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**Model Documentation**

**Natural Gas Transmission and Distribution  
Model**

**of the National Energy Modeling System**

**Volume I**

**January 1996**

**Prepared by:**

**Oil and Gas Analysis Branch  
Energy Supply and Conversion Division  
Office of Integrated Analysis and Forecasting  
Energy Information Administration**

**MASTER**

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## For Further Information...

The Natural Gas Transmission and Distribution Model (NGTDM) of the National Energy Modeling System is developed and maintained by the Energy Information Administration (EIA), Office of Integrated Analysis and Forecasting. General questions concerning the NGTDM may be addressed to James S. Diemer (202/586-6126), Natural Gas Transmission and Distribution Project Leader. Documentation questions should be addressed to Joe Benneche (202/586-6132).

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This report documents the archived version of the NGTDM that was used to produce the natural gas forecasts presented in the *Annual Energy Outlook 1996*, (DOE/EIA-0383(96)). The purpose of this report is to provide a reference document for model analysts, users, and the public that defines the objectives of the model, describes its basic approach, and provides detail on the methodology employed. Previously this report represented Volume I of a two-volume set. Volume II reported on model performance, detailing convergence criteria and properties, results of sensitivity testing, comparison of model outputs with the literature and/or other model results, and major unresolved issues.

The model documentation is updated annually to reflect significant model methodology and software changes that take place as the model develops. The next version of the documentation is planned to be released in the first quarter of 1997.

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# 1. Introduction

The Natural Gas Transmission and Distribution Model (NGTDM) is the component of the National Energy Modeling System (NEMS) that is used to represent the domestic natural gas transmission and distribution system. NEMS was developed in the Office of Integrated Analysis and Forecasting of the Energy Information Administration (EIA). NEMS is the third in a series of computer-based, midterm energy modeling systems used since 1974 by the EIA and its predecessor, the Federal Energy Administration, to analyze domestic energy-economy markets and develop projections. From 1982 through 1993, the Intermediate Future Forecasting System (IFFS) was used by the EIA for its analyses, and the Gas Analysis Modeling System (GAMS) was used within IFFS to represent natural gas markets. Prior to 1982, the Midterm Energy Forecasting System (MEFS), also referred to as the Project Independence Evaluation System (PIES), was employed.

NEMS was developed to enhance and update EIA's modeling capability by internally incorporating models of energy markets that had previously been analyzed off-line. In addition, greater structural detail in NEMS permits the analysis of a broader range of energy issues. The time horizon of NEMS is the midterm period (i.e., through 2015).<sup>1</sup> In order to represent the regional differences in energy markets, the component models of NEMS function at regional levels appropriate for the markets represented, with subsequent aggregation/disaggregation to the Census Division level for reporting purposes.

The projections in NEMS are developed using a market-based approach<sup>2</sup> to energy analysis, as had the earlier models. For each fuel and consuming sector, NEMS balances energy supply and demand, accounting for the economic competition between the various fuels and sources. NEMS is organized and implemented as a modular system.<sup>3</sup> The NEMS models represent each of the fuel supply markets, conversion sectors, and end-use consumption sectors of the energy system. NEMS also includes macroeconomic and international models. The primary flows of information between each of these models are the delivered prices of energy to the end user and the quantities consumed by product, Census Division, and end-use sector. The delivered prices of fuel encompass all the activities necessary to produce (or import), and transport fuels to the end user. The information flows also include other data such as economic activity, domestic production activity, and international petroleum supply availability.

An integrating routine controls the execution of each of the component models. The modular design provides the capability to execute models individually, thus allowing independent analysis with, as well as development of, individual models. This modularity allows the use of the methodology and level of detail most appropriate for each energy sector. NEMS solves by iteratively calling each model in sequence until the delivered prices and quantities of each fuel in each region have converged within tolerance both within individual models and between the various models, thus achieving an economic equilibrium of supply and demand in the consuming sectors. Model solutions are reported annually through the midterm horizon. A schematic of the NEMS is provided in Figure 1-1, while a list of the associated model documentation reports is in Appendix C.

The NGTDM is the model within the NEMS that represents the transmission, distribution, and pricing of natural gas. The model also includes representations of the end-use demand for natural gas, the production of domestic natural gas, and the availability of natural gas traded on the international market based on information received from other NEMS models. The NGTDM determines the flow of natural gas in an aggregate, domestic pipeline network, connecting domestic and foreign supply regions with 12 demand regions. The methodology employed allows the analysis of impacts of regional capacity constraints in the interstate natural gas pipeline network and the identification of primary pipeline capacity expansion requirements. There is an explicit representation of core and noncore markets

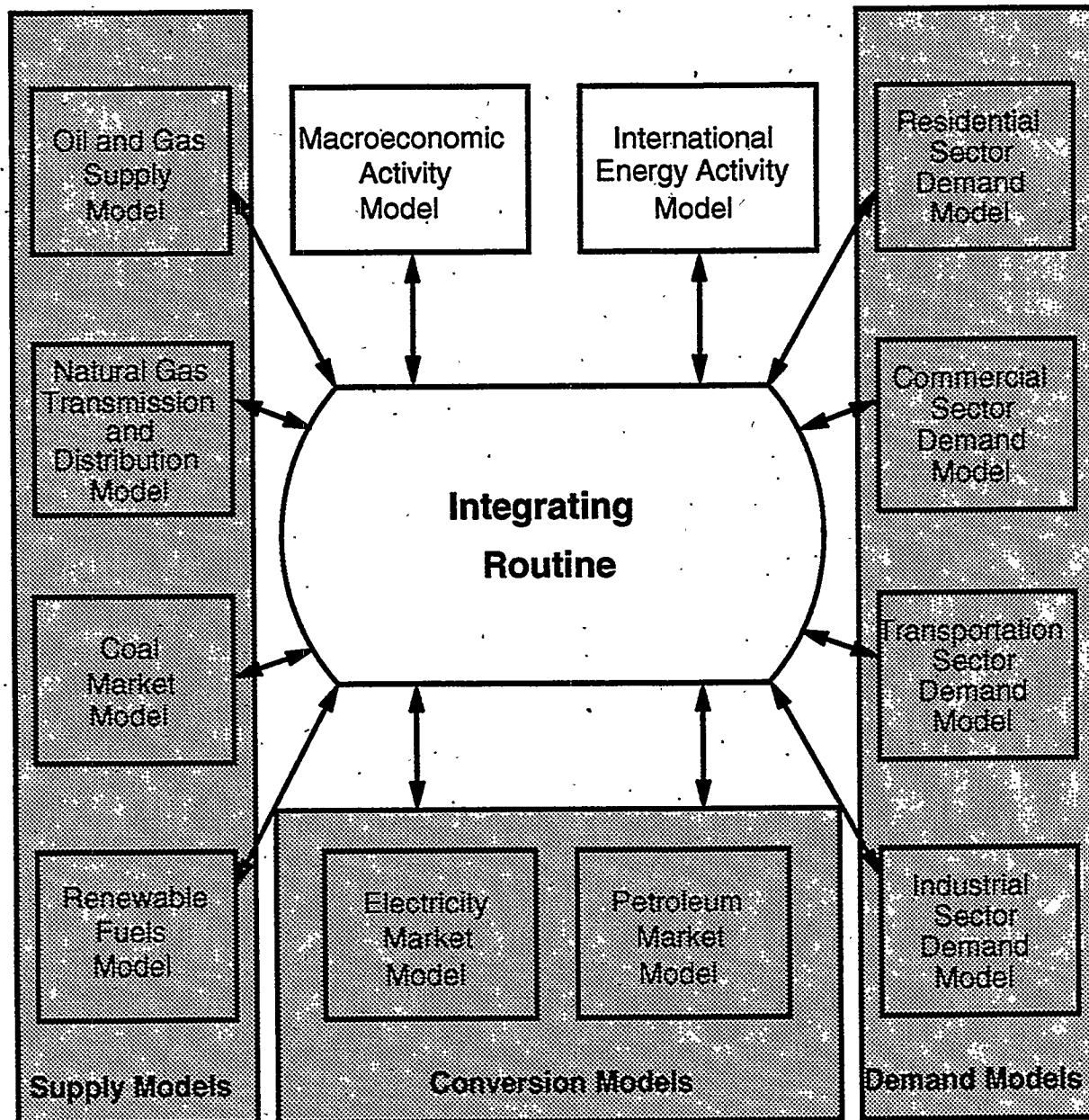
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<sup>1</sup>For the *Annual Energy Outlook 1996* the NEMS was executed for each year from 1990 through 2015.

<sup>2</sup>The central theme of a market-based approach is that supply and demand imbalances will eventually be rectified through an adjustment in prices that eliminates excess supply or demand.

<sup>3</sup>The NEMS is composed of 13 models and a system integration routine. These components are frequently referred to as "modules" in other NEMS related publications; however, in this publication they will all be referred to as "models." Footnotes will be added when the formal name is different from the referenced name. The components of the NGTDM will be referred to as "modules."

**Figure 1-1. Schematic of the National Energy Modeling System**



for natural gas transmission and distribution services, and the key components of pipeline tariffs are represented in a pricing algorithm. Natural gas pricing and flow patterns are derived by obtaining a market equilibrium across the three main elements of the natural gas market: the supply element, the demand element, and the transmission and distribution network that links them. The NGTDM consists of four modules: the Annual Flow Module, the Capacity Expansion Module, the Pipeline Tariff Module, and the Distributor Tariff Module. A model abstract is provided in Appendix A.

This report documents the archived version of the NGTDM that was used to produce the natural gas forecasts used in support of the *Annual Energy Outlook 1996*, DOE/EIA-0383(96). The purpose of this report is to provide a reference document for model analysts, users, and the public that defines the objectives of the model, describes its basic design, provides detail on the methodology employed, and describes the model inputs, outputs, and key assumptions. It is intended to fulfill the legal obligation of the EIA to provide adequate documentation in support of its models (Public Law 94-385, Section 57.b.2).

This report represented Volume I of a two-volume set. Volume II reported on model performance, detailing convergence criteria and properties, results of sensitivity testing, comparison of model outputs with the literature and/or other model results, and major unresolved issues. A second volume will not be produced for the *Annual Energy Outlook 1996*. Subsequent chapters of this report provide:

- An overview of the NGTDM (Chapter 2)
- A description of the interface between the NEMS and the NGTDM (Chapter 3)
- An overview of the solution methodology of the NGTDM (Chapter 4)
- The solution methodology for the Annual Flow Module (Chapter 5)
- The solution methodology for the Distributor Tariff Module (Chapter 6)
- The solution methodology for the Capacity Expansion Module (Chapter 7)
- The solution methodology for the Pipeline Tariff Module (Chapter 8)
- A description of model assumptions, inputs, and outputs (Chapter 9).

The archived version of the model is available from the National Energy Information Center (NEIC) and is identified as NEMS96 (part of the National Energy Modeling System archive package as archived for the *Annual Energy Outlook 1996*, DOE/EIA-0383(96)).

The document includes extensive appendices to support the material presented in the main body of the report. Appendix A presents the model abstract. Appendix B lists the major references used in developing the NGTDM. Appendix C lists the various NEMS Model Documentation Reports that are cited throughout the NGTDM documentation. Appendix E provides a mapping between the model variables which are assigned values through READ statements in the model and the data input files that are read. In addition these files contain detailed descriptions of the input data, including variable names, definitions, sources, units and derivations.<sup>4</sup> Appendix F documents the derivation of all empirical estimations used in the NGTDM. Variable cross reference tables are provided in Appendix G. A mapping of equations presented in the documentation to the relevant subroutine in the code is provided in Appendix H. Lastly, Appendix I documents the switches that have been built into the model to conduct automated sensitivity analysis.

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<sup>4</sup>A PC diskette with these data files is available upon request by contacting Joe Benneche (202) 586-6132.



## 2. Overview

The purpose of this chapter is to provide a brief overview of the Natural Gas Transmission and Distribution Model (NGTDM) and its capabilities. The NGTDM is the component of the National Energy Modeling System (NEMS) that represents the mid-term natural gas market. The NGTDM models the natural gas transmission and distribution network in the Lower 48 States that links the suppliers (including importers) and consumers of natural gas, thus determining the regional market clearing natural gas end-use and supply (including border) prices. The demand regions modeled are the 12 NGTDM regions (Figure 2-1). These regions are based on the 9 Census Divisions, with Census Division 5 split into South Atlantic and Florida, Census Division 8 split into Mountain and Arizona/New Mexico, Census Division 9 split into California and Pacific, and Alaska and Hawaii handled independently. Forecasts are reported annually through 2015 for natural gas end-use prices in the residential, commercial, industrial, electric generation, and transportation sectors.

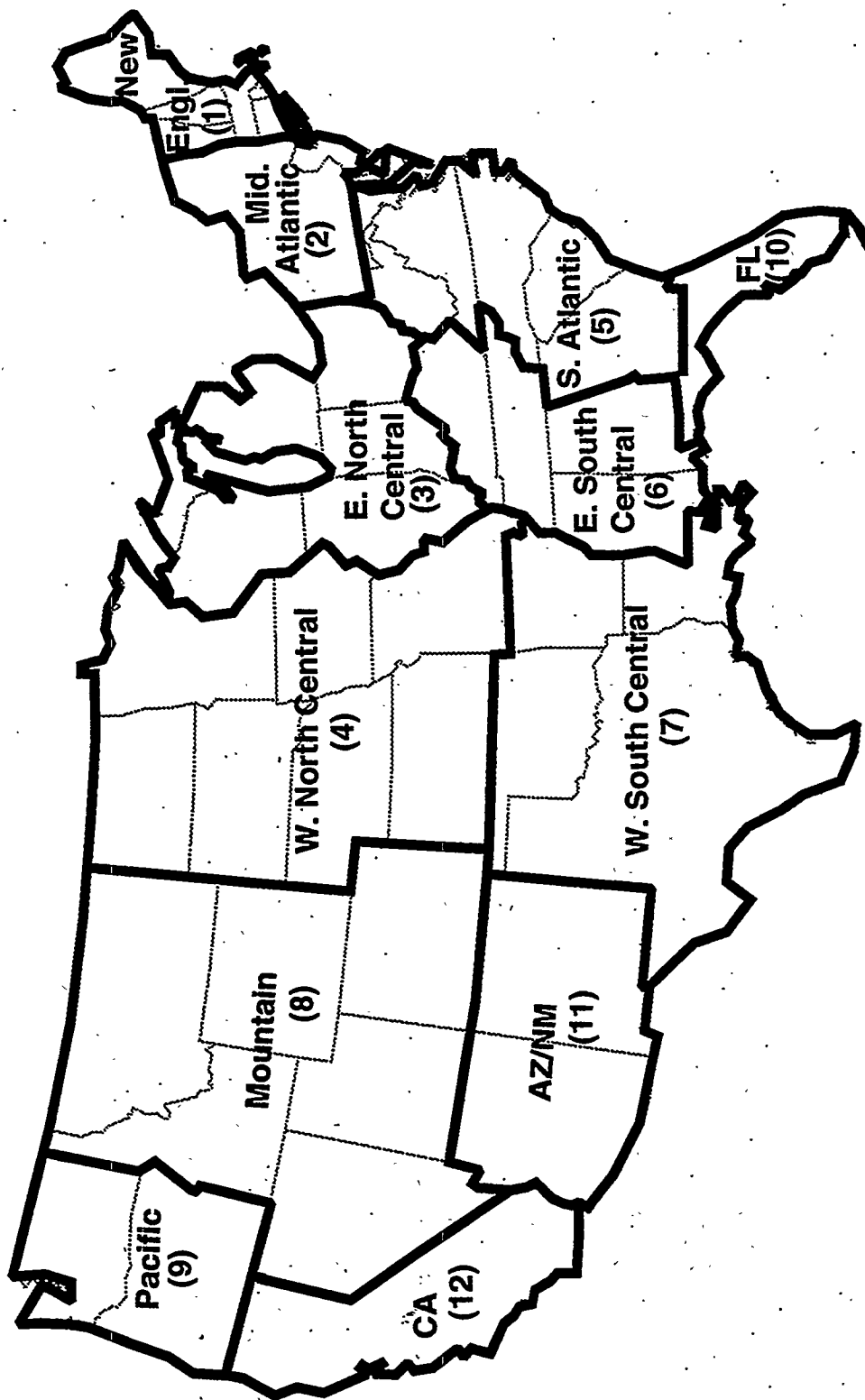
The model structure consists of four major components. The Annual Flow Module (AFM) is the integrating module of the NGTDM. It simulates the natural gas price determination process by bringing together all major economic and technological factors that influence regional natural gas trade in the United States. The Capacity Expansion Module (CEM) forecasts the development of new natural gas pipeline and storage facilities and sets maximum annual utilization rates based on a seasonal analysis of supply capabilities and demand requirements. The Pipeline Tariff Module (PTM) represents the development of firm/interruptible tariffs for transportation and storage services provided by interstate pipeline companies. The Distributor Tariff Module (DTM) represents the development of markups for distribution services provided by local distribution companies and for transmission services provided by intrastate pipeline companies. The modeling techniques employed are linear programs for the AFM and the CEM, an accounting algorithm for the PTM, and a largely empirical process based on historical data for the DTM.

The NGTDM provides a number of key modeling capabilities that were not available in its predecessor model, the Gas Analysis Modeling System (GAMS). These capabilities give the NGTDM the ability to:

- Represent interregional flows of gas and pipeline capacity constraints
- Represent regional supplies
- Represent different types of transmission service (firm and interruptible)
- Calculate emissions associated with pipeline fuel use
- Determine the amount and the location of additional pipeline and storage facilities on a regional basis
- Capture the economic tradeoffs between pipeline capacity additions and increases in regional storage capability
- Provide a peak/off-peak, or seasonal analysis capability in the area of capacity expansion
- Quantify capital investment in capacity expansion
- Distinguish customers by category (core and noncore) in end-use sectors.

These capabilities will be described in greater detail in the subsequent chapters of this report which describe the individual modules of the NGTDM.

Figure 2-1. Natural Gas Transmission and Distribution Model (NGTDM) Regions





## Model Objectives

The purpose of the NGTDM is to derive natural gas end-use and wellhead prices and flow patterns for movements of natural gas through the regional interstate network. The prices and flow patterns are derived by obtaining a market equilibrium across the three main elements of the natural gas market: the supply element, the demand element, and the transmission and distribution network that links them. The domestic supply, imports, and demand representations are provided as inputs to the NGTDM from other National Energy Modeling System (NEMS) modules. The representations of the key features of the transmission and distribution network, which include interregional network capacities and transmission and distribution service pricing, are the focus of the various components of the NGTDM.

The need to model these specific characteristics of the natural gas industry stems from the structural changes that have taken place in the industry over the last 10 years. These changes include complete deregulation of the wellhead market, the unbundling of pipeline services, and the introduction of competitive forces related to pipeline expansion decisions, and transmission and distribution service pricing. Some of these changes have already had a large effect on the market, while other changes have recently been initiated and have yet to provide a significant impact on the prices and availability of services. Two key factors support the need to include an explicit representation of the transmission and distribution of natural gas within NEMS. The first is the substantial decline in wellhead prices which results in the acquisition cost of the commodity itself generally being less than half of the end-use price. The second is the ongoing evolution of the market. This ongoing evolution also supports the need for significant flexibility in how prices for transmission and distribution services are represented in the NGTDM and how the interregional flows respond to prices over time. Because of this, the NGTDM is a completely new system that provides, in addition to mid-term forecasts of end-use prices, forecasts of prices for, availability of, expansion of, and utilization of interstate natural gas pipeline services.

Prior to model development, a working paper was compiled by the EIA to establish the specific requirements for the overall NEMS, as well as for each of the component modules.<sup>5</sup> Requirements pertaining specifically to the NGTDM were based on: (1) analyses performed with EIA's IFFS/GAMS forecasting system, (2) limitations of GAMS, (3) the regulatory reform agenda of the Federal Energy Regulatory Commission (FERC), and (4) Department of Energy (DOE) policy initiatives as outlined in the National Energy Strategy.<sup>6</sup> These requirements, along with recommendations from a recent Model Quality Audit of the GAMS by the Office of Statistical Standards,<sup>7</sup> yielded a list of design guidelines for the NGTDM that support a broad array of desired analyses. Based on these guidelines, the NGTDM needed to:

- Represent pipeline capacity limitations exiting the major producing regions and entering the major market areas
- Employ a solution procedure based on an interregional trade equilibrium model that attempts to minimize simultaneously the global costs of supply and transportation subject to gas supplies available in each region, regional demand requirements, and pipeline capacity constraints
- Incorporate a transmission/storage capacity expansion/planning module that would recognize on-going, and planned/announced capacity expansion projects, as well as other capacity expansion needs throughout the forecast period
- Have the ability to endogenously determine market based rates for pipeline transportation services
- Have the ability to partition the natural gas market to apply either market based or cost based rates to specific segments of end-use sectors or to the market as a whole

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<sup>5</sup>Energy Information Administration, Office of Integrated Analysis and Forecasting, "Requirements for a National Energy Modeling System," December 12, 1991.

<sup>6</sup>National Energy Strategy, First Edition, 1991/1992 (Washington, DC, February 1991).

<sup>7</sup>Carpenter, Paul R., *Review of the Gas Analysis Modeling System* (Boston, MA: Incentives Research, Inc., August 1991).

- Employ a short-run supply curve that includes a direct representation of marginal sources of supply
- Represent Canadian and Mexican pipeline gas trade and liquefied natural gas trade
- Account for emissions of criteria pollutants that are emitted as a by-product of the natural gas transmission and distribution industry
- Account for capital investment requirements of storage and capacity expansion projects in the transmission and distribution sector.

During the development of the model methodology, a study was made of existing models and modeling techniques that might be used to meet the above requirements. Based on this study and the reports mentioned previously, it was determined that no model currently in existence could satisfy the NEMS requirements, and thus a new model was needed. The results of the study are presented in Appendix D. Documents that were referenced in support of the model development effort are listed in Appendix B.

The following sections provide brief overviews of the four components of the NGTDM.

## Annual Flow Module

The Natural Gas Annual Flow Module (AFM) is the main integrating module of the NGTDM. One of its major functions is to simulate the natural gas price determination process. The AFM brings together all major economic and technological factors that influence regional natural gas trade in the United States. The economic considerations include the demand for and the supply of natural gas, competition from substitute fuels and conservation options, and competition from imported natural gas.

The AFM integrates all components of the NGTDM (the AFM itself, the Capacity Expansion Module, the Pipeline Tariff Module and the Distributor Tariff Module). Through this integration process, the AFM derives average annual natural gas prices (wellhead, city gate, and end-use) that reflect an interregional trade market equilibrium among competing gas supplies, end-use sector consumption and transportation routes. End-use prices are derived for both core and noncore markets. Within NEMS the classification of customers as core versus noncore is predetermined.

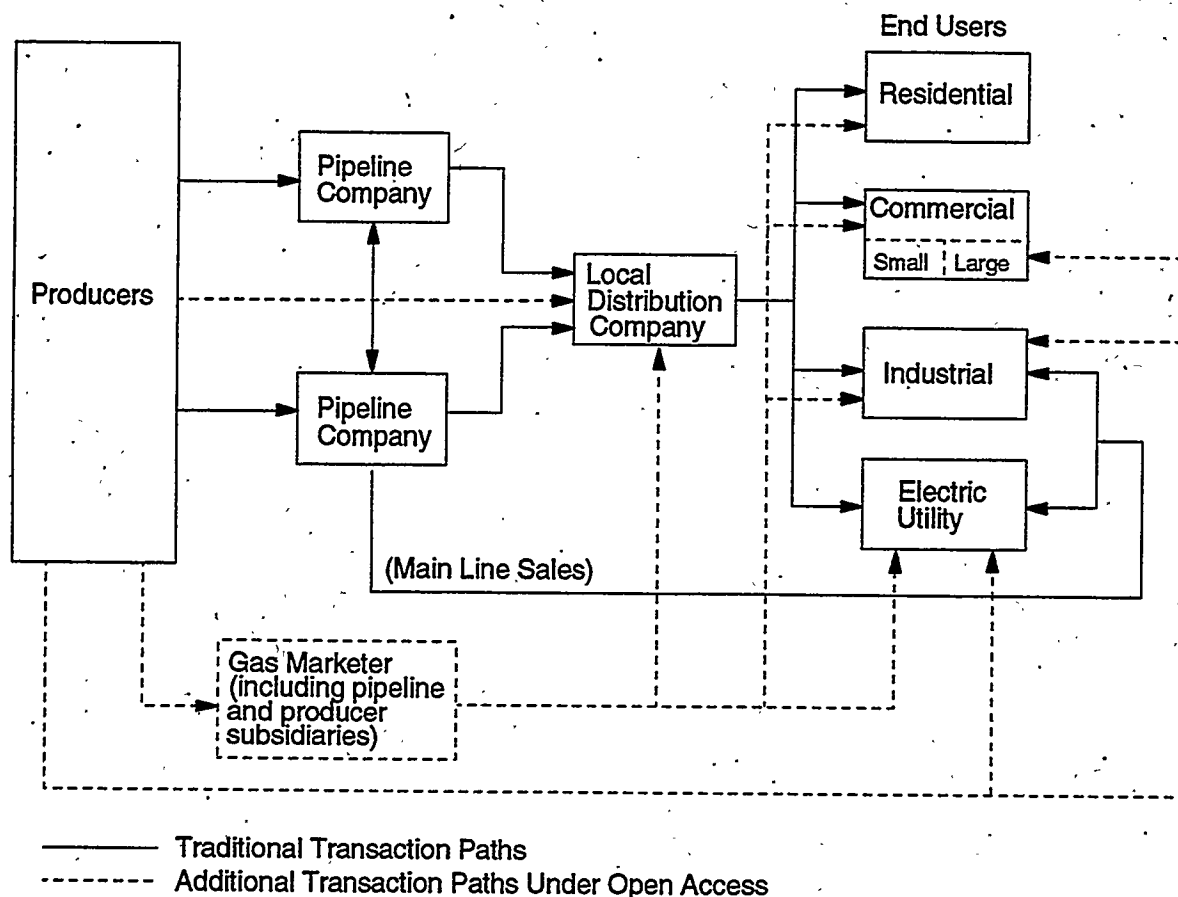
The historical evolution of the price determination process simulated by the AFM is depicted schematically in Figure 2-2. Until recently, the marketing chain was very straightforward, with end-users and local distribution companies contracting with pipeline companies, and the pipeline companies in turn contracting with producers. Prices typically reflected average costs of providing service plus some regulator-specified rate of return. Although this approach is still employed, more pricing flexibility is being introduced, particularly in the interstate pipeline industry. Pipeline companies are also offering a range of services under competitive and market-based pricing arrangements. Additionally, new players—for example marketers of spot gas and brokers for pipeline capacity—have entered the market, creating new links connecting suppliers with end-users. The marketing links will become increasingly complex in the future.

The level of competition for pipeline services (generally a function of the number of pipelines having access to a customer and the amount of capacity available) is currently driving the prices for interruptible transmission service and is beginning to have an effect on firm service prices. Currently, there are significant differences across regions in pipeline capacity utilization.<sup>8</sup> These regional differences are evolving as new pipeline capacity is constructed to relieve the capacity constraints in the Northeast and on the West Coast, and to expand markets in the Midwest. As capacity changes take place, prices of services should adjust accordingly to reflect new market conditions.

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<sup>8</sup>Energy Information Administration, *Capacity and Service on the Interstate Natural Gas Pipeline System, 1990: Regional Profiles and Analyses*, DOE/EIA-0551 (Washington, DC, May 1992).

**Figure 2-2. Principal Buyer/Seller Transaction Paths for Natural Gas Marketing**



Federal initiatives (most recently compiled in FERC Order No. 636) are reducing barriers to market entry and are encouraging the development of more competitive markets for pipeline services. Potential mechanisms used to make the transmission sector more competitive include the widespread capacity releasing programs, market-based rates, and the formation of market centers with deregulated upstream pipeline services. Some combination of these mechanisms will probably be used in the future. As the outcome is unknown at this point, the AFM is not designed to model any specific type of program. It is instead designed to simulate the overall impact of the movement towards market based pricing of transmission services.

The regional supply detail in the AFM, in conjunction with the AFM representation of pipeline capacity, supports analysis of regional shifts in supply and demand patterns. Regional differences in marginal sources of supply are also captured. Finally, the AFM addresses: transmission fuel consumption and losses; emissions associated with transmission fuel consumption; the impact of the Canadian and Mexican natural gas markets on the U.S. gas market; and capacity rationing (accomplished via the pricing of services).

## Capacity Expansion Module

The primary purpose of the Capacity Expansion Module (CEM) is to simulate the decision-making process for expanding pipeline and/or storage capacity in the U.S. gas market. In simulating gas pipeline capacity expansion, the CEM: (1) determines the amount of pipeline and storage capacity to be added between or within regions in the NGTDM, and (2) establishes effective (or practical) maximum annual utilization rates for each of the interregional pipeline routes represented in the Annual Flow Module. Maximum utilization rates (or load factors) on pipeline routes are established to capture the impact of variations in seasonal demand on the maximum amount of gas which

can practically flow between regions within a year. Pipeline and storage capacity additions are used in the Annual Flow Module (in combination with the maximum load factors) to set limits on annual interregional flows and to set working gas storage levels. These capacity additions are also used in the Pipeline Tariff Module when determining future storage rates and interregional pipeline tariffs.

The CEM was designed to address the guidelines that support a broad array of desired analyses and policy questions to be answered, such as:

- What impact will the increased demand for natural gas attributable to greater market penetration of new end-use gas technologies have on the utilization of the U.S. pipeline grid and requirements for new capacity? In what regions is capacity likely to be added?
- What might be the impact of a proactive natural gas policy on the utilization of pipeline capacity and the need for pipeline expansion?
- How will unbundling and the increasingly market-oriented pricing of gas supply and transmission services affect the differences between delivered prices for residential/commercial and industrial and electric generators sector gas users?

Regulation affecting the demand for gas and the supply of gas, such as emissions controls and tax credits, are modeled within the demand models of NEMS and the Oil and Gas Supply Model, respectively. The Pipeline Tariff Module and the Distributor Tariff Module provide tariffs to the CEM. Therefore, regulations affecting the setting of rates are specified within these two tariff modules, and are subsequently incorporated within the CEM. When the NGTDM is used to analyze the impact of new regulations which will increase or decrease expansion costs, these adjustments will be incorporated within the Pipeline Tariff Module, where the interstate tariffs associated with expanded pipeline or storage capacity are calculated (e.g., incremental versus rolled-in rates for new capacity). Within the CEM, parameters can be set to capture the impact of changes in lead times associated with the regulatory approval process for pipeline and storage expansion.

The design of the CEM is consistent with the NEMS requirements for modeling natural gas pipeline capacity and capacity expansion: "The model will respond to external decisions (assumptions) about throughput capacity for natural gas facilities including the expansion of facilities (interstate pipelines, storage and import facilities), and maintenance and replacement of facilities, as well as the associated costs. The output reports will contain capacity requirements and utilization rates distinguished by region."<sup>9</sup>

## Pipeline Tariff Module

The primary purpose of the Pipeline Tariff Module (PTM) is to compute tariffs for transportation and storage services provided by interstate pipeline companies. These tariffs are used within the Annual Flow Module to derive supply and end-use prices and within the Capacity Expansion Module to derive capacity additions. The tariffs are computed for individual pipeline companies, then aggregated to the major gas pipeline corridors or arcs (in the United States) specified in the NGTDM network, as described in Chapter 4. An accounting system is used to track costs and compute rates under various rate design and regulatory scenarios. Tariffs are computed for both firm and interruptible transportation and storage services. Transportation tariffs are computed for interregional arcs defined by the NGTDM network. These network tariffs represent an aggregation of the tariffs for individual pipeline companies supplying the network arc. Storage tariffs are defined at regional NGTDM network nodes, and, likewise, represent an aggregation of individual company storage tariffs. Note that these services are unbundled and do not include the price of gas, except for the cushion gas used to maintain minimum gas pressure. Furthermore, the module cannot address competition for pipeline or storage services along an aggregate arc or within an aggregate region, respectively.

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<sup>9</sup>Energy Information Administration, *Requirements*, pp. 12-13.

Since the tariffs determined by the PTM represent an aggregation of individual pipeline companies, the PTM is not designed to address the issue of analyzing competition within a regional pipeline corridor. It should also be noted that the PTM deals only with the interstate market, and thus does not capture the impacts of State-specific regulations for intrastate pipelines. Intrastate transportation charges are accounted for within the Distributor Tariff Module.

Pipeline tariffs for transportation and storage services represent a significant portion of the price of gas to end-users. Consumers of natural gas are grouped generally into two categories: (1) those who need firm or guaranteed service because gas is their only fuel option or because they are willing to pay for security of supply, and (2) those who do not need guaranteed service because they can either periodically terminate operations or use fuels other than natural gas. The first group of customers (core customers) purchase firm transportation services, while the latter group (noncore customers) purchase interruptible services or released capacity. Pipeline companies guarantee to their core customers that they will provide peak day service up to the maximum capacity specified under their contracts even though these customers may not actually request transport of gas on any given day. In return for this service guarantee, these customers pay monthly reservation fees (or demand charges). These reservation fees are paid in addition to charges for transportation service based on the quantity of gas actually transported (usage fees or commodity charges). The PTM transportation and storage rates to core customers are based on the average cost-of-service provided by the pipeline to all of its comparably situated core customers.

The actual reservation and usage fees (tariffs) that pipelines are allowed to charge are regulated by the Federal Energy Regulatory Commission (FERC). FERC's ratemaking traditionally allows (but does not necessarily guarantee) a pipeline company to recover its costs, including what the regulators consider a fair rate of return on capital. A fundamental decision in cost-based rate design is the apportionment of costs among customer classes. How costs are apportioned determines the extent of differences in the rates charged to different classes of customers and for different types of service. For example, the more fixed costs that are included in usage fees, the more noncore customers share in paying pipeline costs. However, transferring a larger share of fixed costs to reservation fees leads to core customers bearing a larger share of system costs. The PTM is designed to provide flexibility in allocating fixed and variable costs to core and noncore customers so that various policy initiatives may be examined. A recent change in the PTM is a revenue crediting mechanism to capture the gross effects of revenue crediting for pipeline-provided interruptible services. Should revenues from interruptible customers exceed costs allocated to them, a portion of the excess revenues is credited back to firm customers and the remainder is left for pipeline profits.

Since requirements of noncore customers generally are not taken into account in determining the peak-day delivery requirements of pipeline systems, the availability of capacity to serve these customers during peak consumption periods can be limited, and interruptions can occur. FERC sets maximum and minimum rates a pipeline is allowed to charge for interruptible service; thus, pipeline companies are allowed to offer discounts from the maximum usage fee at their discretion provided they do not unduly discriminate among customers. Since rates may be discounted to the variable cost of moving gas, and the major portion of the pipeline costs are fixed costs, the pipelines have considerable discretion in setting rates. Additionally, various rate making policy options currently under discussion by FERC may allow peak-season rates to rise substantially above the 100-percent load factor rate (also known as the full cost-of-service rate). In capacity-constrained markets, transportation rates based on marginal costs will be significantly above the full cost of service rates.

In the PTM, fixed and variable cost allocation provides flexibility in modeling a pipeline company's response to recent FERC regulatory decisions to unbundle pipeline sales and transportation services, and to encourage market-based responses to competition. The cost allocation is specified at the pipeline company-level. After individual company revenue requirements are determined, they are aggregated across companies to the arc-level specified by the NGTDM network. The PTM estimates maximum and minimum interruptible transportation service rates which are used to determine interruptible service arc-level tariffs charged to noncore customers. The maximum rate computed by the PTM is the full cost-of-service rate (currently the 100-percent load factor rate). The minimum rate is the variable cost of transporting gas. The actual rate charged noncore customers is a function of market conditions. The lower bound is set between the regulated maximum and minimum rates as a function of pipeline capacity utilization. In noncapacity constrained markets, the lower bound becomes the effective rate. The effective rate charged in the Annual Flow Module in capacity-constrained markets is based on marginal costs and, on occasion, exceeds the maximum rate computed by the PTM.

Theoretically, the PTM could compute either incremental or rolled-in (average) rates for new capacity, thus allowing a more comprehensive analysis of the results of supply and demand shifts on capacities and flow patterns, as well as a more representative analysis of the pricing of natural gas transportation and distribution services.<sup>10</sup>

## Distributor Tariff Module

The primary purpose of the Distributor Tariff Module (DTM) is to determine the components of end-use prices that are regulated by State and local authorities. These consist of (1) distributor markups charged by local distribution companies for the distribution of natural gas from the city gate to the end user and (2) markups charged by intrastate pipeline companies for intrastate transportation services. Intrastate pipeline tariffs are specified exogenously to the model and are currently set to zero. However, these tariffs are accounted for in the model indirectly. End-use service is distinguished within the DTM by sector and service type.

Distribution markups represent a significant portion of the price of gas to customers. These customers include the residential, commercial, industrial, electric generators, and transportation (compressed natural gas vehicles) sectors. Each sector has different distribution service requirements. For example, the core customers in the model (residential, transportation, commercial and some industrial and electric generator customers) require guaranteed on-demand (firm) service because natural gas is their only fuel option. In contrast, large portions of the industrial and electric generator sectors may not rely solely on guaranteed service because they can either periodically terminate operations or switch to other fuels. These customers are referred to as noncore. They can elect to receive some gas supplies through a lower priority (and lower cost) interruptible transportation service. During periods of peak demand, services to these sectors can be interrupted in order to meet the natural gas requirements of core customers. In addition, these customers may select to bypass the local distribution company pipelines and hook up directly to interstate or intrastate pipelines.

The actual rates that local distribution companies and intrastate carriers are allowed to charge are regulated by State authorities. State ratemaking traditionally allows (but does not necessarily guarantee) local distribution companies and intrastate carriers to recover their costs, including what the regulators consider a fair return on capital. These rates are derived from the cost of providing service to the end-use customer. The State authority determines which expenses can be passed through to customers and establishes an allowed rate of return. These measures provide the basis for distinguishing rate differences among customer classes and type of service by allocating costs to these classes and services based on a rate design. The DTM does not directly account for the separate cost components in deriving a revenue requirement for distribution services, but approximates the change in the total revenue requirement from year to year.

The DTM represents distribution tariffs to the core customers (excluding the transportation sector) by estimating annual changes to total distribution costs, and subsequently the related tariffs, starting from a base year. Base year values for total costs and distributor tariffs are established using historical data. The annual change in total cost is dependent on an assumed increase in operational efficiencies, as well as the annual change in natural gas consumption and in national average capital and employment costs. The revenue requirements from core customers are adjusted due to an assumed contribution of revenues from noncore customers. The allocation of these revenue requirements to individual sectors is primarily dependent on the relative annual change in consumption across sectors. User-specified parameters allow adjustment of the markups to account for shifts due to regulatory policy. Many of these modeling choices are the result of data limitations.<sup>11</sup>

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<sup>10</sup>Throughout the report, reference will be made to the current formulation of the NGTDM where incremental rates will be used as a market test for capacity expansion, and where the AFM will use rolled-in rates in solving for flows and prices in the firm market and market-based rates for the interruptible market. However, the capability exists within the PTM to compute different types of rates allowing it, and thus the NGTDM, to respond to different rate design and regulatory scenarios.

<sup>11</sup>EIA data surveys currently do not collect the cost components required to derive revenue requirements and cost-of-service for local distribution companies and intrastate carriers; nor are these data collected by other public or private sources. These cost components can be compiled from rate filings to Public Utility Commissions; however, an extensive data collection effort is beyond the scope of NEMS at this time. This data collection may be considered for a future development effort.

Distributor markups to the noncore customers are set at historical levels and are held constant. A user-specified option is available for allowing these rates to decline (or increase) steadily throughout the forecast. The natural gas vehicle (NGV) sector markups are calculated separately for fleet and personal vehicles. Markups for fleet vehicles are set and held constant at historical levels with taxes added (although a user-specified decline rate is allowed). Markups for personal vehicles are set at the industrial sector core price, plus taxes, plus an assumed distribution cost. This price is capped at the gasoline equivalent price, as long as minimum costs are covered.

Since the markups determined by the DTM represent an aggregation of individual local distribution companies and intrastate pipeline companies, this module is not designed to address the issue of analyzing competition for distribution services within a region. It should also be noted that the DTM deals only with issues at an aggregate regional level, and thus does not capture the impacts of State-specific regulations on intrastate tariffs and by-pass issues. Finally, the procedures used by the DTM to estimate markups are limited by the types and availability of data.





### 3. Interface Between the NEMS and the NGTDM

This chapter presents the general role that the Natural Gas Transmission and Distribution Model (NGTDM) plays in the NEMS. First a general description of the NEMS is provided, along with an overview of the NGTDM. Second, the data passed to the NGTDM from other NEMS models will be described along with the methodology used within the NGTDM to transform these prior to their use in the model. The natural gas demand representation provided to the NGTDM from the Electricity Market Model (EMM) and from the end-use demand models of NEMS is described, followed by a section on the natural gas supply interface. Finally, the information that is passed to other NEMS models from the NGTDM will be described.

#### A Brief Overview of NEMS and the NGTDM

The NEMS represents all of the major fuel markets—crude oil and petroleum products, natural gas, coal, electricity, and imported energy—and iteratively solves for an annual supply/demand balance for each of the 9 Census Divisions, accounting for the price responsiveness in both energy production and end-use demand, and for the interfuel substitution possibilities. NEMS solves for an equilibrium in each forecast year by iteratively operating a series of fuel supply and demand models to compute the end-use prices and consumption of the fuels represented.<sup>12</sup> The end-use demand models—for the residential, commercial, industrial, and transportation sectors—are detailed representations of the important factors driving energy consumption in each of these sectors. Using the delivered prices of each fuel, computed by the supply modules, the demand models evaluate the consumption of each fuel, taking into consideration the interfuel substitution possibilities, the existing stock of fuel and fuel conversion burning equipment, and the level of economic activity. Conversely, the fuel conversion and supply models determine the end-use prices needed in order to supply the amount of fuel demanded by the customers, as determined by the demand models. Each supply module considers the factors relevant to that particular fuel, for example: the resource base for oil and gas, the transportation costs for coal, or the refinery configurations for petroleum products. Electric generators and refineries are both suppliers and consumers of energy.

Within the NEMS system, the NGTDM provides the interface between the Oil and Gas Supply Model (OGSM) and the demand models in NEMS, including the EMM. The NGTDM determines the price and flow of dry natural gas supplied internationally from the contiguous U.S. border<sup>13</sup> or domestically from the wellhead (and indirectly from natural gas processing plants) to the domestic end-user.<sup>14</sup> In so doing, the NGTDM models the markets for the transmission (pipeline companies) and distribution (local distribution companies) of natural gas in the contiguous United States. The primary data flows between the NGTDM and the other oil and gas models in NEMS, the Petroleum Market Model (PMM) and the OGSM, are depicted in Figure 3-1.

Functionally, each of the demand models in NEMS provides the level of natural gas that would be consumed at the burnertip by the represented sector at a given end-use price; and the OGSM provides the level of natural gas which would be produced (or imported) at the wellhead (or border crossing) for a given supply price. The NGTDM uses this information to build "short-term" supply or demand curves which are used to approximate a given model's response to prices within a limited range.<sup>15</sup> Given these short-term demand and supply curves, the NGTDM model solves for the end-use, wellhead, and border prices that represent a natural gas market equilibrium, while accounting for the cost and market for transmission and distribution services (including its physical and regulatory constraints). These solution prices, and associated production levels, are in turn passed to the OGSM and the demand models,

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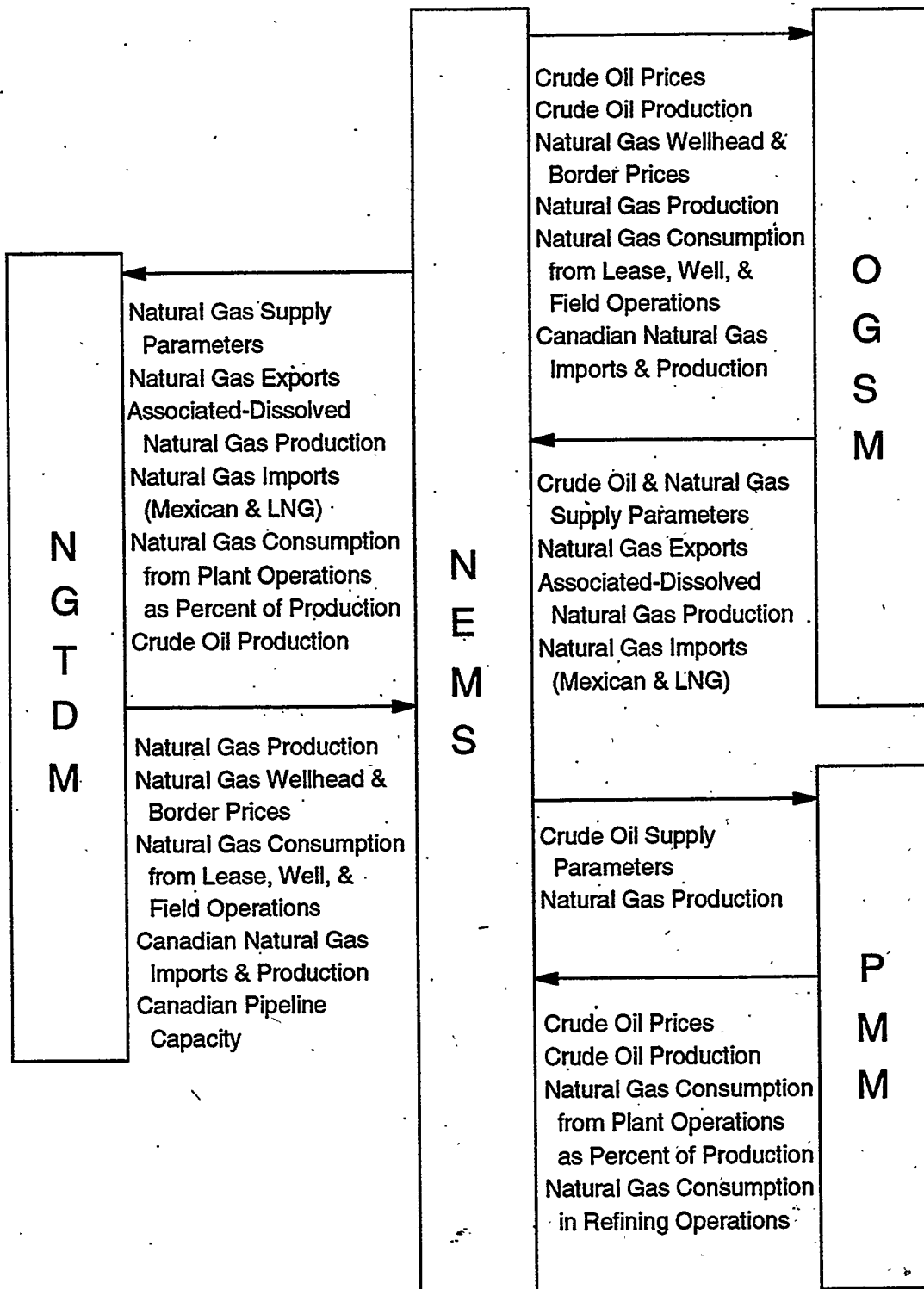
<sup>12</sup>A more detailed description of the NEMS system, including the convergence algorithm used, can be found in "National Energy Modeling System Integrating Module Documentation Report." DOE/EIA-M057, December 1993.

<sup>13</sup>Because of the distinct separation in the natural gas market between Alaska, Hawaii, and the contiguous United States, natural gas consumption in, and the associated supplies from, Alaska and Hawaii are modeled separately from the contiguous United States within the NGTDM.

<sup>14</sup>Natural gas exports are also represented within the model.

<sup>15</sup>Special parameters are provided by OGSM for the construction of supply curves for domestic nonassociated natural gas production and by EMM for the construction of demand curves for natural gas consumed by electric generators that can use residual fuel oil as an alternate.

**Figure 3-1. Primary Data Flows Between Oil and Gas Models of NEMS**



including the EMM, as primary input variables. In addition to the basic calculations performed within these models, the parameters which define the natural gas supply or demand curves used in the NGTDM are updated (as appropriate) to reflect the prices most recently provided by the NGTDM.

The NGTDM model is composed of four primary components or modules: the Annual Flow Module, the Capacity Expansion Module, the Pipeline Tariff Module, and the Distributor Tariff Module. The Annual Flow Module is the central module of the NGTDM, since it is used to derive flows and prices of natural gas in conjunction with an annual natural gas market equilibrium. Conceptually the Annual Flow Module is a simplified representation of the natural gas transmission and distribution system, structured as a network composed of nodes and arcs. The other three primary components serve as satellite modules to the Annual Flow Module, providing parameters which define some of the characteristics of these nodes and arcs. Other parameters for defining the natural gas market (such as supply and demand curves) are derived based on information passed from other NEMS models. The Capacity Expansion Module provides the Annual Flow Module with regional underground storage activity<sup>16</sup> and maximum annual flow limits along each of the arcs in the network. The Pipeline and Distributor Tariff Modules provide set the tariffs to be charged along each of the interregional, intraregional, intrastate, and distribution arcs. Data are also passed back to these satellite modules from the Annual Flow Module and between the satellite modules themselves.

The NGTDM is called once for each iteration of NEMS, but all modules are not run for every call. The Pipeline Tariff Module and the Capacity Expansion Module are executed once for each forecast year, on the first iteration of each year and the last iteration of each year, respectively. The Annual Flow Module and the Distributor Tariff Module are executed once every NEMS iteration. The calling sequence of and the interaction among the NGTDM modules is as follows for each year of execution of NEMS:

- First Iteration:

The Pipeline Tariff Module determines tariffs for interregional and interstate pipeline company transportation and storage services, using a cost based simulation, and establishes tariff curves for pipeline and storage expansion.

- Each Iteration:

The Distributor Tariff Module sets markups for intrastate transmission and for distribution services based on historical data and assumed parameters. Next, the Annual Flow Module incorporates tariffs from the Pipeline Tariff Module and markups from the Distributor Tariff Module into a linear program that solves for interregional flows based on supply availability, demand requirements, and pipeline capacity constraints. The linear program determines a market equilibrium solution by maximizing consumer and producer surpluses, while minimizing supply and transportation costs, thus determining natural gas end-use and supply prices and domestic production. Pipeline capacity constraints for the first year (or years) of execution are determined from historical data. Subsequent year's constraints are taken from the previous year's Capacity Expansion Module results.

- Last Iteration:

The Capacity Expansion Module employs the pipeline and storage expansion curves calculated in the Pipeline Tariff Module, the tariffs from the Distributor Tariff Module, and expected future supply availability and consumption levels from other models in the NEMS. The Capacity Expansion Module represents two natural gas market seasons within a linear program structure to determine pipeline and storage capacity expansion (beyond planned additions) for a future year, by minimizing the pipeline and storage expansion costs required to meet the expected consumption levels of natural gas. The resulting pipeline capacity build requirements and seasonal flow patterns are used to establish effective limits on the annual load along pipelines, for use in the Annual Flow Module. In addition, annual net

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<sup>16</sup>The CEM determines annual net storage withdrawals by firm and interruptible service types. The sum of these two values by region in the forecast period equals zero.

storage withdrawals for the firm and interruptible service networks are set based on resulting peak/offpeak flows to and from storage in the Capacity Expansion Module.

The primary outputs from the NGTDM, which are used as input in other NEMS models, result from establishing a natural gas market equilibrium solution: end-use prices, wellhead and border crossing prices, and associated production and Canadian import levels. In addition, the model provides a forecast of lease and plant fuel consumption, pipeline fuel use and the corresponding emissions, as well as pipeline and distributor tariffs, pipeline and storage capacity expansion, and interregional natural gas flows. The capital investments associated with the expansion of pipeline and storage capacity are provided to the macroeconomic model of NEMS.

## Natural Gas Demand Representation

Natural gas which is produced within the United States is consumed in lease and plant operations, delivered to consumers, exported internationally, and consumed as pipeline fuel. The consumption of gas as lease, plant, and pipeline fuel is determined within the NGTDM. Gas used in well, field, and lease operations is set equal to an exogenously specified percentage (Appendix E, PCTLSE\_SUPL) of dry gas production. Gas consumed in natural gas processing plants is similarly calculated, however, the percentages that are used are provided by the Petroleum Market Model.<sup>17</sup> Pipeline fuel use depends on the amount and distance of gas transported and distributed in each region, as described in Chapter 5. The level of natural gas exports are currently determined exogenously to NEMS and passed to the NGTDM from the OGSM model. Exports are distinguished by six Canadian and three Mexican border crossing points, as well as for exports of liquefied natural gas to Japan from Alaska. The representation of gas delivered to consumers is described below.

### Classification of Natural Gas Consumers

Natural gas that is delivered to consumers is represented within the NEMS at the Census Division level and by five primary end-use sectors: residential, commercial, industrial, transportation, and electric generation.<sup>18</sup> These demands are further distinguished by customer class (core or noncore), reflecting the type of natural gas transmission and distribution service that is predominately purchased. The "core" customers require guaranteed service, particularly during peak days/periods during the year. The "noncore" customers require a lower quality of transmission services and therefore, consume gas under a less certain and/or less continuous basis. In the NGTDM, the core customers are assumed to purchase firm transmission services and the noncore customers are assumed to purchase interruptible transmission services.

Currently in NEMS, all customers in the transportation, residential, and commercial sectors are classified as core.<sup>19</sup> Within the industrial sector the noncore segment includes the industrial boiler market and refineries. The noncore segment of the electric generation sector is further separated into two subclasses, depending on the alternative fuel a plant would burn should natural gas be unavailable or relatively uneconomic. The subclass of noncore electric generation plants that has the option of burning distillate fuel in lieu of natural gas is referred to as "competitive-with-distillate." The second subclass of noncore plants can burn either natural gas or residual fuel oil and is therefore referred to as "competitive-with-residual fuel." The electric generating units defining each of the three customer classes modeled are as follows: (1) core—gas steam units or gas combined cycle units, (2) competitive-with-distillate—dual-fired turbine units or gas turbine units, (3) competitive-with-residual fuel—dual-fired steam plants

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<sup>17</sup>The factors used in calculating regional lease and plant fuel consumption are initially based on historical averages and held constant throughout the forecast period. However, in the historical years (and, if chosen, the first two forecast years as presented in the latest available *Short-Term Energy Outlook* (STEO), DOE/EIA-0202), these factors are scaled so the resulting national lease and plant fuel consumption will match the annual published value (Appendix E, QLPIN, STQLPIN). The scaled values for either the last historical (or STEO year, if selected) are used throughout the forecast period. A similar adjustment is performed on the factors used in calculating pipeline fuel consumption.

<sup>18</sup>Natural gas burned in the transportation sector is defined as compressed natural gas that is burned in natural gas vehicles; and the electric generation sector includes all electric power generators except cogenerators.

<sup>19</sup>The NEMS is structurally able to classify a segment of these sectors as noncore, but currently sets the noncore consumption for the residential, commercial, and transportation sectors at zero.

(consuming both natural gas and residual fuel oil). Within the NGTDM, natural gas is exported to Mexico under firm transmission service and to Canada under interruptible transmission service.

For any given NEMS iteration within a forecast year, the individual demand models in NEMS determine the level of natural gas consumption for each region and customer class at the end-use price for the same region, class, and sector, as calculated by the NGTDM in the previous NEMS iteration. Within the NGTDM, each of these consumption levels (and its associated price) is used in conjunction with an assumed price elasticity (set to zero if fixed consumption levels are to be used) as a basis for building a short-term demand curve. These curves are used within the NGTDM to minimize the required number of NEMS iterations by approximating the demand response to a different price. In so doing, the price where the implied market equilibrium would be realized can be approximated. Each of these market equilibrium prices is passed to the appropriate demand model during the next NEMS iteration to determine the consumption level that the model would actually forecast at this price. The NGTDM disaggregates the Census division regional consumption levels into the regional representation that the NGTDM requires. The demand curve representation and the regional mapping for the electric generation sector differ from the other NEMS sectors as described in the following sections.

### ***Regional Representations of Demand***

Natural gas consumption levels by all nonelectric<sup>20</sup> sectors are provided by the NEMS demand models for the 9 Census divisions, the primary integrating regions represented in the NEMS. Alaska and Hawaii are included within the Pacific Census Division. The EMM represents the electricity generation process for 13 electricity supply regions—the 9 North American Electric Reliability Council (NERC) Regions and 4 selected NERC Subregions (Figure 3-2). Electricity generation in Alaska and Hawaii is handled separately. Within the EMM, the electric generators' consumption of natural gas is disaggregated into subregions which can be aggregated into Census Divisions or into the regions used in the NGTDM.

With the few following exceptions, the regional detail provided at a Census division level is adequate to build a simple network representative of the contiguous U.S. natural gas pipeline system. First, Alaska and Hawaii are not connected to the rest of the Nation by pipeline and are therefore treated separately from the contiguous Pacific Division in the NGTDM. Second, Florida receives its gas from a distinctly different route than the rest of the South Atlantic Division and is therefore isolated. A similar statement applies to Arizona and New Mexico relative to the Mountain Division. Finally, California is split off from the contiguous Pacific Division because of its relative size coupled with its unique energy related regulations. The resulting 12 primary regions represented in the Annual Flow Module are referred to as the "NGTDM Regions" (as shown in Figure 2-1).

The regions which are represented in the EMM do not always align with State borders and generally do not share common borders with the Census divisions or NGTDM regions (Figure 3-2). Therefore, demand in the electric generation sector is represented in the NGTDM at the regions (NGTDM/EMM) resulting from the combination of the NGTDM regions overlapped with the EMM regions, translated to the nearest State border (Figure 3-3). For example, the South Atlantic NGTDM region (number 5) includes three NGTDM/EMM regions (part of EMM regions 1, 3, and 9). Within the EMM, the disaggregation into subregions is based on the relative geographic location (and natural gas-fired generation capacity) of the current and proposed electricity generation plants within each region.

The consumption levels for each of the nonelectric sectors are disaggregated from the 9 Census divisions to the 12 NGTDM regions by applying historically based shares which are held constant throughout the forecast (Appendix E, NG\_CENSHR). For the Pacific Division, natural gas consumption estimates for Alaska are first subtracted to establish a consumption level for just the contiguous Pacific Division before the historical share is applied. The consumption of gas in Hawaii was considered to be negligible. Within the NGTDM, a relatively simple module (described later) was included for approximating the consumption of natural gas by each nonelectric sector in Alaska. These estimates, combined with the consumption levels provided by the EMM for consumption by electric generators in Alaska, are also used in the calculation of the production of natural gas in Alaska.

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<sup>20</sup>The "nonelectric" sectors refer to sectors that do not produce electricity using natural gas (i.e., the residential, commercial, industrial, and transportation demand sectors.)

Figure 3-2. Electricity Market Model (EMM) Regions

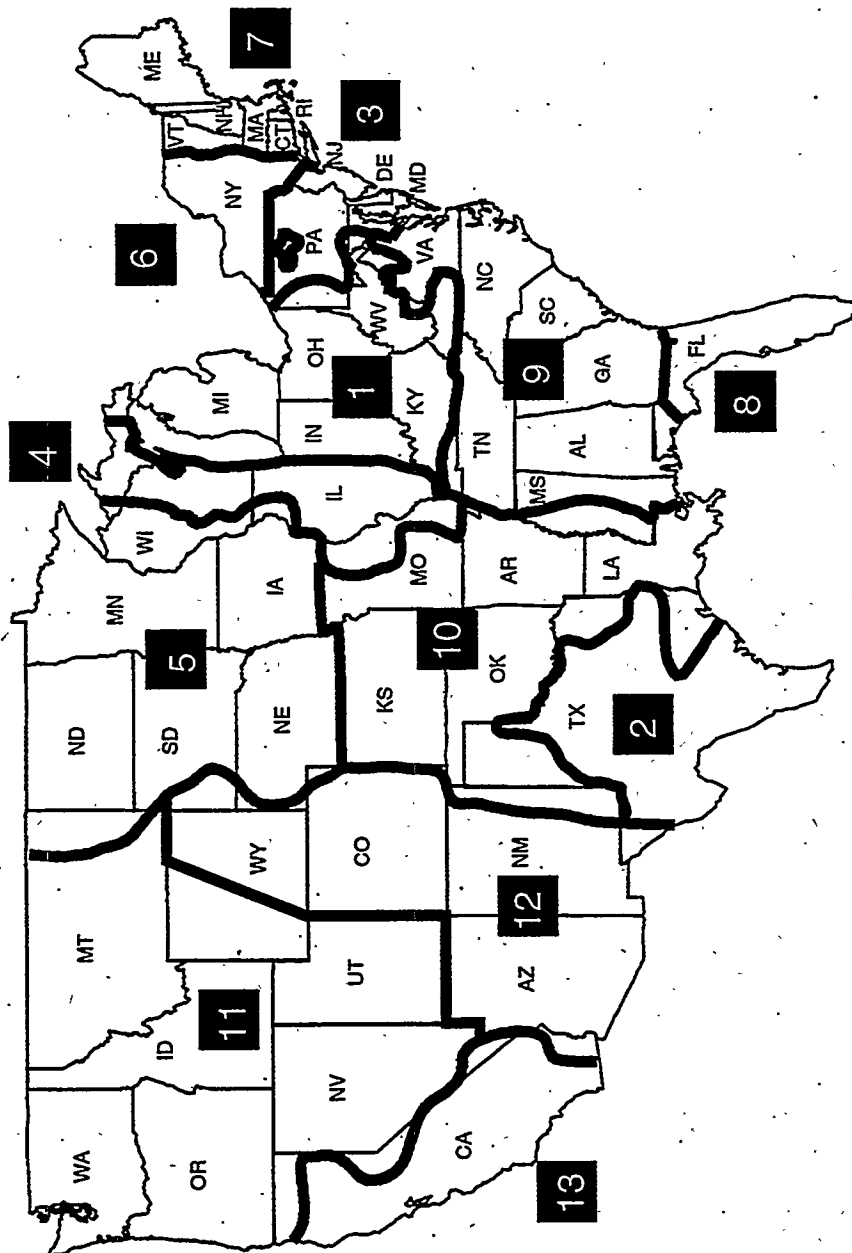
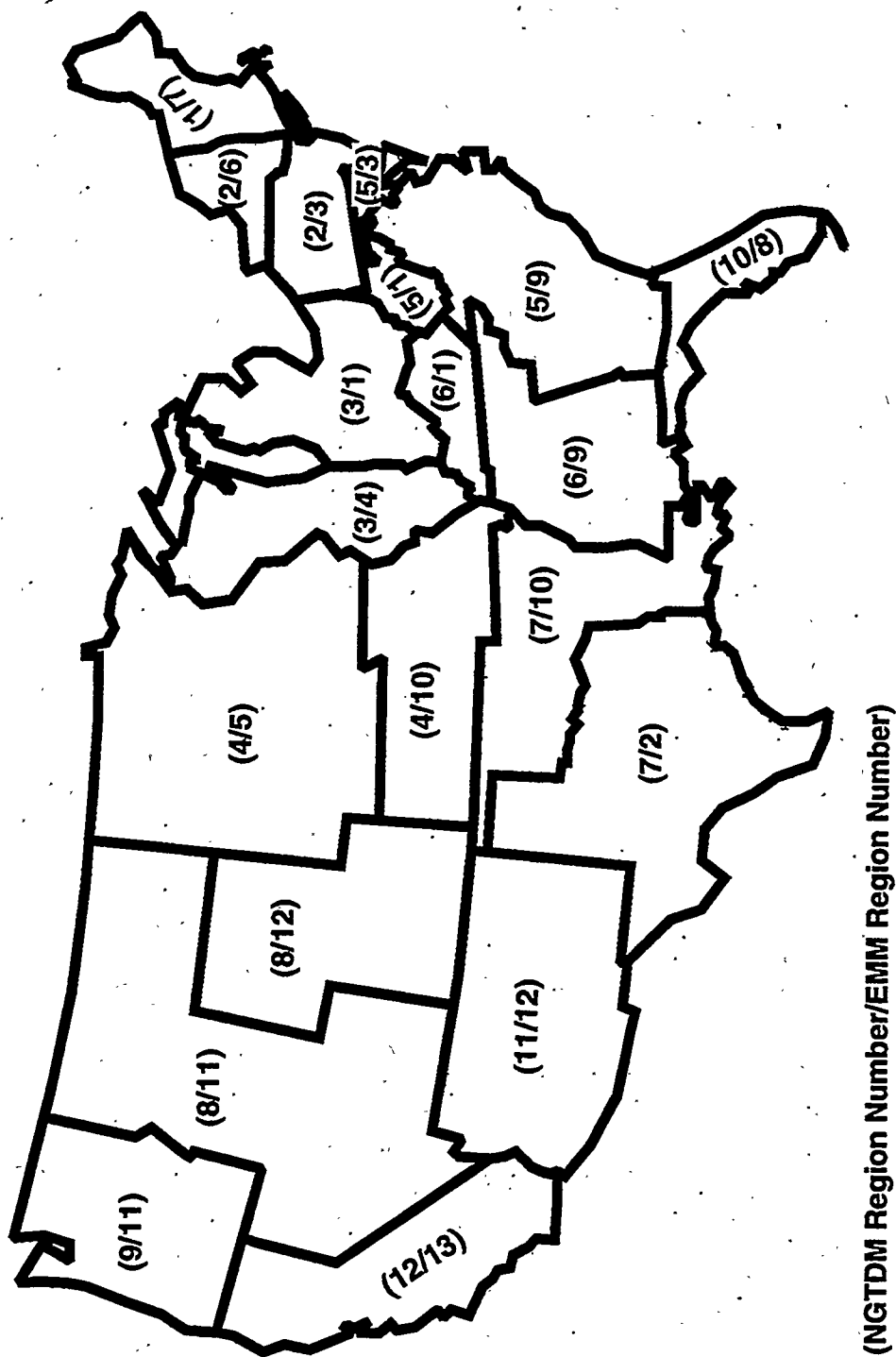


Figure 3-3. Natural Gas Transmission and Distribution Model/Electricity Market Model (NGTDM/EMM) Regions



## Natural Gas Demand Curves for Nonelectric Sectors

While the primary analysis of energy demand takes place in the NEMS demand models, the NGTDM itself directly incorporates limited price responsive demand curves to speed the overall convergence of NEMS and to improve the quality of the results obtained when the NGTDM is run as a stand-alone model. The NGTDM may also be executed to determine end-use prices for fixed consumption levels (represented by setting the price elasticity of demand in the demand curve equation to zero). These demand curves are defined within a limited range around the price/quantity pair solved for during the most recent NEMS iteration. The form of the demand curves for the firm transmission service type for each nonelectric sector and region is:

$$\text{NGTDM\_CRVNONUF}_{s,r} = \text{QBAS\_NONU\_F}_{s,r} * (\text{PRICE} / \text{NONU\_PR\_F}_{s,r})^{\text{NONU\_ELAS\_F}_{s,r}} \quad (1)$$

where,

$\text{NONU\_PR\_F}_{s,r}$	=	end-use price to core sector $s$ in NGTDM region $r$ in the previous NEMS iteration (dollars per Mcf)
$\text{QBAS\_NONU\_F}_{s,r}$	=	natural gas quantity which the NEMS demand models indicate would be consumed at price $\text{NONU\_PR\_F}$ by core sector $s$ in NGTDM region $r$ (Bcf)
$\text{NONU\_ELAS\_F}_{s,r}$	=	short-term price elasticity of demand for core sector $s$ (Appendix E) Note: Demand curves can be represented with fixed consumption levels by setting elasticities equal to zero.
$\text{PRICE}$	=	end-use price at which demand is to be evaluated (dollars per Mcf)
$\text{NGTDM\_CRVNONUF}_{s,r}$	=	estimate of the natural gas which would be consumed by core sector $s$ in region $r$ at the price $\text{PRICE}$ (Bcf)
$s$	=	core sector (1-residential, 2-commercial, 3-industrial, 4-transportation)

The form of the demand curve for the nonelectric interruptible transmission service type is identical, with the following variables substituted:  $\text{NGTDM\_CRVNONUI}_X$ ,  $\text{NONU\_PR\_I}$ ,  $\text{QBAS\_NONU\_I}$ , and  $\text{NONU\_ELAS\_I}$ .

## Natural Gas Demand Curves for Electric Generators

Natural gas demand by electric generators is represented somewhat differently in the NGTDM from the nonelectric demands because of greater cross price affects. Within the EMM natural gas consumption in the short-term depends first on the dispatch order of the gas burning plants, which is a function of the price of gas relative to the price of fuels burned by other powerplants, and second, on the percentage of gas used in dual-fired plants. If a change in the relative fuel prices results in a change in the dispatch order (relative to a base), the associated consumption level for natural gas burned by electric generators is likely to change as well. However, with the general exception of the competitive-with-residual fuel plant types, the gas consumption level of electric generators is unlikely to respond to changes in the gas price that do not affect the dispatch order. The dispatching of powerplants is represented in the EMM, not in the NGTDM. Therefore, in the NGTDM the gas consumption by electric generation within the core and competitive-with-distillate service types is fixed at the values calculated by the EMM in the previous NEMS iteration.

In the EMM, natural gas consumption by plants classified as competitive-with-residual fuel can change significantly in response to a different price even with no switch in the merit order. Consumption levels can change because these plants can switch between burning natural gas and burning residual fuel oil, which has historically been priced competitively with natural gas. A representation of the natural gas demand response within the EMM for the competitive-with-residual fuel plant types is incorporated in the NGTDM using parameters provided by the EMM. This representation will be relatively accurate within a range of natural gas prices which do not lead to a merit order change.

Since the demand for natural gas in the competitive-with-residual fuel class within the EMM is a function of the relative price of the two competing fuels, the demand curve to represent this customer class is specified within the



NGTDM as a function of the price of natural gas relative to the price of residual fuel oil to electric generators, as illustrated in Figure 3-4. For a given demand for electricity and a given dispatch order for a region within the EMM, there is a maximum (GSHRMAX) and a minimum (GSHRMIN) level of natural gas which would be consumed by the competitive-with-residual fuel class (represented by the vertical lines in the figure). GRATMIN is the lowest price ratio which would result in a consumption level equal to GSHRMIN, and GRATMAX is the highest price ratio which would result in a consumption level equal to GSHRMAX. For each NGTDM/EMM region, the EMM provides these price/quantity pairs to the NGTDM based on the dispatch order from the current NEMS iteration. These are two of the four price/quantity pairs provided by the EMM, which the NGTDM connects to form a piecewise linear demand curve for the competitive-with-residual fuel class within the electric generation sector. The EMM also provides the quantity of gas (GSHRPAR) that would be consumed at the price ratio which represents parity (GRATPAR), and the quantity of gas that would be consumed at the natural gas price (converted to a price ratio in the NGTDM) which was sent to the EMM in the previous NEMS iteration (SHROLD and RATOLD). Within the NGTDM the residual fuel oil price to electric generators (used in converting the price ratio into a natural gas price) is held constant at the level established in the previous NEMS iteration and is calculated as a quantity-weighted average of the low-sulfur and high-sulfur residual fuel prices (QRLELGR, QRHELGR) to the electric generation sector.

## Natural Gas Supply Interface

The primary categories of natural gas supply represented in the NGTDM for the contiguous Lower 48 States are nonassociated and associated-dissolved gas from onshore and offshore regions, pipeline imports from Mexico and Canada, liquefied natural gas imports, gas transported via the Alaskan Natural Gas Transportation System (ANGTS), synthetic natural gas produced from coal and from liquid hydrocarbons, and other supplemental supplies. The only supply categories from this list which are allowed to vary within the NGTDM in response to a change in the current year's natural gas price are synthetic natural gas produced from liquid hydrocarbons and nonassociated gas from onshore and offshore regions. The supply levels for the remaining categories are fixed at the beginning of each forecast year (i.e., before market clearing prices are determined), with the exception of associated-dissolved gas (determined in OGSM) which varies with a change in the oil production in the current forecast year. The annual oil production level is determined in the Petroleum Market Model and can vary between each iteration of NEMS.

Within the OGSM, natural gas supply activities are modeled for the 12 supply regions (6 onshore, 3 offshore, and 3 Alaskan geographic areas) shown in Figure 3-5. A separate component of the OGSM models the foreign sources of natural gas which are transported via pipeline from Canada and Mexico, and by way of oceanic vessels in liquefied form (liquefied natural gas). Six Canadian and three Mexican border crossings demarcate the foreign pipeline interface between the OGSM and the NGTDM. Supplies from the four existing liquefied natural gas terminals are also represented (as supply points) in the NGTDM, although only two of the four existing terminals are currently in operation. The annual levels of liquefied natural gas imports are determined in the OGSM and are provided to the NGTDM at the beginning of each forecast year. Similarly the OGSM establishes the level of gas which will flow into the contiguous United States via the ANGTS.

## Supplemental Gas Sources

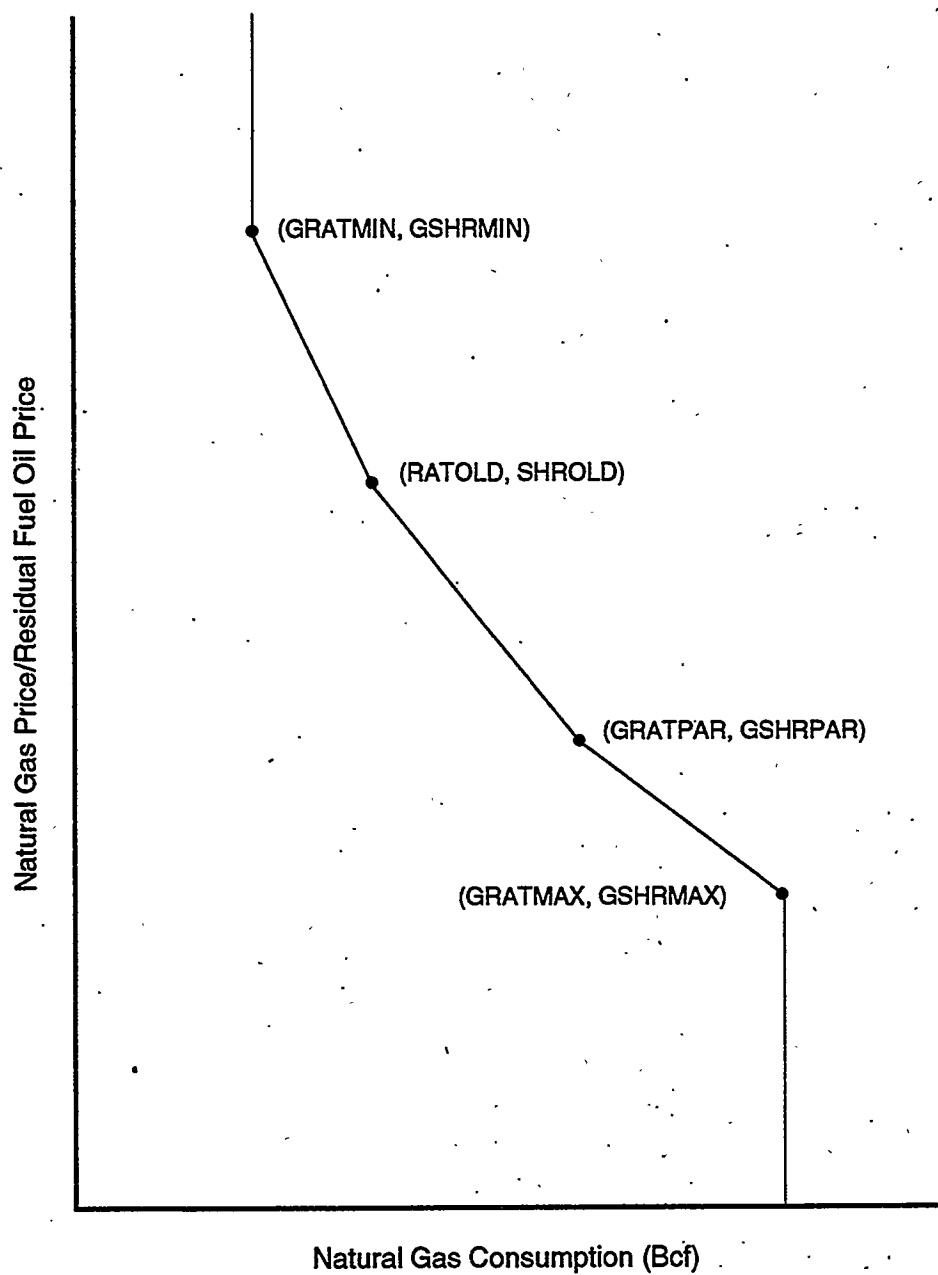
Sources for synthetically produced natural gas are geographically specified in the NGTDM based on current plant locations. Synthetic gas from coal is exogenously specified, independent of the price of natural gas in the current forecast year. The Coal Module of NEMS sets the annual forecast of natural gas produced from the Great Plains Coal Gasification Plant in North Dakota. To represent synthetic gas production from liquid hydrocarbons (currently produced only in Illinois) a statistically estimated price responsive supply curve is incorporated within the NGTDM:

$$VAL = SNGA1 * VALUE^{SNGA2} \quad (2)$$

where,

VAL = synthetic gas production from liquid hydrocarbons in Illinois (Bcf)

**Figure 3-4. Example Natural Gas Demand Curve for Competitive-With-Residual Fuel Oil Class of Electric Generators**



VALUE = firm service natural gas market price in the East North Central Census Division (which contains Illinois), (dollars per Mcf)  
 SNGA1, SNGA2 = estimated parameters (Appendix F, Table F3)

The synthetic gas production level resulting from the above equation is limited to be no less than an exogenously specified minimum (Appendix E, SNGMIN) and not to increase by more than 50 percent above the level in the previous forecast year. Synthetic gas production from liquid hydrocarbons in Hawaii is held constant throughout the forecast at an historically based level (Appendix E, SNGHI), as are other supplemental supplies<sup>21</sup> (Appendix E, OSUP\_TOT, OSUP\_RSHR).

## Natural Gas Imports Via Pipeline

The OGSM provides most of the parameters used in the NGTDM for representing the imports of gas from Mexico and Canada into the United States by pipeline. Border crossing points are established at each NGTDM region adjoining an international border. The annual import levels for gas from Mexico are generated exogenously and passed to the NGTDM via the OGSM. The OGSM also provides parameters for defining a national Canadian natural gas supply curve, an exogenous forecast for consumption of natural gas in Canada, and additional parameters for representing the transmission system for gas within Canada. The NGTDM exogenously sets a forecast of the physical capacity of natural gas pipelines crossing the border from Canada into the United States. This physical capacity limit is then multiplied by set of exogenously specified utilization rates (with parameters for setting an assumed annual growth rate) to establish maximum effective capacity limits for these pipelines. "Effective capacity" is defined as the maximum annual physically sustainable capacity of a pipeline times an assumed maximum likely utilization rate, based on the expected seasonal demand profiles of the customers being served. The functional form of the Canadian natural gas supply curve is represented as follows:

$$\text{CN\_PRODUC} = \text{OGRESCAN}_{2y} * \text{OGPRRCAN}_{2y} * \frac{(1 + \text{OGELSCAN}_{21} * \frac{\text{CN\_WELPRC} - \text{CN\_WPRCLAG}}{\text{CN\_WPRCLAG}})}{\quad} \quad (3)$$

where,

CN\_PRODUC = Canadian domestic natural gas production in year y (Bcf)  
 OGRESCAN<sub>2y</sub> = Canadian natural gas reserves in beginning-of-year y (from OGSM in Bcf)  
 OGPRRCAN<sub>2y</sub> = expected natural gas production-to-reserves ratio in Canada in year y (from OGSM as fraction)  
 OGELSCAN<sub>21</sub> = estimated short run price elasticity of extraction for Canada (from OGSM)  
 CN\_WELPRC = average Canadian wellhead price in year y (dollars per Mcf)  
 CN\_WPRCLAG = average Canadian wellhead price in year y-1 (dollars per Mcf) [for the first forecast year this is set to CN\_WELPRC89, (Appendix E)]

The amount of natural gas available to flow into the United States from Canada is calculated as:

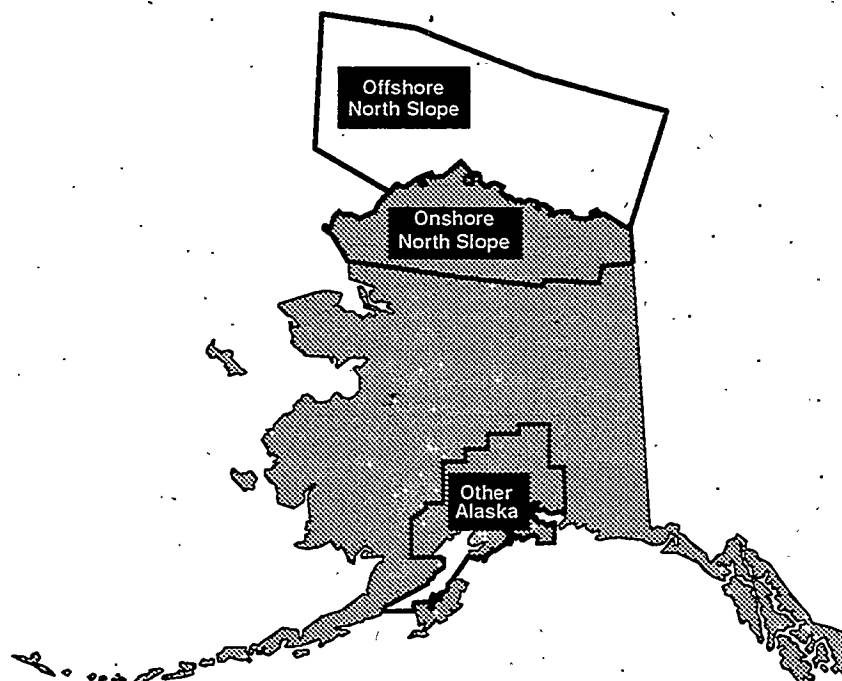
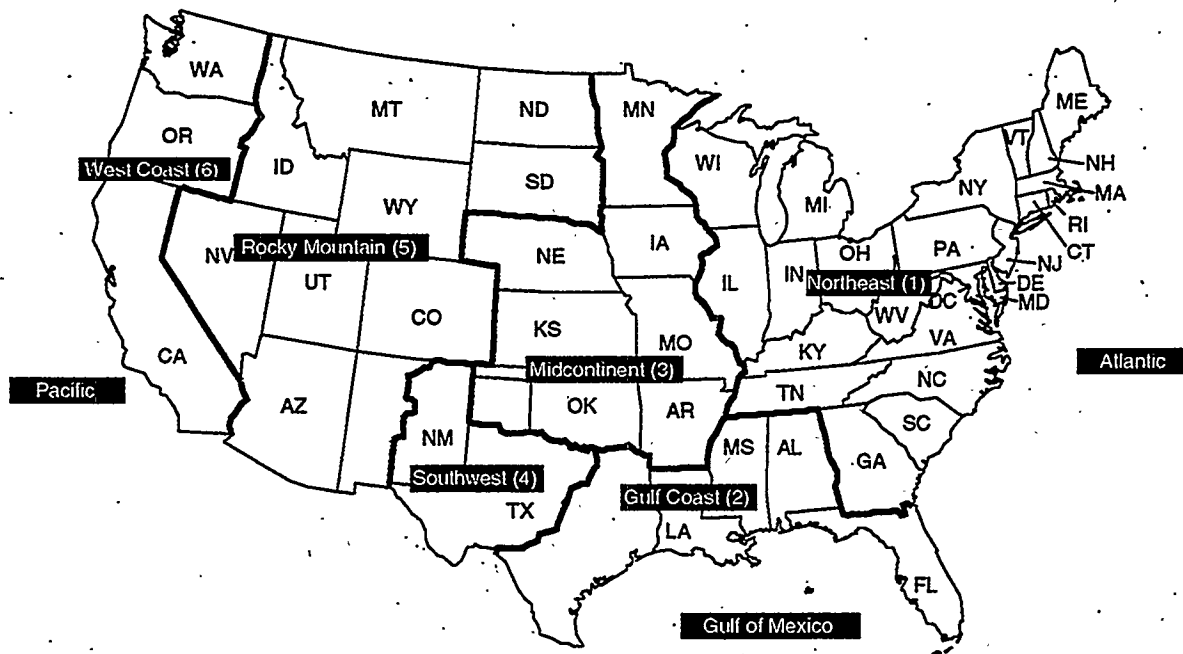
$$\text{TOT\_BRDQ} = \text{CN\_PRODUC} - \frac{\text{OGCNCON}_{2y} - (\text{CANFLO\_OUT}_y + \sum_{i=1}^6 \text{OGQNGEXP}_{i,y}) * (1 - \text{OGCNEXLOSS})}{1 - \text{OGCNDMLLOSS}} \quad (4)$$

where,

TOT\_BRDQ = total gas available to flow into the United States from Canada (measured at the wellhead), (Bcf)

<sup>21</sup>Other supplemental supplies include propane-air, refinery gas, coke oven gas, manufactured gas, biomass gas, and air injection for Btu stabilization.

**Figure 3-5. Oil and Gas Supply Model (OGSM) Regions**



CN_PRODUC	=	Canadian domestic natural gas production in year y (Bcf)
OGCNCON <sub>2,y</sub>	=	consumption of natural gas in Canada (from OGSM in Bcf)
CANFLO_OUT <sub>y</sub>	=	gas flowing into Canada from the U.S. which was originally produced in Canada <sup>22</sup> in year y (Bcf)
OGQNGEXP <sub>i,y</sub>	=	exports of gas from the United States into Canada by border crossing i in year y (from OGSM in Bcf)
OGCNDMLOSS	=	percentage of gas produced in Canada to satisfy Canadian demand that is consumed in transit (from OGSM as fraction)
OGCNEXLOSS	=	percentage of gas produced in the United States to satisfy Canadian demand that is consumed in transit within Canada (from OGSM as fraction)

If the value of TOT\_BRDQ exceeds the total effective capacity of the natural gas pipelines used to flow gas into the United States from Canada, then it is assumed that the share of TOT\_BRDQ which will flow across each of the representative border crossings in the model (CN\_FLOSHR) will be equivalent to that border crossing's share of the total effective capacity. Under most likely model scenarios this has been shown to be true through the 2010 time frame. However, if available Canadian supplies are less than total effective pipeline capacity across the border, the allocation of TOT\_BRDQ to each of the six border crossings is calculated as follows:

$$CN\_FLOSHR_i = \frac{(OGCNPARM1 * \frac{CN\_FLOLAG_i}{\sum_{i=1}^6 CN\_FLOLAG_i}) + (1-OGCNPARM1) * \frac{(CN\_BRDPRC_i - OGCNPMARKUP_i)^{OGCNPARM2}}{\sum_{i=1}^6 (CN\_BRDPRC_i - OGCNPMARKUP_i)^{OGCNPARM2}}}{1} \quad (5)$$

where,

CN_FLOSHR <sub>i</sub>	=	the share of the gas available to flow from Canada into the United States to flow across border crossing i (fraction)
CN_FLOLAG <sub>i</sub>	=	the amount of gas which flowed from Canada into the United States across border crossing i in the previous year (adjusted for pipeline additions <sup>23</sup> in year y), (Bcf)
OGCNPARM1	=	parameter which reflects the importance of the historical flow pattern in the determination of actual allocation of gas (from OGSM, 0 < OGCNPARM1 < 1)
OGCNPARM2	=	parameter which reflects the responsiveness of the flow pattern to differentials in border prices netbacked to the wellhead (from OGSM, OGCNPARM2 = 1)
CN_BRDPRC <sub>i</sub>	=	the market price at border crossing i (dollars per Mcf)
OGCNPMARKUP <sub>i</sub>	=	assumed markup from the average Canadian wellhead price to border crossing i (from OGSM in dollars per Mcf)

If the resulting shares indicate flow levels across some border crossings which exceed their maximum effective capacity level, then the "unflowable" portion is made available at border crossings with available pipeline capacity, and the values for the variable CN\_FLOSHR are adjusted accordingly. These shares are ultimately used in the calculation of the Canadian wellhead price:

$$CN\_WELPRC = \sum_{i=1}^6 CN\_FLOSHR_i * (CN\_BRDPRC_i - OGCNPMARKUP_i) \quad (6)$$

where,

<sup>22</sup>A significant amount of natural gas flows into Minnesota from Canada on an annual basis only to be routed back to Canada through Michigan (and a very small amount through Montana). The amount of gas entering the United States that is not imported from Canada, and the percentage of this amount which travels back through Michigan, are set at exogenously specified levels for the forecast (Appendix E -- CANFLO\_IN, CANFLO\_SHR).

<sup>23</sup>The 1990 capacity additions for the Canadian import arcs are specified exogenously (Appendix E, CN\_NEWCAP90).

CN_WELPRC	=	Canadian wellhead price (dollars per Mcf)
CN_FLOSHR <sub>i</sub>	=	the share of the gas available to flow from Canada into the United States to flow across border crossing i (fraction)
CN_BRDPRC <sub>i</sub>	=	the market price at border crossing i (dollars per Mcf)
OGCNPMARKUP <sub>i</sub>	=	assumed markup from the average Canadian wellhead price to border crossing i (from OGSM in dollars per Mcf)

The system of equations which represents the pricing and flow of gas from Canada into the United States can not be solved in a top/down fashion, but requires an iterative process due to the interrelationships involved. Furthermore, the solution algorithm used within the NGTDM requires prespecified supply curves (or fixed supply levels) at each border crossing before solving. A short-term supply curve is generated for a single border crossing point, through the use of the equations shown above, by holding the border prices for the other crossing points at their solution values from the previous NEMS iteration (or the previous year, in the first iteration).<sup>24</sup>

### Supply Curves for Domestic Dry Gas Production

Most of the parameters for generating short-term supply curves for dry natural gas production are provided to the NGTDM by the OGSM. The six onshore OGSM regions within the contiguous United States do not generally share common borders with the NGTDM regions. As was done with the EMM regions, the NGTDM represents onshore supply for the 17 regions resulting from overlapping the OGSM and NGTDM regions (Figure 3-6).

These supply curves are defined as being net of lease and plant fuel consumption (i.e., the amount of dry gas available for market after any necessary processing and before being transported via pipeline). Within the NGTDM, dry gas production is delineated by two categories, nonassociated and associated-dissolved. Nonassociated gas is largely defined as gas that is produced from gas wells, and is assumed to vary in response to a change in the natural gas price. Whereas, associated-dissolved gas is defined as gas that is produced from oil wells, and can be classified as a byproduct in the oil production process.

Total domestic natural gas production is the sum of nonassociated and associated-dissolved production. Associated-dissolved gas production is provided by OGSM for the 17 NGTDM/OGSM onshore regions and the 3 offshore regions, while production parameters are provided by OGSM for the NGTDM to generate nonassociated gas production curves for the same regions. Within the NGTDM, total natural gas production curves are generated by adding the associated-dissolved production to the nonassociated gas production curves, effectively shifting the production curves to the right along the quantity axis.<sup>25</sup>

The NGTDM includes the option of selecting one of three different functional forms for the supply curve for nonassociated dry natural gas production (net of lease and plant fuel) in the domestic onshore and offshore regions. All three forms are constructed from a common key point (or price/quantity pair) which is based on an expected extraction rate, estimated in the OGSM. The "expected" or base production level from an onshore region is calculated as follows:

$$\text{BASE\_Q}_r = \text{OGRESNGON}_r \cdot \text{OGPRRNGON}_r \cdot \text{PER} \quad (7)$$

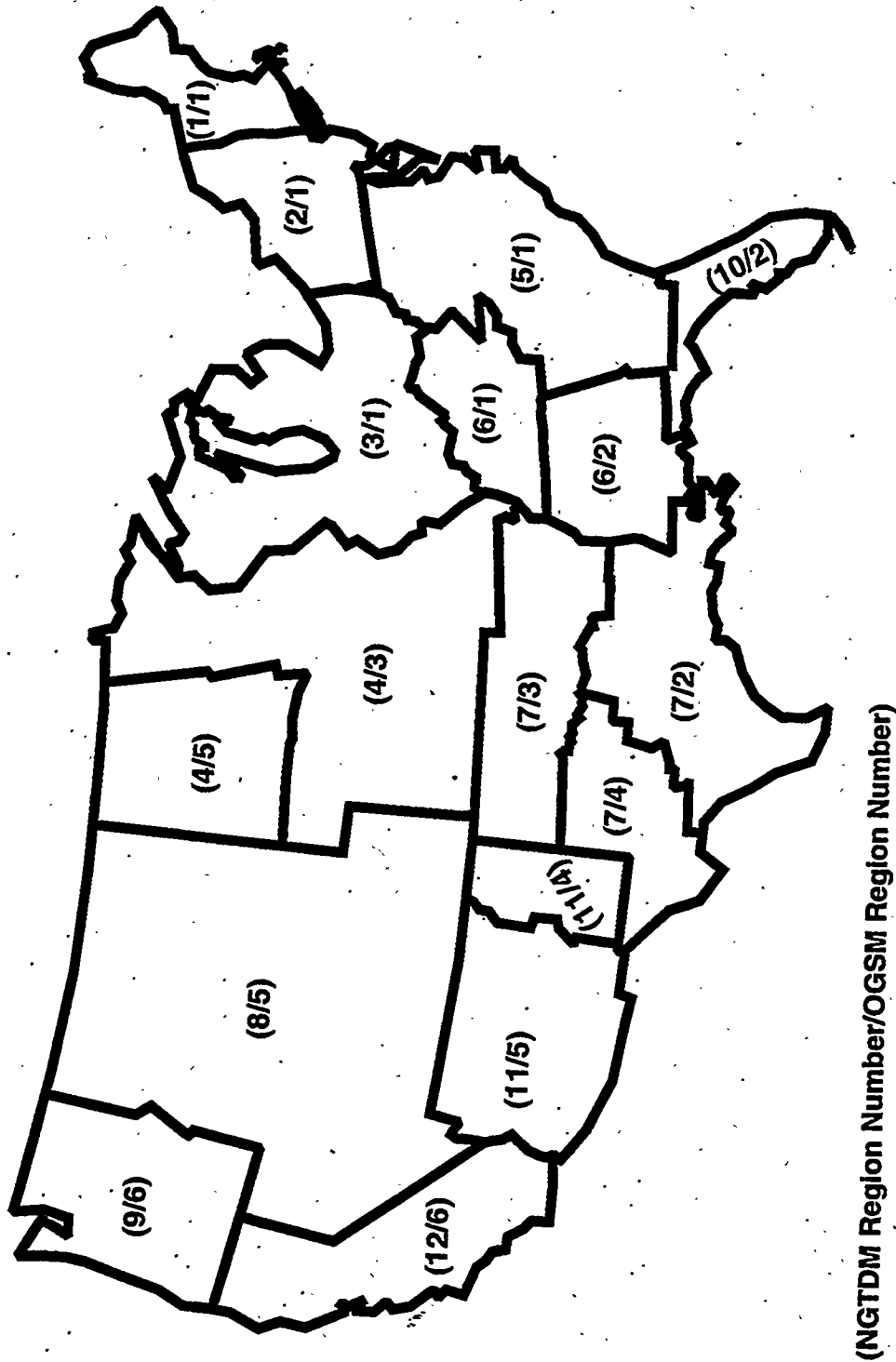
where,

BASE_Q <sub>r</sub>	=	expected nonassociated production (net of lease and plant), NGTDM/OGSM region r (Bcf)
OGRESNGON <sub>ry</sub>	=	dry gas reserves at the beginning-of-year y in onshore NGTDM/OGSM region r (from OGSM in Bcf)

<sup>24</sup>An initial value is exogenously specified for CN\_BRDPRC (Appendix E, CN\_BRDPRC90).

<sup>25</sup>For convenience in the code, the synthetic production of gas from coal is similarly added to the total production curve.

**Figure 3-6. Natural Gas Transmission and Distribution Model/Oil and Gas Supply Model (NGTDM/OGSM) Regions**



(NGTDM Region Number/OGSM Region Number)

$OGPRRNGON_{r,y}$  = expected extraction rate in year y from reserves in onshore NGTDM/OGSM region r (from OGSM as fraction)  
 $PER$  =  $1 - PCTLSE\_SUPL_r - PCTPLT\_PADD_{p,y}$ , a factor for netting lease and plant fuel out of dry gas production (fraction)  
 $PCTPLT\_PADD_{p,y}$  = percent of dry gas production which is consumed in natural gas processing plant operations, for PADD<sup>26</sup> region p in year y (from the PMM as fraction)  
 $PCTLSE\_SUPL_r$  = percent of dry gas production which is consumed in well, field, and lease operations [Appendix E, fraction]  
 Note: For the offshore regions  $BASE\_Q_r = OGRESNGOF_{r,y} * OGPRRNGOF_{r,y}$

The price ( $BASE\_P_r$ ) associated with  $BASE\_Q_r$  is a function of the previous year's wellhead price<sup>27</sup> and a multiplicative benchmark factor ( $PSHIFT\_SCALE$ ). The benchmark factor is used to calibrate the model to an historical (or forecasted, as represented in the *Short-Term Energy Outlook (STEO)*) national average natural gas wellhead price.<sup>28</sup> This benchmark factor represents the ratio between the national average wellhead price solved by the model and the corresponding historical or STEO wellhead price. (It is endogenously defined within the NGTDM and held constant throughout the forecast period.) The amount the production will vary from  $BASE\_Q_r$  is a function of how different the wellhead price (at which the function is being evaluated) is from  $BASE\_P_r$ . The calculation of the additional quantity of production ( $DEL\_Q_r$ )<sup>29</sup> which would result at a given wellhead price ( $VALUE$ ) is different under each of the three options.<sup>30</sup> Options one and two are presented below, with option 3 following.

#### Option 1

$$DEL\_Q_r = BASE\_Q_r * OGELSNNGON_{r,y} * (VALUE - BASE\_P_r) / BASE\_P_r \quad (8)$$

where,

$OGELSNNGON_{r,y}$  = estimated short-term price elasticity (from OGSM), for offshore regions the variable  $OGELSNNGOF_r$  is used

#### Option 2:

$$DEL\_Q_r = BASE\_Q_r * ELAS * (VALUE - BASE\_P_r) / BASE\_P_r \quad (9)$$

where,

If  $VALUE \geq BASE\_P_r$ ,

$ELAS = PARM\_SUPCRV2_1$ , (user specified short-term price elasticity, assumed to be less than one, Appendix E)

If  $VALUE < BASE\_P_r$ ,

$ELAS = PARM\_SUPCRV2_2$ , (user specified short-term price elasticity, assumed to be greater than one, Appendix E)

<sup>26</sup>Petroleum Administration for Defense Districts (PADD) are the regions modeled in the PMM. The PADD region which most overlaps the indicated NGTDM/OGSM region is used in this and other equations, as necessary.

<sup>27</sup>For the first forecast year, the value for  $BASE\_P$  is set to the 1989 national average wellhead price (Appendix E --  $WPRLAGON$ ,  $WPRLAGOF$ ).

<sup>28</sup>For the AEO96 reference case, the model was calibrated to the natural gas wellhead price published in the *Short-Term Energy Outlook* (3rd Quarter), DOE/EIA-0202(95,3Q) for 1996.

<sup>29</sup>If  $DEL\_Q_r$  is negative, the resulting production level will be less than  $BASE\_Q_r$ .

<sup>30</sup>A model user can select one of the three functional forms for the supply curves by setting the variable  $TYP\_SUPCRV$  equal to either 1, 2, or 3, accordingly. For generating the forecast published in the *Annual Energy Outlook 1996*, option 3 was selected.



Option 1 is symmetric for price increases and decreases. Option 2 assumes production responds more strongly to price declines than to increases. The justification for incorporating a different elasticity above and below the "expected" production level on the supply curve is that producers have a vested interest in selling close to their planned for or expected production level. Much lower than anticipated gas sales do not allow the producer the necessary cash flow to stay in business. In such cases, prices would be lowered enough to increase sales and resulting revenues. However, there are practical upper limits on the rates of extraction from reserves, causing an upward push on the price when there are market pressures to produce at elevated extraction rates.

Option 3 is a combination of Options 1 and 2. In a close range around the base point (plus or minus an assumed percentage — $PARM\_SUPCRV3_1$ — of the base quantity), the short-term wellhead price elasticity ( $PARM\_SUPCRV3_2$ ) does not change from one side of the base point to the other (as in Option 1), but is assumed to be highly inelastic. Outside of this range, the short-term price elasticities are set to the same values used under Option 2. However, these segments of the curve are shifted (left, below the base price, and right, above the base price) to intersect the end points of the segment of the curve running through the base point, as follows:

### Option 3

$$DEL\_Q_r = (BASE\_Q_r * PARM) + (1 + PARM) * BASE\_Q_r * ELAS * (VALUE - BASE\_P_r) / BASE\_P_r \quad (10)$$

where,

If VALUE is within the range  $BASE\_P_r \pm (BASE\_P_r * PARM\_SUPCRV3_1 / PARM\_SUPCRV3_2)$

$$PARM = 0.$$

$$ELAS = PARM\_SUPCRV3_2$$

If VALUE is greater than  $BASE\_P_r + (BASE\_P_r * PARM\_SUPCRV3_1 / PARM\_SUPCRV3_2)$

$$PARM = + PARM\_SUPCRV3_1$$

$$ELAS = PARM\_SUPCRV2_2$$

If VALUE is less than  $BASE\_P_r - (BASE\_P_r * PARM\_SUPCRV3_1 / PARM\_SUPCRV3_2)$

$$PARM = - PARM\_SUPCRV3_1$$

$$ELAS = PARM\_SUPCRV2_1$$

The assumed values for all of the parameters and elasticities shown above are referenced in Appendix E.

Figure 3-7 graphically depicts an example of how a region's supply curve would appear under each of the three options.

After establishing a value for  $DEL\_Q_r$  for a specified wellhead price in a given region, the corresponding total dry gas production would be calculated as:

$$NGPRD\_L48 = BASE\_Q_r + DEL\_Q_r + ((ADGPRDON_r + OGCCAPPRD_r) * PER) \quad (11)$$

where,

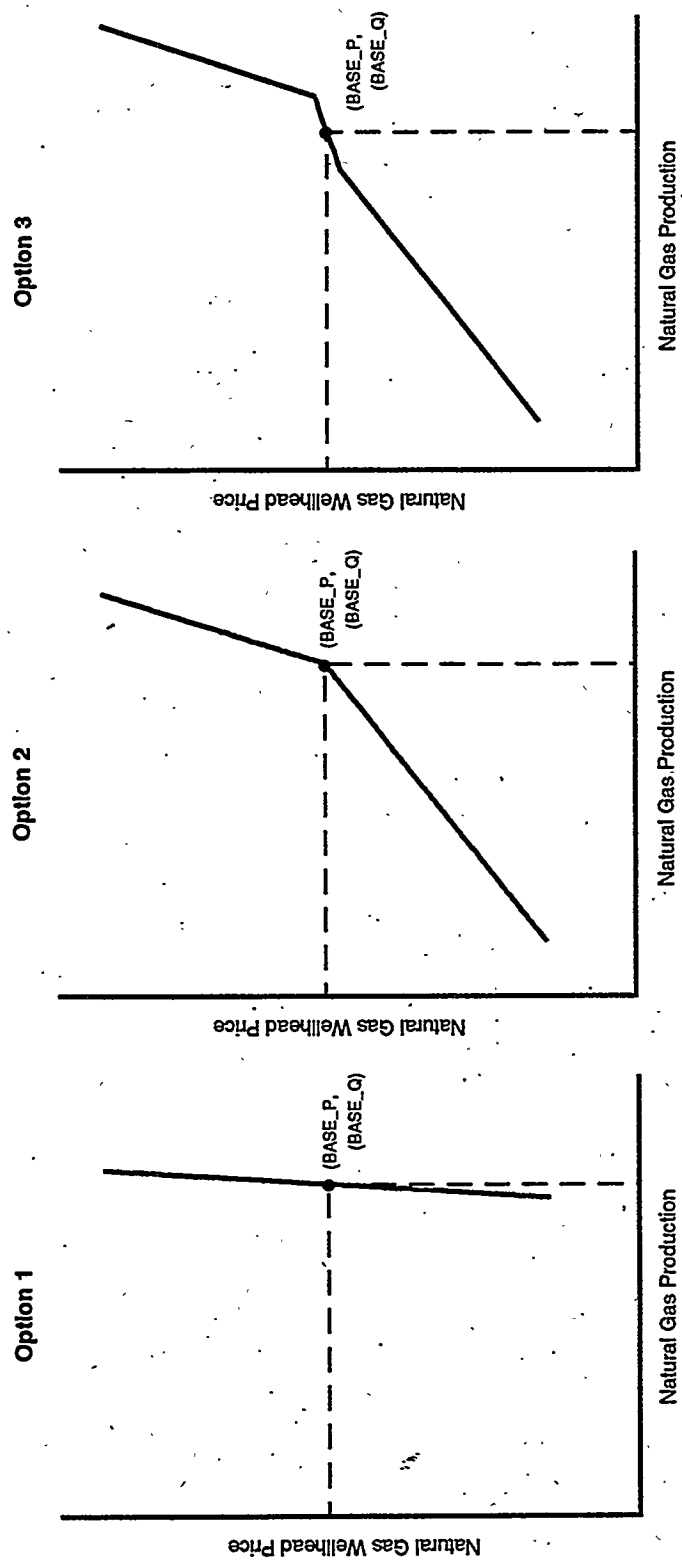
NGPRD\_L48 = dry gas production in onshore NGTDM/OGSM region r (BCF)

OGCCAPPRD = dry gas production in onshore NGTDM/OGSM region r attributable to the Climate Change Action Plan's coalbed methane outreach program, as set in OGSM (BCF)

For an offshore region, the corresponding variables used in the code are NGPRD\_OCS and ADGPRDOF\_r (with PER set to 1).

For control purposes, upper and lower limits are placed on the nonassociated dry gas production levels established within the NGTDM. The lower and upper limits imposed on nonassociated gas production in each NGTDM/OGSM onshore and offshore region are  $BASE\_Q$  times  $PARM\_MINPR$  and  $PARM\_MAXPR$ , respectively (Appendix E).

**Figure 3-7. Nonassociated Natural Gas Supply Curve Options**



## Alaskan Natural Gas Module

The NEMS demand models provide a forecast of natural gas consumption for the total Pacific Census Division, which includes Alaska. Currently natural gas which is produced in Alaska cannot be transported to the Lower 48 States via pipeline. Therefore, the production and consumption of natural gas in Alaska is handled separately within the NGTDM from the contiguous States. Estimates of contiguous Pacific Division consumption levels are derived within the NGTDM by first estimating Alaskan natural gas consumption for all sectors, and then subtracting these from the core market consumption levels in the Pacific Division provided by the NEMS demand models. The use of natural gas in compressed natural gas vehicles in Alaska is assumed to be negligible. The consumption of gas by Alaskan residential and commercial customers is a function of a forecast for the number of customers (exogenously derived) and the landed cost of crude oil imports (forecast within the NEMS):

$$(res): QALK\_NONU\_F_d = EXP(AK\_C_1) * WOPLAG^{AK\_C_2} * AK\_RN_y^{AK\_C_3} / 1000. \quad (12)$$

$$(com): QALK\_NONU\_F_d = EXP(AK\_D_1) * WOPLAG^{AK\_D_2} * AK\_CN_y^{AK\_D_3} / 1000. \quad (13)$$

where,

$QALK\_NONU\_F_d$	=	consumption of natural gas by residential (d=1) or commercial (d=2) customers in Alaska (Bcf)
$WOPLAG$	=	landed cost of crude oil in the previous forecast year [the 1989 value used in forecast year 1990 (WOP89) is a data input, Appendix E] (dollars per barrel)
$AK\_C$	=	estimated parameters for residential consumption equation (Appendix F, Table F1)
$AK\_D$	=	estimated parameters for commercial consumption equation (Appendix F, Table F1)
$AK\_RN_y$	=	number of residential customers (exogenously specified, Appendix F, Table F2)
$AK\_CN_y$	=	number of commercial customers (exogenously specified, Appendix F, Table F2)

Gas consumption by Alaskan industrial customers is a function of the landed cost of crude oil imports and time:

$$(ind): QALK\_NONU\_F_d = ( AK\_E_1 + (AK\_E_2 * WOPCUR) + (AK\_E_3 * (T)) ) / 1000. \quad (14)$$

where,

$QALK\_NONU\_F_d$	=	consumption of natural gas by industrial customers (d=3), (Bcf)
$WOPCUR$	=	average national landed cost of crude oil in the current forecast year
$AK\_E$	=	estimated parameters for industrial consumption equation (Appendix F, Table F1)
$T$	=	time parameter, where $T=1$ for 1969 (the first historical data point) and $T=CNTYR+21$ in forecast year $CNTYR$ (where $CNTYR$ equals 1 for 1990).

At a sectoral level, Alaskan consumption is disaggregated into the total delivered to customers in South Alaska ( $AK\_CONS\_S$ ) versus a North Alaska ( $AK\_CONS\_N$ ) total using historically derived shares (Appendix E,  $AK\_PCTSOUTH$ ). This distinction is needed for the derivation of natural gas production forecasts for the north and south regions [not accounting for the additional production necessary should the Alaskan Natural Gas Transportation System (ANGTS) open], as follows:

$$(S. AK): AK\_PROD_{r=1} = (EXPJAP + AK\_CONS\_S) / (1 - AK\_PCTLSE_{r=1} - AK\_PCTPLT_{r=1} - AK\_PCTPIP_{r=1}) \quad (15)$$

$$(N. AK): AK\_PROD_{r=2} = AK\_CONS\_N / (1 - AK\_PCTLSE_{r=2} - AK\_PCTPLT_{r=2} - AK\_PCTPIP_{r=2}) \quad (16)$$

where,

$AK\_PROD_r$	=	dry gas production in South (r=1) or North (r=2) Alaska (Bcf)
$AK\_CONS\_S$	=	total gas consumption by customers in South Alaska (Bcf)

AK_CONS_N	=	total gas consumption by customers in North Alaska (Bcf)
EXPIAP	=	quantity of gas liquefied and exported to Japan (from OGSM in Bcf)
AK_PCTLSE <sub>r</sub>	=	assumed percent of gas production which is consumed in lease operations in region r (fraction)
AK_PCTPLT <sub>r</sub>	=	assumed percent of gas production which is consumed in plant operations in region r (fraction)
AK_PCTPIP <sub>r</sub>	=	assumed percent of gas production which is consumed as pipeline fuel in region r (fraction)

The variables for AK\_PCTLSE, AK\_PCTPLT, and AK\_PCTPIP are based on historical percentages (Appendix E) and are held constant throughout the forecast, with the exception that PCTLSE is decreased by 50 percent should ANGTS become fully operational. (These variables are also used to estimate the consumption levels for pipeline fuel and lease and plant fuel in Alaska.) The OGSM provides a forecast of natural gas exports to Japan, the level of flow through ANGTS which would reach the contiguous U.S. border when and if it is connected, and the maximum production level for South Alaska (currently used only as a verification check in the NGTDM). The production of natural gas in Alaska which is necessary to support ANGTS (AK\_PROD<sub>res</sub>) is derived in the NGTDM using the flow level at the border established in OGSM, and assumed values for PCTLSE, PCTPLT, and PCTPIP related to production to be marketed via ANGTS.

Estimates for natural gas wellhead and end-use prices in Alaska are roughly estimated in the NGTDM for proper accounting, but have a very limited impact on the NEMS system. The average Alaskan wellhead price over the North and South regions (not accounting for the impact should ANGTS be connected) is calculated as:

$$AK\_WPRC = AK\_F_1 + (AK\_F_2 * WPRLAG) + (AK\_F_3 * (AK\_PROD_1 + AK\_PROD_2)) \quad (17)$$

where,

AK_WPRC	=	average Alaskan natural gas wellhead price (dollars per Mcf)
AK_PROD <sub>r</sub>	=	dry gas production in Alaskan region r (1=South; 2= North) (Bcf)
WPRLAG	=	average Alaskan natural gas wellhead price in previous forecast year (dollars per Mcf) [the 1989 value used in forecast year 1990 is WPR89, Appendix E]
AK_F	=	estimated parameters (Appendix F, Table F1)

However, if ANGTS is connected, the wellhead price in North Alaska is overwritten to be equal to the price at the U.S./Canadian border crossing point, most representative of where ANGTS will connect, plus an assumed markup (Appendix E, ANGTS\_TAR). With the exception of the industrial sector, end-use prices are set equal to the average wellhead price resulting from the equation above plus a fixed markup (Appendix E -- AK\_RM, AK\_CM, AK\_EM). The Alaskan industrial sector price is calculated as:

$$PALK\_NONU\_F_s = AK\_G_1 + (AK\_G_2 * WOPCUR) \quad (18)$$

where,

PALK_NONU_F <sub>s</sub>	=	price of natural gas to Alaskan industrial customers (s=3), (dollars per Mcf)
WOPCUR	=	landed price of crude oil in current forecast year (dollars per barrel)
AK_G	=	estimated parameters (Appendix F, Table F1)

Historically, the industrial price was shown to vary more in response to the crude oil price and much less in response to the natural gas wellhead price.

## 4. Overview of Solution Methodology

The previous chapter described the function of the NGTDM within the NEMS. This chapter will present an overview of the NGTDM model structure and of the methodologies used to represent the natural gas transmission and distribution industries. First, a detailed description of the network used in the NGTDM to represent the U.S. natural gas pipeline system is presented. Next, a general description of the interrelationships between the modules within the NGTDM is presented, along with an overview of the solution methodology used by each module.

### NGTDM Regions and the Pipeline Flow Network

#### *General Description of the NGTDM Network*

In the NGTDM, a transmission and distribution network (Figure 4-1) simulates the interregional flow of gas in the contiguous United States. This network is a simplified representation of the physical natural gas pipeline system and establishes the possible interregional transfers to move gas from supply sources to end-users. Each NGTDM region contains one transshipment node—a junction point representing flows coming into and out of the region. Nodes have also been defined at the Canadian and Mexican borders. Arcs connecting the transshipment nodes are defined to represent flows between these nodes; and thus, to represent interregional flows. Each of these interregional arcs represents an aggregation of pipelines that are capable of moving gas from one region into another region. Bidirectional flows are allowed in cases where the aggregation includes some pipelines flowing one direction and other pipelines flowing in the opposite direction.<sup>31</sup> Bidirectional flows can also be the result of directional flow shifts within a single pipeline system due to seasonal variations in flows.

Flows are further represented by establishing arcs from the transshipment node to each demand sector/subregion represented in the NGTDM region. A demand group in a particular NGTDM region can only be satisfied by gas flowing from that same region's transshipment node. Similarly, arcs are also established from supply points into transshipment nodes. The supply from each NGTDM/OGSM region is directly available to only one transshipment node, through which it must first pass if it is to be made available to the interstate market (at an adjoining transshipment node).

Figure 4-2 shows an illustration of all possible flows into and out of a transshipment node. Each transshipment node has one or more arcs to represent flows from or to other transshipment nodes. The transshipment node also has an arc representing flow to each end-use sector in the region (residential, commercial, industrial, electric generators, and transportation), including separate arcs to each electric generator subregion. Arcs are also established from nodes at the international borders to represent exports. Each transshipment node has one or more arcs flowing in from each supply source represented. These supply points may represent onshore or offshore production, liquefied natural gas imports, synthetic natural gas production, gas produced in Alaska and transported via the Alaska Natural Gas Transportation System, or Canadian or Mexican imports in the region. In addition, each onshore supply region also includes any synthetic natural gas produced from coal, as well as other supplemental supplies. Finally, annual net underground storage withdrawals, transported under firm and interruptible service, are accounted for at each transshipment node. Also accounted for but not presented in Figure 4-2 are discrepancies (i.e., historically observed differences between independently reported natural gas supply and disposition levels).

Once all of the types of end-use destinations and supply sources are defined for each transshipment node, a general network structure results. Each transshipment node does not necessarily have all supply source types flowing in, or all demand source types flowing out. For instance, the transshipment nodes at the Canadian border may only have Canadian supply defined going into the node. Also, some transshipment nodes will have liquefied natural gas

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<sup>31</sup>Historically, one out of each pair of bidirectional arcs in Figure 4-1 represents a relatively small amount of gas flow during the year. These arcs are referred to as "the bidirectional arcs" and are identified as going from 9 to 8, 11 to 8, 4 to 8, 11 to 7, 4 to 7, 3 to 4, 5 to 6, 5 to 3, 2 to 3, 2 to 5, 6 to 7, and 1 to 2. Minimum flows constraints are established for these arcs at historically observed flow levels.

Figure 4-1. Natural Gas Transmission and Distribution Model Network

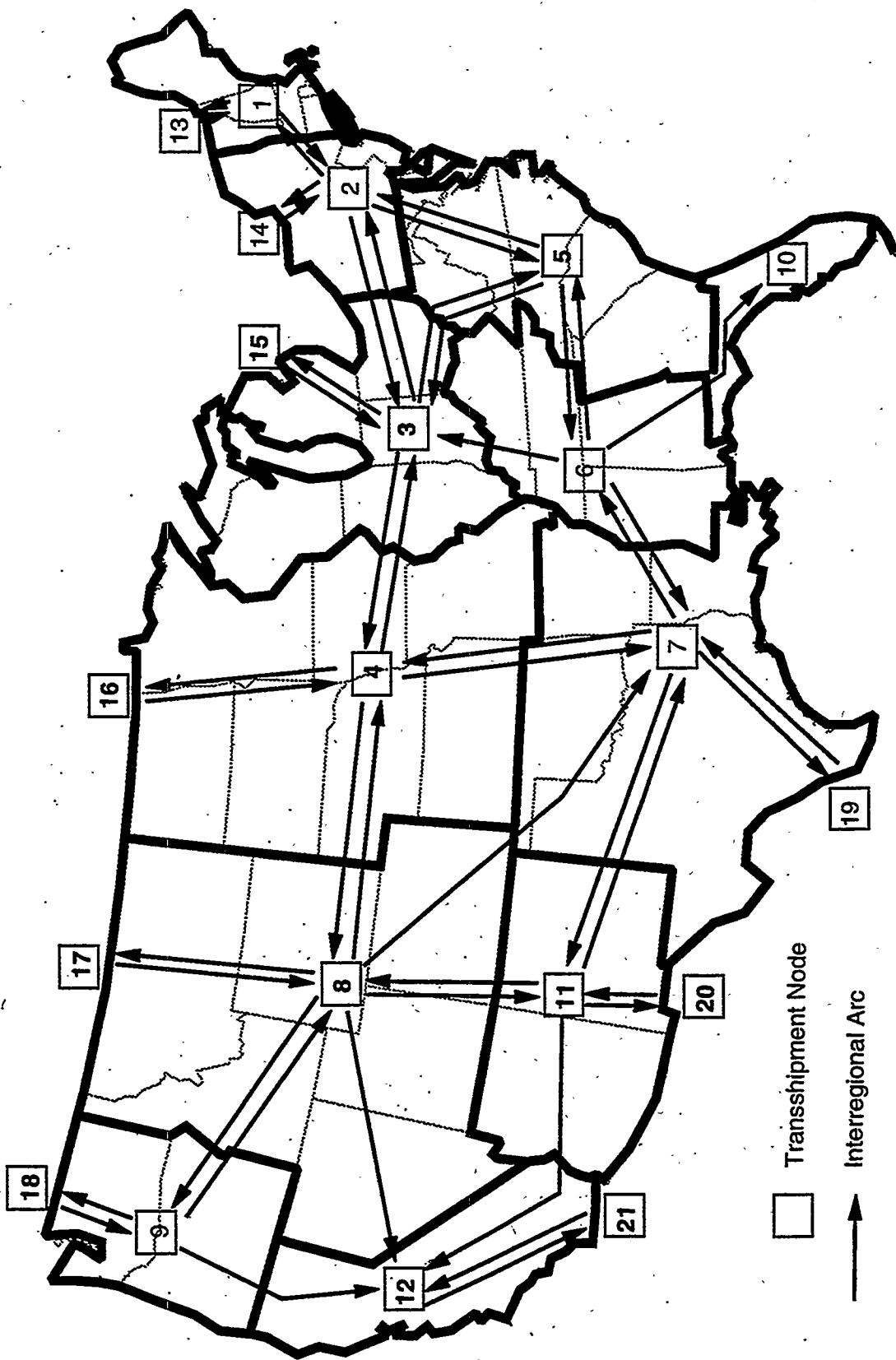
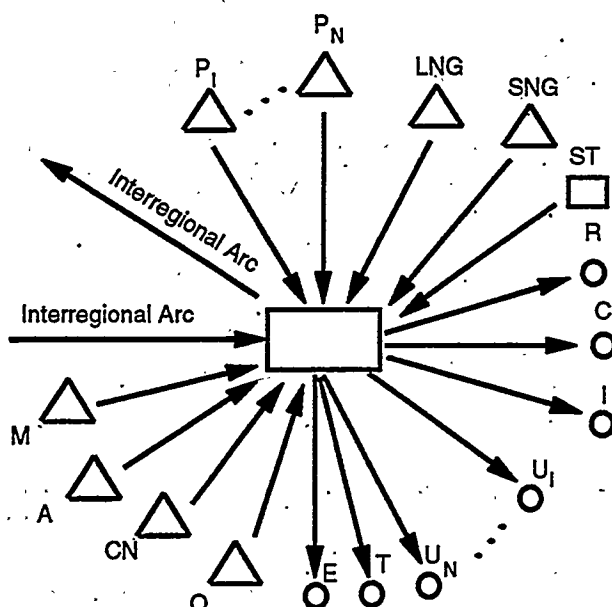


Figure 4-2. Transshipment Node



□ - Transshipment Node

△ - Supply Point

○ - Demand Point

□ - Storage Point

$P_i$  - Production in NGTDM/OGSM Region  $i$

LNG - Liquefied Natural Gas

SNG - Synthetic Natural Gas

O - Offshore Supplies

CN - Canadian Supplies

A - Alaskan Supplies

M - Mexican Supplies

R - Residential Demand

C - Commercial Demand

I - Industrial Demand

$U_i$  - Electric Utility Demand in NGTDM/EMM Region  $i$

T - Transportation Demand

E - Exports

ST - Net Storage Withdrawals

available while others will not. The specific end-use sectors and supply types specified for each transshipment node in the network are listed in Table 4-1. This table also indicates in tabular form the mapping of Electricity Market Model regions and Oil and Gas Supply Model regions to NGTDM regions, (Figures 3-4 and 3-7 in Chapter 3).

As described in earlier chapters, there are significant differences in market structure and dynamics between the firm and interruptible service markets. The basic network structure separately represents the flow of gas within the firm and interruptible service markets within the Annual Flow Module. Conceptually this can be thought of as two parallel networks, with three areas of overlap. First, the firm and interruptible transmission service flows along each arc are interrelated and their sum is constrained to the pipeline capacity available along the arc. Second, the firm and interruptible service networks share common supply sources. At each supply source there is a single price regardless of whether the supplies are used to meet core or noncore demand (or both), because it is assumed that the supply component of the market will remain fully competitive.<sup>32</sup> Third, the quantity of net injections transported under interruptible service into underground storage is equal to the net withdrawals from storage in the same region that are to be transported under firm service. The actual levels of underground storage injections and withdrawals associated with the firm and interruptible service markets are determined within the Capacity Expansion Module (since it contains a seasonal representation) and used within the Annual Flow Module.

### ***Specifications of a Network Arc***

Each arc of the network has associated parameters (inputs) and model variables (outputs). The parameters that define an arc are the pipeline direction, available capacity, the tariffs, the percentage of gas which travels on the arc that is lost or used (in power compressor stations) along the way, a mileage indicator, and a minimum flow level (Figure 4-3). In the case of bidirectional arcs, the arc with an historically lower flow rate is identified as a "bidirectional" arc for special handling.

Once a model solution has been reached (i.e., the quantity of the natural gas flow along each interregional arc is determined), pipeline fuel use associated with interregional transfers (from transshipment node to transshipment node) can be computed for each arc by multiplying the percentage loss of gas (given by the efficiency parameter) by the flow along the arc. In turn, the emissions (carbon, carbon monoxide, carbon dioxide, sulfur oxides, nitrogen oxides, volatile organic compounds, and methane) associated with the consumption of pipeline fuel can be estimated. (Details are given in Chapter 5.)

For the firm service market the pipeline tariff (indicated as "TAR" in subsequent equations) is a function of two basic parameters: a usage fee and the revenue the pipeline is collecting from customers who have reserved capacity on the pipeline. Since the NGTDM does not explicitly represent the capacity reserved on a pipeline, this revenue is allocated over the amount of gas that is expected to flow on the arc rather than the amount of space reserved. Therefore, the reservation fee (the per-unit fee for reserving capacity on a pipeline) is not explicitly calculated. It is instead approximated as the total revenue from reservation fees divided by the amount of gas expected to flow. Thus, the total pipeline tariff for the firm service market is the sum of the usage fee and this approximation of the reservation fee. For the interruptible service market, the tariff parameter is simply a per-unit usage fee (as specified by the Pipeline Tariff Module). It is not necessary for the firm and interruptible usage fees to be equal.

For the arcs from the transshipment nodes to the end-use sectors, the parameters defined are capacities, tariffs, and the percentage of gas used in compressor stations. The tariffs here represent the sum of several charges or adjustments, including interstate pipeline tariffs in the region, intrastate pipeline tariffs, and distributor markups when applicable. The model variable associated with each of these arcs is the flow along the arc, which is equal to the amount of demand satisfied plus gas consumed in compressor stations. For arcs from supply points to transshipment nodes, the parameters are capacities, tariffs, minimum flows, and compressor station usage. In this case the tariffs theoretically represent gathering charges, but in actuality are used to align model results with historical prices in each

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<sup>32</sup>Due in part to the seasonal load differences between core and noncore consumption, there are reasons to believe that the supply prices to the two markets are different on an annual basis. Structurally, the model is designed to handle such a supply price differential, but the supporting data have yet to be developed. However, more recent trends show less variation in seasonal wellhead prices than had previously been observed.



**Table 4-1. Demand and Supply Types at Each Transshipment Node in the Network**

Transshipment Node	Demand Types	Supply Types
1	R, C, I, T, U(1/7)	P(1/1), LNG Everett Mass.
2	R, C, I, T, U(2/6), U(2/3)	P(2/1)
3	R, C, I, T, U(3/1), U(3/4)	P(3/1), SNG
4	R, C, I, T, U(4/5), U(4/10)	P(4/3), P(4/5)
5	R, C, I, T, U(5/1), U(5/3), U(5/9)	P(5/1), LNG Cove Pt Maryland, LNG Elba Island Georgia, Atlantic Offshore
6	R, C, I, T, U(6/1), U(6/9)	P(6/1), P(6/2)
7	R, C, I, T, U(7/2), U(7/10)	P(7/2), P(7/3), P(7/4), LNG Lake Charles Louisiana, Offshore Louisiana, Gulf of Mexico
8	R, C, I, T, U(8/11), U(8/12)	P(8/5)
9	R, C, I, T, U(9/11)	P(9/6)
10	R, C, I, T, U(10/8)	P(10/2)
11	R, C, I, T, U(11/12)	P(11/4), P(11/5)
12	R, C, I, T, U(12/13)	P(12/6); Pacific Offshore
13	Canadian Exports	Canadian Imports
14	Canadian Exports	Canadian Imports
15	Canadian Exports	Canadian Imports
16	Canadian Exports	Canadian Imports
17	Canadian Exports	Canadian Imports
18	Canadian Exports	Canadian Imports, Alaskan Supply
19	Mexican Exports	Mexican Imports
20	Mexican Exports	Mexican Imports
21	Mexican Exports	Mexican Imports

R - Residential demand; C - Commercial demand; I - Industrial demand; T - Transportation demand

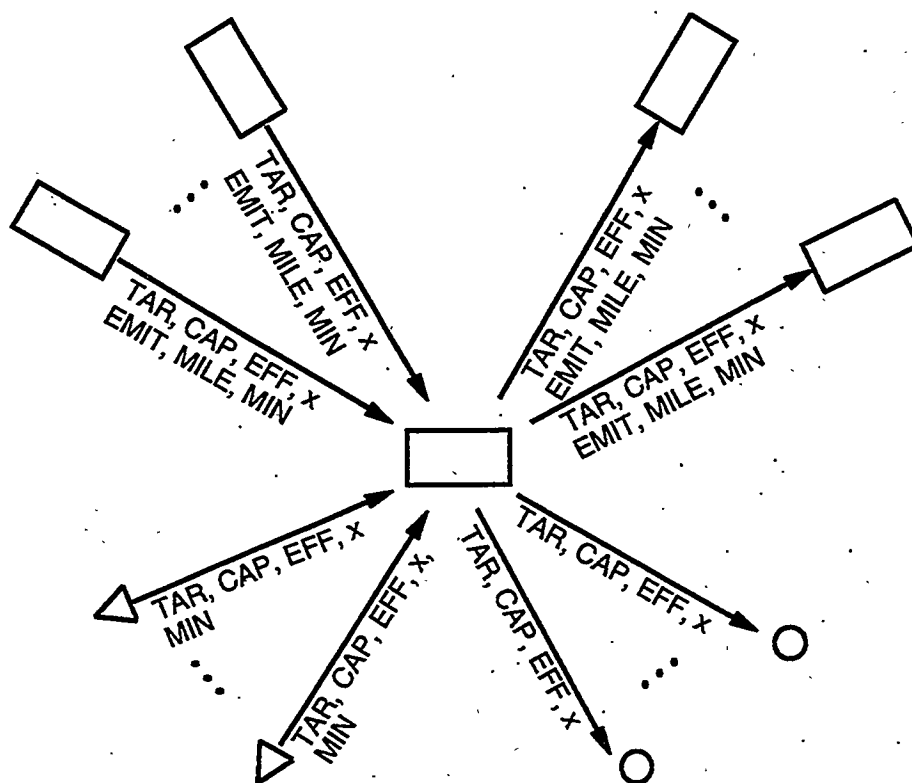
U(n1/n2) - Electric generator's demand in NGTDM/EMM region (n1/n2) as shown in Figure 3-3




P(n1/n2) - Production in NGTDM/OGSM region (n1/n2) as shown in Figure 3-6 (also includes synthetic natural gas from coal and other supplemental supplies)

SNG - Synthetic Natural Gas from liquid hydrocarbons


LNG - Liquefied Natural Gas

Figure 4-3. Network Parameters and Variables



-  - Transshipment Node
-  - Supply Point
-  - Demand Point

Parameters: (model inputs)

- TAR - Tariff
- EFF - Efficiency
- CAP - Capacity
- MILE - Mileage
- EMIT - Emissions
- MIN - Minimum Flow
-  - Direction

Variables: (model outputs)

- x - Flow

region. Minimum flows are set on supply arcs by splitting the assumed minimum production levels for each source (described in Chapter 3) into firm and interruptible components based on the relative levels of core and noncore consumption in the Lower 48 States. Although capacity limits can be set for the arcs to and from end-use and supply points, respectively, the current version of the model does not impose such limits on the flows along these arcs.

In an effort to represent potential interruptions in transportation service to the noncore market, a "relief valve" was put in the system. The noncore demand requirements can optionally be met through a highly priced "backstop" supply source, which is made directly available at the end-user nodes. Backstop supply is designed to be used only in the event that pipeline capacity (existing plus capacity to be built for the firm service market) is not sufficient to meet the noncore demand requirements. Backstop supply displaces noncore consumption which would be expected not to transpire in the Annual Flow Module due to fuel switching or generally lower consumption levels in response to higher gas prices. The incorporation of backstop supply is a modeling tool and is not intended to represent a real supply source.

Note that any of the above parameters, supplies, or demands may be set equal to zero. For instance, some pipeline arcs may be defined in the network that currently have zero capacity where new capacity is expected in the future. On the other hand, some arcs such as those to end-use sectors are defined with infinite pipeline capacity because the model does not forecast limits on the flow of gas from transshipment nodes to end users.

## **Overview of the NGTDM Modules and Their Interrelationships**

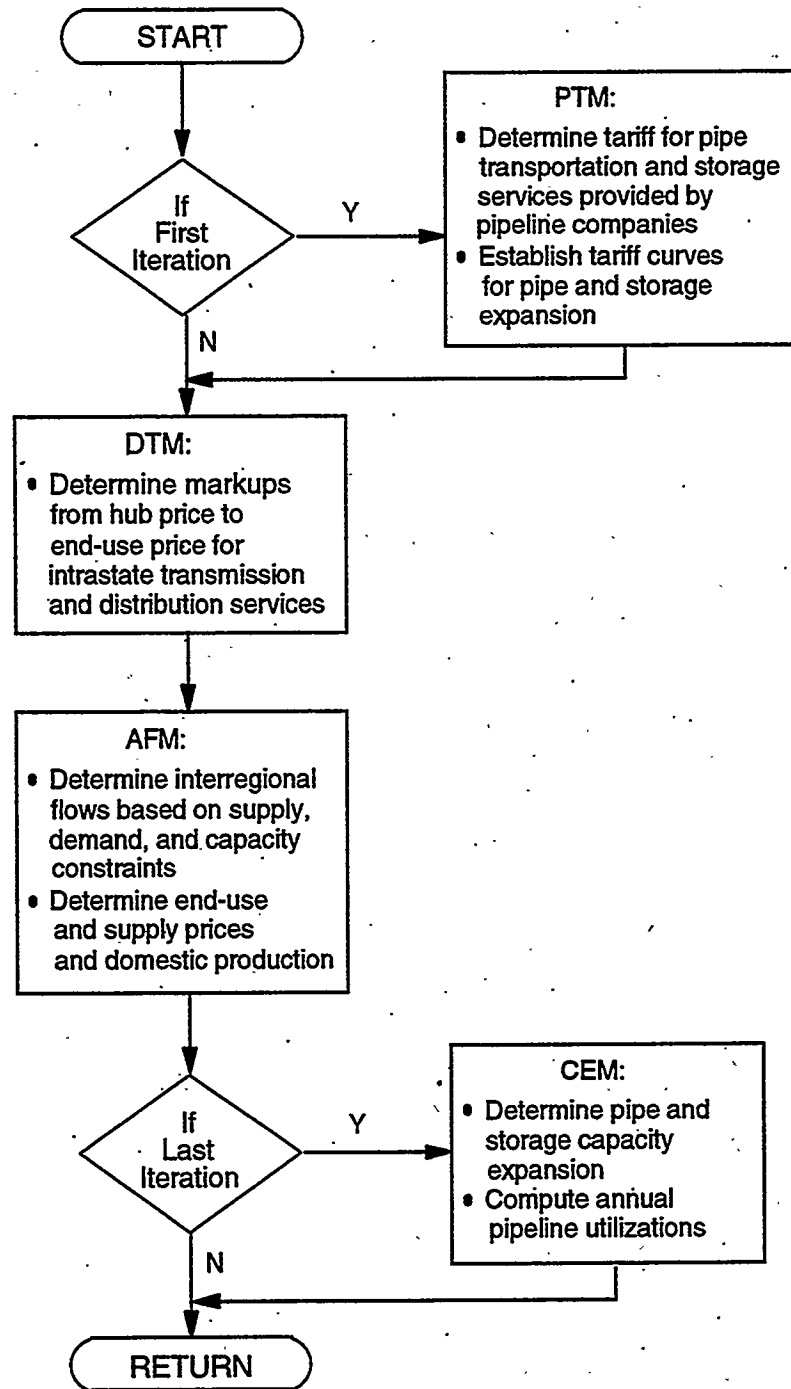
The NEMS generates an annual forecast of the outlook for U.S. energy markets for the years 1990 through 2015. Although the NGTDM is executed for each iteration of each forecast year solved by the NEMS, it is not necessary that all of the individual components of the model be executed for all iterations. Of the NGTDM's four components or modules, the Capacity Expansion Module and the Pipeline Tariff Module are executed only once per forecast year. The Annual Flow Module and the Distributor Tariff Module are executed every iteration of each forecast year. A process diagram of the NGTDM is provided in Figure 4-4, showing the general calling sequence.

The primary function of the Capacity Expansion Module is to forecast interregional pipeline and underground storage expansions and produce annual pipeline load profiles based on seasonal loads. Using this information from the Capacity Expansion Module and other data, the Pipeline Tariff Module uses an accounting process to derive interregional and intraregional pipeline tariffs for firm and interruptible transmission service to be used in the Annual Flow Module and the Capacity Expansion Module. The Distributor Tariff Module provides distributor tariffs for use in the Annual Flow Module and the Capacity Expansion Module. The Distributor Tariff Module must be called each iteration because some of the distributor tariffs are based on consumption levels which may change from iteration to iteration. Finally, using the information provided by other NGTDM modules and other NEMS models, the Annual Flow Module solves for natural gas prices and quantities which reflect a market in equilibrium for the current forecast year. A brief summary of each of the NGTDM modules follows.

### ***The Annual Flow Module***

The Annual Flow Module (AFM) is considered the central module within the NGTDM, with the Capacity Expansion Module, Pipeline Tariff Module, and Distributor Tariff Module (in addition to other NEMS models) providing it with critical information. Its objective is to determine the market equilibrium associated with natural gas supplies, demands, and transportation costs, thereby generating supply and end-use prices and production levels for use by other NEMS models. Formulated as a linear program, the AFM determines a market equilibrium by maximizing the sum of consumer and producer surplus, while minimizing transmission and distribution charges, subject to system constraints. As the name indicates, it has been designed to represent annual flows from supply points to demand points traveling along a pipeline network. As defined above, the network in the AFM represents firm and interruptible service markets separately along parallel networks, connected only at the supply points and through capacity constraints along the network arcs.

Figure 4-4. NGTDM Process Diagram



To accomplish its goal, the AFM uses regional price curves to represent regional supplies and demands. These curves represent linear approximations of the price response that can be expected from the more detailed NEMS models that provide the parameters used to build the curves. Each forecast year the Oil and Gas Supply Model provides the parameters to build the supply curves, and each iteration the demand models provide the parameters to build the demand curves.

The Capacity Expansion Module, Pipeline Tariff Module, and Distributor Tariff Module also provide data required by the AFM. The Capacity Expansion Module provides pipeline capacity additions, pipeline utilizations for firm flows and total flows, and net storage withdrawal levels associated with the firm and interruptible service markets. The Pipeline Tariff Module calculates interregional and intraregional pipeline tariffs for both firm and interruptible service. Similarly, the Distributor Tariff Module provides the AFM with markups for local distribution and intrastate transportation services.

Annual flow results from the AFM are provided to the Pipeline Tariff Module and the Capacity Expansion Module. The Capacity Expansion Module uses firm flows to set minimum flows for its capacity expansion forecasts, and the Pipeline Tariff Module uses both firm and interruptible flows in conjunction with cost estimates to set unitized pipeline tariffs.

### ***The Capacity Expansion Module***

The Capacity Expansion Module (CEM) is the only module in the NGTDM that includes a seasonal representation of the natural gas market. In each NEMS forecast year, the CEM determines incremental pipeline and storage capacity required to satisfy expected firm service demands in a future year based on an analysis of the expected supply, storage, and transportation requirements. The peak and off-peak seasons are analyzed, concurrently within the CEM, to determine pipeline and storage capacity needs. The storage decision affects the need for pipeline capacity upstream from the storage facility and influences the relative utilization of the pipeline between the peak and off-peak seasons. A brief description of the seasonal network used in the CEM is presented next, followed by an overview of the model solution methodology.

#### **Seasonal Network Representation in the Capacity Expansion Module**

The basic network structure defined for the CEM is nearly identical to the general NGTDM network described above, with the exception that a two-period (peak and off-peak) representation of the annual market is now being modeled. The "peak period" is defined as the months in the year with distinctly higher levels of natural gas consumption on a national basis.<sup>33</sup> As in the Annual Flow Module, interregional flows to satisfy firm transmission service are handled separately from the flows to satisfy interruptible service, both in the peak and off-peak periods.

Conceptually the Capacity Expansion Module consists of four parallel networks. Each network represents the flow of gas either during the peak period under firm service, the off-peak period under firm service, the peak period under interruptible service, or the off-peak period under interruptible service. Interaction between the two periods occurs primarily through the use of storage. Arcs are established from each off-peak firm and interruptible transshipment node to the storage point in the region to represent storage injections. Likewise, arcs are established from each storage point into the associated transshipment nodes in both the firm and interruptible peak period networks. These arcs represent storage withdrawals in the peak period to be transported under firm and interruptible service to satisfy core and noncore demands, respectively. An additional link between the two periods occurs due to the existence of annual supply sources as opposed to separate peak and off-peak supply. Thus, supply from each supply source in a region is available to both the peak and off-peak transshipment node in the region, and arcs are established to allow for these flows. An illustration of the two-period network is shown in Figure 4-5 for a base network with three

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<sup>33</sup>The data inputs to the Capacity Expansion Module define the months designated as peak versus offpeak. Currently the data in the Capacity Expansion Module reflect a peak period from December through April. Due to a lag in the reporting of monthly consumption data, November falsely appears to be a "nonpeak" month. This should be corrected in the future once a method is developed for generating adjusted monthly consumption data.

transshipment nodes. For simplicity, the example does not show the further disaggregation of the network into its firm and interruptible components.

## Overview of the CEM Solution Methodology

The functional requirement for the CEM is to make natural gas pipeline and storage capacity expansion decisions and to estimate corresponding pipeline and storage utilization levels based on assumptions similar to those used by the natural gas industry. The CEM has been designed as a seasonal natural gas transportation model, with storage serving as a link between supplies and seasonal demands. As with the Annual Flow Module, both firm and interruptible services are also represented. Formulated as a linear program, the objective is to minimize production and transportation costs, as well as costs associated with pipeline and storage expansion decisions. Although the basic network structure, its parameters (inputs), and its model variables (outputs) have been designed to be similar to that in the Annual Flow Module, some elements had to be defined as seasonal.

The CEM is executed within the NGTDM once at the end of each forecast year to determine the pipeline and storage expansion which will come on line "n" years in the future. Capacity is expanded to accommodate the transmission service needs of core consumers that are expected to occur in that year. The parameter "n" represents the average number of years in which the decision to expand capacity cannot be reversed due to contractual obligations. The results generated by the CEM during the current forecast year do not affect the current forecast year's market solution, but are used in the Annual Flow Module and the Pipeline Tariff Module when the NGTDM determines a natural gas market equilibrium solution for the n<sup>th</sup> year in the future.

The data inputs for the CEM from the NEMS system include macroeconomic parameters from the Macroeconomic Activity Model of NEMS, as well as expected values for natural gas consumption levels in future years. The NEMS Integration Routine provides the CEM with estimates of future natural gas consumption levels for the nonelectric sectors.<sup>34</sup> Consumption forecasts for the core and noncore electricity generating sector are a function of the estimates provided by the Electricity Market Model. Parameters are provided by the Oil and Gas Supply Model to the CEM for estimating potential future supply levels. In addition, minimum interregional firm service flow constraints (based on Annual Flow Module solution values in the previous forecast year) are set in the CEM to represent the inertia of core customers from annually switching pipeline routes used in transporting their natural gas (e.g., due to long-term contract commitments).

The CEM uses the same regions and end-use sectors defined within the Annual Flow Module. However, the Annual Flow Module is an annual model; whereas, the CEM requires a seasonal analysis to represent more accurately the decision to expand pipeline and/or storage capacity to meet peak-day core market demands. The CEM includes a methodology for converting from annual to seasonal (peak and off-peak) consumption levels, as well as a means for capturing core peak-day requirements in the capacity expansion decision. The factors for estimating seasonal load patterns are historically based model inputs which are held constant throughout the forecast in the current model. Future model enhancements may allow for the representation of structural changes in seasonal consumption patterns (e.g., demand side management, changing building structures, and/or technological innovations).

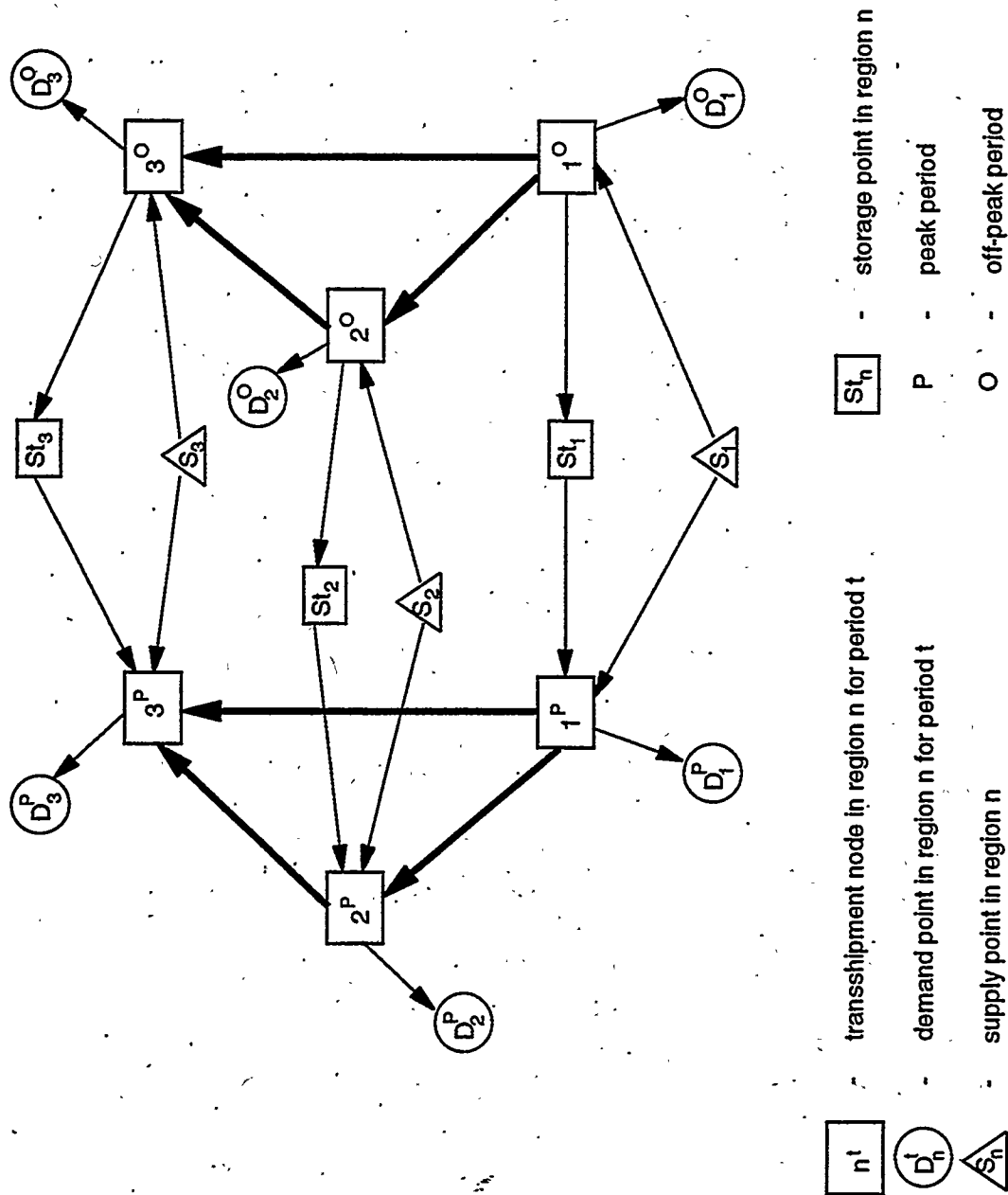
Dry gas production is represented in the CEM with a price responsive equation (or curve) developed from inputs from the Oil and Gas Supply Model. Although the supply representation within the CEM reflects annual levels, the formulation allows for upper bounds on the level of supply available within the peak or off-peak period from each supply source (formulated as the annual supply times the percentage of the year represented by the given period).

Imports from Mexico and Canada are represented as constant supplies and tracked at a seasonal level (peak and off-peak). Mexican imports are provided by the Oil and Gas Supply Model and are supplied to the core market only. Canadian imports are available to both core and noncore markets and are determined from exogenously specified Canadian pipeline capacities and utilizations. Also, Canadian produced natural gas which passes through the United States on its way to Canadian markets (as described in Chapter 3) is split into peak and off-peak levels based on assumed shares.

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<sup>34</sup>These expected consumption levels are based on annual growth rates in previous historical or forecast years, capped by maximum allowable growth rates within the NGTDM.

Figure 4-5. Example Two-Period Network



Storage is used to satisfy peak season consumption by injecting gas into storage in the off-peak period and withdrawing the gas during the peak season. Thus, storage is considered a supply source in the peak period, and a demand requirement in the off-peak period. This limits the amount of off-peak capacity that is available on an interruptible basis for consumption in the period. In addition, regional historically observed reporting discrepancies are accounted for in the model, with seasonal splits based on national consumption in the peak and off-peak periods.

The Pipeline Tariff Module provides interregional pipeline tariffs and storage charges associated with existing and incremental expansion of regional pipeline and storage facilities. This information is sent to the CEM in the form of storage and pipeline "capacity supply curves." These "capacity supply curves" are based on exogenously specified capital cost curves for expansion and on macroeconomic parameters from the NEMS Macroeconomic Activity Model.

If the CEM determines that pipeline (or storage) capacity will be added, the Pipeline Tariff Module will in turn adjust the associated revenue requirements (and resulting tariff parameters) for the year in which the new capacity is scheduled to come on-line to account for the expansion costs. In addition, the pipeline capacities and seasonal utilization patterns established in the CEM are used in defining maximum annual interregional flow constraints in the Annual Flow Module, reflecting the impact of the variation in seasonal consumption on pipeline loads. The seasonal storage injections and withdrawals are used as a basis for setting annual net storage withdrawals by core and noncore customers in the Annual Flow Module. The Pipeline Tariff Module also uses the levels of storage and pipeline capacity expansion established in the CEM when determining the associated capital expenditures (an input to the Macroeconomic Activity Model of the NEMS).

The NGTDM has an option available which allows the user to either (1) run the CEM described above, (2) use a designated data file (created by the CEM during a previous run) which contains the capacity and utilization data needed by the NGTDM, or (3) first use a designated data file for a user-specified number of years and then run the CEM code for the remaining forecast years. This is controlled by the input parameter EXCEM. If the parameter is set to the model base year (e.g., 1990), then option 1 is selected; if it is set to a large number (e.g., 9999), then option 2 is selected; if it is set to an interim forecast year (e.g., 2000), then option 3 is invoked. Under option 3 the designated data file is used prior to the specified year and the CEM is run for the remaining forecast years.

### ***The Pipeline Tariff Module***

The Pipeline Tariff Module (PTM) is executed within the NGTDM once each forecast year to calculate pipeline and storage tariffs for the Annual Flow Module, the Capacity Expansion Module, and the Distributor Tariff Module. The tariffs calculated within the PTM are computed for individual pipeline companies and are then aggregated as required. An accounting system is used to track costs and compute rates under various rate design and regulatory scenarios. Tariffs are computed for both storage and firm and interruptible transportation services. Transportation tariffs are computed for interregional arcs defined by the NGTDM network, as well as intraregional connections. These network tariffs represent an aggregation of the tariffs for individual pipeline companies supplying the network arc. Storage tariffs are defined at regional NGTDM network transshipment nodes, and likewise, represent an aggregation of individual storage company tariffs. These tariffs are for transmission services only and do not include the price of gas.

More specifically, the PTM computes (1) reservation costs assigned to firm transportation service customers, (2) usage fees for firm transportation service, (3) minimum, maximum, and reference level (a function of pipeline capacity utilization, but between the minimum and maximum) transportation rates for interruptible service, and (4) rates for storage service. For fully regulated services, cost-of-service based revenue requirements are computed by the PTM and are used within the Annual Flow Module to price transportation services. Where markets are competitive or are loosely regulated (i.e., interruptible transportation), the Annual Flow Module uses the reference level transportation rate set by the PTM as a lower bound for service in determining the actual rate charged. The



resulting rate (dependent on marginal costs) should be within the bounds of the minimum and maximum rates computed by the PTM.<sup>35</sup>

The impacts of the capacity expansion decisions made in the Capacity Expansion Module are reflected in the pipeline tariffs computed by the PTM. The Capacity Expansion Module determines the location and quantities of additional pipeline capacity and storage facilities at the aggregate level represented by the NGTDM network. Interregional pipeline or regional annual storage capacity expansion requirements are provided to the PTM by the Capacity Expansion Module. Also, since capacity expansion decisions need to take into account the marginal changes in pipeline tariffs in response to increased capital requirements, the PTM initially establishes tariffs (reservation fee) associated with a series of incremental expansions. Many of the calculations of components of the revenue requirements require the use of macroeconomic variables that are provided by the NEMS Macroeconomic Activity Model.

### ***The Distributor Tariff Module***

The Distributor Tariff Module (DTM) determines regional and sector-specific markups that are applied to regional hub prices<sup>36</sup> to derive regional end-use prices for each sector and market type (core and noncore). The end-use markups are comprised of four separate cost components: distributor tariffs, intraregional pipeline tariffs, intrastate pipeline tariffs, and a citygate benchmark factor. The distributor tariff component represents the tariff for services provided by local distribution companies from the citygate to end-users, and is determined within the DTM. Intraregional and intrastate tariffs are regional charges by pipeline companies for intraregional interstate and intrastate transportation services, respectively. Intraregional interstate tariffs are determined by the Pipeline Tariff Module, and intrastate tariffs are specified exogenously. Citygate benchmark factors are determined endogenously to the model, and serve to align the model with core and noncore historical citygate prices. These markups from the hub to each end-use sector are used within both the Annual Flow Module and the Capacity Expansion Module.

The DTM uses different methodologies to estimate regional core and noncore distributor tariffs. Noncore distributor tariffs are based on the corresponding historical tariffs while the annual change in core distributor tariffs (excluding the transportation sector<sup>37</sup>) are a function of the annual change in core consumption and in costs of capital and wages, the noncore contribution to core revenues, and technological efficiency improvements. Not accounting for taxes, core distributor tariffs associated with the compressed natural gas fleet vehicle sector are a function of historical distributor tariffs, while those associated with the personal vehicle sector are based on the industrial core market distributor tariffs with an assumed dispensing cost. Distributor tariffs are calculated within the model each iteration of each forecast year, with historical levels used during historical years.

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<sup>35</sup>The NGTDM compares the effective tariff (i.e., the difference between the price at two adjoining nodes) to ascertain if the limit was violated. Currently the model does not have a correcting mechanism if the constraint is violated and simply reports the occurrence in a report. Regulators have discussed the possibility of lifting this limit.

<sup>36</sup>The hub price is equal to the market clearing price of all supplies at the transshipment node in the region in which the gas is consumed.

<sup>37</sup>The core transportation sector is comprised of fleet vehicle and personal vehicle consumption of compressed natural gas.



## 5. Annual Flow Module Solution Methodology

As a key component in the NGTDM, the Annual Flow Module (AFM) determines the market equilibrium between supply and demand of natural gas. This translates into finding the price such that the quantity of gas that consumers would desire to purchase equals the quantity that producers would be willing to sell, accounting for the transmission and distribution costs, pipeline fuel use, capacity limitations, and mass balances. Structurally, the AFM consists of a network of regions connected by a parallel system of pipelines designed to service two types of customers, core and noncore. Supplies are defined as total regional supplies available to both parallel networks, while demands are defined separately as core or noncore regional demands. Because of the characteristics of these two markets, pipeline tariffs are rated differently along the same arc. To achieve market equilibrium, the AFM has been formulated as a linear program which maximizes consumer plus producer surpluses while minimizing transportation costs.<sup>38</sup> Supply and demand prices and quantities, as well as resulting flow patterns, are obtained from the linear programming solution and sent to other NGTDM modules or other NEMS models after some processing. A simple system diagram of the information flowing to and from the AFM is presented in Figure 5-1. A brief explanation of how supplies and demands are represented in the AFM, how the linear program has been formulated for the AFM, and how the AFM results are processed for the other NGTDM modules and NEMS models is presented below.

### Network Characteristics in the AFM

As described earlier, the AFM network consists of two parallel networks (firm and interruptible service), each containing 12 regions (or nodes), 6 Canadian border crossing nodes, and 3 Mexican border crossing nodes. Net storage withdrawals are represented at 10 of the 12 regional nodes for both firm and interruptible services. Arcs connecting the nodes are characterized by pipeline efficiencies, physical capacities, pipeline tariffs, minimum flows, and maximum utilizations. The efficiencies are exogenously defined<sup>39</sup> and represent reduction in flows due to pipeline fuel consumption. Pipeline tariffs (defined in the Pipeline Tariff Module) represent fees for moving gas along pipelines. Pipeline tariffs in the firm market include reservation and usage fees while pipeline tariffs in the interruptible market are composed solely of usage fees. Minimum flows are defined for each arc in order to maintain continuity in flows from one model year to the next. Maximum pipeline utilizations (established in the Capacity Expansion Module) are defined to maintain consistency between capacity expansion decisions and flow patterns. Finally, a designated percentage of the pipeline capacity is not allowed to be used, to represent the capacity that would not be released, and is held as a safety margin under normal weather conditions (Appendix E, WTHRFAC).

### Supply and Demand Representations

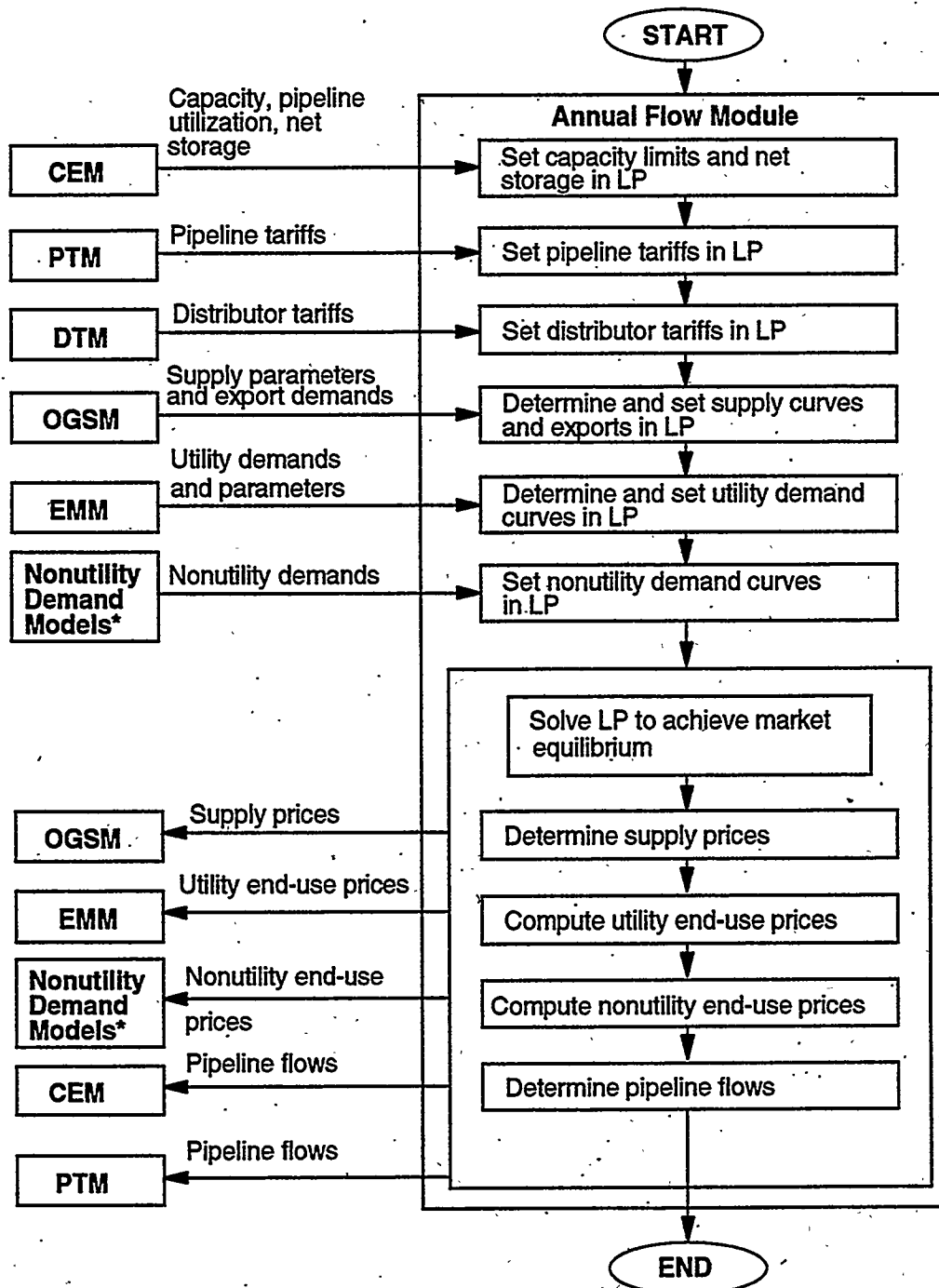
Supply and demand are represented as price curves in each region in the AFM network. These curves represent estimates of short term responses that can be expected from the NEMS models that provide the AFM with regional supply and demand levels. Demand is defined as core or noncore and tied exclusively to either the firm or interruptible service network, respectively; while supply is defined as total supply available (in most cases) to either network, constrained by minimum flows along selected supply arcs going to each of the two networks. The supply and demand types are addressed below.

Supply in the AFM includes associated-dissolved and nonassociated production sources (onshore, offshore, and Alaska), imports (Canadian and Mexican by pipeline, and as liquefied natural gas), synthetic natural gas (from liquids and coal), and other supplemental supply. Of these, the associated-dissolved production, liquefied natural gas, Mexican imports, Alaska production, and other supplemental supply categories are considered to be constant (or fixed). With the exception of associated-dissolved natural gas, supplies with fixed levels are assumed to be available

<sup>38</sup> Adapted from the Project Independence Evaluation System (PIES) model.

<sup>39</sup> Almost every arc in the NGTDM network has an associated efficiency variable. With the exception of the interstate pipeline arcs, all of these factors are set to 1.0 (Appendix E – NEFF\_PIPE, UEFF\_PIPE, SEFF\_PIPE, MEXEFF, CANEFF, AEFF\_PIPE, AEFF\_PIPE\_SCALE93).

Figure 5-1. Annual Flow Module System Diagram



\*Residential Demand Model, Commercial Demand Model, Industrial Demand Model, and Transportation Demand Model

only to the firm network, while supplies with variable levels (i.e., relatively price responsive in the short-term) are available to either network.

Some supply quantities are provided directly by the Oil and Gas Supply Model and/or other NEMS models, while others are determined within the NGTDM, as described in Chapter 4. For example, onshore and offshore production and Canadian imports are determined within the NGTDM based on parameters provided by the Oil and Gas Supply Model, whereas the Oil and Gas Supply Model establishes the level of natural gas flowing into the contiguous United States via the Alaskan Natural Gas Transportation System (ANGTS). The Oil and Gas Supply Model also defines the liquefied natural gas quantities imported through the four gasification terminals modeled by the NGTDM, as well as the level of associated-dissolved gas production. Synthetic natural gas from liquids in Illinois is determined by the NGTDM (as a function of the associated region's market price), with synthetic natural gas from Hawaii held constant throughout the forecast. Natural gas from coal in North Dakota is provided by the Coal Market Model. Finally, other supplemental supplies are set to historical levels by the NGTDM and held constant throughout the forecast. Table 4-1 provides more detail on the regional representation of natural gas supply in the NGTDM. Another type of supply (or pseudo supply) available is backstop supply; however, it is undesirable for the system to use this supply source. Backstop supply is designed to be used only if the system has insufficient supply or pipeline capacity to meet a minimum level of demand. If it is used, a high price is sent to the demand models which, in turn, are expected to respond by sending lower demand levels. Backstop supply is priced high<sup>40</sup> in order to prevent it from becoming economically attractive.

Demand includes end-use sector demands as well as exports (Canadian and Mexican), defined for both core and noncore customers. Although both types of customers are represented by demand curves, core demands are kept nearly constant while noncore demands are allowed to vary more depending on sector type. Export demands are set exogenously in the Oil and Gas Supply Model and are assigned as core or noncore within the NGTDM using exogenously specified shares (Appendix E -- CANFRMITR\_SHR, MEXFRMITR\_SHR).

## **AFM Linear Program Formulation**

A linear programming algorithm has been developed to determine the least cost approach to achieving an equilibrium between the supply and demand for natural gas in the AFM. Equilibrium occurs when the price at which consumers are willing to purchase a product is equal to the price at which producers together with transporters are willing to supply the product to the end-user. Economically, this is the point where the sum of consumers' surplus and producers' surplus is maximized.<sup>41</sup> The methodology employed in solving the natural gas supply and demand equilibrium assumes that marginal costs are the basis for determining market-clearing prices to noncore customers and that core customers are charged the average price of gas delivered to the associated region. The problem is based on a transmission and distribution system composed of two parallel networks. These two networks serve as a means of distinguishing between firm and interruptible transmission and distribution services, and are interconnected only at supply points and through capacity constraints. This section defines the linear programming methodology used to establish a market equilibrium in the AFM, from which supply and end-use prices are obtained. First, the representation of consumer plus producer surplus used in the objective function is derived, then a general description of the entire formulation is presented, followed by the explicit mathematical equations.

### ***Derivation of the Representation of Consumer and Producer Surplus***

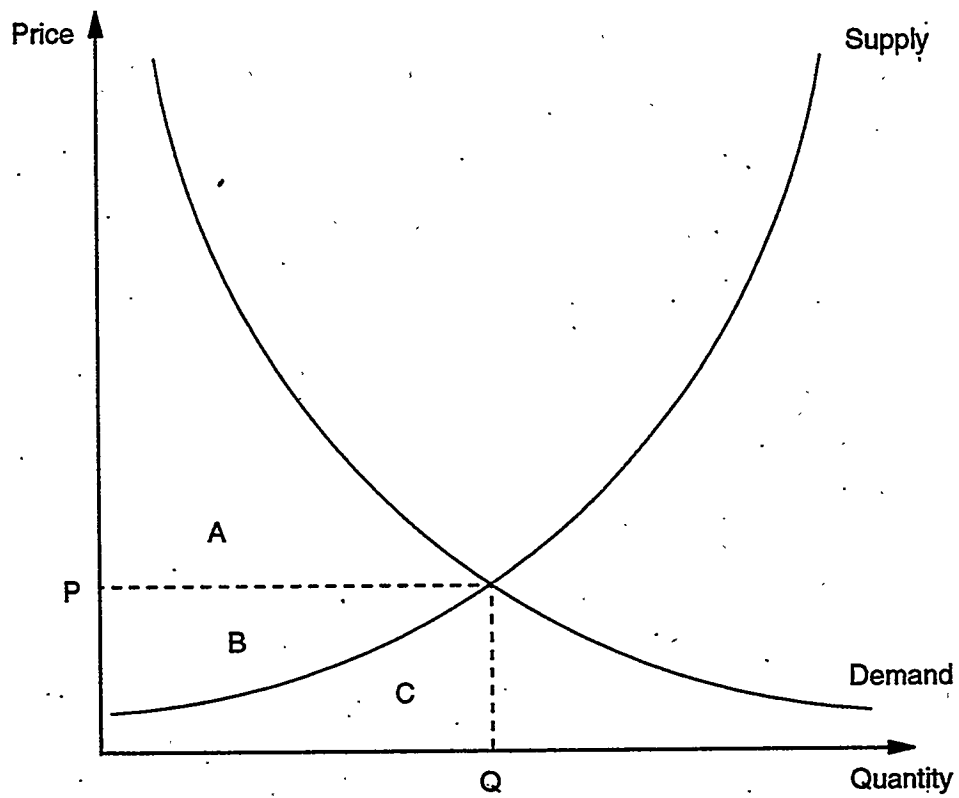
The objective of the linear program designed for the AFM is to determine a market equilibrium between the supply and demand of natural gas. As mentioned above, this occurs when the sum of consumers' surplus and producers' surplus has been maximized. Figure 5-2 illustrates this sum as the area under the demand curve (A+B+C) minus the area under the supply curve (C) to the left of the point of market equilibrium (P,Q). This section describes the computation of the area under the supply and demand curves that are used in the objective function equation.

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<sup>40</sup>The backstop supply price is a user input (Appendix E, NG\_BKSTOP\_PR).

<sup>41</sup>Adapted from the Project Independence Evaluation System (PIES) model.

**Figure 5-2. Supply and Demand Curves**



Area A: Consumers' Surplus

Area B: Producers' Surplus

Area C: Total Cost to the Producers

P: Price at Market Equilibrium

Q: Quantity at Market Equilibrium

A method for determining the area under the demand curve is established by first representing the demand curves as step functions, as shown in Figure 5-3. A base quantity and price are given and  $n$  steps on either side of the base point are defined. Toward this end, let  $(QDEM0, PDEM0)$  represent a known point (the base point) on the curve and an estimate of where the model will solve. The parameters  $UDEM_k$  and  $UDEM_{-k}$  are defined as the incremental quantities represented by each step on the curve (i.e., the length of each step on the demand curve), and  $PDEM_k$  and  $PDEM_{-k}$  represent the corresponding actual prices. Note that the subscript  $k$  identifies the  $k^{th}$  step on the curve to the right of the point  $(QDEM0, PDEM0)$ , and the subscript  $-k$  corresponds to the  $k^{th}$  step on the curve to the left of  $(QDEM0, PDEM0)$ .

The variable  $ydem$  is defined as the total deviation from the base point, and the set of model variables  $ydem_k$  and  $ydem_{-k}$  are used to define  $ydem$ . Each variable represents a portion of the length of the specified step, such that:

$$\begin{aligned} 0 &\leq ydem_k \leq UDEM_k \\ 0 &\leq ydem_{-k} \leq UDEM_{-k} \end{aligned} \quad (19)$$

and,

$$ydem = \sum_{k=1}^n ydem_k - \sum_{k=1}^n ydem_{-k} \quad (20)$$

In order for  $ydem$  to represent the distance either to the right or left of the initial point  $(QDEM0, PDEM0)$ , the following conditions must hold. If  $ydem$  is greater than zero, then each  $ydem_{-k}$  is at the lower bound of zero; and, if  $ydem$  is less than zero, then each  $ydem_k$  is equal to zero. If  $ydem$  is equal to zero, then each  $ydem_k$  and  $ydem_{-k}$  is equal to zero, and the model solved at  $(QDEM0, PDEM0)$ .

In short, the demand curve is represented as a step function by defining an initial point on the curve  $(PDEM0, QDEM0)$ ,  $n$   $ydem_k$  variables,  $n$   $ydem_{-k}$  variables, and the corresponding prices.

Given the above conditions for the relationship between  $ydem_k$  and  $ydem_{-k}$ , the area under the demand curve is approximated by:

$$\sum_{k=1}^n (PDEM_k * ydem_k - PDEM_{-k} * ydem_{-k}) + C \quad (21)$$

where,

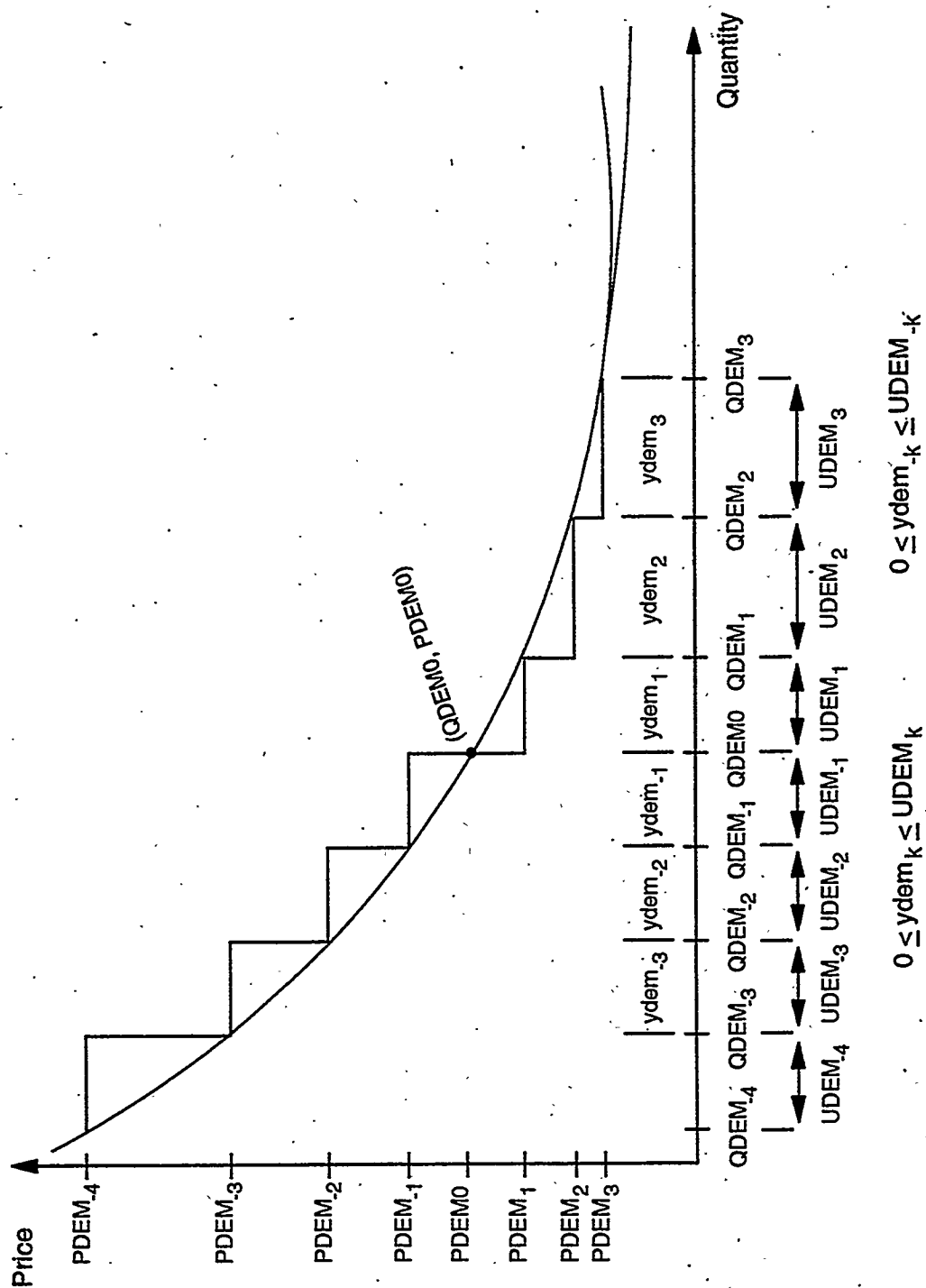
$$\begin{aligned} C &= \text{the area under the demand curve from 0 to } QDEM0 \\ \sum PDEM_k * ydem_k &= \text{the area under the demand curve from } QDEM0 \text{ to step } k \\ \sum PDEM_{-k} * ydem_{-k} &= \text{the area under the demand curve from step } -k \text{ to } QDEM0 \end{aligned}$$

Note that  $C$  is a constant since the demand curve and  $QDEM0$  are given. The variable  $ydem$  represents the distance either to the right or left of the initial point  $(QDEM0, PDEM0)$ , and the equation approximates the integral evaluated from zero to that point.

The area under the demand curve as calculated in the above equation is incorporated in the objective function of the linear program with some modifications. First, the model is formulated as a minimization problem requiring the signs of the coefficients on the equation representing the area under the demand curve to change. Second, since the inclusion of a constant in the objective function does not change the model solution, the  $C$  term is excluded from the objective function. As a result, the following term becomes a part of the objective function:

$$\sum_{k=1}^n (PDEM_{-k} * ydem_{-k} - PDEM_k * ydem_k) \quad (22)$$

Figure 5-3. Approximation of Area Under the Demand Curve





When the area to the right of QDEM0 (ydem greater than zero)<sup>42</sup> is calculated, the following properties must hold:

- (1) At most one ydem<sub>k</sub> is not equal to zero or UDEM<sub>k</sub>.
- (2) If ydem<sub>k</sub> is not equal to one of its limits, then ydem<sub>j</sub>, for all j less than k, is equal to its upper limit UDEM<sub>j</sub>; and ydem<sub>j</sub>, for all j greater than k, is equal to its lower limit of zero.

At optimality, the conditions listed above for ydem can be shown to hold.<sup>43</sup> If the optimal quantity satisfied is on step k of the demand curve, i.e., ydem<sub>k</sub> is not at either of its bounds, then ydem<sub>j</sub>, for j less than k must be at its upper bound (UDEM<sub>j</sub>), because it will always be more beneficial to bring in more of quantity ydem<sub>j</sub> than to bring in any of ydem<sub>k</sub> since the coefficient of ydem<sub>j</sub> is negative and PDEM<sub>j</sub> greater than PDEM<sub>k</sub>. Similarly, ydem<sub>j</sub> for j greater than k will be zero because it will not be beneficial to bring in any of ydem<sub>j</sub> before bringing in all of ydem<sub>k</sub> since the coefficient of ydem<sub>j</sub> is negative and PDEM<sub>j</sub> is less than PDEM<sub>k</sub>. Furthermore, ydem<sub>j</sub> for all j will be zero because it will not be beneficial to bring in any of ydem<sub>j</sub> since its coefficient is positive.

Likewise, if the optimal quantity satisfied corresponds to step -k (some quantity must be subtracted from the base demand), where ydem<sub>k</sub> is not at either of its bounds, then ydem<sub>j</sub>, for j less than k, must be at its upper bound (UDEM<sub>j</sub>), because it will always be more beneficial to subtract more of quantity ydem<sub>j</sub> than to subtract any ydem<sub>k</sub>, since the coefficient of ydem<sub>j</sub> is positive and PDEM<sub>j</sub> is less than PDEM<sub>k</sub>. Similarly, ydem<sub>j</sub>, for j greater than k, will be zero because it will not be beneficial to subtract any of ydem<sub>j</sub> before subtracting all of ydem<sub>k</sub>, since the coefficient of ydem<sub>j</sub> is positive and PDEM<sub>j</sub> is greater than PDEM<sub>k</sub>. Furthermore, ydem<sub>j</sub> for all j will be zero even though the coefficient of ydem<sub>j</sub> is negative. This can be deduced by observing that if the quantity at ydem<sub>j</sub> were above zero, the increase in quantity would have to be negated by increasing ydem<sub>k</sub>, which has a higher price, thus causing the objective function to rise.

## Supply Curves

As with the demand curves, the area under the supply curve can be estimated by first representing the supply curves as step functions and then summing the area under the steps on each curve. This is accomplished in a manner similar to the methodology used for demand curves; however, the base point (QSUP0, PSUP0) is assumed to be at QSUP0 equals zero. Thus, the ysup is represented only by ysup<sub>k</sub> and the supply term in the objective function becomes  $\sum PSUP_k * ysup_k$ . The base point (QSUP0, PSUP0) is set at the solution value (gas production, wellhead price) resulting from the previous NEMS iteration. The size of each ysup is set progressively larger as k increases, therefore allowing for smaller gradations around the base point (to better approximate the original supply curve). For the first two NEMS iterations, the size of each ysup is exogenously specified. Subsequently, the step sizes are decreased (as the NEMS converges to an equilibrium solution) based on the difference in the wellhead price solutions from the previous two NEMS iterations.

## General Description of the AFM Linear Program Formulation

The objective of the linear program designed for the AFM is to determine a market equilibrium between the supply and demand of natural gas. Since the network consists of multiple supply sources, multiple demand points, and transshipment arcs, transportation costs also must be included. Thus, system equilibrium will occur when the sum of all the consumers' surplus, all the producers' surplus, and all the transportation costs (negative) is maximized. After translating this into a cost minimization problem, the follow objective function results.

$$\text{minimize} \quad \{ \text{transportation costs} - ( \sum (\text{consumer surplus}) + \sum (\text{producer surplus}) ) \}$$

where,

<sup>42</sup>The analogous properties hold for the left of QDEM0 (ydem less than zero).

<sup>43</sup>See page B-16 in the PIES model documentation for a complete description.

$$\Sigma (\text{consumer surplus}) + \Sigma (\text{producer surplus}) =$$

(the area under the demand curve to the left of equilibrium)-  
 (the area under the supply curve to the left of equilibrium)

Capacity flow constraints are defined for each interregional arc in the overall network. Two types of constraints have been defined. One limits total annual flows along an arc and the other serves to limit annual firm service flows along the arc. The total flow constraint is an inequality constraint defined to ensure that total flow (firm plus interruptible) along an arc does not exceed the maximum allowable annual flow along the pipeline. The maximum allowable flow is defined as the maximum physical capacity (adjusted for normal weather representation) times the maximum total utilization (defined by the Capacity Expansion Module) for that arc. Similarly, the firm flow constraint is an inequality constraint defined to ensure that firm flow along an arc does not exceed the maximum allowable annual firm flow along the pipeline. The maximum allowable firm flow is defined as the maximum physical capacity (adjusted for normal weather representation) times the maximum firm utilization (defined by the Capacity Expansion Module) for that arc. The resulting constraints are given below for each interregional arc.

For each interregional arc i,j:

$$(\text{flow on the arc to satisfy the core market}) + (\text{flow along an arc to satisfy the noncore market}) \leq ((\text{physical capacity on the arc}) * (1 - \text{weather adjustment factor for normal weather}) * (\text{annual capacity utilization factor for total flow}))$$

$$(\text{flow on the arc to satisfy the core market}) \leq ((\text{physical capacity on the arc}) * (1 - \text{weather adjustment factor for normal weather}) * (\text{annual capacity utilization factor for firm flow}))$$

A mass balance constraint exists for each transshipment node in each parallel network to ensure that the total input to a node equals the total output from the node (including net storage withdrawals, discrepancies, and losses). In general, gas flowing into a transshipment node comes from other transshipment nodes, supply points, and (in some cases) storage, while gas flowing from a transshipment node goes to demand points, other transshipment nodes, and (in some cases) storage. Storage flows in the AFM are assumed to be constant for a particular year (defined by the Capacity Expansion Module) and are represented as net withdrawals (i.e., natural gas flowing out of storage to a node minus natural gas flowing into storage from a node). Net storage withdrawals are defined separately for the firm and interruptible networks. Discrepancies represent the difference between historically reported supply versus disposition values (i.e., the balancing item).<sup>44</sup> The model incorporates an exogenous forecast of the national discrepancy,<sup>45</sup> shared out to regions based on historically based shares (Appendix E -- NATL\_DISCR, STEO\_DISR\_SHR). A general transshipment node mass balance constraint is listed below for both networks.

For each firm service transshipment node i:

$$(\text{flow into a transshipment node from another firm service transshipment node}) + (\text{flow into a transshipment node from supply points in the region}) + (\text{net storage withdrawals corresponding to firm service}) - (\text{losses}) = (\text{flow out of the transshipment node to other firm service transshipment nodes}) + (\text{flow out of the transshipment node to core market demand points in the region}) + (\text{discrepancy})$$

For each interruptible service transshipment node i:

$$(\text{flow into a transshipment node from another interruptible service transshipment node}) + (\text{flow into a transshipment node from supply points in the region}) + (\text{net storage withdrawals corresponding to interruptible service}) - (\text{losses}) = (\text{flow out of the transshipment node to other interruptible service})$$

<sup>44</sup>Historically, the level of the balancing item in the accounting of natural gas supply and disposition are not insignificant. If the natural gas consumption forecast is in line with history and the balancing item is not accounted for, the production forecast in the model will be significantly out of line with (below) history. Therefore the model incorporates an exogenously specified forecast of this balancing item or discrepancy (Appendix E, NATL\_DISCR).

<sup>45</sup>For the years 1997 to 2000 and 2001 to 2015, 7 BCF and 35 BCF, respectively, were exogenously subtracted from the national discrepancy forecast to represent fugitive emissions savings from the Climate Change Action Plan.

transshipment nodes) + (flow out of the transshipment node to noncore demand points in the region) + (discrepancy)

A mass balance constraint also is included for each core and noncore demand point. This constraint ensures that the quantity allocated to an end-use point equals the quantity demanded at that point. Consumption in the AFM is defined by region and is represented by demand curves. It is the linear approximations to these curves that are used to represent demands in the linear programming problem. Although these curves allow demands to drop to levels below base level demands in an effort to achieve a market equilibrium, supply or pipeline utilization limits may prevent some regional demands from being met. In order to prevent the linear program from going infeasible, a highly priced backstop supply is available at each demand point. If backstop supply is needed, high prices result and the other NEMS models will respond with lower demands. General transshipment node mass balance constraints are listed below for both parallel networks.

(flow out of a transshipment node to core market demand points in the region) + (flow from a backstop supply point to core market demand points in the region) - (losses) = (quantity consumed at that node for firm service)

(flow out of a transshipment node to noncore demand points in the region) + (flow from a backstop supply point to noncore demand points in the region) - (losses) = (quantity consumed at that node for interruptible service)

Each supply point also has a mass balance constraint represented. Since gas may flow from a supply point to a transshipment node (in the same region) in either the firm or interruptible network, this constraint ensures that the total quantity flowing from the supply point equals the amount supplied. The constraint states that total supply is equal to the portion of supply flowing to the firm network plus the portion of supply flowing to the interruptible network. The general constraint is presented below:

(quantity supplied from the supply curve) = (flow from the supply point to a transshipment node to satisfy the core market) + (flow from the supply point to the transshipment node to satisfy the noncore market)

Due to the nature of a linear program, an optimal solution will not allow flow to occur simultaneously on a primary arc from Region A to Region B and on its bidirectional arc from Region B to Region A because such a situation would incur higher transportation costs (as compared with a case where flow occurs only in one direction and represents net flow). Since an arc in the network may represent an aggregation of some pipelines flowing one direction and other pipelines flowing the opposite direction, flows along bidirectional arcs need to be explicitly represented. This is accomplished by setting minimum flows along the bidirectional arcs in both the firm and interruptible networks equal to historically observed levels (Appendix E -- AFLOW\_F, AFLOW\_I). The general equations are presented below.

(flow along the bidirectional arc to satisfy the core market)  $\geq$  (minimum firm flow requirement for the arc)

(flow along the bidirectional arc to satisfy the noncore market)  $\geq$  (minimum interruptible flow requirement for the arc)

Minimum levels are also set for flows along primary arcs within the firm network. These minimum flows help to generate some continuity in flow patterns (which may not always occur in a linear programming environment) that are generally associated with core market contract demands. These minimum levels are a percentage (Appendix E, APCT\_MINF) of flows resulting from last year's solution,<sup>46</sup> and are defined as lower bounds on the flow variables. The general bound equation follows.

(flow along the primary arc to satisfy the core market)  $\geq$  (minimum firm flow requirement for the arc)

<sup>46</sup>In the first forecast year, minimum flows are assigned as a percentage of historically derived flows for 1990 (Appendix E - AFLOW\_F, AFLOW\_I).

Nominal minimum flows are also defined for flows along primary arcs in the interruptible network. As with the firm network, the minimum flows are set equal to a percentage (Appendix E, APCT\_MINI) of the flows resulting from the last forecast year's solution, and are defined as lower bounds on the flow variables. This is represented in the following bound equation.

$$(\text{flow along the primary arc to satisfy the noncore market}) \geq (\text{minimum interruptible flow requirement for the arc})$$

Minimum flows are defined on the arcs (to the firm and interruptible transshipment nodes) from the supply sources which are not already specifically targeted for either the firm or interruptible network. This is done to insure that each of these sources supplies a reasonable mix of natural gas to both the firm and interruptible networks. The sum of the minimum flows from each of these supply sources is set equal to the associated minimum supply level (described in Chapter 3). The firm/interruptible split used in setting minimum flows for all of these arcs is equal to the national core and noncore consumption split (after accounting for the supplies specifically targeted to a particular firm or interruptible network). This is represented in the following bound equation.

$$(\text{flow along the supply arc to satisfy the core market}) \geq (\text{minimum firm flow requirement for the arc})$$

$$(\text{flow along the supply arc to satisfy the noncore market}) \geq (\text{minimum interruptible flow requirement for the arc})$$

Finally, a number of bound constraints are needed to completely describe the step functions for the supply and demand curves. These bounds serve to define the lengths of each of the steps on the linearized curves.

### Mathematical Specification of the AFM Linear Program Formulation

This section presents the set of equations which completely defines the linear programming formulation for the AFM, including an objective function, flow constraints, mass balance constraints, and bounds on model variables. The objective function has been defined as the market equilibrium between natural gas supplies and demands, including relevant transportation costs and backstop supply. This has been translated into the following objective function equation.

$$\begin{aligned} \text{minimize}_{x, y_{\text{sup}}, y_{\text{dem}}, q_{\text{zz}}} & \sum_{ij} \text{STAR}_{ij}^F * x_{ij}^F + \sum_{ij} \text{STAR}_{ij}^I * x_{ij}^I + \sum_{si} \text{STAR}_{si}^F * x_{si}^F + \sum_{si} \text{STAR}_{si}^I * x_{si}^I \\ & + \sum_{id} \text{STAR}_{id}^F * x_{id}^F + \sum_{id} \text{STAR}_{id}^I * x_{id}^I + \sum_{id} \text{PZZ}_{id}^F * q_{zz}^F + \sum_{id} \text{PZZ}_{id}^I * q_{zz}^I \\ & + \sum_{sik=1}^c (\text{PSUP}_{sik} * y_{\text{sup},sik}) \\ & - \sum_{idk=1}^n (\text{PDEM}_{idk}^F * y_{\text{dem},idk}^F - \text{PDEM}_{id,-k}^F * y_{\text{dem},id,-k}^F) \\ & - \sum_{idk=1}^n (\text{PDEM}_{idk}^I * y_{\text{dem},idk}^I - \text{PDEM}_{id,-k}^I * y_{\text{dem},id,-k}^I) \end{aligned} \quad (23)$$

where the subscripted indices are:

- $i, j$ , and  $m$  = transshipment node
- $d$  = demand point
- $s$  = supply point
- $st$  = storage point
- $k$  = step on the curve

$c$  = number of steps on the supply curve  
 $n$  = number of steps represented to the left or right of the initial demand point (QDEM0,PDEM0)  
 $i,j$  = arc connecting transshipment nodes  $i$  and  $j$   
 $i,d$  = arc from transshipment node  $i$  to demand point  $d$   
 $s,i$  = arc from supply point  $s$  to transshipment node  $i$   
 $st,i$  = arc from transshipment node  $st$  to storage point  $i$   
 $i,st$  = arc from transshipment node  $i$  to storage point  $st$

the superscripted indices are:

$F$  = firm  
 $I$  = interruptible

the parameters are:

$TAR$  = per unit reservation fee and usage fee (dollars per Mcf)  
 $EFF$  = efficiencies (fraction)  
 $PCAPMAX$  = physical capacity (Bcf)  
 $WTHRXCAP$  = weather factor for normal weather (fraction) [Appendix E, WTHR\_XCAP]  
 $AUTILZ$  = pipeline utilization (from Capacity Expansion Module as fraction)  
 $MINF$  = minimum flow requirement (Bcf)  
 $PZZ$  = price of backstop supply  
           (set to an arbitrarily high value), (dollars per Mcf)  
 $PSUP$  = prices on the supply steps (dollars per Mcf)  
 $PDEM$  = prices on the demand steps (dollars per Mcf)  
 $QDEM0$  = base demand level (Bcf)  
 $QSTR$  = net withdrawals from storage (Bcf)  
 $DISCR$  = discrepancies (Bcf)  
 $UDEM$  = size of demand step (Bcf)  
 $USUP$  = size of supply step (Bcf)  
 $LSUP$  = minimum supply level (Bcf)

the variables are:

$x_{i,j}$  = flow from  $i$  to  $j$  (Bcf)  
 $y_{dem,i,d,k}$  = for demand point  $(i,d)$ , amount of corresponding demand step taken (Bcf)  
 $y_{sup,s,i,k}$  = for supply point  $(s,i)$ , the amount of supply step  $k$  taken (Bcf)  
 $qzz_{i,d}$  = amount of backstop supply used for demand point  $(i,d)$ , (Bcf)

Capacity Constraint Along Each Arc  $i,j$ :

$$x_{i,j}^F + x_{i,j}^I \leq PCAPMAX_{i,j} * (1 - WTHRXCAP_{i,j}) * AUTILZ_{i,j}^T \quad (24)$$

$$x_{i,j}^F \leq PCAPMAX_{i,j} * (1 - WTHRXCAP_{i,j}) * AUTILZ_{i,j}^F \quad (25)$$

Mass Balance Constraints at Each Transshipment Node ( $m$ ):

$$\sum_i x_{i,m}^F * EFF_{i,m} + \sum_s x_{s,m}^F * EFF_{s,m} + QSTR_{st}^F = \sum_d x_{m,d}^F + \sum_i x_{m,i}^F + DISCR_m^F \quad (26)$$

$$\sum_i x_{i,m}^I * EFF_{i,m} + \sum_s x_{s,m}^I * EFF_{s,m} + QSTR_{st}^I = \sum_d x_{m,d}^I + \sum_i x_{m,i}^I + DISCR_m^I \quad (27)$$

Mass Balance Constraints at Each Demand Point (i,d):

$$x_{i,d}^F * EFF_{i,d} + qzz_{i,d}^F = QDEM0_{i,d}^F + \sum_{k=1}^n (ydem_{i,d,k}^F - ydem_{i,d,-k}^F) \quad (28)$$

$$x_{i,d}^I * EFF_{i,d} + qzz_{i,d}^I = QDEM0_{i,d}^I + \sum_{k=1}^n (ydem_{i,d,k}^I - ydem_{i,d,-k}^I) \quad (29)$$

Mass Balance Constraint at Each Supply Point (s,i):

$$\sum_{k=1}^c ysup_{s,i,k} = x_{s,i}^F + x_{s,i}^I \quad (30)$$

Minimum Bounds on Flows Along Bidirectional Arcs (i,j):

$$x_{i,j}^F \Rightarrow MINF_{i,j}^F \quad (31)$$

Minimum Bounds on Flows from Each Designated Supply Point (s,i):

$$x_{s,i}^F \Rightarrow MINF_{s,i}^F \quad (32)$$

$$x_{s,i}^I \Rightarrow MINF_{s,i}^I \quad (33)$$

Minimum Bounds on Flows Along Primary Arcs (i,j):

$$x_{i,j}^F \Rightarrow MINF_{i,j}^F \quad (34)$$

$$x_{i,j}^I \Rightarrow MINF_{i,j}^I \quad (35)$$

The following bound constraints also must be defined for the steps on the supply and demand curves:

$$\begin{array}{lll} 0 \leq ydem_{i,d,k}^F & \leq & UDEM_{i,d,k}^F \\ 0 \leq ydem_{i,d,-k}^F & \leq & UDEM_{i,d,-k}^F \\ 0 \leq ydem_{i,d,k}^I & \leq & UDEM_{i,d,k}^I \\ 0 \leq ydem_{i,d,-k}^I & \leq & UDEM_{i,d,-k}^I \\ LSUP_{s,i,k} \leq ysup_{s,i,k} & \leq & USUP_{s,i,k} \end{array}$$

For the most part LSUP is zero, except on the first step of the supply curve where a minimum supply level may be defined.

Thus, the above equations mathematically specify the linear program objective function and the model constraints. The linear programming solution is obtained using a commercial software package designed to solve these problems.

## Processing of AFM Results

The AFM is responsible for providing other models within NEMS with natural gas end-use and supply prices and quantities which correspond to a market equilibrium between natural gas supply and demand. In addition, the AFM must provide NEMS with resulting pipeline fuel consumption, lease and plant consumption, and emissions levels associated with the network results. Once the linear programming problem is solved, these principal model forecast results are processed using information extracted from the resulting matrix. For example, since the AFM solves at

a regional level which differs somewhat from the NEMS Census divisions and other model's regional definitions (as described in Chapter 3), the AFM results must be aggregated into the regions required by the receiving models prior to being passed to NEMS. Another major processing step is the calculation of average market prices to the core customers. The various methodologies used to generate these model results are presented below.

## ***Supply Prices and Quantities***

The AFM provides wellhead prices and quantities for onshore, offshore, Alaska, and Canadian production, for Canadian, Mexican, and liquefied natural gas imports (at the border crossing), and for synthetic natural gas and other supplemental supplies. With the exception of Canadian import and wellhead prices, these values are obtained directly from the linear programming solution with little or no processing required. For example, wellhead prices obtained from the model solution need to be translated from one regional representation to another. The Mexican and LNG import prices as extracted from the LP are adjusted using item-specific benchmark factors that remain constant throughout the forecast year. Each benchmark factor represents the difference between the model solution (in the last historical year) and the related historical regional import price. Some of these results are passed to the Oil and Gas Supply Model, the Petroleum Market Model and the Coal Market Model for processing, while others are passed to the integrating routine of NEMS for convergence and reporting purposes.

To determine Canadian import and wellhead prices, a netback pricing routine is used in conjunction with benchmark factors. For Canadian import prices, this involves taking the price at the node nearest to the border crossing node, reducing it by the tariff along the arc connecting the two nodes, and then adding a benchmark factor. For example, since Canadian imports from border crossing node 13 go into node 1 on the AFM network (see network defined in Chapter 4), the netback price at node 13 is the node price at node 1, minus the tariff along arc 13 to 1. A benchmark factor is then added to the result to arrive at the Canadian import price. As with the Mexican and LNG import prices, the benchmark factor represents the delta between the netback pricing model result (in the last historical year) and the corresponding historical Canadian import price. Similarly, Canadian wellhead prices are determined by first taking each of the resulting Canadian imports prices (at the border crossing) and subtracting the corresponding Canadian markups from the wellhead, and then taking a quantity-weighted average of the results (adjusted for losses).

## ***End-Use Prices***

The AFM provides regional end-use prices for the Electricity Market Model (electric generation sector) and the other NEMS demand models (nonelectric sectors). For the nonelectric sectors, prices correspond to core and noncore service at the Census Division level. However, for the electric generation sector, prices are determined for three types of customers (core segment, noncore segment competitive-with-residual fuel oil, and noncore segment competitive-with-distillate fuel oil), at two different regional levels (the Census Division level and the NGTDM/EMM subregion level). End-use prices for some sectors/segments within the model are easily determined from the AFM linear programming solution, while others are determined through more rigorous procedures.

End-use prices corresponding to the noncore, nonelectric sector for each Census Division are easily determined from the NGTDM regional prices produced by solving the AFM linear program. Once retrieved from the linear programming solution, the NGTDM regional prices are aggregated into Census Division level results (using a simple quantity-weighted averaging technique) and converted into the appropriate units.

End-use prices for core services cannot be taken directly from the linear programming solution because the linear program prices natural gas at the margin when, in fact, prices for the core segment need to be represented as average prices. A methodology has been established to calculate average regional transshipment node prices, from which average end-use prices for the core segment can be determined. This methodology is based on the premise that the NGTDM network (discounting bidirectional flows) can be viewed as having a quasi "tree" structure, with the primary supply sources at the bottom (or root) and the more distant demand regions at the top. Using this tree structure, average firm transshipment node prices are calculated starting from the root and moving up to the top branches. At each regional transshipment node, the average price is calculated as a quantity-weighted average of gas coming from

other regions and gas produced within the region. Gas produced from other regions is priced at the average transshipment node price in the other region, plus the cost-based tariff to move the gas from the other region. Note that average prices are calculated after the linear program has been solved. This should not directly impact other NGTDM model results (e.g., interregional flows) since core demands are relatively inelastic to price changes (reflected in the fact that the model assumes a price elasticity of zero for the core demand curves).

End-use prices for core customers in a region are then set by adding the intraregional tariff, the intrastate tariff, the distributor tariff, and a citygate benchmark factor to the average regional transshipment node price (see Chapter 6 for details). These regional prices are then aggregated to the Census Division level using a simple quantity-weighted average technique and converted to the appropriate units. Note that regional core transportation end-use prices are determined in a similar fashion but are defined individually for fleet vehicles (PGFTRFV) and personal vehicles (PGFTRPV). A quantity-weighted averaging routine is used to determine the combined end-use price for the core transportation sector.

Electric generation sector prices are sent to the Electricity Market Model at the NGTDM/EMM subregion level and to NEMS (for convergence and reports) at the Census Division level. The Electricity Market Model requires prices to be reported for all three market segments, while NEMS requires that prices for the competitive markets be combined into an average noncore price. Different methodologies are used to determine the delivered natural gas price to each of the three electric generation market segments. Electric generation sector prices to core customers in each NGTDM/EMM region are determined by adding the intraregional tariff, the intrastate tariff, the distributor tariff, and a citygate benchmark factor to the average associated NGTDM regional firm transshipment node price (defined above), processed to represent the appropriate regions (NGTDM/EMM subregions for the Electricity Market Model and Census Divisions for NEMS), and converted into the proper units. Two user-defined options exist for determining electric generation sector prices to the competitive (residual and distillate) segments: (1) the sum of interruptible transshipment node price, the intraregional, intrastate, and distributor tariffs, and a benchmark factor, or (2) a function of their corresponding competitive fuel price. See Chapter 6 for details. Next, a quantity-weighted averaging routine is used to combine the two competitive segments into a single average end-use price to send to NEMS.

### ***Pipeline Fuel Consumption and Associated Emissions***

For each arc of the network, pipeline fuel consumption is calculated by multiplying the flow on the arc by the percentage (specified as a fraction) lost due to pipeline fuel use. This percentage lost is 1 minus the efficiency specified along the arc. The efficiency term is defined using input data in conjunction with a multiplicative scaling factor which is used to calibrate the results to equal the most recent national historical or STEO pipeline fuel consumption. The pipeline fuel use along each arc of the network must be translated to fuel use by NGTDM region. This disaggregation is accomplished by multiplying the fuel use on each arc by regional shares based on the mileage of pipe in a given region (Appendix E, NG\_ARCSIZE). A similar loss factor is applied along each intraregional arc to account for losses accrued in the distribution process.

Pipeline fuel consumption is used as a basis for calculating the emissions which result from pipeline compressor engine use. Both reciprocating engines and gas turbines are used to power compressors. The latter engines outnumber the former by a factor of approximately 3.3, primarily because they accommodate higher capacity flows at a greater efficiency. However, the reciprocating engines allow for greater variation in flows and are able to send flows in both directions along the pipe. According to estimates by Argonne National Laboratory (presented in the *NES Environmental Analysis Model (NESEAM): ANL Technical Memorandum*, Section "Natural Gas" of the Appendix C), 77 percent of the engines used for pipeline transportation are gas turbines and 23 percent are reciprocating piston compression engines.

The NGTDM quantifies eight types of pollutants discharged by the combustion of natural gas at gas pipeline compressor stations: total carbon, nitrogen oxides, sulfur oxides, carbon monoxide, carbon dioxide, methane, volatile organic compounds, and particulate. Since data on particulate emissions are not available and particulate emission levels are assumed to be small, estimates for particulate emissions are not included. Estimates for the discharge levels of the other pollutants are calculated as functions of the pipeline fuel consumption. In the last five years,



pipeline fuel consumed by the compressor stations represents about 3.6 percent of the annual amount of gas delivered to consumers. Natural gas pipeline emissions by NGTDM region are calculated as the product of the annual pipeline fuel consumption in the region times an emissions factor, as follows:

$$EMNT_{r,p,y} = QGPTR_{r,y} * EMISRAT_p / (CFNGC * 2205.0) \quad (36)$$

where,

- $p$  = subscript that designates any of the eight types of pollutants discussed above (1-total carbon, 2-carbon monoxide, 3-carbon dioxide, 4-sulfur oxides, 5-nitrogen oxides, 6-volatile organic compounds, 7-methane, 8-particulates)
- $QGPTR_{r,y}$  = annual pipeline fuel consumption in year  $y$  for Census Division  $r$  (Trillion BTU)
- $EMISRAT_p$  = emissions factor (Appendix E) (thousand pounds emissions per billion cubic feet pipeline fuel consumed)
- $CFNGC$  = Conversion factor (Trillion BTU/BCF)
- $EMNT_{r,p,y}$  = natural gas pipeline annual emissions, in thousand metric tons (MMT) in Census Division  $r$  and year  $y$ .

[Note: The constant 2205.0 in the equation converts the result in pounds to metric tons.]

A separate carbon emissions routine within the NEMS overrides the emissions levels calculated within the NGTDM and establishes the final reported carbon emissions levels for the NEMS.

### **Realized Pipeline Tariff**

The Pipeline Tariff Module provides the AFM with a minimum and maximum usage fee, as well as an estimated usage fee for use in the model for transporting gas between regions under interruptible service. Once the linear program is solved, the realized tariff along each arc in the network equals the difference between the market clearing prices at the two connected transshipment nodes. If the natural gas flow along the arc is less than its capacity limit, the realized tariff equals the usage fee assigned when the linear program was formulated. If the flow along the arc is at its limit, the realized tariff will be greater than (or possibly equal to) the usage fee originally specified and could exceed its maximum allowed level. A check is made to identify any realized tariff greater than its allowed maximum. Currently no adjustment is made within the model if this maximum is exceeded, although it typically is not. Proposals have been discussed concerning the Federal Energy Regulatory Commission (FERC) lifting this regulatory limit on interruptible tariffs.



## 6. Distributor Tariff Module Solution Methodology

This chapter discusses the solution methodology for the Distributor Tariff Module (DTM) of the Natural Gas Transmission and Distribution Model (NGTDM). The DTM develops distributor tariffs and the corresponding markups that are applied to regional hub prices to derive end-use prices within a region. The hub prices are equal to either the market clearing price for supplies to noncore customers or average market prices for supplies to core customers. These markups include an intraregional interstate, an intrastate, and a sector specific distributor tariff, as well as a benchmark factor. The intraregional interstate tariffs are provided by the Pipeline Tariff Module. The intrastate tariffs are set exogenously; and the benchmark factors are established endogenously to calibrate citygate prices to historical values.<sup>47</sup> Distributor tariffs are assigned within the DTM.

Distributor tariffs, and therefore markups, are determined separately for the residential, commercial, industrial, electric generator, and transportation (compressed natural gas vehicle) sectors. Distributor tariffs for the industrial sector and electric generators are segmented by core and noncore markets, whereas residential, commercial, and natural gas vehicle customers are classified as core. It is assumed that core customers receive all of their natural gas under firm (or near-firm) transportation agreements and that noncore customers transport their gas under interruptible or short-term capacity release transportation agreements. As described in Chapter 3, the noncore electric generator sector has been further divided into two customer classes within NEMS: dual-fired electric generating units that are switchable to residual fuel oil (competitive-with-residual fuel), and gas turbines and dual-fired turbines that are switchable to distillate fuel oil (competitive-with-distillate). Consequently, distributor tariffs, markups, and end-use prices are defined separately for these two noncore service types. Similarly, the core transportation sector is composed of two categories of compressed natural gas (CNG) consumers (fleet vehicles and personal vehicles) and also has separate pricing components.

The primary task of the DTM is to determine regional core and noncore (where applicable) distributor tariffs for each end-use sector. Distributor tariffs to core customers are based on estimates of (1) the cost of providing service to the core end user, (2) recovery of fixed costs from the noncore segment of the market, (3) industry efficiency improvements, and (4) bypass by large industrial and electric utility consumers. Noncore distributor tariffs are based on historical tariffs, with assumed decline rates. A primary factor in the selection of methodologies for developing distributor tariffs was the lack of publicly available data to develop a detailed cost-based accounting methodology similar to the approach used for interstate pipeline tariffs in the Pipeline Tariff Module.

The calculation of the following are discussed in the remainder of this chapter in the given order: the end-use prices by sector, the price markups from the hub to the end-user by sector, and finally the components of these markups (primarily the distributor tariffs).

### Markups and End-Use Pricing in Natural Gas Markets

#### **End-Use Prices**

End-use prices for the residential, commercial, industrial, transportation, and electric generation sectors are comprised of five components: (1) the regional hub price of natural gas, (2) the tariff for intraregional movements of natural gas on the interstate network, (3) a tariff for intrastate pipeline services, (4) a tariff covering the costs of distribution services, and (5) a citygate benchmark factor. The latter four components are consolidated into a markup. In establishing the final end-use price, both the markup and the supply price at the hub are adjusted using an "efficiency" factor to account for the use of fuel in transporting natural gas from the regional hub to the end user.

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<sup>47</sup>The intrastate tariffs are currently set to zero and are indirectly accounted for within the distributor tariffs.

## Nonelectric Sector End-Use Prices

The primary equations for determining core and noncore natural gas end-use prices for the nonelectric sectors are provided below. (The transportation sector is presented separately following these equations.)

### Core

$$\text{NONU\_PR\_F}_{ij} = (\text{NG\_AVGPR\_F}_j + \text{LPMU\_NONU\_F}_{ij}) / (\text{NEFF\_PIPE}_{ij} * \text{AEFF\_PIPE}_{jj}) \quad (37)$$

### Noncore

$$\text{NONU\_PR\_I}_{ij} = (\text{NG\_MAGPR\_I}_j + \text{LPMU\_NONU\_I}_{ij}) / (\text{NEFF\_PIPE}_{ij} * \text{AEFF\_PIPE}_{jj}) \quad (38)$$

where,

NONU_PR_F	=	natural gas end-use price to the core nonelectric sectors (dollars per Mcf)
NG_AVGPR_F	=	hub price for firm service [derived from Annual Flow Module solution matrix (dollars per Mcf)] <sup>48</sup>
LPMU_NONU_F	=	markup from firm service hub price to core nonelectric sectors, before adjusting for pipeline fuel use (dollars per Mcf)
NONU_PR_I	=	natural gas end-use price for noncore nonelectric sectors (dollars per Mcf)
NG_MAGPR_I	=	hub price for interruptible service [from Annual Flow Module solution matrix (dollars per Mcf)]
LPMU_NONU_I	=	markup from interruptible service hub price to noncore nonelectric sectors, before adjusting for pipeline fuel use (dollars per Mcf)
NEFF_PIPE	=	efficiency factor for accounting for fuel use to transport natural gas from the regional hub to end-use customers [Appendix E]
AEFF_PIPE	=	efficiency factor for accounting for fuel use in the intraregional interstate transport of gas [Appendix E]
i	=	end-use sector index
j	=	region index (jj equates to intraregional activity).

Before completing the processing of nonelectric end-use prices, the DTM checks the prices against a minimum threshold price of \$0.00001 per Mcf. The purpose of this check is to send a nonzero price to the NEMS Integrating Module in situations where there is no gas consumption by a sector in a given region. Should the end-use price be very small, the price is reset to the last price that is available (either from a previous iteration, model year, or historical period) for the sector and region.

Regional transportation sector end-use prices (assumed to be core) are determined in a similar fashion, but are defined individually for fleet vehicle and personal vehicle use.

### Core fleet vehicles

$$\text{TRFV\_PR\_F}_j = (\text{NG\_AVGPR\_F}_j + \text{LPMU\_TRFV\_F}_j) / (\text{NEFF\_PIPE}_{i=j} * \text{AEFF\_PIPE}_{jj}) \quad (39)$$

### Core personal vehicles

$$\text{TRPV\_PR\_F}_j = (\text{NG\_AVGPR\_F}_j + \text{LPMU\_TRPV\_F}_j) / (\text{NEFF\_PIPE}_{i=j} * \text{AEFF\_PIPE}_{jj}) \quad (40)$$

where,

TRFV_PR_F	=	natural gas end-use price for the fleet vehicle sector (dollars per Mcf)
LPMU_TRFV_F	=	markup from firm service hub price to the fleet vehicle transportation sector, before adjusting for pipeline fuel use (dollars per Mcf)

<sup>48</sup> A description of the calculation of an average hub (or transshipment node) price is presented in Chapter 5.

TRPV_PR_F	=	natural gas end-use price for the personal vehicle transportation sector (dollars per Mcf)
LPMU_TRPV_F	=	markup from firm service hub price to the personal vehicle transportation sector, before adjusting for pipeline fuel use (dollars per Mcf)
NG_AVGPR_F	=	hub price for firm service [derived from Annual Flow Module solution matrix (dollars per Mcf)]
NEFF_PIPE	=	efficiency factor to account for fuel used to transport natural gas from the regional hub to end-use customers [Appendix E]
AEFF_PIPE	=	efficiency factor to account for fuel used for the intraregional transport of natural gas [Appendix E]
i	=	end-use sector index (i=4 for transportation sector)
j	=	region index (j,j equates to intraregional activity).

If the regional end-use price of CNG for personal vehicles (TRPV\_PR\_F) is greater than the regional commercial sector motor gasoline price (defined by the Petroleum Market Model), then the resulting price is determined to be the greater of the following:

- 1: PMGCM<sub>j</sub> \* CFNGN
- 2: TRPV\_PR\_F<sub>j</sub> - (RETAIL\_COST \* RETAIL\_PCT)

where,

PMGCM	=	commercial sector motor gasoline price (dollars per MMBtu)
TRPV_PR_F	=	end-use price of CNG consumed by personal vehicles (dollars per Mcf)
RETAIL_COST	=	dispensing charge above fuel cost (dollars per Mcf) [Appendix E]
RETAIL_PCT	=	discount on dispensing charge (fraction -- 0.20)
CFNGN	=	conversion factor (=1.031 MMBtu per Mcf)
j	=	region index.

### Electric Sector End-Use Prices

An equation similar to that used for the nonelectric sectors is used for determining core end-use prices for the electric generation sector:

$$UTIL\_PR\_F_{j,n} = (NG\_AVGPR\_F_j + LPMU\_UTIL\_F_{j,n}) / (UEFF\_PIPE_{j,n} * AEFF\_PIPE_{j,j}) \quad (41)$$

where,

UTIL_PR_F	=	end-use price for core electric generator sector (dollars per Mcf)
NG_AVGPR_F	=	hub price for firm service [derived from Annual Flow Module solution matrix (dollars per Mcf)]
LPMU_UTIL_F	=	markup from the firm service hub price to the core electric generator sector, before adjusting for pipeline fuel use (dollars per Mcf)
UEFF_PIPE	=	efficiency factor to account for fuel used to transport natural gas from the regional hub to electric generator customers [Appendix E]
AEFF_PIPE	=	efficiency factor to account for fuel used for intraregional transport of natural gas [Appendix E]
j	=	region index (j,j equates to intraregional activity)
n	=	Electricity Market Module region index.

The end-use prices for the two categories of the noncore electric generator sector are calculated as follows:

#### Competitive-with-residual fuel

$$UTIL\_PR\_IR_{j,n} = (NG\_MAGPR\_I_j + LPMU\_UTIL\_IR_{j,n}) / (UEFF\_PIPE_{j,n} * AEFF\_PIPE_{j,j}) \quad (42)$$

#### Competitive-with-distillate

$$UTIL\_PR\_ID_{j,n} = (NG\_MAGPR\_I_j + LPMU\_UTIL\_ID_{j,n}) / (UEFF\_PIPE_{j,n} * AEFF\_PIPE_{j,n}) \quad (43)$$

where,

UTIL_PR_IR	=	natural gas end-use price for noncore competitive-with-residual fuel electric generation sector (dollars per Mcf)
LPMU_UTIL_IR	=	markup from interruptible hub price to the noncore competitive-with-residual fuel electric generation sector, before adjusting for pipeline fuel use (dollars per Mcf)
UTIL_PR_ID	=	natural gas end-use price for noncore competitive-with-distillate electric generation sector (dollars per Mcf)
LPMU_UTIL_ID	=	markup from interruptible hub price to the noncore competitive-with-distillate electric generation sector, before adjusting for pipeline fuel use (dollars per Mcf)
NG_MAGPR_I	=	hub price for interruptible service [from Annual Flow Module solution matrix (dollars per Mcf)]
UEFF_PIPE	=	efficiency factor to account for fuel used to transport natural gas from the regional hub to end-use customers [Appendix E]
AEFF_PIPE	=	efficiency factor to account for intraregional transport of natural gas [Appendix E]
j	=	NGTDM region index
n	=	Electricity Market Module region index.

An option for a second methodology for setting noncore electric generator prices is available and has been used in the past. The specific equations follow:

#### Competitive-with-residual fuel

$$UTIL\_PR\_IR_{j,n} = PR\_MIN_{j,n} \quad (44)$$

where,

UTIL_PR_IR	=	natural gas end-use price for the noncore competitive-with-residual fuel electric generation sector (dollars per Mcf)
PR_MIN	=	discounted alternative fuel price (dollars per Mcf)
j	=	NGTDM region index
n	=	Electricity Market Module region index.

The discounted alternative fuel price is the product of the alternative fuel price (residual fuel oil) times a discount factor. The discount factor is the lesser of the natural gas-to-residual fuel oil price ratio provided by the Electricity Market Module (GRATMAX, equal to the price at which electric generators will burn the maximum amount of gas as opposed to residual fuel oil) or the natural gas-to-residual fuel oil price ratio specified within the NGTDM (Appendix E, NGRATMAX).

#### Competitive-with-distillate

$$UTIL\_PR\_ID_{j,n} = PERCDISC_{j,n} * PDSEL_j * CFNGU \quad (45)$$

where,

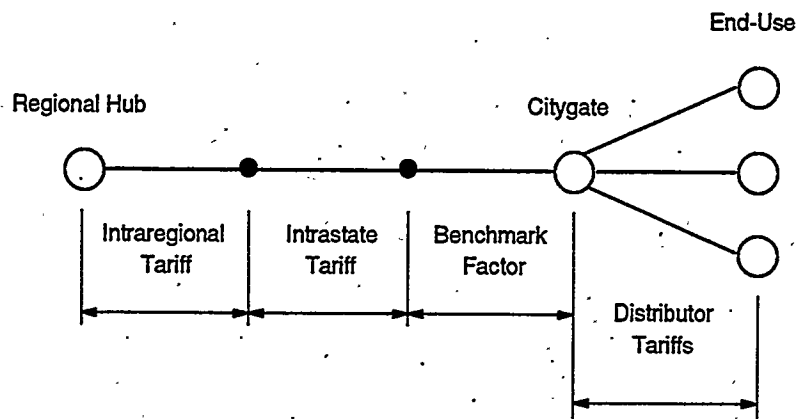
UTIL_PR_ID	=	natural gas end-use price for noncore competitive-with-distillate electric generation sector (dollars per Mcf)
PDSEL	=	alternative fuel price (distillate fuel oil) to the electric generation sector (dollars per MMBtu)
PERCDISC	=	percent discount off alternative fuel price (Appendix E, UPDP1)
CFNGU	=	conversion factor [assigned by NEMS system at 1.034 (MMBtu per Mcf)]
j	=	NGTDM region index
n	=	Electricity Market Module region index.

Under this alternative option, the effective distributor tariff resulting from setting the end-use price based on the alternative fuel is checked against an assumed minimum (Appendix E -- URFLOOR, UDFLOOR). If the minimum is violated the end-use price is adjusted accordingly. Under both options, an aggregate noncore end-use price for the electric generation sector (UTIL\_PR\_I) is calculated as the quantity-weighted average of both components.

## Markups

All of the markups from the firm or interruptible hub to the end-use price mentioned above are comprised of four separate cost components -- distributor tariffs, intraregional tariffs, intrastate tariffs, and a citygate benchmark factor. These tariff and benchmark components are presented in Figure 6-1. The distributor tariff component is region and sector specific, while the other components are only region specific. Distributor tariffs are calculated within the model each iteration of each forecast year, with historical levels used during historical years. The methodologies used to calculate distributor tariffs for core and noncore customers are defined in the next two sections of this chapter. Intraregional pipeline tariffs are provided by the Pipeline Tariff Module each forecast year, while the intrastate tariffs are input assumptions that remain constant throughout the forecast. Citygate benchmark factors are determined endogenously to the model.

Figure 6-1. Tariff and Benchmark Components of Regional Markups



The generic equation for the markups from a hub price to an end-user follows:

$$LPMU_j = DTAR_j + PTAR_{j,j} + INTRA\_TAR_j + CGBENCH_j \quad (46)$$

where,

- LPMU = markup from an either firm or interruptible hub price to either the core or noncore end-use price for a given sector within region j
- DTAR = distributor tariff for either the core or noncore category of a given end-use sector within region j
- PTAR = tariff for intraregional (firm--PTAR\_F or interruptible--PTAR\_I) service provided by interstate pipelines within region j
- INTRA\_TAR = tariff for (firm--INTRA\_TARF or interruptible--INTRA\_TARI) intrastate pipeline services [Appendix E]

CGBENCH = (firm--CGBENCHF or interruptible--CGBENCHI) citygate benchmark factor  
 j = region index (j,j equates to intraregional activity)

The specific variables used in the NGTDM and referenced in the documentation for each of the sectors/categories represented are shown below (where s represents a sector index):

Sector/Category	LPMU	DTAR
Core nonelectric	LPMU_NONU_F <sub>j</sub>	NONU_DTAR_F <sub>j</sub>
Noncore nonelectric	LPMU_NONU_I <sub>j</sub>	NONU_DTAR_I <sub>j</sub>
Fleet vehicles	LPMU_TRFV	DTAR_TRFV_F
Personal vehicles	LPMU_TRPV	DTAR_TRPV_F
Core electric generator	LPMU_UTIL_F	UTIL_DTAR_F
Noncore electric generator	LPMU_UTIL_I	UTIL_DTAR_I
Competitive-with-residual fuel	LPMU_UTIL_IR	UTIL_DTAR_IR
Competitive-with-distillate	LPMU_UTIL_ID	UTIL_DTAR_ID

## Core Distributor Tariffs

A new algorithm has been developed for the DTM that sets distributor tariffs for core customers. The algorithm is responsive in part to revenues generated from the noncore segment of the market, user-specified industry efficiency improvements, and user-specified assumptions on bypass by large industrial and electric utility consumers. The methodology is based on the concept that a portion of the revenues from interruptible customers are used to offset firm revenue requirements as viewed by a local distribution company (LDC). The transportation sector is not included among the sectors for which this algorithm is used because of the current nature of the market: the use of compressed natural gas as a vehicle fuel is evolving from government/industry sponsored demonstration programs to large scale commercial use. Therefore, a separate methodology is used to determine distributor tariffs for the transportation sector. These are described separately below.

## Residential, Commercial, Industrial, and Electric Generation Sectors

In general, the new DTM algorithm estimates the annual change in total costs associated with providing distribution services to core customers, accounts for any recovery of fixed costs from the noncore segment of the market, and adjusts the previous year's distributor tariffs for each of the end-use sectors to reflect the resulting annual change in revenue requirement. First, regional core market revenue requirements ( $RR^F_{r,s}$ ) are set based on an endogenously derived total cost ( $TC^F_{r,s}$ ) for core distribution services and an assumed noncore market contribution ( $ICC_r$ ) to fixed costs. Next, core distributor tariffs ( $DTAR^F_{r,s}$ ) are estimated for each sector and region based on the core distributor tariff ( $DTAR^F_{r,s,t-1}$ ) from the previous year and the annual percentage change in natural gas volumes consumed by core customers ( $Vol^F_{r,s}$ ). These tariffs are then used to estimate the revenue requirements ( $RR^F_{r,s}$ ) that would be met from core customers if these estimated distributor tariffs ( $DTAR^F_{r,s}$ ) were charged. Finally, core distributor tariffs ( $DTAR^F_{r,s}$ ) for the current forecast year are set by adjusting these estimated regional core distributor tariffs by apportioning the associated difference in revenue requirements ( $\alpha_r$ ) between the forecasted and estimated values to the sectors represented based on their relative contribution to the total revenue requirement. The following equations describe this process in mathematical terms.



## Variable Definitions

The variables used in the subsequent equations are defined as follows.

### Subscripts and Superscripts

F =	core market (receiving firm transportation service)
I =	noncore market (receiving interruptible transportation service)
r =	region
s =	sector
res =	residential sector
com =	commercial sector
ind =	industrial sector
util =	electric generation sector
t,y =	year
t-1 =	previous year

### Variables

RR =	market revenue requirements (87\$)
RR_E =	estimated market revenue requirements (87\$)
TC =	total cost to provide distribution services to customers (87\$)
ICC =	noncore revenue contribution to fixed costs (87\$)
Vol =	volume of natural gas consumption (Bcf)
ByPass =	percent of noncore volumes that bypass the LDC [Appendix E -- I_BYPASS, (fraction)]
DTAR =	distributor tariffs (87\$/Mcf)
minDTAR <sup>I</sup> =	minimum noncore distributor tariff [Appendix E -- MINMU_I, (87\$/Mcf)]
DTAR_E =	estimated market distributor tariff (87\$/Mcf)
MIN_DELTA =	minimum offset to shift DTAR from negative to positive (87\$/Mcf) [\$0.50 plus the lowest nonpositive distributor tariff from the previous year]
$\alpha$ =	delta between forecasted RR and estimated RR (87\$)
$\beta$ =	percent of profit from noncore revenues contributed to offset core market distribution costs [Appendix E -- DTM_BETA, (fraction)]
g =	percent change in total core market distribution costs (fraction)
k =	capital costs (87\$)
w =	employment costs (87\$)
TechEff =	technical efficiency factor [Appendix E, TECHEFF]

### Model Variables

MC_ECIWSPNS =	employment cost index -- private wage and salary (provided by the Macroeconomic Model)
MC_CPI =	consumer price index (provided by the Macroeconomic Model)
COSTCAP =	cost of capital
AVG_COSTCAP =	average cost of capital
WT_DEBT =	weighting for debt/equity contribution to cost of capital [Appendix E, (fraction)]
NG_REALRMGBLUS =	real dollar yield on 10 year U.S. Government bonds (forecast values provided by the Macroeconomic Model, historical values in H_REALRMGBLUS -- Appendix E)
MC_RMPUAANS =	yield on AA utility bonds (forecast values provided by the Macroeconomic Model, historical values in H_RMPUAANS -- Appendix E)
AVG_RMPUAANS =	20-year rolling average of yield on AA utility bonds
MC_PDGP =	GDP deflator index (provided by Macroeconomic Model)

## Determine Regional Core Revenue Requirements

Regional core revenue requirements are a function of total core customer related costs and the recover of fixed costs from noncore customers within the region.

Regional core revenue requirements = regional total firm costs - regional noncore contribution to fixed costs

$$RR^F_r = TC^F_r - ICC_r \quad (47)$$

Assuming that a portion (ByPass) of the noncore customers bypass the LDC,<sup>49</sup> that the regional noncore recovery of fixed costs is a proportion  $\beta$  of the regional noncore profits collected by the LDC, and that noncore profits represent noncore revenues that exceed the cost of providing noncore services, then:

Regional noncore contribution to fixed costs = [ total regional noncore volume \* (1 - LDC bypass) \* (regional noncore distributor tariff - minimum regional noncore distributor tariff) \*  $\beta$

$$ICC_r = \sum_s (Vol^I_{r,s} * (1 - ByPass_r) * (DTAR^I_{r,s} - \min DTAR^I_r)) * \beta \quad (48)$$

Due to the lack of available data for regional costs related to core distributor services, historical values for these costs are derived from the data that are available and annual changes in costs are forecast using model input parameters. Some of these parameters were based on statistical estimates presented by Mary Lashley Barcella in her paper, "Natural Gas Distribution Costs and Efficiency Implications for Regulation." The paper presents a total distributor cost equation with parameters estimated on the basis of data from 50 local gas distribution companies covering the period 1969 through 1988. The parameter estimates from her work have been used to forecast the annual change in total regional distributor costs associated with core customers, as represented by the explicit values shown below:

$$g_r = \% \Delta TC^F_r = [ 0.400 * \% \Delta (Vol^F_{r,rs} + Vol^F_{r,com}) + 0.117 * \% \Delta (Vol^F_{r,ind} + Vol^F_{r,nul}) + 0.2678 * \% \Delta k + 0.1671 * \% \Delta w ] \quad (49)$$

The percentage change in volumes are calculated as:

$$\% \Delta Vol = \frac{Vol_t - Vol_{t-1}}{Vol_{t-1}} \quad (50)$$

The percentage change in employment costs (w) are calculated using the variables MC\_ECIWSPNS and MC\_CPI, set within the Macroeconomic Model of the NEMS, as estimates to employments costs:

$$\% \Delta w = \frac{\frac{MC\_ECIWSPNS_t}{MC\_CPI_t} - \frac{MC\_ECIWSPNS_{t-1}}{MC\_CPI_{t-1}}}{\frac{MC\_ECIWSPNS_{t-1}}{MC\_CPI_{t-1}}} \quad (51)$$

The percentage change in cost of capital (k) is similarly obtained using an average cost of capital (represented as a three year rolling average). The cost of capital is estimated using a weighted average of the yield on AA bonds (20-year rolling average) and the yield on 10-year government bonds. The corresponding equations are:

$$\% \Delta k = \frac{AVG\_COSTCAP_t - AVG\_COSTCAP_{t-1}}{AVG\_COSTCAP_{t-1}} \quad (52)$$

where,

<sup>49</sup>Only noncore customers are assumed to bypass the local distribution companies.

$$\text{AVG\_COSTCAP}_t = \frac{\text{COSTCAP}_t + \text{COSTCAP}_{t-1} + \text{COSTCAP}_{t-2}}{3} \quad (53)$$

$$\text{COSTCAP}_t = \text{WT\_DEBT} * \text{AVG\_RMPUAANS}_t + (1 - \text{WT\_DEBT}) * \text{NG\_REALRMGBLUS} \quad (54)$$

$$\text{AVG\_RMPUAANS}_t = \frac{\sum_{y=t-19}^t [\text{MC\_RMPUAANS}_y - (100 * (\text{MC\_PGDP}_t / \text{MC\_PGDP}_{t-1}) - 1)]}{20} \quad (55)$$

Finally, the total cost for distributor service to core customers for the forecast year, by region, is:

$$\text{TC}_r^F = \text{TC}_{r,t-1}^F * (1 + g_r) * \text{TechEff} \quad (56)$$

The TechEff term is present to capture the impact of advances in technical efficiencies.

#### Estimate Core Distributor Tariffs and Corresponding Revenue Requirements

Regional core distributor tariffs are estimated for each end-use sector as a function of corresponding firm tariffs in the previous year and the annual percentage change in core consumption or volumes.

$$\text{DTAR\_E}_{r,s,t}^F = [(\text{DTAR}_{r,s,t-1}^F + \text{MIN\_DELTA}_t) * (1 + \gamma_i * \% \Delta \text{Vol}_{r,s}^F)] - \text{MIN\_DELTA}_t \quad (57)$$

where  $\gamma_i$  (Appendix E, TCF\_COEFF) are the various parameter estimates for the end-use sector terms from Mary Lashley Barcella's study (also used in equation 49). Note that the MIN\_DELTA term was added to the distributor tariff and then subtracted from the estimated tariff in order to counter the impact of applying a percentage change to any negative tariffs.

The  $\% \Delta \text{Vol}_{r,s}^F$  term represents percentage change in volume, calculated as follows:

$$\% \Delta \text{Vol}_{r,\text{util}}^F = \frac{\text{Vol}_{r,\text{util},t}^F - \text{Vol}_{r,\text{util},t-1}^F}{\text{Vol}_{r,\text{util},t-1}^F + \text{Vol}_{r,\text{ind},t-1}^F} \quad (58)$$

$$\% \Delta \text{Vol}_{r,\text{ind}}^F = \frac{\text{Vol}_{r,\text{ind},t}^F - \text{Vol}_{r,\text{ind},t-1}^F}{\text{Vol}_{r,\text{util},t-1}^F + \text{Vol}_{r,\text{ind},t-1}^F} \quad (59)$$

$$\% \Delta \text{Vol}_{r,\text{res}}^F = \frac{\text{Vol}_{r,\text{res},t}^F - \text{Vol}_{r,\text{res},t-1}^F}{\text{Vol}_{r,\text{res},t-1}^F + \text{Vol}_{r,\text{com},t-1}^F} \quad (60)$$

$$\% \Delta \text{Vol}_{r,\text{com}}^F = \frac{\text{Vol}_{r,\text{com},t}^F - \text{Vol}_{r,\text{com},t-1}^F}{\text{Vol}_{r,\text{res},t-1}^F + \text{Vol}_{r,\text{com},t-1}^F} \quad (61)$$

These distributor tariffs are then used to obtain an estimate of regional core revenue requirements:

$$\text{RR\_E}_{r,t}^F = \text{DTAR\_E}_{r,\text{res},t}^F * \text{Vol}_{r,\text{res},t}^F + \text{DTAR\_E}_{r,\text{com},t}^F * \text{Vol}_{r,\text{com},t}^F + \text{DTAR\_E}_{r,\text{ind},t}^F * \text{Vol}_{r,\text{ind},t}^F + \text{DTAR\_E}_{r,\text{util},t}^F * \text{Vol}_{r,\text{util},t}^F \quad (62)$$

## Determine Final Core Distributor Tariffs

Final core distributor tariffs for each region are determined by adding an adjustment factor to the estimated distributor tariff to account for the difference between the forecasted and estimated core revenue requirements. This adjustment factor (adjDTAR) is set by apportioning this difference in revenue requirements to the represented sectors based on an estimate of each sector's relative contribution to the total revenue requirement, as follows:

$$\alpha_{r,t} = RR_{r,t}^F - RR_{r,t}^E \quad (63)$$

$$adjDTAR_{r,s,t}^F = \frac{\alpha_{r,t}}{Vol_{r,s,t}^F} * \frac{(DTAR_{r,s,t-1}^F + MIN\_DELTA_r) * Vol_{r,s,t}^F}{\sum_s [(DTAR_{r,s,t-1}^F + MIN\_DELTA_r) * Vol_{r,s,t}^F]} \quad (64)$$

$$DTAR_{r,s,t}^F = DTAR_{r,s,t}^E + adjDTAR_{r,s,t}^F \quad (65)$$

## Determine Base Year Total Core Market Distribution Costs

Total core market distribution costs need to be established in the base year to provide a lagged value for total costs in equation 56. This can be calculated using a form of equation 47 above:

$$TC_r^F = RR_r^F + ICC_r \quad (66)$$

For the base year, the model reads historical firm and interruptible citygate prices by region and core and noncore end-use prices by sector and region. From these data core and noncore distributor tariffs are derived for each sector in each region. Given user specified assumptions for ByPass, minDTAR<sub>r</sub><sup>i</sup>, and β, equation 48 above can be used to derive ICC<sub>r</sub>. Then, assuming that regional revenue requirements are equal to firm revenues, firm revenue requirements (RR<sub>r</sub><sup>F</sup>) can be estimated as the product of firm distributor tariffs and volumes. Thus, base year total costs are derived.

## Transportation Sector

Consumers of compressed natural gas (CNG) have been classified into two end-use categories within the core transportation sector: fleet vehicles and personal vehicles. Two different pricing methodologies are defined for determining distributor tariffs to these two end-use categories, with the sector average (NONU\_DTAR<sub>F</sub><sub>i=j=region</sub>) being determined as a quantity weighted average of both end-use categories. Distributor tariffs associated with fleet vehicles are a function of the historical distributor tariffs, a decline rate, and state and federal taxes, as shown:

$$DTAR\_TRFV\_F_j = [HNONU\_DTAR\_F_{i=j,h} * (1 - TRN\_DECL)^{YR\_DECL}] + STAX_j + FTAX \quad (67)$$

where,

DTAR_TRFV_F	=	distributor tariff for the fleet vehicle transportation sector, before adjusting for pipeline fuel use (dollars per Mcf)
HNONU_DTAR_F	=	historical distributor tariff for the transportation sector (assumed to be primarily for fleet vehicles), before adjusting for pipeline fuel use (dollars per Mcf)
TRN_DECL	=	fleet vehicle distributor decline rate [Appendix E, (fraction)]
YR_DECL	=	difference between the current year and the last historical year over which the decline rate is applied
STAX	=	CNG state taxes (dollars per Mcf)
FTAX	=	CNG federal tax (dollars per Mcf)
i	=	end-use sector index
j	=	region index
h	=	index for last year historical data are available.

The methodology used to determine distributor tariffs for CNG consumed by personal vehicles is called the full cost price method. Under this method, the distributor tariff is derived as a function of the full cost of delivering CNG to these alternate fuel vehicles. Thus, the distributor tariff is set equal to the sum of the core industrial distributor tariff, the cost of dispensing CNG at a high volume service station, State motor vehicle fuel tax applied to CNG, and Federal motor vehicle fuel tax applied to CNG, as shown in the following equation:

$$DTAR\_TRPV\_F_j = NONU\_DTAR\_F_{i=3,j} + RETAIL\_COST + STAX_j + FTAX \quad (68)$$

where,

DTAR_TRPV_F	=	distributor tariff for the personal vehicle transportation sector, before adjusting for pipeline fuel use (dollars per Mcf)
NONU_DTAR_F	=	distributor tariff for the core industrial sector, i=3 (dollars per Mcf)
RETAIL_COST	=	cost of dispensing CNG [Appendix E, (dollars per Mcf)]
STAX	=	State motor vehicle fuel tax applied to CNG [Appendix E, (dollars per Mcf)]
FTAX	=	Federal motor vehicle fuel tax applied to CNG [Appendix E, (dollars per Mcf)]
i	=	end-use sector index (i=3 for the industrial sector)
j	=	region index.

## Noncore Distributor Tariffs

### Industrial Sector

Regional distributor tariffs for noncore industrial customers are established by applying a decline rate to the regional historical distributor tariffs that correspond to the last year historical data are available. Note that a small delta has been added to the historical tariff and then subtracted from the declined tariff in order to reverse the impact of a decline rate on the negative historical tariffs (if any). The corresponding equation is:

$$NONU\_DTAR\_I_{i=3,j} = [(1 - NONU\_DTAR\_DECL)^{YRDECL} * (HNONU\_DTAR\_I_{i=3,j,h} + CGDELTA\_N_j)] - CGDELTA\_N_j \quad (69)$$

where,

NONU_DTAR_I	=	distributor tariff for the noncore industrial sector (i=3), before adjusting for pipeline fuel use (dollars per Mcf)
HNONU_DTAR_I	=	historical distributor tariff for the noncore industrial sector, i=3 (dollars per Mcf)
NONU_DTAR_DECL	=	decline rate [Appendix E, (fraction)]
YRDECL	=	difference between the current year and the last historical year over which the decline rate is applied
CGDELTA_N	=	delta to reverse the impact of a decline rate on any negative historical tariffs [Appendix E, (dollars per Mcf)]
i	=	end-use sector index (i=3 for industrial sector)
j	=	region index
h	=	index for last year historical data are available.

### Electric Generator Sector

The methodology used to define distributor tariffs for both the competitive-with-distillate and the competitive-with-residual fuel categories of the noncore electric generator sector is similar to that used for the noncore industrial sector. A decline rate is applied to the regional historical tariffs that correspond to the last year historical data are available. Again, a small delta has been added to the historical tariff and then subtracted from the declined tariff in order to reverse the impact of a decline rate on any negative historical tariff, as follows:

### Competitive-with-residual fuel

$$UTIL\_DTAR\_IR_{j,n} = [(1 - UTILIR\_DECL)^{YRDECL} * (HUTIL\_DTAR\_IR_{j,n,h} + CGDELTA\_U_j)] - CGDELTA\_U_j \quad (70)$$

### Competitive-with-distillate

$$UTIL\_DTAR\_ID_{j,n} = [(1 - UTILID\_DECL)^{YRDECL} * (HUTIL\_DTAR\_ID_{j,n,h} + CGDELTA\_U_j)] - CGDELTA\_U_j \quad (71)$$

where,

UTIL_DTAR_IR	=	distributor tariff for the noncore competitive-with-residual fuel electric sector, before adjusting for pipeline fuel use (dollars per Mcf)
HUTIL_DTAR_IR	=	historical distributor tariff for the noncore competitive-with-residual fuel electric sector (dollars per Mcf)
UTILIR_DECL	=	decline rate for competitive-with-residual fuel distributor tariff [Appendix E, (fraction)]
UTIL_DTAR_ID	=	distributor tariff for the noncore competitive-with-distillate electric sector, before adjusting for pipeline fuel use (dollars per Mcf)
HUTIL_DTAR_ID	=	historical distributor tariff for the noncore competitive-with-distillate electric sector (dollars per Mcf)
UTILID_DECL	=	decline rate for competitive-with-distillate distributor tariff [Appendix E, (fraction)]
YRDECL	=	difference between the current year and the last historical year over which the decline rate is applied
CGDELTA_U	=	delta to reverse the impact of a decline rate on a negative historical tariff [Appendix E, (dollars per Mcf)]
j	=	region index
n	=	Electricity Market Model region index
h	=	index for last year historical data are available.

## Regional Citygate Benchmark Factors

Regional citygate benchmark factors are established for each year that historical and Short-Term Energy Outlook (STEO) data are available, and are used to calibrate the model to historical and STEO values. In historical years, citygate benchmark factors represent the differences between historical citygate prices and citygate prices derived by the NGTDM for the historical years. Given the mathematical relationships in the model, the differences between the historical and model core citygate prices are equal to the differences between the historical and model residential (defined as core) prices. Therefore, the firm citygate benchmark factors are calculated as follows:

$$CGBENCHF_{j,t} = (HPGFRSGR_{j,t} - NONU\_PR\_F_{i=1,j,t}) * NEFF\_PIPE_{i=1,j} * AEF\_PIPE_{j,j} \quad (72)$$

where,

CGBENCHF	=	citygate benchmark factor (dollars per Mcf)
HPGFRSGR	=	historical natural gas end-use price for the residential sector [Appendix E, (dollars per Mcf)]
NONU_PR_F	=	model solution for the natural gas end-use price for the residential sector, i=1 (dollars per Mcf)
NEFF_PIPE	=	efficiency factor to account for fuel used to transport natural gas from the regional hub to end-use customers [Appendix E]
AEFF_PIPE	=	efficiency factor to account for fuel used for intraregional transport of natural gas [Appendix E]
t	=	model year index
i	=	end-use sector index (i=1 for residential sector)
j	=	region index.

An equivalent method for calculating the interruptible benchmark factor was used. The differences in the historical and model noncore industrial end-use prices equal the differences in historical and model citygate prices. Therefore, the interruptible benchmark factors are calculated as follows:

$$\text{CGBENCHI}_{j,t} = (\text{HPGIINGR}_{j,t} - \text{NONU\_PR\_I}_{i=3,j,t}) * \text{NEFF\_PIPE}_{i=3,j} * \text{AEFF\_PIPE}_{j,j} \quad (73)$$

where,

- CGBENCHI = citygate benchmark factor (dollars per Mcf)
- HPGIINGR = historical natural gas end-use price for the noncore industrial sector [Appendix E, (dollars per Mcf)]
- NONU\_PR\_I = model solution for the natural gas end-use price for the noncore industrial sector, i=3 (dollars per Mcf)
- NEFF\_PIPE = efficiency factor to account for fuel use to transport natural gas from the regional hub to end-use customers [Appendix E]
- AEFF\_PIPE = efficiency factor to account for fuel use for the intraregional transport of natural gas [Appendix E]
- t = model year index
- i = end-use sector index (i=3 for industrial sector)
- j = region index.

For the first iteration of the first model forecast year (1990) of the simulation, the benchmark factors are set to zero within the DTM. For subsequent iterations and years of the historical period (1990 through 1994), the NGTDM computes benchmark factors as described above. In the STEO years (1995 and 1996) a similar process was applied. However, since the STEO only provides national level forecasts for the residential and electric generation sectors, regional STEO end-use prices were derived by scaling the regional model results accordingly. In addition, the scaled noncore electric generation end-use prices were used instead of noncore industrial prices.

When the model converges each historical and STEO year, the firm and interruptible benchmark factors from the last iteration are assigned to the arrays HCGBENCHF and HCGBENCHI, respectively. After the historical/STEO period is completed, these firm and interruptible factors are averaged over these years to generate average regional citygate benchmark factors for the respective networks. These factors are held constant for each region during the remaining forecast years.





## 7. Capacity Expansion Module Solution Methodology

The Capacity Expansion Module (CEM) is a component of the Natural Gas Transmission and Distribution Model (NGTDM). Its function is to determine future interstate pipeline and storage capacity expansion requirements, firm and total pipeline utilization estimates, and net storage withdrawal levels to meet core and noncore demand. This information is subsequently used by the Annual Flow Module and/or the Pipeline Tariff Module. A flow diagram illustrating the general structure of the CEM is provided in Figure 7-1. These results are determined based on an equilibrium between expected changes in gas consumption levels and supply availability corresponding to a CEM forecast year (represented as the Annual Flow Module model year "t", plus "n" look-ahead years).<sup>50</sup> Like the Annual Flow Module, it is structured as a transportation network servicing both core and noncore customers; however, it bases its capacity and storage utilization/expansion decisions on seasonal firm service loads, thus accounting for peak period and off-peak period consumption requirements. This two-period network structure allows for a more accurate representation of the capacity build decisions and storage requirements, as well as a mechanism for setting maximum utilization levels for the Annual Flow Module.

Formulated as a linear program, the CEM determines the capacity expansion and flow decisions which correspond to the least cost solution for achieving an equilibrium between expected supply and demand levels for natural gas. It is designed to determine pipeline and storage expansion and utilization levels that correspond to satisfying core and noncore demands represented in both the peak and off-peak periods. Price curves for storage and pipeline expansion are employed to represent the costs associated with expansion options. The decision to expand capacity in the model is based on the criterion that peak period firm service requirements for design weather conditions<sup>51</sup> must be met. Thus, when current capacity levels are fully utilized, the model simultaneously determines the relative difference in price to the consumer among the following activities: (1) adding more pipeline capacity, (2) adding more storage capacity to enable the transfer of gas to a core customer in the peak period, (3) adding no more pipeline or storage capacity but taking an alternate route, and/or (4) temporary interruptions of supplies to some noncore customers. Given that the price to the consumer is a combination of the wellhead price, the transportation charge, and the storage fee, the availability of supply and its relative regional price are included in this determination. The location and amount of pipeline and/or storage capacity expansion determined by the CEM serve to satisfy the Nation's expected firm service requirements for the lowest price to the consumer.

For this model to operate properly, a number of parameters are derived. Some are derived from data passed from other NEMS models, such as supply curve coefficients and expected core and noncore consumption levels. Others are based on the results from other NGTDM modules, such as the price (or tariff) curves for interregional pipeline and storage capacity expansion provided by the Pipeline Tariff Module. Finally, some of the parameters for the CEM are based on exogenously determined relationships and are assigned directly within the module.

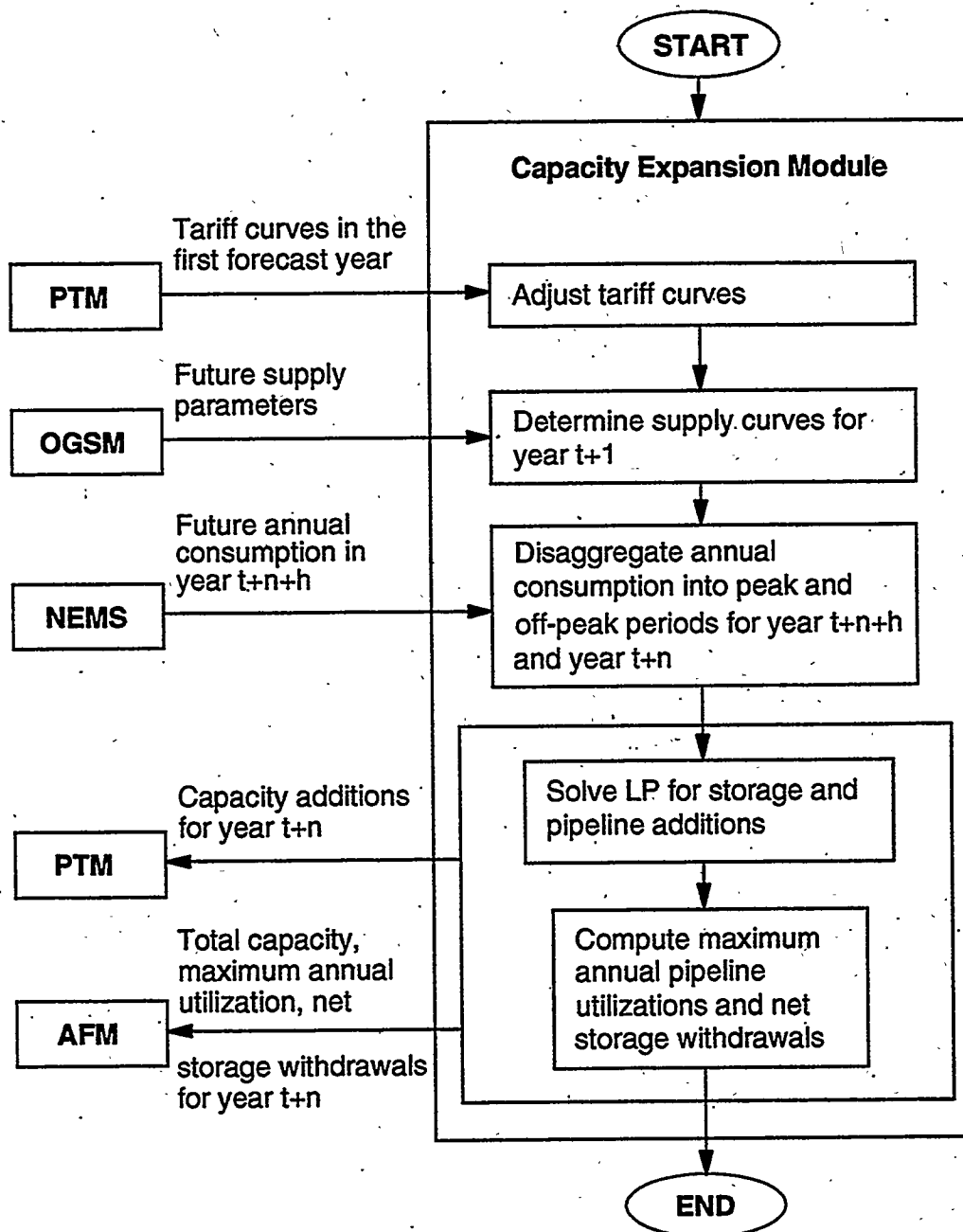
The following sections present the CEM in more detail. The methodologies used to represent supply, demand, pipeline capacity price curves, and storage capacity price curves used in the CEM are presented first. Then, a general description of the CEM linear program is presented, followed by a mathematical specification. Finally, the methodologies used to calculate the maximum pipeline utilizations and the net storage flows used by the Annual Flow Module are provided. The variables for which the CEM solves are: (1) the flows along each arc (including flows associated with storage), (2) the incremental pipeline capacity expansion required for each arc, and (3) the storage capacity expansion required for each region.

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<sup>50</sup>The look-ahead year n is an input parameter that represents the minimum planning horizon for constructing new pipeline and storage capacity in the CEM.

<sup>51</sup>Design weather is defined as the pattern of temperatures which results in degree days which are a certain percent colder than normal. Firm service customers (primarily local distribution companies) use demand estimates under design weather conditions for assessing their future need for firm pipeline transportation service.

Figure 7-1. Capacity Expansion Module System Diagram



## Supply Representation

As with the Annual Flow Module, natural gas supply sources have been classified into the following basic categories: nonassociated and associated-dissolved onshore and offshore dry gas production, Canadian and Mexican imports, liquefied natural gas imports, Alaskan gas transported via the Alaskan Natural Gas Transportation System, synthetic natural gas, and other supplemental supplies. Of these categories, all except nonassociated onshore and offshore, and synthetic natural gas production are considered to be constant (or fixed) supplies within the CEM each year. The approach used to represent variable<sup>52</sup> supply sources is similar to that used in the Annual Flow Module. When a supply source is designated as fixed, the annual production is split into peak and off-peak levels based on assumed shares (Appendix E, SUP\_PKSHR). When a supply source is designated as variable, the portion of the annual production which can be used in either period is capped at assumed percentages of the annual production (Appendix E -- SUP\_PUTILZ, SUP\_OUTILZ).

### **Dry Gas Production**

Both onshore and offshore dry gas production levels are a function of regional beginning-of-year natural gas reserve levels and expected production-to-reserves ratios, with functional forms identical to those used in the Annual Flow Module. The parameters defining these supply curves (provided by the Oil and Gas Supply Model) correspond to production levels for the year following the Annual Flow Module forecast year (current model year plus 1) and, therefore, serve as an approximation for supplies available to the CEM in the CEM forecast year (defined as current model year plus n). As in the Annual Flow Module, maximum and minimum supply levels are represented for each region. The minimum supply is defined as a specified percentage (Appendix E, PARM\_MINPR) below the product of the reserves and the production-to-reserves ratio. Likewise, the maximum supply is determined to be a specified percentage (Appendix E, PARM\_MAXPR) above the product of the reserves and the production-to-reserves ratio.

### **Natural Gas Pipeline Imports**

Imports from Mexico and Canada for each CEM forecast year are represented for each border crossing node as fixed supply sources. Mexican imports are made available to the firm network only. These imports are provided directly by the Oil and Gas Supply Model as annual supplies. The CEM then uses exogenously defined values (Appendix E, SUP\_PKSHR) to split these annual numbers into seasonal supply levels (peak and off-peak splits). Canadian peak/off-peak and firm/interruptible imports are determined from Canadian pipeline capacities and utilizations (annual and seasonal). Canadian pipeline capacities are exogenously defined by pipeline (Appendix E, CANCAP), and then aggregated to the six border crossing arcs within the NGTDM network. Seasonal utilizations (Appendix E -- CAN\_UTILZ) are exogenously defined for the NGTDM and kept constant until a user-defined year (Appendix E, CAN\_UTIL\_SYR1), after which the peak and off-peak utilizations are increased based on a growth rate (Appendix E, CAN\_UTIL\_GRW1) and their approach to an exogenously defined maximum utilization Appendix E, CAN\_UTIL\_MAX. In a subsequent year (CAN\_UTIL\_SYR2) the growth rate is changed to CAN\_UTIL\_GRW2. The peak firm utilization is set as a fraction (Appendix E, CAN\_UTIL\_PF\_P) of the peak utilization. Annual utilizations are approximated using the AFM output values from the most recent forecast year. The Canadian produced natural gas which passes through the United States on its way to Canadian markets (as described in Chapter 3) is split into peak and off-peak levels based on assumed shares (Appendix E, CANFLO\_PFSHR).

### **Liquefied Natural Gas Imports and the Alaskan Natural Gas Transportation System**

The levels of liquefied natural gas imports into the four designated entry points, and the level of gas entering the United States via the Alaskan Natural Gas Transportation System, are provided to the CEM, as well as the Annual

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<sup>52</sup>The production levels for variable supply sources are endogenously determined within the CEM as a function of the natural gas price.

Flow Module, by the Oil and Gas Supply Model. For both of these sources, the level of supply assumed in the CEM for a future forecast year, is the level of supply the Annual Flow Module will actually see in that forecast year, (i.e., the CEM operates under perfect foresight with regard to these two supply categories).

For the *Annual Energy Outlook 1996*, the liquefied natural gas imports are provided by the Oil and Gas Supply Model. To accomplish this, the solution price from the Annual Flow Module at the nearest associated market node is provided to the Oil and Gas Supply Model at the end of each forecast year. This price is used as a basis for deciding whether or not the capacity at the associated gasification plant will be expanded. The Oil and Gas Supply Model assumes that any added capacity will not be available for use until at least "n" years (as defined in the CEM) after the decision is made to expand. The decision to build is not reversed, even if the price in intervening years falls below the originally required threshold price. The utilization rates for the gasification plant capacities are set exogenously. Because of the lead time for these builds, the Oil and Gas Supply Model is able to provide the CEM with the import levels for liquefied natural gas for "n" years beyond the current forecast year.

Within the Oil and Gas Supply Model, the initial build (for those segments not already in existence) and the potential expansion decisions for the Alaskan Natural Gas Transportation System (ANGTS) is structurally identical to the method used for endogenously forecasting the expansion of liquefied natural gas gasification facilities. Therefore, the representation of the ANGTS in the CEM likewise is similar to the approach taken for representing liquefied natural gas imports in the CEM. Natural gas supplied through the ANGTS is provided by the Oil and Gas Supply Model based on the border price at the U.S./Canadian border adjoining the Pacific Census Division. The Oil and Gas Supply Model assumes that the final pipeline connection (and any subsequent expansions) of the ANGTS will be completed at least "n" years after the referenced border price is high enough to recover costs for the completion of the project.

### ***Associated-Dissolved Gas, Synthetic Natural Gas, and Other Supply Sources***

Within the CEM (as in the AFM) associated-dissolved gas, synthetic natural gas from coal, and other supplemental supplies are fixed quantities. Associated-dissolved gas production and synthetic production of natural gas from coal are provided by the Oil and Gas Supply Model and the Coal Market Model, respectively. The levels of natural gas used in the CEM for these two categories are from the most recent forecast year solved by the Annual Flow Module. Since both of these supply categories correspond to current year levels, they serve as an approximation for synthetic natural gas from coal and associated-dissolved gas available to the CEM in the CEM forecast year (defined as Annual Flow Module forecast year plus n). Synthetic natural gas produced from liquid hydrocarbons is treated as a variable supply type within the CEM and is calculated as a function of the market price for natural gas, with the same functional form and constraints used in the Annual Flow Module. Finally, since other supplemental supplies are assumed to remain constant throughout the forecast in the Annual Flow Module, they also are assumed constant in the CEM (Appendix E – OSUP\_TOT, OSUP\_RSHR).

## **Demand Representation**

Demands within the CEM include end-use consumption, export demands, and pipeline fuel consumption. As with the Annual Flow Module, end-use and export demands for forecast years beyond the current model year are defined by other models within NEMS, while pipeline fuel is accounted for through exogenously defined pipeline efficiencies (Appendix E, AEFF\_PIPE). End-use consumption levels are provided on an annual basis by region (Census or NGTDM/EMM) and type of customer (core versus noncore<sup>53</sup>), and are represented as consumption levels in the CEM, unlike the demand curves used in the AFM. Similarly, natural gas export forecasts are provided on an annual basis for each border crossing node and are defined to be fixed; however, Canadian exports are assumed to service noncore customers only while Mexican exports service only core customers.

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<sup>53</sup>For the electric generator sector, the noncore customer class is further subdivided into "competitive with distillate" and "competitive with residual fuel oil," as described in Chapter 3.

Since the CEM is a seasonal model, each of the annual levels must be separated into peak and off-peak consumption. The CEM contains exogenously specified percentages for disaggregating these annual consumption levels into peak and off-peak periods. These shares (Appendix E -- NON\_POSHR\_F, NON\_POSHR\_I, UTIL\_POSHR\_F, UTIL\_POSHR\_I, UTIL\_POSHR\_C for consumption; EXP\_PSHR for exports) have been estimated using historical monthly consumption data reported by sector and region, combined with annual estimates of demands for firm and interruptible service. Historically observed heating degree days have been included in the residential and commercial sector estimates so that the resulting shares reflect normal weather patterns (average monthly heating degree days). A future model enhancement may be to establish these peak/off-peak shares endogenously. For example, seasonal shifts in the demand for electricity (as represented within the Electricity Market Model) could be used as a basis for endogenously determining shifts in seasonal demands for natural gas by the electric generator sector. Likewise, seasonal shares for the other sectors could be specified at a more disaggregate level, such as by type of end-use (e.g., space heating).

The forecast years and regions representing end-use sector consumption in the CEM differ from one sector to another. For the industrial, transportation, and electric generators sectors, forecast consumption levels correspond to "n" years beyond the current model year, while residential and commercial consumption levels correspond to "n+h" years beyond the current model year. The "n" represents the number of years required to construct a pipeline and the "h" corresponds to the planning horizon used by a local distribution company when assessing capacity requirements.<sup>54</sup> As for regional representation, electric generators consumption forecasts are defined by NGTDM/EMM regions (Chapter 3), while consumption forecasts for the other end-use sectors are specified by Census Divisions. As in the Annual Flow Module, estimates of Alaskan natural gas consumption are generated in the CEM in order to derive separate consumption levels for the Pacific Contiguous Division. Similarly, consumption levels within three of the Census Divisions are further subdivided to form separate NGTDM regions using the same fixed historically derived shares as are used in the Annual Flow Module. These splits include: Florida split from the rest of the South Atlantic Division, California split from the rest of the Pacific Contiguous Division, and Arizona and New Mexico split from the rest of the Mountain Division.

Consumption forecasts are provided by a number of different sources. The NEMS system provides consumption forecasts for the core industrial sector and all the noncore end-use sectors with the exception of the electricity generating sector. Consumption forecasts for the core and noncore electricity generating sector are a function of the estimates provided by the Electricity Market Model. The consumption forecasts for the core residential, commercial, and transportation customer classes, however, are estimated within the NGTDM and are based on a maximum growth rate applied to the current year consumption levels (up to a maximum level). More specifically, the forecasted consumption level equals the current year consumption level times a growth rate. If this value exceeds a maximum level defined by the NEMS system, then the forecast level is set equal to the maximum level. If, however, the current year level exceeds the maximum level, then zero growth<sup>55</sup> is assumed and the forecast level is set equal to the current year level.

## Pipeline Capacity Price Curve

Initial pipeline capacity price curves are developed by the Pipeline Tariff Module at the beginning of the forecast. These curves are based on estimates of capital costs of expansion and parameters (such as interest rates) from the NEMS macroeconomic model. (See Chapter 8 for a complete description of how these tariffs are calculated.) Each cost curve represents the per unit reservation charge on a particular interregional arc based on the annual physical capacity (design day capacity<sup>56</sup> times 365). The base quantity (initial step) represents the existing pipeline capacity for the base year (Appendix E, PCAP\_MAX). The corresponding price is the base year reservation charge (i.e., the demand charge) expressed on a per unit basis. Subsequent steps represent incremental expansion and the corresponding incremental tariff. It is assumed that the price curve is nondecreasing to prevent the model from deciding to build just to lower costs. To keep the curve increasing when additional capacity is expected to result

<sup>54</sup>These variables were defined as follows in the *Annual Energy Outlook 1996*:  $n=2$ ,  $h=0$ .

<sup>55</sup>It is assumed that consumption levels will not decline.

<sup>56</sup>A pipeline's design day capacity (or certificated capacity) represents a level of service that can be maintained over an extended period of time and may not represent the maximum throughput capability of the system on any given day.

in declining prices (such as when incremental capacity expansion is the result of added compression), the step on the curve associated with this additional capacity is held at the price associated with the previous step, i.e., the step representing the level of capacity without the addition. A generic pipeline capacity price curve is presented in Figure 7-2. The QCAP represents the capacity along an arc, and the PCAP represents the corresponding unit cost. The UCAP is the maximum capacity that can be used on each step (the length of the step), and the ycap represents how much capacity was needed for a given solution.

In forecast year  $t$ , the CEM determines the capacity expansion for year  $t+n$  (the CEM forecast year). Therefore, each year the CEM must adjust the price curves based on capacity expansion which was determined in the previous CEM forecast year, and set to come on-line in year  $t+n-1$ . Specifically, the quantity associated with the base step on the curve will be adjusted to equal the capacity which will exist on the arc at the end of year  $t+n-1$ . Note that adjustments to the curve have already been made in previous CEM forecasts to reflect expansion in any of the intervening years to year  $t+n-1$ . The associated base level tariff is determined as a quantity weighted average of the tariffs corresponding to the current year ( $t$ ) capacity and the capacity additions made during years  $t+1, t+2, \dots, t+n-1$ . The original tariff levels defined for the remaining steps (i.e., the capacity addition steps) are then adjusted upward by a specific price delta (Appendix E, DELPR\_CAP) to ensure that existing pipeline capacity is sufficiently utilized (on a national level) before a decision to add new capacity is made.

## Storage Capacity Price Curve

Initial working gas storage capacity price curves are determined by the Pipeline Tariff Module at the beginning of the forecast. These curves are based on estimates of capital costs of expansion, costs of holding base gas in storage, and parameters (such as interest rates) from the NEMS macroeconomic model. (See Chapter 8 for a complete description of how these tariffs are calculated.) Each cost curve represents the storage charge per unit (PSTR) as a function of the annual working gas capacity for a particular region. This storage charge is exclusive of any transportation costs to move gas to or from storage areas. The base quantity (initial step) represents the existing working gas storage capacity (Appendix E, WORKT). The corresponding price is the initial storage charge per unit. Subsequent steps represent incremental expansion and the corresponding incremental charge. The final step on the curve represents an upper limit on working gas storage capacity expansion due to known physical limits in a region (Appendix E, NODFAC) or other nonprice dependent factors. A generic working gas storage capacity price curve is presented in Figure 7-3. The QSTR represents the storage capacity at a node, and the PSTR represents the corresponding unit storage cost. The USTR is the maximum storage capacity that can be used on each step (the length of the step), and the ystr represents how much storage was needed for a given solution.

Each year the CEM must adjust these working gas storage price curves based on the current capacity levels, similar to the adjustment made to the pipeline capacity price curves. Specifically, the quantity associated with the base step on the curve is adjusted to equal the working gas storage capacity which exists in the region at the end of year  $t+n-1$ , where  $t$  is the current model year and  $n$  is the number of years beyond the current model year for which the CEM is determining expansion. Since in model year  $t$  the capacity expansion for year  $t+n$  is being determined, the base step includes working gas capacity for current year  $t$  as well as the capacity expansions defined in years  $t+1, t+2, \dots, t+n-1$ . The associated base level tariff is determined as a quantity-weighted average of the tariff associated with the existing capacity and the tariffs for each of the previously determined expansions for years  $t+1, t+2, \dots, t+n-1$ , as well as the original base storage capacity in model year  $t$ . As with the pipeline capacity price curves, the original tariff levels defined for the remaining steps are then adjusted upward by a specific price delta (Appendix E, DELPR\_STR). This measure ensures that existing storage capacity is sufficiently utilized (on a national level) before new storage capacity gets added.

## Linear Program Formulation

A linear programming (LP) framework is used in the CEM as the basis for determining expansion requirements for pipeline and storage facilities. As described in Chapter 4, the CEM structure is based on a natural gas transmission and distribution system composed of four parallel networks interconnected at the supply points and the storage points. These networks serve to represent the seasonal nature (peak and off-peak) and types of service (firm and

Figure 7-2. Pipeline Capacity Price Curve

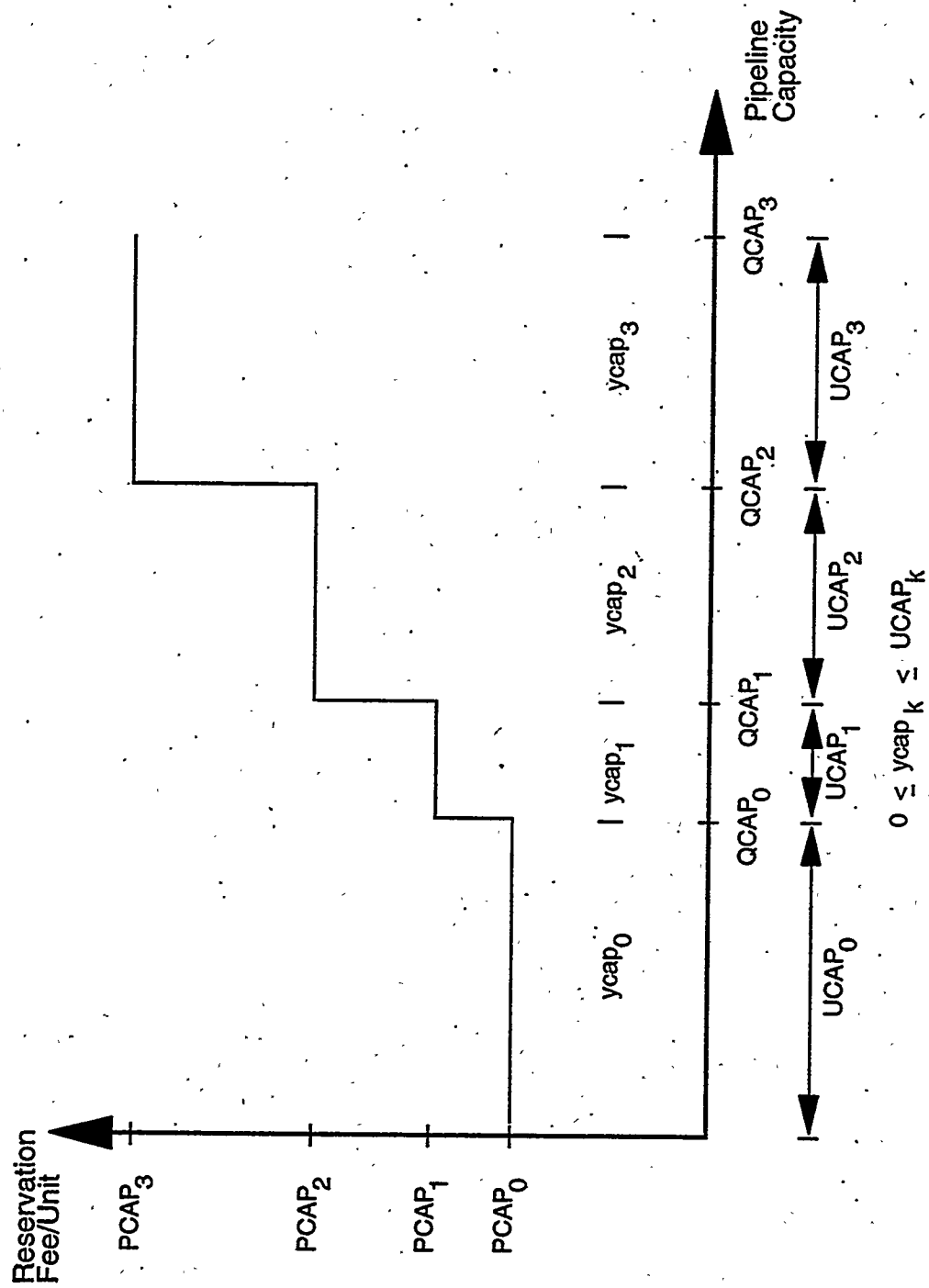
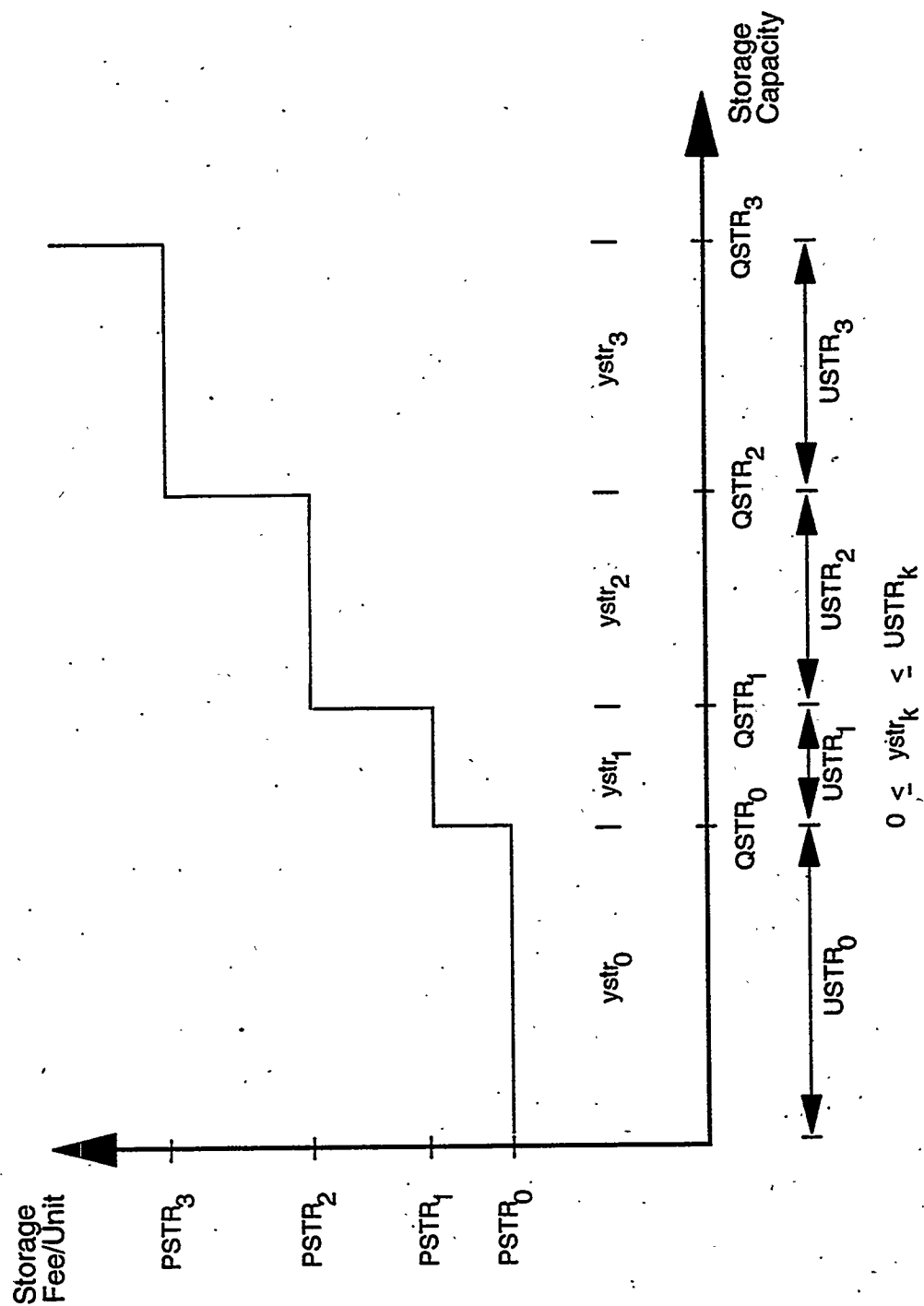


Figure 7-3. Storage Capacity Price Curve





interruptible) associated with the natural gas market. Thus, peak firm, peak interruptible, off-peak firm, and off-peak interruptible service are modeled by the four networks. The CEM LP is solved in two phases: The first phase establishes pipeline and storage capacity expansion requirements, and the second establishes final firm, interruptible, peak and off-peak flows. This section describes the CEM LP formulation, the process used to determine the pipeline and storage capacity expansion requirements, and the methodology used to define annual pipeline utilizations and net storage results.

## ***General Description of the Linear Program Formulation***

The objective of the linear program designed for the CEM is to minimize the cost of supplying and transporting natural gas to the end-user, subject to operational and supply constraints, with the requirement to satisfy all demand for firm service under design weather conditions. This section gives a general description and justification of the linear programming formulation (objective function and constraints), and a subsequent section includes the explicit mathematical equations representing the formulation.

The objective function has been formulated to minimize costs. These costs include the costs of supplies, transportation along the established network, and costs of additional pipeline and storage capacity. The objective function can be represented as follows:

$$\begin{array}{l} \text{minimize} \quad \{ \text{transportation costs} + \text{supply costs} + \text{pipeline expansion costs} + \text{storage expansion costs} \\ \quad + \text{backstop supply costs} \} \end{array}$$

A mass balance constraint is included for each transshipment node. This constraint ensures that the total input to the node equals the total output from the node. In general, gas flowing into a transshipment node comes from other transshipment nodes, supply points, and (in some cases) storage, while gas flowing from a transshipment node goes to demand points, other transshipment nodes, and (in some cases) storage. Flows into and out of storage have been defined to be network dependent because gas generally is injected into storage in the off-peak period and used to satisfy core customer demand during the peak period. (Peak noncore customers also may draw from storage if it is not needed for core customers.) Therefore, in the linear program formulation, gas flows into a regional storage point from transshipment nodes (in the same region) on the off-peak firm and/or interruptible service networks, and flows out of the same storage point to transshipment nodes (again in the same region) on the peak firm and/or interruptible service networks. As in the AFM, the mass balance equations in the CEM include discrepancies or balancing items that are historically seen between production and consumption data collection efforts. The national level exogenous forecast for discrepancy, as used in the AFM, is split between the four networks and 12 regions based on the CEM consumption splits. A general transshipment node mass balance constraint is listed below for each of the four parallel networks.

For each peak period firm service network transshipment node:

$$\begin{aligned} & (\text{flow into the transshipment node from other peak period firm service network transshipment nodes}) + (\text{flow} \\ & \text{into the transshipment node from supply points in the region}) + (\text{flow into the transshipment node from} \\ & \text{storage in the region}) + (\text{peak firm discrepancies}) - (\text{losses}) = (\text{flow out of the transshipment node to peak} \\ & \text{period core demand points in the region}) + (\text{flow out of the transshipment node to other peak period firm} \\ & \text{service network transshipment nodes}) \end{aligned}$$

For each peak period interruptible service network transshipment node:

$$\begin{aligned} & (\text{flow into the transshipment node from other peak period interruptible service network transshipment nodes}) \\ & + (\text{flow into the transshipment node from supply points in the region}) + (\text{flow into the transshipment node} \\ & \text{from storage in the region}) + (\text{peak interruptible discrepancies}) - (\text{losses}) = (\text{flow out of the transshipment} \\ & \text{node to peak period noncore demand points in the region}) + (\text{flow out of the transshipment node to other} \\ & \text{peak period interruptible service network transshipment nodes}) \end{aligned}$$

For each off-peak period firm service network transshipment node:

$$(\text{flow into the transshipment node from other off-peak period firm service network transshipment nodes}) + (\text{flow into the transshipment node from supply points in the region}) + (\text{off-peak firm discrepancies}) - (\text{losses}) = (\text{flow out of the transshipment node to storage in the region}) + (\text{flow out of the transshipment node to off-peak period core demand points in the region}) + (\text{flow out of the transshipment node to other off-peak period firm service network transshipment nodes})$$

For each off-peak period interruptible service network transshipment node:

$$(\text{flow into the transshipment node from other off-peak period interruptible service network transshipment nodes}) + (\text{flow into the transshipment node from supply points in the region}) + (\text{off-peak interruptible discrepancies}) - (\text{losses}) = (\text{flow out of the transshipment node to storage in the region}) + (\text{flow out of the transshipment node to off-peak period noncore demand points in the region}) + (\text{flow out of the transshipment node to other off-peak period interruptible service network transshipment nodes})$$

A mass balance constraint also is included for each storage point. This constraint ensures that in a forecast year the total gas input into storage equals the total gas output from storage, net of losses (Appendix E, EFF\_STR). As mentioned above, gas flows to storage from the off-peak period firm and/or interruptible service networks, and gas flows out of storage to the peak period firm and/or interruptible service networks. The flow comes from and goes to the transshipment node corresponding to the same region as the storage point. Unlike forecast years, in historical years total net storage withdrawals are not zero. Therefore actual net storage withdrawal levels are accounted for in these mass balance equations when historical years are being represented. A mass balance constraint for storage in a forecast year is presented below.

For each storage point:

$$(\text{flow of gas into a storage point from the off-peak period firm service network transshipment node}) + (\text{flow of gas into a storage point from the off-peak period interruptible service network transshipment node}) - (\text{losses}) = (\text{flow of gas out of the storage point to the peak period firm service network transshipment node}) + (\text{flow of gas out of the storage point to the peak period interruptible service network transshipment node})$$

Each demand point also has a mass balance constraint represented. This constraint ensures that the quantity allocated to the end-use point equals the expected consumption level associated with that point. All expected core market consumption (peak and off-peak) must be satisfied; however, pipeline and storage facilities can only be built to meet peak core demands. It is assumed that the resulting capacity levels will be sufficient to accommodate flows to satisfy core off-peak period requirements. Since new facilities are not built for the satisfaction of noncore demand, a backstop supply is a modeling structure introduced to represent the portion of the noncore demand for natural gas which cannot be satisfied by conventional supply sources and must be interrupted. A general demand node mass balance constraint is listed below for each of the four parallel networks.

For each peak period core demand point:

$$(\text{flow from a peak period firm service network transshipment node in a region to a peak period core demand point in the region}) - (\text{losses}) = (\text{quantity consumed at that peak period core demand point})$$

For each peak period noncore demand point:

$$(\text{flow from a peak period interruptible service network transshipment node in a region to a peak period noncore demand point in the region}) + (\text{backstop supply}) - (\text{losses}) = (\text{quantity consumed at that peak period noncore demand point})$$

For each off-peak period core demand point:

(flow from an off-peak period firm service network transshipment node in a region to an off-peak period core demand point in the region) - (losses) = (quantity consumed at that off-peak period core demand point)

For each off-peak period noncore demand point:

(flow from an off-peak period interruptible service network transshipment node in a region to an off-peak period noncore demand point in the region) + (backstop supply) - (losses) = (quantity consumed at that off-peak period noncore demand point)

Supply utilization constraints are included for each supply point, and are represented as peak supply constraints and off-peak supply constraints. Since gas may flow from a supply point to a transshipment node (in the same region) in any of the four parallel networks, these supply constraints ensure that the flows (including losses) do not exceed the total amount supplied at that point. The constraints also ensure that the quantity flowing from the supply point has been properly split between the peak and off-peak period during any one year. The peak supply constraint states that, for any supply type and any supply level, a specified portion (Appendix E, SUP\_PUTILZ) of the annual supply flow must be used to supply peak demands. Similarly, the off-peak supply constraint states that a specified portion of the annual supply flow must be used to supply off-peak demands (Appendix E, SUP\_OUTILZ). The latter constraint is defined slightly differently for onshore and offshore dry gas production: the supply quantity supplied to the off-peak networks must be less than or equal to a specified portion of the total annual dry gas production level. The constraints are as follows.

For each supply point:

(flow from the supply point to a peak period firm service network transshipment node) + (flow from the supply point to a peak period interruptible service network transshipment node) = (peak share of total supply) \* (total annual quantity supplied from the supply curve)

For each onshore and offshore supply point:

(flow from the supply point to an off-peak period firm service network transshipment node) + (flow from the supply point to an off-peak period interruptible service network transshipment node) ≤ (off-peak share of total supply) \* (total annual quantity supplied from the supply curve)

For each supply point excluding onshore and offshore supplies:

(flow from the supply point to an off-peak period firm service network transshipment node) + (flow from the supply point to an off-peak period interruptible service network transshipment node) = (off-peak share of total supply) \* (total annual quantity supplied from the supply curve)

Capacity expansion and flow constraints are defined for each interregional arc in the overall network. These constraints ensure that pipeline capacity is built, as necessary, to satisfy only core peak period demand, and that the total flows along the interregional arcs are less than or equal to the available capacities (base<sup>57</sup> plus added capacity). Within these constraints, seasonal maximum arc utilization rates are used to capture the variation in load patterns and operational limitations throughout the season. Constraints have been established for firm service peak period flows, total peak period flows, and total off-peak period flows for each interregional arc in the network. In general, maximum seasonal pipeline utilizations are set equal to the fraction of the year represented by the season times an assumed maximum utilization rate for the type of service represented (Appendix E - ARC\_PUTILZ, ARC\_PFUTILZ, ARC\_OUTILZ) times a factor representing the percentage of the pipe reserved to account for the potential of abnormal weather (Appendix E, WTHRFAC).

It is the firm service peak period capacity constraint that ensures that no pipeline capacity is built beyond what is needed to satisfy peak period core market requirements. It states that total peak firm flow along an arc must equal

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<sup>57</sup>Recall from previous sections that capacity expansion levels are being determined for year t+n; therefore, the base capacity refers to the capacity existing at the end of the year t+n-1.

total capacity (base plus added capacity) times a maximum peak firm arc utilization rate. It is the equality requirement that does not allow new capacity to be built unless peak core demands require additional quantities to flow along the specific arc(s). The peak total (firm and interruptible) period capacity constraint has been established as an inequality constraint to ensure that the flows to satisfy noncore peak period requirements are less than or equal to the remaining peak season effective capacity (i.e., total capacity times the maximum peak season utilization rate) once the core market requirements have been met. In addition, an off-peak period capacity constraint (also as an inequality constraint) has been developed to ensure that the total off-peak season flows on the arc are less than or equal to the off-peak season effective capacity (i.e., total capacity times the maximum off-peak season utilization rate). The resulting constraints are given below for each interregional arc.

For each peak firm service interregional arc:

$$(\text{flow along the arc to satisfy core market peak period requirements}) = (\text{level of base capacity used} + \text{level of pipeline capacity expansion}) * (\text{peak period interregional arc maximum utilization rate for firm service})$$

For each peak firm and interruptible service interregional arc:

$$(\text{flow along the arc to satisfy noncore peak period requirements}) + (\text{flow along the arc to satisfy core market peak period requirements}) \leq (\text{base capacity} + \text{level of pipeline capacity expansion}) * (\text{peak period interregional arc maximum utilization rate})$$

For each off-peak firm and interruptible service interregional arc:

$$(\text{flow along the arc to satisfy noncore off-peak period requirements}) + (\text{flow along the arc to satisfy core market off-peak period requirements}) \leq (\text{base capacity} + \text{level of pipeline capacity expansion}) * (\text{off-peak period interregional arc maximum utilization rate})$$

Storage expansion and flow constraints are defined for each node in the lower 48-State portion of the network. These constraints ensure that storage capacity is built, as necessary, to satisfy peak period core market requirements and that the flows from storage are less than or equal to the total available storage capacity (base<sup>58</sup> plus added capacity). Constraints have been established for firm service peak period flows and total peak period flows from storage locations at each node. Storage utilization rates (Appendix E -- STR\_UTILZ, STR\_FUTILZ) have been used to define the maximum storage levels used for peak firm service and total peak storage. The peak firm service constraint has been established as an equality constraint to ensure that no storage capacity is built beyond what is needed to satisfy peak period core market requirements. The total peak constraint has been established as an inequality constraint to ensure that the flows to satisfy noncore requirements are less than or equal to the effective storage capacity remaining after the core market requirements have been met. The resulting constraints are given below.

For each storage point:

$$(\text{flow from the storage point to the peak period firm service network transshipment node}) = ((\text{level of base storage capacity used}) + (\text{storage capacity expansion})) * (\text{peak period maximum storage utilization rate for firm service})$$

For each storage point:

$$(\text{flow from the storage point to the peak period interruptible service network transshipment node}) + (\text{flow from the storage point to satisfy core market requirements}) \leq ((\text{base storage capacity}) + (\text{storage capacity expansion})) * (\text{peak period maximum storage utilization rate for total peak service})$$

<sup>58</sup>Recall from previous sections that storage capacity expansion levels represent working gas capacities and are being determined for year t+n; therefore, the base storage refers to the working gas storage capacity existing at the end of the year t+n-1.

Similar to the AFM, minimum interstate pipeline flows have been defined for the CEM firm service networks (in the form of lower bounds on the flow variables). These minimum flows are defined to be a fraction of the resulting firm flows in the Annual Flow Module in the current model year plus an estimated utilization of the new capacity added between the current model year (t) and the beginning of the CEM forecast year (t+n). As in the Annual Flow Module, this fraction is exogenously specified (Appendix E -- APCT\_MINF, APCTMINI) and is intended to represent the level of flexibility core customers exhibit in changing their selected routes for transporting natural gas from year-to-year, even if relative costs would indicate a change would be prudent (e.g., flexibility would be lessened due to the existence of long-term contracts). Finally, maximum utilization rates are used in estimating firm flows from the last AFM solution for the peak and off-peak periods while accounting for the potential impact of new capacity builds over the next "n" years. The resulting constraints are described below.

For each interregional arc on the peak firm service network:

$$\text{peak firm flow} \geq (\text{minimum flow fraction}) * (\text{estimated firm flow}) * (\text{peak period share of firm flow})$$

For each interregional arc on the off-peak firm service network:

$$\text{off-peak firm flow} \geq (\text{minimum flow fraction}) * (\text{estimated firm flow}) * (\text{off-peak period share of firm flow})$$

Additional constraints are represented as lower and/or upper bounds on the flow variables. These include lower bounds set for flows along all arcs (and networks) with bidirectional flows,<sup>59</sup> as well as upper and lower bounds set on all flows into (off-peak firm and interruptible) and out of (peak firm and interruptible) storage. The upper and lower bounds on storage flows are set to a fraction<sup>60</sup> of approximated firm and interruptible net flows into and out of storage in a period. These approximations are based on the last historical year's peak/off-peak values (Appendix E, PKNETSTR), adjusted for changes in the physical storage additions over the forecast period, and split into firm and interruptible categories using exogenous shares (Appendix E -- PKSTFR\_F, OPPSTFR\_F). Finally, a number of bound constraints are needed to completely describe the step functions for the supply, capacity expansion, and storage expansion curves. These bounds serve to define the lengths of each of the steps on the curves.

Thus, the linear program solves for the level and location of storage and pipeline capacity expansion, as well as the associated peak and off-peak flows. Note that the amount of capacity expansion is a continuous function. Although, for a given pipeline company, capacity may be added only through discrete projects, the arcs in the CEM represent aggregates of pipeline companies. Taken together these companies can add capacity in virtually any desired quantity through combinations of additional compressor capacity, looping, or other means.

## ***Mathematical Specification of the Linear Programming Formulation***

This section presents the set of equations which establishes the linear programming formulation for the CEM. This set is comprised of an objective function, flow constraints, and bounds on model variables.

<sup>59</sup>Minimum flows for bidirectional arcs in the CEM are set by multiplying the corresponding minimum flows established in the Annual Flow Module by assumed peak shares (Appendix E -- BIARC\_PFSHR, BIARC\_PISHR).

<sup>60</sup>The fractions used to set the minimum storage flow constraints for the peak firm, peak interruptible, off-peak firm, and off-peak interruptible arcs are 0.80, 0.70, 0.80, 0.75, respectively. The fractions used to set the maximum storage flow constraints are 1.2, 1.25, 1.9, and 1.9 for the same arcs.

$$\begin{aligned}
& \text{minimize} \\
& x, y_{\text{sup}}, y_{\text{cap}}, y_{\text{str}}, q_{\text{zz}} \quad \sum_{ij} \text{TAR}_{ij}^F (x_{ij}^{PF} + x_{ij}^{OF}) + \sum_{ij} \text{TAR}_{ij}^I (x_{ij}^{PI} + x_{ij}^{OI}) + \sum_{si} \text{TAR}_{si}^P (x_{si}^{PF} + x_{si}^{PI}) \\
& + \sum_{si} \text{TAR}_{si}^O (x_{si}^{OF} + x_{si}^{OI}) + \sum_{id} \text{TAR}_{id}^{PF} x_{id}^{PF} + \sum_{id} \text{TAR}_{id}^{PI} x_{id}^{PI} + \sum_{id} \text{TAR}_{id}^{OF} x_{id}^{OF} \\
& + \sum_{id} \text{TAR}_{id}^{OI} x_{id}^{OI} + \sum_{si} \sum_{k=1}^c \text{PSUP}_{s,i,k} y_{\text{sup},s,i,k} + \sum_{ij} \sum_{k=0}^c \text{PCAP}_{i,j,k} y_{\text{cap},i,j,k} \\
& + \sum_{st,i} \sum_{k=0}^c \text{PSTR}_{st,i,k} y_{\text{str},st,i,k} + \sum_{id} \text{PZZ}_{id}^{PI} q_{\text{zz},id}^{PI} + \sum_{id} \text{PZZ}_{id}^{OI} q_{\text{zz},id}^{OI}
\end{aligned} \tag{74}$$

where,

the subscripted indices are:

$ij$ , and $m$	=	transshipment node
$d$	=	demand type
$s$	=	supply type
$st$	=	storage
$k$	=	step on the curve
$c$	=	number of steps on the curve
$ij$	=	arc connecting transshipment nodes $i$ and $j$
$id$	=	arc from transshipment node $i$ to demand point $d$
$si$	=	arc from supply point $s$ to transshipment node $i$
$st,i$	=	arc from transshipment node $i$ to storage point $st$
$i,st$	=	arc from transshipment node $i$ to storage point $st$

the superscripted indices are:

$P$	=	peak period
$O$	=	off-peak period
$F$	=	firm
$I$	=	interruptible

the parameters are:

$\text{TAR}$	=	tariff (pipeline usage from node to node, gathering charge from supply point to node, or distributor charge from node to end-use point), (dollars per Mcf)
$\text{EFF}$	=	efficiencies (fraction)
$U$	=	maximum allowable utilization of an arc in the season (fraction)
$UP$	=	maximum percentage of supply available for demand type (fraction)
$UST$	=	maximum percentage of storage available to demand type (fraction)
$Q\text{DEMO}$	=	quantity demanded (Bcf)
$\text{ESTFLOW}$	=	flow from Annual Flow Module in year $t$ , plus estimated utilization of capacity added after year $t$ through year $t+n$ (Bcf)
$\text{SHR}$	=	period share of total flow (fraction)
$\text{MINBIFLO}$	=	minimum flow for bidirectional arcs (Bcf)
$\text{MNSTR}$	=	minimum flow allowed into or out of storage for specified network (Bcf)
$\text{MXSTR}$	=	maximum flow allowed into or out of storage for specified network (Bcf)
$\text{DMD}$	=	total demand for a demand type (Bcf)
$\text{PCTMFLO}$	=	percent minimum flow requirement (fraction)
$\text{PSUP}$	=	prices on the supply steps (dollars per Mcf)
$\text{PCAP}$	=	prices on the pipeline capacity steps (dollars per Mcf)
$\text{PSTR}$	=	prices on the storage capacity steps (dollars per Mcf)

PZZ	=	price of backstop supply (dollars per Mcf)
LSUP	=	lower bound on supply step (Bcf)
USUP	=	size of supply step (Bcf)
UCAP	=	size of pipeline capacity step (Bcf)
USTR	=	size of storage capacity step (Bcf)
DISCR	=	discrepancy between supply and demand (Bcf)

the variables are:

$x_{i,j}$	=	flow from i to j (Bcf)
$ysup_{s,i,k}$	=	for supply point (s,i), the amount of supply step k taken (Bcf)
$ycap_{i,j,k}$	=	for arc i,j, the amount of pipeline capacity step k built (Bcf)
$ycap_{i,j,0}$	=	for arc i,j, the amount of base pipeline capacity taken (Bcf)
$ystr_{st,i,k}$	=	for storage point (st,i), the amount of storage capacity step k built (Bcf)
$ystr_{st,i,0}$	=	for storage point (st,i), the amount of base capacity taken (Bcf)
$qzz_{i,d}$	=	amount of backstop supply used for demand point (i,d), (Bcf)

Mass Balance Constraints at Each Transshipment Node (m):

$$\sum_{i \in m} x_{i,m}^{PF} * EFF_{i,m}^P + \sum_s x_{s,m}^{PF} * EFF_{s,m}^P + \sum_{st} x_{st,m}^{PF} + DISCR_m^{PF} = \sum_d x_{m,d}^{PF} + \sum_{i \in m} x_{m,i}^{PF} \quad (75)$$

$$\sum_{i \in m} x_{i,m}^{PI} * EFF_{i,m}^P + \sum_s x_{s,m}^{PI} * EFF_{s,m}^P + \sum_{st} x_{st,m}^{PI} + DISCR_m^{PI} = \sum_d x_{m,d}^{PI} + \sum_{i \in m} x_{m,i}^{PI} \quad (76)$$

$$\sum_{i \in m} x_{i,m}^{OF} * EFF_{i,m}^O + \sum_s x_{s,m}^{OF} * EFF_{s,m}^O + DISCR_m^{OF} = \sum_{st} x_{m,st}^{OF} + \sum_d x_{m,d}^{OF} + \sum_{i \in m} x_{m,i}^{OF} \quad (77)$$

$$\sum_{i \in m} x_{i,m}^{OI} * EFF_{i,m}^O + \sum_s x_{s,m}^{OI} * EFF_{s,m}^O + DISCR_m^{OI} = \sum_{st} x_{m,st}^{OI} + \sum_d x_{m,d}^{OI} + \sum_{i \in m} x_{m,i}^{OI} \quad (78)$$

Mass Balance Constraints at Each Storage Point (st,i):

$$(x_{i,st}^{OF} + x_{i,st}^{OI}) * EFF_{i,st}^O = x_{st,i}^{PF} + x_{st,i}^{PI} \quad (79)$$

Mass Balance Constraints for Demand Points (i,d):

$$x_{i,d}^{PF} * EFF_{i,d}^P = QDEM0_{i,d}^{PF} \quad (80)$$

$$x_{i,d}^{PI} * EFF_{i,d}^P + qzz_{i,d}^{PI} = QDEM0_{i,d}^{PI} \quad (81)$$

$$x_{i,d}^{OF} * EFF_{i,d}^O = QDEM0_{i,d}^{OF} \quad (82)$$

$$x_{i,d}^{OI} * EFF_{i,d}^O + qzz_{i,d}^{OI} = QDEM0_{i,d}^{OI} \quad (83)$$

Supply Utilization Constraints at Each Supply Point (s,i):

$$x_{s,i}^{PF} + x_{s,i}^{PI} = \sum_{k=1}^c ysup_{s,i,k} * UP_{s,i}^P \quad (84)$$

For onshore and offshore supply types only,

$$x_{s,i}^{OF} + x_{s,i}^{OI} \leq \sum_{k=1}^c ysup_{s,i,k} * UP_{s,i}^O \quad (85)$$

For all supply types other than onshore and offshore,

$$x_{s,i}^{OF} + x_{s,i}^{OI} = \sum_{k=1}^c ysup_{s,i,k} * UP_{s,i}^O \quad (86)$$

Pipeline Capacity Constraints for Each Arc (i,j):

$$x_{i,j}^{PF} = U_{i,j}^{PF} * (ycap_{i,j,0} + \sum_{k=1}^c ycap_{i,j,k}) \quad (87)$$

$$x_{i,j}^{PI} + x_{i,j}^{PF} \leq U_{i,j}^P * (ycap_{i,j,0} + \sum_{k=1}^c ycap_{i,j,k}) \quad (88)$$

$$x_{i,j}^{OF} + x_{i,j}^{OI} \leq U_{i,j}^O * (ycap_{i,j,0} + \sum_{k=1}^c ycap_{i,j,k}) \quad (89)$$

Storage Capacity Constraint for Each Region (st,i):

$$x_{st,i}^{PF} = UST_{st,i}^{PF} * (ystr_{st,i,0} + \sum_{k=1}^c ystr_{st,i,k}) \quad (90)$$

$$x_{st,i}^{PI} + x_{st,i}^{PF} \leq UST_{st,i}^P * (ystr_{st,i,0} + \sum_{k=1}^c ystr_{st,i,k}) \quad (91)$$

Minimum Bounds on Peak and Off-peak Firm Flows for each Arc (i,j):

$$x_{i,j}^{PF} \geq PCTMFLO_{i,j}^F * ESTFLOW_{i,j}^F * SHR_{i,j}^{PF} \quad (92)$$

$$x_{i,j}^{OF} \geq PCTMFLO_{i,j}^F * ESTFLOW_{i,j}^F * SHR_{i,j}^{OF} \quad (93)$$

Other bound constraints set minimum flows along bidirectional arcs, as well as minimum and maximum flows into and out of storage:

$$x_{i,j}^{xx} \geq MINBI_{xx} \quad \text{for each bidirectional flow arc (i,j), and each network (xx = PF, PI, OF, OI)}$$

$$MNSTR_{st,i}^{xx} \leq x_{st,i}^{xx} \leq MXSTR_{st,i}^{xx} \quad \text{for each flow (xx = PF, PI, OF, OI) into and out of storage (st,i)}^{61}$$

The following bound constraints also are defined for the steps on the supply, capacity expansion, and storage expansion curves:

$$\begin{aligned} LSUP_{s,i,k} &\leq ysup_{s,i,k} && \leq USUP_{s,i,k} && \text{for each supply point (s,i), and } k=1,2,\dots,n. \\ 0 &\leq ycap_{i,j,k} && \leq UCAP_{i,j,k} && \text{for each arc i,j, and } k=0,1,2,\dots,n. \\ 0 &\leq ystr_{st,i,k} && \leq USTR_{st,i,k} && \text{for each storage point (st,i), and } k=0,1,2,\dots,n. \end{aligned}$$

<sup>61</sup>The variables MNSTR and MXSTR are not used in the source code directly, but represent the result of a set of equations.



For the most part LSUP is zero, except on the first step of the supply curve where a minimum supply level may be defined.

Thus, the above equations and bounds mathematically specify the linear program objective function and the key model constraints. A commercial software package<sup>62</sup> designed to solve linear programming problems is utilized to modify and solve the linear program matrix, and to access the resulting solution.

## Implementation of the Linear Program Within the CEM

The CEM linear program solves for the level and location of pipeline and storage capacity expansion, as well as the corresponding peak and off-peak flows associated with firm and interruptible service. To provide this information, the linear program matrix is solved in two phases—the first establishes the pipeline and storage expansion levels, and the second establishes the final flows.

In the first phase of the CEM, the linear program is defined according to the equations above, and solved. From this solution, pipeline and storage capacity expansions and peak firm flows are established. However, base capacity on some pipeline arcs and in some regional storage locations may not be fully utilized because of insufficient peak core demand requirements. Given how the model is formulated, this under utilization, in turn, restricts the amount of off-peak and interruptible flows that can occur along the under utilized arcs, and into/out of under utilized storage facilities. This occurrence is dictated by the pipeline and storage capacity constraints. The second phase serves to remove this connection between peak firm flows and other flows, while still maintaining the peak firm flow levels resulting in the first phase.

In the second phase, the peak period capacity constraints (equations 88 and 91) must be represented such that interruptible volumes can flow along the unused capacity. To accomplish this, pipeline and storage capacities ( $ycap_{ij}$  and  $ystr_{st,i}$ ) are held constant and set equal to the solution levels (YCAP and YSTR) from the first CEM phase (base utilization plus added capacity). This is represented with the changes in the equation from 'ycap' to 'YCAP' and from 'ystr' to 'YSTR.' Also, a constant term is added to the constraint that identifies the unused base capacity which may be used for interruptible flows only. The corresponding equations are presented below.

Pipeline Capacity Constraint for Peak Period Flows on Arc (i,j):

$$x_{ij}^{PI} + x_{ij}^{PF} \leq U_{ij}^P(YCAP0_{ij} + \sum_{k=1}^C YCAP_{ij,k}) + U_{ij}^P(QCAP0_{ij} - YCAP0_{ij}) \quad (94)$$

Storage Capacity Constraint for Peak Period Flows in Each Region (st,i):

$$x_{st,i}^{PI} + x_{st,i}^{PF} \leq U_{st,i}^P(YSTR0_{st,i} + \sum_{k=1}^C YSTR_{st,i,k}) + U_{st,i}^P(QSTR0_{st,i} - YSTR0_{st,i}) \quad (95)$$

<sup>62</sup>All of the linear programming problems within the NEMS will be solved using the Optimization and Modeling Library (OML), a product of Ketron Management Science, a Division of Bionetics Corporation.

where,

$x_{ij}$	=	flow from i to j (Bcf)
U	=	maximum allowable utilization of an arc in the season (fraction)
QCAP0	=	base pipeline capacity (capacity level existing at the end of year t+n-1) (Bcf)
YCAP	=	actual pipeline capacity added (Bcf)
YCAP0	=	base pipeline capacity utilized (Bcf)
$x_{st,i}$	=	flow from storage (st) to node (i) (Bcf)
UST	=	maximum percentage of storage available (fraction)
QSTR0	=	base storage capacity (capacity level existing at the end of year t+n-1), (Bcf)
YSTR	=	actual storage capacity added (Bcf)
YSTR0	=	base storage capacity utilized (Bcf)

With the completion of the second phase, the CEM has generated pipeline and storage capacity expansion results, as well as seasonal flows corresponding to core and noncore markets. The capacities are used directly in the Annual Flow Module, while the flows are used to generate annual pipeline capacity utilization factors for use in the Annual Flow Module. The procedure to generate annual capacity utilization factors is presented in the next section.

## Processing of CEM Results

The primary purpose of the CEM is to provide the Annual Flow Module and Pipeline Tariff Module each year with a forecast of physical pipeline capacity and working gas storage capacity for forecast year t+n, to determine maximum pipeline capacity utilizations corresponding to annual firm and total interregional flows (to be used in the maximum annual flow constraints within the Annual Flow Module), and to determine firm and interruptible net storage withdrawals (to be used in the node mass balance constraints within the Annual Flow Module). Capacity expansion results are used to determine the forecasted capacity levels; firm and total flows are used to determine pipeline utilizations; and, seasonal firm and interruptible flows into and out of storage are used to calculate firm and interruptible net storage withdrawals. These calculations are presented below.

Pipeline and storage capacity expansion levels for forecast year t+n are generated by solving the CEM linear program, and are used to determine forecasted capacities. Physical pipeline capacity along the interregional arc from transshipment node i to node j is calculated as the base capacity (including planned expansions -- Appendix E, PNEW\_CAP) plus the corresponding level of expansion in year t+n.

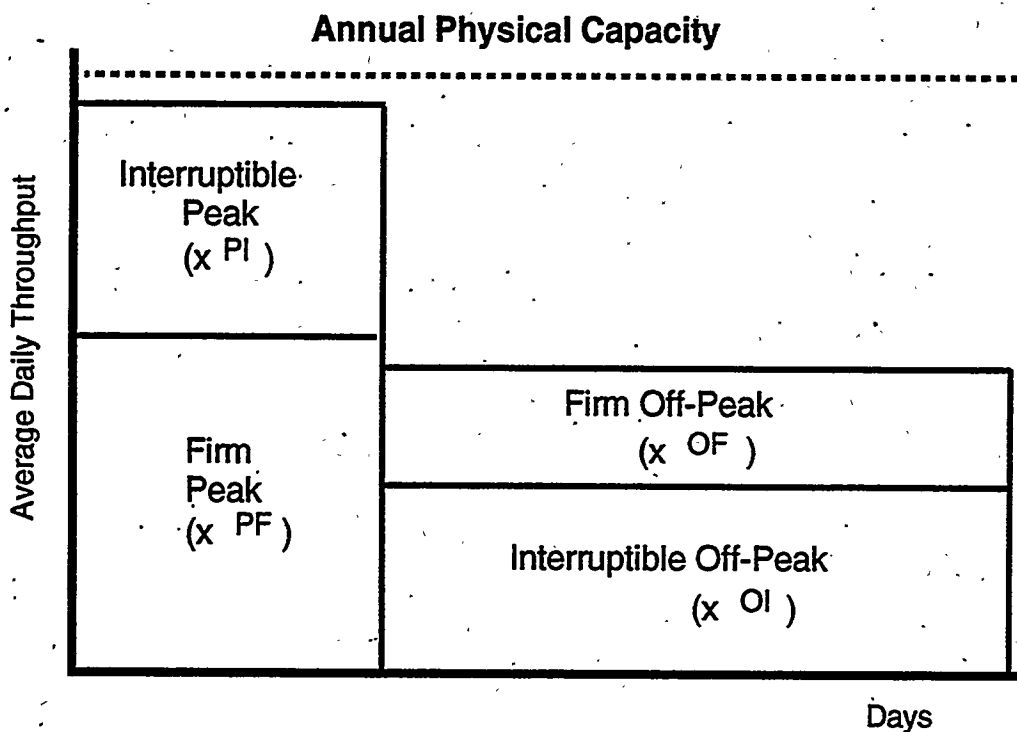
$$\text{PhyCap}_{ij} = \text{QCAP0}_{ij} + \sum_{k=1}^n \text{ycap}_{ij,k} \quad (96)$$

Likewise, regional working gas storage for year t+n is calculated as base working gas (including planned expansions -- Appendix E, PNEW\_STRX) plus the corresponding level of expansion in year t+n.

$$\text{StrCap}_{st,i} = \text{QSTR0}_{st,i} + \sum_{k=1}^n \text{ystr}_{st,i,k} \quad (97)$$

Since loads on a pipeline tend to be variable throughout a year (with full utilization more prevalent during the peak season and lower utilization during the off-peak season), the purpose of the maximum annual flow constraints in the Annual Flow Module is to better represent seasonal flows on an annual basis. This is accomplished by using the seasonal flow patterns resulting in the CEM and translating them into annual pipeline utilizations. The CEM calculates both firm and total annual pipeline utilizations to be used within the maximum annual flow constraints for both firm and total flows in the Annual Flow Module. A graphical depiction of the load curve that represents seasonal flows is presented in Figure 7-4.

Figure 7-4. Example of a Seasonal Flow Pattern Along an Arc



Firm annual utilizations are a function of peak firm flows, off-peak firm flows, and peak firm utilization rates. Peak firm utilization rates (Appendix E, ARC\_PFUTILZ) define the maximum portion of total physical annual capacity available to the peak firm service network along a specific arc, and are used in conjunction with other utilizations to establish arc-specific load duration curves represented in the CEM. Assuming that the resulting peak firm flow reflects full utilization of the capacity available to the core market during the peak season, an equivalent maximum annual capacity available to the core market can be calculated by dividing the peak firm flow by the peak firm utilization. Next, dividing the total firm flow (peak and off-peak) by this maximum annual firm capacity produces maximum firm annual utilizations used by the Annual Flow Module. The following equations result.

For the core market, along each arc  $i,j$ :

$$AUTILZ_{i,j}^F = \frac{((\text{the flow along the arc to satisfy peak period core market requirements}) + (\text{the flow along the arc to satisfy off-peak period core market requirements}))}{(\text{equivalent annual firm capacity})}$$

given, equivalent annual firm capacity =  $\frac{(\text{the flow along the arc to satisfy peak period core market requirements})}{(\text{peak firm utilization rate})}$

$$\text{AUTILZ}_{ij}^F = \frac{(x_{ij}^{PF} + x_{ij}^{OF})}{\text{ECAP}_{ij}^F} \quad (98)$$

$$\text{ECAP}_{ij}^F = \frac{x_{ij}^{PF}}{\text{UTILZ}_{ij}^{PF}}$$

where,

$$\begin{aligned} \text{AUTILZ}_{ij}^F &= \text{annual firm capacity utilization rate along arc } ij \text{ (fraction)} \\ x_{ij}^{PF} &= \text{peak firm flow along arc } ij \text{ (Bcf)} \\ x_{ij}^{OF} &= \text{off-peak firm flow along arc } ij \text{ (Bcf)} \\ \text{ECAP}_{ij}^F &= \text{equivalent capacity available to core market along arc } ij \text{ (Bcf)} \\ \text{UTILZ}_{ij}^{PF} &= \text{peak firm capacity utilization rate along arc } ij \text{ (fraction)} \end{aligned}$$

Likewise, total capacity utilization rates are a function of peak firm flows, off-peak firm flows, peak interruptible flows, off-peak interruptible flows, and peak utilization rates. Peak utilization rates (Appendix E, ARC\_PUTILZ) define the maximum portion of total physical annual capacity available in the peak period along a specific arc, and are used in conjunction with other utilizations to establish arc-specific load duration curves represented in the CEM. Assuming that the resulting peak flows reflect full utilization of the capacity available during the peak season, an equivalent maximum annual capacity available to the natural gas market can be calculated by dividing the total peak flow by the peak utilization. Next, dividing the total flow (peak and off-peak, firm and interruptible) by this maximum annual capacity produces maximum annual total utilizations used by the Annual Flow Module. The following equations result.

For the total natural gas market, along each arc  $ij$ :

$$\text{AUTILZ}_{ij}^T = ((\text{the flow along the arc to satisfy peak period core market requirements}) + (\text{the flow along the arc to satisfy off-peak period core market requirements}) + (\text{the flow along the arc to satisfy peak period noncore requirements}) + (\text{the flow along the arc to satisfy off-peak period noncore requirements})) / (\text{equivalent total annual capacity})$$

given, equivalent total annual capacity = ((the flow along the arc to satisfy peak period core market requirements) + (the flow along the arc to satisfy peak period noncore requirements) / (peak utilization rate)

$$\text{AUTILZ}_{ij}^T = \frac{(x_{ij}^{PF} + x_{ij}^{OF} + x_{ij}^{PI} + x_{ij}^{OI})}{\text{ECAP}_{ij}^T} \quad (99)$$

$$\text{ECAP}_{ij}^T = \frac{(x_{ij}^{PF} + x_{ij}^{PI})}{\text{UTILZ}_{ij}^P}$$

where,

$$\begin{aligned} \text{AUTILZ}_{ij}^T &= \text{total annual capacity utilization rate along arc } ij \text{ (fraction)} \\ x_{ij}^{PF} &= \text{peak firm flow along arc } ij \text{ (Bcf)} \\ x_{ij}^{OF} &= \text{off-peak firm flow along arc } ij \text{ (Bcf)} \\ x_{ij}^{PI} &= \text{peak interruptible flow along arc } ij \text{ (Bcf)} \\ x_{ij}^{OI} &= \text{off-peak interruptible flow along arc } ij \text{ (Bcf)} \\ \text{ECAP}_{ij}^T &= \text{equivalent total annual capacity available to the natural gas market along arc } ij \text{ (Bcf)} \\ \text{UTILZ}_{ij}^P &= \text{peak capacity utilization rate along arc } ij \text{ (fraction)} \end{aligned}$$

Contingencies have been written into the code to ensure that the total utilization remains greater than the firm, and that the total utilization is above a minimum threshold utilization.

Finally, net storage withdrawals are determined by subtracting off-peak flows going into storage from peak flows going out of storage. This is done at each node for each class of customer (i.e., firm or interruptible). Thus, an annual representation of the seasonal flow patterns established by the CEM is generated for use by the Annual Flow Module. This is defined by the following equations:

$$\text{NETSTR}_i^F = X_{st,i}^{PF} - X_{st,i}^{OF} \quad (100)$$

$$\text{NETSTR}_i^I = X_{st,i}^{PI} - X_{st,i}^{OI} \quad (101)$$

where,

$\text{NETSTR}_i^F$	=	net storage at node i for firm market (Bcf)
$\text{NETSTR}_i^I$	=	net storage at node i for interruptible market (Bcf)
$X_{st,i}^{PF}$	=	peak firm flow out of storage at node i (Bcf)
$X_{st,i}^{OF}$	=	off-peak firm flow into storage at node i (Bcf)
$X_{st,i}^{PI}$	=	peak interruptible flow out of storage at node i (Bcf)
$X_{st,i}^{OI}$	=	off-peak interruptible flow into storage at node i (Bcf)



## 8. Pipeline Tariff Module Solution Methodology

This Chapter discusses the solution methodology for the Pipeline Tariff Module (PTM) of the Natural Gas Transmission and Distribution Model (NGTDM). In this Module, for fully regulated services, the rates developed by the methodology are used as actual costs for transportation and storage services. Where interruptible services are more loosely regulated or where markets are deemed competitive, the methodology computes maximum and minimum rates for service. The minimum rate is used as a lower bound on the price of services. The actual price charged for these more loosely regulated services or the "market clearing price" is determined by the Annual Flow Module. Under current regulatory policy, the maximum price computed by the methodology (the 100-percent load factor rate) will act as a cap on the market clearing price. This "price cap" will not be enforced if deregulation of service is assumed or if Federal Energy Regulatory Commission provides for alternative pricing/cost recovery mechanisms.

The PTM tariff calculation is divided into two phases: a base-year initialization phase and a forecast year update phase. These two phases include the following steps: (1) determine the total cost of service, (2) classify line items of the cost of service as fixed and variable costs, (3) allocate fixed and variable costs to rate component (reservation and usage fee, [volumetric charge]) based on the rate design, (4) aggregate costs to the network arc/network node, (5) for transportation services, allocate costs to type of service (firm and interruptible),<sup>63</sup> and (6) compute arc-specific (node-specific) rates. For the base-year phase, the cost of service is developed from the financial data base while for the forecast year update phase the costs are estimated using a set of econometric equations. These steps are used to determine (1) transportation rates for the Annual Flow Module, (2) transportation rates for the Capacity Expansion Module to determine pipeline capacity expansion, and (3) storage rates for the Capacity Expansion Module to determine storage capacity expansion. A general overview of the methodology for deriving rates is presented in the box on the next page, while the PTM system diagram is presented in Figure 8-1.

### Base-Year Initialization Phase

The purpose of the base-year initialization phase is to provide, for the base year of the NEMS forecast horizon, an initial set of NGTDM network-level transportation and storage revenue requirements and tariffs. The base-year information is developed from existing pipeline company transportation and storage data. The base-year initialization process draws heavily on two data bases developed by the Office of Oil and Gas, EIA. These data represent the existing physical pipeline and storage system. The physical system is at a more disaggregate level than the NGTDM network. The first data base provides detailed company-level financial, cost, and rate base parameters. This financial data base contains information on capital structure, rate-base, and revenue requirements by major line item of the cost of service for the base year of the model. The second data base covers the physical attributes of the natural gas pipelines, including contract demand and pipeline layout. The physical pipeline layout data are used, along with the contract data, to derive the allocation and billing determinants. These determinants subsequently are used to compute unit rates for transportation services along each arc (and for storage services at each node) of the NGTDM network.

This section discusses three separate processes that occur during the base-year initialization phase: (1) the computation of the cost of service and rates for services, (2) the construction of capacity expansion cost/tariff curves, and (3) manipulations required to pass the rates to the Annual Flow Module and curves to the Capacity Expansion Module.

The computation of base-year cost of service and rates for services involves six distinct procedures as outlined in the box below. Each of these procedures is discussed in detail below.

In order to facilitate capacity expansion decisions in the Capacity Expansion Module, the PTM constructs cost/tariff curves which relate incremental pipeline or storage facility capacity expansion to corresponding rates. These curves

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<sup>63</sup>This step is not carried out for storage service because no distinction is made between firm and interruptible storage services.

## PTM Methodology for Deriving Rates

### For Each Company

- Derive the Total Cost of Service (COS)
  - Base Year - Read COS Line Items from Data Base
  - Forecast Year
    - Include Costs for Capacity Expansion
    - Estimate COS Line Items from Forecasting Equations
- Classify Line Items as Fixed and Variable Costs
- Allocate Costs to Rate Component Based on Rate Design

### For Each Node and Arc

- Aggregate Costs to Network Arcs and Nodes
- Allocate Costs to Services
  - Derive Allocation Determinants
  - Derive Costs by Type of Service
- Compute Rates for Services
  - Derive Billing Determinants
  - Derive Unit Fees

are developed from historically based estimates of capital and revenue requirements for capacity expansion projects using the computational procedures for determining base-year cost of service and rates.

Prior to passing the rates to the Annual Flow Module and Capacity Expansion Module, the PTM rates must be adjusted to maintain consistency among the three modules. PTM rates are calculated in nominal dollars and then converted to real dollars for use in the Annual Flow Module and Capacity Expansion Module.

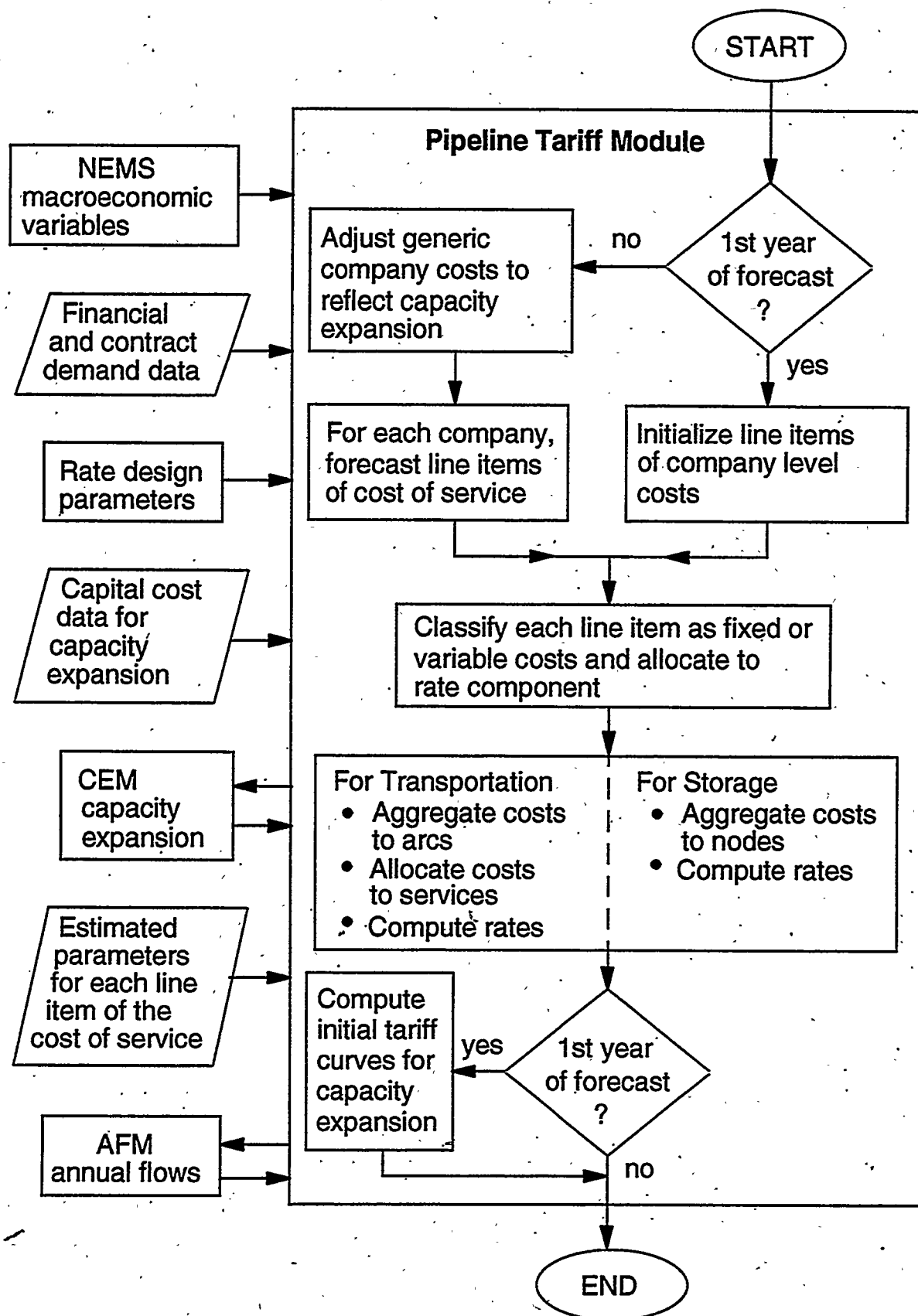
## Computation of Rates

An overview of the processing of costs in the PTM ratemaking procedure is illustrated in Figure 8-2. In the base-year initialization phase of the PTM, rates are computed using the six-step process outlined above. The first three steps are performed for the transportation and storage functions at the company level: (1) derivation of the total cost of service, (2) classifying line item costs as fixed and variable costs, and (3) allocation of fixed and variable costs to rate components based on rate design. The fourth step is to transform the costs from the company level to the network (arc and node) level. Allocation of costs to services (Step 5) and computation of rates (Step 6) are carried out at the arc level for transportation and the node level for storage. Step 5 is only executed for the transportation function because there is only one type of storage service represented in the PTM.

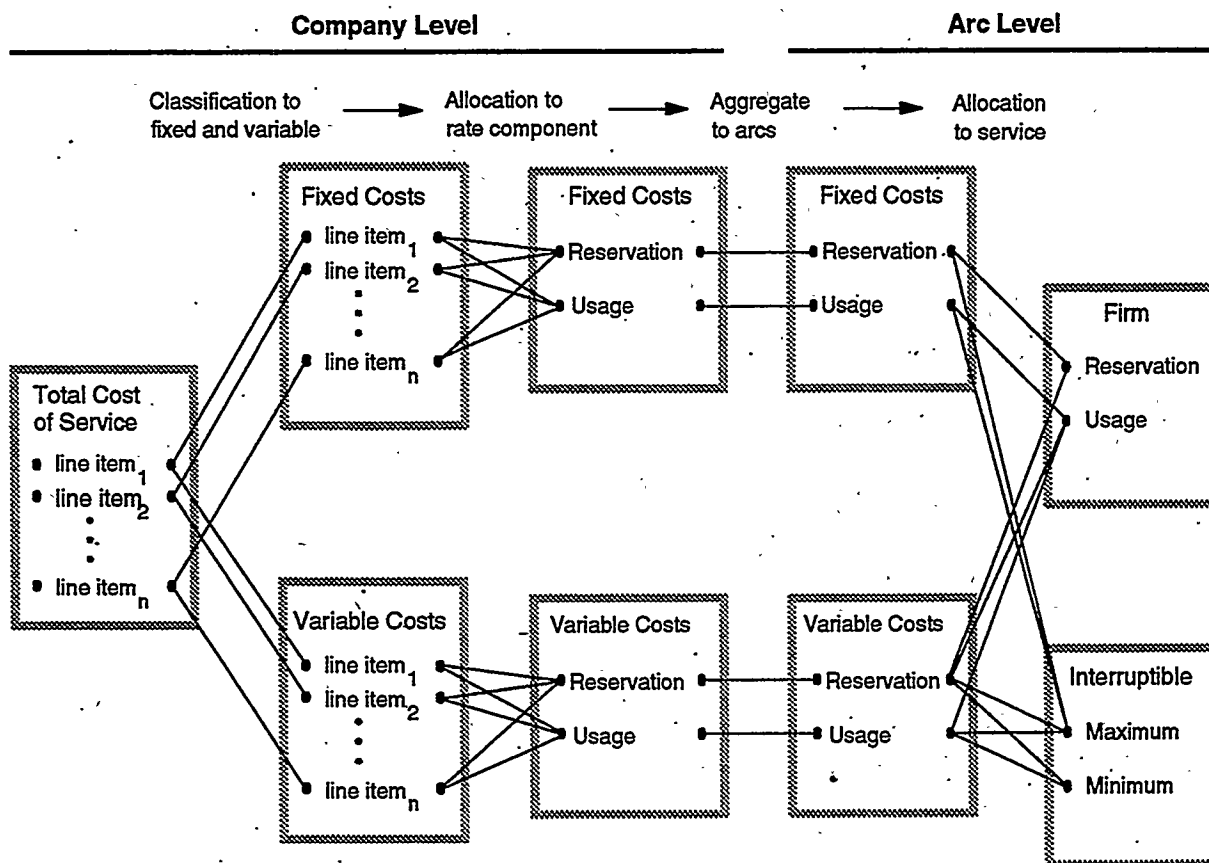
The equations apply, in general, to both transportation and storage functions. However, not all variables used in an equation are defined for both functions. For example, costs associated specifically with transportation services, such as compressor station labor costs are set to zero when the equation is used to determine storage-related costs.



Figure 8-1. Pipeline Tariff Module System Diagram



**Figure 8-2. Processing Transportation Service Costs in the Ratemaking Process**



### Step 1: Derivation of the Total Cost-of-Service

The total cost-of-service for a pipeline company is computed as the revenue requirement minus any revenue credits. The total revenue requirement (TRR) consists of a just and reasonable return on the rate base plus normal operating expenses. Revenue credits reflect revenues generated by nonjurisdictional services and one time costs that are outside of the scope of the PTM. Therefore, the total cost of service is computed as follows:

$$TCOS = TRR - REVC \quad (102)$$

$$TRR = TRRB + TNOE \quad (103)$$

where,

- TCOS = total cost-of-service (dollars<sup>64</sup>)
- TRR = total revenue requirement (dollars)
- TNOE = total normal operating expenses (dollars)
- REVC = revenue credits to cost-of-service (dollars) (Appendix E)
- TRRB = total return on rate base (dollars)

Derivations of return on rate base, total normal operating expenses, and revenue credits are presented in the following subsections.

<sup>64</sup>All costs discussed in this chapter are in nominal dollars, unless explicitly stated otherwise.

**Return.** In order to compute the return portion of the cost-of-service, the determination of capital structure and rate base is necessary. Capital structure is important because it determines the cost of capital to the pipeline company. The weighted average cost of capital is applied to the rate base to determine the return component of the cost-of-service, as follows:

$$\text{TRRB} = \text{WAROR} * \text{APRB} \quad (104)$$

where,

TRRB = total return on rate base [before taxes, (dollars)]  
 WAROR = weighted-average before-tax return on capital (fraction)  
 APRB = adjusted pipeline rate base (dollars)

In addition, for reporting purposes, the return on rate base is broken out into the three components as shown below.

$$\text{PFEN} = (\text{PFES}/\text{TOTCAP}) * \text{PFER} * \text{APRB} \quad (105)$$

$$\text{CMEN} = (\text{CMES}/\text{TOTCAP}) * \text{CMER} * \text{APRB} \quad (106)$$

$$\text{LTDN} = (\text{LTDS}/\text{TOTCAP}) * \text{LTDR} * \text{APRB} \quad (107)$$

where,

PFEN = total return on preferred stock (dollars)  
 PFES = value of preferred stock (dollars)  
 TOTCAP = total capitalization (dollars)  
 PFER = coupon rate for preferred stock (fraction)  
 APRB = adjusted pipeline rate base (dollars)  
 CMEN = total return on common stock equity (dollars)  
 CMES = value of common stock equity (dollars)  
 CMER = common equity rate of return (fraction)  
 LTDN = total return on long-term debt (dollars)  
 LTDS = value of long-term debt (dollars)  
 LTDR = long-term debt rate (fraction)

The cost of capital (WAROR) is computed as the value-weighted average cost of capital for preferred stock, common stock equity, and long-term debt, as follows:

$$\text{WAROR} = (\text{PFES} * \text{PFER} + \text{CMES} * \text{CMER} + \text{LTDS} * \text{LTDR}) / \text{TOTCAP} \quad (108)$$

$$\text{TOTCAP} = \text{PFES} + \text{CMES} + \text{LTDS} \quad (109)$$

where,

WAROR = weighted-average before-tax return on capital (fraction)  
 PFES = value of preferred stock (dollars)  
 PFER = preferred stock rate (fraction)  
 CMES = value of common stock equity (dollars)  
 CMER = common equity rate of return (fraction)  
 LTDS = value of long-term debt (dollars)  
 LTDR = long-term debt rate (fraction)  
 TOTCAP = total capitalization (dollars)

The total rate base is computed as the sum of net plant in service, cash working capital, other working capital and transition expense balance minus accumulated deferred income taxes. That is,

$$\text{APRB} = \text{NIS} + \text{CWC} + \text{OWC} + \text{TPEB} - \text{ADIT} \quad (110)$$

where,

APRB = adjusted pipeline rate base (dollars)  
 NIS = net capital cost of plant in service (dollars)  
 CWC = cash working capital (dollars)  
 OWC = other working capital (dollars)  
 TPEB = transition expense balance (dollars)<sup>65</sup>  
 ADIT = accumulated deferred income taxes (dollars)

The net plant in service is the original capital cost plant in service minus the accumulated depreciation.

$$\text{NIS} = \text{GPIS} - \text{ADDA} \quad (111)$$

where,

NIS = net capital cost of plant in service (dollars)  
 GPIS = original capital cost of plant in service [gross plant in service (dollars)]  
 ADDA = accumulated depreciation, depletion, and amortization (dollars)

**Total Normal Operating Expenses.** Total normal operating expense line items include depreciation, taxes, administrative and general expenses, customer expenses, and operation and maintenance expenses. In the PTM, taxes are disaggregated further into Federal, State, and other taxes and tax credits to permit tax policy analysis. Operation and maintenance expenses also are disaggregated into several categories to enhance accuracy in forecasting expenses by function.

$$\text{TNOE} = \text{DDA} + \text{TOTAX} + \text{TAG} + \text{TCE} + \text{TOM} \quad (112)$$

where,

TNOE = total normal operating expenses (dollars)  
 DDA = depreciation, depletion, and amortization costs (dollars)  
 TOTAX = total Federal and State income tax liability (dollars)  
 TAG = total administrative and general expense (dollars)  
 TCE = total customer expense (dollars)<sup>66</sup>  
 TOM = total operations and maintenance expense (dollars)

Depreciation, depletion, and amortization costs, administrative and general expense, and customer expense are available directly from the financial data base.

Total taxes are computed as the sum of Federal and State income taxes and other taxes, less tax credits, as follows:

$$\text{TOTAX} = \text{FSIT} + \text{OTTAX} - \text{FSITC} \quad (113)$$

$$\text{FSIT} = \text{FIT} + \text{SIT} \quad (114)$$

where,

TOTAX = total Federal and State income tax liability (dollars)  
 FSIT = Federal and State income tax (dollars)  
 OTTAX = all other taxes assessed by Federal, State, or local governments except income taxes (dollars)  
 FSITC = Federal and State investment tax credits (dollars)

<sup>65</sup>The transition expense balance is the remaining balance of approved but yet to be recovered transition costs associated with restructuring gas supply contracts for Order 636.

<sup>66</sup>Customer expense includes direct payroll distributions of salaries and wages associated with the following services: customer accounts, customer service, information, and sales.

FIT = Federal income tax (dollars)

SIT = State income tax (dollars)

Federal income taxes are derived from returns to common stock equity and preferred stock (after-tax profit) and the Federal tax rate. The after-tax profit is determined as follows:

$$ATP = APRB * (PFER * PFES + CMER * CMES) / TOTCAP \quad (115)$$

where,

ATP = after-tax profits (dollars)

APRB = adjusted pipeline rate base (dollars)

TOTCAP = total capitalization (dollars)

PFER = preferred stock rate (fraction)

PFES = value of preferred stock (dollars)

CMER = common equity rate of return (fraction)

CMES = value of common stock equity (dollars)

and the Federal income taxes are

$$FIT = (FRATE * ATP / 1 - FRATE) \quad (116)$$

where,

FIT = Federal income tax (dollars)

FRATE = Federal income tax rate (fraction) (Appendix E)

ATP = after-tax profits (dollars)

State income taxes are computed by multiplying the sum of taxable returns and the associated Federal income tax by a weighted-average State tax rate associated with each pipeline company. The weighted-average State tax rate is based on peak service volumes in each State delivered by the pipeline company. State income taxes are computed as follows:

$$SIT = SRATE * (FIT + ATP) \quad (117)$$

where,

SIT = State income tax (dollars)

SRATE = average State income tax rate (fraction) (Appendix E)

FIT = Federal income tax (dollars)

ATP = after-tax profits (dollars)

Total operations and maintenance expense consists of three major categories: supervision and engineering expenses, compressor station expenses, and other operations and maintenance expenses.<sup>67</sup> Compressor station expenses are disaggregated further into two categories: compressor station operating and maintenance labor expenses and compressor station operating and maintenance non-labor expenses. That is, total operating and maintenance expense (TOM) equals

$$TOM = SEOM + CSOML + CSOMN + OTOM \quad (118)$$

where,

TOM = total operations and maintenance expense (dollars)

SEOM = supervision and engineering expense (dollars)

CSOML = compressor station operating and maintenance labor expense (dollars)

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<sup>67</sup>Some expenses in this category apply only to transportation costs. Consequently, compressor-related and similar expenses will not be calculated for storage facilities.

CSOMN = compressor station operating and maintenance non-labor expense (dollars)  
 OTOM = other operations and maintenance expense (dollars)

**Revenue Credits.** The revenue requirement is reduced (increased) by various revenue credits (expenses) to determine the total cost-of-service. These credits may relate to one-time expenditures that are outside the scope of the other cost categories.

After the determination of the total cost of service, each line item is classified as a fixed or variable cost as described in Step 2.

## Step 2: Classification of Cost of Service Line Items as Fixed and Variable Costs

The PTM classifies each line item of the cost of service (computed in Step 1) as a fixed and variable cost. Fixed costs are independent of storage/transportation usage, while variable costs are a function of usage. Fixed and variable costs are computed by multiplying each line item of the cost of service by the percentage of the cost that is fixed and the percentage of the cost that is variable. The classification of fixed and variable costs is defined by the user as part of the scenario specification. The classification of line item cost  $R_i$  to fixed and variable cost is determined as follows:

$$R_{i,f} = ALL_f \cdot R_i / 100 \quad (119)$$

$$R_{i,v} = ALL_v \cdot R_i / 100 \quad (120)$$

where,

$R_{i,f}$  = fixed cost portion of line item  $R_i$  (million dollars)  
 $ALL_f$  = percentage of line item  $R_i$  representing fixed cost  
 $R_i$  = total cost of line item  $i$  (million dollars)  
 $R_{i,v}$  = variable cost portion of line item  $R_i$  (million dollars)  
 $ALL_v$  = percentage of line item  $R_i$  representing variable cost  
 $i$  = line item index  
 $100 = ALL_f + ALL_v$

An example of this procedure is illustrated in Table 8-1.

## Step 3: Allocation of Fixed and Variable Costs to Rate Components

Allocation of fixed and variable costs to rate components is conducted only for transportation services because storage service is modeled in a more simplified manner using a one-part rate.

The rate design to be used within the PTM is specified by input parameters, which can be modified by the user to reflect changes in rate design over time. The PTM allocates the fixed and variable costs computed in Step 2 to rate components as specified by the rate design. For transportation service, the components of the rate consist of a reservation and a usage fee. The reservation fee is a charge assessed based on the amount of the capacity reserved. It typically is a monthly fee that does not vary with throughput. The usage fee is a charge assessed for each unit of gas that moves through the system. For storage service the rate components are aggregated into one volumetric charge that is based on the amount of working gas capacity.<sup>68</sup>

The actual reservation and usage fees that pipelines are allowed to charge are regulated by the Federal Energy Regulatory Commission. How costs are allocated determines the extent of differences in the rates charged for different classes of customers for different types of services. In general, the more fixed costs are allocated to usage fees, the more costs are recovered based on throughput. Thus high load factor customers pay a larger share of system costs. Allocating a larger share of fixed costs to reservation fees, however, leads to low load factor customers

<sup>68</sup>This simplified representation of one volumetric charge related to the working gas capacity is designed to include all the costs that in actual practice are recovered through reservation, inventory, injection, and withdrawal charges.

**Table 8-1. Illustration of Fixed and Variable Cost Classification**

Cost of Service Line Item	Total	Allocation Factors (percent)		Cost Component	
		Fixed Cost	Variable Cost	Fixed	Variable
Total Return					
Preferred Stock	1,000	100	0	1,000	0
Common Stock	30,000	100	0	30,000	0
Long-Term Debt	29,000	100	0	29,000	0
Normal Operating Expenses					
Depreciation	30,000	100	0	30,000	0
Taxes					
Federal Tax	25,000	100	0	25,000	0
State Tax	5,000	100	0	5,000	0
Other Tax	1,000	100	0	1,000	0
Tax Credits	1,000	100	0	1,000	0
Administrative & General	50,000	90	10	45,000	5,000
Customer	2,000	100	0	2,000	0
Operations & Maintenance					
Supervision & Engineering	7,000	100	0	7,000	0
Compression Station/Labor	5,000	100	0	5,000	0
Compression Station/Non-labor	1,000	20	80	200	800
Other O & M	40,000	80	20	32,000	8,000
Revenue Requirement	227,000			213,200	13,800
Revenue Credits	25,000	100	0	25,000	0
Total Cost-of-Service	202,000			188,200	13,800

bearing a larger share of system costs.

Costs are assigned either to the reservation fee or to the usage fee according to the rate design specified for the pipeline company. The rate design can vary among pipeline companies. Three typical rate designs are described in Table 8-2. The PTM provides two options for specifying the rate design. In the first option, a rate design for each pipeline company can be specified for each forecast year. This option permits different rate designs to be used for different pipeline companies while also allowing individual company rate designs to change over time. Since pipeline company data subsequently are aggregated to the network arc, the composite rate design at the arc-level is the volumetric-weighted average of the pipeline company rate designs. The second option permits a global specification of the rate design, where all pipeline companies have the same rate design for a specific time period but can switch to another rate design in a different time period. In this option, the user will have the capability to specify the initial and final rate designs and the forecast year in which the rate design changes. Currently, the first option is used in PTM (Appendix E, MATRIX).

The allocation of fixed costs to reservation and usage fees entails multiplying each fixed cost line item of the total cost of service by the corresponding fixed cost rate design classification factor. A similar process is carried out for variable costs. This procedure is illustrated in Tables 8-3a and 8-3b and is generalized in the equations below.

The classification of transportation line item costs  $R_{i,r}$  and  $R_{i,u}$  to reservation and usage cost is determined as follows:

$$R_{i,r} = ALL_{f,r} * R_i / 100 \quad (121)$$

$$R_{i,u} = ALL_{f,u} * R_i / 100 \quad (122)$$

$$R_{i,v,r} = ALL_{v,r} * R_i / 100 \quad (123)$$

$$R_{i,v,u} = ALL_{v,u} * R_i / 100 \quad (124)$$

where,

- $R$  = line item cost (dollars)
- $ALL$  = percentage of reservation or usage line item  $R$  representing fixed or variable cost (Appendix E -- AFR, AVR, AFU, AVU)
- $100 = ALL_{f,r} + ALL_{f,u}$
- $100 = ALL_{v,r} + ALL_{v,u}$
- $i$  = line item number index
- $f$  = fixed cost index
- $v$  = variable cost index
- $r$  = reservation cost index
- $u$  = usage cost index

At this stage in the procedure, the line items comprising the fixed and variable cost components of the reservation and usage fees can be summed to obtain total fixed and variable costs allocated to reservation and usage components of the rates.

After ratemaking Steps 1, 2 and 3 are completed for each company, company-level costs are transformed to arc-level (node-level) rates for transportation (storage) services. This process, carried out for each arc and node in the NGTDM network, is accomplished in ratemaking Steps 4, 5 and 6 as presented below.

#### Step 4: Aggregation of Classified Cost of Service to Network Arcs and Nodes

As discussed above, for transportation services the PTM develops fixed and variable costs and allocates them to reservation and usage rate components at the pipeline company level. The PTM apportions these components to distinct segments of a pipeline path based on the share of the mileage-based capacity reservations on the segment. These pipeline path segments represent the portions of the physical pipeline system that fall within the transshipment



**Table 8-2. Approaches to Rate Design**

Modified Fixed Variable (Three-Part Rate)	Modified Fixed Variable (Two-Part Rate)	Straight Fixed Variable (Two-Part Rate)
<ul style="list-style-type: none"> <li>Two-part reservation fee. - Return on equity and related taxes are held at risk to achieving throughput targets by allocating these costs to the usage fee. Of the remaining fixed costs, 50 percent are recovered from a peak day reservation fee and 50 percent are recovered through an annual reservation fee.</li> <li>Variable costs allocated to the usage fee. In addition, return on equity and related taxes are also recovered through the usage fee.</li> </ul>	<ul style="list-style-type: none"> <li>Reservation fee based on peak day requirements. - all fixed costs except return on equity and related taxes recovered through this fee.</li> <li>Variable costs plus return on equity and related taxes are recovered through the usage fee.</li> </ul>	<ul style="list-style-type: none"> <li>One-part capacity reservation fee. All fixed costs are recovered through the reservation fee, which is assessed based on peak day capacity requirements.</li> <li>Variable costs are recovered through the usage fee.</li> </ul>

nodes that define a network arc. The costs associated with each segment are mapped to the network arc by aggregating the cost information across all pipeline segments identified with an arc.<sup>69</sup> The capacity reservation shares (Appendix E, PS) used to apportion costs to pipeline segments are derived exogenously from the capacity reserved and distances associated with each segment and the capacity reserved and distances for the complete pipeline path. The shares do not change throughout the forecast.

This procedure is illustrated for two hypothetical pipeline companies (Figure 8-3). In the example, it is assumed that the total costs to be distributed to distinct pipeline segments are  $R_A$  and  $R_B$  for Company A and Company B, respectively. Notice that Company A is defined by network a, b, c, d, e in the upper portion of Figure 8-3 and Company B is defined by network a, b, c, d in the middle half of the figure. Company A receives 4000 MMBtu/day at point a, discharges 2000 MMBtu/day at point c and ships the remaining 2000 MMBtu/day to point e. Company B ships 3,000 MMBtu along its entire route, from point a to point c. It is assumed further that segment b-d of Company A's pipeline path and segment b-c of Company B's pipeline path are to be mapped into the network arc defined by the transshipment nodes 1-2 at the bottom of Figure 8-3. Note that company A's segment b-d actually is composed of two segments: segment b-c and segment c-d.

<sup>69</sup>In the forecast years, arc-level costs include costs associated with generic companies representing pipeline capacity added subsequent to the base year. Generic companies are discussed in the section describing the forecast year updating process.

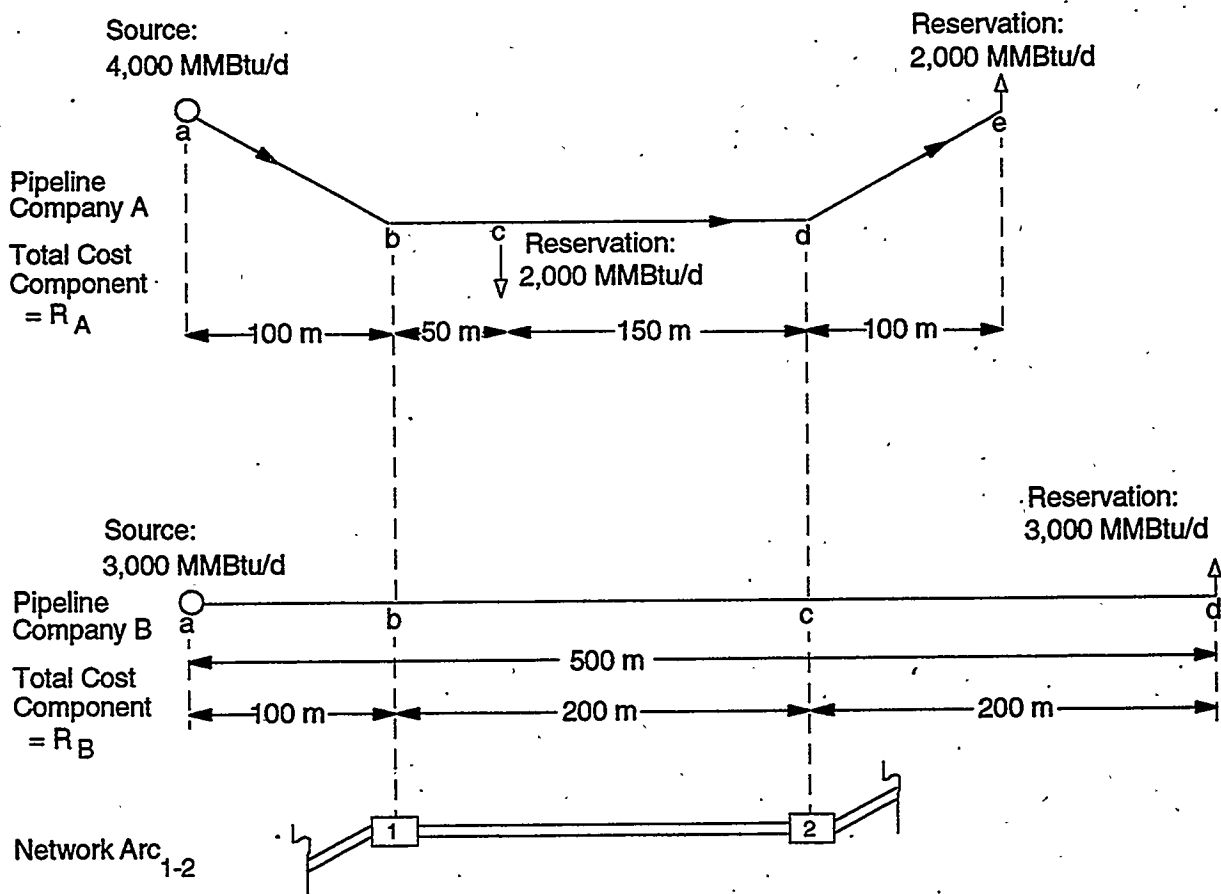
**Table 8-3a. Illustration of Allocation of Fixed Costs to Rate Components**

Cost of Service Line Item	Total	Allocation Factors (percent)		Cost Assigned to Rate Component	
		Reservation	Usage	Reservation	Usage
Total Return					
Preferred Stock	1,000	0	100	0	1,000
Common Stock	30,000	0	100	0	30,000
Long-Term Debt	29,000	100	0	29,000	0
Normal Operating Expenses					
Depreciation	30,000	100	0	30,000	0
Taxes					
Federal Tax	25,000	0	100	0	25,000
State Tax	5,000	0	100	0	5,000
Other Tax	1,000	100	0	1,000	0
Tax Credits	1,000	100	0	1,000	0
Administrative & General	45,000	100	0	45,000	0
Customer	2,000	100	0	2,000	0
Operations & Maintenance					
Supervision & Engineering	7,000	100	0	7,000	0
Compression Station/Labor	5,000	100	0	5,000	0
Compression Station/Non-labor	200	100	0	200	0
Other O & M	32,000	100	0	32,000	0
Revenue Requirement	213,200			152,200	61,000
Revenue Credits	25,000	100	0	25,000	0
Total Cost-of-Service	188,200			127,200	61,000

**Table 8-3b. Illustration of Allocation of Variable Costs to Rate Components**

Cost of Service Line Item	Total	Allocation Factors (percent)		Cost Assigned to Rate Component	
		Reservation	Usage	Reservation	Usage
<b>Total Return</b>					
Preferred Stock	0	0	100	0	0
Common Stock	0	0	100	0	0
Long-Term Debt	0	0	100	0	0
<b>Normal Operating Expenses</b>					
Depreciation	0	0	100	0	0
<b>Taxes</b>					
Federal Tax	0	0	100	0	0
State Tax	0	0	100	0	0
Other Tax	0	0	100	0	0
Tax Credits	0	0	100	0	0
Administrative & General	5,000	0	100	0	5,000
Customer	0	0	100	0	0
<b>Operations &amp; Maintenance</b>					
Supervision & Engineering	0	0	100	0	0
Compression Station/Labor	0	0	100	0	0
Compression Station/Non-labor	800	0	100	0	800
Other O & M	8,000	0	100	0	8,000
Revenue Requirement	13,800			0	13,800
Revenue Credits	0	0	100	0	0
<b>Total Cost-of-Service</b>	<b>13,800</b>			<b>0</b>	<b>13,800</b>

Figure 8-3. Example of Apportioning Pipeline Costs to Network Arcs



The mileage-based capacity reservation ( $V$ ) is determined as the capacity reserved in each pipeline segment multiplied by the length of the pipeline segment. For Company A the reservation on segment b-c is the quantity  $(4000 \times 50)$  MMBtu-miles and the reservation on segment c-d is the quantity  $(2000 \times 150)$  MMBtu-miles per day. For company B, the reservation on segment b-c is the quantity  $(3000 \times 200)$  MMBtu-miles per day. The total reservation along the pipeline path for company A is the sum of the reservations on each segment, or 1,100,000 MMBtu-miles per day.<sup>70</sup>

Once the reservations on the segments are determined, the pipeline costs are apportioned to each segment as follows. The share of cost ( $R_A$ ) allocated to Company A's pipeline segment b-c is determined as the cost multiplied by the ratio of the reservations on segment b-c to the reservations on the total pipeline path, expressed as follows:

$$R_A^{b-c} = R_A \cdot V_A^{b-c} / V_A^T \quad (125)$$

where,

$R_A^{b-c}$  = portion of  $R_A$  allocated to Company A segment b-c  
 $R_A$  = total component cost for Company A (dollars)

<sup>70</sup>Derived based on capacity reservations on arc a-b equal to  $(4000 \times 100)$  MMBtu-miles per day, plus capacity reservations on arc b-c of  $(4000 \times 50)$  MMBtu-miles per day, plus capacity reservations on arc c-d of  $(2000 \times 150)$  MMBtu-miles per day and capacity reservations  $(2000 \times 100)$  MMBtu-miles per day on arc d-e.

$V_A^{b-c}$  = reservations on Company A segment b-c  
 $V_A^T$  = total reservation on Company A pipeline path

In this example,  $V_A^{b-c}$  equals 200,000 MMBtu-miles per day and  $V_A^T$  equals 1,100,000 MMBtu-miles per day.

Similarly, the allocation of costs to Company A's segment c-d [ $R_A^{c-d} = R_A \cdot (3/11)$ ] and to Company B's segment b-c [ $R_B^{b-c} = R_B \cdot (6/15)$ ] are obtained. Finally, the costs are aggregated to the network arc by summing all distinct costs for Company A's segment b-c and segment c-d and Company B's segment b-c.

$$R_{1-2} = R_A^{b-c} + R_A^{c-d} + R_B^{b-c} \quad (126)$$

where,

$R_{1-2}$  = total costs allocated to arc 1-2  
 $R_A^{b-c}$  = portion of  $R_A$  allocated to Company A segment b-c  
 $R_A^{c-d}$  = portion of  $R_A$  allocated to Company A segment c-d  
 $R_B^{b-c}$  = portion of  $R_B$  allocated to Company B segment b-c

Through this procedure, company-level fixed and variable costs are assigned to arcs on the NGTDM network and for each arc these costs have been assigned to a rate component. Thus the following variables are defined:

$FCR_a$  = fixed costs assigned to the reservation component of the rate  
 $VCR_a$  = variable costs assigned to the reservation component of the rate  
 $FCU_a$  = fixed costs assigned to the usage component of the rate  
 $VCU_a$  = variable costs assigned to the usage component of the rate  
 $a$  = arc

Apportioning storage costs to network nodes is a more straightforward process because the costs are simply assigned to the nodes as a function of the share of storage capacity located in each region. Through the procedure provided in the following equations company-level fixed and variable costs are shared out and aggregated to nodes on the NGTDM network.

$$FCS_n = FCS_n + (NS_{p,n} \cdot SF_p) \quad (127)$$

$$VCS_n = VCS_n + (NS_{p,n} \cdot SV_p) \quad (128)$$

where,

$VCS_n$  = variable costs of storage (million dollars)  
 $FCS_n$  = fixed costs of storage (million dollars)  
 $NS_{p,n}$  = share of company p gas storage capacity located at the node n [Appendix E, (fraction)]  
 $SF_p$  = company p fixed costs for storage service (million dollars)  
 $SV_p$  = company p variable costs for storage service (million dollars)  
 $p$  = pipeline company index  
 $n$  = node index

## Step 5: Allocation of Arc-Level Transportation Costs to Services

The arc-level fixed and variable costs are allocated to firm and interruptible transportation services. In allocating these costs, a portion of the fixed costs are assigned to noncore customers. Historically, rate designs have placed some of the recovery of fixed costs at risk by assigning the recovery of these costs to noncore customers. Should the revenues obtained from interruptible service be less than those anticipated in the ratemaking process, the pipeline

company would not recover all of its fixed costs. Variable costs are allocated based on total annual throughput for each type of service. The development of the allocation determinants is discussed next.

**Allocation Determinants for Fixed Costs.** The allocation determinants for fixed costs are based, in part, on the firm capacity reservations and annual interruptible transportation volumes along an arc. The procedure for obtaining arc-level reservations and flows in the base year is comparable to the process described above for aggregating segment costs to an arc.<sup>71</sup> The allocation determinants for fixed costs are defined as follows. The fixed cost allocation determinant for firm service is defined as the annualized peak-day reservations for firm service divided by the sum of the annualized peak-day firm reservations and an adjusted annual throughput volume for interruptible service. In equation form, this allocation determinant (FADFS) is defined as follows:

$$FADFS_a = (PRESV_a * 365 / (PRESV_a * 365 + ISERV_a * RADJ_a * (1 + IEXPCT_a / 100))) \quad (129)$$

where,

- FADFS<sub>a</sub> = allocation determinant for fixed costs recovered from firm service (ratio)
- PRESV<sub>a</sub> = peak-day reservations for firm transportation service (Bcf per day) [Appendix F, CONDEM]
- ISERV<sub>a</sub> = annual throughput volume for interruptible transportation service (Bcf per year)
- IEXPCT<sub>a</sub> = expected annual rate of growth in interruptible transportation [Appendix E, (percent, currently set to 0)]
- RADJ<sub>a</sub> = adjustment factor for discounting [Appendix E -- BASERADJ, (ratio)]
- a = arc

The interruptible throughput volume is adjusted in the above equation for two reasons. First, the interruptible volumes are adjusted to reflect anticipated changes in interruptible transportation volumes using the user-specified IEXPCT parameter. Second, the volume is adjusted downward via the RADJ factor to reflect anticipated discounting of interruptible transportation services. This adjustment factor (RADJ) reflects the degree of discounting that took place in the prior forecast year and is defined as follows:

$$RADJ_a = AFM\_PTAR_{I_a}^{t-1} / PMAX_a^{t-1} \quad (130)$$

where,

- t = current year index
- RADJ<sub>a</sub> = adjustment factor for discounting [Appendix E -- BASERADJ, (ratio)]
- AFM\_PTAR<sub>I<sub>a</sub></sub><sup>t-1</sup> = average interruptible service rate in year t-1 [Appendix E, (dollars per Mcf)]
- PMAX<sub>a</sub><sup>t-1</sup> = maximum interruptible service rate in year t-1 (dollars per Mcf)
- a = arc

Similarly, the allocation determinant for fixed costs assigned to interruptible service (FADIS) is defined as

$$FADIS_a = \frac{ISERV_a * RADJ_a * (1 + IEXPCT_a / 100)}{PRESV_a * 365 + ISERV_a * RADJ_a * (1 + IEXPCT_a / 100)} \quad (131)$$

where,

- FADIS<sub>a</sub> = allocation determinant for fixed costs assigned to interruptible service [1-FADFS<sub>a</sub> (ratio)]
- ISERV<sub>a</sub> = annual throughput volume for interruptible transportation service (Bcf per year)
- RADJ<sub>a</sub> = adjustment factor for discounting [Appendix E -- BASERADJ, (ratio)]
- IEXPCT<sub>a</sub> = expected rate of growth in interruptible transportation [Appendix E, (percent)]
- PRESV<sub>a</sub> = peak-day reservations for firm transportation service (Mcf per day) [Appendix E, CONDEM]
- a = arc

<sup>71</sup>In subsequent years, flow volumes are input to the PTM at the arc-level.

**Allocation Determinants for Variable Costs.** The allocation determinants for variable costs are based on the annual firm and interruptible service volumes on the arc. The allocation determinant that assigns variable costs to firm service (VADFS) is defined as the annual throughput volume for firm transportation on the arc (FSERV) divided by the total annual throughput volume for firm and interruptible service on the arc, as follows:

$$VADFS_a = FSERV_a / (FSERV_a + ISERV_a) \quad (132)$$

where,

VADFS<sub>a</sub> = allocation determinant for variable costs assigned to firm service (ratio)  
 FSERV<sub>a</sub> = annual throughput volume for firm transportation service (Bcf per year)  
 ISERV<sub>a</sub> = annual throughput volume for interruptible transportation (Bcf per year)  
 a = arc

The allocation determinant that assigns variable costs to interruptible services (VADIS) is defined as the annual throughput volume for interruptible service divided by the total annual throughput volume for firm and interruptible service, as follows:

$$VADIS_a = ISERV_a / (FSERV_a + ISERV_a) \quad (133)$$

where,

VADIS<sub>a</sub> = allocation determinant for variable costs assigned to interruptible service (ratio)  
 ISERV<sub>a</sub> = annual throughput volume for interruptible transportation service in (Bcf per year)  
 FSERV<sub>a</sub> = annual throughput volume for firm transportation (Bcf per year)  
 a = arc

The determinants are applied to costs previously allocated to rate components (in Step 4) to derive the costs allocated to the firm transportation rate components. Similarly allocation determinants are applied to obtain the costs allocated to interruptible transportation. These procedures are outlined in equation form below.

**Derivation of Reservation Costs for Firm Transportation.** Costs allocated to the firm transportation reservation fees consist of the firm transportation portion of the fixed and variable costs assigned to the reservation fee. This cost is derived by applying the allocation determinants as follows:

$$RCFS_a = (FADFS_a * FCR_a) + (VADFS_a * VCR_a) \quad (134)$$

where,

RCFS<sub>a</sub> = reservation costs assigned to core customers (million dollars per year)  
 FADFS<sub>a</sub> = allocation determinant for fixed costs recovered from firm service (ratio)  
 FCR<sub>a</sub> = fixed costs assigned to the reservation component of the rate (million dollars per year)  
 VADFS<sub>a</sub> = allocation determinant for variable costs recovered from firm service (ratio)  
 VCR<sub>a</sub> = variable costs assigned to the reservation component of the rate (million dollars per year)  
 a = arc

**Derivation of Usage Costs for Firm Transportation.** Costs allocated to the firm transportation usage fees consists of the firm transportation portion of the fixed and variable costs assigned to the usage fee. This cost is derived by applying the allocation determinants as follows:

$$UCFS_a = (FADFS_a * FCU_a) + (VADFS_a * VCU_a) \quad (135)$$

where,

UCFS<sub>a</sub> = usage costs assigned to core customers (million dollars per year)  
 FADFS<sub>a</sub> = allocation determinant for fixed costs recovered from firm service (ratio)  
 FCU<sub>a</sub> = fixed costs assigned to the usage component of the rate (million dollars per year)  
 VADFS<sub>a</sub> = allocation determinant for variable costs recovered from firm service (ratio)

$VCU_a$  = variable costs assigned to the usage component of the rate (million dollars per year)  
 $a$  = arc

**Derivation of Fixed and Variable Costs Allocated to Interruptible Transportation.** Costs allocated to interruptible transportation service consist of a portion of the fixed and variable costs assigned to the reservation and usage rate components. This cost is derived by applying the allocation determinants as follows:

$$CIS_a = (FADIS_a * (FCU_a + FCR_a)) + (VADIS_a * (VCU_a + VCR_a)) \quad (136)$$

where,

$CIS_a$  = costs assigned to noncore customers (million dollars per year)  
 $FADIS_a$  = allocation determinant for fixed costs recovered from interruptible service (ratio)  
 $FCU_a$  = fixed costs assigned to the usage component of the rate (million dollars per year)  
 $FCR_a$  = fixed costs assigned to the reservation component of the rate (million dollars per year)  
 $VADIS_a$  = allocation determinant for variable costs recovered from interruptible service (ratio)  
 $VCU_a$  = variable costs assigned to the usage component of the rate (million dollars per year)  
 $VCR_a$  = variable costs assigned to the reservation component of the rate (million dollars per year)  
 $a$  = arc

The costs allocated to interruptible transportation service are not used to derive the maximum and minimum rates that may be charged for interruptible service. These costs are presented here to account fully for all costs that make up the total cost of service and to facilitate the discussion of the derivation of the costs allocated to firm transportation service. The computation of rates for firm and interruptible service is presented in Step 6.

#### Step 6: Computation of Rates

**Firm Transportation Service.** Firm transportation service rates ( $PTAR_F$ ) are composed of arc-level reservation and usage fees ( $PTAR\_REV\_F$  and  $UFEE$ ), as well as Order 636 transition costs ( $PTAR\_191\_F$  and  $PTAR\_GSR\_F$ ). Arc-level reservation and usage fees for firm service are determined by dividing the costs corresponding to each rate component by the appropriate billing determinants. Thus, the reservation fee is determined as the reservation costs recovered from firm service ( $RCFS_a$ ) divided by the annualized reservations for firm transportation service. That is,

$$RFEE_a = RCFS_a / (PRESV_a * 365) \quad (137)$$

where,

$RFEE_a$  = reservation fee for firm service in dollars per Mcf of capacity reserved  
 $RCFS_a$  = reservation costs assigned to core customers (million dollars per year)  
 $PRESV_a$  = peak-day reservations for firm transportation service (Bcf per day) [Appendix E, CONDEM]  
 $a$  = arc

However, the NGTDM pipeline network uses tariffs in the form of dollars per Mcf of throughput. Therefore, the reservation fee component of the NGTDM pipeline tariff is derived by dividing the reservation costs assigned to firm service ( $RCFS_a$ ) by the expected annual firm transportation service throughput. That is,

$$PTAR\_REV\_F_a = RCFS_a / PTMD\_FFL_a \quad (138)$$

where,

$PTAR\_REV\_F_a$  = reservation fee component of the firm service pipeline tariff (dollars per Mcf of throughput)  
 $RCFS_a$  = reservation costs assigned to core customers (million dollars per year)  
 $PTMD\_FFL_a$  = expected annual throughput volume for firm transportation (Bcf per year)  
 $a$  = arc



To ensure that recovery of costs is close to full-recovery, the reserve portion of firm tariff is set to be no less than reservation fee (RFEE) divided by firm loading factor (LFAC\_F). That is,

$$PTAR\_REV\_F_a = \text{MAX}(PTAR\_REV\_F_a, RFEE_a/LFAC\_F) \quad (139)$$

where,

PTAR\_REV\_F<sub>a</sub> = reservation fee component of the firm service pipeline tariff (dollars per Mcf of throughput)  
 RFEE<sub>a</sub> = reservation fee for firm service (dollars per Mcf of capacity reserved)  
 LFAC\_F = load factor for deriving the minimum firm rate (Appendix E)  
 a = arc

The usage fee is determined as the usage costs recovered from core customers (UCFS<sub>a</sub>) divided by the expected annual throughput volume for firm service, as follows:

$$UFEE_a = UCFS_a/PTMD\_FFL_a \quad (140)$$

where,

UFEE<sub>a</sub> = usage fee for firm service (dollars per Mcf)  
 UCFS<sub>a</sub> = usage costs assigned to core customers (million dollars per year)  
 PTMD\_FFL<sub>a</sub> = expected annual throughput volume for firm transportation (Bcf per year)  
 a = arc

The total firm pipeline tariff is the sum of the reservation and usage components as shown below:

$$PTAR\_F_a = PTAR\_REV\_F_a + UFEE_a \quad (141)$$

where,

PTAR\_F<sub>a</sub> = pipeline tariff for firm service sent to the Annual Flow Module (dollars per Mcf)  
 PTAR\_REV\_F<sub>a</sub> = reservation fee component of the firm service pipeline tariff (dollars per Mcf of throughput)  
 UFEE<sub>a</sub> = usage fee for firm service (dollars per Mcf)  
 a = arc

To account for regulatory oversight and to assist in stabilizing the tariffs, a check is performed each year to limit the annual increase in the firm tariff components to a user specified escalation rate. This limit is imposed as shown in the following equation:

$$PTAR\_F_{a,t} = \text{MIN}(PTAR\_F_{a,t}, PTAR\_F_{a,t-1} * (1 + \text{MAXESC})) \quad (142)$$

where,

PTAR\_F<sub>a,t</sub> = pipeline tariff for firm service sent to the Annual Flow Module (dollars per Mcf)  
 PTAR\_F<sub>a,t-1</sub> = pipeline tariff for firm service in previous year (dollars per Mcf)  
 MAXESC = maximum allowable annual escalation rate for tariffs [Appendix E, (fraction)]  
 a = arc  
 t = forecast year

Various accounting mechanisms have been built into the tariff computation procedures to account specifically for Order 636 transition costs. These mechanisms are implemented in the base year (and subsequent years) and therefore they are presented in this section of the Chapter.<sup>72</sup>

Balances in purchase gas adjustment accounts (otherwise known as Account 191) are collected on a per unit basis of firm throughput. The costs are assumed to be collected over a multi-year period. The Account 191 surcharge is computed as follows:

<sup>72</sup>The magnitude of Order 636 transition costs, the years during which they are collected and the share of costs assigned to different classes of service are data driven. See reference in Appendix E (PNEWFAC, PSTRADED) for the default values.

$$PTAR_{191\_F_a} = (ANUM191 / FSERV_a) / A191YRS \quad (143)$$

where,

$PTAR_{191\_F_a}$  = firm tariff surcharge for Account 191 transition costs (dollars per Mcf)  
 $ANUM191$  = Account 191 transition costs assigned to arc a (million dollars)  
 $FSERV_a$  = annual throughput volume for firm transportation (Bcf per year)  
 $A191YRS$  = number of years Account 191 costs are assumed to be collected (Appendix E)  
 $a$  = arc

Tariff surcharges to collect gas supply realignment costs (GSR costs) are computed in a similar manner; however, flexibility is provided to assign a portion of the costs to core customers and a portion of the costs to noncore customers as follows:

$$PTAR_{GSR\_F_a} = [(AGSRCOSTS_a * SHARE_{GSR\_F}) / FSERV_a] / GSRYRS \quad (144)$$

where,

$PTAR_{GSR\_F_a}$  = firm tariff surcharge for GSR transition costs (dollars per Mcf)  
 $AGSRCOSTS_a$  = GSR transition costs assigned to arc a (million dollars)  
 $SHARE_{GSR\_F}$  = fraction of GSR transition costs assigned to firm service (Appendix E)  
 $FSERV_a$  = annual throughput volume for firm transportation (Bcf per year)  
 $GSRYRS$  = number of years GSR costs are assumed to be collected (Appendix E)  
 $a$  = arc

The total firm tariff sent to the Annual Flow Module network is the sum of the firm tariff and any Order 636 surcharges. The total tariff is computed as shown below.

$$PTAR_{F_a} = PTAR_{F_a} + PTAR_{191\_F_a} + PTAR_{GSR\_F_a} \quad (145)$$

where,

$PTAR_{F_a}$  = total tariff for firm service passed to the Annual Flow Module (dollars per Mcf)  
 $PTAR_{191\_F_a}$  = firm tariff surcharge for Account 191 transition costs (dollars per Mcf)  
 $PTAR_{GSR\_F_a}$  = firm tariff surcharge for GSR transition costs (dollars per Mcf)  
 $a$  = arc

This firm tariff is then checked against an upper limit on firm tariff (Appendix E, LIMITFIRM) to prevent the tariff from becoming unrealistically high due to low utilization along the arc.

**Interruptible Transportation Service.** The actual interruptible transportation rates are determined within the linear programming solution procedure, but are bounded by regulated maximum and minimum rates provided by the PTM. The arc-level maximum and minimum rates for interruptible transportation service are derived from variable costs, reservation and usage fees for firm service, and a load factor permitted by FERC for interruptible service (LFAC) (currently set equal to 100 percent). The maximum tariff ( $MAX_a$ ) is computed as the sum of the reservation fee (divided by the load factor) and the usage fee. That is,

$$MAX_a = RFEE_a / LFAC_I + UFEE_a \quad (146)$$

where,

$MAX_a$  = maximum rate for interruptible service (dollars per Mcf)  
 $RFEE_a$  = reservation fee for firm service (dollars per Mcf)  
 $LFAC_I$  = load factor for deriving the maximum interruptible rate [(ratio) = 1.00, from RDESIGN]  
 $UFEE_a$  = usage fee for firm service (dollars per Mcf)  
 $a$  = arc

Similar to the firm pipeline tariffs, the regulated maximum interruptible tariff is allowed to increase at a rate no greater than a user specified escalation rate, as shown in the equation below:

$$MAX_{a,t} = \min (MAX_{a,t}, MAX_{a,t-1} * (1+MAXESC)) \quad (147)$$

where,

$MAX_{a,t}$  = maximum rate for interruptible service (dollars per Mcf)  
 $MAX_{a,t-1}$  = maximum rate for interruptible service in previous year (dollars per Mcf)  
 $MAXESC$  = maximum allowable annual escalation rate for tariffs [Appendix E, (fraction)]  
 $a$  = arc  
 $t$  = forecast year

The minimum tariff ( $MIN_a$ ) is computed as the sum of all variable costs associated with the arc ( $VSUM_a$ ) divided by the total annual firm and interruptible throughput volume, as follows:

$$MIN_a = VSUM_a / (FSERV_a + ISERV_a) \quad (148)$$

$$VSUM_a = VCR_a + VCU_a \quad (149)$$

where,

$MIN_a$  = minimum rate for interruptible service (dollars per Mcf)  
 $VSUM_a$  = total variable costs for firm and interruptible service (million dollars)  
 $FSERV_a$  = annual throughput volume for firm transportation (Bcf)  
 $ISERV_a$  = annual throughput volume for interruptible transportation service (Bcf)  
 $VCR_a$  = variable costs assigned to the reservation component of the rate (million dollars)  
 $VCU_a$  = variable costs assigned to the usage component of the rate (million dollars)  
 $a$  = arc

Interruptible transportation rates may also include some surcharge attributable to Order 636 transition costs. Gas supply realignment costs are partially collected through a surcharge on interruptible rates. The computation of this surcharge is shown below.

$$PTAR\_GSR\_I_a = [(AGSRCOSTS_a * SHARE\_GSR\_I) / ISERV_a] / GSRYRS \quad (150)$$

where,

$PTAR\_GSR\_I_a$  = interruptible tariff surcharge for GSR transition costs (dollars per Mcf)  
 $AGSRCOSTS_a$  = GSR transition costs assigned to arc  $a$  (million dollars)  
 $SHARE\_GSR\_I$  = fraction of GSR transition costs assigned to interruptible service ( $SHARE\_GSR\_I = 1.0 - SHARE\_GSR\_F$ )  
 $ISERV_a$  = annual throughput volume for interruptible transportation (Bcf per year)  
 $GSRYRS$  = number of years GSR costs are assumed to be collected (Appendix E)  
 $a$  = arc

The surcharge of gas supply realignment costs on interruptible rates is then checked against the surcharge of gas supply realignment costs on firm rates to ensure that the surcharge on interruptible rates does not exceed the surcharge on firm rates. That is,

$$PTAR\_GSR\_I_a = \min(PTAR\_GSR\_I_a, PTAR\_GSR\_F_a) \quad (151)$$

where,

$PTAR\_GSR\_I_a$  = interruptible tariff surcharge for GSR transition costs (dollars per Mcf)  
 $PTAR\_GSR\_F_a$  = firm tariff surcharge for GSR transition costs (dollars per Mcf)  
 $a$  = arc

The interruptible surcharge is then added to the minimum and maximum interruptible rates, when applicable (e.g., during the years GSR costs are assumed to be collected). That is,

$$MIN_a = MIN_a + PTAR\_GSR\_I_a \quad (152)$$

$$MAX_a = MAX_a + PTAR\_GSR\_I_a$$

where,

$$\begin{aligned} MAX_a &= \text{maximum rate for interruptible service (dollars per Mcf)} \\ MIN_a &= \text{minimum rate for interruptible service (dollars per Mcf)} \\ PTAR\_GSR\_I_a &= \text{interruptible tariff surcharge for GSR transition costs (dollars per Mcf)} \\ a &= \text{arc} \end{aligned}$$

The interruptible tariff that is computed represents the cost of moving interruptible gas along an arc, and is used in the Annual Flow Module network. The value for this tariff lies between the minimum and maximum interruptible tariffs, and is determined using a scale factor (SCALE\_I). The interruptible tariff is calculated by the following equation:

$$PTAR\_I_a = MIN_a + SCALE\_I_a * (MAX_a - MIN_a) \quad (153)$$

where,

$$\begin{aligned} PTAR\_I_a &= \text{total tariff for interruptible transportation service passed to the Annual Flow Module (dollars per Mcf)} \\ MAX_a &= \text{maximum rate for interruptible service (dollars per Mcf)} \\ MIN_a &= \text{minimum rate for interruptible service (dollars per Mcf)} \\ SCALE\_I_a &= \text{scale factor for interruptible tariff (fraction)} \\ a &= \text{arc} \end{aligned}$$

The scale factor (SCALE\_I) is a nonlinear function of the interruptible utilization rate on that arc in the previous year. Its value is between zero and one. If the utilization rate was low last year, the scale factor will be close to zero and, thus, the interruptible tariff closer to the minimum interruptible tariff to encourage more use on this arc. On the other hand, if the utilization was close to full capacity in the previous year, the interruptible tariff will be close to the maximum interruptible tariff to discourage use on this arc. This algorithm reflects the behavior of the pipeline company in a competitive market where price would quickly react to market changes. The computation of this scale factor is shown below:

$$SCALE\_I_a = UTIL\_RATE\_I_a * UTIL\_RATE\_I_a * e^{(UTIL\_RATE\_I_a - 1.0)} \quad (154)$$

where,

$$\begin{aligned} SCALE\_I_a &= \text{scale factor for interruptible tariff (fraction)} \\ UTIL\_RATE\_I_a &= \text{utilization rate for interruptible service (fraction)} \\ a &= \text{arc} \end{aligned}$$

Utilization rate is defined based on flows and effective capacity (PREVTCAP<sub>a</sub>) from the previous year.

$$UTIL\_RATE\_I_a = AISERV_a / (PREVTCAP_a - AFSERV_a) \quad (155)$$

$$PREVTCAP_a = PCAP\_MAX_a * AUTILZ\_T_a * (1 - WTHR\_XCAP_a) \quad (156)$$

where,

$$\begin{aligned} UTIL\_RATE\_I_a &= \text{utilization rate for interruptible service (fraction)} \\ AISERV_a &= \text{previous year interruptible flow on arc (Bcf)} \\ AFSERV_a &= \text{previous year firm flow on arc (Bcf)} \\ PREVTCAP_a &= \text{effective total capacity in previous year (Bcf)} \\ PCAP\_MAX_a &= \text{maximum effective capacity on arc (Bcf)} \\ AUTILZ\_T_a &= \text{total utilization on arc (fraction)} \\ WTHR\_XCAP_a &= \text{weather factor (fraction)} \end{aligned}$$

The interruptible tariff resulting from the above calculation is then checked against a maximum interruptible tariff (Appendix E, LIMITINT) to prevent the tariff from becoming unrealistically high due to low utilization along the arc.

**Revenue Credit Option.** A revenue credit algorithm has been designed and implemented as an option in the PTM. Its purpose is to capture the effects of capacity release on firm pipeline tariffs through the treatment of interruptible revenues. With this algorithm, a pipeline company<sup>73</sup> is allowed to transfer a portion of their incremental revenue from interruptible service to firm service. The incremental revenue of interruptible service is defined as the portion above expected revenue which is determined by using a conservative estimate of interruptible flow defined for the pipeline company. The portion transferred to firm service then becomes a credit to firm service, resulting in a reduction in the firm revenue requirements and, thus, firm tariffs. The methodology used to calculate the amount of incremental revenue transferred from interruptible service to firm service, and ultimately used to adjust firm service tariffs, follows.

First, incremental revenue from interruptible service (INC\_REV) is calculated as the difference between the actual revenue recovered and the revenue expected to be recovered, both from interruptible service. The actual revenue recovered from interruptible service equals the interruptible flow (ISERV) times a derived interruptible tariff (CAL\_TAR\_I). The revenue expected to be recovered from interruptible service is also referred to as the cost assigned to interruptible service (CIS). Finally, the derived interruptible tariff along an arc is based on the corresponding marginal node prices produced by the AFM in the previous year. The corresponding equations are as follows:

$$INC\_REV_a = MISERV_a * CAL\_TAR\_I_a - (CIS_a / MC\_PGDP) \quad (157)$$

$$CAL\_TAR\_I_a = NG\_MAGPR\_I_{AT} * AEFF\_PIPE_{AF,AT} - NG\_MAGPR\_I_{AF} \quad (158)$$

where,

- INC\_REV = incremental revenue on arc (millions of 1987 real dollars)
- MISERV = interruptible flow from AFM calculated in previous year (1 year lag) (Bcf)
- CIS = cost assigned to interruptible service in current year (millions of nominal dollars)
- MC\_PGDP = GDP deflator (from Macroeconomic Activity Model)
- CAL\_TAR\_I = derived interruptible tariff (\$87/Mcf)
- NG\_MAGPR\_I = marginal node price (from AFM, \$87/Mcf)
- AEFF\_PIPE = pipeline/arc efficiency [Appendix E, (fraction)]
- a = arc
- AF = source node along arc
- AT = destination node along arc

Next, incremental costs are defined as incremental flows times the minimum tariff (for interruptible service) needed to recover variable costs. Incremental flows are the difference between interruptible flows along an arc for this year and the previous year. Thus,

$$INC\_COST_a = INC\_FLOW_a * MIN_a \quad (159)$$

where,

- INC\_COST = incremental cost on arc (millions of 87 dollars)
- INC\_FLOW = incremental flow on arc (Bcf)
- MIN = the minimum tariff for interruptible service (\$87/Mcf)
- a = arc

<sup>73</sup> According to regulation, revenue crediting can be adopted into the rate making process of an individual pipeline company. However, in the PTM module, revenue crediting is implemented at the arc level, instead.

Incremental profit is then calculated as the difference between incremental revenues and incremental costs, as follows:

$$INC\_PRFT_a = INC\_REV_a - INC\_COST_a \quad (160)$$

where,

INC\_PRFT = incremental profit on arc (millions of 1987 dollars)  
 INC\_REV = incremental revenue on arc (millions of 1987 dollars)  
 INC\_COST = incremental cost on arc (millions of 1987 dollars)  
 a = arc

A portion of this incremental profit is defined as the revenue credited (CREDIT\_F) to firm service. This credit is then converted to a rate (RATEADJ\_F<sub>a</sub>) which is used to reduce firm rates (PTAR\_F<sub>a</sub>). That is,

$$CREDIT\_F_a = RCREDIT\_F_a * INC\_PRFT_a \quad (161)$$

$$RATEADJ\_F_a = CREDIT\_F_a / MFserv_a \quad (162)$$

$$PTAR\_F_a = PTAR\_F_a - RATEADJ\_F_a \quad (163)$$

where,

CREDIT\_F = amount of credit transferred to firm service on arc (millions of 87\$)  
 RCREDIT\_F = the percentage of revenue reallocated as revenue credit to firm service [Appendix E, (fraction)]  
 INC\_PRFT = incremental profit (millions of 87\$)  
 RATEADJ\_F = the adjusting rate used to credit firm tariff on arc (\$87/Mcf)  
 MFserv = previous year firm flow provided by the AFM, including Alaska flow, in current year (Bcf)  
 PTAR\_F = firm pipeline tariff on arc (\$87/Mcf)  
 a = arc

Once the firm tariff is adjusted, a check is made to ensure that the resulting firm tariff is no less than the minimum interruptible tariff times a scale factor. This test serves to ensure that an unrealistic over-adjustment has not been made.

$$PTAR\_F_a = \max (PTAR\_F_a, MIN_a * SCALE\_F\_MIN) \quad (164)$$

where,

PTAR\_F<sub>a</sub> = firm pipeline tariff on arc (\$87/Mcf)  
 MIN<sub>a</sub> = minimum interruptible tariff on arc (\$87/Mcf)  
 SCALE\_F\_MIN = scale factor (Appendix E)  
 a = arc

**Storage Service.** Storage facilities are defined in the NGTDM network at regional nodes. In the base-year initialization phase, storage facility costs, capacities, inventories, and other data for existing companies are allocated to regional NGTDM network nodes using storage facility data in FERC and EIA data series.<sup>74</sup> An interstate pipeline company's total reported storage cost is allocated to NGTDM region nodes according to the regional

<sup>74</sup>FERC Form 2 provides total storage costs for interstate pipeline companies with storage facilities. Form EIA-191 provides injections, withdrawals, inventories, and base and working gas capacity by field/reservoir for storage facilities owned by all storage companies. The Form EIA-191 filings include information that allows facilities to be designated as owned by interstate pipeline and other firms.

distribution of natural gas storage capacity in the company's own storage facilities, as reported on Form EIA-191.<sup>75</sup> Because storage costs are related to base gas storage capacity, the cost allocation is based on the company's regional share of base gas storage capacity relative to its total base gas storage capacity. Regional interstate pipeline company-level costs are aggregated to the corresponding NGTDM region node (Equations 127 and 128).

The regional storage costs for interstate pipeline companies are converted to per-unit-capacity costs by dividing the aggregate regional cost by the aggregate regional base gas storage capacity. The interstate pipeline per-unit storage capacity cost obtained for each region is applied to the non-interstate (intrastate and third party owners) regional storage capacity to obtain their estimated storage costs. These costs are added to the NGTDM region aggregate interstate pipeline company costs (FCS and VCS) to obtain the total storage facility costs (FCST and VCST) at the region node.

Next, the node-level storage tariff is computed as the sum of fixed and variable total costs divided by the working gas capacity, as shown below.

$$STAR_n = VSUM_n / WGCTT_n \quad (165)$$

where,

$STAR_n$  = storage tariff (dollars per Mcf)  
 $VSUM_n$  = total storage costs (million dollars)  
 $WGCTT_n$  = working gas capacity, jurisdictional and non-jurisdictional (Bcf)  
 $n$  = node

The total cost of storage is defined as the sum of all fixed and variable total storage costs as shown below:

$$VSUM_n = VCST_n + FCST_n \quad (166)$$

where,

$VSUM_n$  = total storage cost (million dollars)  
 $VCST_n$  = variable storage costs (million dollars)  
 $FCST_n$  = fixed storage cost (million dollars)  
 $n$  = node

To account for regulatory oversight and to assist in stabilizing the tariffs, a check is performed each year to limit the annual increase in the storage tariff to a user specified escalation rate. This limit is imposed as shown in the following equation.

$$STAR_{n,t} = \text{MIN}(STAR_{n,t}, STAR_{n,t-1} * (1 + \text{MAXESC})) \quad (167)$$

where,

$STAR_{n,t}$  = storage tariff (dollars per Mcf)  
 $STAR_{n,t-1}$  = storage tariff from previous year (dollars per Mcf)  
 $\text{MAXESC}$  = maximum allowable annual escalation rate for tariffs [Appendix E, (fraction)]  
 $n$  = node  
 $t$  = forecast year

This method of computing storage tariffs does not conform strictly to industry practices; rather it conforms to the representation of storage in other modules of the NGTDM.

<sup>75</sup>To distribute costs regionally, it is assumed that reported costs represent only costs associated with storage facilities owned by the company and do not include costs of storing gas in other facilities.

## **Construction of Capacity Expansion Cost (Pipeline/Storage) Tariff Curves**

As part of the base-year initialization process, the PTM constructs cost (or pipeline/storage tariff) curves for the Capacity Expansion Module. The primary criterion in determining when and where physical pipelines and storage facilities will need to be expanded is the need of customers purchasing firm service to receive gas on future peak days. A secondary criterion is that the costs associated with pipeline and storage expansion are kept to a minimum. In general, pipeline companies and local distribution companies (LDC) recognize that the high costs incurred in adding pipeline and storage capacity may lead to increased per-unit charges to customers purchasing firm service, which in the short-term may lead to slight decreases in consumption levels. In the long-term, increased delivery costs may lead to much more significant demand shifts when end-use capital purchasing decisions are affected.

To facilitate the cost minimization process in the Capacity Expansion Module, separate cost/tariff curves for incremental pipeline capacity expansion and storage expansion projects are developed for the incremental pipeline and storage services by the PTM and input to the Capacity Expansion Module. These cost/tariff curves relate incremental capacity expansion by arc (region) to corresponding pipeline (storage) tariffs.

The cost/tariff curves are constructed through a process comparable to the base-year initialization procedure described earlier. The PTM has an exogenous data input file of pipeline and storage capacity cost curves that relate capital cost to corresponding capacity expansion. Pipeline and storage capital cost data are developed from the incremental costs required to add an additional increment of capacity along a network arc or to a storage node in the NGTDM. These incremental costs reflect the capital costs associated with adding compressors, looping,<sup>76</sup> and other means of expanding pipeline capacity, or the capital costs associated with adding new or expanding existing natural gas storage fields. The PTM also obtains from an exogenous data base the operating costs, depreciation schedules, and other components of revenue requirements associated with pipeline or storage expansion. The exogenous data are defined by region and are based on historic industry averages.

Construction of the pipeline capacity (storage) tariff cost curves is comparable to the process in which base-year transportation (storage) tariffs are developed. However, instead of using the existing pipeline company data bases, the components of revenue requirements for the capacity expansion cost curves are obtained from a separate exogenous data base containing the capital and revenue requirements for capacity expansion projects. Using these data, together with the base-line initialization equations discussed below, the PTM develops the reservation fee associated with each level of capacity expansion provided by the Capacity Expansion Module. The pipeline capacity (storage) expansion tariff curves are constructed in the base year and are used by the Capacity Expansion Module in all subsequent forecast years.<sup>77</sup>

## **Passing Rates to the Annual Flow Module and Curves to Capacity Expansion Module**

As discussed in Chapter 5, the PTM passes the following items to the Annual Flow Module: (1) reservation costs assigned to core customers, (2) usage fees for firm transportation service, (3) minimum transportation rate for interruptible service, (4) maximum transportation rate for interruptible service, and (5) rates for storage service. All PTM data elements passed to the Annual Flow Module must be converted to real dollars using the GDP deflators from the NEMS macroeconomic model. Similarly, when passing the capacity expansion cost tariff curves to the Capacity Expansion Module, the rates must be converted to real dollars.

## **Forecast Year Update Phase**

The purpose of the forecast year update phase is to project, for each subsequent year of the forecast period, the line items of the cost-of-service discussed above that are used to develop rates. In each remaining year of the simulation,

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<sup>76</sup>Looping is the construction of a pipeline parallel to an existing line to increase the capacity of the system.

<sup>77</sup>The pipeline tariff is in dollars per MMBtu-mile and the storage tariff, including injection and inventory costs, is in dollars per MMBtu of working gas capacity.



the PTM forecasts the pipeline company-level parameters required to determine the cost of capital, rate-base, operation and maintenance expense, and taxes. Additionally, arc-specific billing determinants are projected for the forecast year. These parameters are used to calculate the arc-specific (node-specific) rates using the procedure described in the base-year initialization phase. The forecasting relationships are discussed in detail below.

The PTM also accounts for revenues and volumetric flows for new capacity in the forecast year by assigning these parameters to arc- or region-specific generic pipeline or storage companies. These parameters are forecast at the arc-level in subsequent years. Generic pipeline and storage companies are discussed in more detail below.

After all the line items of the cost-of-service are forecasted, the PTM proceeds to: (1) classify line items of the cost of service as fixed and variable costs, (2) allocate fixed and variable costs to rate component (reservation and usage fee, volumetric charge) based on the rate design, (3) aggregate costs to the network arc/network node, (4) for transportation services, allocate costs to type of service (firm and interruptible), and (5) compute arc-specific (node-specific) rates.

### **Generic Pipeline and Storage Companies for Capacity Expansion**

The Capacity Expansion Module projects pipeline capacity expansion at the arc level and storage expansion at the regional level, as opposed to determining expansion for individual companies. The PTM creates arc-specific generic pipeline companies and regional, node-specific, generic storage facilities to incorporate the effects of capacity expansion on an arc or node. Thus, the PTM tracks costs attributable to capacity added during the forecast period separately from the costs attributable to facilities in service in the base year. The PTM uses an exogenous data base to obtain the capital costs which correspond to the level of capacity expansion provided by the Capacity Expansion Module in the forecast year.<sup>78</sup> The exogenous data base contains costs in real dollars. These costs must be converted to nominal dollars in the forecast year using the GDP deflators provided by the NEMS macroeconomic model. Other line items of the cost-of-service for the generic companies are derived from historical industry averages and are provided by an exogenous data base. These costs too must be converted to nominal dollars and also must be scaled to reflect the size of expansion determined by the Capacity Expansion Module.

The new capacity expansion expenditures allowed in the rate-base within the forecast year is derived for each arc and node from the amount of incremental capacity additions determined by the Capacity Expansion Module as shown below.

$$NCAE = \sum_{s=2}^S (CAPCST_{a,s} - CAPCST_{a,s-1}) * (EXPAND_{a,s} / AVAIL_{a,s}) \quad (168)$$

$$NCAE = \sum_{s=2}^S (CAPCST_{n,s} - CAPCST_{n,s-1}) * (EXPAND_{n,s} / AVAIL_{n,s}) \quad (169)$$

where,

- NCAE = new capacity expansion expenditures allowed in the rate base within the forecast year (dollars)
- CAPCST = total capital cost to expand capacity (dollars)
- EXPAND = amount of incremental capacity added by the Capacity Expansion Module (Bcf)
- AVAIL = maximum amount of capacity expansion available (Bcf)
- a = arc
- n = node
- s = index for type of expansion, 1 = existing capacity, 2 = compression, 3 = looping, 4,5,6 = new pipe

<sup>78</sup>Capital requirements for new storage capacity expansion are determined from the incremental base gas capacity expansion and the wellhead price in the forecast year which is used as cushion gas to maintain adequate pressures.

The total capital cost to expand capacity at each arc is derived below.

$$CAPCST_{a,s} = CAPCST_{a,s-1} + (ARCCC_{a,s} * ((ARCEX_{a,s} - ARCEX_{a,s-1}) * 1,000,000) * MILES_a) / 365 \quad (170)$$

where,

CAPCST = total capital cost to expand capacity (dollars)  
 ARCCC = capital cost per unit of expansion (dollars-day per Mcf-mile)  
 ARCEX = allowable expansion size for an arc (Bcf)  
 MILES = length of transportation arc in miles [Appendix E]  
 a = arc  
 s = index for type of expansion; 1 = existing capacity, 2 = compression, 3 = looping, 4,5,6 = new pipe

An upper bound limiting the amount of additional capacity that can be achieved through adding compression, looping, and adding new pipe is defined for each arc as a function of the base year arc capacity. The bounds are defined as follows:

$$ARCEX_{a,s} = PCAP\_MAX_a * ARCFAC_{a,s} \quad (171)$$

where,

ARCEX = maximum allowable capacity expansion (Bcf)  
 PCAP\_MAX = base year design capacity (Bcf)  
 ARCFAC = arc capacity expansion factor [Appendix E, (fraction)]  
 a = arc  
 s = expansion step

Unit capital costs for expanding capacity are adjusted to reflect regional differences in costs, as shown below.

$$ARCCC_{a,s} = CCOST_{a,s} * (1 + CSTFAC_{a,s}) \quad (172)$$

where,

ARCCC = capital cost per unit of expansion (dollars-day per Mcf-mile)  
 CCOST = capital cost to expand 1 unit of pipeline capacity [Appendix E, (dollars-day per Mcf-mile)]  
 CSTFAC = factor to accommodate regional difference in cost [Appendix E, (fraction)]  
 a = arc  
 s = expansion step

Similar to pipeline capacity expansion, capital costs for expanding storage at each node is derived below.

$$CAPCST_{n,s} = CAPCST_{n,s-1} + (NODECC_{n,s} * (NODEEX_{n,s} - NODEEX_{n,s-1}) * 1,000,000) \quad (173)$$

where,

CAPCST = total capital cost to expand capacity (dollars)  
 NODECC = capital cost per unit of expansion (dollars per Mcf)  
 NODEEX = allowable expansion size for a node (Bcf)  
 n = node  
 s = expansion step

An upper bound limiting the amount of additional storage capacity that can be added at each node is defined as a function of the base year node capacity. The bounds are defined as follows:

$$NODEEX_{n,s} = (WGCT_n + WGCNT_n) * NODFAC_{n,s} \quad (174)$$

where,

NODEEX = maximum allowable capacity expansion at a given storage node (Bcf)

WGCT = jurisdictional working gas capacity in the base year (Bcf)  
 WGCNT = non-jurisdictional working gas capacity in the base year (Bcf)  
 NODFAC = node capacity expansion factor [Appendix E -- FACTOR, (fraction)]  
 n = node  
 s = expansion step

For pipeline capacity expansion, the peak day reservations are set equal to the daily capacity (the capacity provided by the Capacity Expansion Module divided by 365 days per year). The annual flow through the pipeline is calculated as the capacity multiplied by a utilization factor provided by the Capacity Expansion Module or assumed exogenously. For storage capacity expansion, the amount of gas withdrawn is set equal to the working gas capacity.

After the generic pipeline company transportation and storage volumes and cost-of-service are determined, the generic company is treated within the PTM as an additional arc-specific pipeline company and/or regional node-specific storage facility. Cost-of-service for the aggregate of all prior years' capacity expansion projects is projected to the forecast year according to the subsequent year's forecasting procedure discussed below. Company-level cost-of-service for the new incremental capacity in the forecast year are determined according to the base-year initialization procedure discussed above and added to the projected cost-of-service of the aggregate prior years' capacity.

### ***Forecasting Cost-of-Service***<sup>79</sup>

The primary purpose in forecasting cost-of-service is to capture major changes in the composition of the revenue requirements and major changes in cost trends through the forecast period. These changes may be caused by new construction or maintenance and life extension of nearly depreciated plants, as well as by changes in the cost and availability of capital.

The projection of the cost-of-service is approached from the viewpoint of a long-run marginal cost analysis for gas pipeline systems. Thus, costs that are viewed as fixed for the purposes of a rate case actually vary in the long-run with one or more external measures of size or activity levels in the industry. For example, capital investments for replacement and refurbishment of existing facilities are a long-run marginal cost of the pipeline system. Once in place, however, the capital investments are viewed as fixed costs for the purposes of rate cases.

The same is true of operations and maintenance expenses which, except for short-run variable costs such as fuel, are most commonly classified as fixed costs in rate cases. For example, customer expenses logically vary over time based on the number of customers served and the cost of serving each customer. The unit cost of serving each customer, itself, depends on factor cost changes (e.g., wage rates), the extent or complexity of service provided to each customer, and the efficiency of the technology level employed in providing the service.

The long-run marginal cost approach generally projects total costs as the product of unit cost for the activity multiplied by the incidence of the activity. Unit costs are projected from factor cost changes combined with time trends describing changes in level of service, complexity, or technology. The level of activity is projected in terms of variables external to the PTM (e.g., annual throughput, etc.) which are both logically and empirically related to the incurrence of costs.

Implementation of the long-run marginal cost approach involves forecasting relationships developed through empirical studies of historical change in pipeline/storage facility costs, accounting algorithms, exogenous assumptions, and inputs from other NEMS modules. These forecasting algorithms may be classified into three distinct projected pipeline cost areas, as follows:

- The projection of existing and incremental rate base and capital costs
- The projection of capital-related components of the revenue requirement
- The projection of operations and maintenance expenses of the revenue requirements.

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<sup>79</sup> All cost components in the forecast equations in this section are in nominal dollar, unless explicitly stated otherwise.

The empirically derived forecasting algorithms discussed below are determined for each pipeline company.

### Projection of Rate Base and Cost of Capital

The approach for projecting rate base and capital costs is summarized in Table 8-4. Long-run marginal capital costs of pipeline companies are reflected in changes in the rate base. Once projected, the rate base is translated into capital-related components of the revenue requirements based on projections of the cost of capital, capitalization, and algorithms for depreciation and tax effects.

**Rate-Base Components.** The projected rate base in year  $t$  is computed as in the base year. That is, the rate base in year  $t$  is the net plant in service in year  $t$  plus working capital and transition expenses in year  $t$ .

$$PRB_t = GPIS_t - ADDA_{t-1} + CWC_t + OWC_t \quad (175)$$

where,

PRB = pipeline rate base before adjustment in dollars  
 GPIS = original capital cost of plant in service (gross plant in service) in dollars  
 ADDA = accumulated depletion, depreciation, and amortization in dollars  
 CWC = cash working capital in dollars  
 OWC = other working capital in dollars  
 $t$  = forecast year

The variables of the rate-base equation are forecast by the following set of equations. First, gross plant in service in the forecast year is determined by the prior year's gross plant in service, new capacity expansion (as determined by the Capacity Expansion Module), current capital additions to existing plants for replacement and refurbishment, and cost associated with new facilities for complying with Order 636. Gross plant in service is forecast as follows:

$$GPIS_t = \begin{matrix} GPIS_{t-1} + BLAE_t + PNEWFAC_t & \text{(existing pipe)} \\ GPIS_{t-1} + NCAE_t & \text{(generic pipe)} \end{matrix} \quad (176)$$

where,

GPIS = original capital cost of plant in service (gross plant in service) in dollars  
 NCAE = new capacity expansion expenditures allowed in rate base within the forecast year in dollars  
 BLAE = capital expenditures associated with base year capacity (refurbishment/replacement expenditures) in dollars  
 PNEWFAC = cost of new facilities required to comply with Order 636 (nominal dollars)<sup>80</sup>

Capital expenditures associated with base year capacity (refurbishment on existing pipeline/storage) are obtained by using three available options (BLAESWT = 0, 1, 2). The first option (used in AEO95) sets capital expenditures for pipeline refurbishment/replacement to zero. The second option sets refurbishment to be a proportion of the annual depreciation expense. The proportion is a function of the age of the plant. Option three allows the user to exogenously define total annual capital expenditures for refurbishment for the whole pipeline industry. The industry-wide expense is distributed to individual companies as a function of the gas plant in service. These options are defined as follows:

option 1 (BLAESWT=0):

$$BLAE_t = 0 \quad (177)$$

option 2 (BLAESWT=1):

<sup>80</sup>New facilities transition cost will be added to original capital cost of plant in service, on an individual pipeline basis. See Appendix E (A191YRS, ANUM191, AGSRCOSTS, SHARE\_GSR\_F, GSR\_YRS, NEWCOST\_PER) for default assumptions on costs and depreciation schedules.

**Table 8-4. Approach to Projection of Rate Base and Capital Costs**

Projection Component	Approach
<p><b>1. Rate Base</b></p> <p>a. Gross plant in service</p> <p>    I. Capacity expansion costs for generic pipeline/storage</p> <p>    II. Replacement/refurbishment costs for existing pipeline/storage</p> <p>b. Accumulated Depreciation, Depletion &amp; Amortization</p> <p>c. Cash and other working capital</p> <p>d. Transition expenses</p> <p>e. Accumulated deferred income taxes</p> <p>f. Depreciation, depletion, and amortization</p>	<p>Provided by the Capacity Expansion Module</p> <p>Accounting algorithm or user defined options</p> <p>Existing Pipelines: empirically estimated Generic Pipelines: accounting algorithm</p> <p>Empirically estimated</p> <p>Accounting algorithm with exogenous specification for recovery/absorption</p> <p>Existing Pipelines: empirically estimated Generic Pipelines: accounting algorithm</p> <p>Existing Pipelines: empirically estimated Generic Pipelines: accounting algorithm</p>
<p><b>2. Cost of Capital</b></p> <p>a. Long-term debt rate</p> <p>b. Preferred equity rate</p> <p>c. Common equity return</p>	<p>Base year average rate, adjusted using projected bond yields</p> <p>Base year rate (fixed)</p> <p>Incorporate changes in dividend/bond yields</p>
<p><b>3. Capital Structure</b></p>	<p>Held constant at base year values</p>

$$BLAE_t = DDA_t * ADDA_t / GPIS_{t-1} \quad (178)$$

where,

BLAE = capital expenditures associated with base year capacity (refurbishment/ replacement expenditures) in dollars

DDA = depreciation, depletion and amortization costs in dollars

ADDA = accumulated depreciation, depletion, and amortization in dollars

GPIS = original capital cost of plant in service (gross plant in service) in dollars

t = forecast year

option 3 (BLAESWT=2):

$$BLAE_t = BLAETOT * (GPIS_{t-1} / INDUSTRYGPIS_{t-1}) \quad (179)$$

where,

BLAE = capital expenditures associated with base year capacity (refurbishment/ replacement expenditures) in dollars

BLAETOT = user-defined total capital expenditure for refurbishment/replacement for the pipeline industry in dollars

GPIS = original capital cost of plant in service (gross plant in service) in dollars

INDUSTRYGPIS = total capital cost of plant in service (gross plant in service) for pipeline industry in dollars

t = forecast year

Accumulated depreciation, depletion, and amortization is given by:

$$ADDA_t = ADDA_{t-1} + DDA_t \quad (180)$$

where,

ADDA = accumulated depreciation, depletion, and amortization in dollars

DDA = depreciation, depletion, and amortization costs in dollars

A regression equation is used to define the annual depreciation, depletion, and amortization for existing pipelines, while an accounting algorithm is used for generic pipelines. For existing pipelines, this expense is forecast as follows:

$$DDA_t = (1-\rho)*\beta_0 + \beta_1*NETPLT_t + \beta_2*DEPSHR_t + \rho*DDA_{t-1} - \rho*(\beta_1*NETPLT_{t-1} + \beta_2*DEPSHR_{t-1}) \quad (181)$$

where,

DDA = depreciation, depletion, and amortization costs in dollars

$\beta_0, \beta_1, \beta_2$  = coefficients estimated based on an empirical study (Appendix F, Table F4)

$\rho$  = estimated auto-correlation coefficients (Appendix F, Table F4)

NETPLT = net capital cost of plant in service (dollars)

DEPSHR = ratio of accumulated depreciation, depletion, and amortization expenses to gross plant in service (a proxy for pipeline age)

A certain portion of the cost of new facilities required to comply with Order 636 can also be depreciated during the recovery period. Thus during this period, the depreciation, depletion, and amortization costs for existing pipeline are calculated as follows:

$$DDA_t = DDA_t + PNEWFAC/NEWCOST\_PER \quad (182)$$

where,

DDA = depreciation, depletion, and amortization costs in nominal dollars

PNEWFAC = cost of new facilities required to comply with Order 636 (nominal dollars)

NEWCOST\_PER = period allowing recovery of new facility costs (Appendix E)

The net plant in service and the proxy for pipeline age are defined as follows:

$$\begin{aligned} \text{NETPLT}_t &= \text{GPIS}_{t-1} - \text{ADDA}_{t-1} \\ \text{DEPSHR}_t &= \text{ADDA}_{t-1} / \text{GPIS}_{t-1} \end{aligned} \quad (183)$$

where,

GPIS = original capital cost of plant in service (gross plant in service) in dollars  
ADDA = accumulated depreciation, depletion, and amortization in dollars

The accounting algorithm used to define the annual depreciation, depletion, and amortization for generic pipelines assumes straight line depreciation over a 30 year life; as follows:

$$\text{DDA}_t = \sum_{s=1991}^t (\text{NCAE}_s / 30) \quad (184)$$

where,

DDA<sub>t</sub> = depreciation, depletion, and amortization costs in dollars  
NCAE<sub>s</sub> = new capacity expansion expenditures occurring in year s (in dollars)  
s = the year new expansion occurred  
30 = 30 years of plant life  
t = forecast year

Cash working capital is set equal to zero, because historically it has been at or near zero. Thus,

$$\text{CWC}_t = 0 \quad (185)$$

where,

CWC = cash working capital in dollars

Other working capital consists of material and supplies, gas held in storage, and other components that vary by company. Other working capital is calculated as a function of gross plant in service, as follows:

$$\begin{aligned} \text{OWC}_t &= \text{GPIS}_t^{\beta_0} * \text{GPIS}_{t-1}^{-\rho * \beta_0} * e^{[\beta_1 * (\text{MC\_PGDP}_t - \rho * \text{MC\_PGDP}_{t-1})]} * \\ &e^{[\beta_2 * (\text{TYEAR} - \rho * (\text{TYEAR} - 1.0))]} * \text{OWC}_{t-1}^{\rho} * \text{CONST} \end{aligned} \quad (186)$$

where,

OWC = other working capital in dollars  
GPIS = original capital cost of plant in service (gross plant in service) in dollars  
 $\beta_0$  = estimated coefficient on gross plant in service  
 $\rho$  = estimated auto correlation coefficient  
 $\beta_1$  = estimated coefficient on price level  
MC\_PGDP<sub>t</sub> = implicit GDP price deflator (from the Macroeconomic Activity Model)  
 $\beta_2$  = estimated coefficient on time trend  
TYEAR = year in Julian units (i.e., 1995)  
CONST = estimated constant term  
t = forecast year

[Note: See Table F4 in Appendix F for derivation of coefficients and regression statistics]

The rate base is adjusted for accumulated deferred income taxes and other expenses as follows:

$$\text{APRB}_t = \text{PRB}_t - \text{ADIT}_t + \text{TPEB} \quad (187)$$

where,

APRB = adjusted pipeline rate base in dollars  
 PRB = pipeline rate base before adjustment in dollars  
 ADIT = accumulated deferred income taxes in dollars  
 TPEB = transition expense balance in dollars  
 t = forecast year

Accumulated deferred income taxes depends on income tax regulations in effect, differences in tax and book depreciation, and the time vintage of past construction. The relationship established for the existing pipeline is different from the relationship for generic pipeline. The accumulated deferred income taxes for existing pipeline/storage is derived as follows:

$$ADIT_t = \beta_0 + \beta_1 * ADIT_{t-1} + \beta_2 * NETPLT_t \quad (188)$$

where,

$\beta_0, \beta_1, \beta_2$  = coefficients estimated based on empirical study (Appendix F, Table F4)  
 ADIT = accumulated deferred income taxes in dollars  
 NETPLT = difference between original capital cost of plant in service and accumulated depreciation in previous period (net plant in service) in dollars  
 t = forecast year

Accumulated deferred income taxes for generic companies is calculated using an accounting algorithm. It is assumed that for rate making purposes, straight line depreciation (SLD) is used. However, for tax purposes, modified accelerated cost recovery system (MACRS) with a 15 1/2 year schedule is used. ADIT is derived from the difference between two depreciation schedules and the tax rate. Selecting the formula used to calculate ADIT depends on the difference between two depreciation schedules and the book value of the asset (calculated using the MACRS depreciation schedule). The formulae are as follows:

$$\begin{aligned}
 ADIT_t = & \begin{cases} ADIT_{t-1} + (DEPRMACRS_t - DEPRSL_t) * FRATE & \text{if } DEPRMACRS > DEPRSL \\ ADIT_{t-1} & \text{if } DEPRMACRS < DEPRSL \text{ and } BOOKVL > 0 \\ ADIT_{t-1} - DEPRSL_t * FRATE & \text{if } BOOKVL = 0 \end{cases} \quad (189)
 \end{aligned}$$

where,

ADIT = accumulated deferred income taxes in dollars  
 DEPRMACRS = annual depreciation expense using MACRS  
 DEPRSL = annual depreciation expense using 30 year straight line schedule  
 FRATE = federal tax rate (Appendix F, Table F4)  
 BOOKVL = book value of plant, which is calculated using straight line depreciation schedule  
 t = forecast year

and,

$$\begin{aligned}
 DEPRMACRS_t &= \sum_{s=1991}^t NCAE_s * MACRS\_RATE_{t-s+1} \\
 DEPRSL_t &= \sum_{s=1991}^t NCAE_s / 30
 \end{aligned} \quad (190)$$

where,

NCAE = new capacity expansion expenditures occurring in year s (in dollars)  
 MACRS\_RATE = rate of depreciation by MACRS schedule (Appendix F, Table F4)  
 s = the year new expansion occurred  
 t = forecast year



**Cost of Capital.** The capital-related components of the revenue requirement depend upon the size of the rate base and the cost of capital to the pipeline company. In turn, the company cost of capital depends upon the rates of return on debt and equity and the amounts of debt and equity in the overall capitalization.

Company cost of capital consists of long-term debt, preferred stock, and common equity. The rate of return variables for debt and equity will be related to forecast macroeconomic variables. For existing pipeline, it is assumed that the long-term debt rate will vary as a function of the difference in the long-term debt rate and the yield on AA utility bonds (provided by the Macroeconomic Activity Model) in the base year, as follows:

$$\begin{aligned} \text{LTDR}_{i,t} &= \text{MC\_RMPUAANS}_t / 100.0 + \text{DLTDR}_{i,b} \\ &= \text{MC\_RMPUAANS}_t / 100.0 + (\text{LTDR}_{i,b} - \text{MC\_RMPUAANS}_b / 100.0) \end{aligned} \quad (191)$$

where,

$\text{LTDR}_{i,t}$  = long-term debt rate [Appendix E -- PLTDR, (fraction)]  
 $\text{MC\_RMPUAANS}_t$  = AA utility bond index rate provided by the Macroeconomic Activity Model (percentage)  
 $\text{DLTDR}_{i,b}$  = difference in the long term debt rate and the yield on AA utility bond for pipeline company i in base year  
*i* = pipeline company i  
*b* = base year  
*t* = forecast year

The rate of return on common equity for existing pipelines is considered to be a function of the long-term debt rate and the difference between the long-term debt rate and the rate of return on common equity in the base year. That is,

$$\begin{aligned} \text{CMER}_{i,t} &= \text{LTDR}_{i,t} + \text{DCMER}_{i,b} \\ &= \text{LTDR}_{i,t} + (\text{CMER}_{i,b} - \text{LTDR}_{i,b}) \end{aligned} \quad (192)$$

where,

$\text{CMER}_{i,t}$  = common equity rate of return [Appendix E -- PCMER, (fraction)]  
 $\text{LTDR}_{i,t}$  = long-term debt rate [Appendix E -- PLTDR, (fraction)]  
 $\text{DCMER}_{i,b}$  = the difference between rate of return on common equity and rate of return on long-term debt in base year  
*i* = pipeline company i  
*b* = base year  
*t* = forecast year

The rate of return on preferred stock for existing pipelines is also tied to the AA bond rate through the long term debt rate, as following:

$$\text{PFER}_{i,t} = \text{LTDR}_{i,t} + \text{DPFER}_{i,b} \quad (193)$$

where,

$\text{PFER}_{i,t}$  = rate of return for preferred stock [Appendix E -- PPFER, (fraction)]  
 $\text{LTDR}_{i,t}$  = long-term debt rate [Appendix E -- PLTDR, (fraction)]  
 $\text{DPFER}_{i,b}$  = the difference between rate of return on preferred stock and rate of return on long-term debt<sup>81</sup>  
*i* = pipeline company i  
*b* = base year  
*t* = forecast year

<sup>81</sup> The DPFER variable is assigned as 0.5% and kept constant for each pipeline throughout the entire forecast. This value represents analyst's judgement because attempts to derive it from historical data produced unrealistic results.

For generic pipelines, the rate of return on long term debt (LTDR) is defined as an industry average rate of return weighted by gross plant in service (GPIS) in the base year. In the forecast years, it is equal to the sum of the AA utility bond rate and a deviation constant calculated in the base year. The derivation is shown below:

$$\begin{aligned}
 LTDR_t &= \sum_i (LTDR_{i,t} * \frac{GPIS_{i,b}}{\sum_j GPIS_{j,b}}) \\
 &= \sum_i (MC\_RMPUAANS_t / 100.0 + DLTD_{i,b}) * \frac{GPIS_{i,b}}{\sum_j GPIS_{j,b}} \\
 &= MC\_RMPUAANS_t / 100.0 + \sum_i (DLTD_{i,b}) * \frac{GPIS_{i,b}}{\sum_j GPIS_{j,b}} \\
 &= MC\_RMPUAANS_t / 100.0 + GLTDR0
 \end{aligned} \tag{194}$$

where,

- LTDR<sub>t</sub> = industry average long-term debt rate for generic pipeline (fraction)
- LTDR<sub>i,t</sub> = long-term debt rate for existing pipeline company i [Appendix E -- PLTDR, (fraction)]
- MC\_RMPUAANS<sub>t</sub> = AA utility bond index rate provided by the Macroeconomic Activity Model (percentage)
- DLTD<sub>i,b</sub> = the difference between the long term debt rate and the yield on AA utility bond for pipeline company i
- GLTDR0 = deviation constant is the derived average difference between the rate of long term debt and the yield on AA utility bond in the base year
- GPIS<sub>i,t</sub> = original capital cost of plant in service (gross plant in service) in dollars
- i = existing pipeline company i
- b = base year
- t = forecast year

The rate of return on common equity (CMER) for generic pipelines is tied to the AA utility bond rate through the long-term debt rate (LTDR). CMER is equal to the sum of long term debt rate for generic pipeline and a deviation constant. The derivation is shown below:

$$\begin{aligned}
 CMER_t &= \sum_i (CMER_{i,t} * \frac{GPIS_{i,b}}{\sum_j GPIS_{j,b}}) \\
 &= \sum_i (LTDR_{i,t} + DCMER_{i,b}) * \frac{GPIS_{i,b}}{\sum_j GPIS_{j,b}} \\
 &= \sum_i (LTDR_{i,t} * \frac{GPIS_{i,b}}{\sum_j GPIS_{j,b}}) + \sum_i (DCMER_{i,b} * \frac{GPIS_{i,b}}{\sum_j GPIS_{j,b}}) \\
 &= LTDR_t + GCMER0
 \end{aligned} \tag{195}$$

where,

- CMER<sub>t</sub> = industry average common equity rate for generic pipeline (fraction)
- CMER<sub>i,t</sub> = rate of return on common equity for existing pipeline company i [Appendix E -- PCMER, (fraction)]
- LTDR<sub>t</sub> = industry average long-term debt rate for generic pipeline (fraction)
- LTDR<sub>i,t</sub> = long-term debt rate for existing pipeline company i [Appendix E -- PLTDR, (fraction)]
- DCMER<sub>i,b</sub> = the difference between rate of return on common equity and rate of return on long-term debt for pipeline company i in base year
- GCMER0 = deviation constant is the derived average difference between the rate of return on common equity and the yield on AA utility bond in base year
- GPIS<sub>i,t</sub> = original capital cost of plant in service (gross plant in service) in dollars
- i = pipeline company i
- b = base year

t = forecast year

Similarly, the rate of return on preferred stock (PFER) is equal to the sum of the long term debt rate for generic pipelines and a deviation constant. It can be derived as shown below:

$$\begin{aligned}
 PFER_t &= \sum_i (PFER_{i,t} * \frac{GPIS_{i,b}}{\sum_j GPIS_{j,b}}) \\
 &= \sum_i (LTDR_{i,t} + DPFER_{i,b}) * \frac{GPIS_{i,b}}{\sum_j GPIS_{j,b}} \\
 &= LTDR_t + \sum_i (DPFER_{i,b} * \frac{GPIS_{i,b}}{\sum_j GPIS_{j,b}}) \\
 &= LTDR_t + GPFER_0
 \end{aligned} \tag{196}$$

where,

- PFER<sub>t</sub> = average rate of preferred stock for generic pipelines (fraction)
- PFER<sub>i,t</sub> = rate of return for preferred stock for the existing pipeline company i [Appendix E -- PPFER, (fraction)]
- LTDR<sub>t</sub> = industry average long-term debt rate for generic pipeline (fraction)
- LTDR<sub>i,t</sub> = long-term debt rate for existing pipeline company i [Appendix E -- PLTDR, (fraction)]
- DPFER<sub>i,b</sub> = the difference between rate of return on preferred stock and rate of return on long-term debt for company i
- GPFER<sub>0</sub> = deviation constant is the derived average difference between the rate of return on preferred stock and the yield on AA utility bond in base year
- GPIS<sub>i,t</sub> = original capital cost of plant in service (gross plant in service) in dollars
- i = pipeline company i
- b = base year
- t = forecast year

For existing companies, the values of common stock, preferred stock and long term debt are assumed to be constant in real dollars; therefore, in nominal dollars these are increased by the inflation rate for the forecast period:

$$\begin{aligned}
 PFES_{i,t} &= PFES_{i,t-1} * GDPINFL_t \\
 CMES_{i,t} &= CMES_{i,t-1} * GDPINFL_t \\
 LTD_{i,t} &= LTD_{i,t-1} * GDPINFL_t
 \end{aligned} \tag{197}$$

where,

- PFES<sub>i,t</sub> = value of preferred stock in nominal dollars
- CMES<sub>i,t</sub> = value of common equity in nominal dollars
- LTD<sub>i,t</sub> = long-term debt in nominal dollars
- GDPINFL<sub>t</sub> = implicit GDP price inflator relative to previous year (from the Macroeconomic Activity Model)
- i = pipeline company i
- t = forecast year

The capital structure for generic pipelines are assumed constant. The three components of capital structure (GPFESTR, GCMESTR, and GLTDSTR) are defined as the average 1990 capital structure of the pipeline directly represented in the PTM (Appendix E -- PFES, CMES, LTD), and are used, along with the adjusted pipeline rate base, to determine the values of preferred stock, common stock, and long term debt:

$$\begin{aligned}
 PFES_t &= GPFESTR_t * APRB_t \\
 CMES_t &= GCMESTR_t * APRB_t \\
 LTD_t &= GLTDSTR_t * APRB_t
 \end{aligned}
 \tag{198}$$

where,

PFES = value of preferred stock in nominal dollars  
 CMES = value of common equity in nominal dollars  
 LTD = long-term debt in nominal dollars  
 GPFESTR = average historical ratio of preferred stock to total capital used as capital structure for generic pipeline (constant over forecast period)  
 GCMESTR = average historical ratio of common stock to total capital used as capital structure for generic pipeline (constant over forecast period)  
 GLTDSTR = average historical ratio of long term debt to total capital used as capital structure for generic pipeline (constant over forecast period)  
 APRB = adjusted pipeline rate base (dollars)  
 t = forecast year

Capital structure is the percent of total capitalization represented by each of the three capital components: long-term debt costs, preferred equity, and common equity. The proportions of total capitalization due to common stock, preferred stock, and long-term debt is considered fixed at the base-year values throughout the forecast. Assuming that the fractions of total capitalization remain the same over the forecast horizon,<sup>82</sup> the weighted average cost of capital in the forecast year is given by:

$$WAROR_t = [(PFER_t * PFES_t) + (CMER_t * CMES_t) + (LTDR_t * LTDS_t)] / TOTCAP_t \tag{199}$$

where,

WAROR = weighted-average before-tax rate of return on capital (fraction)  
 PFER = coupon rate for preferred stock (fraction)  
 PFES = value of preferred stock (dollars)  
 CMER = common equity rate of return (fraction)  
 CMES = value of common stock (dollars)  
 LTDR = long-term debt rate (fraction)  
 LTDS = value of long-term debt (dollars)  
 TOTCAP = sum of the value of long-term debt, preferred stock, and common stock equity [Equation 109 (dollars)]  
 t = forecast year

### Projection of Capital-Related Components of the Revenue Requirements

The approach to the projection of capital-related components of the revenue requirements is summarized in Table 8-5. Given the rate-base and capitalization projections discussed above, the components of revenue requirements are relatively straightforward to project. The capital-related components of the revenue requirements include total return; Federal and State tax credits; Federal and State income taxes; other taxes; and depreciation, depletion, and amortization costs. These cost components are projected as follows:

The total return is computed from the projected weighted cost of capital and estimated rate base, as follows:

<sup>82</sup>Changes in capital structure could be treated later as an enhancement to the PTM. This would involve consideration of, among other factors, sources and uses of funds, dividend payout policies, and regulatory caps on how much common equity is permitted in determining rates. It is not clear that this enhancement would offer large benefits to the forecast.

**Table 8-5. Approach to Projection of Revenue Requirements: Capital-Related Costs and Taxes**

Projection Component	Approach
1. Rate Base-related Components	
a. Total return	Direct calculation from projected rate base and rates of return
b. Federal/State tax credits	Held constant in real terms at base year values
c. Federal/State income taxes	Accounting algorithms based on tax rates
2. Other Taxes	Held constant in real terms at base year values

$$TRRB_t = WAROR_t * APRB_t \quad (200)$$

where,

$TRRB$  = total return on rate base (before taxes) in dollars  
 $WAROR$  = weighted-average-before-tax rate of return on capital (fraction)  
 $APRB$  = adjusted pipeline rate base in dollars  
 $t$  = forecast year

The return on rate base for existing companies is broken out into the three components as shown below.

$$PFEN_t = (PFES/TOTCAP_t) * PFER_t * APRB_t \quad (201)$$

$$CMEN_t = (CMES/TOTCAP_t) * CMER_t * APRB_t \quad (202)$$

$$LTDN_t = (LTDS/TOTCAP_t) * LTDR_t * APRB_t \quad (203)$$

where,

$PFEN$  = total return on preferred stock (dollars)  
 $PFES$  = value of preferred stock (dollars)  
 $TOTCAP$  = total capitalization (dollars)  
 $PFER$  = coupon rate for preferred stock (fraction)  
 $APRB$  = adjusted pipeline rate base (dollars)  
 $CMEN$  = total return on common stock equity (dollars)  
 $CMES$  = value of common stock equity (dollars)  
 $CMER$  = common equity rate of return (fraction)  
 $LTDN$  = total return on long-term debt (dollars)  
 $LTDS$  = value of long-term debt (dollars)  
 $LTDR$  = long-term debt rate (fraction)  
 $t$  = forecast year

For generic companies the capital structure is assumed to be constant over the forecast period. Therefore, the return on rate base for generic companies (new expansion portion of pipeline/storage) is defined using a simpler format:

$$PFEN_t = (GPFESTR) * PFER_t * APRB_t \quad (204)$$

$$CMEN_t = (GCEMSTR) * CEMR_t * APRB_t \quad (205)$$

$$LTDN_t = (GLTDSTR) * LTDR_t * APRB_t \quad (206)$$

where,

- PFEN = total return on preferred stock (dollars)
- CMEN = total return on common stock equity (dollars)
- LTDN = total return on long-term debt (dollars)
- GPFESTR = average historical ratio of preferred stock to total capital used as capital structure for generic pipeline (constant over forecast period)
- GCEMSTR = average historical ratio of common stock to total capital used as capital structure for generic pipeline (constant over forecast period)
- GLTDSTR = average historical ratio of long term debt to total capital used as capital structure for generic pipeline (constant over forecast period)
- PFER = coupon rate for preferred stock (fraction)
- CEMER = common equity rate of return (fraction)
- LTDR = long-term debt rate (fraction)
- APRB = adjusted pipeline rate base (dollars)
- t = forecast year

Total taxes consists of Federal income taxes, State income taxes, and other taxes at average rates, minus tax credits for Federal and State income taxes. Federal income taxes and State income taxes are calculated in the same manner as in the base year (Equations 113-117) using average tax rates. The equation for total taxes is as follows:

$$TOTAX_t = FSIT_t + OTTAX_t - FSITC_t \quad (207)$$

where,

- TOTAX = total Federal and State income tax liability (dollars)
- FSIT = Federal and State income tax (dollars)
- FSITC = Federal and State investment tax credits (dollars)
- OTTAX = all other taxes assessed by Federal, State, or local governments except income taxes (dollars)
- t = forecast year

Federal income tax credits are assumed to remain constant in real terms at the base year level throughout the forecast and therefore they are adjusted for inflation. Other taxes relate to a combination of ad valorem taxes (which grow with company revenue), property taxes (which grow in proportion to gross plant), and all other taxes (assumed constant in real terms). Other taxes are determined as a function of the previous year's level times the inflation rate from the previous year.

$$OTTAX_t = OTTAX_{t-1} * (MC\_PGDP_t / MC\_PGDP_{t-1}) \quad (208)$$

where,

- OTTAX = all other taxes assessed by Federal, State, or local governments except income taxes (dollars)
- MC\_PGDP = implicit GDP price deflator (from the Macroeconomic Activity Model)
- t = forecast year

### Projection of Normal Operating Expenses and Revenue Credits

The remaining projected components of the revenue requirements are normal operating expenses and revenue credits. Normal operating expenses are further disaggregated into depreciation, depletion, and amortization expenses, total taxes (previously estimated above), administrative and general expense, customer expenses, and total operations and

maintenance expenses. The approach to the projection of these line items is summarized in Table 8-6. The projected costs are based on long-run marginal cost relationships in the pipeline industry which relate cost incurrence to external measures of industry size or activity and which relate unit costs to measurable changes in factor costs, the level and nature of the service, and technology. In some cases costs are assumed to be held constant because of limited resources available to develop data and develop the empirical estimates.

The total cost of service for a forecast year is as follows:

$$TCOS_t = TRRB_t + TNOE_t - REVC_t \quad (209)$$

where,

TCOS = total cost-of-service (dollars)  
 TRRB = total return on rate base [before taxes (dollars)]  
 TNOE = total normal operating expenses (dollars)  
 REVC = revenue credits to cost-of-service (dollars)  
 t = forecast year

Revenue credits to cost-of-service is determined as a function of the previous year's level times the inflation rate from the previous year, as follows:

$$REVC_t = REVC_{t-1} * (MC\_PGDP_t / MC\_PGDP_{t-1}) \quad (210)$$

where,

REVC = revenue credits to cost-of-service (dollars)  
 MC\_PGDP = implicit GDP price deflator (from the Macroeconomic Activity Model)  
 t = forecast year

The revenue requirement consists of a just and reasonable return on the rate base plus normal operating expenses.

$$TRR_t = TRRB_t + TNOE_t \quad (211)$$

where,

TRR = total revenue requirement (dollars)  
 TRRB = total return on rate base [before taxes (dollars)]  
 TNOE = total normal operating expenses (dollars)  
 t = forecast year

The total normal operating expenses costs consist of the following components:

$$TNOE_t = DDA_t + TOTAX_t + TAG_t + TCE_t + TOM_t \quad (212)$$

where,

TNOE = total normal operating expenses (dollars)  
 TOTAX = total Federal and State income tax liability (dollars)  
 DDA = depreciation, depletion, and amortization costs (dollars)  
 TAG = total administrative and general expense (dollars)  
 TCE = total customer expense (dollars)  
 TOM = total operating and maintenance expense (dollars)  
 t = forecast year

A regression equation is used to define the annual depreciation, depletion, and amortization for existing pipelines, while an accounting algorithm is used for generic pipelines. For existing pipelines, this expense is forecast as follows:

**Table 8-6. Approach to Projection of Revenue Credits and Normal Operating Expenses**

Projection Component	Approach
1. Revenue Credits to Cost of Service	Held constant at base-year value adjusted for inflation
2. Depreciation, Depletion, and Amortization	Empirically estimated
3. Administrative & General - salaries, pension benefits, regulatory expenses, and other expenses	Empirically estimated
4. Customer Expense	Held constant at base-year value adjusted for inflation
5. Total Operating and Maintenance Expense	Empirically estimated

$$DDA_t = (1-\rho) \cdot \beta_0 + \beta_1 \cdot \text{NETPLT}_t + \beta_2 \cdot \text{DEPSHR}_t + \rho \cdot DDA_{t-1} - \rho \cdot (\beta_1 \cdot \text{NETPLT}_{t-1} + \beta_2 \cdot \text{DEPSHR}_{t-1}) \quad (213)$$

where,

$DDA$  = depreciation, depletion, and amortization costs in dollars  
 $\beta_0, \beta_1, \beta_2$  = coefficients estimated based on an empirical study (Appendix F, Table F4)  
 $\rho$  = estimated auto-correlation coefficients (Appendix F, Table F4)  
 $\text{NETPLT}$  = net capital cost of plant in service (dollars)  
 $\text{DEPSHR}$  = ratio of accumulated depreciation, depletion, and amortization expenses to gross plant in service (a proxy for pipeline age)

A certain portion of the cost of new facilities required to comply with Order 636 can also be depreciated during the recovery period. During this period, the depreciation, depletion, and amortization costs for existing pipeline are calculated as:

$$DDA_t = DDA_t + \text{PNEWFAC} / \text{NEWCOST\_PER} \quad (214)$$

where,

$DDA$  = depreciation, depletion, and amortization costs in nominal dollars  
 $\text{PNEWFAC}$  = cost of new facilities required to comply with Order 636 (nominal dollars)  
 $\text{NEWCOST\_PER}$  = period allowing recovery of new facility costs (Appendix E)

The net plant in service and the proxy for pipeline age are defined as follows:



$$\begin{aligned} \text{NETPLT}_t &= \text{GPIS}_{t-1} - \text{ADDA}_{t-1} \\ \text{DEPSHR}_t &= \text{ADDA}_{t-1} / \text{GPIS}_{t-1} \end{aligned} \quad (215)$$

where,

GPIS = original capital cost of plant in service (gross plant in service) in dollars  
ADDA = accumulated depreciation, depletion, and amortization in dollars

The accounting algorithm used to define the annual depreciation, depletion, and amortization for generic pipelines assumes straight line depreciation over a 30 year life, as follows:

$$\text{DDA}_t = \sum_{s=1991}^t (\text{NCAE}_s / 30) \quad (216)$$

where,

DDA<sub>t</sub> = depreciation, depletion, and amortization costs in dollars  
NCAE<sub>s</sub> = new capacity expansion expenditures occurring in year s (in dollars)  
s = the year new expansion occurred  
30 = 30 years of plant life  
t = forecast year

For projection purposes, total customer expense is a function of last year's level times the inflation rate from the previous year.

$$\text{TCE}_t = \text{TCE}_{t-1} * (\text{MC\_PGDP}_t / \text{MC\_PGDP}_{t-1}) \quad (217)$$

where,

TCE = total customer expense (dollars)  
MC\_PGDP = implicit GDP price deflator (from the Macroeconomic Activity Model)  
t = forecast year

Total administrative and general costs (TAG<sub>it</sub>) are determined using an estimated equation and an efficiency adjustment term. The efficiency adjustment term is included to incorporate the observation that the efficiency of the natural gas pipeline system has been dramatically improved as a result of the increase in competition associated with open access.<sup>83</sup> The estimated equation used for the unadjusted TAG (Appendix F, Table F4) is determined as a function of gross plant in service, labor and rental cost indices, and some pipeline specific variables, as defined below:

$$\text{TAG}_{it}^{(\text{unadj})} = e^{(\alpha_{1i} * \text{FD}_i + \alpha_{2i} * \text{TF}_{it})} * \text{GPIS}_{it-1}^{\beta_1} * W_t^{\beta_2} * \text{PK}_t^{(1-\beta_2)} \quad (218)$$

where,

TAG<sub>it</sub><sup>(unadj)</sup> = total administrative and general costs before adjusting for efficiency (1987 real dollars)  
FD<sub>i</sub> = pipeline specific dummy variable that represents pipeline specific unobserved effects (equals 1 if pipeline company i, 0 otherwise)  
TF<sub>it</sub> = pipeline specific open access variable  
= TRNSHR<sub>it</sub> \* FD<sub>i</sub>, where, TRNSHR<sub>it</sub> is industry average share of gas transported for others. [TRNSHR<sub>it</sub> equals historical average shares during 1990 to 1994 (source: FERC Form 2), and is assumed to be 1.0 after 1994]  
GPIS<sub>it-1</sub> = original capital cost of plant in service (gross plant in service at the beginning of the year) in dollars (used as a proxy for size of company i)  
W<sub>t</sub> = real labor cost index, all private sector  
= MC\_ECIWSP<sub>t</sub> / MC\_PGDP<sub>t</sub>, where MC\_ECIWSP<sub>t</sub> is labor cost index and MC\_PGDP<sub>t</sub> is GDP price index from Macroeconomic Activity Model  
PK<sub>t</sub> = rental of office space for corporations (RENTBLDG<sub>t</sub>)

<sup>83</sup>"Efficiency in the Natural Gas Industry," by Kevin Forbes, SAIC, January 31, 1995.

- $\alpha_{1,i}, \alpha_{2,i}$  = rental cost index times rate of return (source: DRI)
- $\beta_1, \beta_2$  = firm-specific coefficients estimated based on empirical study (Appendix F, Table F4)
- $\beta_1, \beta_2$  = coefficients estimated based on empirical study (Appendix F, Table F4)
- $i$  = pipeline company index
- $t$  = forecast year

Next, the estimated TAG equation is used to determine total administrative and general costs which include the efficiency adjustment ( $TAG_{i,t}^{(adj)}$ ). Similar methods are used for existing and generic pipelines to accomplish this. For both cases, the adjusted TAG equation is composed of two cost components: a discounted cost frontier and a discounted inefficiency measure. For generic pipelines, the inefficiency term is also multiplied by the GPIS (used as a proxy for size). The equations are presented below:

Existing pipeline:

$$TAG_{i,t}^{(adj)} = (1 - d_1)^{(t-1)} * TAG_{i,t}^{(frontier)} + (1 - d_2)^{(t-2)} * TAG\_IEFF\_E_{i,t} \quad (219)$$

where,

- $TAG_{i,t}^{(adj)}$  = total administrative and general costs with efficiency adjustment for existing pipeline  $i$  in year  $t$  (1987 real dollars)
- $TAG_{i,t}^{(frontier)}$  = cost frontier of total administrative and general costs for existing pipeline  $i$  in year  $t$  (1987 real dollars)
- $TAG\_IEFF\_E_{i,t}$  = TAG inefficiency measurement for existing pipeline  $i$  in year  $t$  (see Endnote 2)
- $d_1$  = discount rate of TAG cost frontier [Appendix E -- TAG\_DCLE\_CF, (fraction)]
- $d_2$  = discount rate of TAG inefficiency for existing pipeline [Appendix E -- TAG\_DCLE, (fraction)]
- $i$  = pipeline company index
- $t$  = forecast year

Generic pipeline:

$$TAG_{i,t}^{(adj)} = (1 - d_1)^{(t-1)} * TAG_{i,t}^{(frontier)} + (1 - d_2)^{(t-2)} * TAG\_IEFF\_G_{i,t} * GPIS_{i,t-1} \quad (220)$$

where,

- $TAG_{i,t}^{(adj)}$  = total administrative and general costs with efficiency adjustment for generic pipeline  $i$  in year  $t$  (1987 real dollars)
- $TAG_{i,t}^{(frontier)}$  = cost frontier of total administrative and general costs for generic pipeline  $i$  in year  $t$  (1987 real dollars)
- $TAG\_IEFF\_G_{i,t}$  = TAG unit inefficiency factor (e.g., inefficiency per GPIS) for generic pipeline  $i$  (calculated in base year and kept constant in forecast years, see Endnote 2)
- $GPIS_{i,t-1}$  = original capital cost of plant in service (gross plant in service at the beginning of the year) in dollars (used as a proxy for the size of company  $i$ )
- $d_1$  = discount rate of TAG cost frontier [Appendix E -- TAG\_DCLE\_CF, (fraction)]
- $d_2$  = discount rate of TAG inefficiency for generic pipeline [Appendix E -- TAG\_DCLG, (fraction)]
- $i$  = pipeline company index
- $t$  = forecast year

The cost frontier for total administrative and general costs ( $TAG_{i,t}^{(frontier)}$ ) is defined the same for both existing and generic pipelines: the coefficients and dummy variables of the most efficient pipeline company are substituted into the estimated equation ( $TAG_{i,t}^{(unadj)}$ ). This defines the least cost for a company with the same size. The inefficiency term, however, is defined differently. For existing pipeline, the inefficiency measurement ( $TAG\_IEFF\_E_{i,t}$ ) is defined as the difference between the unadjusted cost and the cost frontier (after discounting). Thus, the amount of inefficiency is calculated each year by subtracting the discounted cost frontier from the unadjusted costs. For generic pipelines, the inefficiency measurement term ( $TAG\_IEFF\_G_{i,t}$ ) is the product of a unit inefficiency factor times a discount rate. The unit inefficiency factor is defined as the inefficiency per GPIS (used as a proxy for the size of expansion). This factor is calculated as the difference between the unadjusted pipeline TAG costs and the frontier

TAG costs using the historical arc average data in the base year. The discount rate is applied to model the potential efficiency improvement in new generic pipelines.

Finally, the total administrative and general costs are converted to nominal dollars to be consistent with the convention used in this module.

$$TAG_{i,t} = TAG_{i,t}^{(adj)} * MC\_PGDP_t \quad (221)$$

where,

- $TAG_{i,t}$  = total administrative and general costs with efficiency adjustment for generic pipeline i in year t (nominal dollars)
- $TAG_{i,t}^{(adj)}$  = total administrative and general costs with efficiency adjustment for generic pipeline i in year t (1987 real dollars)
- $MC\_PGDP_t$  = implicit GDP price deflator (from the Macroeconomic Activity Model)
- $t$  = forecast year

As with the TAG calculations, the total operation and maintenance costs (TOM<sub>i</sub>) are determined using an estimated equation and an efficiency adjustment term. The estimated equation used for the unadjusted TOM (Appendix F, Table F4) is determined as a function of gross plant in service, labor and rental cost indices, and some pipeline specific variables, as defined below:

$$TOM_{i,t}^{(unadj)} = e^{(\alpha_{1i} * FD_i + \alpha_{2i} * TF_{i,t})} * GPIS_{i,t-1}^{\beta_1} * W_t^{\beta_2} * PK_t^{(1-\beta_2)} \quad (222)$$

where,

- $TOM_{i,t}^{(unadj)}$  = total operation and maintenance costs before adjusting for efficiency (1987 real dollars)
- $FD_i$  = pipeline specific dummy variable that represents pipeline specific unobserved effects (equals 1 if pipeline company i, 0 otherwise)
- $TF_{i,t}$  = pipeline specific open access variable
- $TF_{i,t}$  =  $TRNSHR_t * FD_i$ , where,  $TRNSHR_t$  is industry average share of gas transported for others. [ $TRNSHR_t$  equals historical average shares during 1990 to 1994 (source: FERC Form 2), and is assumed to be 1.0 after 1994]
- $GPIS_{i,t-1}$  = original capital cost of plant in service (gross plant in service at the beginning of the year) in dollars (used as a proxy for size of company i)
- $W_t$  = real labor cost index, all private sector
- $W_t$  =  $MC\_ECIWSP_t / MC\_PGDP_t$ , where  $MC\_ECIWSP_t$  is labor cost index and  $MC\_PGDP_t$  is GDP price index from Macroeconomic Activity Model
- $PK_t$  = the user cost of capital for compressor stations
- $\alpha_{1i}, \alpha_{2i}$  = firm-specific coefficients estimated based on empirical study (Appendix F, Table F4)
- $\beta_1, \beta_2$  = coefficients estimated based on empirical study (Appendix F, Table F4)
- $i$  = pipeline company index
- $t$  = forecast year

In the above equation, the user cost of capital for compressor stations is defined as the rental price of capital, represented as:

$$PK_t = (REALAA + PIPE\_DEPR - \frac{PIPE_t - PIPE_{t-1}}{PIPE_{t-1}}) * PIPE_t \quad (223)$$

where,

- $PK_t$  = the user cost of capital for compressor stations
- $PIPE\_DEPR$  = assumed depreciation rate on compressor station equipment (= 0.10 annually, from PTARIFF)

PIPE<sub>t</sub> = Producer price index for compressor station equipment [initial values of PIPE are 1.133 (index of 1990) and 1.184 (index of 1991)]<sup>84</sup>  
 REALAA = the real rate of AA utility bonds

Next, the estimated TOM equation is used to determine total operation and maintenance costs which include the efficiency adjustment (TOM<sub>i,t</sub><sup>(adj)</sup>). Similar methods are used for existing and generic pipelines to accomplish this. For both cases, the adjusted TOM equation is composed of two cost components: a discounted cost frontier and a discounted inefficiency measure. For generic pipelines, the inefficiency term is also multiplied by the GPIS (used as a proxy for size). The equations are presented below:

Existing pipeline:

$$TOM_{i,t}^{(adj)} = (1 - d_1)^{(t-1)} * TOM_{i,t}^{(frontier)} + (1 - d_2)^{(t-2)} * TOM\_IEFF\_E_{i,t} \quad (224)$$

where,

TOM<sub>i,t</sub><sup>(adj)</sup> = total operation and maintenance costs with efficiency adjustment for existing pipeline i in year t (1987 real dollars)  
 TOM<sub>i,t</sub><sup>(frontier)</sup> = cost frontier of total operation and maintenance costs for existing pipeline i in year t (1987 real dollars)  
 TOM\\_IEFF\\_E<sub>i,t</sub> = TOM inefficiency measurement for existing pipeline i in year t (see Endnote 2)  
 d<sub>1</sub> = discount rate of TOM cost frontier [Appendix E -- TOM\_DCLE\_CF, (fraction)]  
 d<sub>2</sub> = discount rate of TOM inefficiency for existing pipeline [Appendix E -- TOM\_DCLE, (fraction)]  
 i = pipeline company index  
 t = forecast year

Generic pipeline:

$$TOM_{i,t}^{(adj)} = (1 - d_1)^{(t-1)} * TOM_{i,t}^{(frontier)} + (1 - d_2)^{(t-2)} * TOM\_IEFF\_G_{i,t} * GPIS_{i,t-1} \quad (225)$$

where,

TOM<sub>i,t</sub><sup>(adj)</sup> = total operation and maintenance costs with efficiency adjustment for generic pipeline i in year t (1987 real dollar)  
 TOM<sub>i,t</sub><sup>(frontier)</sup> = cost frontier of total operation and maintenance costs for generic pipeline i in year t (1987 real dollars)  
 TOM\\_IEFF\\_G<sub>i</sub> = TOM unit inefficiency factor (e.g., inefficiency per GPIS) for generic pipeline i (calculated in base year and kept constant in forecast years, see Endnote 2)  
 GPIS<sub>i,t-1</sub> = original capital cost of plant in service (gross plant in service at the beginning of the year) in dollars (used as a proxy for size of company i)  
 d<sub>1</sub> = TOM\_DCLE\_CF: discount rate of TOM cost frontier [Appendix E -- TOM\_DCLE\_CF, (fraction)]  
 d<sub>2</sub> = discount rate of TOM inefficiency for generic pipeline [Appendix E -- TOM\_DCLG, (fraction)]  
 i = pipeline company index  
 t = forecast year

The cost frontier for total operating and maintenance costs (TOM<sub>i,t</sub><sup>(frontier)</sup>) is defined the same for both existing and generic pipelines: the coefficients and dummy variables of the most efficient pipeline company are substituted into the estimated equation (TOM<sub>i,t</sub><sup>(unadj)</sup>). This defines the least cost for a company with the same size. The inefficiency term, however, is defined differently. For existing pipeline, the inefficiency measurement (TOM\\_IEFF\\_E<sub>i,t</sub>) is defined as the difference between the unadjusted cost and the cost frontier (after discounting). Thus, the amount of inefficiency is calculated each year by subtracting the discounted cost frontier from the unadjusted costs. For generic pipelines, the inefficiency measurement term (TOM\\_IEFF\\_G<sub>i</sub>) is the product of a unit inefficiency factor times a discount rate. The unit inefficiency factor is defined as the inefficiency per GPIS (used as a proxy for the size of expansion). This factor is calculated as the difference between the unadjusted pipeline TAG costs and the frontier

<sup>84</sup>Source of historical data: Bureau of Labor Statistics (1987=1.00).

TAG costs using the historical arc average data in the base year. The discount rate is applied to model the potential efficiency improvement in new generic pipelines.

Finally, the total operation and maintenance costs are converted to nominal dollar to be consistent with the convention in this module.

$$TOM_{i,t} = TOM_{i,t}^{(adj)} * MC\_PGDP_t \quad (226)$$

where,

$TOM_{i,t}$  = total operation and maintenance costs with efficiency adjustment for generic pipeline i in year t (nominal dollars)

$TOM_{i,t}^{(adj)}$  = total operation and maintenance costs with efficiency adjustment for generic pipeline i in year t (1987 real dollar)

$MC\_PGDP$  = implicit GDP price deflator (from the Macroeconomic Activity Model)

$t$  = forecast year

### **Computation of Rates for Forecast Years**

Rates for the forecast years are computed using the procedures for the base-year initialization phase discussed above. These procedures include the following steps: (1) classify line items of the cost of service as fixed and variable costs, (2) allocate fixed and variable costs to rate component (reservation and usage fee, volumetric charge) based on the rate design, (3) aggregate costs to the network arc/network node, (4) for transportation services allocate costs to type of service (firm and interruptible), and (5) compute arc-specific (node-specific) rates. Estimation of pipeline costs for forecast years was presented in the previous section. Adjustment of the billing determinants in each year of the forecast is discussed below.

The method used to forecast billing determinants is consistent with (1) the assumptions used in the scenario definition, (2) the capacity factor/load factor assumptions, and (3) the incremental new capacity derived from the capacity expansion algorithm. Base-year peak-day billing determinants will not change throughout the forecast period for capacity in place in the base year. Rather, changes in billing determinants from capacity additions will be captured through arc-specific generic pipeline companies. Forecast pipeline and storage capacity requirements are determined by the Capacity Expansion Module. Incremental annual pipeline capacity and storage requirements and capital cost requirements by arc provided by the Capacity Expansion Module are assigned to arc-specific generic pipeline companies and storage facilities. Arc-specific adjustments to billing determinants are modeled through the addition to base-year volumes of incremental annual and peak service volumes for each generic pipeline company. Annual volume billing determinants will change based on throughput solved for in the Annual Flow Module in the previous year with an adjustment to include an estimate of throughput on incremental expansion in the current year assuming a load factor provided by the Capacity Expansion Module.

Billing determinants are determined, at the arc-level, by peak-day design delivery requirements, annual firm transportation volumes, annual interruptible transportation volumes, and the arc distances between regional nodes. Since regional growth in pipeline capacity is aggregated to the arc-level, arc distance between regional nodes remains constant throughout the forecast period. Consequently, changes in billing determinants are effected solely through changes in peak-day design and annual natural gas flows through each network arc during the forecast period.



## 9. Model Assumptions, Inputs, and Outputs

This last chapter summarizes the model and data assumptions used by the Natural Gas Transmission and Distribution Model (NGTDM) solution methodology and also presents the data inputs to and the outputs from the NGTDM.

### Assumptions

This section presents a brief summary of the assumptions used within the Natural Gas Transmission and Distribution Model (NGTDM). Generally, there are two types of data assumptions that affect the NGTDM solution values. The first type can be derived based on historical data (past events), and the second type is based on experience and/or events that are likely to occur (expert or analyst judgment). A discussion of the rationale behind assumed values based on analyst judgment is beyond the scope of this report. Information on the performance testing of the NGTDM through variation in key inputs to the model is provided in Volume II of this document (the Model Developer's Report, January 3, 1995), which discusses the model performance and results of sensitivity testing.<sup>85</sup> All FORTRAN variables related to model input assumptions, both those derived from known sources and those derived through analyst judgment, are identified in this chapter, with background information and actual values referenced in Appendix E.

The assumptions summarized in this section are referred to in Chapters 3 through 8. They are used in NGTDM equations as starting values, coefficients, factors, shares, bounds, or user specified parameters. Six general categories of data assumptions have been defined: classification of market services, demand, transmission and distribution service pricing, pipeline tariffs and associated regulation, pipeline capacity and utilization, and supply. These assumptions, along with their variable names, are summarized below.

#### Market Service Classification

Nonelectric sector natural gas customers are classified as either core or noncore customers, with core customers transporting their gas under firm (or near firm) transportation agreements and noncore customers transporting their gas under interruptible or short-term capacity release transportation agreements. The residential, commercial, and transportation (vehicles using compressed natural gas) sectors are assumed to be core customers. The transportation sector is further subdivided into fleet and personal vehicle customers. Industrial end users fall into both categories, with industrial boilers and refineries assumed to be noncore and all other industrial users assumed to be core.

Electric generator customers of natural gas are classified as either (1) core, (2) noncore, priced competitive with distillate fuel oil, or (3) noncore, priced competitive with residual fuel oil. The classification is based on the type of electric generation boiler. The electric generation units defining each of the three customer classes modeled are as follows: (1) core — gas steam units or gas combined cycle units, (2) noncore priced competitive-with-distillate — dual-fired turbine units or gas turbine units, (3) noncore priced competitive-with-residual fuel — dual-fired steam plants (consuming both natural gas and residual fuel oil).

#### Demand

The shares (*NG\_CENSHR*) for disaggregating nonelectric Census Division demands to NGTDM regions are held constant throughout the forecast period and are based on average historical relationships.

The Alaskan natural gas consumption levels for residential, commercial, and industrial sectors (Equations 12, 13, 14) are defined as a function of the exogenously specified number of customers and the landed costs of crude oil

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<sup>85</sup>Sensitivity testing was performed on the version of the model used to produce the AEO95. This document will not be updated to reflect the AEO96 version of the NGTDM.

in the current and previous forecast years (*Tables F1, F2*). Alaskan gas consumption is disaggregated into North and South Alaska in order to separately compute the natural gas production forecasts in these regions (Equations 15, 16). The value of gas consumption in South Alaska as a percent of total Alaskan gas consumption (*AK\_PCTSOUTH*) is based on average historical data. Similarly, the Alaskan lease fuel, plant fuel, and pipeline fuel consumption levels are calculated as historically based percentages of total dry production in Alaska (*AK\_PCTPLT*, *AK\_PCTPIP*, *AK\_PCTLSE*). To compute natural gas prices by end-use sector for Alaska, fixed markups derived from historical data (*AK\_RM*, *AK\_CM*, *AK\_EM*) are added to the average Alaskan natural gas wellhead price over the North and South regions (Equation 17). Historically based percentages and markups are held constant throughout the forecast period.

The lease fuel consumption in each NGTDM region is computed as an historically derived percentage of dry gas production (*PCTLSE\_SUPL*) in each NGTDM/OGSM region. These percentages are held constant throughout the forecast period.

Pipeline fuel use is derived using the efficiency factors associated with each arc in the NGTDM network. Exogenously specified shares are used to allocate fuel use along an interregional arc to its associated regions based on the relative pipeline mileage in a given region (*NG\_ARCSIZE*). These shares are held constant throughout the forecast period.

The NGTDM estimates ambient emissions from the pipeline fuel consumption.<sup>86</sup> These emissions are a function of pipeline fuel use and emissions coefficients (Equation 36). An average emission coefficient vector was derived for each emission type represented in NEMS, using coefficients for different types of compressors and the 1990 national composition of compressor capacity (e.g., 23 percent reciprocating engine and 77 percent gas turbines). Emission control technologies currently used in compressors and the national composition of the compressor capacity are assumed not to change over the forecast period. Thus, the emission factors (*EMISRAT*) are kept constant throughout the forecast period.

In the Capacity Expansion Module, peak and off-peak consumption levels are calculated as exogenously specified percentages of expected annual consumption levels. These exogenous peak and off-peak shares (*NON\_POSHR\_F*, *NON\_POSHR\_I*, *UTIL\_POSHR\_F*, *UTIL\_POSHR\_I*, *UTIL\_POSHR\_C*, *EXP\_PSHR*) by market type and sector are estimated based on historical monthly natural gas consumption and are held constant throughout the forecast period.

## Pricing of Distribution Services

End-use prices for residential, commercial, industrial, transportation, and electric generation customers are derived by adding markups to the regional hub price of natural gas. Each regional end-use markup consists of an intraregional tariff (determined by the PTM), an intrastate tariff (*INTRA\_TARF*, *INTRA\_TARI*), a distribution tariff (endogenously defined), and a citygate benchmark factor [endogenously defined based on historical citygate prices (*HCGPR\_F*, *HCGPR\_I*)]. Distributor tariffs are defined differently for the core and noncore markets. The distributor tariff algorithm for the core market (with the exception of the transportation sector) uses parameters such as technical efficiency (*TECHEFF*), cost sharing percentages (*DTM\_BETA*), bypass percentages (*I\_BYPASS*), and debt/equity shares (*WT\_DEBT*), all of which are exogenously defined. The algorithm also uses exogenously defined cost coefficients (*TCF\_COEFF*) which represent the relative contribution of an annual change in demands and economic parameters to annual change in costs. The fleet vehicle (FV) component of the core transportation sector defines distributor tariffs using exogenously defined historical data (*HPGFTRGR*, *HCGPR\_F*), a decline rate (*TRN\_DECL*), and state and federal taxes (*STAX*, *FTAX*), while the personal vehicle (PV) component defines distributor tariffs as a markup (*RETAIL\_COST*, *STAX*, *FTAX*) over the core industrial sector distributor tariff. Noncore distributor tariffs are determined using historical estimates (*HPGIINGR*, *HPGIELGR*, *HPGCELGR*, *HCGPR\_I*), and exogenously defined decline rates (*NONU\_DTARI\_DECL*, *UTILIR\_DECL*, *UTILID\_DECL*)<sup>87</sup>.

<sup>86</sup>The emissions levels calculated within the NGTDM are not the official values reported by the NEMS system that are calculated elsewhere.

<sup>87</sup>Currently set to zero.



## Pipeline Tariffs and Regulation

Firm transportation rates for interstate pipeline services (both between NGTDM regions and within a region) are calculated assuming that the costs of new pipeline capacity will be rolled into the existing rate base. However, the test for determining whether or not to build new capacity is done based on incremental rates. Core market transmission services remain subject to cost of service, rate of return regulation. Noncore transmission services are competitively priced with the price floor equal to the variable cost of delivering natural gas (generally compressor station fuel plus a few cents).

In the computation of natural gas pipeline transportation and storage rates, the Pipeline Tariff Module uses a set of data assumptions based on historical data or expert judgment. These include the following:

- Factors (*ARF, ARV, AFR, AFU, AVR, AVU*) to allocate each company's line item costs into the fixed and variable cost components of the reservation and usage fees (Equations 121 to 124, and Chapter 8 cross-reference in Appendix G)
- Capacity reservation shares (*PS*, currently assumed constant throughout the forecast) used to allocate costs to portions of the physical pipeline system
- Share of a pipeline company's storage capacity located in a region (*TNS*), used to allocate fixed and variable costs to network nodes (Equations 127, 128)
- Load factor, upper bound, and maximum allowable annual escalation rate for tariffs (*LFAC\_F, LFAC\_I, IEXPCT, MAXESC, BASERADJ, LIMITFIRM, LIMITINT, PTMDPCTFC*) and FERC Order 636 transition cost parameters (*SHARE\_GSR\_F, PNUM191, PGSR COSTS, PNEWFAC, PSTRADED*) needed for the derivation of pipeline tariffs for firm and interruptible transportation services (Equations 144 and 153) and storage tariffs (Equation 167)
- Capacity expansion cost parameters (*CCOST*) and pipe mileage (*MILES*) used to derive total capital costs to expand pipeline capacity (Equation 170) and storage capacity (Equation 173), respectively.
- Input coefficients (*TAG\_IEFFADJ, TOM\_IEFFADJ, TAG\_DCLE\_CF, TOM\_DCLE\_CF, TAG\_DCLE, TAG\_DCLG, TOM\_DCLE, TOM\_DCLG*) for efficiency components in the TAG and TOM calculations.

All interstate pipeline companies are assumed to have completed the switch from modified fixed variable (MFV) to straight fixed variable (SFV) rate design by January 1994 to comply with Federal Energy Regulatory Commission Order 636 rate design changes. Approved transition costs are assumed to be consistent with FERC's revised cost estimate as published by the General Accounting Office in "Natural Gas: Costs, Benefits, and Concerns Related to FERC Order 636, Final Report," November 1993. It is assumed that the Gas Supply Realignment costs are recovered over a 5-year period beginning in 1994. Furthermore, it is assumed that 90 percent of these costs are assigned to firm transportation markets and 10 percent are assigned to interruptible markets as stipulated in Order 636. Purchase Gas Adjustment Account Balance (Account 191) costs are assumed to be collected over a 2-year period, also beginning in 1994. These costs will be paid only by core customers.

With full implementation of FERC Order 636 and the increasing array of unbundled services being offered by pipelines, it is assumed that segmentation of the natural gas market will continue and ultimately lead to prices reflecting the marginal costs of providing service to diverse groups of end users. The methodology employed in solving for the market equilibrium within the natural gas market assumes that marginal costs are the basis for determining market clearing prices throughout the forecast period. The NGTDM uses the market clearing prices in developing the supply and end-use prices paid by noncore customers. The weighted average cost of gas is used in deriving the cost of natural gas supplies delivered to core customers.

## Pipeline Capacity and Utilization

The Annual Flow Module linear program formulation has been developed to minimize a supply and transportation cost objective function (Equation 23) subject to the following constraints: capacity utilization constraints (Equations 24-25), mass balance constraints (Equations 26-29), and bounds on model flow variables (Equations 31-35). The capacity utilization constraints for the firm market and total market along each interregional arc set the limits on the flows for the firm market and total market, respectively. These utilization levels represent the maximum fraction of the physical capacity on the pipeline that is expected to be used on an annual basis. A small portion (*WTHR\_XCAP*) of this capacity is assumed to be reserved in the event of severe weather. The minimum bounds on flows along transshipment arcs in the firm and interruptible networks (Equations 31-35) are set as percentages (*APCT\_MINF*, *APCT\_MINI*) of flows in the previous forecast year. These minimum flows help to generate some continuity in flow patterns from year to year. The model methodology assumes that pipeline and storage capacities are available 2 years from the decision to add new capacity.

In the CEM, it is assumed that pipelines and local distribution companies build and subscribe to a portfolio of pipeline and storage capacity to serve a colder-than-normal winter consumption levels. This is represented by building 5 to 15 percent (*WTHR\_FAC*) more pipeline capacity than is necessary to support normal winter loads (with lower percentages on arcs supplying areas with warmer winters).

The model represents net injections of natural gas into storage in the off-peak period and net withdrawals during the peak period. Annual net storage withdrawals equal zero in all forecast years (excluding historical years). The Capacity Expansion Module is constrained by an assumed maximum level of incremental storage capacity that can be built in each NGTDM region (*FACTOR*).

Several data assumptions are embedded in the mathematical specification of the linear program in the Capacity Expansion Module. The constraints on the arcs from each supply point during both the peak and off peak periods (*SUP\_PUTILZ*, *SUP\_OUTILZ*, *SUP\_PKSHR*, *EXP\_PSHR*) ensure that the production rates in a period do not exceed a plausible level. The formulation ensures that pipeline capacity is built primarily to satisfy firm peak demand. Exogenously specified seasonal maximum pipeline utilization rates (*ARC\_PUTILZ*, *ARC\_PFUTILZ*, *ARC\_OUTILZ*, *CAN\_UTIL\_MAX*, *CAN\_UTIL\_PF\_P*) are used to capture the variation in load patterns within a period. For Canadian import arcs, exogenously defined growth factors (*CAN\_UTIL\_GRW1*, *CAN\_UTIL\_GRW2*) allow the historically based utilization rates to change during the forecast years. Throughout the forecast years, firm and interruptible storage withdrawal levels are bounded above by the maximum storage levels determined from assumed storage utilization rates (*STR\_UTILZ*, *STR\_FUTILZ*), and below based on a declining percentage (*APCT\_MINF*) of historical levels.

The Capacity Expansion Module provides the Annual Flow Module and Pipeline Tariff Module with a forecast of working gas storage capacity, physical pipeline capacity, and maximum annual pipeline capacity utilization rates. The total available pipeline capacity in a given forecast year is calculated as last year's value plus planned expansions (*PNEW\_CAP*) and any additional expansion determined to be required within the model. Assumed maximum seasonal utilization rates (identified above) are used together with peak and off-peak flows within firm and interruptible markets to calculate the firm and total annual pipeline capacity utilization rates in the Capacity Expansion Module. The existing regional working gas capacity [including planned storage expansions (*BGSCT*, *BGSCNT*, *WGCT*, *WGCNT*, *PNEW\_STRX*)] is added to the determined level of storage expansion to obtain the regional working gas storage capacity levels.

## Supply

The supply curves for domestic dry gas production (Equation 11) incorporate assumed values of short-term price elasticity of supply (*PARM\_SUPCRV2*, *PARM\_SUPCRV3*) depending on the selected functional form. In addition, these supply curves are limited by minimum and maximum levels, calculated as a factor (*PARM\_MAXPR*, *PARM\_MINPR*) times the reserves times the expected production-to-reserves ratio.

Imports from Mexico and Canada at each border crossing point are represented as follows: (1) Mexican imports are assumed constant and provided by the Oil and Gas Supply Model; (2) Canadian imports are largely determined from

exogenously specified Canadian pipeline capacities (*CANCAP*) and exogenously defined maximum seasonal utilizations (*CAN\_UTILZ*, *CAN\_UTIL\_MAX*, *CAN\_UTIL\_GRW1*, *CAN\_UTIL\_GRW2*, *CAN\_UTIL\_PF\_P*). Total gas imports from Canada (Equation 4) exclude the amount of gas that travels into the United States and then back into Canada (*CANFLO\_IN*). Liquefied natural gas imports are provided by the Oil and Gas Supply Model.

Synthetic production of natural gas from coal (provided by the Coal Market Model) is also represented as a constant supply within the Annual Flow Module and the Capacity Expansion Module. However, synthetic gas production from liquid hydrocarbons in Illinois (Equation 2), which is defined within exogenously specified minimum and maximum production levels (*SNGMIN*), is represented as a function (Table F3) of the firm service market natural gas price in the East North Central Census Division. Synthetic gas production from liquid hydrocarbons in Hawaii is held constant throughout the forecast period at an assumed average historical production level (*SNGHI*). Finally, other supplemental supplies (*OSUP\_TOT*, *OSUP\_RSHR*) are held constant throughout the forecast in the Annual Flow Module and the Capacity Expansion Module.

A set of seasonal utilization parameters (*SUP\_PUTILZ*, *SUP\_OUTILZ*, *SUP\_PKSHR*, *EXP\_PSHR*) have been defined to split constant production levels into peak and off-peak categories, and to define seasonal splits for production from supply sources that are price responsive.

Discrepancies that exist between historical supply and disposition level data are modeled at historical levels (*NATL\_DISCR*) in the NGTDM and kept constant throughout the forecast years.

## Model Inputs

The NGTDM is a comprehensive framework which simulates the natural gas transmission and distribution industry in the United States as regulated (by the Federal Energy Regulatory Commission) for the pipeline transportation services across States (at the interstate level) and (by State Public Utility Commissions) for the local distribution services within States (at the intrastate level). The natural gas pipeline network (including storage) ties the suppliers to the end-users of natural gas, and captures the interactions among these institutions that ultimately determine market clearing prices and quantities consumed of natural gas. The NGTDM inputs are grouped into six categories: supply inputs, pipeline financial and regulatory inputs, pipeline capacity and utilization inputs, storage inputs, end-use pricing inputs, and demand inputs. Short input data descriptions and identification of variable names that provide more detail (via Appendix E) on the sources and transformation of the input data are provided below.

### Supply Inputs

- Supply curve parameters and historical/STEO data  
(*WPRLAGON*, *WPRLAGOF*, *OGWPRNG*, *STOGWPRNG*, *OGPRDNG*, *PRNG\_PADD*, *OGPRDNGON*, *OGPRDNGOF*, *WPRLAGON*, *WPRLAGOF*, *OSUP\_TOT*, *OSUP\_RSHR*, *PARM\_SUPCRV2*, *PARM\_SUPCRV3*, *PSHIFTON*, *PSHIFTOF*, *PSHIFT\_SCALE*, *SNGA1*, *SNGA2*)
- Historical/STEO production levels for supplemental natural gas supplies  
(*OGPRSUP3*, *STOGPRSUP*)
- Historical import levels and prices  
(*CN\_BRDPRC90*, *CN\_NEWCAP90*, *CNWELPRC89*, *OGCNPPRD*, *OGCNQPRD*, *OGQNGIMP*, *OGPNGIMP*, *CANFLO\_IN*, *CANFLO\_SHR*)
- Regional wellhead price benchmark variables  
(*STAR\_I*, *STAR\_F*, *STAROF\_I*, *STAROF\_F*)
- Alaskan lease, plant, and pipeline fuel parameters  
(*AK\_PCTPLT*, *AK\_PCTPIP*, *AK\_PCTLSE*)
- Minimum and maximum production-to-reserves ratios  
(*PARM\_MAXPR*, *PARM\_MINPR*)
- Seasonal supply shares  
(*SUP\_PUTILZ*, *SUP\_OUTILZ*, *SUP\_PKSHR*, *EXP\_PSHR*, *CANFLO\_PFSHR*)
- Seasonal wellhead price differentials  
(*PKPRCFAC*, *OPPRCFAC*)

- Maximum and minimum synthetic natural gas production and historical data  
(*CLSYNGWP, SNGMIN, SNGHI, SNG89 and Table F3*)
- Discrepancies between historical regional supply and disposition data  
(*TOTDISCR, NATL\_DISCR, STEO\_DISCR\_SHR*)

## **Pipeline Financial and Regulatory Inputs**

- Rate design specification  
(*ARF, AFR, AVR, ASF, ARV, AFU, AVU, ASV*)
- Pipeline rate base, cost, and volume parameters  
(*DDA, OTTAX, TAG, TCE, SEOM, CSOML, CSOMN, OTOM, CWC, OWC, ADIT, GPIS, ADDA, PFES, CMES, LTD, REVC, PCMER, PPFER, PLTDR, DCMER, DLTDR, AFM\_PTAR\_I, TRNSHR, RENTBLDG*)
- Revenue requirement forecasting equation parameters  
(*Table F4*)
- Revenue crediting parameters  
(*RCREDIT\_F, SCALE\_F\_MIN*)
- Order 636 transition cost parameters  
(*SHARE\_GSR\_F, PNUM191, PGSRCOSTS, PNEWFAC, PSTRANDED*)
- Rate of return set for generic pipeline companies  
(*PPFER, PCMER, PLTDR, DCMER, DLTDR*)
- Federal and State income tax rates  
(*FRATE, SRATE*)
- Parameters for interstate pipeline transportation rates  
(*LFAC\_F, LFAC\_I, IEXPCT, MAXESC, BASERADJ, LIMITFIRM, LIMITINT, PTMDPCTFC*)

## **Pipeline Capacity and Utilization Inputs**

- Seasonal transmission service utilization rates and minimum flows  
(*APCT\_MINF, APCT\_MINI, ARC\_PUTILZ, ARC\_PFUTILZ, ARC\_OUTILZ, BIARC\_PFSHR, BIARC\_PISHR, CAN\_UTILZ, CAN\_UTIL\_MAX, CAN\_UTIL\_GRW1, CAN\_UTIL\_GRW2, CAN\_UTIL\_PF\_P*)
- Initial firm and total pipeline flows and utilization rates  
(*AFLOW\_F, AFLOW\_I, AUTILZ\_F, AUTILZ\_T*)
- Existing pipeline capacity and planned capacity additions  
(*PCAP\_MAX, PNEW\_CAP*)
- Historical and planned Canadian import pipeline capacities  
(*CANCAP, CANEXP*)
- Costs of new construction  
(*CCOST, EXPFAC, CSTFAC, DELPR\_CAP*)
- Pipeline fuel usage parameters and historical/STEO data  
(*NEFF\_PIPE, UEFF\_PIPE, SEFF\_PIPE, AEFF\_PIPE, AEFF\_PIPE\_SCALE, MEKEFF, CANEFF, NG\_ARCSIZE, QGPTR, STQGPTR*)
- Factors related to planning for abnormal weather  
(*WTHR\_FAC, WTHR\_XCAP*)
- Distance and capacity commitments by network arc  
(*MILES, CONDEM*)
- Emissions factors  
(*EMISRAT*)
- Company volume shares by arc  
(*PS*)

## **Storage Inputs**

- Existing storage capacity and planned additions  
(*BGSCCT, BGSCNT, BASET, WGCT, WGCNT, WORKT, PNEW\_STRX*)
- Historical/STEO net storage withdrawals and core/noncore designation  
(*PKNETSTR, OPPNETSTR, PKSTFR\_F, OPPSTFR\_F, NNETWITH*)

- Seasonal utilization parameters  
(*STR\_UTILZ, STR\_FUTILZ*)
- Share of company storage capacity by region  
(*TNS*)
- Costs of storage additions  
(*CCOST, EXPFAC, CSTFAC, DELPR\_STR*)
- Maximum storage capacity potential by region  
(*FACTOR*)

## **End-Use Pricing Inputs**

- Cost coefficients and other parameters used in core distributor tariff algorithm  
(*TCF\_COEFF, I\_BYPASS, TECHEFF, DTM\_BETA, MINMU\_I, DTAR\_REFYR*)
- Distributor tariff decline rates used in noncore distributor tariff calculations  
(*NONU\_DTARI\_DECL*)
- Intrastate tariffs  
(*INTRA\_TARF, INTRA\_TARI*)
- State and Federal taxes, costs to dispense, and other compressed natural gas pricing parameters  
(*STAX, FTAX, RETAIL\_COST, TRN\_DECL*)
- Historical citygate prices  
(*HCGPR\_F, HCGPR\_I*)
- Historical/STEO end-use prices  
(*HPGTELGR, HPGFELGR, HPGIELGR, HPGCELGR, HPGFRS, HPGFCM, HPGFTR, HPGFIN, HPGIRS, HPGICM, HPGIIR, HPGIIN, HPGFRSGR, HPGFCMGR, HPGFINGR, HPGFTRGR, STPNGRS, STPNGCM, STPNGEL*)

## **Demand Inputs**

- Historical consumption in electric generation sector by core, competitive-with-residual fuel, and competitive-with-distillate categories  
(*QGFEELGR, QGCEELGR, QGIELGR*)
- Subregion gas consumption shares for Census Divisions 5, 8 and 9  
(*NG\_CENSHR*)
- Seasonal consumption shares  
(*NON\_POSHR\_F, NON\_POSHR\_I, UTIL\_POSHR\_F, UTIL\_POSHR\_I, UTIL\_POSHR\_C*)
- Historical export quantities and prices  
(*OGPNGEXP*)
- Alaskan consumption and pricing parameters  
(*WOP89, WPR89, AK\_RM, AK\_CM, AK\_EM, AK\_PCTSOUTH, AK\_C, AK\_D, AK\_E, AK\_F, AK\_G and Table F1*)
- Lease and plant fuel consumption parameters and historical/STEO data  
(*PCTLSE\_SUPL, LPTL\_SCALE, QLPIN, STQLPIN*)
- Short-term demand elasticities  
(*NONU\_ELAS\_F, NONU\_ELAS\_I*)

## **Model Outputs**

Once a set of solution values are determined within the NGTDM, those values required by other models of NEMS are passed accordingly. In addition, the NGTDM model results are presented in a series of internal and external reports, as outlined below.

## ***Outputs to NEMS Models***

The NGTDM passes its model solution values to different NEMS models as follows:

- Pipeline fuel consumption and lease and plant fuel consumption by Census Division (to NEMS PROPER)
- Natural gas wellhead prices by Oil and Gas Supply Model region (to NEMS REPORTS)
- Core and noncore natural gas prices by sector and Census Division (to NEMS PROPER)
- Dry natural gas production and supplemental gas supplies by Oil and Gas Supply Model region (NEMS REPORTS)
- Core and noncore (competitive with distillate and residual fuel oil) natural gas prices to electric generators by NGTDM/Electricity Market Model region (to Electricity Market Model)
- Dry natural gas production by Petroleum Administration for Defense Districts region (to Petroleum Market Model)
- Nonassociated dry natural gas production by NGTDM/Oil and Gas Supply Model region (to Oil and Gas Supply Model)
- Canadian natural gas wellhead price and production (to Oil and Gas Supply Model)
- Natural gas imports and prices by border crossing (to Oil and Gas Supply Model)
- Synthetic natural gas from coal supply price by NGTDM/Oil and Gas Supply Model region (to Coal Market Model)
- Capital expenditures for pipeline and storage expansion (Macroeconomic Model).

## ***Internal Reports***

The NGTDM produces reports designed to assist in the detailed analysis of NGTDM model results. These reports include the following information:

- Average natural gas wellhead price by NGTDM region
- Natural gas hub price at each transshipment node, by type of service
- Natural gas distributor tariffs and markups by end-use sector, type of service, and NGTDM region
- Matrices of data describing interregional transmission between NGTDM regions
  - Flows of natural gas by type of service
  - Maximum physical pipeline capacity
  - Maximum annual pipeline capacity utilization
  - Realized annual pipeline capacity utilization
- Peak period and off-peak period expected natural gas consumption levels by region and sector used in the Capacity Expansion Module

- Expected natural gas supply volumes as implied in the Capacity Expansion Module results, by Oil and Gas Supply Model region.
- Pipeline capacity expansion by arc
- Storage capacity expansion by region.

## ***External Reports***

In addition to the reports described above, the NGTDM produces external reports to support recurring publications. These reports contain the following information:

- Natural gas end-use prices and consumption levels by end-use sector, type of service (core and noncore), and Census Division (and for the United States)
- Natural gas wellhead prices and production levels by NGTDM region (and the average for the lower 48 United States)
- Natural gas end-use prices, margins, and revenues
- Natural gas import and export volumes and import prices
- Natural gas supply activity and prices by NGTDM region
- Pipeline fuel consumption by NGTDM region (and for the United States)
- Emissions of carbon dioxide, carbon monoxide, carbon, and methane emitted from the combustion of natural gas at pipeline compressor stations by NGTDM region (and for the United States)
- Natural gas pipeline capacity (entering and exiting a region) by NGTDM region and by Census Division
- Natural gas pipeline capacity utilization (entering and exiting a region) by NGTDM region and Census Division
- Natural gas transmission and distribution revenues, activity levels, and unit costs
- Natural gas underground storage and pipeline capacity by NGTDM region
- Unaccounted for natural gas<sup>88</sup>

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<sup>88</sup>Unaccounted for natural gas is a balancing item between the amount of natural gas consumed and the amount supplied. It includes reporting discrepancies, net storage withdrawals (in historical years), and differences due to convergence tolerance levels.





## **Appendix A**

### **NGTDM Model Abstract**



# NGTDM Model Abstract

**Model Name:** Natural Gas Transmission and Distribution Model

**Acronym:** NGTDM

**Title:** Natural Gas Transmission and Distribution Model

**Purpose:** The NGTDM is the component of the National Energy Modeling System (NEMS) that represents the mid-term natural gas market. The purpose of the NGTDM is to derive natural gas supply and end-use prices and flow patterns for movements of natural gas through the regional interstate network. The prices and flow patterns are derived by obtaining a market equilibrium across the three main components of the natural gas market: the supply component, the demand component, and the transmission and distribution network that links them.

**Status:** ACTIVE

**Use:** BASIC

**Sponsor:**

- Office: Integrated Analysis and Forecasting
- Division: Energy Supply and Conversion
- Branch: Oil and Gas Analysis, EI-823
- Model Contact: Jim Diemer
- Telephone: (202) 586-6126

**Documentation:** Energy Information Administration, *Model Documentation of the Natural Gas Transmission and Distribution Model (NGTDM) of the National Energy Modeling System (NEMS)*, DOE/EIA-M062 (Washington, DC, December 1995).

**Previous Documentation:** Energy Information Administration, *Model Documentation of the Natural Gas Transmission and Distribution Model (NGTDM) of the National Energy Modeling System (NEMS)*, DOE/EIA-M062 (Washington, DC, December 1993).

Energy Information Administration, *Model Documentation of the Natural Gas Transmission and Distribution Model (NGTDM) of the National Energy Modeling System (NEMS)*, DOE/EIA-M062 (Washington, DC, February 1995).

**Reviews Conducted:**

- Paul R. Carpenter, PhD, Incentives Research, Inc., "Review of the Component Design Report Natural Gas Annual Flow Module (AFM) for the Natural Gas Transmission and Distribution Model (NGTDM) of the National Energy Modeling System (NEMS)," Boston, MA, Aug 25, 1992
- Paul R. Carpenter, PhD, Incentives Research, Inc., "Review of the Component Design Report Capacity Expansion Module (CEM) for the Natural Gas Transmission and Distribution Model (NGTDM) of the National Energy Modeling System (NEMS)," Boston, MA, Apr 30, 1993
- Paul R. Carpenter, PhD, Incentives Research, Inc., "Review of the Component Design Report Pipeline Tariff Module (PTM) for the Natural Gas Transmission and Distribution Model (NGTDM) of the National Energy Modeling System (NEMS)," Boston, MA, Apr 30, 1993

- Paul R. Carpenter, PhD, Incentives Research, Inc., "Review of the *Component Design Report Distributor Tariff Module (DTM) for the Natural Gas Transmission and Distribution Model (NGTDM) of the National Energy Modeling System (NEMS)*," Boston, MA, Apr 30, 1993.
- Paul R. Carpenter, PhD, Incentives Research, Inc., "Final Review of the National Energy Modeling System (NEMS) Natural Gas Transmission and Distribution Model (NGTDM)," Boston, MA, Jan 4, 1995.

**Archive Tapes:** NEMS94—(Part of the National Energy Modeling System archive package as archived for the *Annual Energy Outlook 1994*, DOE/EIA-0383(94)).

NEMS95—(Part of the National Energy Modeling System archive package as archived for the *Annual Energy Outlook 1995*, DOE/EIA-0383(95)).

NEMS96—(Part of the National Energy Modeling System archive package as archived for the *Annual Energy Outlook 1996*, DOE/EIA-0383(96)).

**Energy System Covered:** The NGTDM models the U.S. natural gas transmission and distribution network that links the suppliers (including importers) and consumers of natural gas, and in so doing determines the regional market clearing natural gas end-use and supply (including border) prices.

- Coverage:**
- Geographic: Demand regions are the 12 NGTDM regions, which are based on the 9 Census Divisions with Census Division 5 split further into South Atlantic and Florida, Census Division 8 split further into Mountain and Arizona/New Mexico, and Census Division 9 split further into California and Pacific with Alaska and Hawaii handled separately.
  - Time Unit/Frequency: Annually through 2015
  - Product(s): Natural gas
  - Economic Sector(s): Residential, commercial, industrial, electric generators and transportation

- Data Input Sources:**  
(Non-DOE)
- National Oceanographic and Atmospheric Administration (NOAA)  
— Heating degree data
  - *The Potential for Natural Gas in the United States* (National Petroleum Council, December, 1992)  
— Pipeline capacity expansion cost estimates
  - Federal Offshore Statistics, OCS Report, MMS/0068  
— Offshore gas production and market values
  - Canadian Petroleum Association Statistical Summary  
— Canadian natural gas wellhead price and production
  - Alaska Department of Natural Resources  
— State of Alaska historical and projected oil and gas consumption.
  - Information Resources, Inc., "Octane Week"  
— State vehicle natural gas (VNG) taxes

**Data Input Sources: Forms and Publications:**  
**(DOE)**

- EIA-23, "Annual Survey of Domestic Oil and Gas Reserves"
  - Annual estimate of gas reserves by type and State
- EIA-176, "Annual Report of Natural and Supplemental Gas Supply and Disposition"
  - Annual natural gas sources of supply, consumption, and flows on the interstate pipeline network
- EIA-860, "Annual Electric Generator Report"
  - Electric generators plant type and code information, used in the classification of power plants as core or noncore customers. Data from this report are also used in the derivation of historical prices and markups for firm/interruptible service.
- EIA-767, "Steam-Electric Plant Operation and Design Report"
  - Electric generators plant type and boiler information, by month, used in the classification of power plants as core or noncore customers. Data from this report are also used in the derivation of historical prices and markups for firm/interruptible service
- EIA-759, "Monthly Power Plant Report"
  - Natural gas consumption by plant code and month, used in the classification of power plants as core or noncore customers. Data from this report are also used in the derivation of historical prices and markups for firm/interruptible service
- Rate case filings under Section 4 of the Natural Gas Policy Act, as submitted to FERC by each pipeline company
  - Contract demand data and cost allocation by pipeline company
- *Annual Energy Review*, DOE/EIA-0384
  - Gross domestic product and implicit price deflator
- FERC Form 2, "Annual Report of Major Natural Gas Companies"
  - Financial statistics of major interstate natural gas pipelines
  - Annual purchases/sales by pipeline (volume and price)
- FERC-567, "Annual Flow Diagram"
  - Pipeline capacity and flow information
- Federal Energy Regulatory Commission (FERC)
  - FERC Order 636 transition costs
- EIA-191, "Underground Gas Storage Report"
  - Base gas and working gas storage capacity and monthly storage injection and withdrawal levels by region and pipeline company
- EIA-846, "Manufacturing Energy Consumption Survey"
  - Base year average annual core industrial end-use prices
- *Capacity and Service on the Interstate Natural Gas Pipeline System 1990*, DOE/EIA-0556
  - Pipeline capacity and capacity reservations by customer.

- *Natural Gas Monthly*, DOE/EIA-0130
  - Base year historical quantity and price data

**Models and other:**

- National Energy Modeling System (NEMS)
  - Domestic supply, imports, and demand representations are provided as inputs to the NGTDM from other NEMS models
- Interstate Natural Gas Pipeline Data System (PIPENET)
  - Inter-regional pipeline capacity
  - Contract demand data.

**General Output  
Descriptions:**

- Average natural gas end-use prices and consumptions levels by sector and region
- Average natural gas supply prices and production levels by region
- Compressor station emissions of C, CO, CO<sub>2</sub>, CH<sub>4</sub>, and VOC reported as carbon by region
- Pipeline fuel consumption by region
- Pipeline capacity additions and utilization levels by region
- Capital investment in pipeline construction.

**Related Models:** NEMS (part of)

**Part of Another Model:** Yes, the National Energy Modeling System (NEMS).

**Model Features:**

- Model Structure: Modular; four major components: the Annual Flow Module (AFM), the Capacity Expansion Module (CEM), the Pipeline Tariff Module (PTM), and the Distributor Tariff Module (DTM)
  - AFM Integrating module of the NGTDM. Simulates the natural gas price determination process by bringing together all major economic and technological factors that influence regional natural gas trade in the United States
  - CEM Develops pipeline and storage facilities capacity and capacity expansion plans, and establishes effective maximum utilization rates for each pipeline route based on a seasonal analysis of supply and demand capability
  - PTM Develops firm/interruptible tariffs for transportation and storage services provided by interstate pipeline companies
  - DTM Develops markups for distribution services provided by LDC's and intrastate pipeline companies.
- Modeling Technique:
  - AFM Linear program
  - CEM Linear program
  - PTM Accounting algorithm
  - DTM Empirical process

- **Special Features:**

- Represents interregional flows of gas and pipeline capacity constraints
- Represents regional supplies
- Represents different types of transmission service (firm and interruptible)
- Calculates emissions associated with pipeline fuel use
- Determines the amount and the location of pipeline and storage facility capacity expansion on a regional basis
- Captures the economic tradeoffs between pipeline capacity additions and increases in regional storage capability
- Provides a peak/off-peak, or seasonal analysis capability in the area of capacity expansion
- Quantifies capital investment in capacity expansion
- Distinguishes end-use customers by type (core and noncore).

**Model Interfaces:** NEMS

**Computing**

**Environment:**

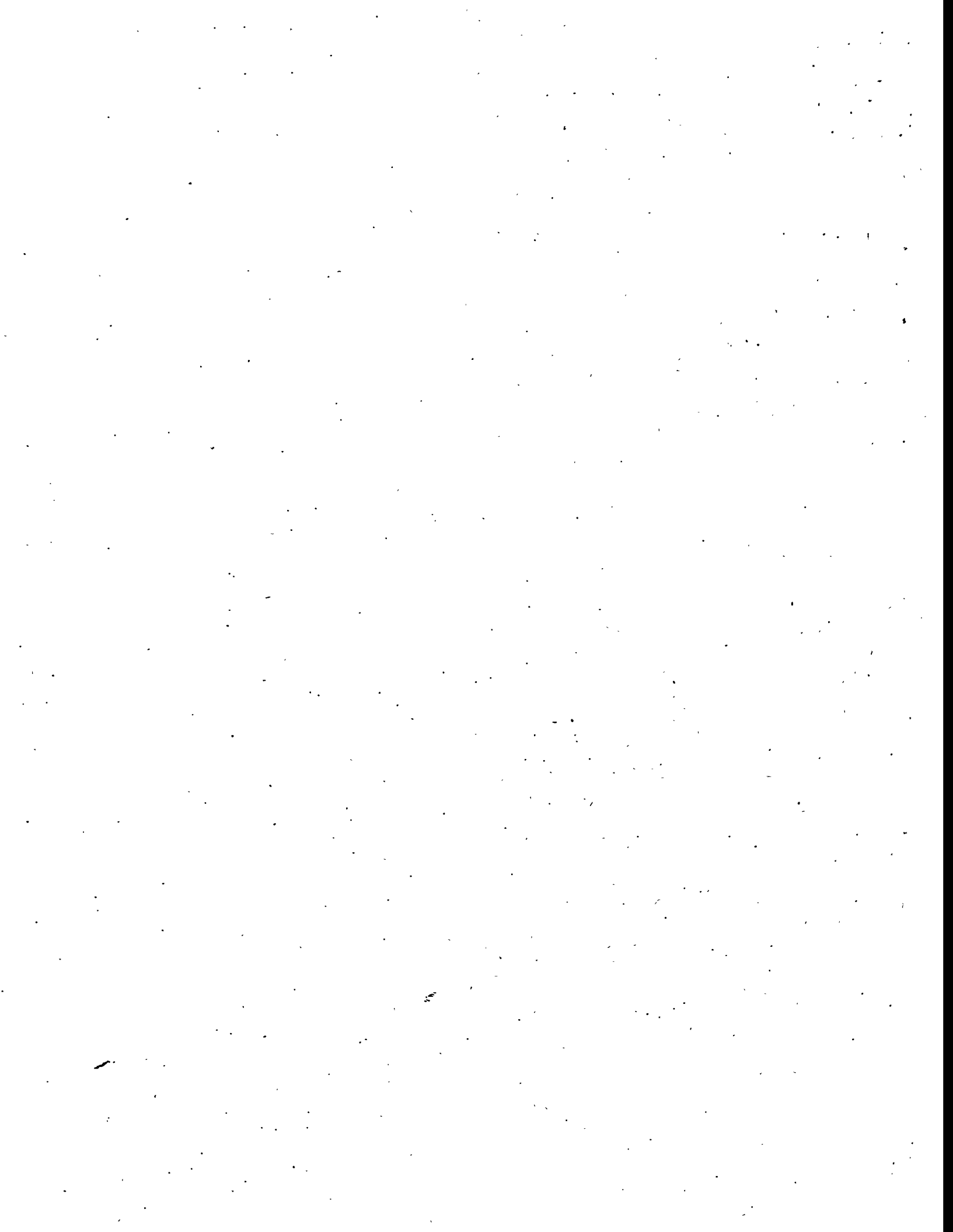
- Hardware Used: RS/6000
- Operating System: UNIX
- Language/Software Used: FORTRAN
- Memory Requirement: unknown
- Storage Requirement: 444K bytes for input data storage; 1162K bytes for source code storage; and 9000K bytes for compiled code storage
- Estimated Run Time:
  - for CEM 2.7 CPU seconds per forecast year
  - for AFM 1.0 CPU seconds per forecast year in 1st iteration  
0.6 CPU seconds per forecast year in subsequent iterations
- Special Features: NGTDM uses a proprietary software package, Optimization and Modeling Library (OML) distributed by the Ketron Management Science Division of the Bionetics Corporation. This is a specially designed linear programming interface that is callable from FORTRAN.

**Status of**

**Evaluation Efforts:**

Model developer's report entitled "Natural Gas Transmission and Distribution Model, Model Developer's Report for the National Energy Modeling System", dated November 14, 1994.

**Date of Last Update:** September 1995.





## **Appendix B**

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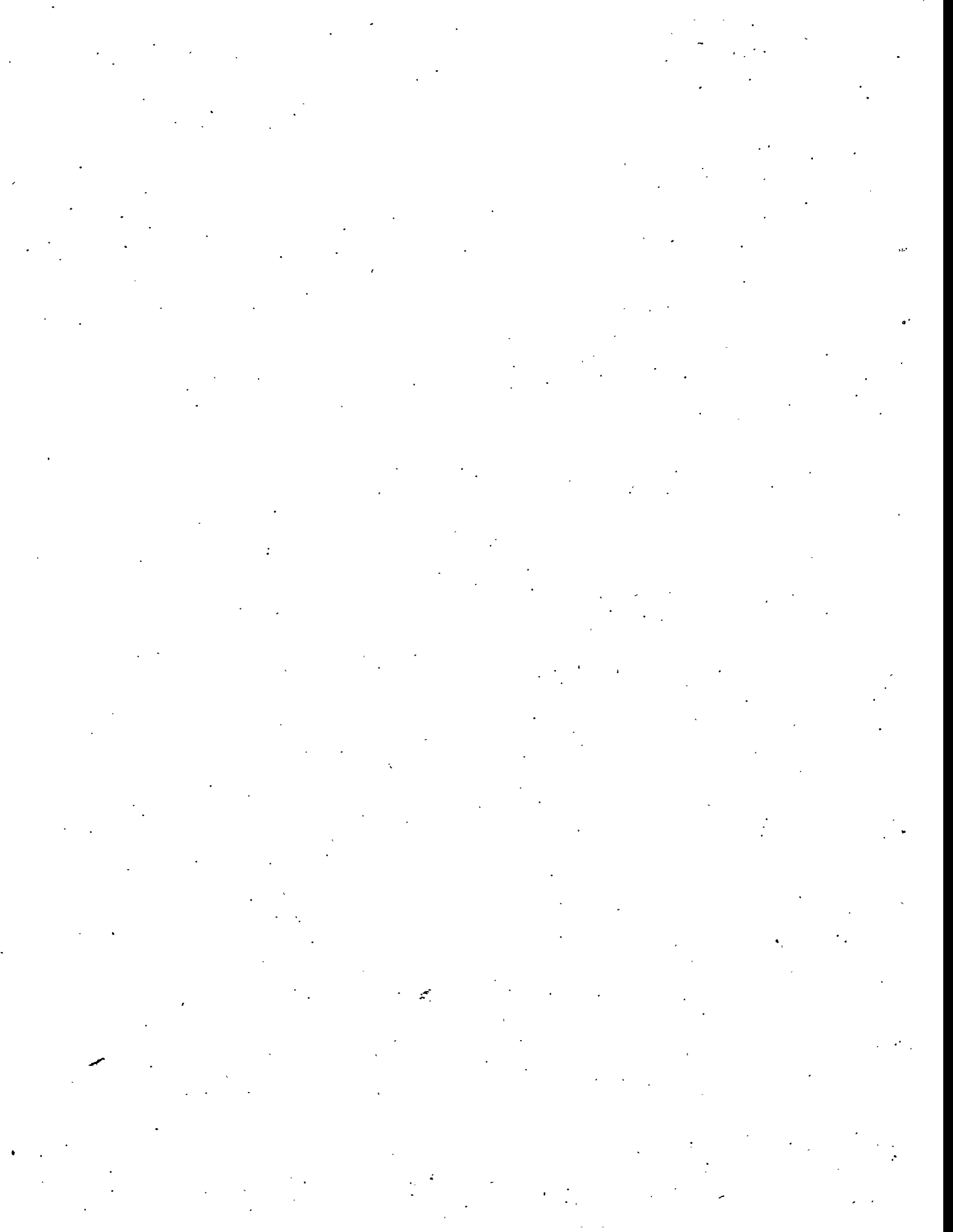
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## **Appendix C**

# **NEMS Model Documentation Reports**





# NEMS Model Documentation Reports

The National Energy Modeling System is documented in a series of 15 model documentation reports, most of which are updated on an annual basis. Copies of these reports are available by contacting the National Energy Information Center, 202/586-8800.

Energy Information Administration, *National Energy Modeling System Integrating Module Documentation Report*, DOE/EIA-M057.

Energy Information Administration, *Model Documentation Report: Macroeconomic Activity Module of the National Energy Modeling System*.

Energy Information Administration, *Documentation of the D.R.I. Model of the U.S. Economy*.

Energy Information Administration, *National Energy Modeling System International Energy Model Documentation Report*.

Energy Information Administration, *World Oil Refining, Logistics, and Demand Model Documentation Report*.

Energy Information Administration, *Model Documentation Report: Residential Sector Demand Module of the National Energy Modeling System*.

Energy Information Administration, *Model Documentation Report: Commercial Sector Demand Module of the National Energy Modeling System*.

Energy Information Administration, *Model Documentation Report: Industrial Sector Demand Module of the National Energy Modeling System*.

Energy Information Administration, *Model Documentation Report: Transportation Sector Demand Module of the National Energy Modeling System*.

Energy Information Administration, *Documentation of the Electricity Market Module*.

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Energy Information Administration, *Model Documentation: Coal Market Module*.

Energy Information Administration, *Model Documentation Report: Renewable Fuels Module*.



## **Appendix D**

# **Alternative Modeling Approaches**



# Alternative Modeling Approaches

During the design phase of the NGTDM, a survey was conducted of models and modeling approaches being used throughout the industry to analyze and forecast natural gas transmission and distribution activities. These approaches, along with other general modeling approaches, were considered as possible candidates for the NGTDM design. This appendix provides an overview of the methods and modeling techniques considered. First, the modeling techniques employed in several different natural gas transmission and distribution models are reviewed. Second, modeling approaches used in models not specifically designed for natural gas transmission and distribution, but which could be applied to this area, are discussed. Finally, conclusions based on the research and comparisons between other models and the methodology selected for the NGTDM are presented.

## Other Natural Gas Transmission and Distribution Models

The natural gas transmission and distribution industry is a segment of the complex natural gas production/delivery/demand system, and therefore is usually modeled as part of a larger, overall modeling system. Because the market structure of the transmission and distribution industry is rapidly evolving, most representations developed in the past are no longer adequate. Several of the models reviewed have detailed supply and demand representations, with fairly simple mechanisms for linking the two. Others have incorporated mechanisms for dealing with such issues as capacity expansion and the unbundling of transportation services, but none offers a comprehensive modeling treatment of the transmission and distribution industry as a whole. Additionally, none of the models reviewed addresses the issue of the environmental impacts associated with the transmission and distribution of natural gas. It was ultimately decided that there were no models in existence that could be used either intact or as a base to begin with and modify for the development of the NGTDM. Although it would have been very difficult to develop a model that addresses all of the regulatory issues and complexities of the industry, the design of the NGTDM considered desirable features of all the modeling approaches reviewed, and the resultant model provides a more comprehensive analysis tool than any other models available. This section provides an overview of the other natural gas models that were considered.

### ***Gas Analysis Modeling System (GAMS)<sup>89</sup>***

EIA's previous model of the natural gas market is the Gas Analysis Modeling System (GAMS), a computer-based partial equilibrium model used to analyze the U.S. natural gas production/delivery/demand system. GAMS produces annual forecasts through 2010 of natural gas production, consumption, and prices. GAMS interacts with a separate supply component which represents the various available sources of natural gas supplies and separate demand components that represent natural gas consumption by end-use sector and Federal region. GAMS consists of a mechanism for representing the costs and losses associated with the transmission and distribution of natural gas and an iterative equilibration process that solves the entire system to determine the wellhead and end-use prices at which an overall supply/demand balance can be achieved. Although the model can be run in a stand-alone mode, it is primarily used as the natural gas module within the Intermediate Future Forecasting System (IFFS),<sup>90</sup> a modeling system representing the supply and demand response within all the primary U.S. energy markets. The GAMS demand representation is provided through IFFS by the Demand Modeling System (DEMS), for the non-electric generators demand sectors, and by the Electricity Market Model (EMM) for the electric generators sector. The representation of onshore Lower-48 natural gas production is provided through direct linkage with the Production

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<sup>89</sup>For complete documentation of GAMS, see Energy Information Administration, *Documentation of the Gas Analysis Modeling System*, DOE/EIA-M044(92) (Washington, DC, December 1991).

<sup>90</sup>For more information on IFFS, see Energy Information Administration, *Documentation of the Integrating Module of the Intermediate Future Forecasting System*, DOE/EIA-M023(91) (Washington, DC, May 1991).

of Onshore Lower-48 Oil and Gas Model (PROLOG).<sup>91</sup> Supply estimates for other sources of gas are either set exogenously or determined endogenously via additional supply submodules.

GAMS was developed in 1982 and 1983 when the complex system of price ceilings in effect under the Natural Gas Policy Act (NGPA) of 1978 covered both interstate and intrastate wellhead purchases of natural gas. The categorization of gas under the NGPA and the contractual nature of the natural gas market that existed at the time were primary factors in the early structure of the model. The laws and regulations concerning the natural gas market have changed rapidly in support of deregulation and increased competitiveness (for a detailed discussion on industry background, see Appendix C). The GAMS model has subsequently undergone a number of methodological changes, to represent the active spot market, the deregulation of wellhead gas prices, and the increase in competitive pressures throughout the industry.

In the original version of GAMS, a detailed pipeline network consisting of 17 pipeline systems was used to reconcile supply and demand in the market equilibration process. This network represented sales of gas from the wellhead, through pipelines, to distributors, and to end-users. Physical movement of gas through the system was not tracked, and pipeline capacities were not accounted for. Reserves were dedicated to the individual pipeline systems and drawn down, as produced, through an elaborate accounting mechanism that tracked gas by NGPA category and contract terms and conditions. The sales structure allowed for analysis of alternative wellhead contract pricing schemes and their effect on the natural gas market. In order to represent both the increased spot market activity and the growing competition within the marketplace, GAMS was subsequently modified to include a pool of spot or decontrolled gas available to all pipelines. Reserves were no longer treated as dedicated to individual pipelines. GAMS was also revised to reflect changes in producer contracts, with contracts treated as respondent to market conditions and new contracts excluding take-or-pay<sup>92</sup> restrictions.

As a result of increased competition and the unbundling of pipeline sales and transportation services, the cost-of-service representation of bundled rates originally used to represent tariffs within GAMS was no longer representative of the market. The tariff component in GAMS was replaced with a simple mechanism that calculates end-use prices by adding exogenously determined regional transmission and end-use distribution costs (which are fixed throughout the forecast) to the national average wellhead price. Competition was represented by allowing these costs to be discounted in the industrial and electric generators sectors. As pricing distinctions responsive to market conditions between different levels of transmission and distribution service developed, the different levels of service were represented by expanding the level of electric generators sector detail. The electricity market module (EMM) provides demand curves to GAMS in the form of step functions defined by a set of price/quantity pairs. The steps on the curves simulate the effect of large-scale fuel switching and changes in the plant dispatching order by electric utilities. To model the price variation associated with different levels of service, these demand curves were redefined to represent three categories of electric generator plant types as follows: (1) core customers assumed to purchase firm service and pay the highest rates, (2) noncore customers assumed to purchase interruptible service and pay lower rates, and (3) customers with fuel switching capabilities sometimes offered discounted rates based on competing fuel prices. In contrast to the detailed electric generators demand representation, each regional demand curve provided to GAMS by DEMS for the non-electric generators sectors is defined simply by a unique reference price/quantity pair and an associated elasticity.

Transmission/distribution losses and pipeline fuel use are taken into account within GAMS during the supply/demand equilibration process by applying factors based on historical data to total throughput. The equilibrating process includes the following steps: (1) estimating a national wellhead price (the initial estimate is the previous year's solution price, and subsequent estimates are based on the previous iteration's price), (2) adding appropriate markups (representing transmission and distribution tariffs) to arrive at regional/sectoral end-use prices, (3) evaluating end-use consumption levels at these prices using the appropriate demand curves, (4) summing these consumption levels and adding losses to arrive at the amount which would be demanded at the wellhead given the estimated wellhead price, and (5) comparing this aggregate consumption (plus losses) to the level (provided by PROLOG) that would be supplied given the estimated wellhead price. If the calculated consumption is not within a specified tolerance of the

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<sup>91</sup>For more information on PROLOG, see Energy Information Administration, "Model Methodology and Data Description of the Production of Onshore Lower-48 Oil and Gas Model," DOE/EIA-M034(91) (Washington, DC, April 1991).

<sup>92</sup>Take-or-pay contract restrictions required a pipeline to pay for the specified quantity of gas whether or not it could be resold.

corresponding supply level, a new wellhead price is estimated and the process is repeated until convergence is achieved.

### ***Data Resources, Inc. (DRI)<sup>93</sup>***

The DRI natural gas market analysis is done in conjunction with an overall analysis of the entire U.S. energy sector. The principal models used are short-term natural gas spot price and demand models, a longer term U.S. and regional energy model (which has detailed sectoral demand submodels), and a U.S. oil and gas drilling/production model. Annual forecasts through 2010 are provided for 11 regions based on Census regions and subdivisions of Census regions.

The DRI modeling system uses an iterative process (based on achieving a wellhead price/residual fuel oil price ratio that is deemed to reflect accurately free-market supply/demand influences) which determines average regional wellhead gas acquisition prices and then applies region- and sector-specific markups to arrive at end-use prices. Average natural gas prices are projected for U.S. domestic wellhead gas (based on spot, contract, and regulation-influenced gas prices) and for Canadian and LNG imports. These prices are then combined into regional "acquisition" prices, based on the varying volume weights of each gas source in the region. Region- and sector-specific markups are then applied to each region's average acquisition cost to arrive at each sector's end-use price for the region. The markups are intended to capture the transmission, distribution, and other delivery costs for each sector in each region. The markups are based on historical EIA data. Thus interstate pipeline transmission rates are not separately and specifically estimated, but rather, are rolled in with local distribution and other charges into the overall retail markups. Growth in price markups is assumed to increase at the rate of inflation, as determined by the GNP deflator. Pipeline capacity constraints and capacity expansion issues are not addressed in the model.

### ***Wharton Econometric Forecasting Associates (WEFA)<sup>94</sup>***

WEFA models the transmission/distribution of natural gas by means of a supply/transportation model within its Natural Gas Modeling System. The North American natural gas market is defined as a collection of many markets (16 hubs) which trade gas both intra-regionally (within hubs) and inter-regionally (between hubs). Markets may be defined geographically, by type of transaction (spot or contract), by quality of service (interruptible or firm), and by season (heating or nonheating). The model is implemented as a spreadsheet that determines the production and consumption in each market and the volume of gas transported between markets and between seasons (storage), using a heuristic algorithm to solve iteratively for a set of prices across regions, seasons, and time periods that achieves a market balance. Annual forecasts are provided through 2020 for natural gas production and wellhead prices in 13 domestic supply basins, and for flows, capacity utilization, transportation costs, and required capacity expansion along the arcs connecting the 16 hubs.

Three key assumptions are made as follows:

- Producers maximize profits and consumers minimize costs, subject to demand requirements and capacity constraints
- Pipeline transportation and storage rates are a function of regulation, and capacity expansion only takes place if it is economic (i.e., if the marginal cost of expansion is less than the marginal price that consumers are willing to pay for the additional gas)

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<sup>93</sup>The most current documentation on DRI's model was written in 1984 and is out of date. A brief report entitled "Natural Gas Forecasting Methodology" provided by Margaret Rhodes of DRI was used for a more accurate description of their current methodology.

<sup>94</sup>The WEFA model is used for internal forecasts only, and thus full documentation does not exist. Information on their current methodology was obtained from a brief methodology description in the *WEFA Natural Gas Service Long-Term Forecast* (Bala Cynwyd, PA, Winter 1992) and from telephone conversations with Morris Greenberg of WEFA.

- Prices are permitted to adjust freely to clear all markets simultaneously.

Initial estimates of regional, end-use gas requirements are determined from econometric models for the non-electric generators sectors and from regional load dispatch models for the electric generators sector. The demand is then assigned to the different supply regions based on initial market shares. Initial estimates of regional/sectoral prices are also used. Actual prices are then determined, and the relevant demands adjusted via price elasticities for subsequent iterations. Transportation tariffs are initialized assuming a load factor of 85 percent, but may be discounted if the actual utilization is less.

Consumption is disaggregated into heating and nonheating seasons, and further disaggregated by users with and without fuel switching capability. Consumers have the flexibility of selecting alternative supply sources. Gas can be transported from regions linked by the pipeline network or withdrawn from storage, both subject to available capacity. Any gas withdrawn from storage during a heating season is replaced during the following nonheating season. Consumers adjust supply sources to minimize costs, given the price of gas in the source region and the transportation (or storage) rate, including fuel and loss. Transportation rates are determined assuming competitive conditions, and rates on routes with excess capacity can be discounted down to variable costs. Alternatively, if pipeline capacity on a given route is constrained, rates may be adjusted upward in the solution process to the point where they exceed the regulated transportation ceiling rate in order to clear the market. In this case, if the marginal value of the expansion, as measured by current and future price differentials and utilization rates, exceeds its marginal cost, capacity is expanded. If such expansion does not occur, transportation-constrained sources will lose market share to unconstrained routes.

Throughout the solution process, prices are adjusted to reduce excesses of supply or demand in any or all regions/seasons/time periods. The process is repeated iteratively until market-clearing prices are determined. Convergence is achieved when the following conditions are met:

- Excess supply/demand is zero in each market
- The delivered cost of gas to each region is the same for every active route
- Pipeline capacity utilization is less than or equal to 100 percent on every route
- The marginal value of transportation on each route is less than or equal to the marginal cost of expansion.

### ***American Gas Association (AGA)<sup>95</sup>***

Natural gas modeling at the American Gas Association is done within the framework of the American Gas Association's Total Energy Resource Analysis model (A.G.A.-TERA). The TERA modeling system provides annual projections through 2010 of natural gas production, consumption, and prices, with projections for the residential, commercial, industrial, and electric generators end-use sectors provided for the nine Census Regions. The approach is a heuristic one that simulates the market and does not assume optimization of either policy or market behavior. The equilibration process involves the interaction of three components: (1) a set of drilling models, (2) a demand/marketplace model, and (3) a deliverability model. The drilling models and the demand/marketplace model provide inputs for the deliverability model, but there is not an automated feedback loop from the deliverability model to the drilling and demand/marketplace models. Analyst intervention is often necessary to equilibrate the market via adjustments in the trial wellhead prices.

The models treat the natural gas transmission and distribution segment of the industry very simply. Flows are not explicitly represented, and capacity constraint/expansion issues are not treated. The prices of natural gas to

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<sup>95</sup>Introduction to the A.G.A.-TERA Energy Modeling System, American Gas Association (Arlington, VA, 1991), provides a very general overview of the overall model; phone conversations with Leon Tucker of the A.G.A. provided specifics on the handling of transmission and distribution.



consumers are calculated as linear functions of the wellhead price via ordinary least squares regression in order to reflect the combination of supply-related costs and transmission and delivery-related costs.

### ***Gas Research Institute (GRI) Energy Overview Model (EOM)<sup>96</sup>***

In producing its yearly Baseline Energy Forecast, the Gas Research Institute (GRI) uses a model known as the Energy Overview Model (EOM). The transmission and distribution segment of the natural gas industry is represented by a separate model, the National Pipeline/Flowing Gas Model developed by Energy and Environmental Analysis, Incorporated (EEA). The EEA model is a simulation model that represents the U.S. pipeline system by means of 12 composite pipeline groups, which are aggregates of actual pipeline systems chosen to represent the major differences in gas supply areas serving the 10 Federal regions. The network has recently been expanded to include the entire North American gas market (including both Canada and Mexico). Each pipeline group has its own inventory of gas reserves, access to one or more of 15 supply regions (as represented in the GRI Hydrocarbon Supply Model), and an individual cost of service estimate for pipeline operations. The EEA model is integrated with the EOM, and thus flows are considered in the market equilibration process. Nonlinear optimization is used to minimize costs subject to supply and demand constraints.

The pipeline model simulates pipelines in their role as both merchants and transporters of gas. Transportation services are provided to distributors and end-users under a mix of rates based on the quality of service. Rates are based on cost-of-service with the flexibility for rate discounting caused by market pressures. An accounting system tracks both committed gas supplies under long-term contracts with pipelines and uncommitted supplies being marketed by producers and sold on the spot market. Associated with committed supplies are detailed contract terms and conditions.

The model represents the distribution of supply from the city gate to end-users by means of an aggregate local distribution company (LDC) in each demand region. Revenue requirement accounts are maintained for each LDC to set distribution margins by end-use sector, with margins and burner-tip gas prices differing by demand region. LDCs themselves offer end-users both sales service and transportation of gas purchased on the spot market.

Seasonal transmission charges for each pipeline group and distribution charges for the LDC in each Federal region are estimated by the model based on cost-of-service estimates. The charges are then allocated to the services provided by the distributor or pipeline. Market pressures and regulatory structures determine the extent to which those charges recover gas transmission and distribution costs. A cost-of-service algorithm estimates year-to-year changes in the overall nongas costs of pipeline operations so as to take into account the response of the costs to changes in system throughput, compression costs (which change with volume and cost of gas), rate base, and the cost of capital. After determining the cost of service for each pipeline group, the model allocates these costs between the sales and transportation services offered to customers based on the mix of each pipeline's merchant and transport services. After allocating costs, the model pipelines establish a structure of differential rates for the various classes of service. The transmission margin included in pipeline resale rates is assigned on a fully allocated basis, meaning that the costs allocated to this service will be fully recovered in providing the service. Pipelines also maintain separate firm and interruptible rates applicable to transportation. Competitive forces and market pressures may prevent pipelines from fully recovering costs for interruptible service. The model allows margins on transportation to distributors to be reduced below full cost recovery to represent the potential discounting pressures on pipeline supplies caused by interpipeline competition. Costs not recovered due to discounting are reported.

The EEA model has recently been updated to include a detailed representation of capacity expansion in support of an ongoing National Petroleum Council (NPC) study.<sup>97</sup> The model takes into account both planned expansion and other future expansion. An input data file describes planned projects for the next 5 years, including their construction costs. For projects beyond the 5-year time horizon, the same data file contains "generic" projects that can be

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<sup>96</sup>*Guide to the Hydrocarbon Supply Model, 1990 Update*, Energy and Environmental Analysis, Inc. (Arlington, VA, October 1990) and conversations with EEA and GRI staff.

<sup>97</sup>The enhanced treatment of capacity expansion in the EEA Pipeline/Flowing Gas Model has not as yet been documented. The above information was provided through conversations with Robert Crawford of EEA.

undertaken if it is economic to do so. Data for these generic projects include cost estimates on a dollars per thousand cubic feet/mile (where mileage figure represents miles that the gas is actually moved). Cost data are determined by using a cost algorithm that reflects today's capacity addition costs. Three sets of cost algorithms are employed: one for the Lower 48 States, one for Canada, and one for frontier areas where expansion is costly. Regional differences in construction costs are not captured. Costs are determined for three types of possible expansion: compression only, looping and compression combined, and construction of new pipe. Potential future projects are set up throughout the system as though they were real ones. Thus the model sees what is analogous to a supply curve for capacity additions at each node. The steps on the "supply" curve are analogous to the amount of each of the three types of expansion possible at that point in the system. The data allow for expansion everywhere in the system, with those areas deemed most likely to have more expansion activity provided higher bounds on the amount of expansion possible.

In solving for capacity expansion, the model begins each forecast year with an estimate of new capacity that would be needed to meet the demands for that year. Each potential new pipeline link has a supply source with an associated volume and price elasticity, and a demand at its destination. The model takes into account how much the supply price would be raised at the source due to the added volume, and how much the demand would be depressed as a result of the associated higher prices. Capacity to be added is controlled by the criteria that any added capacity must be able to operate at a minimum of an 80-percent load factor. New links compete against alternate supply sources and each other—capacity will not be added if there is a cheaper alternative for meeting demand. New costs are compared against the cost of adding capacity. The cost of the added capacity must be less than the price differential on competing links, and the throughput high enough (at least 80 percent) in order for capacity to be added.

Storage is considered to be a supply source during the winter months and a demand source during the summer months. Storage expansion is not endogenously determined. Offline scenarios are run to determine how much storage capacity would increase, and storage is fixed within any given model run. The offline analysis to determine storage expansion is an iterative process in which estimates of expected increases in storage are made, the model is run and results analyzed, estimates are revised and the model rerun until analyst judgment indicates a satisfactory estimate of future storage expansion.

### ***Decision Focus, Inc. (DFI) North American Regional Gas Model (NARG)<sup>98,99</sup>***

Decision Focus, Inc. has developed a multiregion Samuelson spatial equilibrium model used by the Gas Research Institute (GRI) for sensitivity analyses. This model is referred to as the GRI North American Regional Natural Gas Supply-Demand Model.

The model represents approximately 150 distinct gas supply sources in the United States and Canada. Fifteen demand regions are represented, 3 in Canada and 12 in the United States (based on disaggregations of the census regions), with distinctions within each demand region between core and noncore markets.<sup>100</sup> In the United States, all of the residential and commercial and half of the industrial demand are assumed to be core, while the balance of the industrial and all of the electric generators demand are assumed to be noncore.

The model's representation of the North American pipeline system includes:

- A comprehensive pipeline network consisting of current and potential future pipeline links from supply regions to demand regions

<sup>98</sup>Dale M. Nesbitt *et al.*, "Analysis of GRI North American Regional Gas Supply-Demand Model", in *North American Natural Gas Markets: Selected Technical Studies, Energy Modeling Forum (EMF) Report 9*, Volume III, pp. 185-234 (Stanford University, April 1989)

<sup>99</sup>Dale M. Nesbitt *et al.* (DFI), "Appendices for the GRI North American Regional Natural Gas Supply-Demand Model," prepared for Gerald Pine (GRI), February 1990.

<sup>100</sup>The core service customer is guaranteed service (i.e., is assumed to purchase firm service) and generally pays the highest rate for natural gas. The noncore customers consume gas under a less certain and/or less continuous basis (i.e., an interruptible basis) and typically are offered a lower rate than the core customers.

- Tariffs and losses for each pipeline link.

The degree of pipeline detail is consistent with the degree of supply and demand detail elsewhere in the model. In particular, while the model could have been designed to enumerate and distinguish every individual pipeline in the United States, its developers instead sought commonalities among supply regions, pipelines, and demand regions that would allow aggregation. Rather than representing individual pipelines, the model instead represents pipeline corridors from its supply regions to its demand regions. These corridors are explicitly defined by the characterization of the model's supply and demand regions, and by the configuration of the U.S. and Canadian pipeline systems that exist today. Each of the existing pipeline corridors represented in the model begins in a given supply region, extends perhaps through intermediate supply and demand regions, and terminates in a demand region. The network of existing pipeline corridors interconnects all currently producing regions with all currently consuming regions.

The model also enumerates all prospective future pipelines that might be built in the next 50 years. These pipelines connect new producing regions (or subregions) with various demand regions, and connect Canada and Mexico to the United States. They are truly prospective in the sense that they will be built only if they become economic (i.e., only if supplies at the upstream end, marked up to account for the cost of the new pipelines, constitute the most competitive source at the downstream end). In the model, looping is considered as an option for all existing capacity, as well as for the existing links of the new corridors.

The linkage between Canada and the United States is potentially very important. The model therefore distinguishes the pipelines in Canada that directly or indirectly lead to the Lower 48 United States. The model also includes two prospective Canadian export routes to the United States. One of these routes runs from North Alaska through Alberta and ultimately to the United States, and represents the upstream leg of the Alaska Natural Gas Transportation System. The other runs from Northern Canada (MacKenzie and Beaufort Sea), through Alberta, and ultimately to the United States, and represents the pipeline that will have to be built in order to exploit Canadian Arctic gas (the Polar project and prospective expansions).

The current version of the model contains corridor capacity estimates prepared by Benjamin Schlesinger and Associates (BSA, under contract to the California Energy Commission). BSA also provided appropriate corridor transmission costs, which represent the embedded cost of each pipeline and specifically account for discounting behavior on the part of pipeline owners. Pipeline capacities and cost structures for all Canadian pipelines are based on data from the National Energy Board of Canada.

Several generic types of pipeline capacity expansion are explicitly represented (for each pipeline link) within the model:

- Expansion of capacity of a given pipeline by such actions as looping or increasing pressure
- Expansion of capacity along a given corridor by adding a new pipeline
- Addition of an entirely new pipeline corridor.

For each pipeline link, the model assumes that the embedded cost of the capacity currently in place will affect the rates for quantities of gas transported that do not exceed the current known capacity. In order to transport more gas than the current capacity of the corridor, it is necessary to augment the capacity through looping or pressure increases. Such augmentation is possible (at a cost) and is usually bounded by an upper constraint (i.e., looping and pressure increases can each add only a limited quantity of additional capacity). In order to exceed the capacity of an existing, fully looped, maximum pressure pipeline link, it is necessary to add new pipeline capacity. At the incremental cost of securing appropriate rights of way and building such a pipeline, it is possible to expand the capacity of that corridor virtually without bound.

The model thus requires current transportation cost information, capacity expansion costs through augmentation, and new capacity addition costs. For the current version of the model, such data (for every existing and prospective future corridor) were provided by BSA under contract to the California Energy Commission.

## **Stanford University North American Gas Trade Model (GTM)<sup>101</sup>**

The North American Gas Trade Model (GTM) developed at Stanford University in conjunction with the Stanford University International Energy Project is an interregional natural gas trade partial equilibrium model which computes, for 2 single time periods (1990 and 2000), market clearing prices and a possible pattern of trade flows between 11 supply and 14 demand regions in the United States, Mexico, and Canada. Demands within the United States are provided for each of four consuming sectors (residential, commercial, industrial, and electric generators). Key inputs to the model include:

- The regional distribution of gas supplies and demands at alternate price levels
- Transportation charges
- Pipeline capacity constraints
- Canadian and Mexican export quantity limits.

In some regions, prices are free to move so as to equilibrate supplies and demands, while in others there may be disequilibria associated with controls over prices and/or quantities traded. The objective of the solution process is to maximize the sums of producers' and consumers' surpluses, or, alternatively, maximize the sum of consumers' benefits minus the costs of production and transportation. With the exception of the nonlinearity of the objective function, the GTM is a straightforward transportation model. The model is solved using MINOS, a nonlinear programming computer package.

Economic policy and technical constraints are handled as upper or lower bounds on objective function variables. For example, pipeline capacity limits are represented as upper bounds on the transportation variables, and take-or-pay contract limits are represented as lower bounds. The user can specify limits on certain demands or export volumes, which allows the simulation of export and price controls. Taxes or subsidies on individual supplies or demands can be similarly represented by constraints on individual supply and demand variables. Each of these conditions is represented as an upper or lower bound on an individual variable.

The objective function contains linear cost coefficients related to the transportation variables. Supply and demand variables enter in a separable nonlinear form. A market equilibrium is computed by maximizing the objective function subject to supply and demand constraints and upper and lower bounds on individual variables. If supply and demand are unconstrained, the shadow prices will be the marginal costs of production or the price consumers are willing to pay. This information can aid the analyst in making decisions (e.g., whether to expand production or increase capacity).

## **Massachusetts Institute of Technology (MIT) Center for Energy Policy Research<sup>102</sup>**

The Center for Energy Policy Research Energy Laboratory at MIT has developed a North American natural gas trade model as part of a project on international gas issues. The primary purpose of the model is to estimate the costs and benefits to Canada and Canadian firms of alternative gas production and export programs. While it is an interregional trade equilibrium model similar in concept to the Gas Trade Model (GTM) described above, it has been formulated as a linear, rather than a nonlinear, programming problem. The model solves for exports to the United States and investment and production in each Canadian supply area, reporting additional information including marginal costs of production, export prices, marginal export revenues, capital rental charges, resource depletion costs, etc. The model includes nine different pools of Canadian reserves and three gas markets within the United States: West Coast, Middle West, and North East.

<sup>101</sup>Mark A. Beltramo, Alan S. Manne, and John P. Weyant, "A North American Gas Trade Model (GTM)," *Energy Journal*, July 1986, pp. 15-32.

<sup>102</sup>Charles Blitzer, "A North American Natural Gas Model: Part I," *Final Report on Canadian-U.S. Natural Gas Trade*, (Cambridge, MA: MIT Center for Energy Policy Research October 1985).

Constraints involve supply/demand balances, production-reserve relationships, production-investment relationships, export delivery patterns, pipeline capacity constraints, and export revenues. Demand functions are represented by piece-wise linear approximations. Pipeline capacity is input exogenously. Investment in capacity expansion, although incorporated in annual capital costs, is not, however, endogenously determined. Pipeline operating costs are handled as linear functions of export volumes based on operating cost coefficients.

The model can be solved using any one of three objective functions:

- Maximize net benefits to Canada as a whole
- Maximize the sum of net benefits to Canada and to U.S. importers of Canadian gas
- Simulate competitive profit maximizing behavior among Canadian producers, inclusive of royalties.

The second objective function seeks to determine the perfectly competitive solution, in effect maximizing net benefits to Canada (producers' surplus) and net benefits to the United States (consumers' surplus).

### ***Energy Information Administration Gasnet Model<sup>103</sup>***

The Gasnet model is an optimization model, developed by EIA in the late 1970's to forecast short-term seasonal patterns of natural gas distribution given predetermined projections of both supply and demand for natural gas. Although no longer in use within EIA, the Gasnet model was reviewed in doing background research for development of the NGTDM as it explicitly represents a pipeline network, using a series of constrained optimization techniques to simulate the transmission pattern within the natural gas industry. Gasnet provides summary tables listing quarterly estimates of natural gas supply by State and consumption and excess demand by State for the residential, commercial, industrial, and electric generators sectors.

On the demand side, 48 States, the District of Columbia, Mexico, and 5 Canadian provinces are represented. On the supply side, there are 45 producing areas located in the 26 producing U.S. States and 4 Canadian provinces. Four of the producing States are divided into substate regions. Five major interstate pipeline activities are represented in the model: (1) selling gas to end-users, (2) receiving produced gas, (3) injecting or withdrawing gas from storage, (4) exchanging gas with other pipeline companies, and (5) transmitting their own gas volume to other States. Within the model, various nodes are interconnected by arcs. Each node is associated with one or more of the five major activities described above.

The model connects the demand regions and supply areas to estimate the sectoral effects of natural gas shortages. The model represents each pipeline by a system of interconnected nodes allowing the calculation of interstate flows along a pipeline system. A separate module, the Historical Apportionment Model (HAM), computes the distribution of the forecasted gas production through the network on the basis of the historical relative flows (i.e., the pattern determined from the base year data). The HAM model solution provides a base case for the final phase of the modeling process: the linear program. The linear program minimizes the deviations of gas from the desired storage goals, the sum of excess demands and supplies by consuming sector in each State, and the costs of operation for the transmission of gas throughout the entire network, subject to the following constraints:

- Mass balance at each node
- Regional gas production equation for each region
- Balance of supply and demand over all States and demand sectors.

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<sup>103</sup>Energy Information Administration, *Gasnet: Methodology Description* (Washington, DC, August 1978)

## Solution Methods for Solving Network Flows

In developing the methodology for the NGTDM, a number of modeling techniques were evaluated other than those employed in natural gas models. In particular, specific mathematical formulations and solution techniques, such as linear programming (LP), mixed integer programming (MIP), special ordered sets (SOS), and nonlinear programming were considered.<sup>104</sup> In addition to the specific natural gas models discussed above, the following models were reviewed because they employ techniques that were considered for use in the NGTDM.

### **Energy Information Administration Project Independence Evaluation System (PIES)<sup>105</sup>**

The PIES model, developed in the mid-1970's, was EIA's first large scale energy forecasting model. The PIES framework consists of three major components: a demand model, a supply network, and an equilibrating mechanism.

The PIES supply network is composed of production, conversion, and transportation activities. They are linked by means of a distribution network that represents the movement of raw materials or products. The major economic assumption implicit in the PIES structure is that market equilibrium conditions govern the purchase prices and quantities of fuels so that the sum of consumers' and producers' surplus is maximized across all regions and all energy industry sectors, subject to the constrained market conditions introduced by government regulation.

The following assumptions are made: (1) subject to regulatory constraints, participants in the economy act in their own self-interest, (2) consumers are rational and maximize their benefits, and (3) producers maximize profits. A linear programming formulation is used, incorporating step-like approximations to the supply and demand curves.

### **Stanford Research Institute SRI-GULF Energy Model<sup>106</sup>**

The Stanford Research Institute's SRI-Gulf Energy Model is a highly-detailed regional, dynamic model of the supply and demand for energy in the United States. It was developed in 1973 to analyze synthetic fuels strategy for the Gulf Oil Corporation and has subsequently been extended and widely used in other energy analyses. It employs a generalized equilibrium modeling methodology which represents a synthesis of several modeling techniques. The conceptual framework of generalized equilibrium modeling emphasizes: (1) the need to focus modeling efforts on decisions and (2) the coordinated decomposition of complex decision problems using iterative methods. A decision problem is first conceptualized, and then decomposed to define the basic decision and physical processes that must be included in the modeling process. The overall model is then implemented using the following three basic elements of generalized equilibrium modeling: (1) *processes* describing the fundamental submodels, (2) a *network* describing the interactions among the processes, and (3) an *algorithm* for determining the numerical values of the variables in the model.

In the SRI-GULF model, 17 end-use demands are modeled for each of the 9 U.S. Census Divisions through 2025. Approximately 2700 processes are represented, with processes that describe end-use demands for energy and primary resource supply linked by a network of other processes describing market behavior, conversion, and transportation. The algorithm used to solve the model finds the set of variables (primarily prices and quantities) that satisfy the physical and behavioral relations embodied in the processes and the linkages among the variables as defined by the network.

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<sup>104</sup>For further information on formulations, see "An Evaluation of Problem Formulations and Mathematical Programming Software for the Gas Market Model of NEMS," Science Applications International Corporation (McLean, VA, April 1992).

<sup>105</sup>*The Integrating Model of the Project Independence Evaluation System, Volume I - Executive Summary*, Logistics Management Institute (Washington, DC, April 1979).

<sup>106</sup>*Generalized Equilibrium Modeling: The Methodology of the SRI-Gulf Energy Model*, Decision Focus, Incorporated (Palo Alto, CA, May 1977).

Although the model involves hundreds of distinct processes, each can be implemented as one of a few basic processes which consist of: (1) simple conversion processes, (2) allocation processes, (3) primary resource processes, (4) end-use demand processes, (5) transportation processes, (6) complex conversion processes, and (7) secondary industry processes. The main process of interest in the SRI-Gulf model is the allocation process, which allocates the demand for a fuel among the competing sources of supply. The allocation process used in the model is a dynamic process that responds continuously to changes in price. The sharing method is represented in terms of simple market share curves and simple market penetration (behavioral lag) curves that reflect lags or time delays in responding to price changes. This is preferable to an allocation process that responds sharply to small differences in prices (as would be the case if demand were allocated entirely to the lowest price source), as the latter tends to overstate the market response to prices.

## Conclusions

This section consists of two subsections. The first compares the NGTDM with EIA's former modeling system, GAMS, as one of the main goals of the design of the NGTDM was to address the weaknesses of the GAMS in modeling the current natural gas industry and provide EIA with a more effective modeling tool. The second section compares the NGTDM with the other modeling approaches considered, detailing which aspects of each approach were included and why each particular model or approach was, or was not, adopted for the NGTDM.

## Comparison of Capabilities of GAMS to the NGTDM

GAMS has a number of limitations that precluded its use within the NEMS. The NGTDM was designed to address these limitations. As indicated in the Model Quality Audit review of GAMS performed for the Office of Statistical Standards,<sup>107</sup> one of the major limitations of GAMS was that it does not take into account significant regional differences in both supply availability and pricing. When GAMS was first modified to explicitly treat deregulated gas, a simple structure was included to represent a single national pool of deregulated gas. This national representation of deregulated gas means that GAMS does not fully account for regional supply distinctions on the overall market. The NGTDM represents both supply availability and price levels for all supply sources by region.

Another drawback to GAMS is that it does not include a representation of the physical flow of gas, and thus can not be used to analyze pipeline capacity issues. The assumption was made during the initial development of the model that sufficient capacity would exist to satisfy demand, and therefore neither capacity constraints nor future capacity expansion issues were considered. In reality, there are significant differences across regions in capacity utilization, with very heavy utilization occurring in certain sections of the country (specifically the West and Northeast).<sup>108</sup> One of the key determinants of how pipelines will price services in the future will be how intensely their systems are utilized. To represent this, a treatment of both capacity constraints and capacity expansion (pipeline and storage) decisions is necessary. These issues are addressed by a separate Capacity Expansion Module within the NGTDM. Flows are accounted for in the Annual Flow Module (AFM) by incorporating an aggregate representation of the natural gas transmission and distribution network. This allows a more comprehensive analysis of the results of supply and demand shifts on capacities and flow patterns, as well as a more representative analysis of the pricing of natural gas transmission and distribution services.

Also key to the pricing of natural gas transmission and distribution services is the representation of tariffs. While the GAMS representation of tariffs via markups based on fixed historical levels reflects both transmission and local distribution costs, the representation is simplistic and can not be easily adapted to reflect future market conditions. While pipelines and distributors formerly could be assumed to price strictly on the basis of their average cost of service, they are now offering a full range of services under competitive and market-based pricing arrangements. Although not totally deregulated, they have considerable pricing flexibility. The GAMS structure does not reflect

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<sup>107</sup>Carpenter, Paul R., "Review of the Gas Analysis Modeling System," Incentives Research Inc. (Boston, MA, August, 1991). (Also contained in Appendix B of the GAMS Model Quality Audit.)

<sup>108</sup>Carpenter, Paul R., "Review of the Gas Analysis Modeling System," Incentives Research Inc.

this, and thus does not permit regulatory analysis of pricing issues. Tariffs in the NGTDM are endogenously determined along different segments of the physical pipeline system, with separate modules to model tariffs for pipeline and distributor services. The NGTDM also represents differences in pricing various classes of service more adequately than GAMS. GAMS applies the class-of-service pricing distinction only to the electric generators sector. Many industrial sector and large commercial sector users are also taking advantage of the lower prices associated with interruptible service, which is available to all customers. The NGTDM has the capability of distinguishing customers by type of service in all end-use sectors. Cost-based, average pricing is applied to core customers (firm service) within each sector and market-based, marginal pricing is applied to noncore customers (interruptible service).

There are two final areas not addressed in GAMS. The first is that of environmental impacts, which has become an area of considerable importance as a result of the Clean Air Act Amendments (CAAA) of 1990. The NGTDM tracks emissions of criteria pollutants associated with the transmission and distribution of natural gas. The second is that of energy related investment. Energy related investments in areas such as the capacity expansion of natural gas pipelines are quantified in the NGTDM. Key features of the natural gas models reviewed are summarized below in Table D-1. While some of the models, such as WEFA and GRI, do address most of the issues that were of concern in the development of the NGTDM, others, such as the DRI and AGA models, employ a very simplistic

**Table D-1. Natural Gas Models Reviewed**

Model Feature	DRI	WEFA	AGA	GRI	DFI	GTM	MIT	Gasnet	GAMS	NGTDM
Flows represented	no	yes	no	yes	yes	yes	yes	yes	no	yes
Endogenous tariffs	no	yes	no	yes	no	no	no	no	no	yes
Capacity constraints	no	yes	no	yes	yes	yes	yes	no	no	yes
Capacity expansion	no	yes	no	yes	yes	no	yes	no	no	yes
Core/noncore markets	no	yes	no	yes	yes	no	no	no	no	yes
Seasonal	no	yes	no	yes	no	no	no	yes	no	no
Spot and contract gas	yes	yes	no	yes	no	no	no	no	yes	no
Environmental issues	no	no	no	no	no	no	no	no	no	yes

representation of the transmission and distribution segment of the industry. In the DRI and AGA models, flows are not explicitly represented, end-use prices are determined via fixed markups, and capacity constraints and capacity expansion decisions are not represented. These models were thus not suitable to address the requirements of NEMS.



## Comparison of Capabilities of Other Models to the NGTDM

The WEFA and GRI/EEA models address several of the issues which are represented in the NGTDM. Like the NGTDM, these models track flows, take into account capacity constraints and capacity expansion decisions, and have endogenous determination of tariffs. Both models also have structures not represented within the NGTDM, as well as some general drawbacks in comparison to the NGTDM. The WEFA model is implemented as a spreadsheet, and is therefore not directly compatible with the NEMS system. While tariffs are endogenously determined, the methodology is a simple one which does not allow the type of regulatory analysis required by NEMS. While the GRI/EEA model has a more sophisticated determination of tariffs, all pricing is based on cost-of-service, and marginal pricing, which the NGTDM allows for, is the direction in which the industry is going. Capacity and capacity expansion issues are considered to be of great importance, and thus are treated in more detail in the NGTDM than in the GRI/EEA model.

Two features of the WEFA and GRI/EEA models not directly incorporated into the NGTDM are seasonal pricing and the distinction between wellhead spot and contract gas. A detailed treatment of contract pricing provisions for system supply is no longer necessary, since total deregulation of the wellhead market occurred in 1993. In addition, given the resulting competitive nature of the market at the wellhead, it is expected that the majority of new supply contracts will contain clauses tying the contract price to the going price on the spot market, resulting in these prices moving in tandem over time. If the relative difference between the spot and contract gas price is determined to be significant, this distinction can be readily incorporated within the NGTDM. Seasonal pricing is an important issue for future consideration within NEMS, but is beyond the scope of the current design.

The basic structure of the GTM and MIT models is similar to the design of the NGTDM. Both are interregional trade equilibrium models which, like the NGTDM, are formulated as optimization problems that maximize the sum of producers' and consumers' surpluses subject to supply, demand, regulatory, and technological constraints. There are, however, a number of significant enhancements that are provided in the NGTDM. The GTM focuses on long-term market equilibria rather than on mid-term institutional and regulatory issues, which are important for NEMS to address. Like many of the other models, the GTM does not incorporate an endogenous determination of tariffs or capacity expansion decisions. While the structure of the MIT model is similar to that of the NGTDM, it is basically a Canadian model without the U.S. market detail required of NEMS.

Because of the number of supply regions and pipeline corridors, the representation of the transmission and distribution network incorporated in the DFI model is the most detailed of any of the models reviewed. Given that the solution time required to solve a system of this level of detail does not fall within the NEMS guidelines and that tariffs are determined based on exogenously determined values, the structure was not considered to be suitable for NEMS.

Since the Gasnet model was developed during a time-period when the gas market was very different from the current market, it has a structure that could not be easily modified to address the issues relevant to NEMS. It does, however, provide a good example of the general technique of applying network optimization to natural gas transmission and distribution, which is the method that is used in the NGTDM to model the noncore transportation segment of the market.

Of the nonnatural gas models reviewed, PIES was most relevant to the design of the NGTDM. The PIES solution methodology, in fact, forms the basis for the linear programming approach used as the solution methodology in the NGTDM. The allocation process used in the SRI-GULF model was seriously considered to be used as the basis for an heuristic approach to modeling cost-of-service pricing in the core market within the NGTDM. This approach was subsequently abandoned due to added operational and convergence complexity that would be introduced by the use of separate modeling approaches for core and noncore markets.



## **Appendix E**

### **Model Input Variable Mapped to Data Input Files**

This appendix provides a list of the FORTRAN variables, and their associated input files, that are assigned values through FORTRAN READ statements in the source code of the NGTDM. Information about all of these variables and their assigned values (including sources, derivations, units, and definitions) are provided in the indicated input files of the NGTDM. Electronic copies of these input files are available upon request from Joe Benneche (202) 586-6132 or Jim Diemer (202) 586-6126.



Variable	File	Variable	File
A191START	RDESIGN	BASET	CAPACTY
A191YRS	RDESIGN	BENCHF	DTARIFF
ACT_DRY_PROD	HISDATA	BGSCNT	CAPACTY
ADDA	PTARIFF	BGSCT	CAPACTY
ADDYR	CAPACTY	BIARC_PFSHR	INITDAT
ADGPRD89	INITDAT	BIARC_PISHR	INITDAT
ADIT	PTARIFF	BLAEFFFC	PTARIFF
ADIT90	PTARIFF	BLAESWT	PTARIFF
ADIT_FD	PTARIFF	BLAETOT	PTARIFF
ADIT_TEMP	PTARIFF	CANCAP	CAPACTY
AD_FR_OIL	INITDAT	CANEFF	INITDAT
AEFF_PIPE	INITDAT	CANEXP	CAPACTY
AEFF_PIPE_SCALE	INITDAT	CANFLO_IN	INITDAT
AEFF_PIPE_SCALE93	INITDAT	CANFLO_PFSHR	CEMDATA
AFLOW_F	CAPACTY	CANFLO_SHR	INITDAT
AFLOW_I	CAPACTY	CANFRMITR_SHR	INITDAT
AFM_PTAR_I	PTARIFF	CANTAR_F	INITDAT
AFR	ALLOCAT	CANTAR_I	INITDAT
AFU	ALLOCAT	CAN_NODEIN	INITDAT
AK_C	INITDAT	CAN_NOTEOUT	INITDAT
AK_CM	INITDAT	CAN_UTILZ	CEMDATA
AK_CN	INITDAT	CAN_UTIL_GRW1	CEMDATA
AK_D	INITDAT	CAN_UTIL_GRW2	CEMDATA
AK_E	INITDAT	CAN_UTIL_MAX	CEMDATA
AK_EM	INITDAT	CAN_UTIL_PF_P	CEMDATA
AK_F	INITDAT	CAN_UTIL_SYR1	CEMDATA
AK_G	INITDAT	CAN_UTIL_SYR2	CEMDATA
AK_PCTLSE	INITDAT	CAPEXP	PTARIFF
AK_PCTPIP	INITDAT	CCOST	PTARIFF
AK_PCTPLT	INITDAT	CEMH	INITDAT
AK_PCTSOUTH	INITDAT	CGBENCHF	DTARIFF
AK_RM	INITDAT	CGBENCHI	DTARIFF
AK_RN	INITDAT	CGDELTA_N	DTARIFF
ANGTS_TAR	INITDAT	CGDELTA_U	DTARIFF
APCKITR	INITDAT	CLSNGWP	HISDATA
APCKSWTCH	INITDAT	CMES	PTARIFF
APCKYR	INITDAT	CNYEAR	CAPACTY
APCT_MINF	INITDAT	CN_BRDPRC90	INITDAT
APCT_MINI	INITDAT	CN_NEWCAP90	INITDAT
ARC2P	PTARIFF	CN_TOL	INITDAT
ARC_CYCLE	INITDAT	CN_WELPRC89	INITDAT
ARC_OUTILZ	CEMDATA	CONDEM	PTARIFF
ARC_PFUTILZ	CEMDATA	CONST_DMD	INITDAT
ARC_PUTILZ	CEMDATA	CONST_EXP	INITDAT
ARF	ALLOCAT	CONST_SUP	INITDAT
ARV	ALLOCAT	CPCKSWTCH	INITDAT
ASF	ALLOCAT	CPCKYR	INITDAT
ASV	ALLOCAT	CSOML	PTARIFF
AUTILZ_F	CAPACTY	CSOMN	PTARIFF
AUTILZ_T	CAPACTY	CSTFAC	PTARIFF
AVR	ALLOCAT	CWC	PTARIFF
AVU	ALLOCAT	DCMER	PTARIFF
BASERADJ	RDESIGN	DDA	PTARIFF

Variable	File	Variable	File
DDA_FD	PTARIFF	HPGIINGR	HISDATA
DDA_RHO_E	PTARIFF	HPGIRS	HISDATA
DDA_TEMP	PTARIFF	HPGIRSGR	HISDATA
DEBTYR	DTARIFF	HPGITR	HISDATA
DEFPRICE	INITDAT	HPGITRGR	HISDATA
DELFLG_CAP	CEMDATA	HPGTELGR	HISDATA
DELFLG_STR	CEMDATA	HPNGCM	HISDATA
DELPR_CAP	CEMDATA	HPNGIN	HISDATA
DELPR_STR	CEMDATA	HPNGRS	HISDATA
DEPSHR90	PTARIFF	HPNGTR	HISDATA
DEPSHR91	PTARIFF	HWPRLAGOF	HISDATA
DISCR_PK	INITDAT	HWPRLAGON	HISDATA
DISPRC	HISDATA	H_REALRMGBLUS	DTARIFF
DISTO	DTARIFF	H_RMPUAANS	DTARIFF
DLTDR	PTARIFF	IEXPCT	RDESIGN
DOLYR	PTARIFF	IFLOOR	DTARIFF
DTAR_REFYR	DTARIFF	ILAG	INITDAT
DTM_BETA	DTARIFF	INTRA_TARF	DTARIFF
EFF_STR	INITDAT	INTRA_TARI	DTARIFF
EHISYR	INITDAT	IPD1	DTARIFF
EMISRAT	INITDAT	IPD2	DTARIFF
EMMSUB	INITDAT	IPD2YR	DTARIFF
EMMSUB_EL	INITDAT	I_BYPASS	DTARIFF
EMMSUB_NG	INITDAT	KARCEX	PTARIFF
EST_DRY_PROD	HISDATA	KCMER	PTARIFF
EXCEM	INITDAT	KLTD	PTARIFF
EXPFAC	PTARIFF	LFAC_F	RDESIGN
EXPMAP	INITDAT	LFAC_I	RDESIGN
EXP_PSHR	CEMDATA	LIMITFIRM	RDESIGN
FACTOR	PTARIFF	LIMITINT	RDESIGN
FNS	PTARIFF	LPTL_SCALE	INITDAT
FRATE	RDESIGN	LTD	PTARIFF
FTAX	DTARIFF	MACRS_RATE	PTARIFF
GPIS	PTARIFF	MATRIX	RDESIGN
GPIS89	PTARIFF	MAXESC	RDESIGN
GSRSTART	RDESIGN	MAXPROF	INITDAT
GSRYRS	RDESIGN	MAXPRON	INITDAT
HCGPR_F	DTARIFF	MAX_MACRS_YR	PTARIFF
HCGPR_I	DTARIFF	MEXEFF	INITDAT
HPGCELGR	HISDATA	MEXFRMITR_SHR	INITDAT
HPGFCM	HISDATA	MEXTAR_F	INITDAT
HPGFCMGR	HISDATA	MEXTAR_I	INITDAT
HPGFELGR	HISDATA	MILES	PTARIFF
HPGFIN	HISDATA	MILE_FD	PTARIFF
HPGFINGR	HISDATA	MINMU_I	DTARIFF
HPGFRS	HISDATA	MNPERCNT	INITDAT
HPGFRSGR	HISDATA	MU	INITDAT
HPGFTR	HISDATA	NARC_CYCLE	INITDAT
HPGFTRGR	HISDATA	NATL_DISCR	HISDATA
HPGICM	HISDATA	NATL_DISCR	INITDAT
HPGICMGR	HISDATA	NBRNCH	INITDAT
HPGIELGR	HISDATA	NEFF_PIPE	INITDAT
HPGIIN	HISDATA	NETPLT90	PTARIFF

Variable	File
NETPLT91	PTARIFF
NEWCOSTSTART	RDESIGN
NEWCOST_PER	RDESIGN
NGDBG RPT	INITDAT
NGHIST_FLG	INITDAT
NGRATMAX	DTARIFF
NGREG	CAPACTY
NGUNIT	INITDAT
NG_ARC MAP	INITDAT
NG_ARC NUM	INITDAT
NG_ARC SIZE	INITDAT
NG_BK STOP_PR	INITDAT
NG_CEN MAP	INITDAT
NG_CEN SHR	INITDAT
NG_EMM MAP	INITDAT
NG_EMMSUB	INITDAT
NG_SUP MAP	INITDAT
NG_SUP SUB	INITDAT
NNET WITH	HISDATA
NONU_DTARF_DECL	DTARIFF
NONU_DTARI_DECL	DTARIFF
NONU_ELAS_F	INITDAT
NONU_ELAS_I	INITDAT
NON_POSHR_F	FSHARES
NON_POSHR_I	FSHARES
NUMSTRX	CAPACTY
OCS MAP	INITDAT
OFSTRBND	CEMDATA
OGCNPPRD	HISDATA
OGCNQPRD	HISDATA
OGPNGEXP	HISDATA
OGPNGIMP	HISDATA
OGPRDNG	HISDATA
OGPRDNGOF	HISDATA
OGPRDNGON	HISDATA
OGPRSUP3	HISDATA
OGQNGIMP	HISDATA
OGWPRNG	HISDATA
OILPRD89	INITDAT
OISTRBND	CEMDATA
OPPCNT	CEMDATA
OPPNETSTR	CAPACTY
OPPRCFAC	CEMDATA
OPPSTFR_F	CAPACTY
OSUP_RSHR	HISDATA
OSUP_TOT	HISDATA
OTOM	PTARIFF
OTTAX	PTARIFF
OWC	PTARIFF
OWC_FD	PTARIFF
OWC_TEMP	PTARIFF
P2ARCF	PTARIFF
P2ARCT	PTARIFF

Variable	File
PARM_MAXPR	INITDAT
PARM_MINPR	INITDAT
PARM_SUPCRV2	INITDAT
PARM_SUPCRV3	INITDAT
PCAP_MAX	CAPACTY
PCMER	PTARIFF
PCTLSE_SUPL	INITDAT
PDELMX	INITDAT
PDSTEP	INITDAT
PEXP	HISDATA
PFES	PTARIFF
PFSTRBND	CEMDATA
PGR COSTS	PTARIFF
PIMP	HISDATA
PIPE	PTARIFF
PIPEID	RDESIGN
PIPE_DEPR	PTARIFF
PISTRBND	CEMDATA
PKNETSTR	CAPACTY
PKPRCFAC	CEMDATA
PKSTFR_F	CAPACTY
PLTDR	PTARIFF
PMM MAP_NG	INITDAT
PNA	HISDATA
PNEWFAC	PTARIFF
PNEW_CAP	CAPACTY
PNEW_STRX	CAPACTY
PNUM191	PTARIFF
PPFER	PTARIFF
PREV_PIPE	PTARIFF
PREV_RENTBLDG	PTARIFF
PRNG_PADD	HISDATA
PS	PTARIFF
PSHIFTOF	INITDAT
PSHIFTON	INITDAT
PSHIFT_SCALE	INITDAT
PSHIFT_SWCH	INITDAT
PSSTEP	INITDAT
PSTRANDED	PTARIFF
PTMDPCTFC	RDESIGN
PTOT	HISDATA
QEXP	HISDATA
QGCELGR	INITDAT
QGFELGR	INITDAT
QGIELGR	INITDAT
QGNONU_MAXGROW	CEMDATA
QGPTR	HISDATA
QIMP	HISDATA
QLPIN	HISDATA
RCREDIT_F	RDESIGN
REGTREE	INITDAT
RENTBLDG	PTARIFF
RESPRC	HISDATA

Variable	File	Variable	File
RETAIL_COST	DTARIFF	TAG_DCLG	PTARIFF
REVC	PTARIFF	TAG_EFF1	PTARIFF
SCALE_F_MIN	RDESIGN	TAG_EFF2	PTARIFF
SEFF_PIPE	INITDAT	TAG_FD	PTARIFF
SEOM	PTARIFF	TAG_IEFFADJ	PTARIFF
SHARE_GSR_F	RDESIGN	TAG_TF	PTARIFF
SHR_AD17	INITDAT	TARO	CEMDATA
SIGMA	INITDAT	TARP	CEMDATA
SNG89	INITDAT	TCE	PTARIFF
SNGA1	INITDAT	TCF_COEFF	DTARIFF
SNGA2	INITDAT	TCMES	PTARIFF
SNGHI	INITDAT	TECHEFF	DTARIFF
SNGMIN	INITDAT	TFD1	DTARIFF
SPCM	HISDATA	TFD2	DTARIFF
SPEU	HISDATA	TFD2YR	DTARIFF
SPIN	HISDATA	TFLOOR	DTARIFF
SPRS	HISDATA	TILT1	DTARIFF
SQCM	HISDATA	TILT2YR	DTARIFF
SQEU	HISDATA	TFIL2	DTARIFF
SQIN	HISDATA	TNS	PTARIFF
SQRS	HISDATA	TLTD	PTARIFF
SRATE	RDESIGN	TOMEFFC	PTARIFF
STAROF_F	INITDAT	TOMINC1	PTARIFF
STAROF_I	INITDAT	TOMINC2	PTARIFF
STAR_F	INITDAT	TOMSWT	PTARIFF
STAR_I	INITDAT	TOM_DCLE	PTARIFF
STAX	DTARIFF	TOM_DCLE_CF	PTARIFF
STEOYRS	HISDATA	TOM_DCLG	PTARIFF
STEO_DISCR_SHR	INITDAT	TOM_EFF1	PTARIFF
STEO_NG	INITDAT	TOM_EFF2	PTARIFF
STOGPRSUP	HISDATA	TOM_FD	PTARIFF
STOGWPRNG	HISDATA	TOM_IEFFADJ	PTARIFF
STOR_NODES	CEMDATA	TOM_TF	PTARIFF
STPNGCM	HISDATA	TOTDISCR	INITDAT
STPNGEL	HISDATA	TPFES	PTARIFF
STPNGRS	HISDATA	TRNSHR	PTARIFF
STQGPTR	HISDATA	TRN_DECL	DTARIFF
STQLPIN	HISDATA	TST1	DTARIFF
STR_FUTILZ	CEMDATA	TST2	DTARIFF
STR_UTILZ	CEMDATA	TST2YR	DTARIFF
SUPMULT	INITDAT	TYP_SUPCRV	INITDAT
SUPSUB	INITDAT	UBENCH	DTARIFF
SUPSUB_NG	INITDAT	UBENPER	DTARIFF
SUPSUB_OG	INITDAT	UBENYRD	DTARIFF
SUPWTR	INITDAT	UDFLOOR	DTARIFF
SUPWYR	INITDAT	UDPD1	DTARIFF
SUP_OUTILZ	CEMDATA	UDPD2	DTARIFF
SUP_PKSHR	CEMDATA	UDPD2YR	DTARIFF
SUP_PUTILZ	CEMDATA	UEFF_PIPE	INITDAT
SWT_COSTSHIFT	RDESIGN	UNERR	INITDAT
TAG	PTARIFF	URFLOOR	DTARIFF
TAG_DCLE	PTARIFF	URPD1	DTARIFF
TAG_DCLE_CF	PTARIFF	URPD2	DTARIFF



Variable	File
URPD2YR	DTARIFF
UTILID_DECL	INITDAT
UTILID_FLG	INITDAT
UTILIR_DECL	INITDAT
UTILIR_FLG	INITDAT
UTILT1	DTARIFF
UTILT2	DTARIFF
UTILT2Y	DTARIFF
UTIL_DTARF_DECL	DTARIFF
UTIL_ELAS_F	INITDAT
UTIL_ELAS_I	INITDAT
UTIL_POSHR_C	FSHARES
UTIL_POSHR_F	FSHARES
UTIL_POSHR_I	FSHARES
WGCNT	CAPACTY
WGCT	CAPACTY

Variable	File
WOP89	INITDAT
WORKT	CAPACTY
WPR89	INITDAT
WPRLAGOF	INITDAT
WPRLAGON	INITDAT
WTHRFAC	AFMDATA
WTHR_XCAP	AFMDATA
WTPERCNT	INITDAT
WT_DEBT	DTARIFF
W_COAL	DTARIFF
W_DIST	DTARIFF
W_LPG	DTARIFF
W_RESID	DTARIFF
XSPRNT	INITDAT
XSPRNTA	INITDAT
YR_KERNRIVER_IN	PTARIFF



## **Appendix F**

### **Derived Data**



Table F1

**Data:** Parameter estimates for the Alaskan natural gas consumption equations for the residential, commercial, and industrial sectors. Parameter estimates for the Alaskan average natural gas wellhead and industrial price equations.

**Author:** Chetha Phang, EI-823, September 1993.

**Source:** *Natural Gas Annual* 1986, 1988, 1991, DOE/EIA-0131.  
*Annual Energy Review* 1991 (Table 69, Appendix C).  
 Data created using PIPEJCL.ALASKA.DEMAND1.D0512931  
 and PIPEJCL.ALASKA.DEMAND2.D0507931.

**Derivation:** The method of Ordinary Least Squares (OLS) was used to estimate the parameters of the Alaskan natural gas consumption equation for each sector (except for electric generation), the industrial sector natural gas price equation, and the average wellhead price equation. These equations are defined as follows:

Residential Natural Gas Consumption

$$\ln YR_t = AK\_C(1) + AK\_C(2) * \ln OP_{t-1} + AK\_C(3) * \ln RN_t$$

Durbin-Watson = 2.079, R-Squared = 0.9477, N = 11

Variables:	AK_C(1)	AK_C(2)	AK_C(3)
Estimated Value:	5.587	0.03195	0.8958
t-statistic:	(8.54)	(0.60)	(7.23)

Commercial Natural Gas Consumption

$$\ln YC_t = AK\_D(1) + AK\_D(2) * \ln OP_{t-1} + AK\_D(3) * \ln CN_t$$

Durbin-Watson = 1.673, R-Squared = 0.430, N = 12

Variables:	AK_D(1)	AK_D(2)	AK_D(3)
Estimated Value:	7.90	0.255	0.5437
t-statistic	(9.506)	(2.06)	(2.603)

Industrial Natural Gas Consumption

$$YI_t = AK\_E(1) + AK\_E(2) * OP_t + AK\_E(3) * T$$

Durbin-Watson = 1.755, R-Squared = 0.3529, N = 23

Variables:	AK_E(1)	AK_E(2)	AK_E(3)
Estimated Value:	7708.4	339.65	2981.55
t-statistic:	(0.466)	(0.879)	(3.188)

### Average Natural Gas Wellhead Price

$$WP_t = AK\_F(1) + AK\_F(2) * WP_{t-1} + AK\_F(3) * PD_t$$

Durbin-Watson = 1.707, R-Squared = 0.7392, N = 22

Variables:	AK_F(1)	AK_F(2)	AK_F(3)
Estimated Value:	0.093	0.4703	0.00141
t-statistic:	(0.89)	(2.56)	(2.89)

### Industrial Natural Gas Price

$$IP_t = AK\_G(1) + AK\_G(2) * OP_t$$

Durbin-Watson = 2.149, R-Squared = 0.288, N = 12

Variables:	AK_G(1)	AK_G(2)
Estimated Value:	1.0191	0.00645
t-statistic:	(9.997)	(2.009)

where,

- ln = natural logarithm operator
- N = number of observations
- RN<sub>t</sub> = residential consumers (thousands) at current year. (AK\_RN), See Table F2
- CN<sub>t</sub> = commercial consumers (thousands) at current year. (AK\_CN), See Table F2
- OP<sub>t</sub> = total landed costs of crude oil imports (1987\$/barrel) at current year. (WOPCUR)
- YR<sub>t</sub> = natural gas consumption (Bcf)
- YR<sub>t</sub> = residential gas consumption (MMcf) at current year. (QALK\_NONU\_F(1))
- YC<sub>t</sub> = commercial gas consumption (MMcf) at current year. (QALK\_NONU\_F(2))
- YI<sub>t</sub> = industrial gas consumption (MMcf) at current year. (QALK\_NONU\_F(3))
- OP<sub>t-1</sub> = total landed costs of crude oil imports lagged one year. (WOPLAG)
- T = time trend variable having value 1, 2, 3,..., 23 starting from 1969 to 1991. In 2015, the T variable will take on the value of 47. (CNTYR+21)
- PD<sub>t</sub> = dry gas production (Bcf) at current year. (AK\_PROD)
- WP<sub>t</sub> = average wellhead price (1987\$/Mcf) at current year. (WPRCUR)
- WP<sub>t-1</sub> = average wellhead price (1987\$/Mcf) lagged one year. (WPRLAG)
- IP<sub>t</sub> = industrial gas price (1987\$/Mcf). (PALK\_NONU\_F(3))

Notes: Variables displayed in parentheses are used in the source code.

<b>VARIABLES:</b>	AK_C	Parameters for Alaskan residential natural gas consumption (Appendix E).
	AK_D	Parameters for Alaskan commercial natural gas consumption (Appendix E).
	AK_E	Parameters for Alaskan industrial natural gas consumption (Appendix E).
	AK_F	Parameters for average Alaskan natural gas wellhead price (Appendix E).
	AK_G	Parameters for Alaskan industrial natural gas price (Appendix E).

Table F2

**Data:** Exogenous forecast of the number of residential and commercial customers in Alaska

**Author:** Tianchi Wang, SAIC, July 5, 1995.

**Source:** *Natural Gas Annual* (1985-1993), DOE/EIA-0131.

**Derivation:** The number of residential consumers represents the number of residential households. In the last 25 years this number has been steadily increasing, mirroring the population growth in Alaska. Since the current year population is highly dependent on the previous year population, the number of residential consumers was estimated based on its lag value, as follows:

$$\begin{aligned} \log(RN_t) &= 0.276 + 0.9437 * \log(RN_{t-1}) \\ t &= (3.7) \quad (46) \\ R^2 &= 0.99 \\ DW &= 1.504 \text{ (rho is not statistically significant)} \end{aligned}$$

This translates into the following forecast equation:

$$RN_t = 1.3178 * RN_{t-1}^{0.9437}$$

The number of commercial consumers, based on billing units, showed a strong relationship to the number of residential households and the number of commercial consumers in the last year, as follows:

$$\begin{aligned} CN_t &= 0.1625 * RN_t \\ t &= (31) \\ R^2 &= 0.97 \\ DW &= 1.715 \\ rho &= 0.627 \text{ (t=3.3)} \end{aligned}$$

After incorporating the first-order autocorrelation, the forecast function becomes:

$$CN_t = 0.627 * CN_{t-1} + 0.16248 * RN_t - 0.10187 * RN_{t-1}$$

**Notes:** Documented in memo dated July 5, 1995 under SAIC Task 118.

**Units:** Thousands of customers.

**Variables:** AK\_RN      Number of residential natural gas customers (thousands) in Alaska (Appendix E)  
AK\_CN      Number of commercial natural gas customers (thousands) in Alaska (Appendix E)

Table F3

**Data:** Parameter estimates of the regression equation for the projection of Illinois synthetic natural gas production from liquid hydrocarbons.

**Author:** Chetha Phang, EI-823, September 1993.

**Source:** *Natural Gas Annual* 1985, DOE/EIA-0131, Table 11.  
*Natural Gas Annual* 1986, 1987, DOE/EIA-0131, Table 12.  
*Natural Gas Annual* 1988, 1989, 1990, Table 15.  
*Annual Energy Review* 1991 (Tables 71, 81, Appendix C).  
 Data created using PIPEJCL.SNGLQDS.PRDPROJ.D0420931.

**Derivation:** The method of Ordinary Least Squares (OLS) was used to estimate the parameters of the Illinois synthetic gas production from liquid hydrocarbons equation, which is assumed to be a log-linear function of East North Central regional gas price. This production function is expressed as follows:

$$\ln SNG_t = a1 + (a2 * \ln ENCGPR_t)$$

where,

$\ln$  = natural logarithm

$SNG_t$  = synthetic natural gas production from liquid hydrocarbons in Illinois in year t (Bcf)

$ENCGPR_t$  = East North Central regional gas price (1987\$/Mcf) in year t

$a1, a2$  = parameters to be estimated

The OLS regression results based on the given data (1981-1991) showed an evidence of positive serial correlation in the data with Durbin-Watson  $d = 1.125$ . Using the Generalized Difference Equations to correct for the positive serial correlation between the disturbance terms, the second stage regression results were obtained as follows:

$$\ln SNG_t = -0.5161 + 2.81803 * \ln ENCGPR_t$$

t-statistic = (0.98) (6.46)

Durbin-Watson = 1.599, R-Squared = 0.8224, N = 11

The above production equation can be written as:

$$SNG_t = SNGA1 * ENCGPR_t^{SNGA2} \text{ or, } SNG_t = 0.5968 * ENCGPR_t^{2.81803}$$

where,  $SNG_t$  and  $ENCGPR_t$  are defined in the source code as VAL and VALUE, respectively.

**Units:** Not applicable (no units).

**Variables:** SNGA1 Intercept coefficient for the Illinois synthetic gas production function (Appendix E).  
 SNGA2 Slope coefficient for the Illinois synthetic gas production function (Appendix E).



Table F4

**Data:** Coefficients for PTM forecasting equations. Total working capital; total administrative and general expense; accumulated deferred income taxes; depreciation, depletion, and amortization expenses; and total operations and maintenance expense.

**Author:** Science Applications International Corporation

**Source:** Form FERC-2: Data collected for 1980 - 1991.

**Derivation:** Estimations are done by using accounting algorithm or forecast software. Forecasts are based on a series of Fortran-based econometric equations which have been estimated using the Total Statistical Package (TSP) software. Equations are estimated for each pipeline company or generic pipeline: total working capital; total operations and maintenance expense; total administrative and general expense; depreciation, depletion, and amortization expenses; and accumulated income taxes. These equations are defined as follows:

(1) *Total Working Capital*

$$OWC_t = GPIS_t^{\beta_0} * GPIS_{t-1}^{-\rho * \beta_0} * \exp [\beta_1 * (MC\_PGDP_t - \rho * MC\_PGDP_{t-1})] \\ * \exp [\beta_2 * (TYEAR - \rho * (TYEAR - 1.0))] * OWC_{t-1}^{\rho} * OWC\_CONST$$

where,

(a) existing pipeline

$\beta_0, \beta_1, \beta_2$	= (1.92244, 1.99710, -0.170208)
$\rho$	= 0.602771
OWC_CONST	= $(1-\rho) * \exp(C+FD_j)$
FDj	= firm dummy variable which is equal to 1, if j = i, or equal to 0, otherwise. (value of FDj see Table F4.1)
t-statistic	= See Table F4.1
DW	= 1.65411
R-Squared	= 0.985791

(b) generic pipeline

$\beta_0, \beta_1, \beta_2$	= (1.76412, 1.94711, -0.159168)
$\rho$	= 0
OWC_CONST	= 294.161
t-statistic	= 3.12307, 26.9230, 1.70727, -3.31806
DW	= 1.93182
R-Squared	= 0.952241

## (2) Total Administrative and General Expense

The following equation is used to calculate the TAG before adjustments for efficiency are made:

$$TAG_{i,t} = e^{(\alpha_{1,i} * FD_i + \alpha_{2,i} * TF_{i,t})} * GPIS_{i,t-1}^{\beta_1} * W_t^{\beta_2} * PK_t^{(1-\beta_2)}$$

input variables,

$FD_i$	= pipeline specific dummy variable: equal to 1, if pipeline company i, 0 otherwise (values listed in Table F4.2b)
$TF_{i,t}$	= pipeline specific open access variable: $TRNSHR_i * FD_i$ (values for $TRNSHR_i$ listed in Table F4.2a)
$GPIS_{i,t-1}$	= original capital cost of plant in service (gross plant in service)
$W_t$	= real labor cost index, all private sector [= $MC\_ECIWSP_t / MC\_PGDP_t$ ]
$PK_t$	= rental of office space for corporations ( $RENTBLDG_t$ ): equal to rental cost index times rate of return (values listed in Table F4.2a)
i	= pipeline

resulting coefficients,

$\alpha_{1,i}$	= $FD_j$ coefficients (values listed in Table F4.2b)
$\alpha_{2,i}$	= $TF_j$ coefficients (values listed in Table F4.2b)
$\beta_1$	= coefficient of $\ln(GPIS)$ ( $TAG\_EFF1$ value in Table F4.2b)
$\beta_2$	= coefficient of labor cost ( $TAG\_EFF2$ value in Table F4.2b)

All Statistics are applied to transformed data with first order-autocorrelation correction in Log-linear regression function:

t-statistic	= See Table F4.2b
DW	= 1.94
Adjusted R-Squared	= 0.9998

The most efficient company is Trailblazer Pipeline (ID=6410), whose value of TAG represents the cost frontier in the industry.

## (3) Accumulated Deferred Income Tax

(a) existing pipeline

$$ADIT_{i,t} = \beta_0 + \beta_1 * ADIT_{i,t-1} + \beta_2 * NETPLT_i$$

where,

$\beta_0, \beta_1, \beta_2$	= (FDj + POST86, 0.72988, 0.064099)
$FD_j$	= firm dummy variable which is equal to 1, if $j = i$ , or equal to 0, otherwise. (value of $FD_j$ see Table F4.3)
$POST86_i$	= 0.129514E+7
i	= pipeline
t-statistic	= See Table F4.3
DW	= 1.85921
R-Squared	= 0.956792

(b) generic pipeline

Accumulated deferred income taxes for generic companies is calculated using an accounting algorithm. Straight Line Depreciation (SDL) is used for rate making purposes, while Modified Accelerated Cost Recovery System (MACRS) with a 15½ year schedule is used for tax purposes. The amount of depreciation using the MACRS and SDL schedules are derived as follows:

$$\text{DEPRMACRS}_t = \sum_{s=2}^{s=t} \text{NCAE}_s * \text{MACRS\_RATE}_{t-s+1}$$

$$\text{DEPRSL}_t = \sum_{s=2}^{s=t} \text{NCAE}_s / 30$$

where,

$$\text{MACRS\_RATE} = (5.00, 9.50, 8.55, 7.70, 6.93, 6.23, 5.90, 5.90, 5.91, 5.90, 5.91, 5.90, 5.91, 5.90, 5.91, 2.95)$$

$$\text{FRATE} = 35 \%$$

(4) Total Depreciation, Depletion, and Amortization

(a) existing pipeline

$$\text{DDA}_{i,t} = (1-\rho) * \beta_0 + \beta_1 * \text{NETPLT}_t + \beta_2 * \text{DEPSHR}_t + \rho * \text{DDA}_{i,t-1} - \rho * (\beta_1 * \text{NETPLT}_{t-1} + \beta_2 * \text{DEPSHR}_{t-1})$$

where,

$$\beta_0, \beta_1, \beta_2 = (\text{FD}_j, \beta_1, \beta_2)$$

$$= (\text{FD}_j, 0.037362, -0.315983\text{E}7)$$

$$\text{FD}_j = \text{firm dummy variable which is equal to 1, if } j = i, \text{ or equal to 0, otherwise. (value of FD}_j \text{ see Table F4.4)}$$

$$\rho = 0.151232$$

$$i = \text{pipeline}$$

$$\text{t-statistic} = \text{See Table F4.3}$$

$$\text{DW} = 1.77499$$

$$\text{R-Squared} = 0.9634$$

(b) generic pipeline

A regression equation is not used for the generic pipeline; instead, an accounting algorithm is used (presented in Chapter 8).

(5) Total Operations and Maintenance Expense

The following equation is used to calculate the TOM before adjustments for efficiency are made:

$$TOM_{i,t} = e^{(\alpha_{1,i} \cdot FD_i + \alpha_{2,i} \cdot TF_{i,t})} * GPIS_{i,t-1}^{\beta_1} * W_t^{\beta_2} * PK_t^{(1-\beta_2)}$$

and,

$$PK_t = (REALAA + PIPE\_DEPR - \frac{PIPE_t - PIPE_{t-1}}{PIPE_{t-1}}) * PIPE_t$$

input variables,

$FD_i$	= pipeline specific dummy variable: equal to 1, if pipeline company i, 0 otherwise (values listed in Table F4.2b)
$TF_{i,t}$	= pipeline specific open access variable: $TRNSHR_t * FD_i$ (values for $TRNSHR_t$ listed in Table F4.2a)
$GPIS_{i,t-1}$	= original capital cost of plant in service (gross plant in service)
$W_t$	= real labor cost index, all private sector [= $MC\_ECTWSP_t / MC\_PGDP_t$ ]
$PK_t$	= the user cost of capital for compressor stations
$PIPE_t$	= producer price index for compressor stations: 1.133 (index of 1990) and 1.184 (index of 1991) <sup>109</sup> [= $PIPE_{t-1} * (MC\_WPI_t / MC\_WPI_{t-1})$ ]
$PIPE\_DEPR$	= assumed depreciation rate on compressor station equipment (= 0.10 annually, from PTARIFF)
$REALAA_i$	= the real rate of AA utility bonds
$i$	= pipeline

resulting coefficients,

$\alpha_{1,i}$	= $FD_j$ coefficients (values listed in Table F4.4)
$\alpha_{2,i}$	= $TF_j$ coefficients (values listed in Table F4.5)
$\beta_1$	= coefficient of $\ln(GPIS)$ (TOM_EFF1 value listed in Table F4.5)
$\beta_2$	= coefficient of labor cost (TOM_EFF2 value listed in Table F4.5)

All Statistics are applied to transformed data with first order-autocorrelation correction in Log-linear regression function:

t-statistic	= See Table F4.5
DW	= 1.81
Adjusted R-Squared	= 0.99996

The most efficient company is Trailblazer Pipeline (ID=6410), whose value of TOM represents the cost frontier in the industry.

<sup>109</sup>Source of historical data: Bureau of Labor Statistics, 1987=1.00.

### Variables:

ADIT	=	accumulated deferred income taxes in dollars
DDA	=	depreciation, depletion, and amortization costs in dollars
DEPSHR	=	percentage of depreciation, derived from dividing accumulated depreciation by gross plant in service in previous period
FD	=	firm dummy variable which is equal to 1 if $j=i$ , 0 otherwise ( $i$ =pipeline)
FRATE	=	federal tax rate
GPIS	=	original capital cost of plant in service (gross plant in service) in dollars
MACRS_RATE	=	rate of depreciation by MACRS schedule
MC_ECIWSPNS	=	price index of labor (from Macroeconomic Activity Model)
MC_PGDP	=	implicit GDP price deflator for year $t$ (from the Macroeconomic Activity Model)
MC_WPI	=	wholesale cost index provided by Macroeconomic Activity Model
NETPLT	=	difference between original capital cost of plant in service and accumulated depreciation in previous period (net plant in service) in dollars
OWC	=	other working capital in dollars
OWC_CONST	=	estimated constant term
PIPE	=	producer price index for compressor station equipment
PIPE_DEPR	=	assumed depreciation rate on compressor station equipment
REALAA	=	the real rate of AA utility bonds
TAG	=	total administrative and general costs in real dollars
TF	=	pipeline specific open access variable ( $TRNSHR_i * FD_i$ )
TOM	=	total operating and maintenance expense in real dollars
TRNSHR	=	industry average share of gas transported for others
TYEAR	=	year in Julian units (i.e., 1995)
$W_t$	=	real labor cost index, all private sector

Notes: None.

### Units:

ADIT	=	nominal dollar
DDA	=	nominal dollar
DEPSHR	=	fraction
FRATE	=	fraction
GPIS	=	nominal dollar
MACRS_RATE	=	fraction
MC_ECIWSPNS	=	index
MC_PGDP	=	index
MC_WPI	=	index
NETPLT	=	nominal dollar
OWC	=	nominal dollar
PIPE	=	index
PIPE_DEPR	=	fraction
REALAA	=	rate
TAG	=	1987 real dollar (ultimately, converted to nominal dollar)
TOM	=	1987 real dollar (ultimately, converted to nominal dollar)
TRNSHR	=	fraction
TYEAR	=	Julian units (i.e., 1995)
$W_t$	=	index

- Reference: (1) "Documentation of the Pipeline Tariff Model Econometric Equation" by Science Applications International Corporation, April 30, 1993.  
(2) "Final Report, Documentation of Simplified PTM Algorithm," by Science Applications International Corporation, May 22, 1995.

**Table F4.1. Summary Statistics for the Total Working Capital Equation with Dummy Variables**

Coefficient	Estimated Value	Standard Error	t-statistic
C	312.686	86.8191	3.60157
LN_GPIS	1.92244	.069013	27.8560
GDP_INDX	1.99710	1.11522	1.79077
YEAR	-.170208	.044260	-3.84567
FD330	1.06750	.233223	4.57715
FD840	1.02271	.232931	4.39060
FD930	.957291	.231520	4.13481
FD1005	-.665842	.253675	-2.62479
FD1010	-1.14718	.248872	-4.60952
FD1075	-.317635	.234846	-1.35253
FD1450	1.54210	.241970	6.37310
FD1470	.970518E-02	.249324	.038926
FD1705	.350049	.234705	1.49144
FD1913	.257109	.235866	1.09006
FD2520	1.79581	.233402	7.69406
FD3240	.115678	.245968	.470296
FD3320	-.599203	.260134	-2.30344
FD3360	.737649	.235027	3.13856
FD3382	.396329	.230722	1.71778
FD3410	1.57254	.266284	5.90550
FD3450	1.02331	.253706	4.03345
FD3540	2.00584	.234659	8.54791
FD3620	-.955885	.266306	-3.58942
FD3775	-1.67645	.267098	-6.27652
FD3800	-1.79113	.257699	-6.95045
FD3835	.123892	.235964	.525046
FD4098	.764999	.267453	2.86031
FD4135	1.23531	.231506	5.33598
FD4160	-.379134	.244188	-1.55263
FD4875	-.037315	.230755	-.161708
FD5340	-.094529	.250759	-.376972
FD5715	.214417	.230721	.929338
FD5902	-.876017	.285765	-3.06552
FD6090	-1.58252	.277425	-5.70432
FD6210	.020513	.242916	.084444
FD6410	-1.14827	.246102	-4.66584
FD6420	-1.01856	.280325	-3.63351
FD6425	.357665	.236251	1.51392
FD6450	-.286970	.258668	-1.10941
FD6480	1.22267	.251145	4.86838
FD6630	-.589305	.241943	-2.43572
FD7000	.823061	.248338	3.31427
FD7010	1.89759	.334460	5.6736

**Table F4.2a. Some Input Data for Calculating Total Administrative and General Expense Equation**

Year	TRNSHR <sup>(110)</sup>	RENTBLDG <sup>(111)</sup>
1989	0.7550	0.1520
1990	0.8029	0.1600
1991	0.8367	0.1560
1992	0.8780	0.1500
1993	0.9200	0.1520
1994	0.9600	0.1630
1995	1.0000	0.1720
1996	1.0000	0.1780
1997	1.0000	0.1860
1998	1.0000	0.1960
1999	1.0000	0.2040
2000	1.0000	0.2100
2001	1.0000	0.2170
2002	1.0000	0.2250
2003	1.0000	0.2330
2004	1.0000	0.2400
2005	1.0000	0.2480
2006	1.0000	0.2570
2007	1.0000	0.2670
2008	1.0000	0.2760
2009	1.0000	0.2850
2010	1.0000	0.2940
2011	1.0000	0.3030
2012	1.0000	0.3130
2013	1.0000	0.3230
2014	1.0000	0.3340
2015	1.0000	0.3460

<sup>110</sup>Source: FERC Form 2 for 1990-1994, and assumed to be 1.0 after 1994.

<sup>111</sup>Source: DRI.

**Table F4.2b. Total Administrative and General Expense Equation with Dummy Variables**

Variable	Estimated Value	Standard Error	t-statistic
TAG_EFF1	.546521	.082891	6.59328
TAG_EFF2	.746612	.116822	6.39105
FD50	6.30018	1.71136	3.68138
FD330	6.30285	1.75090	3.59978
FD840	6.58232	1.76219	3.73590
FD930	6.28602	1.74518	3.60193
FD1005	6.80030	1.85334	3.66921
FD1010	5.85094	1.84181	3.17673
FD1075	6.48892	1.76860	3.66897
FD1450	5.99875	1.61533	3.71362
FD1470	6.88913	1.82922	3.76615
FD1705	6.68265	1.77822	3.75804
FD1913	5.90418	1.78470	3.30822
FD2050	4.96999	1.75473	2.83234
FD2520	6.56525	1.68432	3.89787
FD3240	6.81193	1.77880	3.82950
FD3320	6.89382	1.85650	3.71335
FD3360	6.26835	1.68926	3.71070
FD3382	5.95047	1.73896	3.42186
FD3410	4.91967	1.70103	2.89217
FD3450	5.89680	1.59192	3.70419
FD3540	6.42158	1.66719	3.85173
FD3620	7.26868	1.89742	3.83081
FD3775	5.33731	1.86108	2.86785
FD3800	6.87890	1.85380	3.71070
FD3835	6.55702	1.78981	3.66353
FD4098	3.56057	1.61480	2.20496
FD4135	6.00837	1.76093	3.41204
FD4160	6.72039	1.82418	3.68406
FD4875	6.13802	1.72427	3.55978
FD5340	6.84856	1.84478	3.71240
FD5715	4.73351	1.72216	2.74859
FD5902	7.01634	1.92765	3.63984
FD6090	6.80537	1.90209	3.57784
FD6210	6.73741	1.81721	3.70755
FD6410	4.11828	1.73453	2.37430
FD6420	7.09078	1.91477	3.70319
FD6425	6.36290	1.80033	3.53430
FD6450	6.05841	1.82361	3.32221
FD6480	3.91832	1.62231	2.41526
FD6630	7.08404	1.81856	3.89540

Variable	Estimated Value	Standard Error	t-statistic
FD7000	4.15445	1.69712	2.44794
TF50	.011031	.100409	.109860
TF330	.368245	.147138	2.50272
TF840	.028614	.088847	.322062
TF930	.148615	.090249	1.64671
TF1005	.148340	.090299	1.64276
TF1010	.065324	.113296	.576584
TF1075	-.148067	.080122	-1.84803
TF1450	-.084154	.112457	-.748322
TF1470	.395586	.114509	3.45464
TF1705	-.257853	.126443	-2.03929
TF1913	-.285061	.098021	-2.90817
TF2050	-.337730	.102031	-3.31009
TF2520	-.258312	.186565	-1.38457
TF3240	-1.69449	.692507	-2.44690
TF3320	-.068891	.100507	-.685436
TF3360	-.517070	.130362	-3.96641
TF3382	.057025	.270856	.210538
TF3410	1.43559	.380451	3.77338
TF3450	.279521	.774890	.360724
TF3540	-.140247	.067834	-2.06751
TF3620	.388410	.379806	1.02265
TF3775	-.171861	.111265	-1.54460
TF3800	.250739	.209853	1.19483
TF3835	-.229598	.117012	-1.96218
TF4098	-.763932E-02	.182092	-.041953
TF4135	.360972	.113808	3.17176
TF4160	-.268591	.135490	-1.98237
TF4875	-.745106	.197142	-3.77954
TF5340	-.274110	.101554	-2.69915
TF5715	.306619	.082403	3.72096
TF5902	-.047441	.093069	-.509738
TF6090	.253314	.124946	2.02739
TF6210	.424396E-02	.087744	.048367
TF6410	-.655675	.185596	-3.53280
TF6420	-.177991	.056635	-3.14278
TF6425	.310575	.213246	1.45641
TF6450	-.057026	.206198	-.276561
TF6480	.707801	.309742	2.28513
TF6630	-.134852	.110205	-1.22365
TF7000	-.235443	.097350	-2.41851



**Table F4.3. Summary Statistics for Accumulated Deferred Income Tax Equation with Dummy Variables**

Coefficient	Estimated Value	Standard Error	t-statistic
$\beta_1$	.729880	.034326	21.2633
$\beta_2$	.064099	.010285	6.23223
POST86	.129514E+07	.597315.	2.16827
FD50	-.585536E+07	.421084E+07	-1.39054
FD330	.103331E+08	.432398E+07	2.38973
FD840	-.150482E+07	.398517E+07	-.377605
FD930	-.127081E+08	.577500E+07	-2.20054
FD1005	.792681E+08	.478025E+08	1.65824
FD1010	.500322E+07	.399926E+07	1.25104
FD1075	.866611E+07	.423324E+07	2.04716
FD1450	-.170162E+07	.138914E+07	-1.22495
FD1470	.288398E+08	.147628E+08	1.95354
FD1705	-.261066.	.430122E+07	-.060696
FD1913	.107255E+07	.392570E+07	.273212
FD2050	-.331096.	.252541E+07	-1.31106
FD2520	100804.	.149690E+07	.067342
FD3240	-.386891E+07	.265839E+07	-1.45536
FD3320	.246935E+07	.143454E+08	.172135
FD3360	-.655528.	.289783E+07	-.226214
FD3382	.134276E+07	.257215E+07	.522039
FD3410	-.415096.	.279459E+07	-1.48536
FD3450	.746529.	.175377E+07	.425670
FD3540	-.253967E+07	.225567E+07	-1.12590
FD3620	-.155808E+07	.187475E+08	-.083108
FD3775	.229058E+08	.130580E+08	1.75416
FD3800	.376959E+08	.384250E+08	.981025
FD3835	.891349E+07	.766289E+07	1.16320
FD4098	-.666686.	.131096E+07	-.508549
FD4135	-.790190E+07	.292055E+07	-2.70562
FD4160	.188337E+08	.957605E+07	1.96675
FD4875	.157189E+07	.105719E+08	.148685
FD5340	.115389E+07	.746511E+07	.154571
FD5715	.766982.	.163080E+07	.470309
FD5902	.383549E+08	.382716E+08	1.00218
FD6090	.526591E+08	.443985E+08	1.18606
FD6210	-.139606E+07	.738119E+07	-.189137
FD6410	.222869E+07	.592477E+07	.376165
FD6420	.530083E+08	.214303E+08	2.47352
FD6425	-.166049E+07	.683077E+07	-.243089
FD6450	.257150E+08	.150151E+08	1.71262
FD6480	-.555813.	.569203.	-.976475
FD6630	-.244766E+08	.231915E+08	-1.05541
FD7000	-.156129E+07	.439756E+07	-.355035

**Table F4.4. Summary Statistics for Depreciation, Depletion, and Amortization Equation with Dummy Variables**

Coefficient	Estimated Value	Standard Error	t-statistic
$\beta_1$	.037362	.215921E-02	17.3036
$\beta_2$	-.315983E+07	.118222E+07	-2.67278
FD50	.524613E+07	835848.	6.27641
FD330	.172594E+07	.105781E+07	1.63161
FD840	.699559E+07	.100105E+07	6.98822
FD930	.563834E+07	.134644E+07	4.18759
FD1005	.971449E+07	.245244E+07	3.96115
FD1010	.363580E+08	.307654E+07	11.8178
FD1075	.920971E+07	.116537E+07	7.90282
FD1450	.242638E+07	785470.	3.08908
FD1470	.130872E+08	.161691E+07	8.09396
FD1705	.142000E+08	.125675E+07	11.2990
FD1913	.923499E+07	.130261E+07	7.08962
FD2050	.170989E+08	.253646E+07	6.74126
FD2520	.384055E+07	759960.	5.05362
FD3240	.584337E+07	.141660E+07	4.12492
FD3320	.307323E+08	.606948E+07	5.06341
FD3360	.380696E+07	.104426E+07	3.64560
FD3382	.637875E+07	881543.	7.23589
FD3410	.233743E+07	619300.	3.77430
FD3450	.231227E+07	634010.	3.64705
FD3540	.314533E+07	595989.	5.27751
FD3620	.369447E+08	.878650E+07	4.20471
FD3775	-.595437E+07	.114663E+08	-.519293
FD3800	.279146E+08	.498743E+07	5.59699
FD3835	.912853E+07	.202461E+07	4.50877
FD4098	.118440E+07	463369.	2.55605
FD4135	.155105E+08	.413476E+07	3.75123
FD4160	.122954E+08	.177809E+07	6.91496
FD4875	.789833E+07	.326112E+07	2.42197
FD5340	.282235E+08	.192597E+07	14.6542
FD5715	.897115E+07	.105040E+07	8.54073
FD5902	.817257E+08	.100491E+08	8.13266
FD6090	.455475E+08	.437448E+07	10.4121
FD6210	.176696E+08	.157079E+07	11.2489
FD6410	.266977E+07	.242852E+07	1.09934
FD6420	.620667E+08	.391804E+07	15.8413
FD6425	.111083E+08	.291027E+07	3.81694
FD6450	.202480E+08	.152389E+07	13.2870
FD6480	.496049E+07	839117.	5.91156
FD6630	.175537E+08	.288080E+07	6.09335
FD7000	.217175E+07	.209350E+07	1.03737

**Table F4.5. Summary Statistics for Total Operations and Maintenance Expense Equation with Dummy Variables**

Coefficient	Estimated Value	Standard Error	t-statistic
TOM_EFF1	.471373	.068874	6.84399
TOM_EFF2	.889413	.053922	16.4945
FD50	6.96331	1.30001	5.35634
FD330	7.57578	1.33699	5.66628
FD840	7.73947	1.34233	5.76570
FD930	7.41393	1.33069	5.57148
FD1005	8.36626	1.41871	5.89707
FD1010	7.66465	1.40895	5.43996
FD1075	8.03127	1.34883	5.95426
FD1450	7.11237	1.22266	5.81714
FD1470	8.38273	1.39905	5.99171
FD1705	7.67533	1.35517	5.66374
FD1913	8.27210	1.36329	6.06775
FD2050	7.99393	1.33608	5.98311
FD2520	7.34498	1.27522	5.75977
FD3240	6.84323	1.33042	5.14365
FD3320	8.28663	1.42266	5.82476
FD3360	7.35924	1.28387	5.73208
FD3382	6.90328	1.31986	5.23031
FD3410	7.37303	1.25586	5.87088
FD3450	6.91595	1.22364	5.65195
FD3540	7.45088	1.26369	5.89613
FD3620	8.26597	1.44693	5.71275
FD3775	5.47017	1.42607	3.83584
FD3800	8.55488	1.41678	6.03824
FD3835	7.10535	1.36952	5.18822
FD4098	4.97742	1.21899	4.08325
FD4135	6.66477	1.34207	4.96602
FD4160	8.67776	1.39450	6.22286
FD4875	6.97743	1.31890	5.29034
FD5340	7.99649	1.41132	5.66598
FD5715	6.99626	1.30970	5.34188
FD5902	8.13507	1.48410	5.48150
FD6090	8.61460	1.46708	5.87194
FD6210	8.15784	1.38849	5.87533
FD6410	5.19687	1.31866	3.94101
FD6420	8.31096	1.47041	5.65214
FD6425	8.16514	1.38047	5.91476
FD6450	7.85647	1.39139	5.64649
FD6480	5.75349	1.21779	4.72453
FD6630	8.14303	1.39281	5.84646

Coefficient	Estimated Value	Standard Error	t-statistic
FD7000	5.28159	1.29356	4.08298
TF50	.020084	.068888	.291553
TF330	-.134264	.206530	-.650097
TF840	-.134700	.039999	-3.36756
TF930	.415624	.148109	2.80619
TF1005	.017809	.057366	.310443
TF1010	.061322	.072269	.848519
TF1075	-.261762	.098872	-2.64748
TF1450	.084376	.167036	.505136
TF1470	.366504	.103084	3.55539
TF1705	.052810	.047528	1.11113
TF1913	-1.18168	.140446	-8.41381
TF2050	-.322587	.055622	-5.79967
TF2520	-.250722	.063448	-3.95163
TF3240	-.073692	.315465	-.233597
TF3320	-.173362	.124727	-1.38993
TF3360	-.381712	.162348	-2.35119
TF3382	.065795	.140738	.467497
TF3410	-.386684	.093987	-4.11423
TF3450	.449951	.740135	.607931
TF3540	-.085064	.075943	-1.12011
TF3620	-.166116	.131860	-1.25979
TF3775	-.102120	.090072	-1.13376
TF3800	-.242226	.085042	-2.84832
TF3835	.565609	.194963	2.90111
TF4098	-.348827	.116545	-2.99307
TF4135	.460569	.105199	4.37809
TF4160	-.495938	.105004	-4.72306
TF4875	-.588361	.291423	-2.01892
TF5340	-.144959	.051680	-2.80494
TF5715	-.298722	.085840	-3.47999
TF5902	.238422	.179567	1.32776
TF6090	.249150	.271168	.918804
TF6210	-.089265	.052300	-1.70679
TF6410	-.962534	.103827	-9.27059
TF6420	-.198308	.057589	-3.44353
TF6425	-.457778	.275375	-1.66238
TF6450	-.147791	.070887	-2.08489
TF6480	-.134680	.060004	-2.24452
TF6630	-.415677	.177621	-2.34025
TF7000	-.629484	.191316	-3.29029



## **Appendix G**

### **Variable Cross Reference Table**



# Variable Cross Reference Table

The linear program (LP) formulation of the Annual Flow Module (AFM) is presented in matrix form in Figure G-1. The rows represent the objective function, variable bounds, and problem constraints, and the columns are the variables to be solved. Each row (constraint) and column (variable) have been given a unique name which also are defined in Figure G-1. The row and column names are used in the code to identify where changes are to be made in the working matrix during each model iteration or model year. Since the variables defined in the AFM LP equations are being referenced differently within 1) the mathematical equations presented in Chapter 5, 2) the LP matrix (referenced above), and 3) the code, a cross reference table (Table G-1) has been generated for these variables.

Similarly, Figure G-2 presents the LP matrix representation of the Capacity Expansion Module (CEM) formulation, as well as definitions of the abbreviations and names used. Again, the columns represent the variables, and the rows represent the objective function, variable bounds, and problem constraints corresponding to the model equations defined in Chapter 7. Table G-2 presents a cross reference of the names used within 1) the mathematical equations presented in Chapter 7, 2) the LP matrix (referenced above), and 3) the code to reference the variables in the model equations.

Note that in both figures, two coefficients are defined for a single variable in the mass balance constraints. This is a shortcut means of representing the coefficient associated with the same flow variable that is needed within two mass balance constraints. For example, when the arc represents flow into a node, the coefficient is the arc efficiency variable; however, when the arc represents flow going out of a node, the flow should not be reduced by efficiency, thus the coefficient is one.

The Distributor Tariff Module (DTM) and Pipeline Tariff Module (PTM) are represented by economic and regression equations (see Chapters 6 and 8 for details). Tables G-3 and G-4 present cross references of model equation variables defined in this document and in the code for the DTM and PTM, respectively.

**Figure G-1. LP Matrix Definition for the Annual Flow Module (AFM)**

X	X	X	X	X	X	X	X	S	F	F	F	I	I	I	R
F	I	F	I	F	I	F	I	S	*	*	*	*	*	*	H
N	N	S	S	N	N	Q	Q	+	*	*	*	*	*	*	S
*	*	+	+	*	*	*	*	+	B	P	N	B	P	N	
*	*	+	+	*	*	*	*	N	?	?	?	?	?	?	
N	N	N	N	?	?	?	?	*	0	0	0	0	0	0	
*	*	*	*	0	0	0	0	*	0	0	0	0	0	0	
*	*	*	*	0	0	0	0	#	#	#	#	#	#	#	

[illegible]

CPN**N**	1	1								<= QCAP0(i,j)*UTILZT(i,j)*(1-PCTW)
CPF**N**	1									<= QCAP0(i,j)*UTILZF(i,j)*(1-PCTW)
MFN**	EFF,-1	EFF	-1						=	-1*NETSTR_F + DISCR_F
MIN**	EFF,-1	EFF	-1						=	-1*NETSTR_I + DISCR_I
MF***???			EFF	1	-1	-1	1		=	0
MI***???			EFF	1				-1 -1 1	=	0
MS++N**		-1 -1		1					=	0

Legend: \*\* = nodes (01-21), ++ = OGSM region (01-06), ? = sector code (R,C,I,T,U),  
 @@ = CENSUS (01-09) or NERC region (01-13), # = step number on curve (1-9)



**Figure G-1. LP Matrix Definition for the Annual Flow Module (AFM) (Continued)**

**Columns**

XFN**N**	=	Firm flow from node to node
XIN**N**	=	Interruptible flow from node to node
XFS++N**	=	Firm flow from supply to node
XIS++N**	=	Interruptible flow from supply to node
XFN**?@@	=	Firm flow to end-use sector
XIN**?@@	=	Interruptible flow to end-use sector
XFQ**?@@	=	Firm flow from backstop supply to end-use sector
XIQ**?@@	=	Interruptible flow from backstop to end-use sector
SS++N**#	=	Steps on regional supply curve
F**B?@@	=	Base step on core demand curve
F**P?@@#	=	Positive steps on core demand curve
F**N?@@#	=	Negative steps on core demand curve
I**B?@@	=	Base step on noncore demand curve
I**P?@@#	=	Positive steps on noncore demand curve
I**N?@@#	=	Negative steps on noncore demand curve
RHS	=	Right hand side of constraint equations

---

**Rows**

AFMOBJ	=	AFM Objective Function
AFMBND	=	AFM Variable Bounds
CPN**N**	=	Pipeline capacity limit--Total flow
CPF**N**	=	Pipeline capacity limit--Firm flow
MFN**	=	Regional mass balance--Firm network
MIN**	=	Regional mass balance--Interruptible network
MF**?@@	=	End-use mass balance--Firm network
MI**?@@	=	End-use mass balance--Interruptible network
MS++N**	=	Supply subregion mass balance

---

Legend: \*\* = nodes (01-21), ++ = OGSM region (01-06), ? = sector code (R,C,I,T,U),  
 @@ = CENSUS (01-09) or NERC region (01-13), # = step number on curve (1-9)

**Figure G-1. LP Matrix Definition for the Annual Flow Module (AFM) (Continued)**

Coefficients, Right Hand Sides (RHS), and Bounds

EFF	=	Regional pipeline efficiency
TARF	=	Supply, distributor, pipeline tariffs--Firm network
TARI	=	Supply, distributor, pipeline tariffs--Interruptible network
PZZF	=	Alt. fuel price for backstop supply--Firm network
PZZI	=	Alt. fuel price for backstop supply--Interruptible network
PSUP	=	Prices on supply curve steps (87\$/mcf)
USUP	=	Quantities on supply curve steps (BCF)
PDEMF	=	Prices on demand curve steps (87\$/mcf)--core (Firm service)
PDEMI	=	Prices on demand curve steps (87\$/mcf)--noncore (Interruptible service)
UDEMF	=	Quantities on demand curve steps (BCF)--core (Firm service)
UDEMI	=	Quantities on demand curve steps (BCF)--noncore (Interruptible service)
MINFF	=	Minimum flow along interregional arc--firm
MINFI	=	Minimum flow along interregional arc--interruptible
MINSF	=	Minimum flow from supply to node--firm network
MINSI	=	Minimum flow from supply to node--interruptible network
QCAP0	=	Physical pipeline capacity (BCF) for year t
UTILZT	=	Pipeline utilization--Total flow
UTILZF	=	Pipeline utilization--Firm flow
PCTW	=	Weather factor percent
NETSTR_F	=	Net firm storage withdrawals
NETSTR_I	=	Net interruptible storage withdrawals
DISCR_F	=	Supply/demand discrepancy for Firm network
DISCR_I	=	Supply/demand discrepancy for Interruptible network

---

**Table G-1. Cross Reference of AFM Variables Between Documentation, LP, and Code**

Documentation	AFM LP Variable	Code Variable
<b>Objective Function Variables:</b>		
$x_{s,i}^F$	XFS++N**	AFLOW_F(s,i)
$x_{s,i}^I$	XIS++N**	AFLOW_I(s,i)
$x_{ij}^F$	XFN**N**	AFLOW_F(i,j)
$x_{ij}^I$	XIN**N**	AFLOW_I(i,j)
$x_{i,d}^F$	XFN**?@@	AFLOW_F(i,d)
$x_{i,d}^I$	XIN**?@@	AFLOW_I(i,d)
$qzz_{i,d}^F$	XFQ**?@@	F_BKSTOP
$qzz_{i,d}^I$	XIQ**?@@	I_BKSTOP
$ysup_{s,i,k}$	SS++N**#	SUP_QTY(s,i,sr)
$QDEM0_{i,d}^F$ & $ydem_{i,d,k}^F$	F**BU@@ F**PU@@# F**NU@@#	UTIL_QTY_F(i,sr)
	F**B?@@ F**P?@@# F**N?@@#	NONU_QTY_F(d,i,sr) (where d = ? = r,c,i,t)
$QDEM0_{i,d}^I$ & $ydem_{i,d,k}^I$	I**BU@@ I**PU@@# I**NU@@#	UTIL_QTY_I(i,sr)
	I**B?@@ I**P?@@# I**N?@@#	NONU_QTY_I(d,i,sr) (where d = ? = r,c,i,t)
<b>Variable Bounds:</b>		
	UDEM(F(BASE FIRM))	BASE_QTY, EXPQTY
	UDEM(I(BASE INT))	BASE_QTY, EXPQTY
$UDEM_{i,d,k}^F$	UDEM(F(POS FIRM))	DQDEL(ns) from DQUANT(ns), DELQ
$UDEM_{i,d,k}^F$	UDEM(F(NEG FIRM))	DQDEL(ns) from DQUANT(ns), DELQ
$UDEM_{i,d,k}^I$	UDEM(I(POS INT))	DQDEL(ns) from DQUANT(ns), DELQ
$UDEM_{i,d,k}^I$	UDEM(I(NEG INT))	DQDEL(ns) from DQUANT(ns), DELQ
$USUP_{s,i,k}$	USUP	SQDEL(ns) from SQUANT(ns)
$MINF_{ij}^F$	MINFF	ACAP_MIN
$MINF_{ij}^I$	MINFI	ACAP_MIN
!!!!	MINSF	MINSUPF
!!!!	MINSI	MINSUPI

**Table G-1. Cross Reference of AFM Variables Between Documentation, LP, and Code  
(Continued)**

Documentation	AFM LP Variable	Code Variable
<b>Objective Function Coefficients</b>		
	PDEMF(BASE FIRM)	BASE_PR, EXPPR
	PDEMI(BASE INT)	BASE_PR, EXPPR
$PDEM^F_{i,d,k}$	PDEMF(POS FIRM)	DPRICE(ns)
$PDEM^F_{i,d,k}$	PDEMF(NEG FIRM)	DPRICE(ns)
$PDEM^I_{i,d,k}$	PDEMI(POS INT)	DPRICE(ns)
$PDEM^I_{i,d,k}$	PDEMI(NEG INT)	DPRICE(ns)
$PSUP_{s,i,k}$	PSUP	SPRICE(ns)
$PZZ^F_{i,d}$	PZZF	NG_BKSTOP_PR
$PZZ^I_{i,d}$	PZZI	NG_BKSTOP_PR
$TAR^F_{s,i}$	TARF(S->N)	STAR_F(s,i)
$TAR^I_{s,i}$	TARI(S->N)	STAR_I(s,i)
$TAR^F_{i,j}$	TARF(N->N)	PTAR_F(i,j)
$TAR^I_{i,j}$	TARI(N->N)	PTAR_I(i,j)
$TAR^F_{i,d}$	TARF(N->D)	UTIL_DTAR_F(i,d) NONU_DTAR_F(i,d) CANTAR_F(i,d) MEXTAR_F(i,d)
$TAR^I_{i,d}$	TARI(N->D)	UTIL_DTAR_I(i,d) NONU_DTAR_I(i,d) CANTAR_I(i,d) MEXTAR_I(i,d)
<b>Capacity Constraints:</b>		
equation: 24 PCAPMAX <sub>ij</sub> AUTILZ <sup>T</sup> <sub>ij</sub> WTHRXCAP <sub>ij</sub>	rowname: CPN**N** QCAP0(i,j) UTILZT(i,j) PCTW	rowname: CPN**N** PCAP_MAX(i,j,p) AUTILZ_T(i,j,p) WTHR_XCAP(i,j)
equation: 25 PCAPMAX <sub>ij</sub> AUTILZ <sup>F</sup> <sub>ij</sub> WTHRXCAP <sub>ij</sub>	rowname: CPF**N** QCAP0(i,j) UTILZF(i,j) PCTW	rowname: CPF**N** PCAP_MAX(i,j,p) AUTILZ_F(i,j,p) WTHR_XCAP(i,j)

**Table G-1. Cross Reference of AFM Variables Between Documentation, LP, and Code  
(Continued)**

Documentation	AFM LP Variable	Code Variable
<b>Mass Balance Constraints at Transshipment Nodes:</b>		
equation: 26 QSTR <sub>ST</sub> <sup>F</sup> DISCR <sub>m</sub> <sup>F</sup>	rowname: MFN** NETSTR_F DISCR_F	rowname: MFN** NETSTR_F(i,p) DISCR_F(i)
equation: 27 QSTR <sub>ST</sub> <sup>I</sup> DISCR <sub>m</sub> <sup>I</sup>	rowname: MIN** NETSTR_I DISCR_I	rowname: MIN** NETSTR_I(i,p) DISCR_I(i)
Coefficients: EFF <sub>lm</sub> EFF <sub>sm</sub>	EFF(N->N) EFF(S->N)	AEFF_PIPE(i,m) SEFF_PIPE(s,sr)
<b>Mass Balance Constraints at Demand Points:</b>		
equation: 28 QDEMO <sub>ld</sub> <sup>F</sup>	rowname: MF**?@@ F**B?@@	rowname: MF**?@@ UTIL_QTY_F, NONU_QTY_F
equation: 29 QDEMO <sub>ld</sub> <sup>I</sup>	rowname: MI**?@@ I**B?@@	rowname: MI**?@@ UTIL_QTY_I, NONU_QTY_I
coefficients: EFF <sub>ld</sub>	EFF(N->D)	UEFF_PIPE(i,d) NEFF_PIPE(i,d) CANEFF(i) MEXEFF(i)
<b>Mass Balance Constraint at Supply Points:</b>		
equation: 30	rowname: MS++N**	rowname: MS++N**
i,j,m= transshipment nodes, s= source, d = demand node, sr= subregion, p= forecast year, ST=storage, k,ns= steps on supply curve, sr= subregion.		

**Figure G-2. LP Matrix Definition for the Capacity Expansion Module (CEM)**

P	P	O	O	P	P	O	O	P	P	O	O	P	O
F	I	F	I	F	I	F	I	F	I	F	I	I	I
N	N	N	N	S	S	S	S	N	N	N	N	Q	Q
*	*	*	*	+	+	+	+	*	*	*	*	*	*
*	*	*	*	+	+	+	+	*	*	*	*	*	*
N	N	N	N	N	N	N	N	?	?	?	?	?	?
*	*	*	*	*	*	*	*	0	0	0	0	0	0
*	*	*	*	*	*	*	*	0	0	0	0	0	0

CEMOBJ	TARF	TARI	TARF	TARI	TARP	TARP	TARO	TARO	TARPF	TARPI	TAROF	TAROI	PZZPI	PZZOI
CEMEND	U													
	L	MINPF		MINOF										

MPFN**	EP, -1		EP				-1							
MPIN**		EP, -1		EP				-1						
MOFN**			EO, -1		EO				-1					
MOIN**				EO, -1		EO				-1				
MSTN**														
MPF**?00							EP							
MPI**?00								EP				1		
MOF**?00									EO					
MOI**?00										EO			1	
CPF**N**	1													
CPI**N**	1	1												
CON**N**			1	1										
CPFSTN**														
CPISTN**														
SPS++N**					1	1								
SOS++N**							1	1						
TPBKSTOP													1	
TOBKSTOP														1

Legend: \*\* = nodes (01-21), ++ = OGSM region (01-06), ? = sector code (R,C,I,T,U),  
 00 = CENSUS (01-09) or NERC region (01-13), # = step number on curve (0-9)

**Figure G-2. LP Matrix Definition for the Capacity Expansion Module (CEM) (Continued)**

	P	P	O	O	S	S	C	R
	F	I	F	I	S	T	N	H
	S	S	S	S	+	N	*	S
	T	T	T	T	+	*	*	
	N	N	N	N	N	*	N	
	*	*	*	*	*	*	*	
	*	*	*	*	*	*	*	
CEMOBJ	U	PFSTU	PISTU	OFSTU	OISTU	USUP	USTR	UCAP
CEMBND	L	PFSTL	PISTL	OFSTL	OISTL	0	0	0
MPFN**	1							DISCRPF(i)
MPIN**	1							DISCRPI(i)
MOFN**		-1						DISCROF(i)
MOIN**			-1					DISCROI(i)
MSTN**	-1	-1	EOSTR	EOSTR				0
MPF**700								QDEMOPF(i,d)
MPI**700								QDEMOPI(i,d)
MOF**700								QDEMOOF(i,d)
MOI**700								QDEMOOI(i,d)
CPF**N**						-UPF(i,j)	=	0
CPI**N**						-UP(i,j)	<=	0 (CEM loop 1)
							<=	QCAP0 - YCAP0 (CEM loop 2)
CON**N**						-UO(i,j)	<=	0
CPFSTN**	1					-UPFSTR	=	0
CPISTN**	1	1				-UPSTR	<=	0 (CEM loop 1)
							<=	QSTR0 - YSTR0 (CEM loop 2)
SPS**N**					-UPP(s,i)		=	0
SOS**N**					-UPO(s,i)		<=	0 (STYP=1,2)
							=	0 (STYP=3,8)
TPBKSTOP								
TOBKSTOP								

Legend: \*\* = nodes (01-21), ++ = OGSM region (01-06), ? = sector code (R,C,I,T,U),  
 00 = CENSUS (01-09) or NERC region (01-13), # = step number on curve (0-9)

**Figure G-2. LP Matrix Definition for the Capacity Expansion Module (CEM) (Continued)**

**Columns**

PFN**N**	=	Peak Firm flow from node to node
PIN**N**	=	Peak Interruptible flow from node to node
OFN**N**	=	Off-Peak Firm flow from node to node
OIN**N**	=	Off-Peak Interruptible flow from node to node
PFS++N**	=	Peak Firm flow from supply to node
PIS++N**	=	Peak Interruptible flow from supply to node
OFS++N**	=	Off-Peak Firm flow from supply to node
OIS++N**	=	Off-Peak Interruptible flow from supply to node
PFN**?@@	=	Peak Firm flow to end-use sector
PIN**?@@	=	Peak Interruptible flow to end-use sector
OFN**?@@	=	Off-Peak Firm flow to end-use sector
OIN**?@@	=	Off-Peak Interruptible flow to end-use sector
PIQ**?@@	=	Peak Interruptible flow from backstop supply to end-use sector
OIQ**?@@	=	Off-Peak Interruptible flow from backstop supply to end-use sector
PFSTN**	=	Peak Firm flow from storage
PISTN**	=	Peak Interruptible flow from storage
OFSTN**	=	Off-Peak Firm flow from into storage
OISTN**	=	Off-Peak Interruptible flow from into storage
SS&N**#	=	Steps on regional supply curve
STN**#	=	Steps on storage capacity expansion curve
CC**N**#	=	Steps on pipeline capacity expansion curve
RHS	=	Right hand side of constraint equations

**Rows**

CEMOBJ	=	CEM Objective Function
CEMBND	=	CEM Variable Bounds
MPFN**	=	Regional mass balance--Peak Firm network
MPIN**	=	Regional mass balance--Peak Interruptible network
MOFN**	=	Regional mass balance--Off-Peak Firm network
MOIN**	=	Regional mass balance--Off-Peak Interruptible network
MSTN**	=	Regional mass balance--Storage points
MPF**?@@	=	End-use mass balance--Peak Firm network
MPI**?@@	=	End-use mass balance--Peak Interruptible network
MOF**?@@	=	End-use mass balance--Off-Peak Firm network
MOI**?@@	=	End-use mass balance--Off-Peak Interruptible network
CPF**N**	=	Pipeline capacity limit--Peak Firm flow
CPI**N**	=	Pipeline capacity limit--Total Peak flow
CON**N**	=	Pipeline capacity limit--Total Off-Peak flow
CPFSTN**	=	Regional storage capacity limit--Peak Firm flow
CPISTN**	=	Regional storage capacity limit--Total Peak flow
SPS++N**	=	Region supply limits for total Peak flows
SOS++N**	=	Region supply limits for total Off-Peak flows
TPBKSTOP	=	Backstop used--Total Peak
TGBKSTOP	=	Backstop used--Total Off-Peak

Legend: \*\* = nodes 01-21, ++ = OGSM region 01-06, ? = sector code,  
 @@ = CENSUS or NERC region, 01-13, # = step number on curve



**Figure G-2. LP Matrix Definition for the Capacity Expansion Module (CEM) (Continued)**

Coefficients, Right Hand Side (RHS), and Bounds

TARF	=	Interregional pipeline tariffs--Firm networks
TARI	=	Interregional pipeline tariffs--Interruptible networks
TARP	=	Supply gathering charges--Peak networks
TARO	=	Supply gathering charges--Off-Peak networks
TARPF	=	Distributor tariffs--Peak Firm network
TARPI	=	Distributor tariffs--Peak Interruptible network
TAROF	=	Distributor tariffs--Off-Peak Firm network
TAROI	=	Distributor tariffs--Off-Peak Intrp. network
PZZPI	=	Alt. fuel price for backstop supply--Peak Interruptible network
PZZOI	=	Alt. fuel price for backstop supply--Off-Peak Interruptible network
PSUP	=	Prices on supply curve steps (87\$/mcf)
USUP	=	Quantities on supply curve steps (BCF)
PSTR	=	Prices on storage capacity curve steps (87\$/mcf)
USTR	=	Quantities on storage capacity curve steps (BCF)
PCAP	=	Prices on pipeline capacity curve steps (\$/mcf)
UCAP	=	Quantities on pipeline capacity curve step (BCF)
MINPF	=	Minimum interregional flow--Peak Firm
MINOF	=	Minimum interregional flow--Off-Peak Firm
PFSTU	=	Maximum flow from storage to Peak Firm network
PFSTL	=	Minimum flow from storage to Peak Firm network
PISTU	=	Maximum flow from storage to Peak Interruptible network
PISTL	=	Minimum flow from storage to Peak Interruptible network
OFSTU	=	Maximum flow from storage to Off-Peak Firm network
OFSTL	=	Minimum flow from storage to Off-Peak Firm network
OISTU	=	Maximum flow from storage to Off-Peak Interruptible network
OISTL	=	Minimum flow from storage to Off-Peak Interruptible network
EP	=	Regional pipeline efficiency--Peak networks
EO	=	Regional pipeline efficiency--Off-Peak networks
EOSTR	=	Regional storage efficiency
UPF	=	Utilization factor for Peak Firm flows (i.e., .33 * .95)
UP	=	Utilization factor for total Peak flows (i.e., .33 * .99)
UO	=	Utilization factor for total Off-Peak flows (i.e., .67 * .80)
UPFSTR	=	Utilization factor for Peak Firm storage flows
UPSTR	=	Utilization factor for total Peak storage flows
UPP	=	Maximum % supply available for Peak flows (i.e., .33 * .99)
UPO	=	Maximum % supply available for Off-Peak flows (i.e., .33 * .85)
DISCRPF	=	Supply/demand discrepancy for Peak Firm network
DISCRPI	=	Supply/demand discrepancy for Peak Interruptible network
DISCROF	=	Supply/demand discrepancy for Off-Peak Firm network
DISCROI	=	Supply/demand discrepancy for Off-Peak Interruptible network
QDEMOPF	=	Peak core (Firm service) demands (BCF) for year t+n+h or t+n
QDEMOPi	=	Peak noncore (Interruptible service) demands (BCF) for year t+n+h or t+n
QDEMOPF	=	Off-Peak core (Firm service) demands (BCF) for year t+n+h or t+n
QDEMOPi	=	Off-Peak noncore (Interruptible service) demands (BCF) for year t+n+h or t+n
QSTRO	=	Existing + Planned storage capacity (BCF) for year t+n
YSTRO	=	Utilized capacity (BCF) in alpha loop 1

**Table G-2. Cross Reference of CEM Variables Between Documentation, LP, and Code**

Documentation	CEM LP variable	Code variable
<b>Objective Function Variables:</b>		
$x_{s,i}^{PF}$	PFS++N**	PF_FLOW(s,i) & PFAK & PFFLOW
$x_{s,i}^{PI}$	PIS++N**	PI_FLOW(s,i) & PIFLOW
$x_{s,i}^{OF}$	OFS++N**	OF_FLOW(s,i) & OFAK & OFFLOW
$x_{s,i}^{OI}$	OIS++N**	OI_FLOW(s,i) & OIFLOW
$x_{ij}^{PF}$	PFN**N**	PF_FLOW(i,j) & PF
$x_{ij}^{PI}$	PIN**N**	PI_FLOW(i,j)
$x_{ij}^{OF}$	OFN**N**	OF_FLOW(i,j) & OF
$x_{ij}^{OI}$	OIN**N**	OI_FLOW(i,j)
$x_{i,d}^{PF}$	PFN**?@@	PF_FLOW(i,d)
$x_{i,d}^{PI}$	PIN**?@@	PI_FLOW(i,d)
$x_{i,d}^{OF}$	OFN**?@@	OF_FLOW(i,d)
$x_{i,d}^{OI}$	OIN**?@@	OI_FLOW(i,d)
$qzz_{i,d}^{PI}$	PIQ**?@@	BKSTOP
$qzz_{i,d}^{OI}$	OIQ**?@@	BKSTOP
$x_{sti}^{PF}$	PFSTN**	PFSTR
$x_{sti}^{PI}$	PISTN**	PISTR
$x_{sti}^{OF}$	OFSTN**	OFSTR
$x_{sti}^{OI}$	OISTN**	OISTR
$ysup_{s,i,k}$	SS++N**#	SQUANT(ns)
QSTRO & ystr <sub>s,i,k</sub>	STN**#	QSTR
QCAPO & ycap <sub>s,i,k</sub>	CN**N**#	QCAP
<b>Variable Bounds:</b>		
USUP <sub>s,i,k</sub>	USUP	SQDEL(ns) from SQUANT(ns)
USTR <sub>s,i,k</sub>	USTR	QSTRCURV(i) & CEM_QSTR(i,nst)
UCAP <sub>s,i,k</sub>	UCAP	QCAPCURV(i) & CEM_QCAP(i,nc)
MXSTR <sub>s,i</sub> (xx=PF,PI,OF,OI)	PFSTU, PISTU, OFSTU, OISTU	PFSTRBND <sub>i,2</sub> , PISTRBND <sub>i,2</sub> , OFSTRBND <sub>i,2</sub> , OISTRBND <sub>i,2</sub>
MNSTR <sub>s,i</sub> (xx=PF,PI,OF,OI)	PFSTL, PISTL, OFSTL, OISTL	PFSTRBND <sub>i,1</sub> , PISTRBND <sub>i,1</sub> , OFSTRBND <sub>i,1</sub> , OISTRBND <sub>i,1</sub>
PCTMFLO <sub>ij</sub> <sup>F</sup> * ESTFLOW <sub>ij</sub> <sup>F</sup> * SHR <sub>ij</sub> <sup>PF</sup> PCTMFLO <sub>ij</sub> <sup>F</sup> * ESTFLOW <sub>ij</sub> <sup>F</sup> * SHR <sub>ij</sub> <sup>OF</sup> MINBIFLO	MINPF MINOF	MINXPF MINXOF MINBIOF, MINBIOI, MINBIPF, MINBIPI

**Table G-2. Cross Reference of CEM Variables Between Documentation, LP, and Code  
(Continued)**

Documentation	CEM LP variable	Code variable
<b>Objective Function Coefficients:</b>		
$TAR^P_{s,i}$	TARP	TARP(styp,j,s)
$TAR^O_{s,j}$	TARO	TARO(styp,j,s)
$TAR^F_{i,j}$	TARF	PTAR_COM_F(i,j)
$TAR^I_{i,j}$	TARI	PTAR_I(i,j)
$TAR^{PF}_{i,d}$ & $TAR^{OF}_{i,d}$	TARPF & TAROF	NONU_DTAR_F(i,d), UTIL_DTAR_F(i,d)
$TAR^{PI}_{i,d}$ & $TAR^{OI}_{i,d}$	TARPI & TAROI	NONU_DTAR_I(i,d), UTIL_DTAR_I(i,d)
$PSUP_{s,j,k}$	PSUP	SUP_PR(styp,j,s)
$PSTR_{stkk}$	PSTR	PSTRCURV(i) & PSTR & CEM_PSTR(i,nst)
$PCAP_{i,j,k}$	PCAP	PCAPCURV(i) & CEM_PCAP(i,nc)
$PZZ^{PI}_{i,d}$	PZZPI	NG_BKSTOP_PR
$PZZ^{OI}_{i,d}$	PZZOI	NG_BKSTOP_PR
<b>Mass Balance Constraints at Transshipment nodes:</b>		
equation: 75 $DISCR^{PF}_m$	rowname: MPFN** $DISCRPF_i$	rowname: MPFN** $DISCR\_PF(i)$
equation: 76 $DISCR^{PF}_m$	rowname: MPIN** $DISCRPI_i$	rowname: MPIN** $DISCR\_PI(i)$
equation: 77 $DISCR^{PF}_m$	rowname: MOFN** $DISCROF_i$	rowname: MOFN** $DISCR\_OF(i)$
equation: 78 $DISCR^{PF}_m$	rowname: MOIN** $DISCROI_i$	rowname: MOIN** $DISCR\_OI(i)$
coefficients: $EFF^P_{i,j}$ $EFF^P_{s,j}$ $EFF^O_{i,j}$ $EFF^O_{s,j}$	EP EP EO EO	AEFF_PIPE(i,j) SEFF_PIPE(s,j) AEFF_PIPE(i,j) SEFF_PIPE(s,j)
<b>Mass Balance Constraint at storage:</b>		
equation: 79	rowname: MSTN**	rowname: MSTN**
coefficients: $EFF^O_{i,st}$	EOSTR	EFF_STR

**Table G-2. Cross Reference of CEM Variables Between Documentation, LP, and Code  
(Continued)**

Documentation	CEM LP variable	Code variable
<b>Mass Balance Constraints at End-use nodes</b>		
equation: 80 $QDEMOPF_{i,d}$	rowname: MPF***@@ $QDEMOPF_{i,d}$	rowname: MPF***@@ $QDEMOPF(i,d)$ & $QDEMOPFU(i)$
equation: 81 $QDEMOPI_{i,d}$	rowname: MPI***@@ $QDEMOPI_{i,d}$	rowname: MPI***@@ $QDEMOPI(i,d)$ & $QDEMOPIU(i)$
equation: 82 $QDEMOOF_{i,d}$	rowname: MOF***@@ $QDEMOOF_{i,d}$	rowname: MOF***@@ $QDEMOOF(i,d)$ & $QDEMOOFU(i)$
equation: 83 $QDEMOOI_{i,d}$	rowname: MOI***@@ $QDEMOOI_{i,d}$	rowname: MOI***@@ $QDEMOOI(i,d)$ & $QDEMOOIU(i)$
coefficients: $EFF_{i,d}^P$ $EFF_{i,d}^O$	EO EP	NEFF_PIPE(i,d) & UEFF_PIPE(i,d) NEFF_PIPE(i,d) & UEFF_PIPE(i,d)
<b>Pipeline Capacity Constraints:</b>		
equation: 87	rowname: CPF**N**	rowname: CPF**N**
equation: 88 (CEM loop 2) right hand side	rowname: CPI**N** (CEM loop 2) QCAP0-YCAP0	rowname: CPI**N** (CEM loop 2) PCAP & QCAP0(i,j)-YCAP(i,j,1)
equation: 89	rowname: CON**N**	rowname: CON**N**
coefficients: $U_{ij}^{PF}$ $U_{ij}^P$ $U_{ij}^O$	CON**N** UPF UP UO	PCAP UPF from ARC_PFUTILZ(i,j) UP from ARC_PUTILZ(i,j) UO from ARC_OUTILZ(i,j)
<b>Storage Capacity Constraints:</b>		
equation: 90	rowname: CPFSTN**	rowname: CPFSTN**
equation: 91 (CEM loop 2) right hand side	rowname: CPISTN** (CEM loop 2) QSTR0-YSTR0	rowname: CPISTN** (CEM loop 2) QSTR0(st)-YSTR(st,1)
coefficients: $UST_{st,i}^{PF}$ $UST_{st,i}^P$	UPFSTR UPSTR	STR_FUTILZ STR_UTILZ(st)
<b>Supply constraints:</b>		
equation: 84	rowname: SPS++N**	rowname: SPS++N**
equations: 85,86	rowname: SOS++N**	rowname: SOS++N**
Rowname/RHS: $UP_{s,i}^P$  $UP_{s,i}^O$	UPP  UPO	UPP using SUP_PUTILZ(styp,j,s) or SUP_PKSHR(styp,j,s) UPO using SUP_OUTILZ(styp,j,s) or SUP_PKSHR(styp,j,s)

**Table G-2. Cross Reference of CEM Variables Between Documentation, LP, and Code  
(Continued)**

Documentation	CEM LP variable	Code variable
Backstop Variables:		
	TPBKSTOP	BKSTOP(d)
	TOBKSTOP	BKSTOP(d)
Post_processing results:		
PhyCap <sub>ij</sub>		PNEW_CAP(i,j)
StrCap <sub>st,i</sub>		PNEW_STR(i)
ECAP <sub>ij</sub> <sup>F</sup>		REC
UTILZ <sub>ij</sub> <sup>PF</sup>		PEAKPCNT * ARC_PFUTILZ(i,j)
ECAP <sub>ij</sub> <sup>T</sup>		REC
UTILZ <sub>ij</sub> <sup>P</sup>		PEAKPCNT * ARC_PUTILZ(i,j)
i,j,m = nodes, s = source, d = demand node, nc = steps on pipe cap curve, nst = steps on storage curve, styp = source type, st = storage node, yr = year, bnd = lower/upper bound.		

**Table G-3. Cross Reference of DTM Variables Between Documentation, and Code**

Documentation	Code Variable	Equation #
$RR_r^F$	RR_F(r)	47, 63, 66
$TC_r^F$ $TC_{r,t-1}^F$	TC_F(r,t) TC_F(r,t-1)	47, 56, 66
$Vol_{rs}^I$	NONU_QTY_IPREV(s,r)	48
$ByPass_r$	I_BYPASS(r)	48
$DTAR_{rs}^I$	NONU_DTAR_IPREV(s,r)	48
$minDTAR^I$	MINMU_I	48
$\beta$	DTM_BETA	48
$g_r, \% \Delta TC_r^F$	TCF_CHANGE	49, 56
$\% \Delta k$	CHCOSTCAP	60
$\% \Delta w$	CHEMPLCOST	49, 52
$\% \Delta Vol_{rs}^F$	CHQTY_RESCOM, CHQTY_INDUTL	49, 51
TechEff	TECHEFF	56
$Vol_r$ $Vol_{r,t-1}$	NONU_QTY_F(s,r), UTIL_QTY_F(r,sr), NONU_QTY_FPREV(s,r), UTIL_QTY_FPREV(r,sr)	50, 58, 59, 60, 61
$DTAR_{rs,t}^F$	EST_DTAR_F(s), EST_UDTAR_F(sr)	57, 62, 65
$DTAR_{rs,t-1}^F$	NONU_DTAR_FPREV(s,r) UTIL_DTAR_FPREV(r,sr)	57, 64
$MIN\_DELTA_r$	MIN_DTAR_F	57
$\% \Delta Vol_{rs}^F$	CHQTY	57, 58, 59, 60, 61
$\gamma_i$	TCF_COEFF(4)	57
$RR_{r,t}^F$	EST_RR_F(r)	62, 63
$Vol_{rs,t}^F$	QBAS_NONU_F(s,r), QBAS_UTIL_F(r,sr)	62, 63
$\alpha_{r,t}$	RR_RATIO(r)	63, 64
$DTAR_{rs,t}^F$	NONU_DTAR_F(r,s) UTIL_DTAR_F(r,sr)	65
t - year, r - region, sr - subregion, s - sector, i - coeff #, F - core, I - noncore		

**Table G-4. Cross Reference of PTM Variables Between Documentation, and Code**

Documentation	Code Variable	Equation #
$R_{1r}$	RF	119, 121, 122
$R_{1v}$	RV	120, 123, 124
$ALL_r$	ARF(rd,i)	119
$ALL_v$	ARV(rd,i)	120
$R_i$	COST(1,i)	119, 120
$R_{ifr}$	RFR(i)	121
$R_{ifu}$	RFU(i)	122
$R_{ivr}$	RVR(i)	123
$R_{ivu}$	RVU(i)	124
$ALL_{rx}$	AFR(rd,i)	121
$ALL_{ru}$	AFU(rd,i)	122
$ALL_{vr}$	AVR(rd,i)	123
$ALL_{vu}$	AVU(rd,i)	124
$R_A^{bc}$	Not used	125
$R_A$	RFR(18)	125
$V_A^{bc} / V_A^T$	PS(P,AF,AT)	125
$R_{1,2}$	FCR,VCR,FCU,VCU	126
$PMAX_A^{t-1}$	MAX(AF,AT)	130
INDUSTRYGPIS <sub>t-1</sub>	PLTOGPIS1	179
GPIS <sub>t-1</sub>	PGPIS	176, 178, 179, 183, 186
UTIL_RATE_I	UTILR_I	154, 155
INC_REV <sub>t</sub>	not used	157, 160
INC_COST	not used	159, 160
CIS <sub>t</sub> / MC_PGDT <sub>t</sub>	REQR_INT	157
PNEWFAC	NEWCOST	182, 214
$\beta_0$	OWC_BETA0	186
$\beta_1$	OWC_BETA1	186
$\beta_2$	OWC_BETA2	186
$\rho$	OWC_RHO	186

**Table G-4. Cross Reference of PTM Variables Between Documentation, and Code  
(continued)**

Documentation	Code Variable	Equation #
$\beta_0$	ADIT_TEMP(1,3)+ADIT_FD	188
$\beta_1$	ADIT_ADIT = ADIT_TEMP(1,1)	188
$\beta_2$	ADIT_NETPLT = ADIT_TEMP(1,2)	188
$\beta_0$	DDA_FD	181, 213
$\beta_1$	DDA_NETPLT	181, 213
$\beta_2$	DDA_DEPSHR	181, 213
$\rho$	DDA_RHO_E	181, 213
DDA <sub>i</sub>	DDASL, DDA(P,T,CT)	184, 216
$\alpha_i * FD_i$	TAG_FD(T)	219
$\alpha_i * TF_{i,t}$	TAG_TF(T)	219
GPIS <sub>i,t-1</sub>	X1	219
PK	RENTBLDG	219
$\beta_1$	TAG_EFF1	219
$\beta_2$	TAG_EFF2	219
$\alpha_i * FD_i$	TOM_FD(T)	222
$\alpha_i * TF_{i,t}$	TOM_TF(T)	222
GPIS <sub>i,t-1</sub>	X1	222
PK	RENT	222
$\beta_1$	TOM_EFF1	222
$\beta_2$	TOM_EFF2	222
T - Pipeline type, t - year, rd - rate design index, i - node		



## **Appendix H**

### **Model Equations**

This appendix presents the mapping of the equation (by equation number) in the documentation with the subroutine in the NGTDM code where the equation is used or referenced.



Chapter 3 Equations		
EQ. #		SUBROUTINE
1	(Firm) (Interr.)	NGTDM_CRVNONUF <sup>X</sup> NGTDM_CRVNONUI <sup>X</sup>
2		NGSYN_LIQH <sup>*</sup>
3-6		NGCAN_IMP <sup>*</sup>
7	(onshore & offshore)	NGTDM_PRE
8-11	(onshore) (offshore)	NGPRD_L48 <sup>*</sup> NGPRD_OCS <sup>*</sup>
12-18		NGTDM_DMDALK
* Function		

Chapter 5 Equations		
EQ. #		SUBROUTINE
19-22		Not applicable
23		NGTDM_LPSI,NGTDM_LPEI,NGTDM_EFFLP, NGTDM_TARPI,NGTDM_TARDI,NGTDM_SUPCI, NGTDM_UTILCI,NGTDM_NONUCI,NGTDM_EXCI
24-27		NGTDM_CAPI
28-29		NGTDM_UTILCI,NGTDM_NONUCI,NGTDM_EFFLP,NGTDM_LPEI
30		NGTDM_SUPCI
31,34-35		NGTDM_CAPI
32-33		NGAFM_SUPMIN
36		PROPEROUT

Chapter 6 Equations	
EQ. #	SUBROUTINE
37-40	NGTDM_POSTNONU
41-45	NGTDM_POSTUTIL
46	NGDTM_DTM, NGDTM_MUF NGTDM_DTM, NGDTM_MUF NGTDM_POSTUTIL
47	NGDTM_FORECAST_DTARF
48	NGDTM_ICC
49-53,56	NGDTM_TCF1
54-55	NGDTM_CALCCOSTC*
57-65	NGDTM_FORECAST_DTARF
66	NGDTM_TCF0
67-68	NGDTM_FORECAST_TRNF
69-71	NGDTM_DTARI
72	NGDTM_BENCHF
73	NGDTM_BENCHI
* FUNCTION	

Chapter 7 Equations	
EQ. #	SUBROUTINE
74	CEMLPSNY, CEMPLPNE, CEMCANIMP, CEMFLOWNN, CEMSUPCI, CEMSCAP, CEMBACK, CEMPCAP, NGCEM_ADJSTR, NGCEM_ADJCAP
75-78	CEMLPST,CEMLPNN,CEMLPSNB,CEMDISCR
79	CEMLPST
80-83	CEMLPNE,CEMDMD
84	CEMLPSUP,CEMCANSUP,CEMSUPCI
85	CEMLPSUP,CEMSUPCI
86	CEMLPSUP,CEMCANSUP,CEMSUPCI
87	CEMLPCAP,CEMCANIMP,CEMDMD,CEMPCAP
88	RESET_RHS,CEMLPCAP,CEMCANIMP,CEMDMD,CEMPCAP
89	CEMLPCAP,CEMCANIMP,CEMDMD,CEMPCAP
90-91	CEMLPST_UTIL,CEMSCAP,RESET_RHS
92-93	CEMCANIMP,CEMFLOWNN
94-95	RESETMATRIX
96-97	GETSOLUTION1
98-99	NGCEM_AFMUTILZ
100-101	GETSOLUTION2

Chapter 8 Equations	
EQ #	SUBROUTINE
102-118	PTMA_CALCULATE_COST
119-124	PTMJ_TRNS_COST_OF_SERVICE
125-126	PTM4_BASE_YEAR_PIPELINE
127-128	PTM4_BASE_YEAR_PIPELINE, PTM6_FORECAST_PIPELINE
129-156	PTMD_ALLOCATE_ARC_LEVEL_COST
157-164	PTMU_COSTSHIFT_IN_RATE
165-167	PTMD_ALLOCATE_ARC_LEVEL_COST
168-169	PTM9_EXPAND_GENERIC
170-174	PTM2_BASE_YEAR_INITIALIZATION
175	PTMA_CALCULATE_COST
176	PTMA_CALCULATE_COST, PTM7_FORECAST_COST
177-183	PTM7_FORECAST_COST
184	PTM9_EXPAND_GENERIC
185-186	PTM7_FORECAST_COST
187	PTMA_CALCULATE_COST
188-189	PTM7_FORECAST_COST
190	PTM7_FORECAST_COST, PTM9_EXPAND_GENERIC
191-207	PTMA_CALCULATE_COST
208	PTM7_FORECAST_COST
209	PTMA_CALCULATE_COST
210	PTM7_FORECAST_COST
211-212	PTMA_CALCULATE_COST
213-215	PTM7_FORECAST_COST
216	PTM9_EXPAND_GENERIC
217-218,220-221,223-226	PTM7_FORECAST_COST
219,222	YVALUE*
FUNCTION	

## Appendix I

### Sensitivity Parameters

This Appendix lists the parameters that have been selected as sensitivity variables within the NGTDM. Most of the sensitivity options key off of two NEMS run time parameters: NGCATG to specify the parameter to be perturbed, and NGKEY to identify which perturbation amount to be used. The remaining sensitivity options are activated through input data files as switches and corresponding quantities. These keys and switches are listed along with the parameter descriptions and their corresponding perturbation activity.





SENSITIVITY PARAMETER LISTING			
Parameter	Switch	Key	Activity
Residential demand	NGCATG = 1	NGKEY = 1	Increase by 0.5% per year 1996-2010
		NGKEY = 2	Decrease by 0.5% per year 1996-2010
Industrial demand	NGCATG = 2	NGKEY = 1	Increase firm demand by 0.5% per year 1996-2010
		NGKEY = 2	Decrease firm demand by 0.5% per year 1996-2010
		NGKEY = 3	Increase interruptible demand by 0.5% per year 1996-2010
		NGKEY = 4	Decrease interruptible demand by 0.5% per year 1996-2010
CEM weather factor	NGCATG = 3	NGKEY = 1	weather factor = 0.20
		NGKEY = 2	weather factor = 0.10
		NGKEY = 3	weather factor = 0.0
AFM weather factor	NGCATG = 4	NGKEY = 1	weather factor = 0.10
		NGKEY = 2	weather factor = 0.0
Peak firm utilization	NGCATG = 5	NGKEY = 1	utilization = 0.70
		NGKEY = 2	utilization = 0.90
		NGKEY = 3	utilization = 0.99
Peak & Offpeak gas consumption shares - residential, commercial, industrial	NGCATG = 6		Peak share = 0.33 Offpeak share=0.67
Cost of new capacity on 8->4	NGCATG = 7		Decrease by \$2.00
Steps on capacity expansion curve 8->4	NGCATG = 8		Drop all steps except the most expensive step for new capacity
Pipeline capacity addition cost all arcs	NGCATG = 9	NGKEY = 1	Increase by 20%
		NGKEY = 2	Decrease by 20%

SENSITIVITY PARAMETER LISTING			
Parameter	Switch	Key	Activity
Base capacity all arcs	NGCATG = 10	NGKEY = 1	Base cap = 0
		NGKEY = 2	Base cap = Commodity charge
		NGKEY = 3	Base cap = Reservation charge
AA Utility Bond index rate	NGCATG = 11	NGKEY = 1	Increase by 2%
		NGKEY = 2	Decrease by 2%
Load Factor for maximum interruptible transportation rate - LFAC_I	NGCATG = 12	NGKEY = 1	Increase by 25%
		NGKEY = 2	Decrease by 25%
	NGCATG = 13		Not used
	NGCATG = 14		Not used
Gas Supply Realignment cost	NGCATG = 15		Double
Pipeline fuel use	NGCATG = 16	NGKEY = 1	Increase by 2%
		NGKEY = 2	Decrease by 2%
	NGCATG = 17		Not used
Supply curve parameters	NGCATG = 18	NGKEY = 1	Increase by 50% elasticity for supply curve type 2
		NGKEY = 2	Decrease by 50% elasticity for supply curve type 2
		NGKEY = 3	Increase by 50% elasticity for supply curve type 3
		NGKEY = 4	Decrease by 50% elasticity for supply curve type 3
		NGKEY = 5	Increase middle segment of supply curve type 3 by 50%
		NGKEY = 6	Decrease middle segment of supply curve type 3 by 50%

SENSITIVITY PARAMETER LISTING			
Parameter	Switch	Key	Activity
Residential demand at node 3	NGCATG = 20	NGKEY = 1	Increase by 0.5% per year 1996-2010
		NGKEY = 2	Decrease by 0.5% per year 1996-2010
Utility demand	NGCATG = 21	NGKEY = 1	Increase by 0.5% per year 1996-2010
		NGKEY = 2	Decrease by 0.5% per year 1996-2010
Refurbishment (BLAE)	BLAESWT = 0 (set in PTARIFF)		No refurbishment costs
	BLAESWT = 1 (set in PTARIFF)		DDA*(ADDA/GPIS)
	BLAESWT = 2 (set in PTARIFF)		BLAETOT
Increment to TOM (Total Operation and Maintenance Expenditure) in PTM	TOMSWT = 0 (set in PTARIFF)		No incremental cost in TOM
	TOMSWT = 1 (set in PTARIFF)	TOMINC1 (set in PTARIFF)  and/or  TOMINC2 (set in PTARIFF)	incremental cost of existing pipelines-- user specified (i.e., 150000000 \$1993)  incremental cost of entire industry (both existing and generic pipeline)-- user specified (i.e., 1000000000 \$1993)

