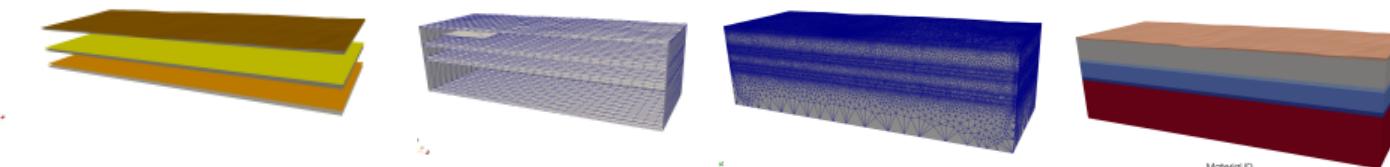
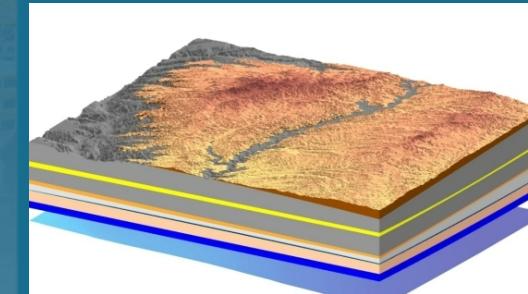




Sandia  
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# Automated Meshing for Simulations of Subsurface Contaminants



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Sandia National Laboratories

Presentation at the International Association for Mathematical Geosciences 21<sup>st</sup> annual conference Aug 29-Sept 3, 2022  
Nancy, France/Virtual  
Sept 1, 2022



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# Outline



Why is fully-automated meshing and simulation model building important?

Why Voronoi meshes (and what are they)?

A shale geological model

Tracer transport in the subsurface

Results of uncertainty simulations

Conclusions and future work

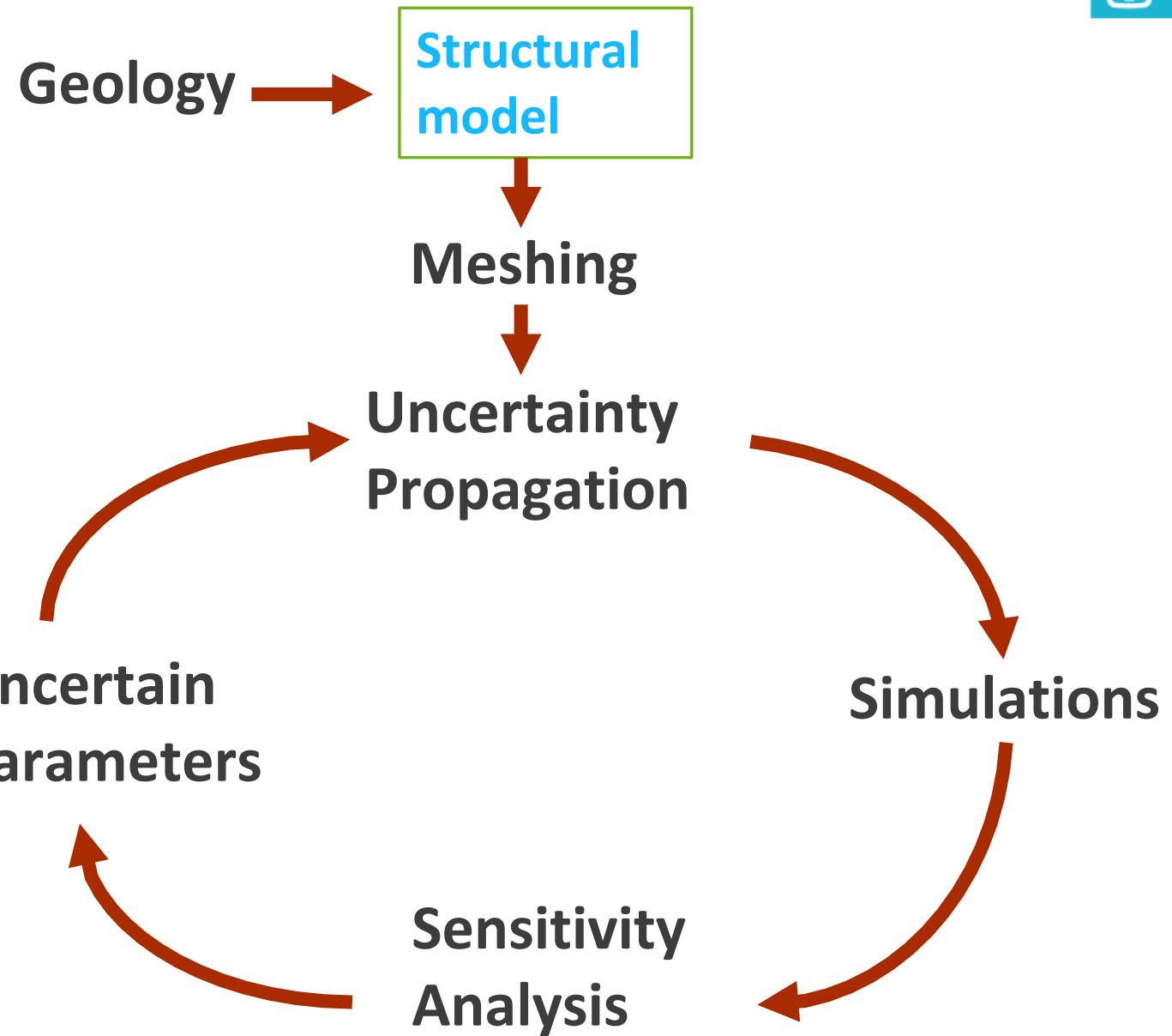
# Why Automate?



**Sensitivity Analysis and Uncertainty Quantification** (SA/UQ) can require hundreds or thousands of model iterations

**Uncertainty in geological structure** and numerical error introduced by the mesh are often neglected because model and mesh building are difficult and human-time intensive

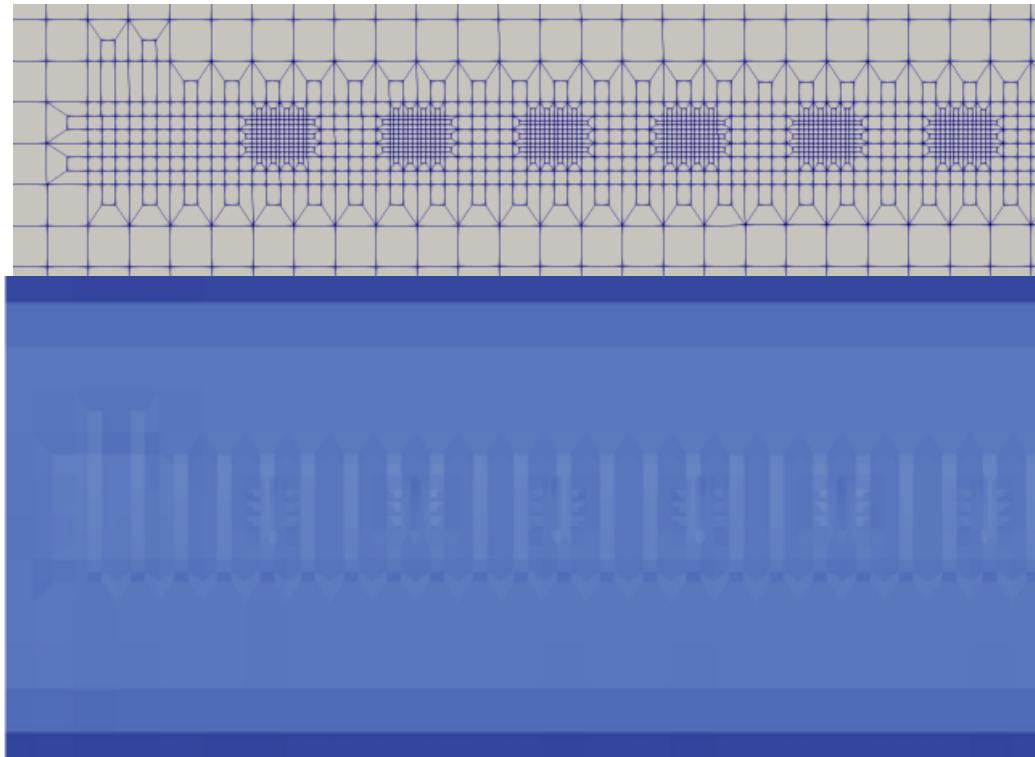
Yet geological structure can have a **first-order impact** on subsurface flow and transport processes



# Why Voronoi meshes?

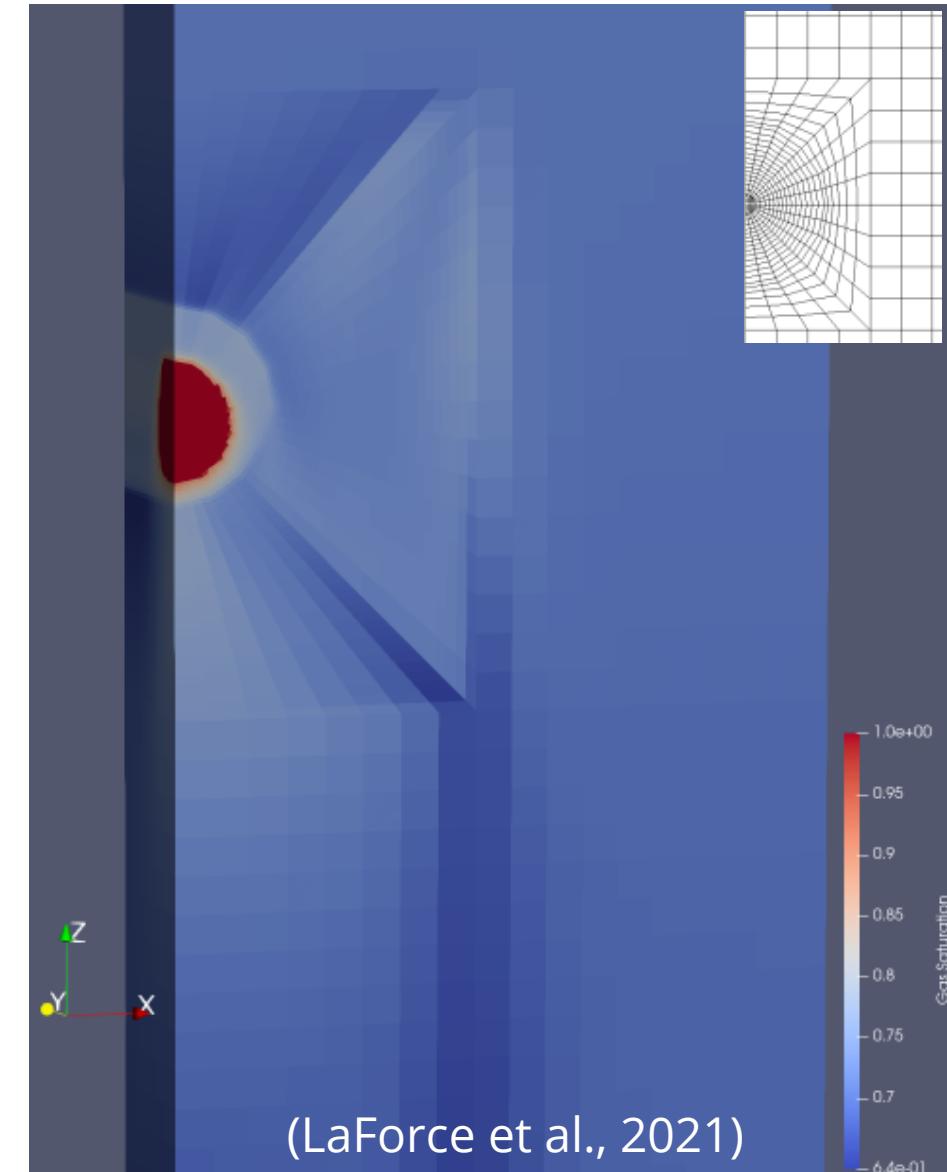
They rigorously honor complex geometries...

...without introducing non-orthogonal fluxes in simulations



Equilibration of an unsaturated heterogeneous model with infiltration using a refined hexahedral mesh.

Gas saturation around a heat source in an unsaturated model using a flexed hexahedral mesh.



(LaForce et al., 2021)

# Why Voronoi meshes?

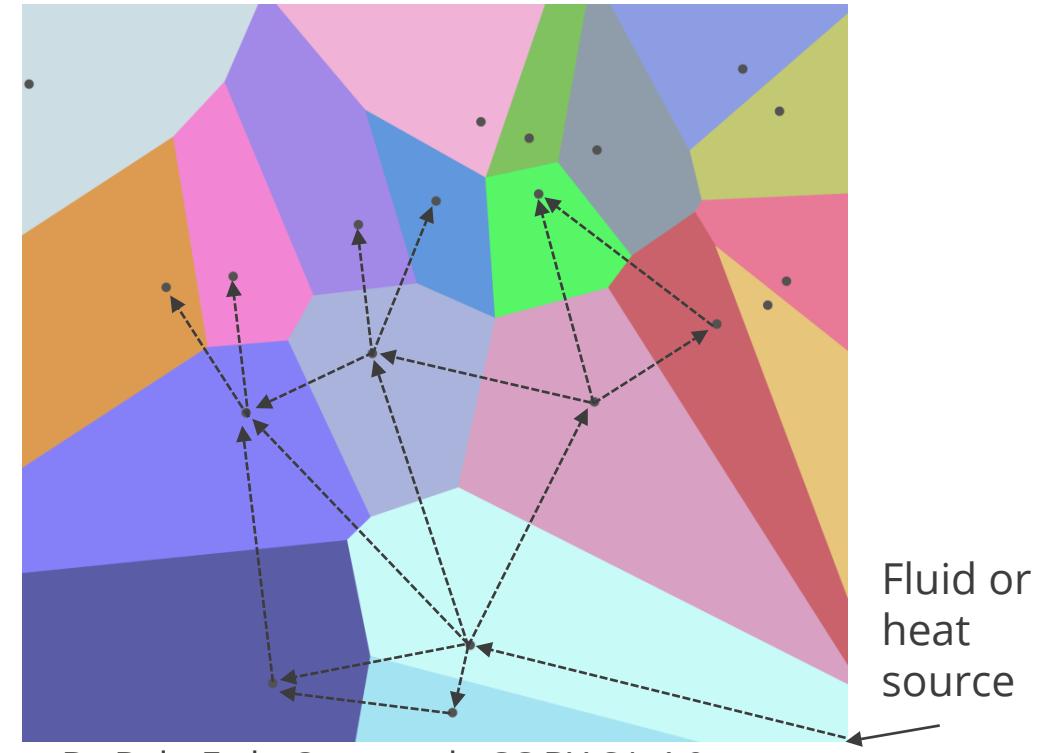
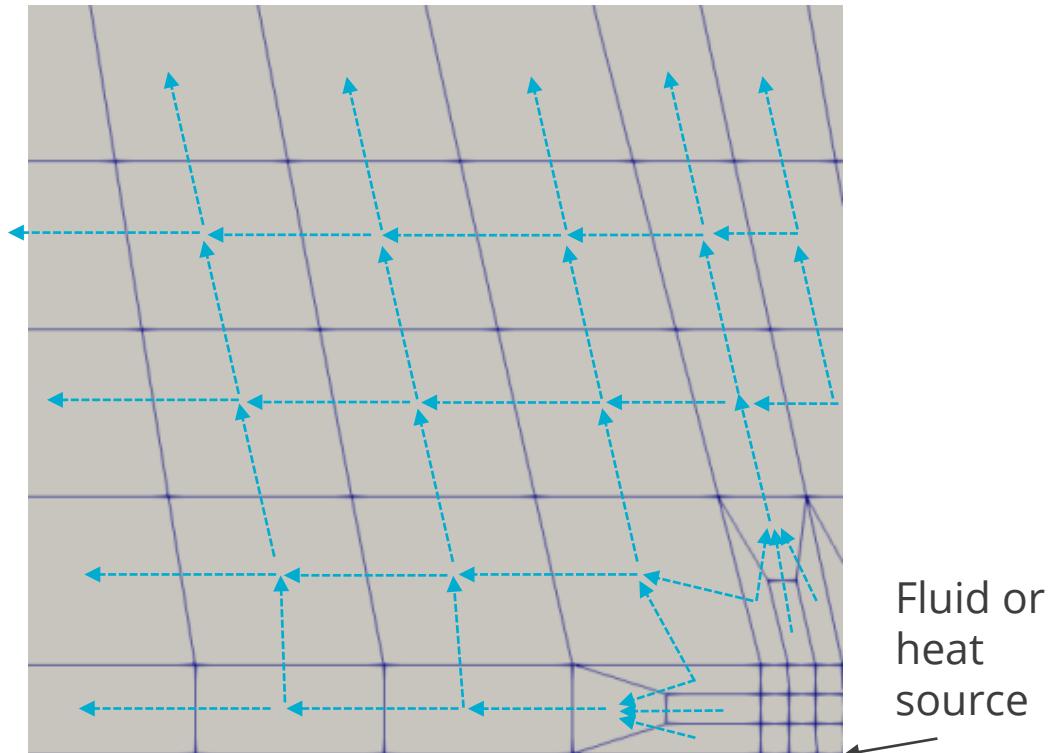


Grid refinement or flexing can bias flow directions

Non-orthogonal fluxes cause errors in two point flux approximation simulations

Fluxes are perpendicular to grid cell faces using Voronoi polyhedral cells

Solvers using two point flux approximation (TOUGH2/PFLOTRAN/FEHM) get accurate results

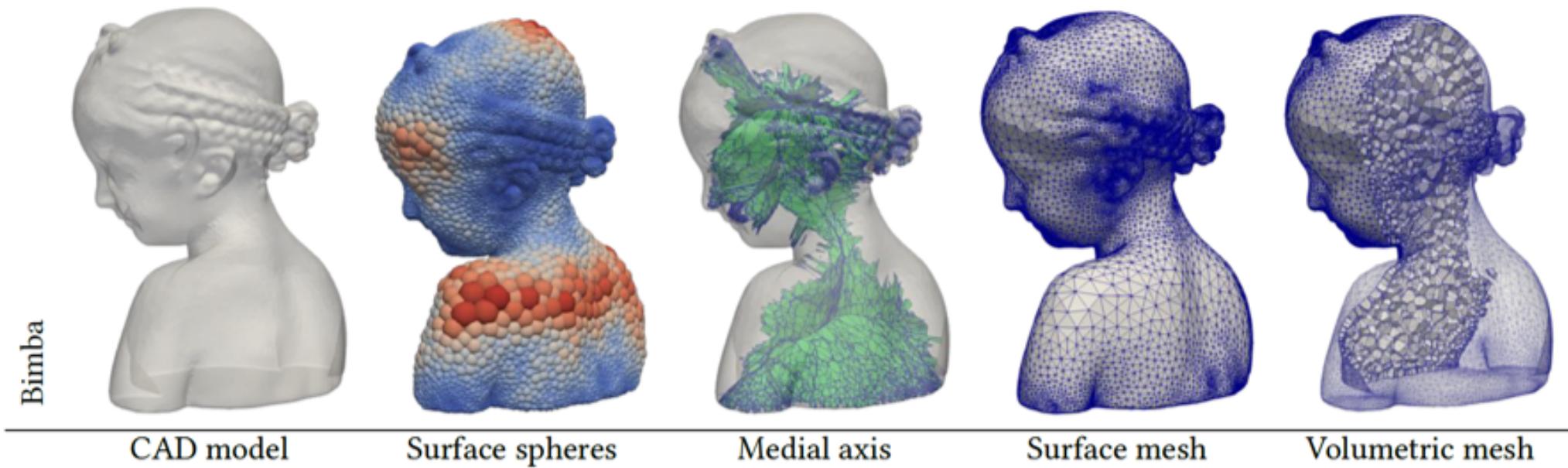


By Balu Ertl - Own work, CC BY-SA 4.0,  
<https://commons.wikimedia.org/w/index.php?curid=38534275>

# VoroCrust-Meshing Voronoi Meshes



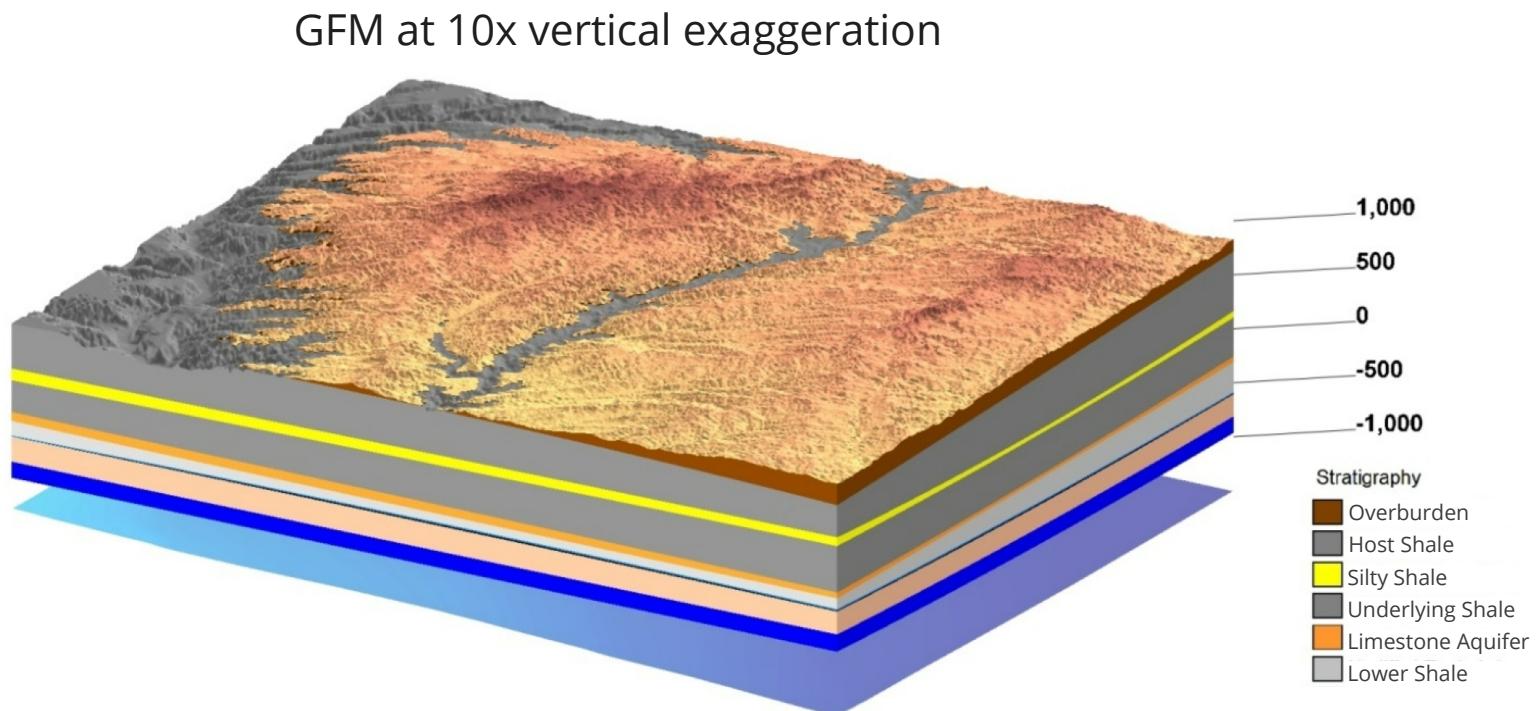
- Accepts as input
  - Any water-tight set of volumes
  - Desired monitoring points
  - Mesh refinement locations
- Fully automated mesh generation
- Surface mesh is triangular
- Interior elements are polyhedral
- Mesh is randomly generated so each VoroCrust run gives a new mesh



# Shale Geological Framework Model



- Single realization of a Pierre Shale Geological Framework Model (GFM) 69 x 83 km
- Pseudo-uncertain models are generated by clipping  $7 \times 2.5$  km sub-models from GFM
- All models must have:
  - At least 15 m dip downward in positive x-direction
  - Surface sediment present over entire model
- 87 prospective geological models created
- 10 models will be randomly sampled in Dakota and populated with parameters

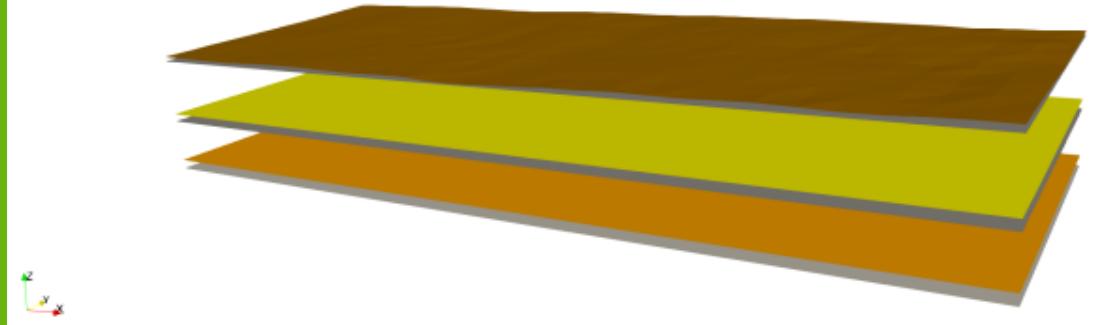


(Sevougian et al, 2019;  
LaForce et al. 2022b)

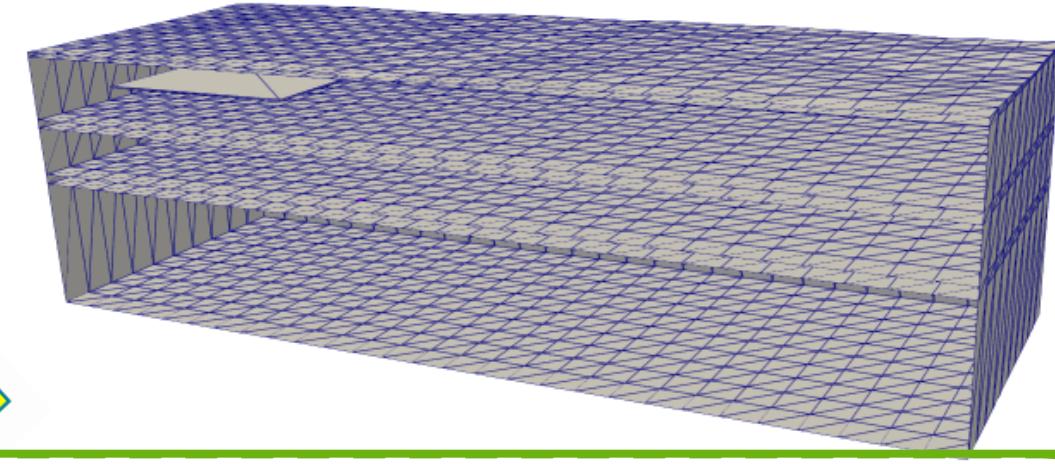
# Meshing and Simulating Realization 1



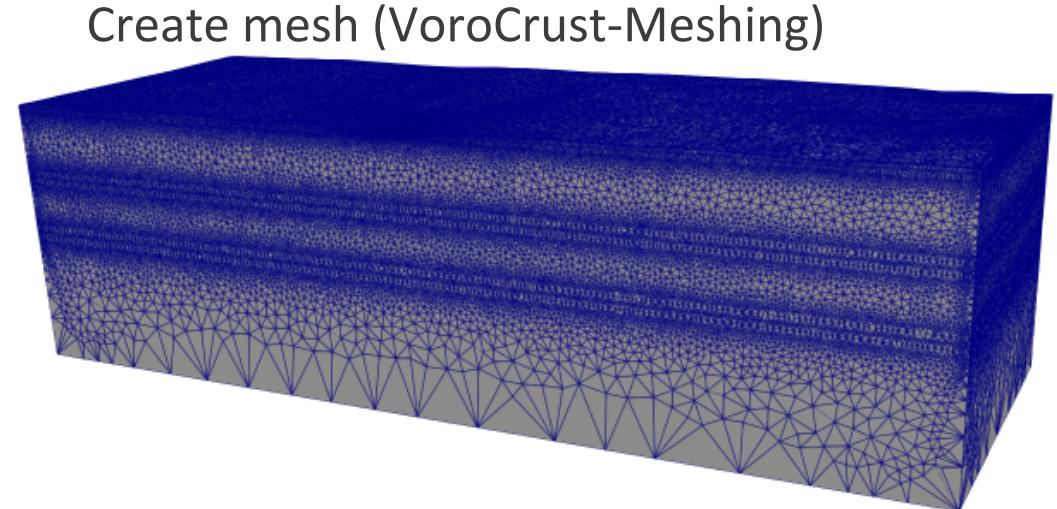
Clip surfaces from GFM (Python3)



Create model volumes (LaGriT)

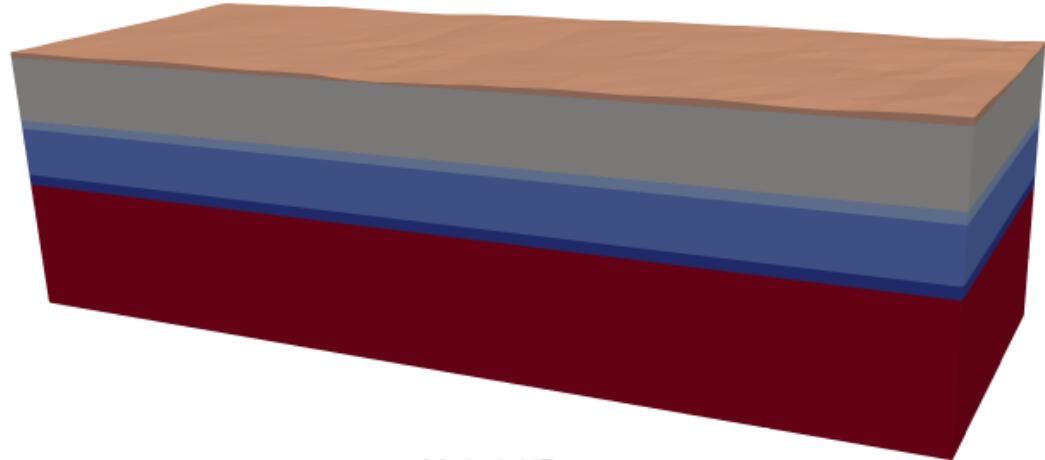


Fully-automated (Python3)



Create mesh (VoroCrust-Meshing)

Create and run simulation (PFLOTRAN)



Partially-automated (Python3)

(LaForce et al. 2022b)



# Steps to Automate



- Convert
  - LaGriT stereolithography (.stl) output file to Wavefront object (.obj) file VoroCrust-Meshing input file
  - VoroCrust-Meshing output file (.vcg) to PFLOTRAN explicit unstructured mesh file (.uge) format
- Add monitoring points to PFLOTRAN simulation input file

Trivial

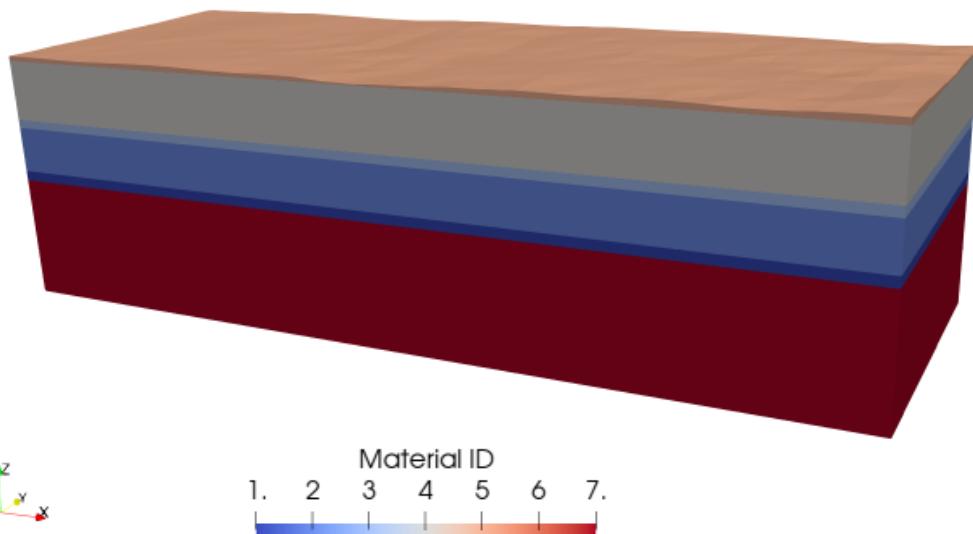
- Running VoroCrust-Meshing and PFLOTRAN flow and transport simulations
  - Meshing took 3-15 hours on workstation
  - Simulations took 1-3 hours on super-computer

Requires queueing system for multiple realizations

# Mesh 1 Statistics



- Largest cell:  $3.15 \times 10^7 \text{ m}^3$  in Lower Shale
- Smallest cell:  $0.478 \text{ m}^3$  in Overburden
- 1.5 million cells

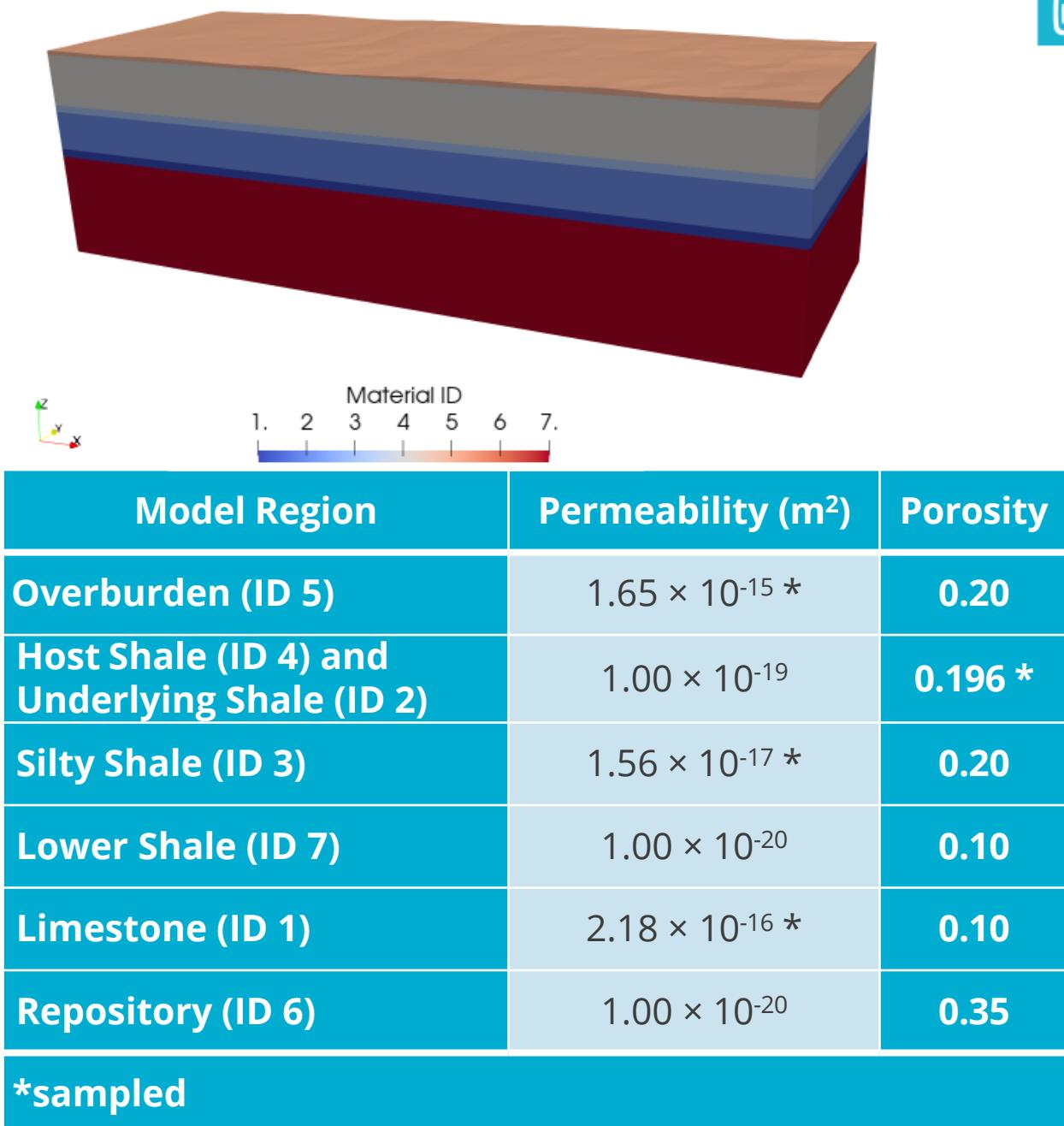


Model Region	Input Volume (m <sup>3</sup> )	Meshed Volume (m <sup>3</sup> )	Relative difference $\frac{abs(V_{in} - V_m)}{V_{in}}$	Number of Grid Cells
Overburden (ID 5)	$6.8390 \times 10^8$	$6.8353 \times 10^8$	$5.40 \times 10^{-4}$	<b>295,696</b>
Host Shale (ID 4)	$8.2916 \times 10^9$	$8.2912 \times 10^9$	$4.28 \times 10^{-5}$	<b>642,293</b>
Silty Shale (ID 3)	$1.2143 \times 10^9$	$1.2142 \times 10^9$	$9.88 \times 10^{-5}$	<b>94,481</b>
Underlying Shale (ID 2)	$6.2624 \times 10^9$	$6.2619 \times 10^9$	$7.82 \times 10^{-5}$	<b>129,830</b>
Limestone (ID 1)	$1.3601 \times 10^9$	$1.3600 \times 10^9$	$9.56 \times 10^{-5}$	<b>78,848</b>
Lower Shale (ID 7)	$1.6878 \times 10^{10}$	$1.6872 \times 10^{10}$	$3.08 \times 10^{-4}$	<b>65,056</b>
Repository (ID 6)	$3.7515 \times 10^7$	$3.7509 \times 10^7$	$1.65 \times 10^{-4}$	<b>221,284</b>
<b>Full Model</b>	$3.4727 \times 10^{10}$	$3.4721 \times 10^{10}$	$1.92 \times 10^{-4}$	<b>1,527,491</b>

# PFLOTTRAN Simulation Model



- $7,000 \times 2,500 \times \sim 1,200$  m
- Geological realization ID: 72
- Four additional sampled parameters
- Tracer source is hypothetical waste repository
  - Dimensions are  $1640 \times 1525 \times 15$  m
  - Depth: 250 m to 400 m
- Tracer properties
  - Released at time  $t = 0$  years
  - Properties representative of  $^{129}\text{I}$
  - Decay and adsorption neglected
- Simulations are fully saturated and isothermal (GENERAL MODE)



# Monitoring Locations



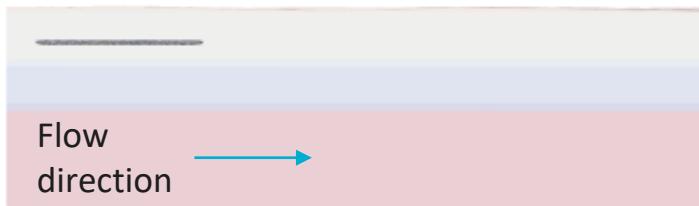
- Groundwater flow in x-direction with head gradient 0.0021 m/m
- Tracer concentration is monitored at blue points shown
  - Three monitoring points 5 km downstream of the repository in potential flow intervals
  - One monitoring point is in the center of the repository
- Average tracer concentration in the repository volume is also monitored



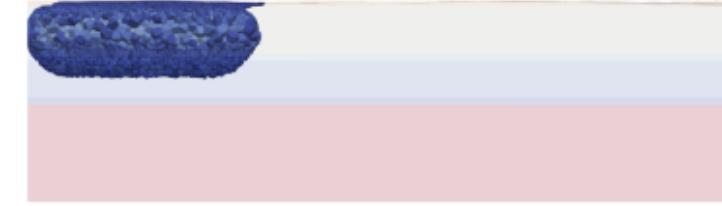
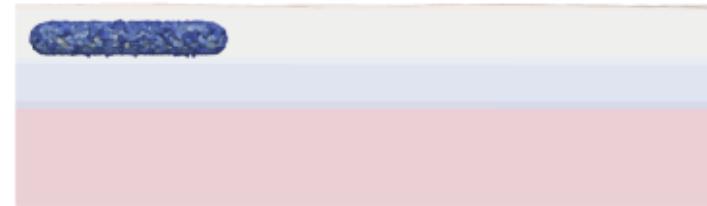
# Mesh 1 Tracer Transport Results



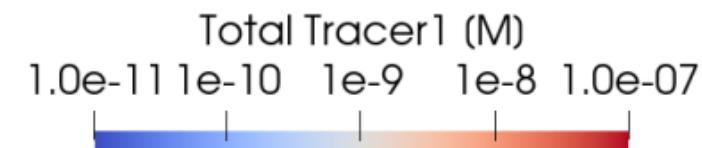
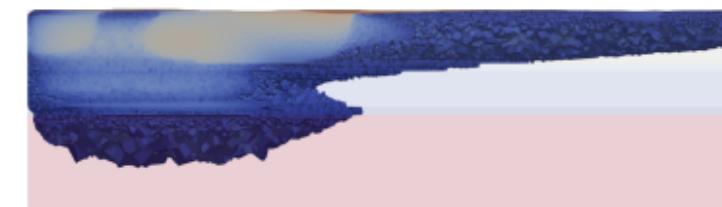
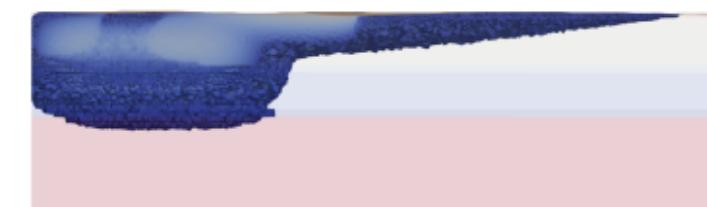
Tracer concentrations above  $1 \times 10^{-11}$  (M) are overlaid on the full model colored according to Material ID



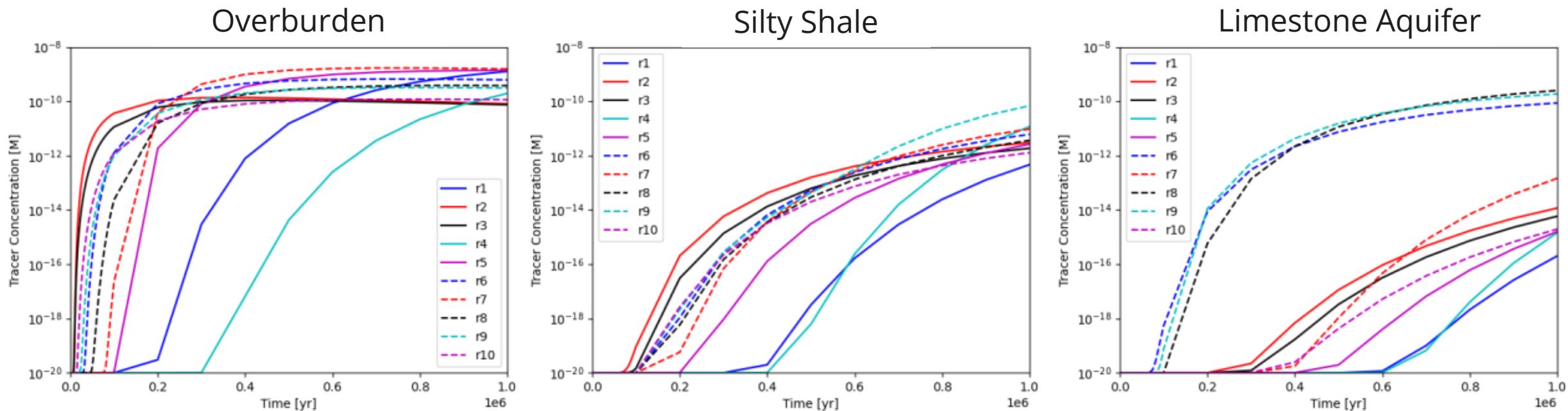
1 year



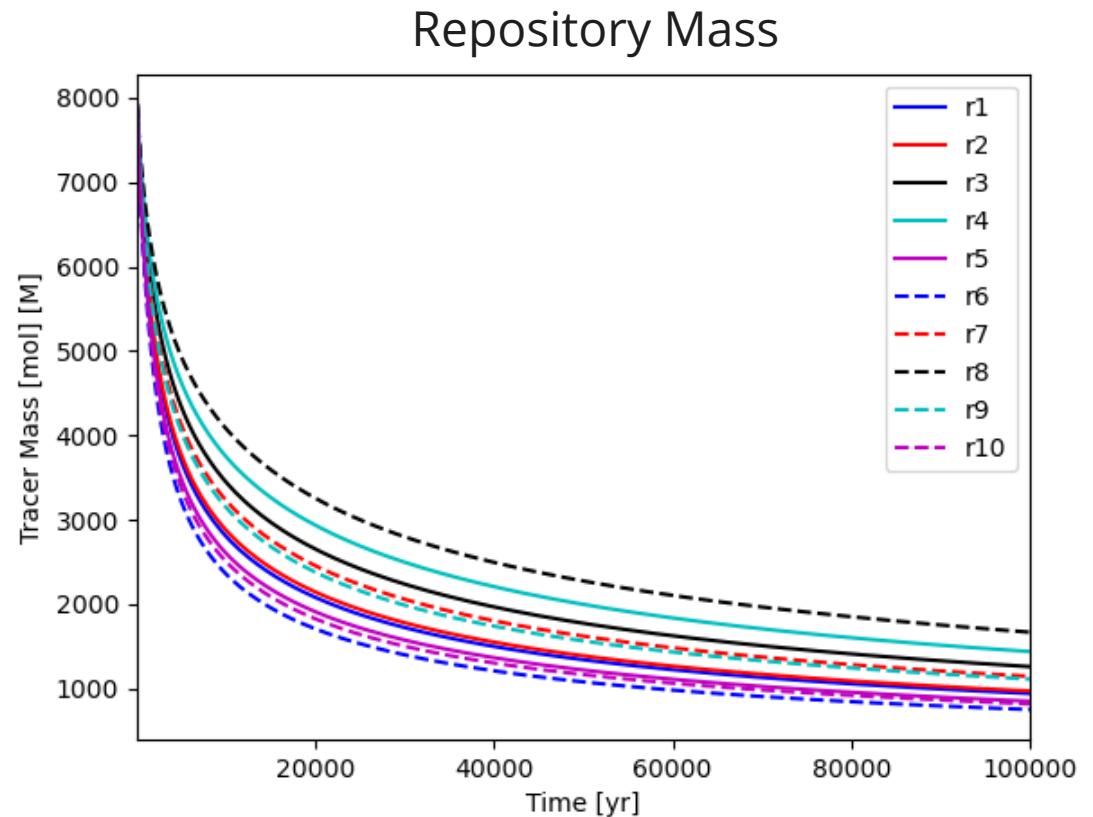
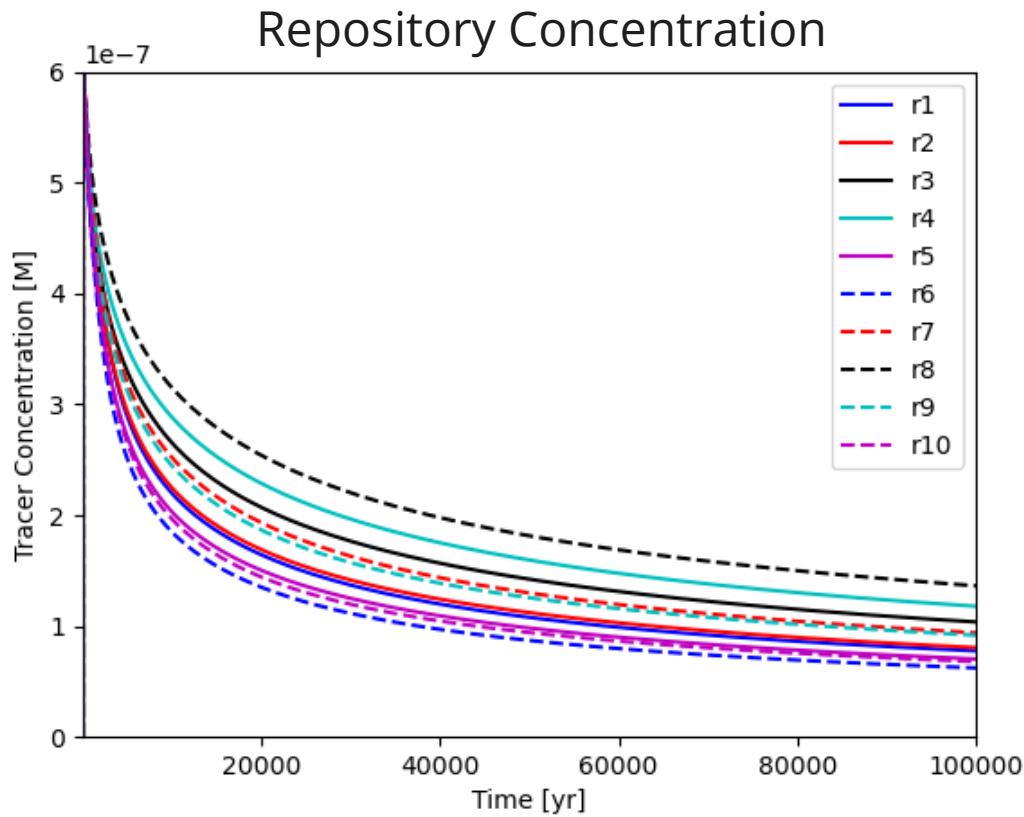
200,000 years



# Probabilistic Results: Downstream



# Probabilistic Results: In the Repository



# Conclusions



- Meshes were generated and simulations run on 10 stochastically-generated realizations of a geological model for tracers released from a hypothetical waste repository
- Simulated tracer concentration downstream and in the repository is produced for all realizations
- Most of the process is automated:
  - Sampling realizations
  - Clipping geological surfaces to realization, building volumes to mesh
  - Creating simulation input decks for each mesh populated with 4 sampled flow parameters
  - Creating meshing input deck and creating mesh from input volumes
- Some pieces require additional work:
  - **Easy:** File conversions, adding monitoring points to simulation
  - **More Challenging:** queueing system for multiple realizations in parallel

# Future work



## Immediate future:

- Open-source version of the meshing software so entire workflow utilizes free and open-source software

## Medium term:

- Full automation using Sandia's Next Generation Workflow
- Complete uncertainty quantification and sensitivity analysis including
  - Thermal and two-phase flow effects
  - Impact of mesh realization/discretization
  - Geological uncertainty

## Longer term:

- Mesh repository features in detail
- Mesh faults that terminate within the model
- Anisotropic meshing to reduce element numbers

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