

BEYOND
FINGERPRINTING

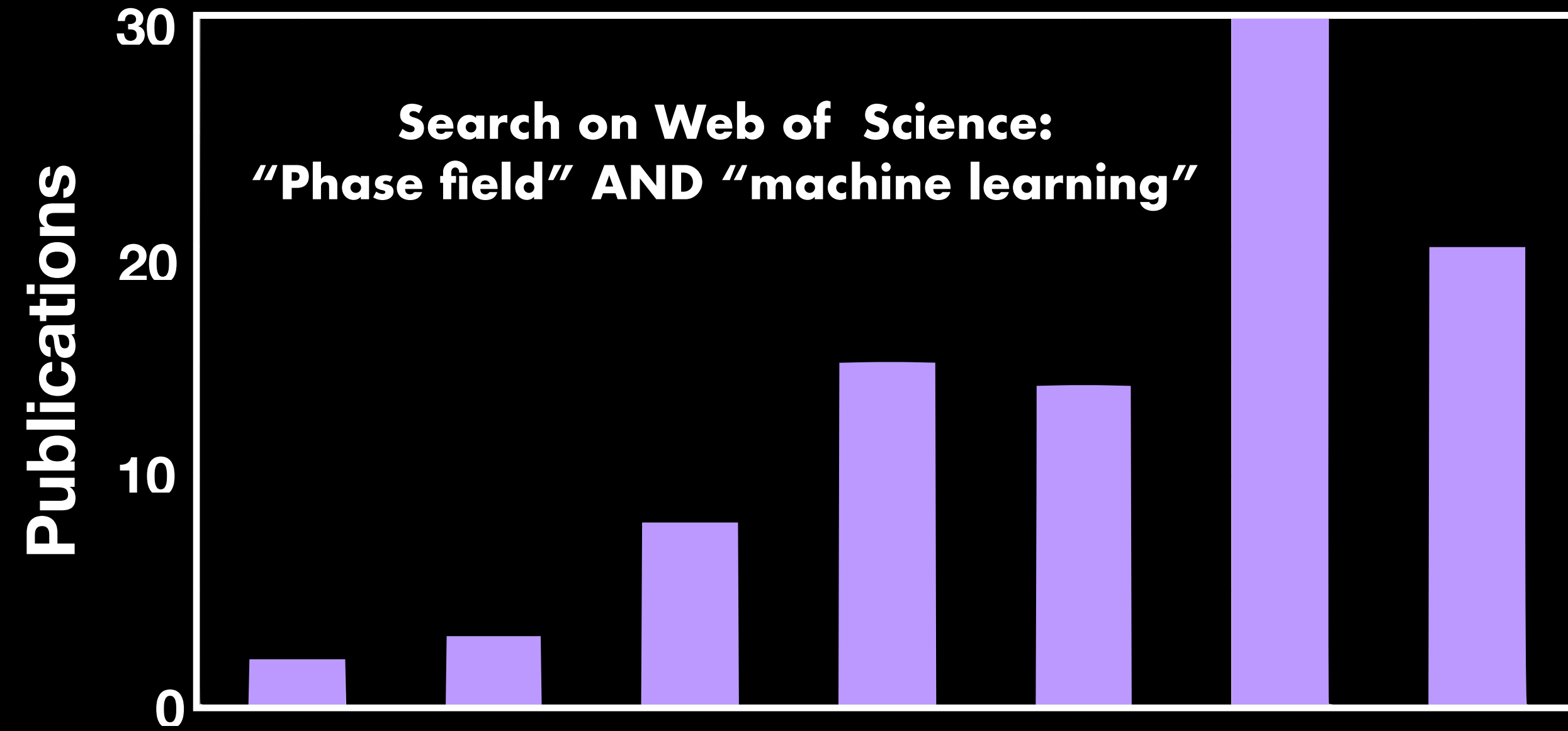
Exceptional service in the national interest

CHIMAD PHASE FIELD XV

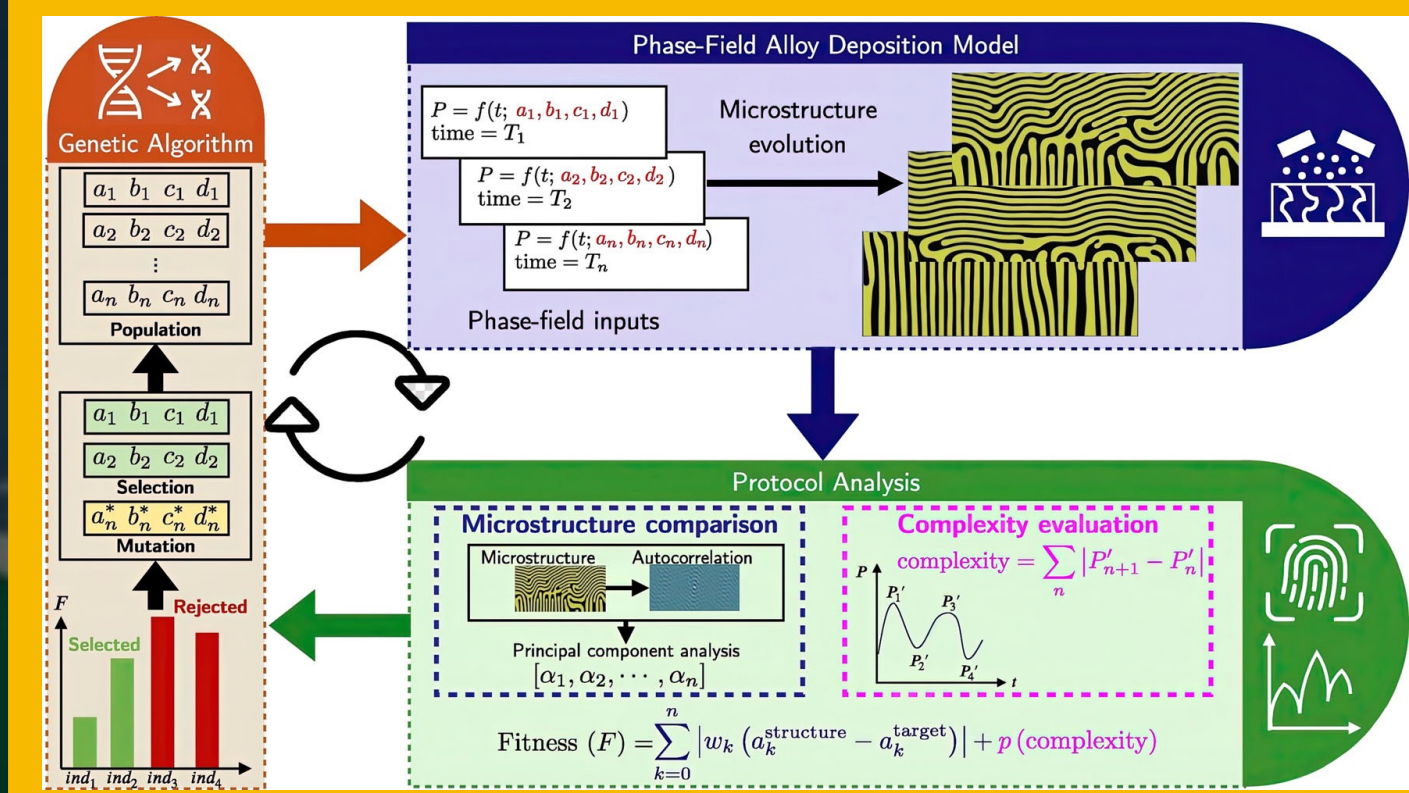
PROPOSED BENCHMARK PROBLEM FOR MACHINE-LEARNING IN PHASE FIELD

RÉMI DINGREVILLE (RDINGRE@SANDIA.GOV)
SANDIA NATIONAL LABORATORIES

OVER THE PAST 5 YEARS, ML HAS INFILTRATED THE PHASE-FIELD METHOD

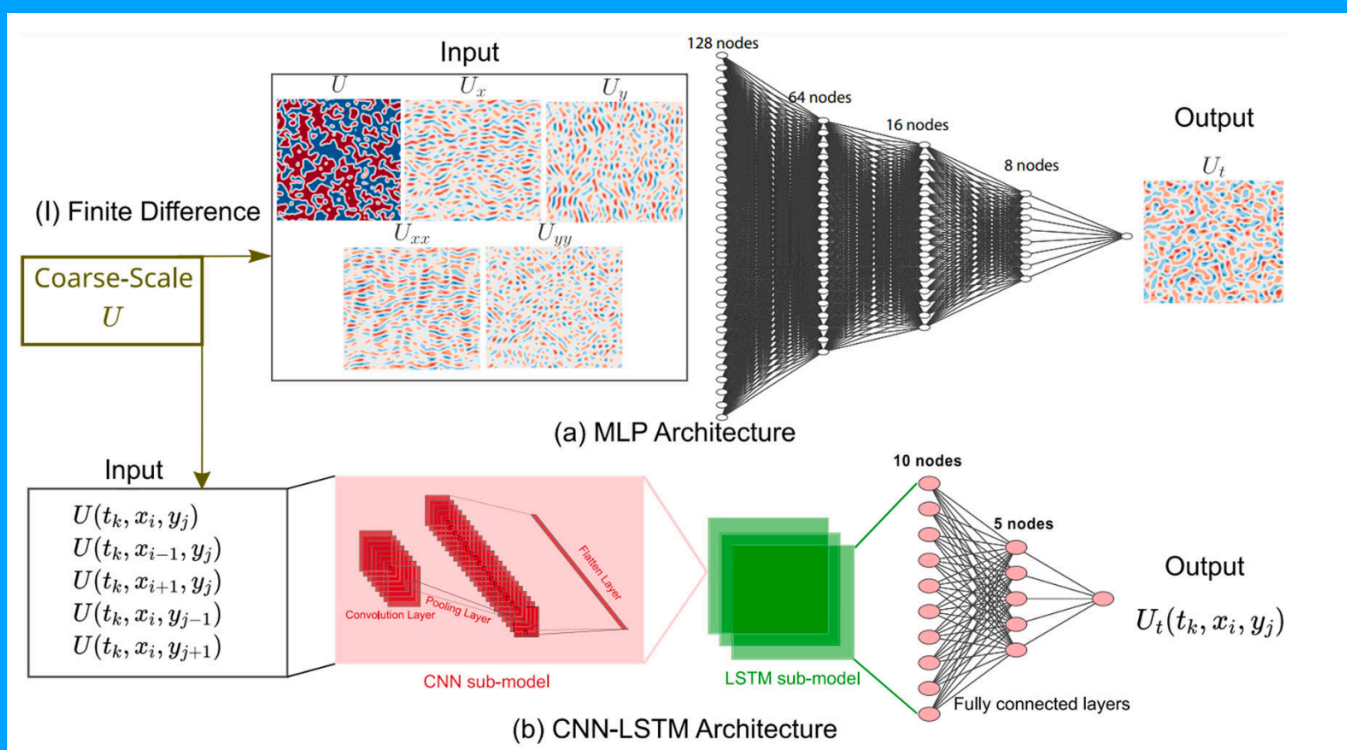


OPTIMIZATION



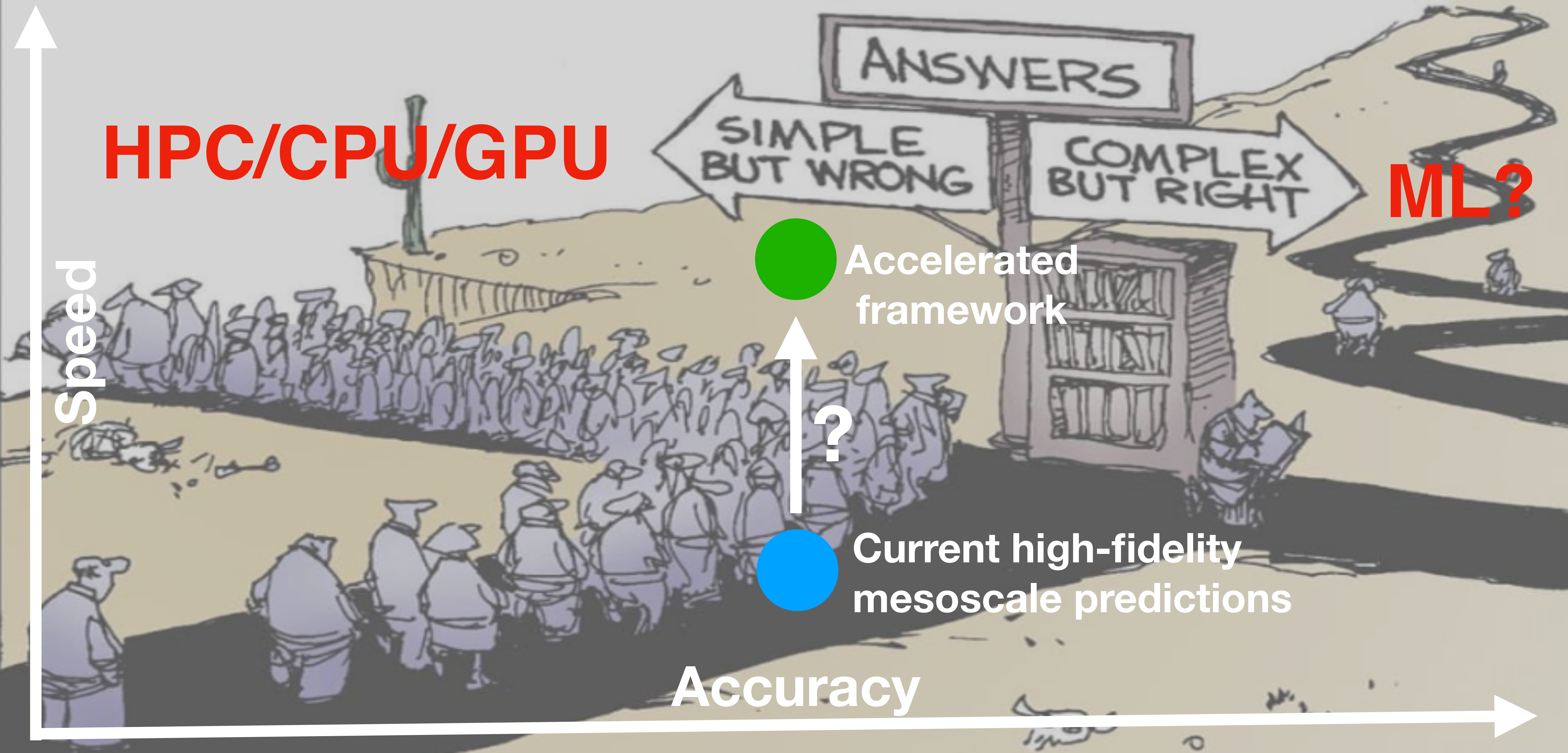
Desai et al., *Mater. Des.*, 2022

ACCELERATION

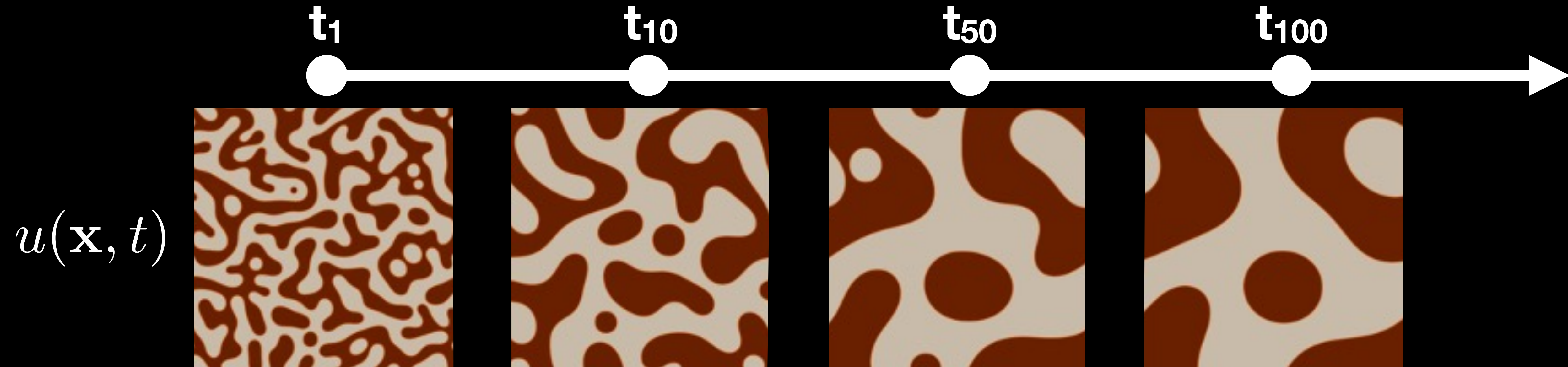


Kiyani et al., *PRE*, 2022

ARE THERE ALTERNATIVES TO MORE CPUs & PARALLELIZED NUMERICAL INTEGRATION SCHEMES?



THE STEREOTYPICAL PROBLEM

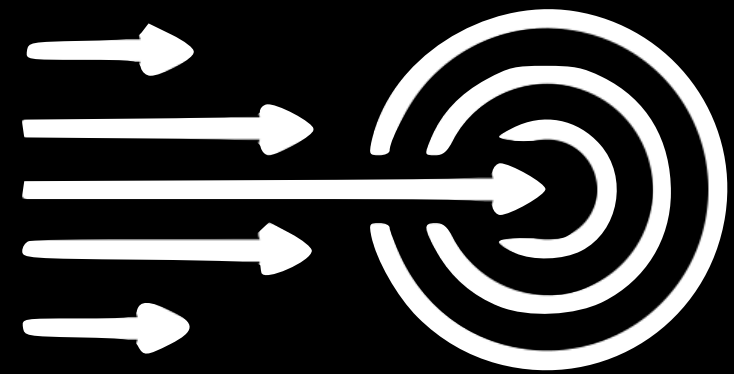


Learning a mapping function:

- History of the microstructure, $u(\mathbf{x}, t)$
- State of microstructure at time t , $\phi(\mathbf{x}, t)$

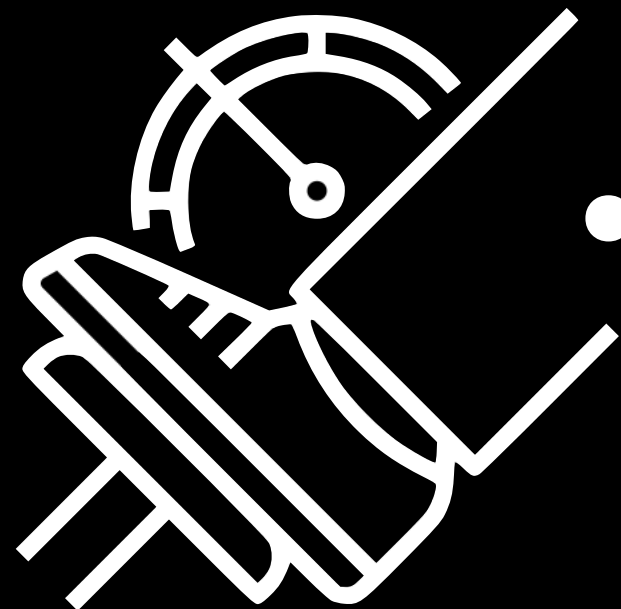
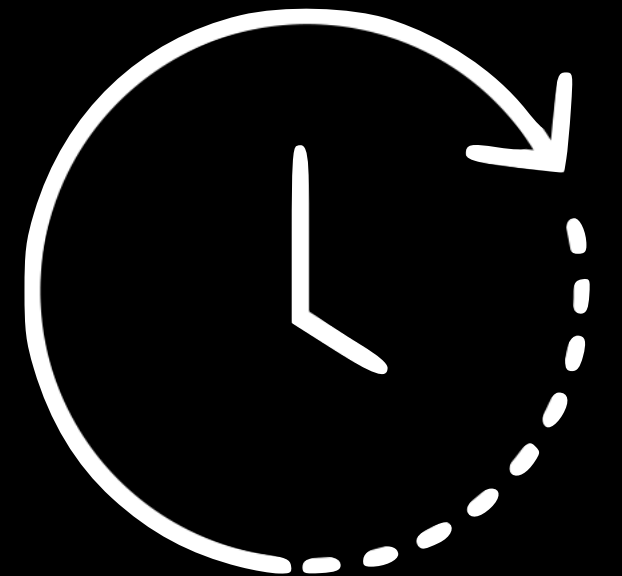
$$\mathcal{G}(u(\mathbf{x}, t)) = \phi(\mathbf{x}, t)$$

What are good metrics to evaluate the performance of a ML-based phase-field capability?



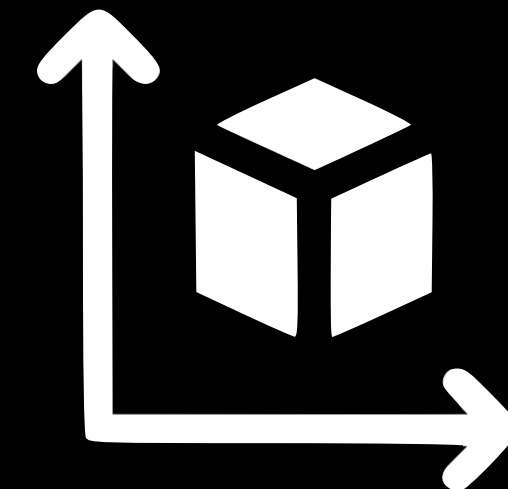
- Spatial accuracy (global vs. local)

- Time accuracy (interpolation vs. extrapolation)

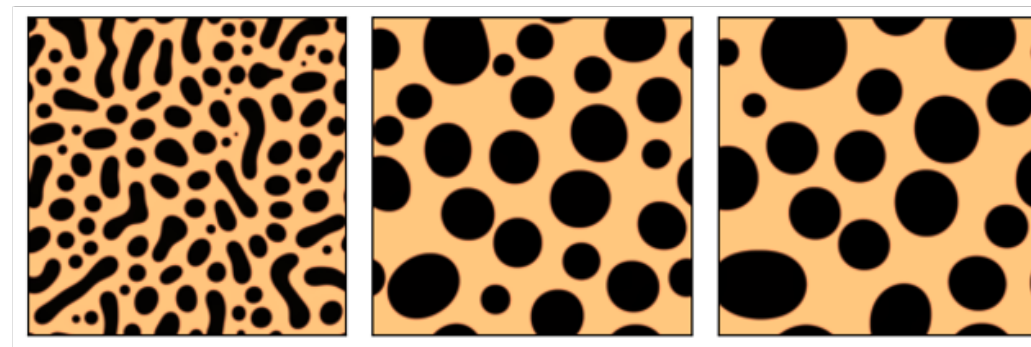


- Speed up & generalization

- Size and time required for training

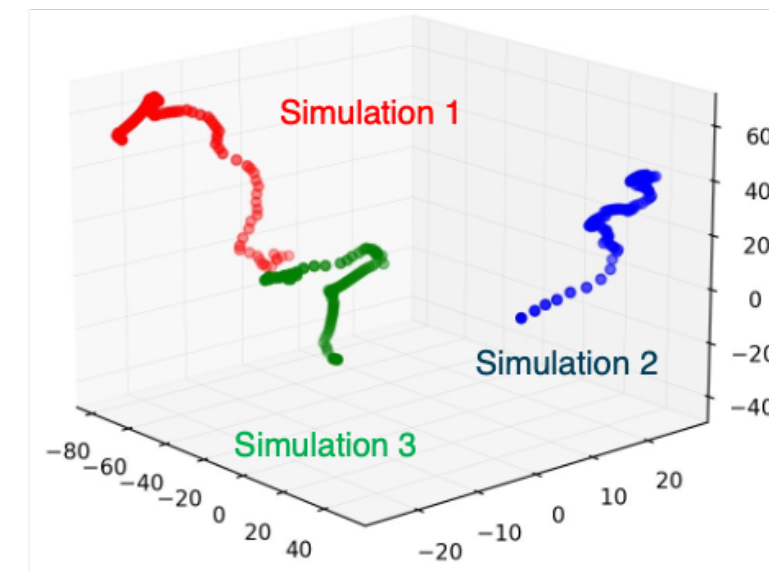


Spatial and temporal accuracies



Microstructure trajectories

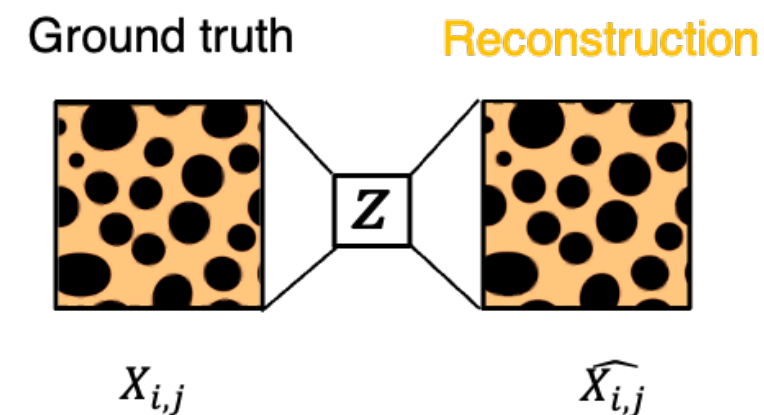
PCA
Autoencoders
Diffusion Maps



Latent dimension trajectories

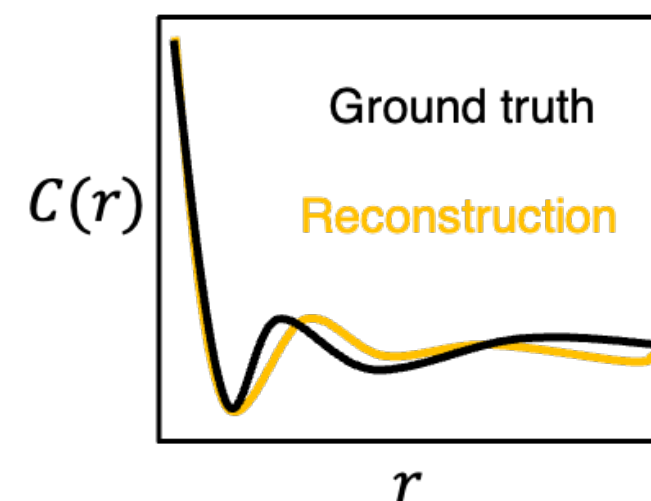
Dimensionality reduction

Global reconstruction



$$RMSE = \sqrt{\sum_i \sum_j (X_{i,j} - \hat{X}_{i,j})^2}$$

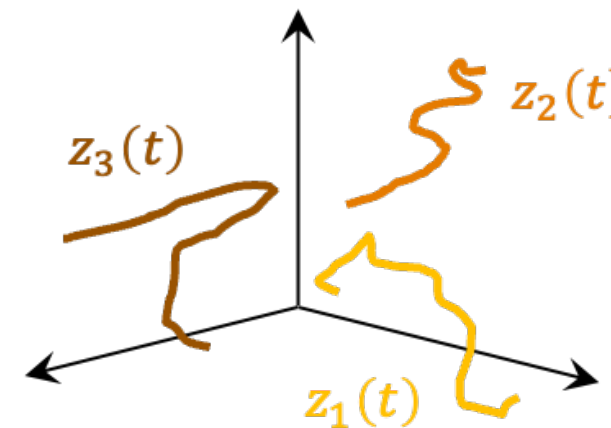
Local reconstruction



- (a) 1st minimum of $C(r)$
(b) 2nd maximum of $C(r)$

Metrics

Smoothness



- (a) $\sum_i \text{sgn}(z'_i(t)) - \text{sgn}(z'_i(t-1))$
(b) $\cos^{-1}(\overline{z'(t)} \cdot \overline{z'(t-1)})$

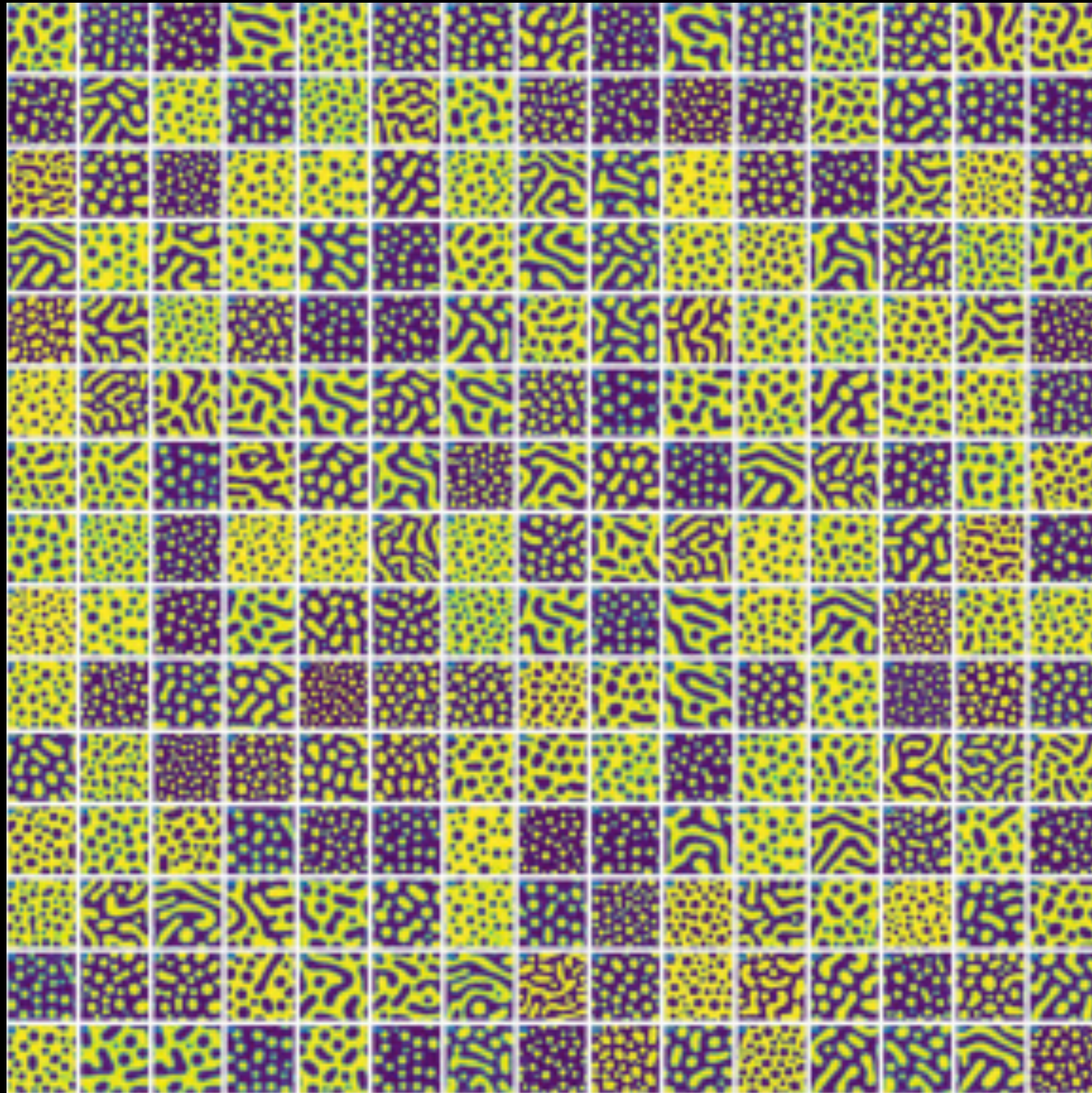
• Spatial accuracy:

- Global: RMSE on reconstruction or other image-based techniques (PSNR...)
- Local: Identification of spatial feature
- Deterministic vs. statistic characterization

• Time accuracy:

- Interpolation vs. extrapolation based on data seen during training
- Smoothness of the low-dimensional representation?

Training data: the 5 Vs



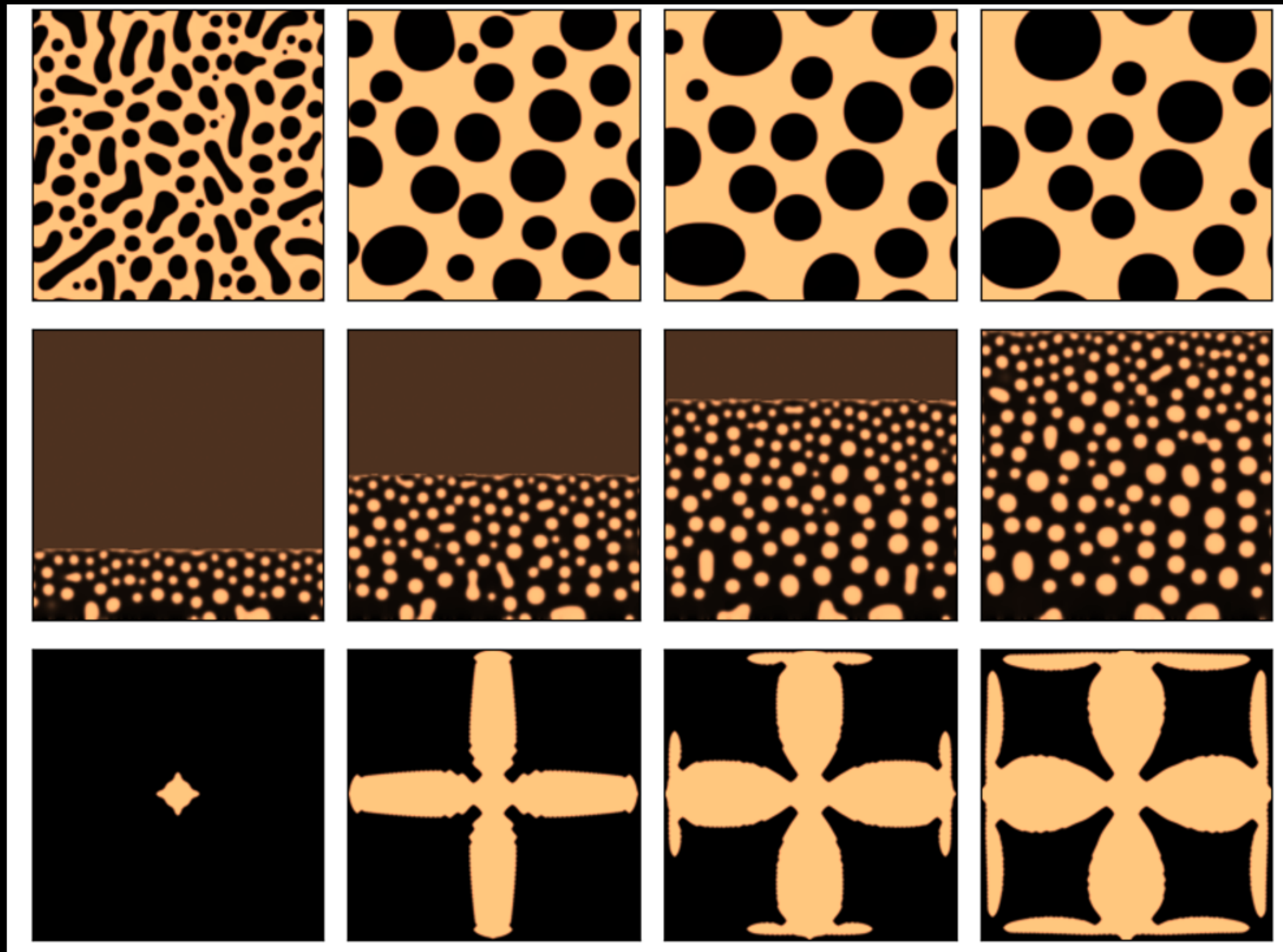
- **Volume:** when is enough enough?
- **Velocity:** how fast can we generate the training data?
- **Variety:** how to change input parameter to have enough flavor?
- **Veracity:** quality and accuracy of the training data being generated
- **Value:** how much added value do we have with one additional data point in our data set?

Speed-up and generalization...

- **CPU (parallelization) vs. GPU**
- **Interoperability:** can I use it with various PF platforms?
- **Representability (unit test):** does the ML-based model correctly represent basic features of the PF model (free energy, conservation of field variables, etc.)?



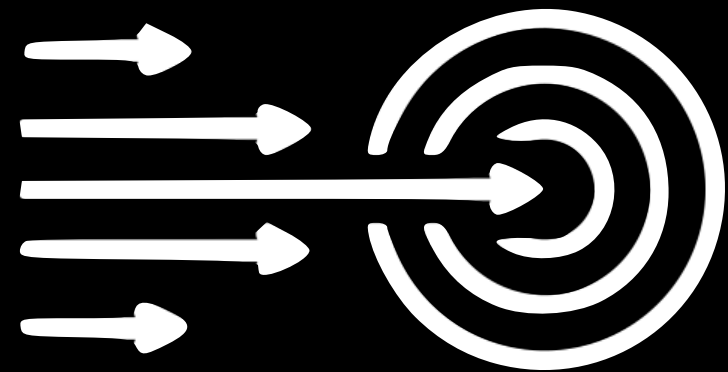
Formulation of a ML-related BM...



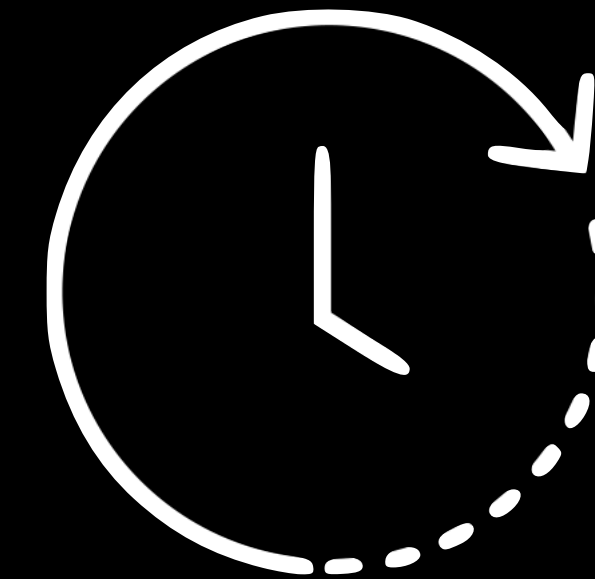
- Other?
 - Oswald ripening (BM2): coupling of conserved and non-conserved dynamics?
 - Nucleation (BM8)

- Spinodal decomposition (BM1)
 - Simple
 - Pre-existing datasets
- Physical vapor deposition
 - Pre-existing datasets
 - Moving boundary and evolving size of computational domain
- Dendrite (BM3)
 - Different length scales
 - Highly sensitive to formulation and numerical scheme

Submission guideline



- Spatial accuracy (global vs. local)
 - Reconstruction vs. time
 - Local reconstruction of specific microstructural features



- Time accuracy (interpolation vs. extrapolation)
 - Interpolation performance for within distribution
 - Extrapolation performance outside of distribution



- Speed up & generalization
 - Speedup compared to DNS
 - Free energy evolution
 - Extrapolation to unseen data?

- Size and time required for training
 - How much data has been used
 - Time and resources required for training

