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# Impact Mechanical Response and Shock/Impact Mitigation of Polymeric Foam Materials

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# Outline

## ➤ Background

## ➤ Impact Response of Polymeric Foams

- Dynamic Experimental Techniques
- Experimental Results of Various Polymeric Foams

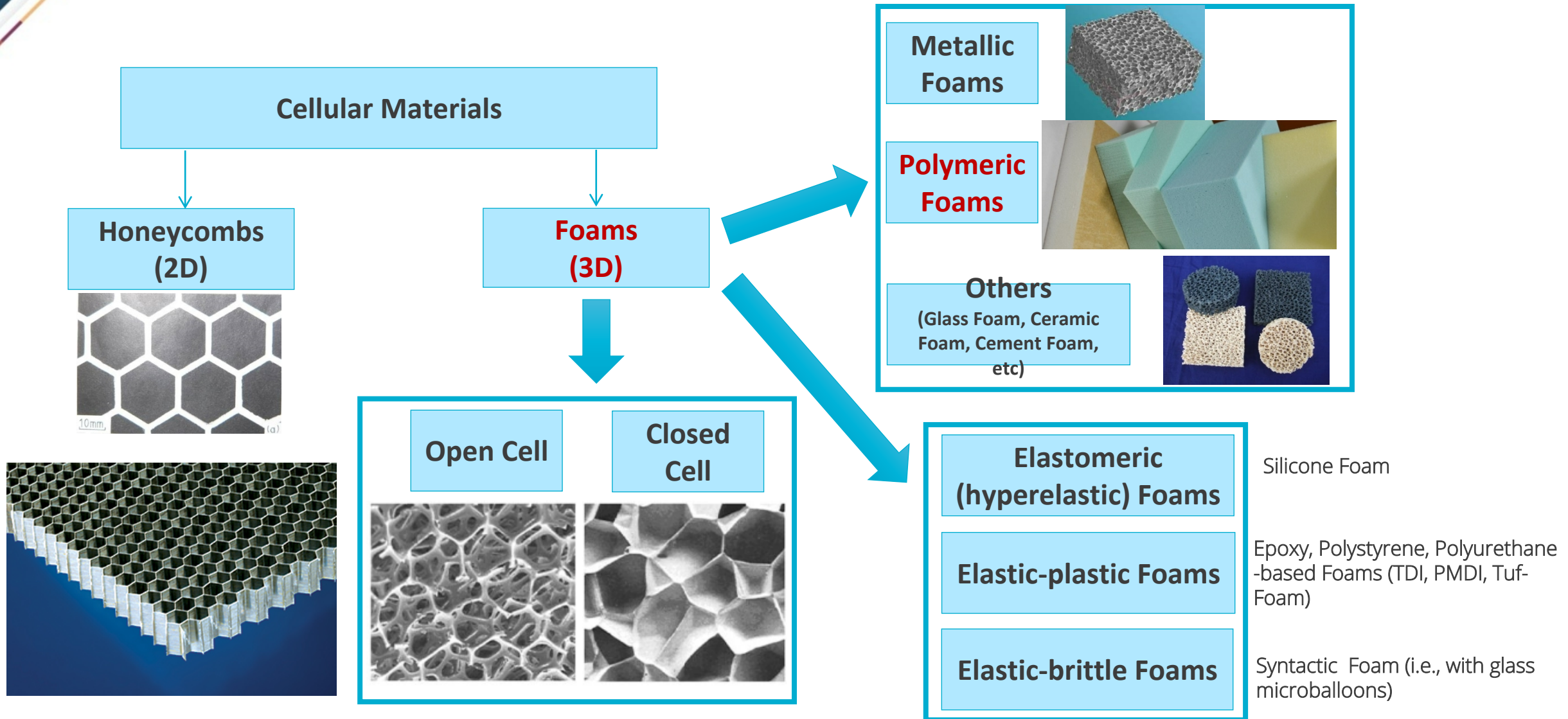
## ➤ Shock/Impact Mitigation Characterization of Polymeric Foams

- Experiments
- Energy Dissipation

## ➤ Summary

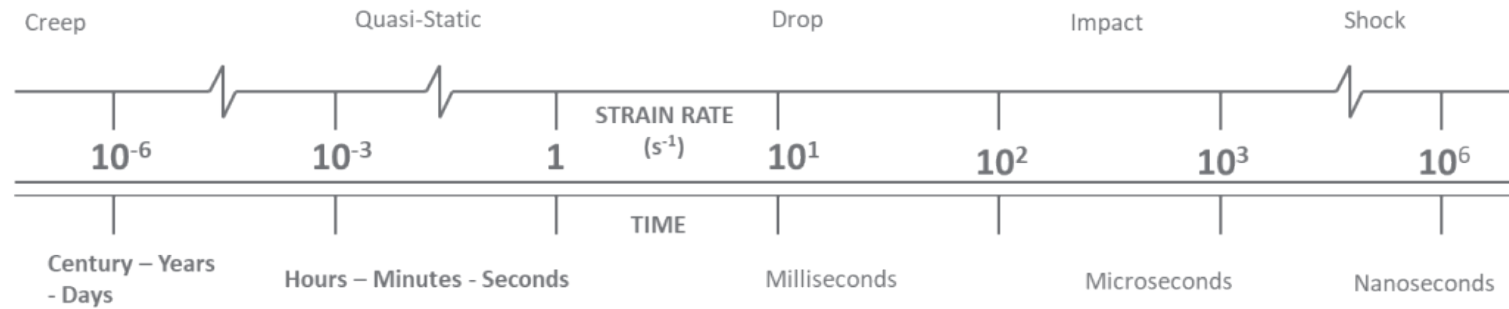


# Cellular and Foam Materials





# Dynamic Experimental Techniques

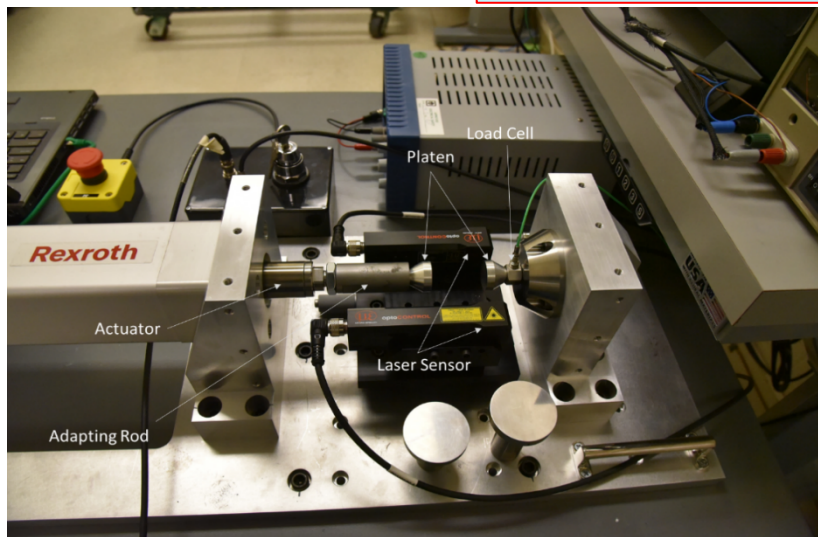


Intermediate-Rate Actuator



Kolsky Bar (a.k.a. Split Hopkinson Bar)

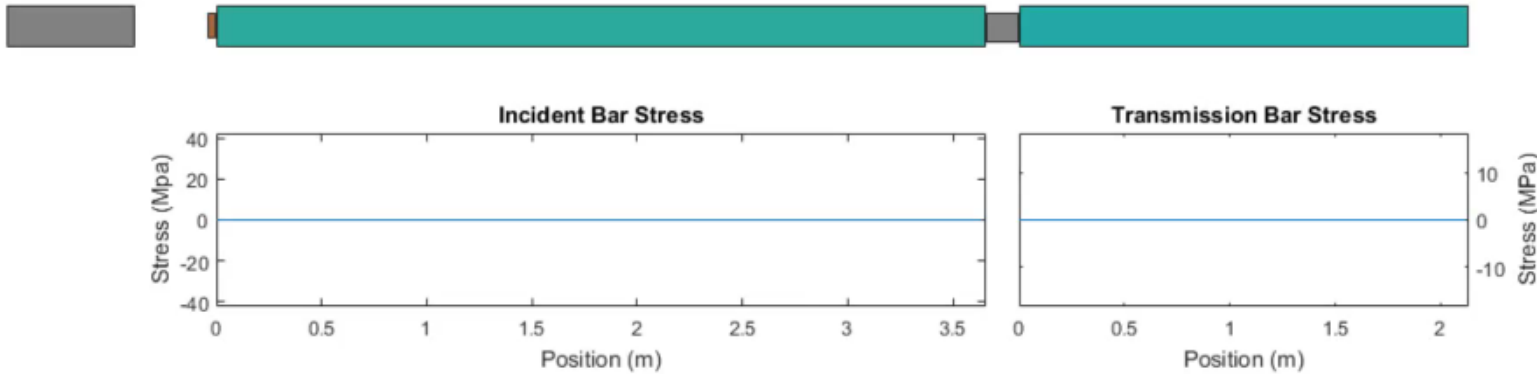
Gas Gun (plate impact)







# Kolsky Bar (Split Hopkinson Bar)



$$\dot{\varepsilon} = \frac{V_1 - V_2}{l_s} = \frac{C_0}{l_s} (\varepsilon_i - \varepsilon_r - \varepsilon_t)$$

$$\varepsilon = \int_0^t \dot{\varepsilon}(\tau) d\tau$$

$$\sigma = \frac{F_1 + F_2}{2A_s} = \frac{E_0 A_0}{2A_s} (\varepsilon_i + \varepsilon_r + \varepsilon_t)$$



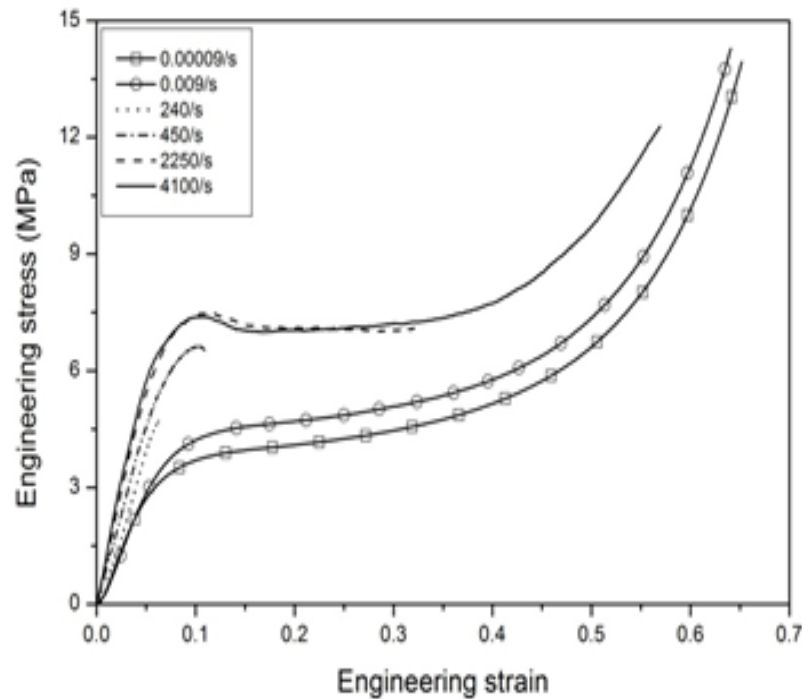
$$\sigma \sim \varepsilon$$



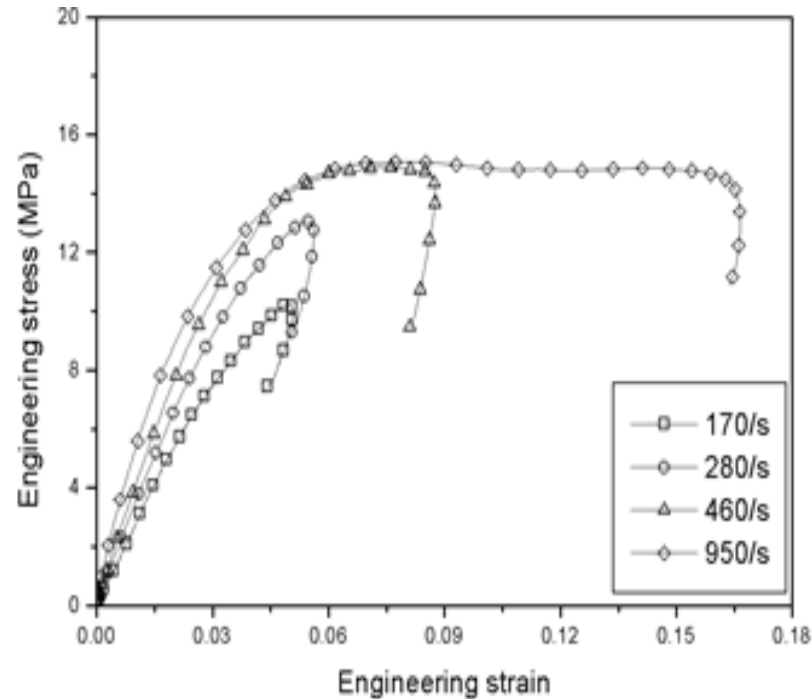


# Dynamic Stress-Strain Response of Elastic-Plastic Foam Materials

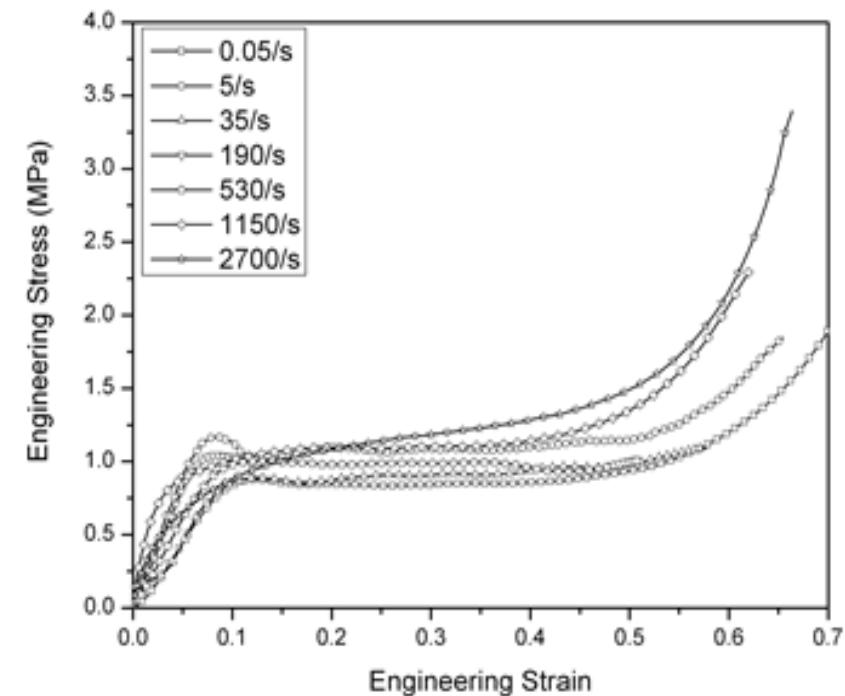
Polyurethane Foam ( $0.24 \times 10^3 \text{ kg/m}^3$ )



Polystyrene Foam ( $0.40 \times 10^3 \text{ kg/m}^3$ )



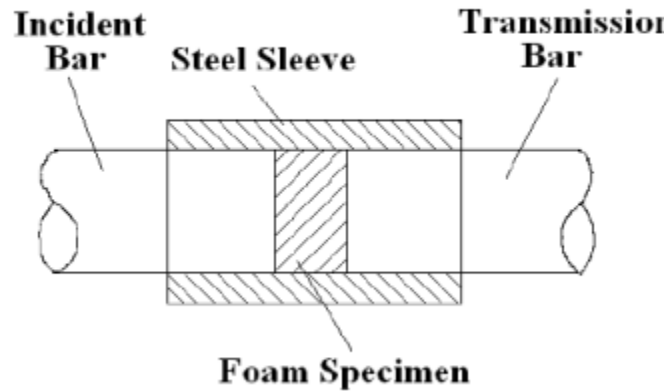
Epoxy Foam ( $0.12 \times 10^3 \text{ kg/m}^3$ )



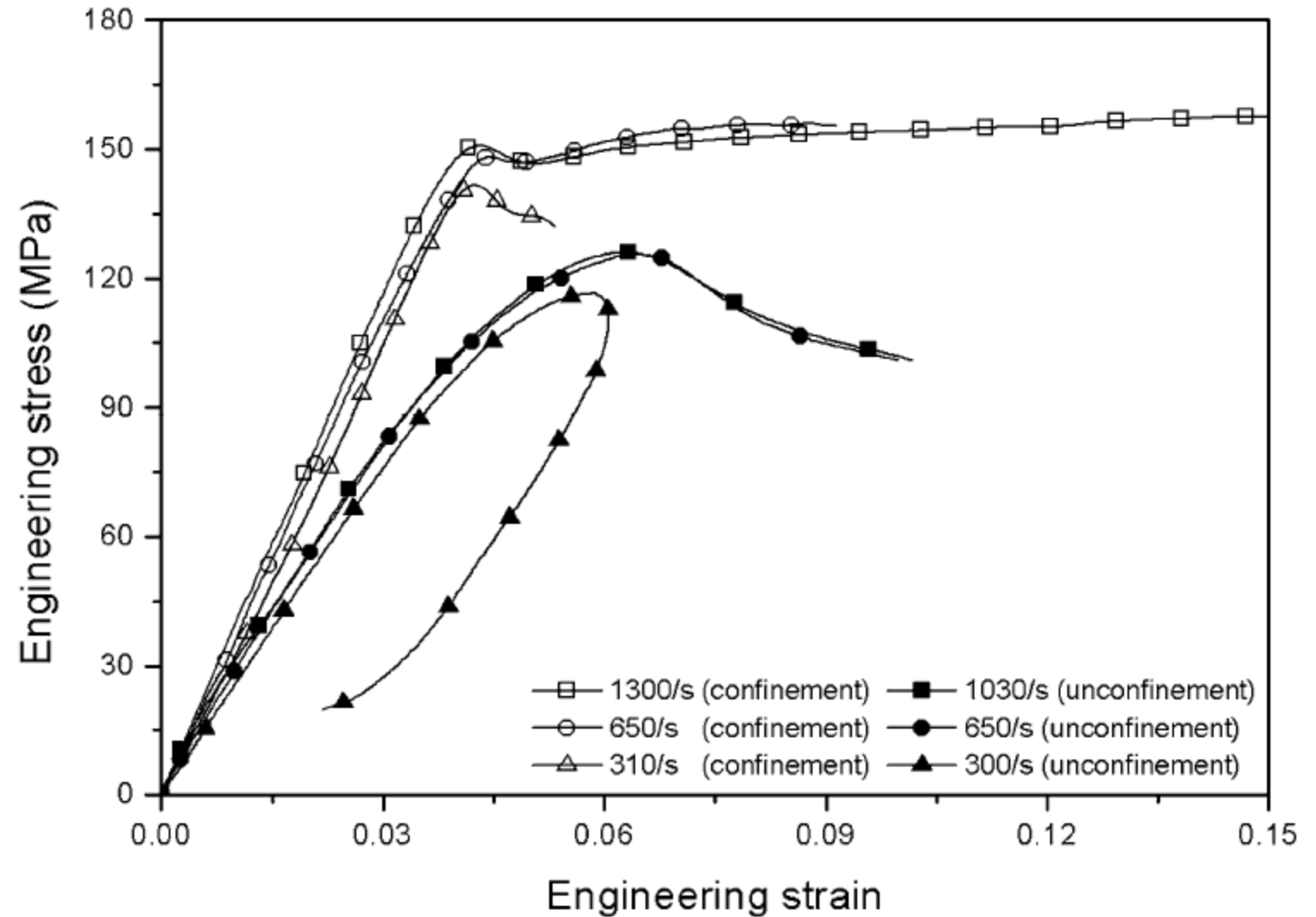
The stress-strain response depends on density, temperature, stress state, etc.



# Dynamic Stress-Strain Response of Elastic-Brittle Foam Materials



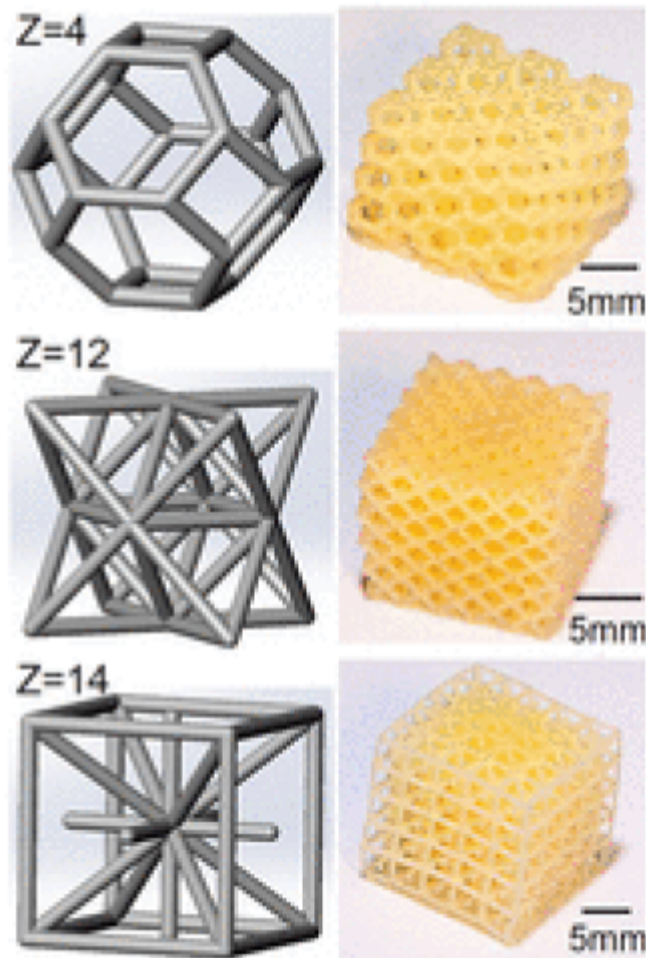
*Unconfined versus Confined*





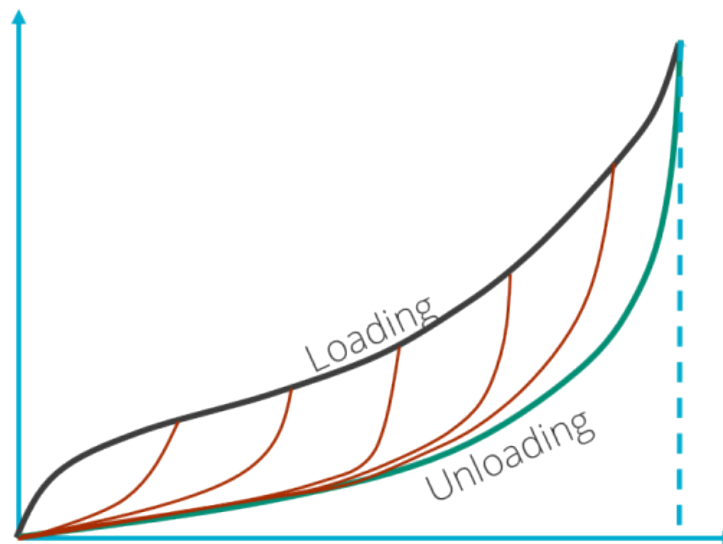
# Dynamic Stress-Strain Response of Hyperelastic Foam Materials

## Liquid Crystal Elastomer (LCE) Lattice Foam



*It has been very challenging to dynamically characterize such soft lattice foam materials at high strain rates with a Kolsky compression bar, due to relatively large (long) specimen size and low wave speed.*

*Kolsky compression bar is also not able to be used to characterize the unloading stress-strain response for such soft materials, which is critical for energy dissipation calculation.*



Energy dissipation:

$$\begin{aligned}\Delta &= E_{\text{loading}} - E_{\text{unloading}} \\ &= \int_{\text{loading}} \sigma d\varepsilon - \int_{\text{unloading}} \sigma d\varepsilon\end{aligned}$$

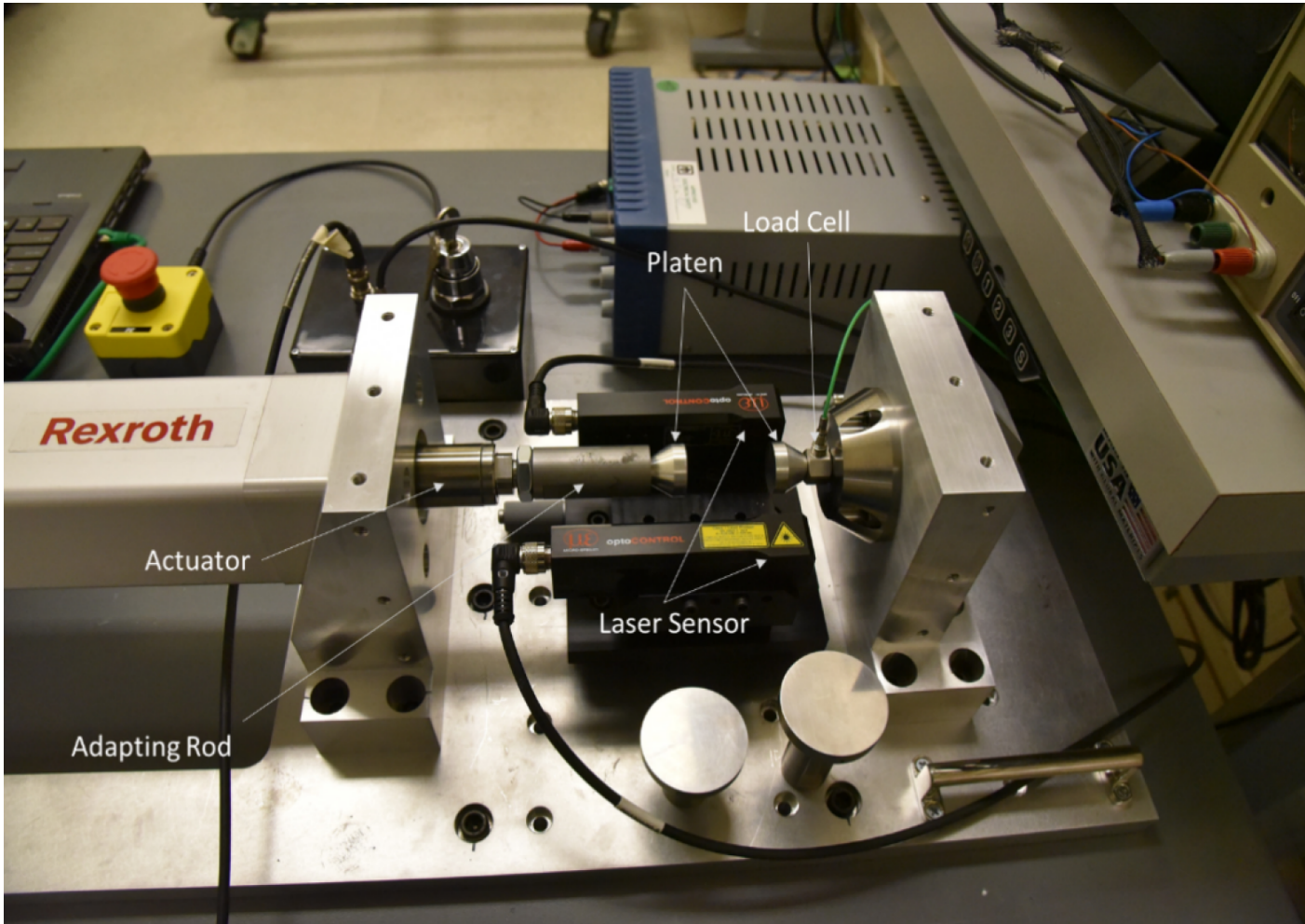
Energy dissipation ratio:

$$\delta = \frac{\Delta}{E_{\text{loading}}} = 1 - \frac{\int_{\text{unloading}} \sigma d\varepsilon}{\int_{\text{loading}} \sigma d\varepsilon}$$





# Bench-top Intermediate-Strain-Rate Test Apparatus



Rexroth® high speed electromechanical actuator

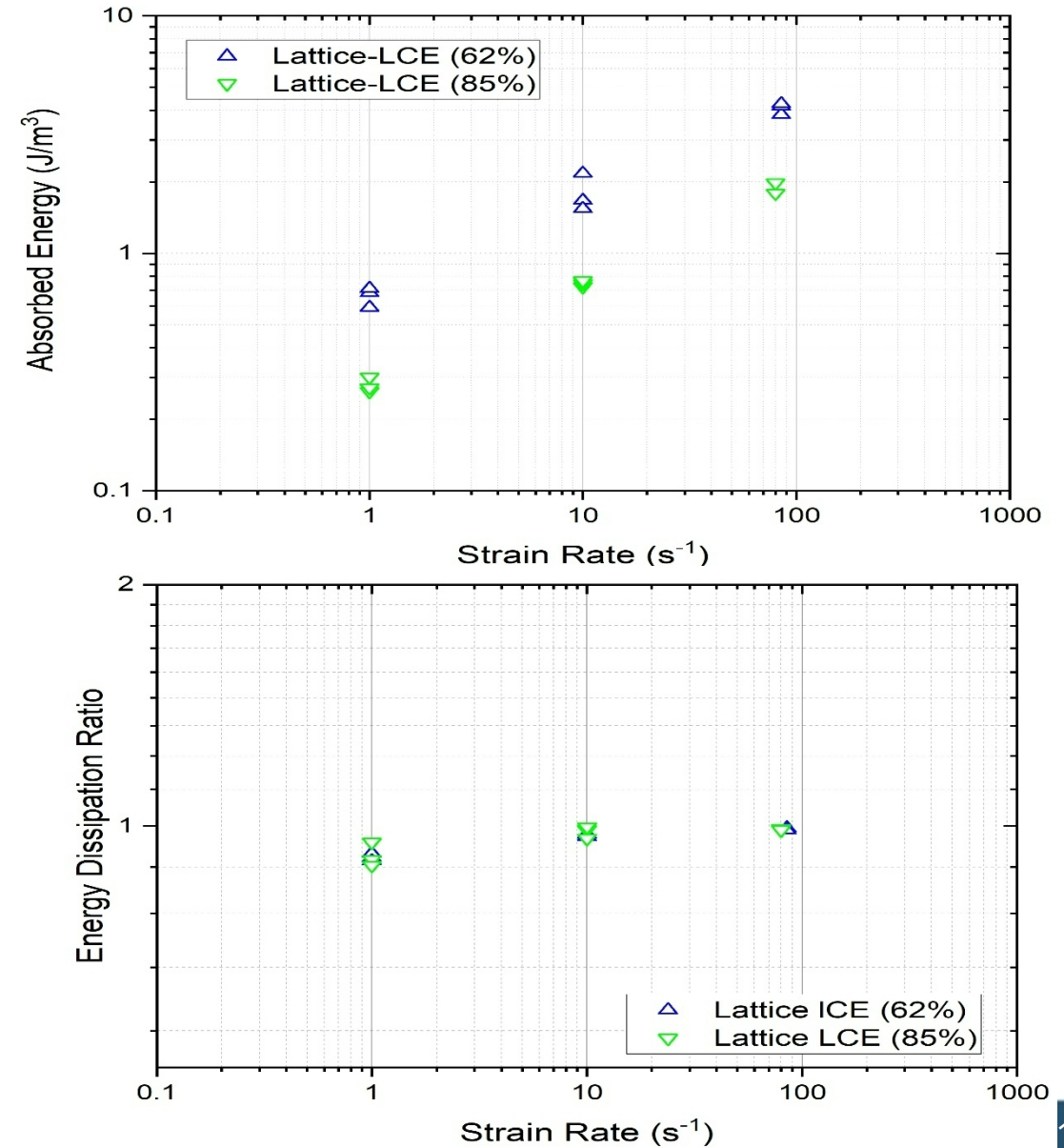
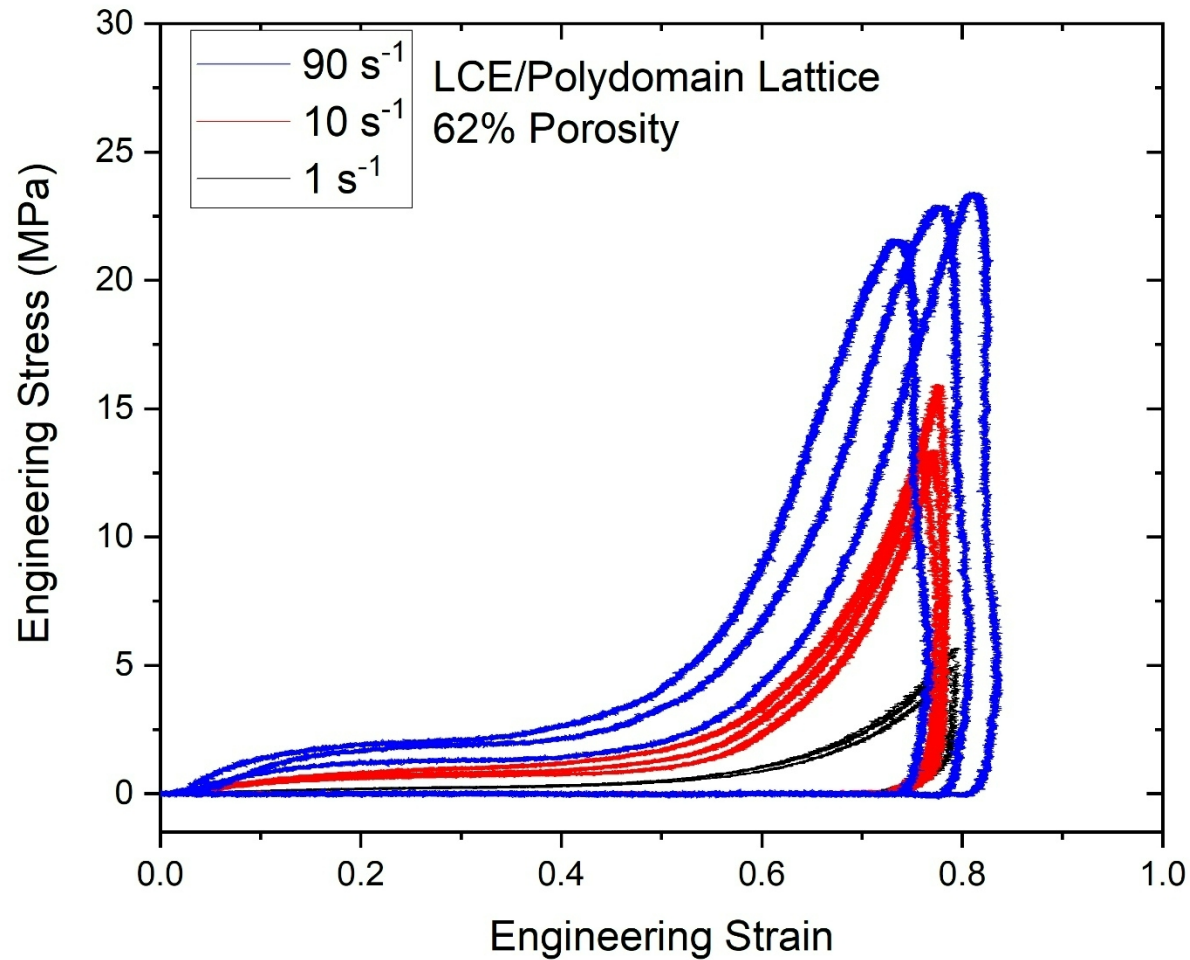
- Maximum impact velocity:  $\sim 1.9$  m/s
- Maximum travel distance: 6" ( $\sim 150$  mm)
- Maximum acceleration:  $\sim 400$  m/s<sup>2</sup>
- Load capacity: 3000 lbs ( $\sim 13300$  N)



For a 10 mm (diameter) by 5 mm (thickness) specimen,

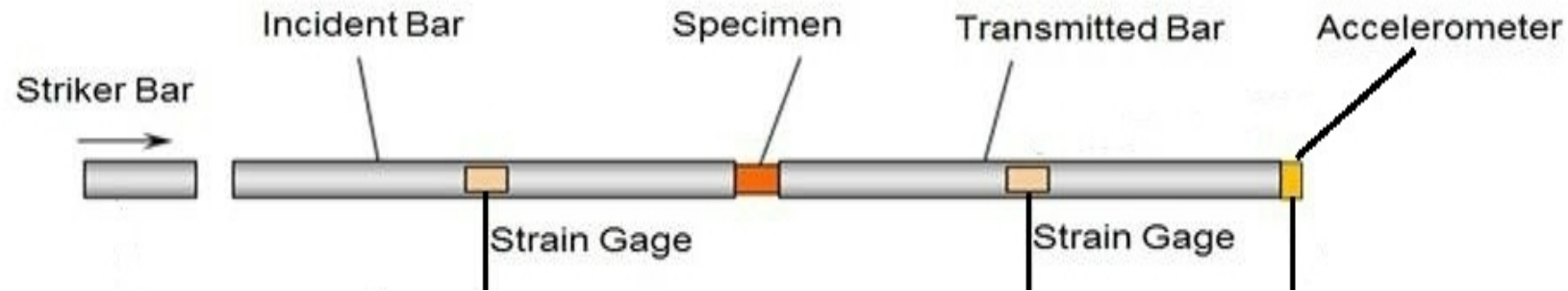
- Maximum stress:  $\sim 170$  MPa
- Maximum strain rate:  $\sim 380$  s<sup>-1</sup>

# Loading-Unloading Stress-Strain Response at Intermediate Rates





# Shock Mitigation Analyses with a Kolsky Compression Bar (Time Domain)



Incident Energy

$$E_i(t) = A_0 C_0 E_0 \int_0^t \varepsilon_i(t)^2 dt$$

Energy Dissipation (Absorbed Energy)

Reflected Energy

$$E_r(t) = A_0 C_0 E_0 \int_0^t \varepsilon_r(t)^2 dt$$

$$\Delta E(t) = E_{input}(t) - E_{output}(t) = A_0 C_0 E_0 \int_0^t [\varepsilon_i^2(t) - \varepsilon_r^2(t) - \varepsilon_t^2(t)] dt$$

Energy Dissipation Ratio

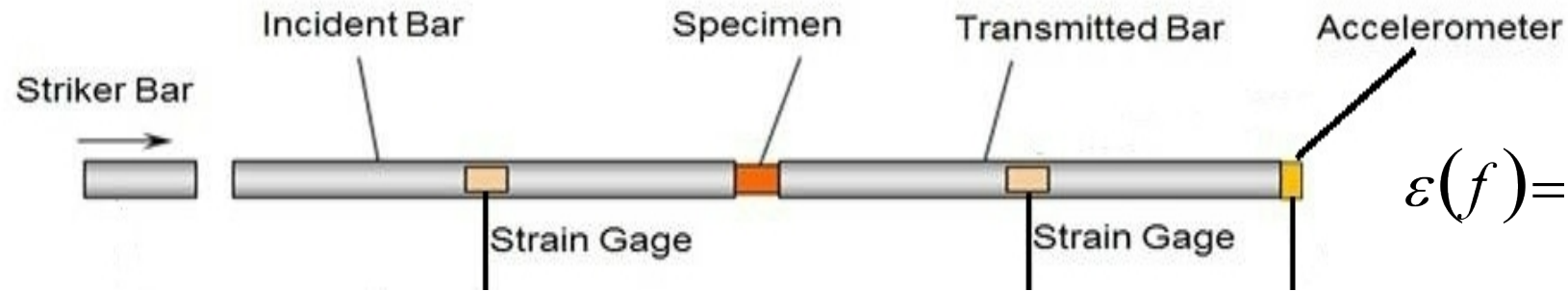
Transmitted Energy

$$E_t(t) = A_0 C_0 E_0 \int_0^t \varepsilon_t(t)^2 dt$$

$$\delta(t) = \frac{\Delta E(t)}{E_{input}(t)}$$



# Shock Mitigation Analyses with a Kolsky Compression Bar (Frequency Domain)



$$\varepsilon(f) = B(f)e^{-j(2\pi f + \phi)}$$

Incident Energy Spectrum Density

$$S_i(f) = A_0 C_0 E_0 |B_i(f)|^2$$

Energy Dissipation Ratio

Reflected Energy Spectrum Density

$$S_r(f) = A_0 C_0 E_0 |B_r(f)|^2$$

$$\delta(f) = \frac{\Delta(f)}{E_i(f) - E_r(f)} = 1 - \frac{|B_t(f)|^2}{|B_i(f)|^2 - |B_r(f)|^2}$$

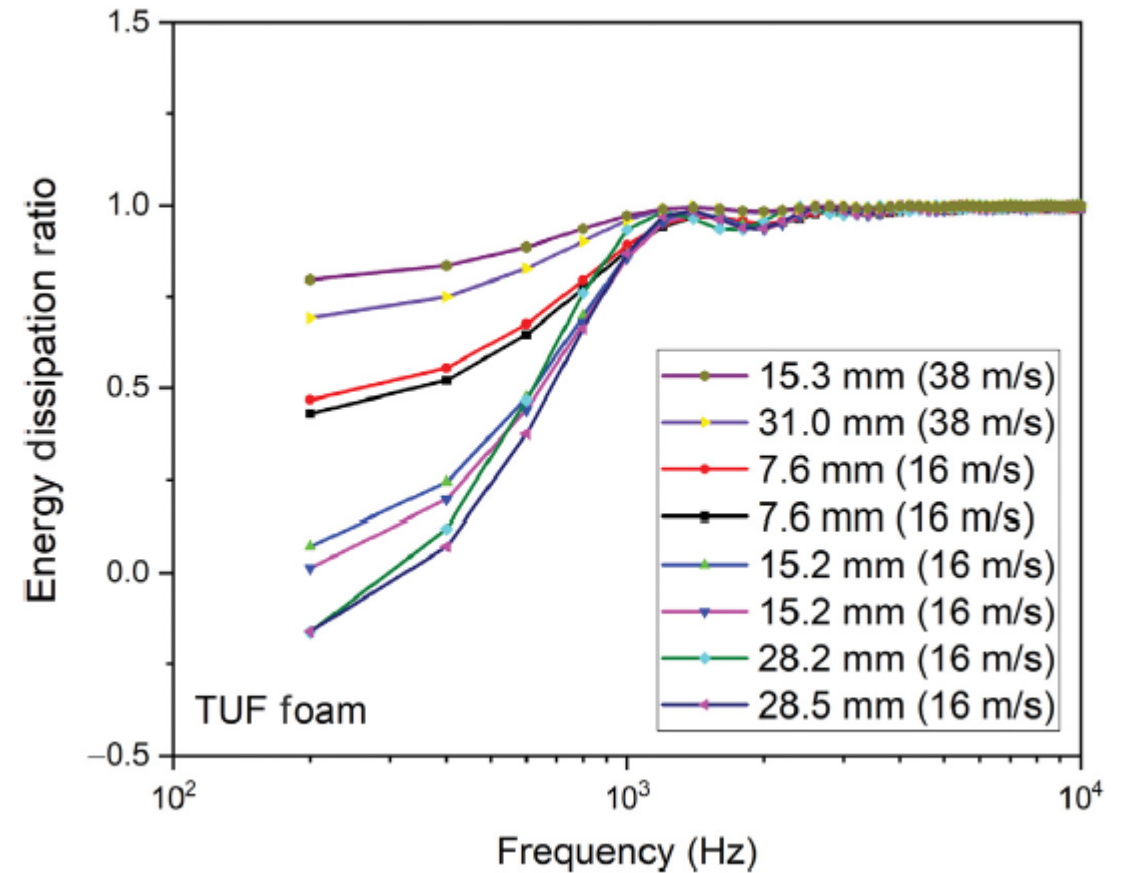
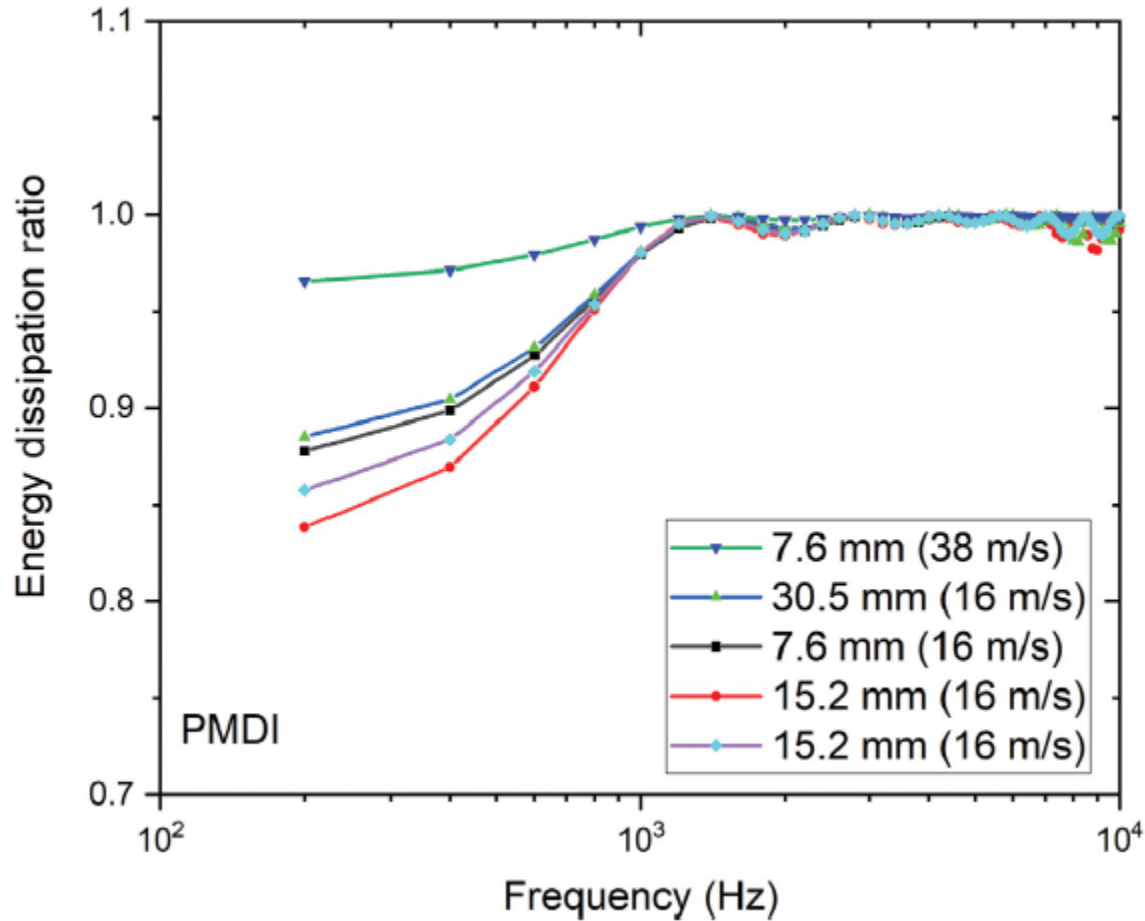
Transmitted Energy Spectrum Density

$$S_t(f) = A_0 C_0 E_0 |B_t(f)|^2$$





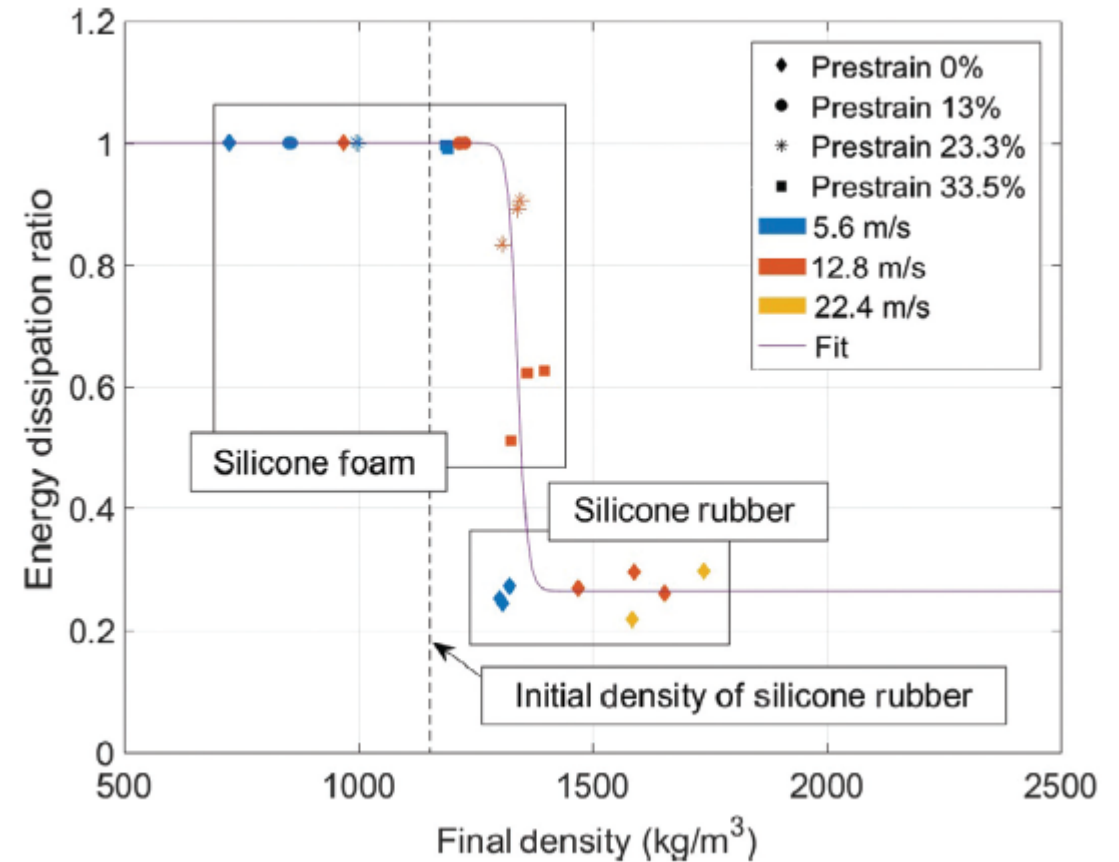
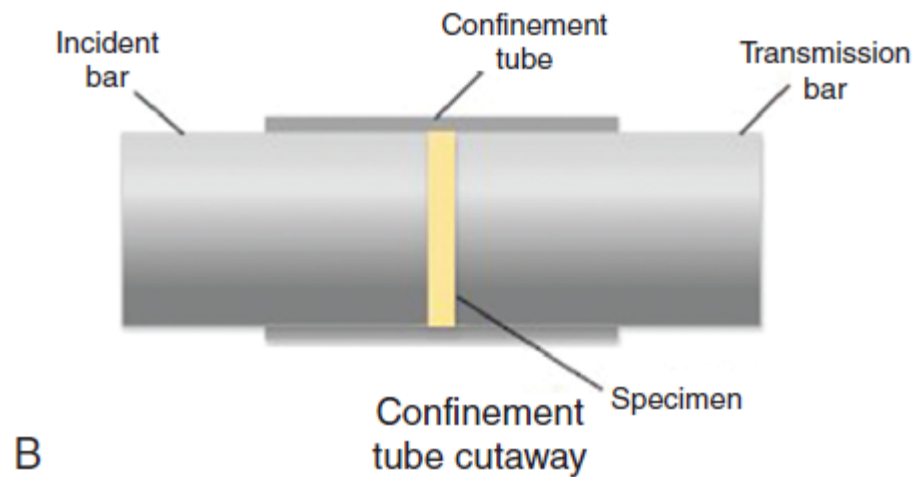
# Frequency-dependent Energy Dissipation of Elastic-Plastic Foams







# Energy Dissipation Characteristic of Confined Silicone Foam





## Summary

***Goal: maximize shock mitigation, optimize material and structural design***

- Material properties need to be fully characterized
  - At different strain rates
  - At different temperatures
  - At different stress states
- Direct energy absorption and dissipation calculation from loading-unloading stress-strain curves
  - Dependent on strain, strain rate, temperature, stress state, etc.
- Structural response in terms of shock mitigation needs to be fully characterized
  - Impact crush response
  - Impact energy dissipation
    - In time domain
    - In frequency domain