

High Temperature Gladstone-Dale Coefficient Measurements in a Free-Piston Shock Tube

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Motivation

- Dissociation at high temperatures will affect optical properties of air
- Composite GD is species dependent
- Constant Gladstone-Dale coefficient cannot be assumed
- Temperature and pressure dependence
- No experimental validation currently exists

To make this measurement, we need:

1. Experimental facility capable of generating 5000K and above at moderate to high pressure
→ Shock Tubes
2. Diagnostic to resolve large discrete density changes

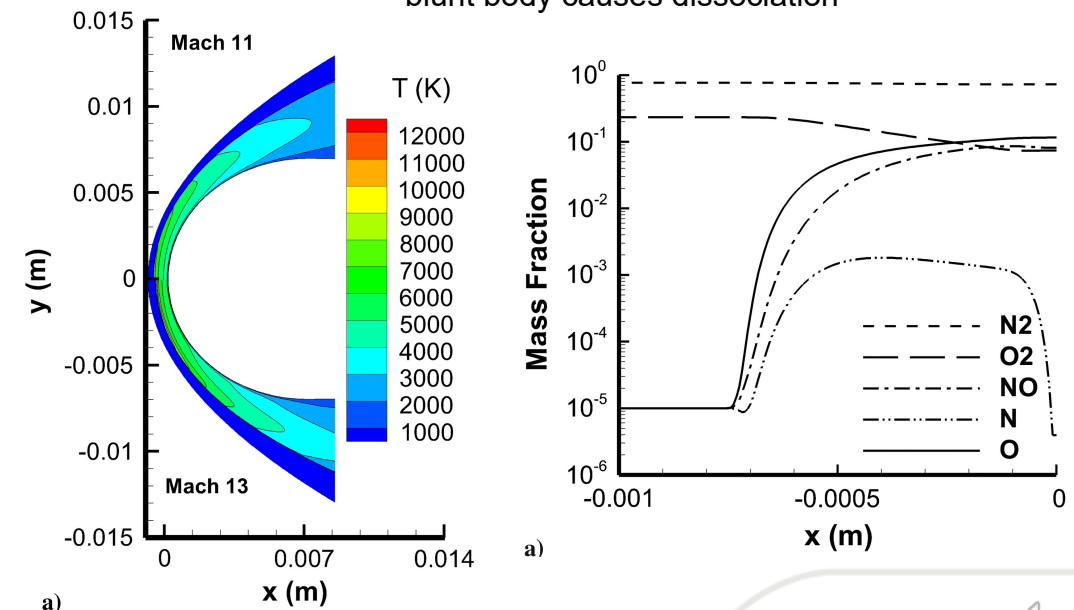
index of refraction

s - denotes species

$$\frac{n - 1}{\rho} = GD = \sum GD_s \frac{\rho_s}{\rho}$$

density Gladstone-Dale Coefficient

Example: Stagnation flow over a blunt body causes dissociation



Gladstone-Dale Simulation

- Wavelength dependence of gas species
 - N_2 , O_2 , NO are well tabulated
 - N and O from experimental data
 - Carbon species and electrons are not considered here

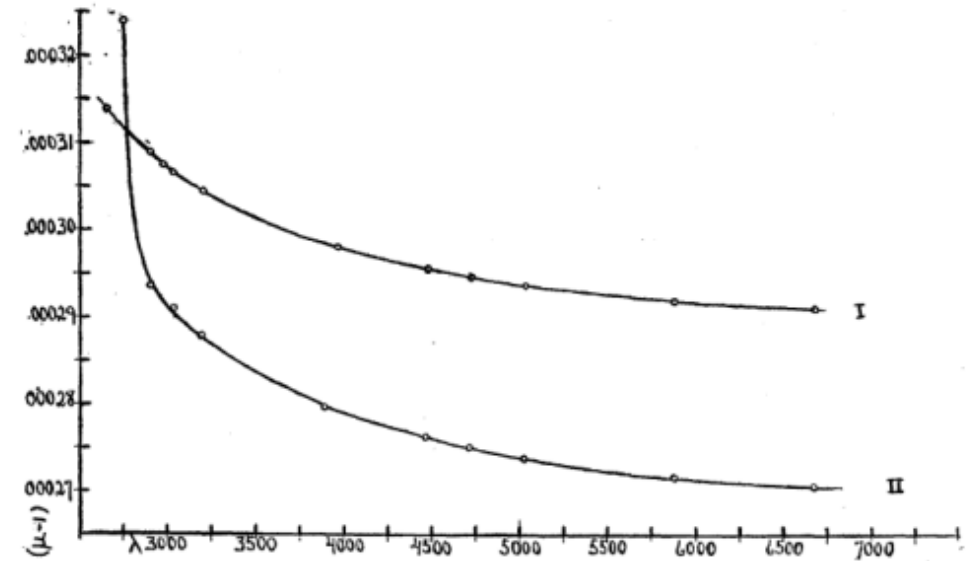
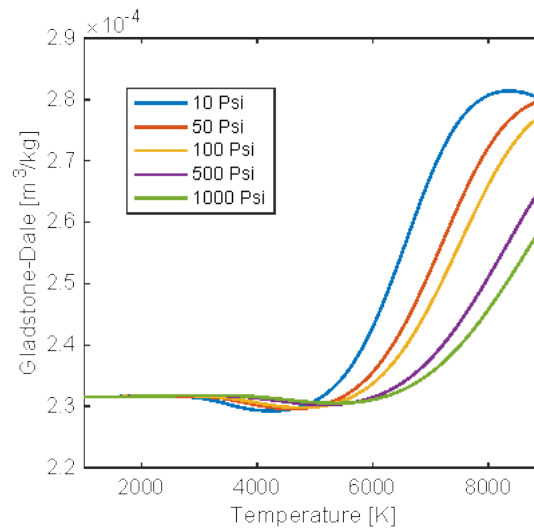
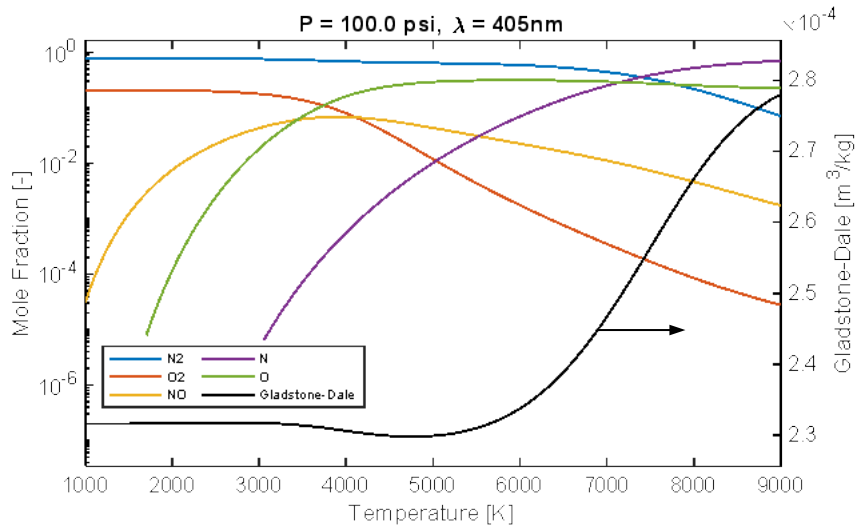


Fig. 3.

Dispersion Curves: I., Air; II., Oxygen. Abscissae: λ in Angstrom units. Ordinates: $(\mu - 1)$.

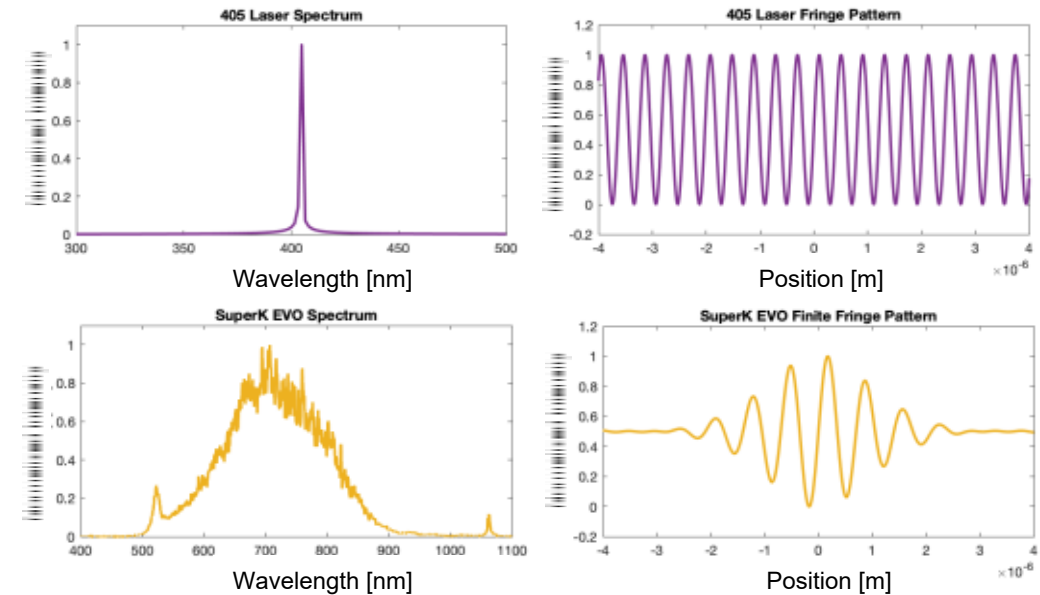
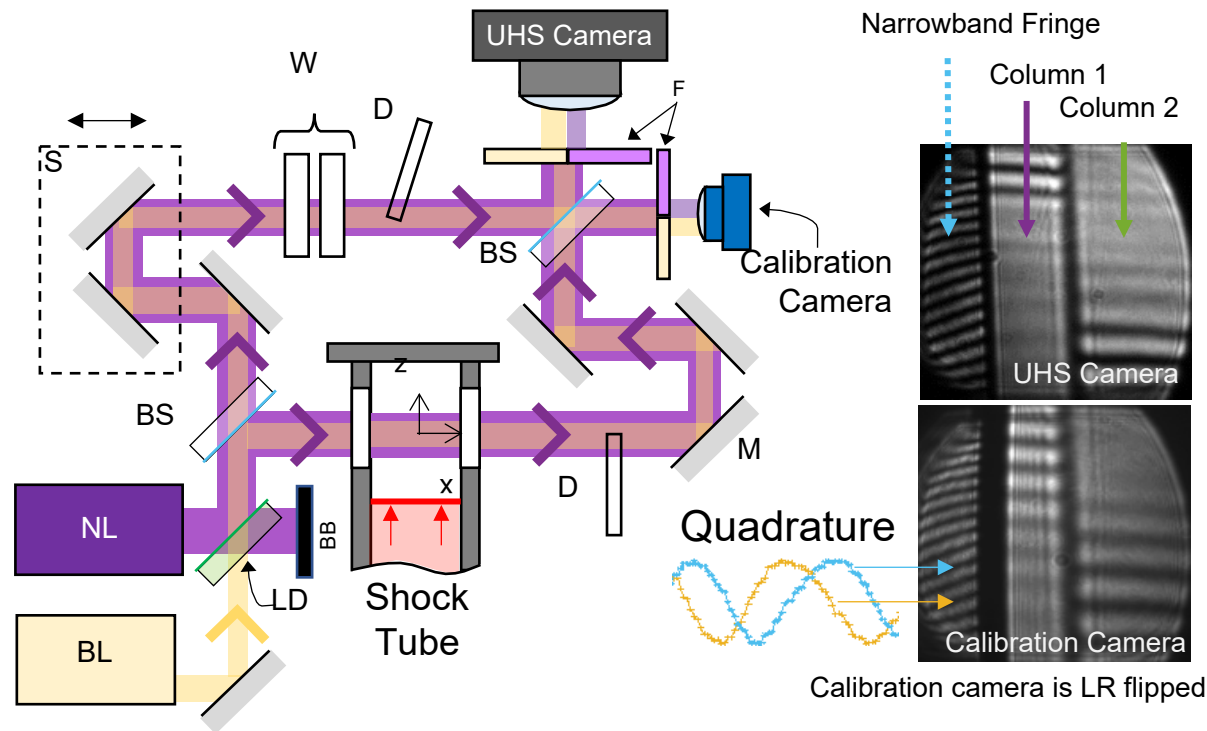
Howell, Janet Tucker. *Physical Review* 6.2 (1915)

- Equilibrium composition of air at constant P varies with T
 - Presence of N and O significant past $\sim 3500 \text{ K}$

QFII Diagnostic

Quadrature Fringe Imaging Interferometer

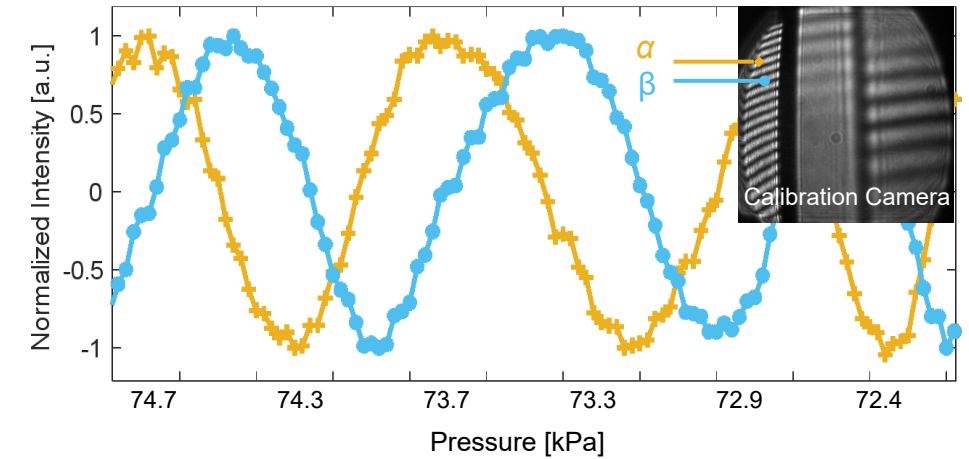
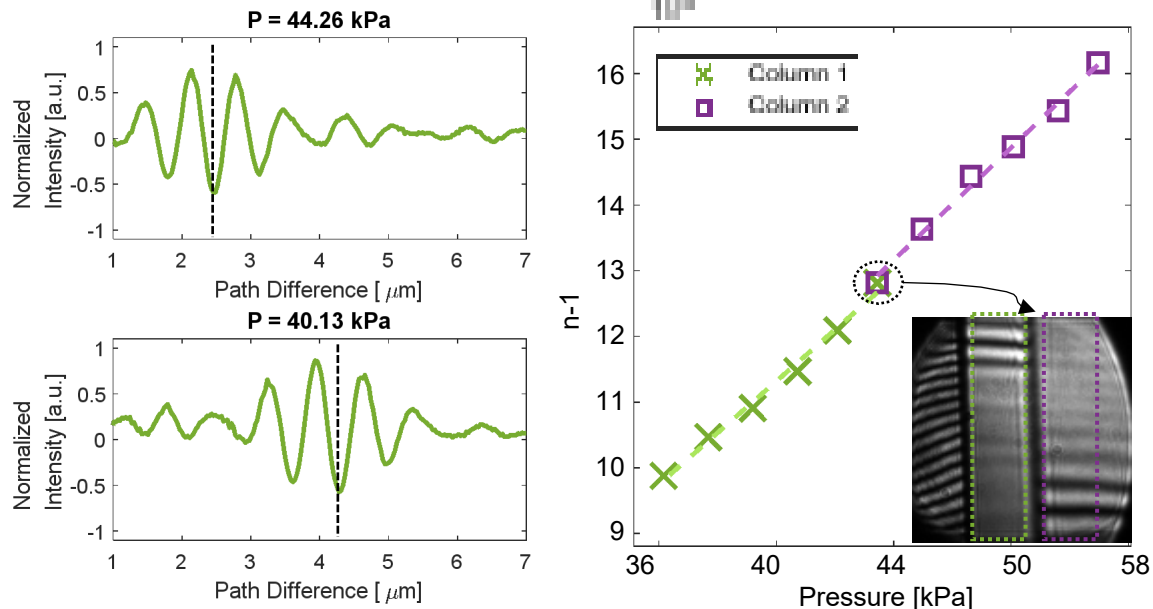
Hybrid broadband and narrowband technique for measuring large and discrete density gradients



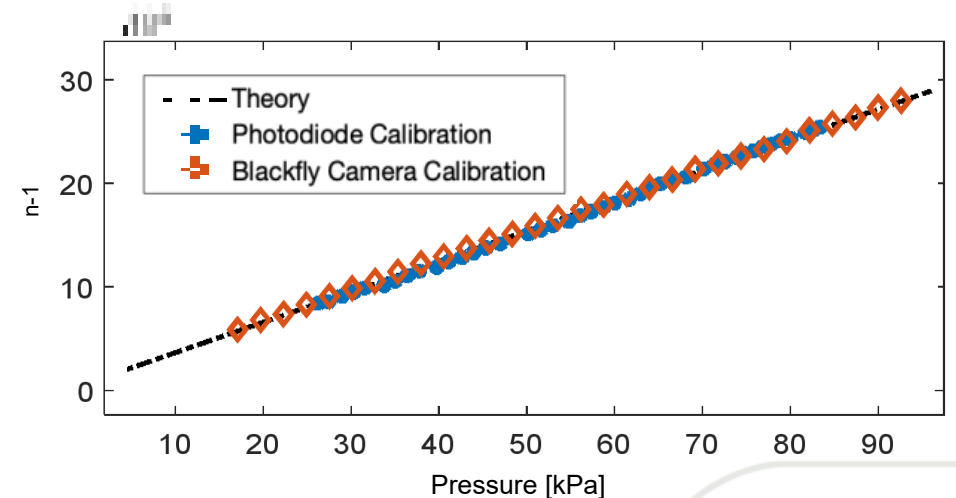
- Narrowband analog quadrature to automate tracking for high resolution
 - 405 nm laser diode
- Balanced broadband pattern for absolute reference
 - SuperK EVO supercontinuum source

Calibration

- Calculate absolute index with narrowband analog quadrature
- This technique leads to the highest resolution and automated tracking
- Calibration verified with linear GD relationship at ambient conditions
- Location of center fringe also related to index

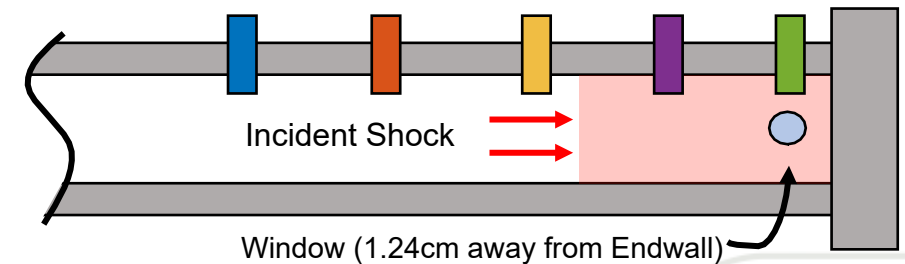
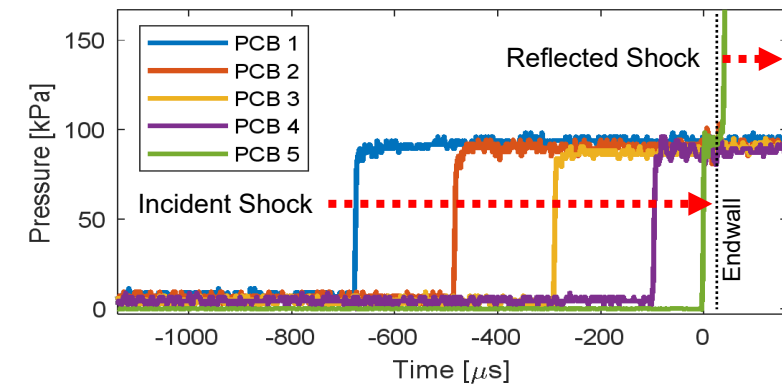
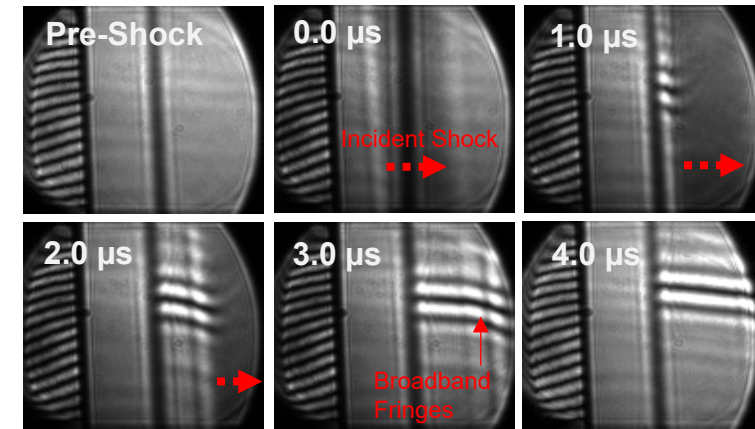
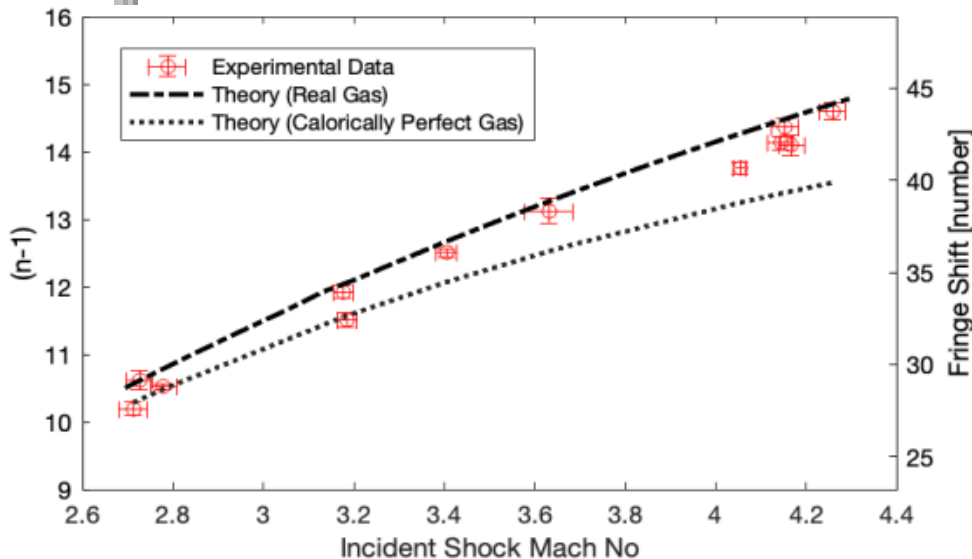


$$\Delta n = \frac{\lambda}{\pi W} \tan^{-1} \left(\frac{\beta(\Delta n) + \alpha(\Delta n) \sin(\phi_{\alpha\beta})}{\alpha(\Delta n) \cos(\phi_{\alpha\beta})} \right)$$



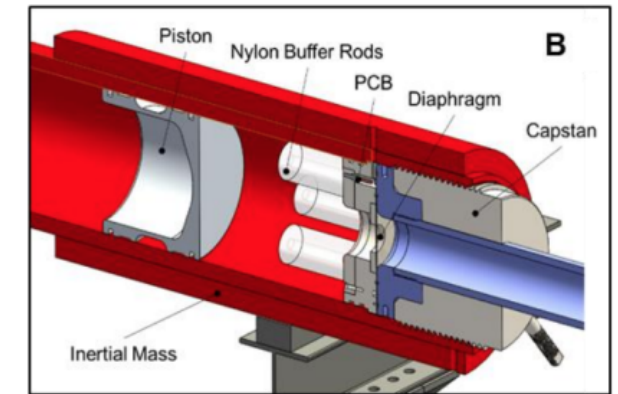
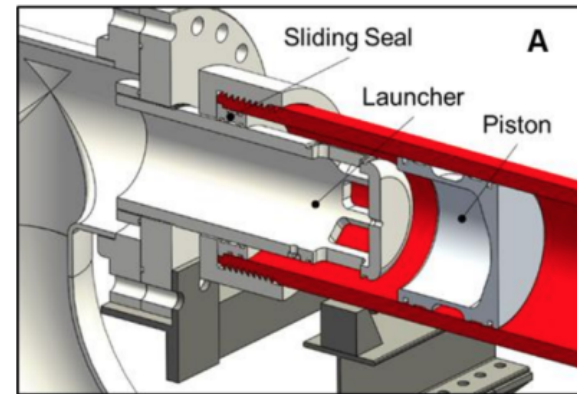
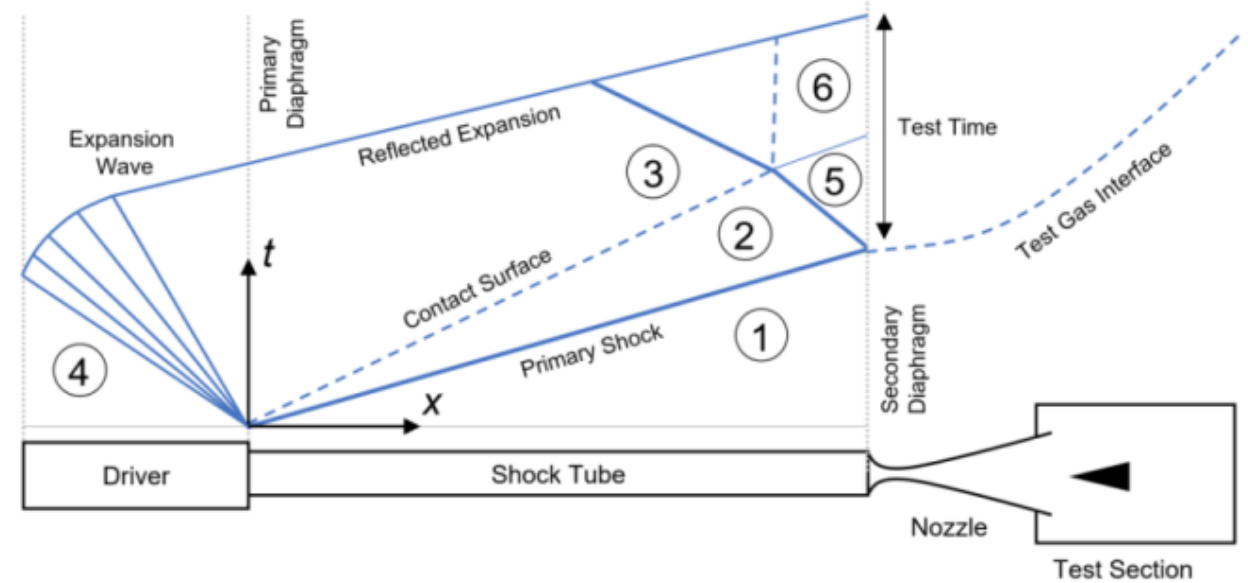
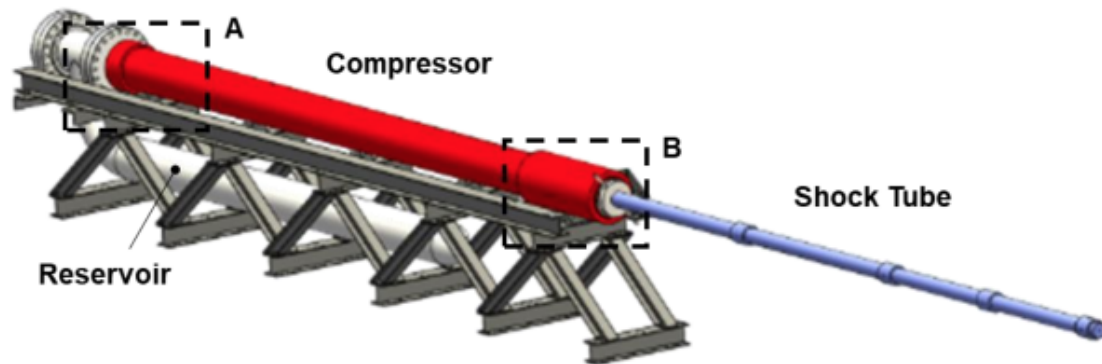
Shock Tube Experiments at Georgia Tech

- Post incident-shock conditions measured with QFII
 - M2.7 - M4.3
 - Constant $P_1 = 10.7 \text{ kPa} = 80 \text{ Torr}$
 - He driver gas and air driven gas
- Results agree with theory within 2%

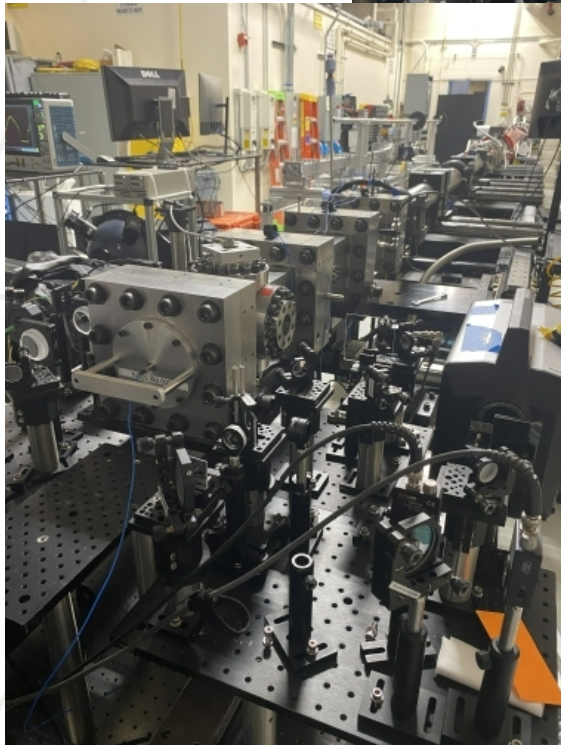
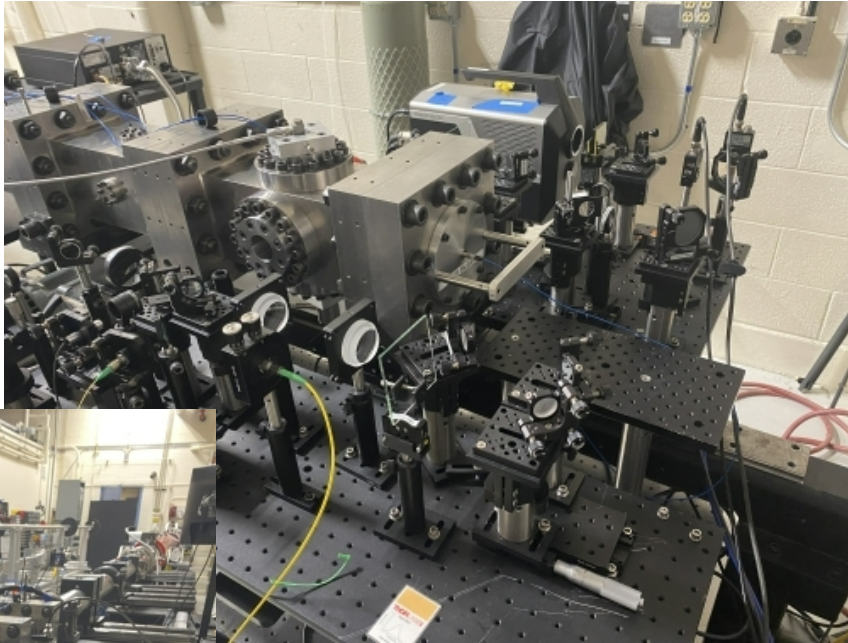


Sandia Free-Piston HST

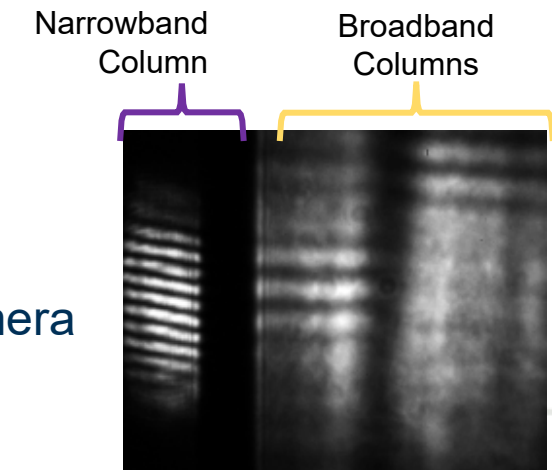
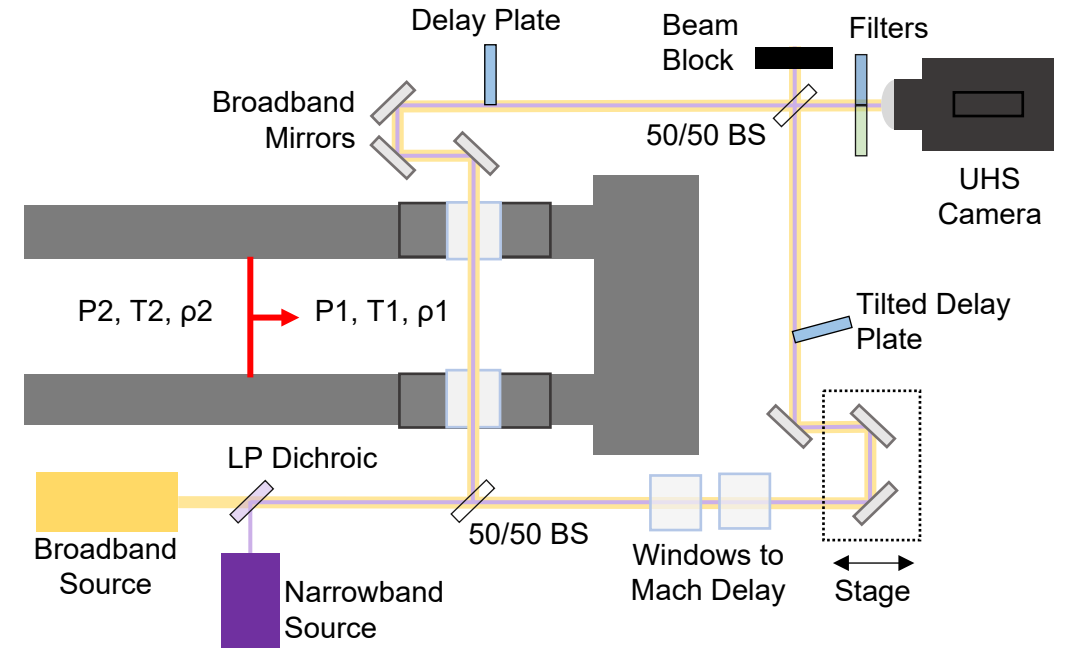
- Capabilities beyond traditional shock tubes
 - 35kg piston compressed driver gas more efficiently
 - Post reflected shock conditions able to reach 6000-8000K at pressures > 100 psi
- Conditions calculated with wave speed and NASA CEA



Experimental Setup

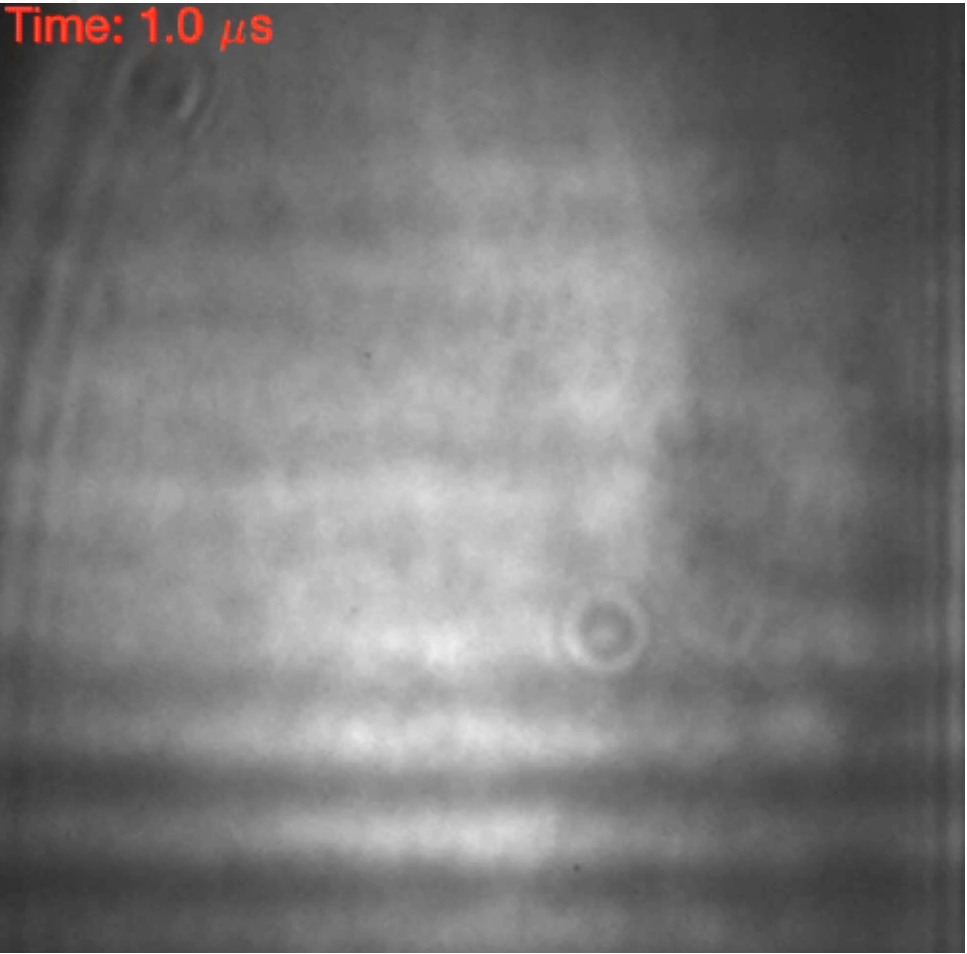


- Mach-Zehnder interferometer
 - 405 nm laser diode
 - SuperK supercontinuum source
- Calibration was done with UHS Shimadzu camera
- External vibrations increased uncertainty
- Triggering off endwall PCB



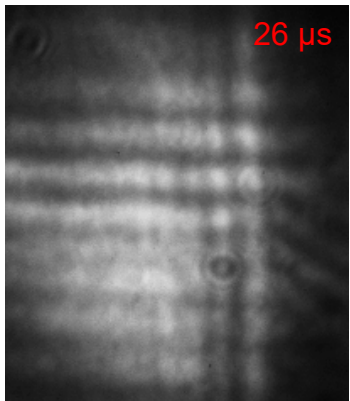
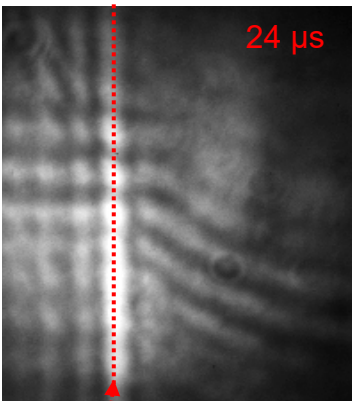
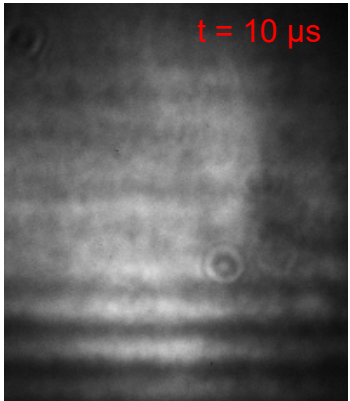
Results - Video

Shimadzu HPV-X2
1MHz, 200 ns exposure



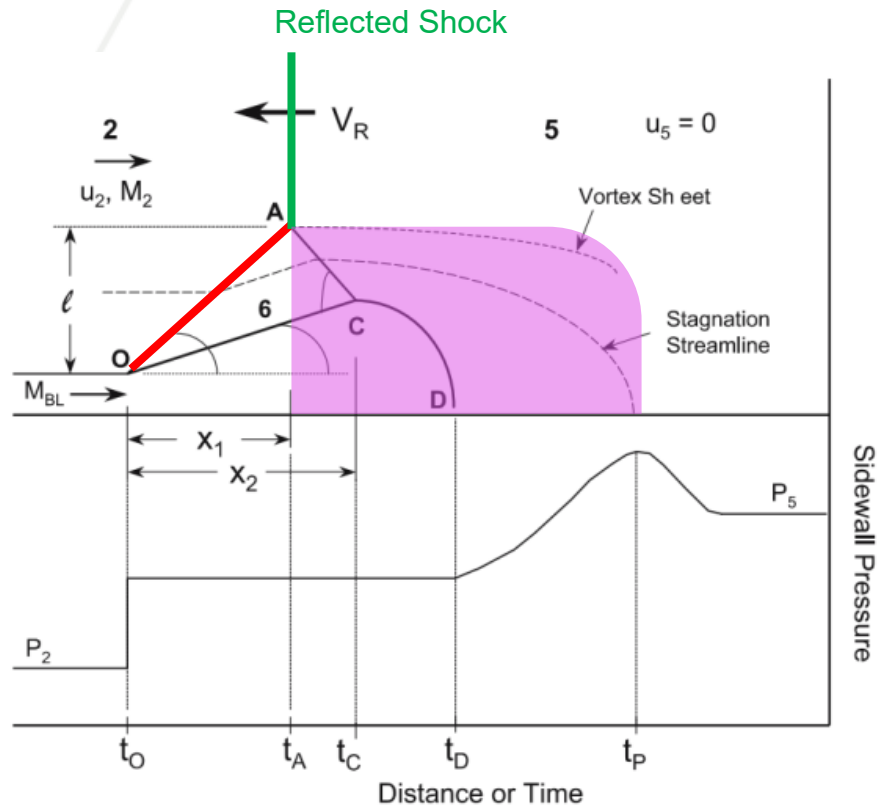

Direction of Reflected Shock Wave
(Incident Shock M13.95)

State 5		State 2	
P5	7.87 Bar	P2	0.63 Bar
T5	7653 K	T2	5343 K
ρ 5	0.24 kg/m ³	ρ 2	0.03 kg/m ³



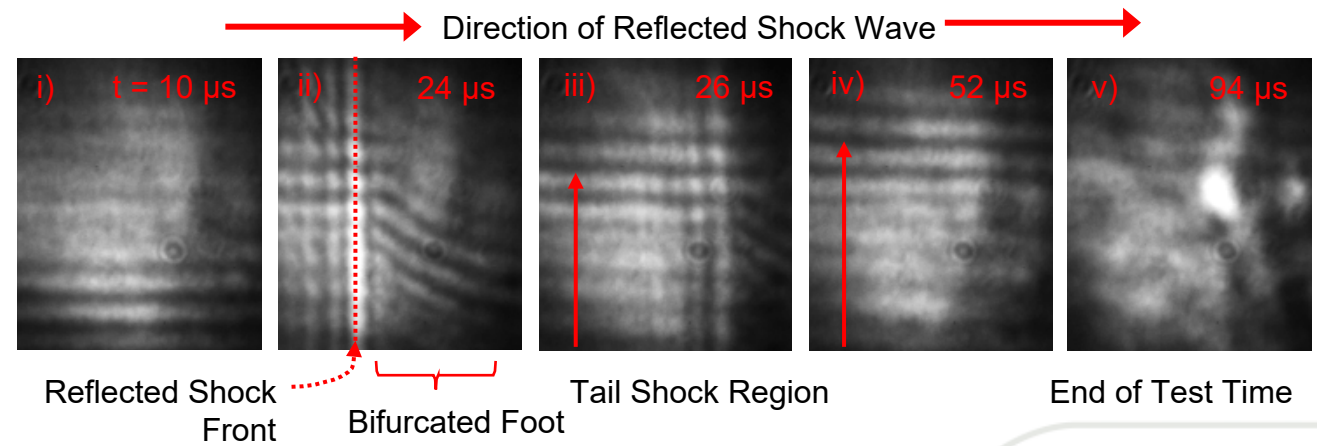
Reflected Shock
Front

Reflected Shock Flow Bifurcation



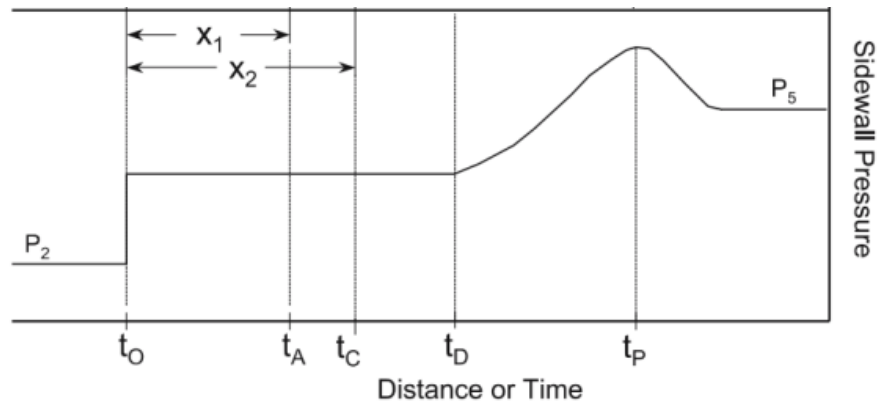
Petersen, E.L., Hanson, R.K. *Shock Waves* **15**, 333–340 (2006).

- In GT experiments, post-incident shock flow shows a nearly discrete index change
- Boundary layer interaction with reflected shock front causes bifurcation
 - Foot
 - Tail Shock (Vortex sheet and stagnation streamline)
- Petersen and Hansen reported similar time scale
 - 20-30 μs before actual P5, T5 conditions

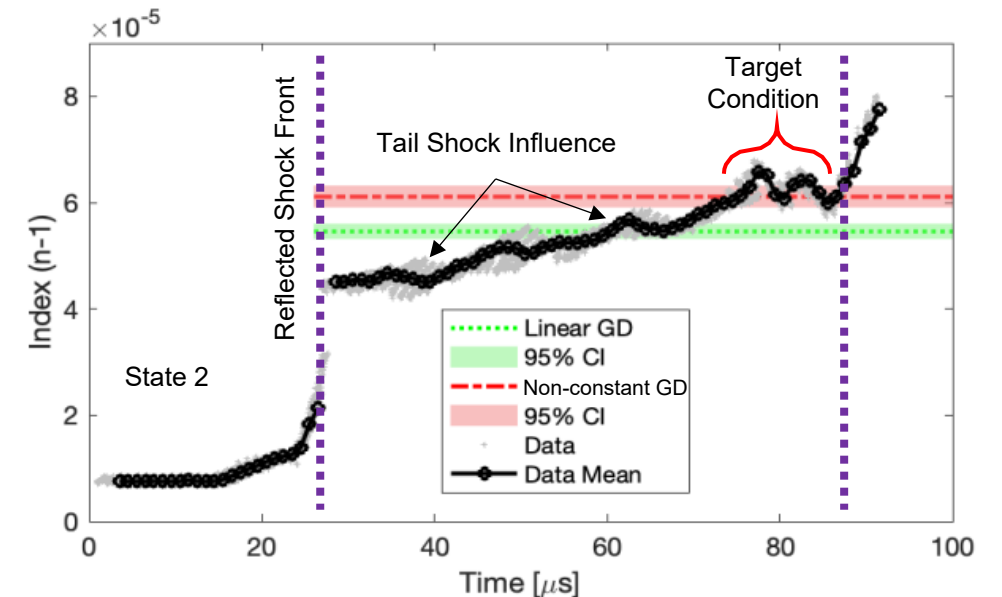
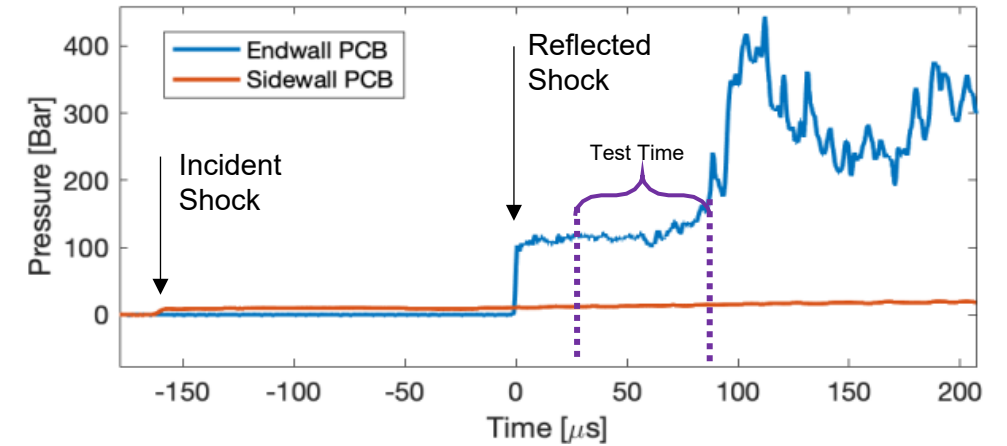


Results - Index of Refraction

- Post-incident and post-reflected shock were within the measurement range
- Rising index right before shock front captures the bifurcation foot
- Index continues to rise due to tail shock influence before measurement time ends
- Bifurcation produces additional challenges to extract index measurement at a single condition

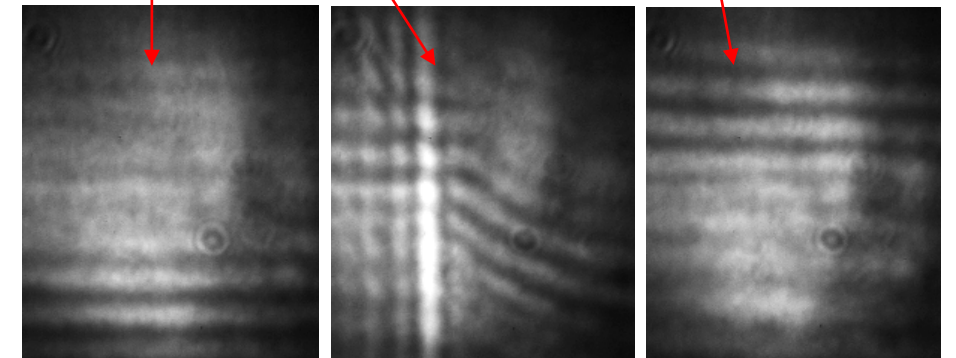
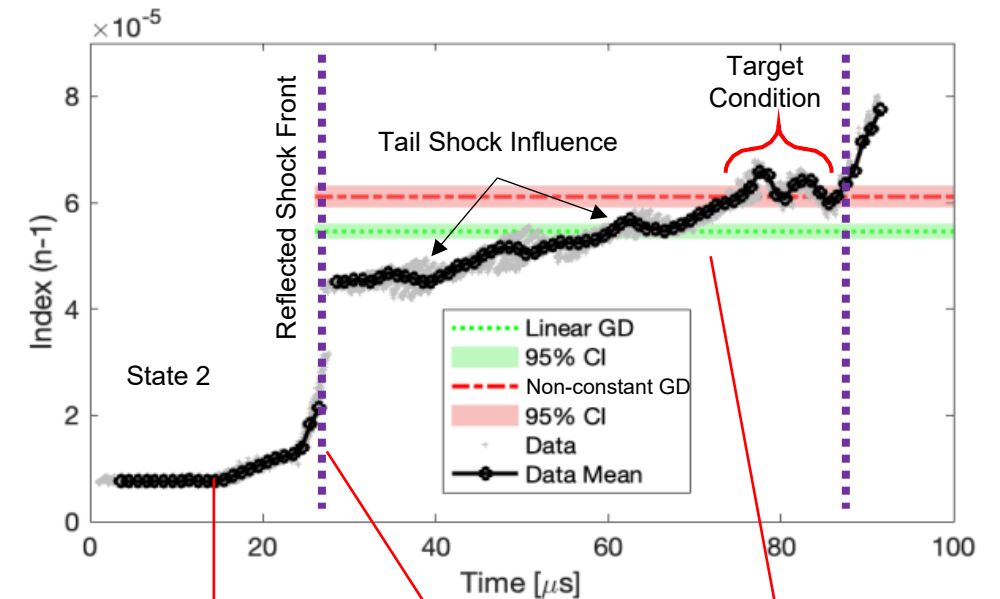
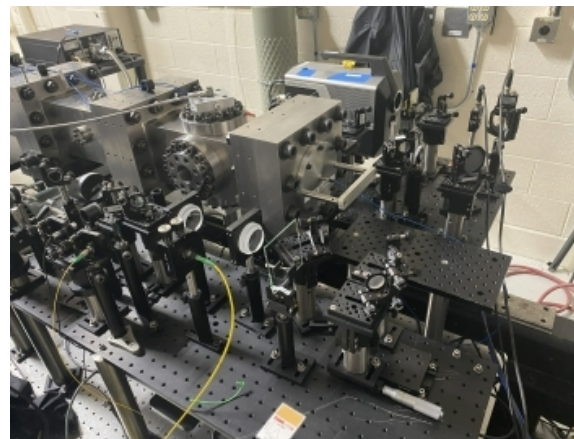
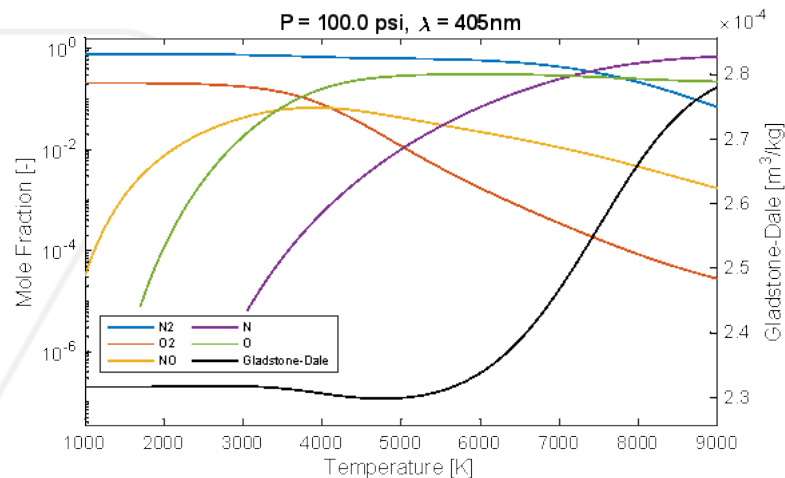


Petersen, E.L., Hanson, R.K. *Shock Waves* **15**, 333–340 (2006).



Summary and Conclusion

- First known Gladstone-Dale coefficient measurements above 5000K at high pressures
- Free-piston facility combined with QFII diagnostic in a high pressure, high temperature reflected shock conditions
- Reflected shock flow has complex bifurcation features
- Higher density conditions necessary to generate better validation data



Thank you for listening! Questions?



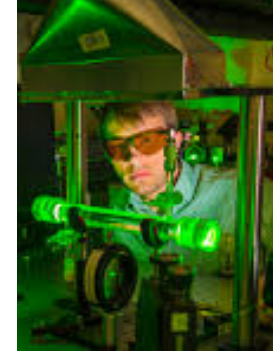
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