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Helical deformation of 3D defects in a premagnetized Z-pinch liner



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2022 APS DPP

Spokane, Washington

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°University of Nevada at Reno

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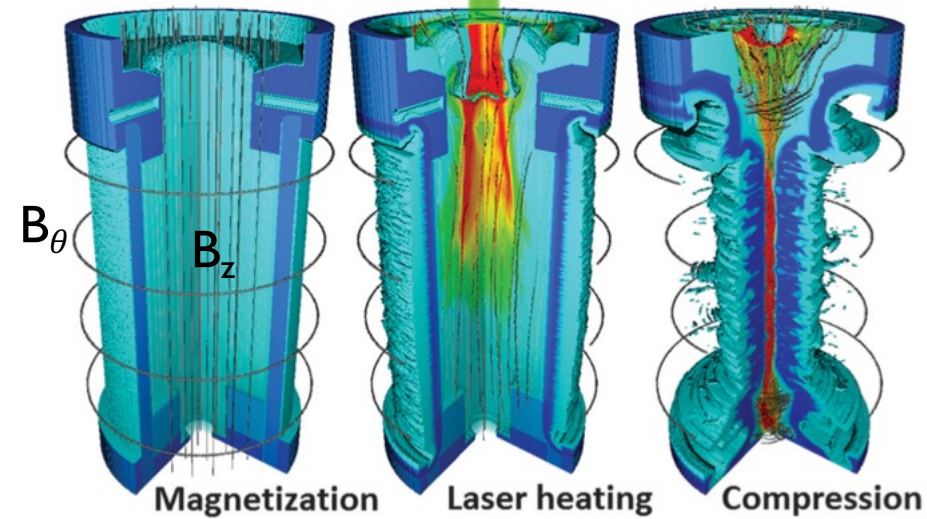


This research was supported by the Sandia Laboratory Directed Research and Development Program under Projects 178661 and 200269



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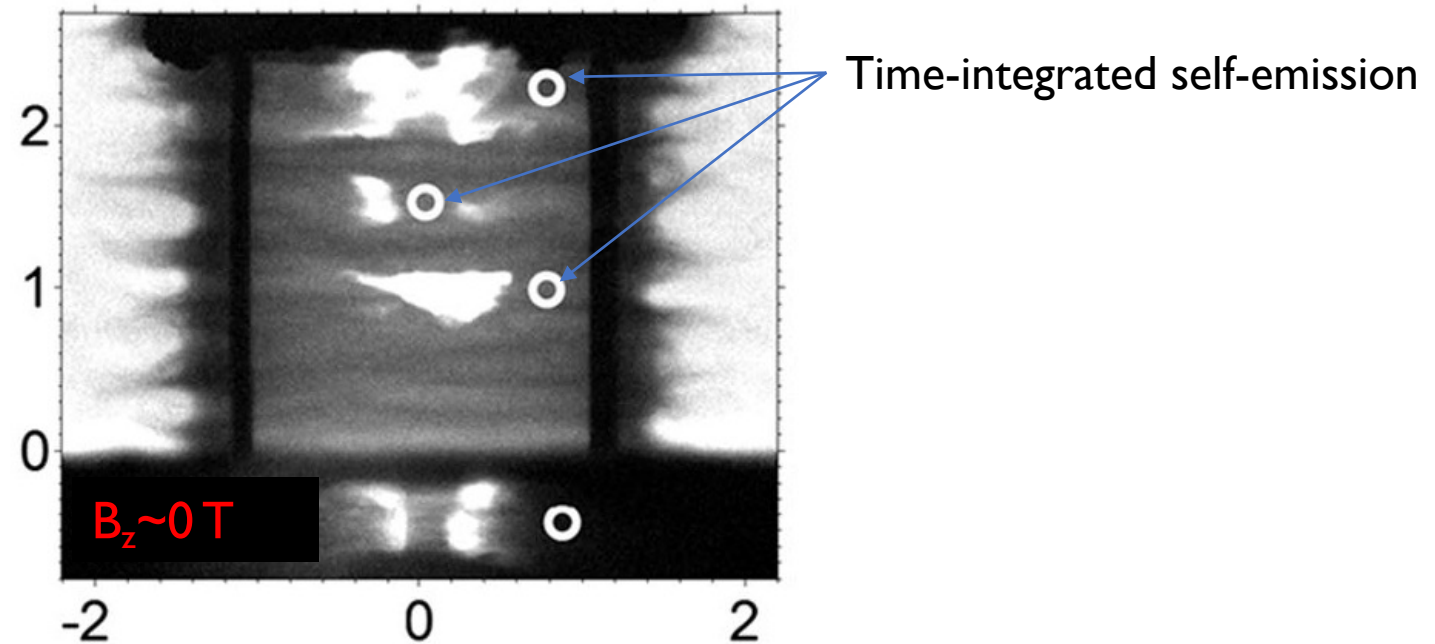
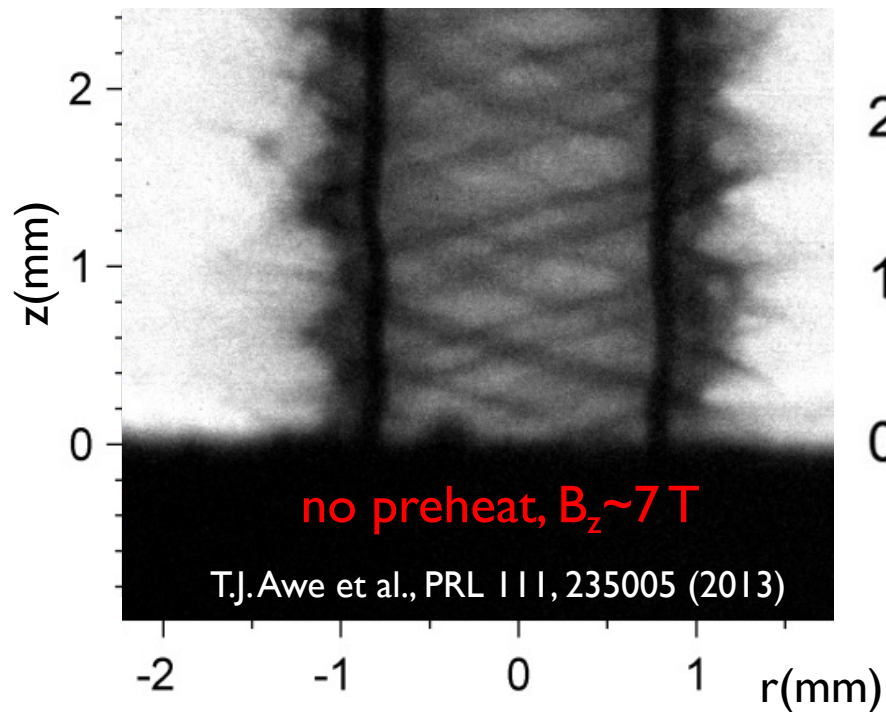
Magnetized liners develop helical structures



MagLIF: azimuthal magnetic field (B_θ) compresses liner filled with premagnetized (B_z) fusion fuel.

S.A. Slutz et al., Phys. Plasmas 17, 056303 (2010)

M.R. Gomez et al., PRL 125, 155002 (2020)



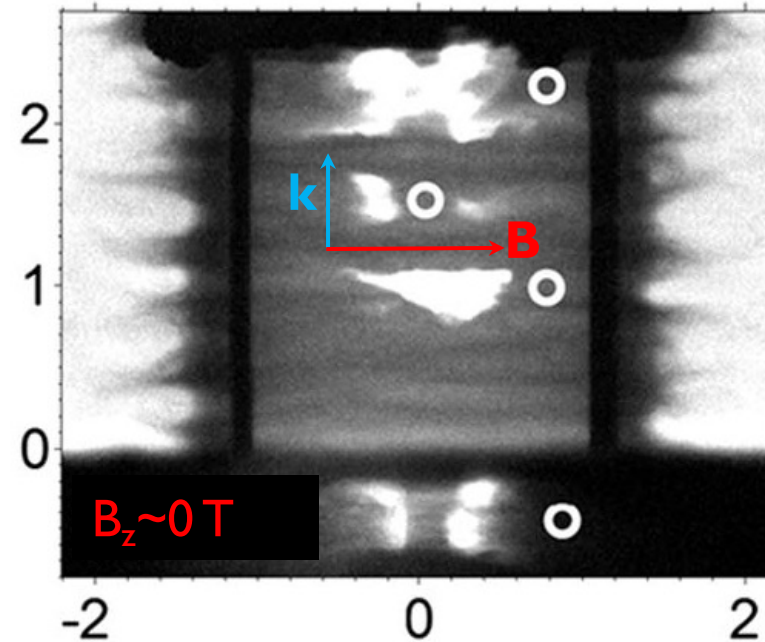
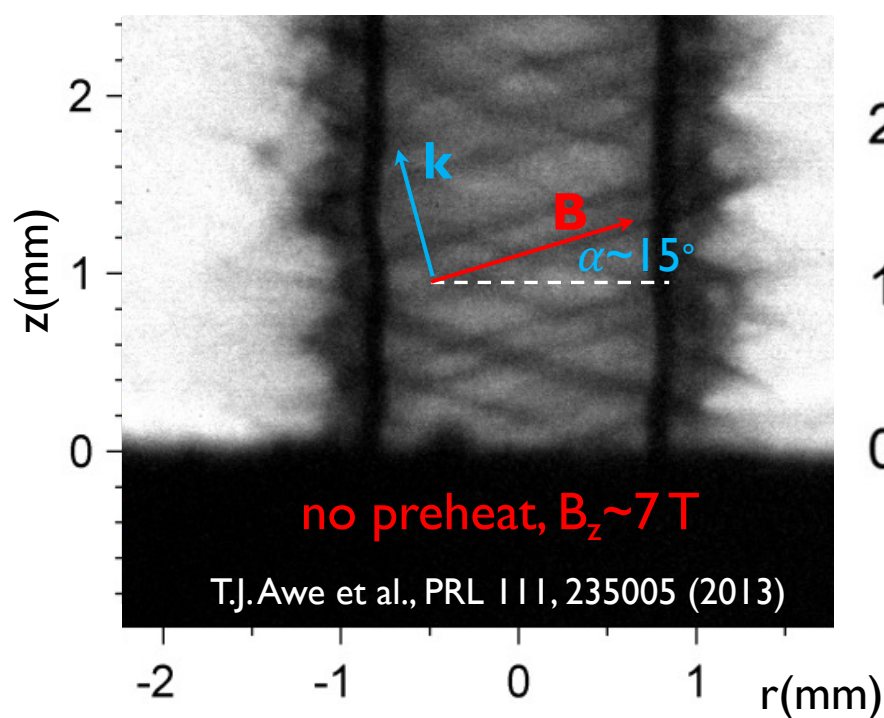
The origin of the helical mode remains an open research question



From instability theory, $\mathbf{k} \cdot \mathbf{B} = 0$ minimizes the (stabilizing) \mathbf{B} field line bending

However, this condition implies a much larger B_z than the expected value:

$$\mathbf{k} \cdot \mathbf{B} = 0 \Rightarrow B_z = B_\theta \tan(\alpha) = 700 \text{ T} \gg 7 \text{ T}$$

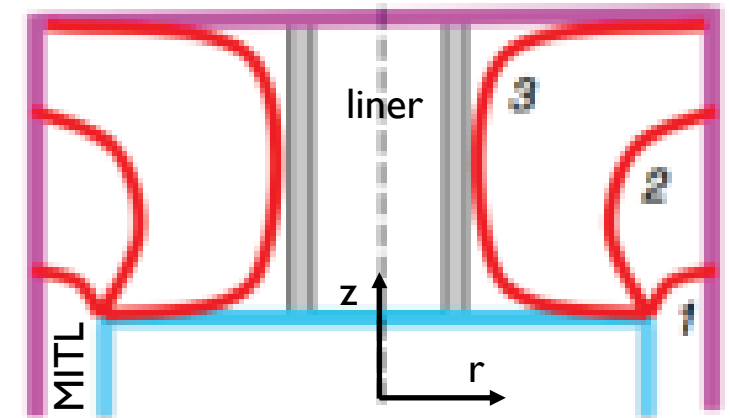


The origin of the helical mode remains an open research question



Low-density plasma from MITL (magnetically insulated transmission line) sweeps up, compresses, and amplifies B_z at liner surface

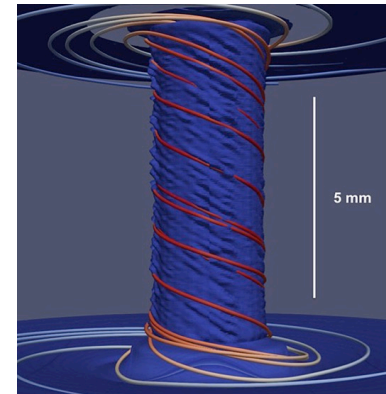
D. D. Ryutov et al., AIP Conf. Proc. 1639 (2014)



3D simulations demonstrate viability of flux compression hypothesis and importance of Hall term in modeling this effect

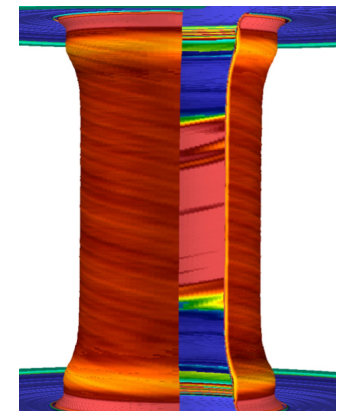
C.E. Seyler, M.R. Martin, and N.D. Hamlin, PoP 25, 062711 (2018)

J.M. Woolstrum et al., PoP 27, 092705 (2020)



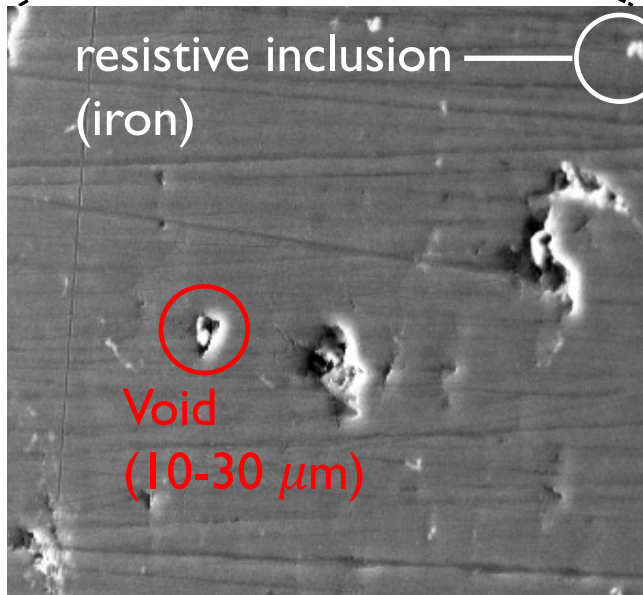
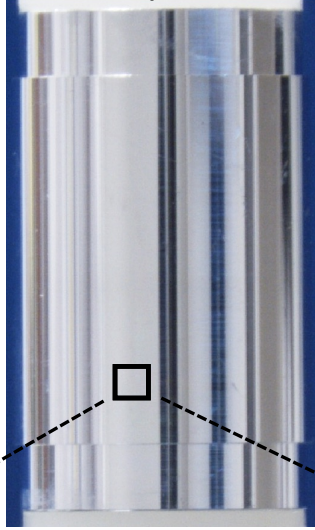
Plasma particles from MITL are helically oriented and bombard the liner, creating a helical temperature perturbation

A.B. Sefkow, Bull. Am. Phys. Soc. 61, 373 (2016)



Metallic liners are inhomogeneous

Be liner (50 nm rms)



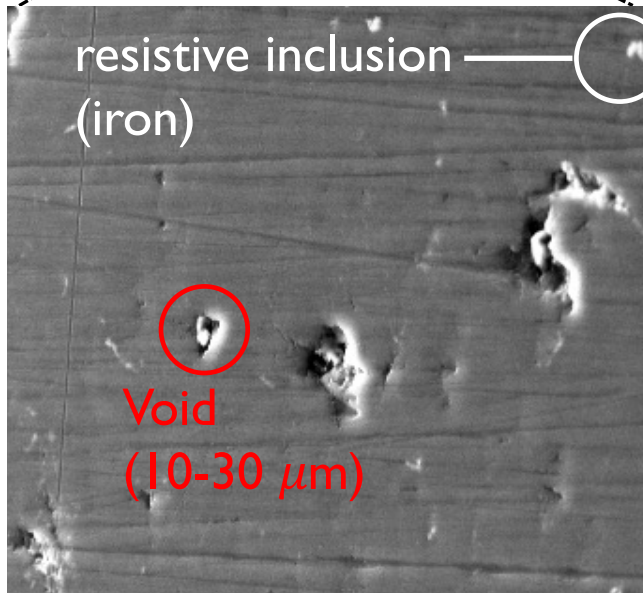
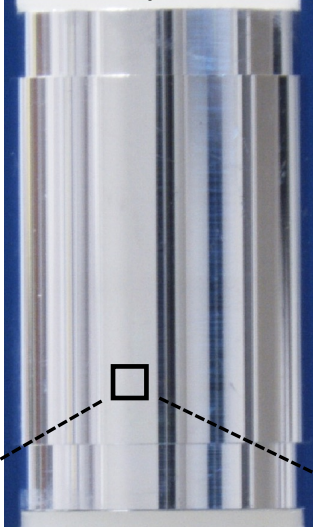
Characterization of Be rod surface
(E. Harding, K. Tomlinson)

Q: Do defects really matter?

3D defects constitute nonlinear perturbations to current density j



Be liner (50 nm rms)

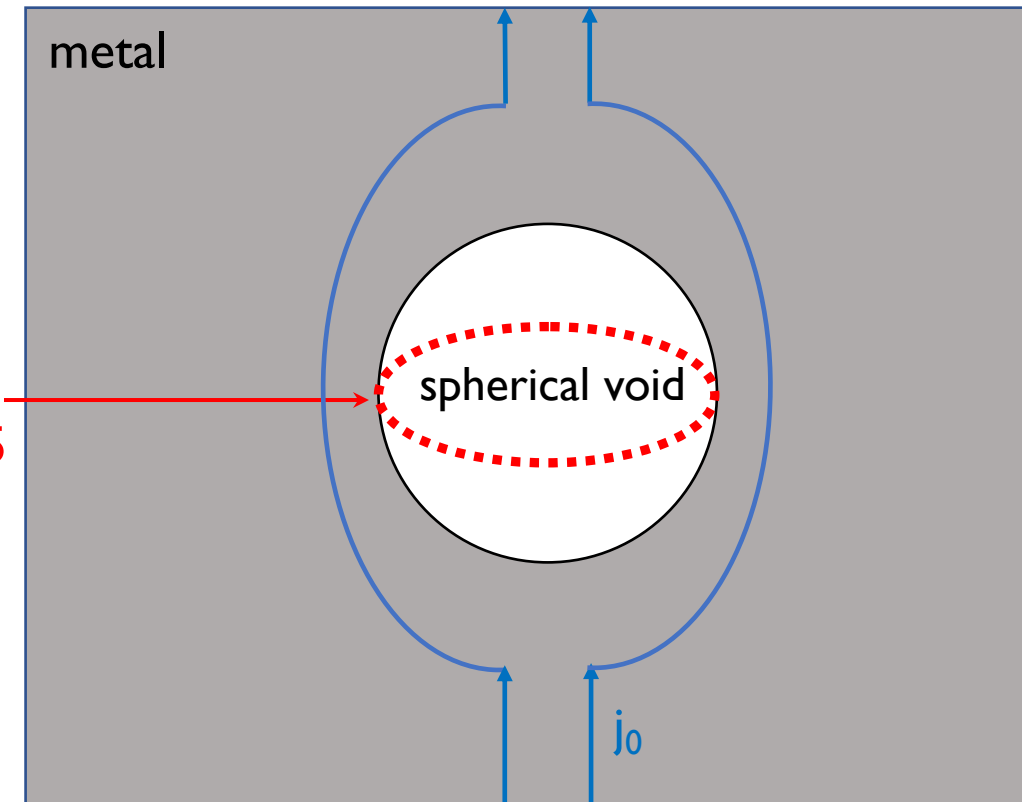


resistive inclusion
(iron)

Void
(10-30 μm)

Characterization of Be rod surface
(E. Harding, K. Tomlinson)

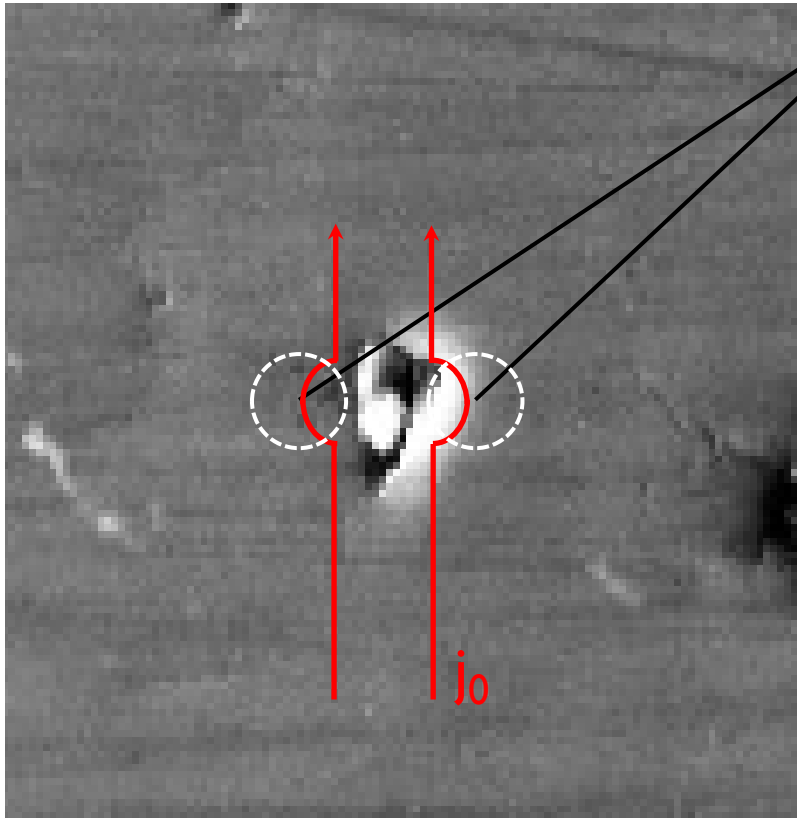
j amplification at
equator: $j_{\text{max}}/j_0=1.5$



- $\delta j = j_{\text{max}} - j_0$ depends on shape, not size

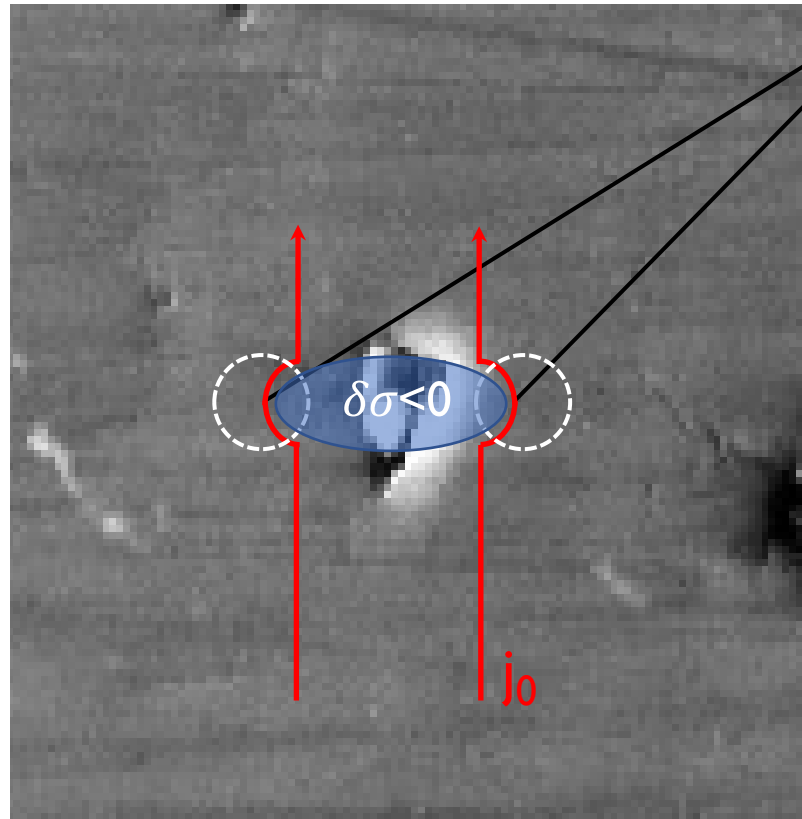
Hydrodynamic analogy with electrical current flow
E.P. Yu, T.J. Awe, K.R. Cochrane et al., Phys. Plasmas **27**, 052703 (2020)

Nonlinear δj initiates a feedback loop unique to current-driven metal



$$\delta j > 0 \Rightarrow \delta(j^2/\sigma) > 0 \Rightarrow \delta T > 0 \Rightarrow \delta\sigma < 0$$

Nonlinear δj initiates a feedback loop unique to current-driven metal

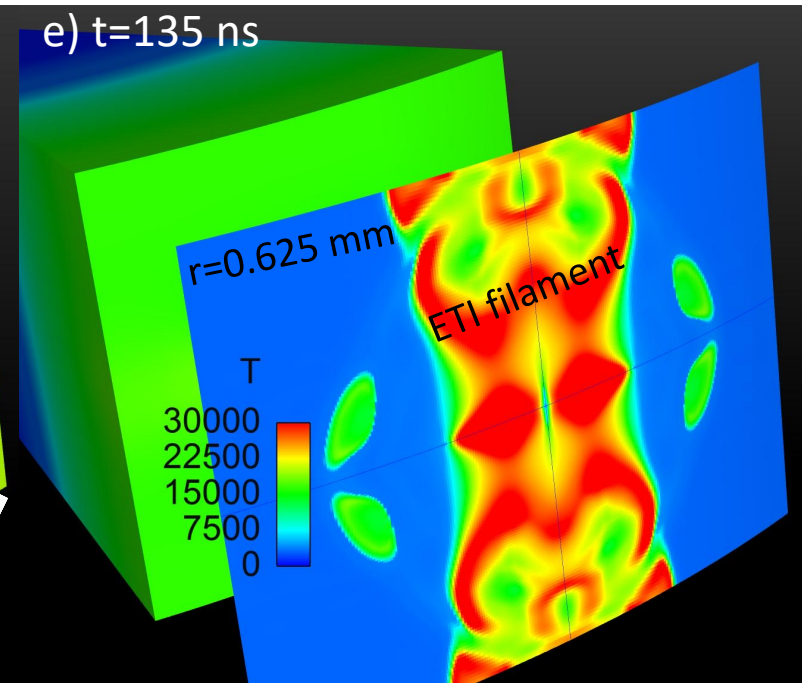
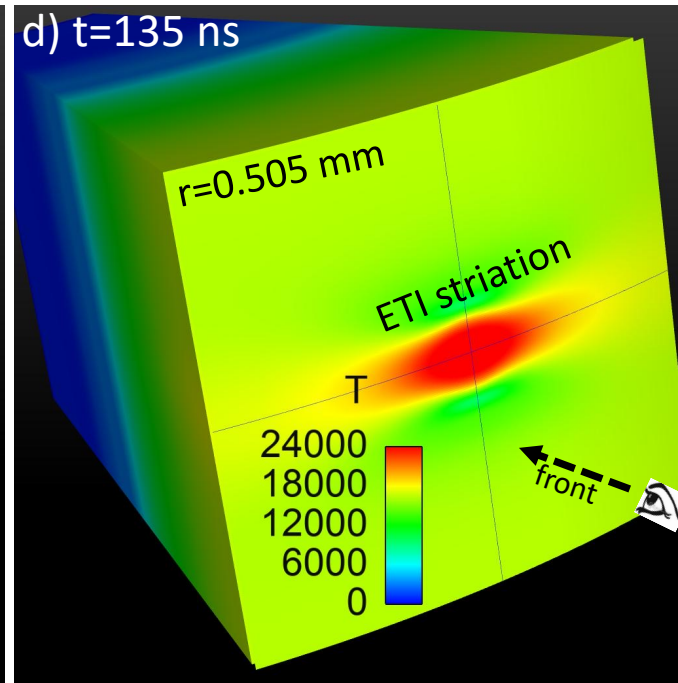
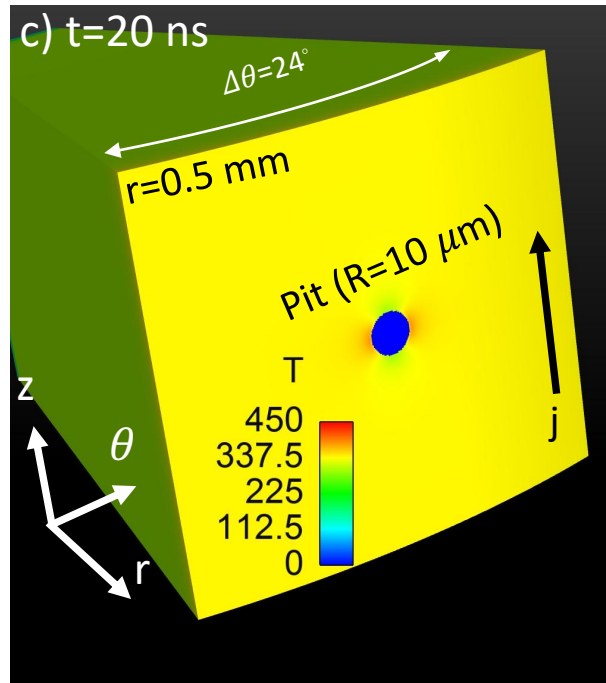
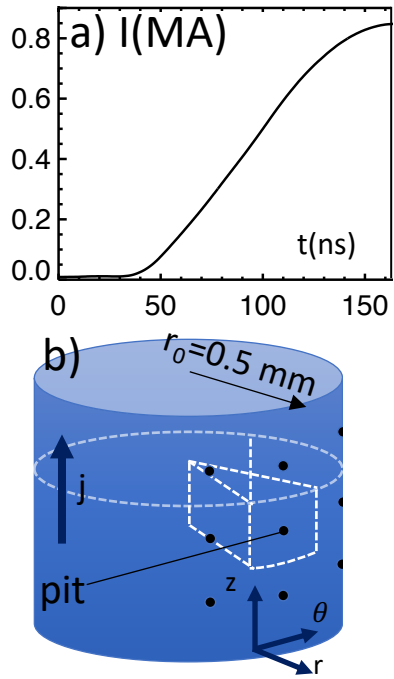


$$\delta j > 0 \Rightarrow \delta(j^2/\sigma) > 0 \Rightarrow \delta T > 0 \Rightarrow \delta\sigma < 0$$



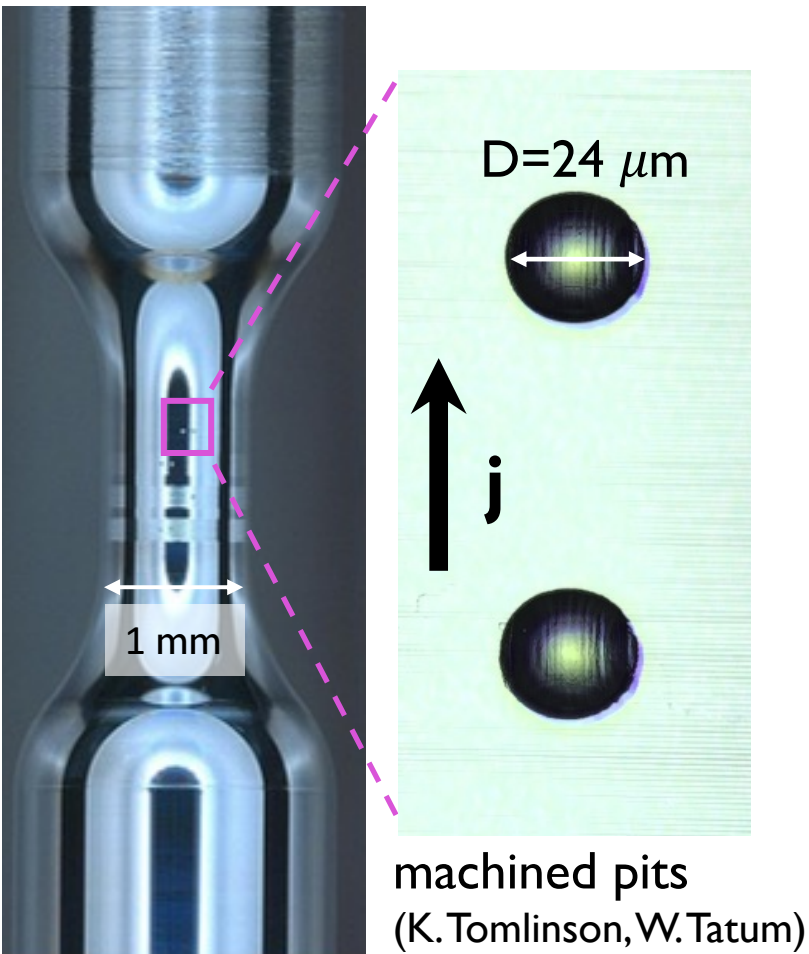
This feedback loop is studied in the electrothermal instability (ETI), which describes how small defects can grow into larger structures.

Simulations show 3D feedback loop transforms pit into larger structures: ETI striation and filament ($B_z=0$)

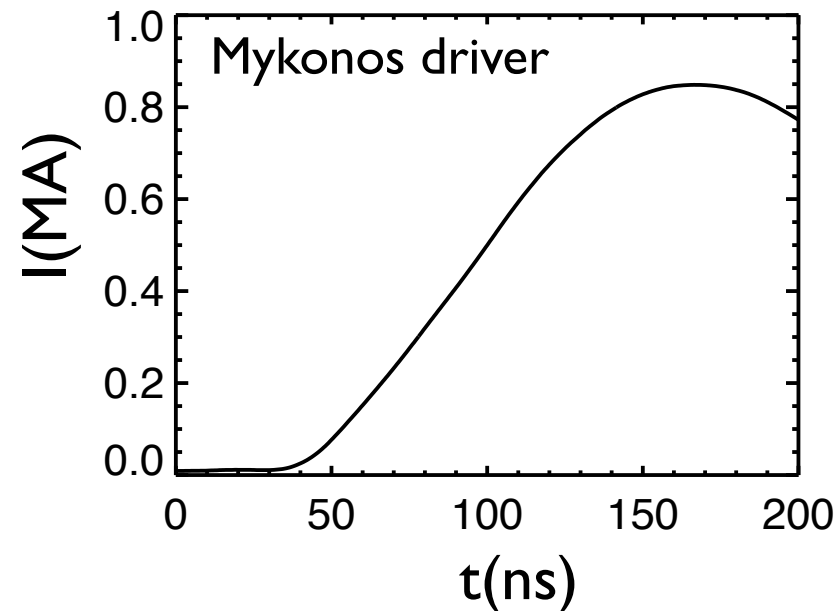


Periodic wedge simulation of aluminum rod + pit, driven by $\sim 1 \text{ MA}$ (Mykonos driver)

Ultraclean aluminum rods driven by ~1 MA current allow us to explore the feedback loop and test simulation predictions ($B_z=0$)



- Ultraclean metal provides a "clean" background (no native inclusions/voids)
- Machined pits play the role of voids.

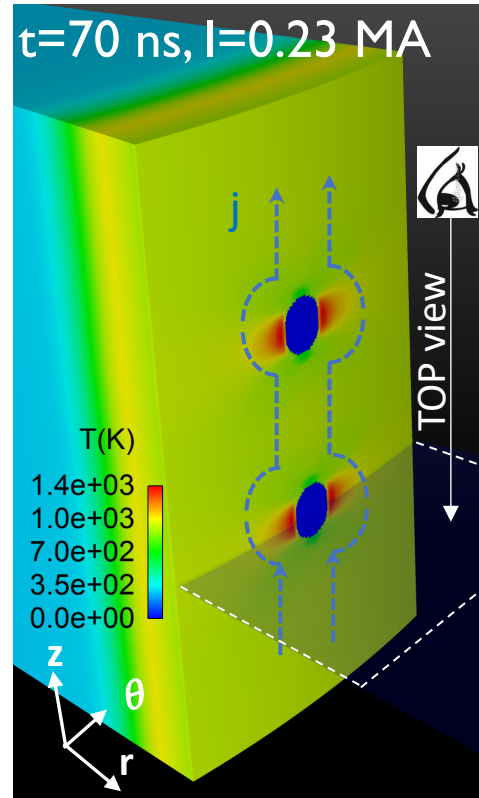
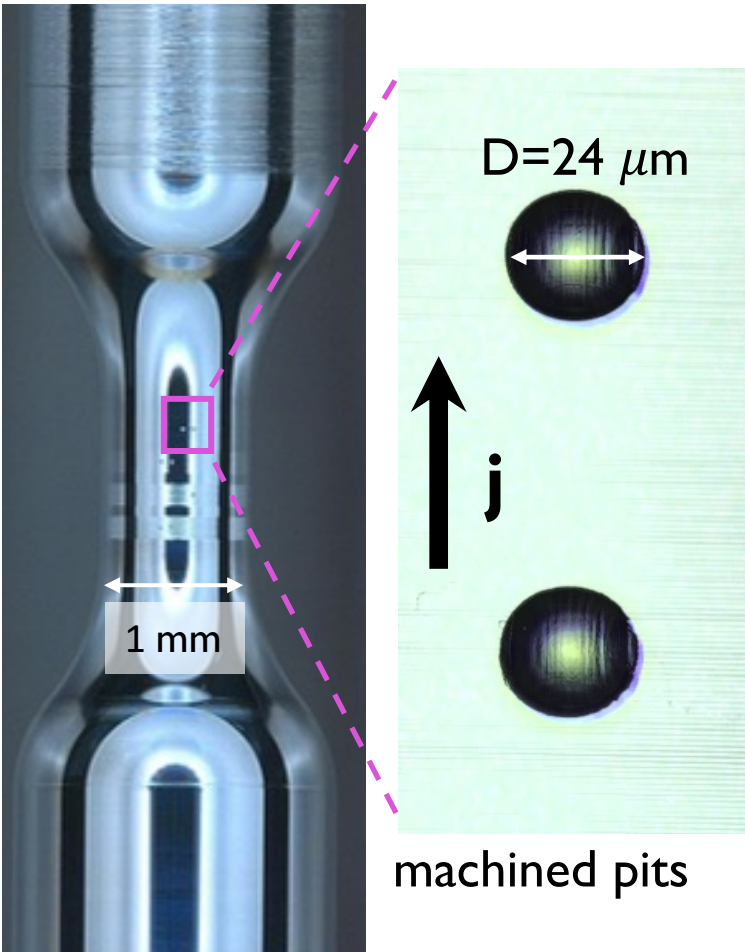


Al 5N rod (99.999% pure)

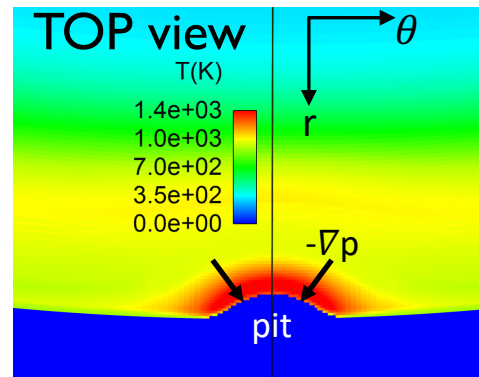
j redistribution causes overheating at the pit equator



3D MHD simulation



Periodic wedge simulation

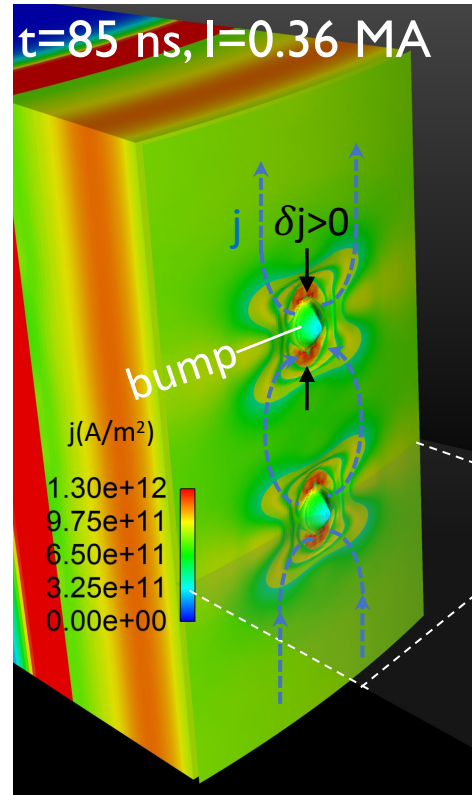
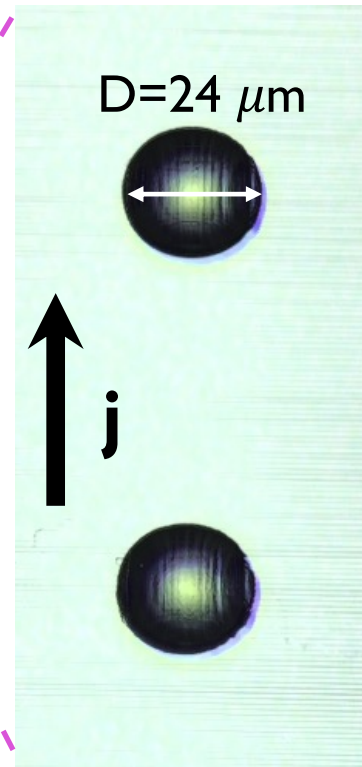
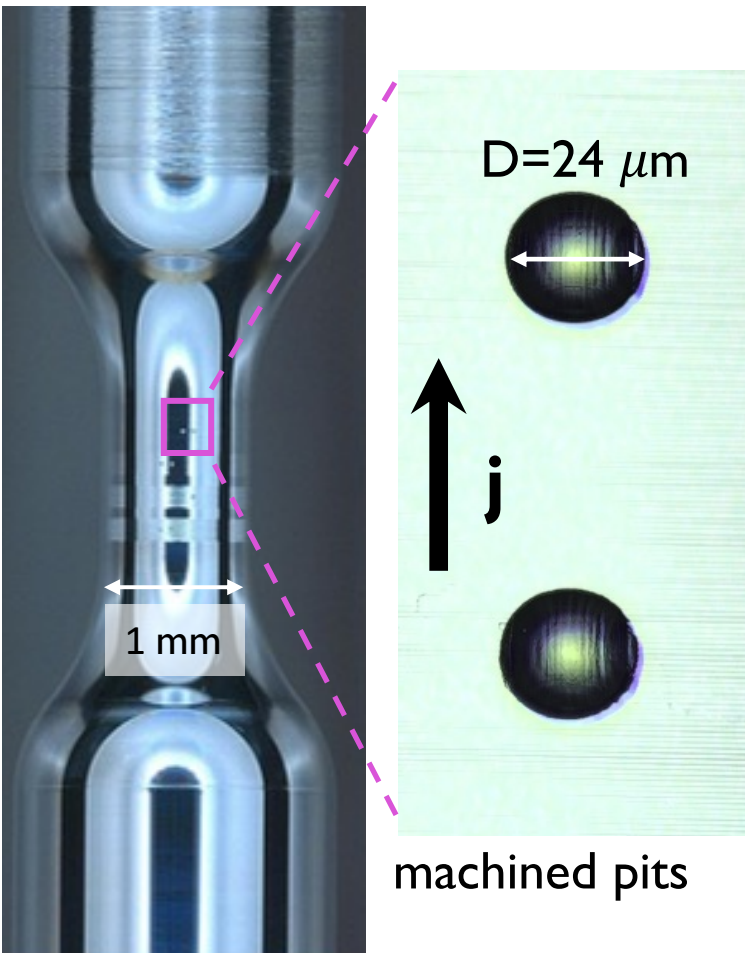


Expansion azimuthally focuses,
due to shaped charge effect

Pit expands and transforms into a bump

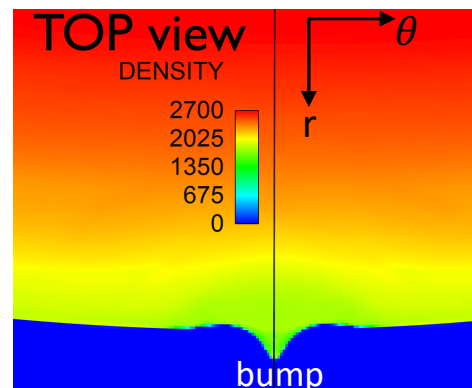


3D MHD simulation

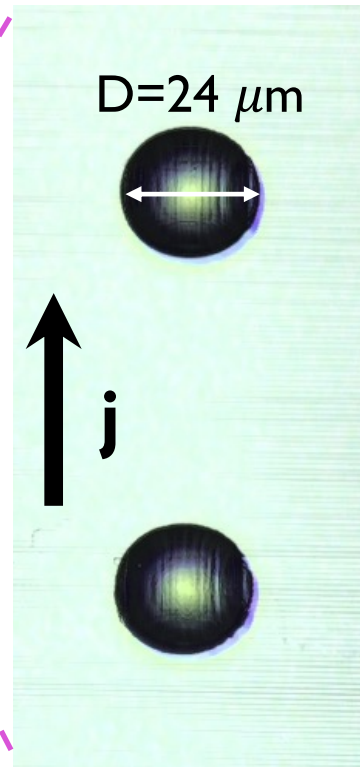
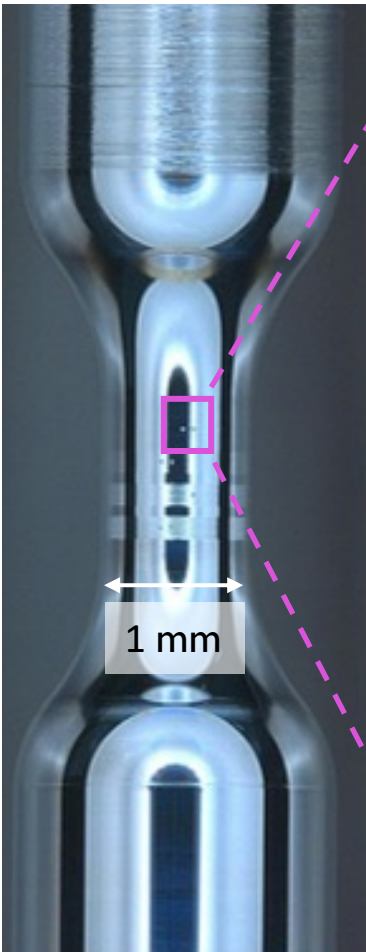


j changes qualitatively from flow around pit to flow over a bump.

j focuses at the top and bottom of the bump, creating hot spots there.

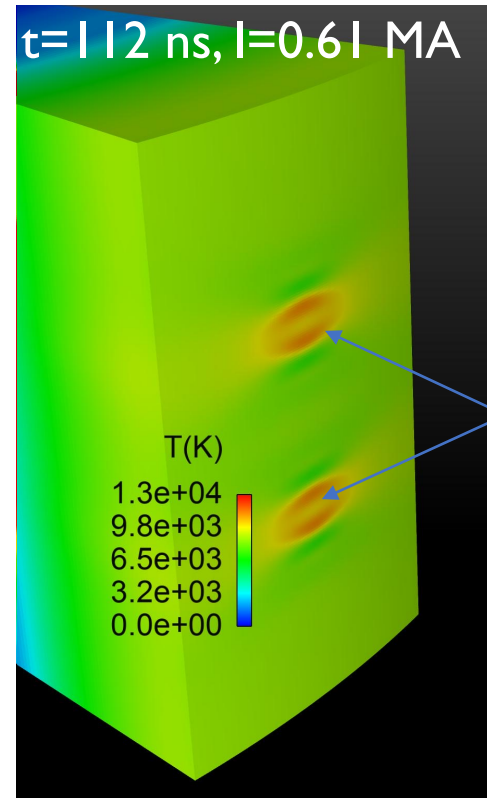


Simulations predict distinctive, testable patterns



machined pits

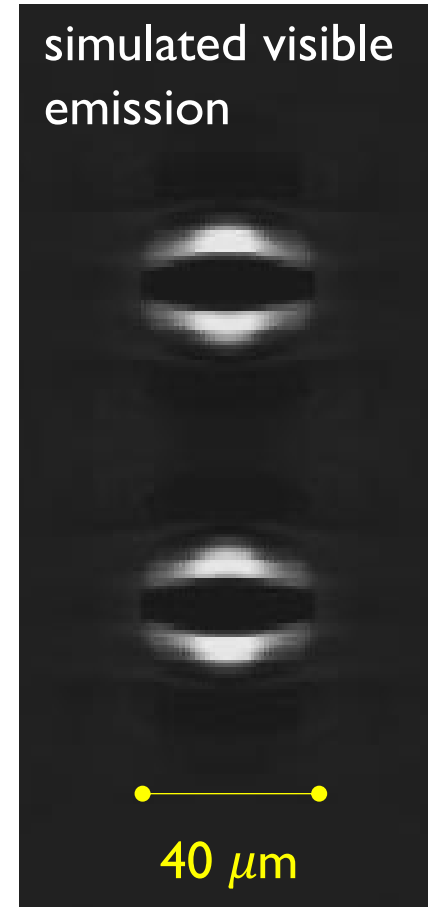
3D MHD simulation



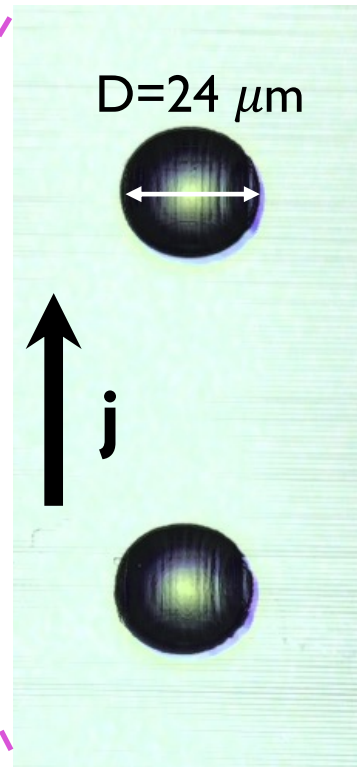
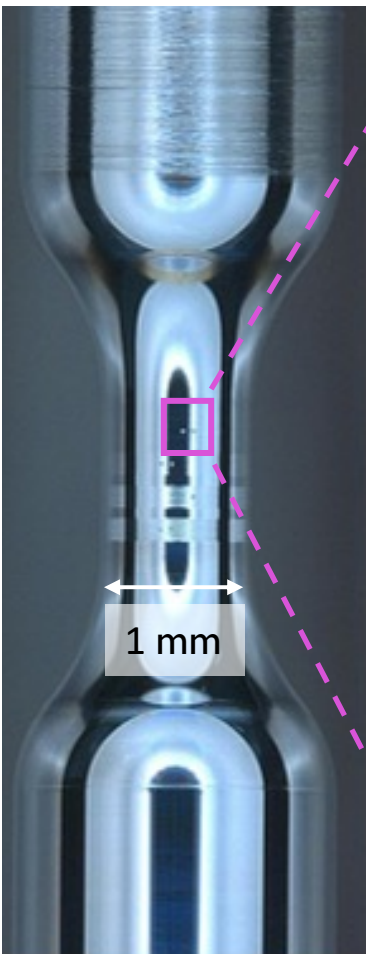
Hot spots

SPECT3D

simulated visible emission

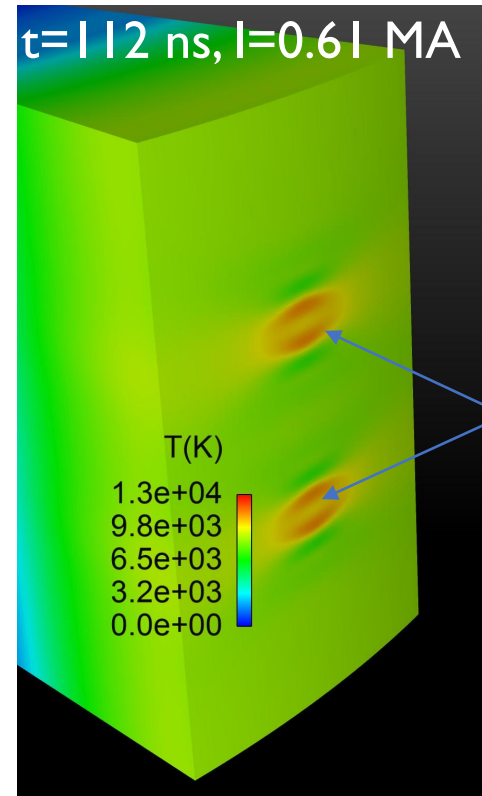


Experimental validation provides confidence in simulation



machined pits

3D MHD simulation



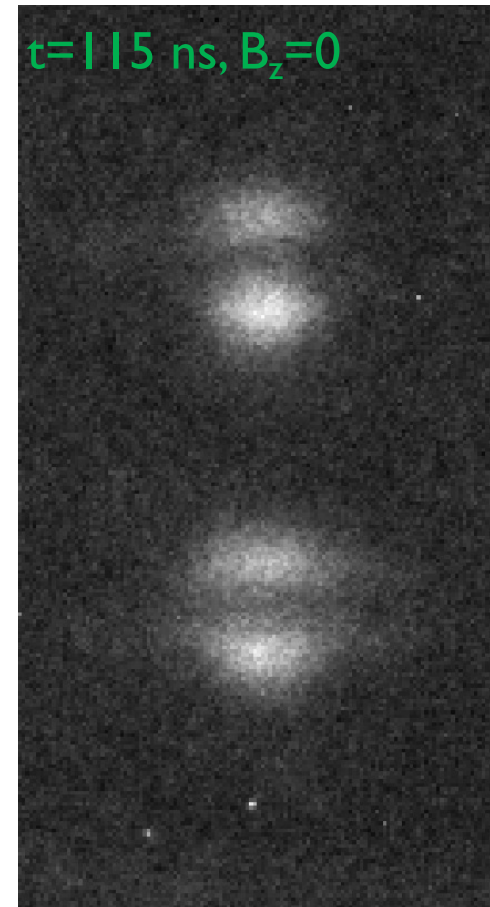
Hot spots

SPECT3D

simulated visible emission



Experiment

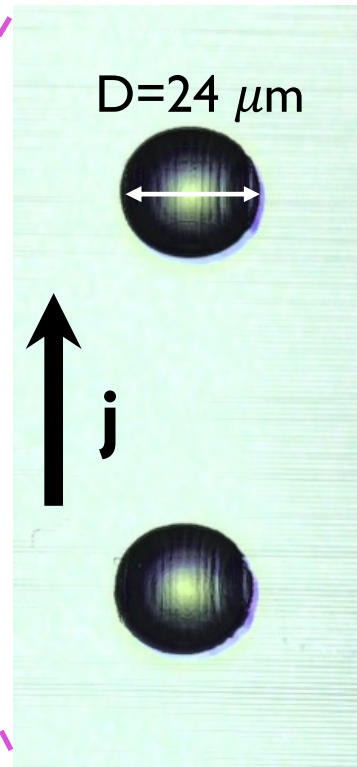
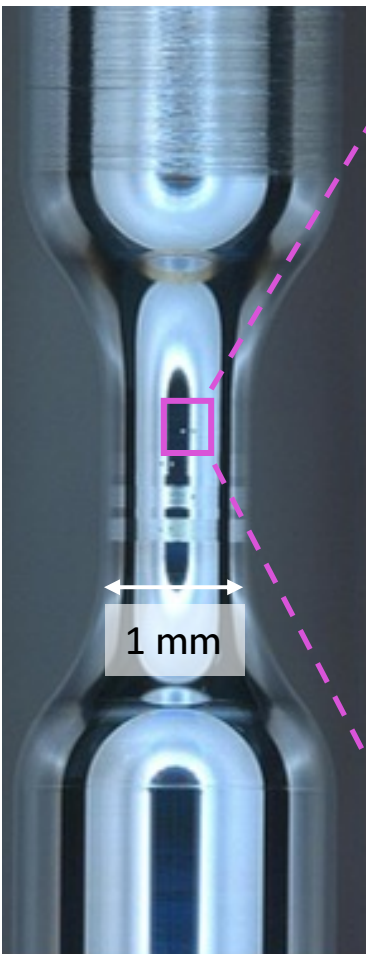


T.J. Awe, E. P. Yu, M.W. Hatch, T. M. Hutchinson, K. Tomlinson, W.D. Tatum, K.C. Yates, B.T. Hutsel, and B.S. Bauer, *Phys. Plasmas* **28**, 072104 (2021)

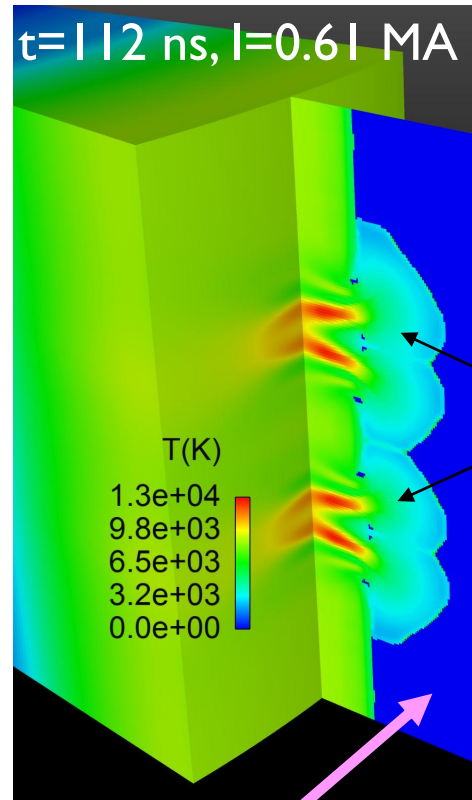
Hot spots explode, creating plumes and craters




3D MHD simulation



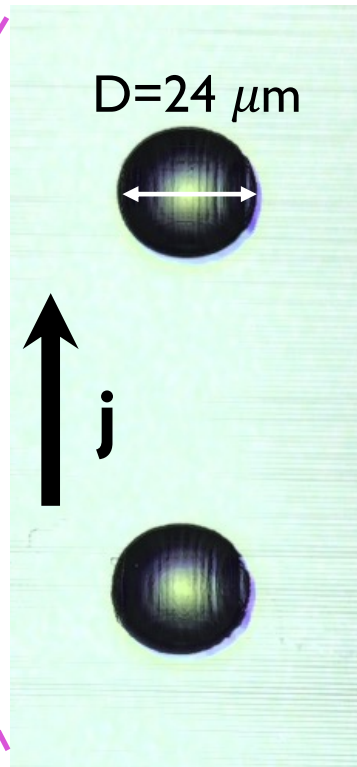
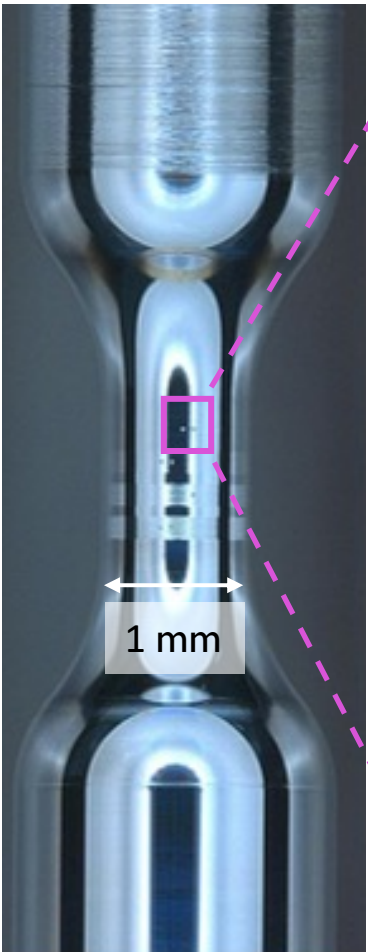
machined pits



Plumes

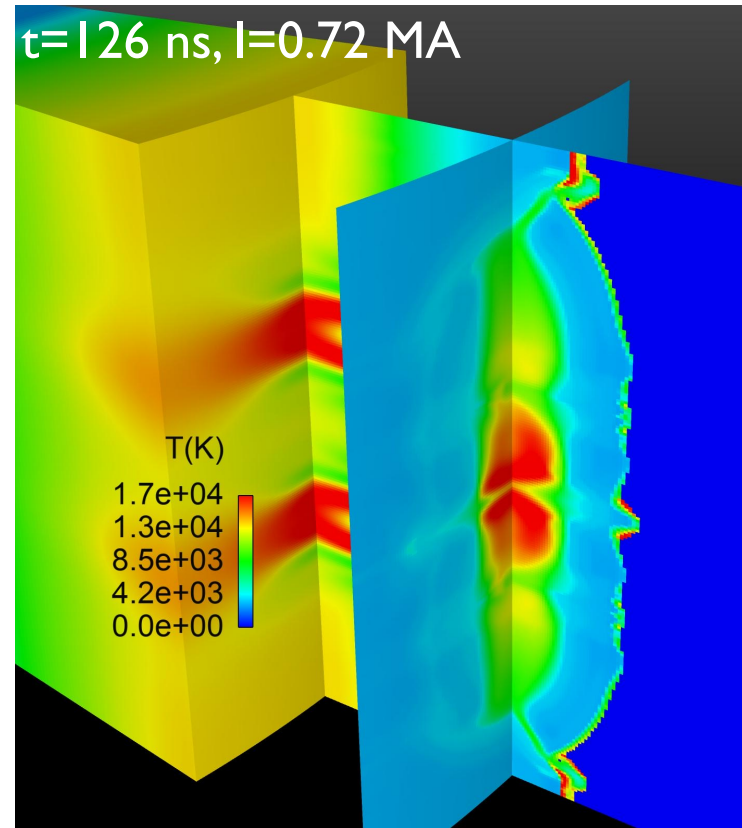
 Cross-sectional view

Pits seed the ETI filament



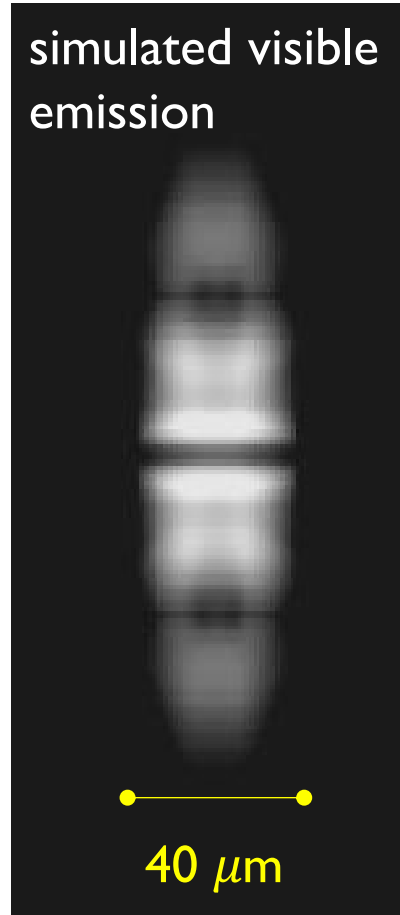
machined pits

3D MHD simulation

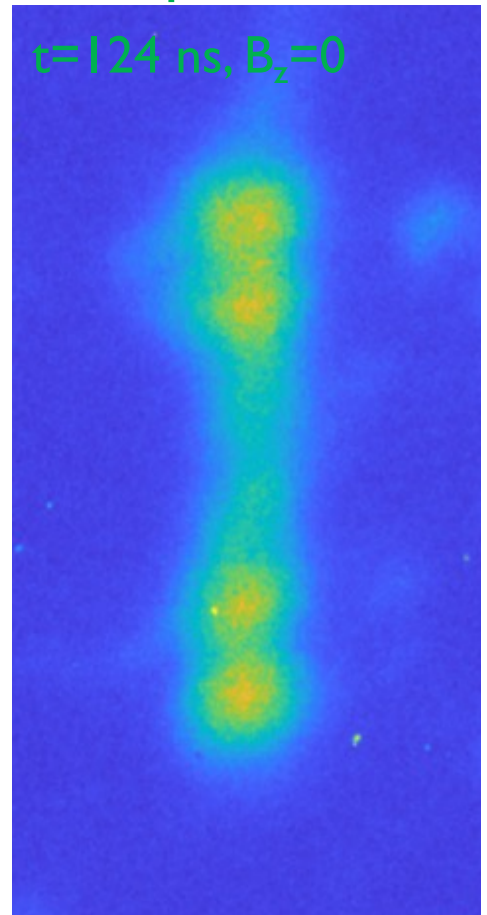


SPECT3D

simulated visible emission

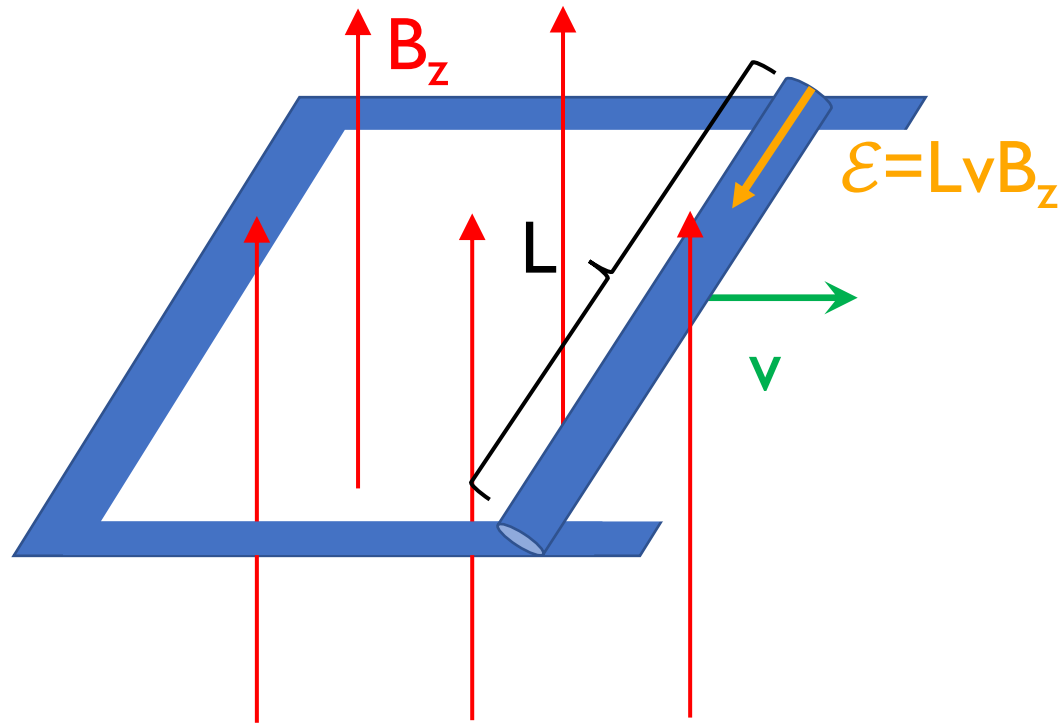


Experiment



Q: how does this picture change when $B_z > 0$?

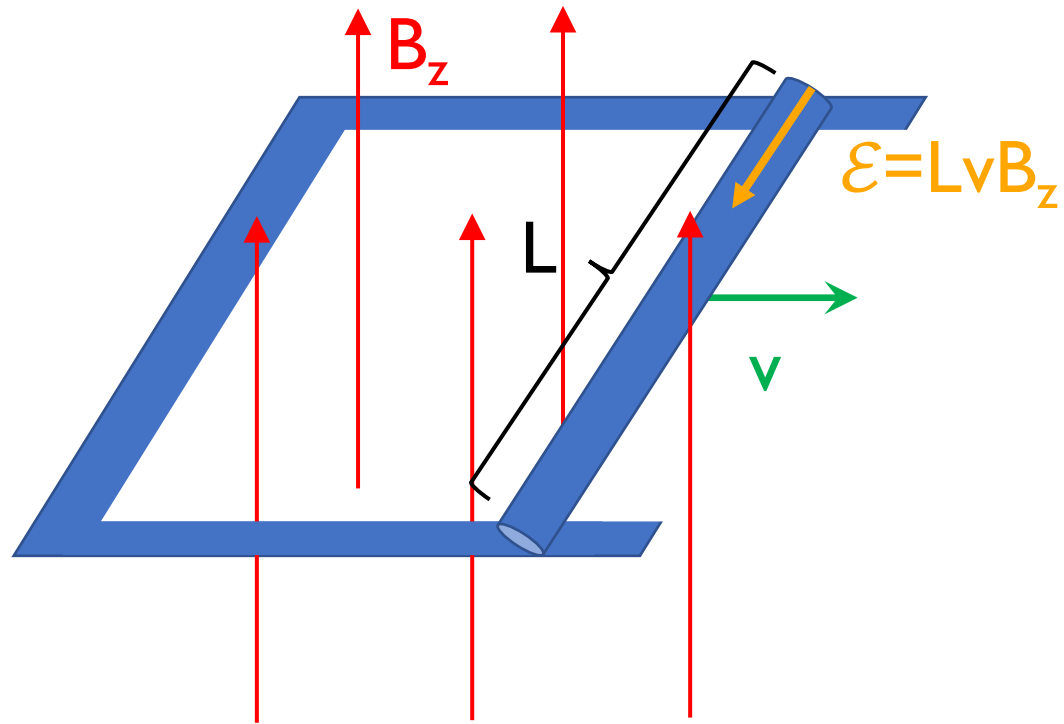
Motional EMF term in Ohm's law drives helical asymmetry in ETI



$$\text{MHD: } \mathbf{j} = \sigma(\mathbf{E} + \underbrace{\mathbf{v} \times \mathbf{B}}_{\text{Motional EMF}})$$

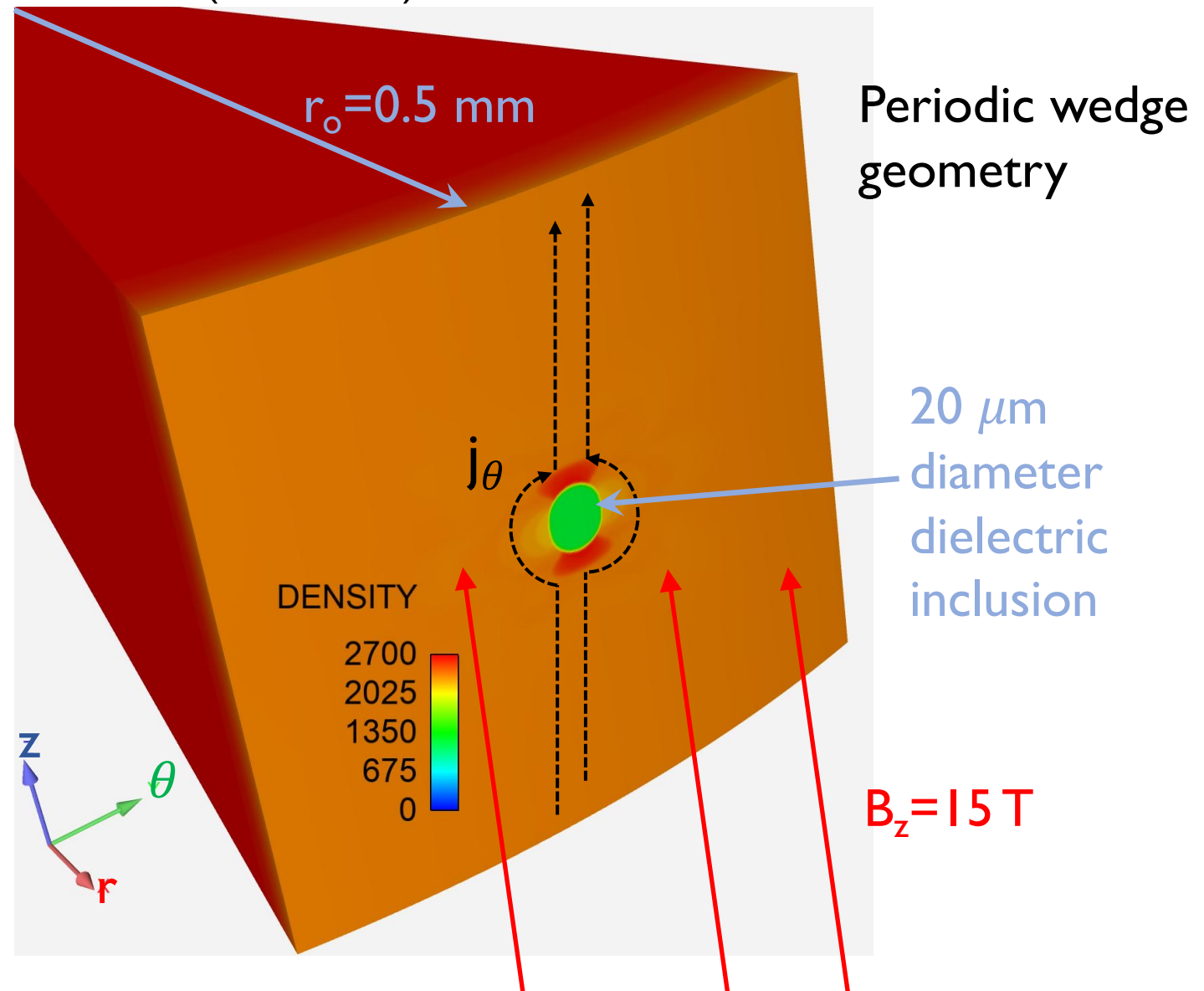
Motional EMF

3D simulation of aluminum rod with resistive inclusion, $B_z=15\text{ T}$

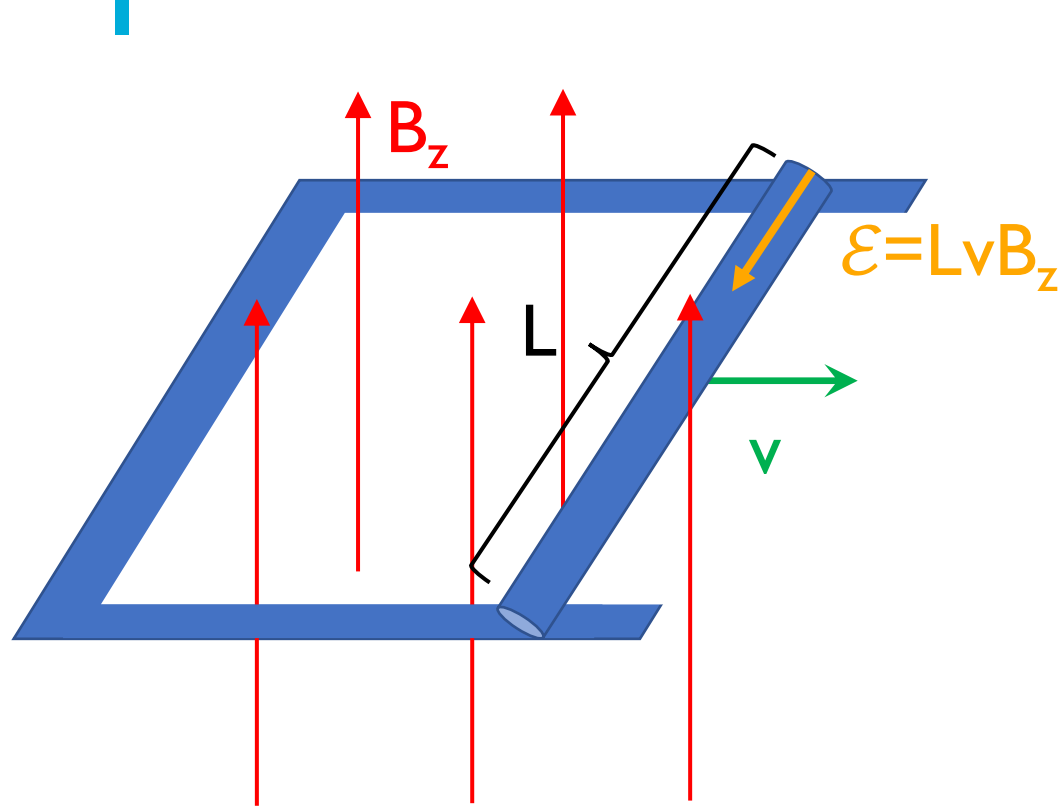


$$\text{MHD: } \mathbf{j} = \sigma(\mathbf{E} + \underbrace{\mathbf{v} \times \mathbf{B}}_{\text{Motional EMF}})$$

$t=70\text{ ns}$ (0.23 MA)

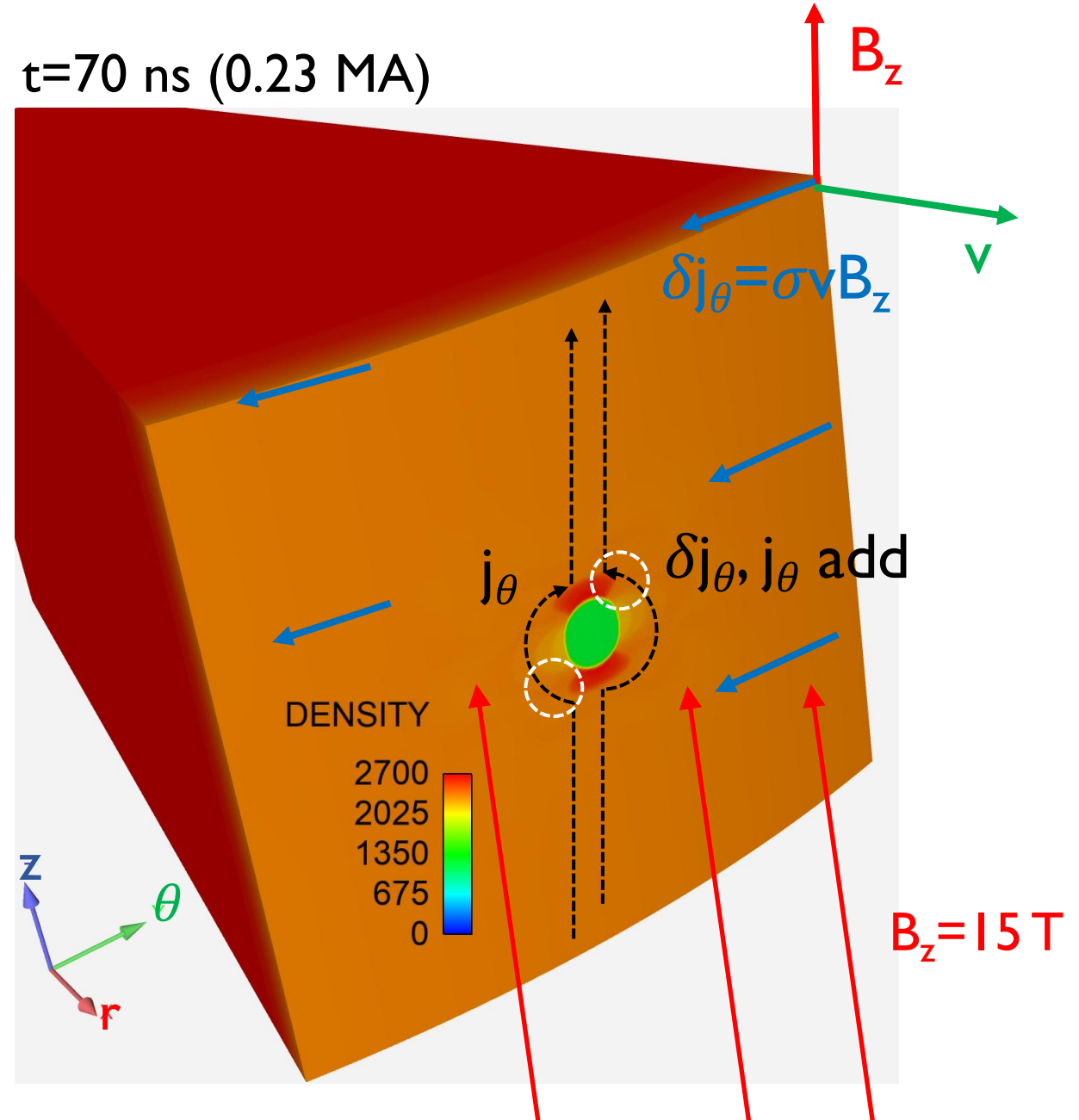


Induced δj introduces asymmetry at NE/SW corners



$$\text{MHD: } j = \sigma(E + \underbrace{v \times B}_{\text{Motional EMF}})$$

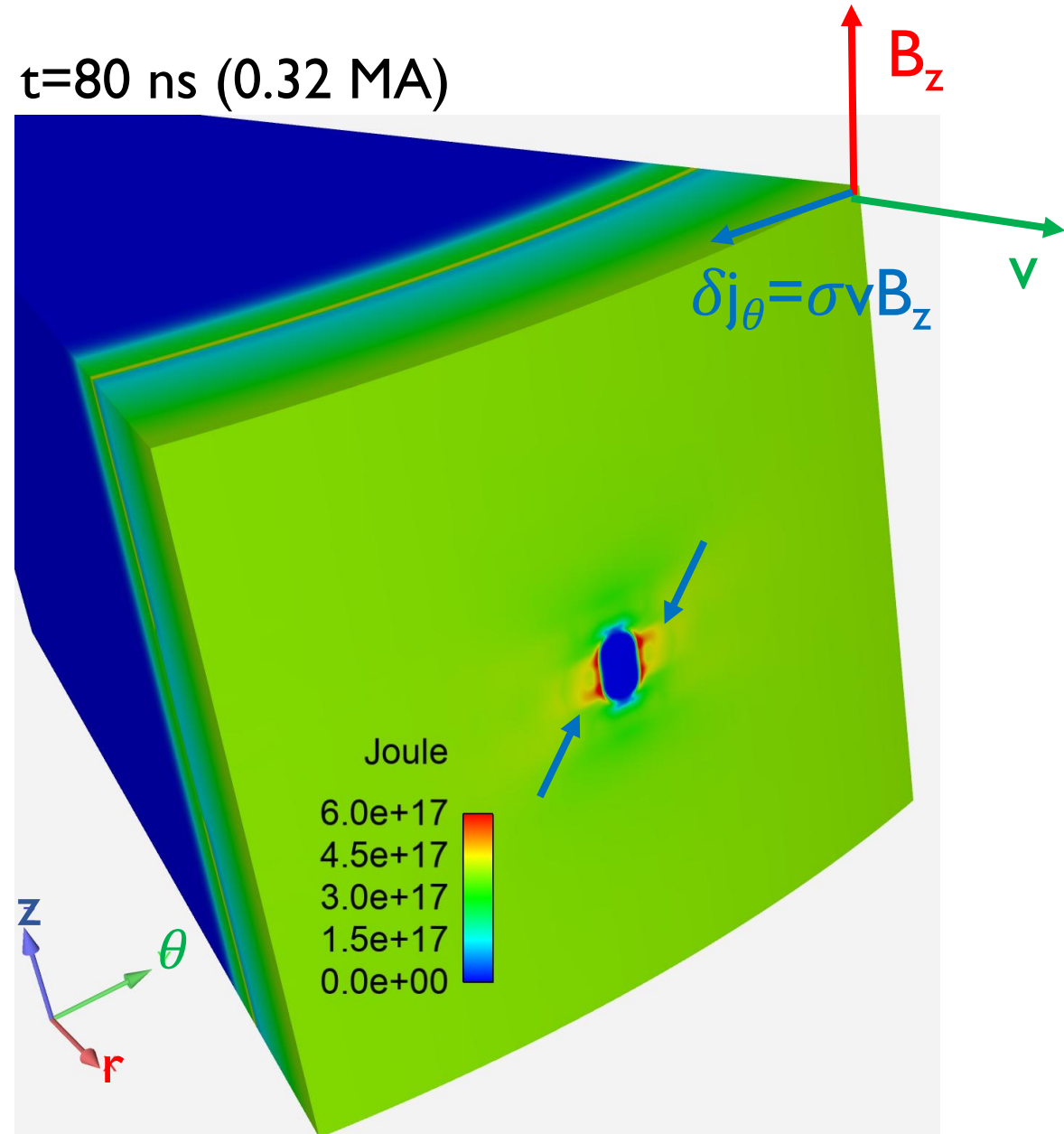
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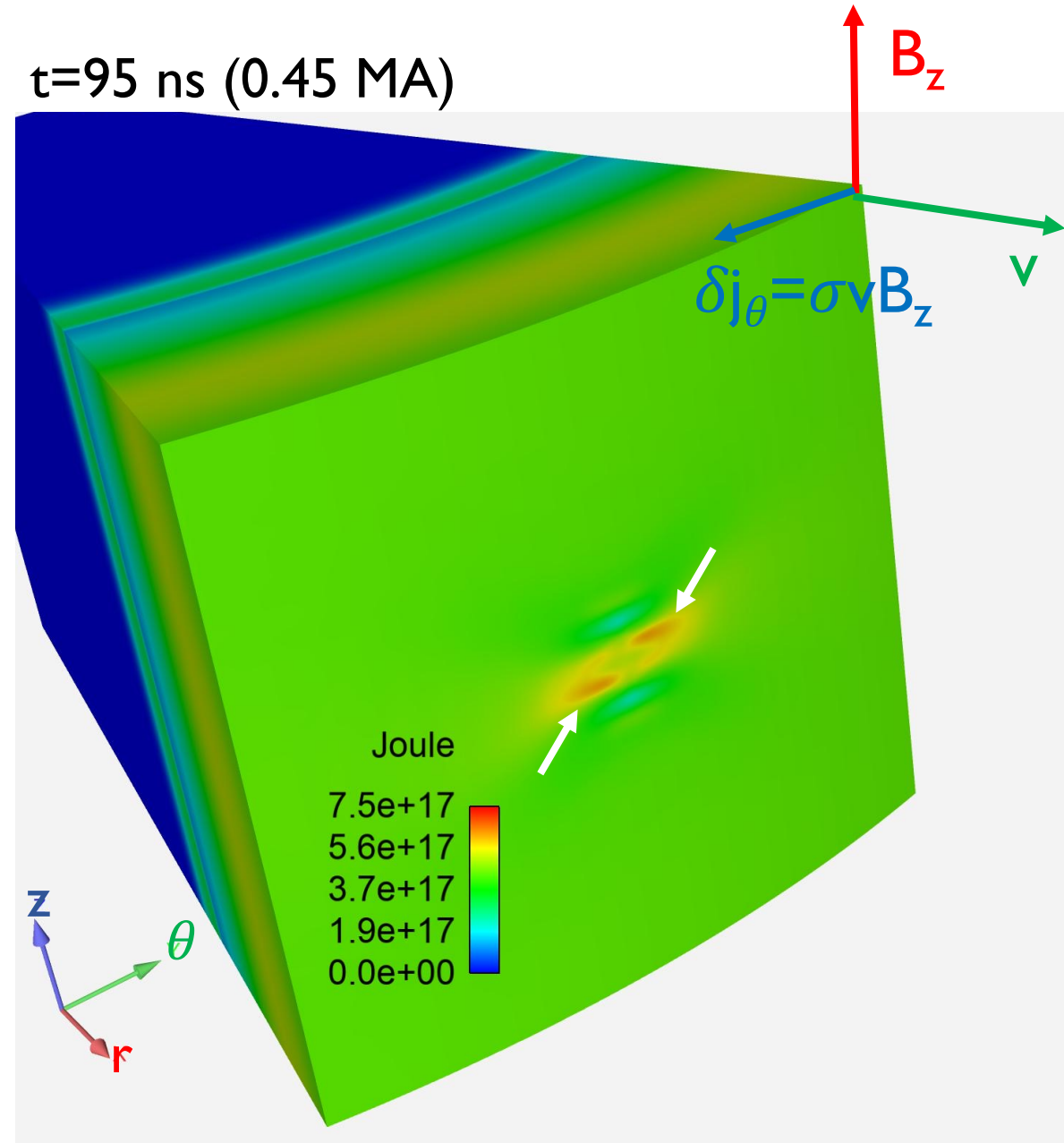


$\delta j_{\theta}/j_{\theta}$ is small ($\sim 10\%$) but results in asymmetry



Asymmetry at NE/SW corners amplifies with time

$t=95 \text{ ns}$ (0.45 MA)



Angle of helical perturbation does not agree with $\mathbf{k} \cdot \mathbf{B} = 0$ condition

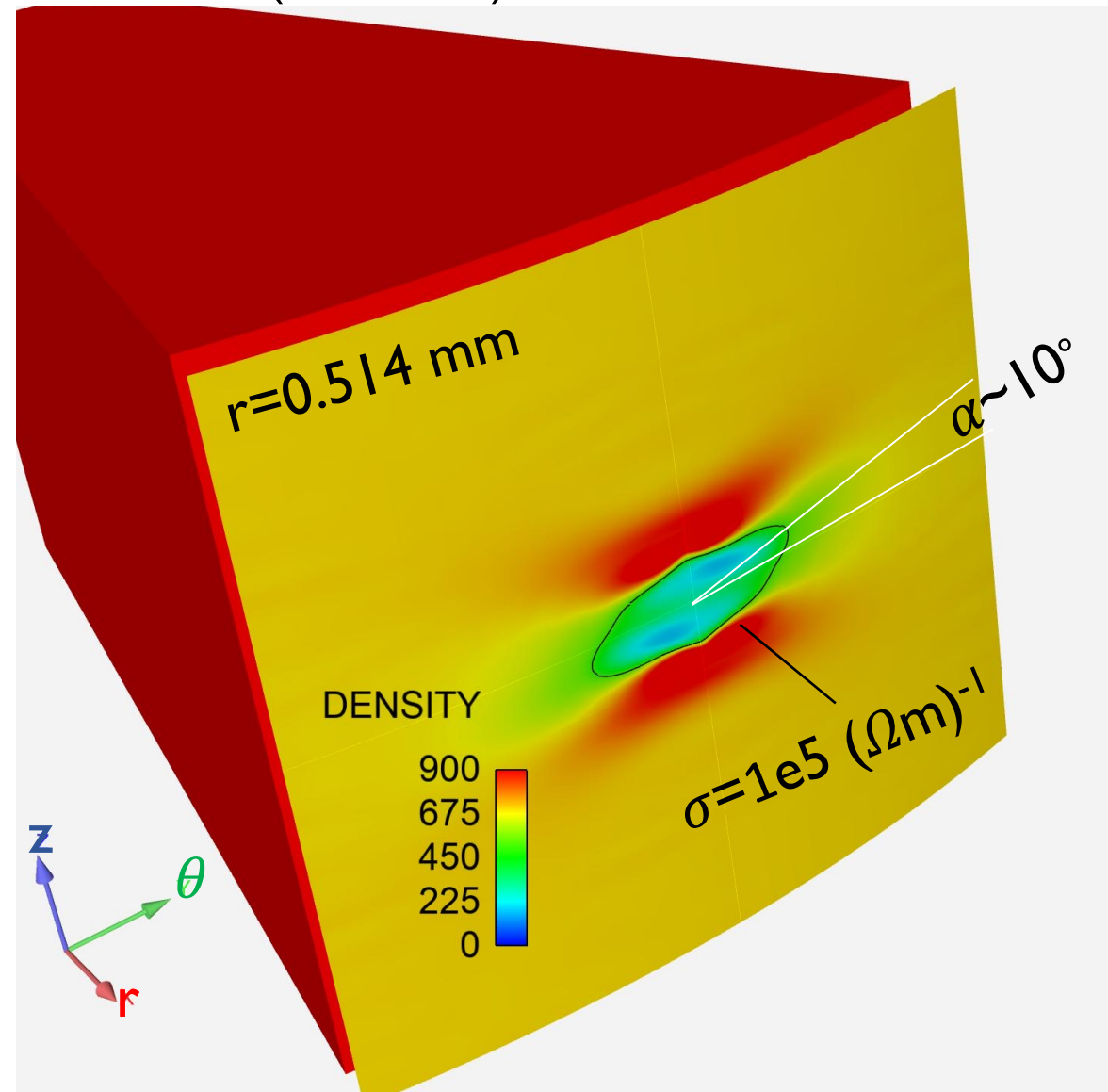


Asymmetric Joule heating results in asymmetric density perturbation with $\alpha \sim 10^\circ$.

This angle is determined by the interaction between δj_θ and j_θ , rather than the condition $\mathbf{k} \cdot \mathbf{B} = 0$.

$\mathbf{k} \cdot \mathbf{B} = 0$ predicts a pitch angle $\arctan(B_z/B_\theta) = 3.5^\circ$

$t = 115 \text{ ns (0.63 MA)}$



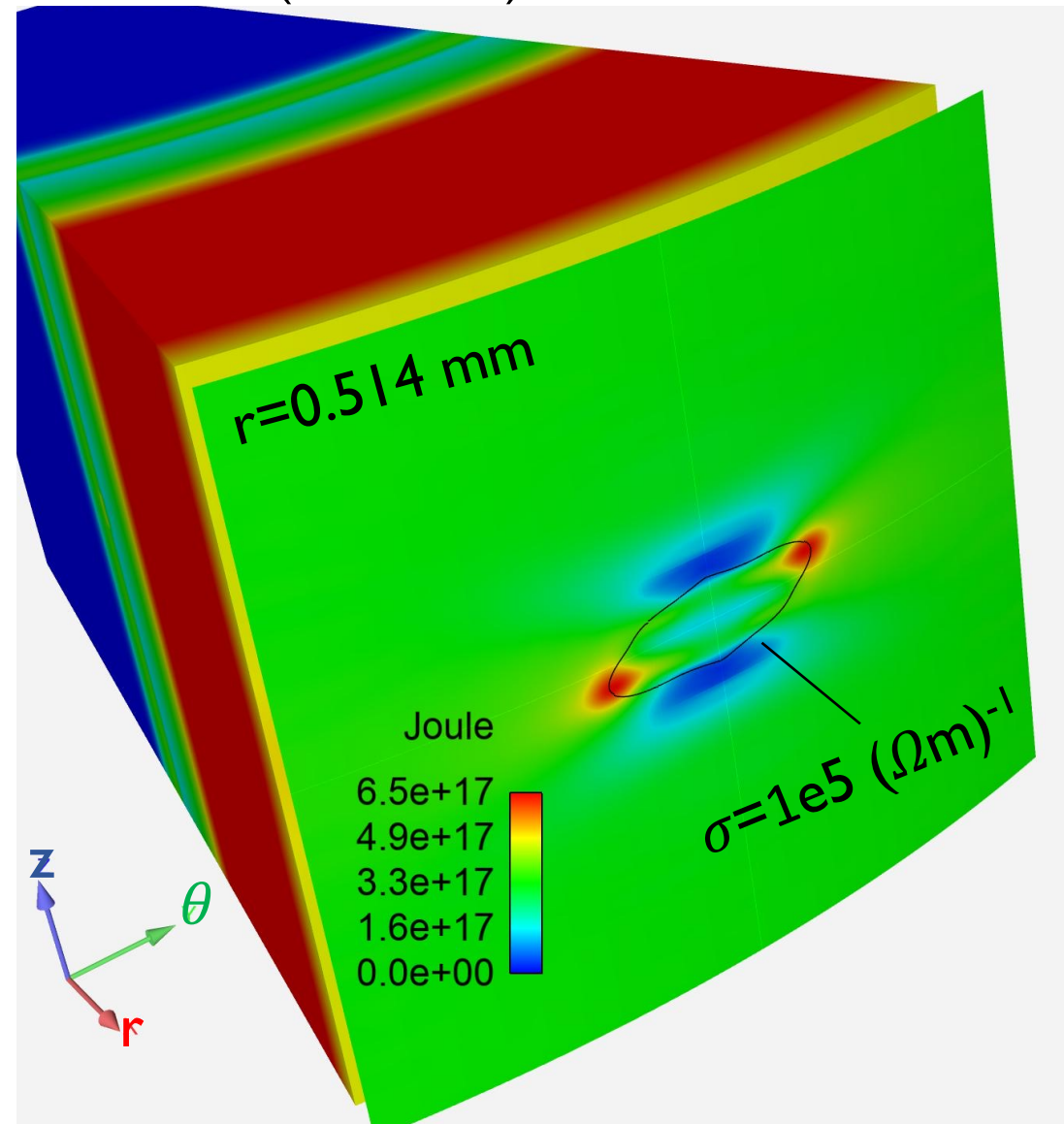
Asymmetric Joule heating will grow density perturbation helically



This mechanism provides a means for helically-oriented striations to form.

However, physics in an aluminum rod driven by 1 MA will be different from beryllium liner driven by 20 MA.

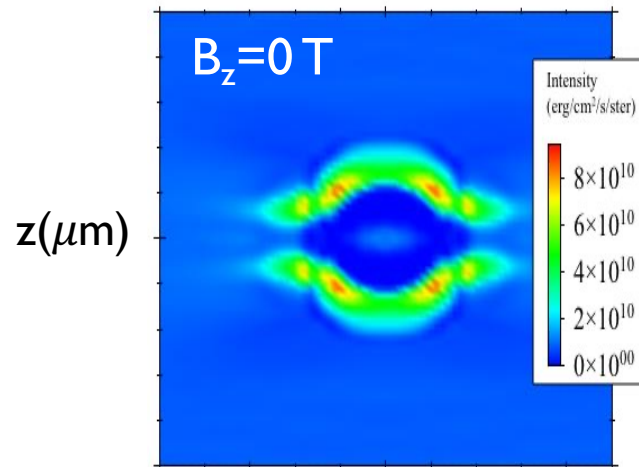
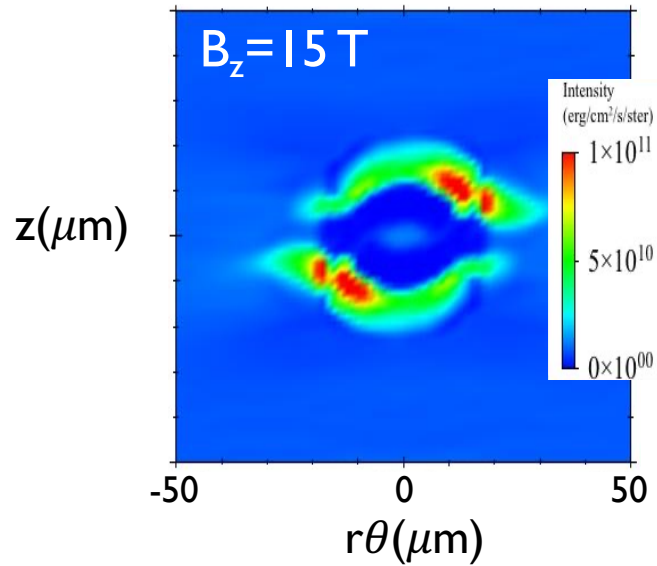
$t = 115 \text{ ns}$ (0.63 MA)



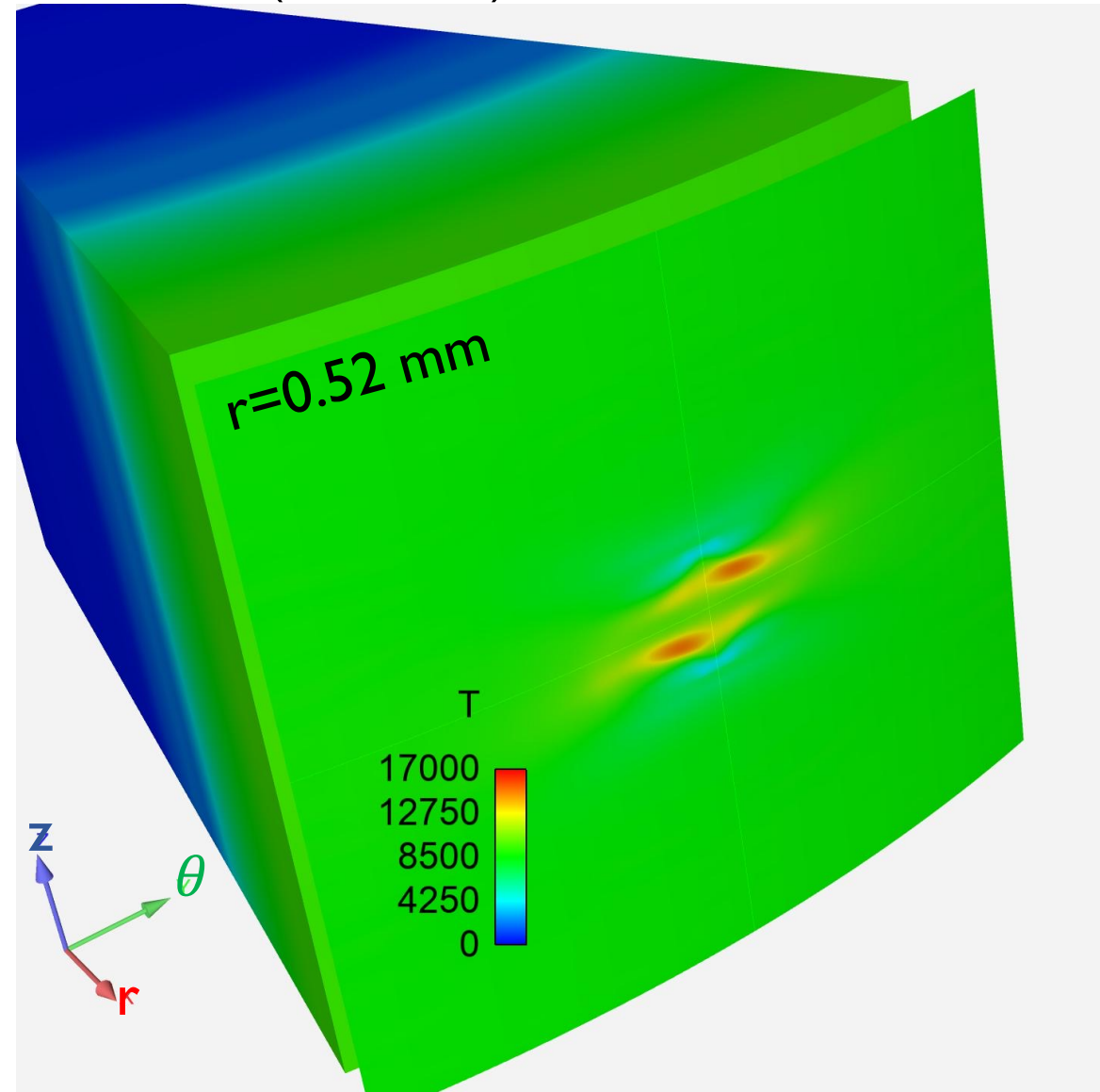
Asymmetric heating due to B_z should be experimentally verifiable



simulated visible emission
(SPECT3D)



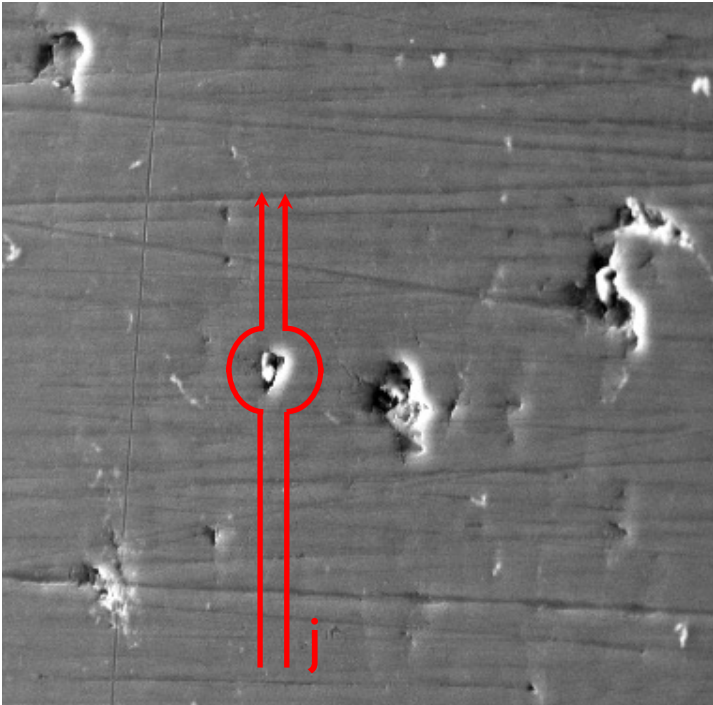
$t = 115 \text{ ns}$ (0.63 MA)



Summary

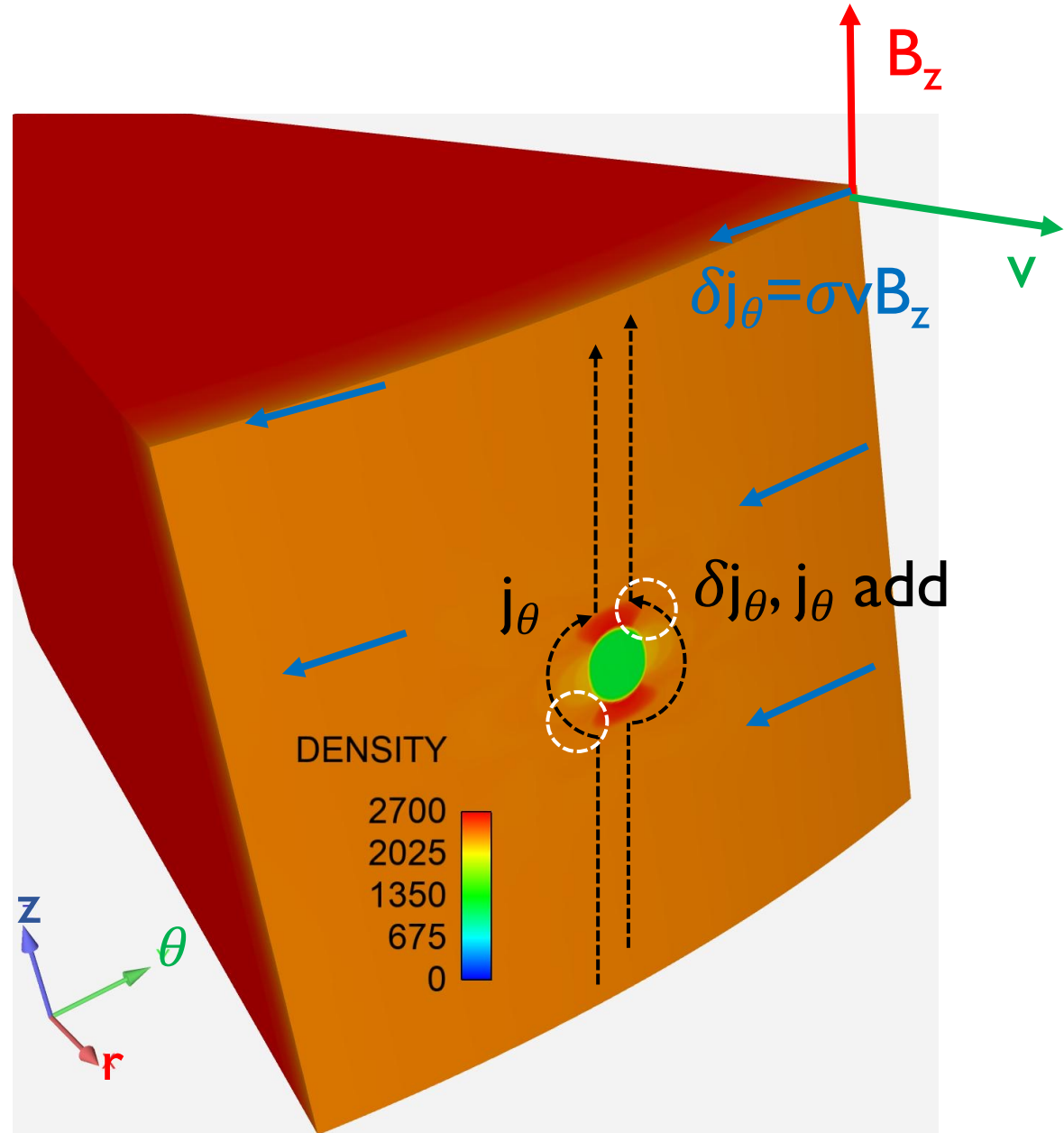


- Metals are full of defects which seed a feedback loop connecting j and σ (ETI)



Summary

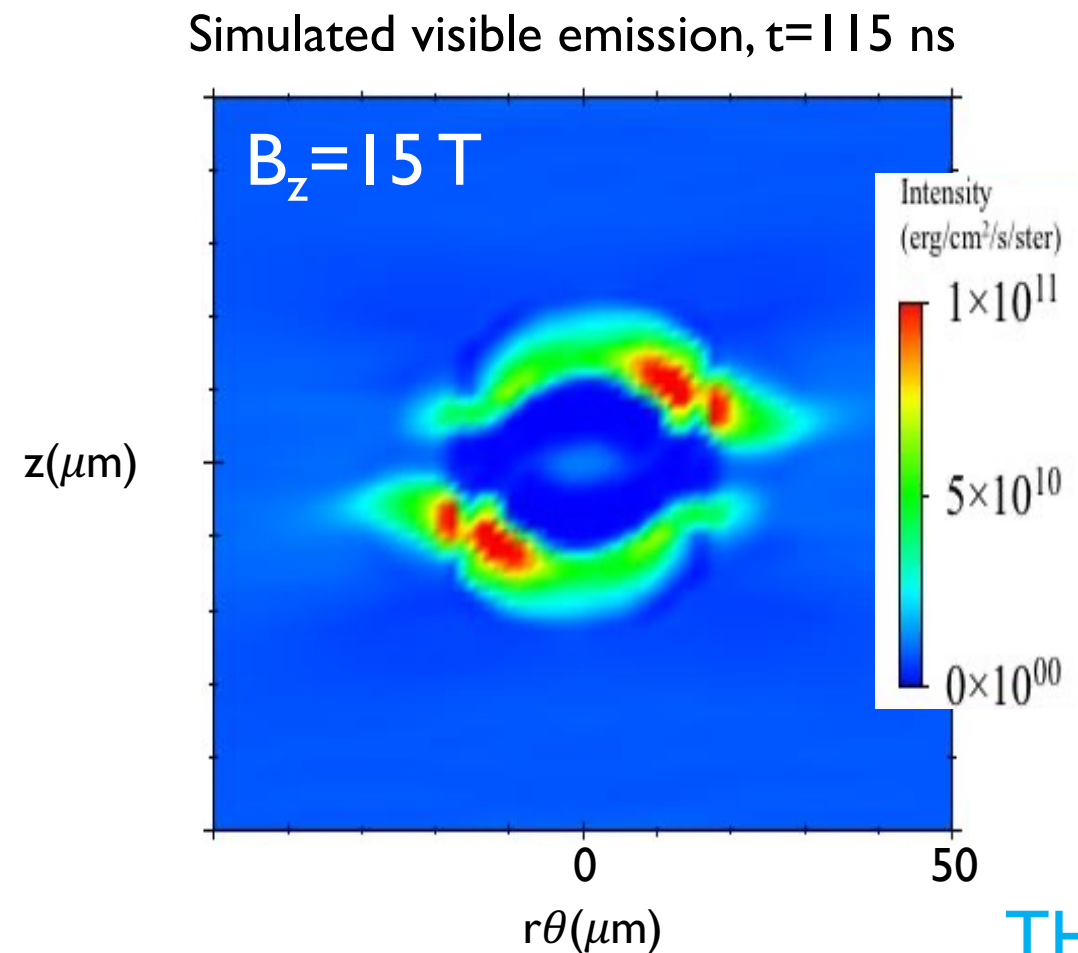
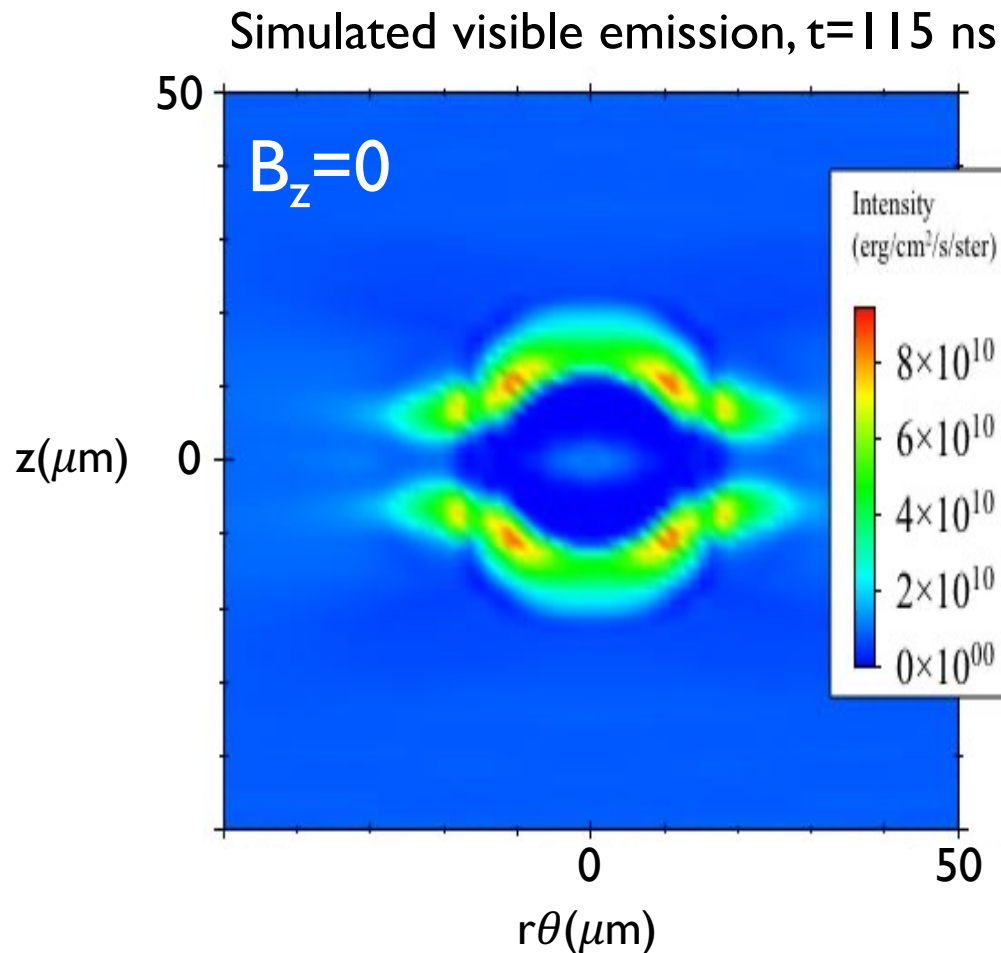
- B_z creates small perturbations in \mathbf{j} around the defect, driven by $\delta\mathbf{j}=\sigma(\mathbf{v}\times\mathbf{B})$, which will amplify due to ETI



Summary



- Simulations predict B_z creates an asymmetric emission pattern. We plan to experimentally verify this prediction on the Mykonos driver.



THANKS!

Backup: $\delta \mathbf{j}$ introduces asymmetry at NE/SW corners

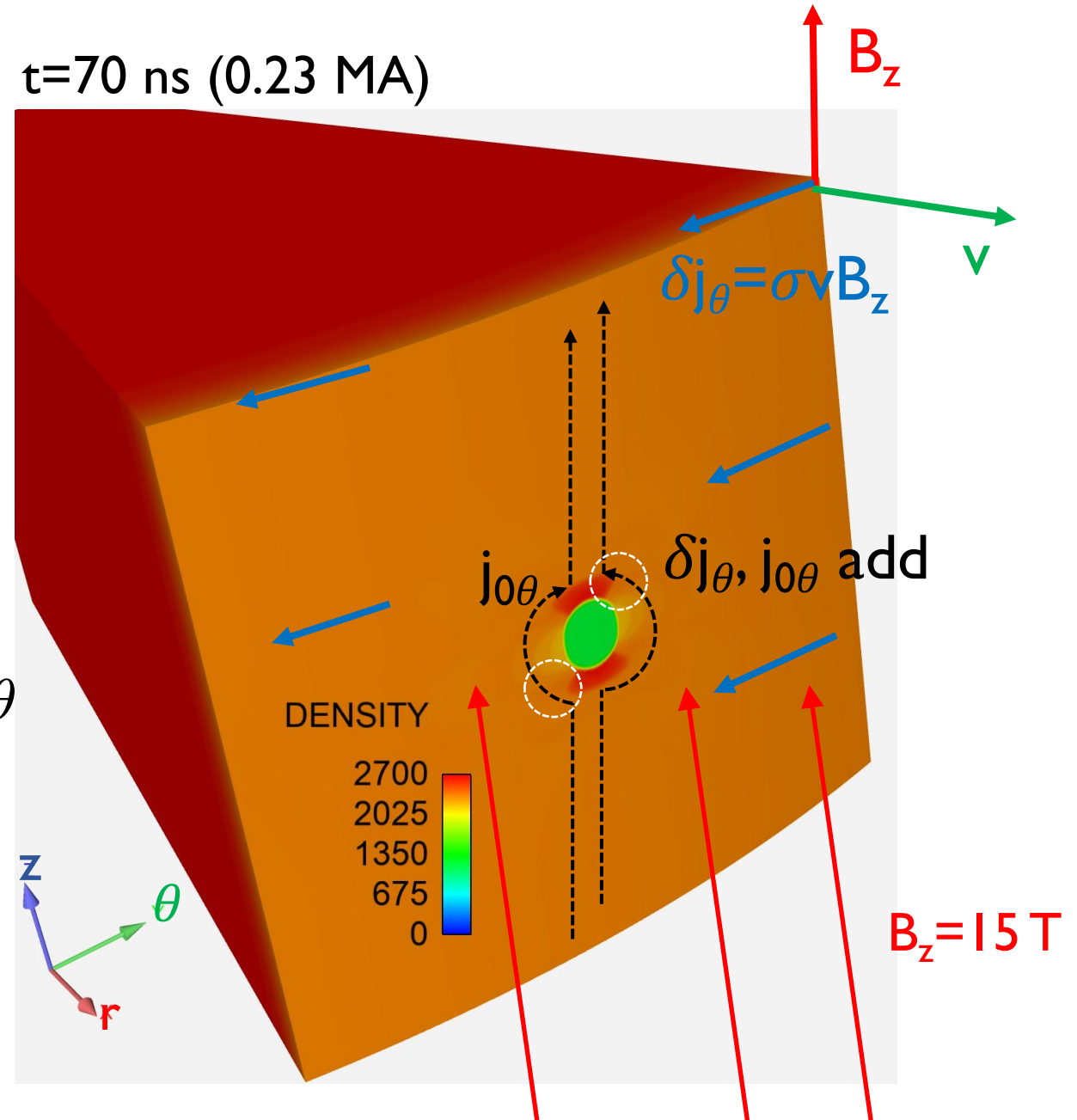


$$\mathbf{j} = \underbrace{\mathbf{j}_0}_{\mathbf{j} \text{ when } B_z=0} + \delta \mathbf{j}$$

$$j^2 = j_0^2 + 2\mathbf{j}_0 \cdot \delta \mathbf{j} + \delta j^2$$

$$j^2 - j_0^2 \simeq 2\mathbf{j}_0 \cdot \delta \mathbf{j} = 2j_{0\theta} \delta j_\theta$$

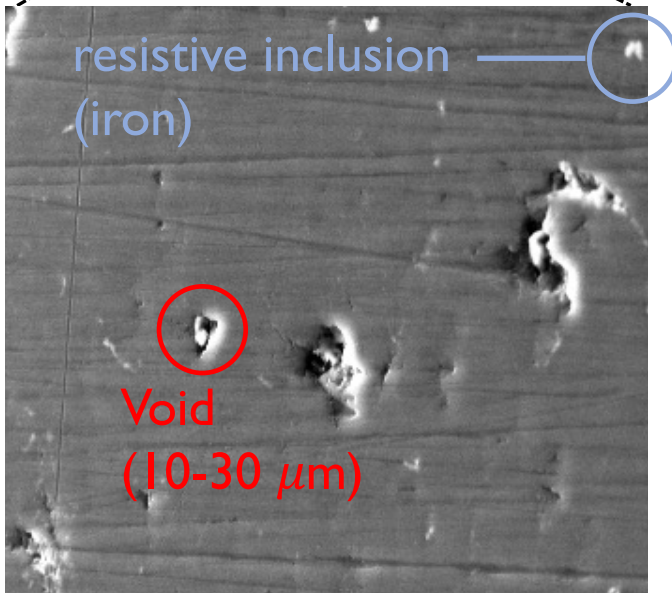
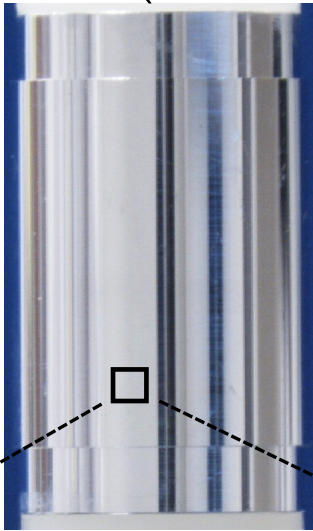
Maximum perturbation in j^2 is where $j_{0\theta}$ is largest i.e., NE/SW corners.



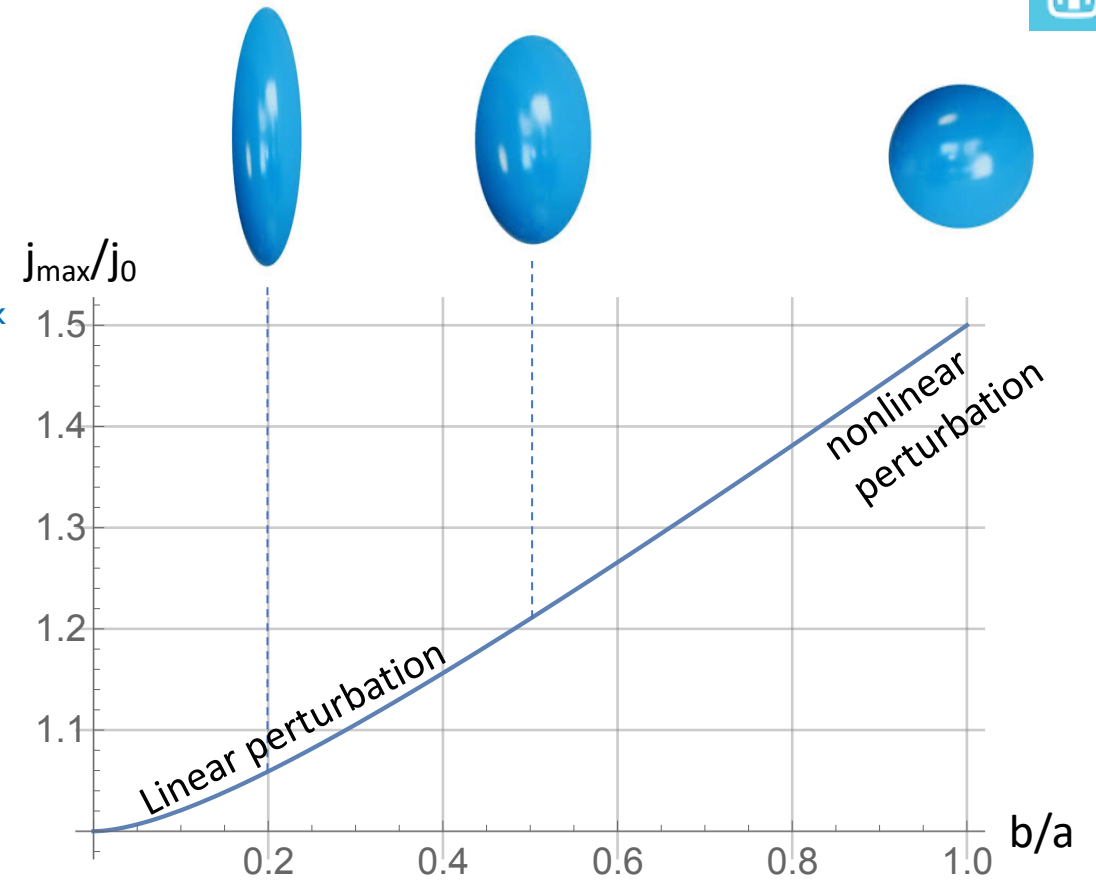
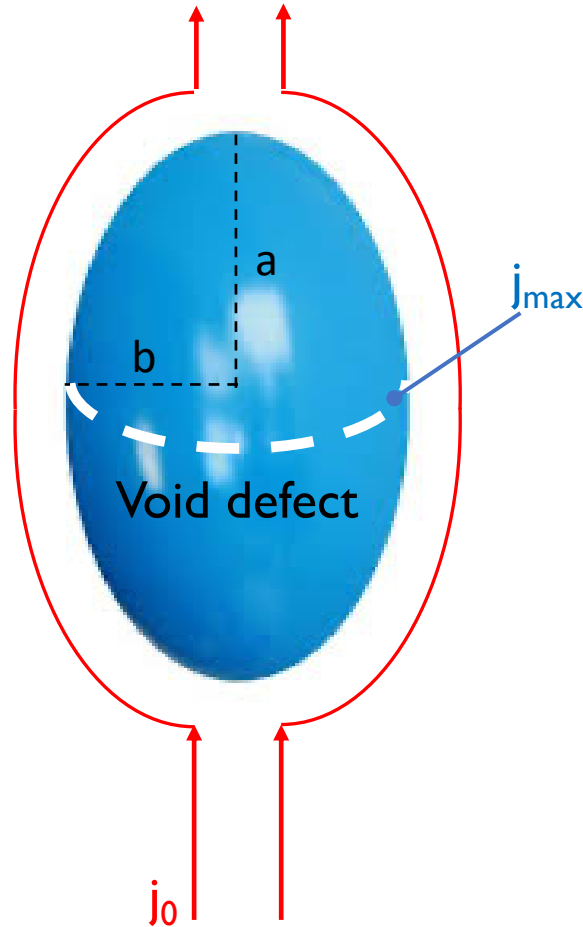
Backup: 3D defects constitute nonlinear perturbations to current density j



Be liner (50 nm rms)



Characterization of Be rod surface
(E. Harding, K. Tomlinson)

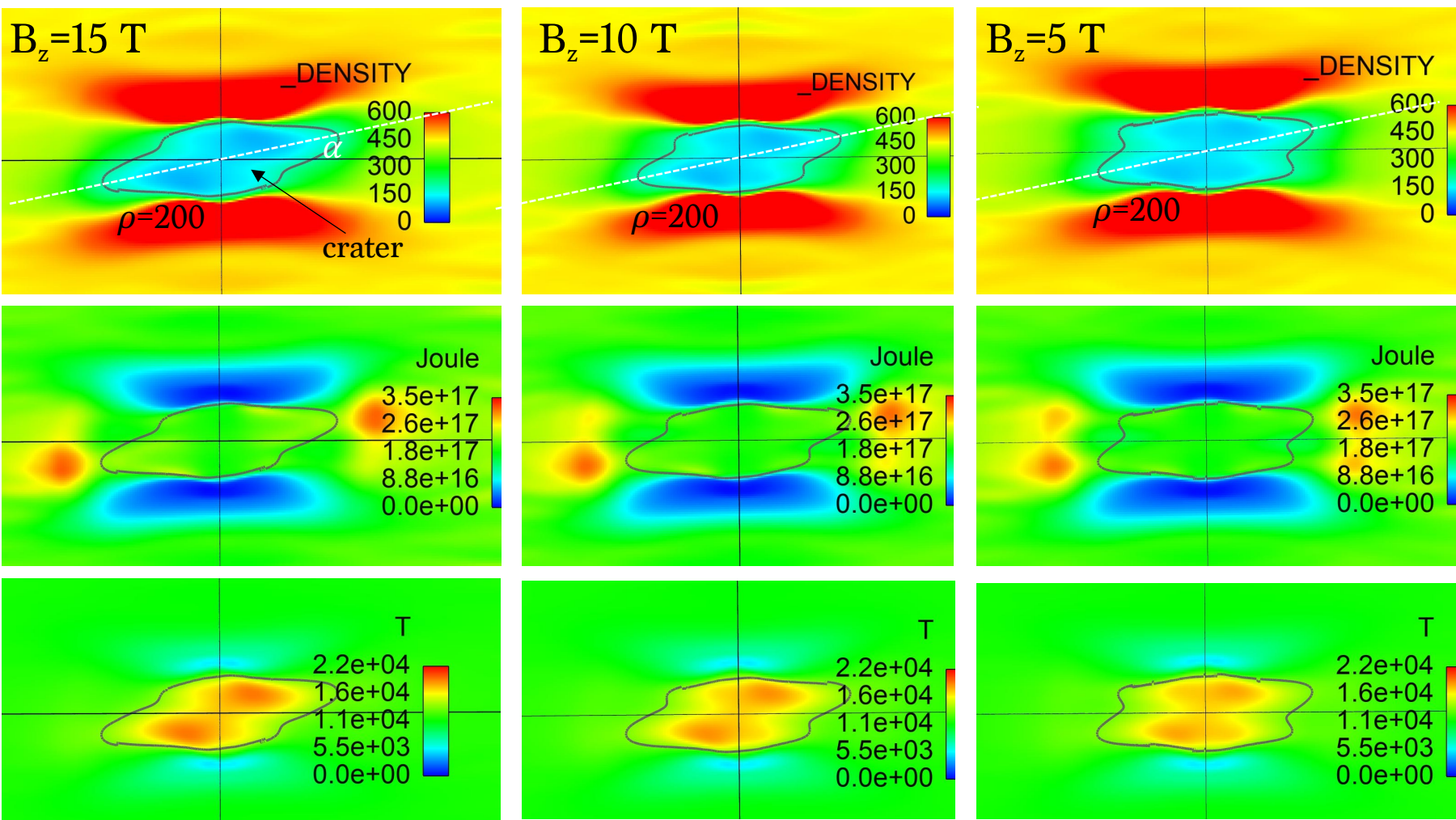


- $\delta j = j_{\max} - j_0$ depends on shape, not size

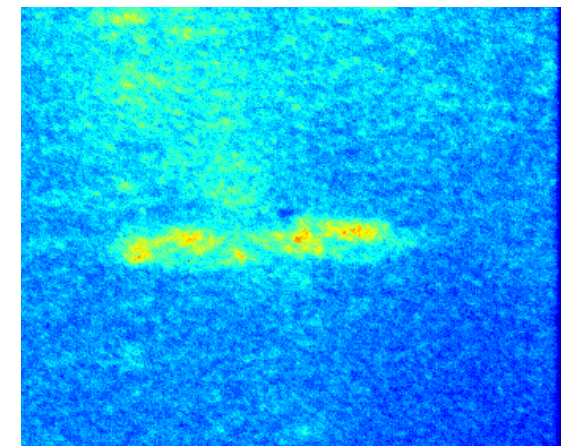
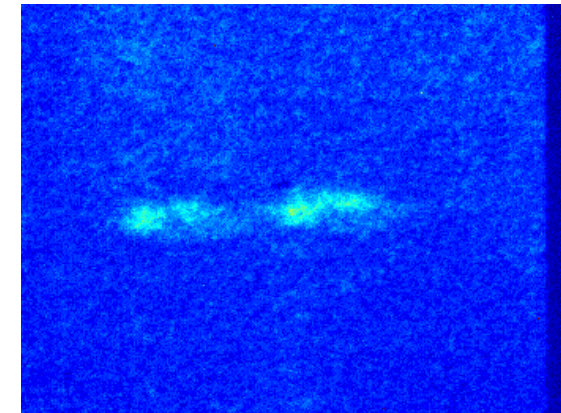
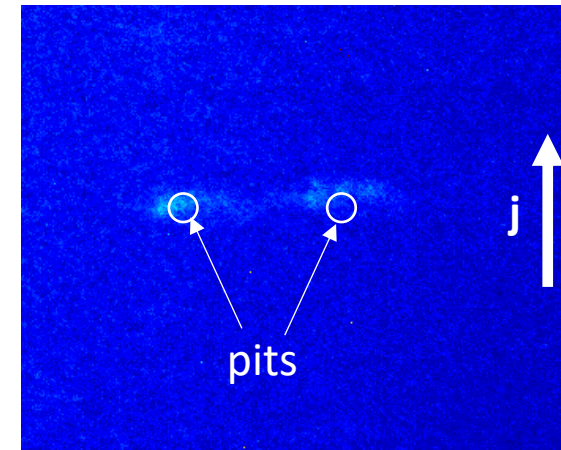
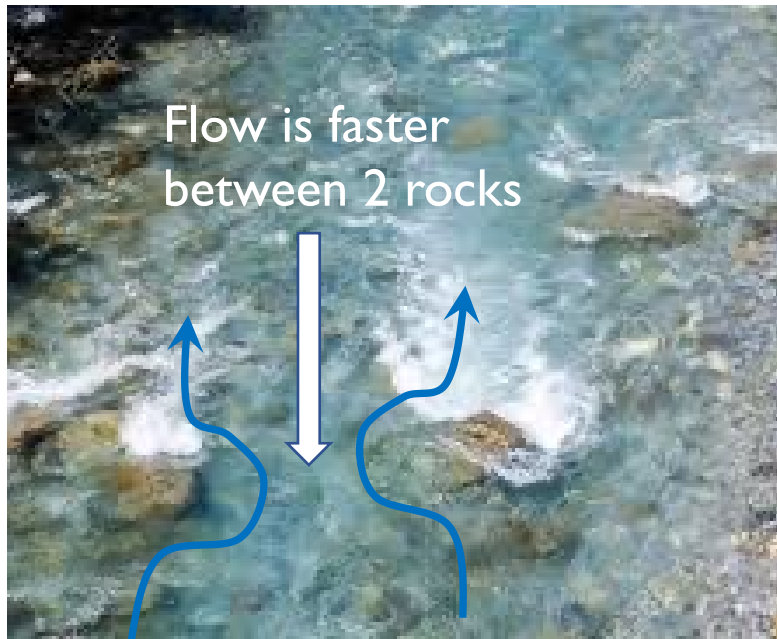
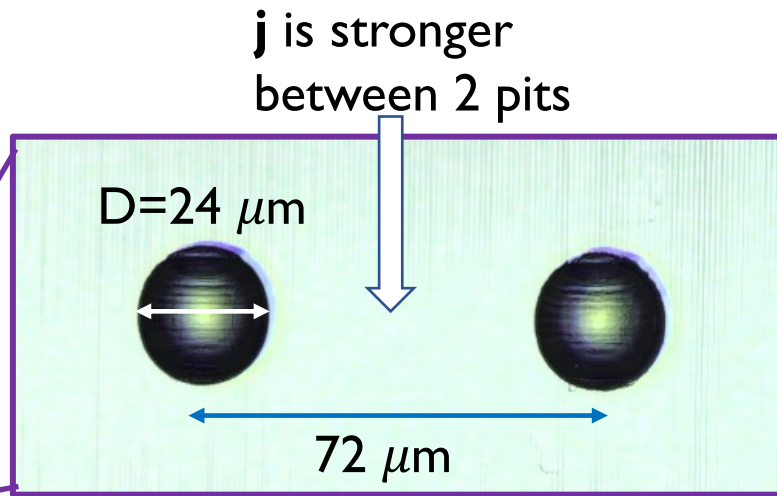
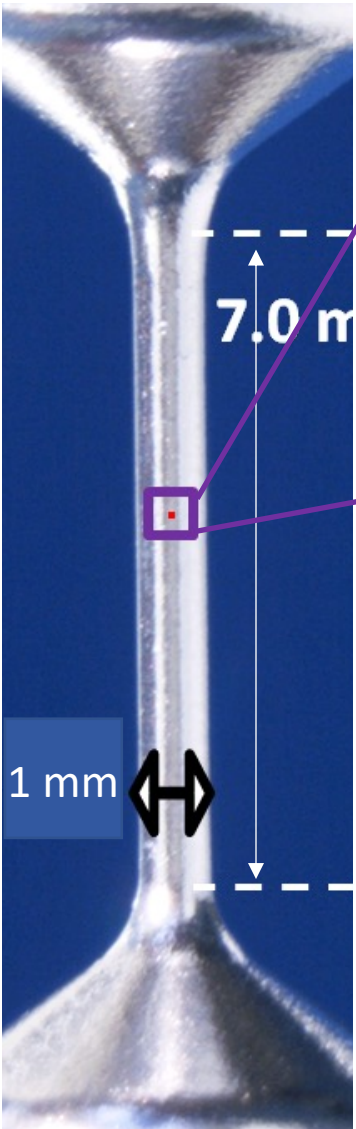
Hydrodynamic analogy with electrical current flow

E.P. Yu, T.J. Awe, K.R. Cochrane et al., Phys. Plasmas **27**, 052703 (2020)

Backup: B_z scan at $t=125\text{ ns}$, $R=5.26\text{e-}4$



Backup: horizontal pits on coated, ultrapure Al rods show azimuthal correlation



Visible emission,
courtesy of [Maren Hatch](#)

time