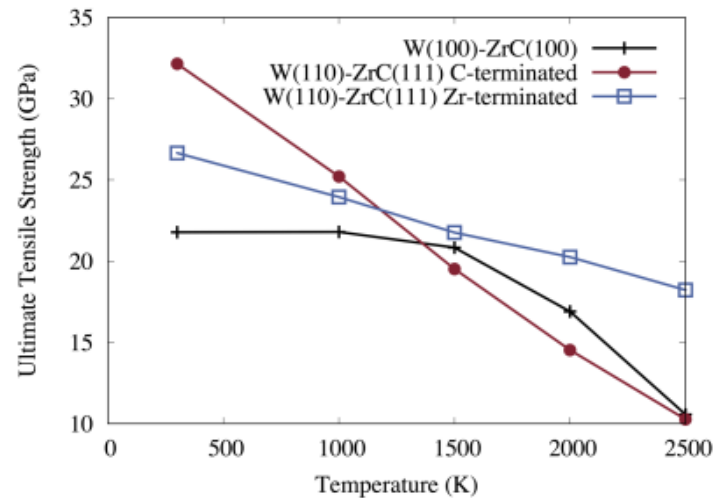
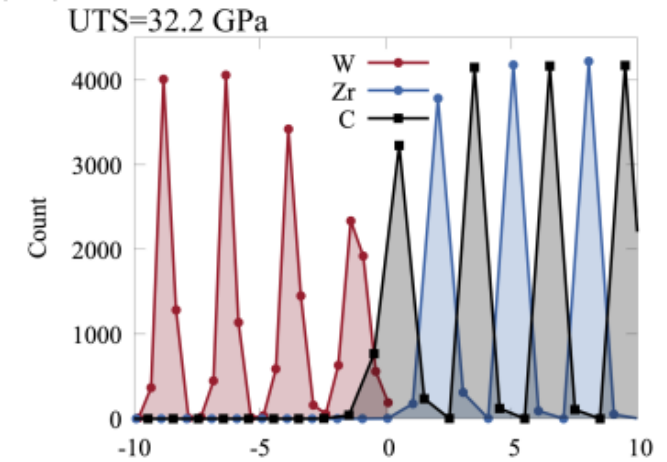
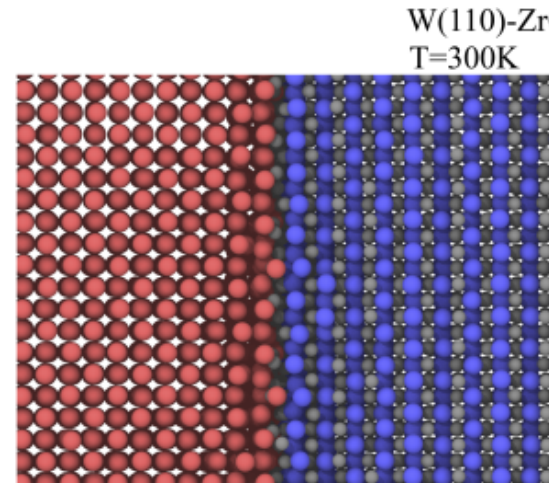
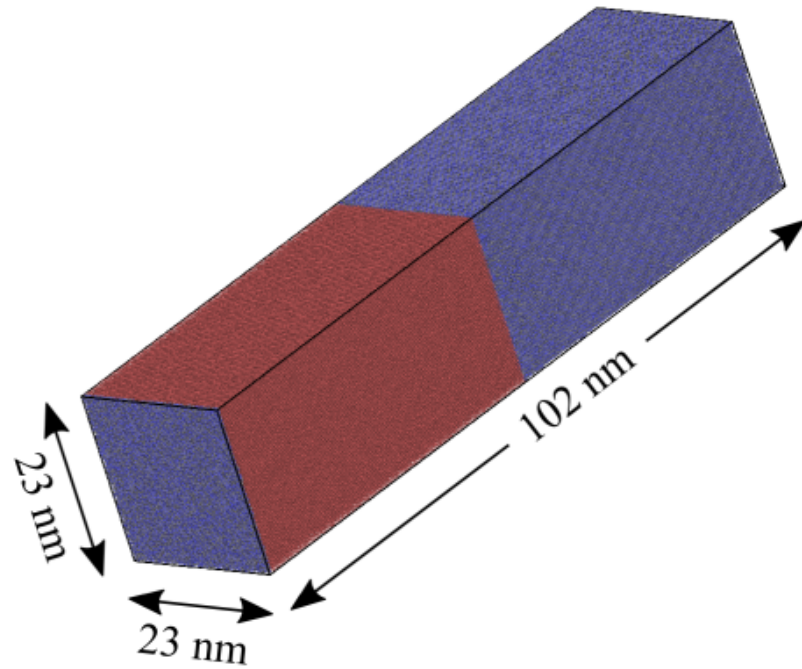
**Spherical ZrC in crystalline W at 1700 K**  
(~10 million atoms, 56 nm per side)



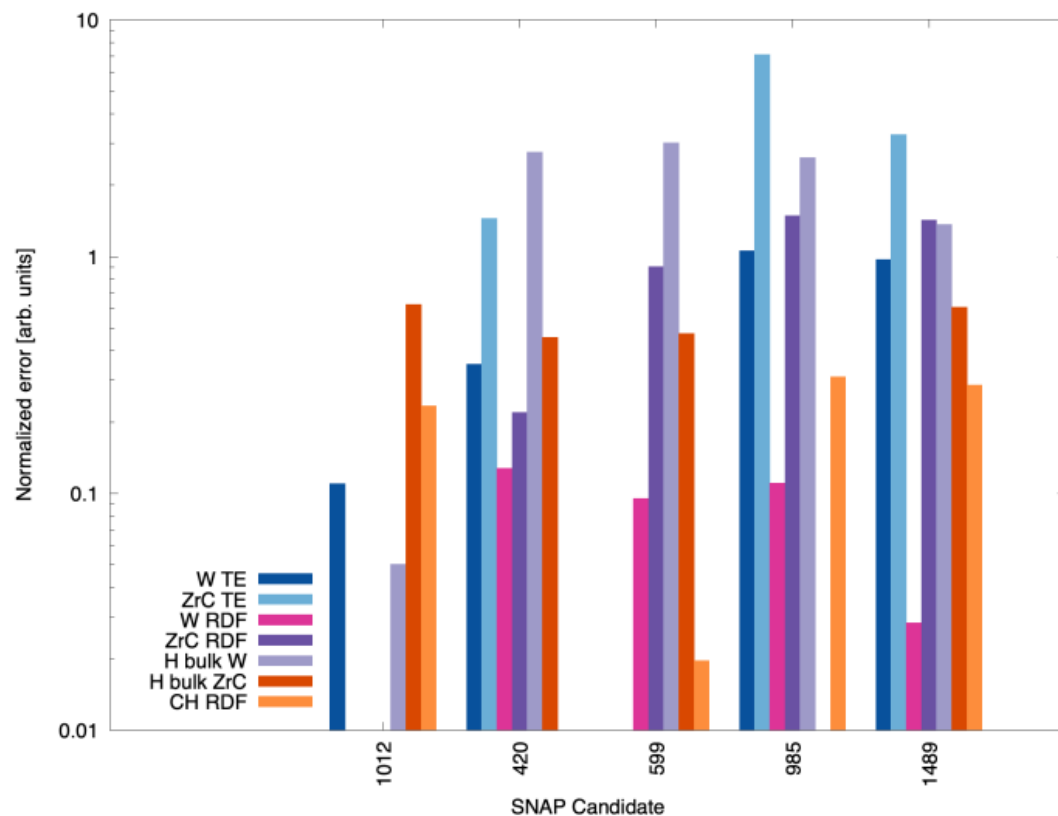
**Material properties predicted by DFT vs. SNAP**

	$B_W$	$B_{ZrC}$	$E_{surf}^W$ (100)	$E_{surf}^W$ (110)	$E_{surf}^{ZrC}$ (100)	$E_{surf}^{ZrC}$ (110)	$a_W^{2600K}$	$a_{ZrC}^{2600K}$
DFT/expt.	301.4	216.0	4.13	3.18	1.63	3.31	1.31	1.85
SNAP	303.3	209.0	3.38	3.22	1.40	2.75	1.05	1.50

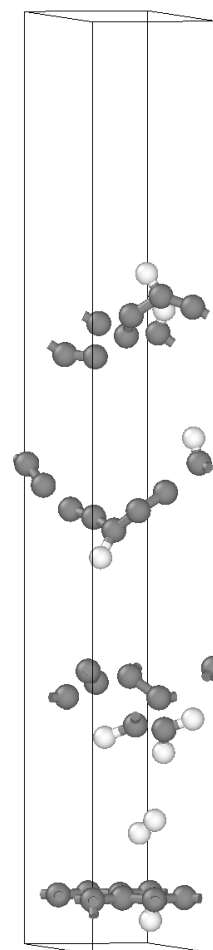
# Example of W-ZrC Performance: bicrystals for tensile testing



# SNAP candidates often exhibit trade-offs.

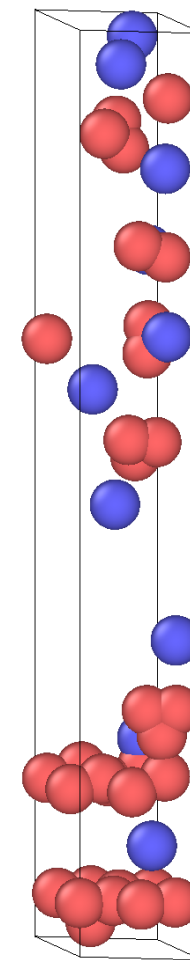


	SNAP (1012)	DFT
H tetrahedral - W	-0.89	0.88
H octahedral - W	-0.71	1.26
H tetrahedral - ZrC	4.53	11.33
H substitutional C - ZrC	1.61	-1.44

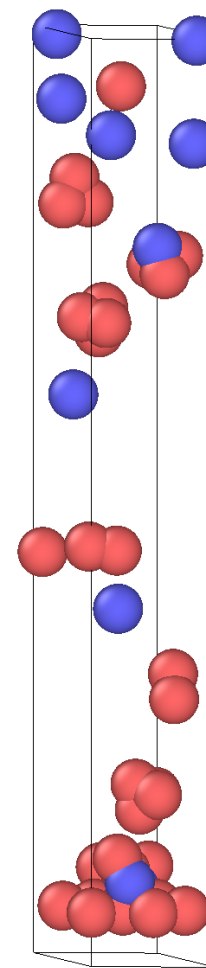


AIMD

CH RDF



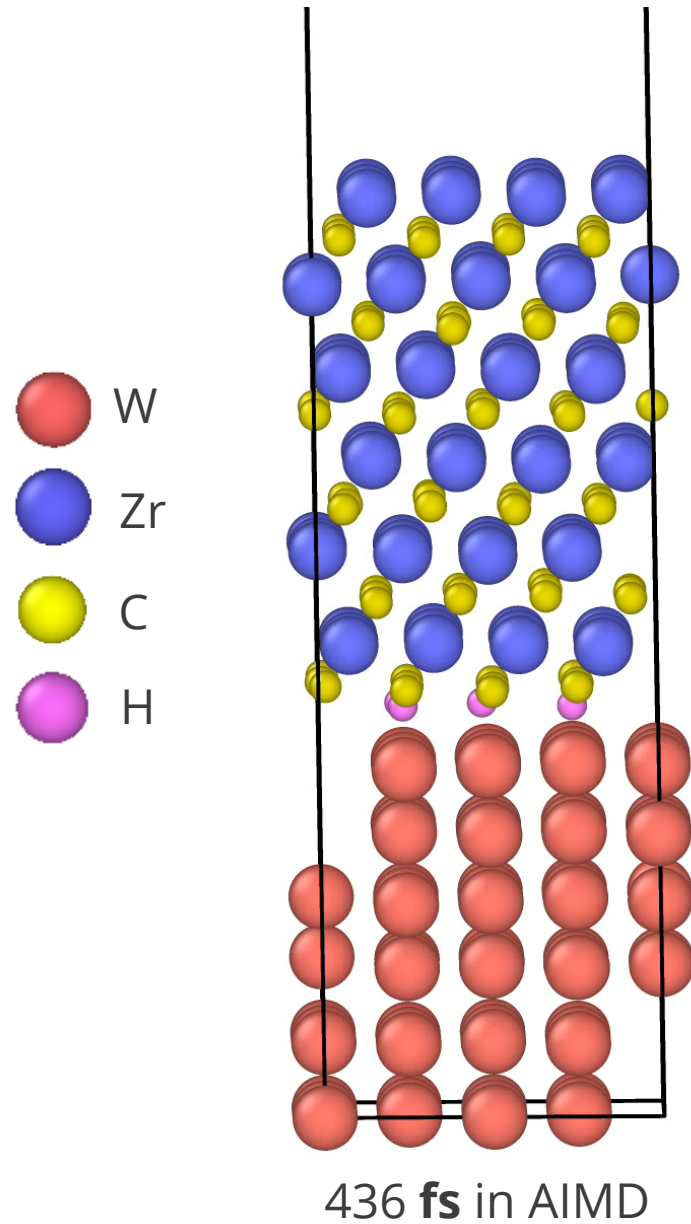
Candidate 420



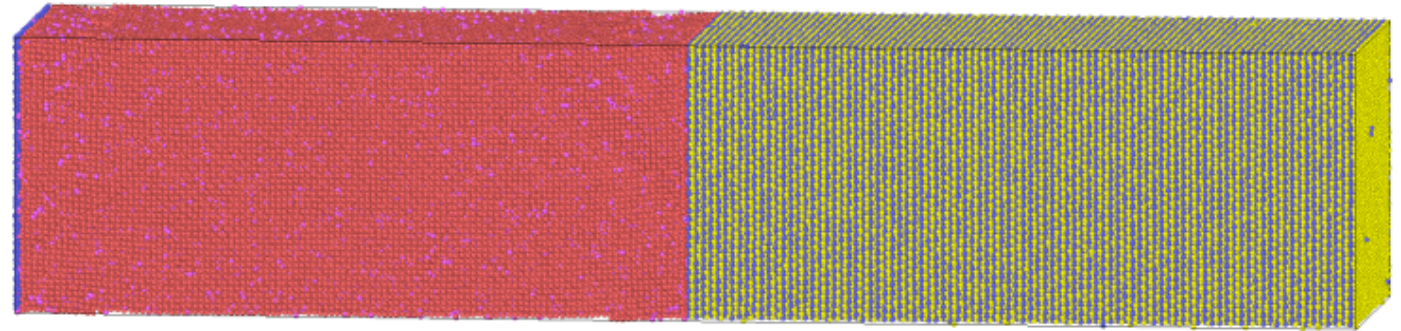
Candidate 985



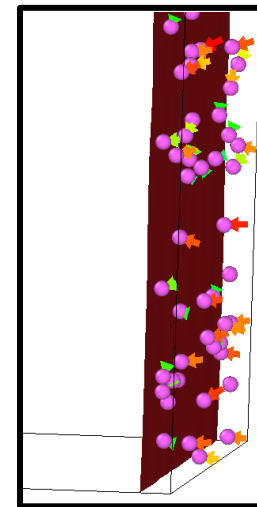
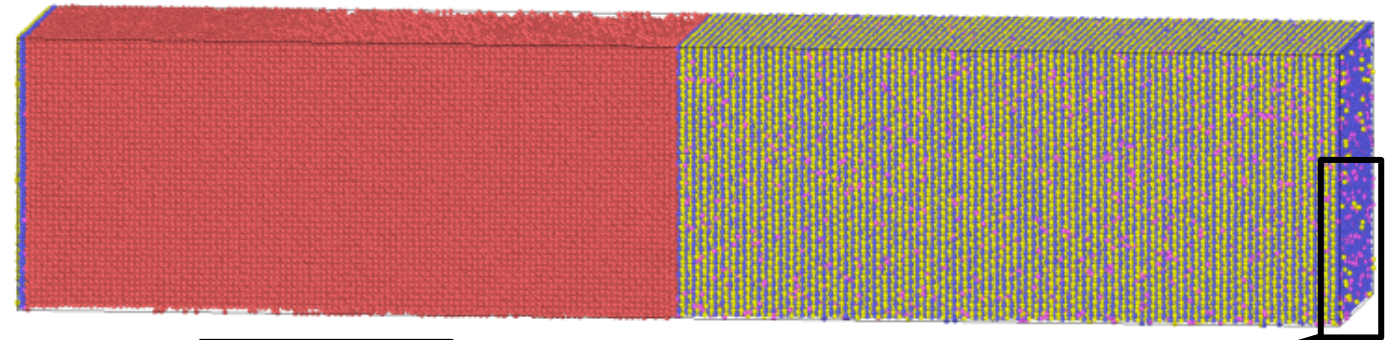
# W-ZrC-H (SNAP candidate 1012) is stable at 1000 K.



400 **ps**  
in MD



200 **ps**  
in MD



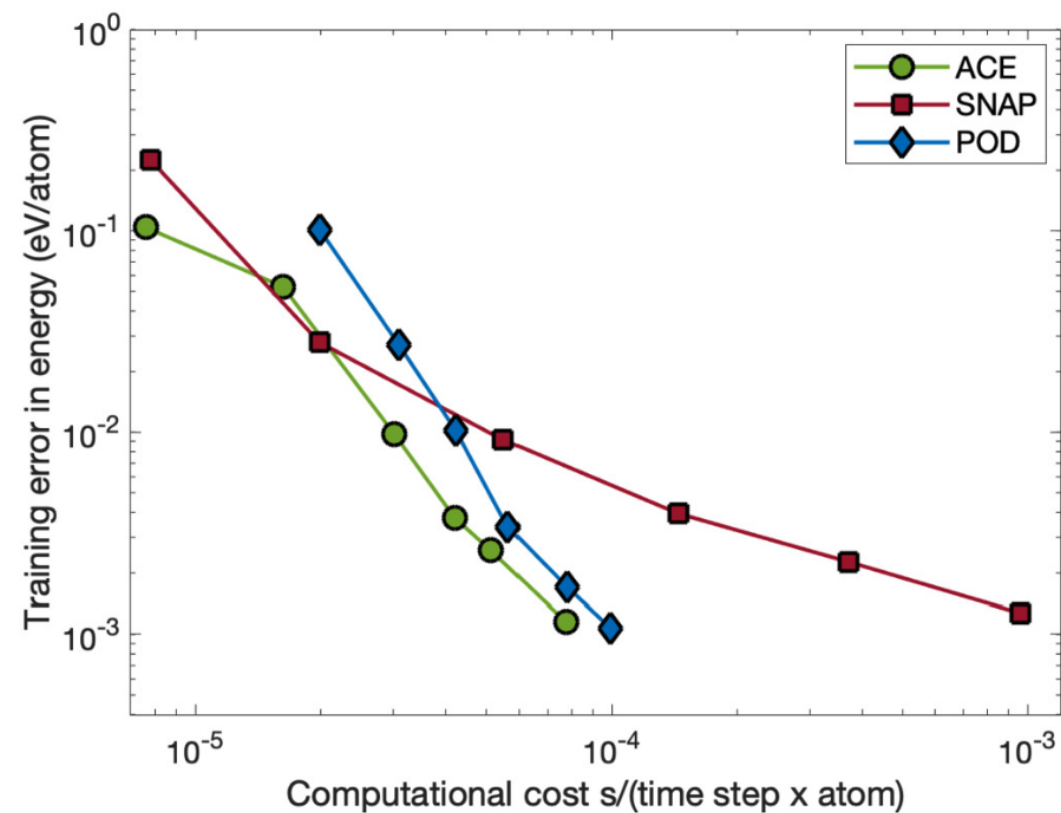
→ Check NEB in DFT compared to SNAP.



# Remaining Machine-Learned Potential Questions/Next Steps



- Can we combine objective function optimization with other MLP forms (ACE, Neural Networks, POD, etc.)? Will these yield lower force, energy, and objective function errors?
- Can we use active learning alongside objective functions?
- What is the best way to capture rare events?  
Can we train on NEB calculations?



Nguyen and Rohskopf / J. Comput. Phys. **480** (2023)

# Summary



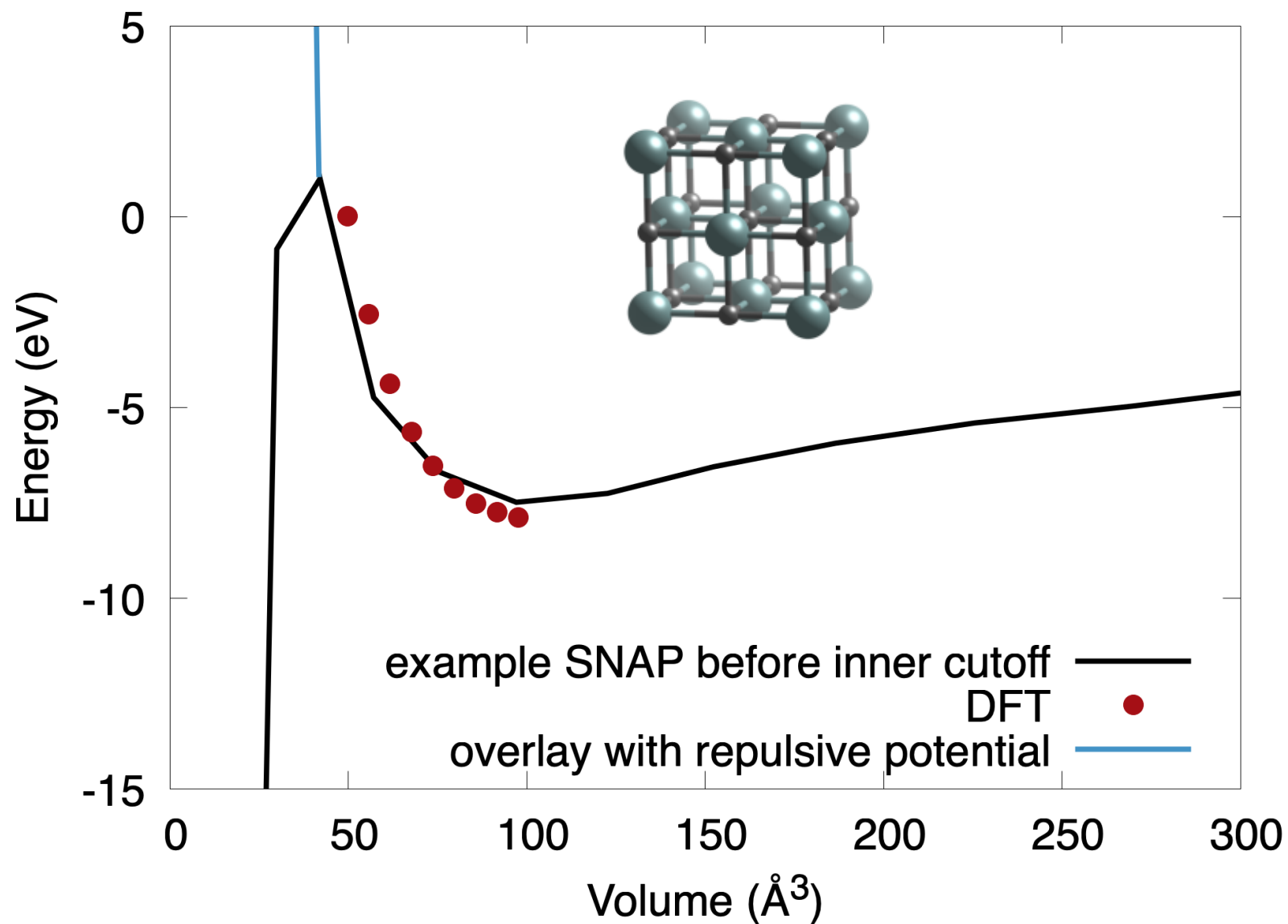
- We developed a W-ZrC SNAP potential that agrees well with DFT and can run millions of atom MD simulations at high temperature.
- Robust training sets include “domain expertise” and “beyond domain expertise” structures.
  - → cover large regions of descriptor space with USPEX and large AIMD simulations
- Low force and energy errors alone do not ensure good potentials.
- W-C bonds correlate to high tensile strength, though at high temperature much of the C in terminating layers diffuses into W.
- Preliminary W-ZrC-H potentials exhibit objective function tradeoffs but can run stable dynamics at 1000 K.



# Additional slides



# Inner cutoff is now live in FitSNAP and LAMMPS.

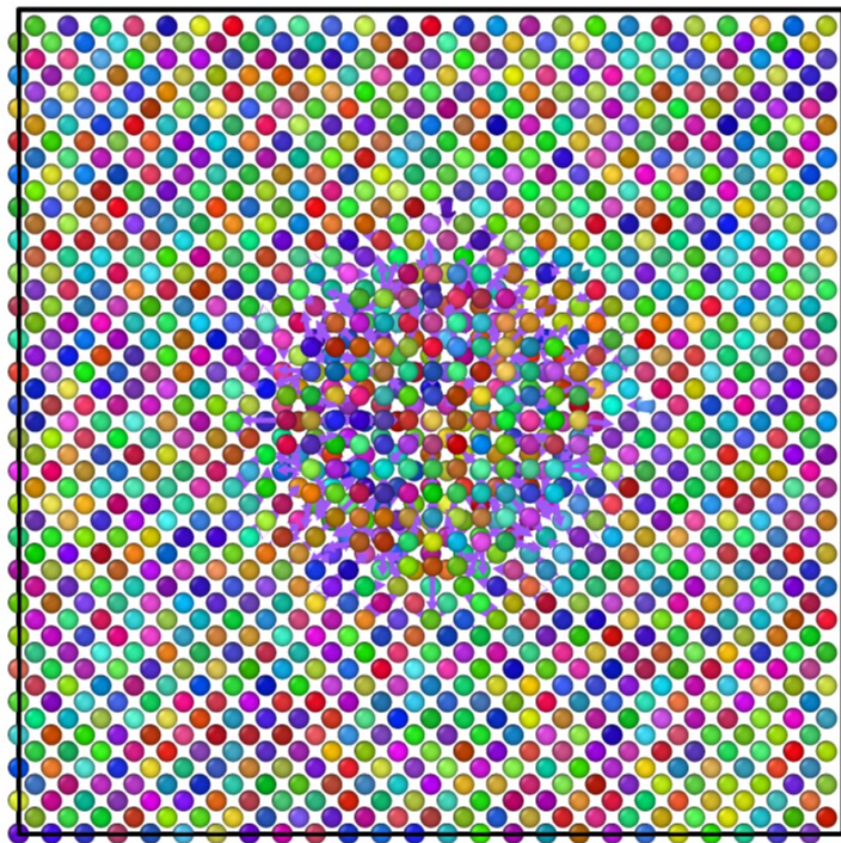




# Candidate potentials need to be checked in NVT/NPT simulations for stability.



“Laminating”

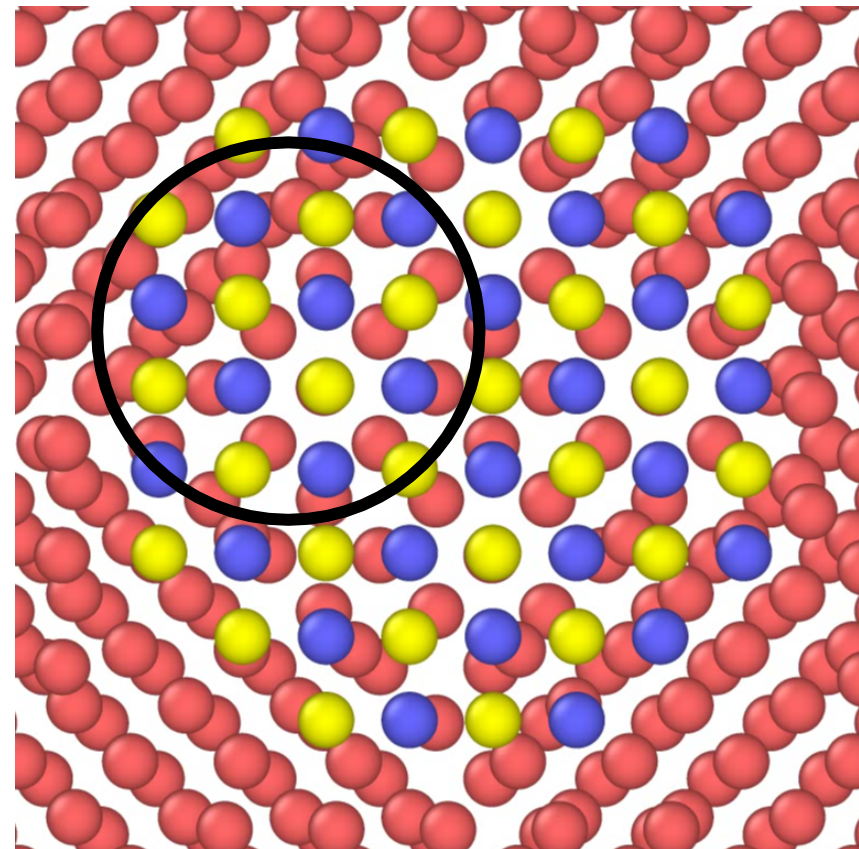


Cluster  
analysis  
<2.2 Å

$$\min(||\epsilon \cdot (D\beta - T)||^2)$$

- Increase group weight for forces on surface training data

“Black holing”



- Add training with low interatomic distances
- Tune zbl overlay
  - Increase repulsive diameter
  - Decrease radial cutoff



# Why do we separate DFT training into different groups?



## Training groups in the W-ZrC potential:

- (“traditional”) DFT
- Surfaces and Interfaces
- AIMD – 300K
- AIMD 1000 - 5000K
- MACtive
- Liquid
- USPEX

## “Traditional” DFT

- Unit cells – small supercells (3-64 atoms)
- High cutoff energy (~500 eV)
- Really high k-points (~8x8x8)

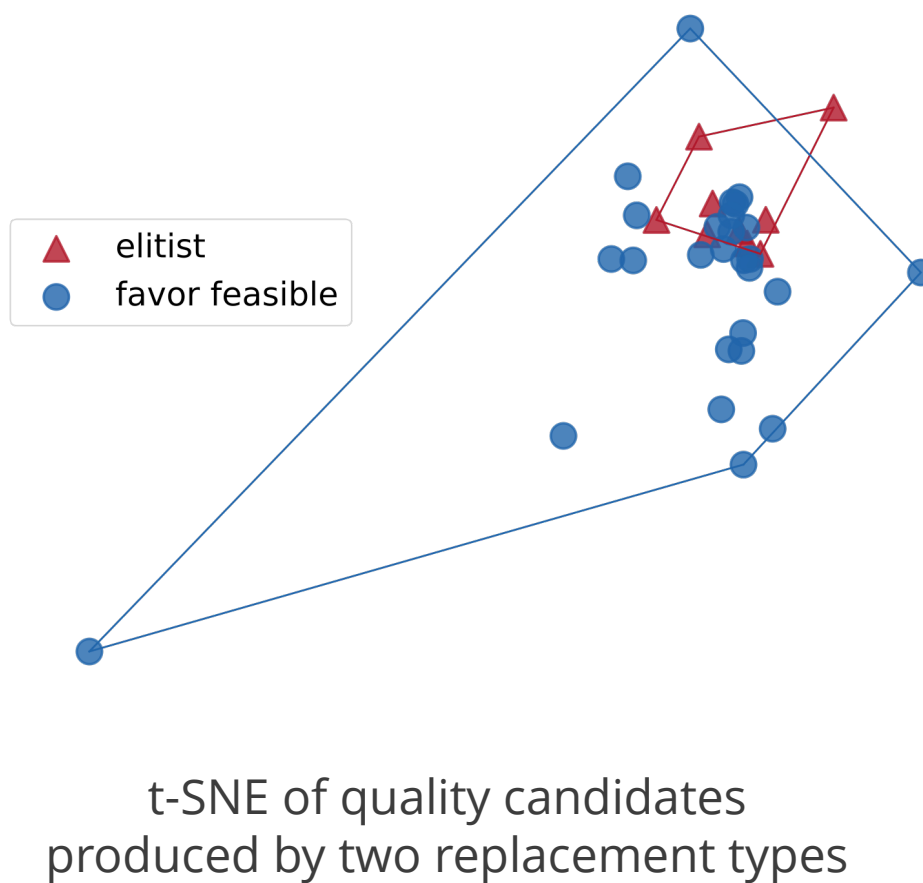
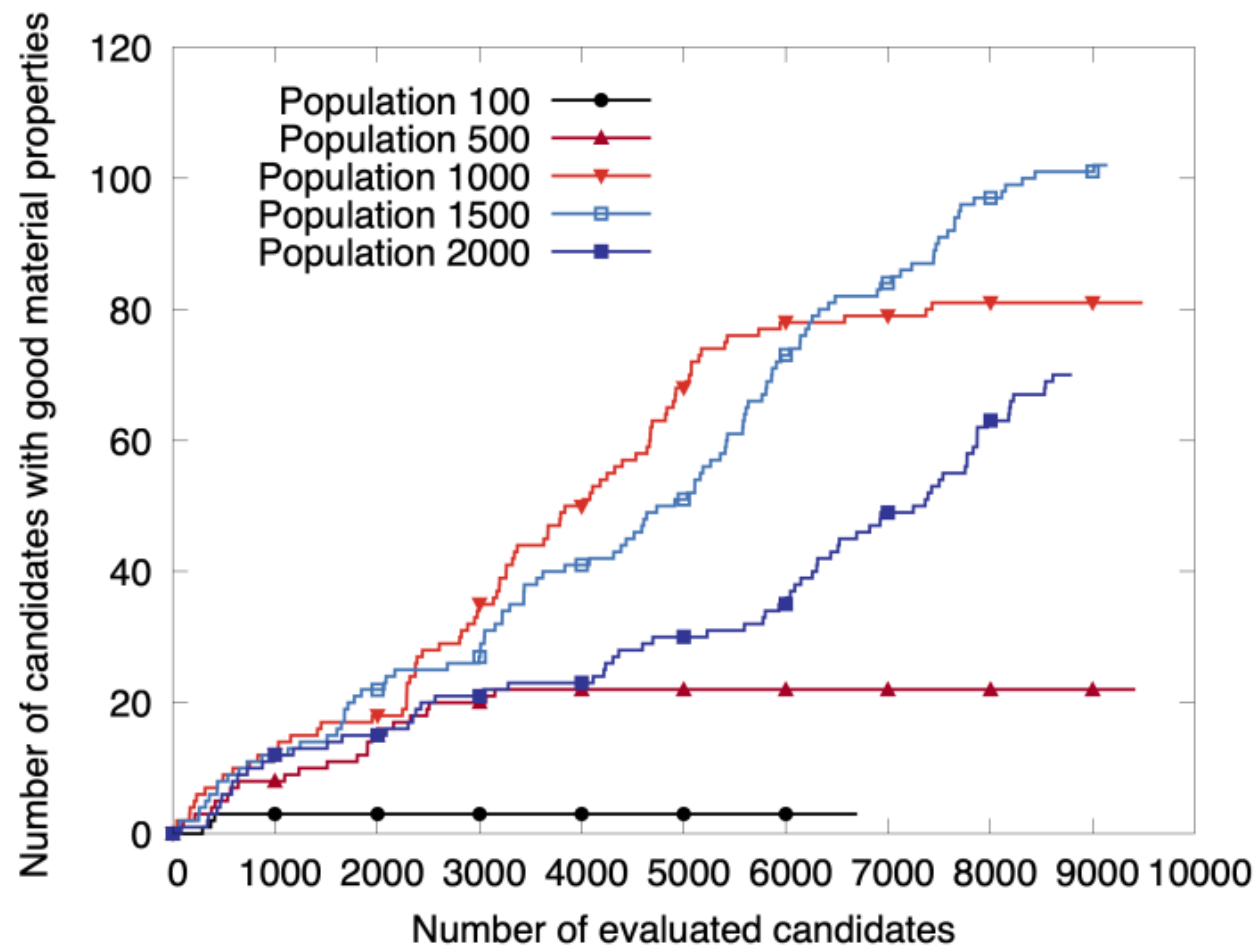
## Ab initio Molecular Dynamics (AIMD)

- Supercells (100-700 atoms)
- Really high cutoff energy (~500 - 750 eV)
- Sampled at gamma point (1x1x1)

## Group weights of final potential:

<u>dft E</u>	<u>dft F</u>	<u>uspex E</u>	<u>uspex F</u>	<u>surf E</u>	<u>surf F</u>	<u>aimd1 E</u>	<u>aimd1 F</u>	<u>aimd2 E</u>	<u>aimd2 F</u>	<u>mactive E</u>	<u>mactive F</u>	<u>liquid E</u>	<u>liquid F</u>
7.32	3.94	6.41	3.94	3.36	6.52	3.5	3.74	4.1	7.94	3.3	3.62	3.68	5.36

# Highlights of Dakota optimization



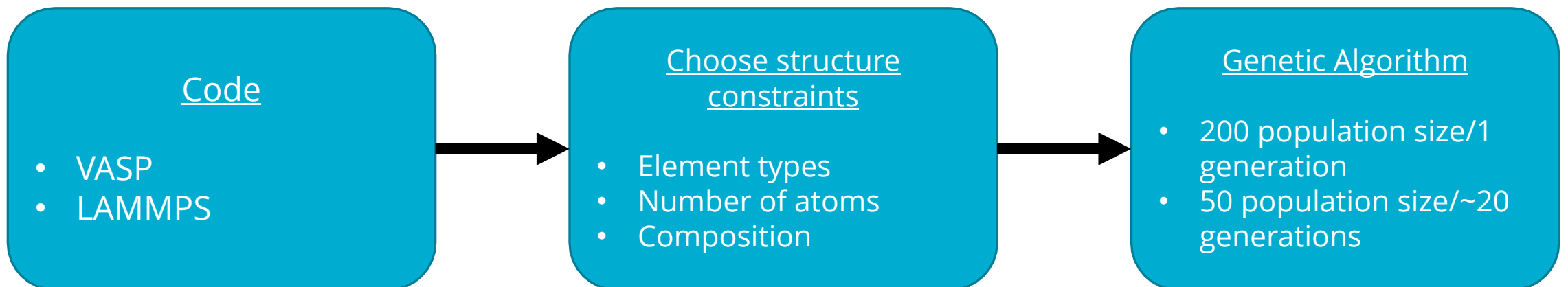
# USPEX – genetic algorithm structure predictor



“USPEX allows to predict crystal structure with arbitrary P-T conditions by knowing only chemical composition of the material.”

- USPEX generates trial structures which are then relaxed and evaluated by an external code interfaced with USPEX
- Based on the ranking of the relaxed structures, USPEX generates new structures, which are again relaxed and ranked

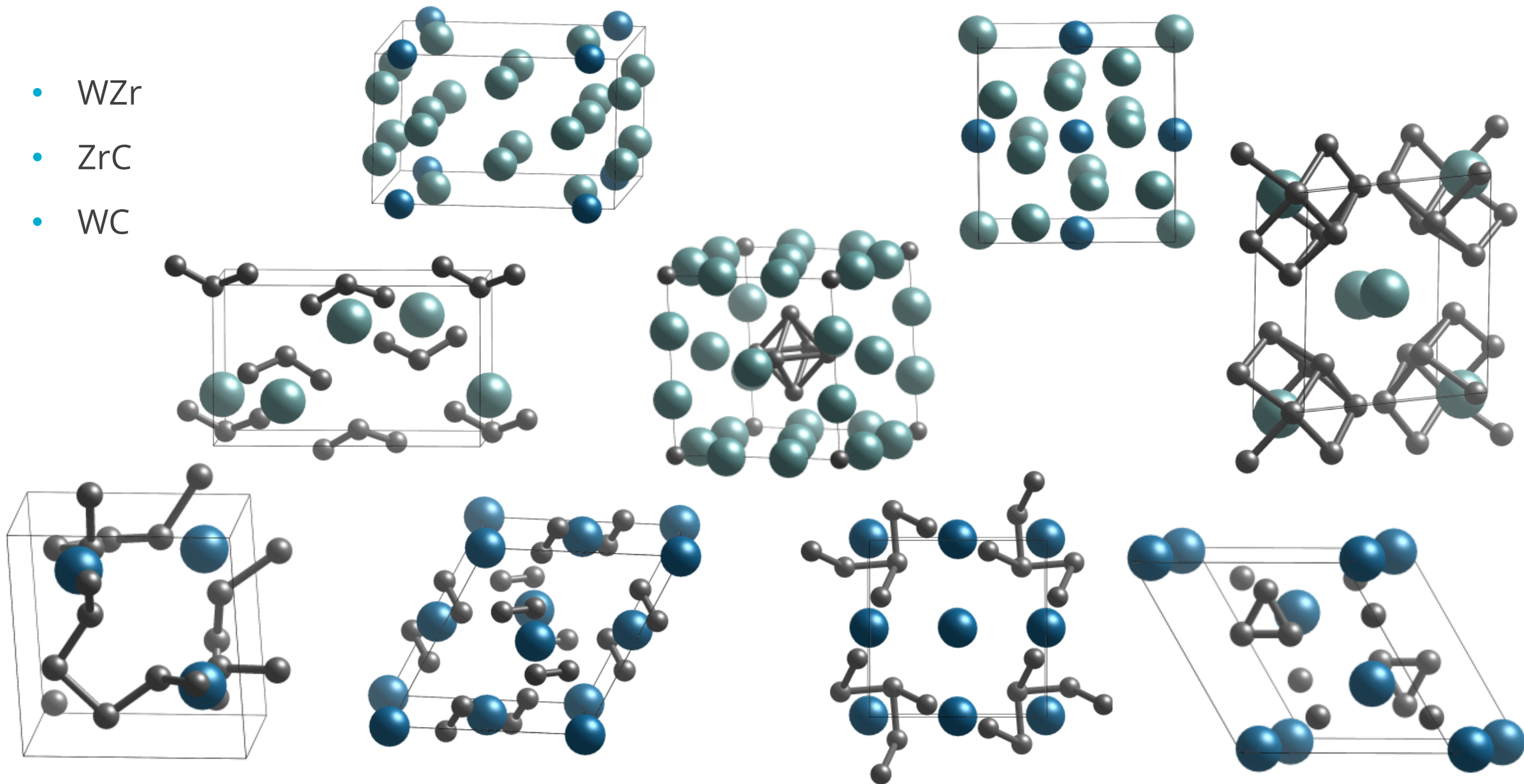
1. Create training data (bypass intended use; generate 1 giant first generation)
2. Test SNAP candidates/produce active training (follows intended use)



# USPEX (method 1) - composition sweeps for training (about 200 structures each)



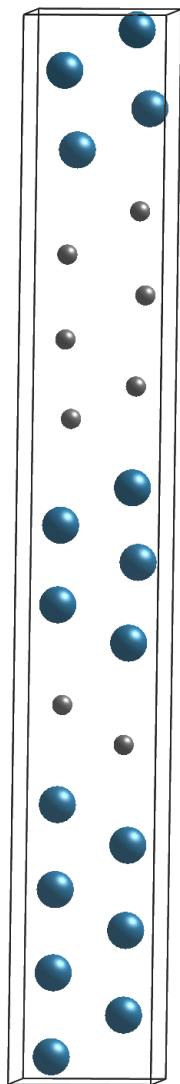
- WZr
- ZrC
- WC



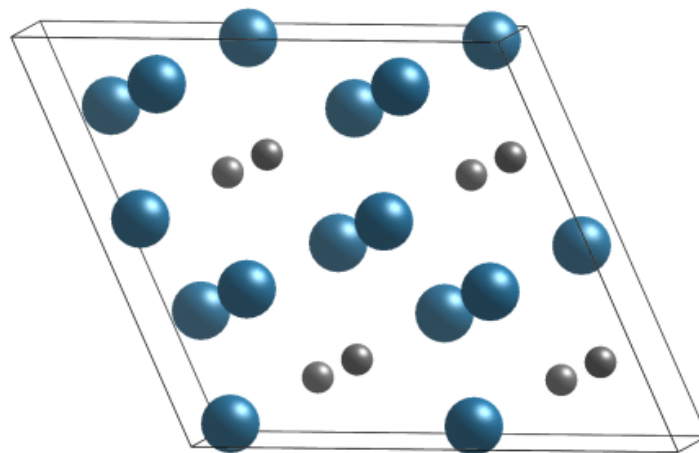
# USPEX (method 2)– Testing SNAP candidates on $W_2C$



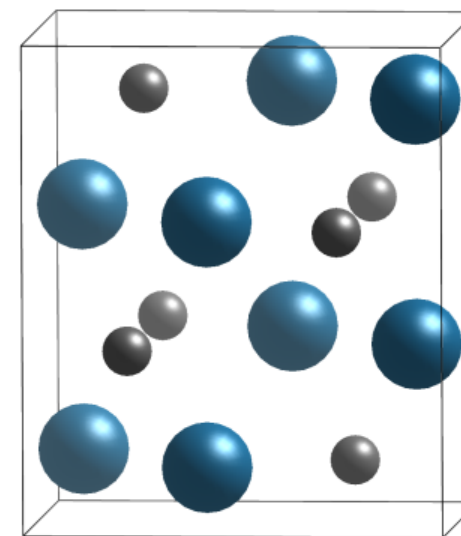
SNAP - **without** USPEX training



SNAP - **with** USPEX training



Materials Project



Most stable structure



# "Active" USPEX (method 2) – Using a SNAP candidate to produce training

