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Impact Mechanical Response and Shock/Impact Mitigation of Polymeric Foam Materials

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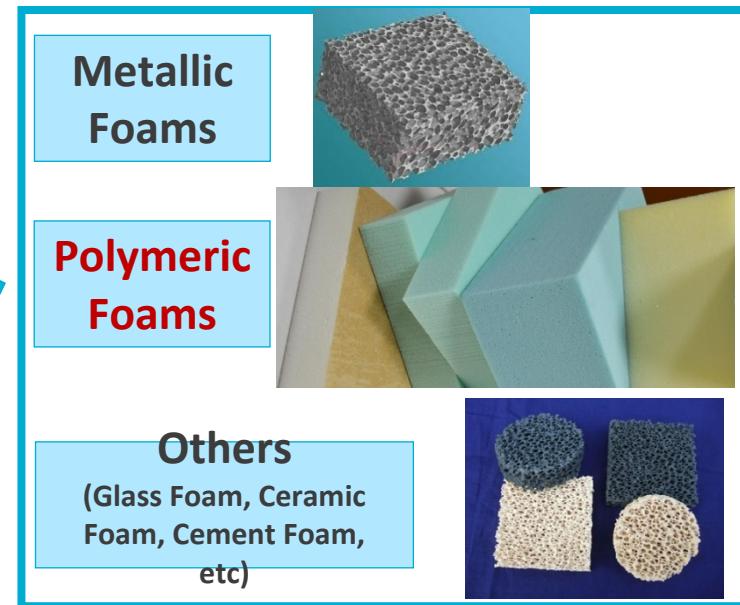
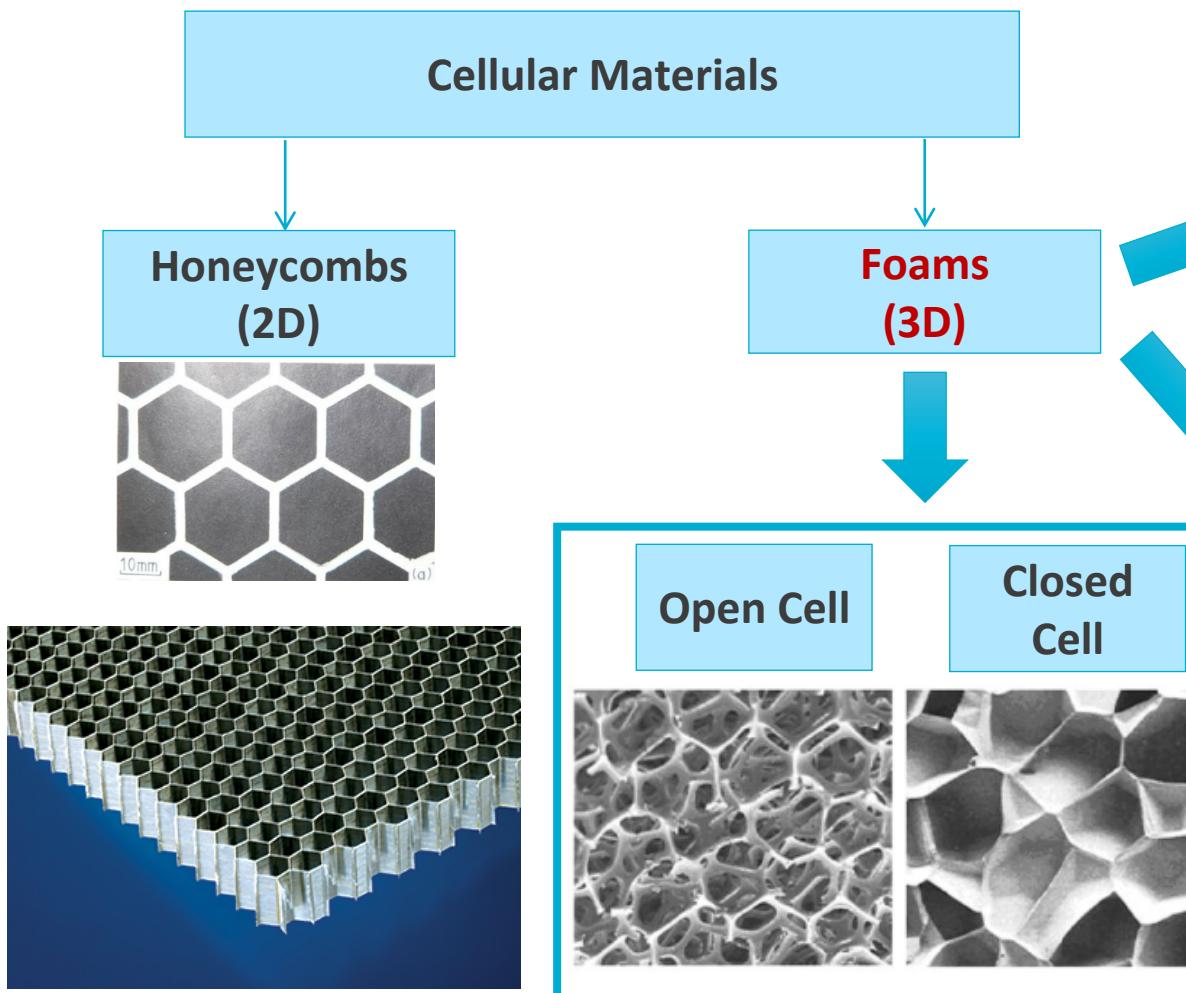
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Outline

- **Background**
- **Impact Response of Polymeric Foams**
 - Dynamic Experimental Techniques
 - Experimental Results of Various Polymeric Foams
- **Shock/Impact Mitigation Characterization of Polymeric Foams**
 - Experiments
 - Energy Dissipation
- **Summary**

Cellular and Foam Materials



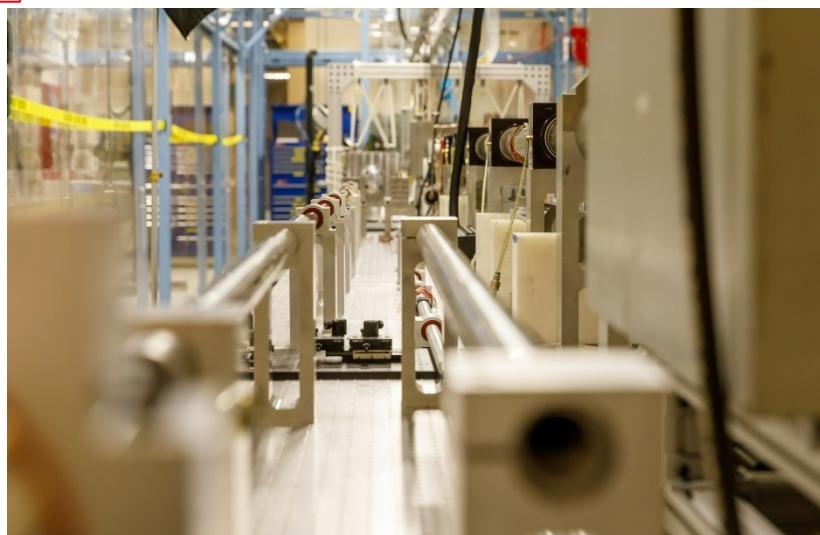
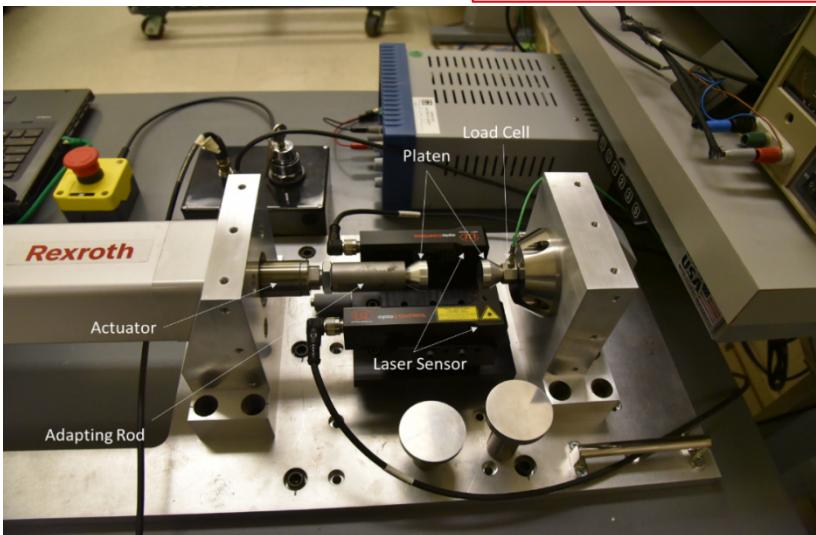
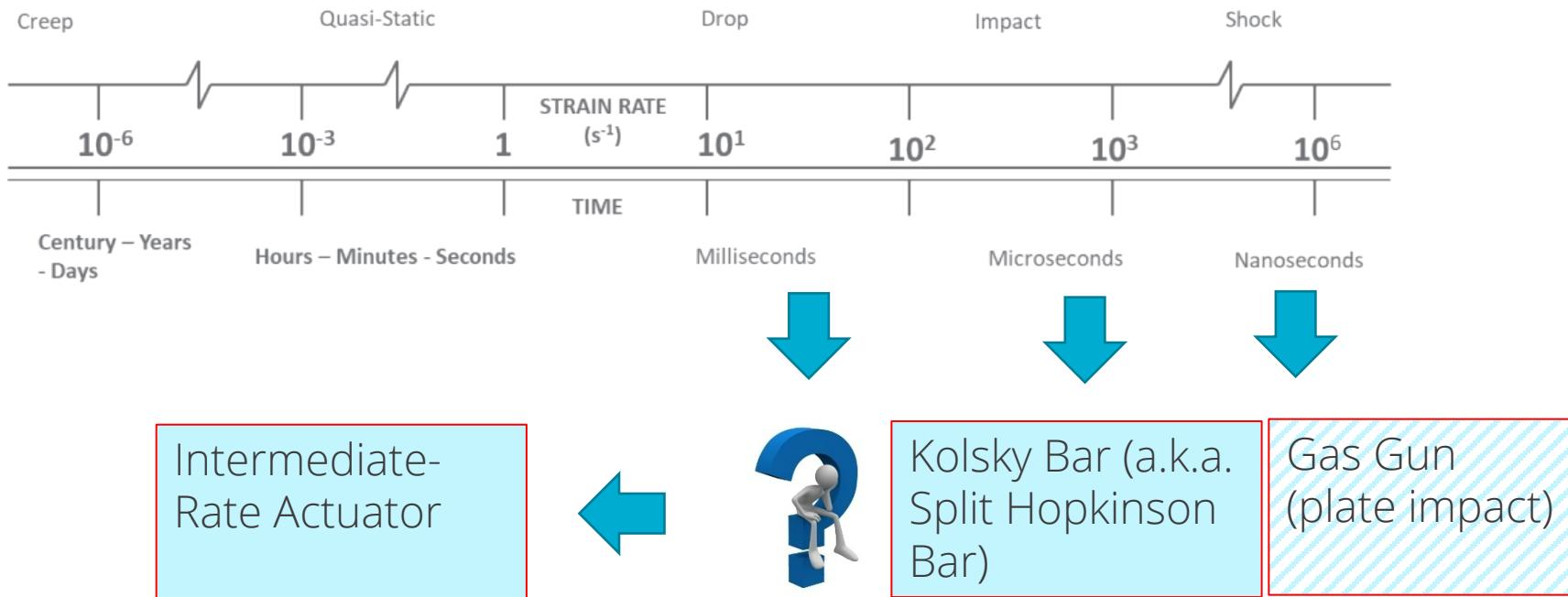
Silicone Foam

Epoxy, Polystyrene, Polyurethane-based Foams (TDI, PMDI, Tuf-Foam)

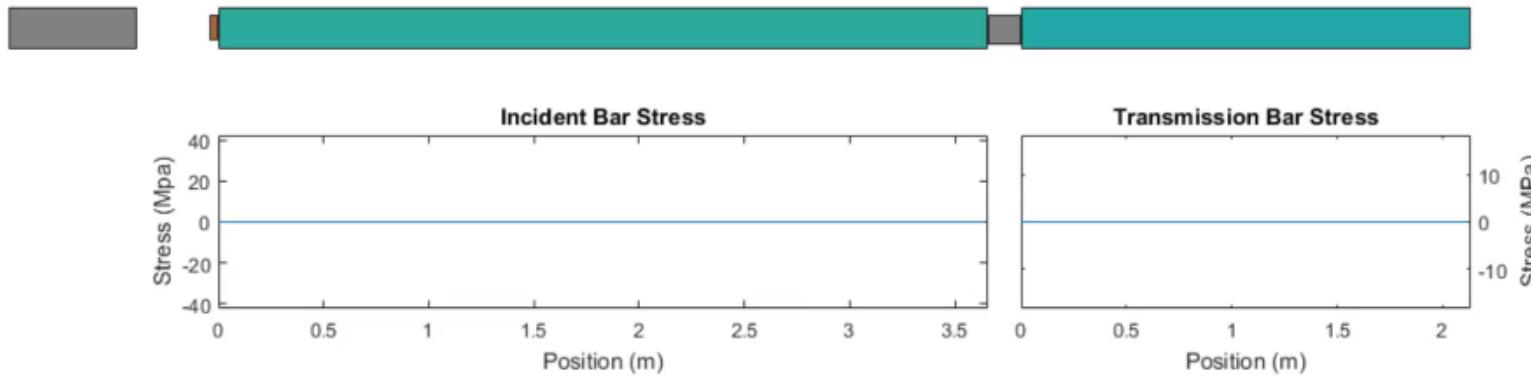
Syntactic Foam (i.e., with glass microballoons)



Dynamic Experimental Techniques



Kolsky Bar (Split Hopkinson Bar)



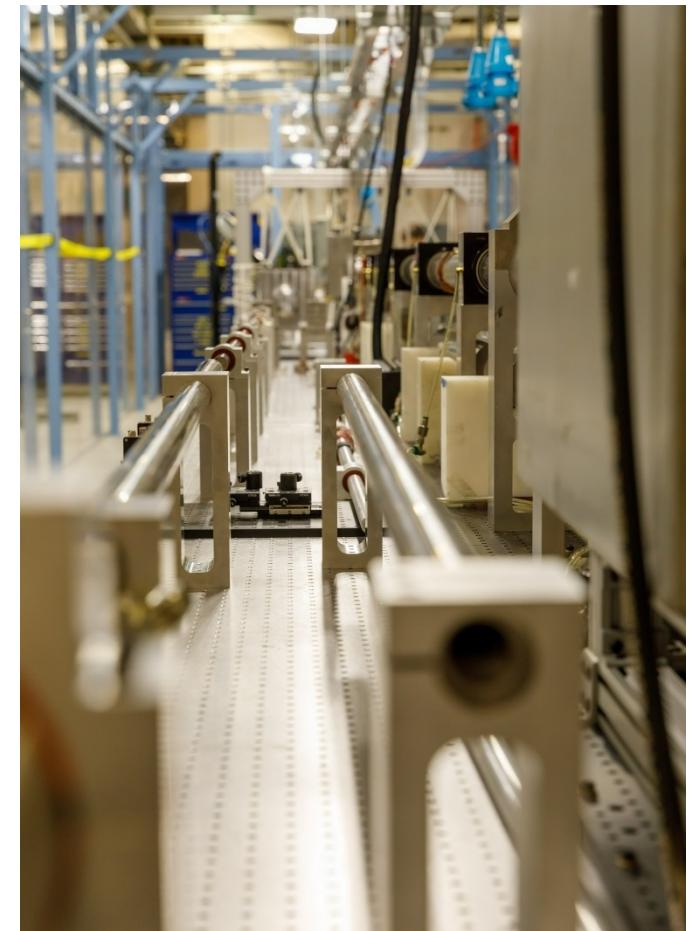
$$\dot{\epsilon} = \frac{V_1 - V_2}{l_s} = \frac{C_0}{l_s} (\epsilon_i - \epsilon_r - \epsilon_t)$$

$$\epsilon = \int_0^t \dot{\epsilon}(\tau) d\tau$$

$$\sigma = \frac{F_1 + F_2}{2A_s} = \frac{E_0 A_0}{2A_s} (\epsilon_i + \epsilon_r + \epsilon_t)$$

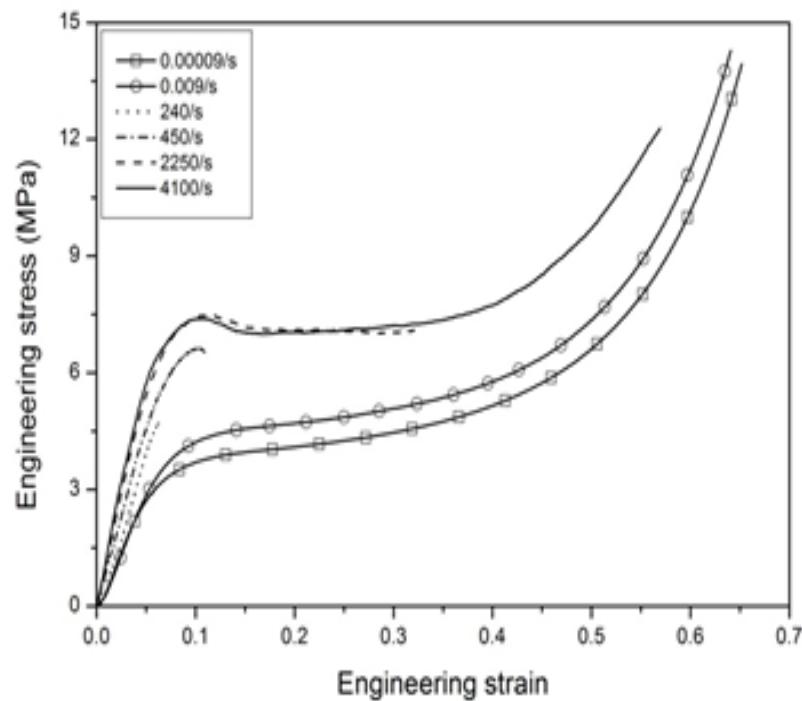


$$\sigma \sim \epsilon$$

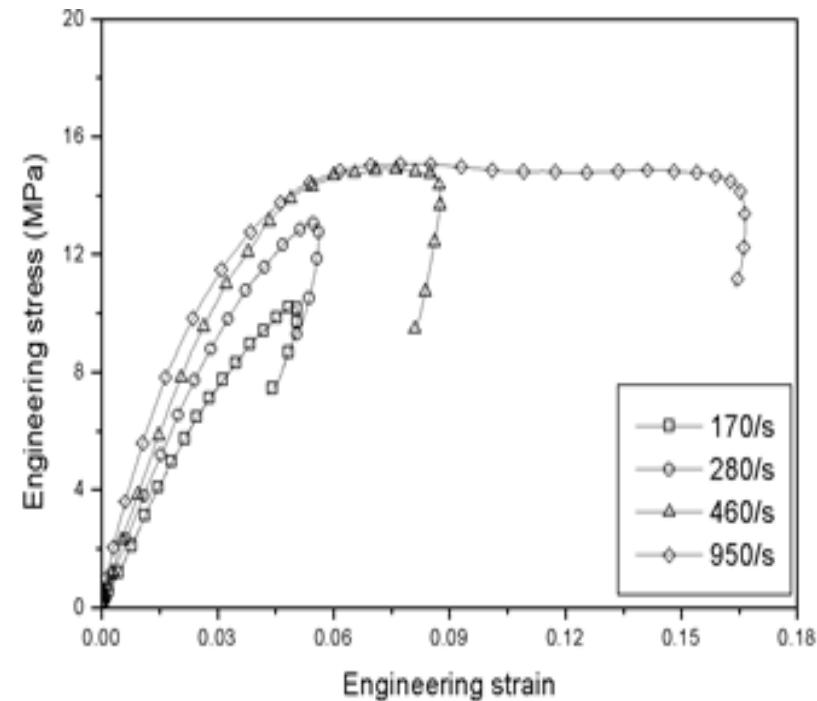


Dynamic Stress-Strain Response of Elastic-Plastic Foam Materials

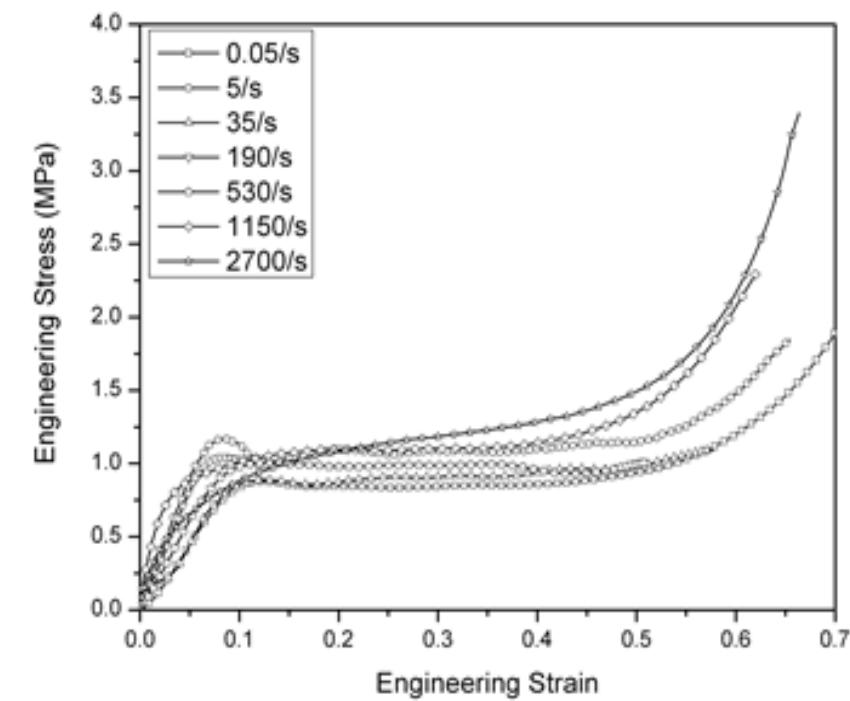
Polyurethane Foam ($0.24 \times 10^3 \text{ kg/m}^3$)



Polystyrene Foam ($0.40 \times 10^3 \text{ kg/m}^3$)

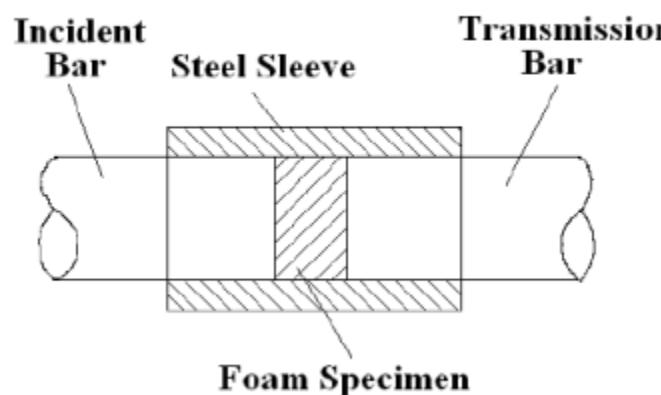


Epoxy Foam ($0.12 \times 10^3 \text{ kg/m}^3$)

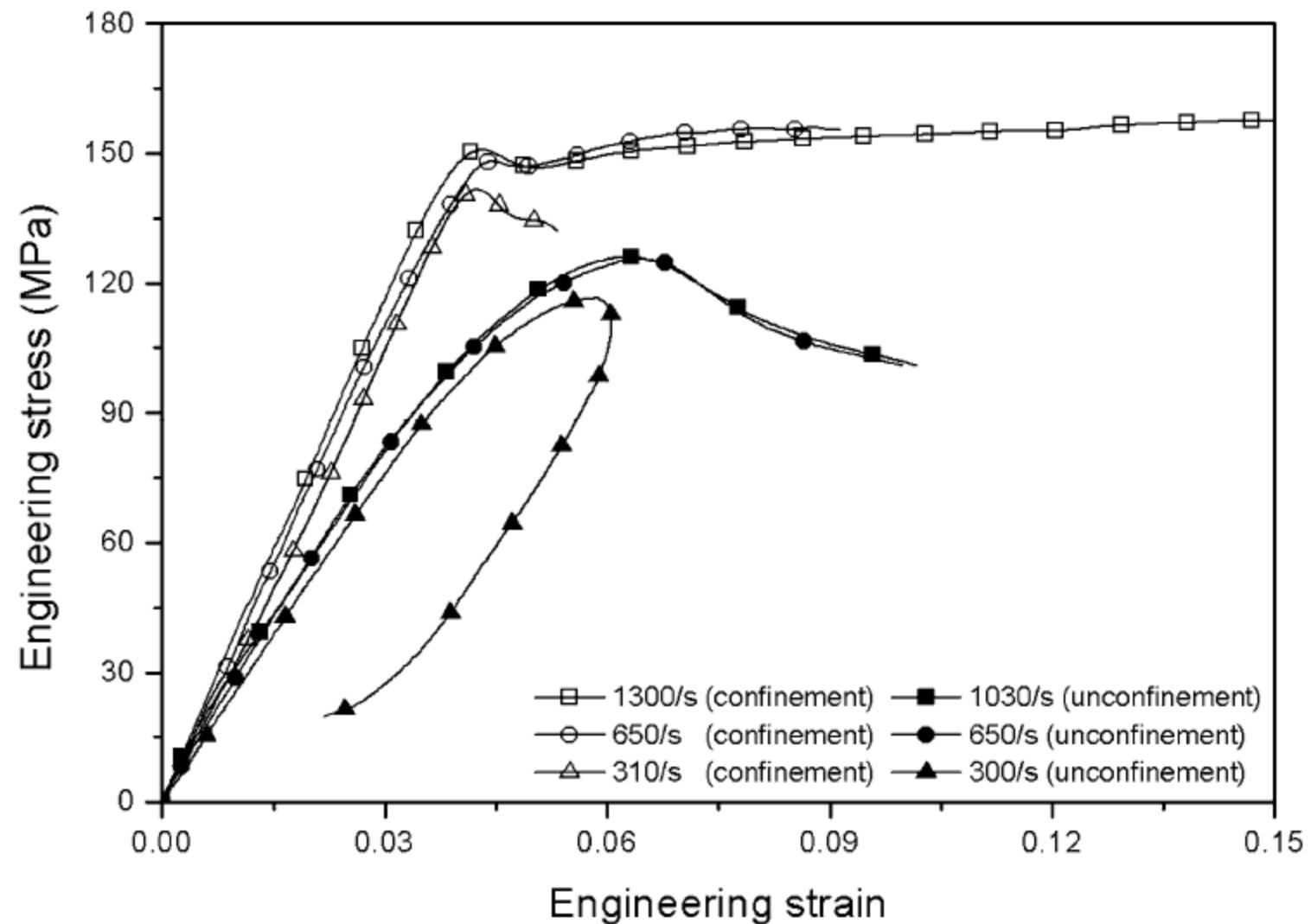


The stress-strain response depends on density, temperature, stress state, etc.

Dynamic Stress-Strain Response of Elastic-Brittle Foam Materials

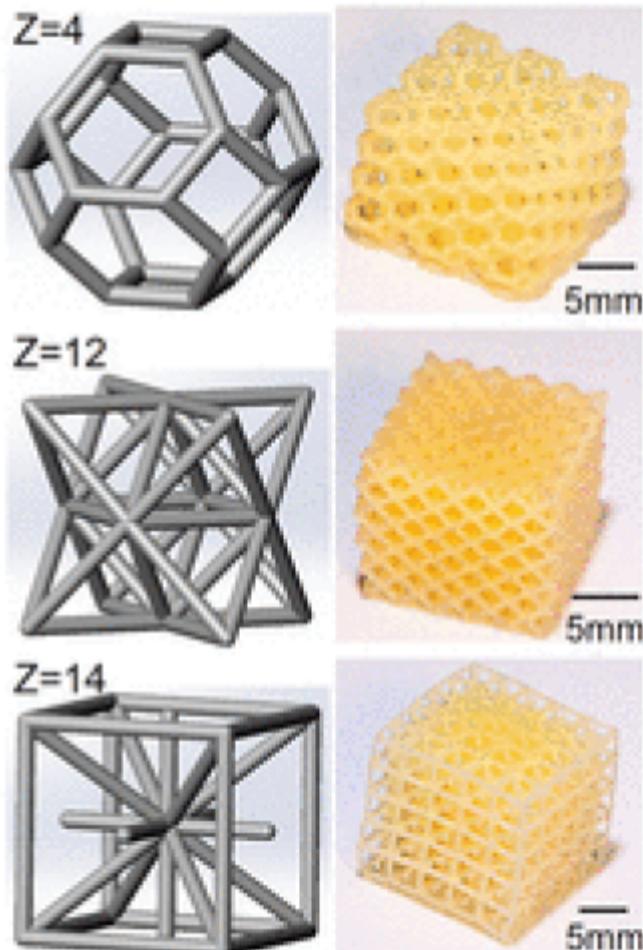


Unconfined versus Confined



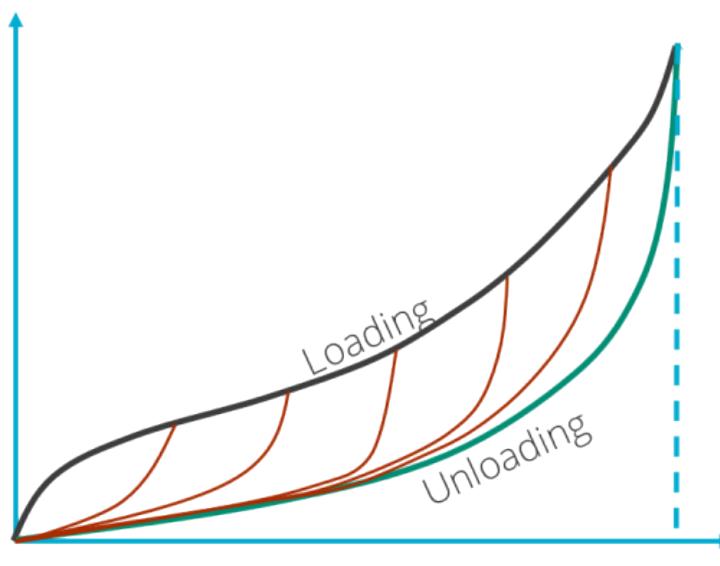
Dynamic Stress-Strain Response of Hyperelastic Foam Materials

Liquid Crystal Elastomer (LCE) Lattice Foam



It has been very challenging to dynamically characterize such soft lattice foam materials at high strain rates with a Kolsky compression bar, due to relatively large (long) specimen size and low wave speed.

Kolsky compression bar is also not able to be used to characterize the unloading stress-strain response for such soft materials, which is critical for energy dissipation calculation.



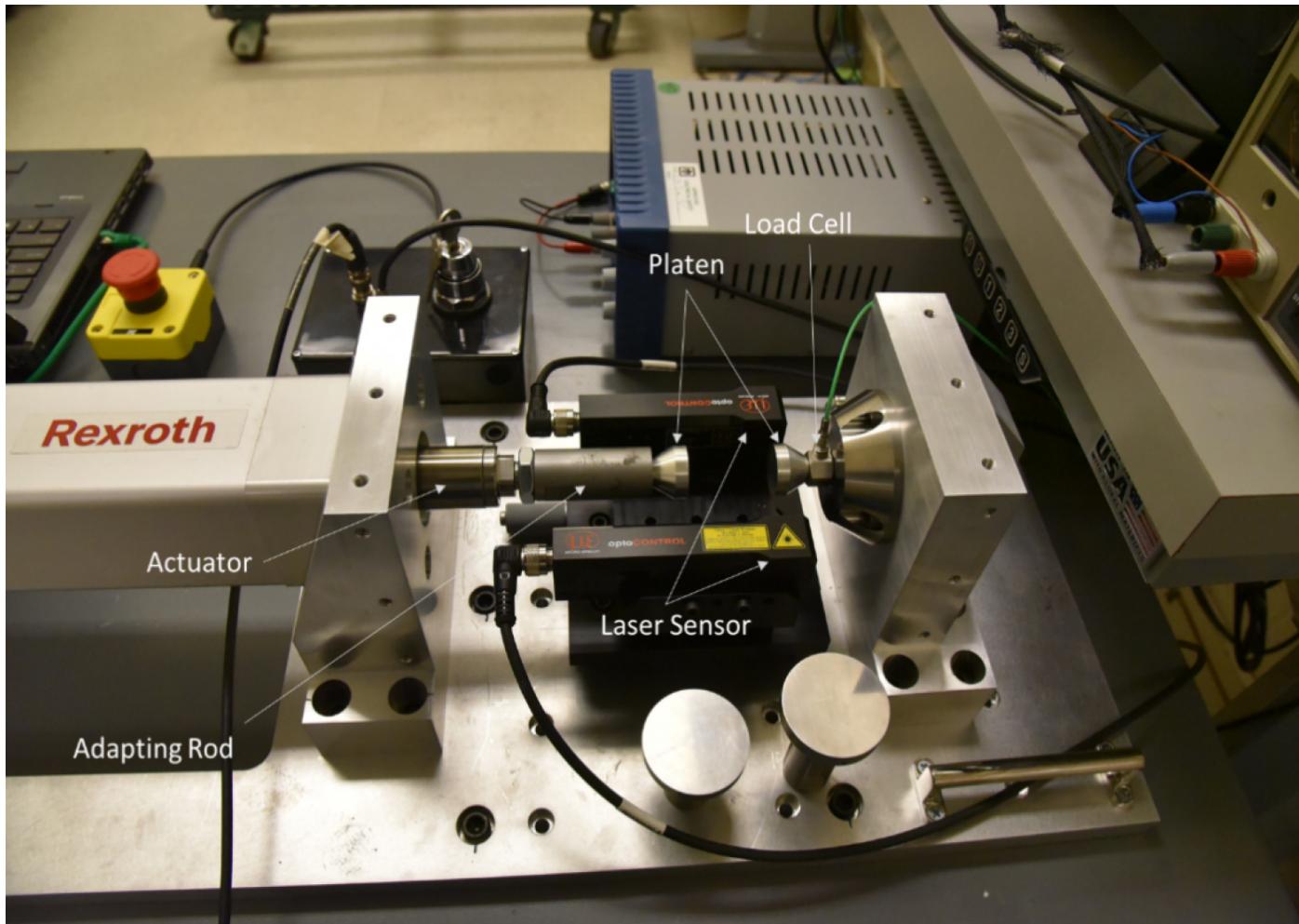
Energy dissipation:

$$\begin{aligned}\Delta &= E_{loading} - E_{unloading} \\ &= \int_{loading} \sigma d\varepsilon - \int_{unloading} \sigma d\varepsilon\end{aligned}$$

Energy dissipation ratio:

$$\delta = \frac{\Delta}{E_{loading}} = 1 - \frac{\int_{unloading} \sigma d\varepsilon}{\int_{loading} \sigma d\varepsilon}$$

Bench-top Intermediate-Strain-Rate Test Apparatus



Rexroth® high speed electromechanical actuator

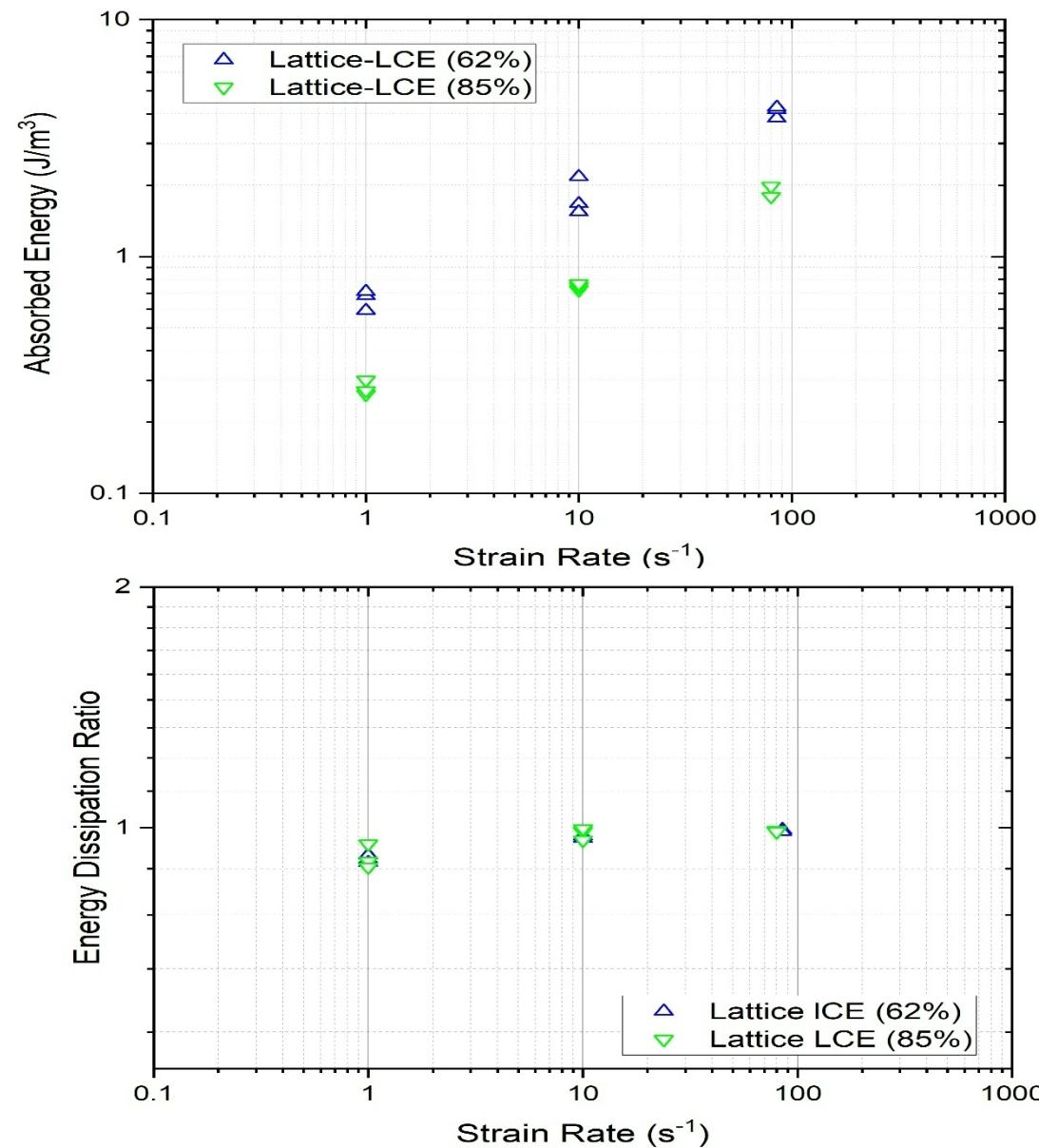
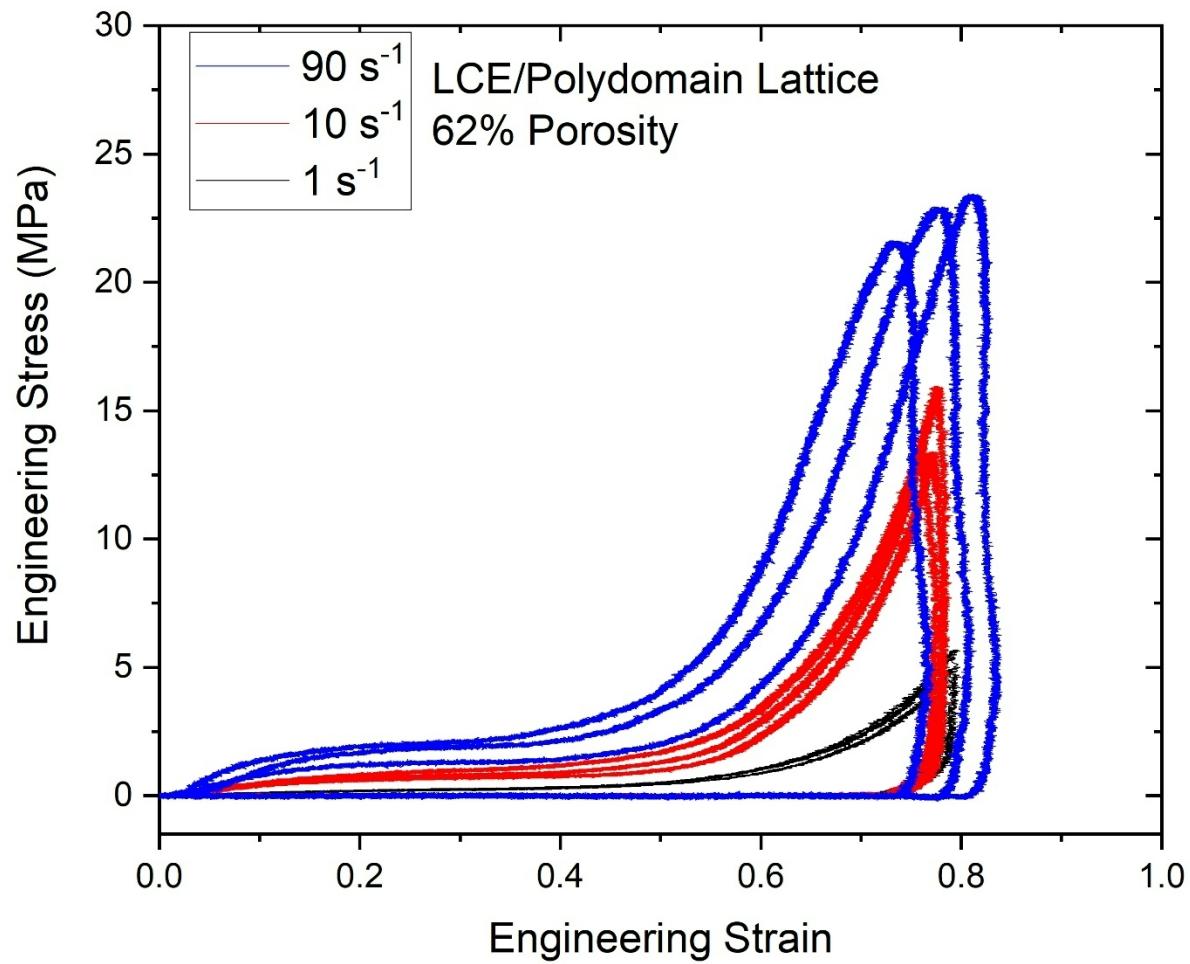
- Maximum impact velocity: ~1.9 m/s
- Maximum travel distance: 6" (~150 mm)
- Maximum acceleration: ~400 m/s²
- Load capacity: 3000 lbs (~13300 N)



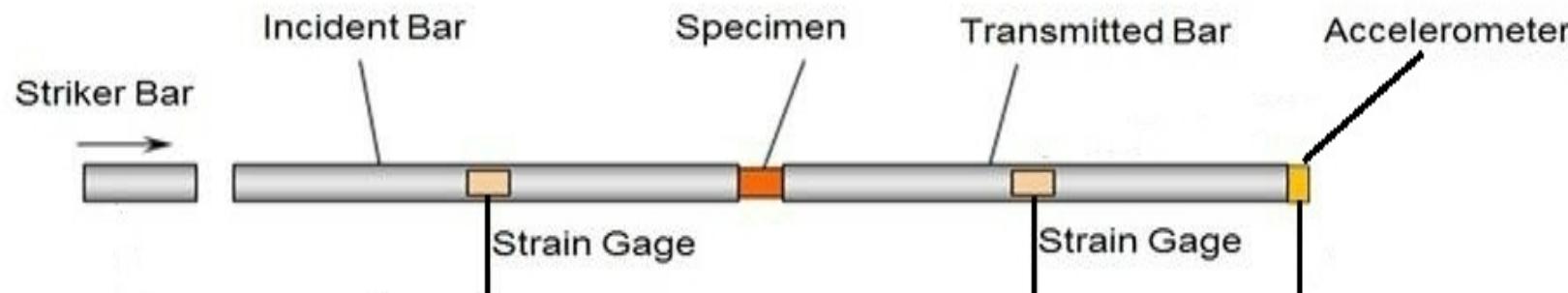
For a 10 mm (diameter) by 5 mm (thickness) specimen,

- Maximum stress: ~170 MPa
- Maximum strain rate: ~380 s⁻¹

Loading-Unloading Stress-Strain Response at Intermediate Rates



Shock Mitigation Analyses with a Kolsky Compression Bar (Time Domain)



Incident Energy

$$E_i(t) = A_0 C_0 E_0 \int_0^t \varepsilon_i(t)^2 dt$$

Energy Dissipation (Absorbed Energy)

Reflected Energy

$$E_r(t) = A_0 C_0 E_0 \int_0^t \varepsilon_r(t)^2 dt$$

$$\Delta E(t) = E_{input}(t) - E_{output}(t) = A_0 C_0 E_0 \int_0^t [\varepsilon_i^2(t) - \varepsilon_r^2(t) - \varepsilon_t^2(t)] dt$$

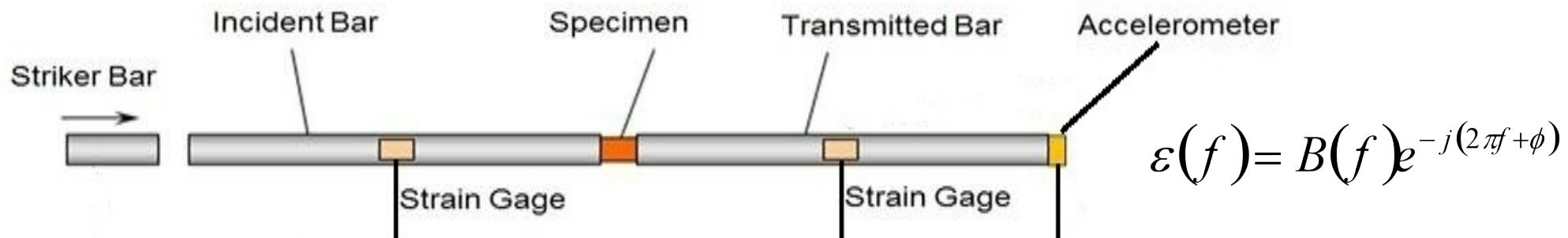
Energy Dissipation Ratio

Transmitted Energy

$$E_t(t) = A_0 C_0 E_0 \int_0^t \varepsilon_t(t)^2 dt$$

$$\delta(t) = \frac{\Delta E(t)}{E_{input}(t)}$$

Shock Mitigation Analyses with a Kolsky Compression Bar (Frequency Domain)



Incident Energy Spectrum Density

$$S_i(f) = A_0 C_0 E_0 |B_i(f)|^2$$

Energy Dissipation Ratio

Reflected Energy Spectrum Density

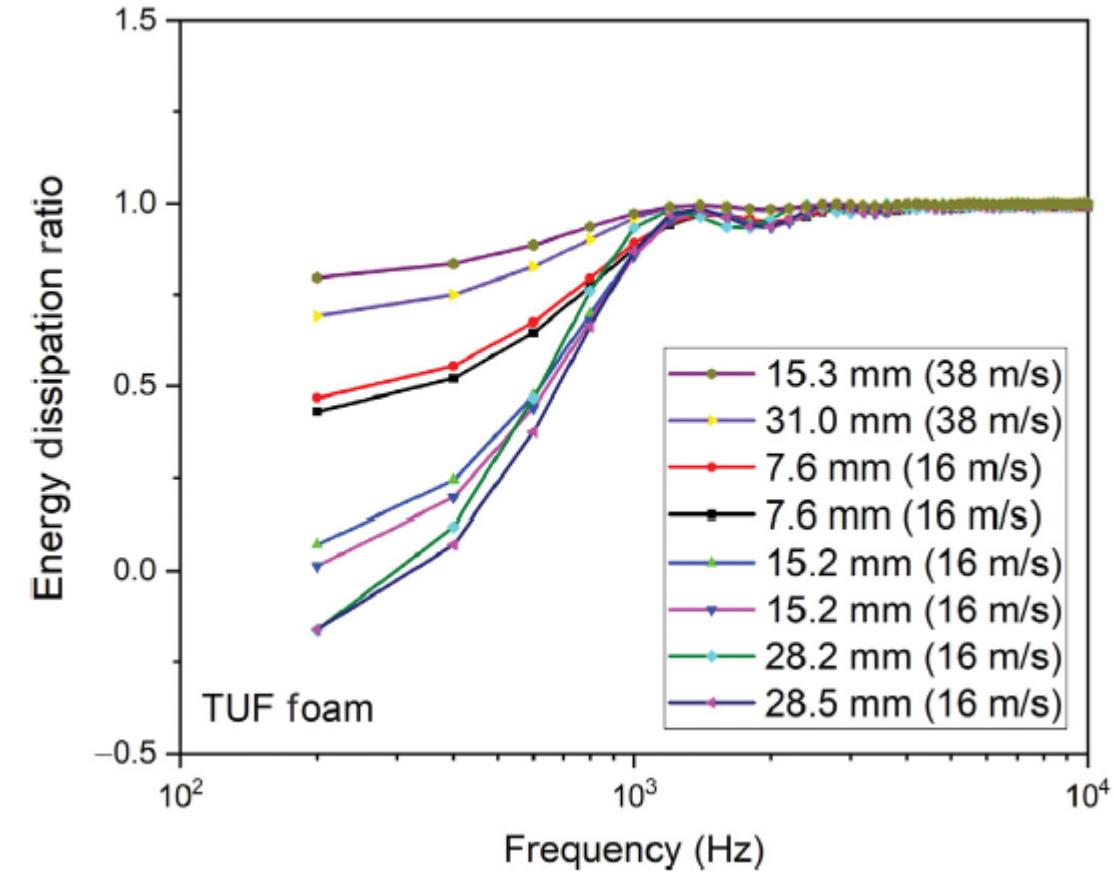
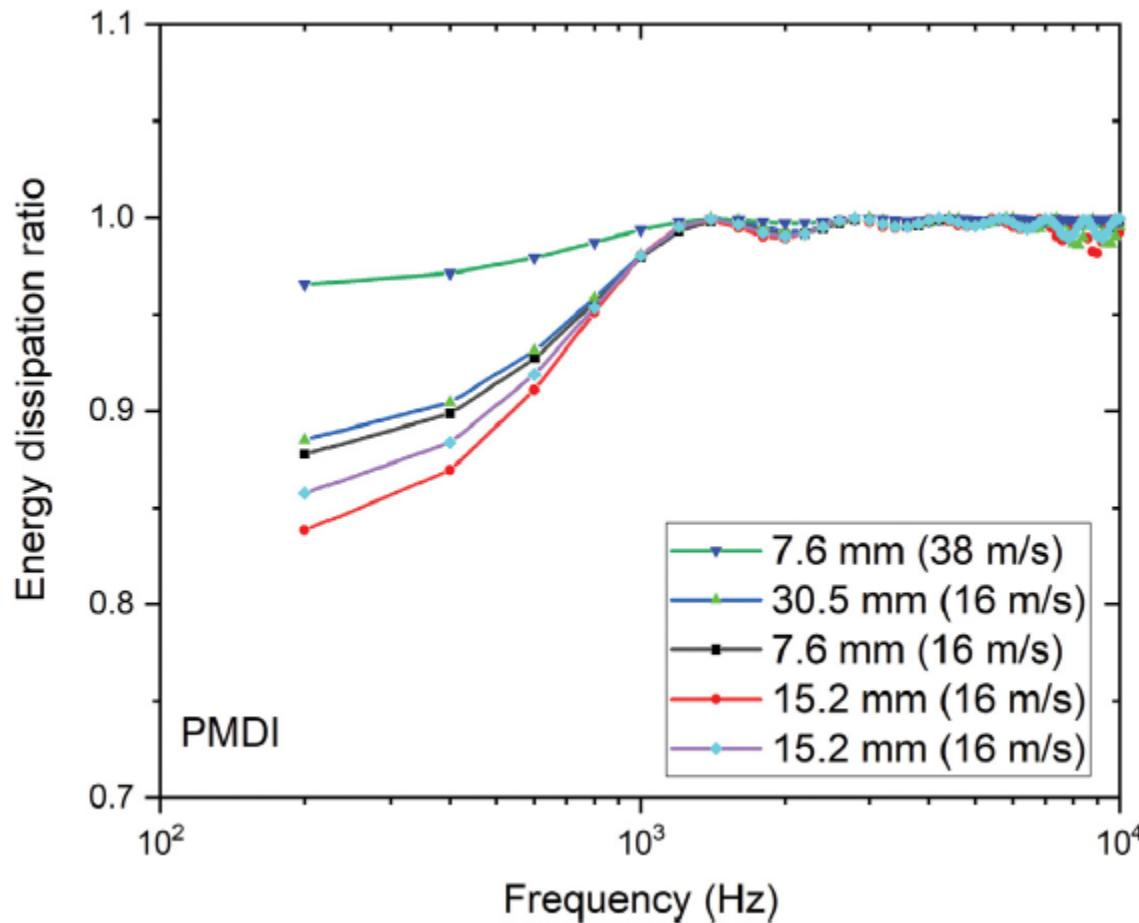
$$S_r(f) = A_0 C_0 E_0 |B_r(f)|^2$$

$$\delta(f) = \frac{\Delta(f)}{E_i(f) - E_r(f)} = 1 - \frac{|B_t(f)|^2}{|B_i(f)|^2 - |B_r(f)|^2}$$

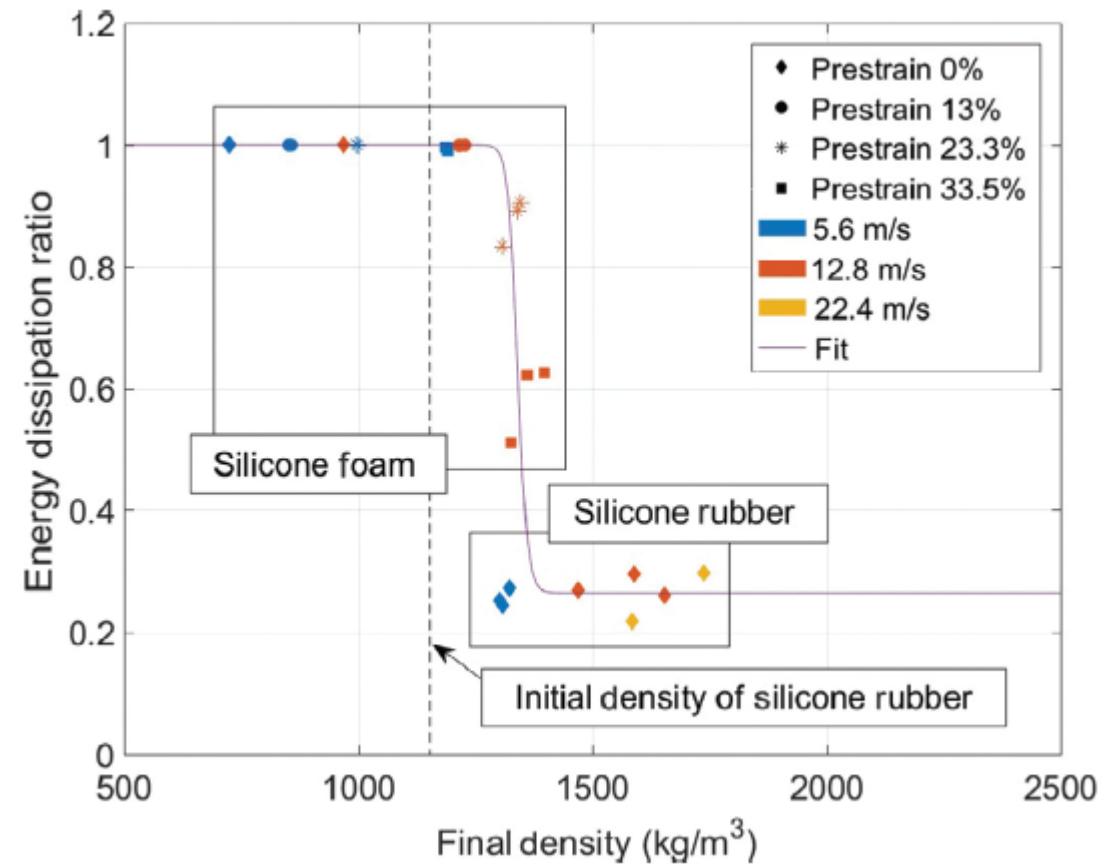
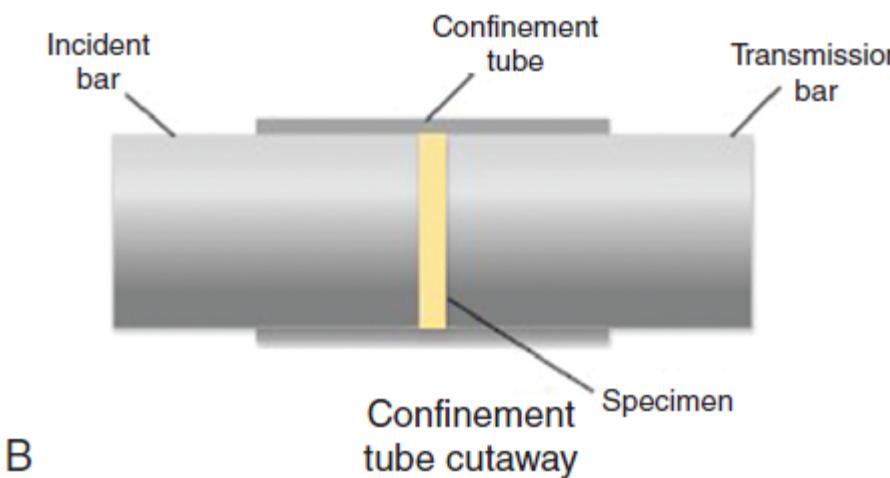
Transmitted Energy Spectrum Density

$$S_t(f) = A_0 C_0 E_0 |B_t(f)|^2$$

Frequency-dependent Energy Dissipation of Elastic-Plastic Foams



Energy Dissipation Characteristic of Confined Silicone Foam





Summary

Goal: maximize shock mitigation, optimize material and structural design

- Material properties need to be fully characterized
 - At different strain rates
 - At different temperatures
 - At different stress states
- Direct energy absorption and dissipation calculation from loading-unloading stress-strain curves
 - Dependent on strain, strain rate, temperature, stress state, etc.
- Structural response in terms of shock mitigation needs to be fully characterized
 - Impact crush response
 - Impact energy dissipation
 - In time domain
 - In frequency domain