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# Detection of False Data Injection Attacks in Power System State Estimation Using Sensor Encoding

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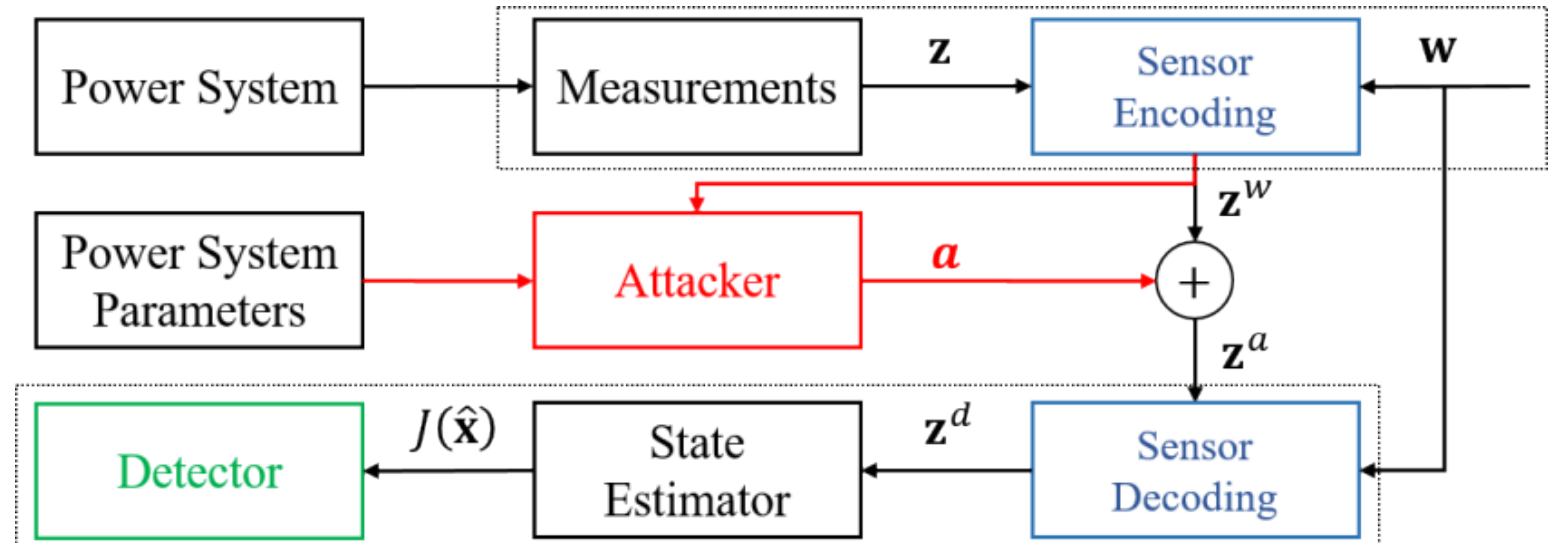


# Outline

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# Introduction

- Smart grids
  - Increased flexibility, cybersecurity risks
- Vulnerable power systems applications<sup>†</sup>
  - Power system state estimators (PSEs), automatic generation control, voltage control, energy markets
- Data deception attacks
  - False data injection (FDI)
  - Integrity of measurements
  - Meter or communication level
- This paper:
  - Encoding method



<sup>†</sup>K. Chatterjee, V. Padmini, and S. A. Khaparde, "Review of cyber attacks on power system operations," in 2017 IEEE Region 10 Symp. (TENSYP), July 2017, pp. 1–6.



# Power System State Estimation

- Model:

$$\mathbf{z} = \mathbf{h}(\mathbf{x}) + \mathbf{e}$$

- Measurements:  $\mathbf{z}$ ;
- States:  $\mathbf{x}$ ;
- Measurement function:  $\mathbf{h}(\mathbf{x})$ ;
- Error:  $\mathbf{e} \sim \mathcal{N}(\mathbf{0}, \mathbf{R})$ ;
- Residuals:  $\mathbf{r} = \mathbf{z} - \mathbf{h}(\mathbf{x})$

- Problem: find  $\mathbf{x}$  that best fits measurements given a goodness of fit score
- Weighted least-squares:

$$\min_{\mathbf{x}} J(\mathbf{x}) = \frac{1}{2} [\mathbf{z} - \mathbf{h}(\mathbf{x})]^T \mathbf{R}^{-1} [\mathbf{z} - \mathbf{h}(\mathbf{x})]$$

- Solution using Newton-Raphson iterative algorithm:

$$\hat{\mathbf{x}}_{k+1} = \hat{\mathbf{x}}_k + (\mathbf{H}_k^T \mathbf{R}^{-1} \mathbf{H}_k)^{-1} \mathbf{H}_k^T \mathbf{R}^{-1} [\mathbf{z} - \mathbf{h}(\hat{\mathbf{x}}_k)]$$

- $\mathbf{H}_k = \frac{\partial \mathbf{h}(\hat{\mathbf{x}}_k)}{\partial \mathbf{x}}$

- Bad data detection using residual-based approaches like  $J(\mathbf{x})$  (a.k.a. chi-squared test  $\chi^2$ )
- Detect an attack when  $J(\mathbf{x}) > \chi_{v,\alpha}^2$

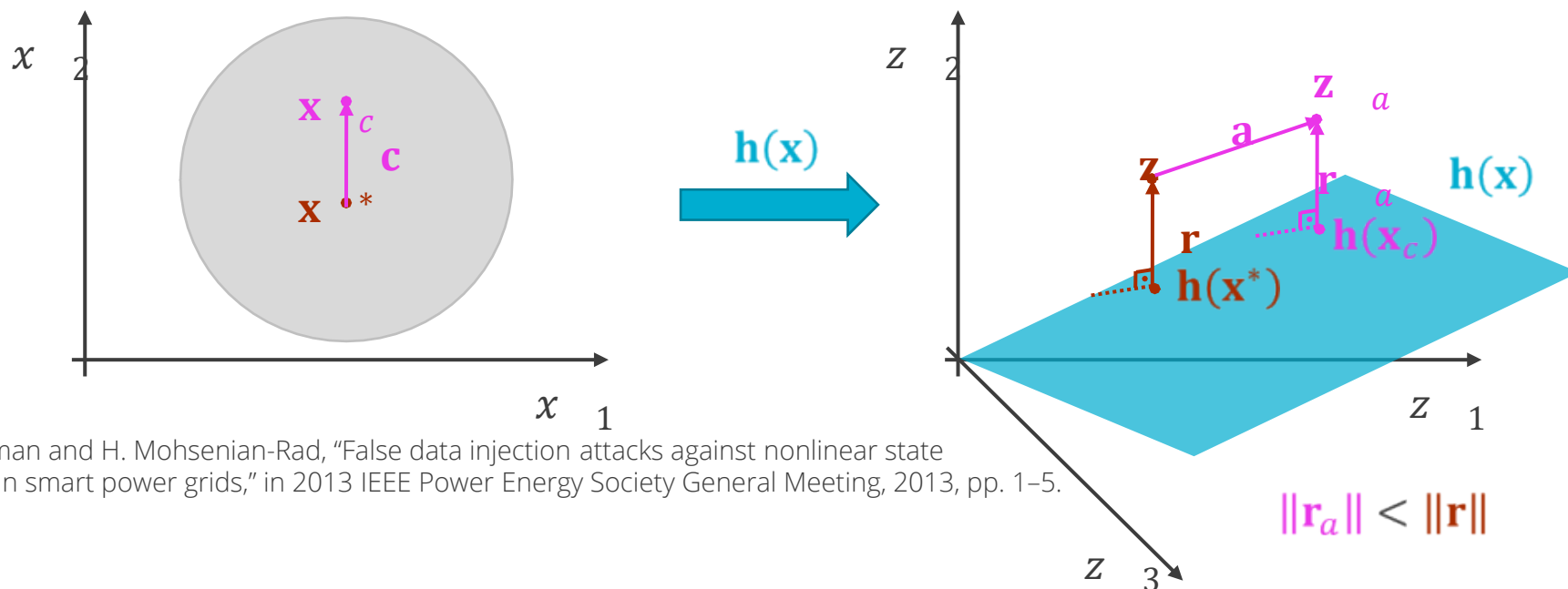


# Stealthy False Data Attacks on PSSE

- Goal: circumvent traditional bad data detection approaches
- Sensors are manipulated so that low residual values  $\mathbf{r}_a$  are obtained by an estimator
  - False data vector induces a solution of PSSE that is feasible
  - Similar to changing (or corrupting) the observed point of operation

$$\mathbf{x}_c = \mathbf{x}^* + \mathbf{c}$$

$$\mathbf{a} = -\mathbf{H}_c(\mathbf{H}_c^T \mathbf{R}^{-1} \mathbf{H}_c)^{-1} \mathbf{H}_c^T \mathbf{R}^{-1} [\mathbf{z} - \mathbf{h}(\mathbf{x}_c)] + \mathbf{h}(\mathbf{x}_c) - \mathbf{h}(\mathbf{x}^*)^\dagger$$



<sup>‡</sup> M. A. Rahman and H. Mohsenian-Rad, "False data injection attacks against nonlinear state estimation in smart power grids," in 2013 IEEE Power Energy Society General Meeting, 2013, pp. 1-5.



- $$\begin{aligned} \mathbf{z}^w &= \mathbf{f}(\mathbf{z}, \mathbf{w}) \\ \mathbf{z}^d &= \mathbf{g}(\mathbf{z}^w, \mathbf{w}) \end{aligned}$$

- Encoding function  $\mathbf{f}$ ;
- Decoding function  $\mathbf{g}$ ;
- Secret encoding vector  $\mathbf{w}$ ;
- Encoded measurement vector  $\mathbf{z}^w$ ;
- If no attack happens we should expect decoded measurement vector  $\mathbf{z}^d = \mathbf{z}$





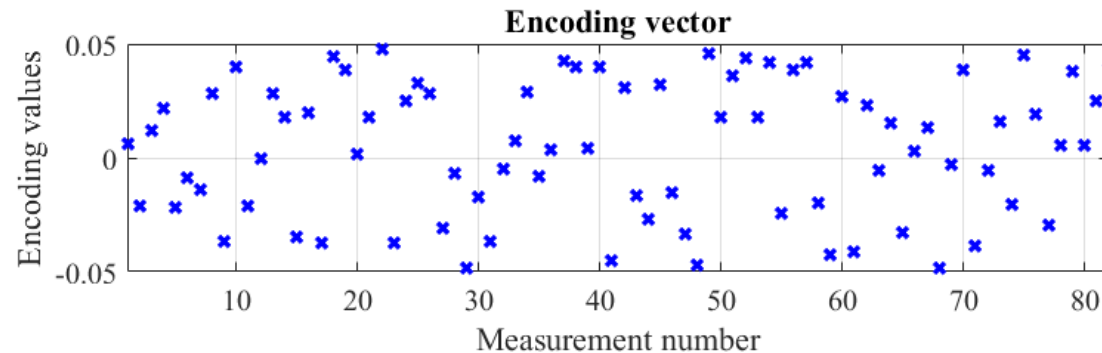
# Naïve Sensor Encoding

- Select a random encoding vector
  - Not too large so it is obvious an encoding vector is being used
  - Not too small so that it will not lead to an FDI detection
  - Defender's  $J(\mathbf{x})$  has to produce a large value
  - Drawback: if an attacker uses  $J(\mathbf{x})$  detector it will detect the encoding vector

$$\mathbf{z}^w = \mathbf{z} + \mathbf{w}$$

$$\mathbf{z}^d = \mathbf{z}^w - \mathbf{w}$$

$$w_i \sim \mathcal{U}(-0.05, 0.05)$$





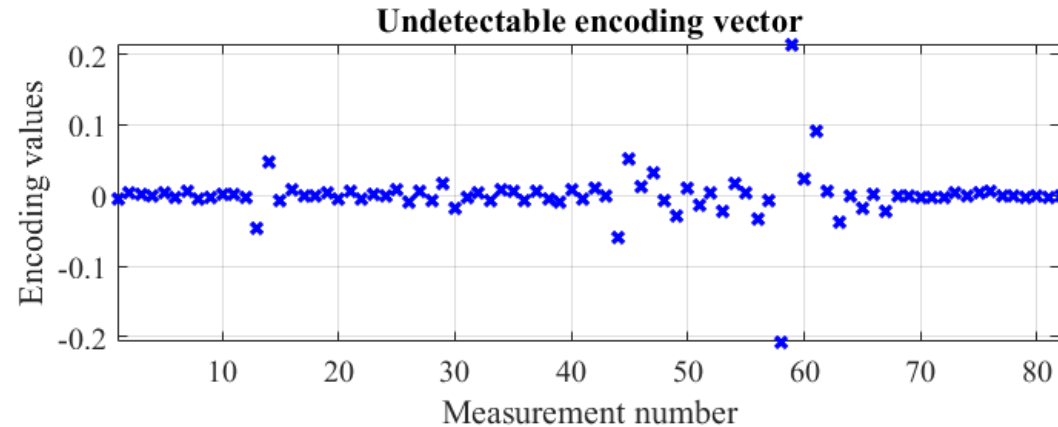
# Undetectable Sensor Encoding

- Select an encoding vector that can bypass an attacker's  $J(\mathbf{x})$  test
  - Design it using the same approach as a stealthy cyber attack

$$\begin{aligned}\mathbf{x}_u &= \mathbf{x}^* + \mathbf{u} \\ \mathbf{z}^w &= \mathbf{z} + \mathbf{w}^u \\ \mathbf{z}^d &= \mathbf{z}^w - \mathbf{w}^u\end{aligned}$$

Deviation in state should be large enough so defender's  $J(\mathbf{x})$  detects FDI

$$u_i \sim \mathcal{U}(-0.1, 0.1)$$

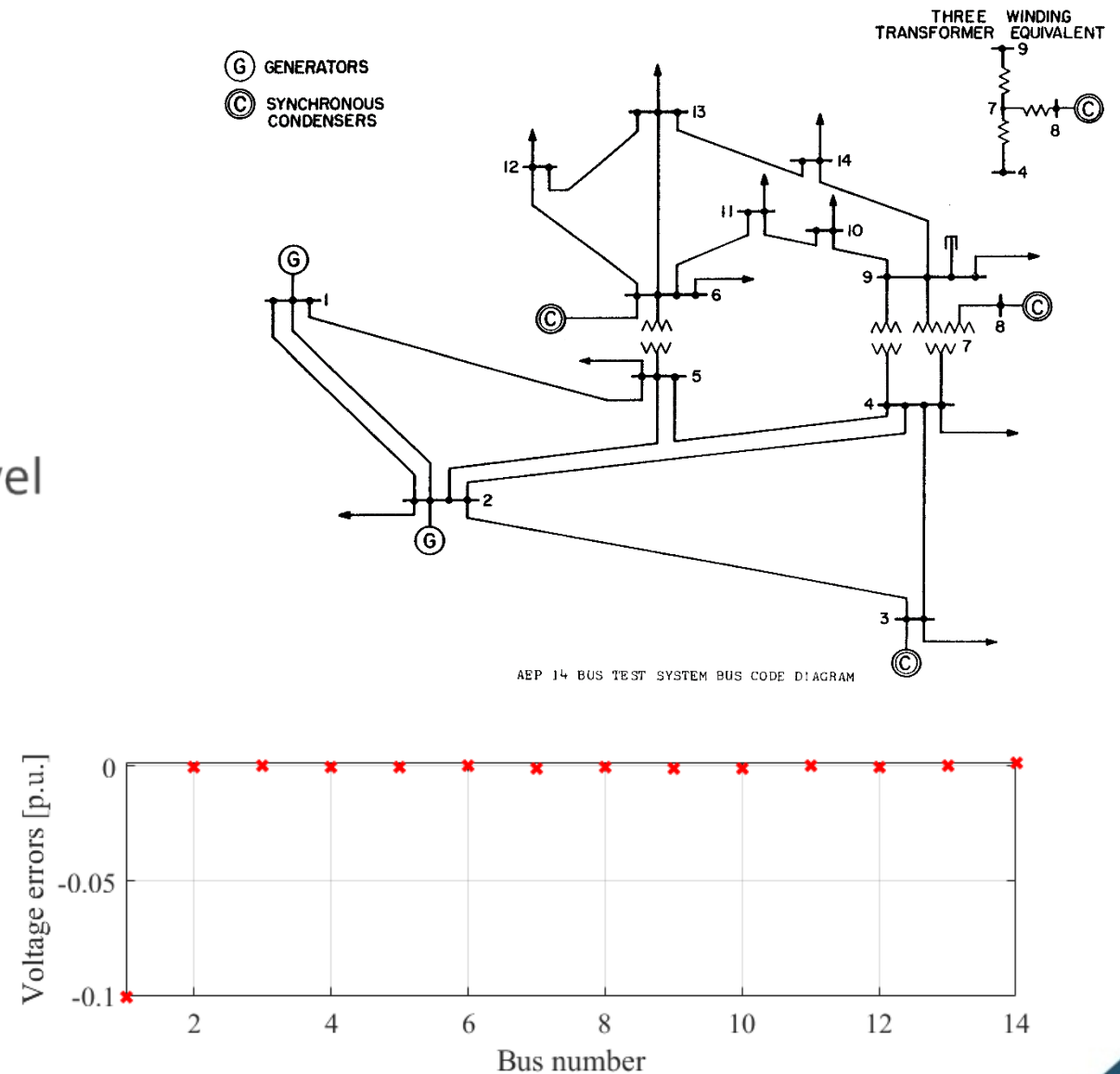
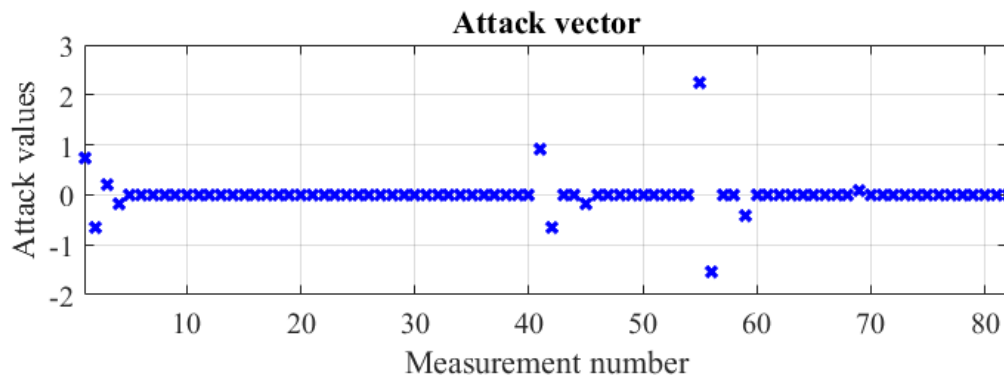






# Case Study

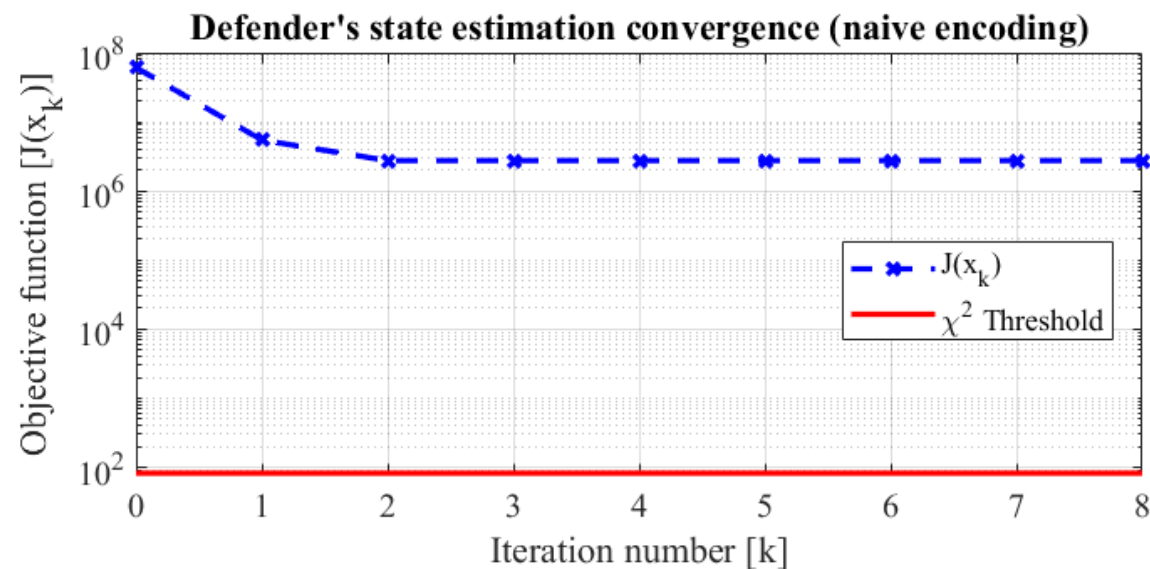
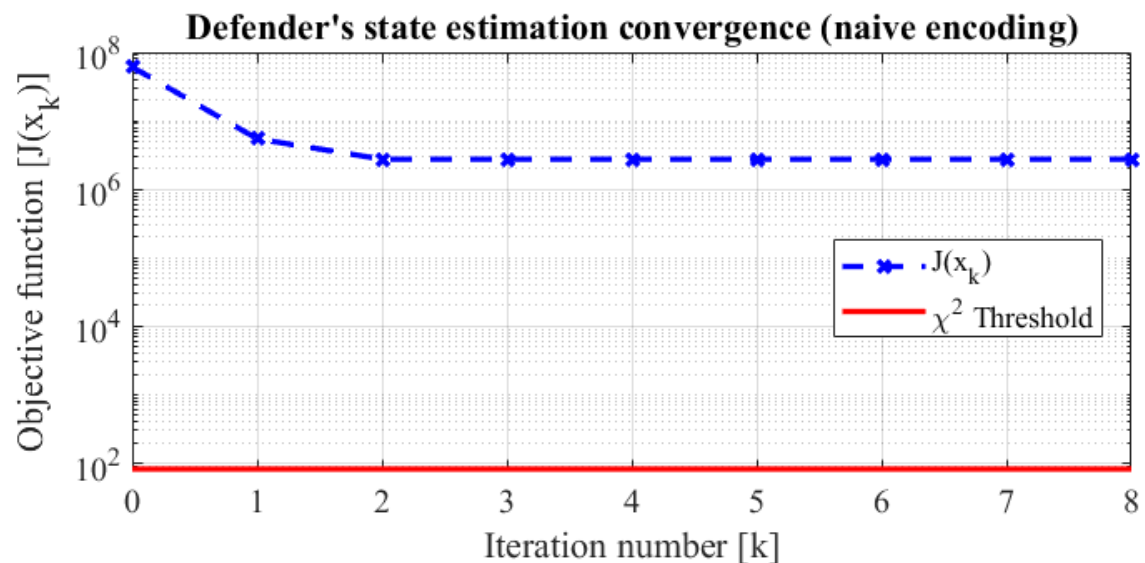
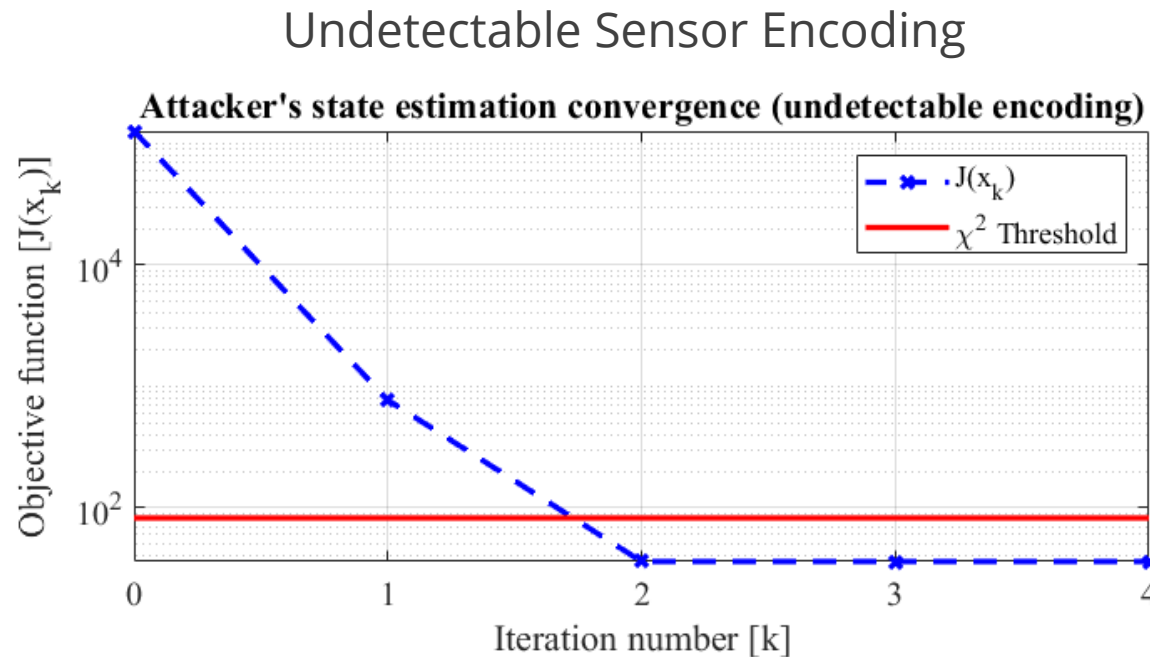
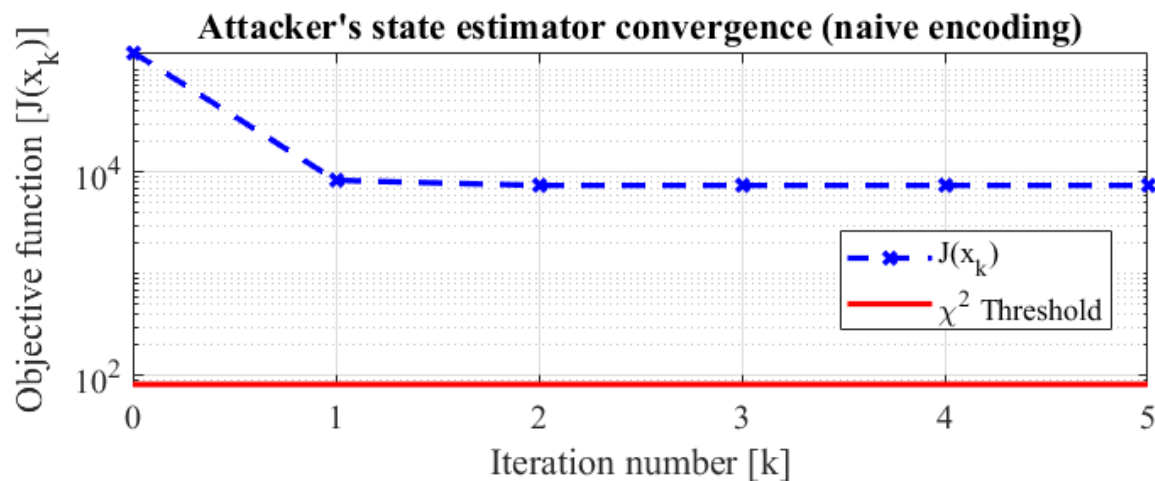
- MATPOWER + Matlab
- IEEE 14-bus test system
- 82 measurements, 27 states (GRL-3.03)
- Measurements corrupted by noise
  - 0.01 p.u. for power, 0.001 p.u. for voltage
- Chi-squared test with 99% confidence level
  - $\chi^2_{55,99\%} = 82.29$
- Goal of the attacker:
  - Inject a bias of 0.1 p.u. to voltage at bus 1





# Results

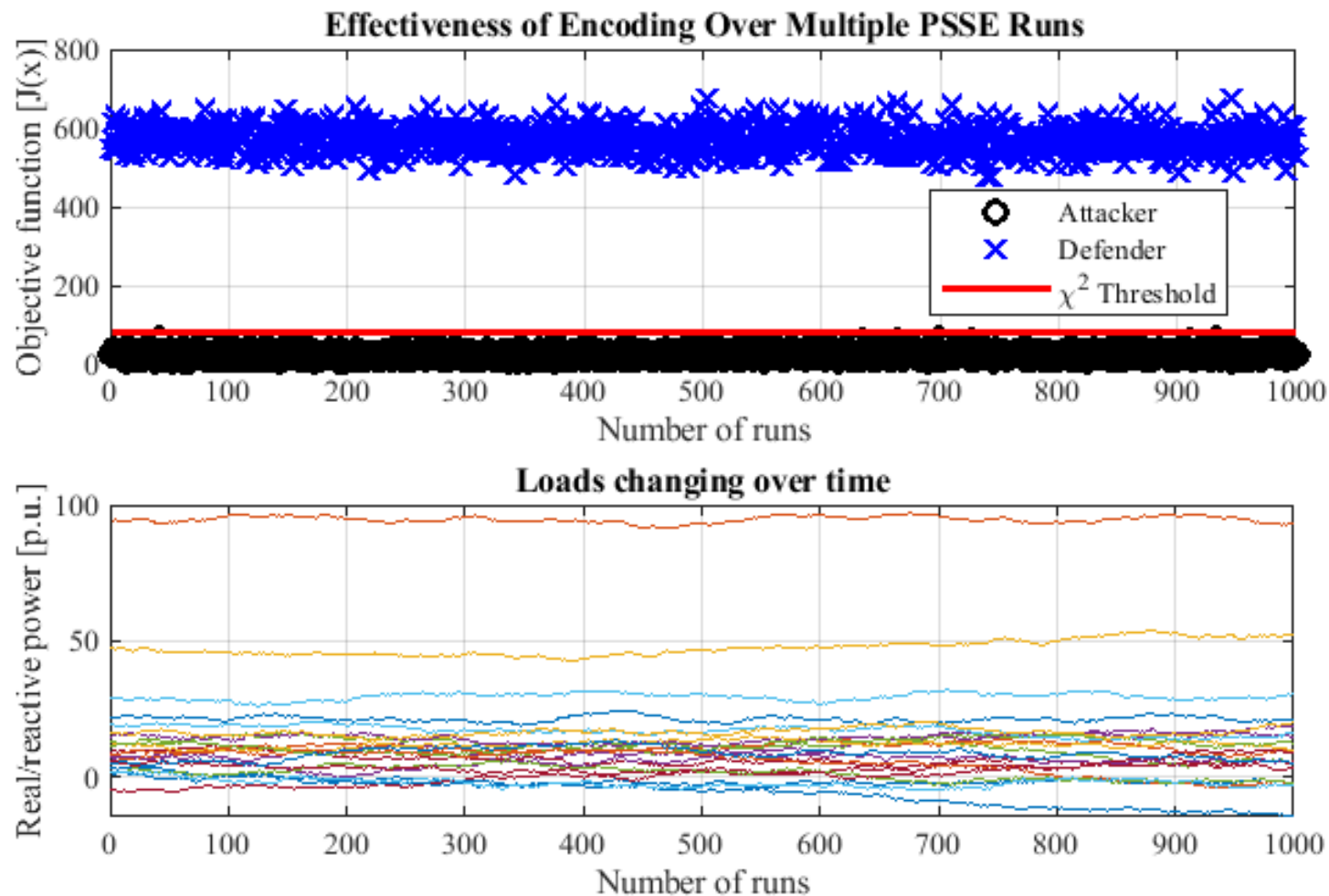
## Naïve Sensor Encoding





# Results

## Undetectable Sensor Encoding Sensitivity to load






## Conclusion

- Two simple methods for defense against FDI attacks on PSSE using sensor encoding
- The encoding vectors induced detection of stealthy FDI cyberattacks on PSSE
- Naïve encoding can be detected by the attacker
  - Does not need any assumption on current system state
- Undetectable encoding cannot be detected by the attacker
  - Requires knowledge of system state at some point in time
- Low-cost method could be applied to PSSEs with minimal intervention
- Following a defense in-depth strategy, could be paired with other cybersecurity controls
  - E.g. communications encryption
- Future work
  - Considerations to practical implementation
  - Enable its application in dynamic PSSE
  - Analysis for design of vectors
  - Constraints on number of encoded measurements



## Acknowledgment

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Thank you!  
Questions?