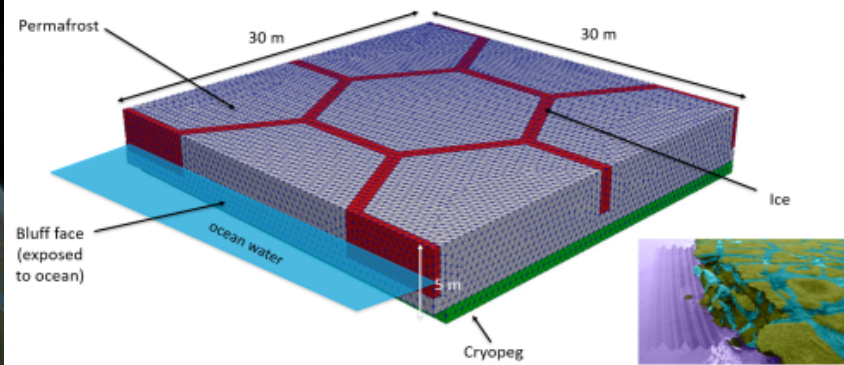
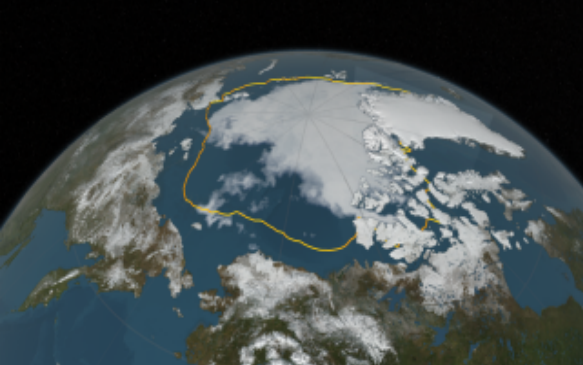




*Exceptional service in the national interest*



# Development of the Arctic Coastal Erosion Model with a Demonstration at Drew Point, AK

**Jennifer M. Frederick**<sup>1</sup>, Diana Bull<sup>1</sup>, Alejandro Mota<sup>1</sup>, Irina K. Tezaur<sup>1</sup>, Benjamin Jones<sup>2</sup>, Emily Bristol<sup>3</sup>, Robert C. Choens<sup>1</sup>, Chris Flanary<sup>4</sup>, Craig Jones<sup>4</sup>, and Melissa Ward Jones<sup>2</sup>

- 1 Sandia National Laboratories, U.S.
- 2 University of Alaska, Fairbanks, U.S.
- 3 University of Texas at Austin, U.S.
- 4 Integral Consulting, Inc., U.S.



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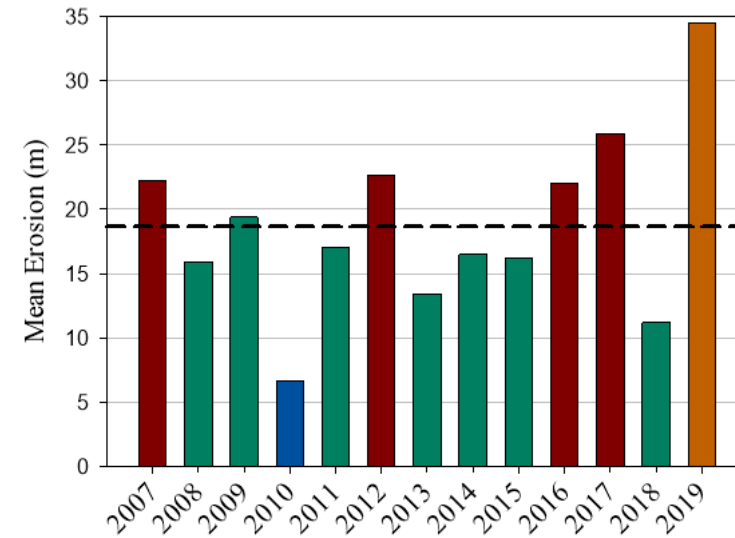
# Motivation

The Arctic is warming at **4 times** the rate of the global average resulting in **accelerated rates of coastal erosion!**

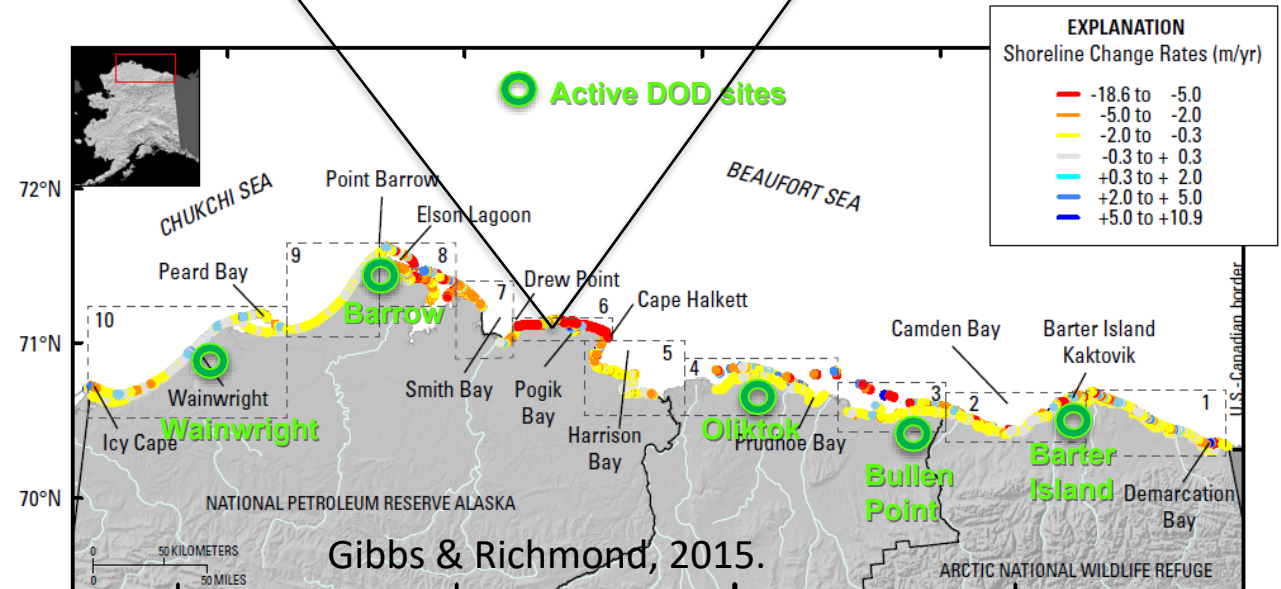
- Primary culprit is **loss of Arctic sea ice**: since 1979 sea ice has lost 51% in area and 75% in volume
  - Increasing **ice-free season**
  - Increasing **wave energy** and **storm surge**
  - Increasing **sea water** temperatures

## *Erosion is threatening:*

- **Coastal communities**: threatened with displacement
- **Coastal infrastructure**: active DoD sites, including toxic waste sites, in northern Alaska
- **Global carbon balance**: permafrost stores greenhouse gases ( $\text{CO}_2$ ,  $\text{CH}_4$ ,  $\text{NO}_2$ ).



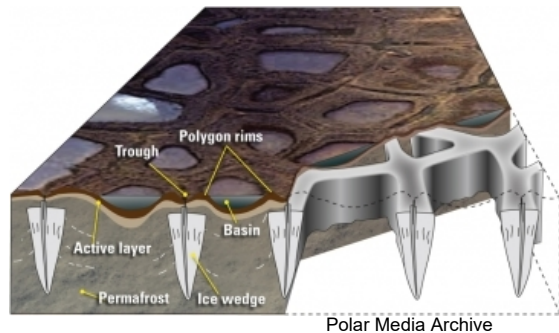
Certain  
locations lost  
>250 m  
b/w 2007-2019!



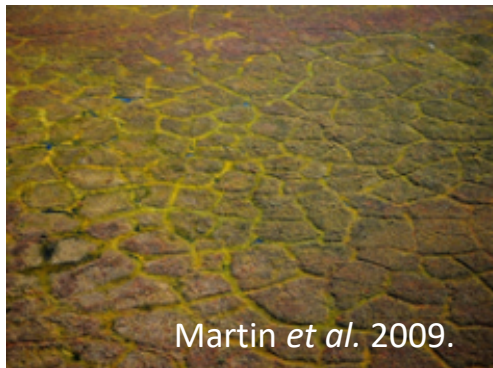
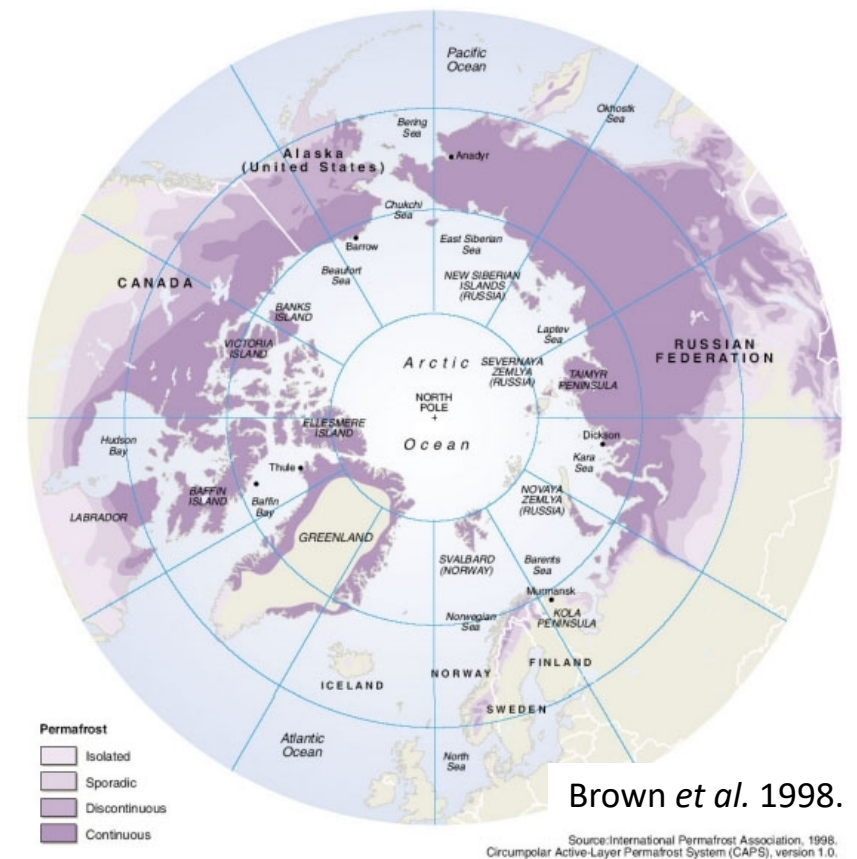
# Permafrost Thaw & Erosion

## *What is permafrost?*

- Ground that remains frozen for 2+ consecutive years.
- 24% of ice-free land area in Northern Hemisphere and 85% of Alaska, Greenland, Canada and Siberia contains permafrost.
- 34% of global coastline is permafrost.



*Left:* schematic illustrating formation of ice wedges and ice-wedge polygon landscapes. *Right:* map of permafrost distribution in Arctic



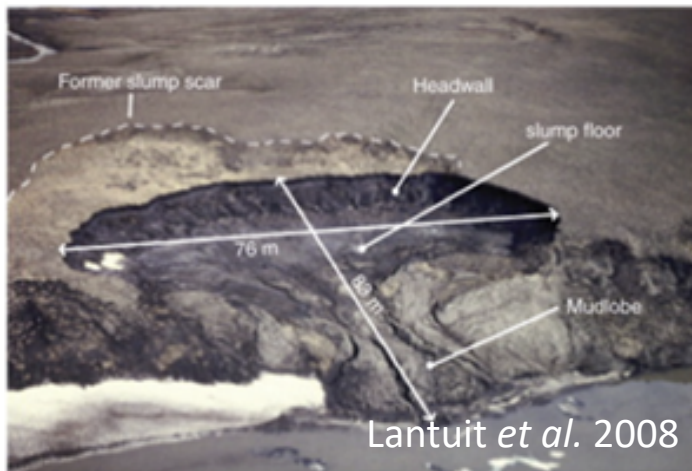
## *Unique coastal permafrost erosion process in Arctic:*

- Predominant geomorphology: **ice-wedge polygons**
  - Ice acts to **bind** unconsolidated soils in permafrost.
  - Ice wedges **grow/expand** up to 10s meters wide and deep.
  - Permafrost thaw can cause subsidence, slumping, **weakening**.



# Coastal Permafrost Failure Mechanisms

- **Retrogressive thaw slumping**: a slope failure characterized by thaw of exposed ground ice and slumping of thawed soil, typically caused by thermo-denudation<sup>1</sup>.
- **Active layer detachment**: failures are translational landslides that occur in summer in thawing soil overlying permafrost, typically caused by thermo-denudation<sup>1</sup>.
- **Block failure**: a niche (recess at bluff base) progresses landward until the overhanging material fails in a shearing or toppling mode known as block failure, caused by thermo-abrasion<sup>2</sup>.
  - Fallen blocks can disintegrate in the near-shore environment **within 1-2 weeks!**



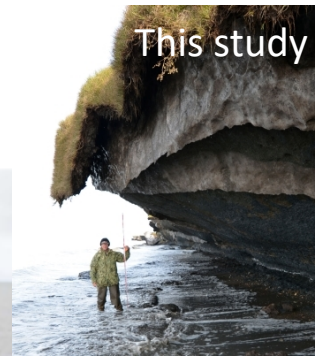
Retrogressive thaw slumping



Active layer detachment



Block failure

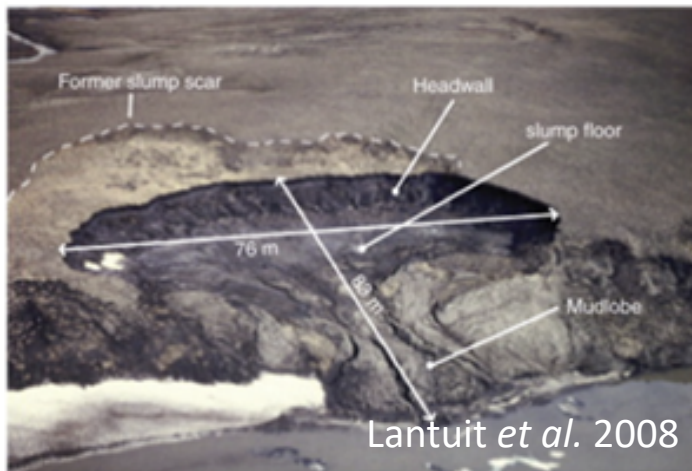


<sup>1</sup>Thawing of permafrost bluffs that proceeds under the influence of gravity. <sup>2</sup>Undercutting of permafrost bluff by warming ocean.

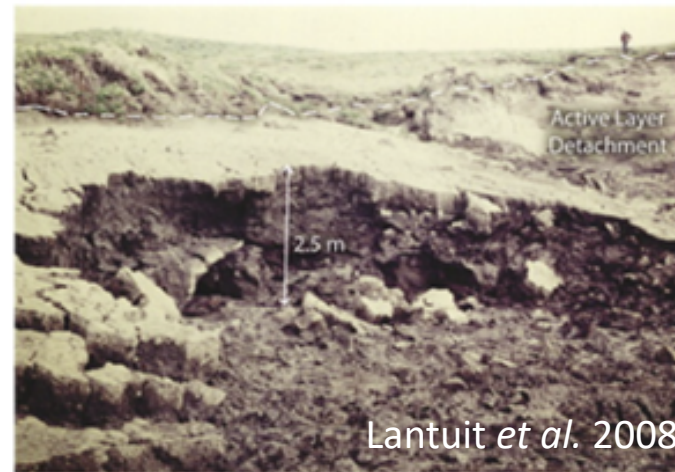


# Coastal Permafrost Failure Mechanisms

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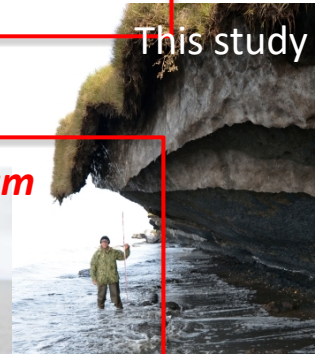
Retrogressive thaw slumping



Active layer detachment



Block failure



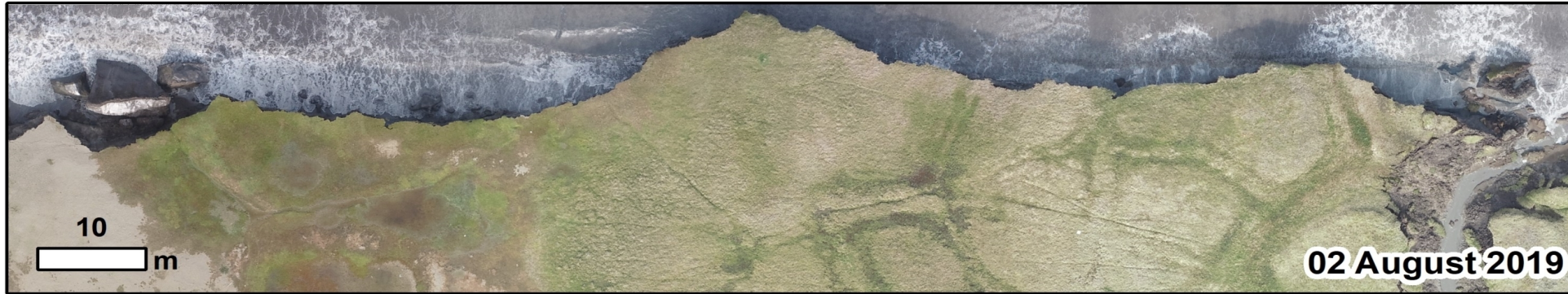
**Dominant failure mechanism  
in northern Alaska**

Ravens et al. 2012

<sup>1</sup>Thawing of permafrost bluffs that proceeds under the influence of gravity. <sup>2</sup>Undercutting of permafrost bluff by warming ocean.



# Example of Bluff Erosion During 2019 UAV Surveys\*



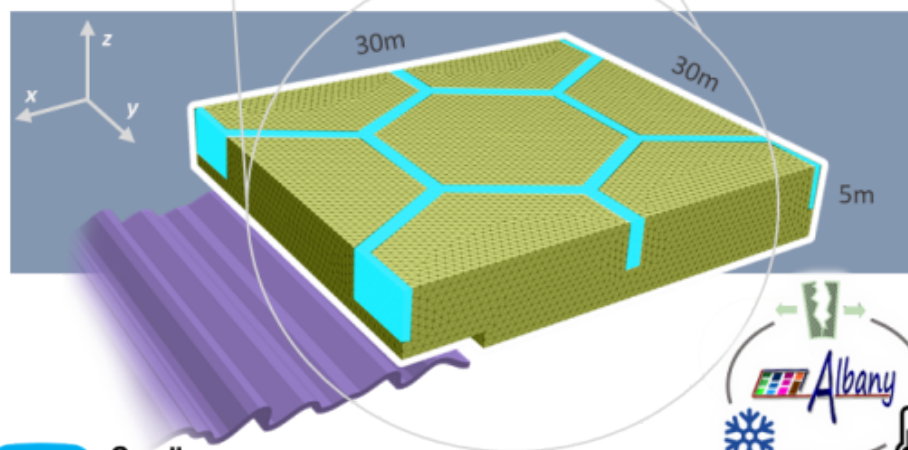
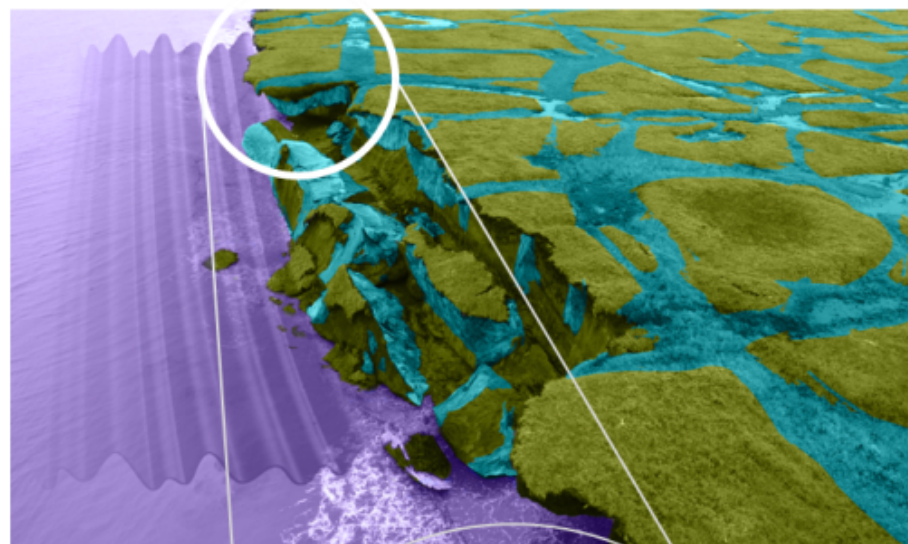
Fallen blocks can  
disintegrate in near-  
shore environment  
**within 1-2 weeks!**

\*Images courtesy of Ben  
Jones, UAF



# ARCTIC COASTAL EROSION (ACE) MODEL

 Ocean
  Ice wedge
  Permafrost
  Boundary Conditions



Sandia National Laboratories



integral

THE UNIVERSITY OF TEXAS AT AUSTIN



## LOCATION SPECIFIC DATA

### BOUNDARY CONDITIONS

Reanalysis (ASR & ERA) (*Historic*)  
 HYCOM (*Historic*)  
 SNAP Downscaled RCP 8.5 Earth System Models (*Projections*)



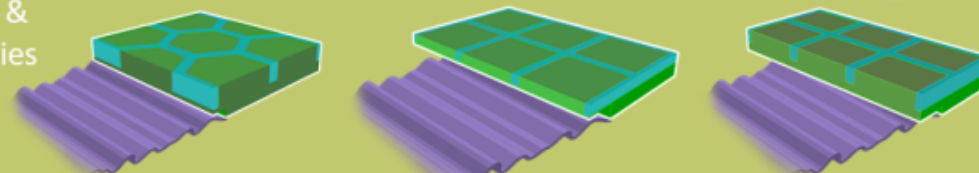
- WIND SPEED / DIRECTION
- ATMOSPHERIC TEMP
- PERMAFROST TEMP
- OCEAN ICE EXTENT
- OCEAN CURRENTS
- OCEAN TEMP

### TERRESTRIAL \ TERRESTRIAL

Albany: 3-D multi-physics based finite element model  
 MECHANICAL: finite deformation plasticity model  
 THERMAL: transient temperature and ice saturation evolution



Geomorphology & Material Properties



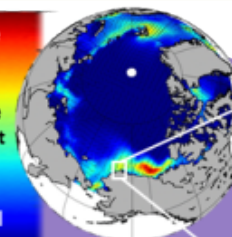
Strength Properties

MATERIAL: ice content determines strength



### OCEAN

Circum-Arctic: wave energy



Nearshore: coupled wave & circulation

Beaufort Sea

1955 Coastline

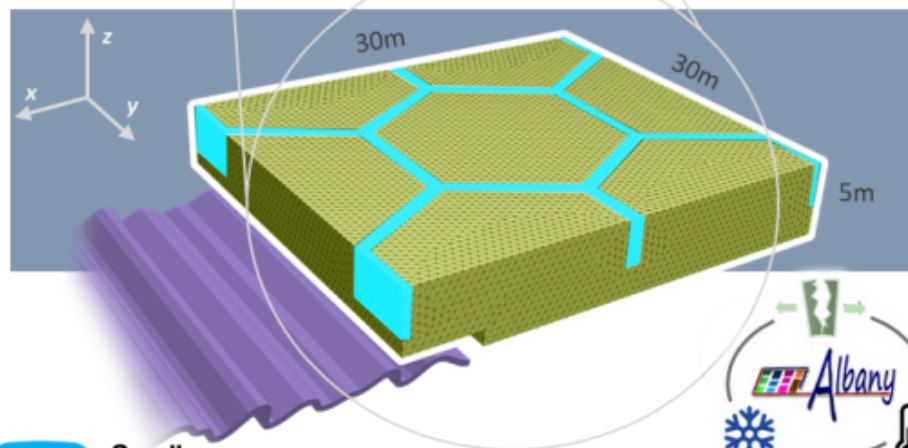
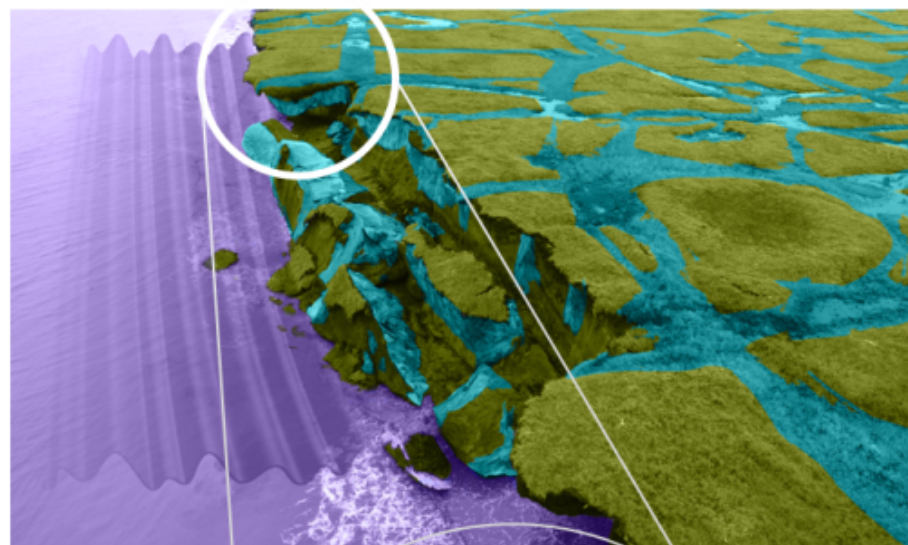
2018 Coastline

Colors distinguish terrain units



# ARCTIC COASTAL EROSION (ACE) MODEL

 Ocean
  Ice wedge
  Permafrost
  Boundary Conditions



Sandia National Laboratories



integral

THE UNIVERSITY OF TEXAS AT AUSTIN



## LOCATION SPECIFIC DATA

### BOUNDARY CONDITIONS

Reanalysis (ASR & ERA) (*Historic*)  
 HYCOM (*Historic*)  
 SNAP Downscaled RCP 8.5 Earth System Models (*Projections*)



- WIND SPEED / DIRECTION
- ATMOSPHERIC TEMP
- PERMAFROST TEMP
- OCEAN ICE EXTENT
- OCEAN CURRENTS
- OCEAN TEMP

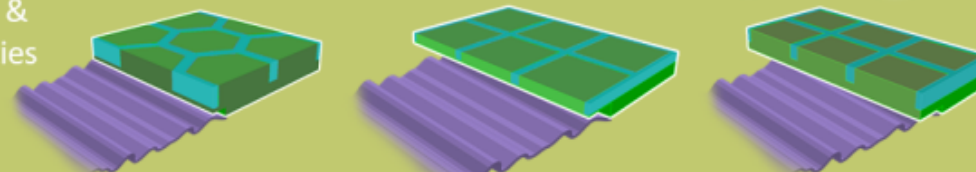
### TERRESTRIAL \ TERRESTRIAL

## This talk

Albany: 3-D multi-physics based finite element model  
 MECHANICAL: finite deformation plasticity model  
 THERMAL: transient temperature and ice saturation evolution



Geomorphology & Material Properties



Strength Properties

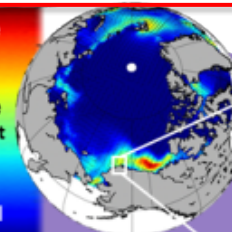
MATERIAL: ice content determines strength



### OCEAN

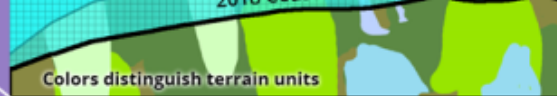
Circum-Arctic: wave energy

Large  
 Wave Height  
 Small



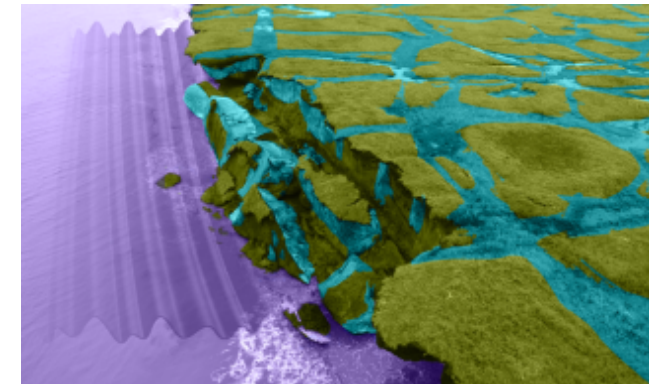
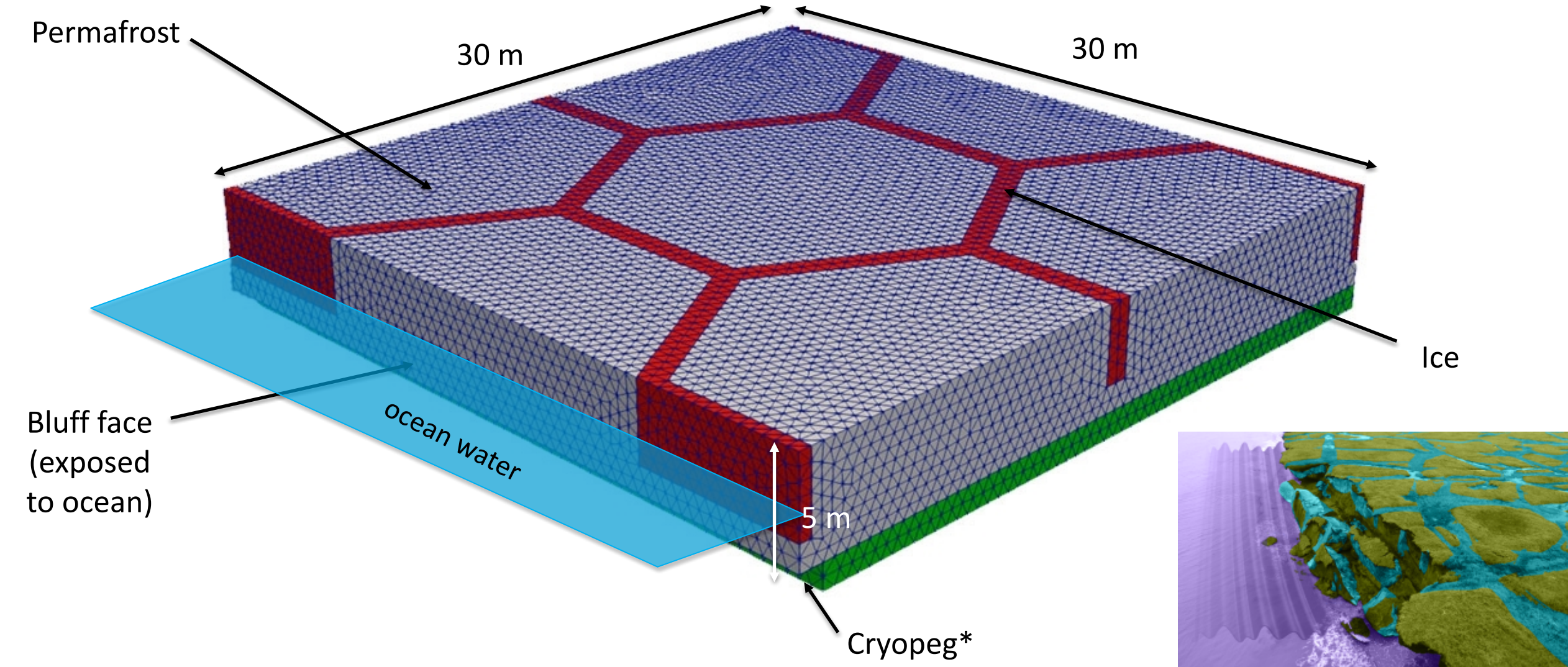
Nearshore:  
 coupled wave & circulation

Beaufort Sea  
 1955 Coastline  
 2018 Coastline





# Anatomy of a Canonical Computational Domain



\* Layer of unfrozen ground that is perennially cryotic (forming part of the permafrost) in which freezing is prevented.

# Finite Element Implementation Within Albany



The ***thermo-mechanical Arctic Coastal Erosion (ACE)*** model is implemented within the ***LCM project*** in Sandia's open-source parallel, C++, multi-physics, finite element code, ***Albany***.



<https://github.com/sandialabs/LCM>

- ***Component-based*** design for rapid development.
- Contains a wide variety of ***constitutive models***.
- Extensive use of libraries from the open-source ***Trilinos*** project.
  - Use of the ***Phalanx*** package to decompose complex problem into simpler problems with managed dependencies.
  - Use of the ***Sacado*** package for ***automatic differentiation***.
- All software available on ***GitHub***.



<https://github.com/trilinos/trilinos>



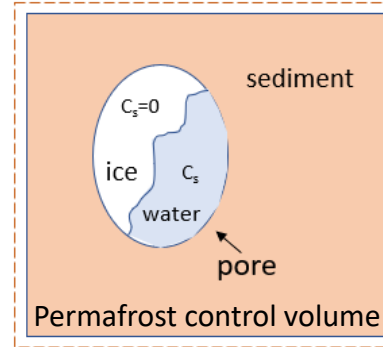
# Thermal Model

- **Transient heat conduction** in a non-homogeneous porous media with water-ice phase change:

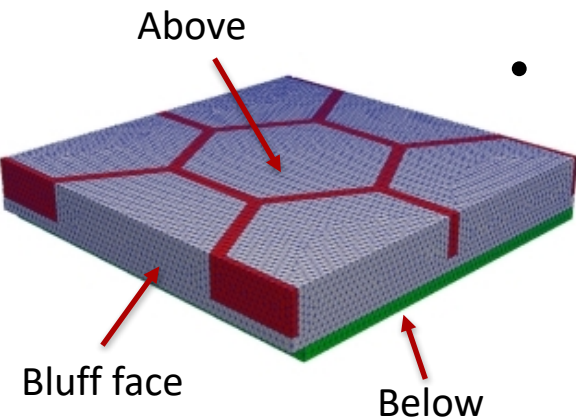
$$(\overline{\rho c_p} + \tilde{\Theta}) \frac{\partial T}{\partial t} = \nabla \cdot (\mathbf{K} \cdot \nabla T)$$

where  $\tilde{\Theta} := \rho_f L_f \frac{\partial f}{\partial T}$  incorporates phase changes through soil freezing curve,  $\frac{\partial f}{\partial T}$ .

- Computes **temperature**  $T$  and **ice saturation**  $f$

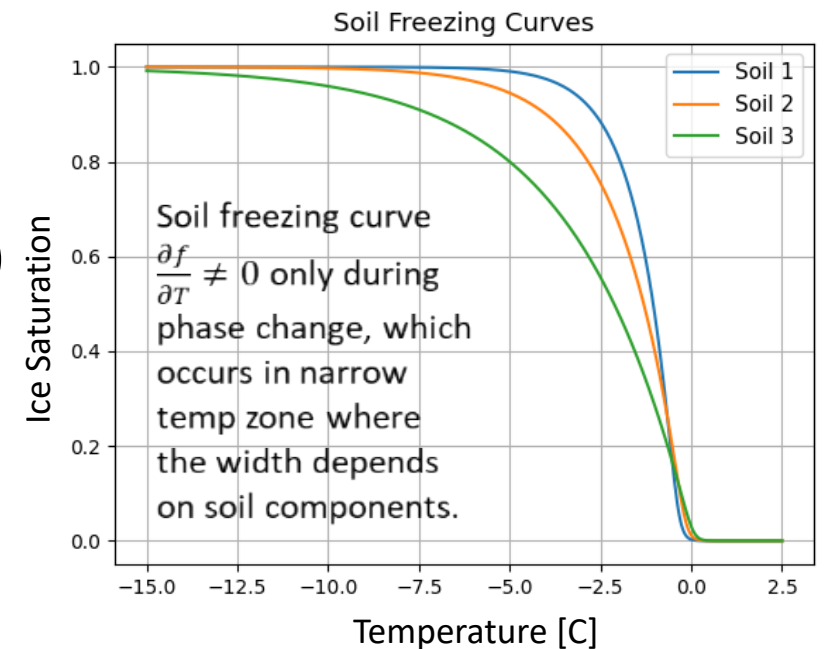


$\bar{\rho}$ : density from mixture model  
 $\bar{c_p}$ : specific heat from mixture model  
 $\mathbf{K}$ : thermal diffusivity tensor  
 $\rho_f$ : ice density  
 $L_f$ : latent heat of water-ice phase change  
 $f$ : ice saturation ( $\in [0,1]$ )  
 $\frac{\partial f}{\partial T}$ : soil freezing curve (depends on salinity)



- **Boundary conditions** (from wave model/data)

- Local geothermal heat flux from below
- Mean annual air temp\* from above
- Air/ocean temp at bluff face
- Ocean salinity at bluff face\*\*



\* Or, alternatively surface ground temperature (if available).

\*\* Used to modify melting temperature of ice.

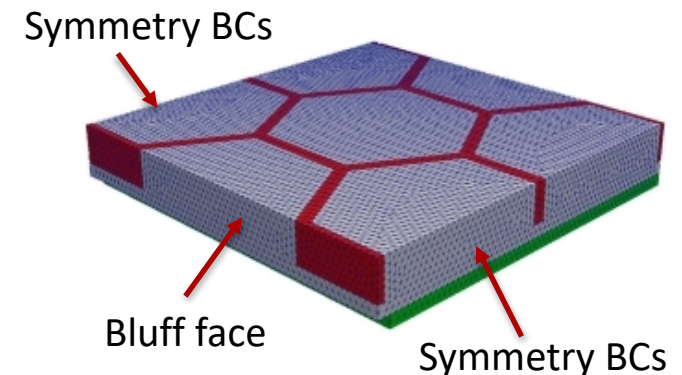
# Mechanical Model

- Finite deformation ***time-dependent*** variational formulation for ***solid mechanics problem*** obtained by minimizing the energy functional:

$$\Phi[\boldsymbol{\varphi}] := \int_{\Omega} A(\mathbf{F}, \mathbf{Z}) dV - \int_{\Omega} \rho \mathbf{B} \cdot \boldsymbol{\varphi} dV - \int_{\partial_T \Omega} \mathbf{T} \cdot \boldsymbol{\varphi} dS$$

$A(\mathbf{F}, \mathbf{Z})$ : Helmholtz free-energy density  
 $\mathbf{Z}$ : material variables  
 $\mathbf{F}$ : deformation gradient ( $\nabla \boldsymbol{\varphi}$ )  
 $\rho$ : density  
 $\mathbf{B}$ : body force  
 $\mathbf{T}$ : prescribed traction

- Computes ***displacements*** and ***new computational geometry*** (following erosion)
- ***J<sub>2</sub> plasticity*** extended to large-deformation regime ***constitutive model*** for ***ice*** and ***permafrost***
  - Incorporates all mechanisms that lead to deformation, plastic flow and creep of polycrystalline materials like ice; minimal calibration parameters; simplest material model w/ plastic behavior.
- ***Boundary conditions:***
  - ***Symmetry BCs*** on lateral sides
  - ***Wave pressure Neumann BC*** on bluff face\* (from wave model).
  - ***Damage variable*** on bluff face in contact with ocean (introduces softening due to dissolution)

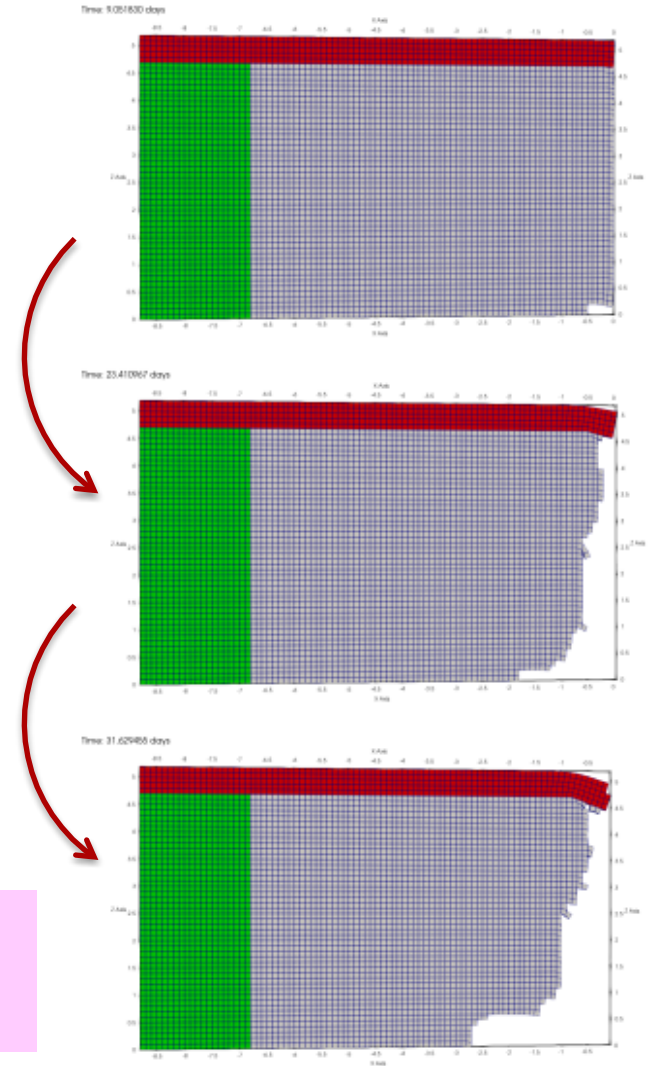
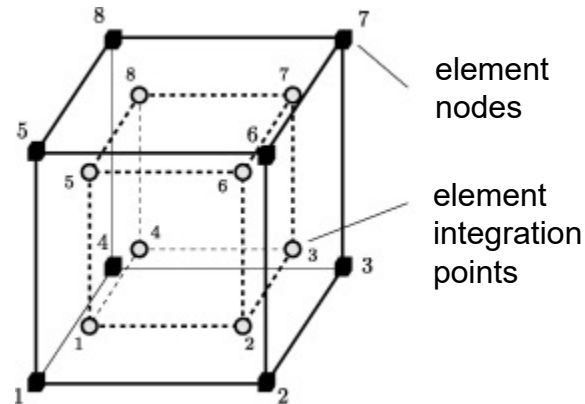


\* Holthuijsen 2007.



# Erosion Failure Criteria

- **Stress criteria**: when material reaches a critical value of the stress in tension or compression.
- **Strain criterion**: when material reaches a critical strain limit defined as a function of peat content (distortion).
- **Kinematic criteria**: when material has tilted excessively, or exceeded a maximum physical displacement, it is assumed to have fallen as part of block erosion.



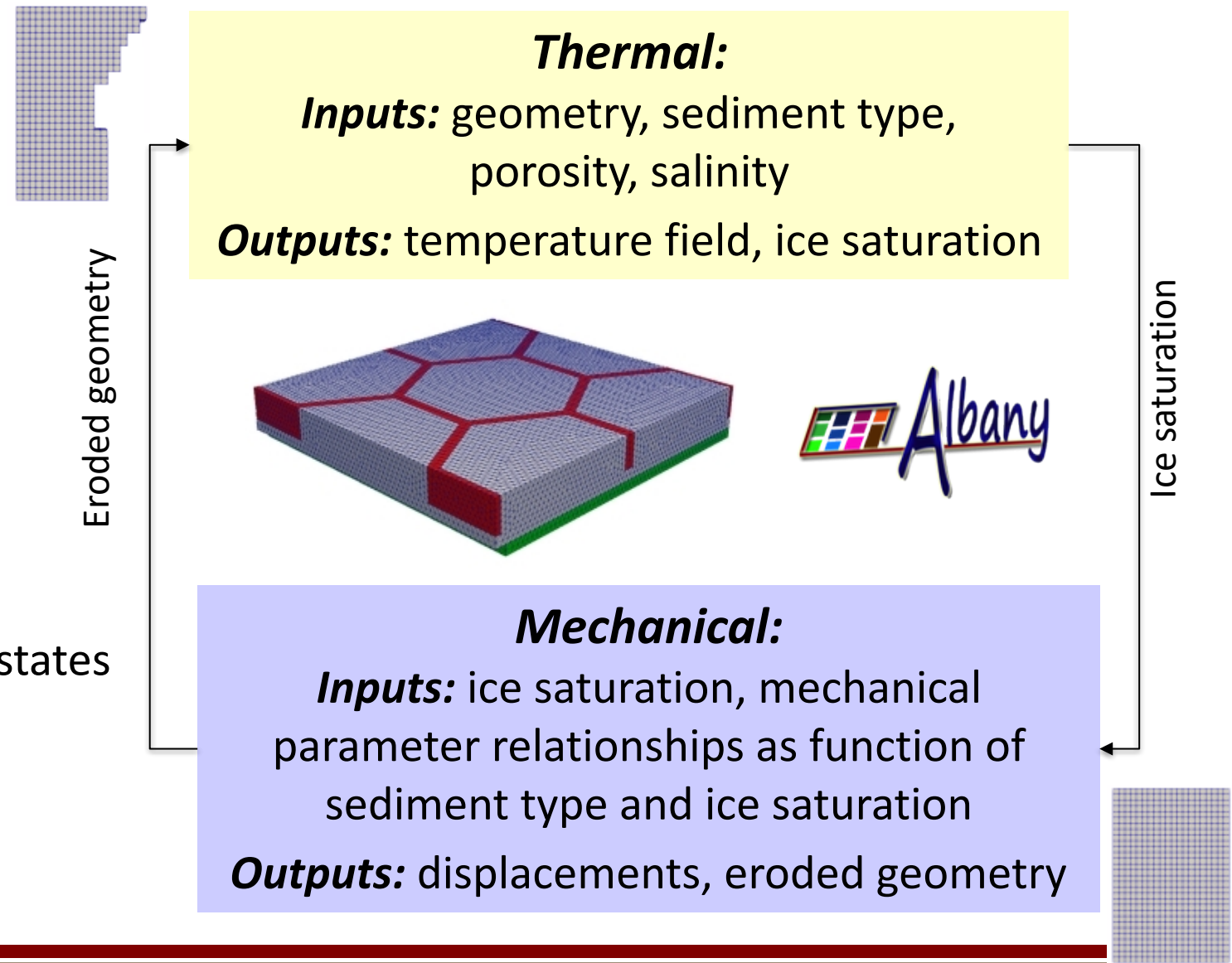
When any of the **failure criteria** are reached for all integration points within an element, “failed” elements are **removed** from mesh.

# Coupled Thermo-Mechanical Formulation

## *Potential key advantages:*

- Failure modes develop from **constitutive relationships** in FEM model (no empirical relationships!)
- 3D unsteady heat flow can include **chemistry**
- Thermal and mechanical problems can be advanced using **different time-steppers** (e.g., implicit-explicit coupling)
- **Tightly coupled** mechanical + thermal states

***Unique characteristic of coupled model:*** coupling happens at the level of material model

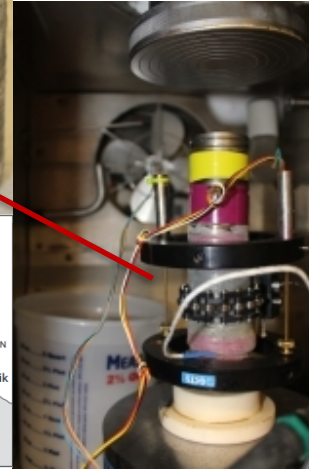
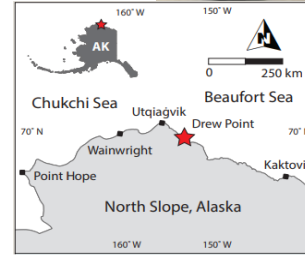




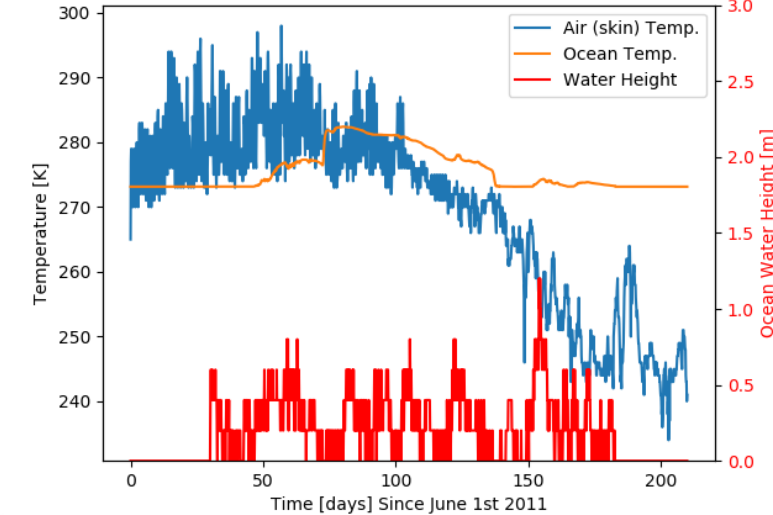
# Parameters & Inputs

## Parameters estimated from core lab experiments:

- Elastic modulus, Poisson's ratio, yield strength
- Sand/silt/clay/peat fractions with depth
- Porosity with depth
- Salinity with depth



BC Data for Drew Point



## Parameters from literature:

- Ice/water/sediment densities, thermal conductivities, heat capacities
- Freezing curve/width as function of sediment type

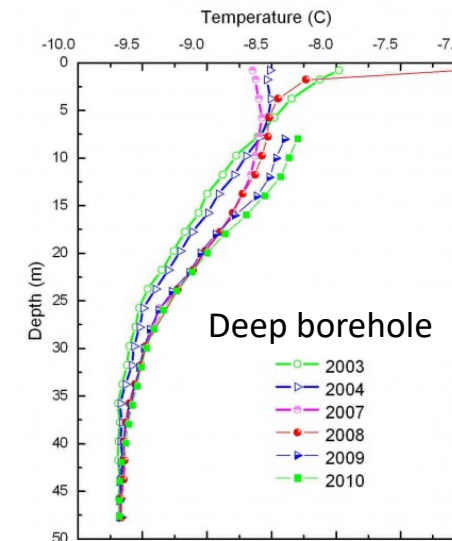
## Parameters estimated from observational data at Drew Point, AK:

- Air temp w/ time, initial bluff temp (USGS weather station data)
- Geothermal heat flux (borehole at Barrow, AK)
- Polygon dimension, ice wedge thickness and depth, bluff height, organic layer (peat) thickness (Aug. 2019 field campaign)

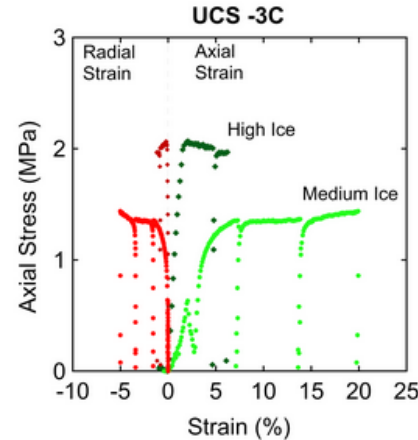
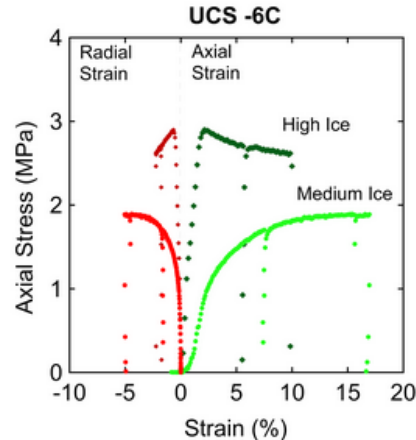
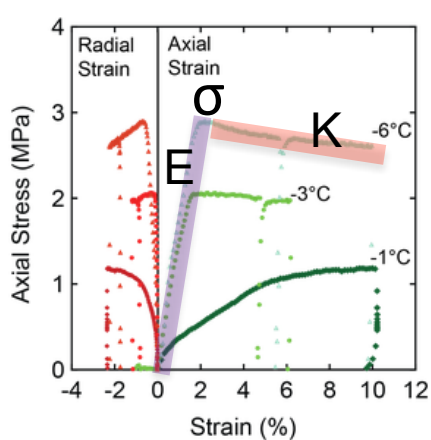
## Parameters from wave model (WW3+SWAN+Delft3D):

- Ocean temperature, salinity and sea-level w/ time (for thermal and wave pressure mechanical BCs)

integral  
consulting inc.



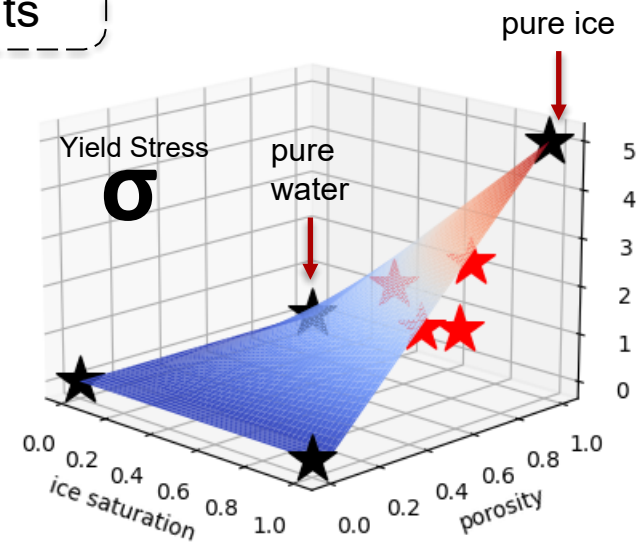
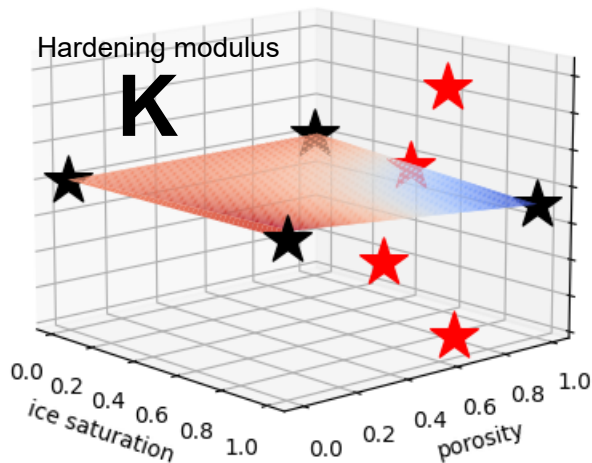
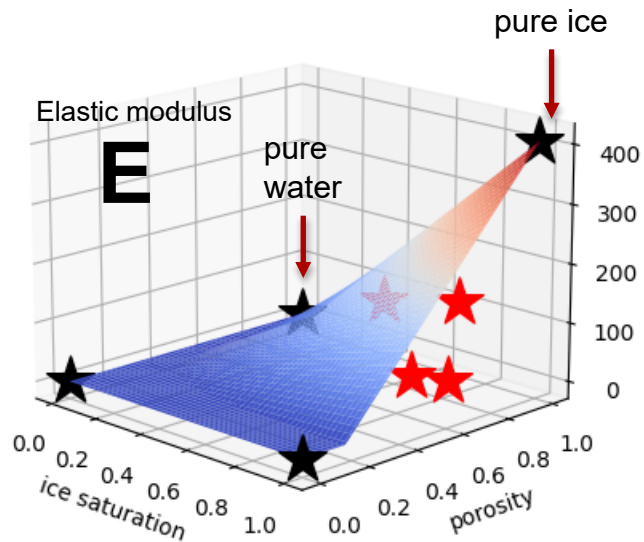
# Material Model Calibration to Experimental Data



Experimental results on permafrost core samples were analyzed to create fits for  $E$ ,  $K$ ,  $\sigma$  as a function of **ice saturation** and **porosity**.

★ experimental data points

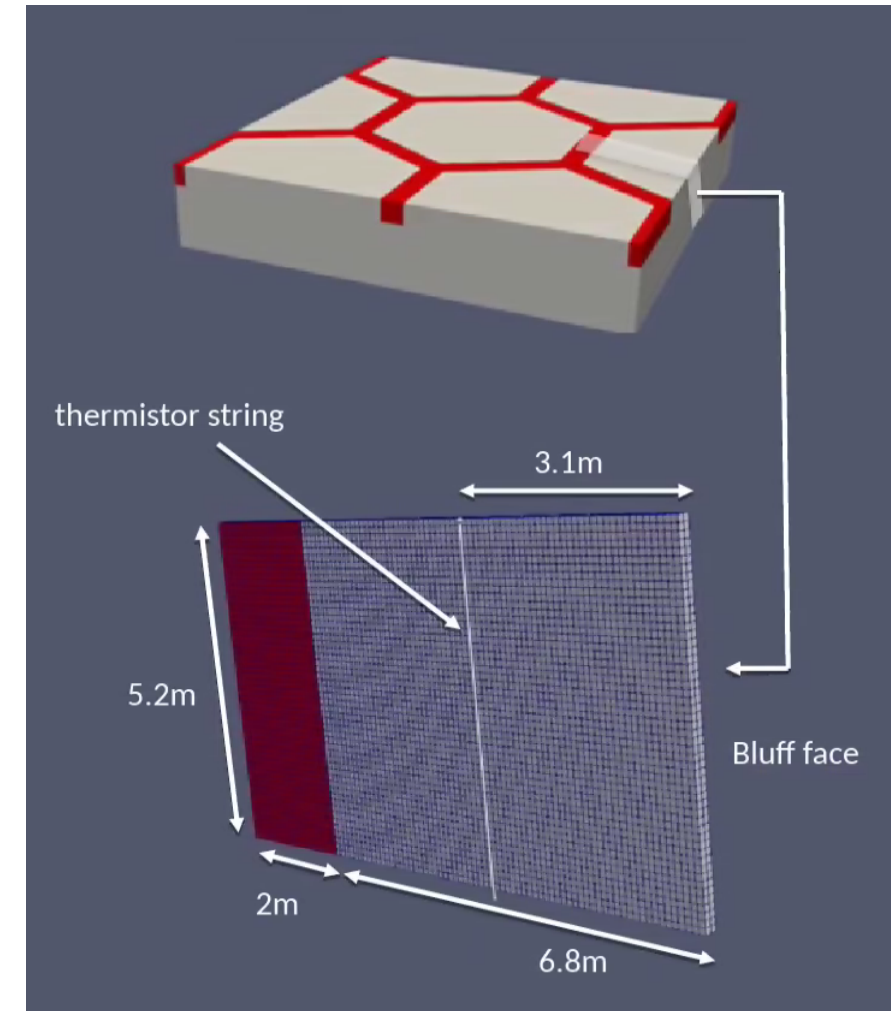
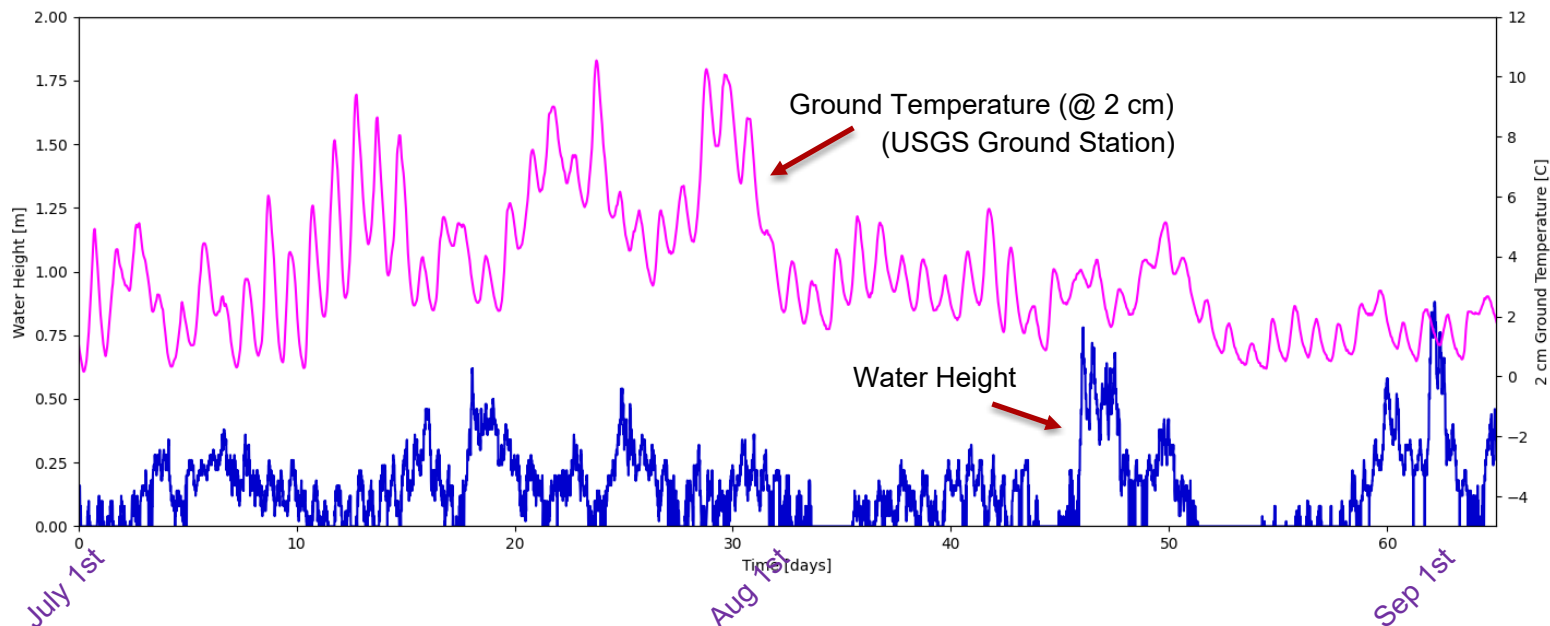
★ theoretical data points





# Thermo-Mechanical Coupling: 2.5D slice\*

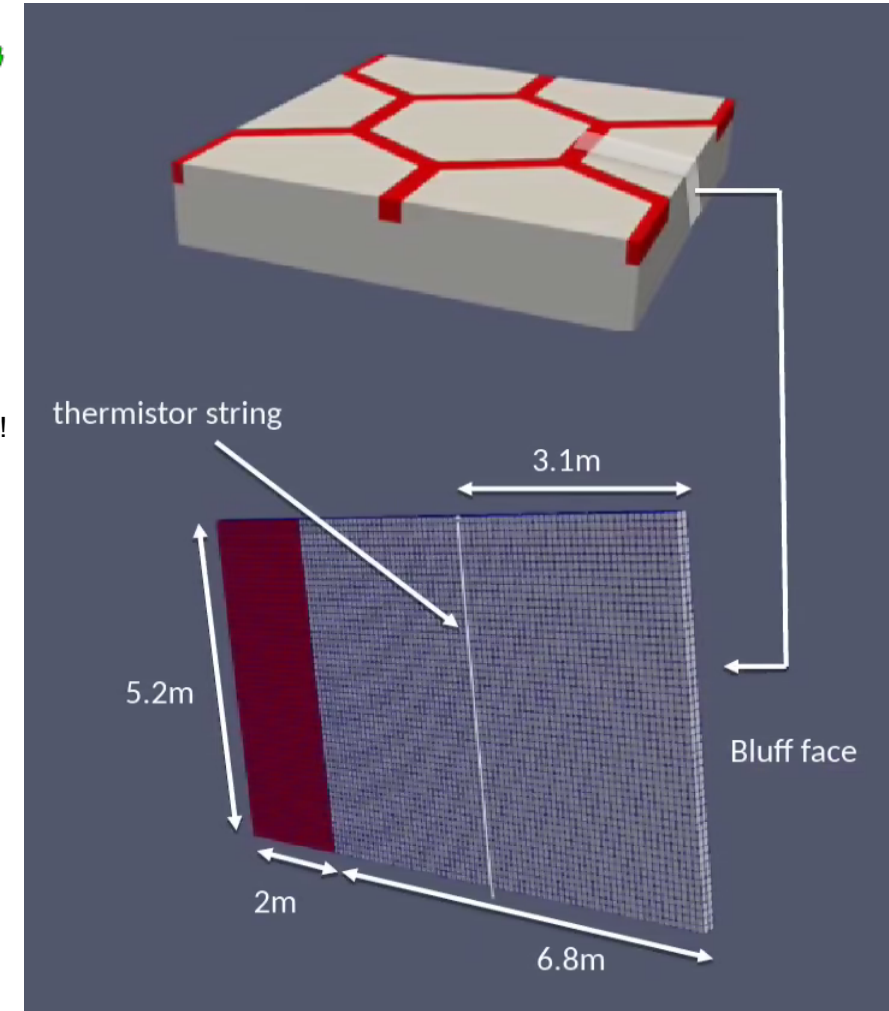
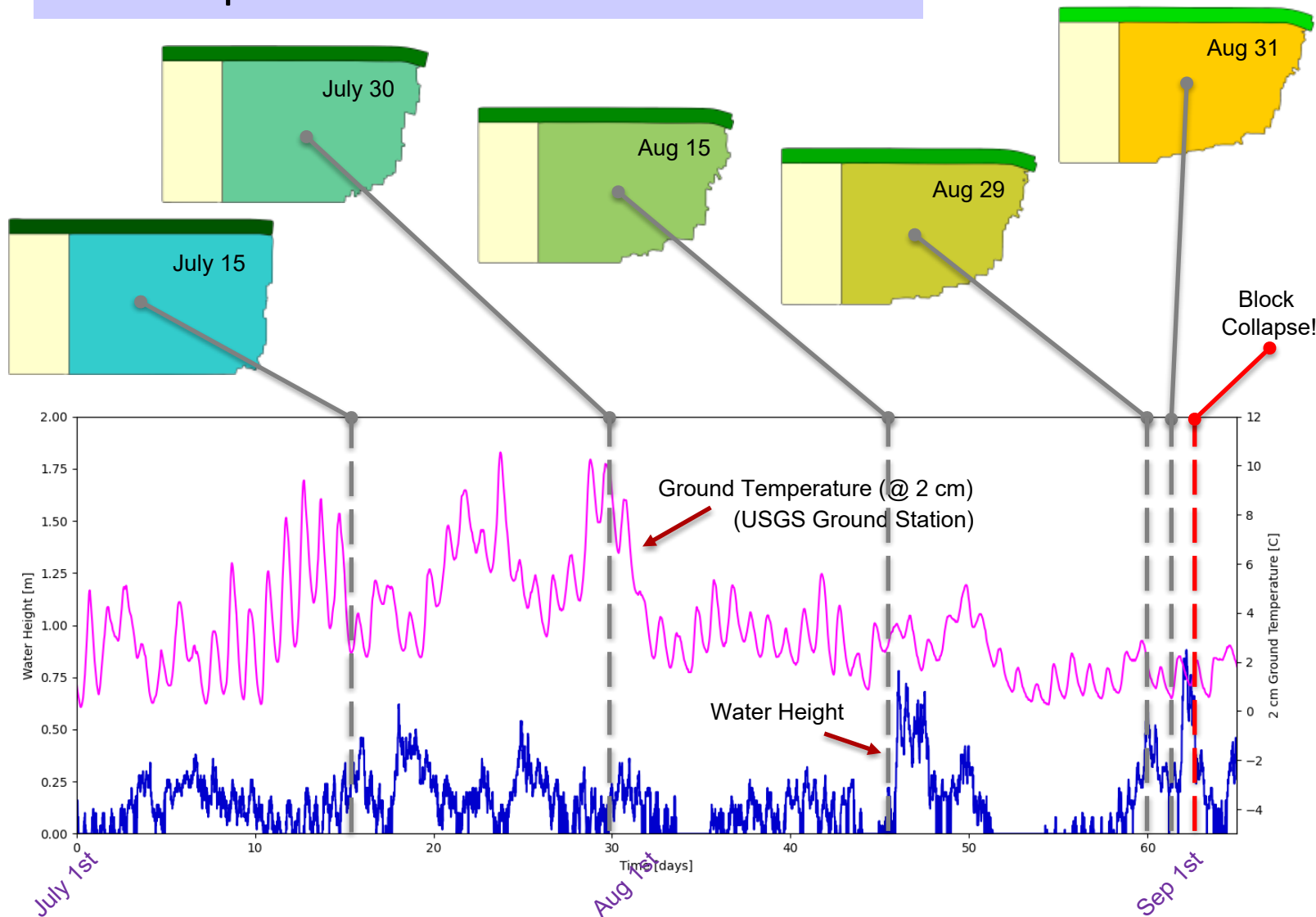
- Computational domain is **2.5D cross-section** of archetypal 3D bluff geometry discretized using a uniform hex grid.
  - **Pseudo-realistic problem** in which a slice of permafrost is exposed to **realistic oceanic and atmospheric forcing BC data** occurring at Drew Point, Alaska in summer 2018
  - **Initial temperature field** obtained from vertical thermistor string placed into DP1-1 ice core at Drew Point.



\* For details, see: Frederick, Mota, Tezaur, Bull, J. Comput. Appl. Math. 2021.

# Thermo-Mechanical Coupling: 2.5D slice\*

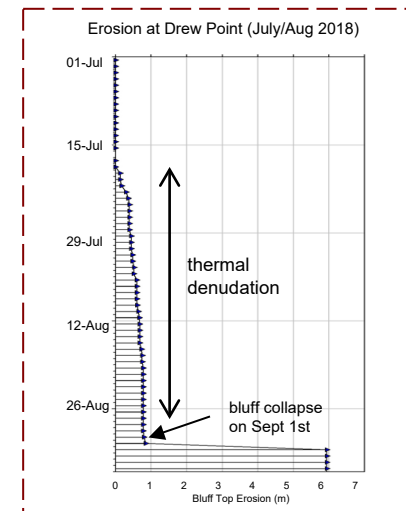
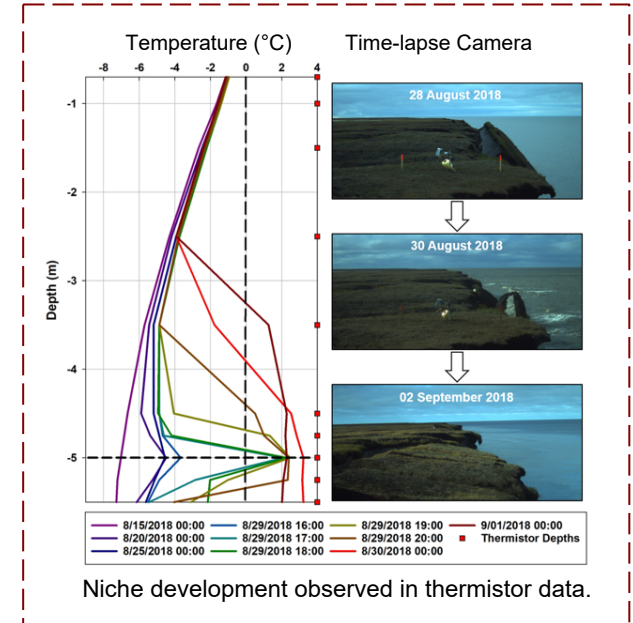
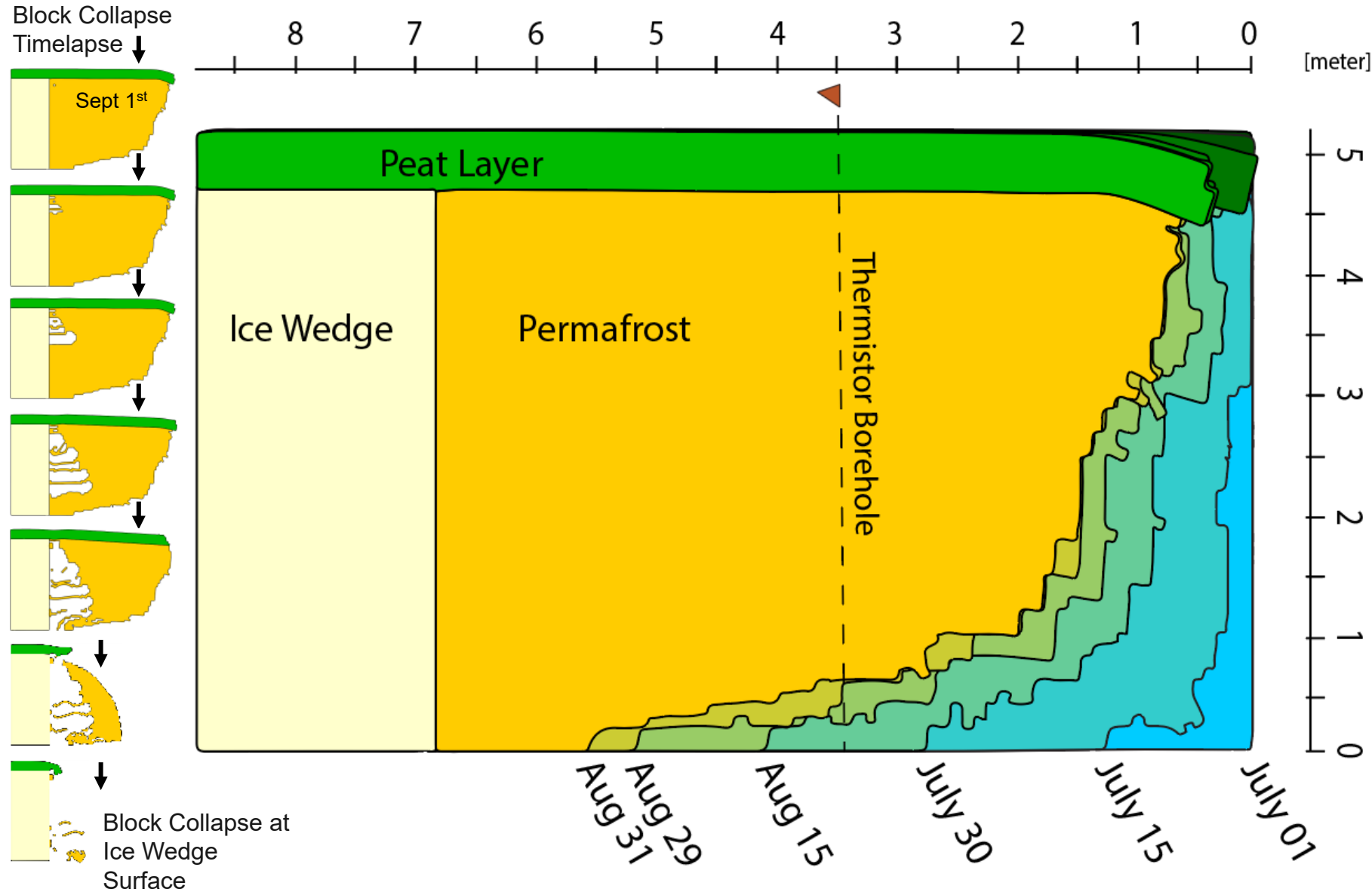
Bluff profiles over simulation time:



\* For details, see: Frederick, Mota, Tezaur, Bull, *J. Comput. Appl. Math.* 2021.

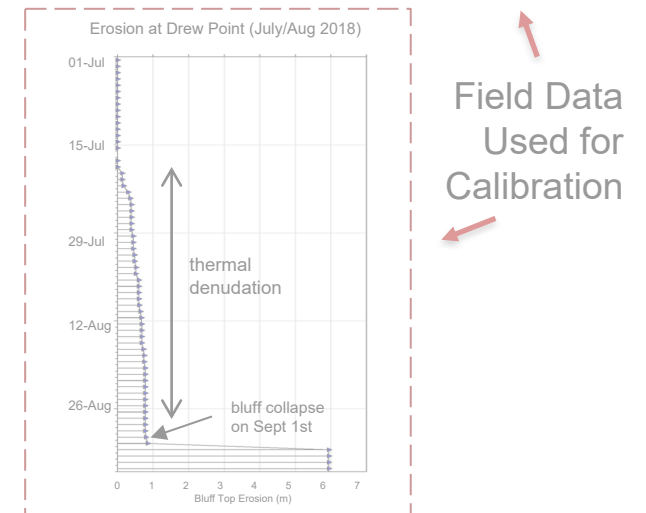
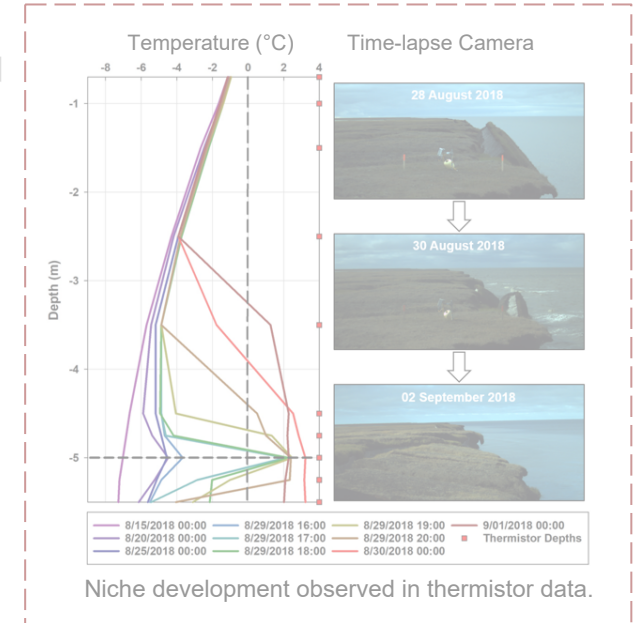
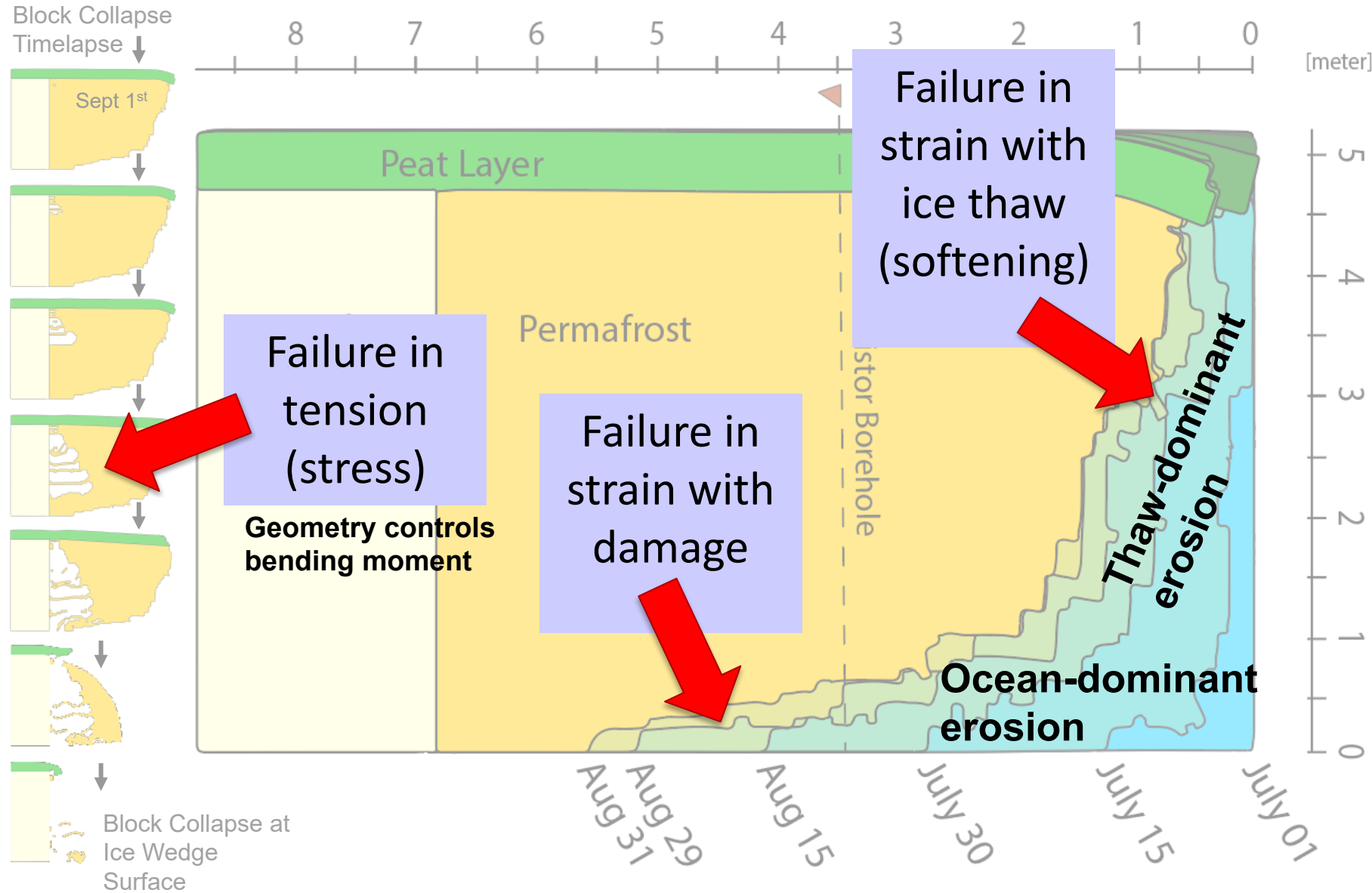


# Thermo-Mechanical Coupling: 2.5D slice



Field Data  
Used for  
Calibration

# Thermo-Mechanical Coupling: 2.5D slice





# Current & Future Work: InteRFACE

- Develop typological understanding of Arctic coastline (terrestrial and oceanographic) to upscale models of erosion and flooding:
  - ACE Model implementation with representative terrestrial configurations
  - Offshore wave environment typology
  
- Currently selecting the terrestrial configurations using the typological assignments
  - Looking to establish 6-7 terrestrial configurations
  - ACE requires unique information not available in landscape work

Offshore Waves

X

Historic	Tp (s)	Hs (m)	Wave Direction	Water Level (m)	Wind Direction	Wind Speed (m/s)	Wave-Wind Orientation
Cluster 1	5.00	1.11	33	-0.15	29	5.5	N-N
Cluster 2	6.30	1.55	113	-0.10	113	6.0	E-E
Cluster 3	7.30	1.40	270	+0.15	263	4.9	W-W
Cluster 4	8.10	2.50	98	-0.20	113	13.0	E-E
Cluster 5	8.75	2.00	330	+0.10	280	7.5	W-W
Cluster 6	9.90	3.00	280	+0.20	316	12.0	W-W

Nearshore Environment



X

Terrestrial Configuration

