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# Uncertainty in Annual Yield: Conceptual Approaches and Implementation in SAM

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# Outline



- What is uncertainty in annual yield (energy) and how is it quantified?
  - P90, i.e., 10<sup>th</sup> percentile of future annual energy
- Typical practice to calculate P90
- An alternative structured approach to uncertainty
- Quantifying uncertainty

# What is P90?



Future annual yield is uncertain: next year's weather, uncertainty in data and models

P90 is the 10<sup>th</sup> percentiles of the distribution of annual yield (energy)

Used to assess investment risk – a factor in the assessment of risk of loan repayment

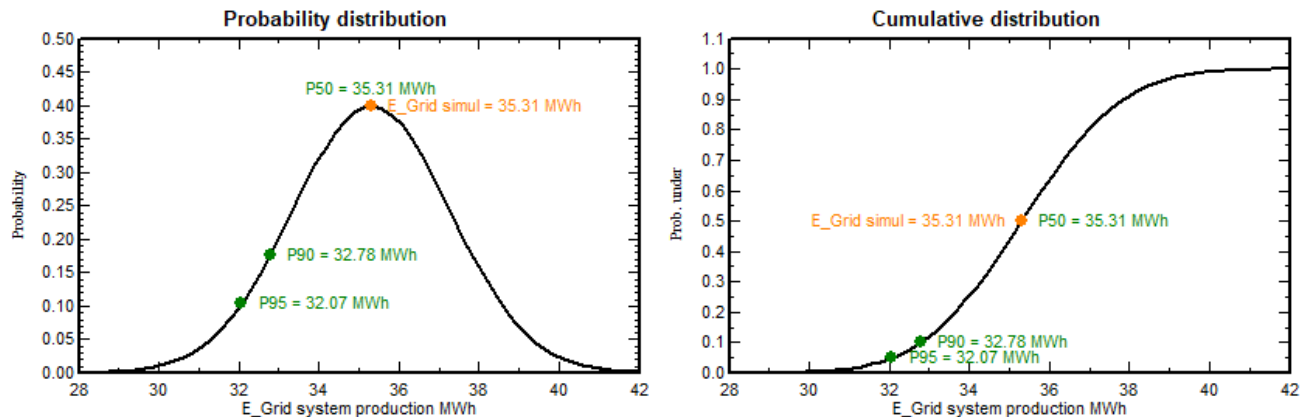


Figure courtesy of PVsyst, [https://www.pvsyst.com/help/p50\\_p90evaluations.htm](https://www.pvsyst.com/help/p50_p90evaluations.htm)

# What is P90, formally?



Future annual energy is uncertain due to uncertainty in:

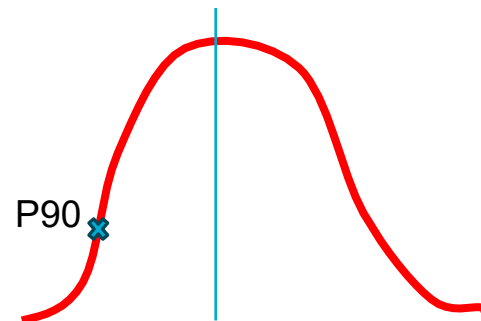
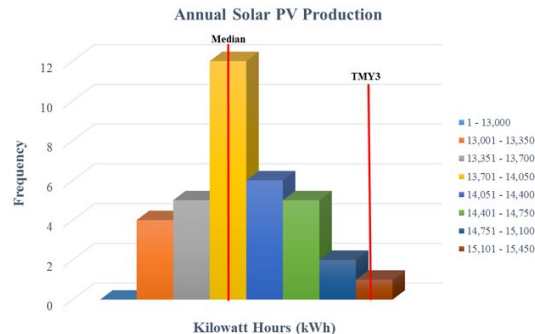
- Future weather <- **MOST SIGNiFICANT FACTOR**
- Historical weather data (when used to represent future weather) - data have measurement (or modeling) uncertainties
- Models and parameters that are used to translate weather to annual energy

Future annual energy  $Y$  is a random variable:  $Y = \sum_{t_i} f(W(t_i); \mathbf{p}) \times \Delta t_i$

- $f$  : performance model (usually a sequence of models) that translates weather  $W(t_i)$  (irradiance, temperature, wind, etc.) to power at each time  $t_i$
- $\mathbf{p}$  : a vector of parameter values for the performance model(s), e.g., module parameters at STC, surface tilt and azimuth, incident angle modifiers

# Typical practice to calculate P90 (“All-in” approach)

1. Model future weather, by assuming either:
  - A. Multiple years of historical weather
  - B. A typical year of weather
2. Select models (and parameters) and calculate yield from modeled energy
3. Account for model/data uncertainties
  - A. Form a distribution with the “typical” annual energy as a central value
  - B. “Widen” the distribution using a variance



$\sigma = \sqrt{\sum_k \sigma_k^2}$ , where  $\sigma_k$  is the variance of annual energy attributable to some source of uncertainty

<https://eepower.com/technical-articles/understanding-the-role-of-uncertainty-in-pv-energy-production>  
<https://solargis.com/blog/best-practices/how-to-calculate-p90-or-other-pxx-pv-energy-yield-estimates>  
[https://www.pvsyst.com/help/p50\\_p90evaluations.htm](https://www.pvsyst.com/help/p50_p90evaluations.htm)

# Challenge and Consequences of the “all-in” approach

How does one enumerate and quantify the variances  $\sigma_k$  ?

- Units of annual energy
- Typical  $\sigma_k$  :
  - Variance in annual energy from weather variability
  - Uncertainty of models?
- Assumed to be “independent”

P90 conflates risk from future weather with uncertainty in models and data

- The P90 value is not uncertain, only imprecise
- “All-in” provides no basis for quantifying the lack of precision in P90
- Difficult to judge the value of reducing epistemic uncertainties

# A structured approach to uncertainty

**Aleatory** (*inherent, random*) uncertainty that cannot (practically) be reduced by better measurements or models

- Future weather is inherently variable and (at some precision) unknowable

**Epistemic** (*state-of-knowledge*) uncertainty that could, in principle, be reduced by more accurate measurements, better models, more data, etc.

- E.g., a temperature coefficient could be known more precisely with more data, or, variation among PV modules could be quantified with more testing.

Commonly used in environmental and engineering risk assessments

# Structured uncertainty yields same P90 but with more information

Models and data are epistemic uncertainties

Future weather is an *aleatory* uncertainty

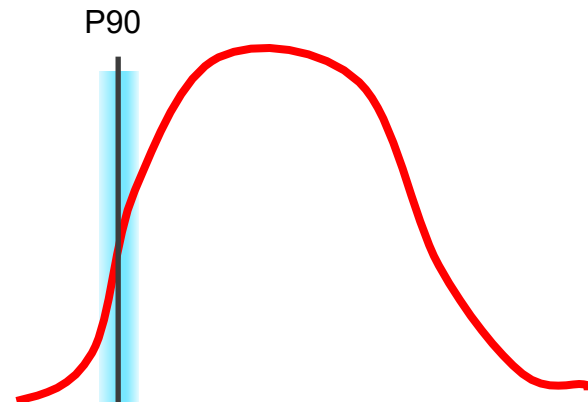
$$Y = \sum_{t_i} f(W(t_i); \mathbf{p}) \times \Delta t_i$$

Can compute a distribution of annual energy considering only uncertainty in future weather, **conditional** on models, parameters, and data

- Expresses risk of not meeting energy yield (revenue) due to future weather

Can compute a “best” estimate with uncertainty resulting from incomplete models and data

- The value of improving models and data can be quantified

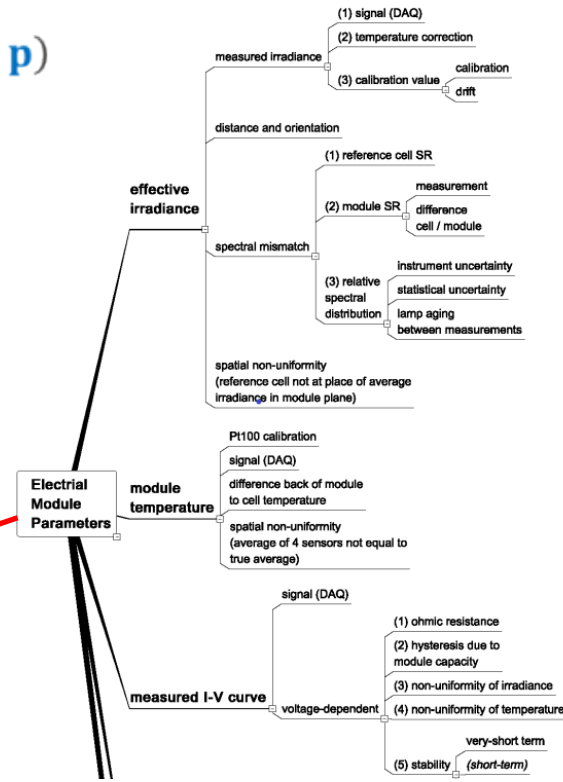
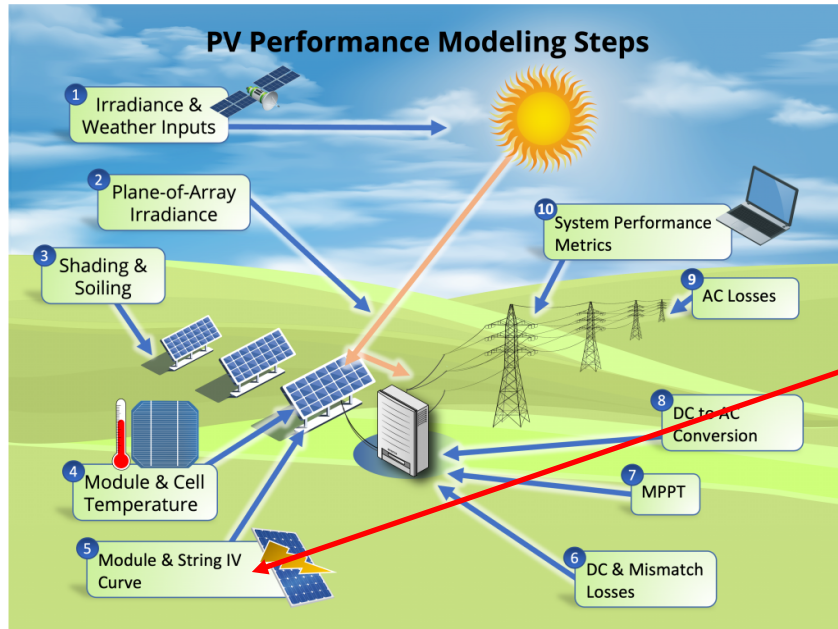




# Quantifying epistemic (model, parameter) uncertainty

Quantify uncertainty in each component of  $f(W; p)$

“Bottom-up approach” is impractical



D. Dirnberger and U. Kräling (2013)  
doi: 10.1109/JPHOTOV.2013.2260595.

# Top down “annual energy factors” approach

“Annual factors” approach recommended by IEA PVPS Task 13 <sup>1</sup>

Combined with the structured approach for uncertainty (implemented in SAM) <sup>2</sup>

Annual variability in weather is separated from all other uncertainties

- For each year of weather  $W$  :

- “Base” annual energy  $\bar{Y}$  ( using “best estimate” models)

$$\bar{Y}(W) = f(W; p)$$

- Apply a set of “uncertainty factors”  $F_k$  to generate a distribution  $Y$  of annual energy

$$Y(W) = \bar{Y} \times \prod_k (1 - F_k)$$

- Repeat for all years  $W$  (e.g., when using historical data)

1. “Uncertainties in PV System Yield Predictions and Assessments”, Reise et al. (2018), IEA-PVPS T13-12:2018

[https://iea-pvps.org/wp-content/uploads/2020/01/Uncertainties\\_in\\_PV\\_System\\_Yield\\_Predictions\\_and\\_Assessments\\_by\\_Task\\_13.pdf](https://iea-pvps.org/wp-content/uploads/2020/01/Uncertainties_in_PV_System_Yield_Predictions_and_Assessments_by_Task_13.pdf)

2. “Quantifying Uncertainty in PV Energy Estimates Final Report”, Prilliman et al. (2023), NREL/TP-7A40-84993

<https://www.nrel.gov/docs/fy23osti/84993.pdf>

# What are “uncertainty factors”?

Each  $F_k$  quantifies uncertainty in the base annual energy from some component model or parameter in the performance model chain.

- $F_k$  has units of fraction of annual energy
- By convention,  $F_k$  is a “loss”, i.e.,  $F_k = 0.03$  means a 3% reduction in annual energy
- Each  $F_k$  should be “independent”

$F_k$  are not easy to quantify, e.g., factor for uncertainty in measured GHI (Hansen and Scheiner, 2022)

Perhaps easier than  $\sigma_k$  (prove me wrong)

E.g., Module rating  $F_k = N(0, 0.5)$

Bias

Variance

Table 1. SAM Default Distributions for Uncertainty Factors

Factor	Distribution type	Parameters
Irradiance transposition	Normal	$\mu = 11.5, \sigma = 2.5$
Horizon shading	Triangular	min.= -1, mode=0, max.=0
Row shading	Triangular	min.= -5, mode= -1, max.=0
Single module rating at STC	Normal	$\mu = 0, \sigma = 2.0$
Inverter availability	Triangular	min.= -5.7, mode= -2.70, max.=0
Spectral response	Normal	$\mu = -1, \sigma = 0.5$
Cell temperature	Normal	$\mu = -2.4, \sigma = 1.0$
Mismatch loss	Triangular	min.= -1.8, mode= -0.8, max.=0
DC wiring	Triangular	min.= -2.5, mode= -1.5, max.= -1
Transformer	Triangular	min.= -2, mode= -1, max.= -0.5
Soiling	Triangular	min.= -1.5, mode= -0.5, max.=0

SAM defaults derived from Reise et al. (2018), IEA-PVPS T13-12:2018

# Conceptual implementation in SAM



“All-in” P90

“=“

Weather risk

“+“

Uncertainty in P90

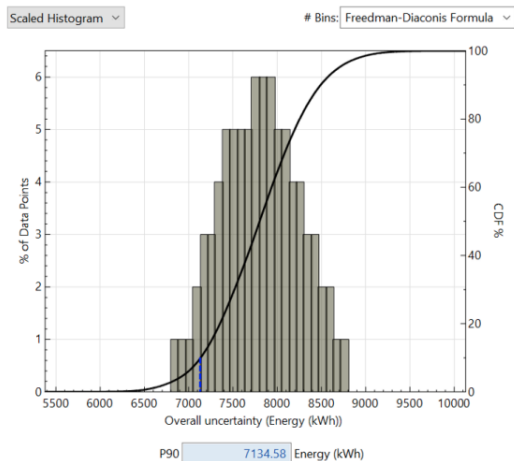


Figure 1. Combined uncertainty graph from SAM uncertainty tool

“=“

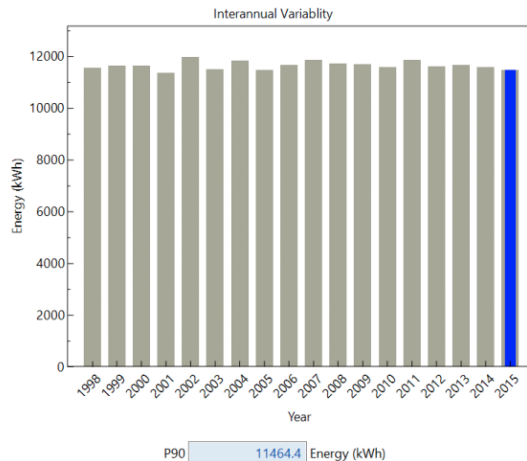


Figure 2. Weather uncertainty graph from SAM uncertainty tool

“+“

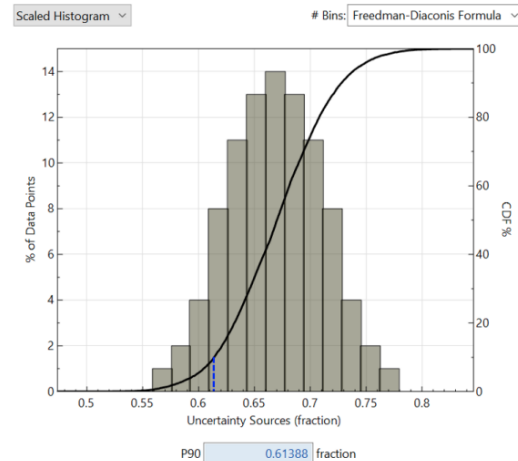


Figure 3. Uncertainty factor graph from SAM uncertainty tool

# Summary



Separating weather and other uncertainties:

- Gives same P90
- Quantifies the relative influences of weather variability and model/data uncertainty
- Perhaps easier to quantify annual factors than components of variance