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Modeling Quantum Tunneling in Terahertz Scanning Tunneling Microscopes

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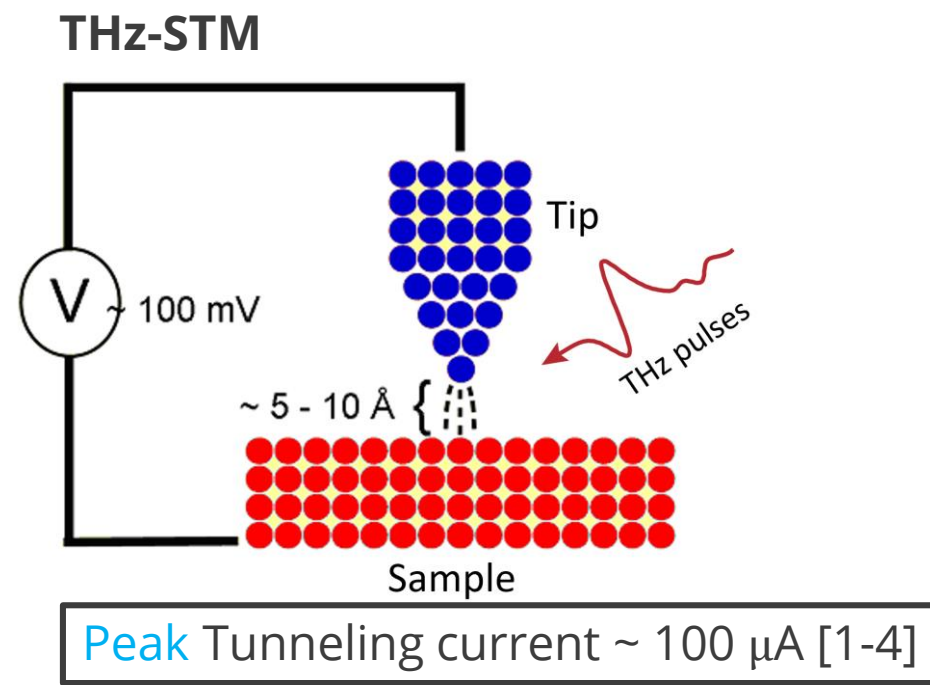
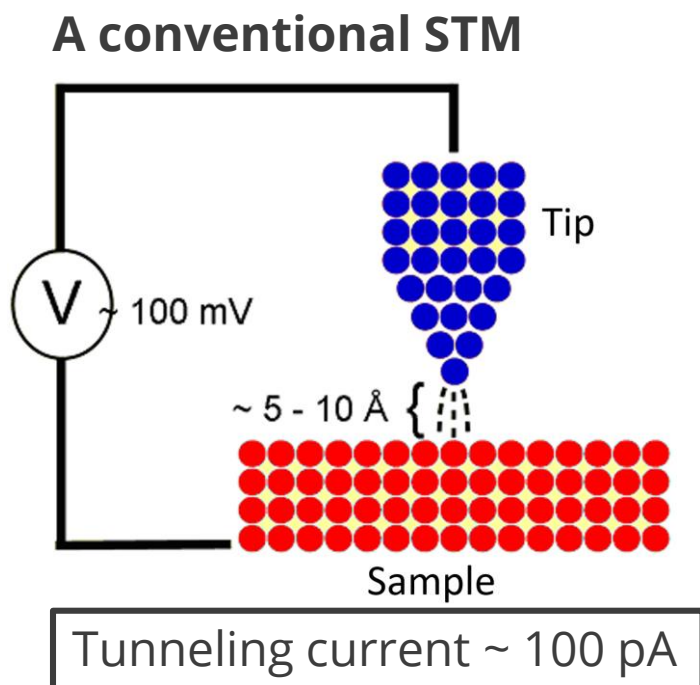
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Why Terahertz Scanning Tunneling Microscope (THz-STM)?



- To record the movement of a single molecule on its intrinsic timescale, STMs must have ultrafast temporal resolution and atomic spatial resolution – THz STM
- Peak THz voltage bias transients greater than 3 V across the STM junction can be achieved → field emission of subpicosecond tunnel currents with current densities exceeding 10^9 A/cm^2 .

[1] Cocker et al., **Nat. Photonics** 7, 620 (2013)

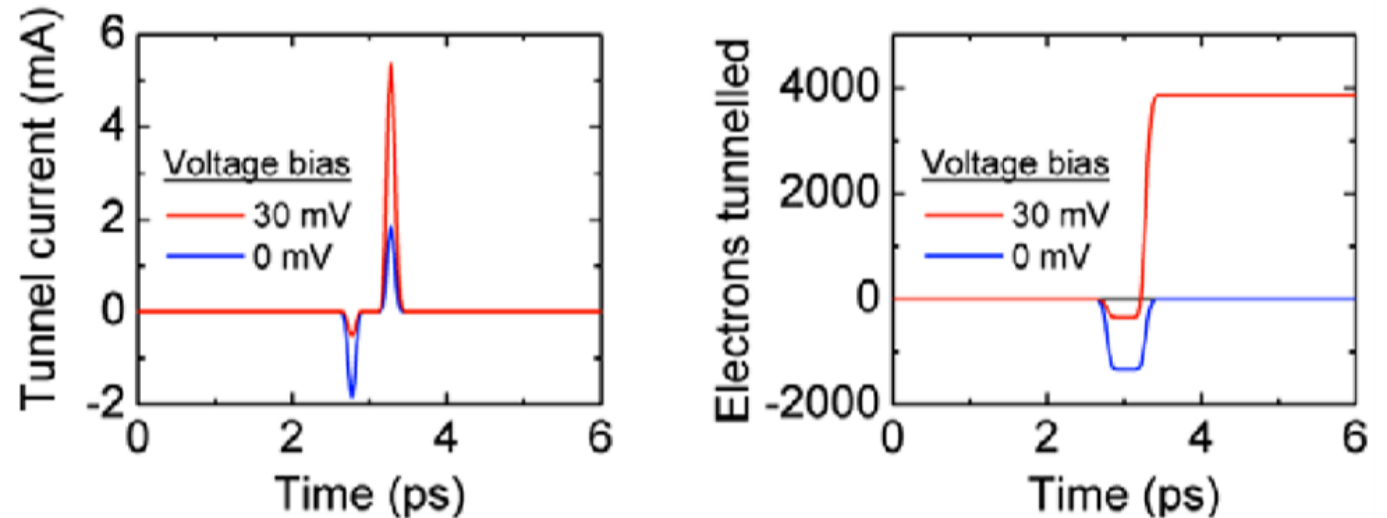
[3] Luo, Y. et al., **Phys. Rev. B** 102, 205417 (2020)

[2] Jelic, V. et al., **Nat. Phys.** 13, 591–598 (2017)

[4] Tachizaki, T., **APL Mater.** 9, 060903 (2021)

Quantum Tunneling at Tip-Sample Junction

- Nonlinear current-voltage behavior of the tunnel junction leads to rectified ultrafast current burst
- It is important to: **understand, improve, and control this rectification**



[1] Cocker et al., **Nat. Photonics** 7, 620 (2013)

- High tunneling voltage at tip-sample junction → Field Emission regime → Effects of **Exchange Correlation Potential** and **Space Charge Potential** become crucial
- Existing theoretical studies[1-3] use Simmons [4] & Bardeen theory of tunneling which ignore both
- We consider them in our model to study the scaling of tunneling current at THz-STMs for different bias, THz field, tip-height and material properties

Goal: Manipulation of electron transport at the tunnel junction

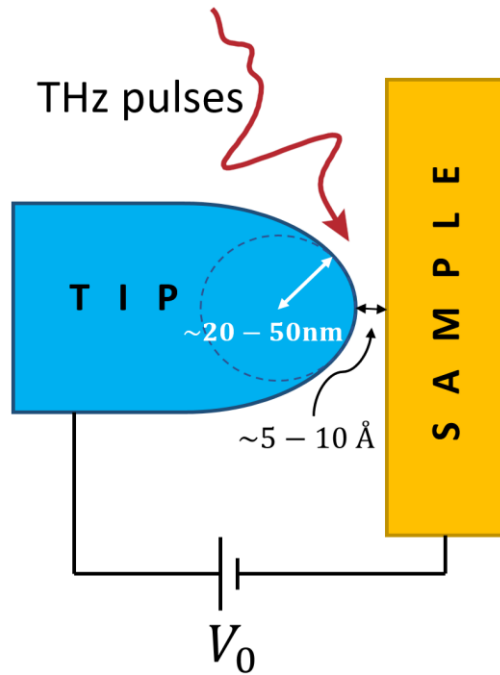
[2] Jelic, V. et al., **Nat. Phys.** 13, 591–598 (2017)

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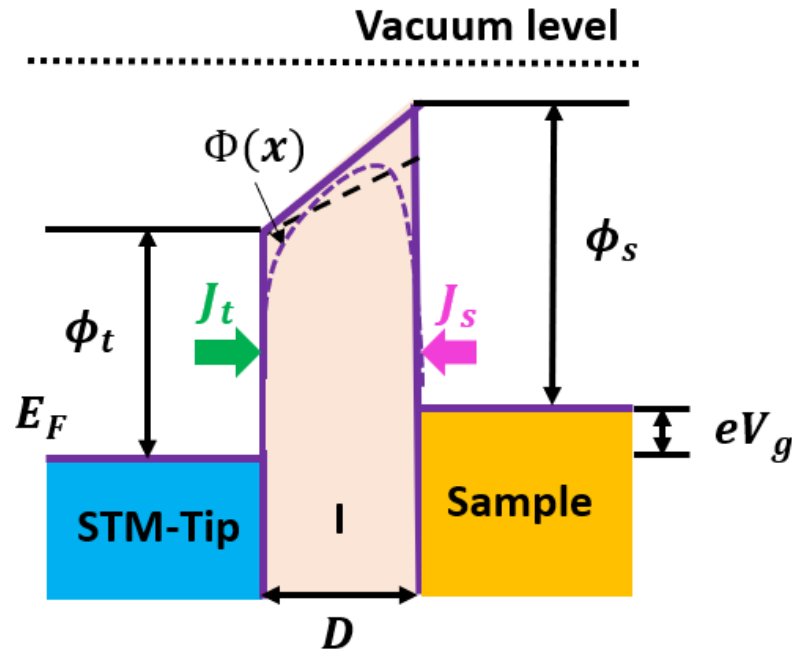
[4] J. G. Simmons, **J. Appl. Phys.** 34, 2581 (1963)

- Introduction
 - Potential barrier between tip and sample
 - Forward and reverse bias
- Self-consistent model formulation for a metal-insulator-metal junction
- Current-voltage characteristics
- Rectification of the tip-sample tunnel junction
 - Validation with experiment
 - For different time-dependent bias voltages
 - For different metal tips
 - For different tip heights
- Summary
- Future work

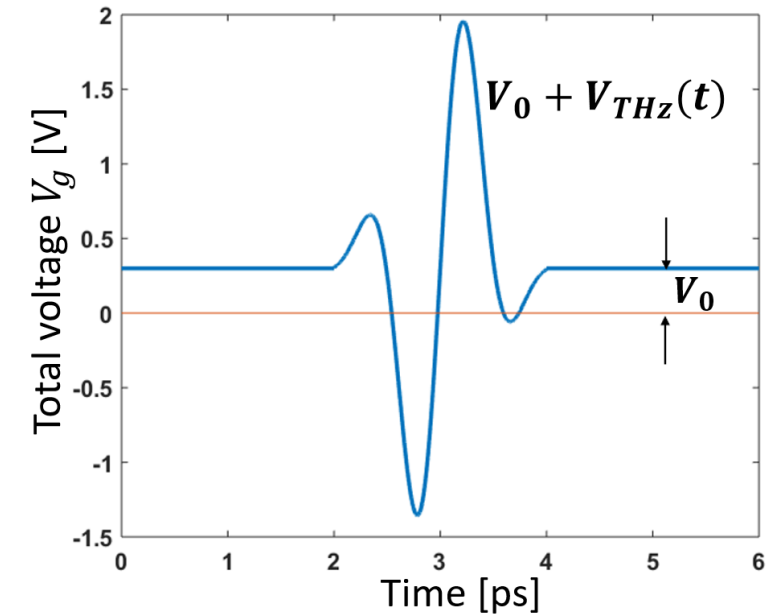
Terahertz Scanning Tunneling Microscope (THz-STM)



- THz pulse is coupled into the STM junction
- Transient tunnel currents between the tip and the sample



- The potential profile at tip-sample junction
 - $\phi_{t/s} = W_{t/s} - X$, $W_{t/s}$ = work function of tip/sample, X = electron affinity of the insulator
 - $J_{t/s}$ = electron current densities emitted from the tip/sample

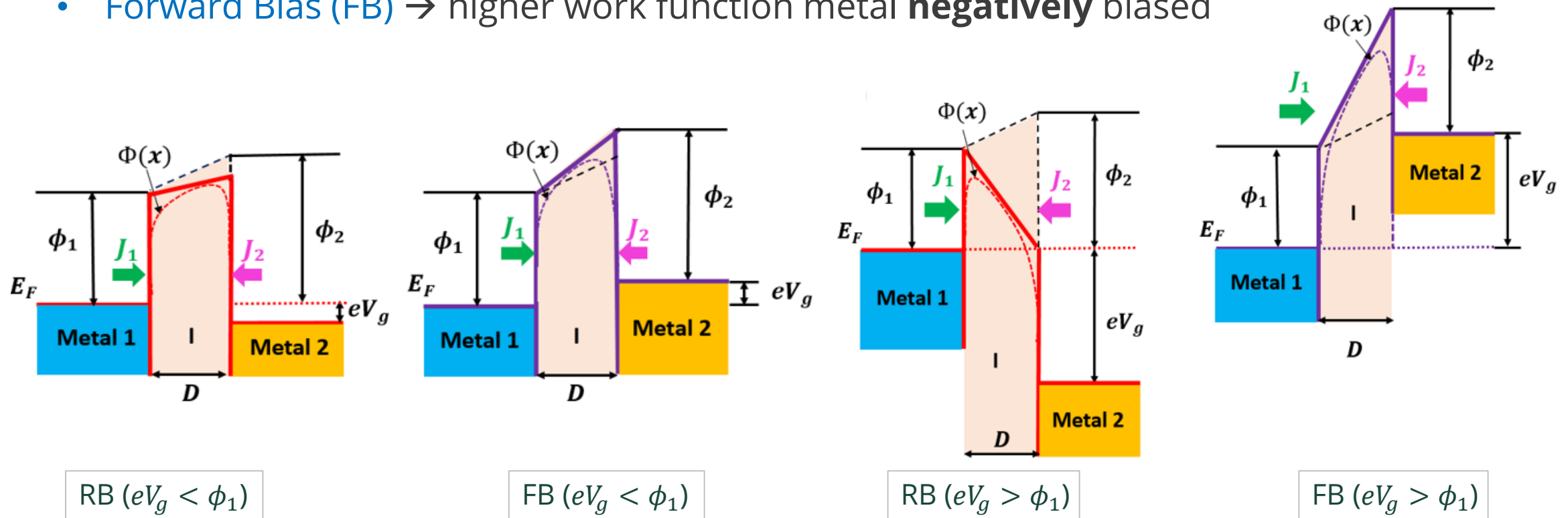


Total voltage applied to the tip-sample junction

Forward and Reverse Bias in dissimilar metal-insulator-metal

Due to the inherent work-function difference between the metal electrodes, current transport is polarity dependent in dissimilar metal-insulator-metal (MIM)

- Reverse Bias (RB) \rightarrow higher work function metal **positively** biased
- Forward Bias (FB) \rightarrow higher work function metal **negatively** biased



Potential Barrier at Tip-Sample Junction

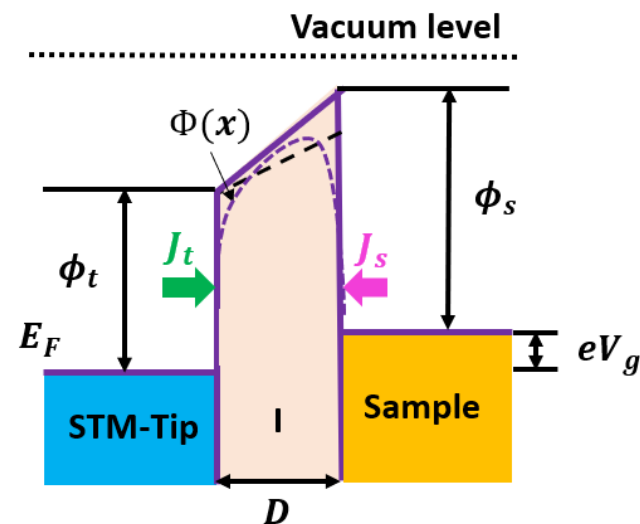


Image charges build up in the metal electrode as carriers approach the metal-insulator interface. The potential associated with these charges reduces the effective barrier height.

Due to electron interaction in a quantum system

Exchange energy is released when two or more electrons with same spin exchange their position.

Correlation energy is a measure of how much the movement of an electron is influenced by the other electrons.

$$\Phi(x) = E_F + \Phi_w(x) + \Phi_{image}(x) + eV(x) + \Phi_{xc}(x)$$

$$\Phi_w(x) = \phi_t + (\phi_s - \phi_t)x/D$$

J. G. Simmons, *J. Appl. Phys.*, 1963.

$$eV(x) = eV_g x/D + eV_{sc}(x)$$

Due to the cloud of free electrons in the insulator. It slows the carriers down.

P. Zhang, **Sci. Rep.** 5, 9826 (2015)

S. Banerjee and P. Zhang, **AIP Adv.** 9, 085302 (2019)

Generalized Self-Consistent Tunneling Model

Symbols have their usual meaning , or, as defined earlier

- The tunneling current density $J_{net} = |J_1 - J_2|$

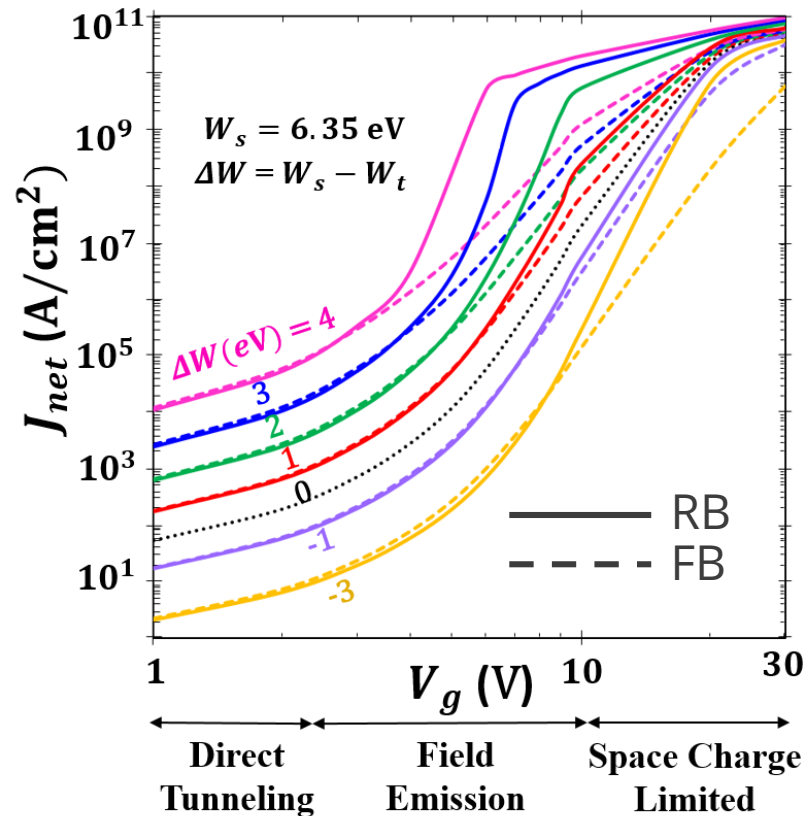
$$J_1 = \int_{-\infty}^{\infty} N_1(E_x) D(E_x) dE_x \quad , \quad J_2 = \int_{-\infty}^{\infty} N_2(E_x) D(E_x) dE_x$$

- Transmission probability ,

$$D(E_x) = \exp \left[-\frac{2}{\hbar} \int_{x_1}^{x_2} \sqrt{2m[\Phi(x) - E_x]} dx \right] \quad (\text{WKB approximation})$$

$$\left. \begin{aligned} N_1(E_x) &= \frac{m_e k_B T}{2\pi^2 \hbar^3} \ln(1 + e^{-(E_x - E_F)/k_B T}) \\ N_2(E_x) &= \frac{m_e k_B T}{2\pi^2 \hbar^3} \ln(1 + e^{-(E_x + eV - E_F)/k_B T}) \end{aligned} \right\} \quad (\text{free-electron theory of metal})$$

J-V Characteristic of a Metal-Insulator-Metal Junction [1]



In field emission regime, the asymmetry between FB and RB currents increases significantly as the work function difference $|\Delta W|$ increases.

Low voltage: Direct tunneling regime → FB current > RB current

High voltage: Field emission regime → RB current \gg FB current – Prominent asymmetry

Very high voltage: Space charge limited regime → Quantum Child-Langmuir limit [2]

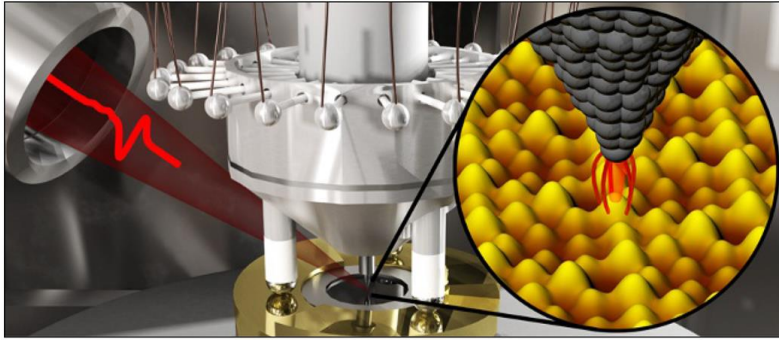
Assumptions

- This DC model can be applied to the tip-sample junction of a THz-STM. The electron **tunneling time is much smaller** than the timeperiod (in the scale of picosecond) of the THz field [1-3].
- The operating media is **ultrahigh vacuum** with relative permittivity $\epsilon_r = 1$ and electron affinity $X = 0$
- Although the tip is round-shaped, the majority of the tunneling current flows through the region near the tip-apex. We modeled this **tip-apex** as a **square** for simplicity.
- We assume the THz bias voltage **$V_{THz}(t)$ is readily available** at the junction. We do not examine the generation, propagation, coupling of the THz pulses to the STM tip.

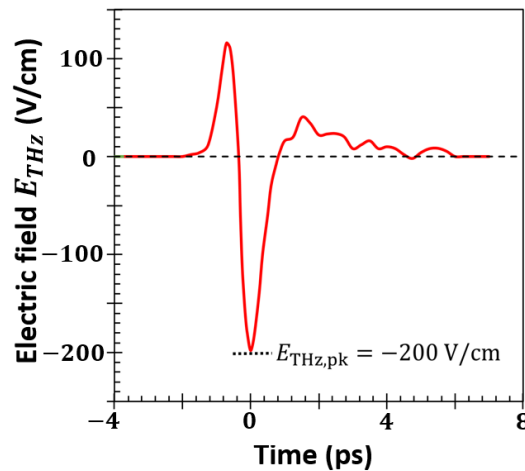
Rectification of the Tunneling Junction Depends on:

- D.C. bias voltage (polarity, amplitude)
- Incident THz field (polarity, shape, peak amplitude)
- Work functions of STM tip and sample (especially their difference ΔW)
- Tip-sample separation
- Operating media

Validation

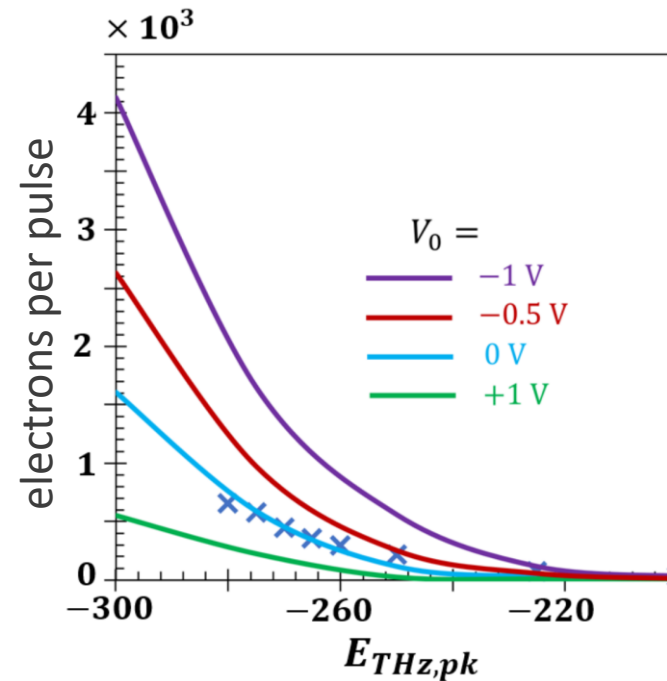


Experimental set up from [1]



THz electric field from [1]

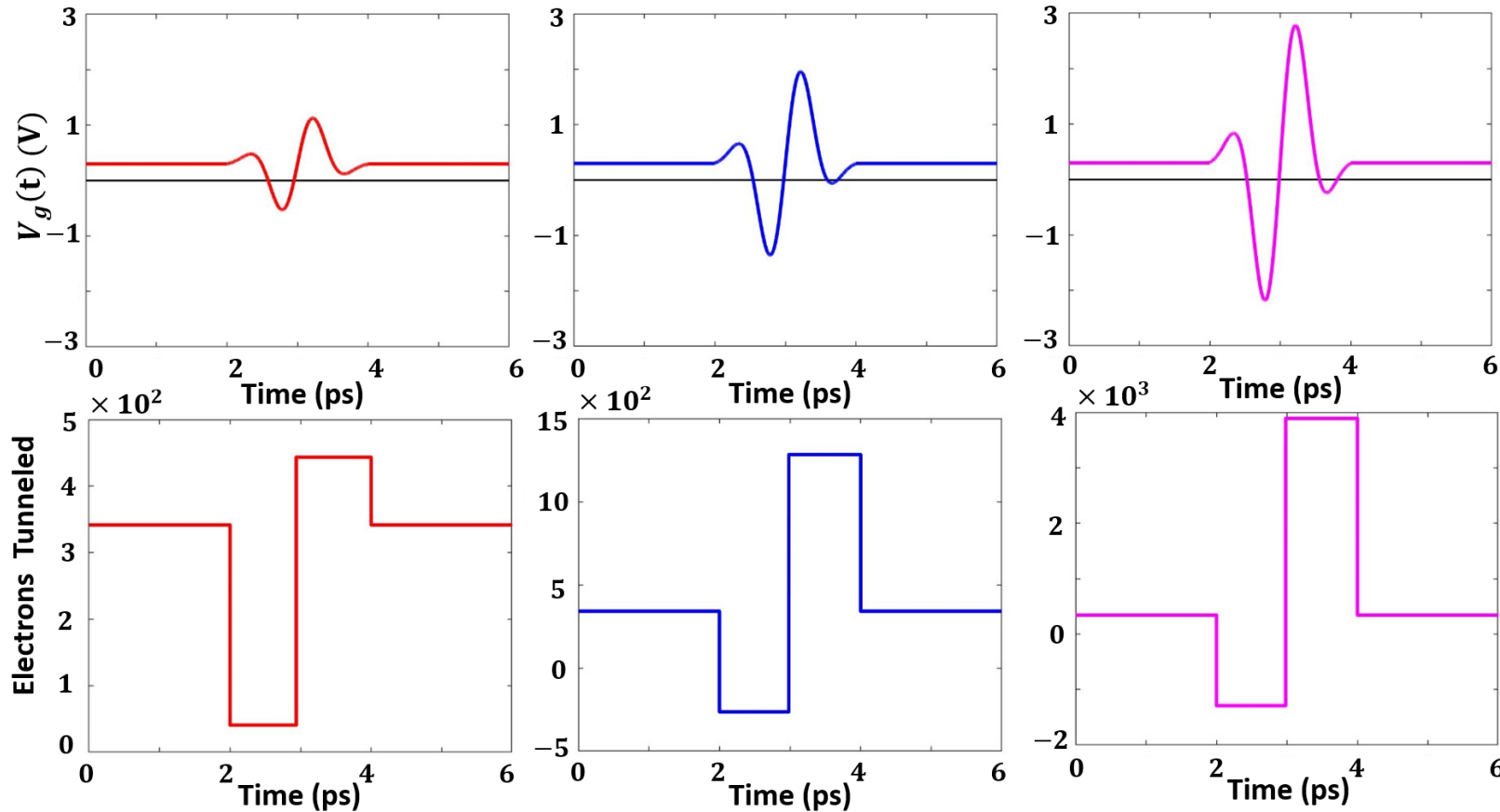
Number of electrons per pulse $N = \int_{t_1}^{t_2} I(t) dt / e$
 $I(t)$ = time dependent tunneling current through the STM tip
 $t_2 - t_1$ = pulse duration, e = electron charge



Crossed symbols – experiment [1]
 Solid Lines – our theory [2]

Highly non-linear I-V characteristics leads to asymmetry in rectification

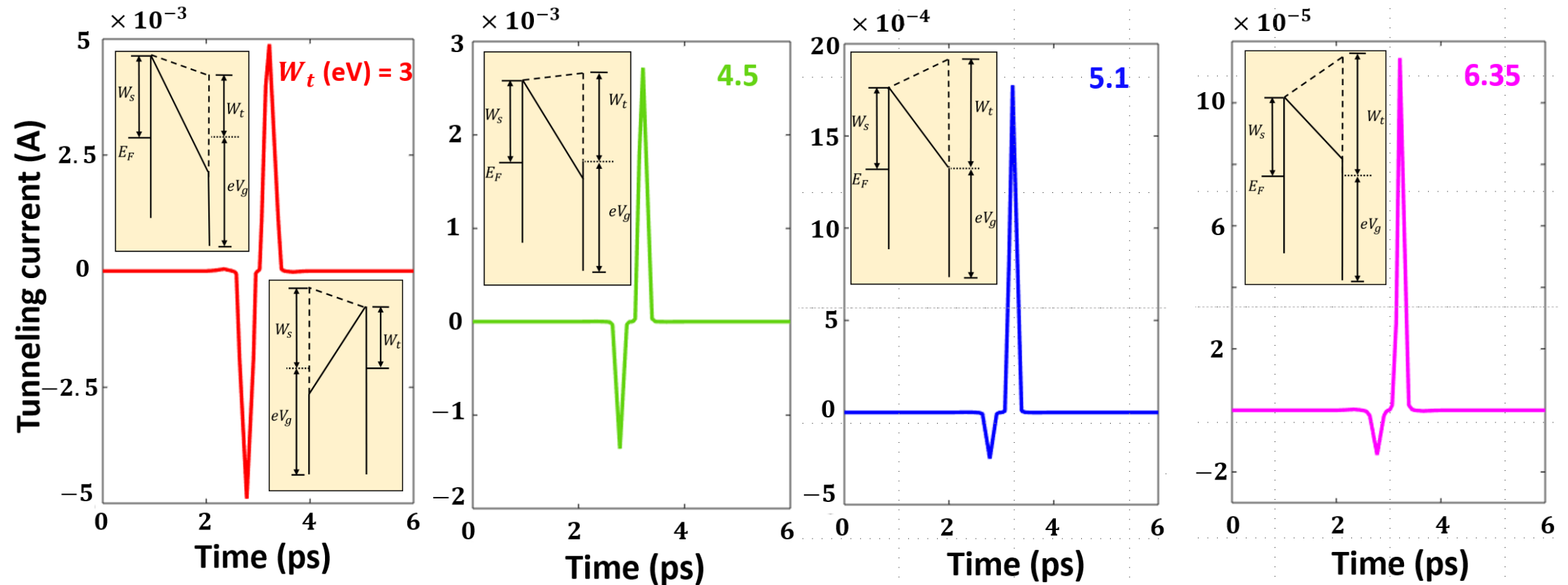
Effects of time-dependent bias voltage $V_g(t) = V_0 + V_{THz}(t)$



$$\begin{aligned}
 V_0 &= 0.3 \text{ V} \\
 W_s &= W_t = 4.5 \text{ eV} \\
 \text{Tip height} &= 0.5 \text{ nm} \\
 \text{Electrons tunneled} &= \int_{t_1}^{t_2} I(t) dt / e
 \end{aligned}$$

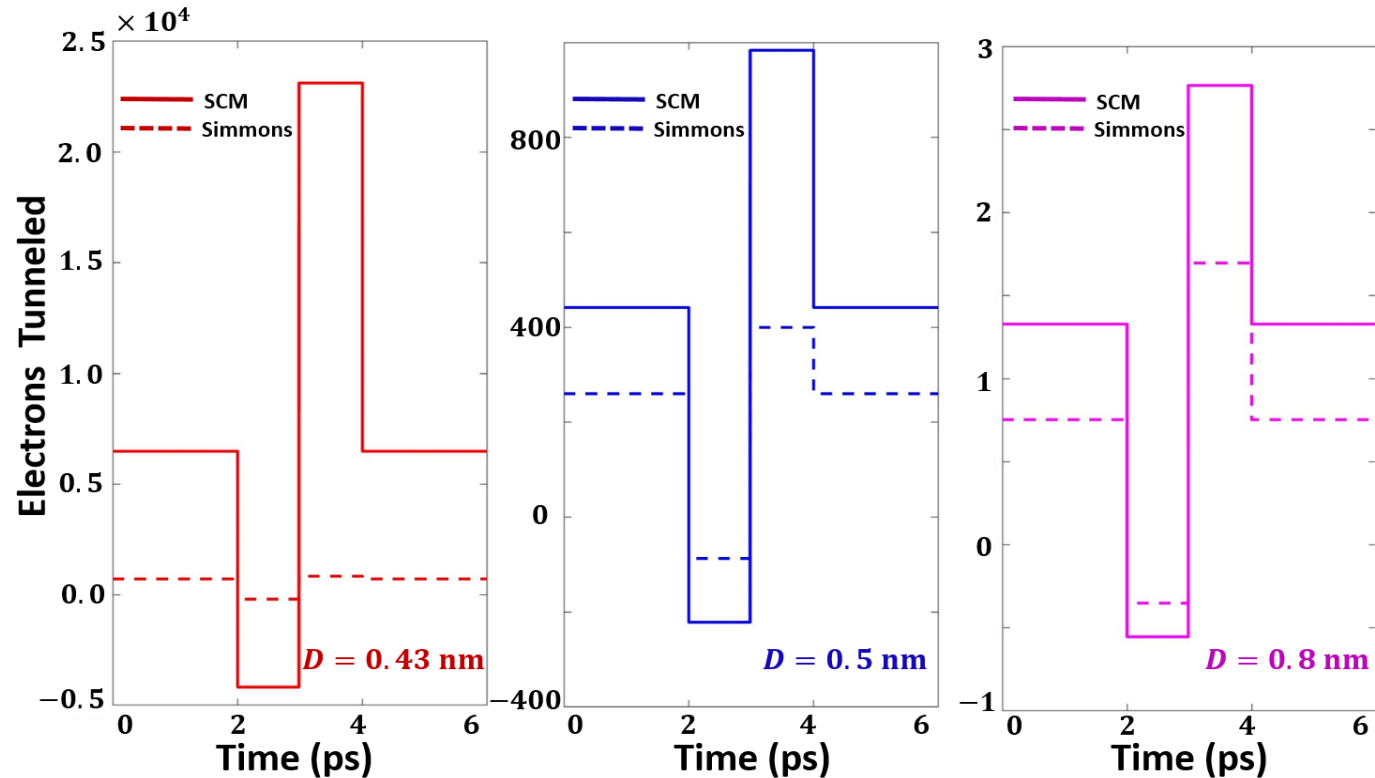
The rectified electrons per pulse in a THz-STM can be manipulated by varying the bias voltage (polarity, amplitude) and THz field (polarity, shape, peak THz field $E_{THz,pk}$)

Effects of Different Tip Metals for Al ($W_s = 4.08\text{eV}$) Sample



- Work function difference between tip and sample \rightarrow Asymmetry \rightarrow **Forward and Reverse Bias**
- In high voltage regime, current is more when lower work function electrode is negatively biased
- Asymmetry increases with the work function difference ΔW

Effects of different tip-heights D [1] and Comparison with the Simmons Formula



$$V_0 = 0.3 \text{ V}$$

$$W_s = W_t = 4.5 \text{ eV}$$

$$\text{Electrons tunneled} = \int_{t_1}^{t_2} I(t) dt / e$$

- For same THz field, the number of tunneled electrons increases with decreasing tip height.
- The difference between Self Consistent Model and Simmons formula [2] increases with decreasing tip height since the **effects of exchange correlation potential** increases as tip height decreases [3].

[1] S. Banerjee, and P. Zhang, **Phys. Rev. Applied** 18, 024011 (2022)

[2] J. G. Simmons, **J. Appl. Phys.** 34, 2581 (1963)

[3] Ang et al., **Phys. Rev. Lett.** 91, 208303 (2003)

Summary

Self-consistent quantum model [1,2,3]

- includes exchange correlation potential & space charge potential
- DC but can be applied here since electron tunneling time \ll THz timeperiod [4]

Field emission voltage regime

- effects of exchange correlation potential are important
- existing models (Simmons, Bardeen) are unreliable

Asymmetry

- different work-functions of tip and sample
- polarity dependent tunneling current
- reverse bias and forward bias

Rectification depends on:

- d.c. bias voltage (polarity, amplitude)
- incident THz field (polarity, shape, $E_{THz,pk}$)
- work functions of STM tip and sample (especially their difference ΔW)
- tip-sample separation.



Manipulation of electron transport

- better rectification can be obtained by enhancing the asymmetry
- asymmetrical THz field, reverse bias, larger workfunction difference improves rectification

[1] P. Zhang, **Sci. Rep.** 5, 9826 (2015)

[2] S. Banerjee and P. Zhang, **AIP Adv.** 9, 085302 (2019)

[3] S. Banerjee, and P. Zhang, **Phys. Rev. Applied** 18, 024011 (2022)

[4] G. Nimtz, and H. Aichmann, **Z. Für Naturforschung A** 76, 295–297 (2021)

Tunneling Probability

- although widely used, WKB approximation need to be examined
- time-independent Schrödinger equation may be solved numerically to get a more accurate transmission probability.

Tip-sample geometry

- we considered the tip and sample surface to be flat and the problem is one-dimensional
- the effects of their geometry may be included in future works

Time dependence

- time-dependent analysis of the electron wave function might be performed
- results might be compared to define regimes where the proposed simple DC model is applicable

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Thank you!