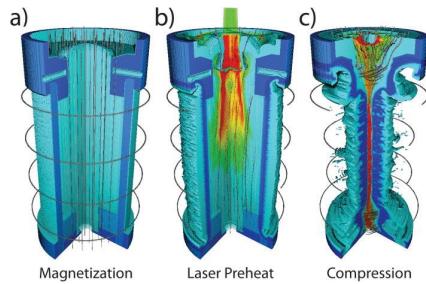


Sandia National Laboratories

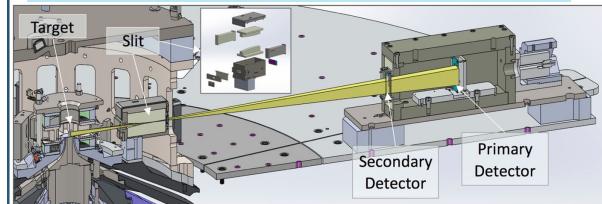
Neutron source reconstruction of one-dimensional neutron images with modified generalized expectation maximization algorithm



[1] P. F. Knapp et al., "Effects of magnetization on fusion product trapping and secondary neutron spectra," *Physics of Plasmas*, vol. 22, no. 5, 2015.

Introduction

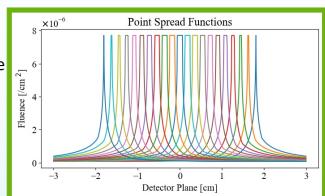
- A one-dimensional imager of neutrons (ODIN) comprised of a tungsten aperture, high density polyethylene (HDPE) converter foils, and CR-39 track detectors
- Images neutrons emitted from Magnetized Liner Inertial Fusion (MagLIF) experiments at the Z facility
- Forward scattering protons from the HDPE generate destructive tracks on the front face of CR-39 detectors which are exposed using a chemical etching process and recorded using an optical scanning system
- Tracks are down selected for primary DD-neutrons expected to have traveled directly through the slit assembly to the detector
- Neutron source profile reconstruction has been performed via a modified generalized expectation maximization algorithm that accounts for intrinsic background in the CR-39



[2] David J. Ampleford, et al, "One dimensional imager of neutrons on the Z machine", *Review of Scientific Instruments* 89, 10132 (2018)

ODIN Data Generation

- An analytical forward model of ODIN has been developed and used to generate response function matrices (P_{ij}) needed to perform inverse problem calculations
- CR-39 tracks are integrated along the radial axis to generate a 1D axial detector response
- A subset of data is used to remove poor detection locations including alignment pinholes and serial number (\mathbf{Y}_i)



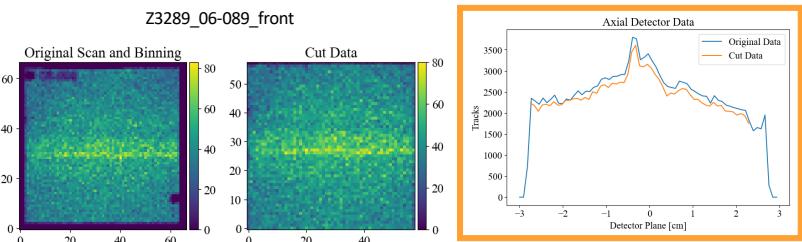
S. A. Ricketts^{1,2}, M. A. Mangan², P. Volegov³, D. N. Fittinghoff³, D. J. Ampleford²

¹Texas A&M University, College Station, TX, USA

²Sandia National Laboratories, Albuquerque, NM, USA

³Lawerence Livermore National Laboratory, Livermore, CA, USA

sricket@sandia.gov

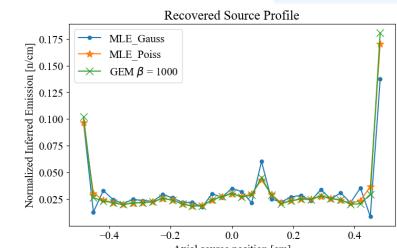
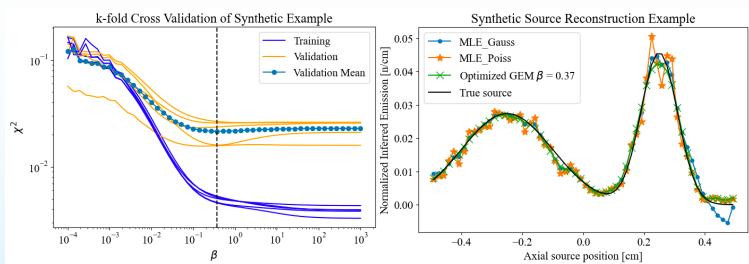


Source Reconstruction Methods

- The discretized Fredholm integral equation of the first kind can be solved for \mathbf{G}_j via maximum likelihood estimation (MLE) algorithms which search for solutions that maximize the likelihood $L(\mathbf{G}) = p(\mathbf{Y}|\mathbf{G})$ given different constraints

$$\sum_{j=1}^m P_{ij} G_j = Y_i, i = 1, 2, \dots, n$$

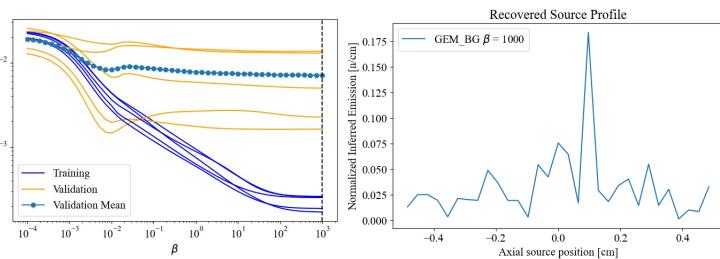
- Such constraints are for Gaussian (MLE_Gauss) or Poissonian (MLE_Poiss) noise as well as a generalized expectation maximization (GEM) which implements a regularization parameter β
- Small β values smooth the solution and large β values approach MLE_Poiss
- A k-fold cross validation is used to determine the optimal regularization parameter



Modified GEM Algorithm

- Reconstructions of axial detector data created nonphysical edge effects caused by intrinsic background tracks in the CR-39
- A modification to the GEM algorithm (GEM_BG) was made to account for this background by adding three basis functions \mathbf{B}_{ik} as additional response functions associated to new coefficients μ_k

$$[P, B] \begin{bmatrix} G \\ \mu \end{bmatrix} = Y$$



Conclusions and Future Work

- The modified algorithm successfully removed edge effects caused by intrinsic noise in the CR-39 and produced an accurate reconstruction of the neutron emission profile
- Uncertainty Quantification including of selection of β parameter
- Integration of multiple CR-39 scans to improve signal to noise ratio
- Comparison to other Z diagnostics including x-ray emission data



Sandia National Laboratories



Sandia National Laboratories

Sandia National Laboratories is a multimission laboratory managed and operated by National Technology & Engineering Solutions of Sandia, LLC, a wholly owned subsidiary of Honeywell International Inc., for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-NA0003525.

