



Sandia  
National  
Laboratories

# A Simplified Finite Element Model for Design of a Resonant Plate



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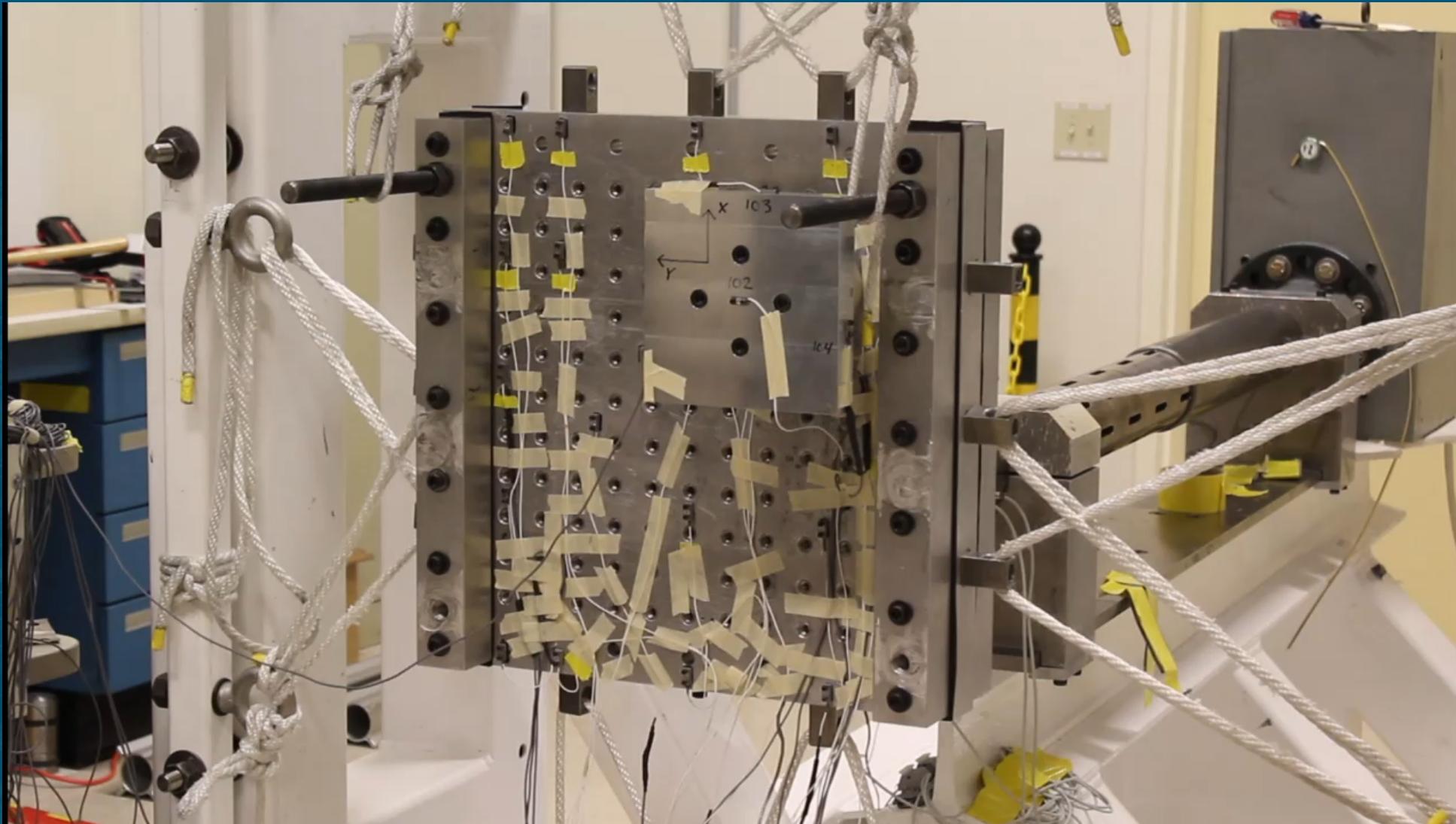


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Create a **model for design** that is as **simple** as it can be and no more complicated than it must be to provide **reasonably accurate results**.

# Resonant Plate Pyroshock Testing



# How These Presentations are Laid Out



## Talk 1:

- Model Overviews & Modal Verification
  - Problem Description
  - Major Simplifications
  - Model for Bare Plate
  - Model for Plate with Damping Bars

## Talk 2:

- Lessons Learned during Model Development

## Talk 3:

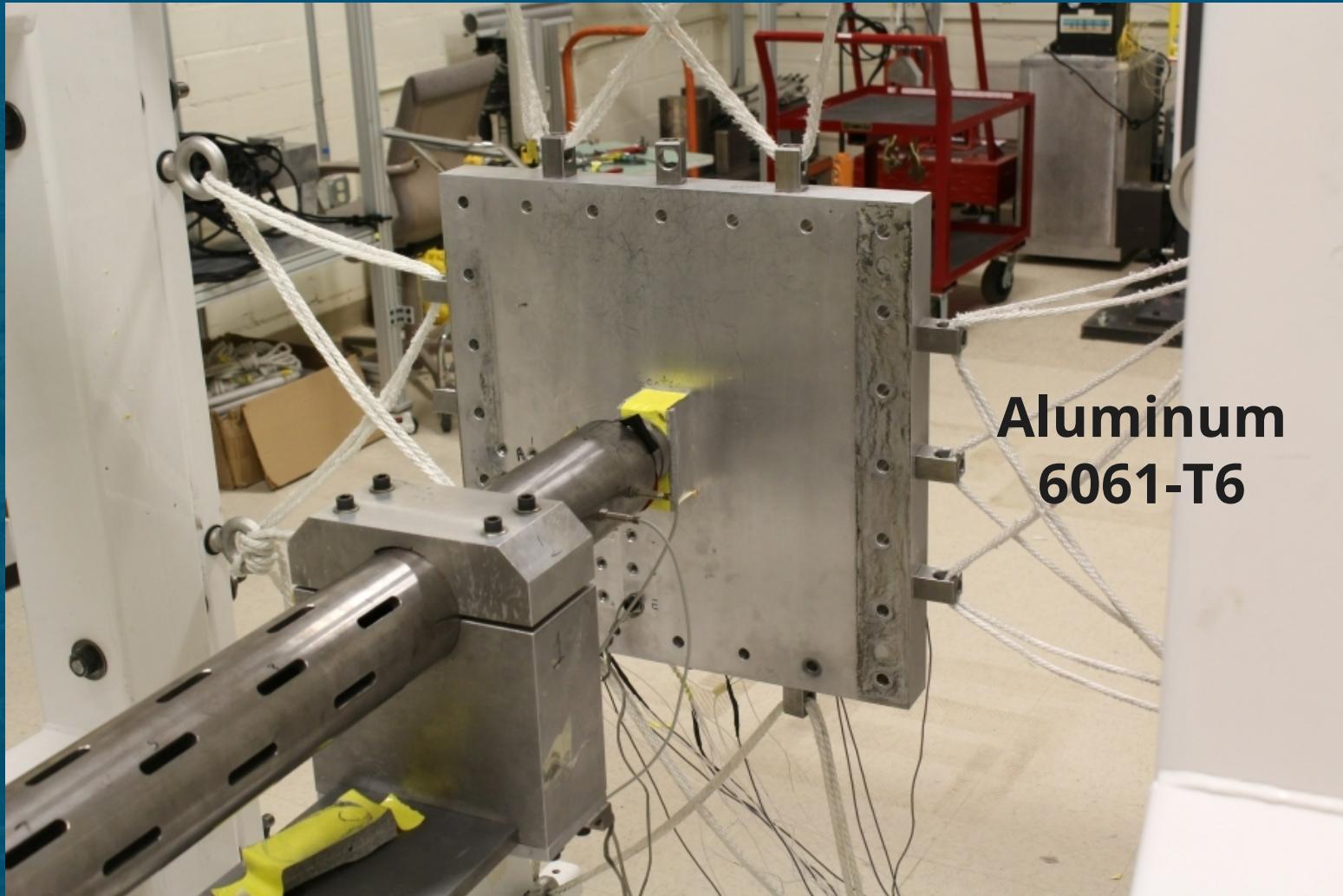
- Shock Verification & Application to Other Plates



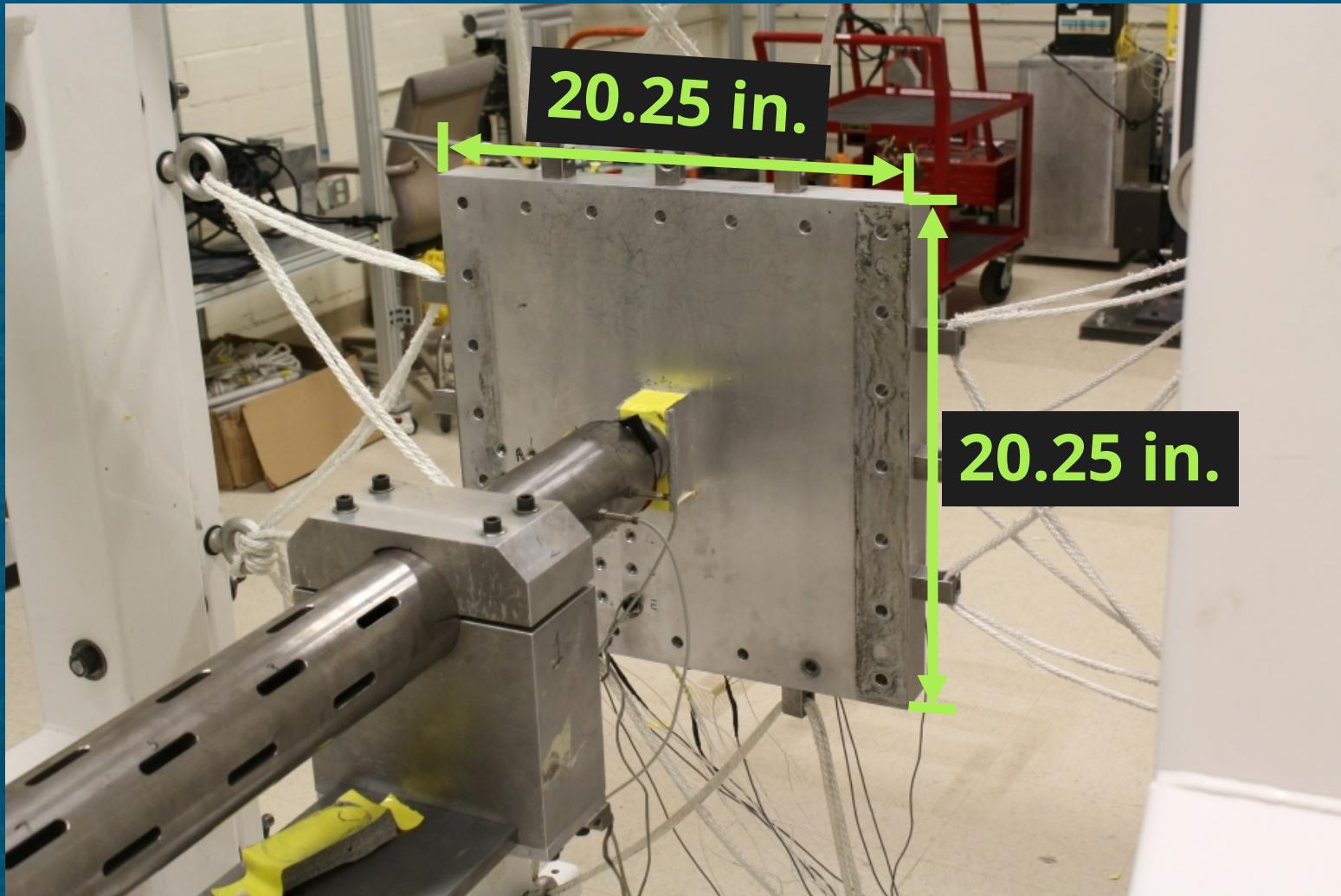
# Problem Description

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# 1kHz Resonant Plate



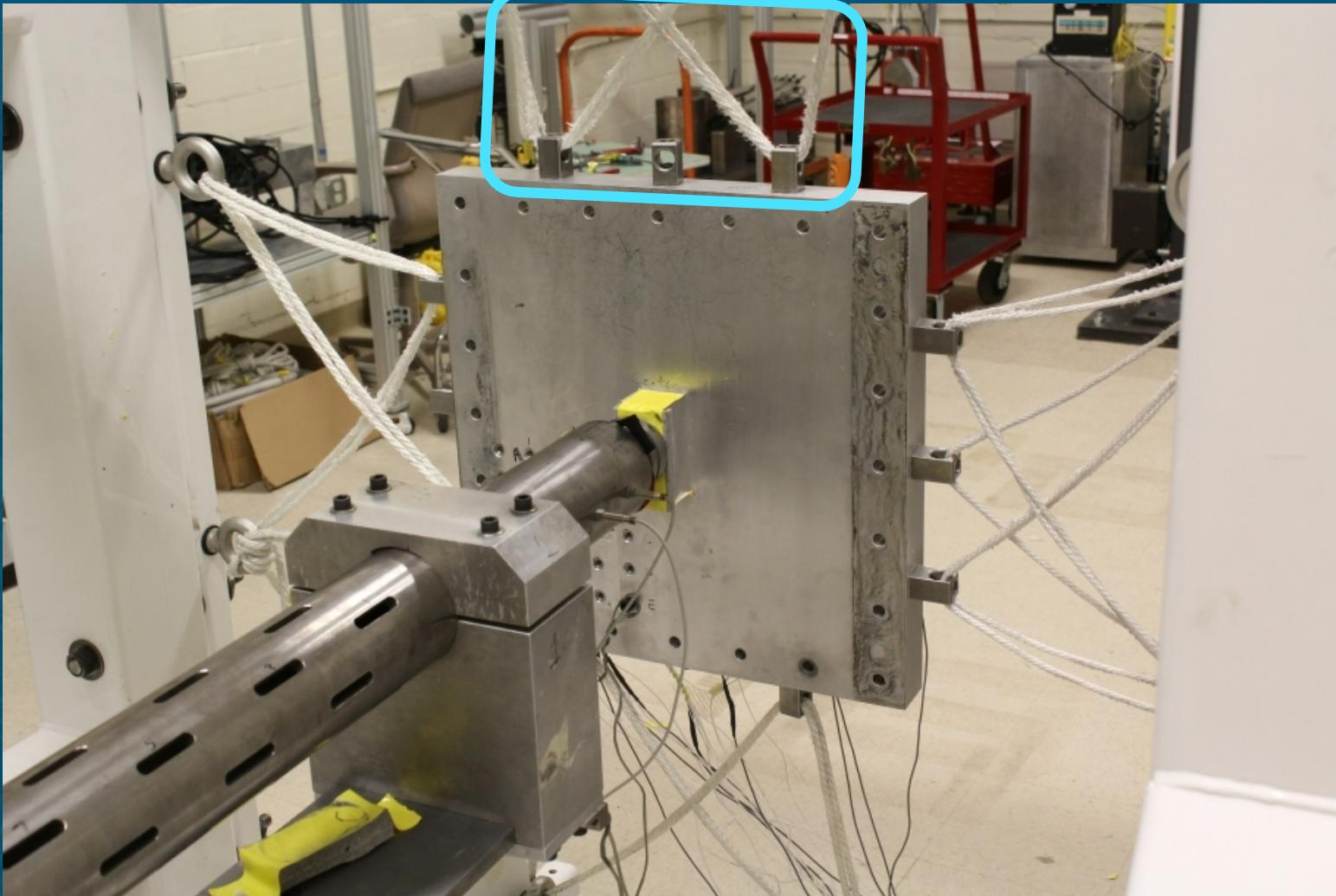
# 1kHz Resonant Plate



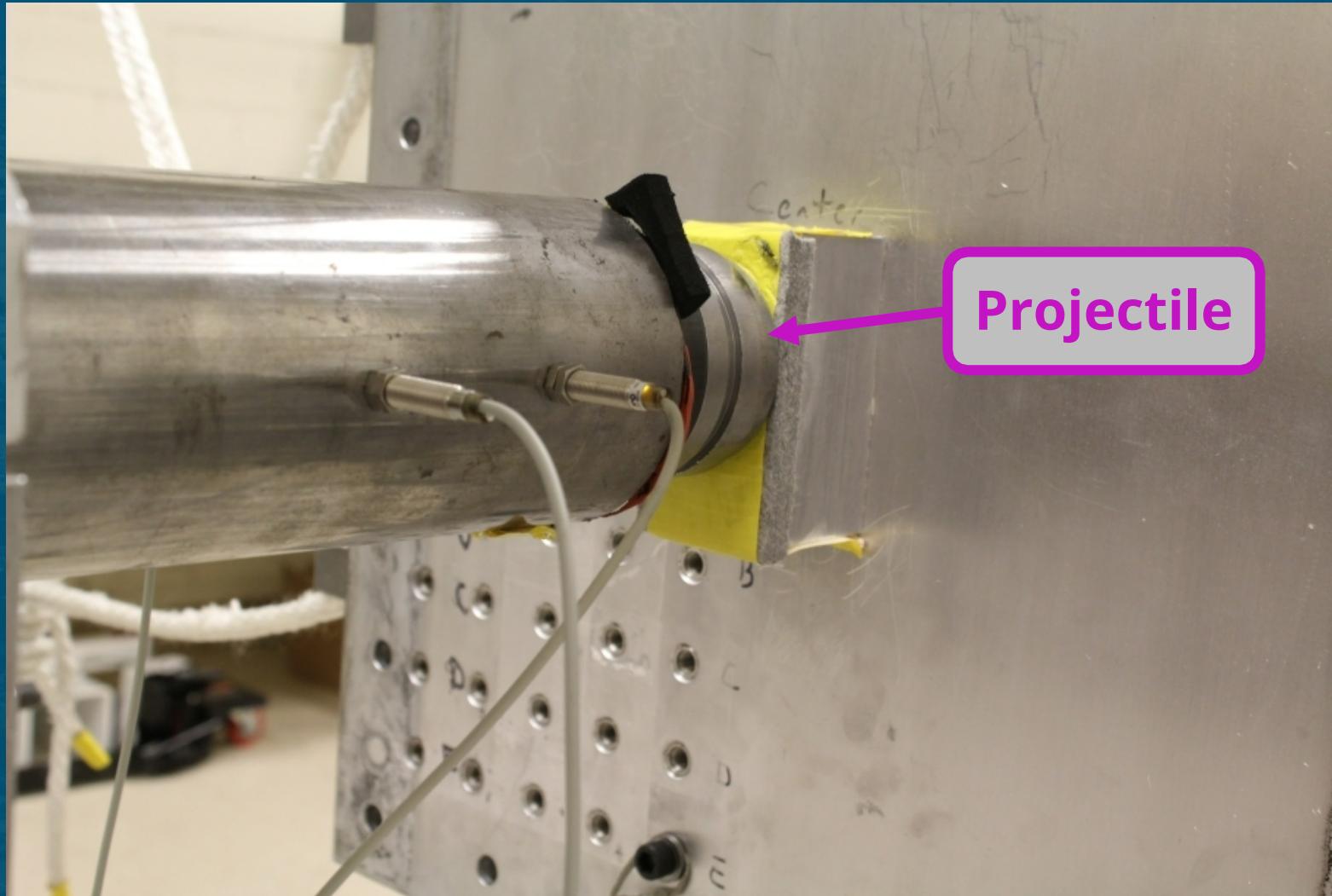
# 1kHz Resonant Plate



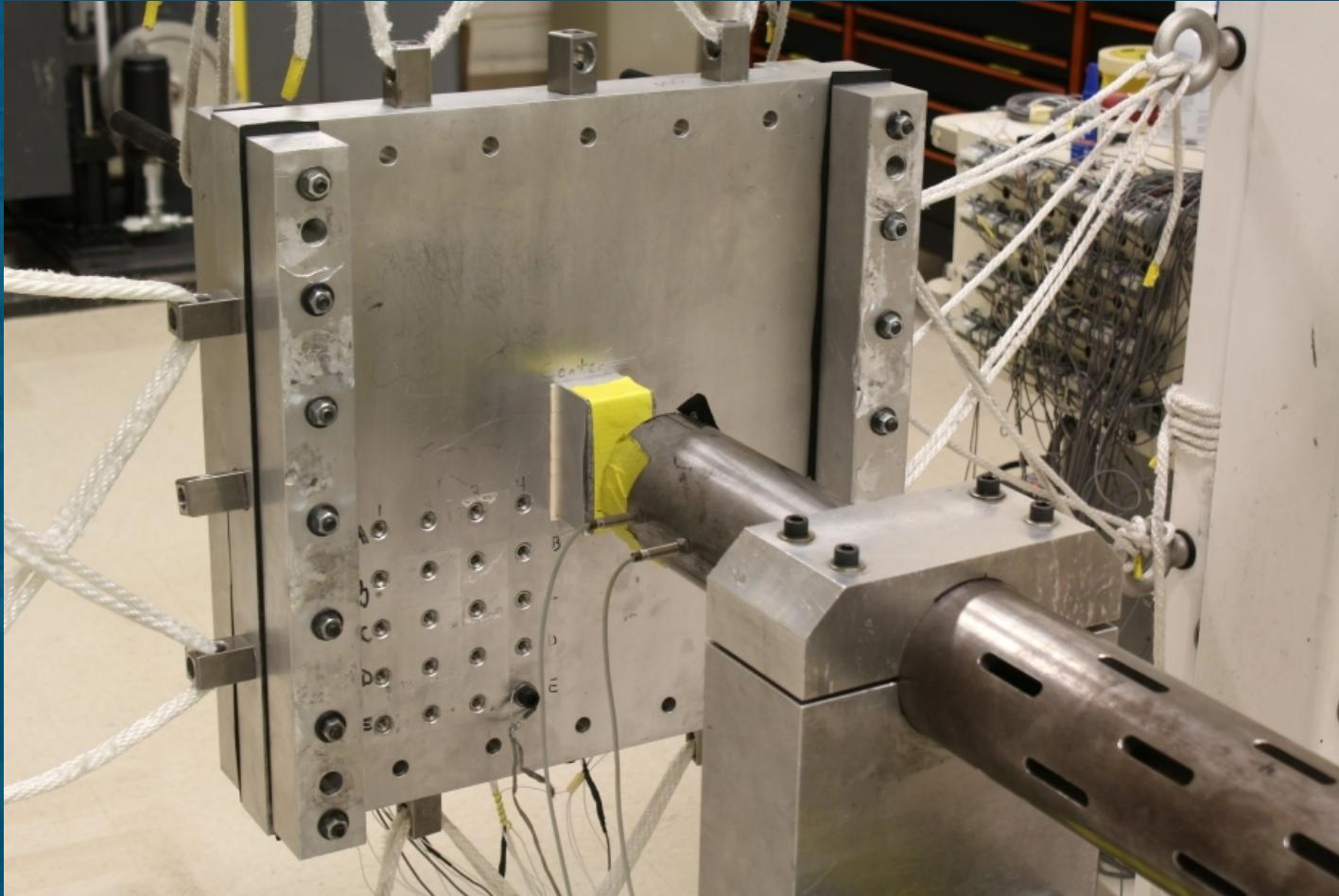
Free-Free



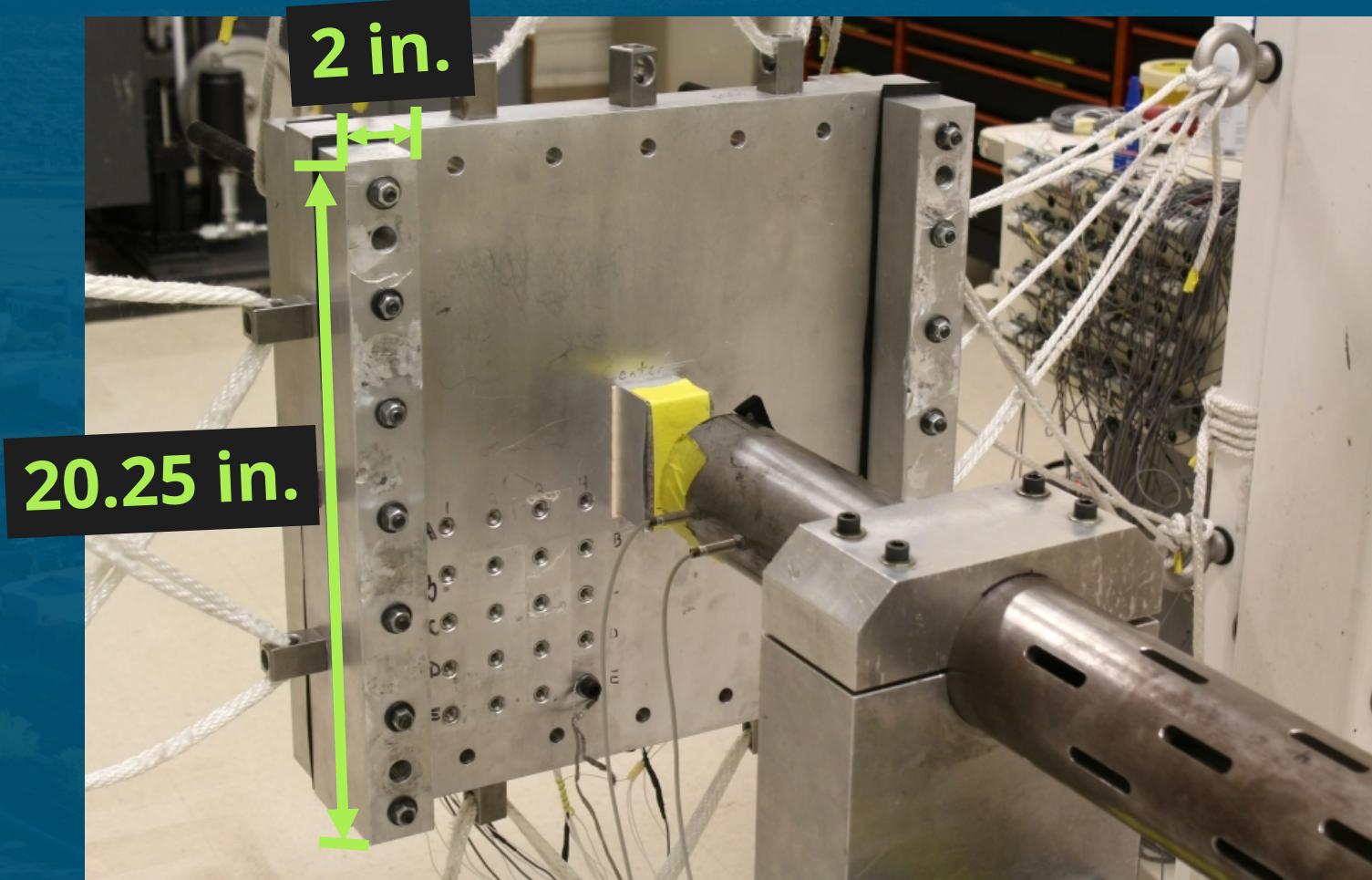
# 1kHz Resonant Plate



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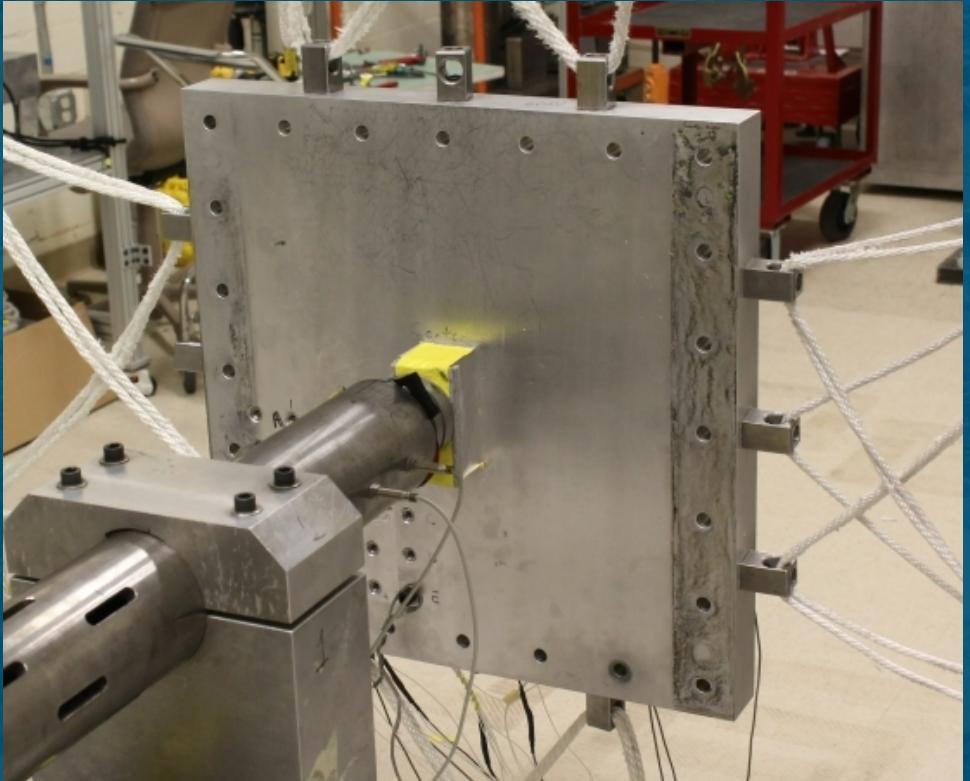
# 1kHz Resonant Plate



# 1kHz Resonant Plate



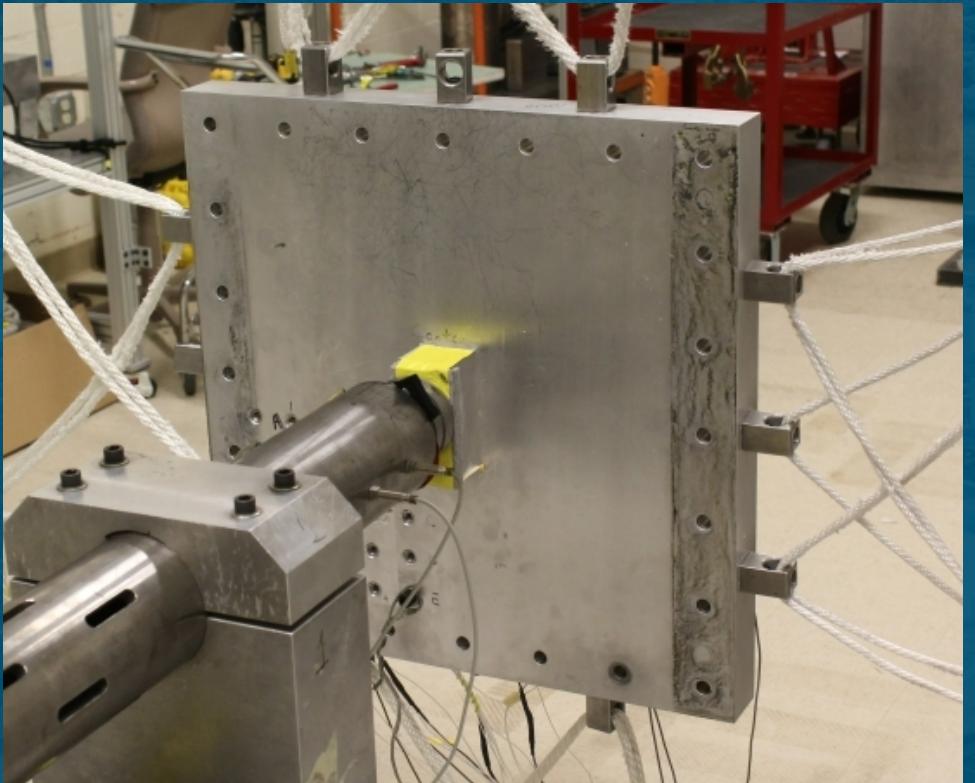
Model the Bare Plate



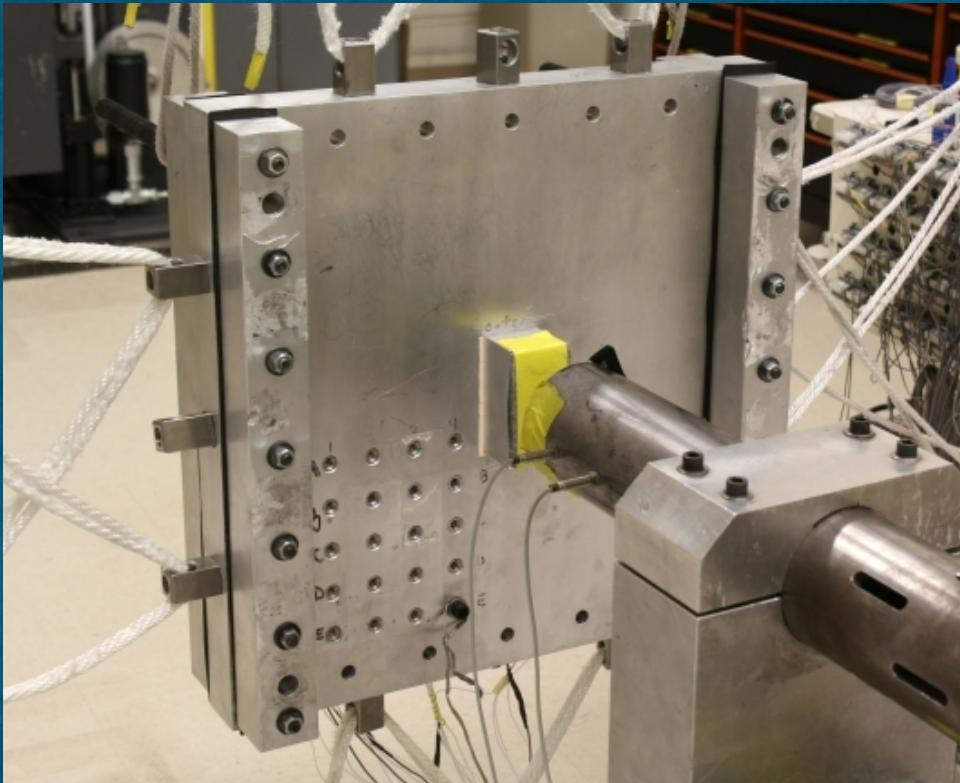
# 1kHz Resonant Plate

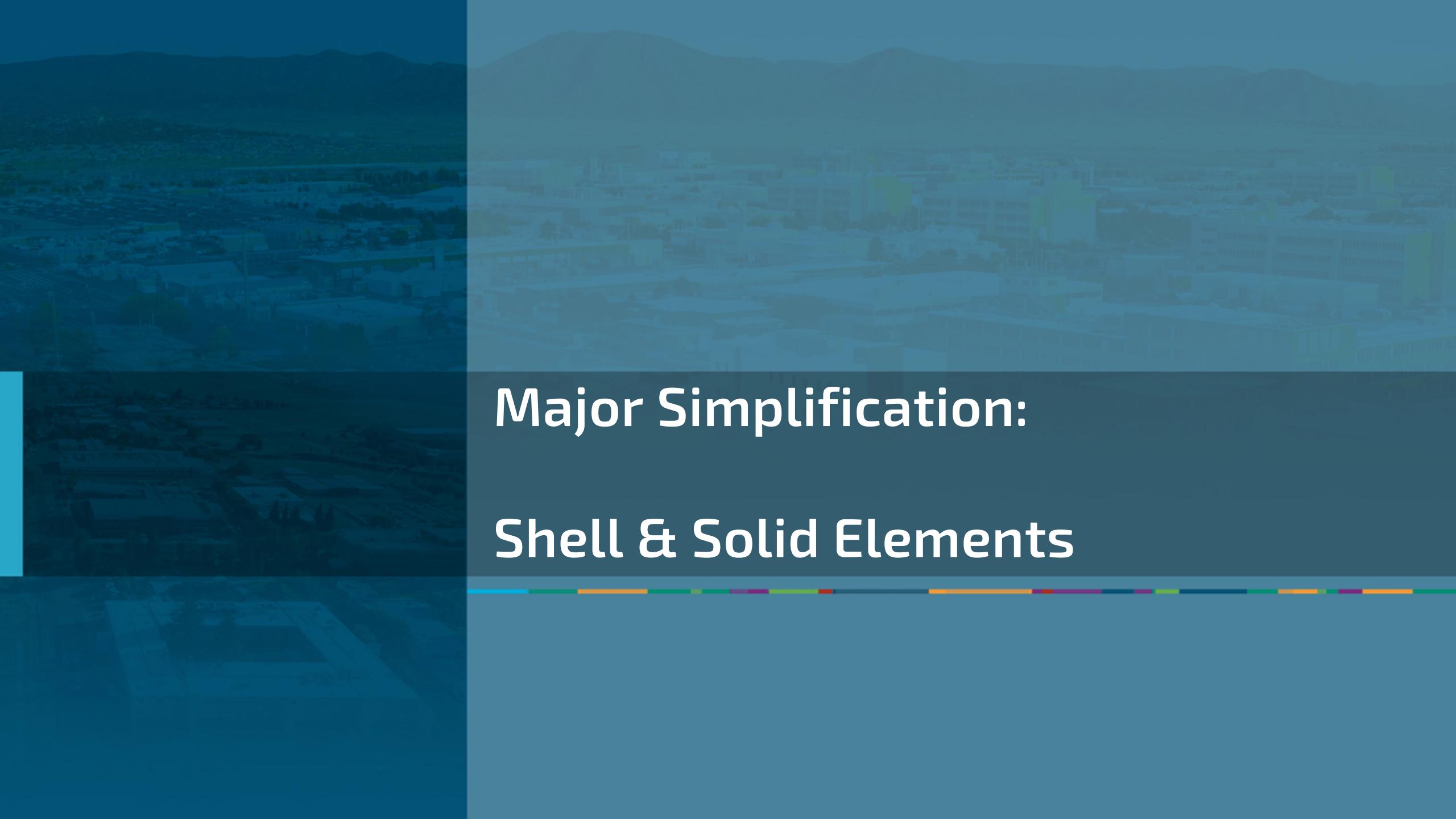


Model the Bare Plate



Then Add Damping Bars





# Major Simplification: Shell & Solid Elements

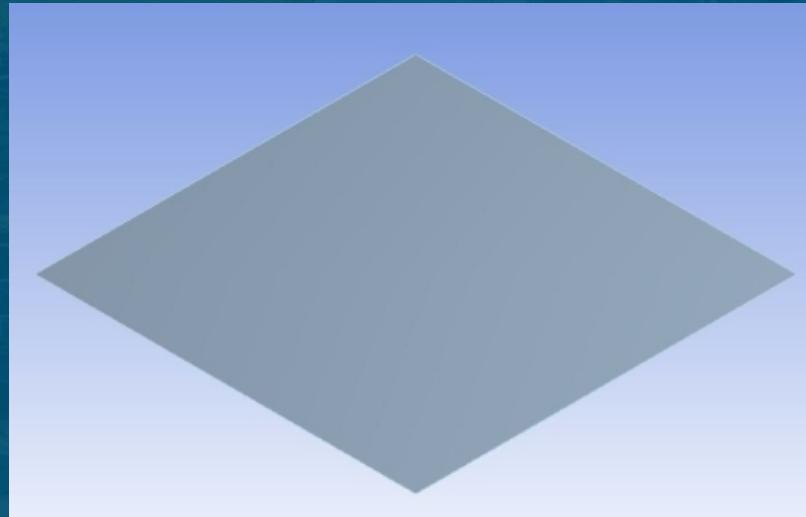
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# Shell vs. Solid Elements in Ansys



## Shell (2D) Elements

- 2-Dimensional
- Best for thin structures



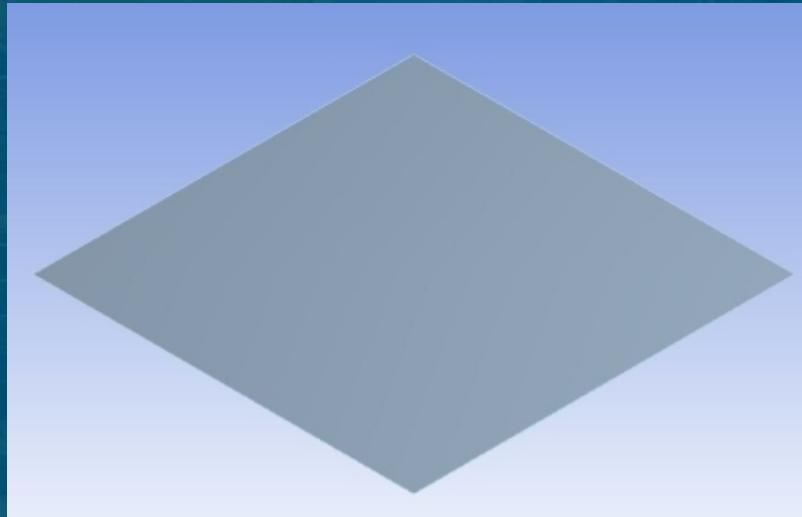
## Solid (3D) Elements

# Shell vs. Solid Elements in Ansys



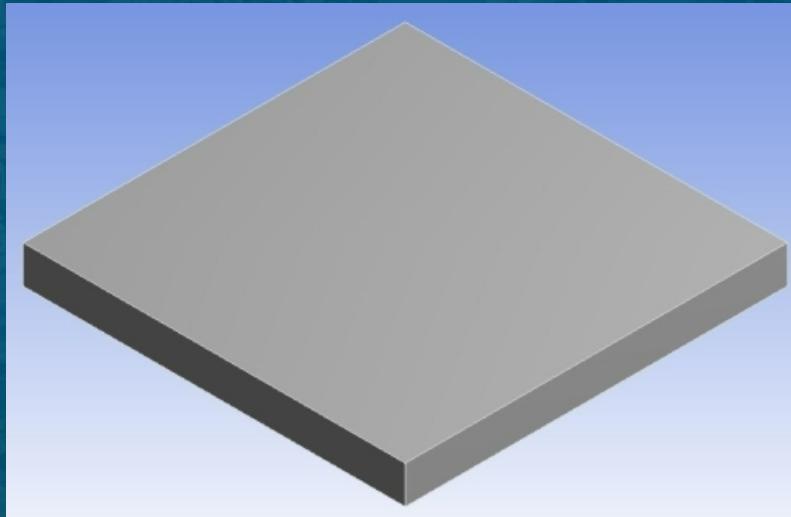
## Shell (2D) Elements

- 2-Dimensional
- Best for thin structures



## Solid (3D) Elements

- 3-Dimensional
- Not restricted to thin structures

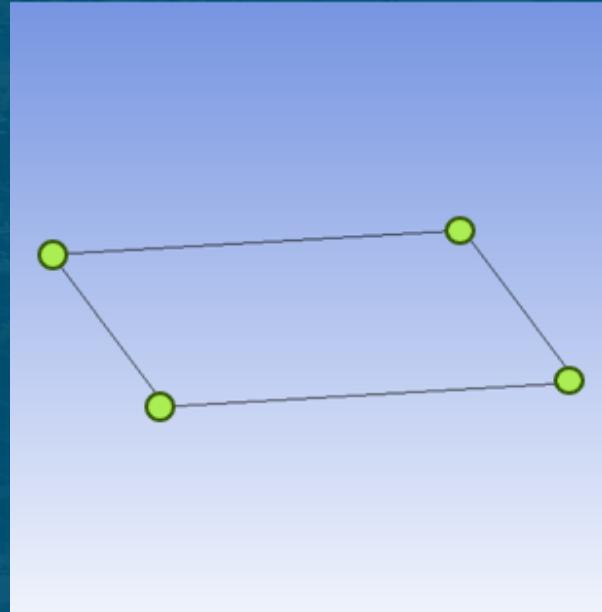


# Shell vs. Solid Elements in Ansys



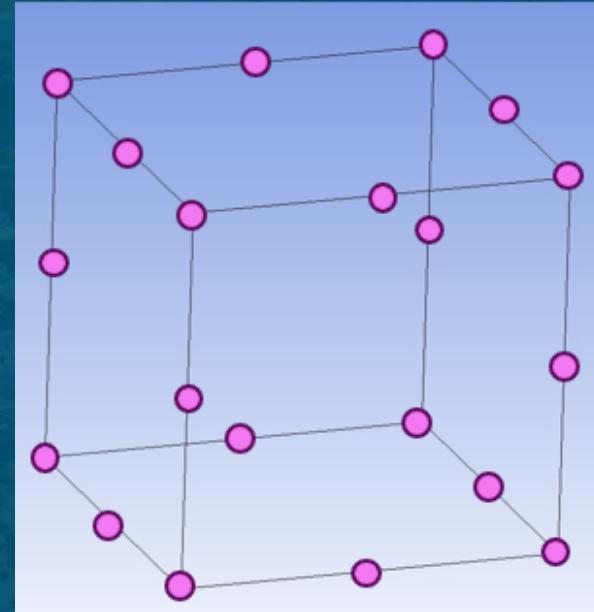
## Shell (2D) Elements

- 4 nodes on a single element
- Nodes have 6 DOF



## Solid (3D) Elements

- 20 nodes on a single element
- Nodes have 3 DOF



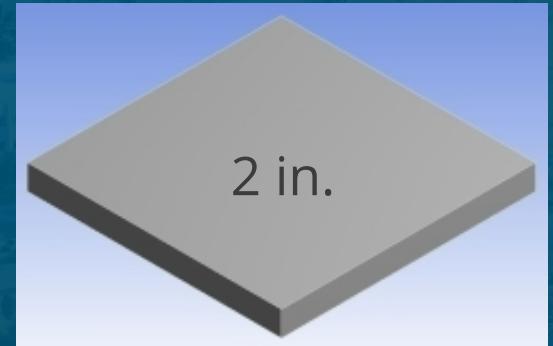
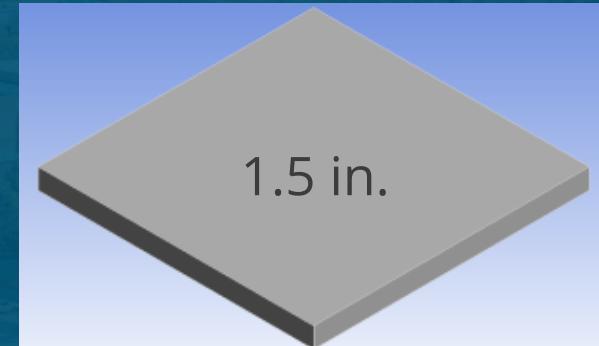
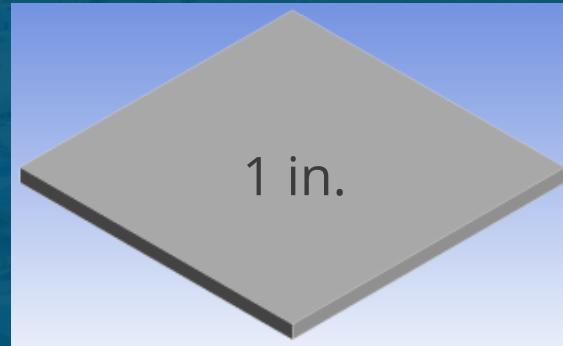
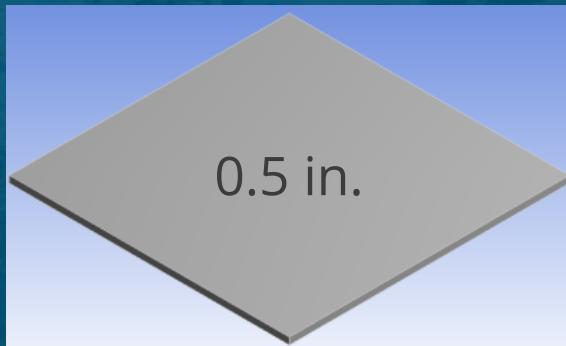
# How Good are Shell Elements in Ansys?



- Model our 1kHz plate with varying thickness

# How Good are Shell Elements in Ansys?

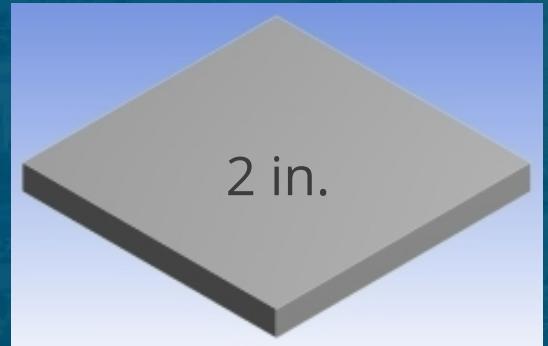
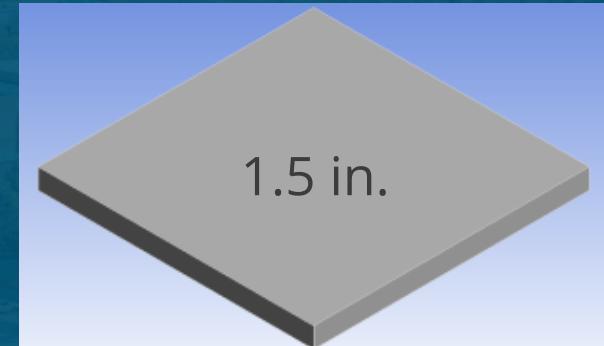
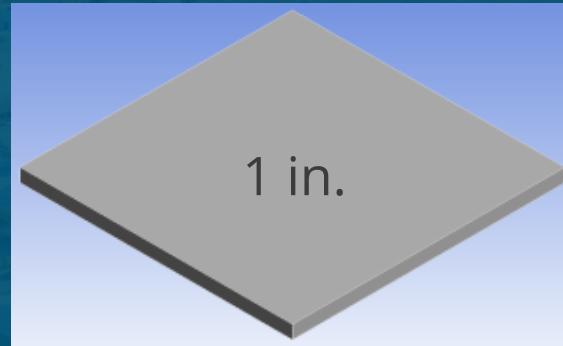
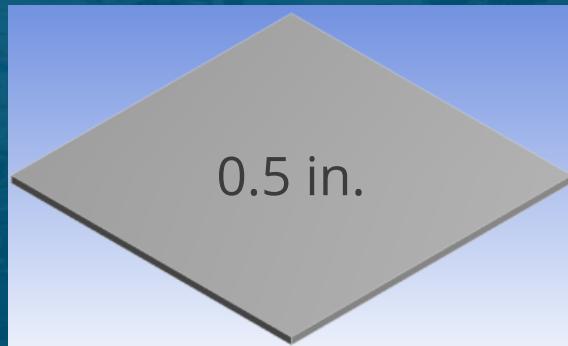
- Model our 1kHz plate with varying thickness
- Start small



# How Good are Shell Elements in Ansys?



- Model our 1kHz plate with varying thickness
- Start small

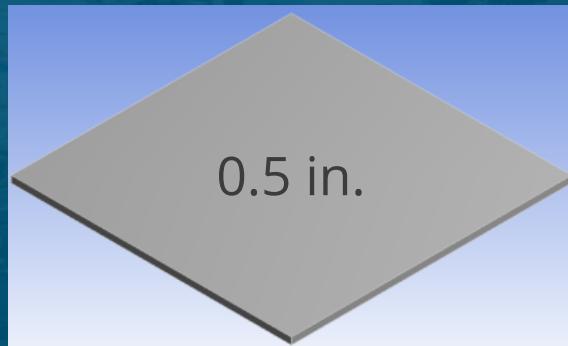


**Rule of Thumb:**  
Thickness  $\leq$  10% Length

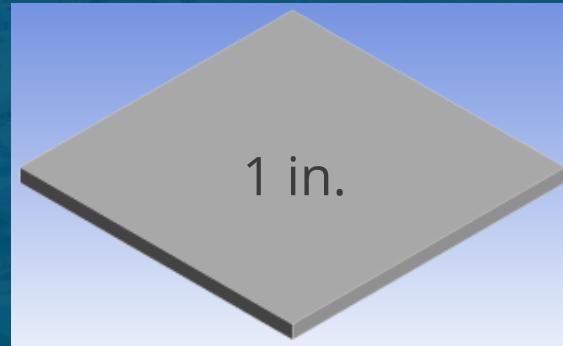
# How Good are Shell Elements in Ansys?



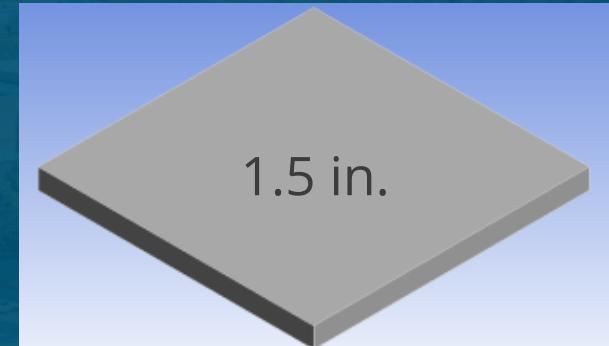
- Model our 1kHz plate with varying thickness
- Start small



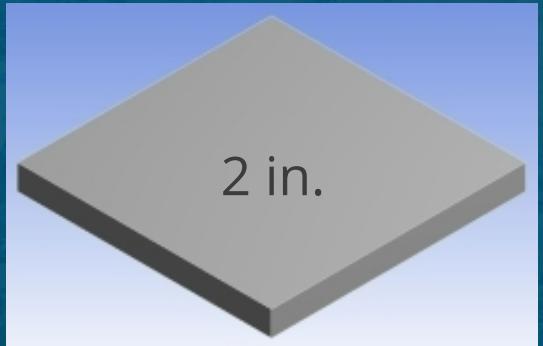
0.5 in.



1 in.



1.5 in.



2 in.

2.5%

5%

7.5%

10%

**Rule of Thumb:**  
**Thickness  $\leq$  10% Length**

# How Good are Shell Elements in Ansys?

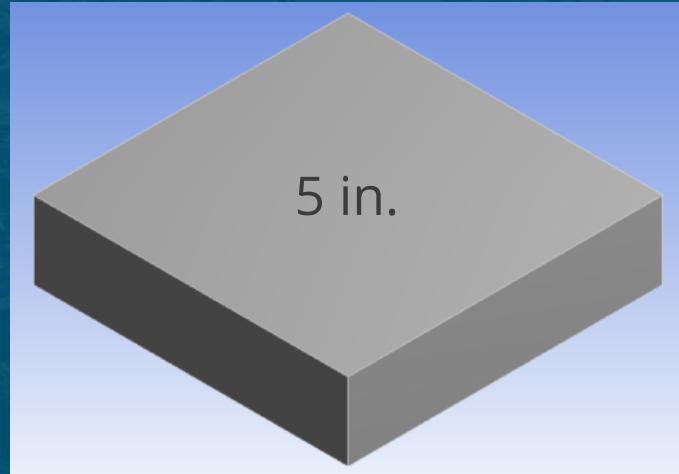


- Model our 1kHz plate with varying thickness
- Start small (  $\leq 10\%$  Length )
- Push the limits

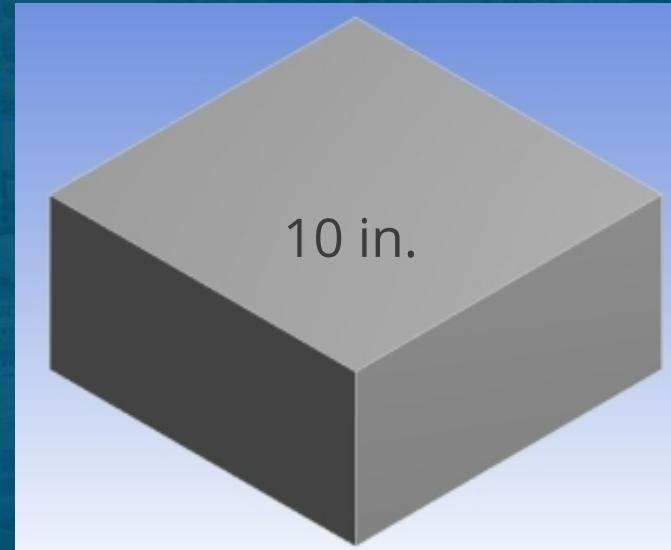
# How Good are Shell Elements in Ansys?



- Model our 1kHz plate with varying thickness
- Start small (  $\leq 10\%$  Length )
- Push the limits



25%



50%

# How Good are Shell Elements in Ansys?

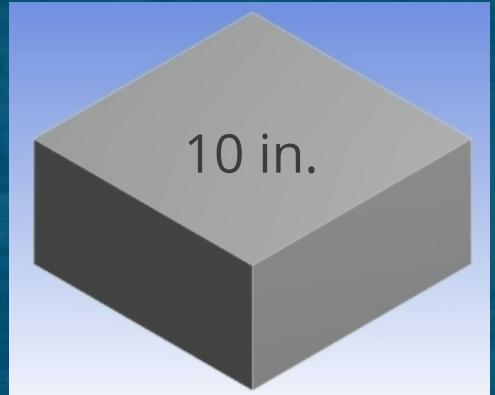
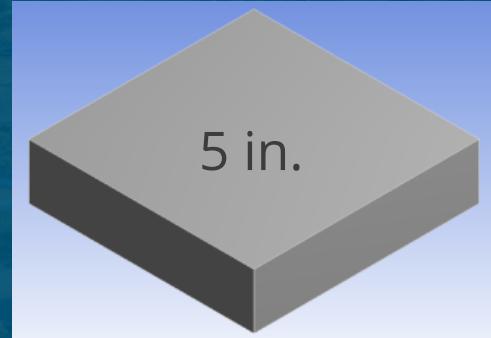
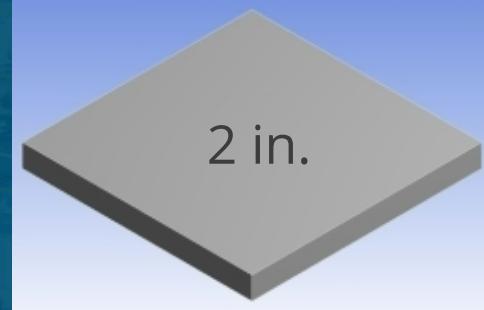
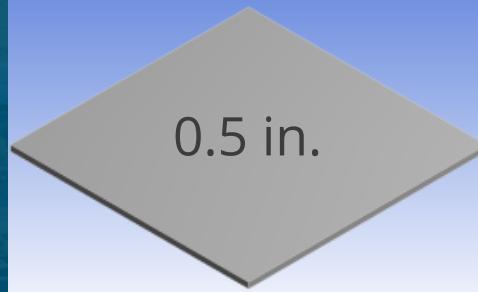


- Model our 1kHz plate with varying thickness
- Start small (  $\leq 10\%$  Length )
- Push the limits (  $> 10\%$  Length )
- Compare natural frequencies of the first 10 flexural modes

# Results: Solid vs. Shell Elements in Ansys



- Model our 1kHz plate with varying thickness
- Compare natural frequencies of the first 10 flexural modes

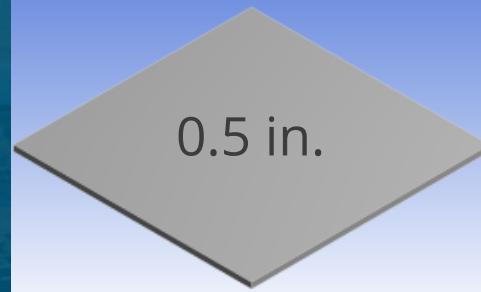


Max.  
% Difference  
in Frequency

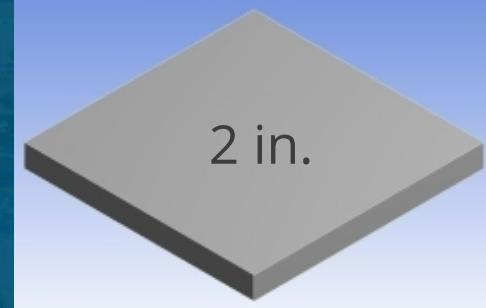
# Results: Solid vs. Shell Elements in Ansys



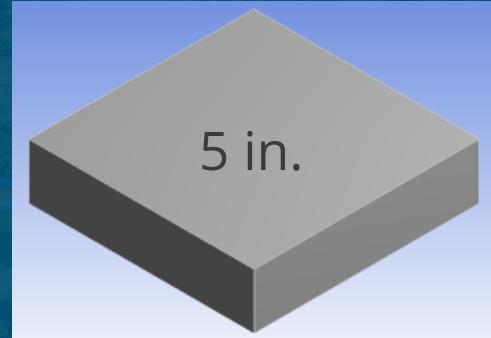
- Model our 1kHz plate with varying thickness
- Compare natural frequencies of the first 10 flexural modes



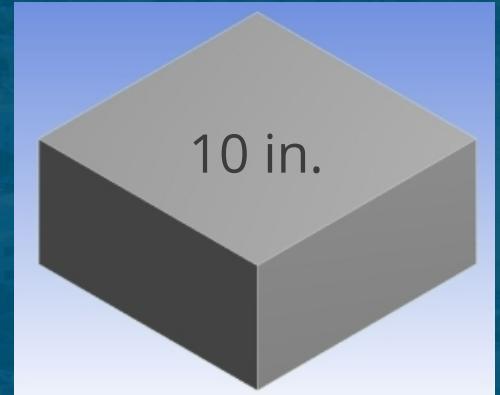
0.5 in.



2 in.



5 in.



10 in.

Max.  
% Difference  
in Frequency

0.36%

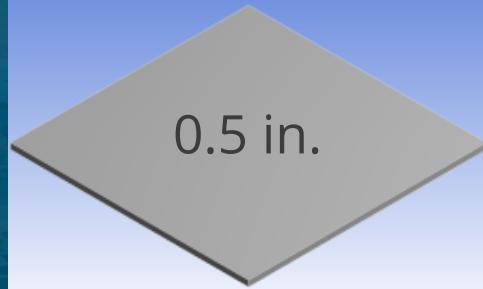
0.10%

0.44%

1.49%

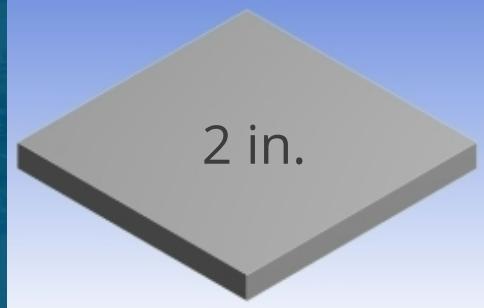
# Results: Solid vs. Shell Elements in Ansys

- Model our 1kHz plate with varying thickness
- Compare natural frequencies of the first 10 flexural modes

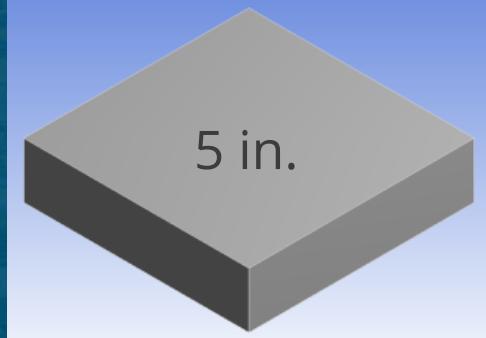


Max.  
% Difference  
in Frequency

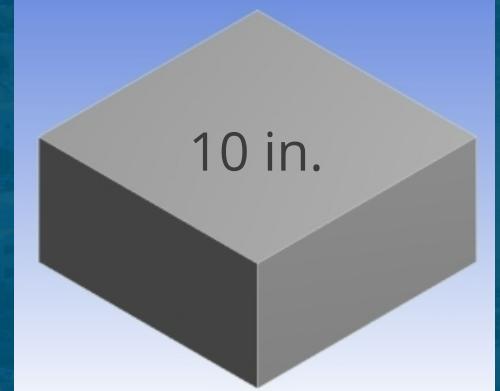
0.36%



0.10%



0.44%



1.49%

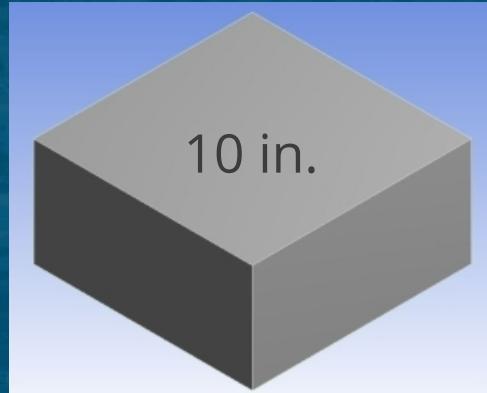
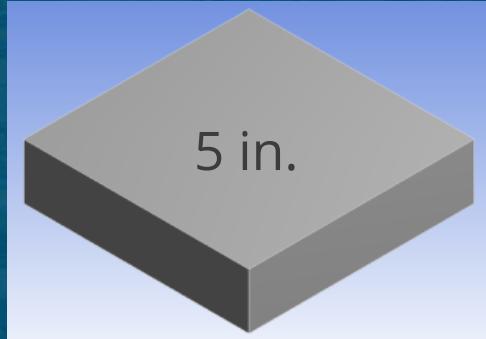
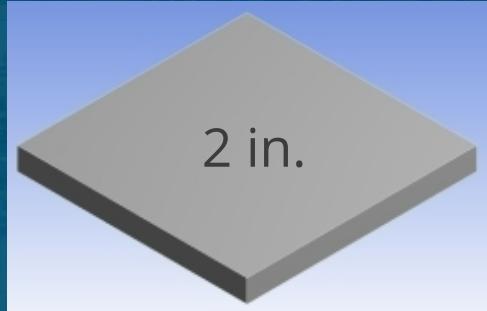
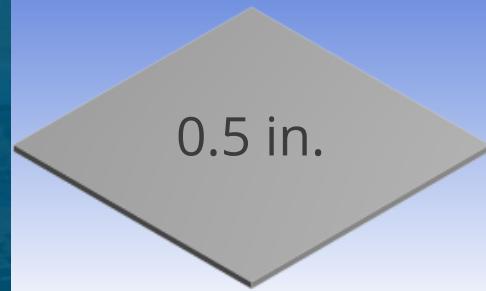
## Key Takeaways

Ansys shell elements performed very well overall

Larger differences occurred in the higher order modes

# Results: Solid vs. Shell Elements in Ansys

- Model our 1kHz plate with varying thickness
- Compare natural frequencies of the first 10 flexural modes

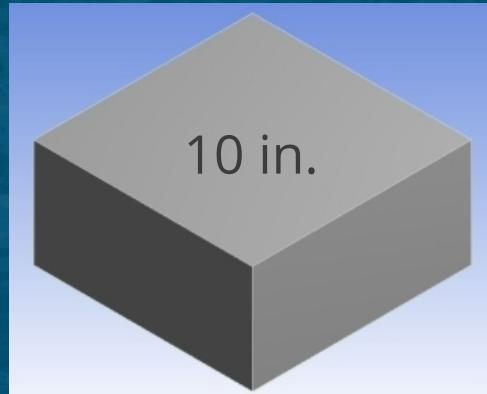
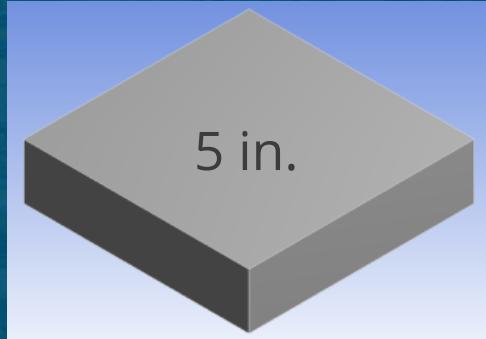
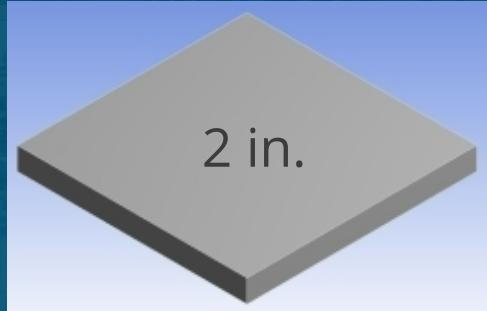
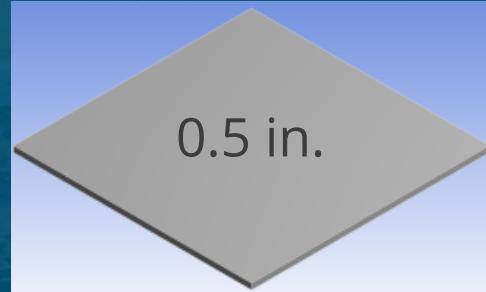


|                  |       |        |        |          |
|------------------|-------|--------|--------|----------|
| Computation Time | 6 sec | 8 sec  | 8 sec  | 7 sec    |
|                  | 9 sec | 28 sec | 77 sec | 1h 49min |

Shell (2D)  
Solid (3D)

# Results: Solid vs. Shell Elements in Ansys

- Model our 1kHz plate with varying thickness
- Compare natural frequencies of the first 10 flexural modes



|                  |        |         |         |          |
|------------------|--------|---------|---------|----------|
| Computation Time | 6 sec  | 8 sec   | 8 sec   | 7 sec    |
|                  | 9 sec  | 28 sec  | 77 sec  | 1h 49min |
| Memory           | 140 MB | 140 MB  | 140 MB  | 140 MB   |
|                  | 363 MB | 1.43 GB | 4.74 GB | 4.71 GB  |

# Summary: Solid vs. Shell Elements in Ansys



- Modeled our 1kHz plate with varying thickness
- Start small (  $\leq 10\%$  Length )
- Push the limits (  $> 10\%$  Length )
- Compared natural frequencies of the first 10 flexural modes

## Results

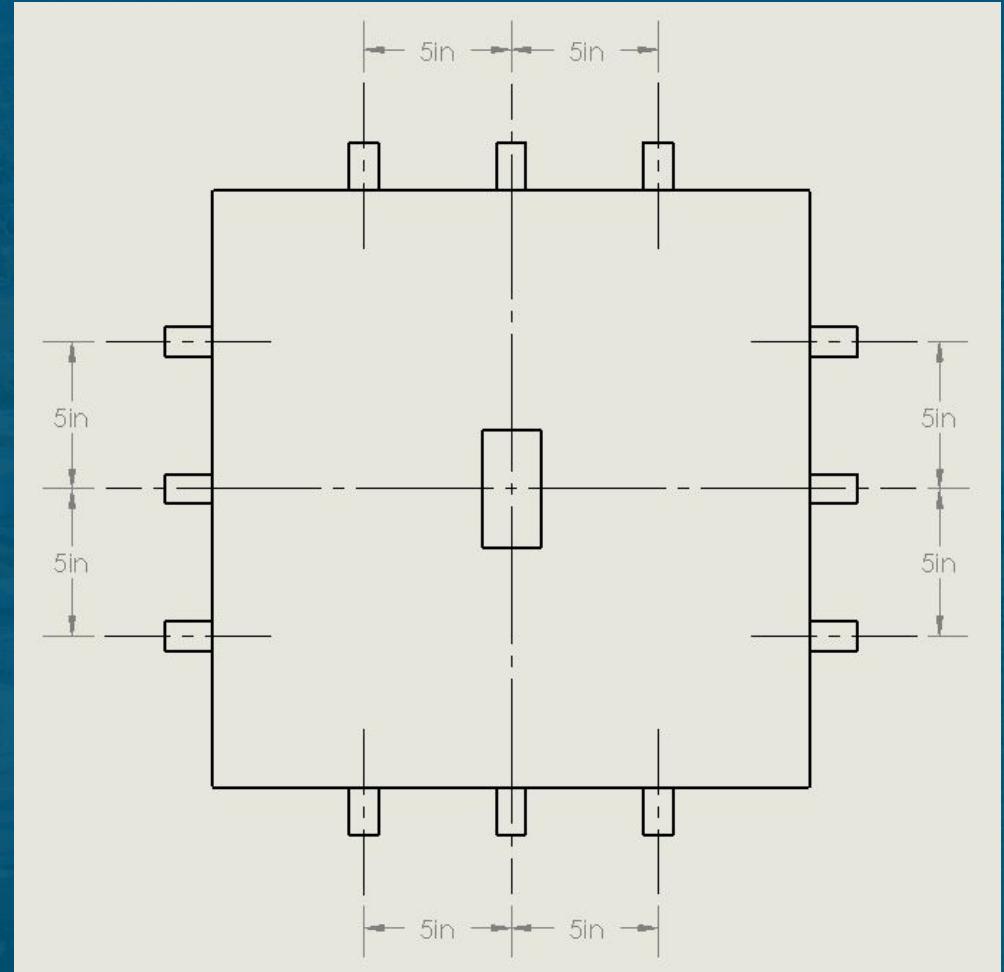
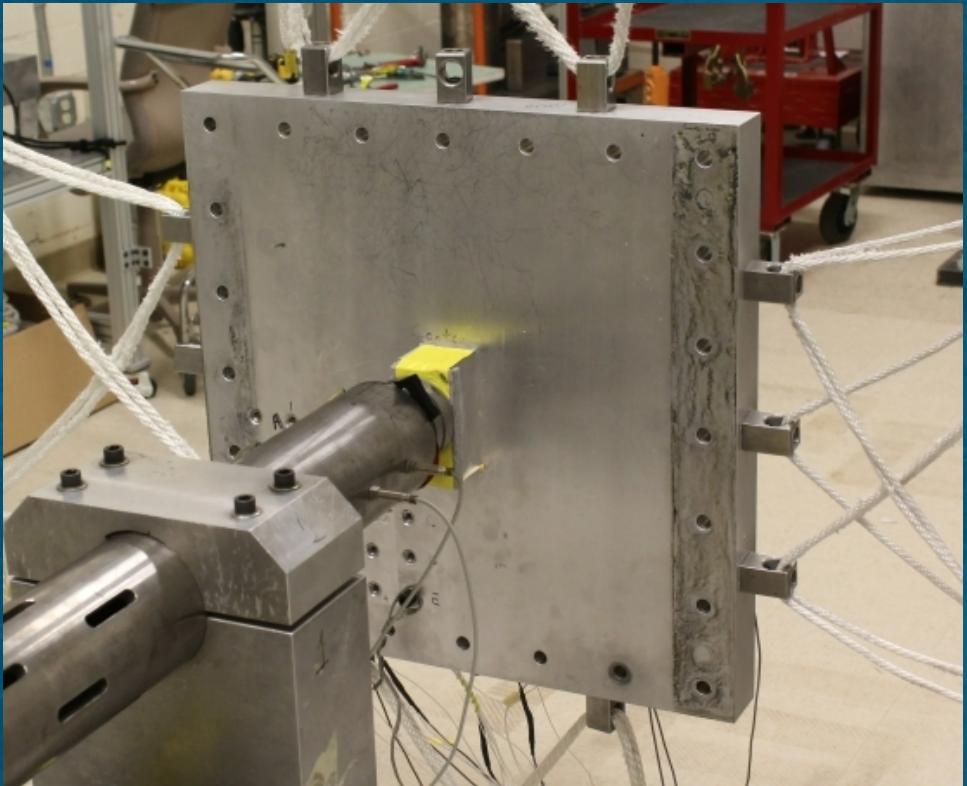
- Ansys shell elements performed much better than expected – even for thick plates
- Shell elements much more efficient than solid elements

The background of the slide is a photograph of a cityscape with a range of mountains in the distance. The city in the foreground is filled with numerous buildings of varying heights, some with green roofs. The sky is clear and blue.

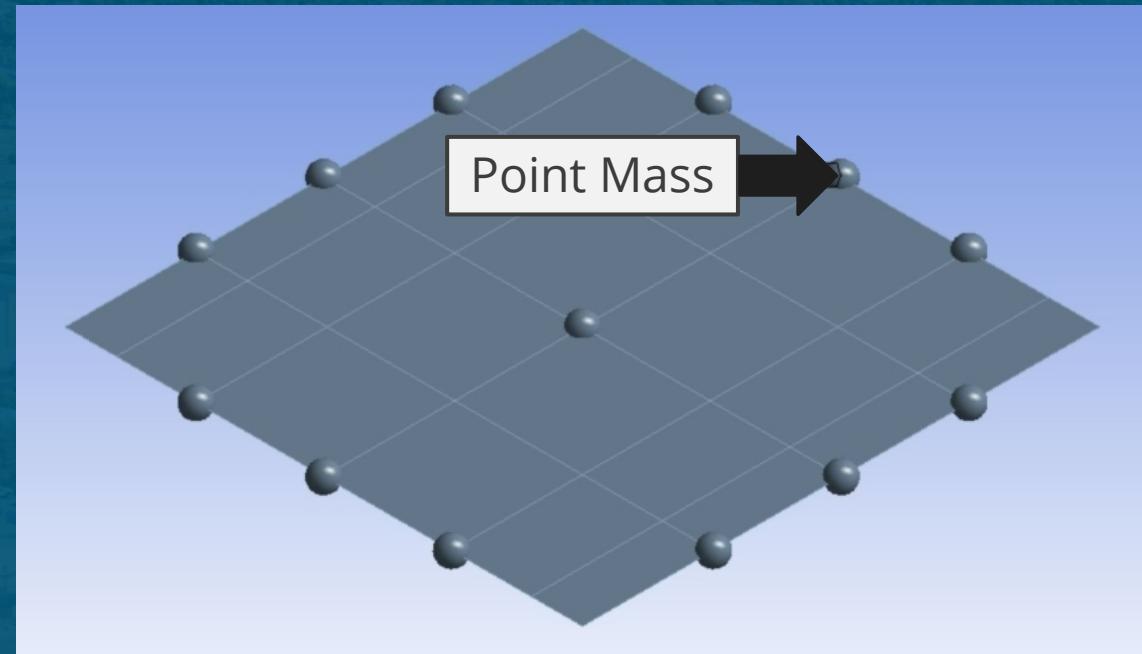
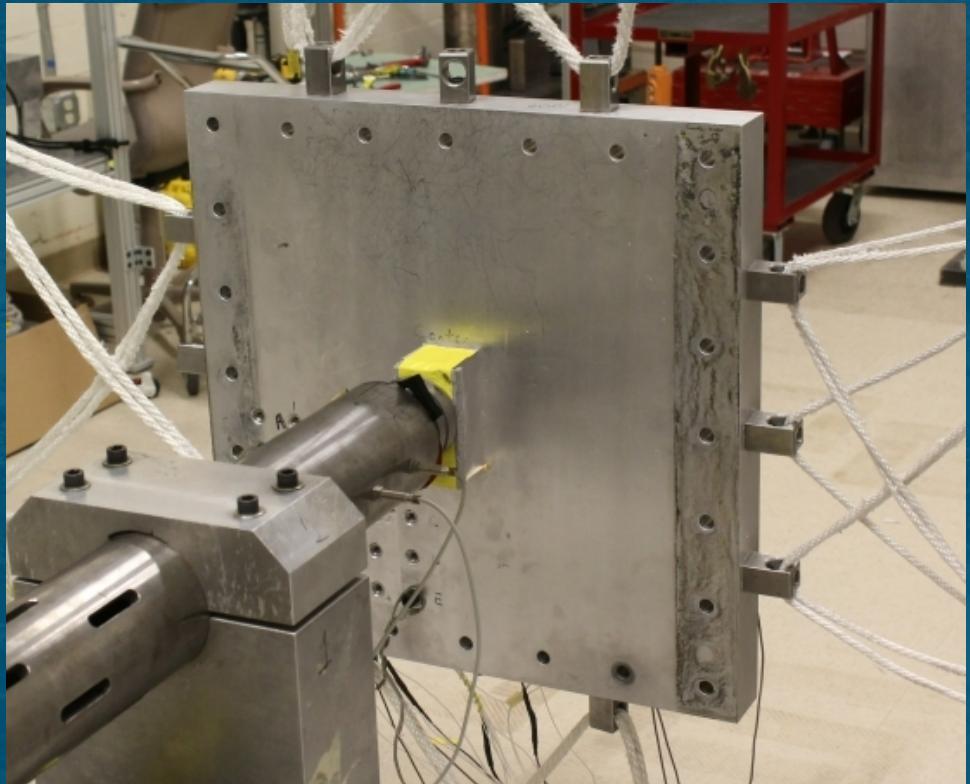
# Model Overview: Bare Plate

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# Model for the Bare Plate



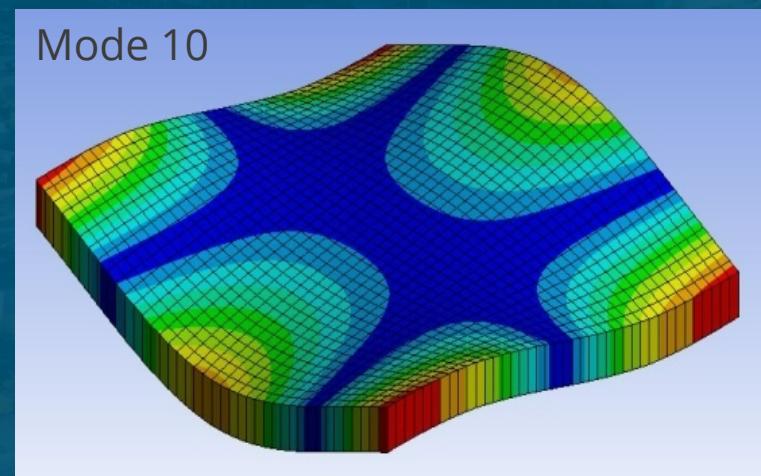
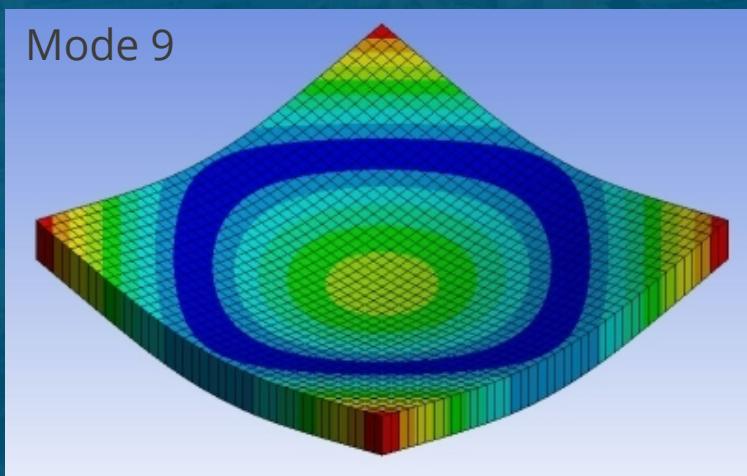
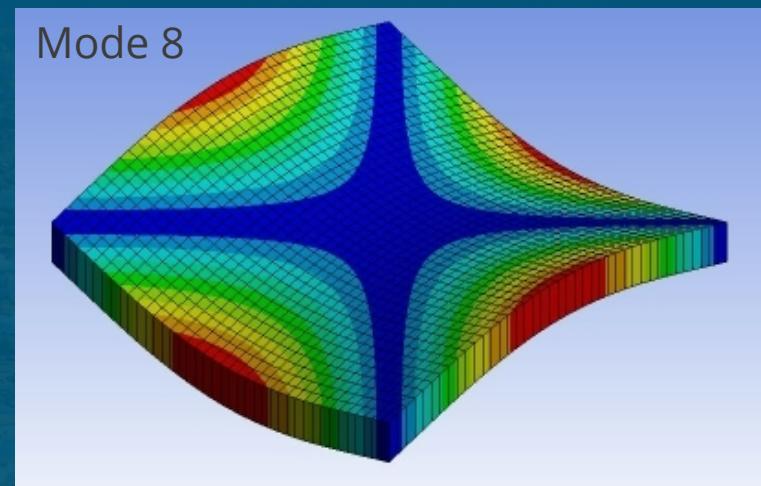
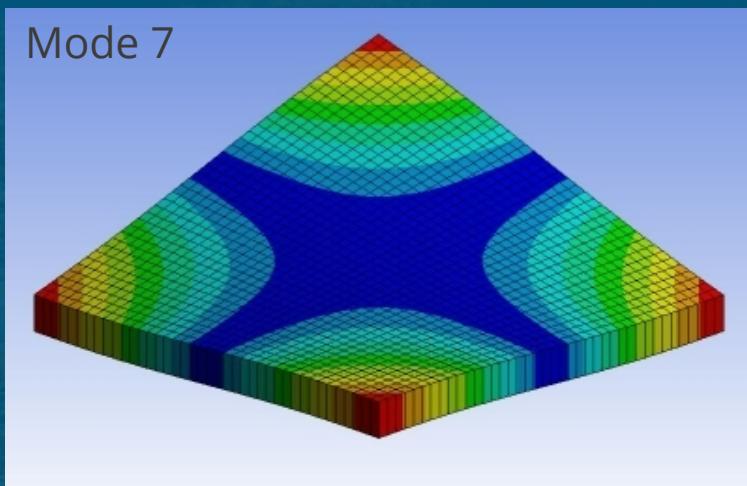
# Model for the Bare Plate



# Mode Shapes for the Bare Plate Model



| Mode | Frequency (Hz) |
|------|----------------|
| 7    | 559.0          |
| 8    | 798.6          |
| 9    | 1039.2         |
| 10   | 1388           |
| 11   | 1388           |
| 12   | 2381.3         |
| 13   | 2453.9         |
| 14   | 2454           |
| 15   | 2488.5         |
| 16   | 3150           |
| 17   | 3619.1         |
| 18   | 3718.7         |
| 19   | 3718.7         |
| 20   | 3777.7         |
| 21   | 3777.7         |

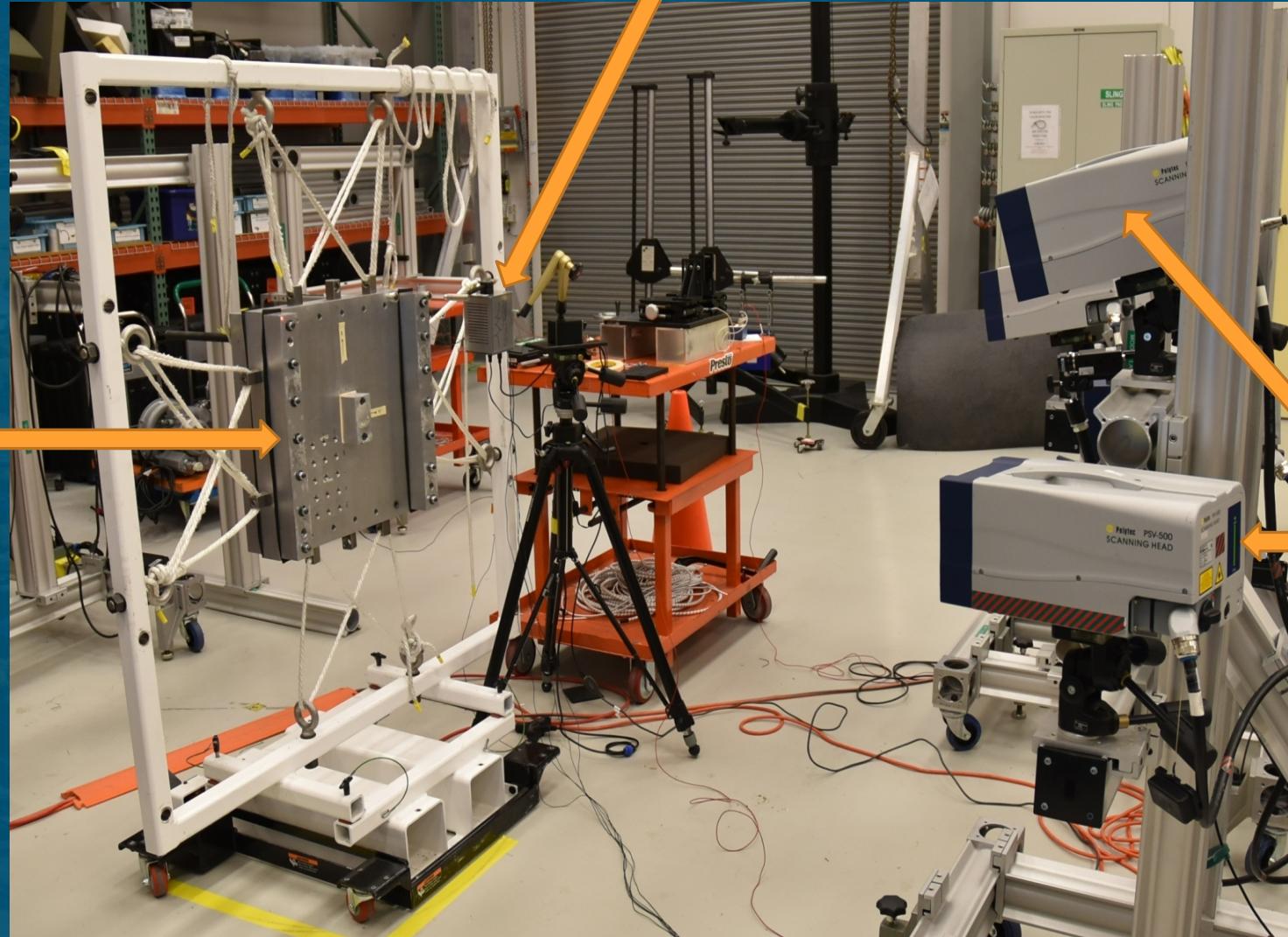


# Validation with Modal Test Data



Automatic Hammer

Test Object



3D Scanning  
Laser Doppler  
Vibrometer

# Validation with Modal Test Data



- Modal Assurance Criterion (MAC) to match modes between model and test

| MAC Value  | Meaning             |
|------------|---------------------|
| > 0.9      | Matched             |
| 0.5 to 0.9 | Investigate Further |
| < 0.5      | Not Correlated      |

- Compared natural frequencies of matched modes

# Validation with Modal Test Data – MAC

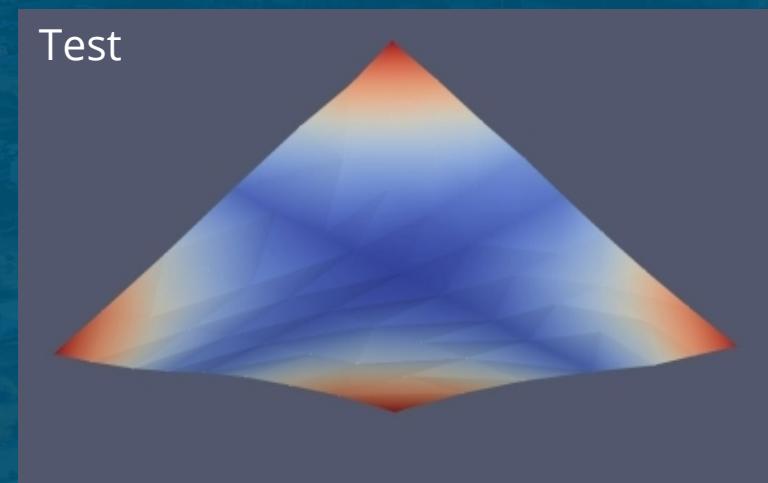
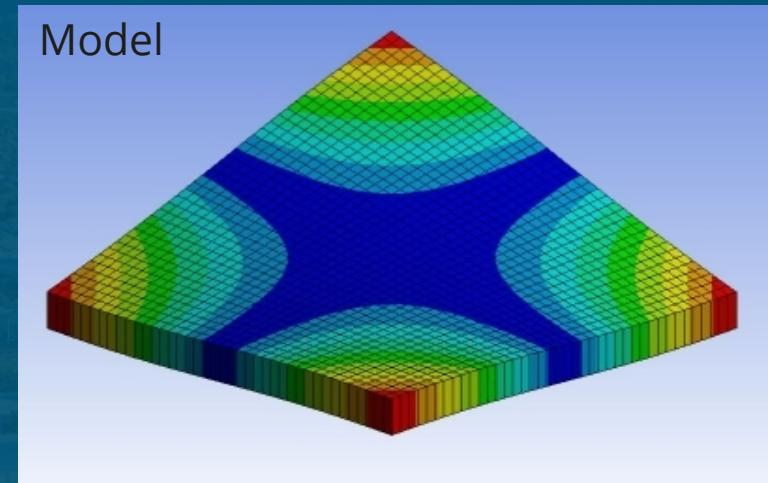


| Model  | Test  |       |        |        |        |        |        |        |  | Frequency<br>% Difference |
|--------|-------|-------|--------|--------|--------|--------|--------|--------|--|---------------------------|
|        | 545.0 | 789.6 | 1020.0 | 1350.0 | 2313.0 | 2347.3 | 2365.0 | 3081.5 |  |                           |
| 559.0  | 1.000 | 0.000 | 0.000  | 0.001  | 0.000  | 0.000  | 0.007  | 0.126  |  | 2.57%                     |
| 798.6  | 0.000 | 1.000 | 0.003  | 0.000  | 0.001  | 0.010  | 0.000  | 0.000  |  | 1.15%                     |
| 1039.2 | 0.000 | 0.001 | 0.999  | 0.000  | 0.017  | 0.078  | 0.001  | 0.001  |  | 1.88%                     |
| 1388.0 | 0.000 | 0.000 | 0.001  | 0.999  | 0.005  | 0.002  | 0.002  | 0.001  |  | 2.82%                     |
| 2381.3 | 0.000 | 0.018 | 0.098  | 0.000  | 0.167  | 0.688  | 0.012  | 0.001  |  | 1.45%                     |
| 2453.9 | 0.000 | 0.000 | 0.000  | 0.000  | 0.644  | 0.211  | 0.059  | 0.000  |  | 6.09%                     |
| 2488.5 | 0.006 | 0.000 | 0.000  | 0.000  | 0.110  | 0.000  | 0.665  | 0.000  |  | 5.22%                     |
| 3150.0 | 0.127 | 0.000 | 0.000  | 0.000  | 0.003  | 0.000  | 0.000  | 0.991  |  | 2.22%                     |

# Validation with Modal Test Data - Mode Shapes



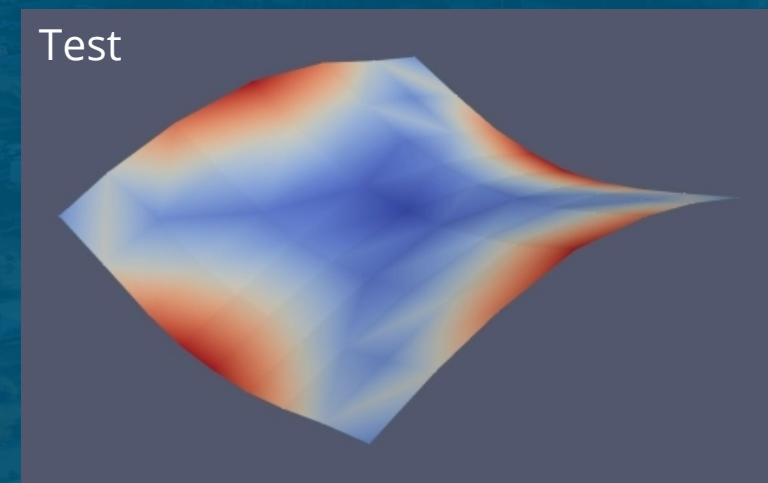
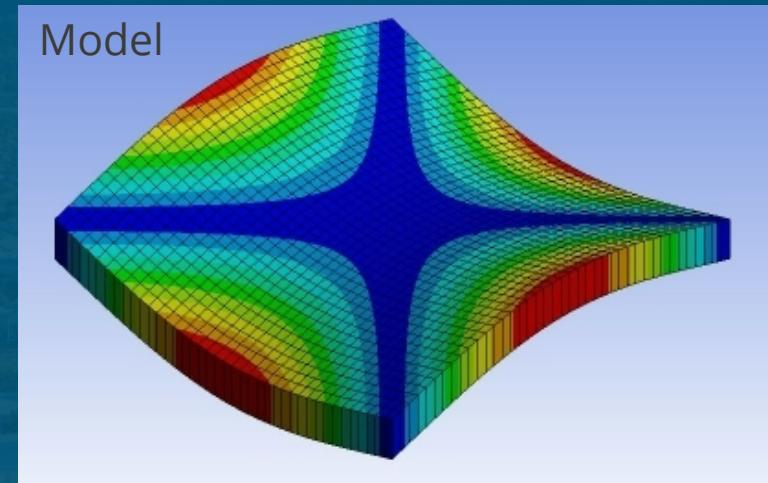
| Model Frequencies (Hz) | Test Frequencies (Hz) | % Difference | MAC Value |
|------------------------|-----------------------|--------------|-----------|
| 559.0                  | 545.0                 | 2.57%        | 1.000     |
| 798.6                  | 789.6                 | 1.15%        | 1.000     |
| 1039.2                 | 1020.0                | 1.88%        | 0.999     |
| 1388.0                 | 1350.0                | 2.82%        | 0.999     |
| 2381.3                 | 2347.3                | 1.45%        | 0.688     |
| 2453.9                 | 2313.0                | 6.09%        | 0.644     |
| 2488.5                 | 2365.0                | 5.22%        | 0.665     |
| 3150.0                 | 3081.5                | 2.22%        | 0.991     |



# Validation with Modal Test Data – Mode Shapes



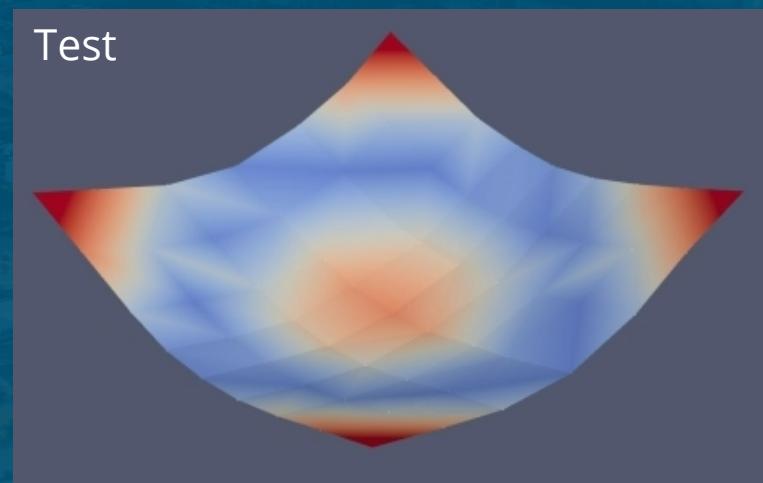
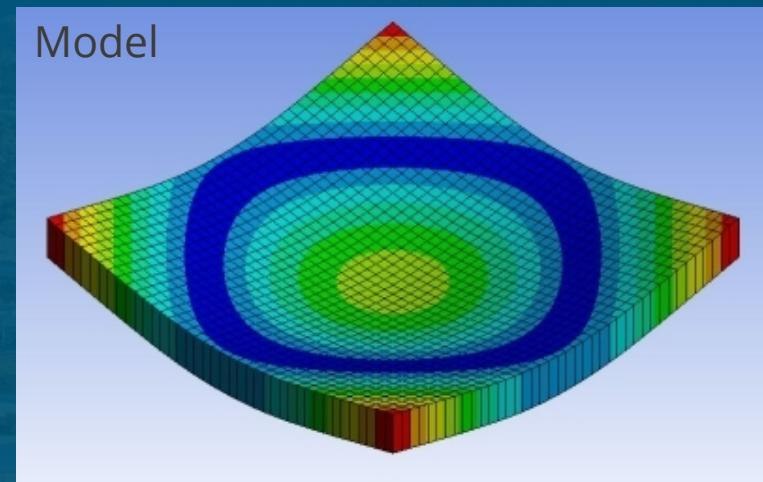
| Model Frequencies (Hz) | Test Frequencies (Hz) | % Difference | MAC Value |
|------------------------|-----------------------|--------------|-----------|
| 559.0                  | 545.0                 | 2.57%        | 1.000     |
| 798.6                  | 789.6                 | 1.15%        | 1.000     |
| 1039.2                 | 1020.0                | 1.88%        | 0.999     |
| 1388.0                 | 1350.0                | 2.82%        | 0.999     |
| 2381.3                 | 2347.3                | 1.45%        | 0.688     |
| 2453.9                 | 2313.0                | 6.09%        | 0.644     |
| 2488.5                 | 2365.0                | 5.22%        | 0.665     |
| 3150.0                 | 3081.5                | 2.22%        | 0.991     |



# Validation with Modal Test Data – Mode Shapes



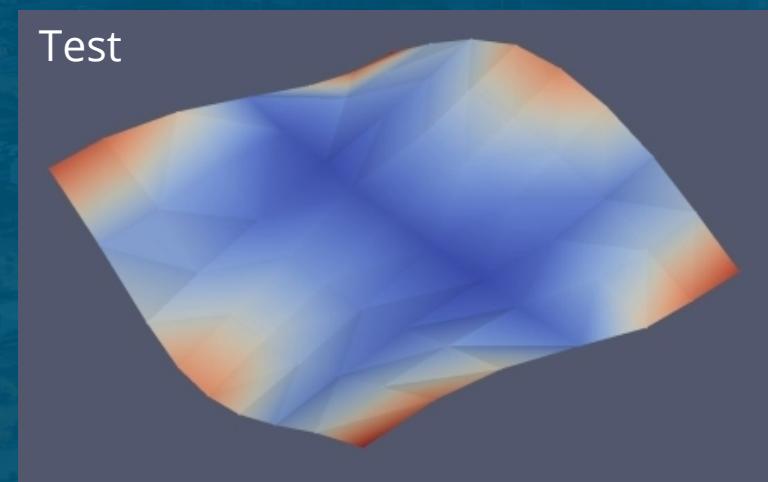
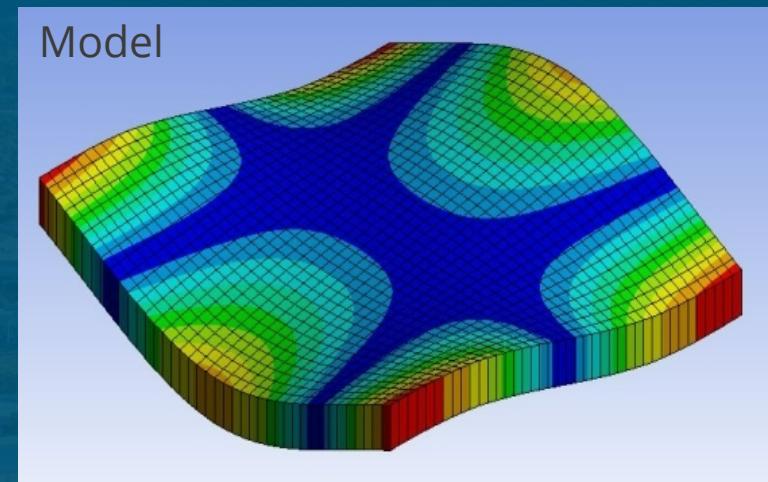
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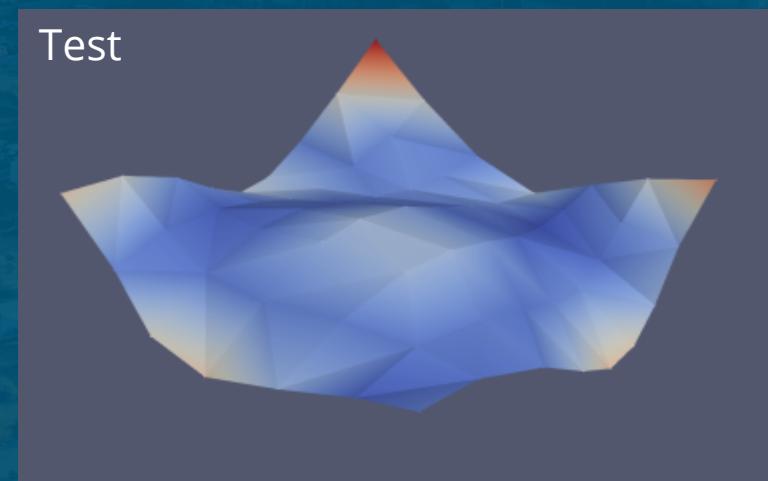
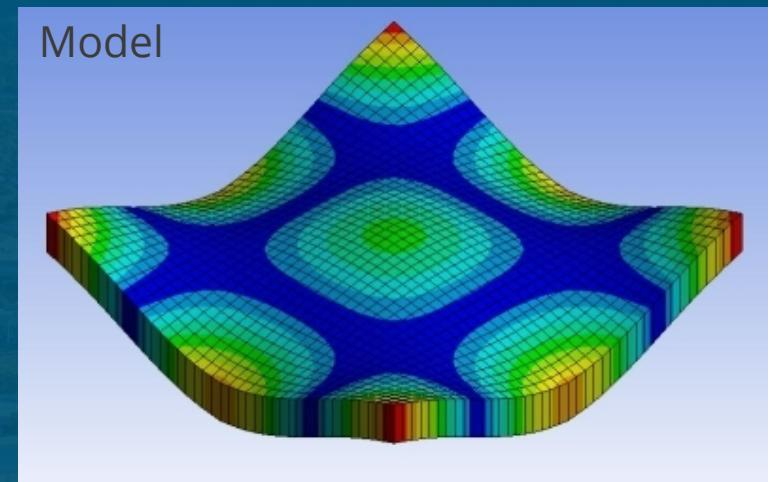
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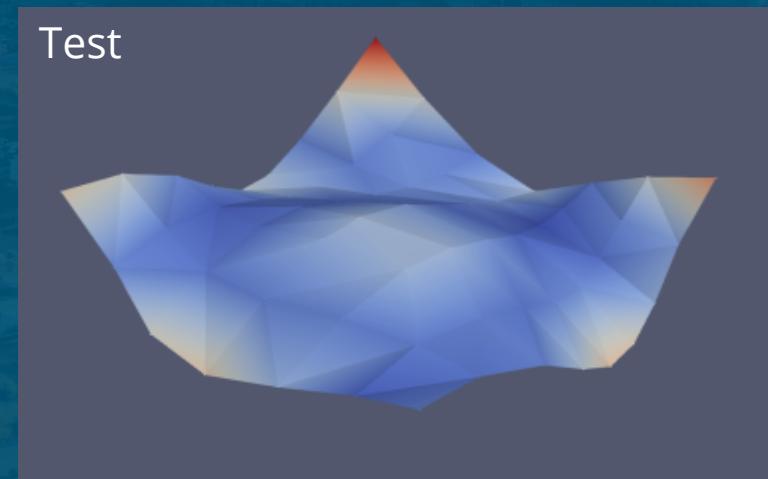
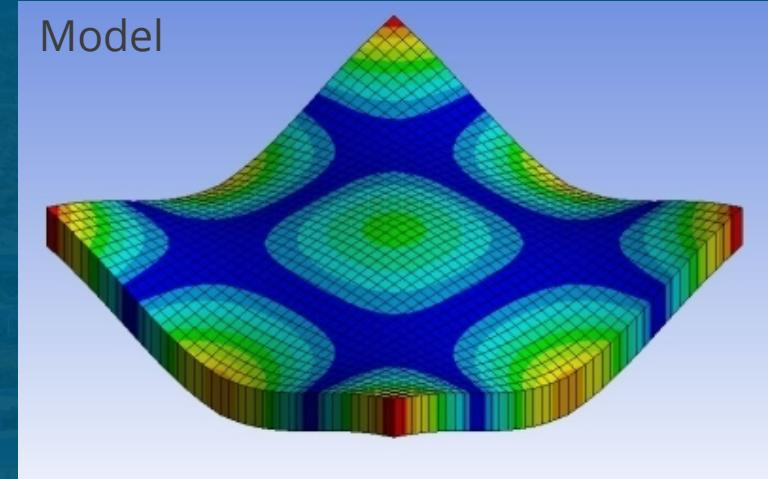
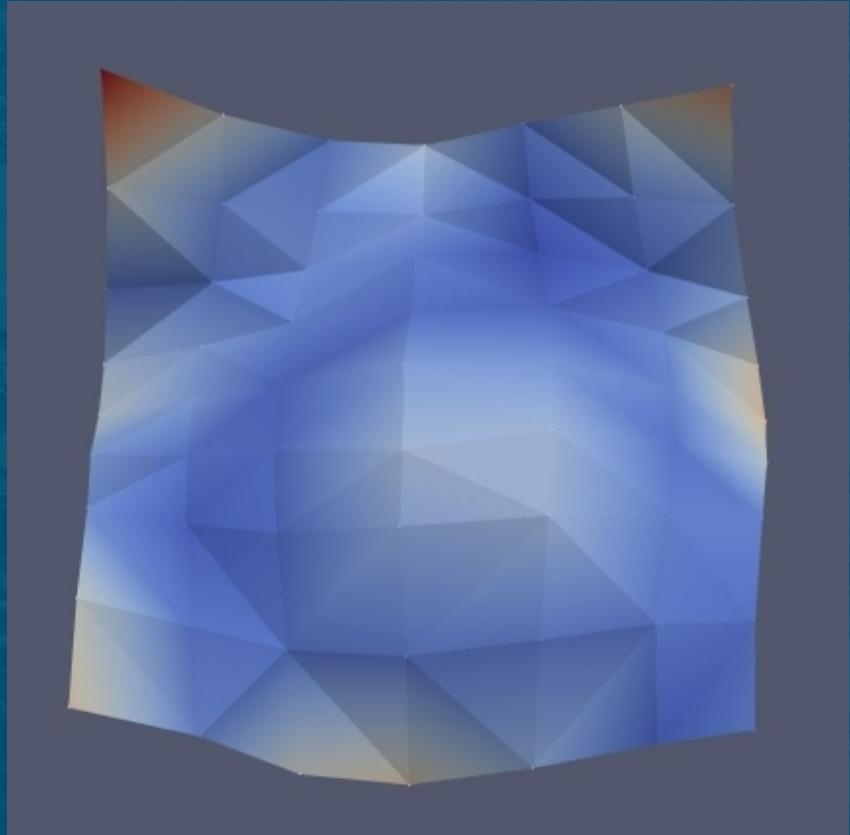
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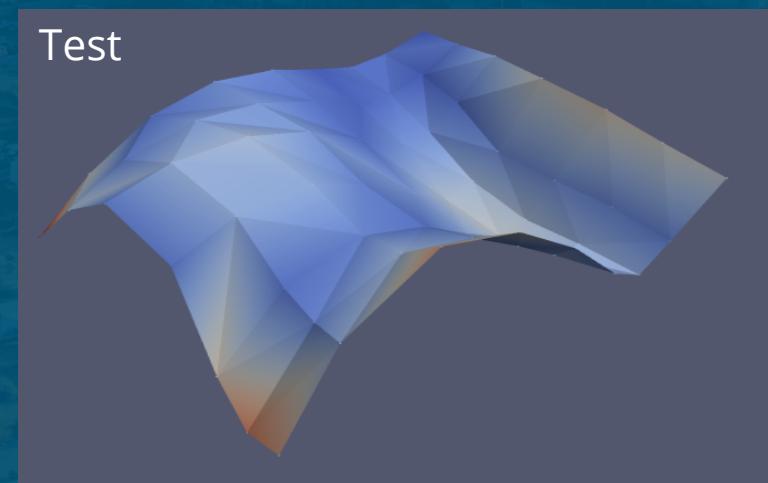
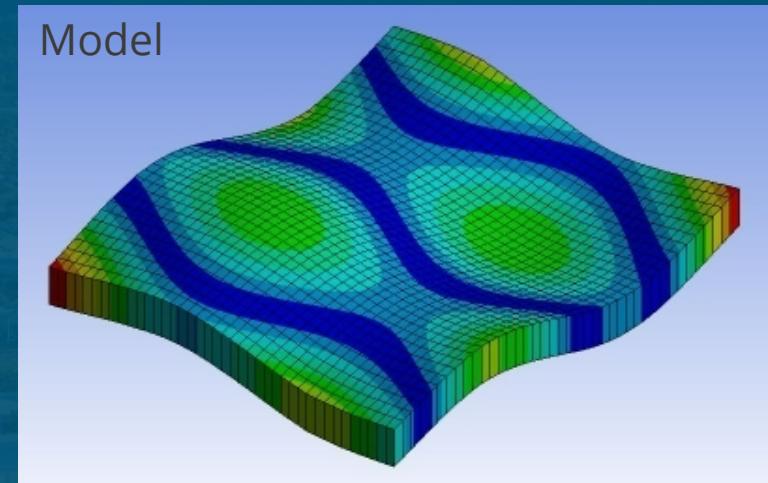
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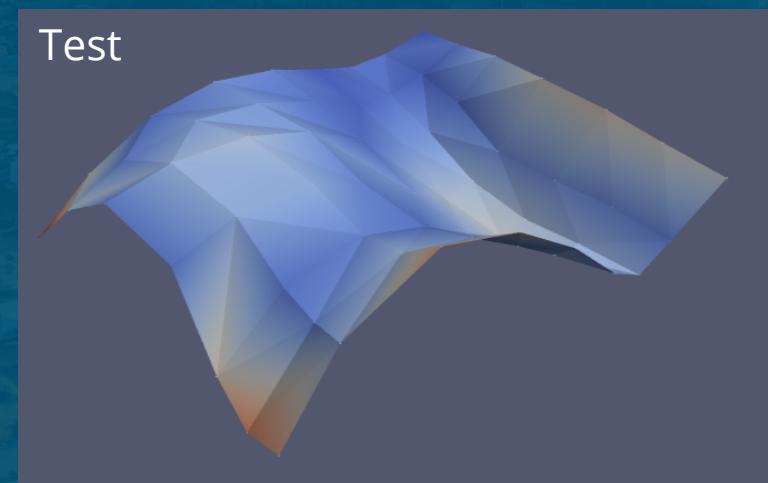
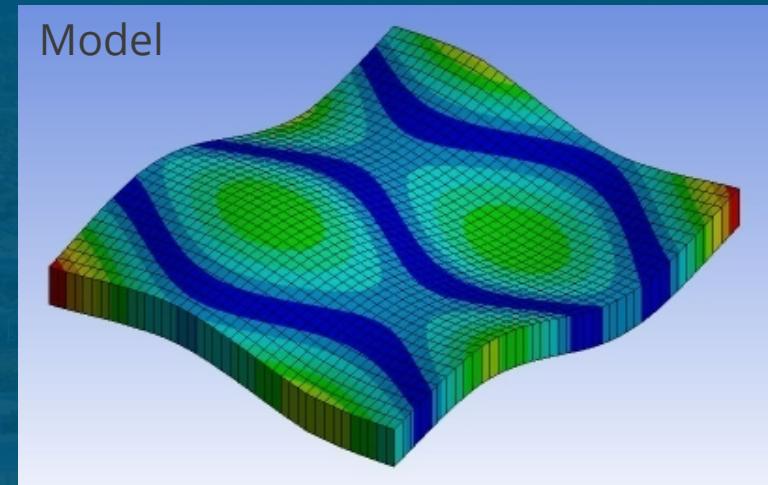
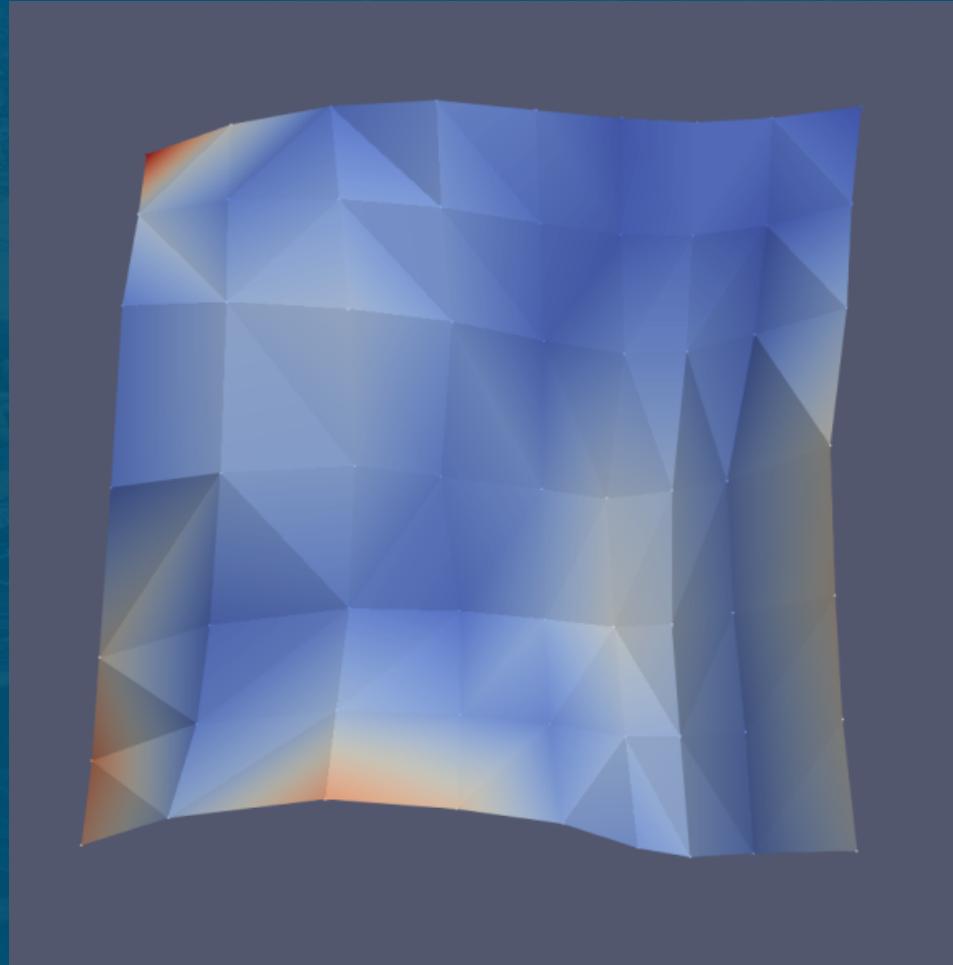
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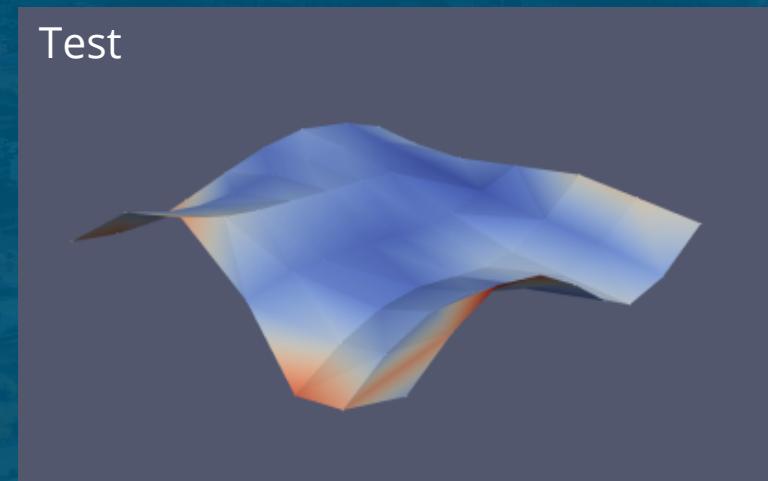
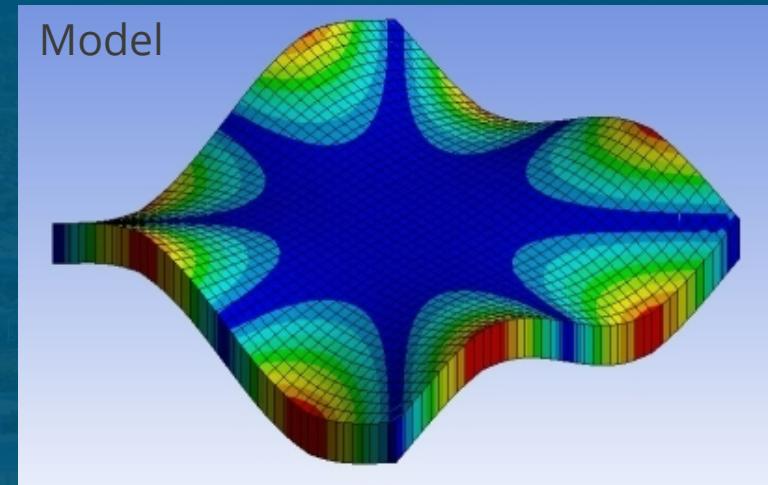
# Validation with Modal Test Data – Mode Shapes



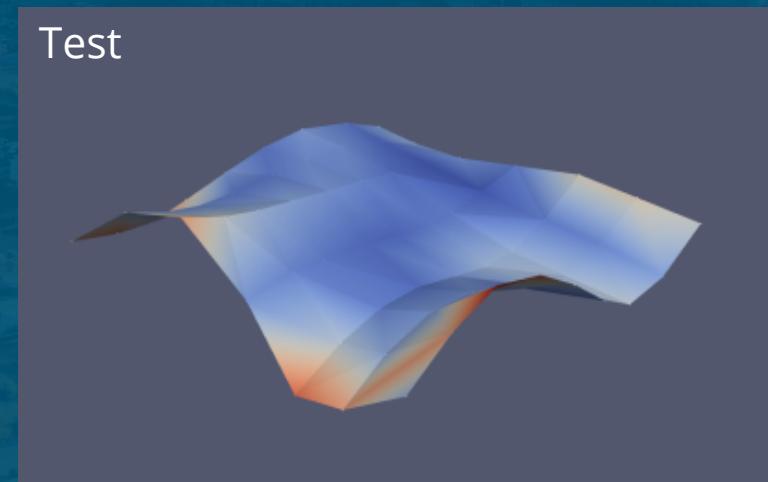
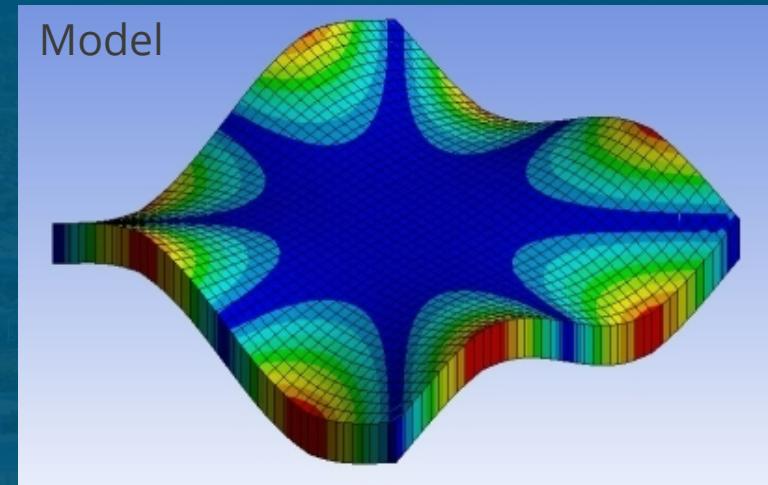
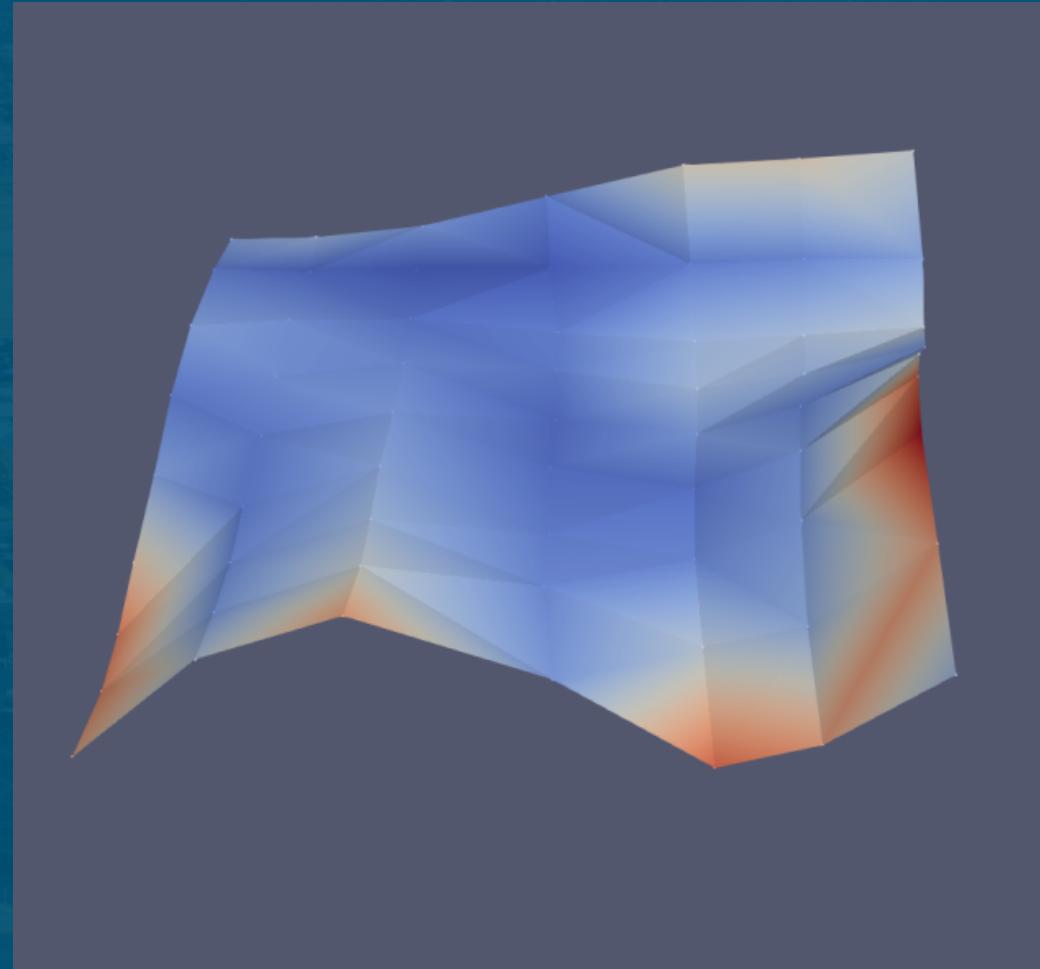
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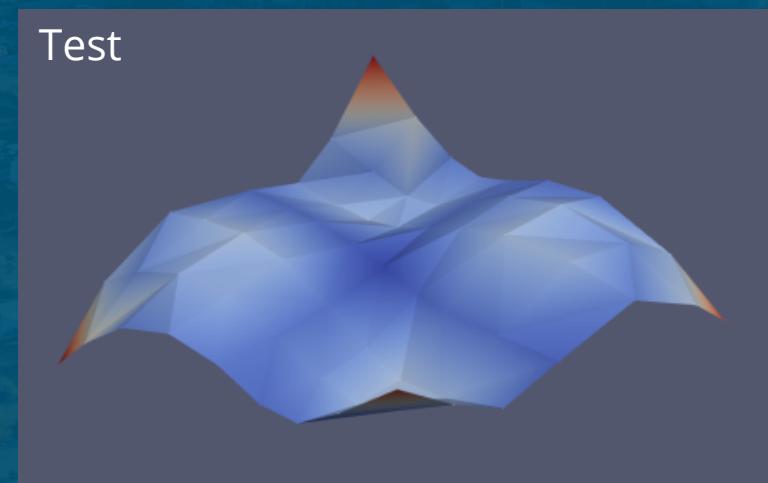
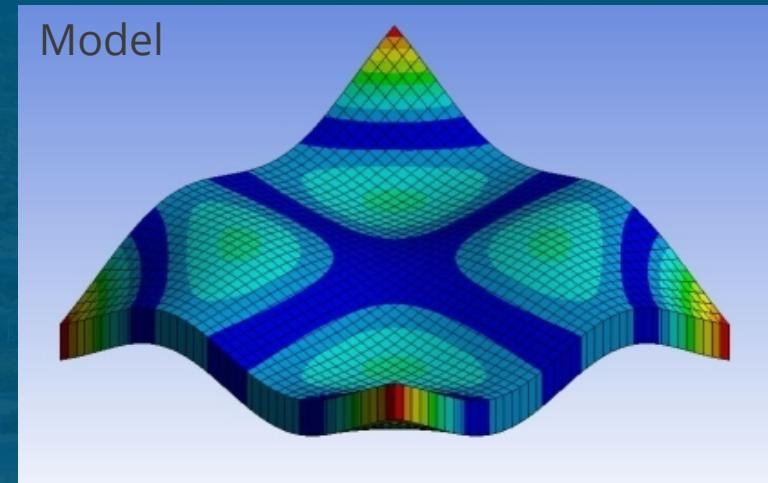
# Validation with Modal Test Data – Mode Shapes



# Validation with Modal Test Data – Mode Shapes



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# Key Takeaways



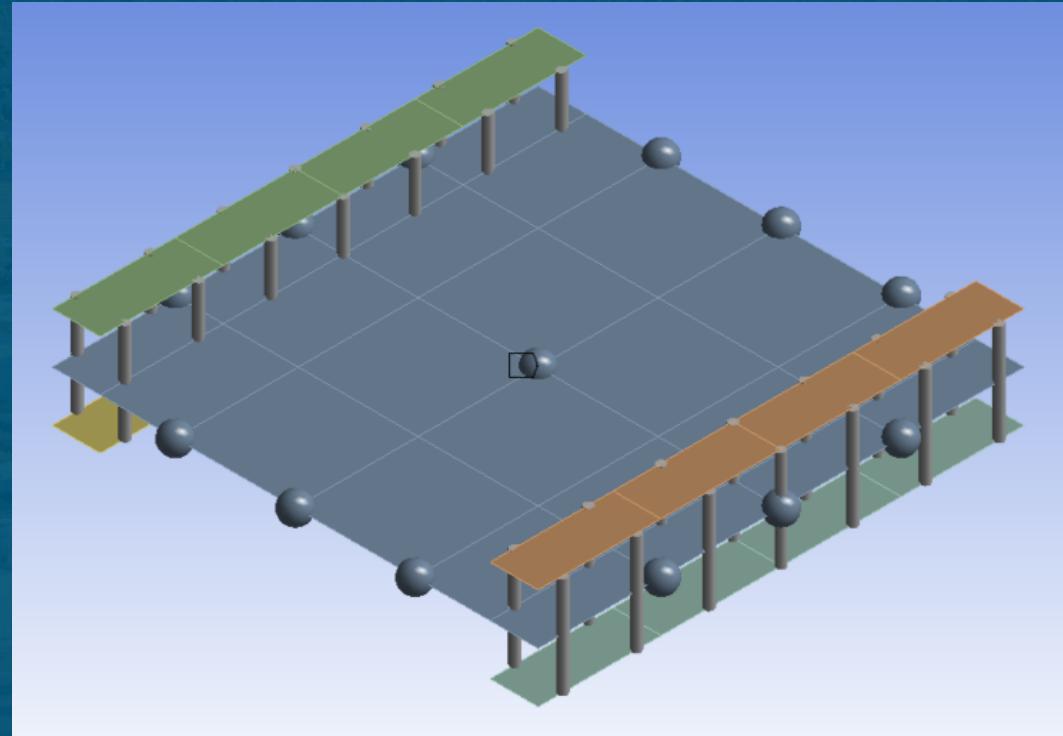
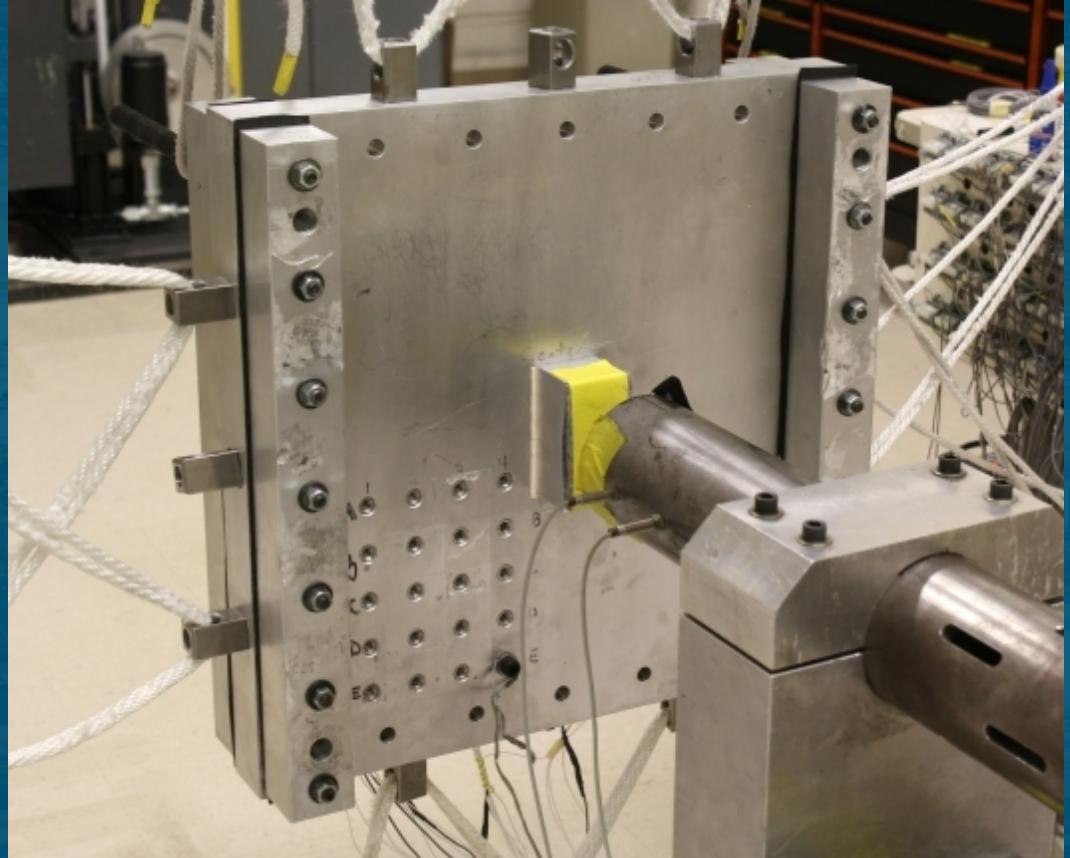
## Model Performance in the Modal Domain

- Relatively accurate up to ~3000 Hz
- Accurate mode shape and frequency for the 1kHz mode
- Some modes did not match with the test very well
  - Not trying to match the test exactly
  - Test had asymmetries (loose bolt)
  - Model for design - asymmetry not desirable

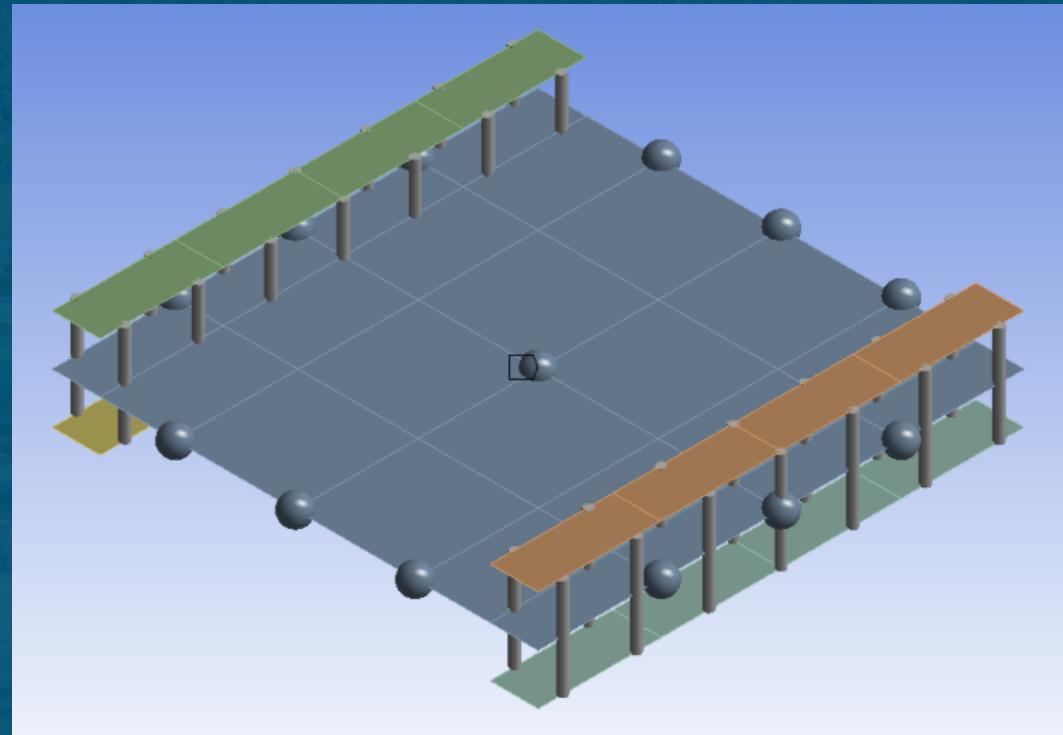
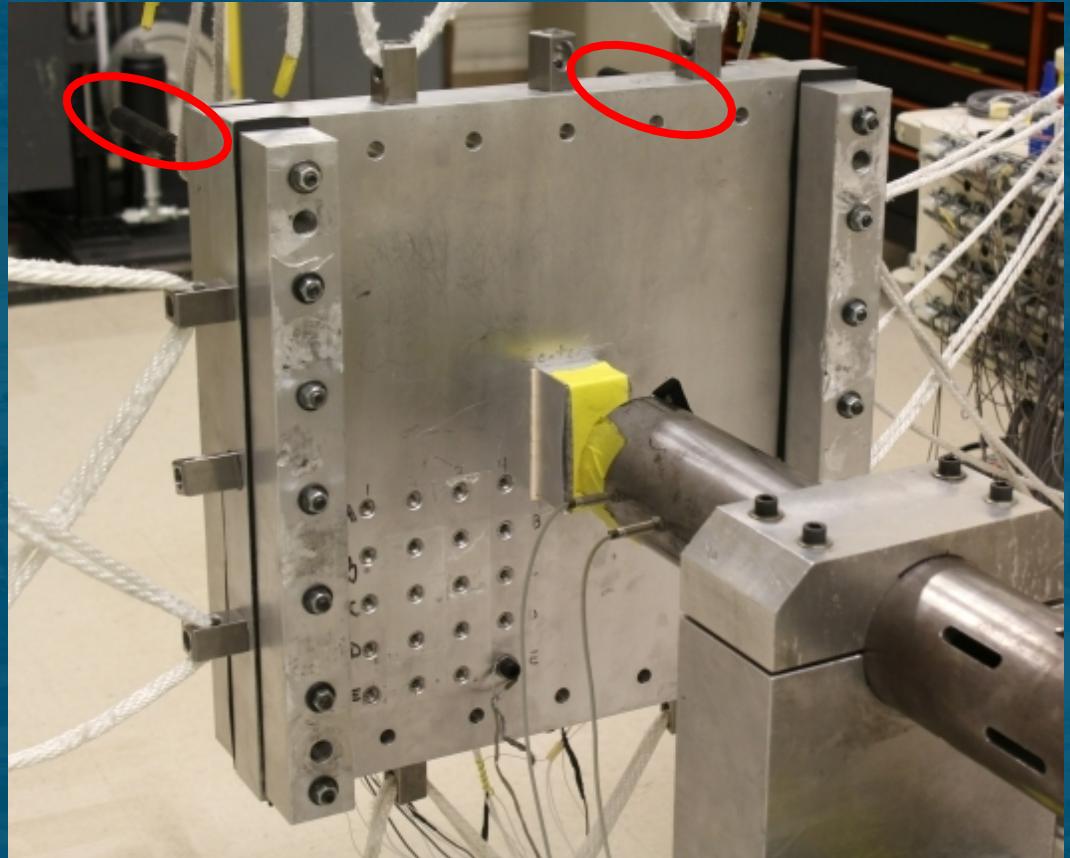
The background of the slide features a wide-angle aerial photograph of a city, likely Linz, Austria, with its characteristic green-roofed buildings. In the distance, a range of mountains is visible under a clear sky.

# Model for the Plate with Damping Bars

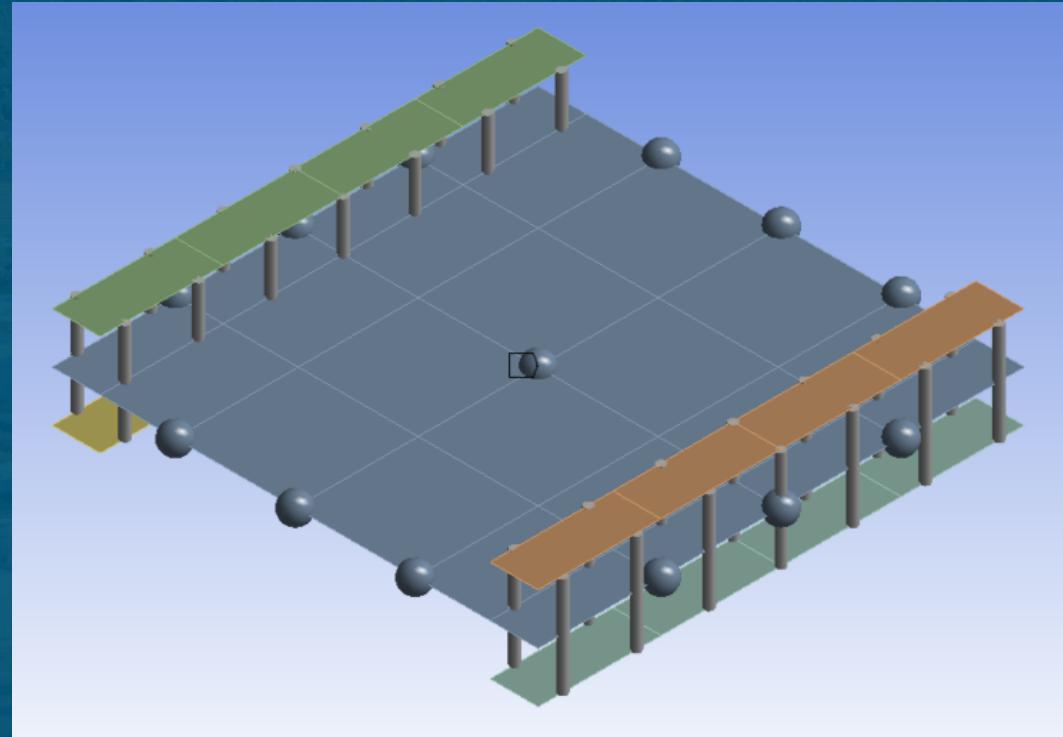
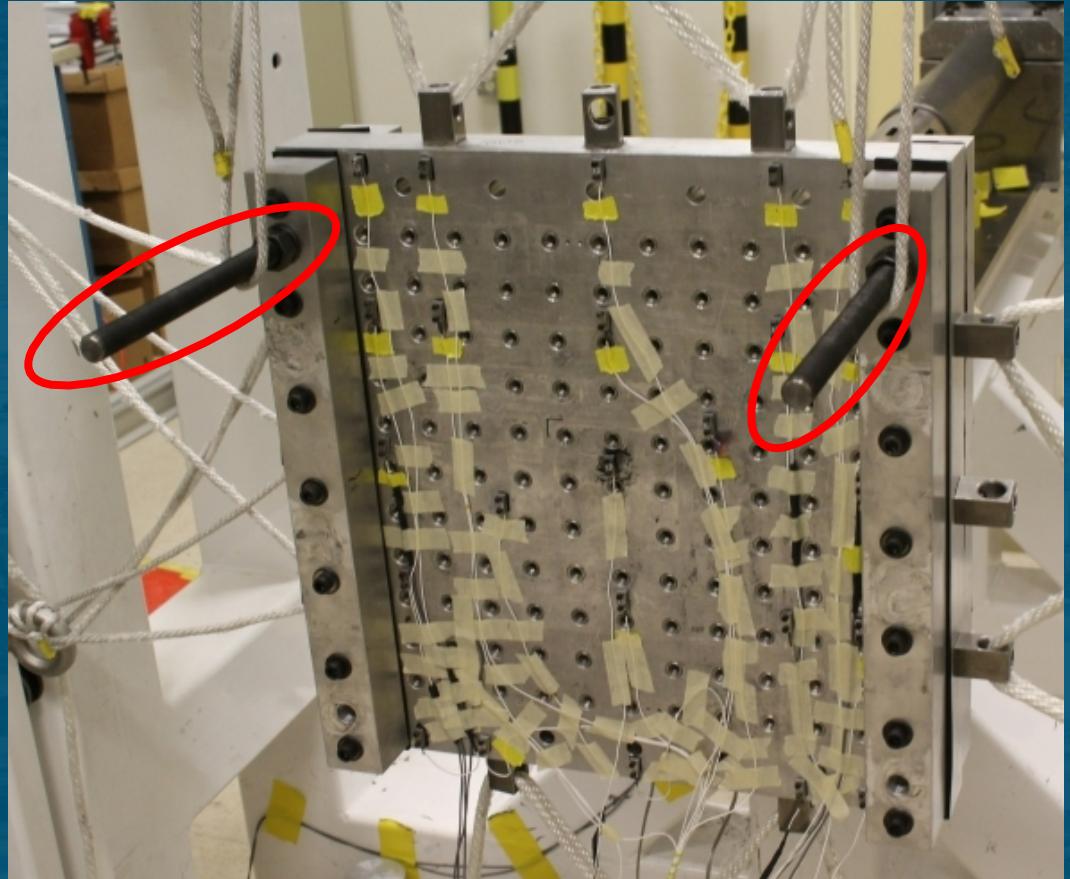
# Model for the Plate with Damping Bars



# Model for the Plate with Damping Bars



# Model for the Plate with Damping Bars



# Validation with Modal Test Data – Test Mode Shapes

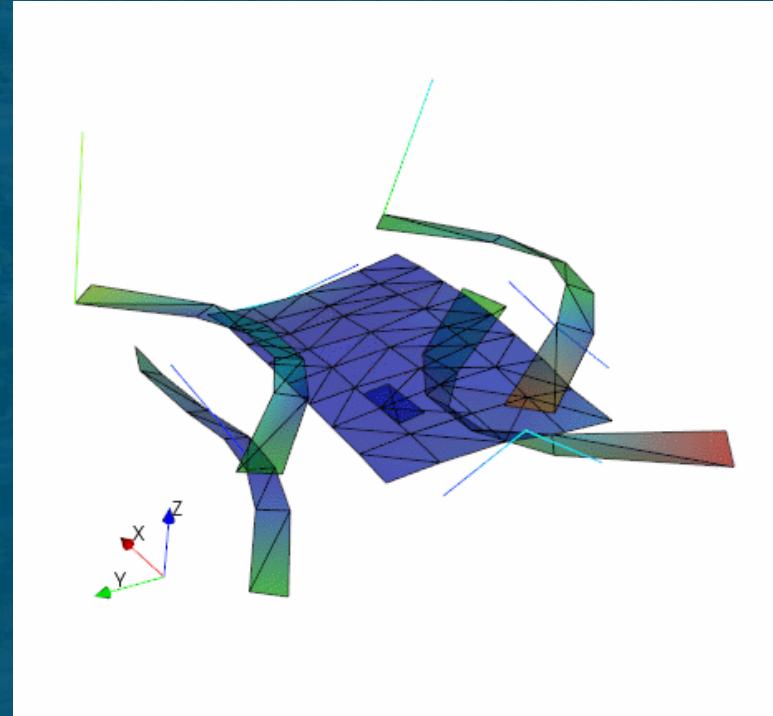
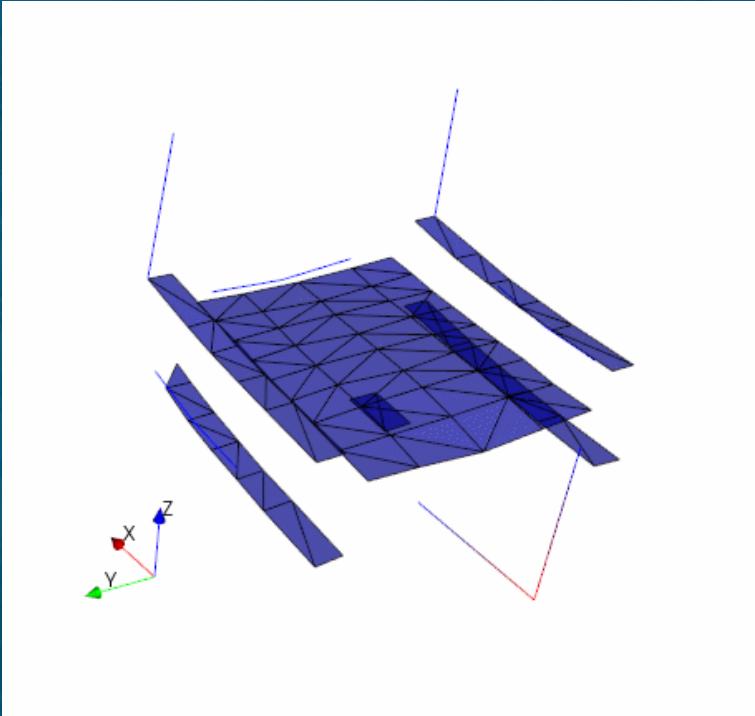
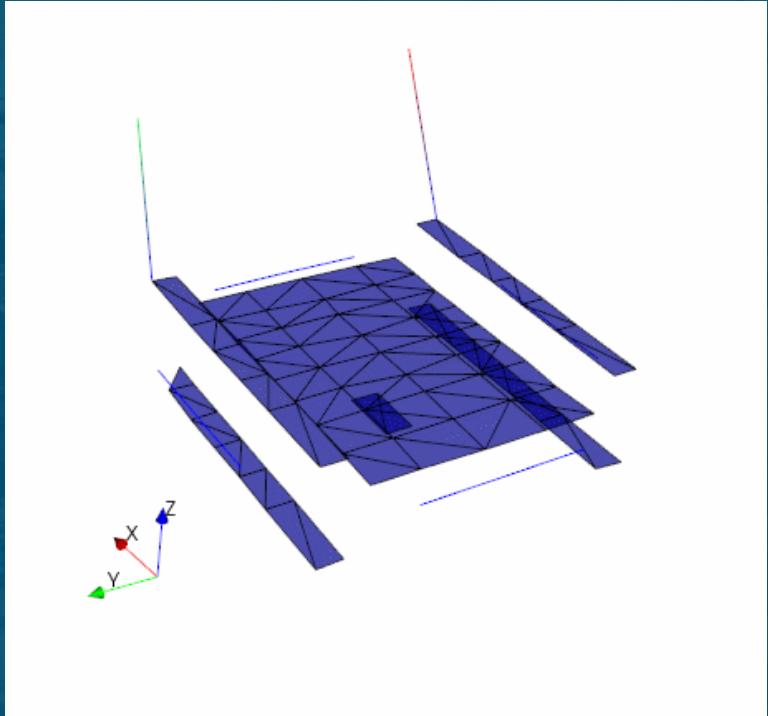


- Compared modes for model and test
- Some modes have very little plate movement

# Validation with Modal Test Data – Test Mode Shapes



- Compared modes for model and test
- Some modes have very little plate movement



## Model

## Test

|        | 390.8 | 582.0 | 1001  | 1288  | 2087  | 2216  | 2345  | 2397  | 2800  |
|--------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| 403.71 | 0.998 | 0.000 | 0.000 | 0.004 | 0.000 | 0.006 | 0.009 | 0.001 | 0.072 |
| 575.3  | 0.000 | 0.991 | 0.023 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 |
| 921.0  | 0.000 | 0.661 | 0.425 | 0.002 | 0.023 | 0.000 | 0.000 | 0.000 | 0.000 |
| 1008.7 | 0.000 | 0.037 | 0.900 | 0.001 | 0.090 | 0.000 | 0.000 | 0.002 | 0.000 |
| 1224.8 | 0.001 | 0.002 | 0.003 | 0.005 | 0.019 | 0.000 | 0.000 | 0.024 | 0.000 |
| 1241.9 | 0.000 | 0.000 | 0.000 | 0.991 | 0.000 | 0.008 | 0.008 | 0.001 | 0.004 |
| 2026.6 | 0.000 | 0.001 | 0.097 | 0.001 | 0.901 | 0.005 | 0.000 | 0.002 | 0.000 |
| 2149.9 | 0.001 | 0.000 | 0.002 | 0.019 | 0.005 | 0.910 | 0.009 | 0.001 | 0.013 |
| 2377.6 | 0.013 | 0.000 | 0.000 | 0.000 | 0.002 | 0.050 | 0.951 | 0.006 | 0.029 |
| 2452.5 | 0.001 | 0.000 | 0.001 | 0.000 | 0.009 | 0.000 | 0.005 | 0.983 | 0.000 |
| 2771.3 | 0.095 | 0.000 | 0.000 | 0.002 | 0.000 | 0.001 | 0.027 | 0.002 | 0.873 |

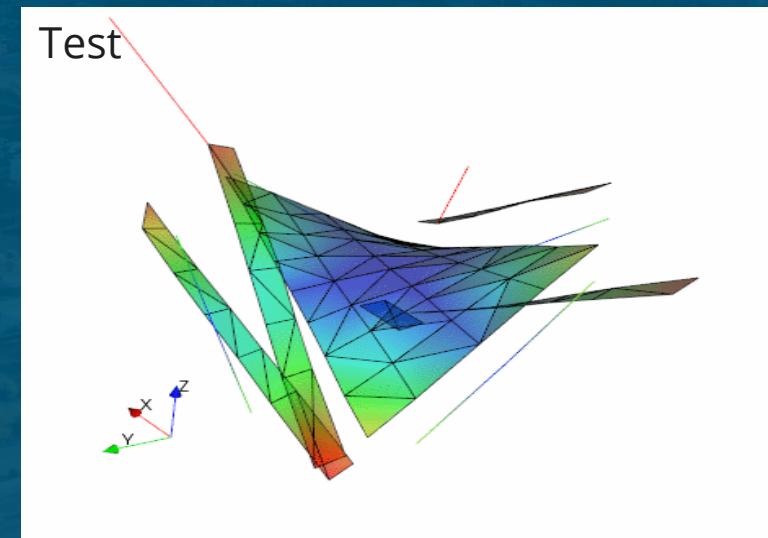
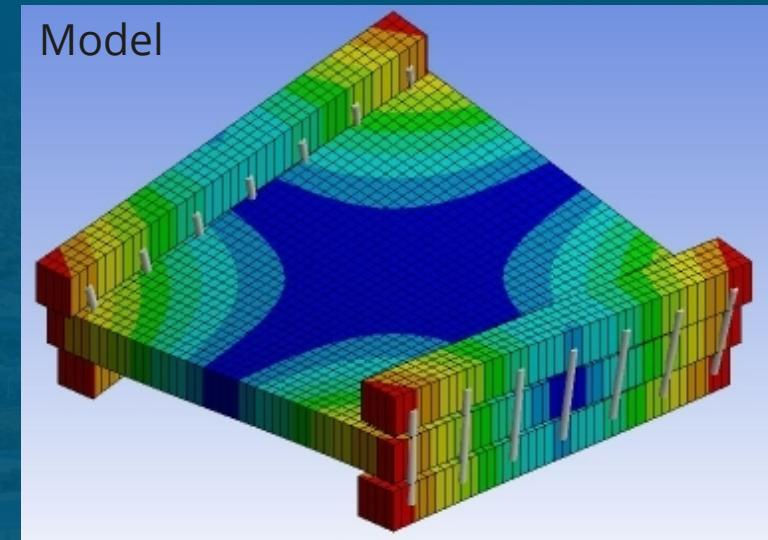
| Frequency<br>% Difference |
|---------------------------|
| 3.31%                     |
| 1.16%                     |
| -----                     |
| 0.72%                     |
| -----                     |
| 3.58%                     |
| 2.90%                     |
| 2.96%                     |
| 1.39%                     |
| 2.30%                     |
| 1.01%                     |



# Validation with Modal Test Data – Mode Shapes & MAC



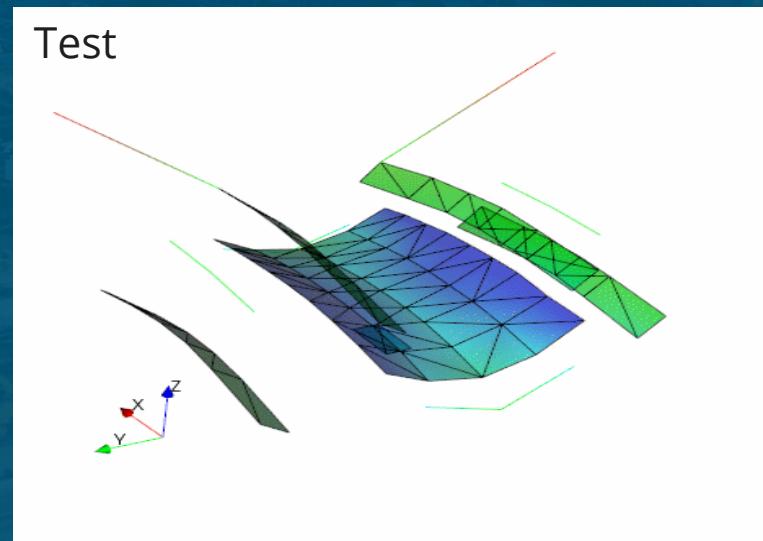
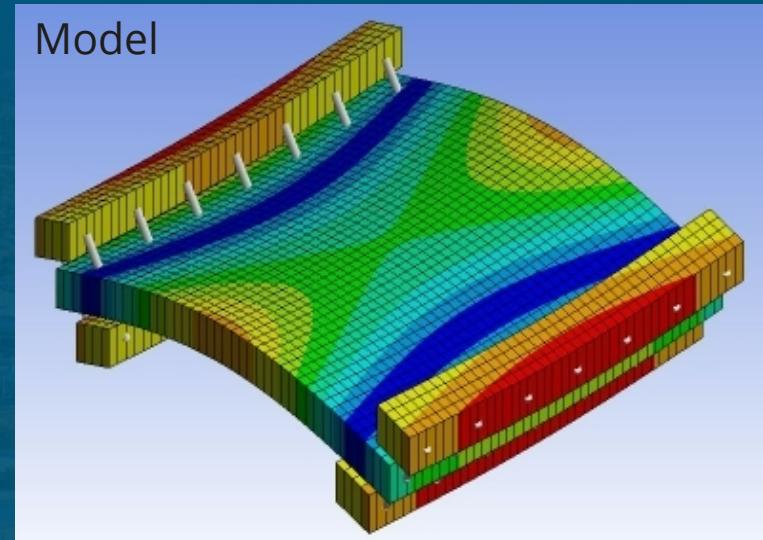
| Model Frequencies (Hz) | Test Frequencies (Hz) | % Difference | MAC Value |
|------------------------|-----------------------|--------------|-----------|
| 403.7                  | 390.8                 | 3.31         | 0.998     |
| 575.3                  | 582.0                 | 1.16         | 0.991     |
| 921.0                  | -----                 | -----        | -----     |
| 1008.7                 | 1001.5                | 0.72         | 0.900     |
| 1224.8                 | -----                 | -----        | -----     |
| 1241.9                 | 1288.0                | 3.58         | 0.991     |
| 2026.6                 | 2087.2                | 2.90         | 0.901     |
| 2149.9                 | 2215.5                | 2.96         | 0.910     |
| 2377.6                 | 2345.0                | 1.39         | 0.951     |
| 2452.5                 | 2397.4                | 2.30         | 0.983     |
| 2771.3                 | 2799.5                | 1.01         | 0.873     |



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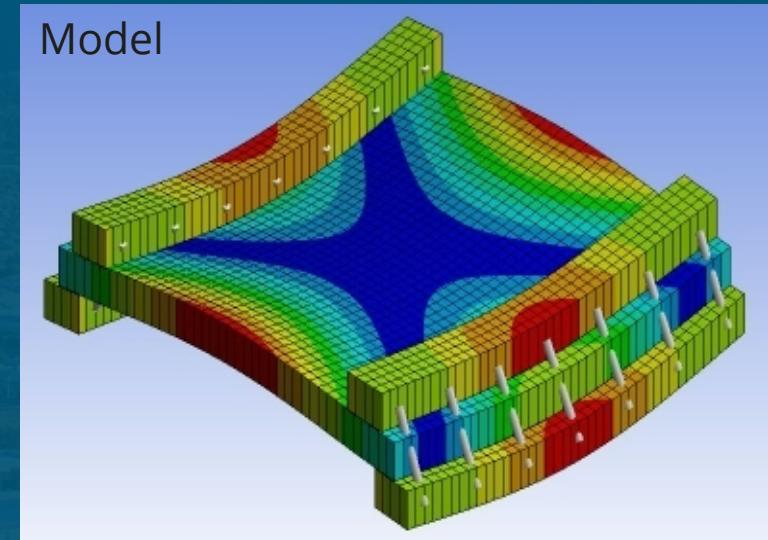
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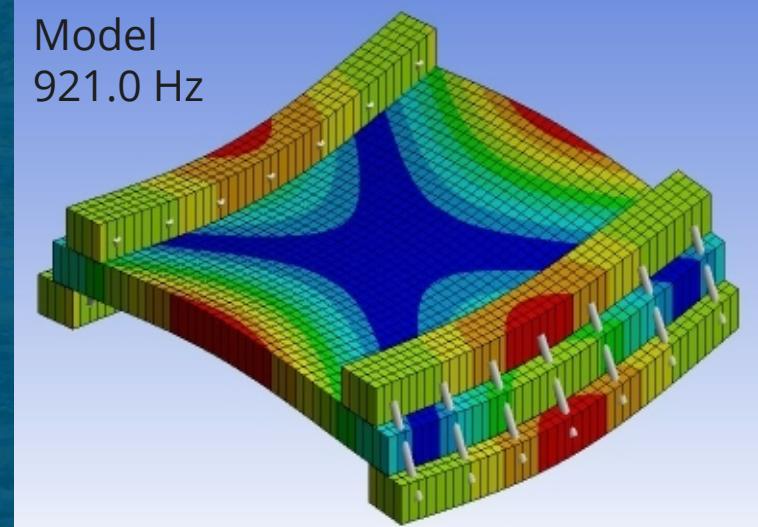
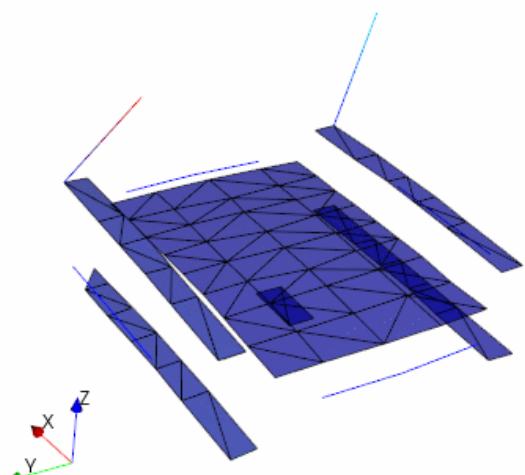
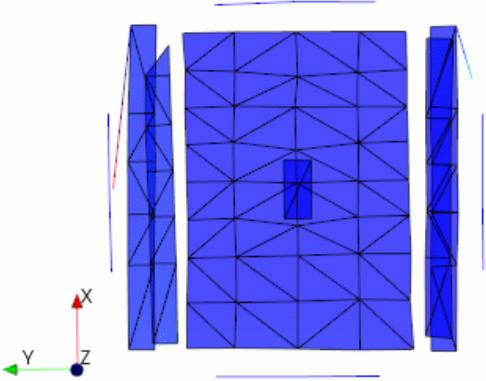
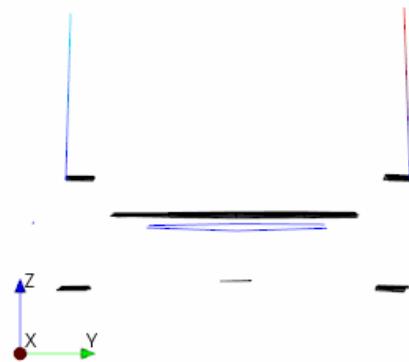
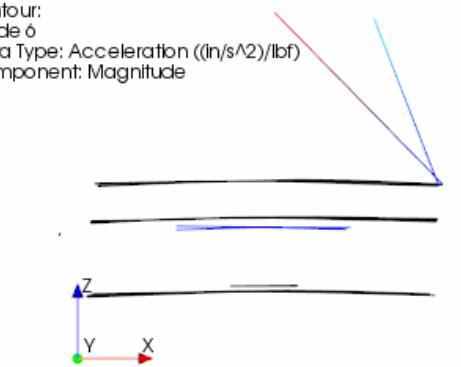
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Test

Displacement:  
Mode 6  
Component: Magnitude  
Frequency: 922.763 Hz  
Damping: 1.181 %Cr  
IDLine1: Generated from reference 1000X-  
IDLine4:

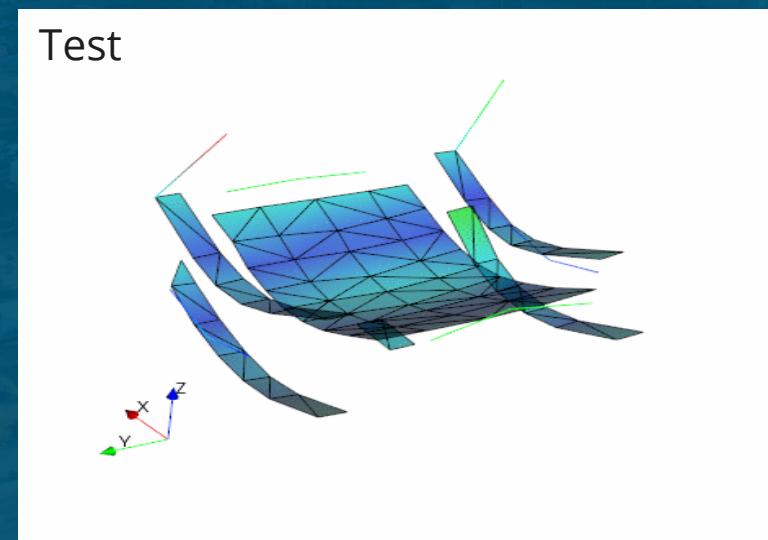
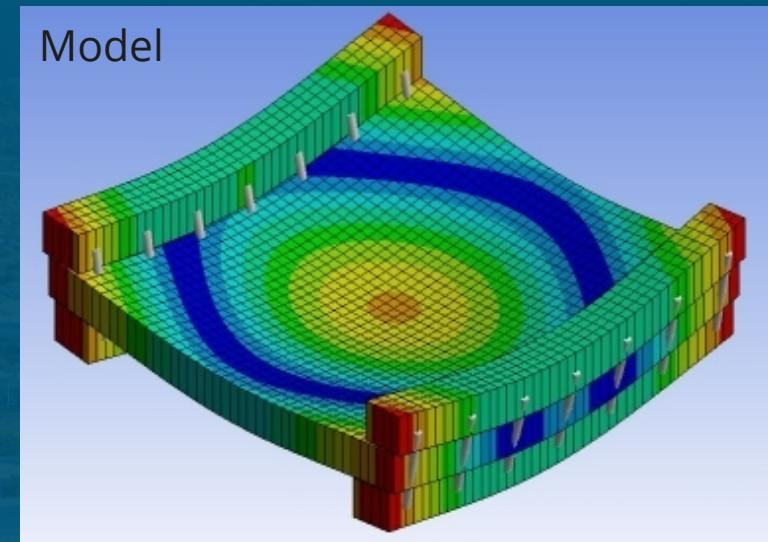
Contour:  
Mode 6  
Data Type: Acceleration ((in/s<sup>2</sup>)/lbf)  
Component: Magnitude



# Validation with Modal Test Data – Mode Shapes & MAC



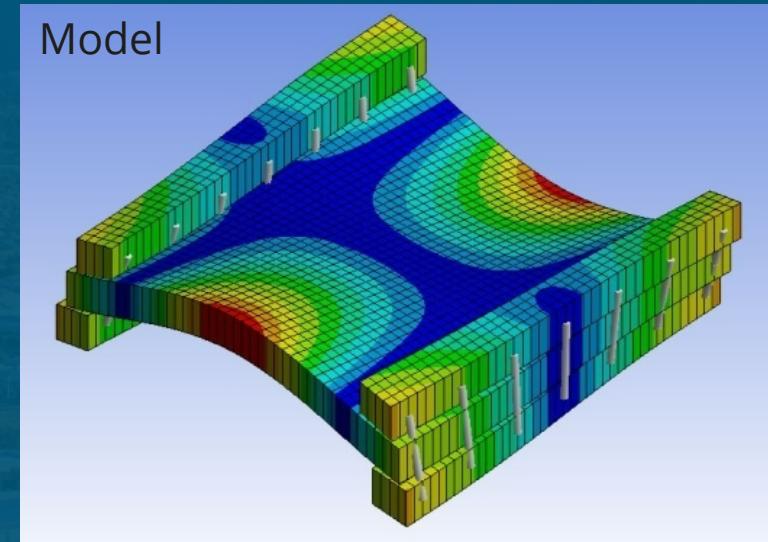
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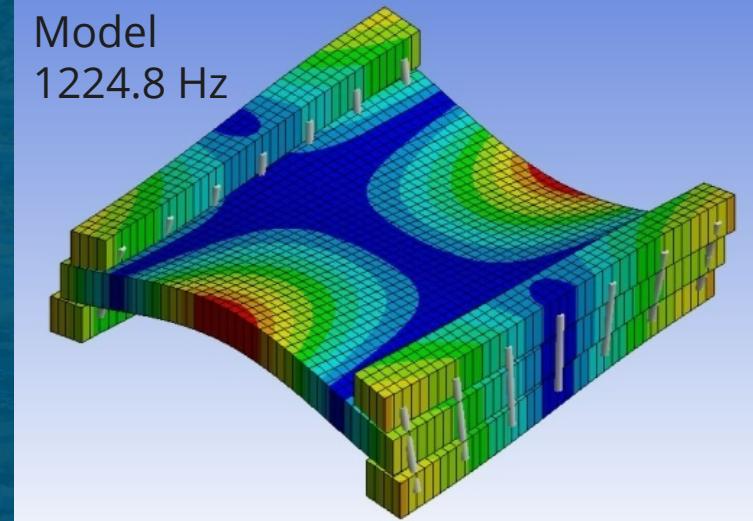
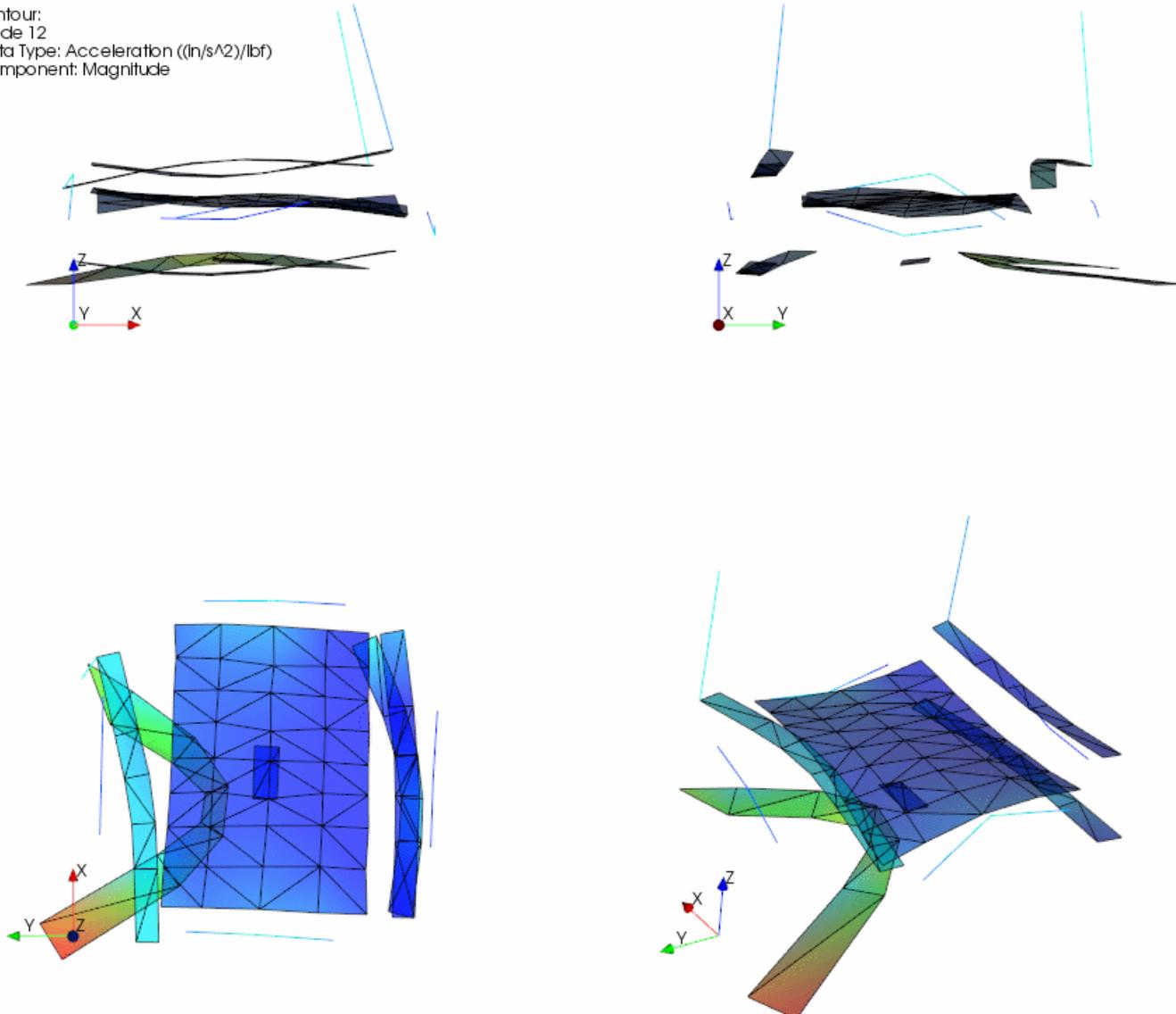


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| 2452.5                 | 2397.4                | 2.30         | 0.983     |
| 2771.3                 | 2799.5                | 1.01         | 0.873     |



Displacement:  
Mode 12  
Component: Magnitude  
Frequency: 1377.750 Hz  
Damping: 1.724 %Cr  
IDLine1: Generated from reference 1000X-  
IDLine4:

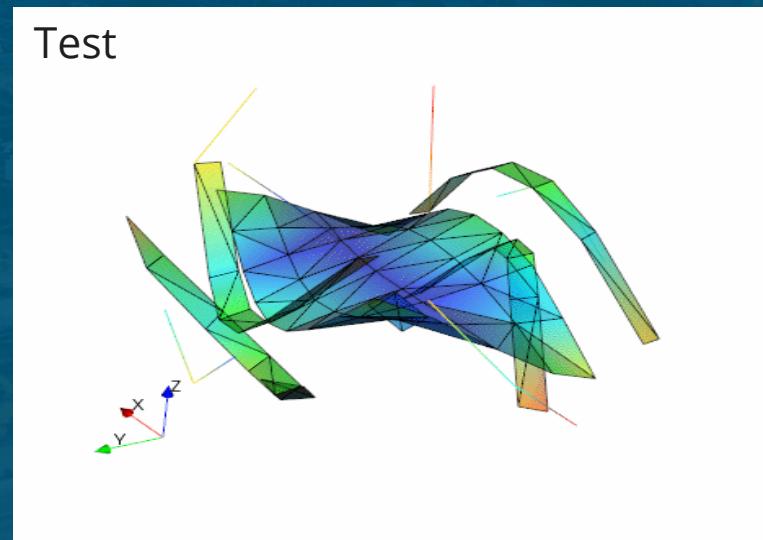
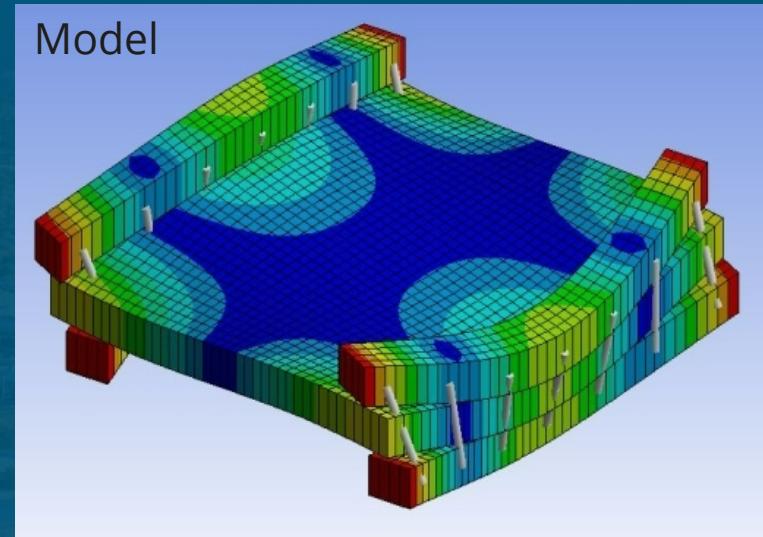
Contour:  
Mode 12  
Data Type: Acceleration ((in/s<sup>2</sup>)/lbf)  
Component: Magnitude



# Validation with Modal Test Data – Mode Shapes & MAC



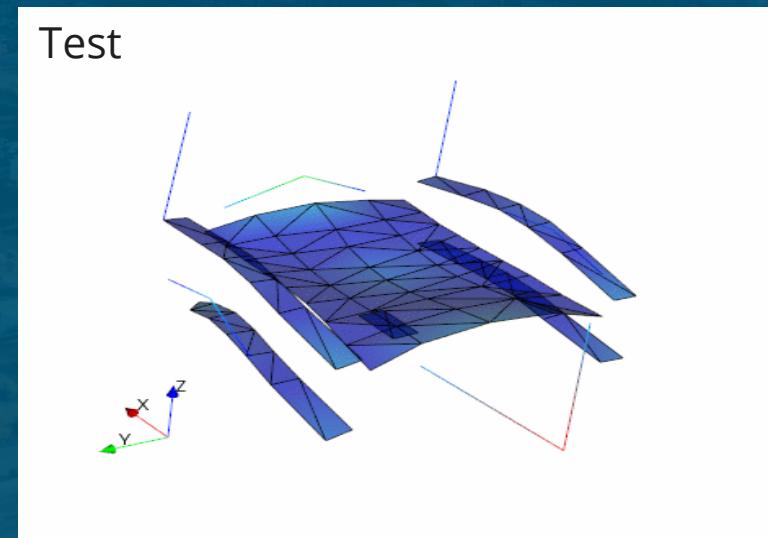
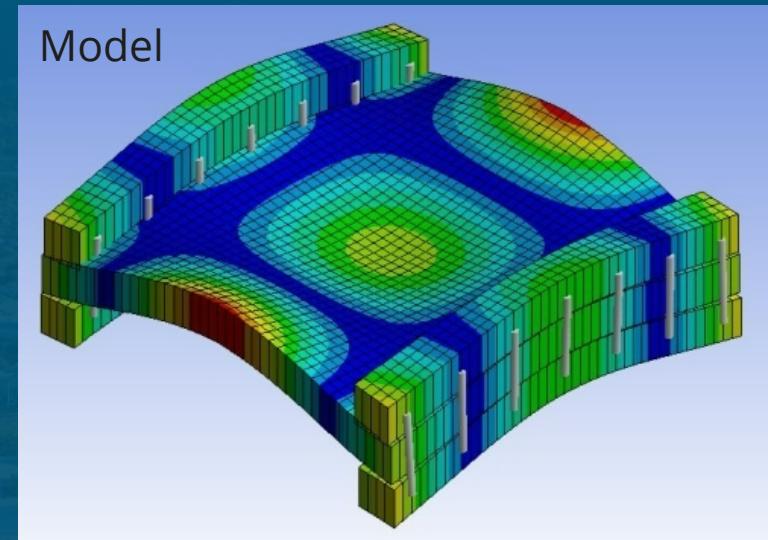
| Model Frequencies (Hz) | Test Frequencies (Hz) | % Difference | MAC Value |
|------------------------|-----------------------|--------------|-----------|
| 403.7                  | 390.8                 | 3.31         | 0.998     |
| 575.3                  | 582.0                 | 1.16         | 0.991     |
| 921.0                  | -----                 | -----        | -----     |
| 1008.7                 | 1001.5                | 0.72         | 0.900     |
| 1224.8                 | -----                 | -----        | -----     |
| 1241.9                 | 1288.0                | 3.58         | 0.991     |
| 2026.6                 | 2087.2                | 2.90         | 0.901     |
| 2149.9                 | 2215.5                | 2.96         | 0.910     |
| 2377.6                 | 2345.0                | 1.39         | 0.951     |
| 2452.5                 | 2397.4                | 2.30         | 0.983     |
| 2771.3                 | 2799.5                | 1.01         | 0.873     |



# Validation with Modal Test Data – Mode Shapes & MAC



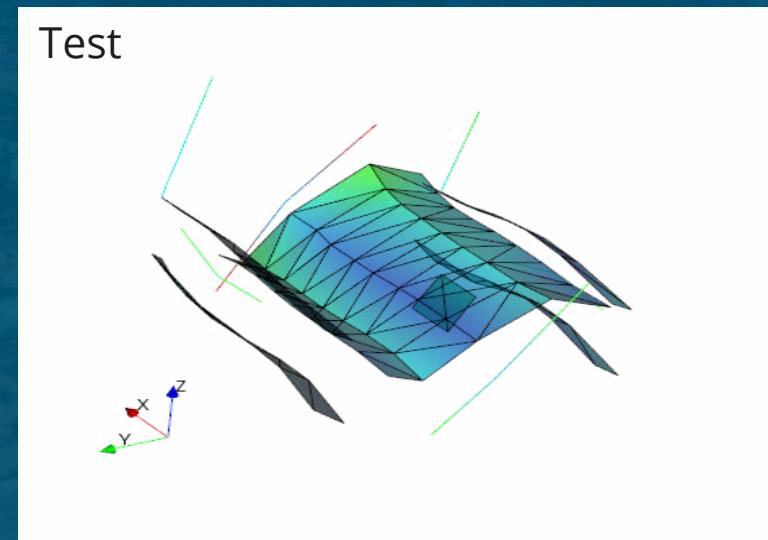
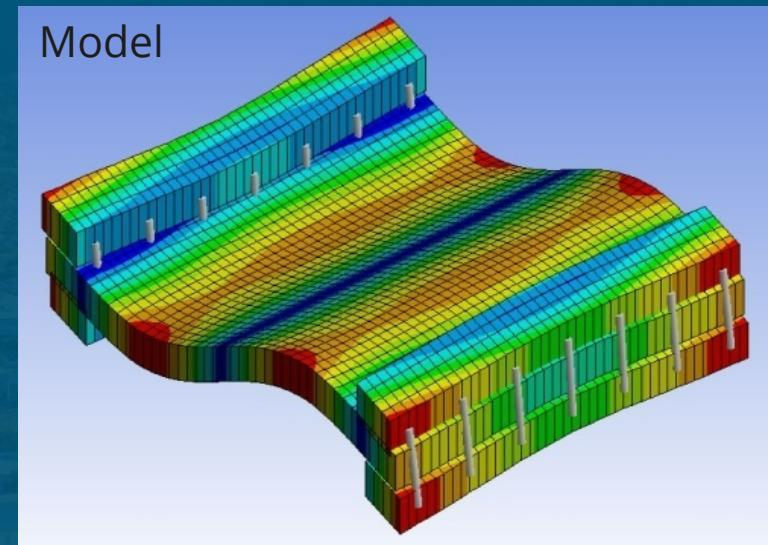
| Model Frequencies (Hz) | Test Frequencies (Hz) | % Difference | MAC Value |
|------------------------|-----------------------|--------------|-----------|
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| 575.3                  | 582.0                 | 1.16         | 0.991     |
| 921.0                  | -----                 | -----        | -----     |
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| 2452.5                 | 2397.4                | 2.30         | 0.983     |
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# Validation with Modal Test Data – Mode Shapes & MAC



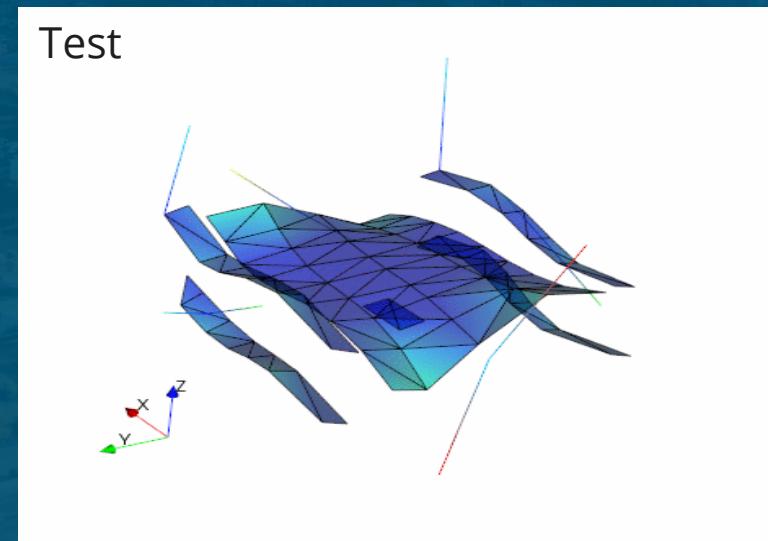
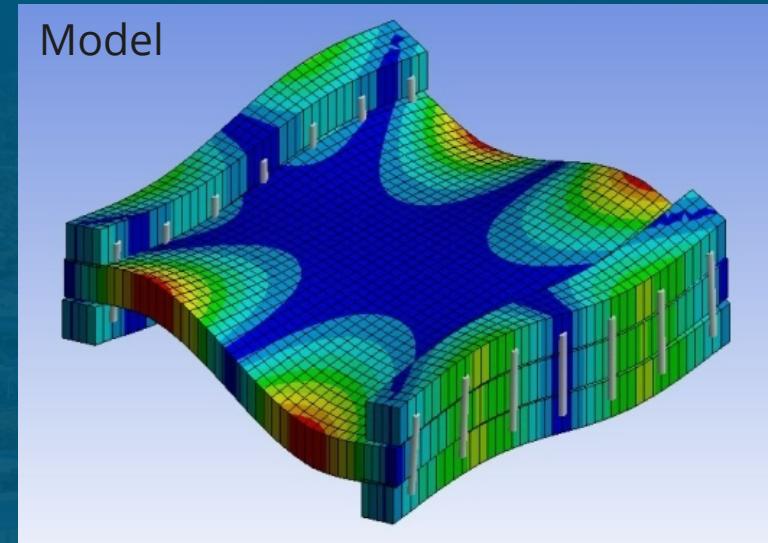
| Model Frequencies (Hz) | Test Frequencies (Hz) | % Difference | MAC Value |
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| 403.7                  | 390.8                 | 3.31         | 0.998     |
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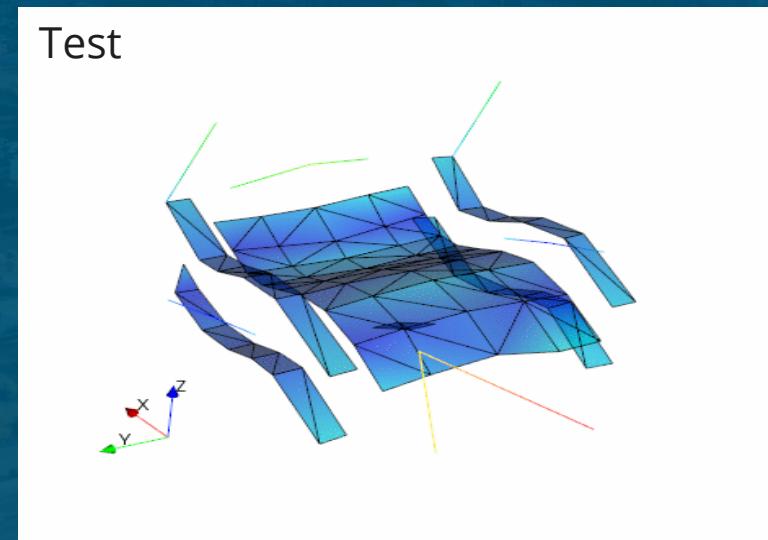
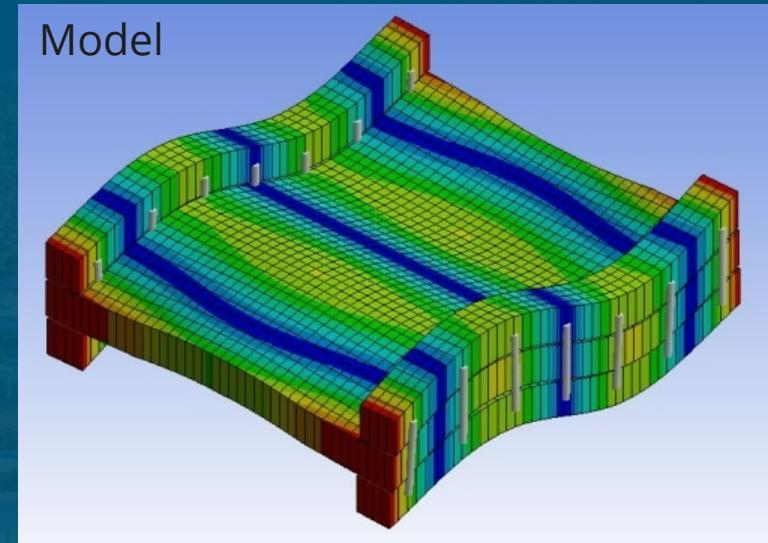
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|------------------------|-----------------------|--------------|-----------|
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| 1241.9                 | 1288.0                | 3.58         | 0.991     |
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# Validation with Modal Test Data – Mode Shapes & MAC



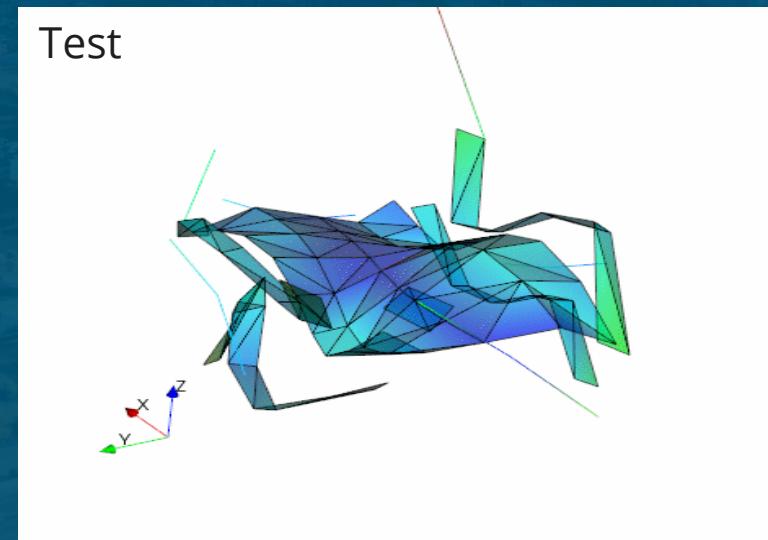
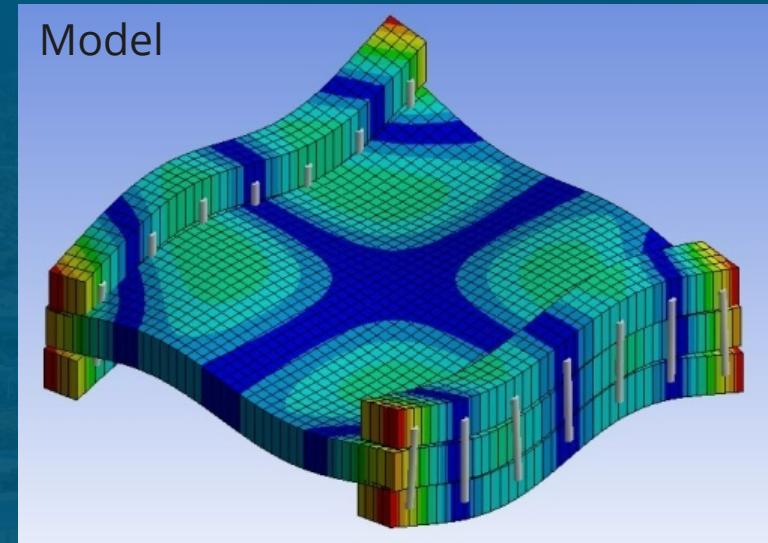
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# Validation with Modal Test Data – Mode Shapes & MAC



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| 2452.5                 | 2397.4                | 2.30         | 0.983     |
| 2771.3                 | 2799.5                | 1.01         | 0.873     |





## Model Performance in the Modal Domain

- Relatively accurate up to ~3000 Hz
  - Not as good as the bare plate model
- Accurate mode shape and frequency for the 1kHz mode
- Some modes did not match with the test
  - Not trying to match the test exactly
  - Possibly caused by simplifications

# Acknowledgements



## Co-authors and Mentors

- Vit Babuska, Dave Soine, and Daniel Lee

## Sandia Co-workers

- Tyler Schoenherr, Bryan Witt, Ron Hopkins, Forrest Arnold, Tino Arias, Dylan Landry, and Kevin Brenner