



Cornell University

Differentiable programming to enable modern optimization methods for MRE



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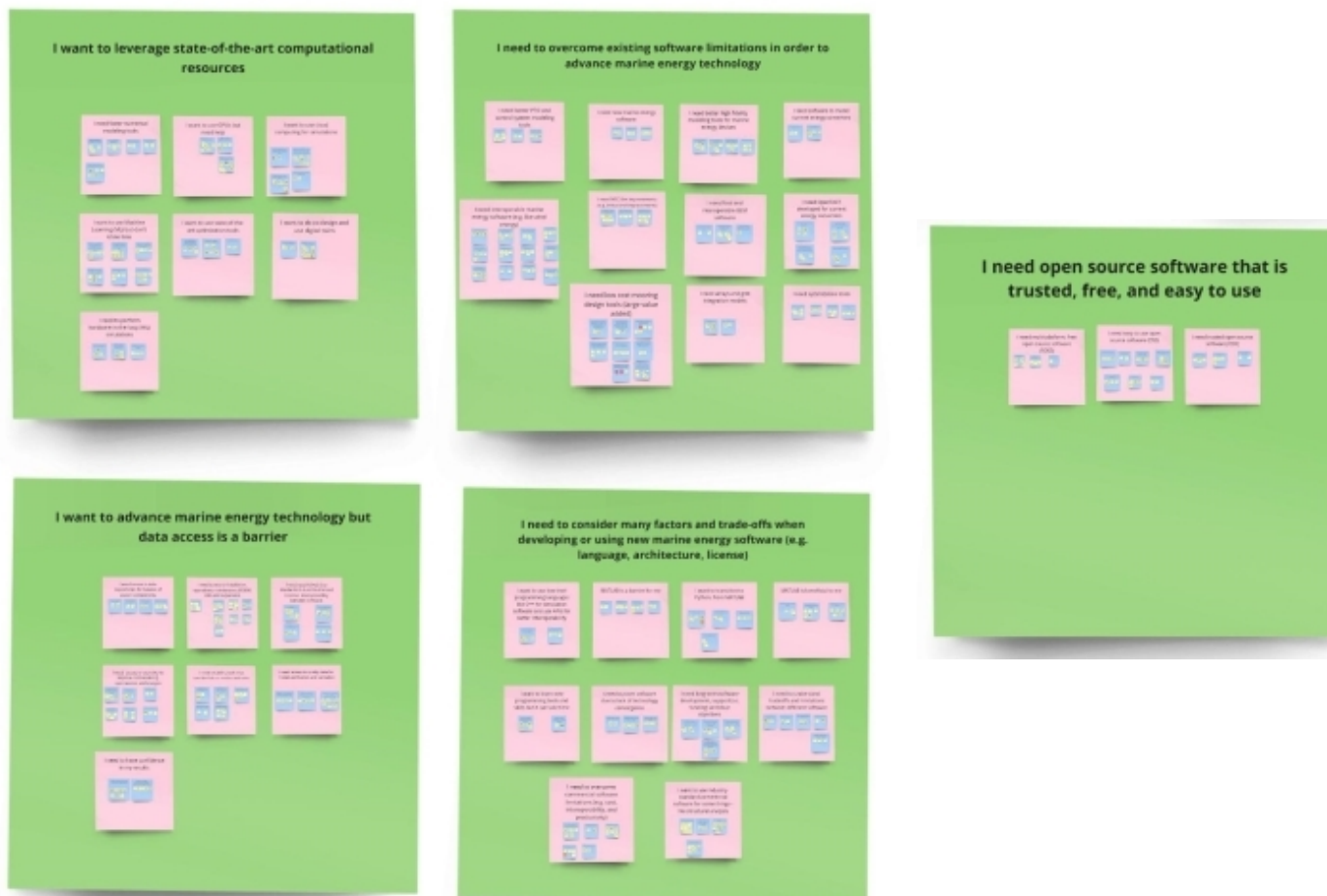


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- Scientific computing is hugely different today as compared to even five years ago in both the software and hardware landscapes.
- The amazing advances delivered by these methods are dependent on a critical technology: *differentiable programming*.
- ***We propose creating a differentiable and portable boundary element method (BEM) solver*** that will allow for modern and complex workflows in the design and optimization of wave energy converters (WECs).
- *Differentiability* will enable the use of novel methods such as adjoint-based multi-disciplinary optimization and data-driven methods such as physics-informed machine learning.
- *Portability* will make high-performance computing more accessible to everyday users through cloud computing and allow running the same code in different architectures such as GPUs.
- If successful, the project is expected to lead to completely new methods in the design of marine renewable energy.

Next-Gen Software needs & gaps assessment



I want to leverage state-of-the-art computational resources

I need faster numerical modeling tools



I want to use GPUs but need help



I want to use cloud computing for simulations



I want to use Machine Learning (ML) but don't know how



I want to use state-of-the-art optimization tools



I want to do co-design and use digital twins



I need to perform hardware-in-the-loop (HIL) simulations



Automatic Differentiation



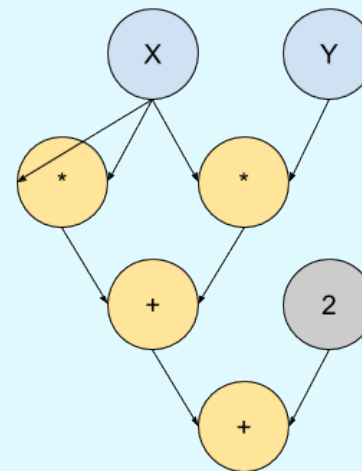
Finite difference

- $\text{cost} = n_{\text{inputs}} * \text{function}$

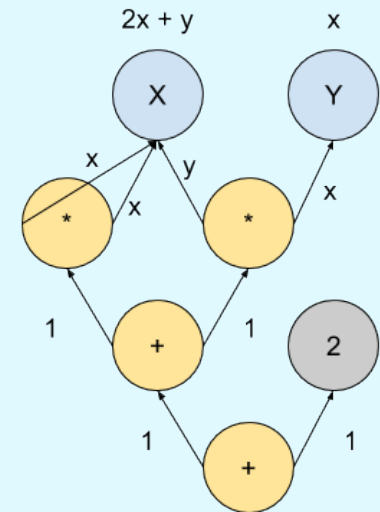
$$f' = \frac{f(x+h) - f(x)}{h}$$

Automatic differentiation

- $\text{cost} = 2 * \text{function}$

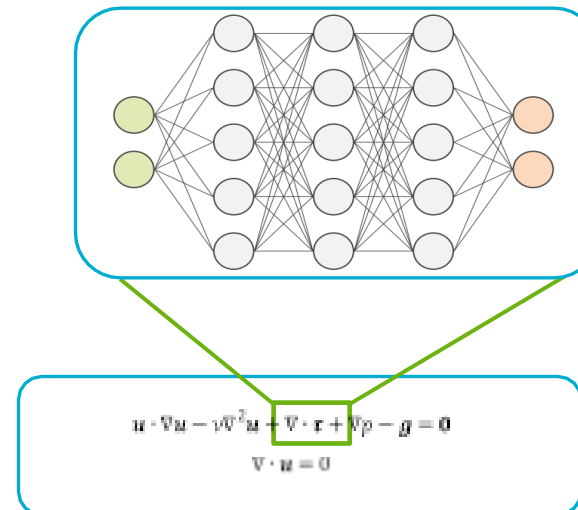
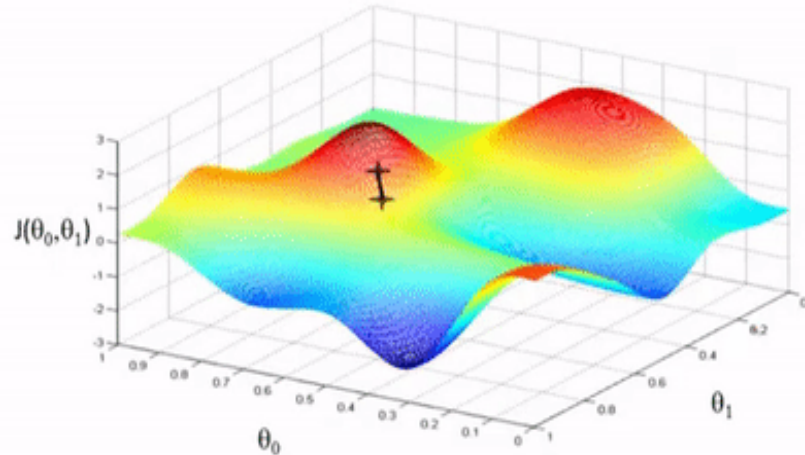
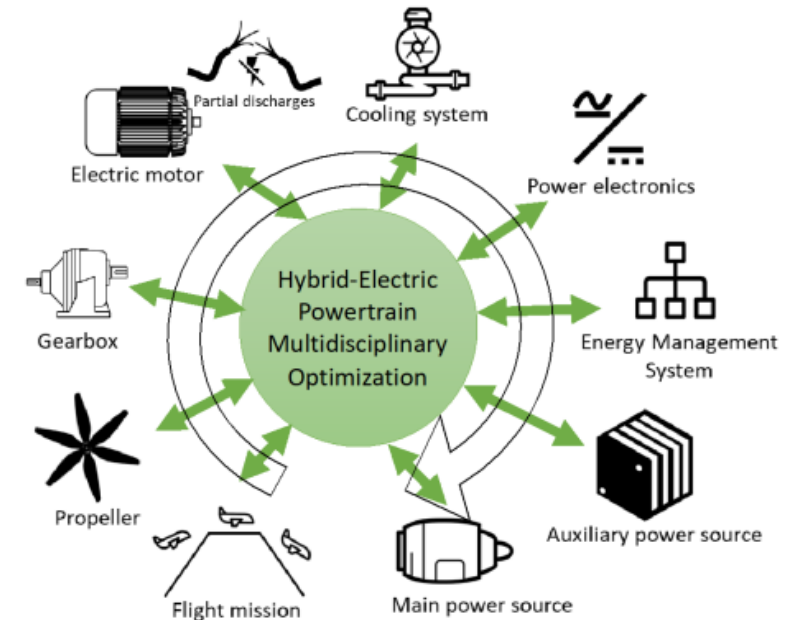


Computational Graph
 $x^2 + xy + 2$

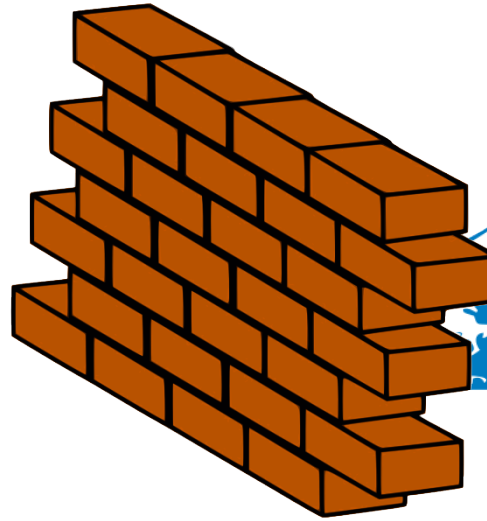
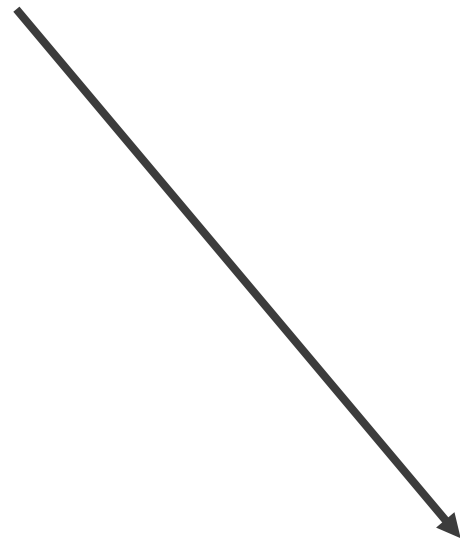
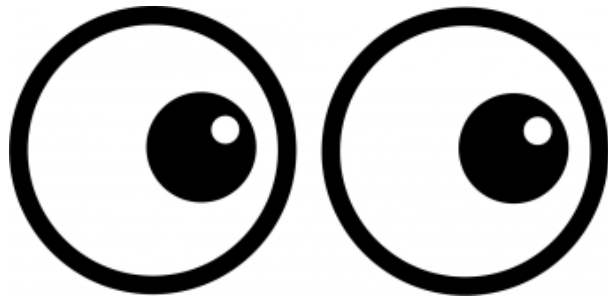


Backpropagation

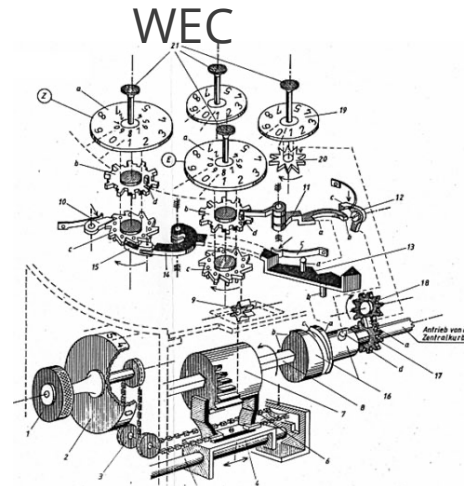
- **Why do we need the gradients?**
 - Adjoint-based optimization
 - Large multi-disciplinary optimization
 - Non-parametric geometry optimization
 - Control co-design
 - Physics-informed machine learning



Current options don't allow automatic differentiation to see hydrodynamics



Hydrodynamics



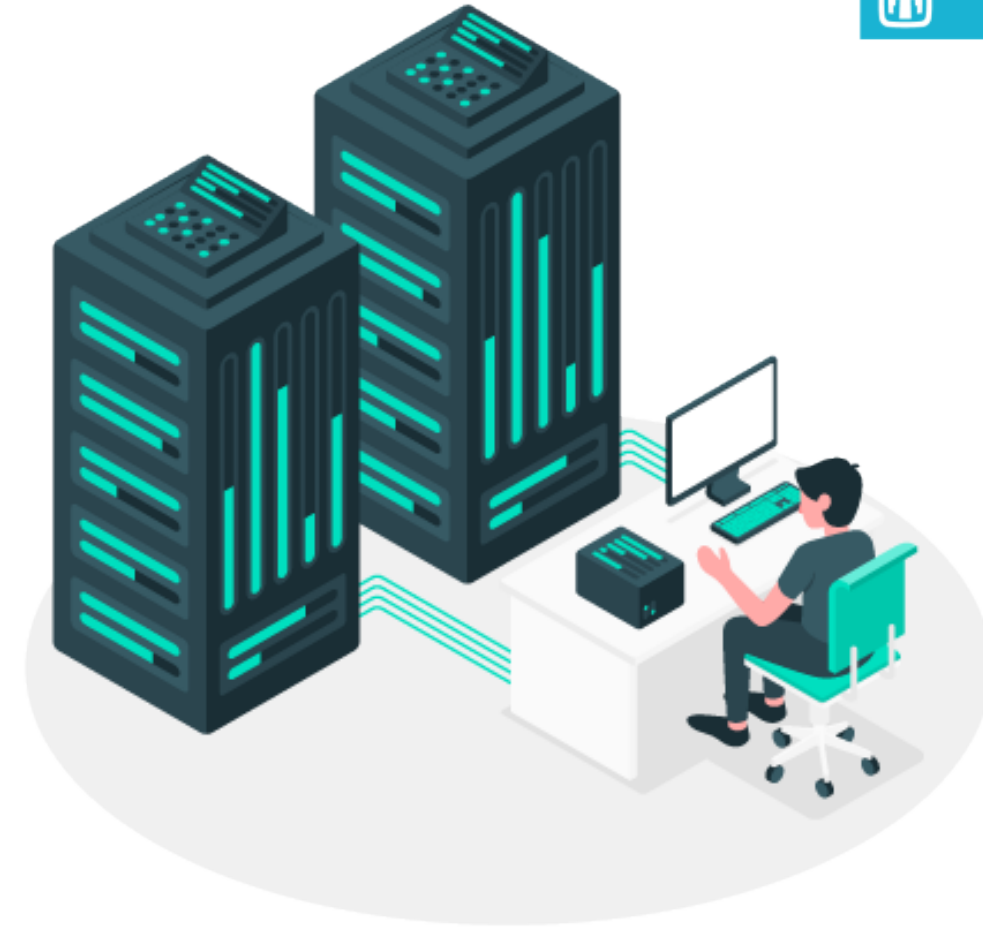
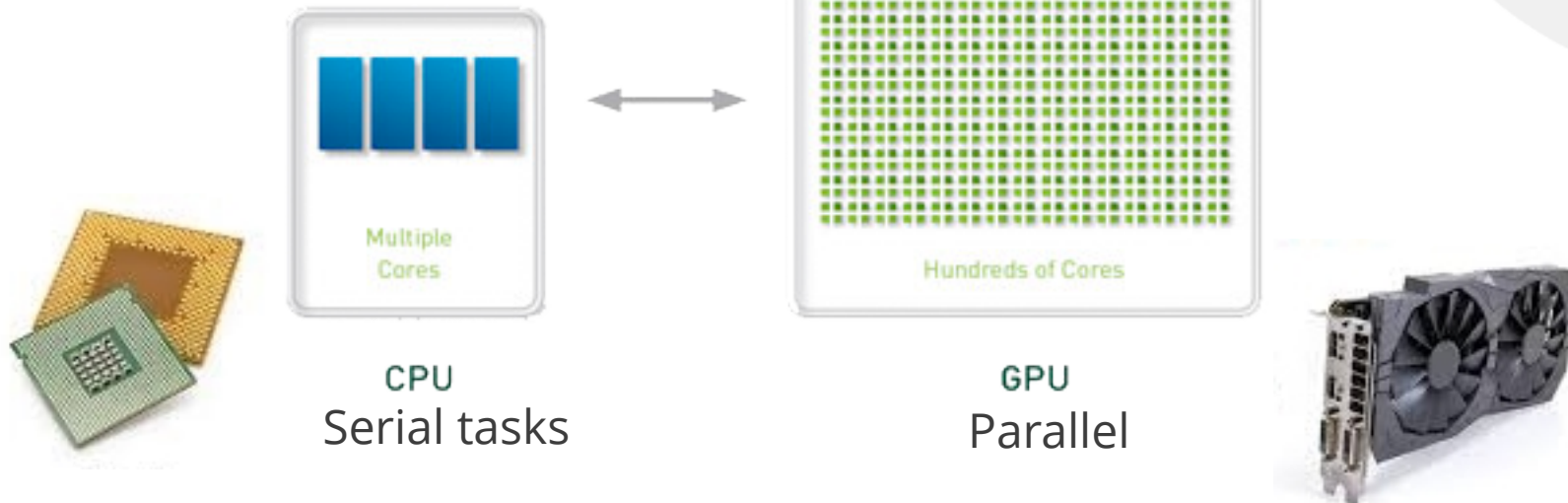
Power take-off (PTO)

PEARL

Propulsion
power management
satellite communications

Same code should run in

- Personal computer
- HPC
- GPUs
- Cloud-computing



Julia

- Two-language problem
- Open source like Python, scientific computing like Matlab
- Large state-of-the art scientific computing, scientific machine learning, and optimization
- Differentiability
- Portability

Examples

- ARPA-E offshore floating wind project: MDO, differentiability
- NASA Recursat project: 15,000x speedup, PIML



Current status



- Contract with Cornell & bi-weekly meeting
- Literature review and understand different solution methods for the Greens function
- Selection of *Wu et al.* method for speed, simplicity, and ability to parallelize.
- Exploration of using splines for geometries and higher order methods for discretization.
- Initial implementation of *Wu et al.* in Julia.

Summary



- Differentiable code would enable adjoint-based multi-disciplinary optimization, advance ML, etc.
- A modern code should be portable, able to run in serial on a personal computer or parallel in a GPU cluster.
- This project is a proof of concept differentiable and portable BEM code.
- BEM is a major road block on several projects currently trying to use automatic differentiation.



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