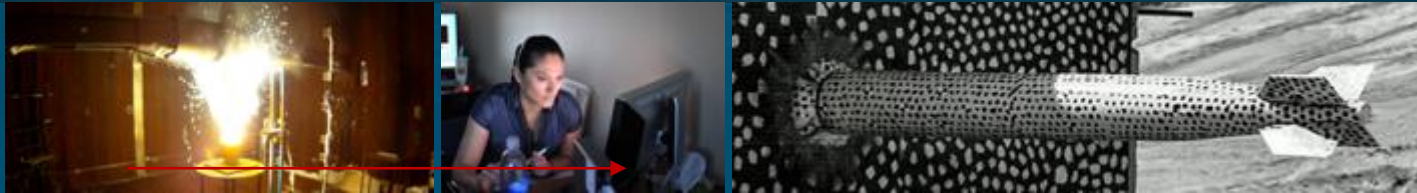




Mesoscale model for spall in additively manufactured metals



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June 23, 2023
Chicago, IL

SANDxxx

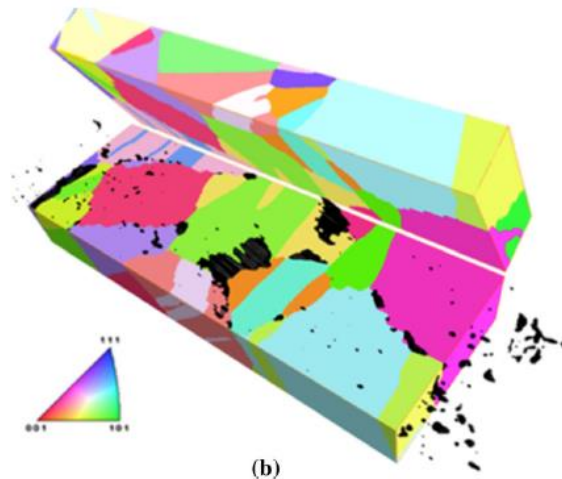
Objective



- Develop a computational model for that
 - Includes realistic AM material features
 - Helps to relate free-surface velocities in plate impact tests to these AM features.
- We are not explicitly modeling microstructural features like voids, dislocations, precipitates, inclusions (although these are known to affect spall*).

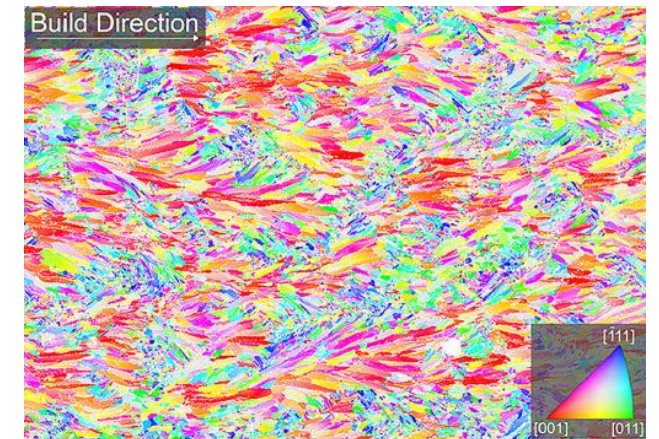
*Sample of work on spall at the microstructural scale

- Trumel et al., J. Mech. Phys. Solids (2009)
- Wayne et al., Scripta Mater. (2010)
- Krishnan et al., Metall. Mat. Trans. A (2014)
- Li et al., Mater. Sci. Eng. A (2016)
- Wang et al., J. Applied Phys. (2017)
- Li et al., Acta Mech. Solida Sinica (2018)
- Li et al., Mater. Sci. Eng. A (2019)
- Nguyen, Luscher, & Wilkerson, Acta Mat. (2019)
- Dongare, Mater. Sci. Eng. A (2019)
- Chiu, in progress (2023)



Microstructural scale
Image: Krishnan et al. (2014)

Length scale for this study



Mesoscale
Image: Specht & Brown (2021)



- Modeling methods
 - Peridynamics background.
 - Crystal plasticity model.
 - Spall kinetics model.
- Impact simulations and comparison with test data.

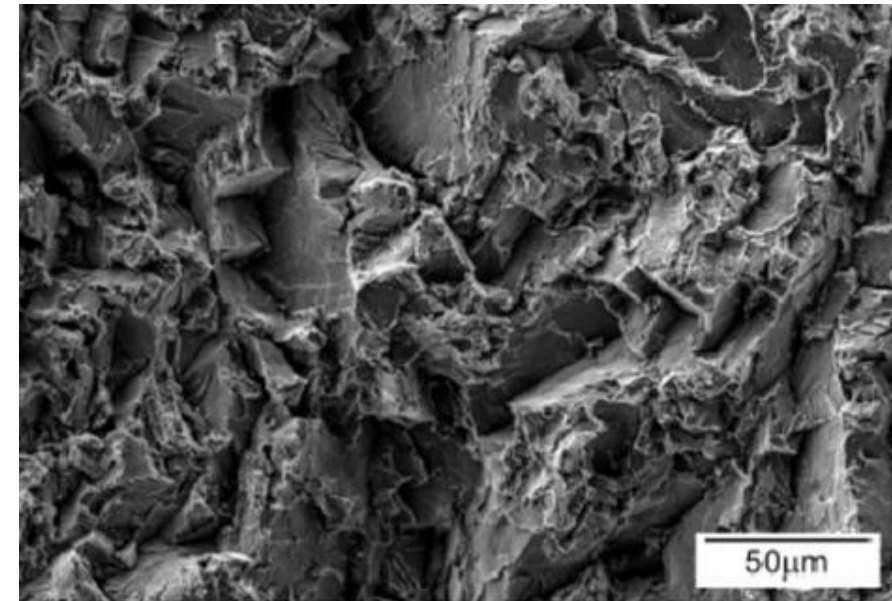
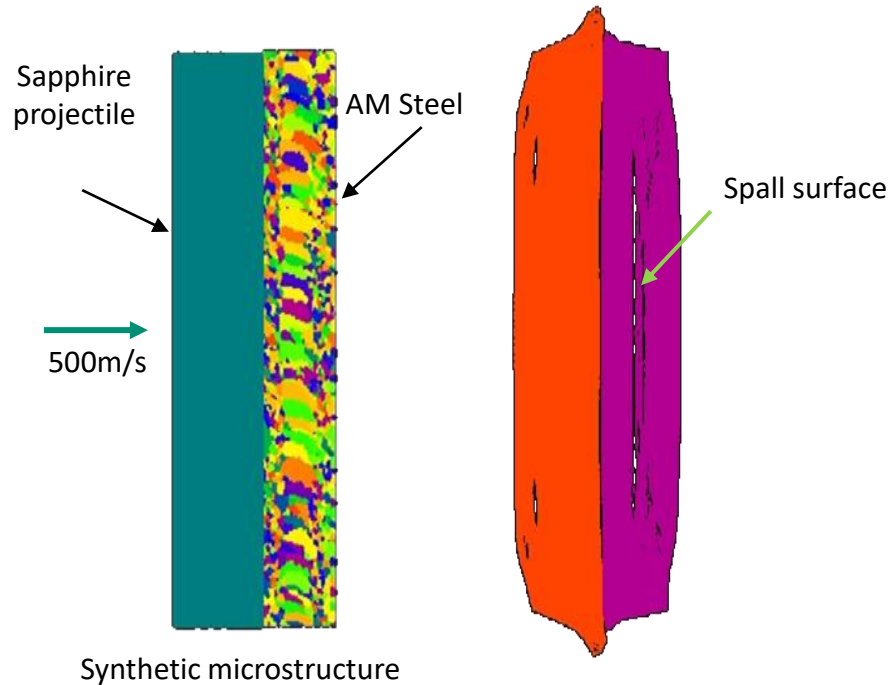
Acknowledgments

Justin Brown, Nathan Brown, John Mitchel

Failure of metals under impact loading



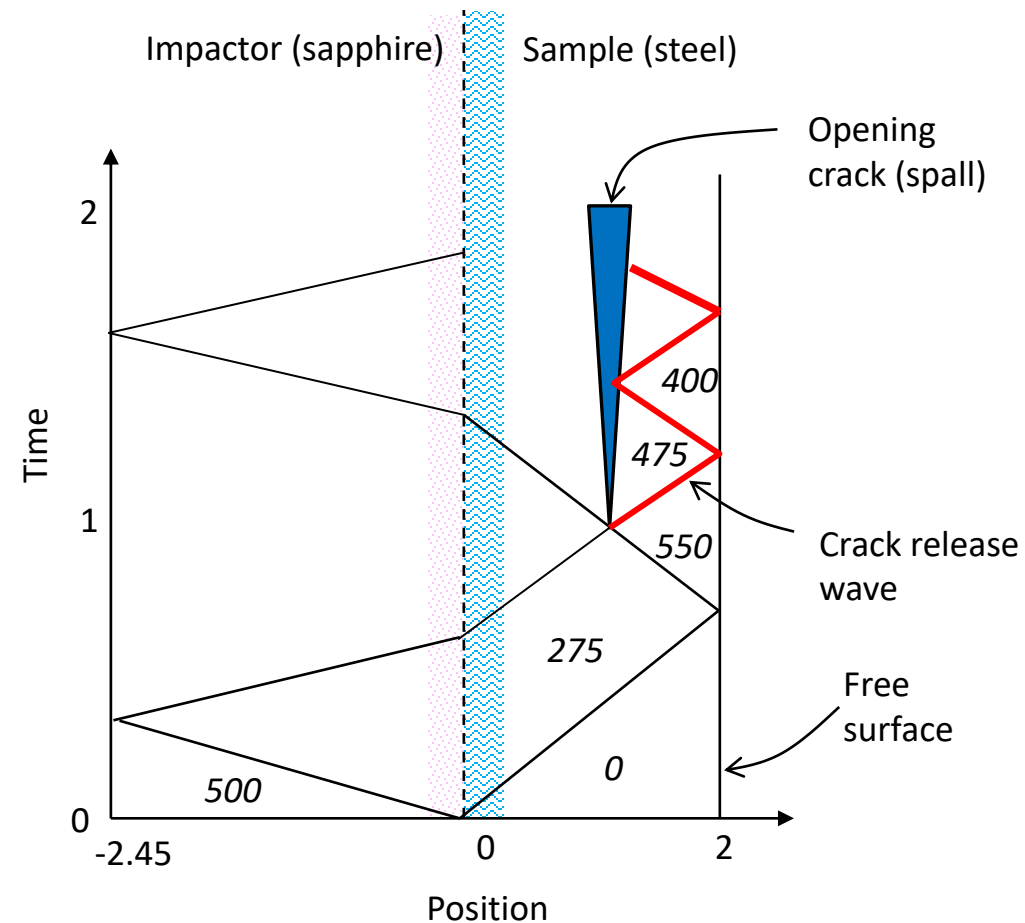
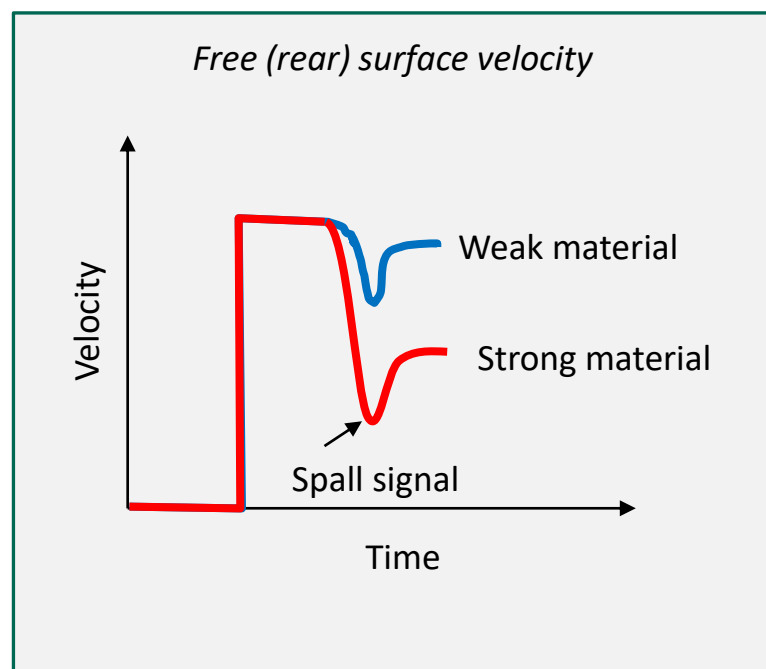
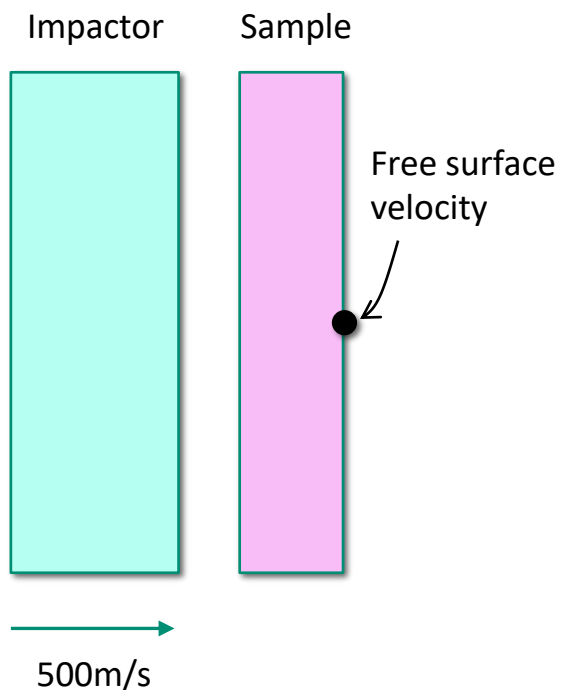
- Plate impact experiments are used in various configurations to measure dynamic material properties.
 - Equation of state data (Hugoniot and release).
 - Dynamic strength under high-rate tensile loading ($\sim 10^5$ 1/s)
 - Spall stress $\gg$ quasi-static tensile strength (typically $> 3\text{GPa}$ for steel).
- Basic test data is the free surface velocity.



Spall surfaces can be irregular*

*Image: E. Svabenska et al., "Effect of shock wave on microstructure of silicon steel", Surfaces & Interfaces (2020).

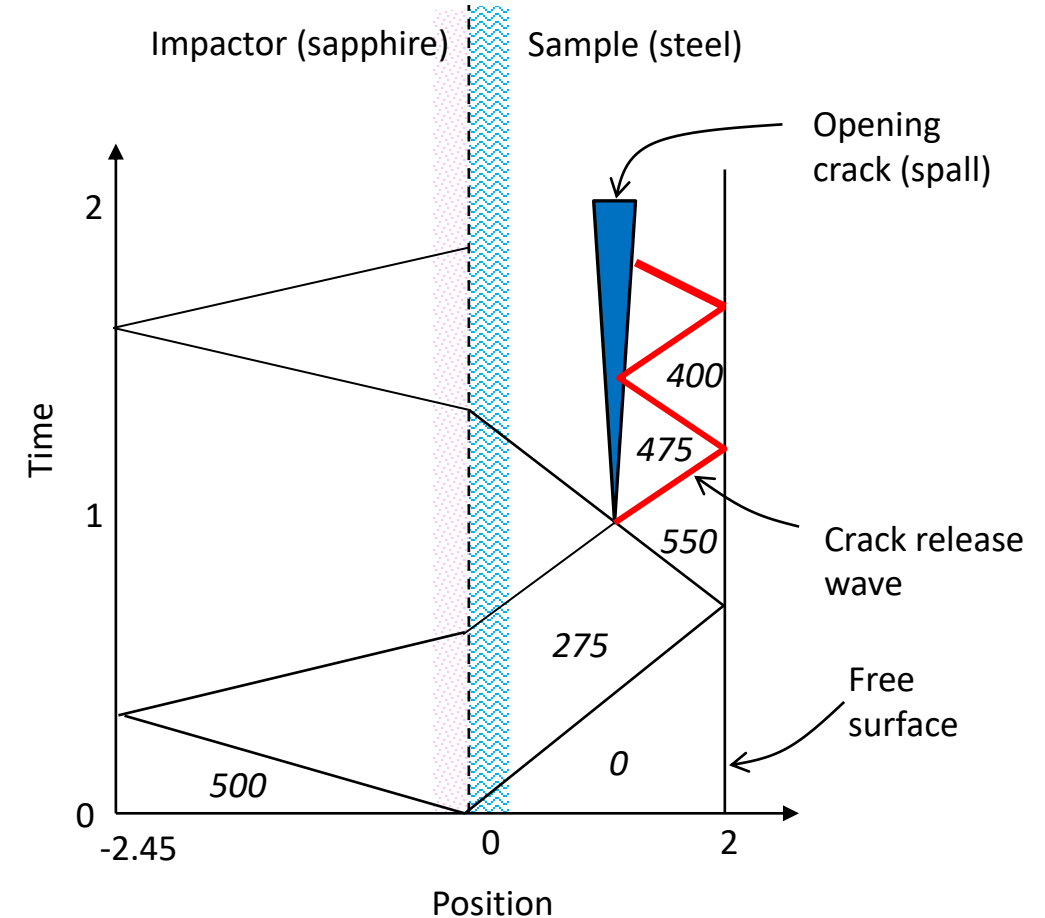
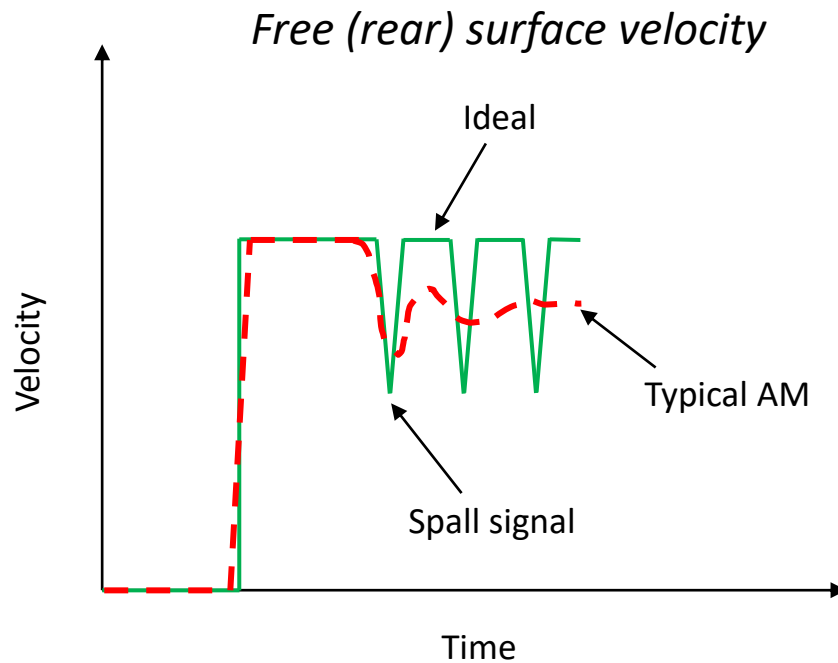
Wave reflections lead to strong tension



Ideal vs. observed AM spall response

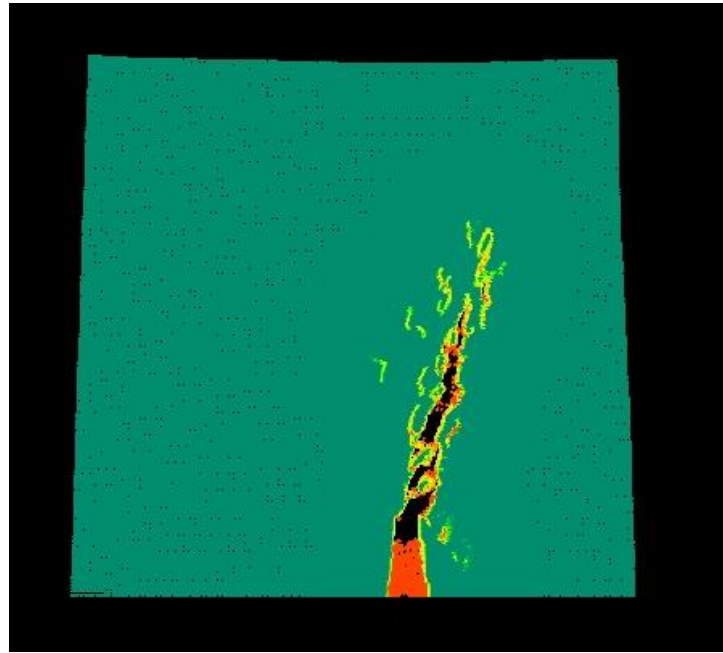


- Ideal:
 - Instantaneous, straight fracture
 - No wave dispersion
- Typically observed:
 - Fracture at a finite rate, complex surface
 - Dispersive shock and reflected waves

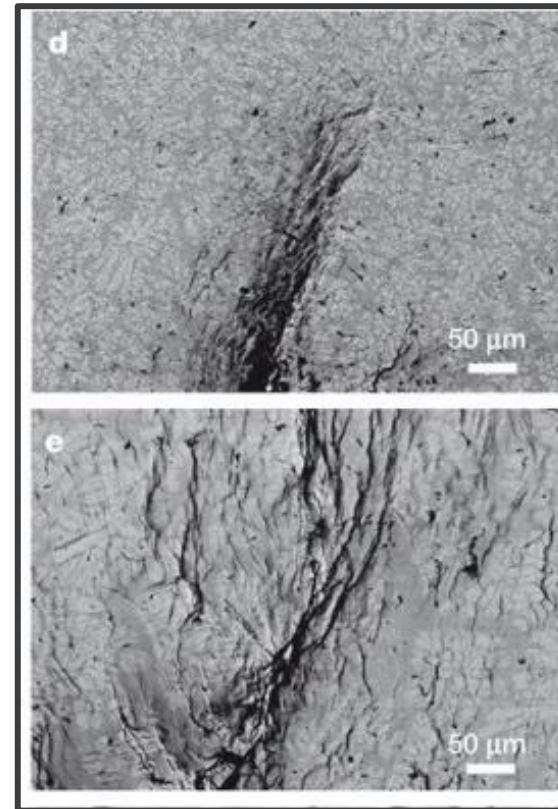


Peridynamics: What it is

- It is a theory of solid mechanics that allows for discontinuities within the basic equations.
- It also allows for long-range forces.



Peridynamic simulation

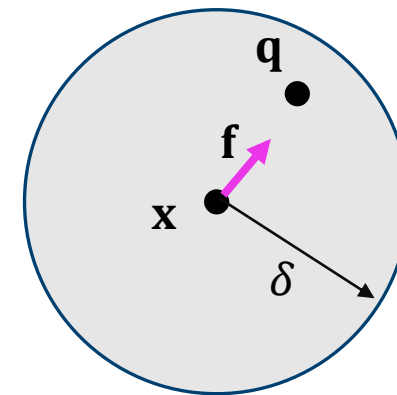
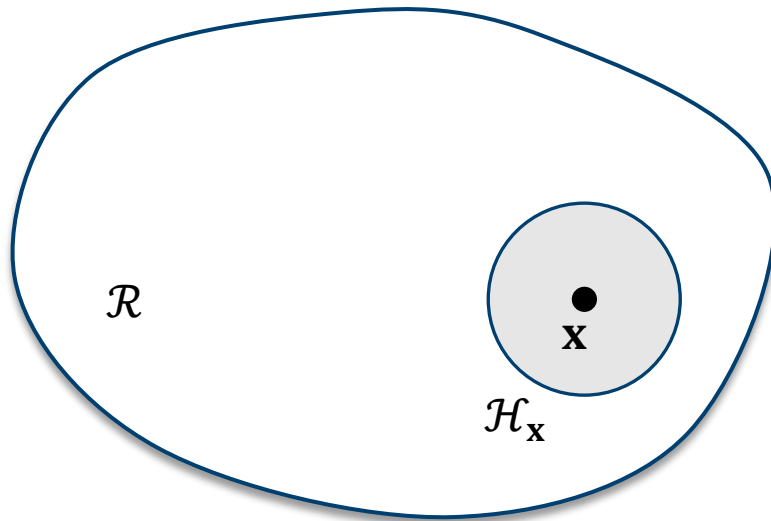


Metallic glass crack tip
Images: Hofmann et al, 2008

- Peridynamic momentum balance in 3D:

$$\rho(\mathbf{x})\ddot{\mathbf{u}}(\mathbf{x}, t) = \int_{\mathcal{H}_x} \mathbf{f}(\mathbf{q}, \mathbf{x}, t) d\mathbf{q} + \mathbf{b}(\mathbf{x}, t) \quad \forall \mathbf{x} \in \mathcal{R}, t \geq 0.$$

- $\mathbf{f}$ is the *pairwise bond force density* of the *bond* from $\mathbf{q}$ to $\mathbf{x}$.

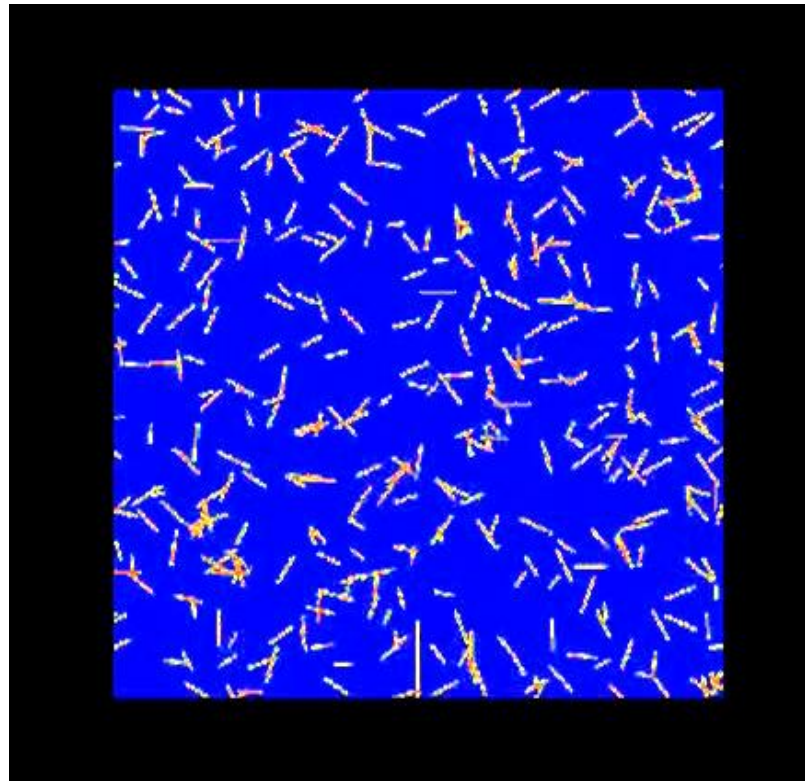


9 | Peridynamics allows fractures to appear spontaneously



- Integral equations: no need to try to differentiate on a singularity.
- Meshless discretization allows grains to be defined in any shape without a FE mesh.
- Bonds fail according to a damage criterion..
 - which in this case is supplied by the Spall Kinetics Model (more later).

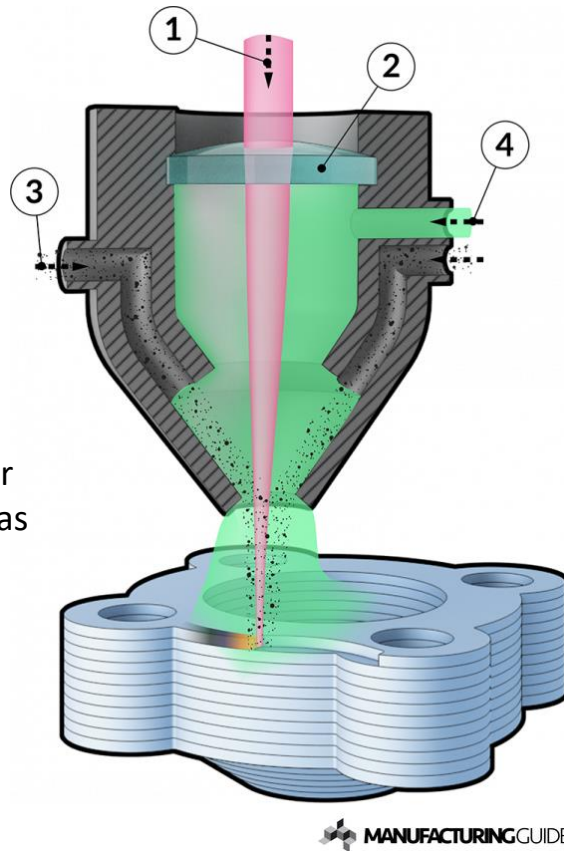
Example of macroscopic failure in a sample with defects
VIDEO



LENS process

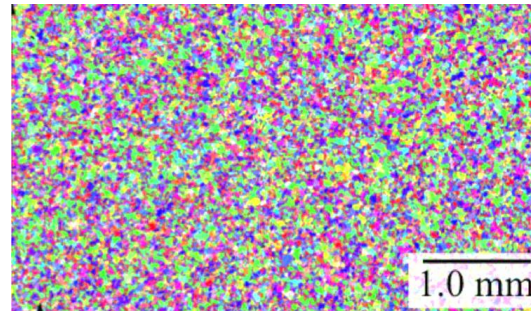


- Large, elongated grains are typically formed
- Nonuniform thermal history

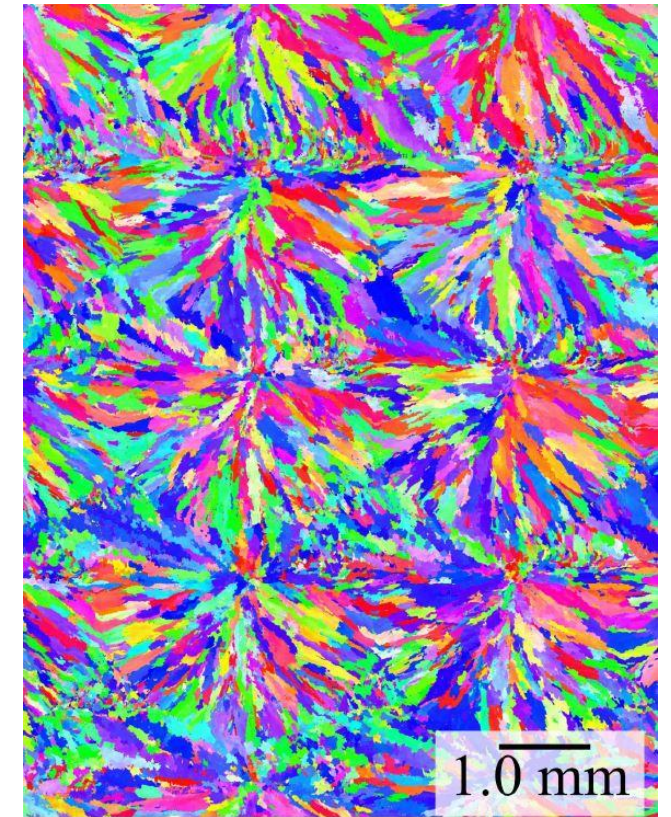


1. Laser
2. Lens
3. Powder
4. Inert gas

Wrought microstructure



Typical AM microstructure



Images:

- <https://www.manufacturingguide.com/en/laser-engineered-net-shaping-lens-0>
- D. Adams et al, SAND2019-7001 (2019)

Crystal plasticity implementation in peridynamics



- Need to capture:
 - Preferential flow directions determined by the slip planes.
 - Anisotropic elastic response.
- Previous work uses:
 - Correspondence approach to material modeling in peridynamics
 - Decomposition of the deformation gradient into sequential plastic and elastic parts:

$$\mathbf{F} = \mathbf{F}^e \mathbf{F}^p$$

- ❖ S. Sun & V. Sundararaghavan, *International Journal of Solids and Structures* (2014).
 - ❖ J. Luo, A. Ramazani, & V. Sundararaghavan, *International Journal of Solids and Structures* (2018).
 - ❖ X. Gu, Z. Qing, & E. Madenci, *Engineering Fracture Mechanics* (2019).
 - ❖ A. Lakshmanan et al., *International Journal of Plasticity* (2021).
- Present work uses a simpler but less general approach.

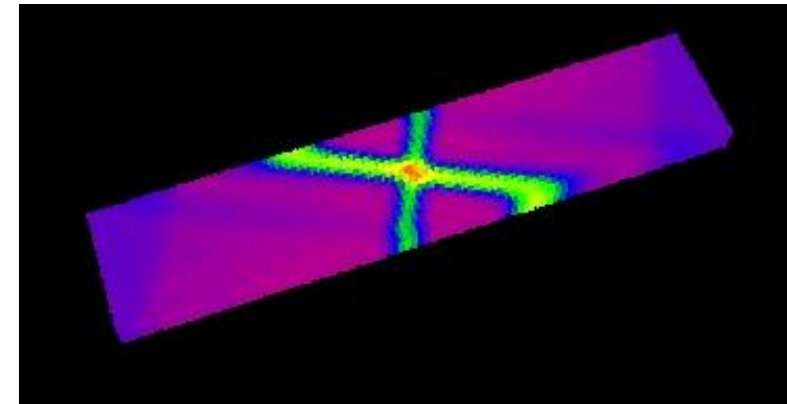
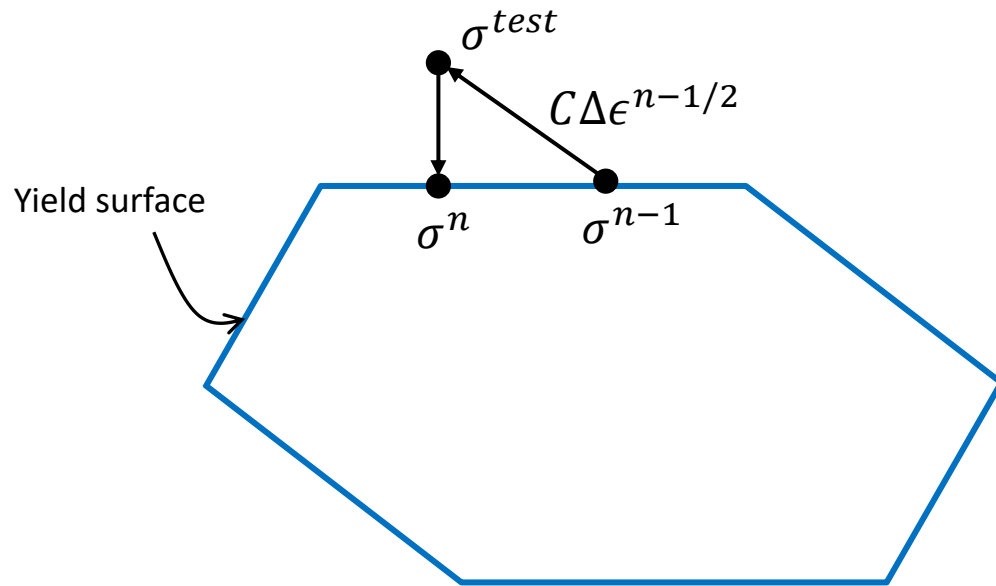
Crystal plasticity model*

- Analogous to the radial return method
- The slip systems limit the deviatoric stress to a polyhedron in the space of deviatoric tensors.
- A test stress is found from the previous cycle stress and the current stress increment.

$$\sigma^{test} = \sigma^{n-1} + C\Delta\epsilon^{n-1/2}$$

where C is the anisotropic 4th order elasticity tensor.

- The new stress σ^n is the point on the surface closest to the test stress.



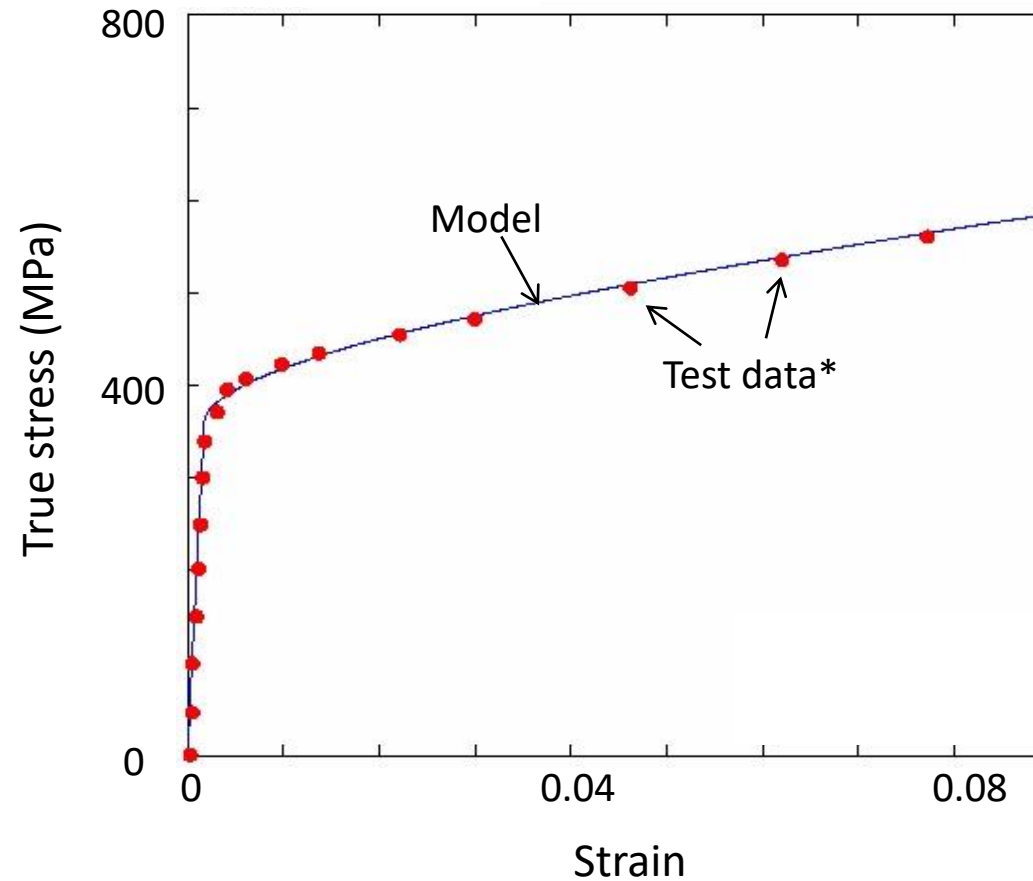
Stretching of a bar with one slip system
Colors show equivalent plastic strain

* P. Maudlin and S. Schiffrl, *Computer Methods in Applied Mechanics and Engineering* (1996)

Fit to quasi-static stress-strain data for AM 304L stainless steel



- Sample was additively manufactured with the Laser Engineered Net Shaping (LENS) process.
- The model also contains temperature and strain rate dependence.



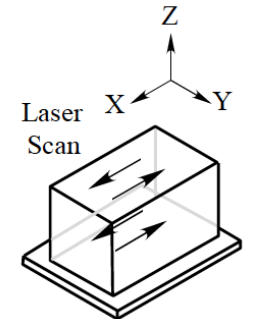
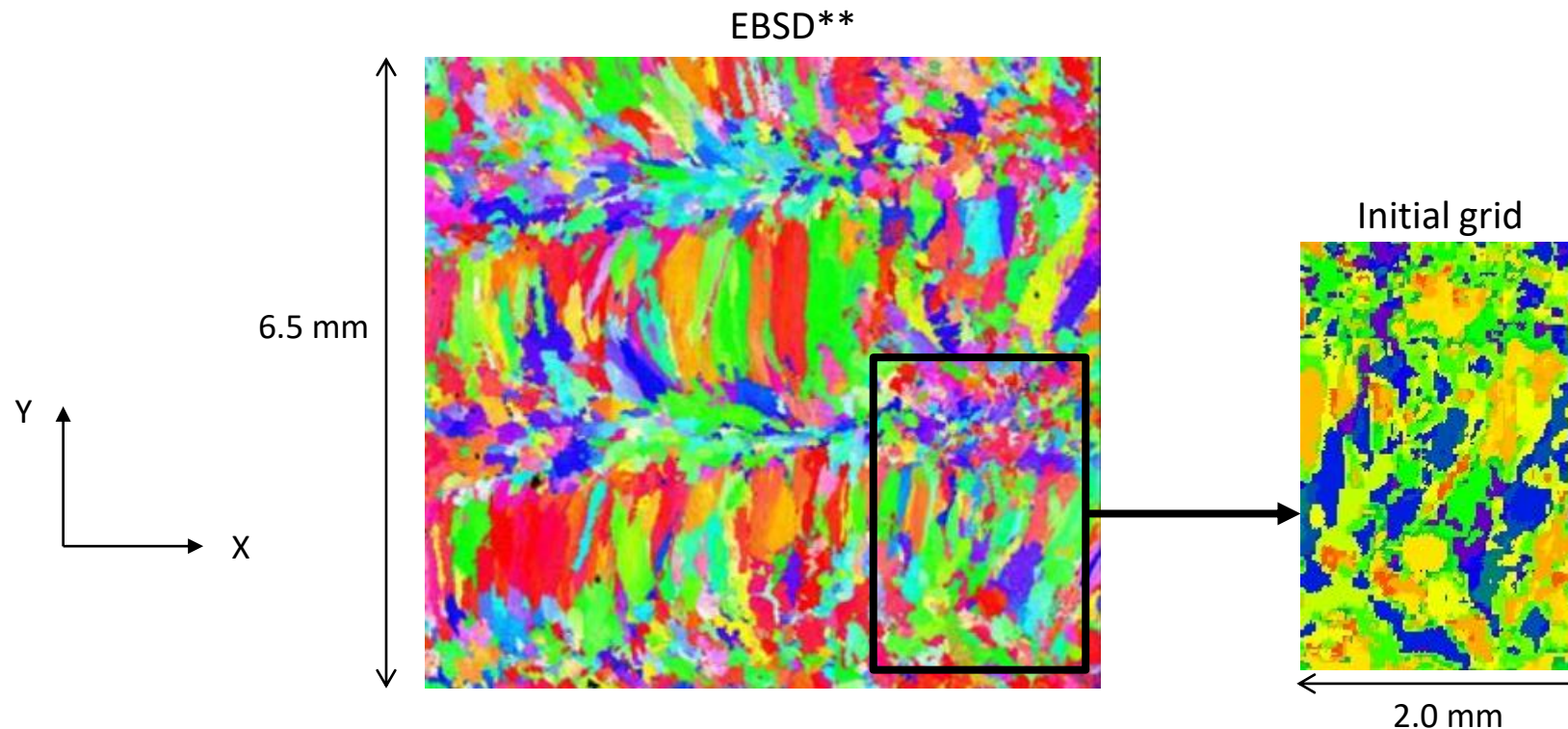
* D. P. Adams et al., Sandia tech report SAND2019-7001 (2019)

Assignment of lattice orientations



- Grains are imported into the model from electron backscatter diffraction (EBSD) images.
- Lattice orientations are assigned randomly using Euler angles.
- These are combined with published anisotropic crystal elasticity data* for 304L SS to compute C for each grain.

$$C_{11} = 209\text{GPa} \quad C_{12} = 133\text{GPa} \quad C_{44} = 121\text{GPa}$$

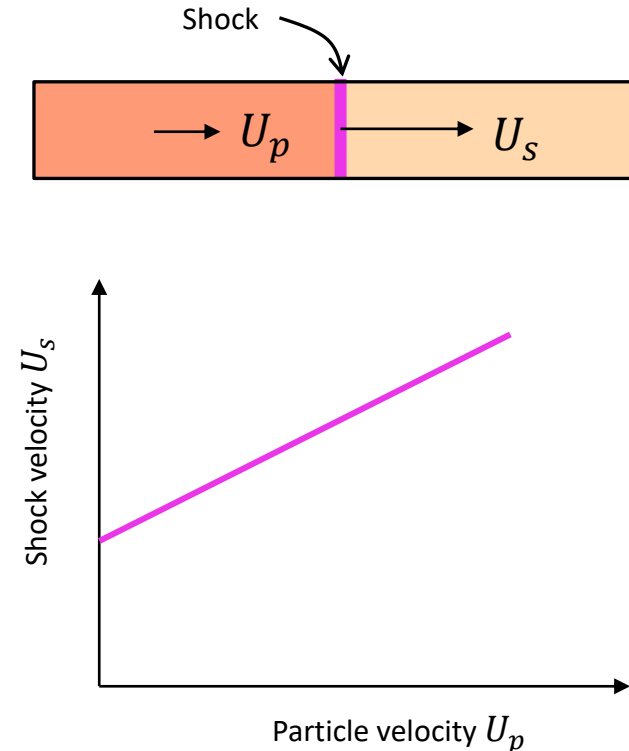
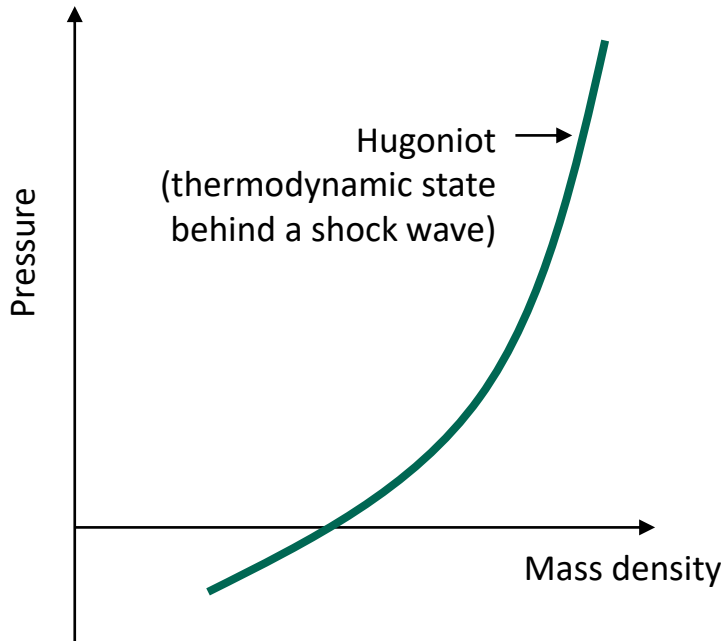


*H. Ledbetter, Physica B+C (1985)

**Image: T. Ruggles

Equation of state

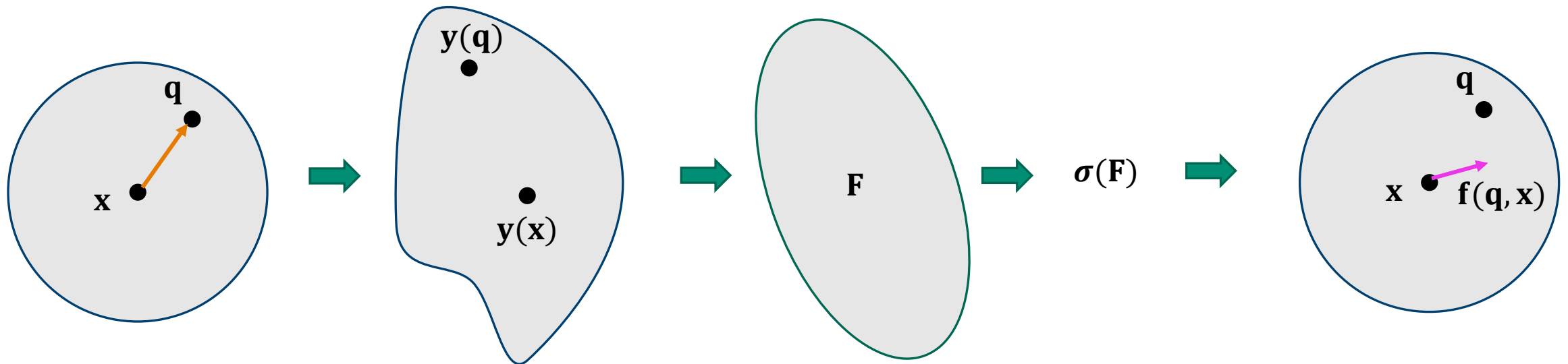
- Add a pressure term to the deviatoric stress found from the crystal plasticity model.
- Mie-Gruneisen EOS:
 - Input: Internal energy density, mass density
 - Output: Pressure, temperature
 - Shock velocity is a linear function of particle velocity behind the shock.
 - Same EOS for all grains



Correspondence material models



- The above material models are implemented using the correspondence framework.
- This adapts a local material model to the peridynamic framework.
 - The deformation of a family is mapped to an approximate deformation gradient tensor $\mathbf{F}$.
 - A stress tensor $\boldsymbol{\sigma}$ is found from a stress-strain relation.
 - The stress tensor is mapped onto the bonds to provide the bond forces $\mathbf{f}(\mathbf{q}, \mathbf{x})$.

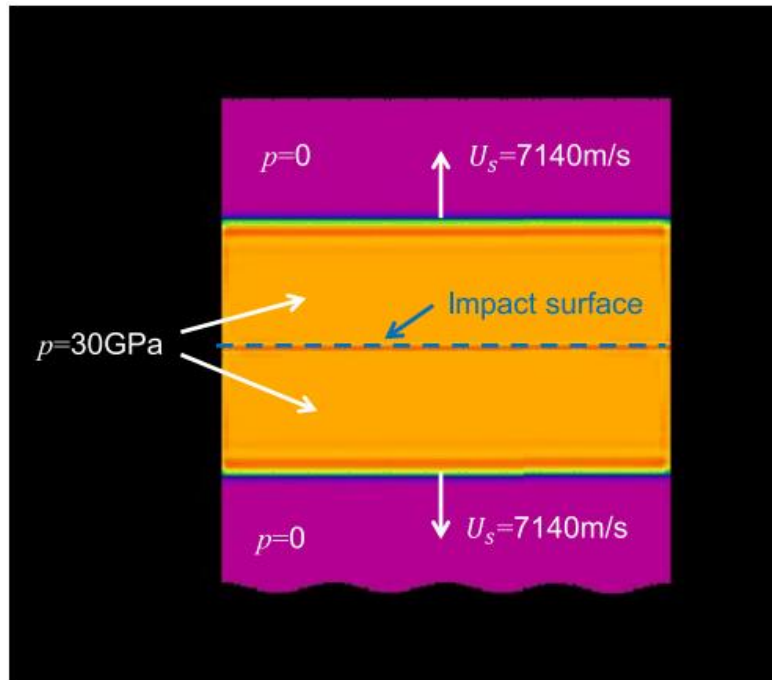


Modeling shock waves in peridynamics

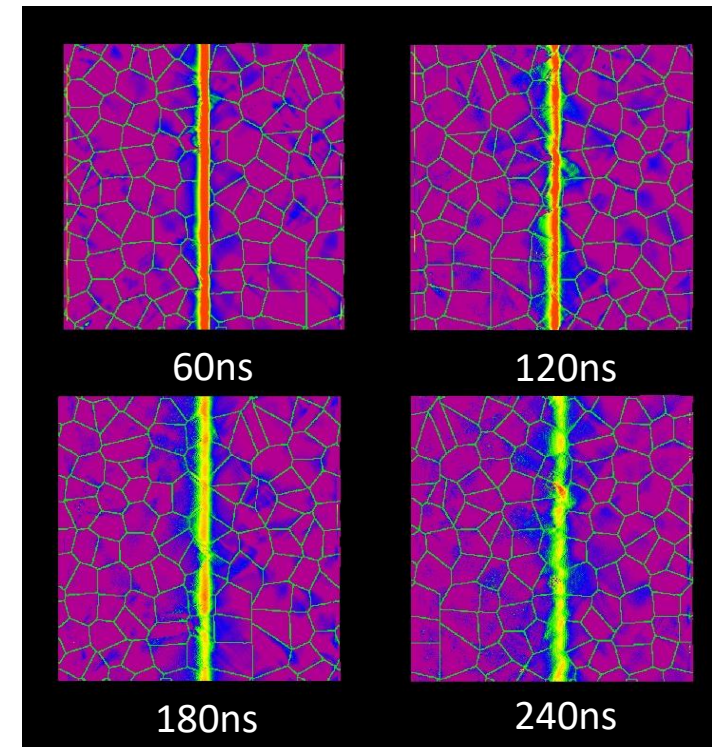


- Von Neumann artificial viscosity is needed.
- Energy balance is treated using a nonlocal version of the first law of thermodynamics.
- For very large deformations, an Eulerian material model formulation is needed.
 - Not used in the present application.

Aluminum impact at 3km/s
Colors show pressure



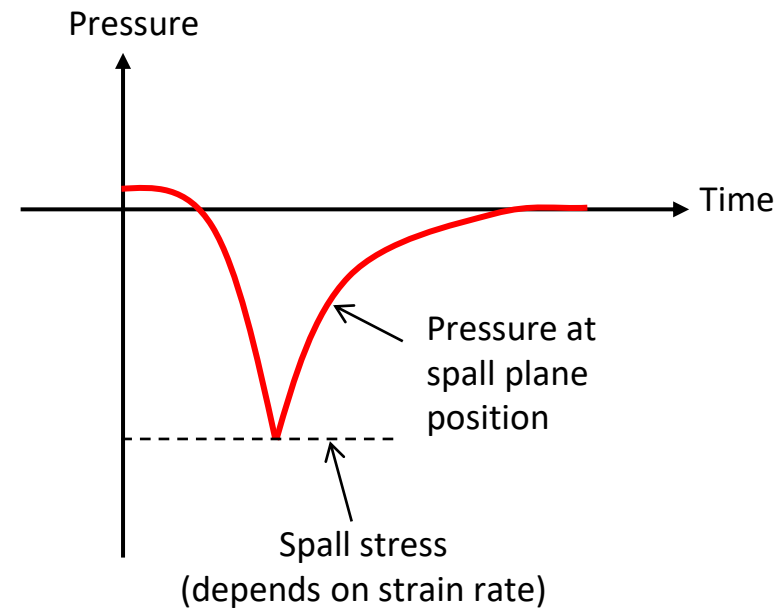
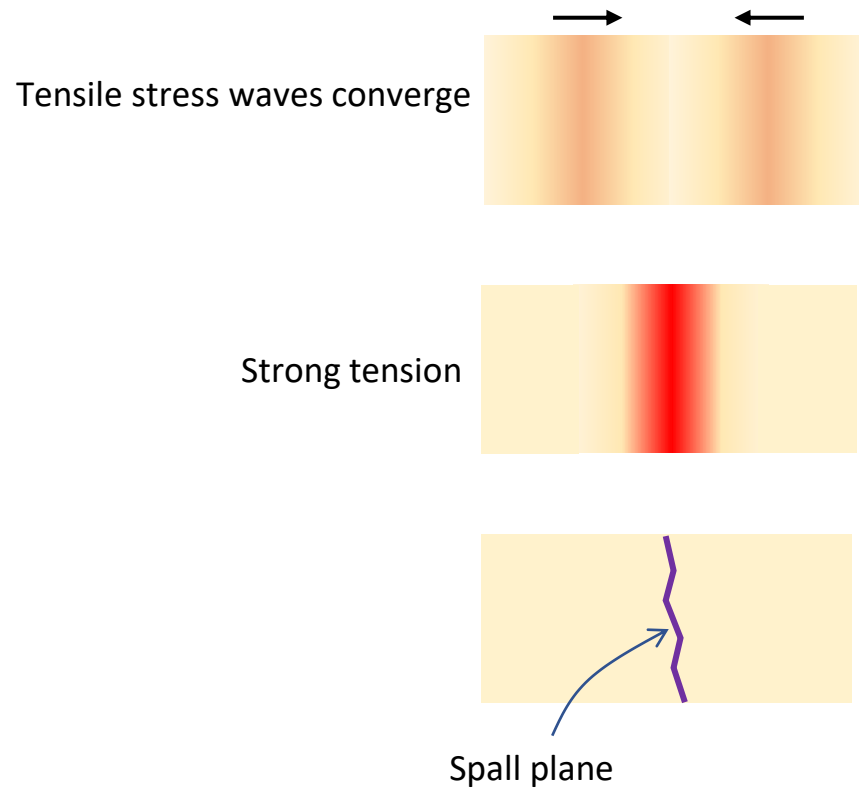
Shock wave in a polycrystal
Colors show strain rate



- SS et al, Modeling shockwaves and impact phenomena with Eulerian peridynamics, *Intl J Impact Engin* (2017)

Spall kinetics model

- Failure occurs over a finite period of time.
- The rate of failure depends on the peak tensile stress and strain rate.

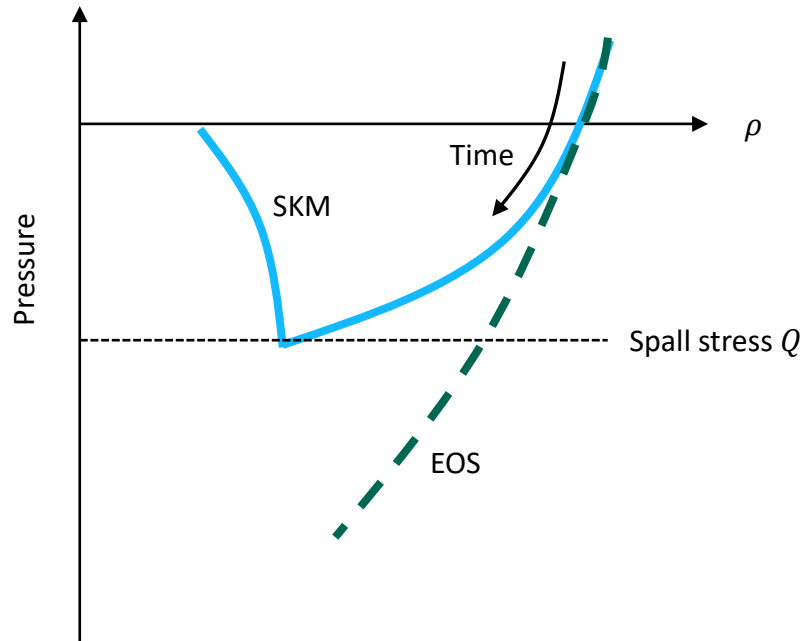


Spall kinetics model: softening and variability

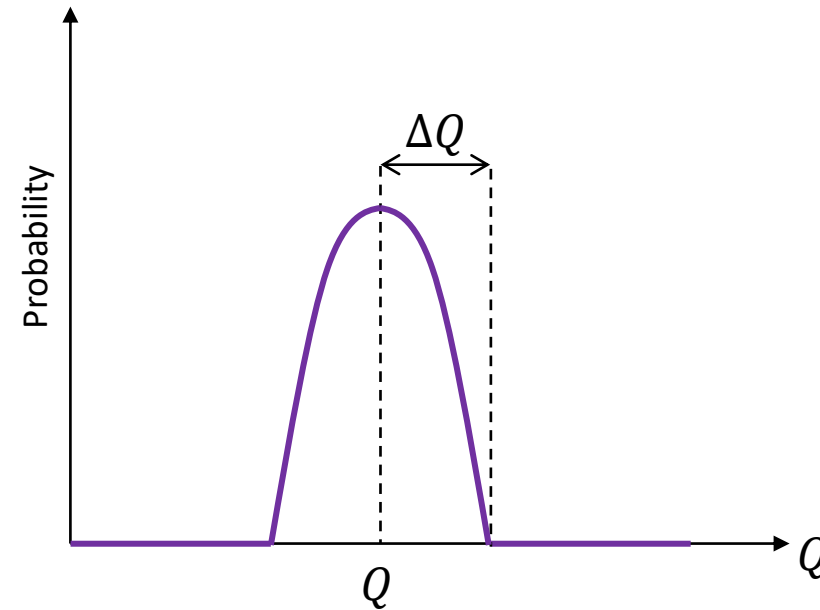


- The EOS is modified to include softening as the critical stress for failure is approached.
- Each grain (from EBSD) is randomly assigned a value of spall stress.

Softening and failure during expansion



Grain-to-grain variability in spall stress



Impact on AM steel at 247m/s: Videos

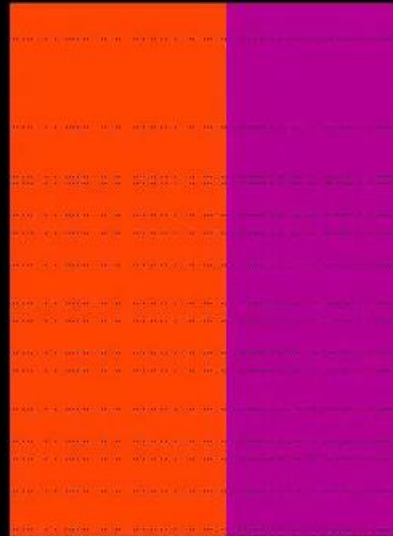


- Total time simulated is $1.8\mu\text{s}$.

Pressure
Red > 4GPa
Purple < -4GPa

X-Velocity
Red > 250m/s
Purple < 0

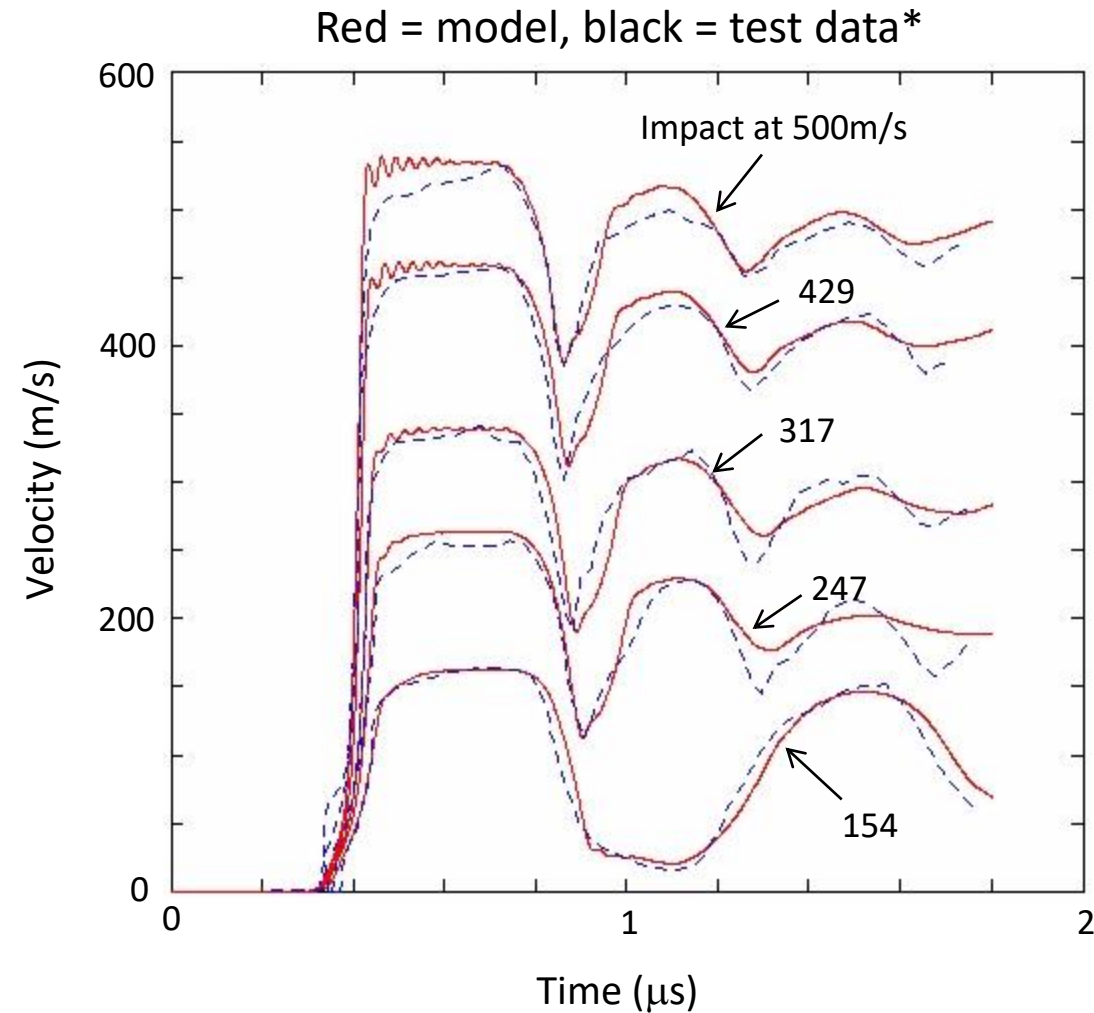
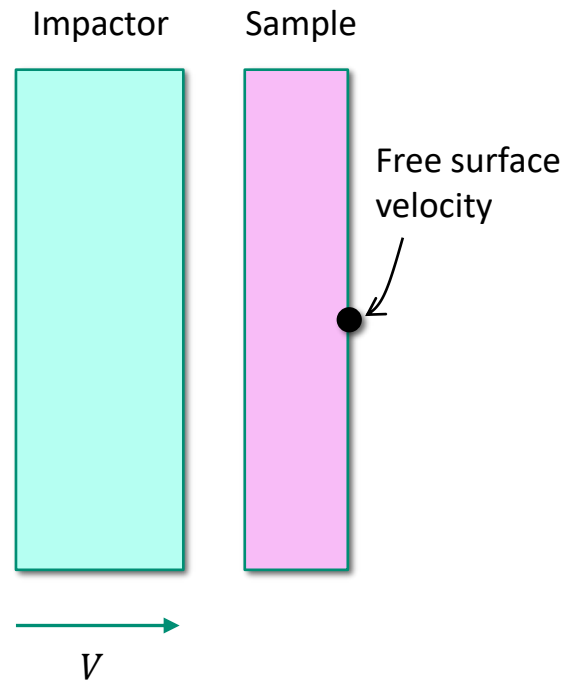
X-Displacement
Red > 0.27mm
Purple < 0



Results: Free surface velocity



- Figure compares model results with test data.



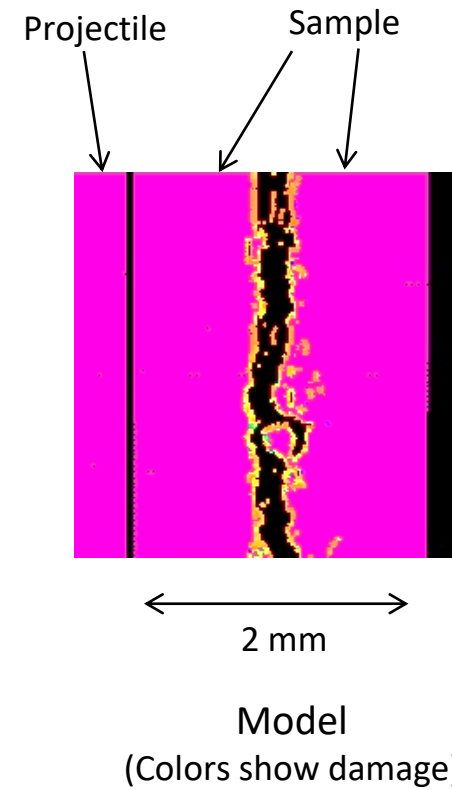
* J. L. Wise et al., AIP Conference Proceedings (2017)
P. E. Specht et al., Sandia tech report SAND2019-12275 (2019)



$$V = 317\text{m/s}$$



Experiment*

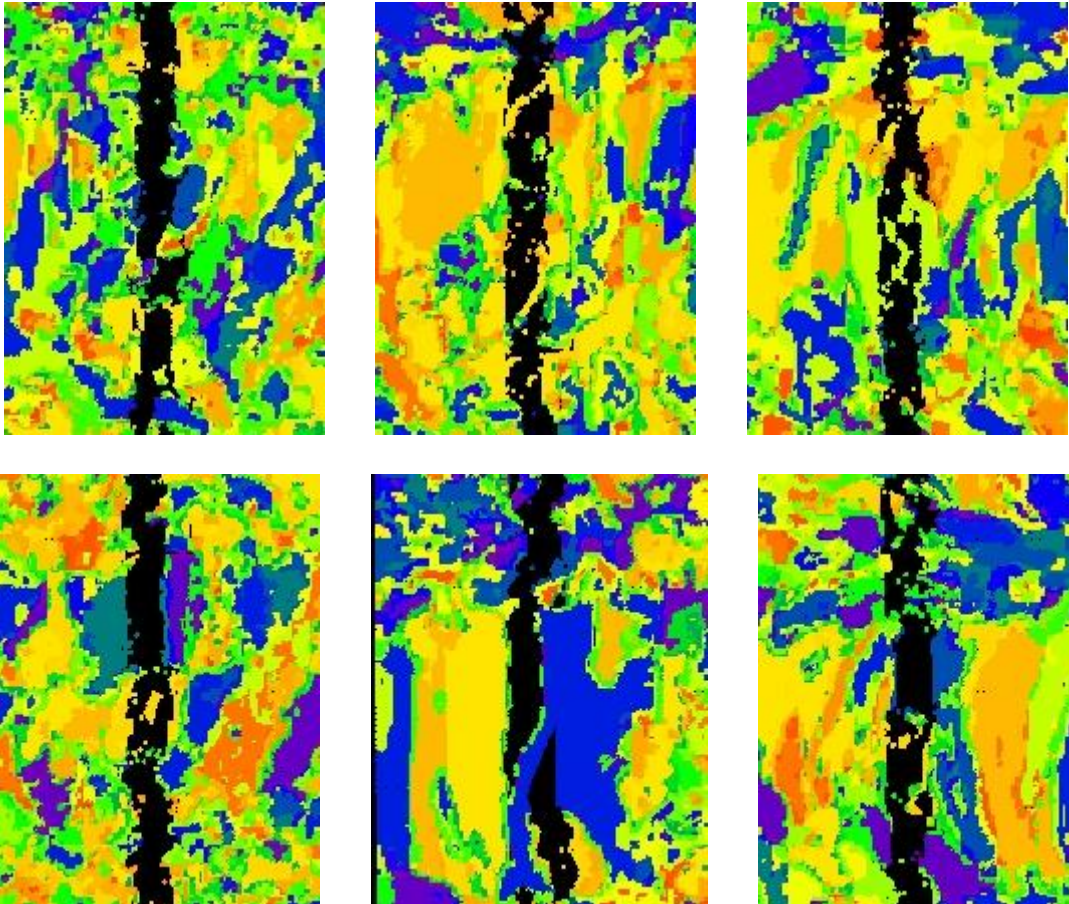


* D. P. Adams et al., Sandia tech report SAND2019-7001 (2019)

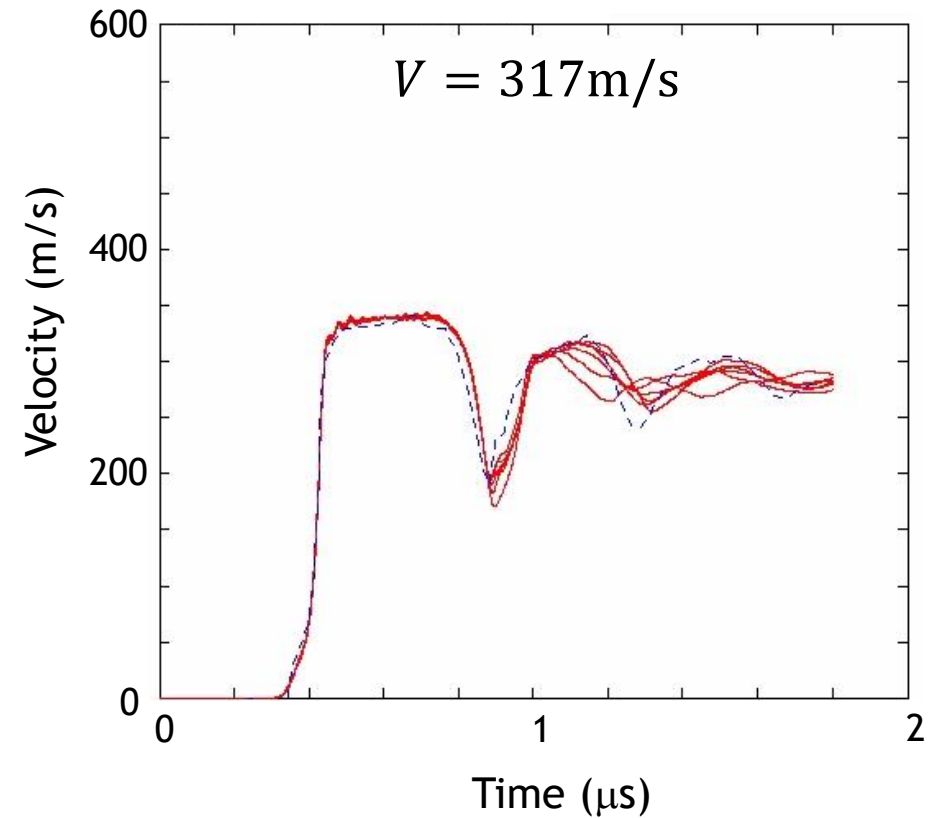
Effect of microstructure



- What is the effect of extracting different samples from within the EBSD image?
- Makes some difference at intermediate impact velocities.



Free surface velocity for the 6 samples, all X-cut





- The large and distorted grain shapes with AM materials affect the dynamic failure properties.
- A number of new capabilities have been implemented in peridynamics:
 - Crystal plasticity
 - Importing microstructures
 - Spall kinetics model
 - Material variability
- The resulting model reproduces the main features of the test data over a range of impact velocities.

This work: S. Silling, D. Adams, and B. Branch, “Mesoscale Model for Spall in Additively Manufactured 304L Stainless Steel”, *International Journal for Multiscale Computational Engineering* (2023)