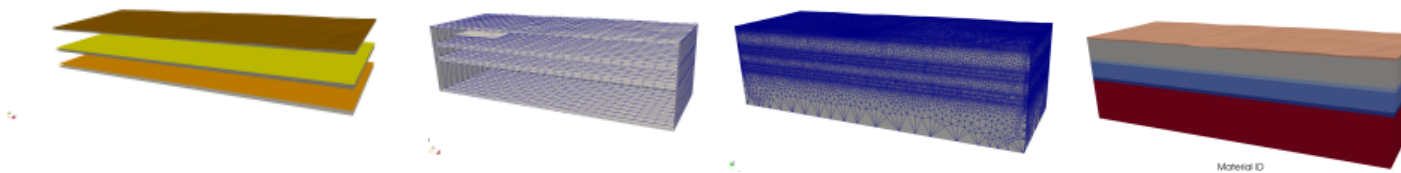
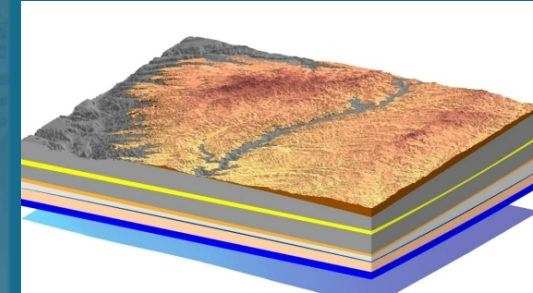




Automated Meshing for Simulations of Subsurface Contaminants



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Sept 1, 2022

Outline



Why is fully-automated meshing and simulation model building important?

Why Voronoi meshes (and what are they)?

A shale geological model

Tracer transport in the subsurface

Results of uncertainty simulations

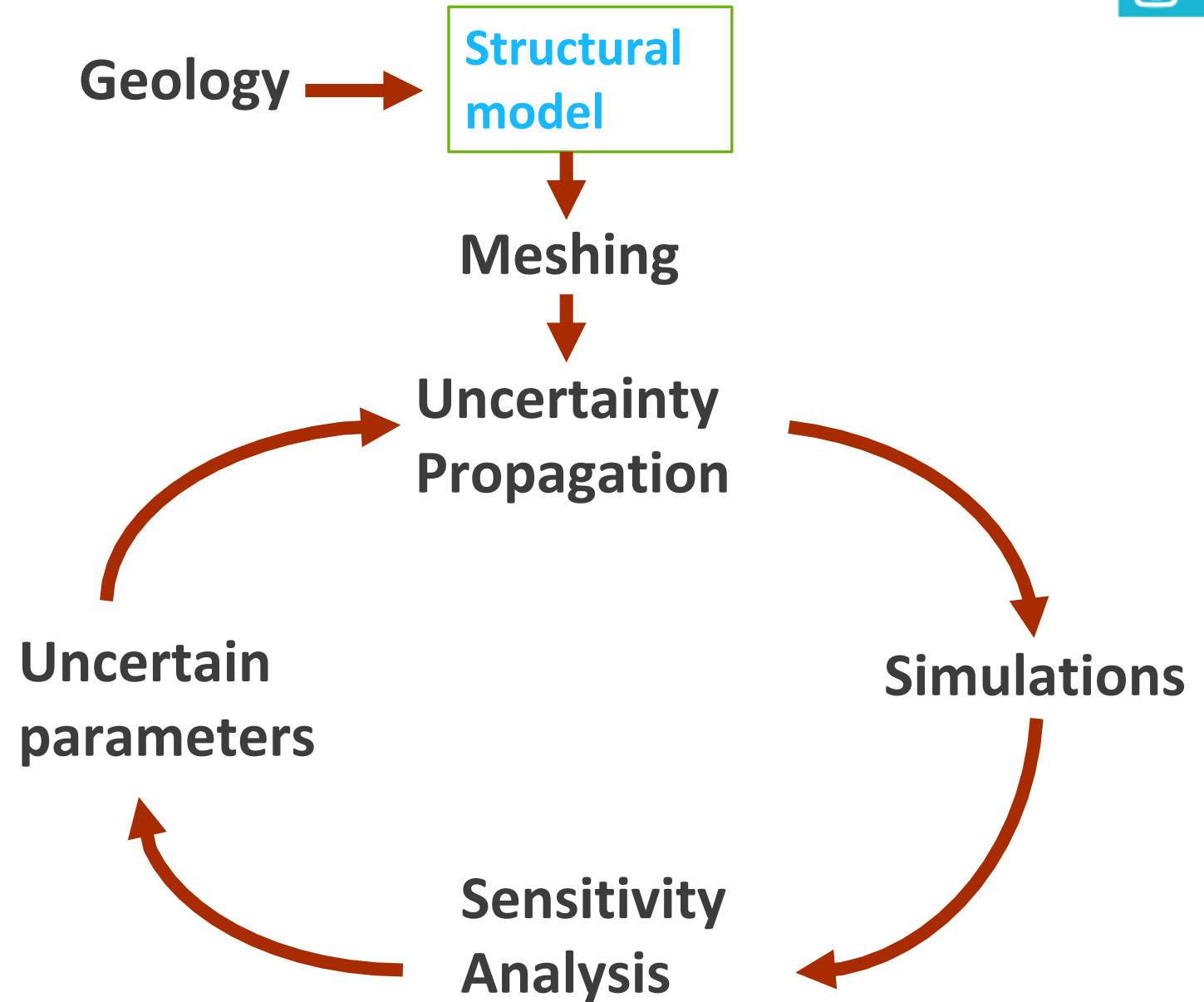
Conclusions and future work

Why Automate?

Sensitivity Analysis and Uncertainty Quantification (SA/UQ) can require hundreds or thousands of model iterations

Uncertainty in geological structure and numerical error introduced by the mesh are often neglected because model and mesh building are difficult and human-time intensive

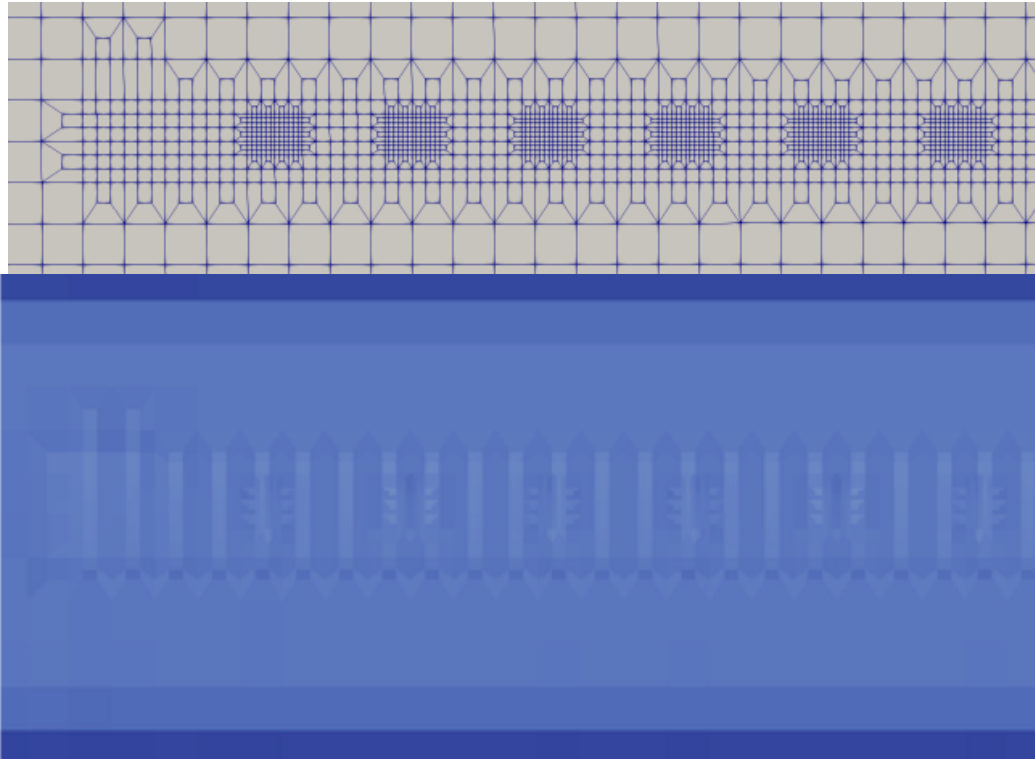
Yet geological structure can have a **first-order impact** on subsurface flow and transport processes



Why Voronoi meshes?

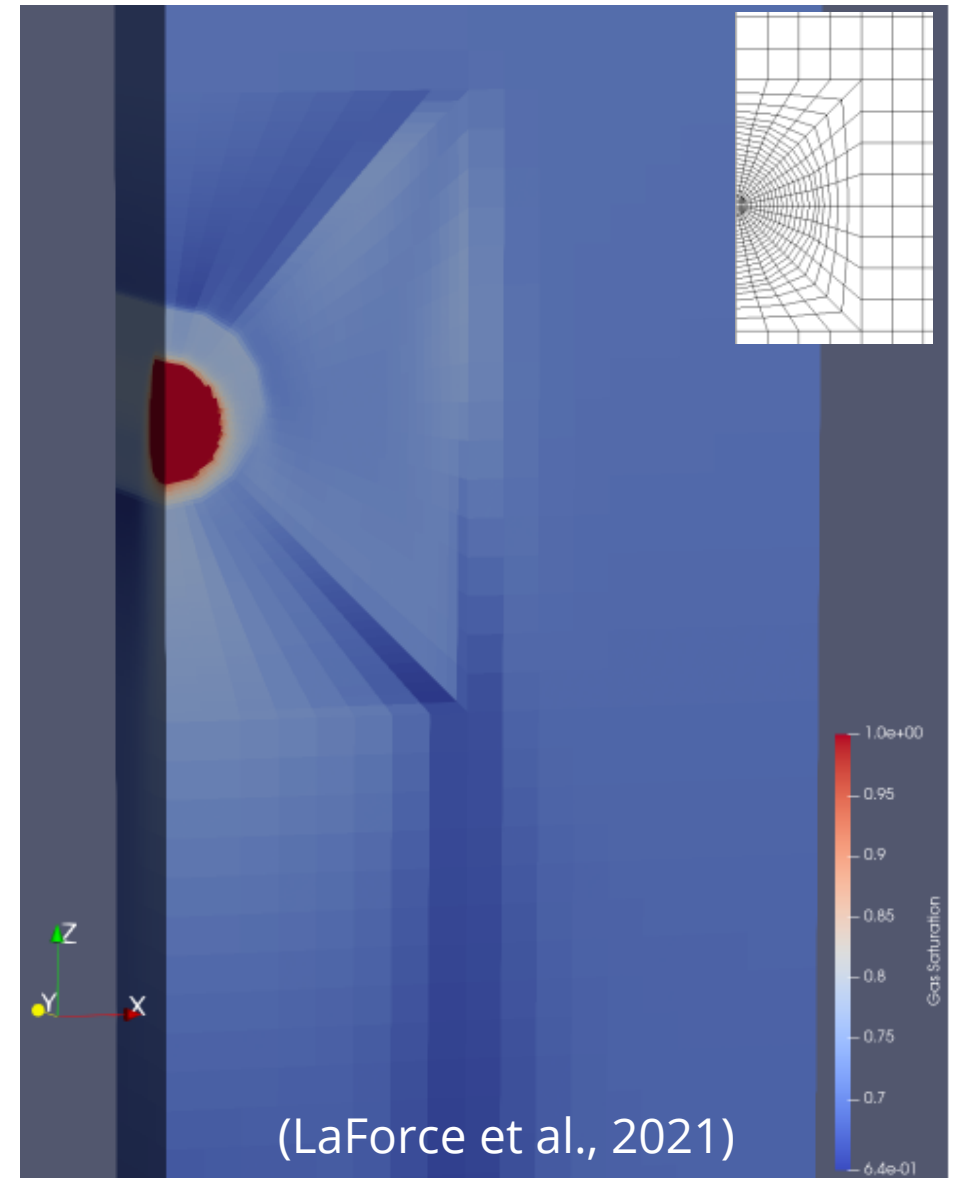
They rigorously honor complex geometries...

...without introducing non-orthogonal fluxes in simulations



Equilibration of an unsaturated heterogeneous model with infiltration using a refined hexahedral mesh.

Gas saturation around a heat source in an unsaturated model using a flexed hexahedral mesh.



(LaForce et al., 2021)

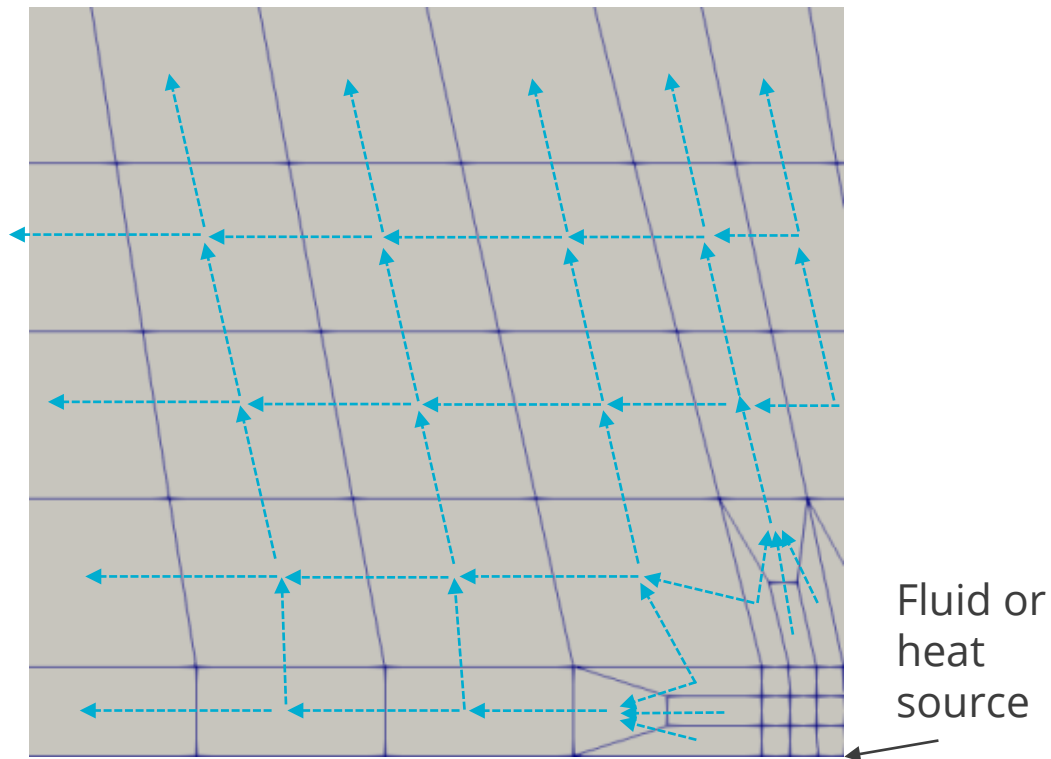


Why Voronoi meshes?



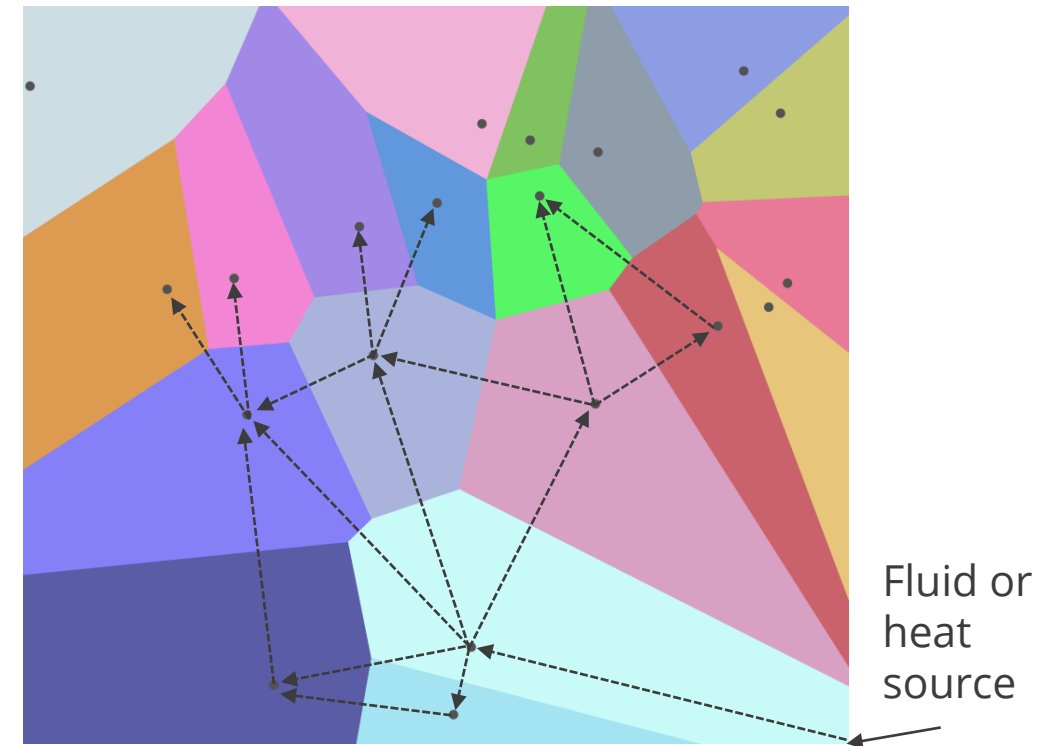
Grid refinement or flexing can bias flow directions

Non-orthogonal fluxes cause errors in two point flux approximation simulations



Fluxes are perpendicular to grid cell faces using Voronoi polyhedral cells

Solvers using two point flux approximation (TOUGH2/PFLOTRAN/FEHM) get accurate results

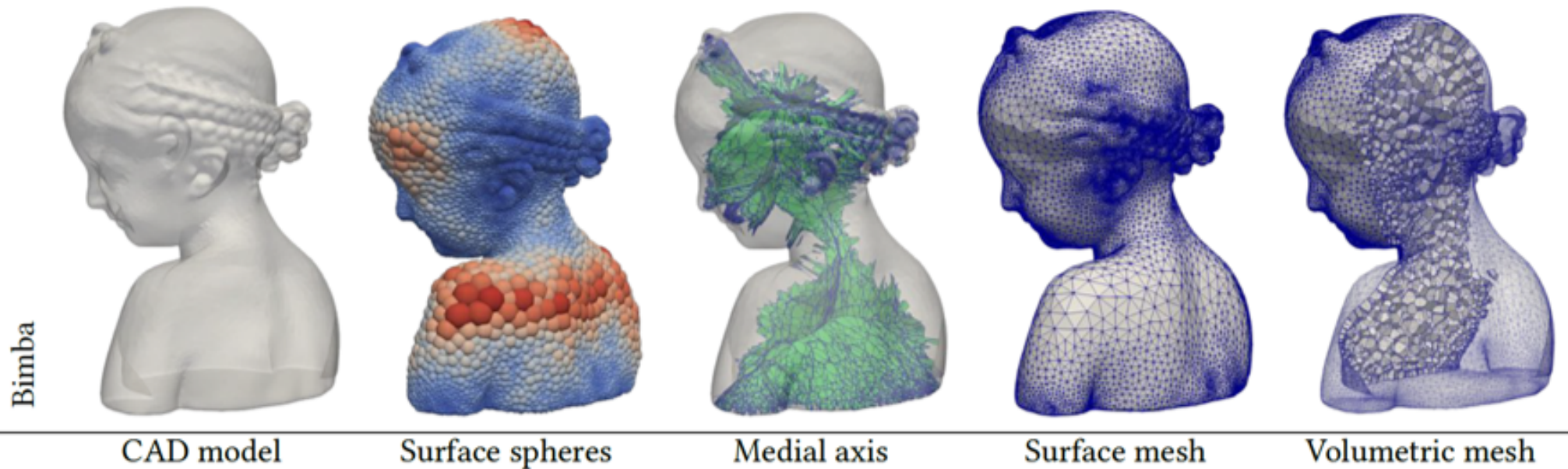


By Balu Ertl - Own work, CC BY-SA 4.0,
<https://commons.wikimedia.org/w/index.php?curid=38534275>

VoroCrust-Meshing Voronoi Meshes



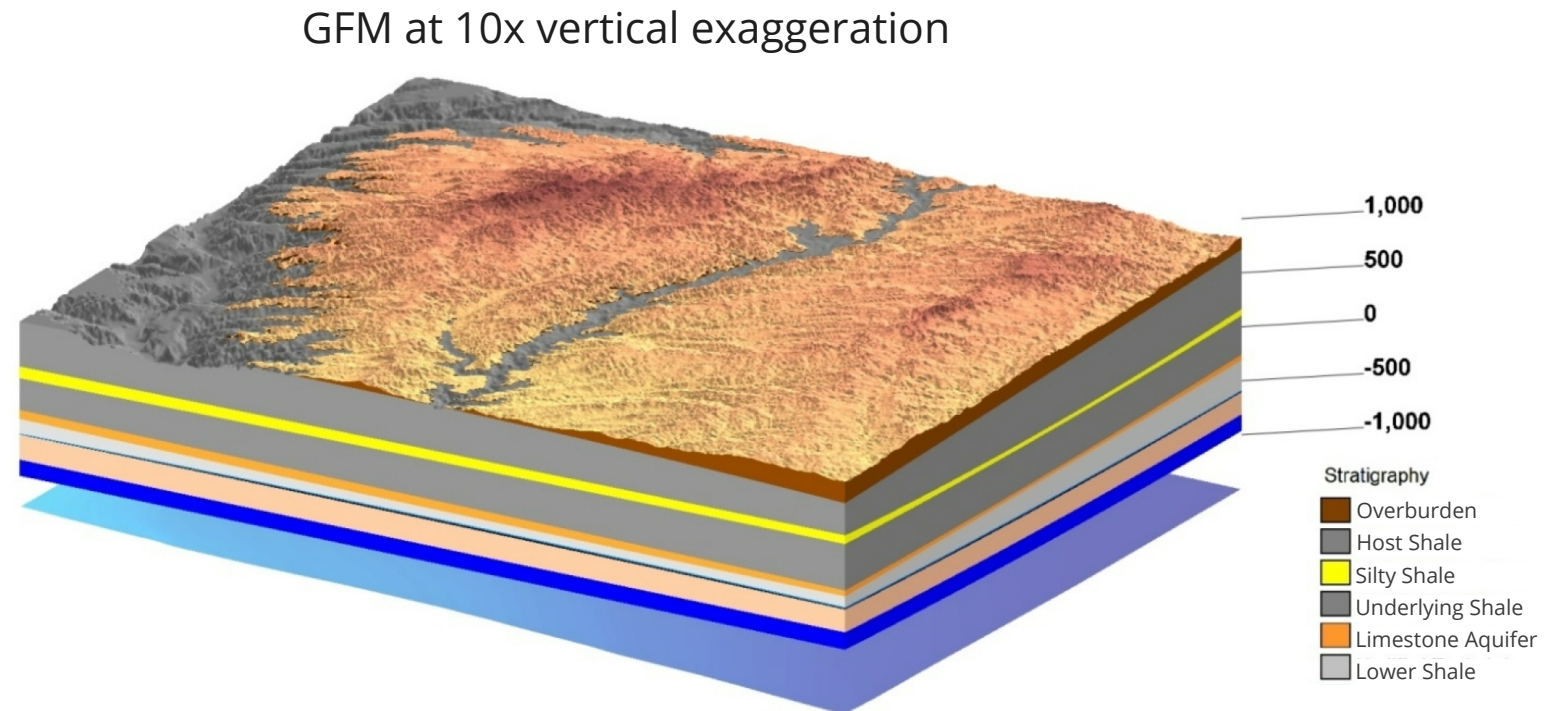
- Accepts as input
 - Any water-tight set of volumes
 - Desired monitoring points
 - Mesh refinement locations
- Fully automated mesh generation
- Surface mesh is triangular
- Interior elements are polyhedral
- Mesh is randomly generated so each VoroCrust run gives a new mesh



Shale Geological Framework Model



- Single realization of a Pierre Shale Geological Framework Model (GFM) 69 x 83 km
- Pseudo-uncertain models are generated by clipping 7 × 2.5 km sub-models from GFM
- All models must have:
 - At least 15 m dip downward in positive x-direction
 - Surface sediment present over entire model
- 87 prospective geological models created
- 10 models will be randomly sampled in Dakota and populated with parameters

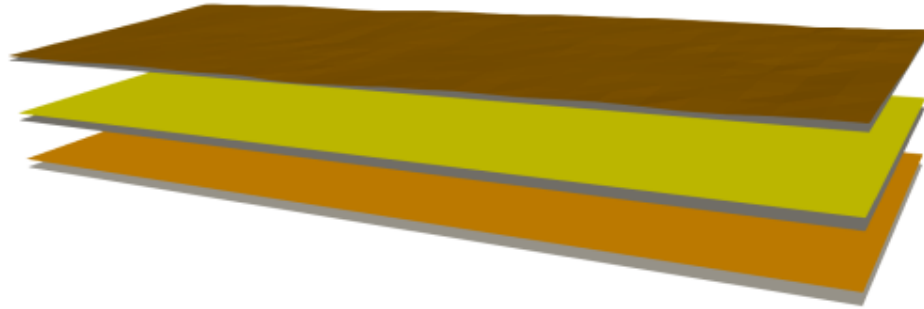


(Sevougian et al, 2019;
LaForce et al. 2022b)

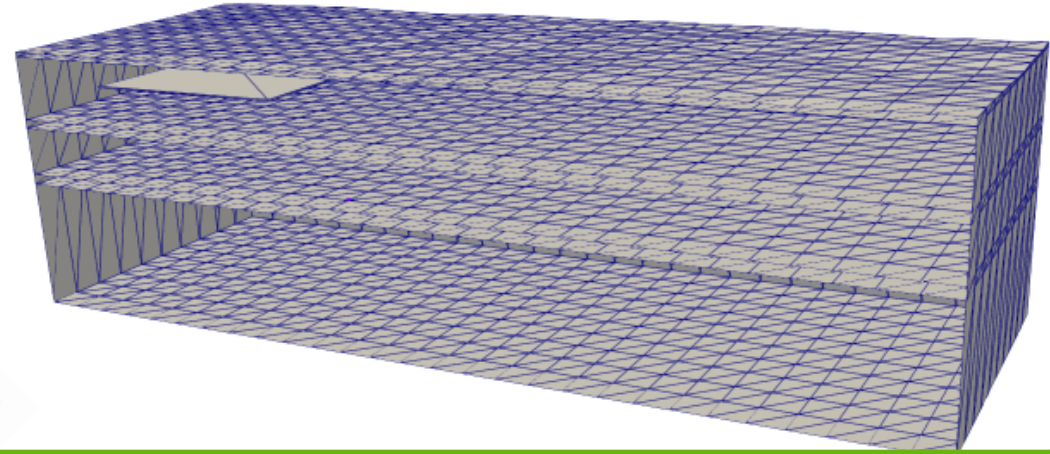
Meshing and Simulating Realization 1



Clip surfaces from GFM (Python3)

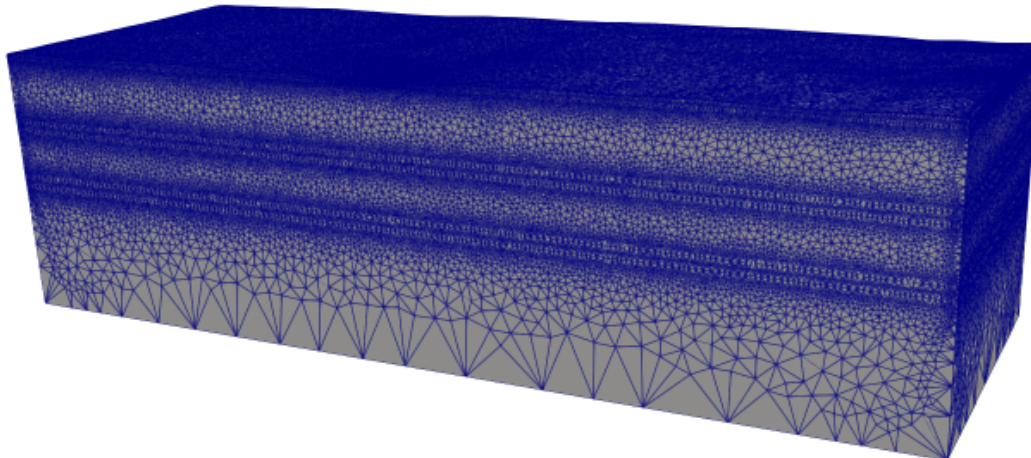


Create model volumes (LaGriT)

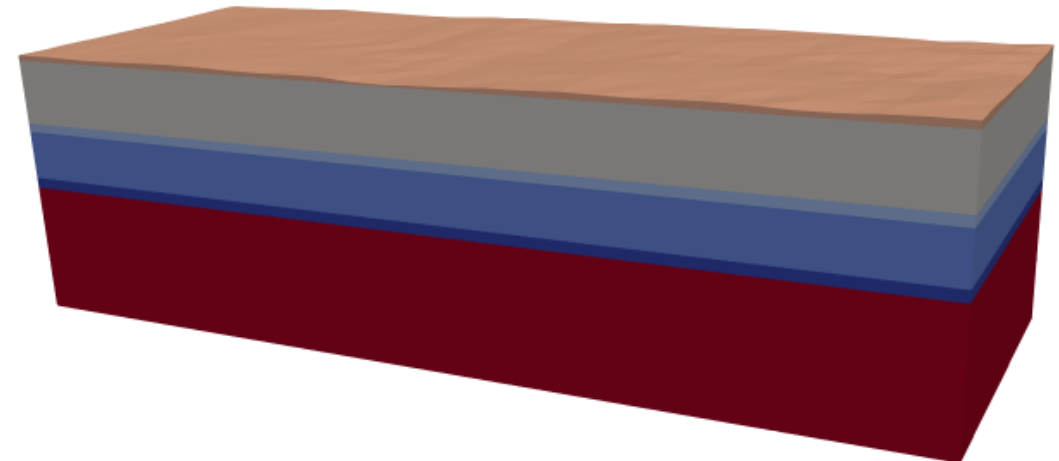


Fully-automated (Python3)

Create mesh (VoroCrust-Meshing)



Create and run simulation (PFLOTRAN)



Partially-automated (Python3)

(LaForce et al. 2022b)



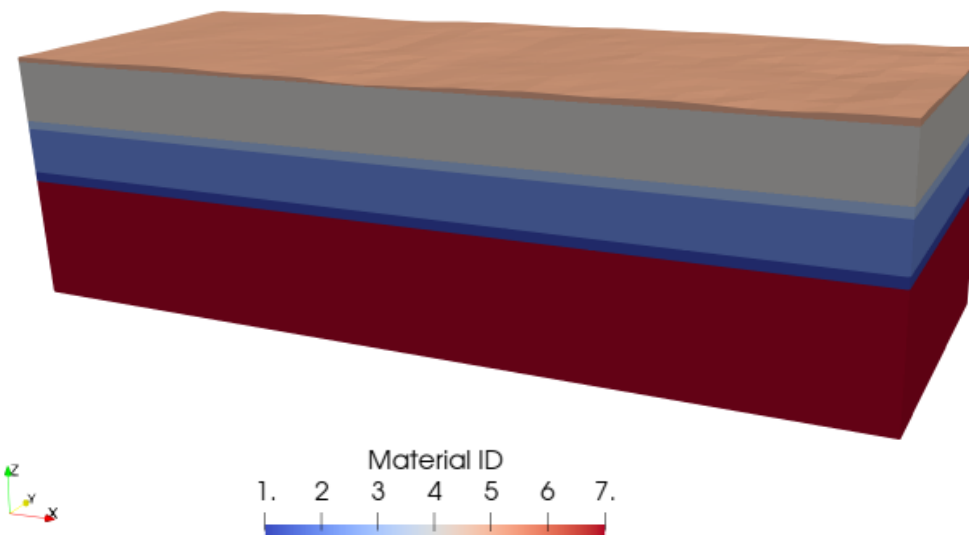
Steps to Automate



- Convert
 - LaGriT stereolithography (.stl) output file to Wavefront object (.obj) file
VoroCrust-Meshing input file
 - VoroCrust-Meshing output file (.vcg) to PFLOTRAN explicit unstructured
mesh file (.uge) format
 - Add monitoring points to PFLOTRAN simulation input file
- Trivial**
- Running VoroCrust-Meshing and PFLOTRAN flow and transport
simulations
 - Meshing took 3-15 hours on workstation
 - Simulations took 1-3 hours on super-computer
- Requires
queueing
system for
multiple
realizations**

Mesh 1 Statistics

- Largest cell: $3.15 \times 10^7 \text{ m}^3$ in Lower Shale
- Smallest cell: 0.478 m^3 in Overburden
- 1.5 million cells

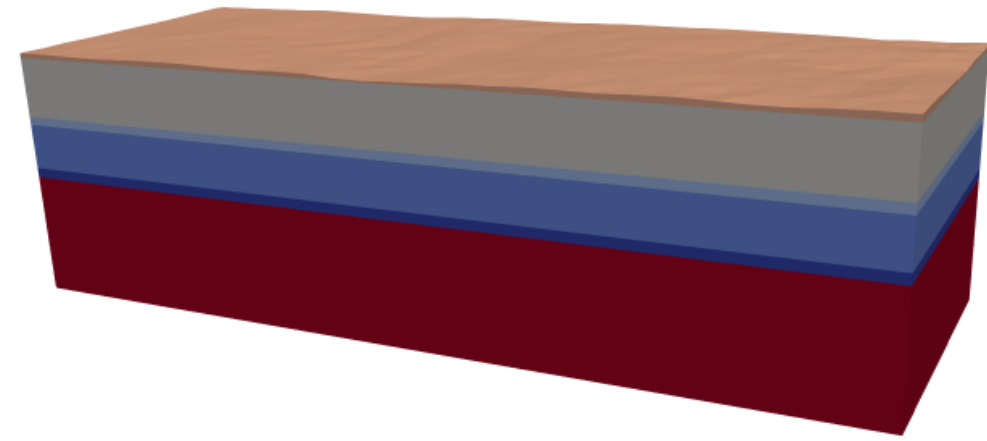


Model Region	Input Volume (m ³)	Meshed Volume (m ³)	Relative difference $\frac{abs(V_{in}-V_m)}{V_{in}}$	Number of Grid Cells
Overburden (ID 5)	6.8390×10^8	6.8353×10^8	5.40×10^{-4}	295,696
Host Shale (ID 4)	8.2916×10^9	8.2912×10^9	4.28×10^{-5}	642,293
Silty Shale (ID 3)	1.2143×10^9	1.2142×10^9	9.88×10^{-5}	94,481
Underlying Shale (ID 2)	6.2624×10^9	6.2619×10^9	7.82×10^{-5}	129,830
Limestone (ID 1)	1.3601×10^9	1.3600×10^9	9.56×10^{-5}	78,848
Lower Shale (ID 7)	1.6878×10^{10}	1.6872×10^{10}	3.08×10^{-4}	65,056
Repository (ID 6)	3.7515×10^7	3.7509×10^7	1.65×10^{-4}	221,284
Full Model	3.4727×10^{10}	3.4721×10^{10}	1.92×10^{-4}	1,527,491

PFLOTRAN Simulation Model



- $7,000 \times 2,500 \times \sim 1,200$ m
- Geological realization ID: 72
- Four additional sampled parameters
- Tracer source is hypothetical waste repository
 - Dimensions are $1640 \times 1525 \times 15$ m
 - Depth: 250 m to 400 m
- Tracer properties
 - Released at time $t = 0$ years
 - Properties representative of ¹²⁹I
 - Decay and adsorption neglected
- Simulations are fully saturated and isothermal (GENERAL MODE)



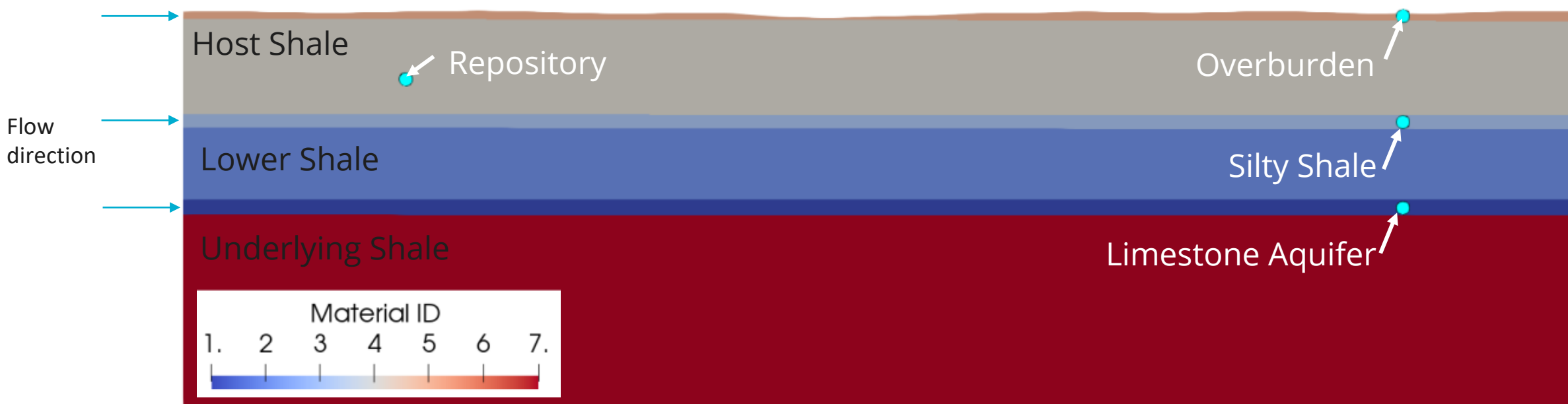
Model Region	Permeability (m ²)	Porosity
Overburden (ID 5)	1.65×10^{-15} *	0.20
Host Shale (ID 4) and Underlying Shale (ID 2)	1.00×10^{-19}	0.196 *
Silty Shale (ID 3)	1.56×10^{-17} *	0.20
Lower Shale (ID 7)	1.00×10^{-20}	0.10
Limestone (ID 1)	2.18×10^{-16} *	0.10
Repository (ID 6)	1.00×10^{-20}	0.35

*sampled

Monitoring Locations



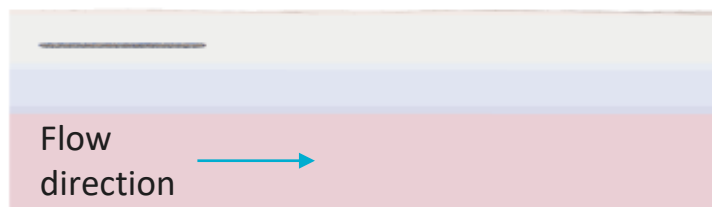
- Groundwater flow in x-direction with head gradient 0.0021 m/m
- Tracer concentration is monitored at blue points shown
 - Three monitoring points 5 km downstream of the repository in potential flow intervals
 - One monitoring point is in the center of the repository
- Average tracer concentration in the repository volume is also monitored



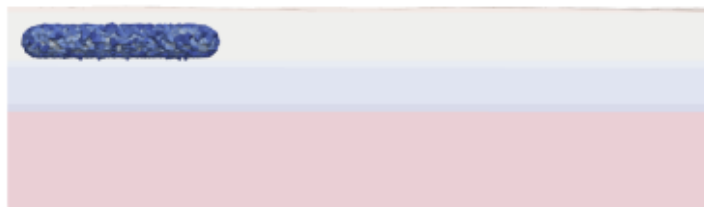
Mesh 1 Tracer Transport Results



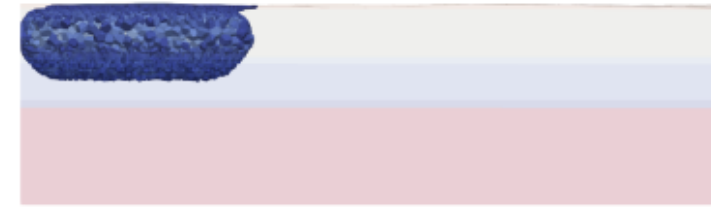
Tracer concentrations above 1×10^{-11} (M) are overlain on the full model colored according to Material ID



1 year



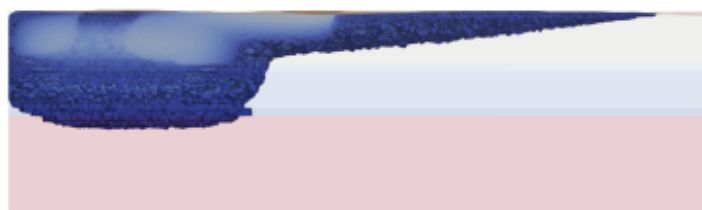
10,000 years



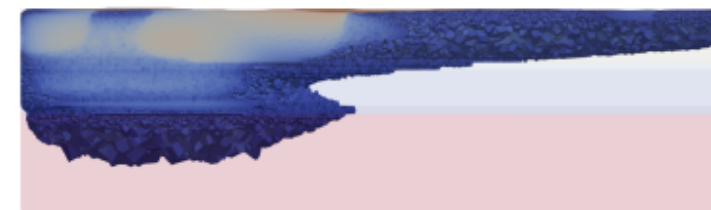
100,000 years



200,000 years



500,000 years



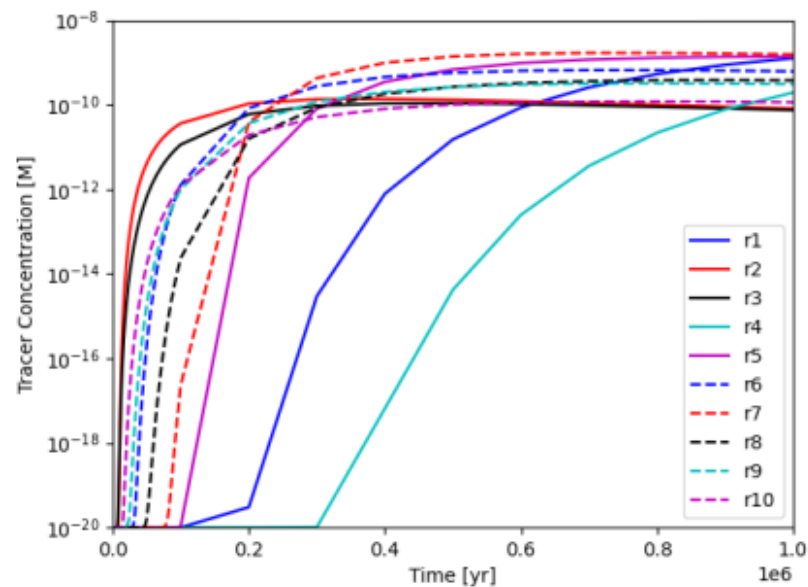
1,000,000 years



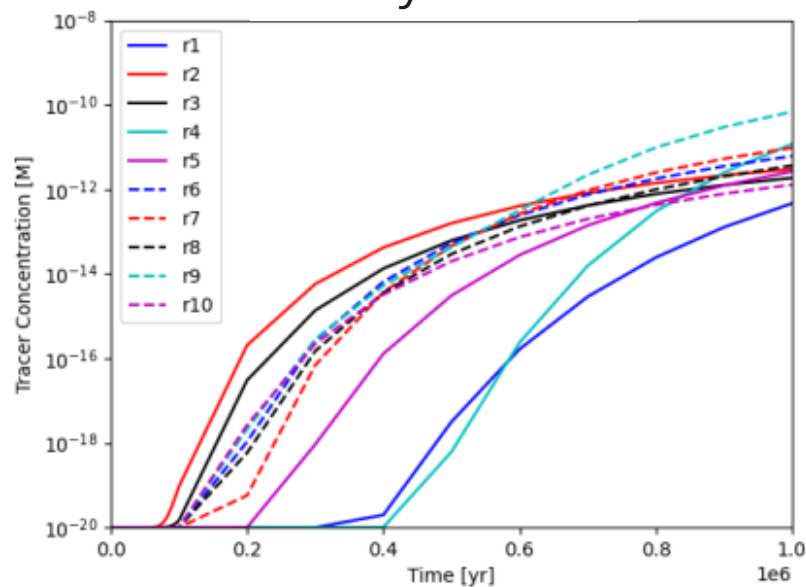
Probabilistic Results: Downstream



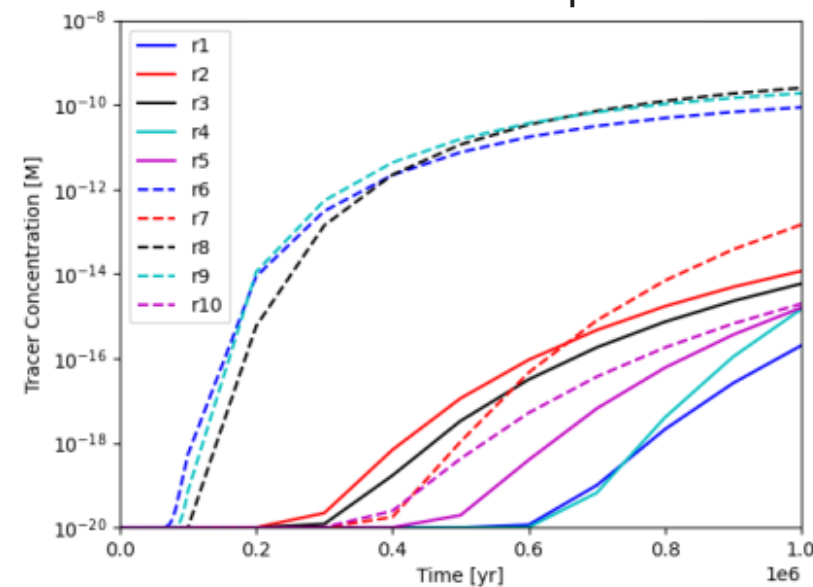
Overburden



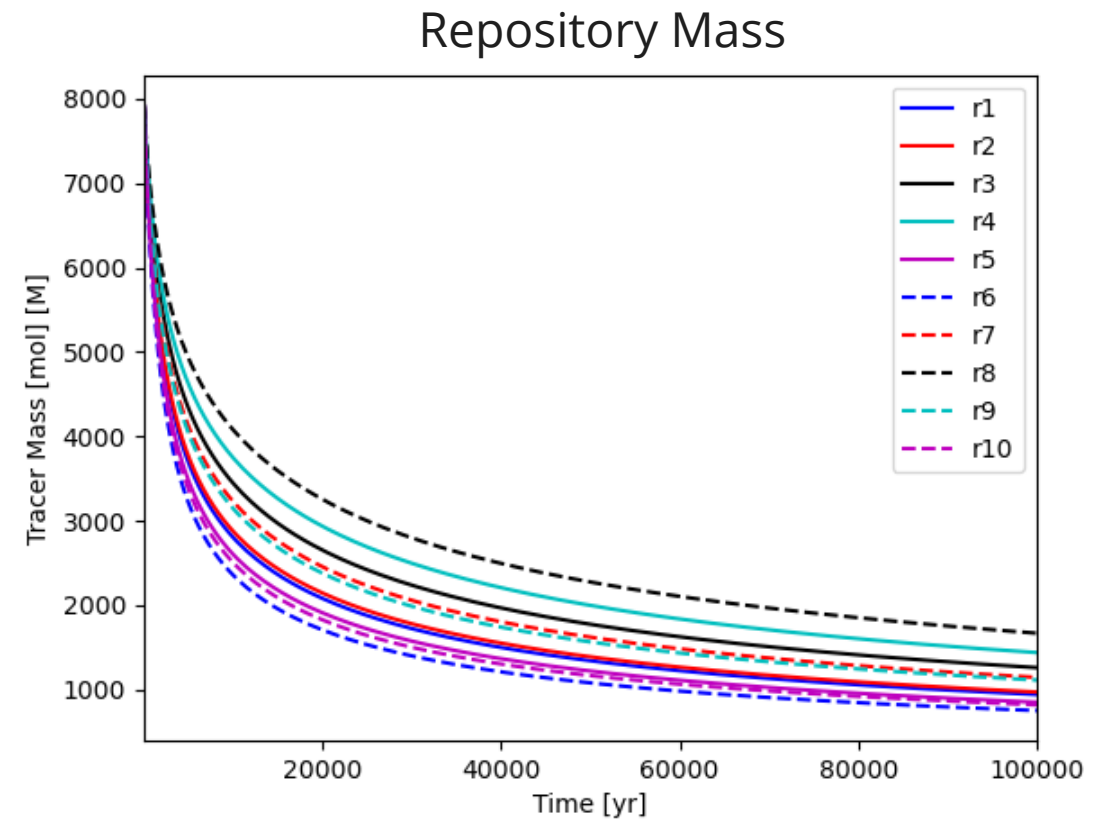
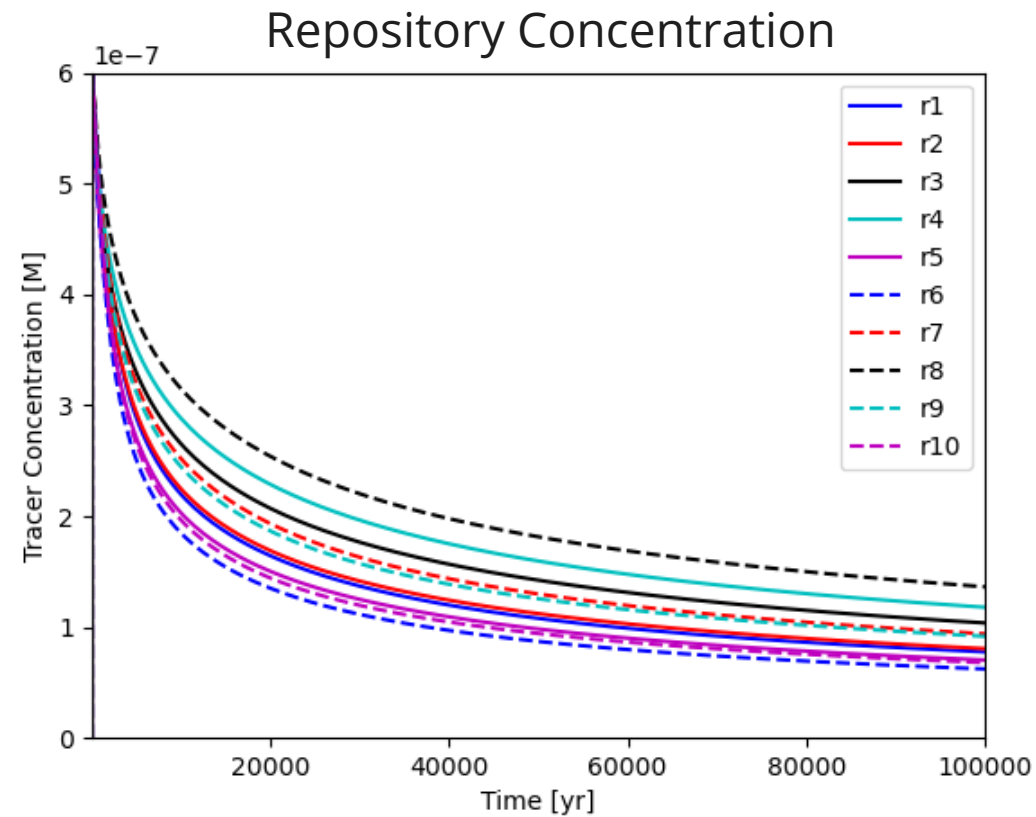
Silty Shale



Limestone Aquifer



Probabilistic Results: In the Repository



Conclusions



- Meshes were generated and simulations run on 10 stochastically-generated realizations of a geological model for tracers released from a hypothetical waste repository
- Simulated tracer concentration downstream and in the repository is produced for all realizations
- Most of the process is automated:
 - Sampling realizations
 - Clipping geological surfaces to realization, building volumes to mesh
 - Creating simulation input decks for each mesh populated with 4 sampled flow parameters
 - Creating meshing input deck and creating mesh from input volumes
- Some pieces require additional work:
 - **Easy:** File conversions, adding monitoring points to simulation
 - **More Challenging:** queueing system for multiple realizations in parallel

Future work



Immediate future:

- Open-source version of the meshing software so entire workflow utilizes free and open-source software

Medium term:

- Full automation using Sandia's Next Generation Workflow
- Complete uncertainty quantification and sensitivity analysis including
 - Thermal and two-phase flow effects
 - Impact of mesh realization/discretization
 - Geological uncertainty

Longer term:

- Mesh repository features in detail
- Mesh faults that terminate within the model
- Anisotropic meshing to reduce element numbers



LaForce, T., Basurto, E., Chang, K.W., Jayne, R., Leone, R., Nole, M., Perry, F.V., Stein, E. (2021) *GDSA Repository Systems Analysis Investigations in FY2021*. SAND2021-11691 R, Sandia National Laboratories, Albuquerque, NM.

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Swiler, L.P., Helton, J.C., Basurto, E., Brooks, D.M., Mariner, P.E., Moore, L.M., Mohanty, S., Sevougian, S.D., and Stein, E.R. (2019). Status Report on Uncertainty Quantification and Sensitivity Analysis Tools in the Geologic Disposal Safety Assessment (GDSA) Framework, SAND2019-13835R.

Software:

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Lichtner, P. C., Hammond, G. E., Lu C., Karra, S., Bisht, G., Andre, B., Mills, R. T., Kumar, J., Frederick, J. M. (2020) **PFLOTRAN** Web page. <http://www.pflotran.org>

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