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# Microscale Modeling of Energetic Materials – Strength & Plasticity Informed by Molecular Dynamics

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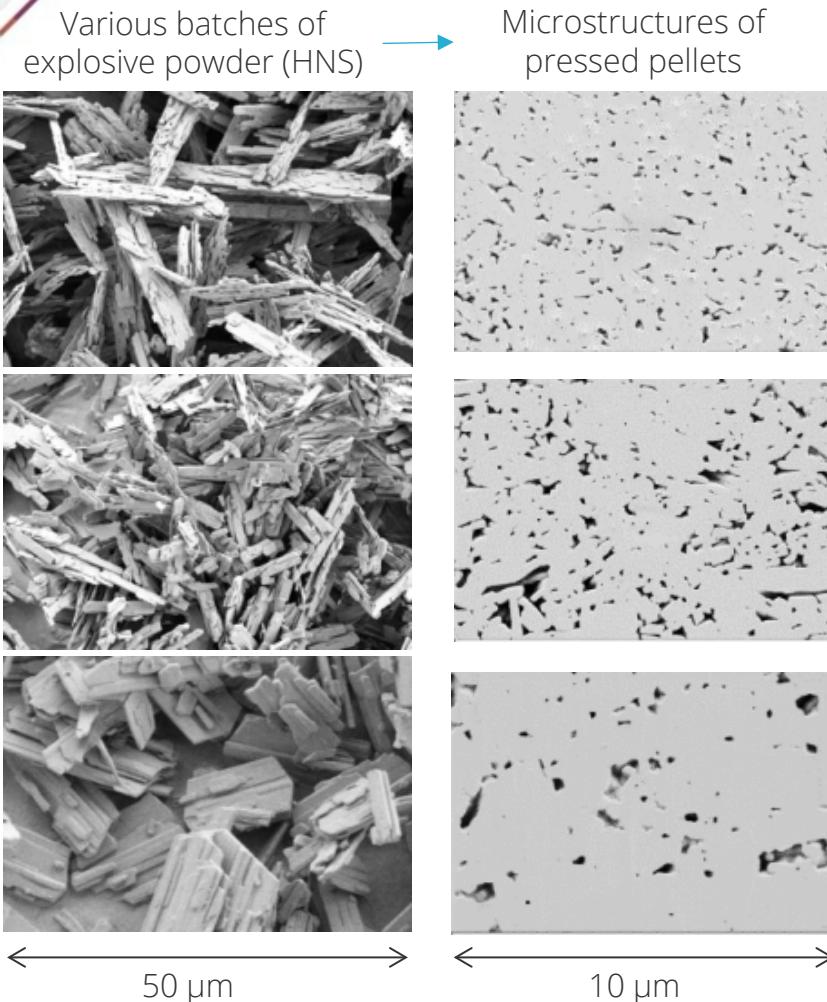
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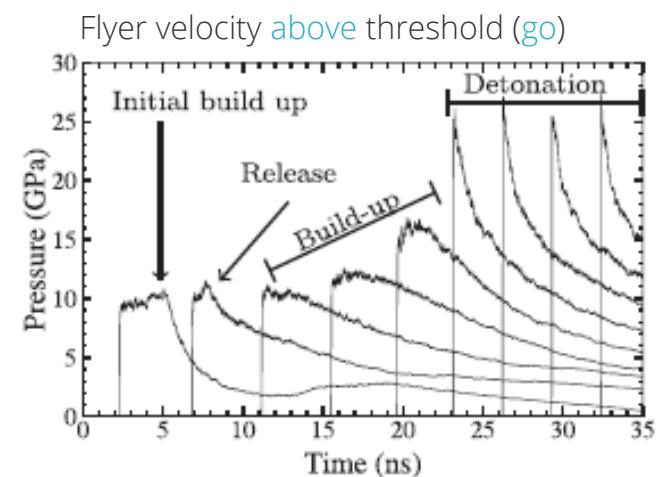
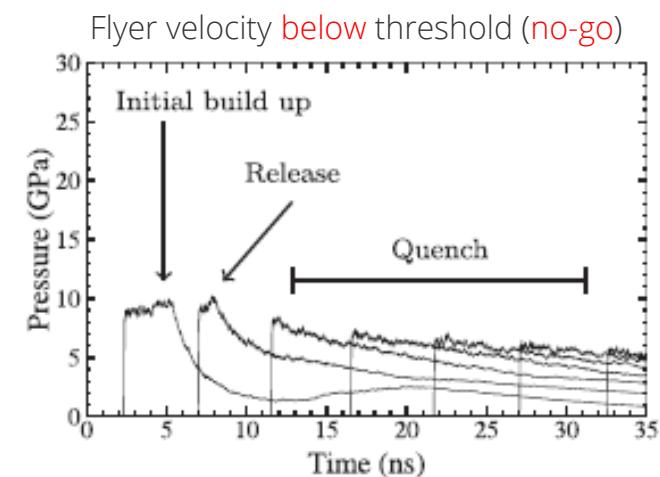
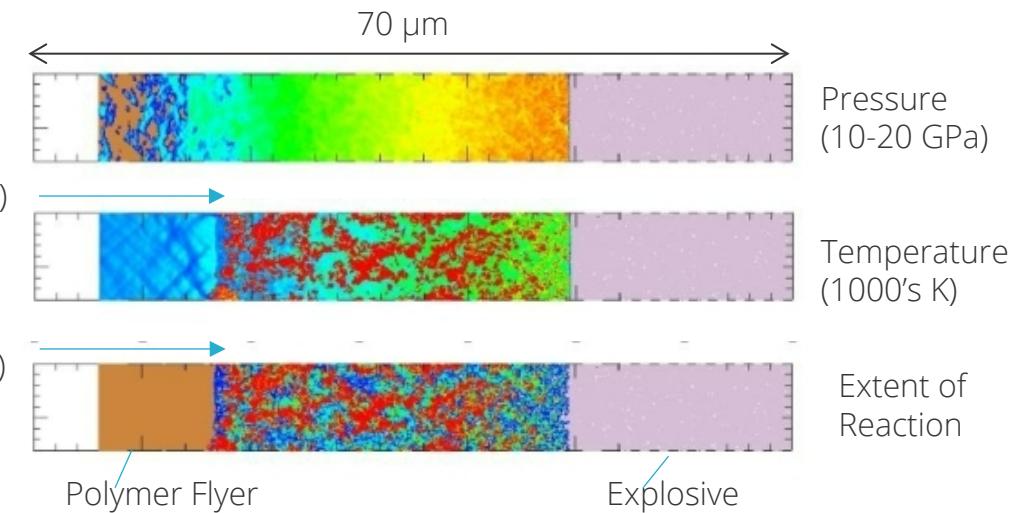
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Co-authors: J. Stewart, R. Knepper, J. Brown, M. Wood, M. Sakano

# Property-Performance Relationships in Energetic Materials

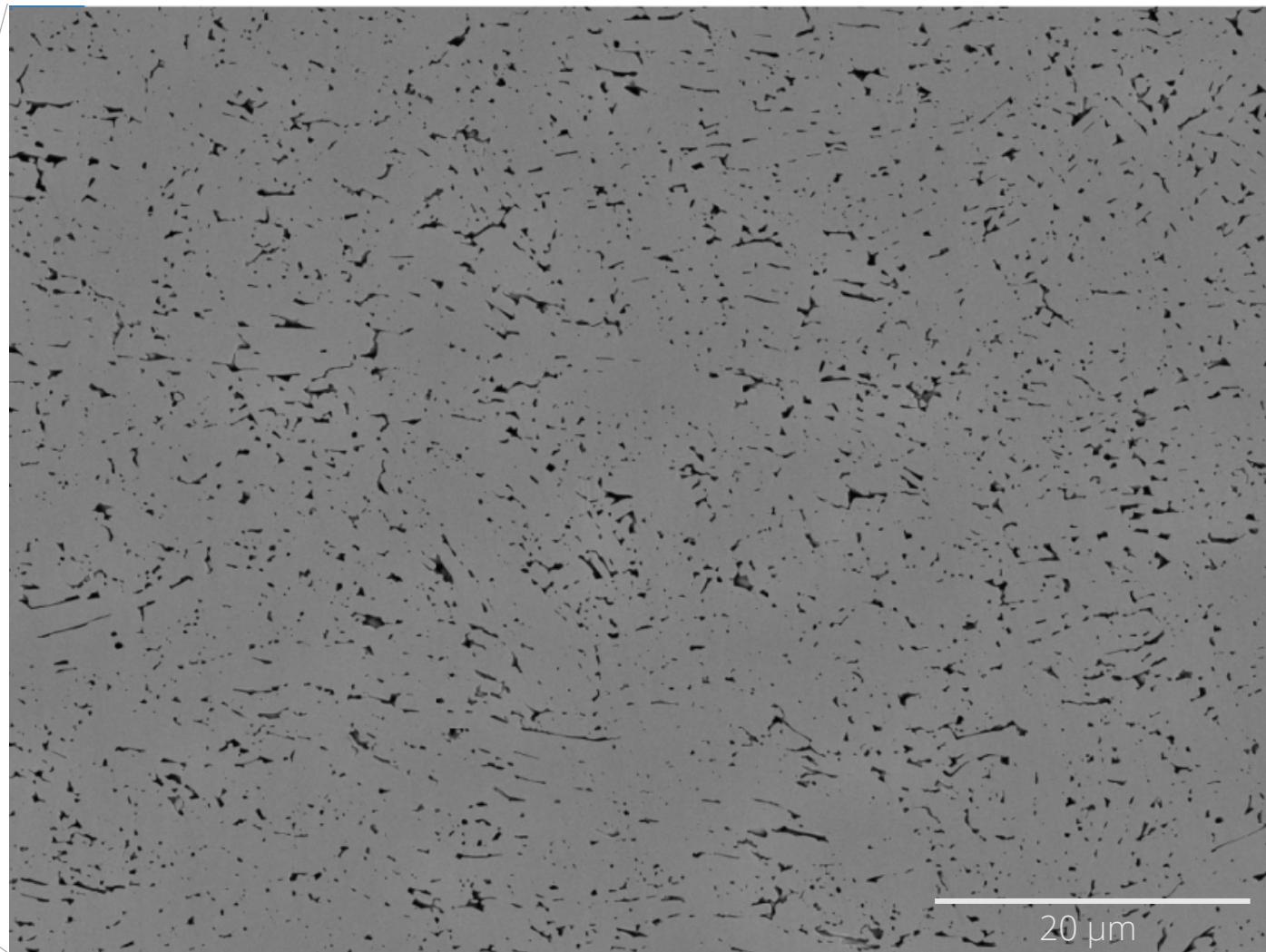
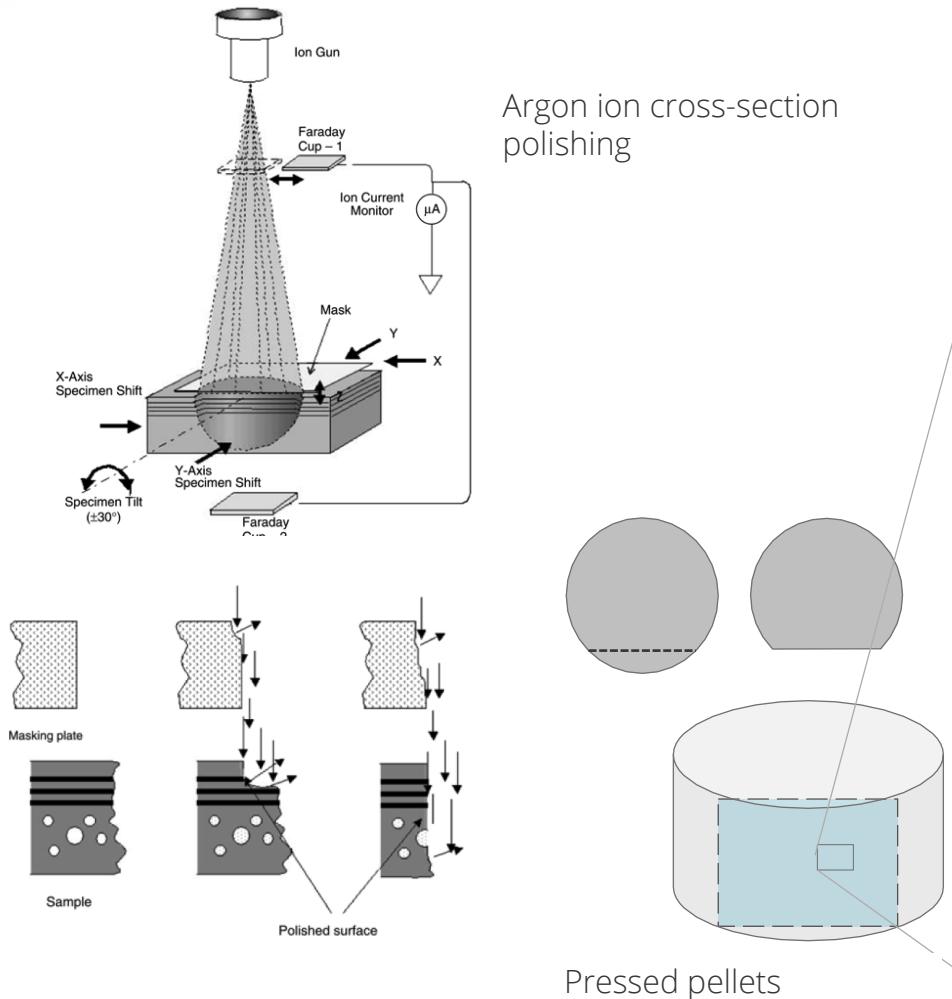


Import microstructures to hydrocode for simulation of run-to-detonation



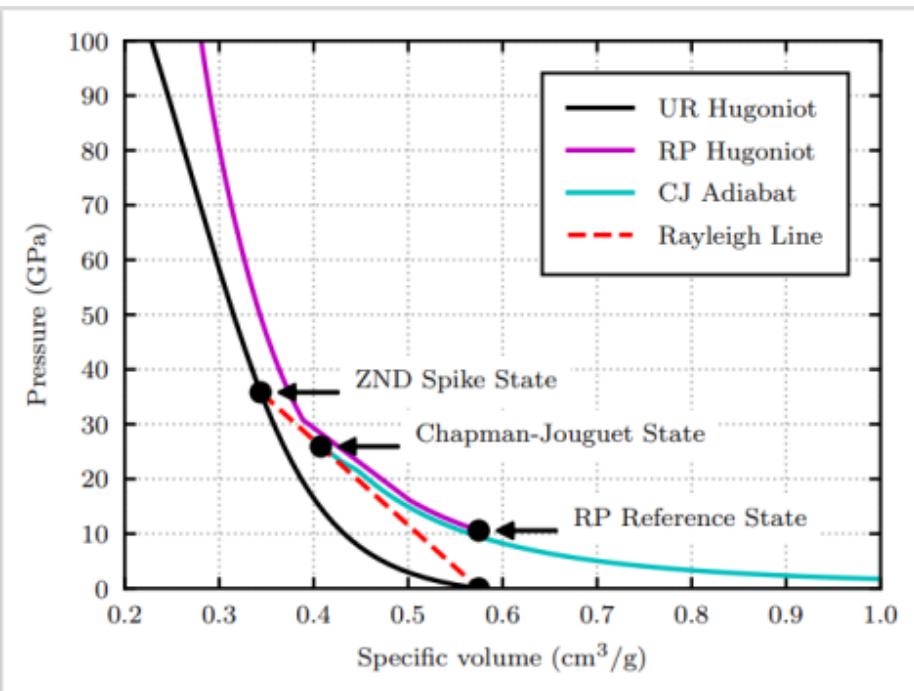
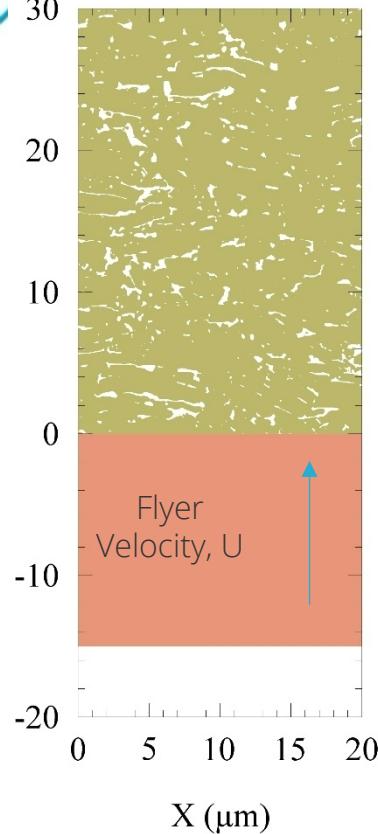
*Direct numerical simulations of energetic material microstructures predict the material's response*

# Microstructure Characterization



High resolution SEM image (10 nm/pixel) [Credit: Rob Knepper, SNL]

# Model Description – EOS, Strength, and Reactive Burn Model



Unreacted (UR) and reaction products (RP) Hugoniots for fully dense (solid) HNS.

- Reaction products EOS uses a SESAME table which includes states off the CJ adiabat (accessed during hotspot formation)

- Plastic deformation of the solid crystal at voids and defects generates heat and increases the local temperature (hot spots)
- Reaction rate depends on local temperature in the solid

$$k = A \exp(-E/RT)$$

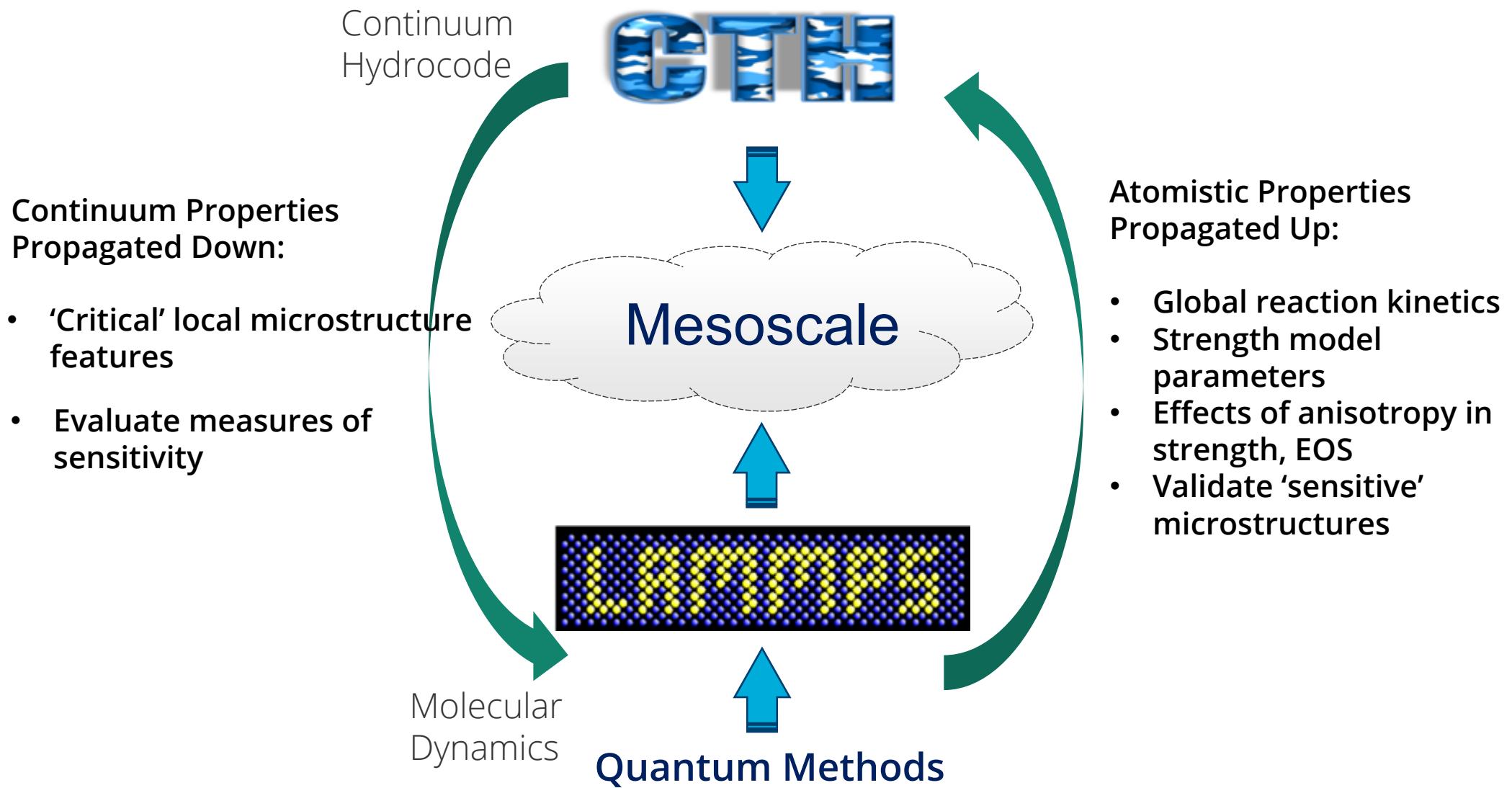
- We use the activation energy,  $E$ , based on thermal decomposition data
- Frequency factor,  $A$ , is adjusted (calibrated) so that flyer impact simulations match experimental data

Constitutive models for strength and plasticity determine the amount of heat generated by viscous heating and ejecta impact during pore collapse

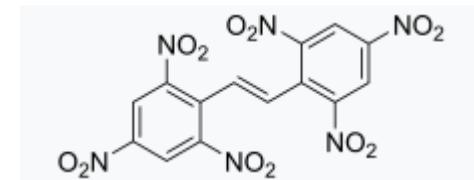
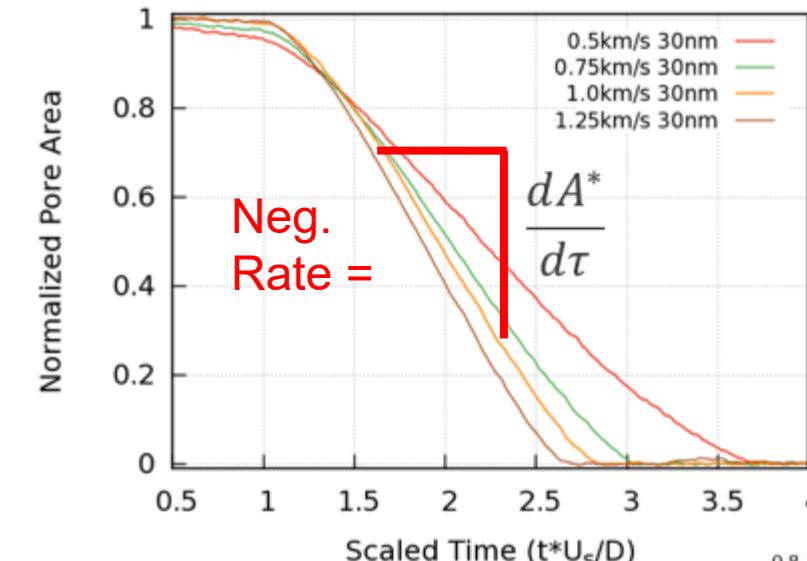
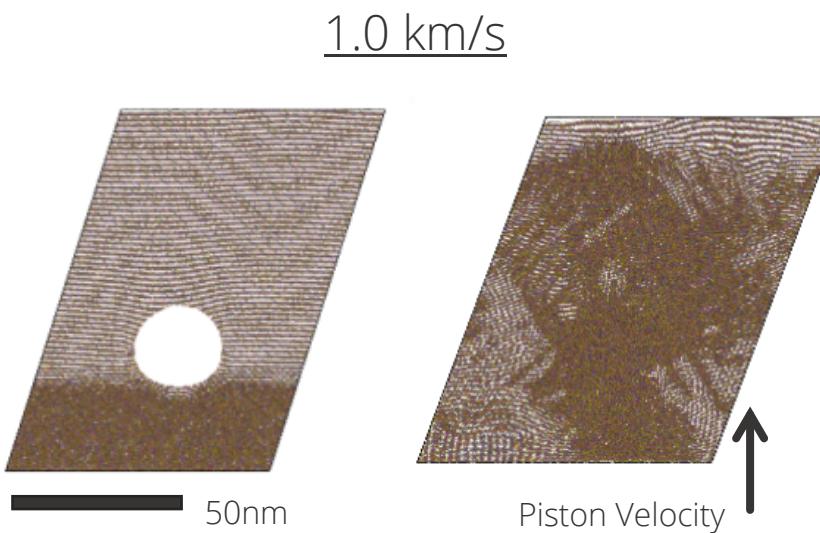
→These models are a **major source of uncertainty in hydrocode simulations**

*Problem: Strength and plasticity of energetic molecular crystals at high strain rates & sub-micron length scales*

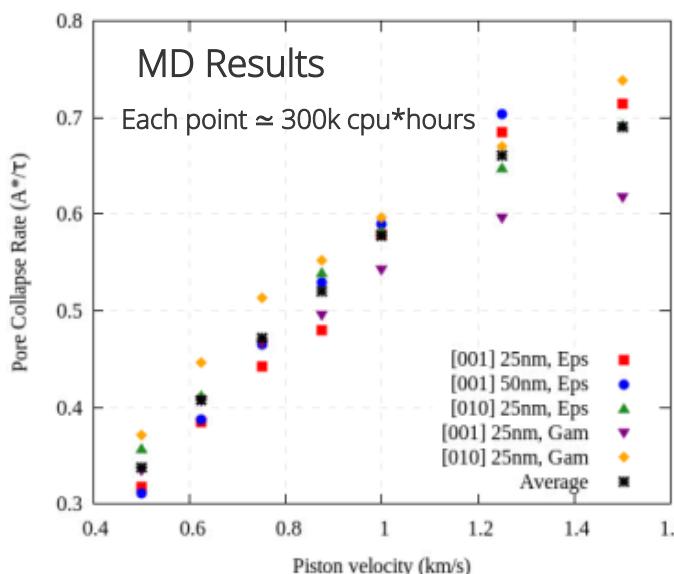
# Coupling Continuum Hydrocode and MD Simulations



# Training Data - Material Strength Measures from MD



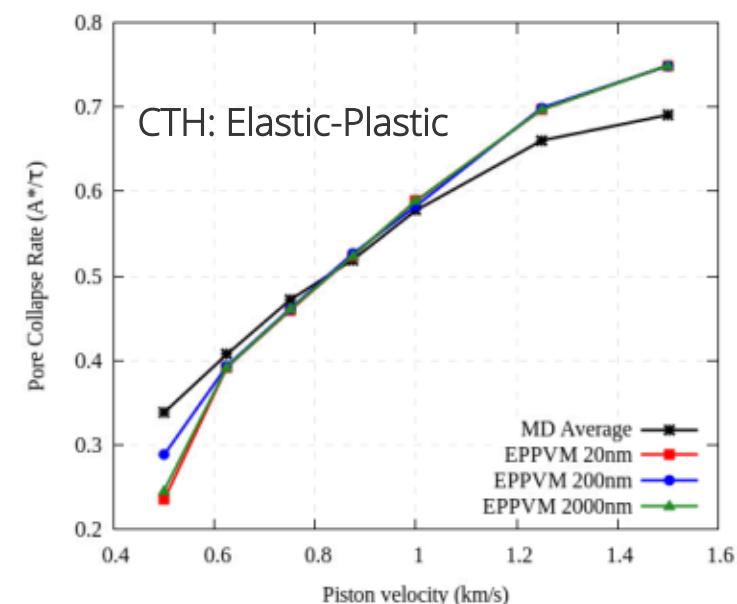
A pore collapse rate of 0.5 means the pore is half closed in the time it takes the shock to travel the diameter of the pore



Viscoplastic: Low  $U_p$ , or large pores

Hydrodynamic: High  $U_p$ , or small pores

How does one accurately model this response in continuum hydrocodes?





# Automated Continuum Strength Model Calibration

## Steinberg Guinan Lund<sup>1</sup> strength model

Yield Strength:

$$Y = \{Y_T(\dot{\varepsilon}_p, T) + Y_{Af}(\varepsilon_p)\}$$

Shear Modulus:

$$G(P, T) = G_0$$

Thermal Activation:  
(Implicit Equation)

$$\dot{\varepsilon}_p = \left\{ \frac{1}{C_1} \exp \left[ \frac{2U_K}{kT} \left( 1 - \frac{Y_T}{Y_P} \right)^2 \right] + \frac{C_2}{Y_T} \right\}^{-1}$$

**Bolded inputs**  
were trained

$$Y_T \leq Y_P$$

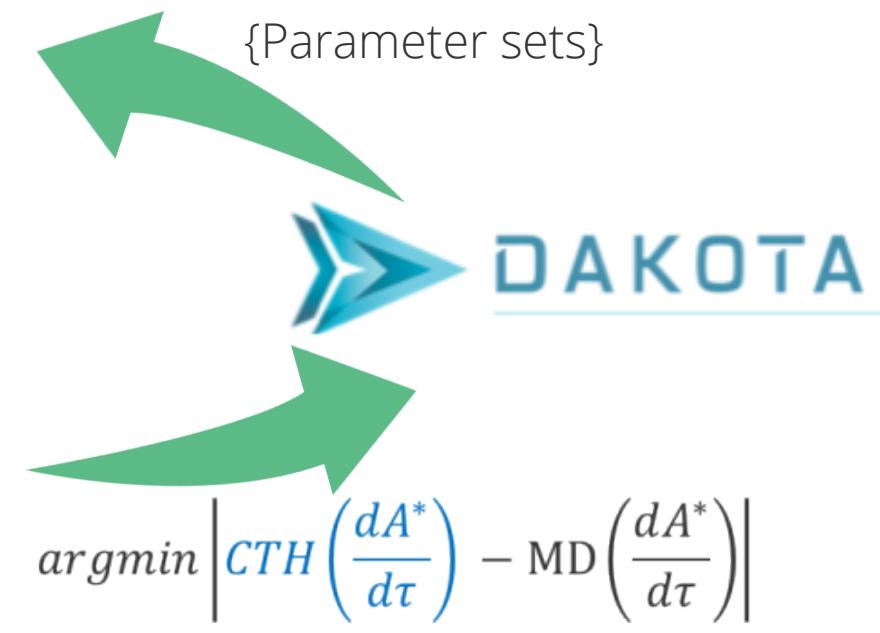
Melting Curve:  
( $Y = 0$  when  $T \geq T_m$ )

$$T_m = T_{m0} \exp \{2a(1 - 1/\eta)\} \eta^{2(\gamma_0 - a - 1/3)}$$

Grüneisen parameter:

$$\gamma = \gamma_0 / (1 + \mu)$$

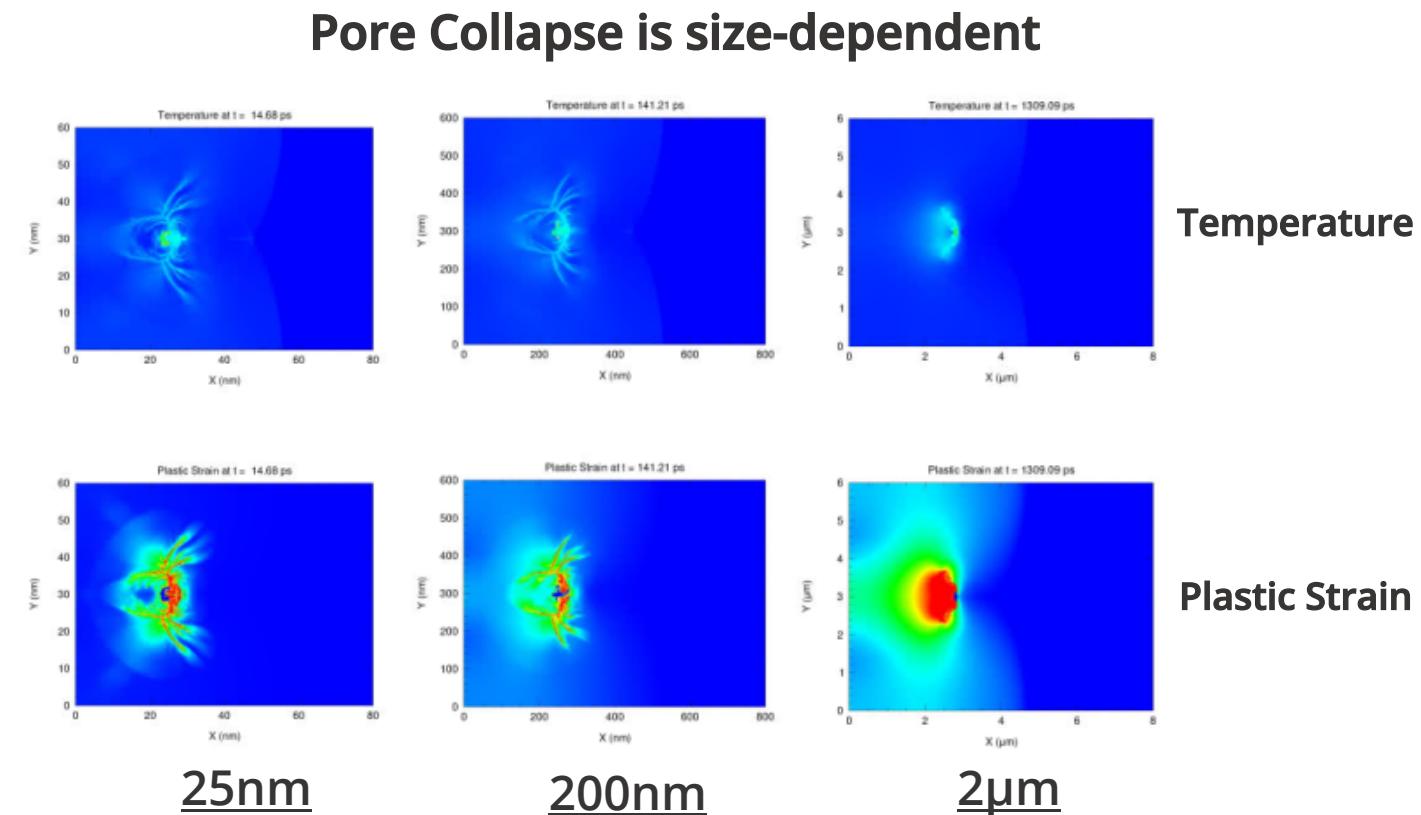
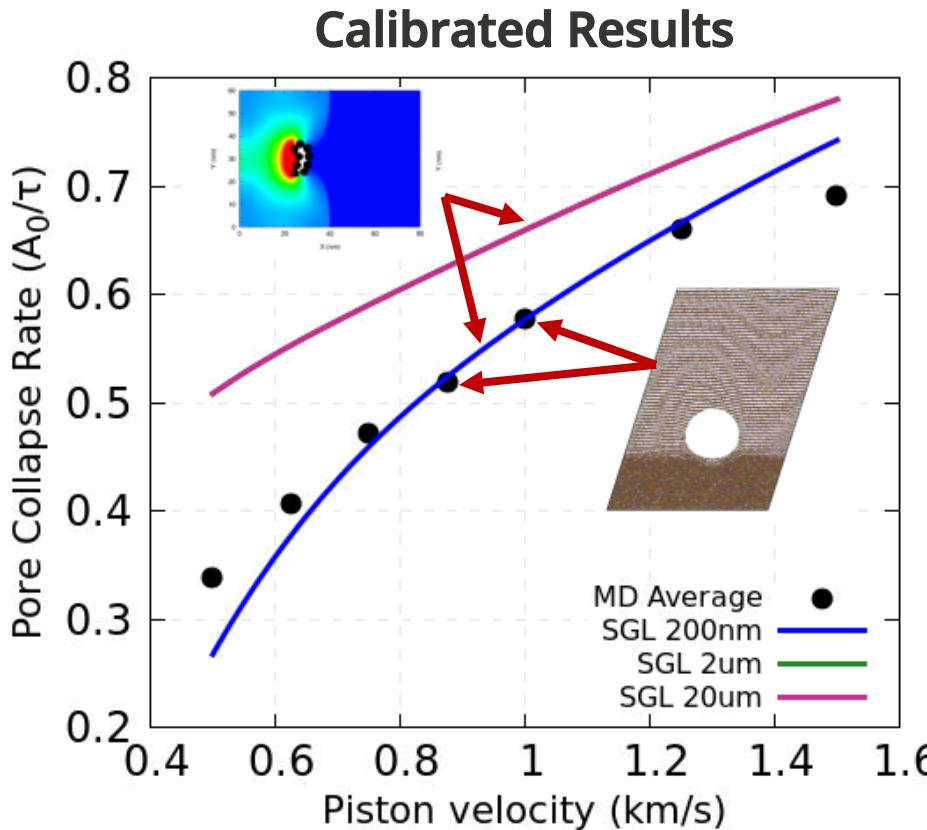
- Assume a constant shear modulus
- Neglect work hardening
- Assume linear variation of the Grüneisen parameter



- Iteratively runs CTH calculations for each parameter set in real time
- DAKOTA workflow is automated

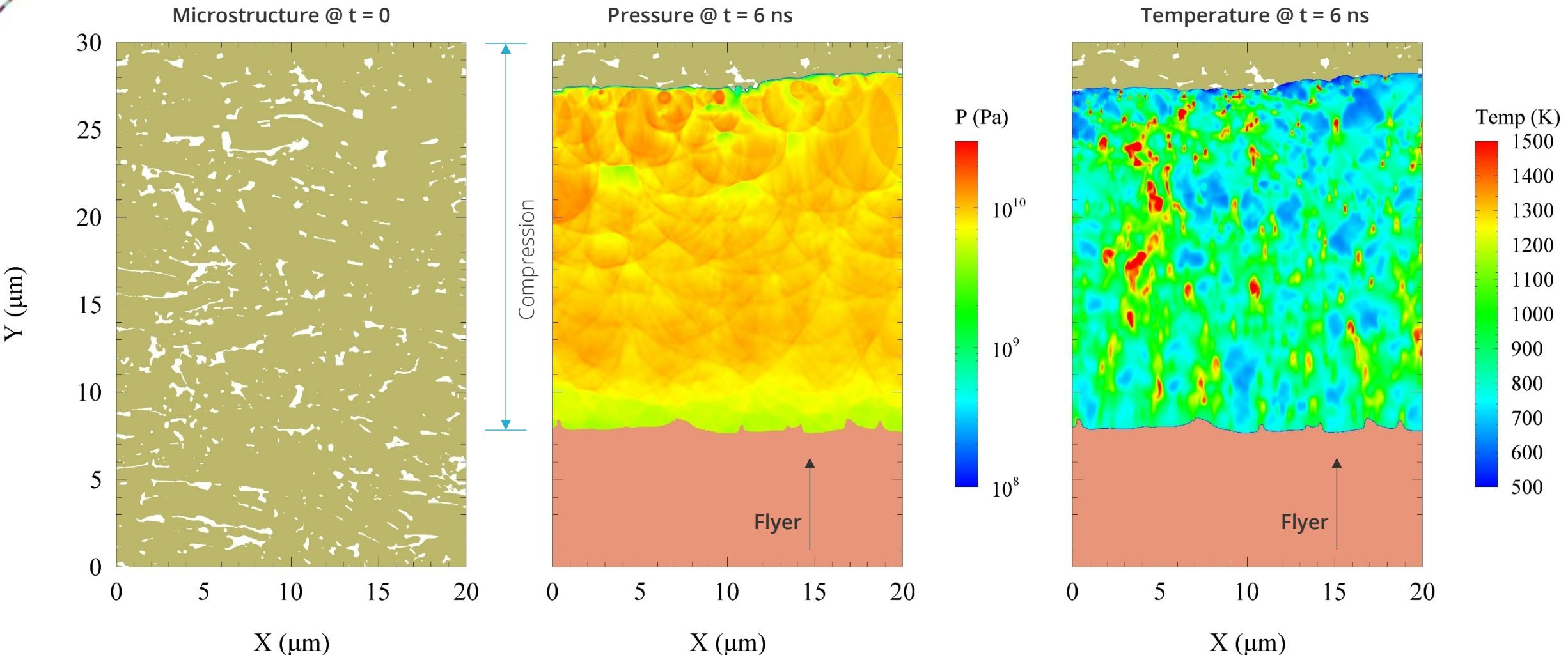
<sup>1</sup>D.J. Steinberg, C.M. Lund, JAP, 65, 1528, (1989)

# Optimization Delivered a Strength Model Calibrated to MD



*Continuum hydrocode (CTH) strength models were trained using results from MD*

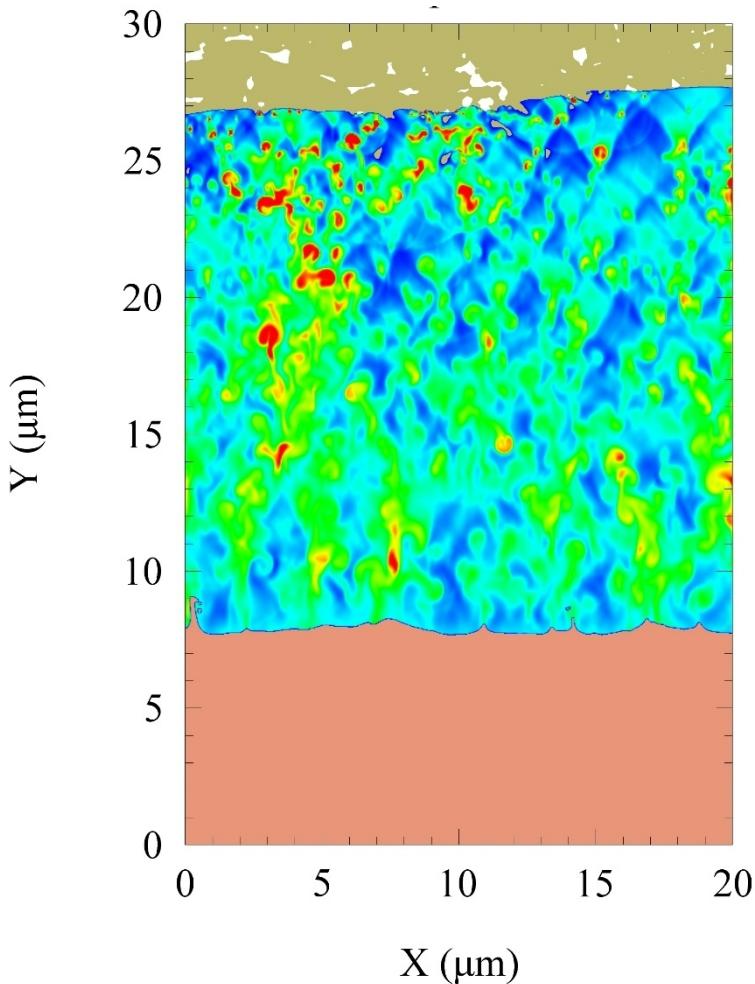
# Hydrocode Simulations - Hotspot Formation



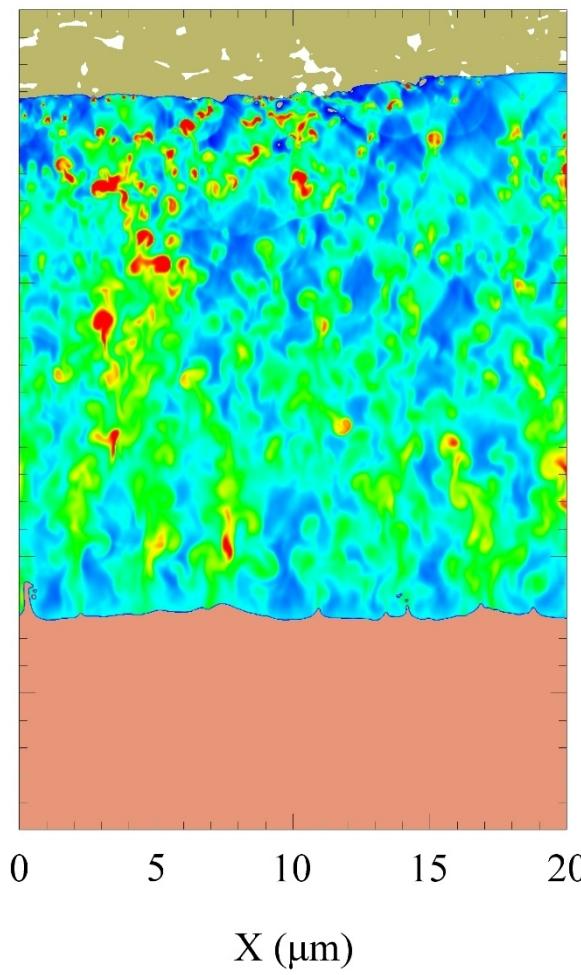
Inert simulation (no reaction) of hotspots, with pressure and temperature fields at time = 6 ns after impact.

# Effects of strength model

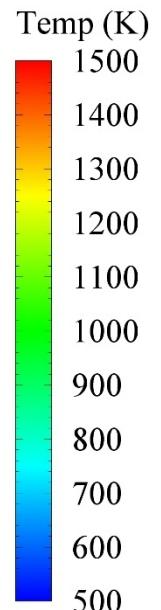
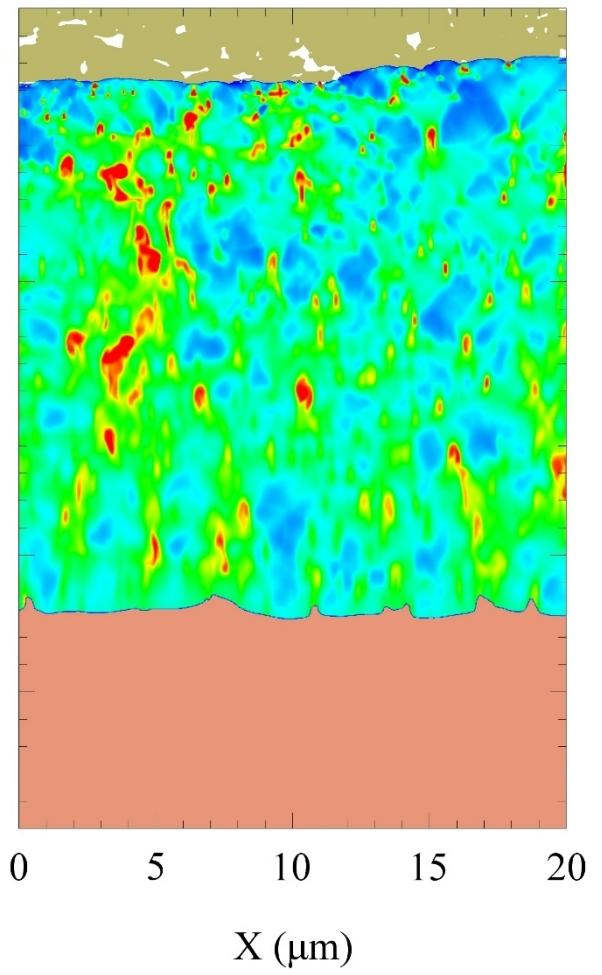
No strength;  
Temperature @  $t = 6$  ns



Elastic-Plastic Model  
Temperature @  $t = 6$  ns

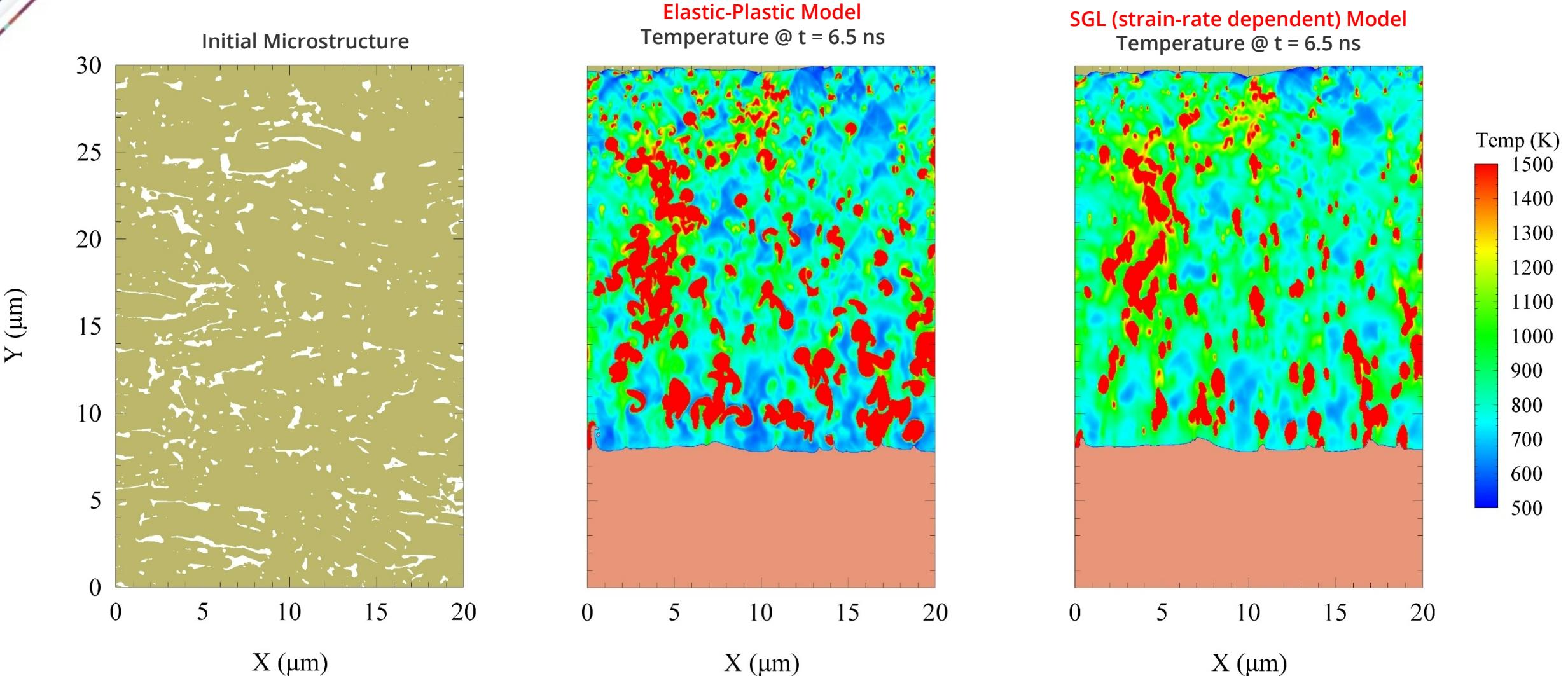


SGL (strain-rate dependent) Model  
Temperature @  $t = 6$  ns



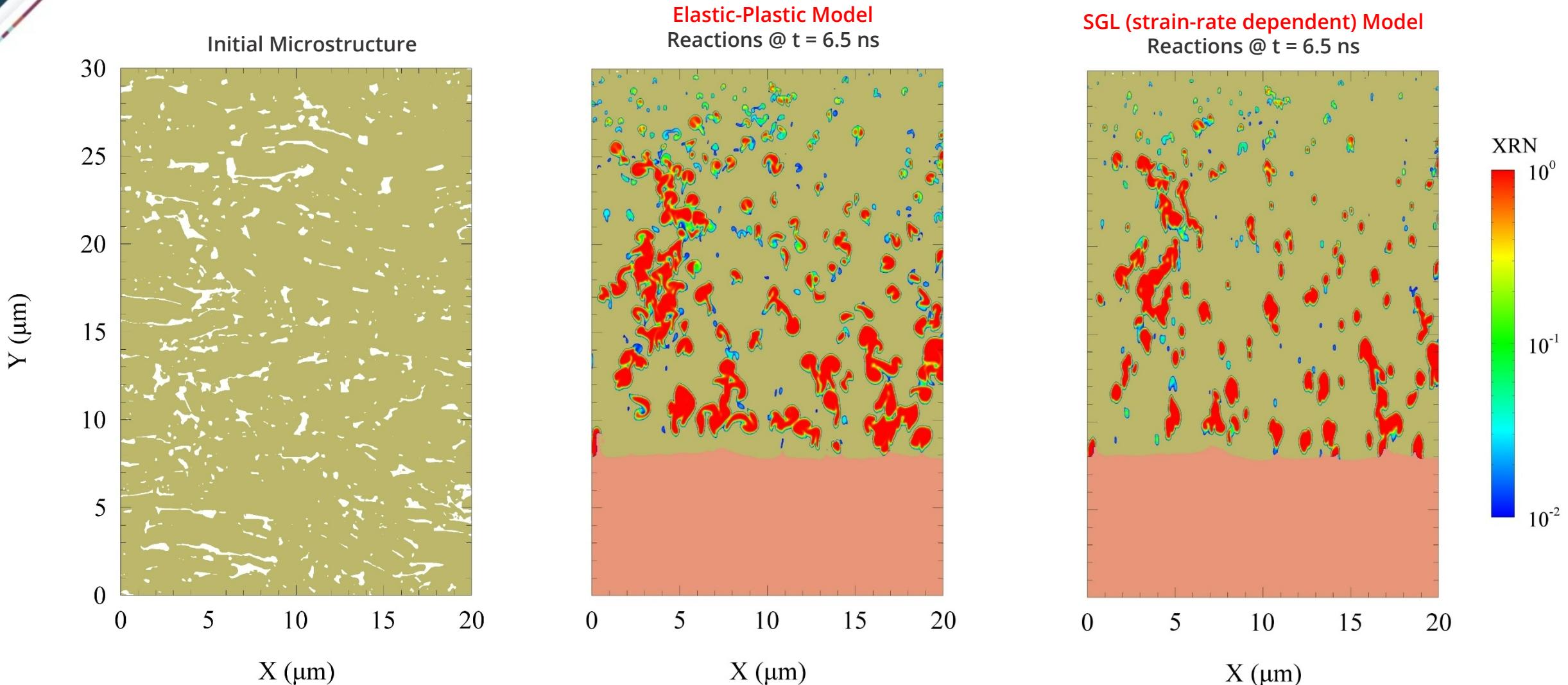
Inert simulation (no reaction) of hotspots due to void collapse and viscous heating;  
(Impact pressure  $\sim 12$  GPa)

# Hotspot Temperature (with Reactions)



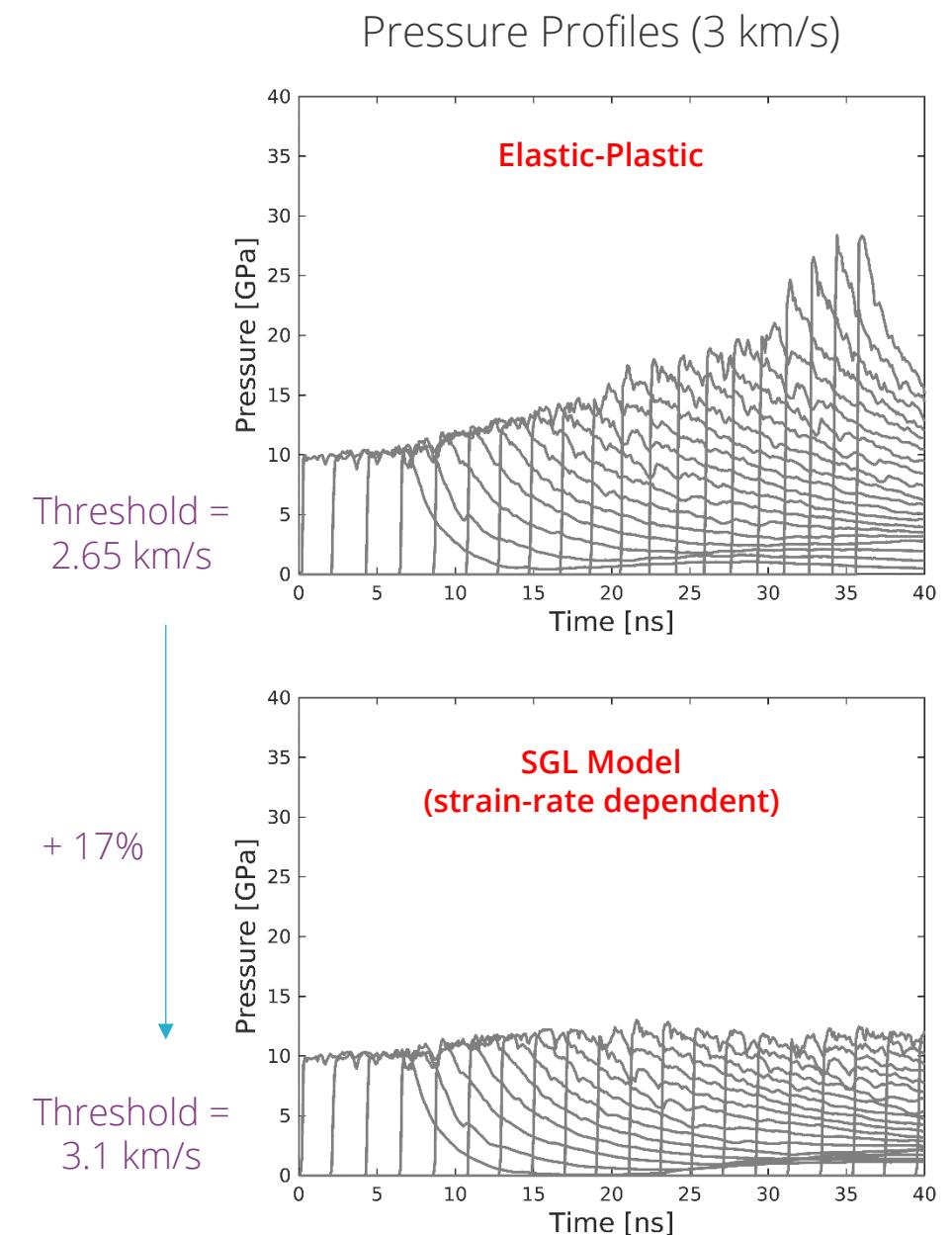
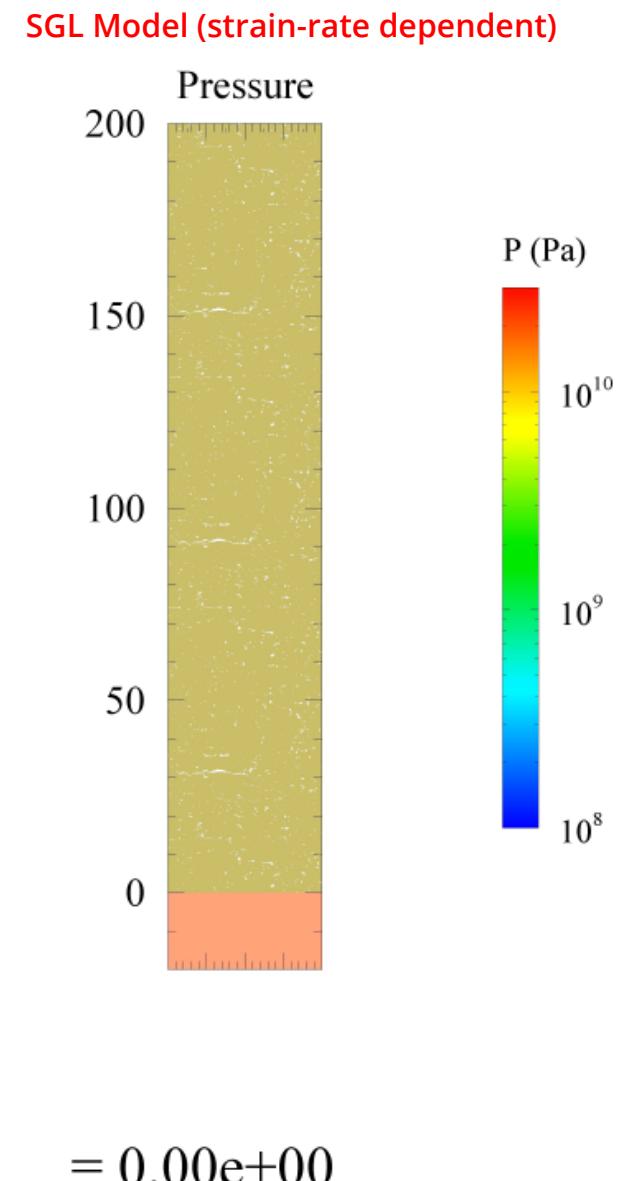
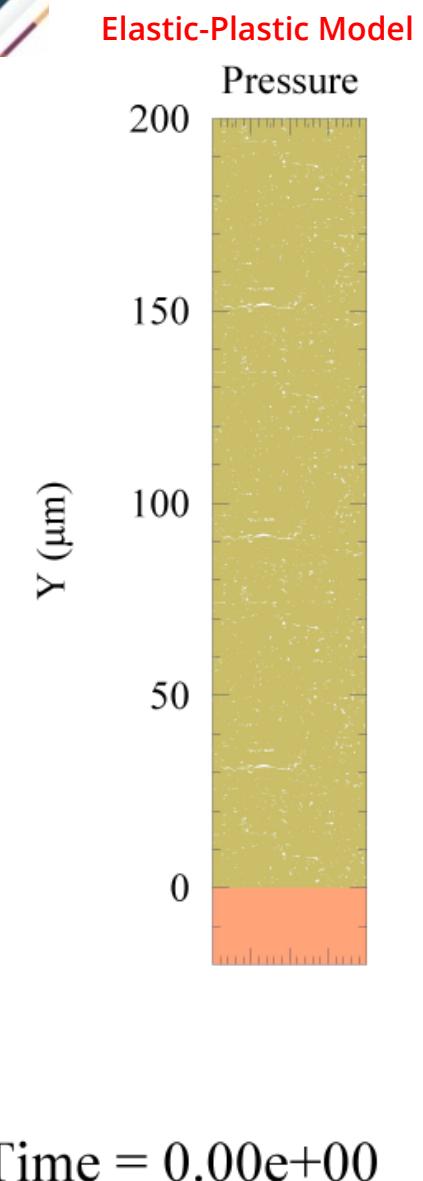
Simulations including reactions show the effects of strength model on the number, size, and shape of hotspots.

# Effects of strength on hotspot reaction



“Extent of reaction” variable (varies between 0-1), illustrates the location of burning hotspots relative to the location of defects in the initial microstructure.

# Full-scale, Direct Numerical Simulations of Detonation





## Concluding Remarks

Multi-scale modeling of energetic materials is rapidly advancing and enabling predictions of microstructure-performance relationships

- SNL has active research programs in Atomistic / Molecular Dynamics and Mesoscale Modeling of HE
- Our objective is to develop *predictive* models of energetic material response (Models that are right, for the right reasons)

Material strength and plasticity play a crucial role in the formation of hotspots

- Models are difficult to validate experimentally at  $< \mu\text{m}$  length scales
- A strain-rate dependent strength model (SGL) was trained using MD results
- The new model significantly influences the details of hotspot formation and run-to-detonation (vs. naïve approaches such as no strength or elastic-plastic)
- This multi-scale approach has added credibility to mesoscale simulations of shock initiation



## Acknowledgements

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- Robert Knepper

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- Judith Brown
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- Julia Hartig

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- Mitch Wood

*Development of a predictive capability for Energetic Materials is a collaborative effort across multiple centers at Sandia*