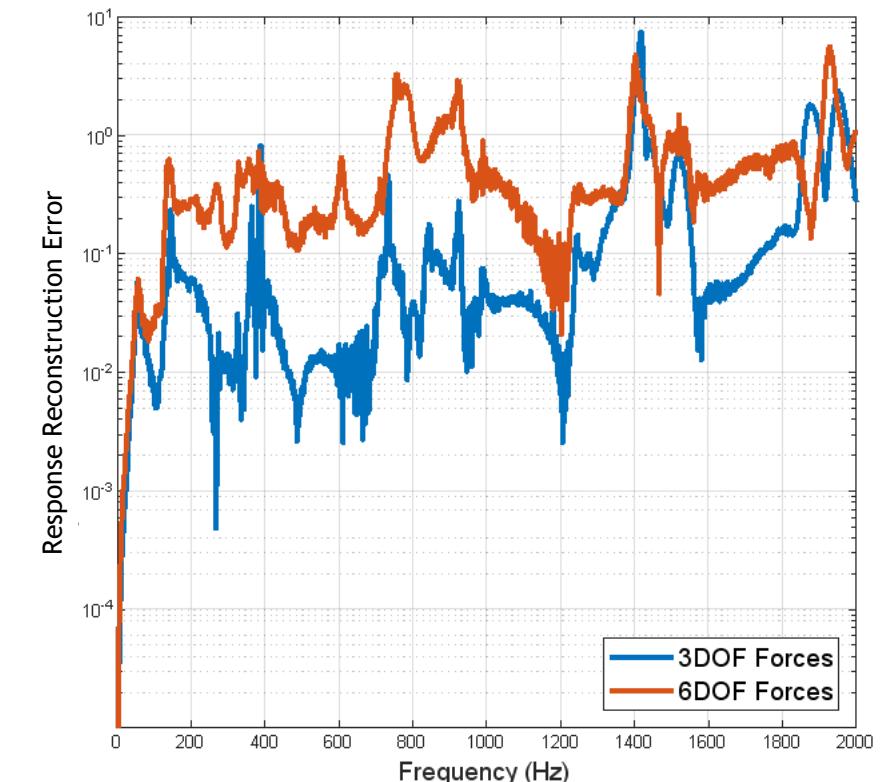


# Errors Using 6DOF Force Estimates to Translate Environments System-to-System



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Co-Author: Brian Owens, [bcowens@sandia.gov](mailto:bcowens@sandia.gov)



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**Component-based TPA provides a theoretical framework for translating vibration environments system-to-system**

Based on inverse force estimation



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**Based on inverse force estimation:**

$$\mathbf{F}_{Estimated} = [\mathbf{H}_{Original}]^+ [\mathbf{X}_{Original}] [\mathbf{H}_{Original}]^{+*}$$



Component-based TPA provides a theoretical framework for translating vibration environments system-to-system

Based on inverse force estimation:

$$F_{Estimated} = [H_{Original}]^+ [X_{Original}] [H_{Original}]^{+*}$$



$$X_{New} = [H_{New}] [F_{Estimated}] [H_{New}]^*$$

## Background and Introduction – General Assumptions about the Forces



The estimated forces are typically validated by comparing the reconstructed response to the measured response

TPA generally uses 3DOF force estimates, although 6DOF force estimates are considered more complete



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$$[H_{Original}][F_{Estimated}][H_{Original}]^*$$



$$X_{Measured}$$

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# Background and Introduction – General Assumptions about the Forces



The estimated forces are typically validated by comparing the reconstructed response to the measured response

$$\begin{bmatrix} H_{Original} \\ F_{Estimated} \end{bmatrix} \begin{bmatrix} H_{Original} \\ F_{Estimated} \end{bmatrix}^* = \begin{bmatrix} \text{Measured Response} \\ \text{Estimated Response} \end{bmatrix} = X_{Measured}$$

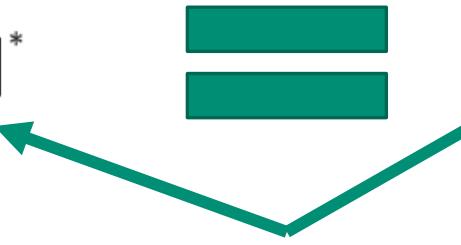
Equality indicates accurate force estimates

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The estimated forces are typically validated by comparing the reconstructed response to the measured response

$$\left[ H_{Original} \right] \left[ F_{Estimated} \right] \left[ H_{Original} \right]^* \quad \begin{matrix} \text{Measured} \\ \text{Response} \end{matrix} \quad X_{Measured}$$

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# Background and Introduction – General Assumptions about the Forces



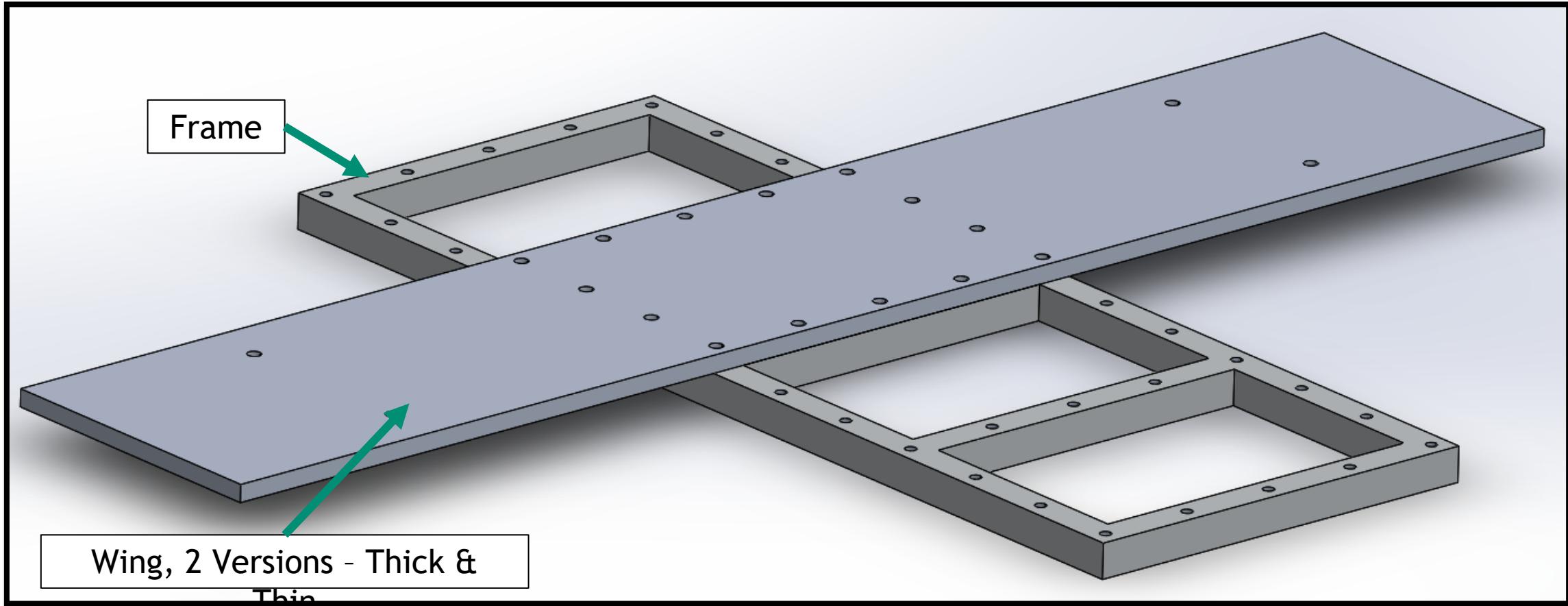
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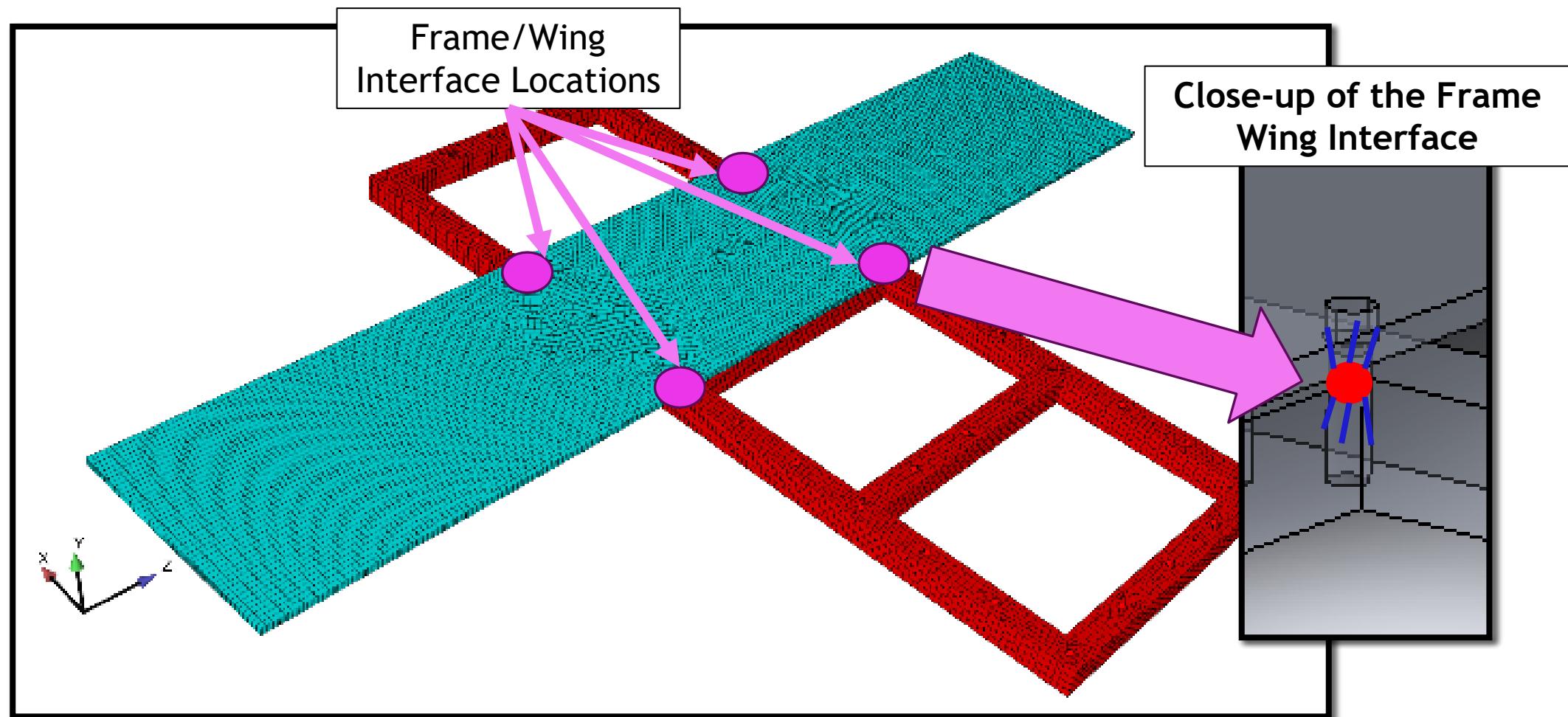
Equality indicates accurate force estimates

TPA generally uses 3DOF force estimates, although 6DOF force estimates are considered more complete – *more complete is typically interpreted as more accurate*

This work presents an example that contradicts these assumptions

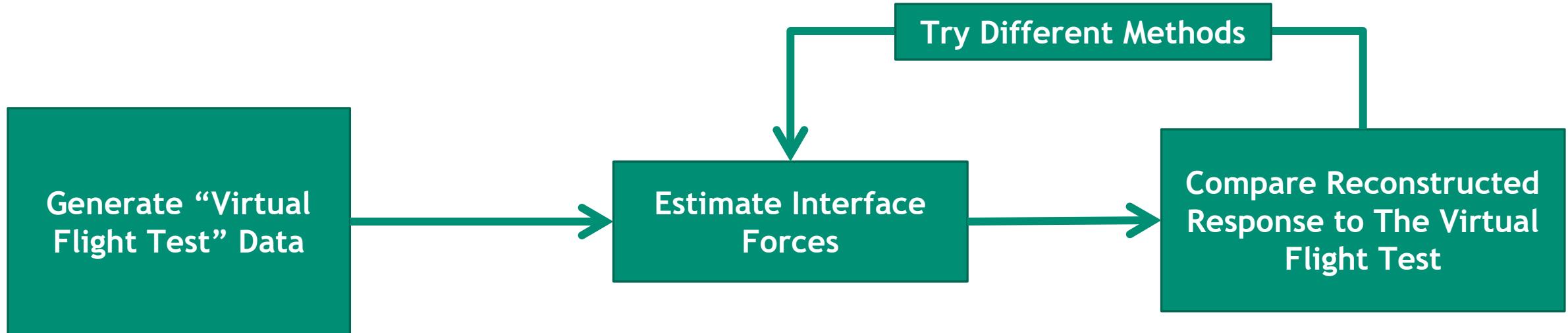


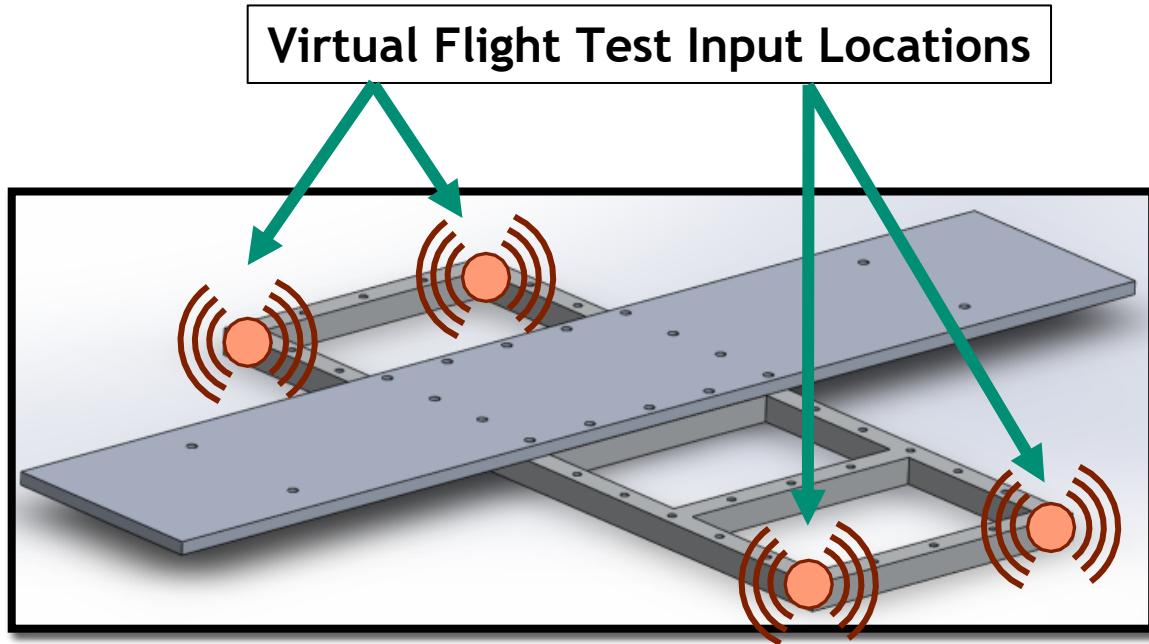
The system is the Round Robin System from the SEM Substructuring Technical Division



The frame/wing interface is modeled with a JOINT2G element that is analogous to a Nastran CBUSH

# System Under Study – Workflow for Evaluating Force Estimation Methods

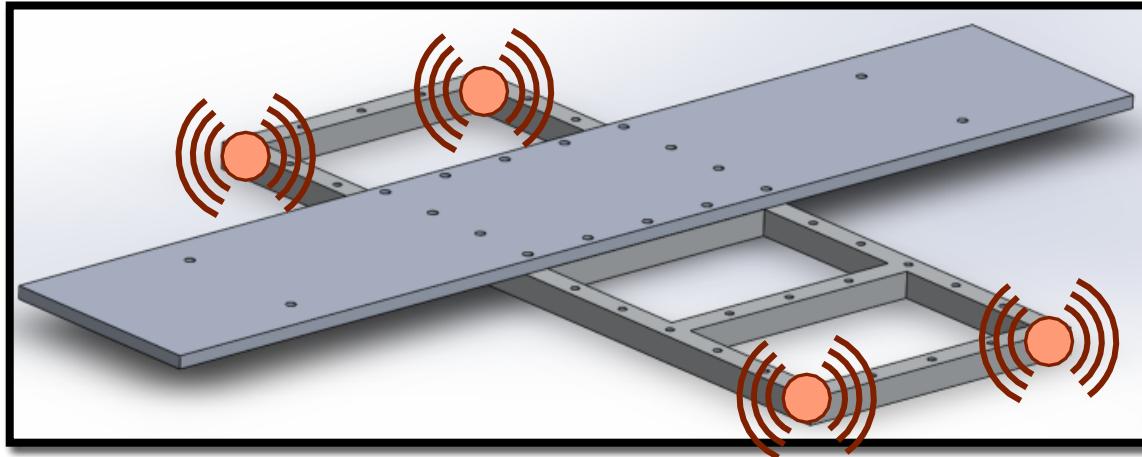




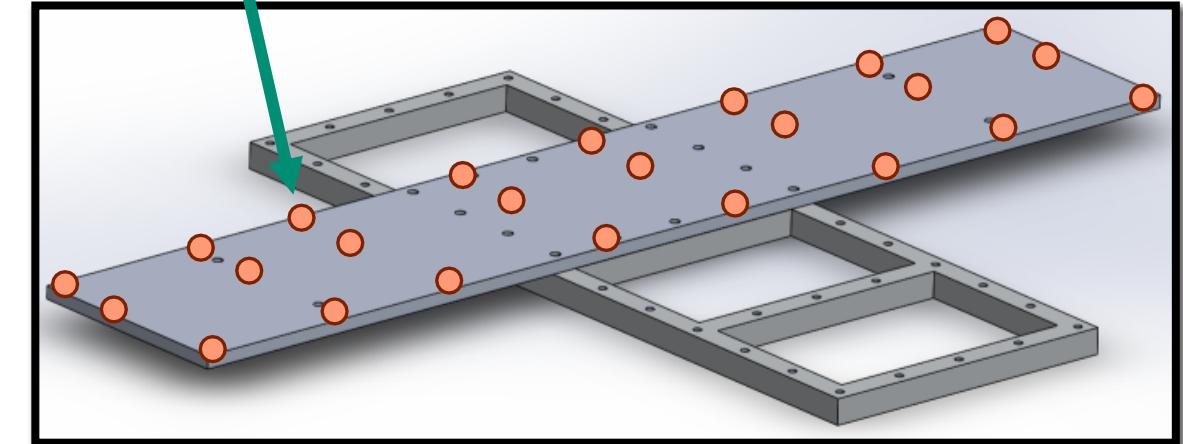
# System Under Study – Generating “Virtual Flight Test” Data



**Virtual Flight Test Input Locations**

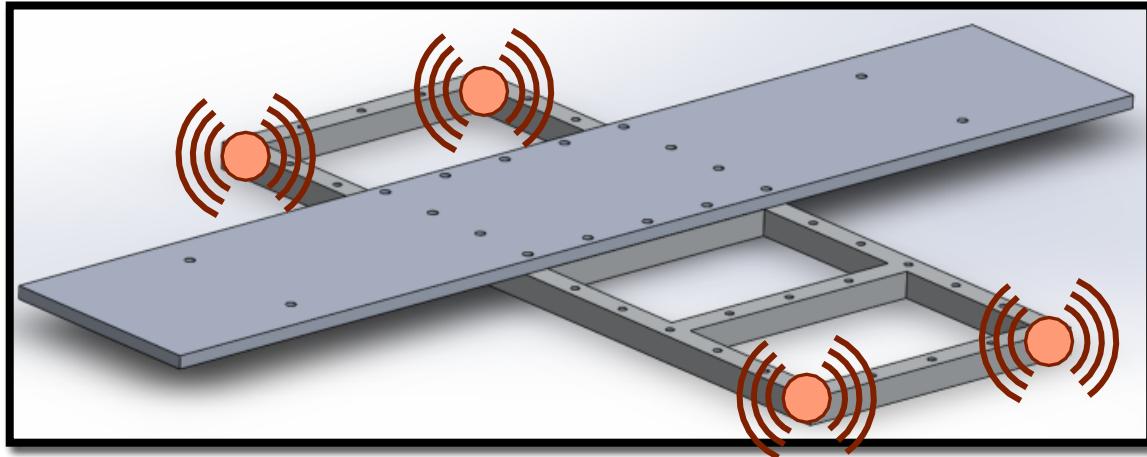


**Response locations distributed over the wing**

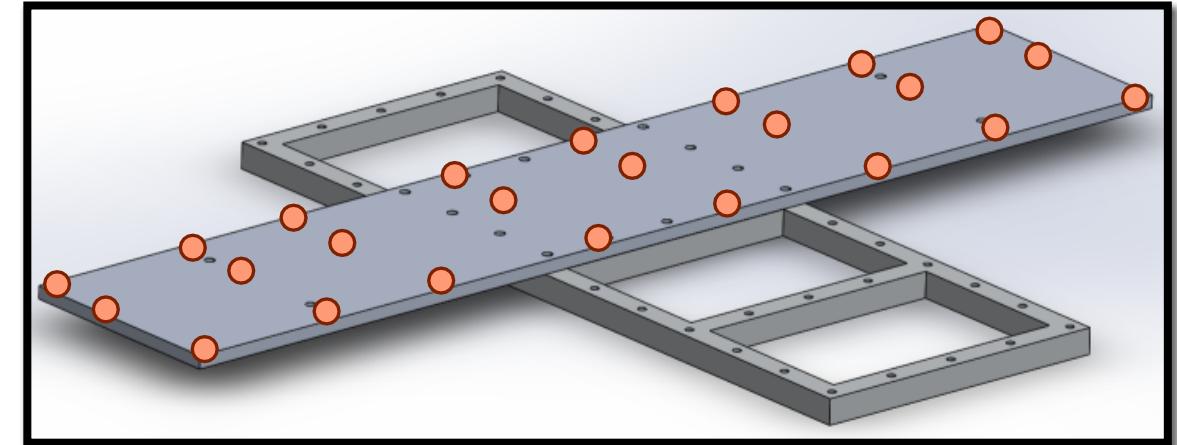




Virtual Flight Test Input Locations

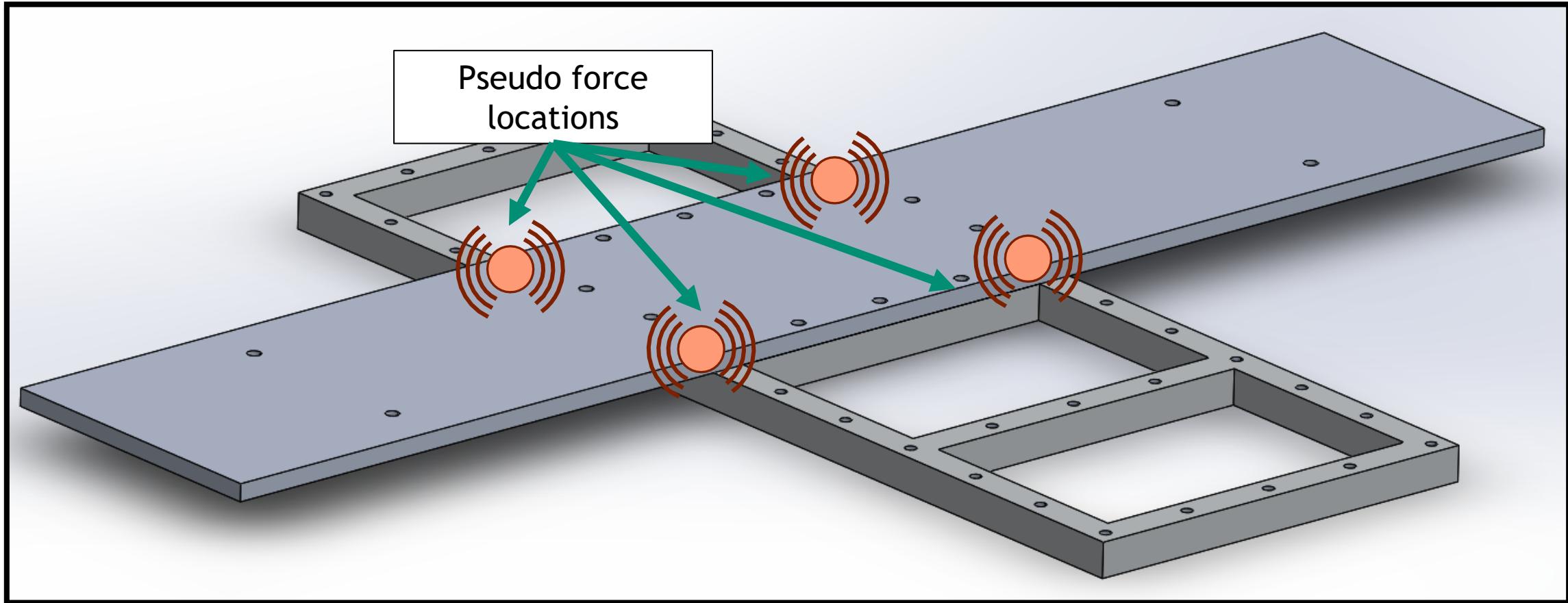


Response locations distributed over the wing



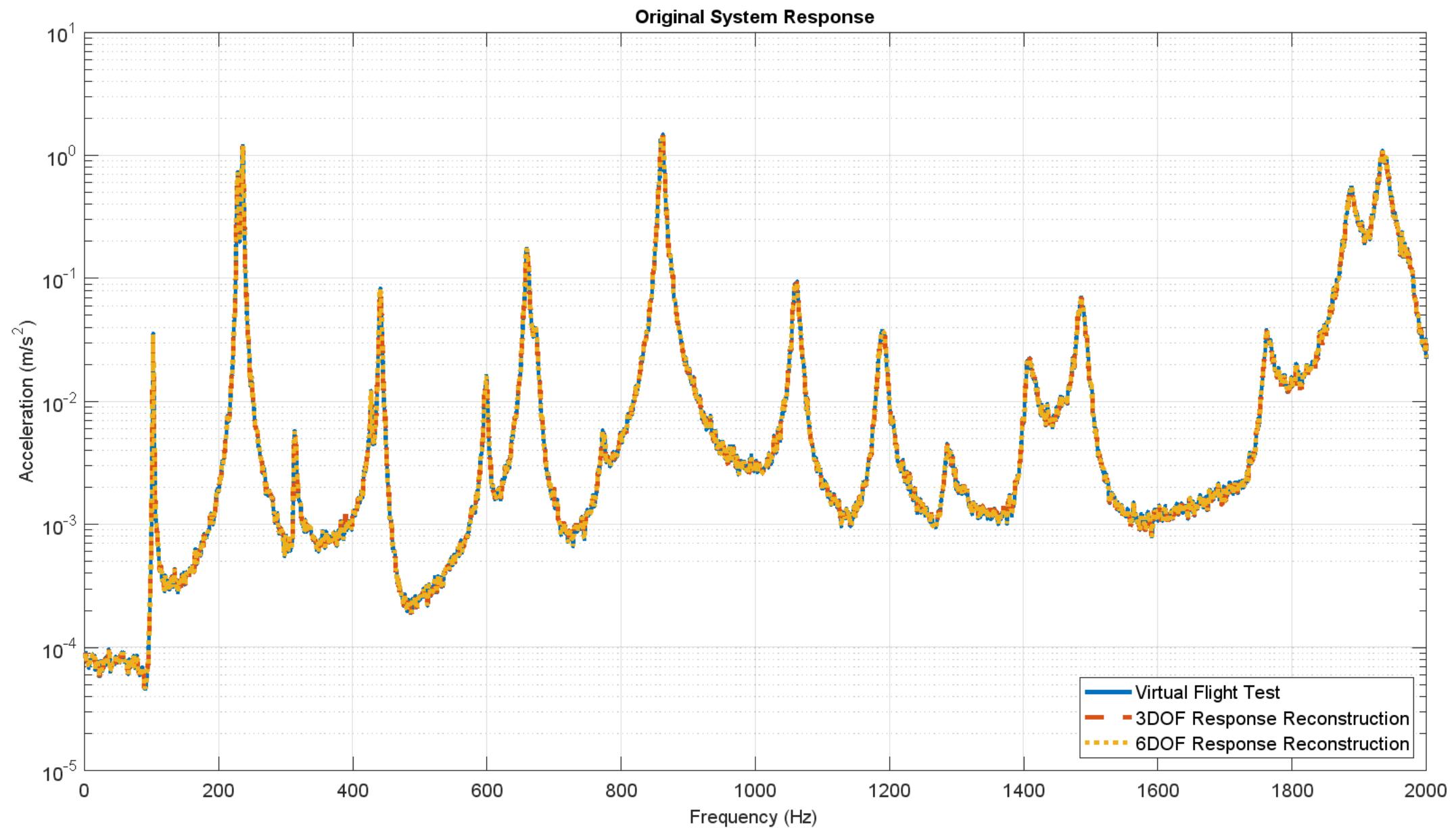
**Broadband excitation is applied to the corners of the frame and response were computed at locations on the wing to generate truth data for both versions of the system**

# System Under Study – Estimating Interface Forces

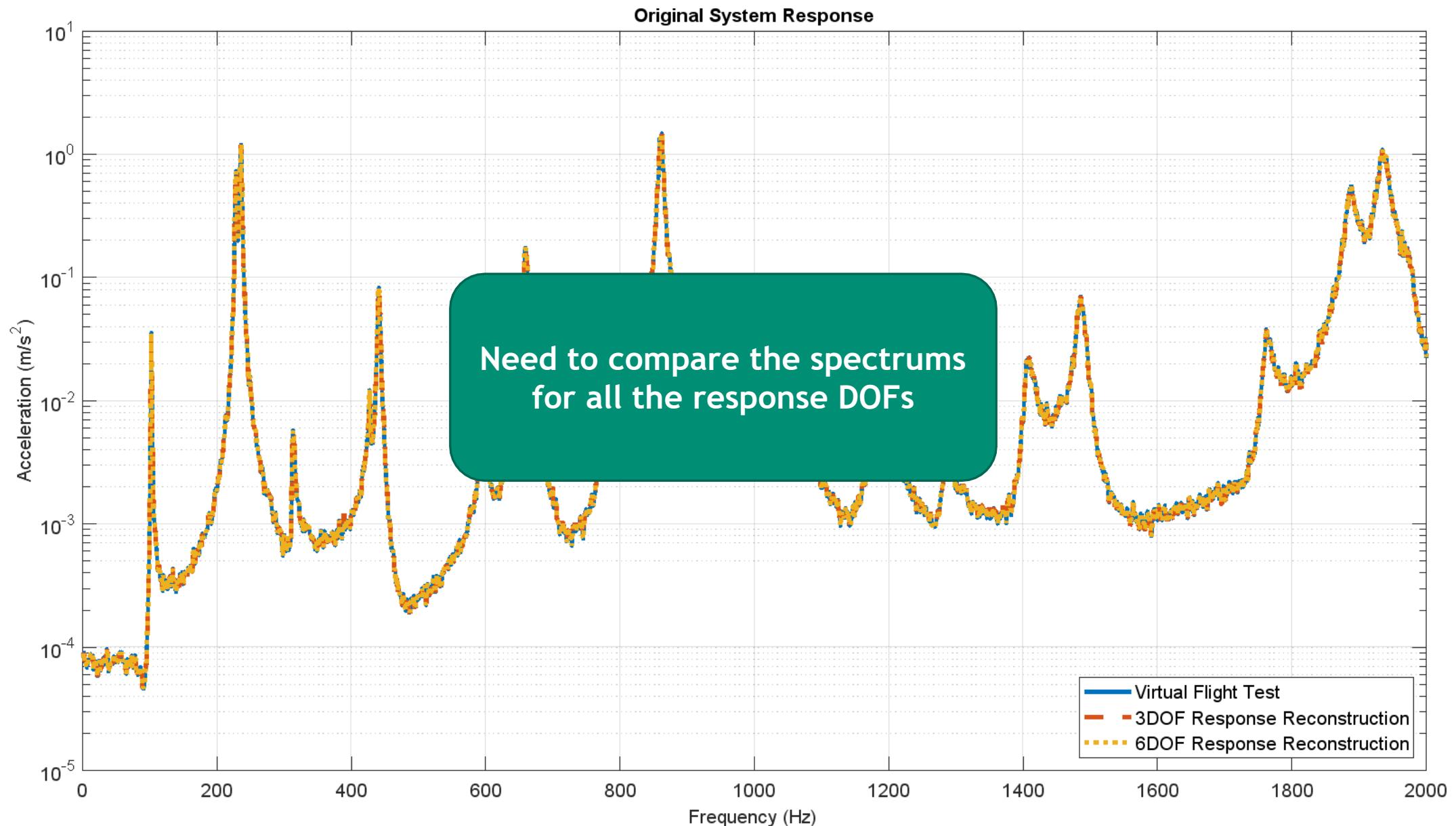


3DOF & 6DOF pseudo forces were estimated at the interface between the frame and wing

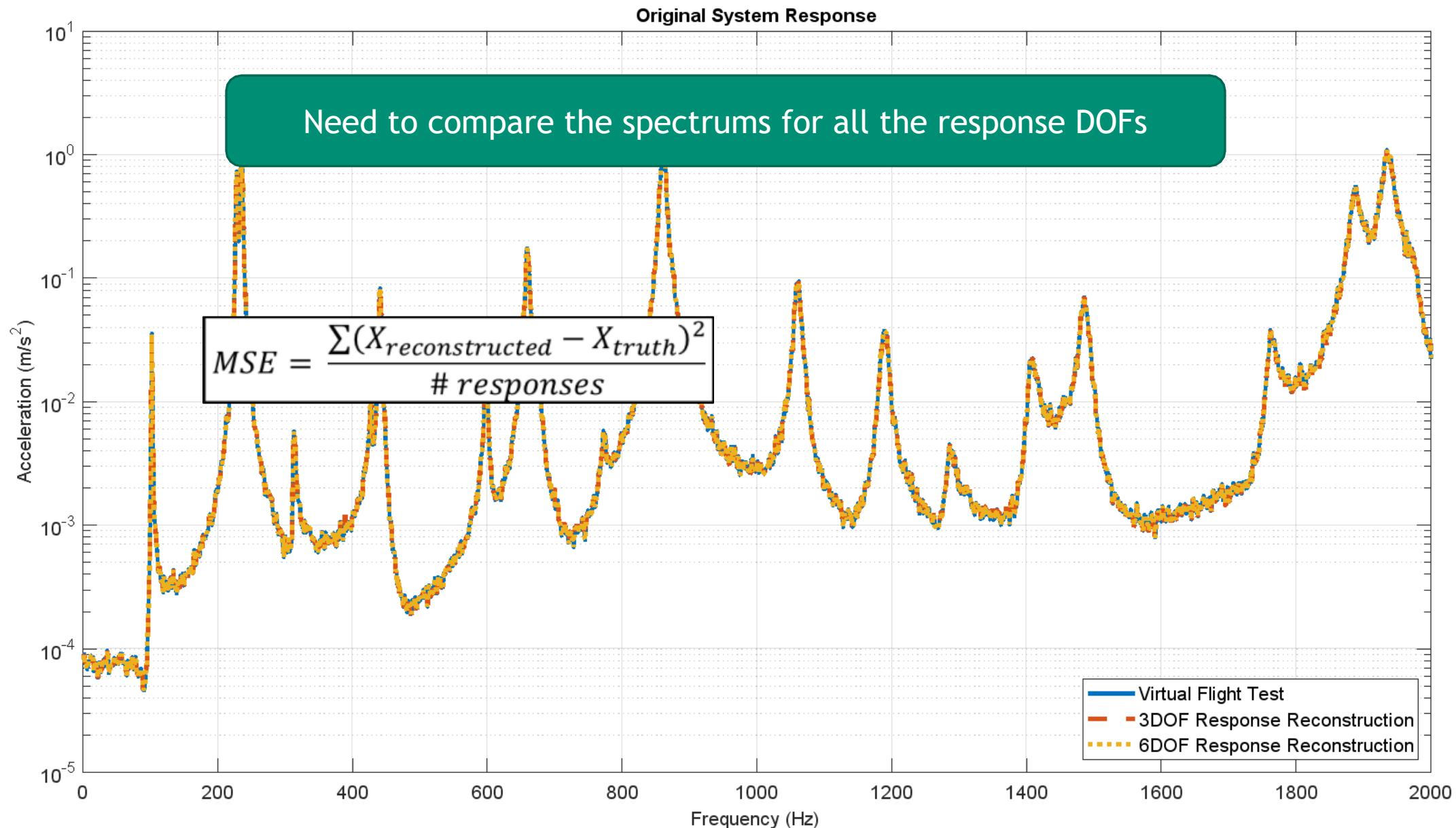
## Results – Standard Force Estimation



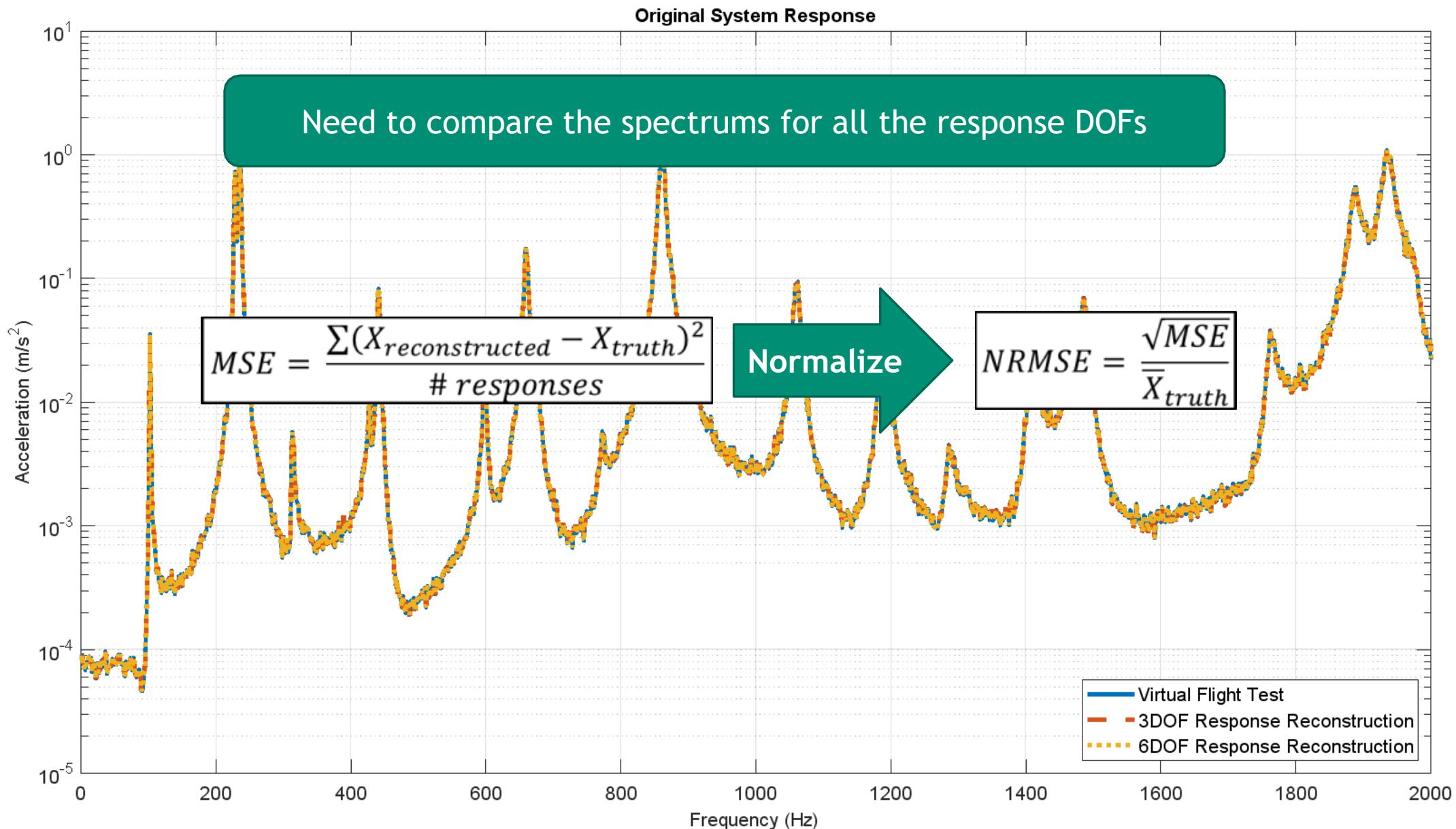
## Results – Standard Force Estimation



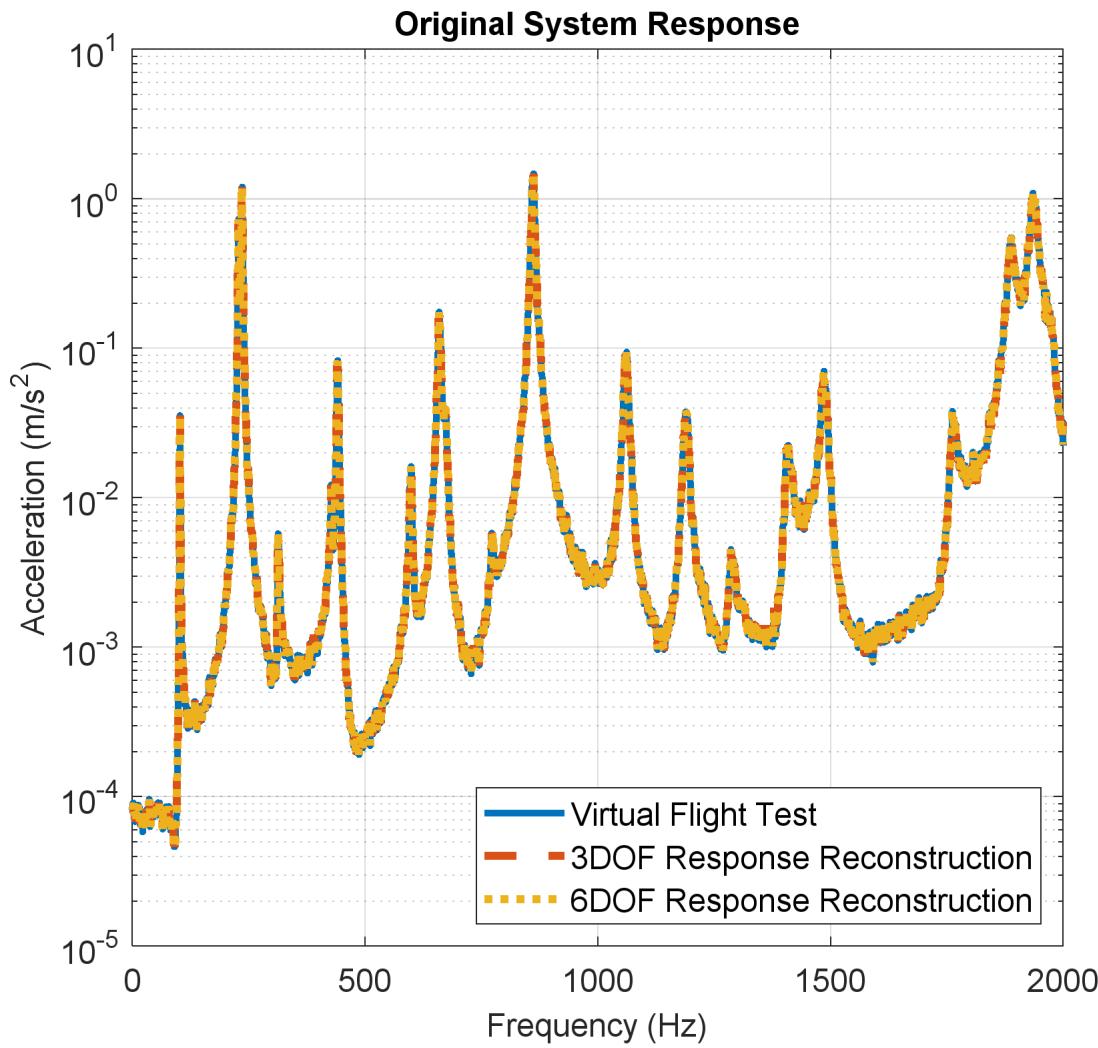
# Results – Standard Force Estimation



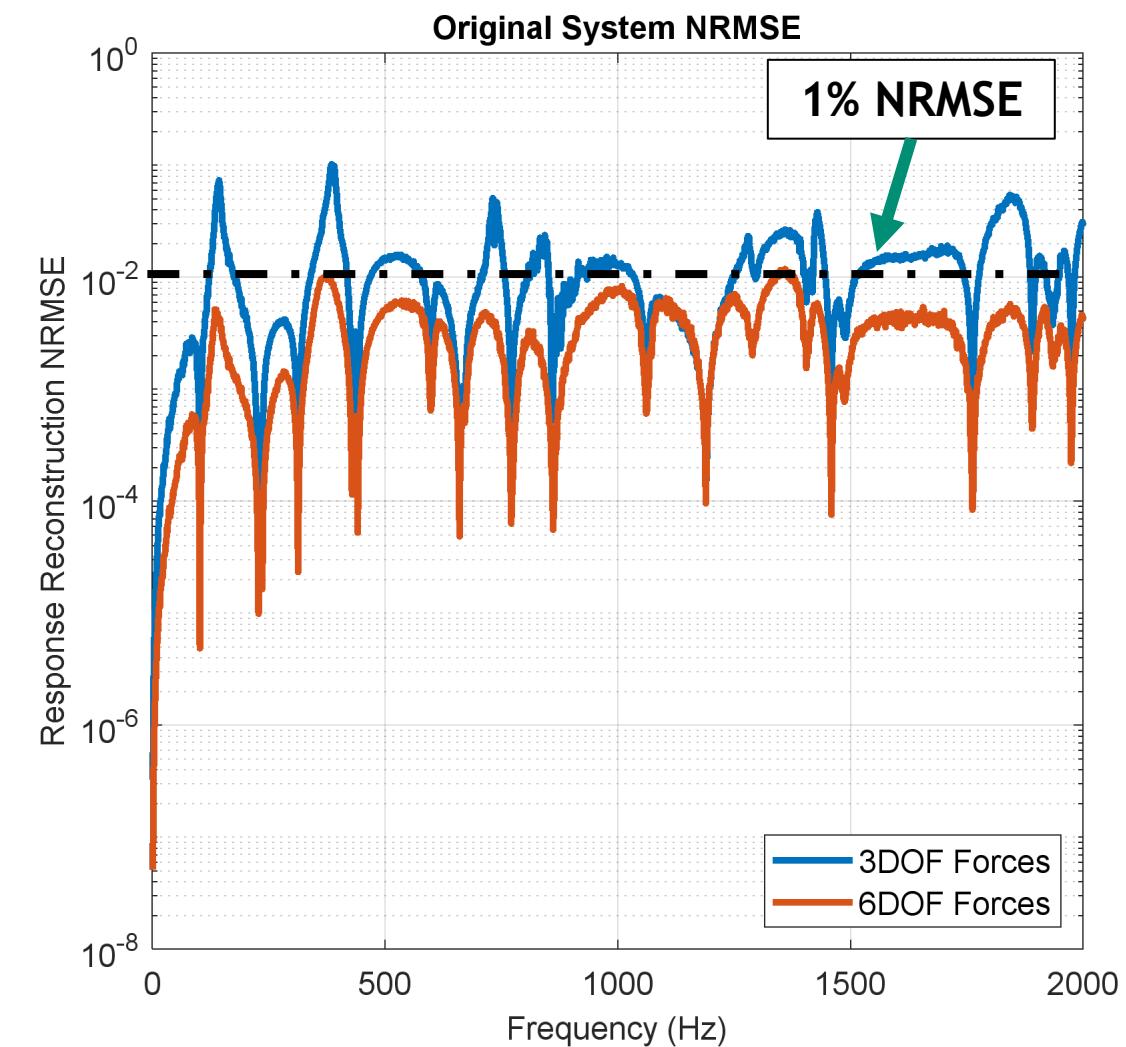
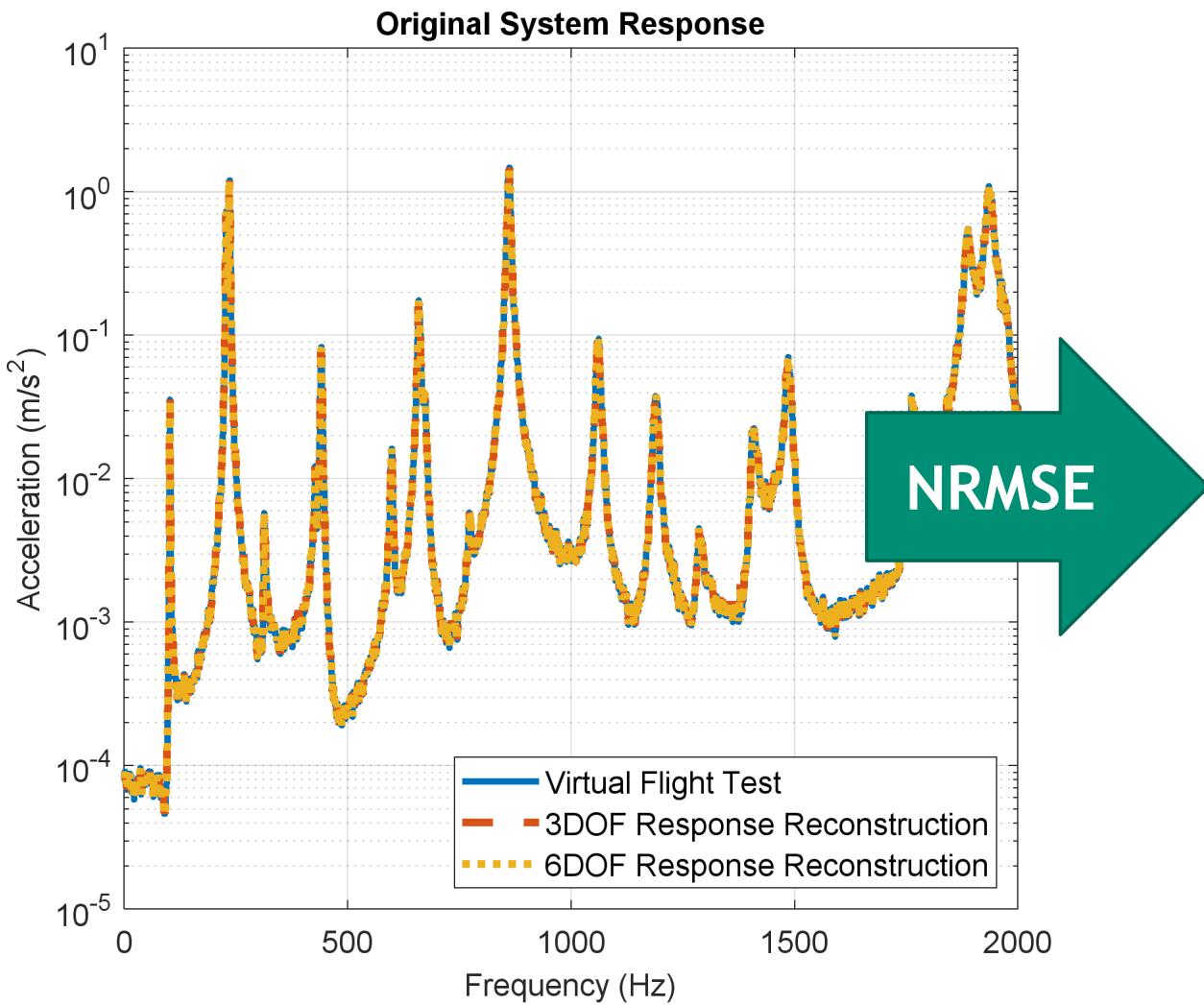
# Results – Standard Force Estimation



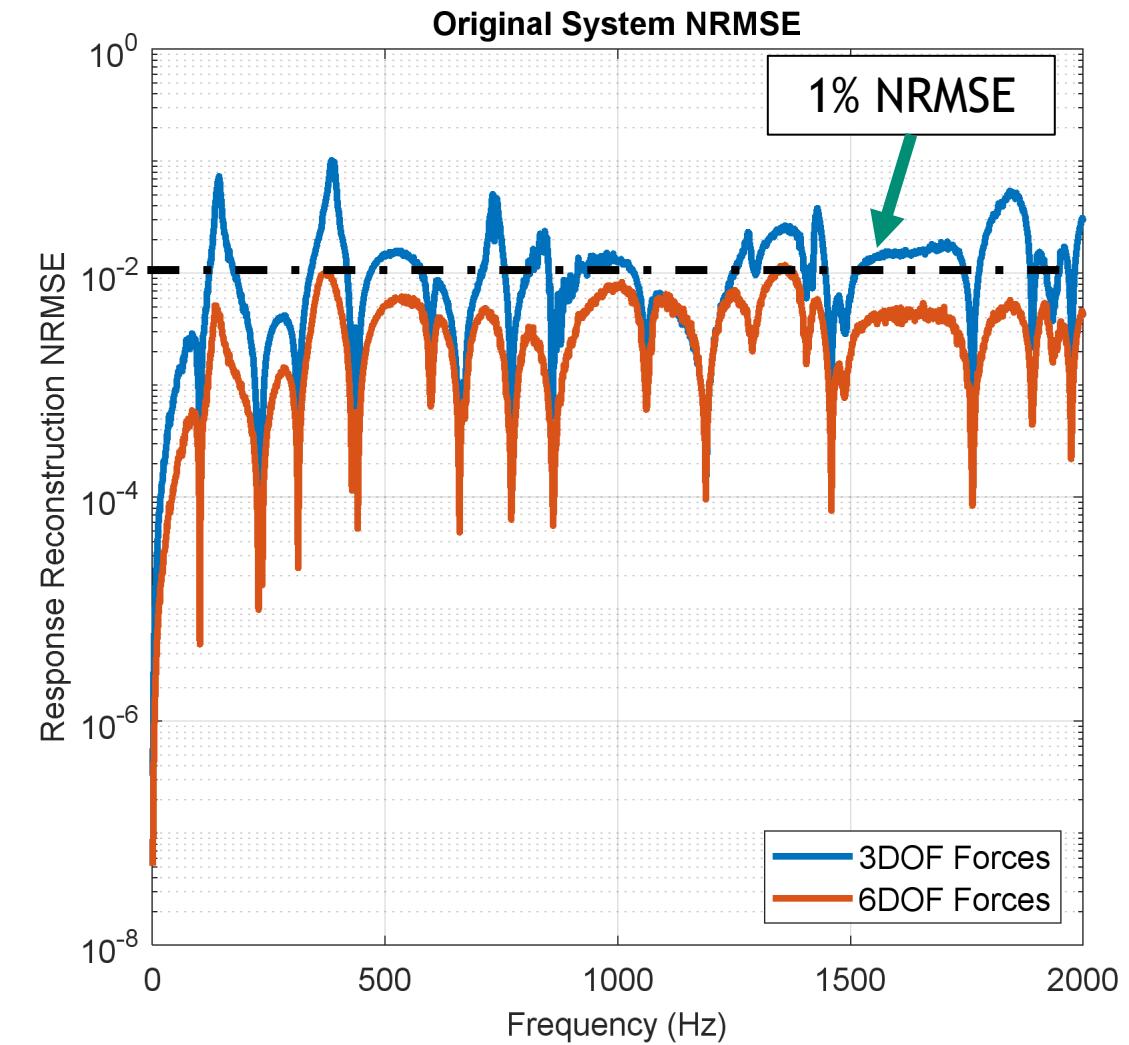
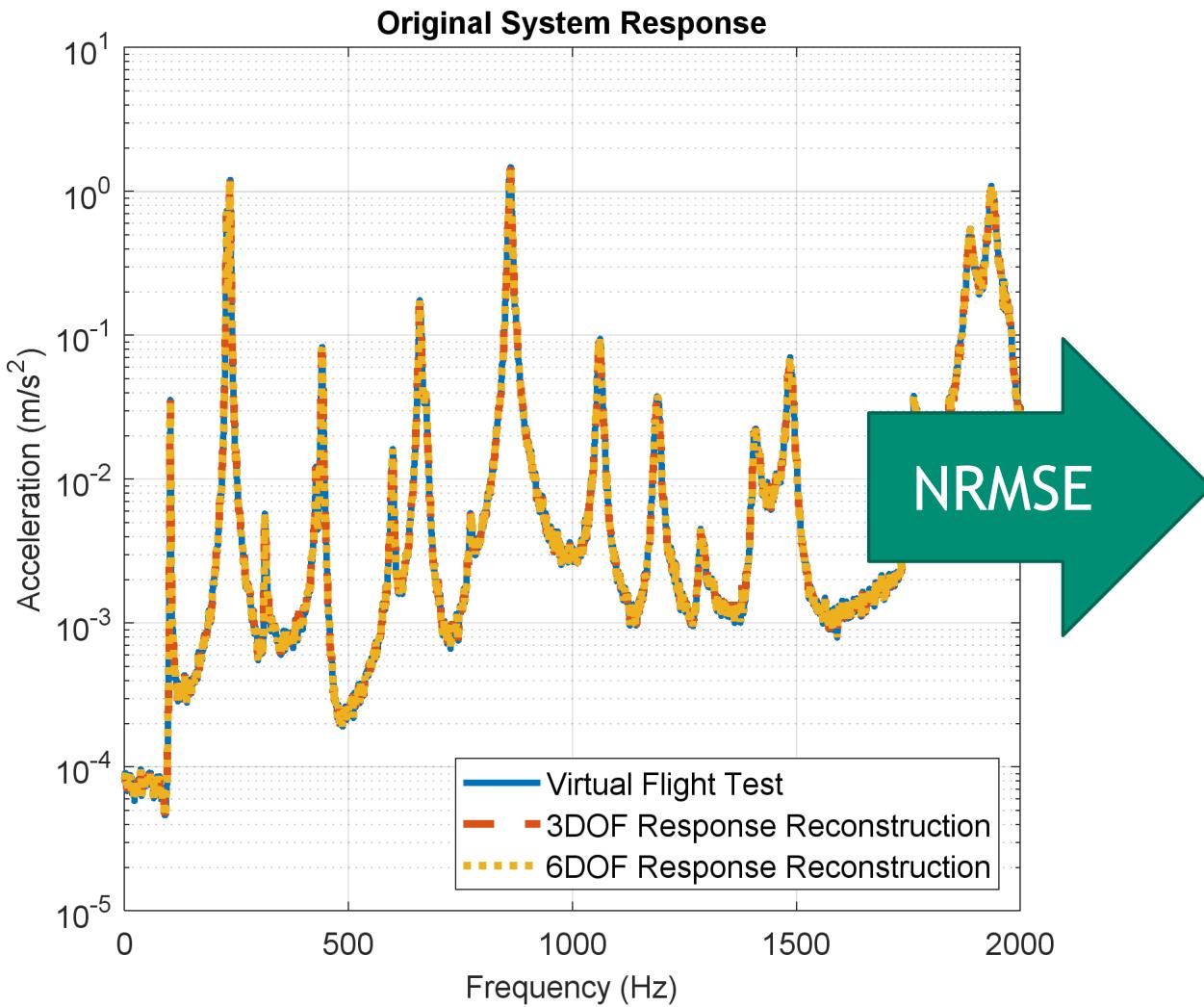
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## Results – Standard Force Estimation

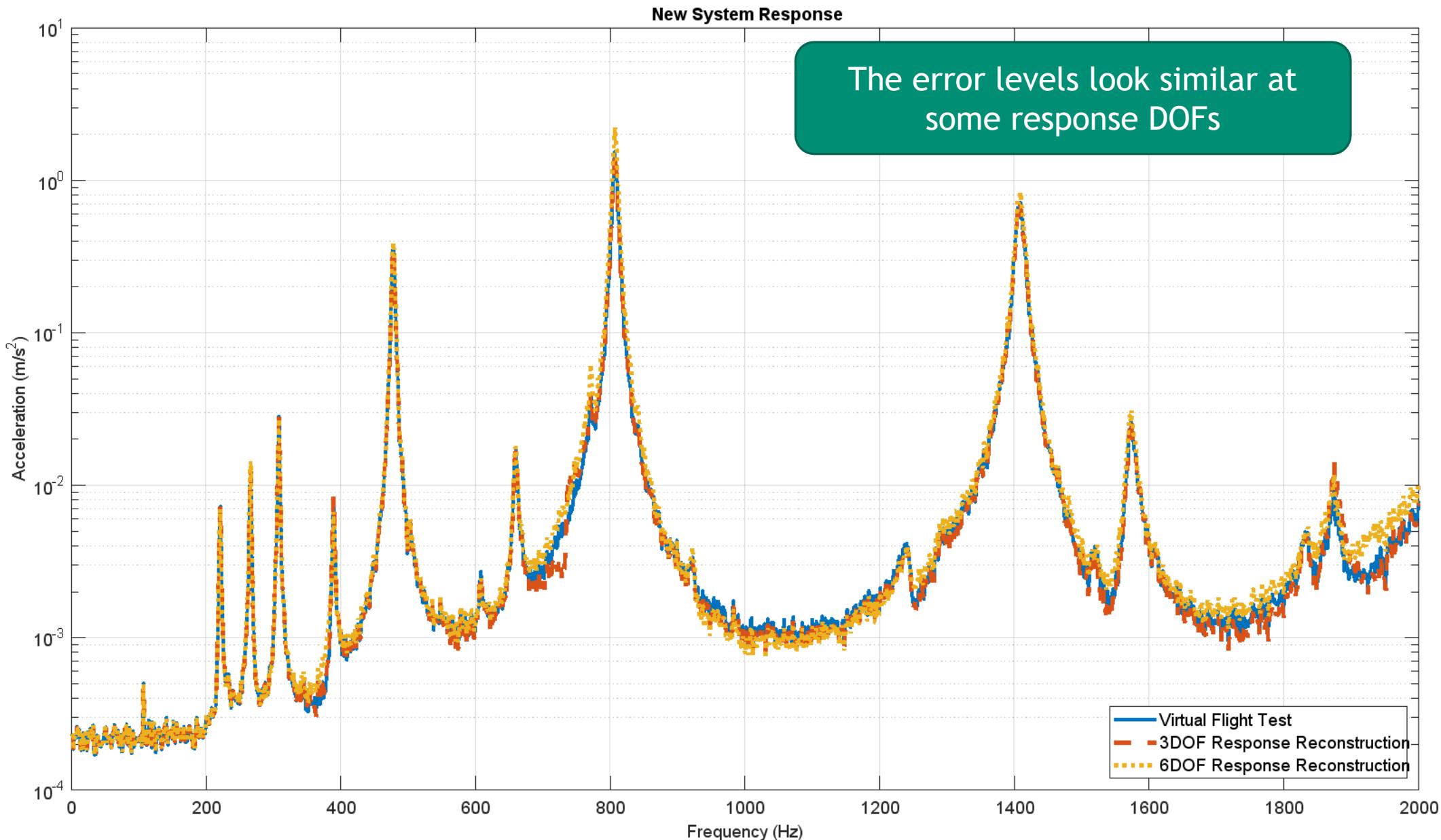


# Results – Standard Force Estimation

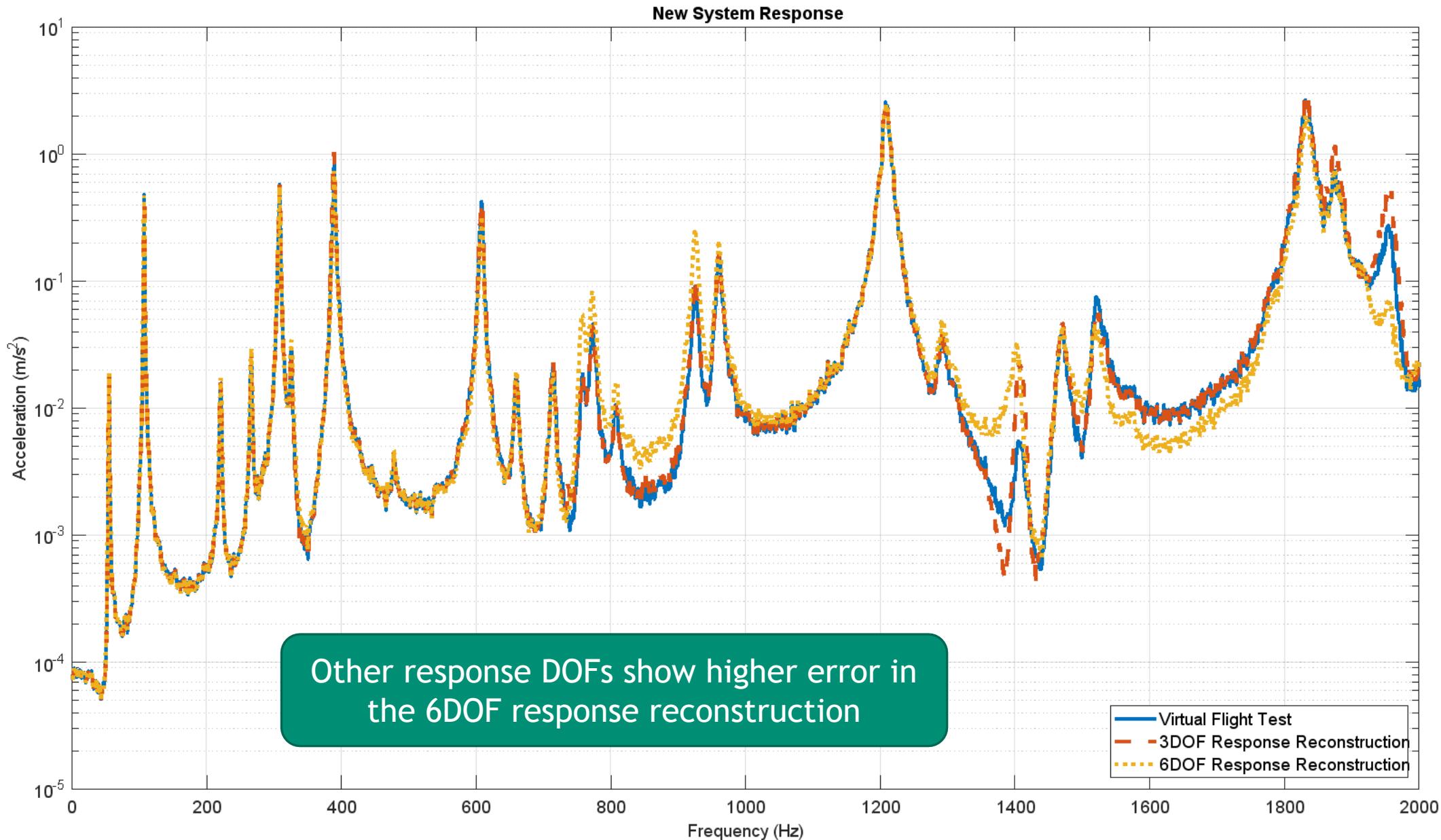


Both response reconstructions are accurate, but the 6DOF reconstruction is slightly better

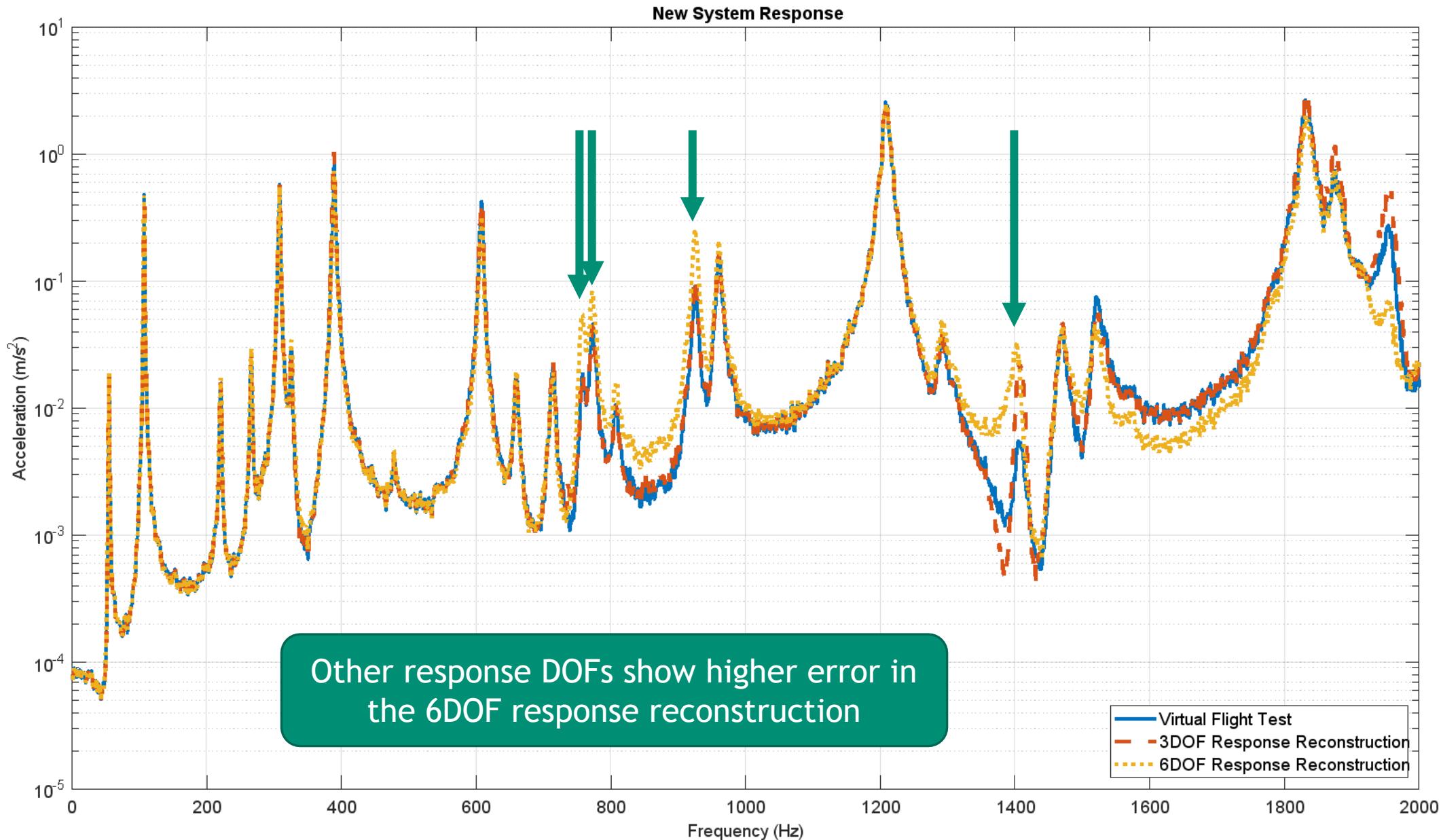
# Results – Standard Force Estimation



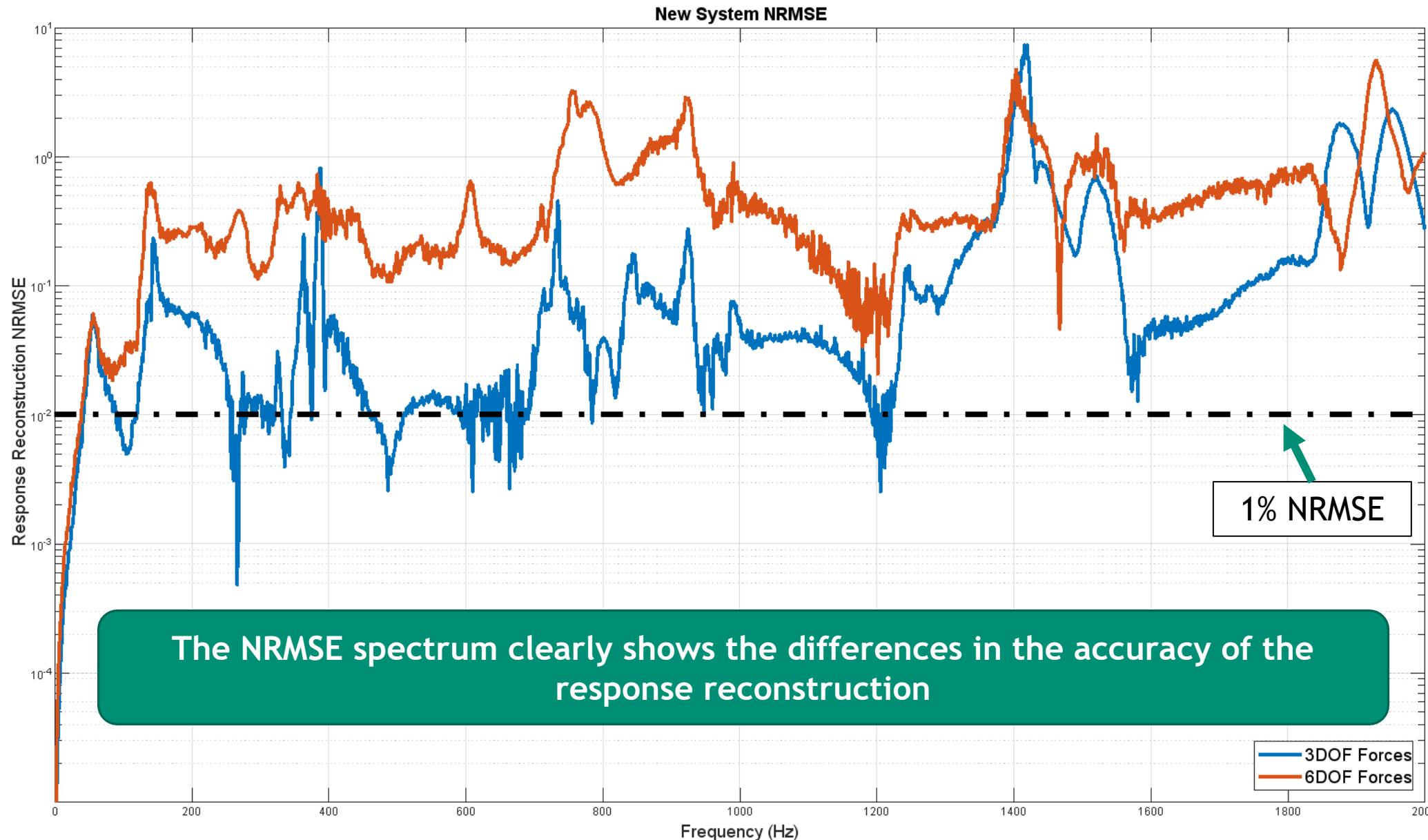
# Results – Standard Force Estimation



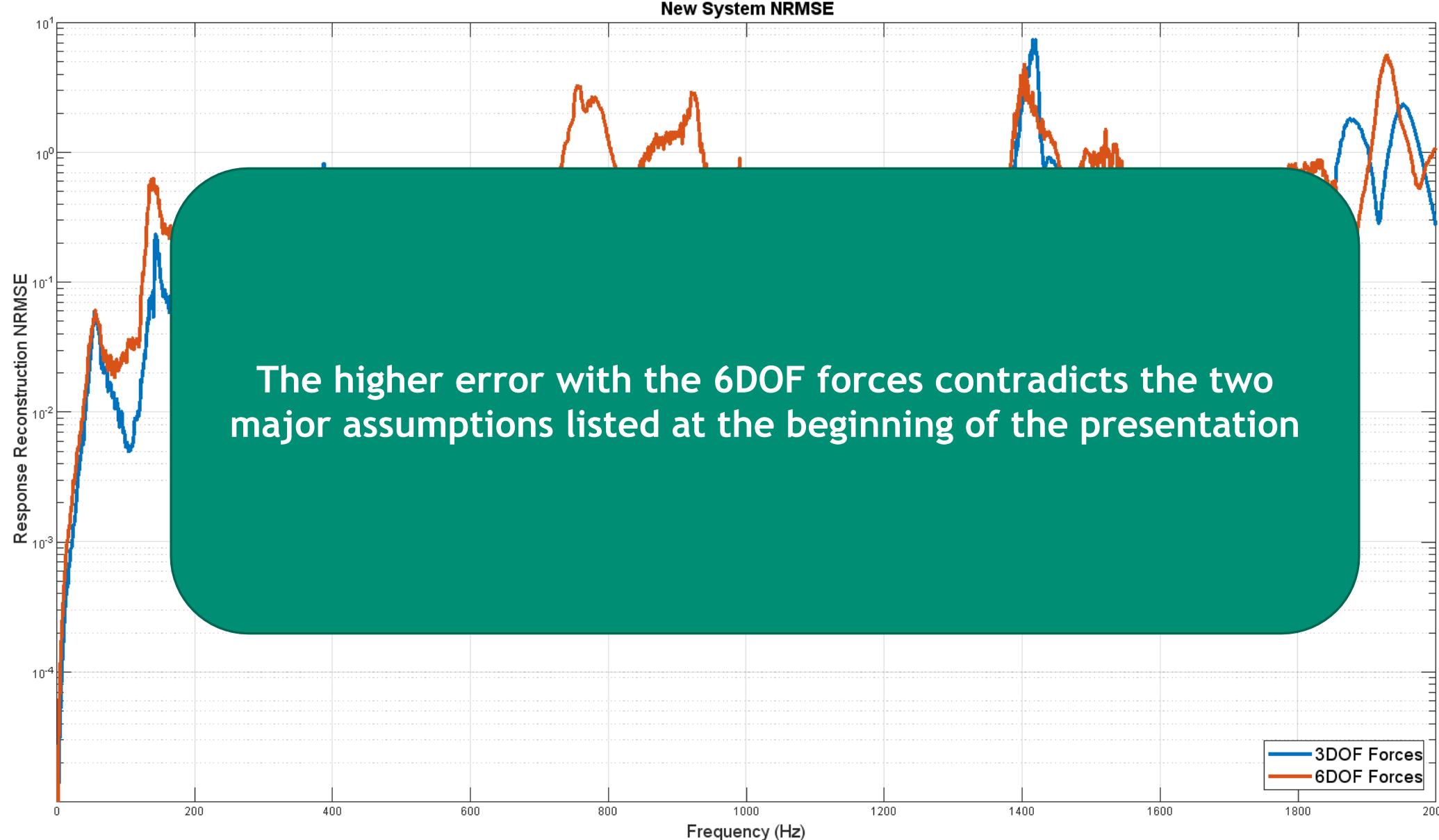
## Results – Standard Force Estimation



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# Results – Standard Force Estimation



## Results – Trouble Shooting the Issue



Swapping the Original and New Systems

Validating the Model Rotations

Singular Value Rejection and Regularization

Adding More Response DOFs to the 6DOF Estimate

Evaluating the Possibility of an Overfit Solution

## Results – Trouble Shooting the Issue



Swapping the Original and New Systems

Validating the Model Rotations

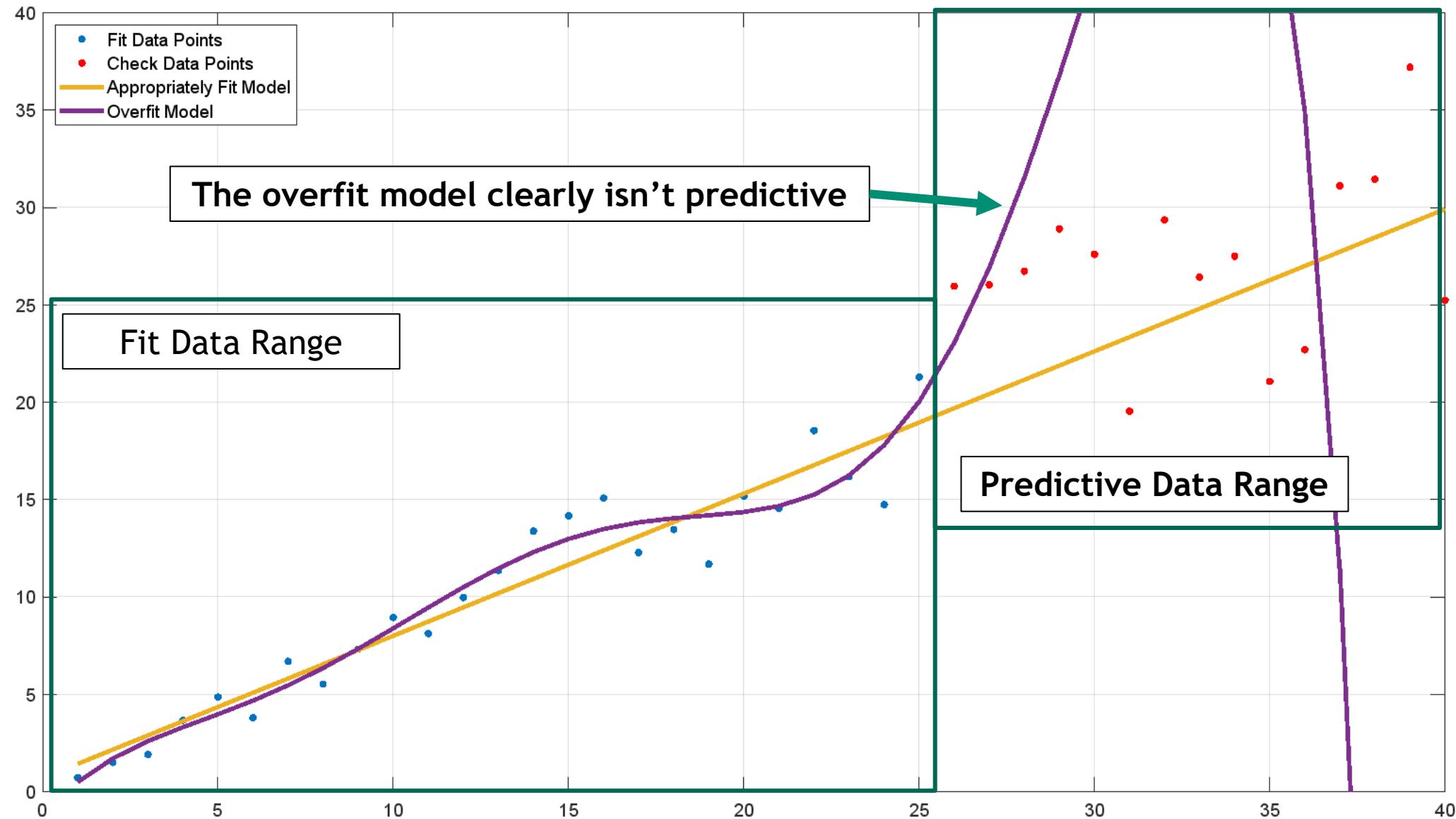
Singular Value Rejection and Regularization

Adding More Response DOFs to the 6DOF Estimate

Evaluating the Possibility of an Overfit Solution

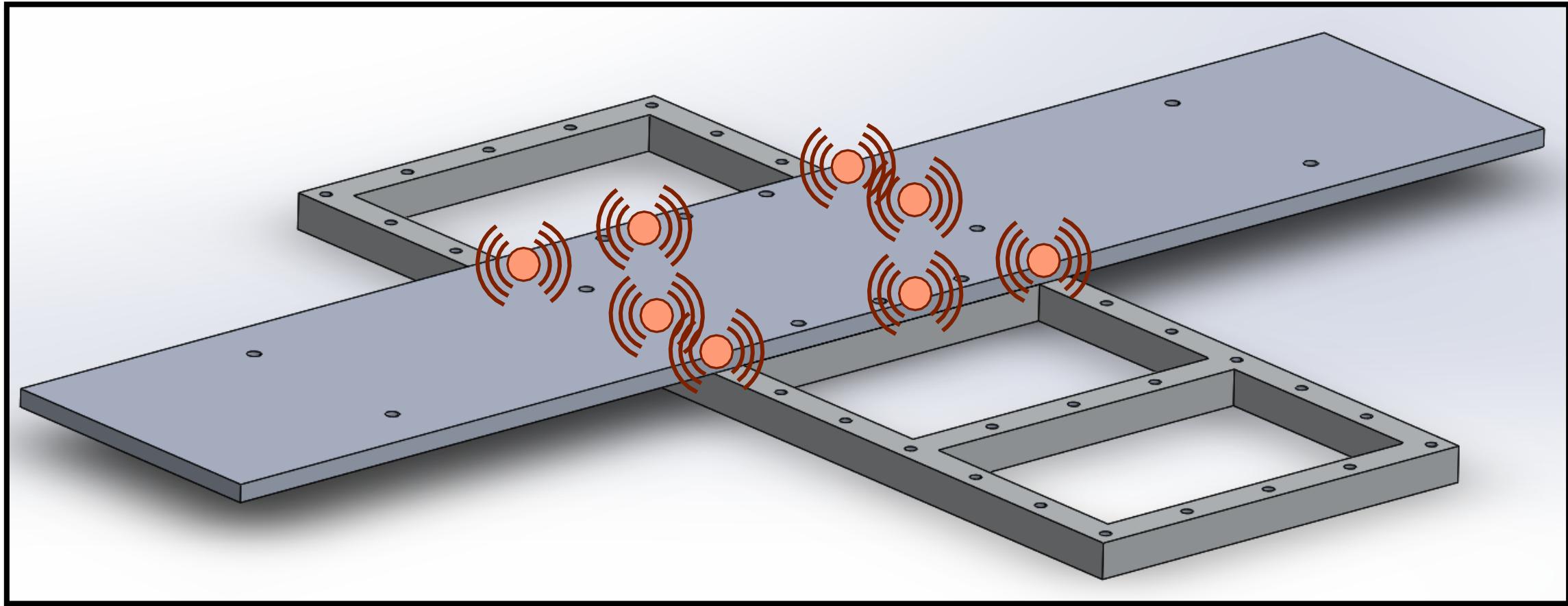
- This seems to provide the best explanation for the errors that are being seen

## Example of an Overfit Solution on 2D Data



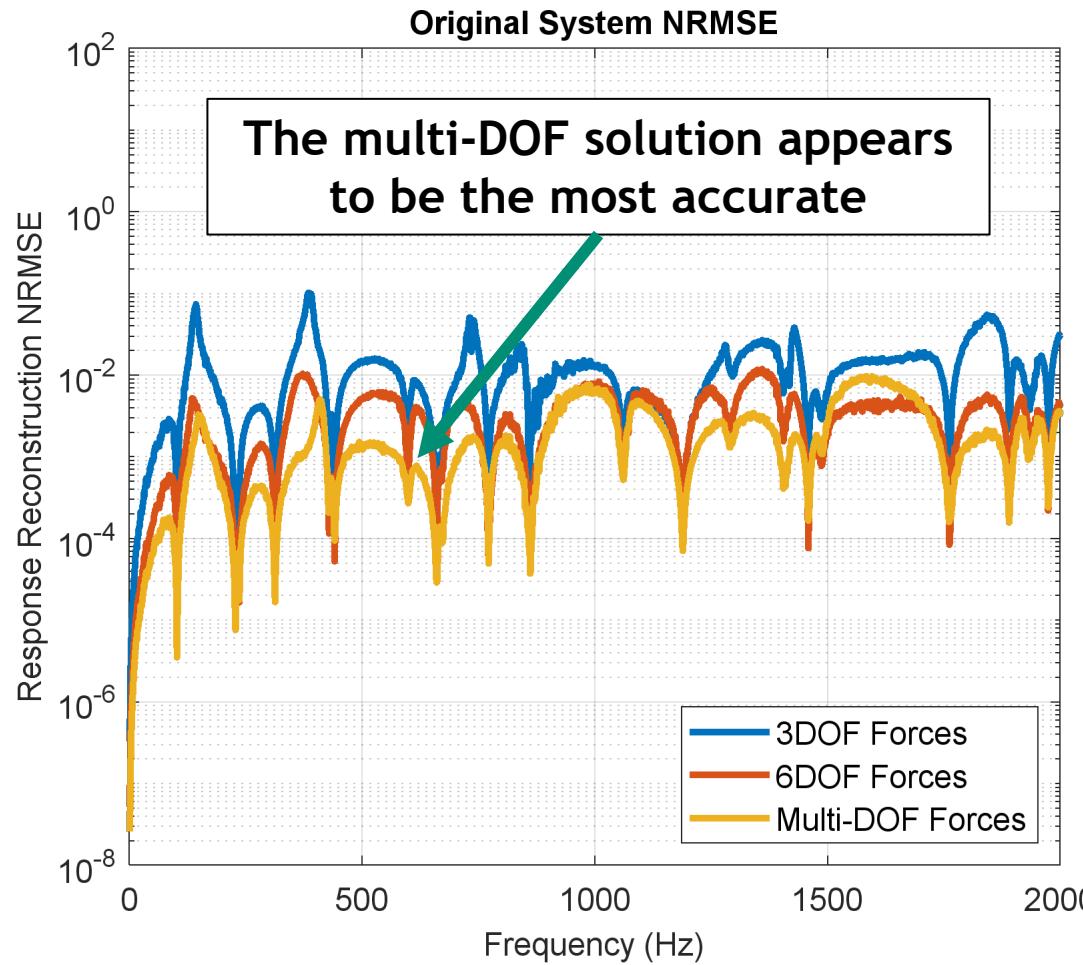


**Overfit Solution Hypothesis:** Adding more 3DOF references into the force estimation should provide similar results to the 6DOF solution

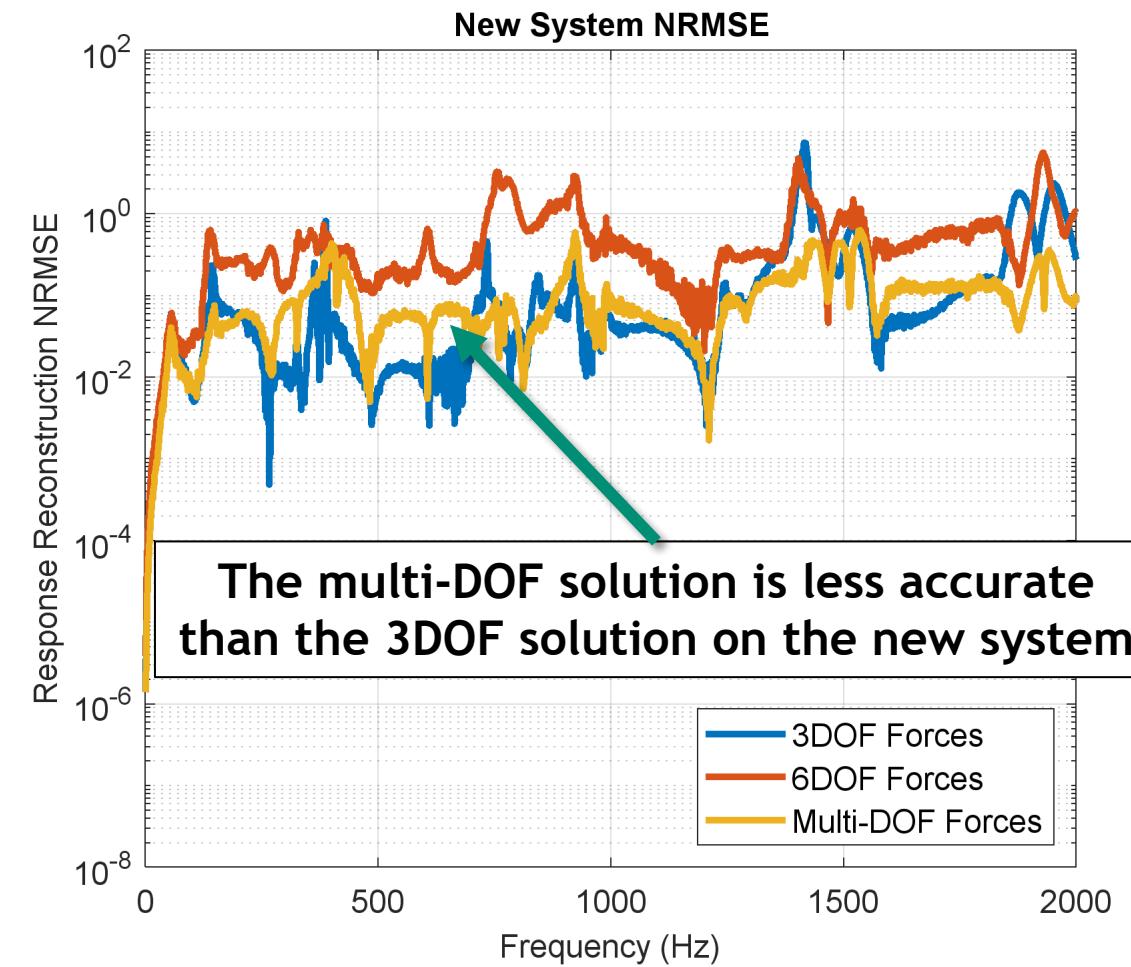
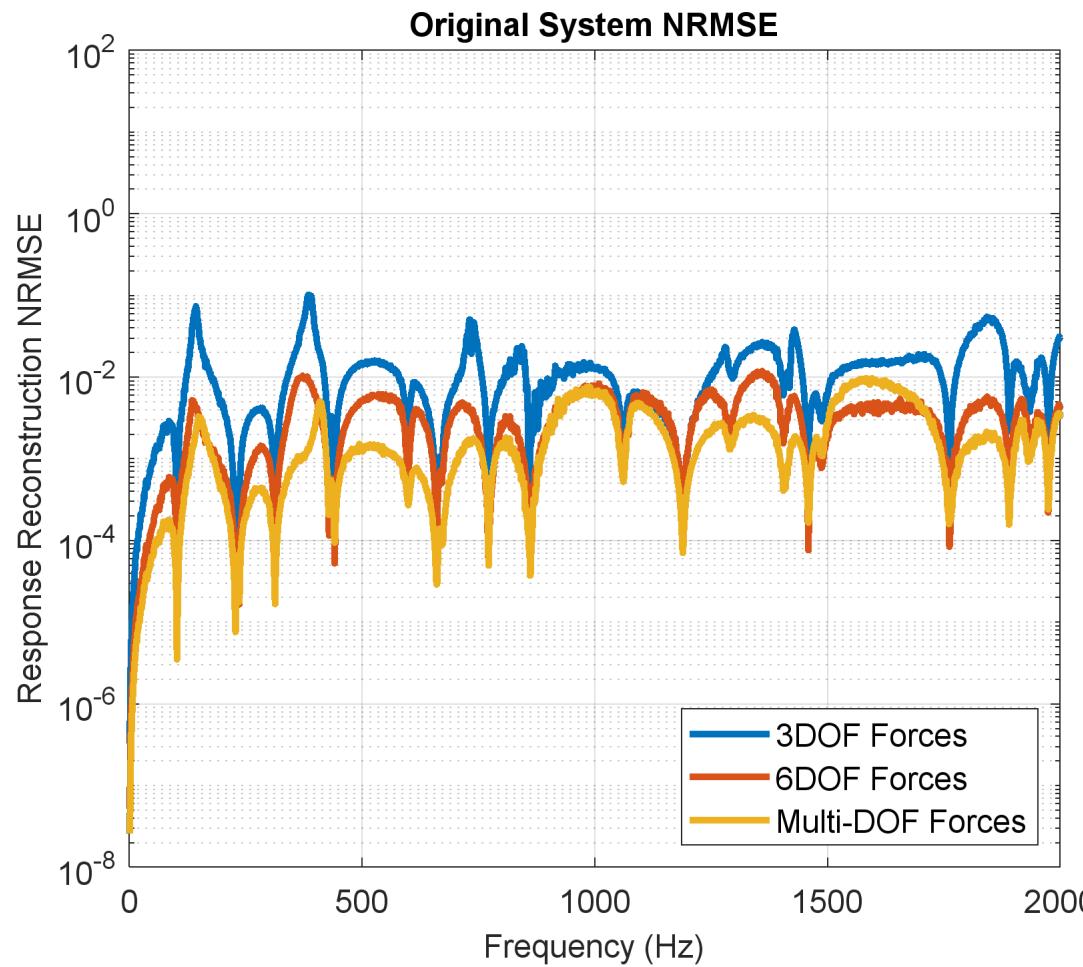


Several 3DOF references were used on the frame to match the number of reference DOFs in the 6DOF estimate

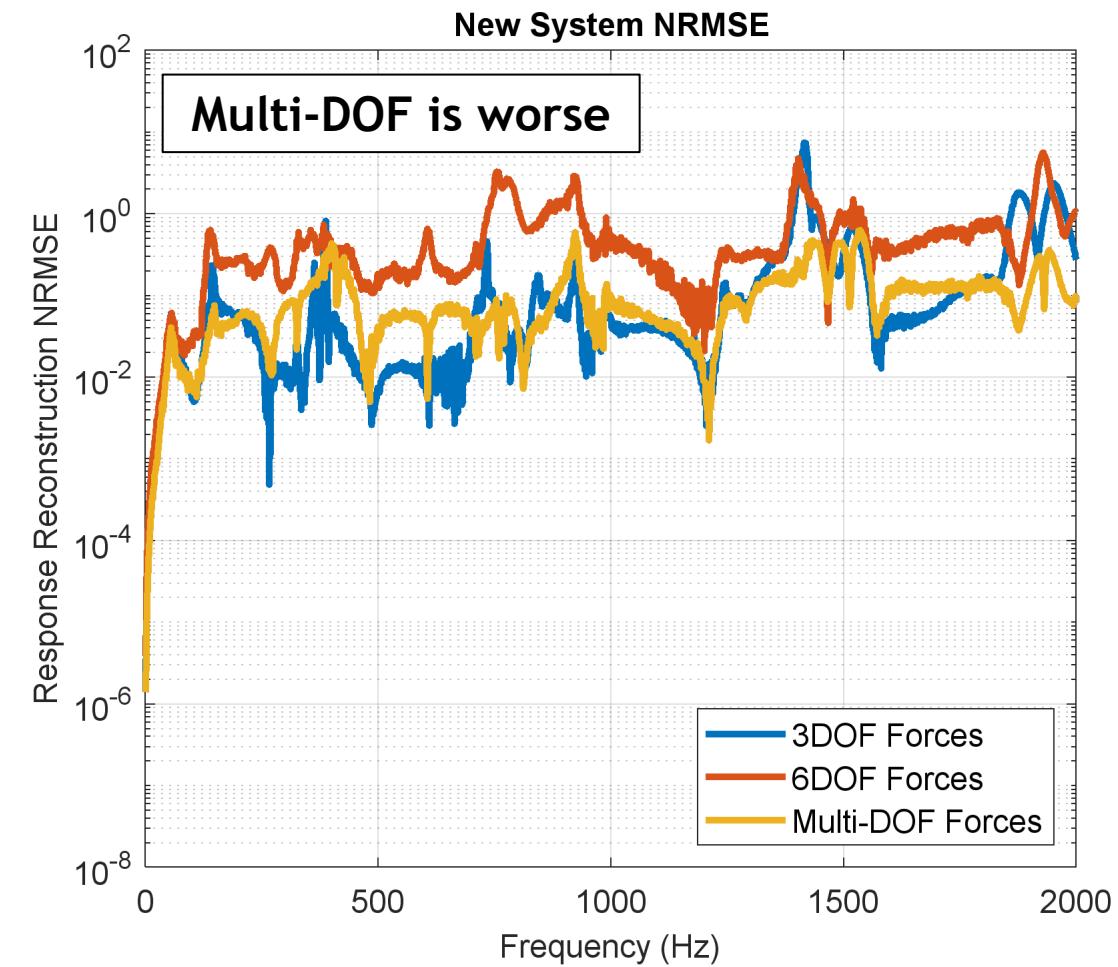
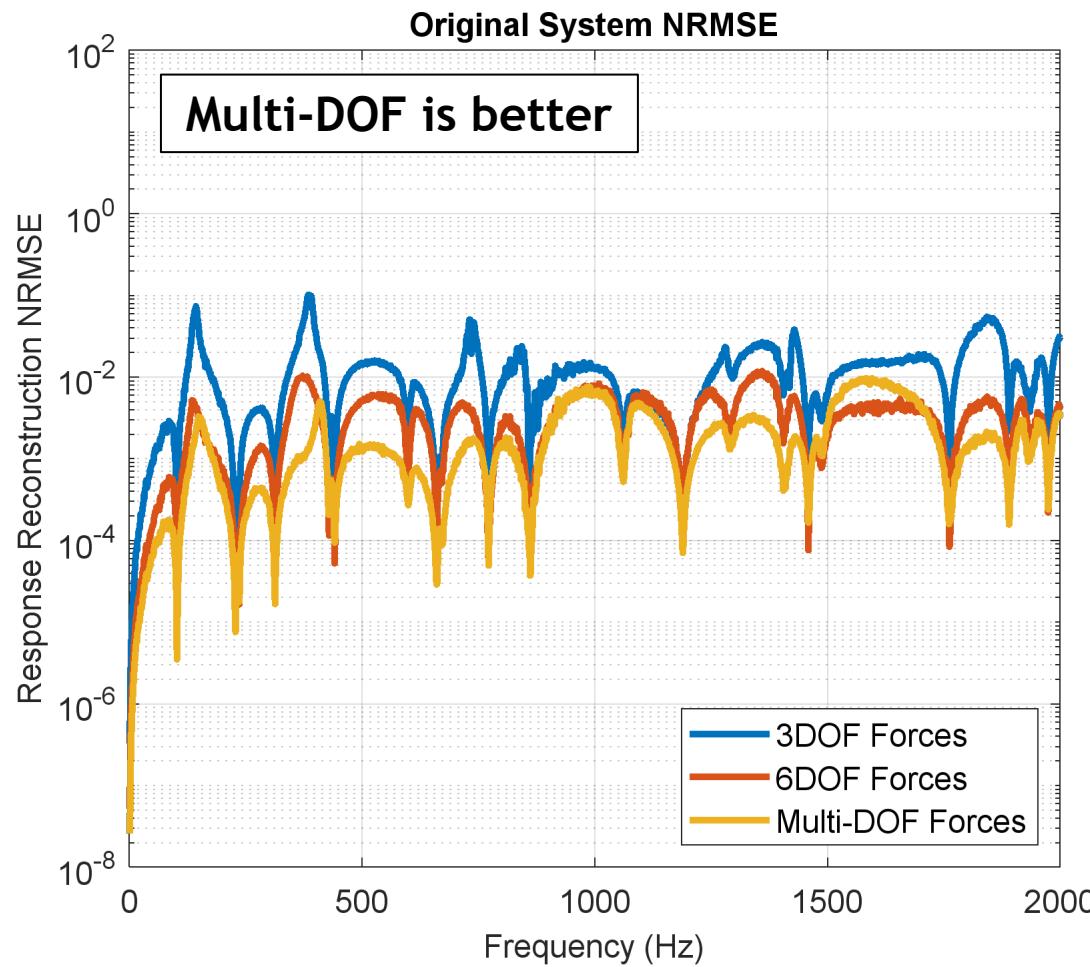
# Testing for the Possibility of an Overfit Solution – Results



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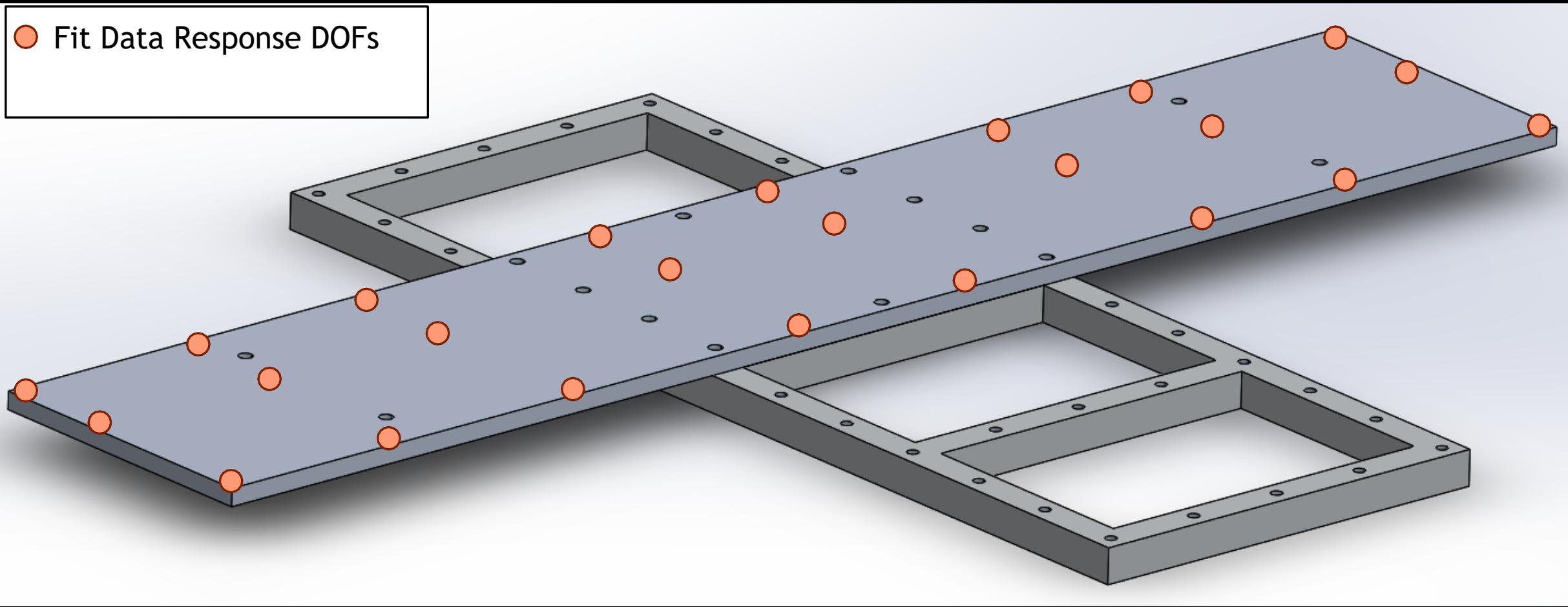
The multi-DOF solution shows similar trends to the 6DOF solution, indicating that the trends are due to an overfit solution



*Could sample splitting be used to check for overfit solutions?*

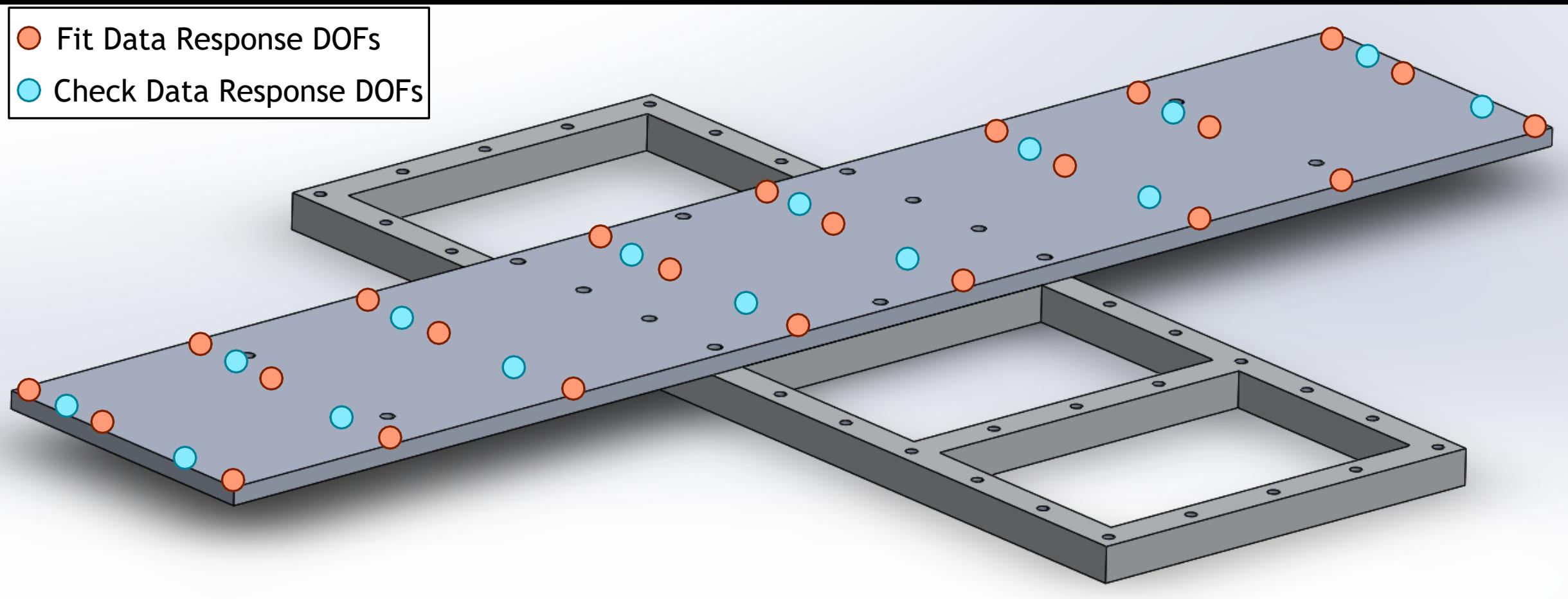
# Testing for the Possibility of an Overfit Solution – Sample Splitting Setup

40



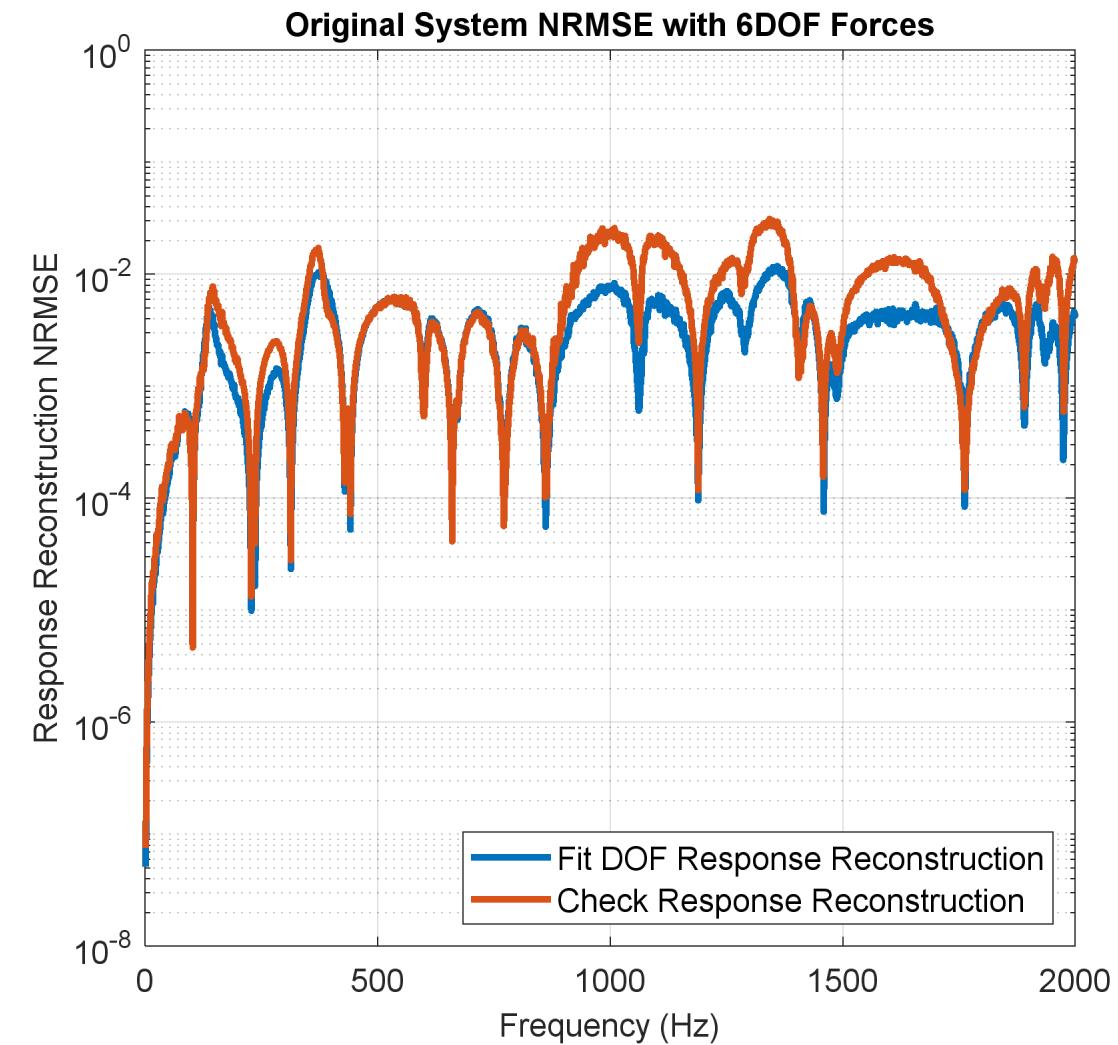
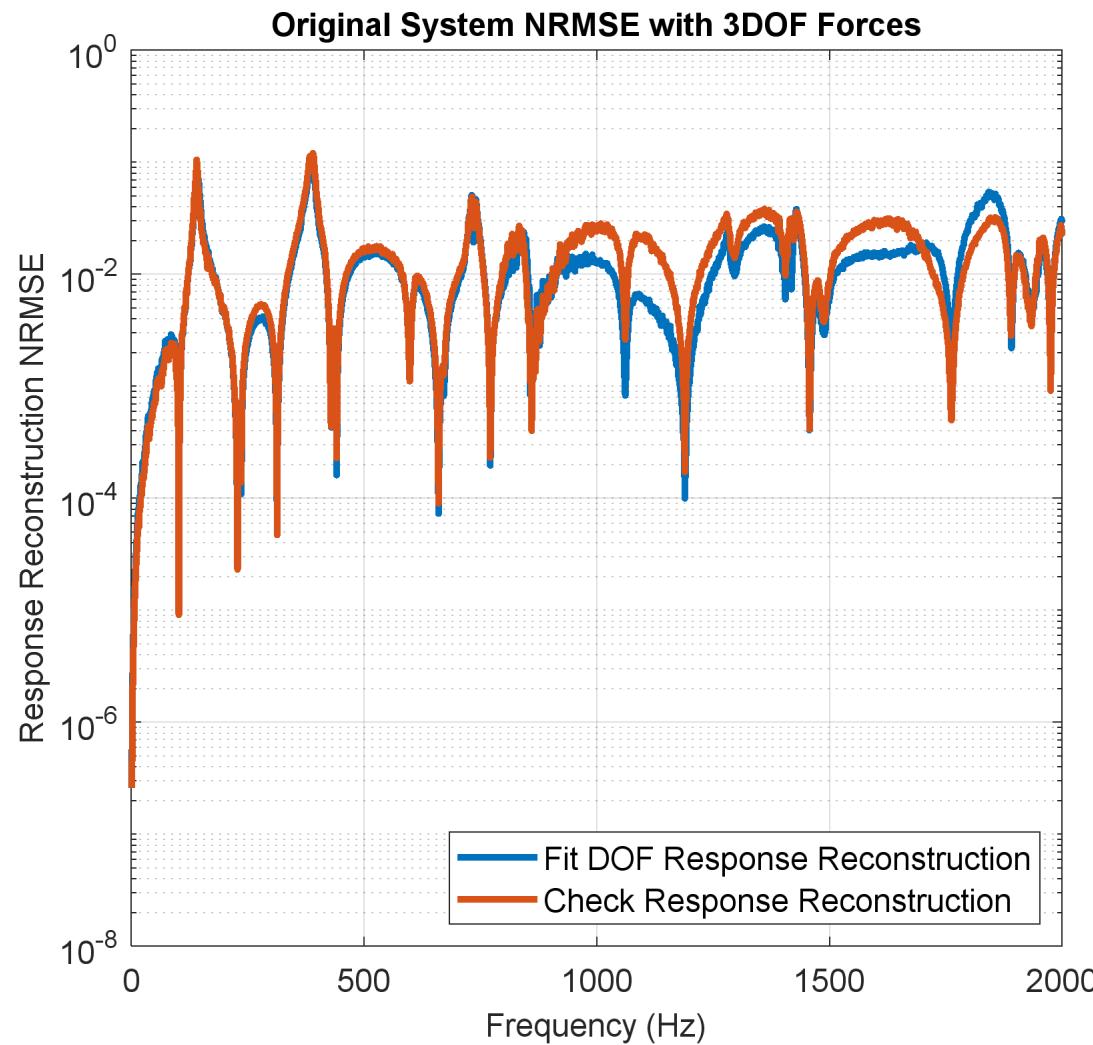
# Testing for the Possibility of an Overfit Solution – Sample Splitting Setup

41



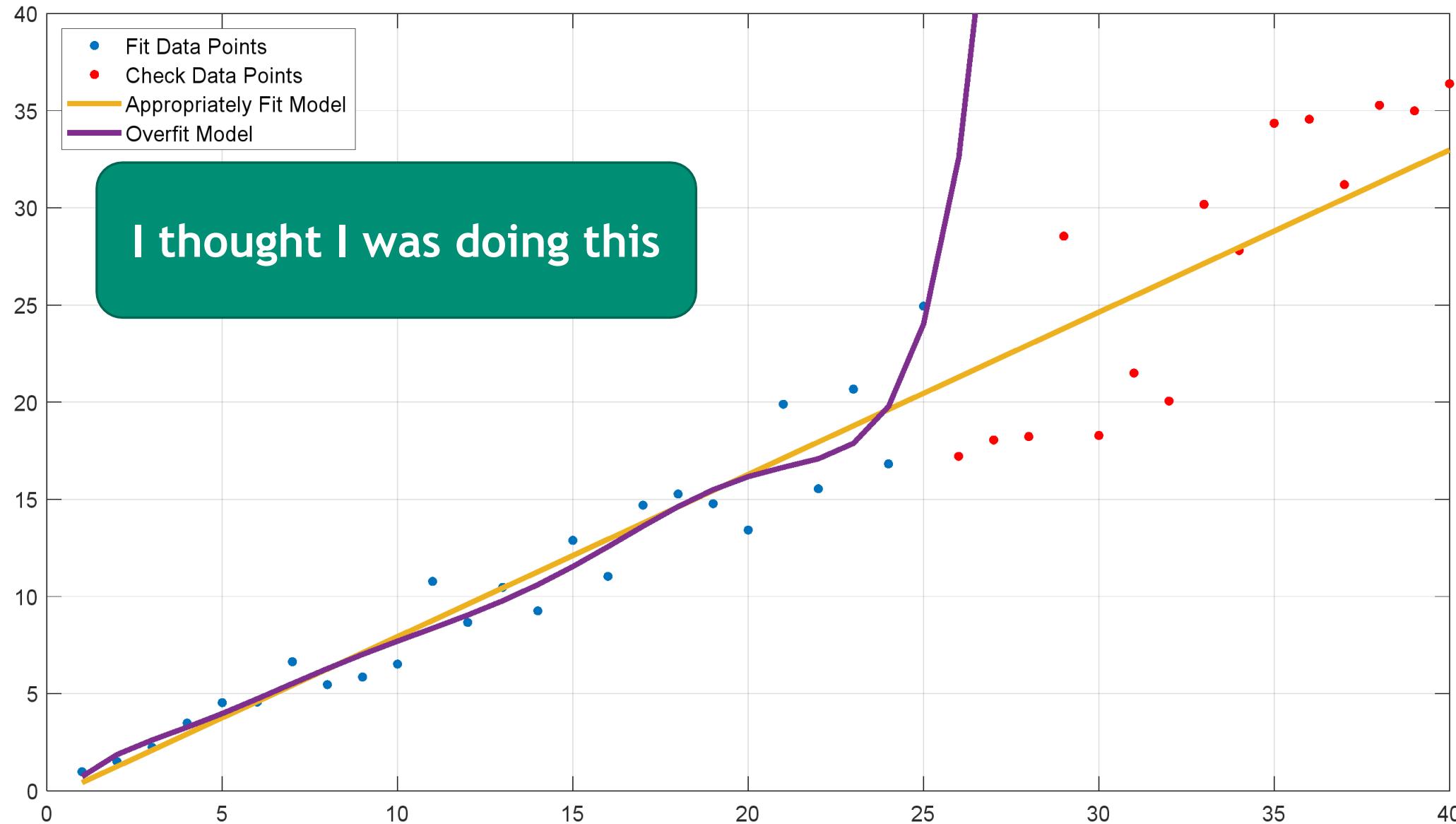
Different response DOFs were used to estimating the forces and perform the response reconstruction check

# Testing for the Possibility of an Overfit Solution – Sample Splitting



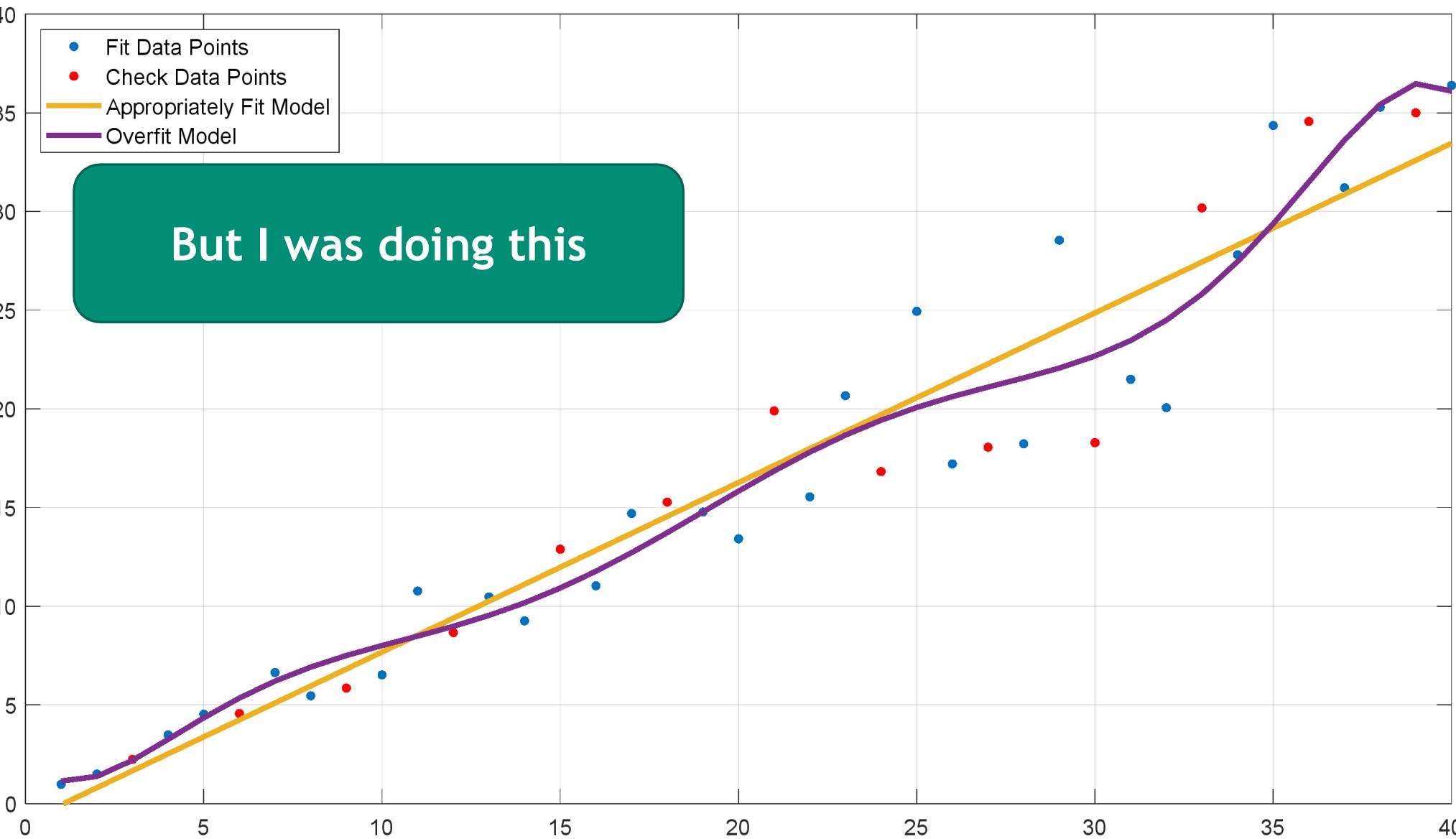
There aren't differences in the NRMSE spectrums for the different DOF sets

## Potential Issue with Sample Splitting – 2D Data Example



I thought I was doing this

## Potential Issue with Sample Splitting – 2D Data Example



## Key Findings and Conclusions



Response reconstruction error may be insufficient for validating force estimates

Need to be careful when choosing reference DOFs for inverse force estimation

Practitioners should consider two forms of error for inverse force estimation:

- Measurement error
- Model form error



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## Key Findings and Conclusions



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***superfluous reference DOFs could lead to a less predictive model***

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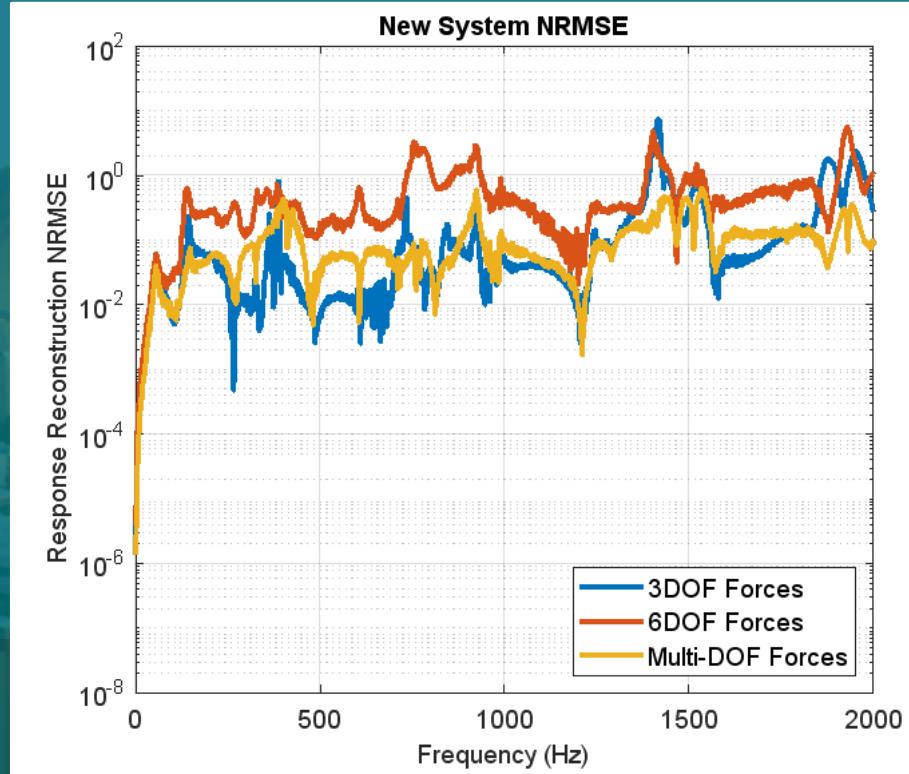
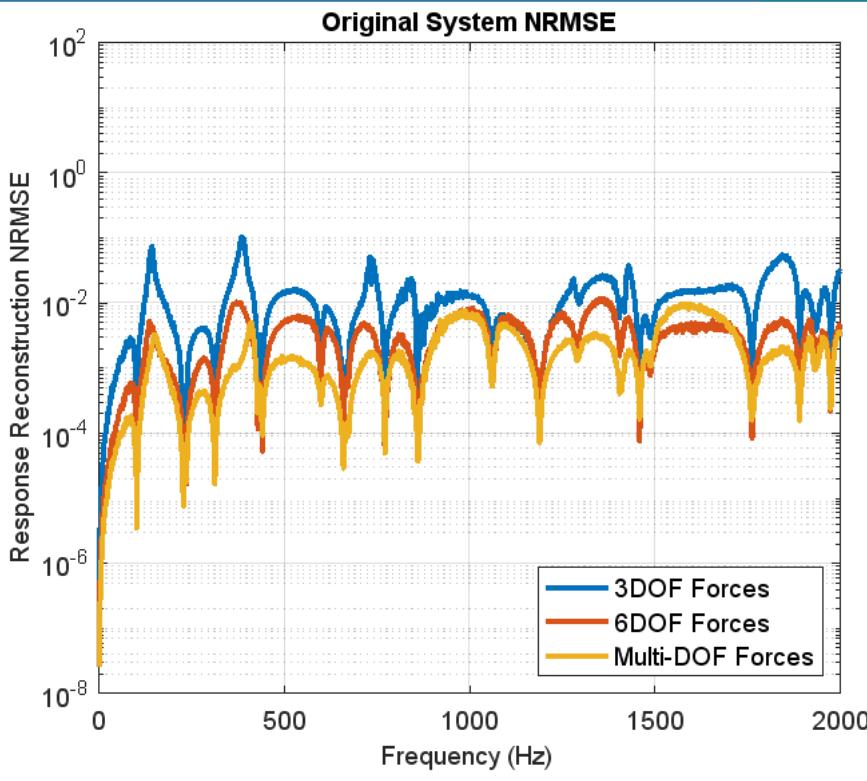


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- **Measurement error**
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# Thank You!

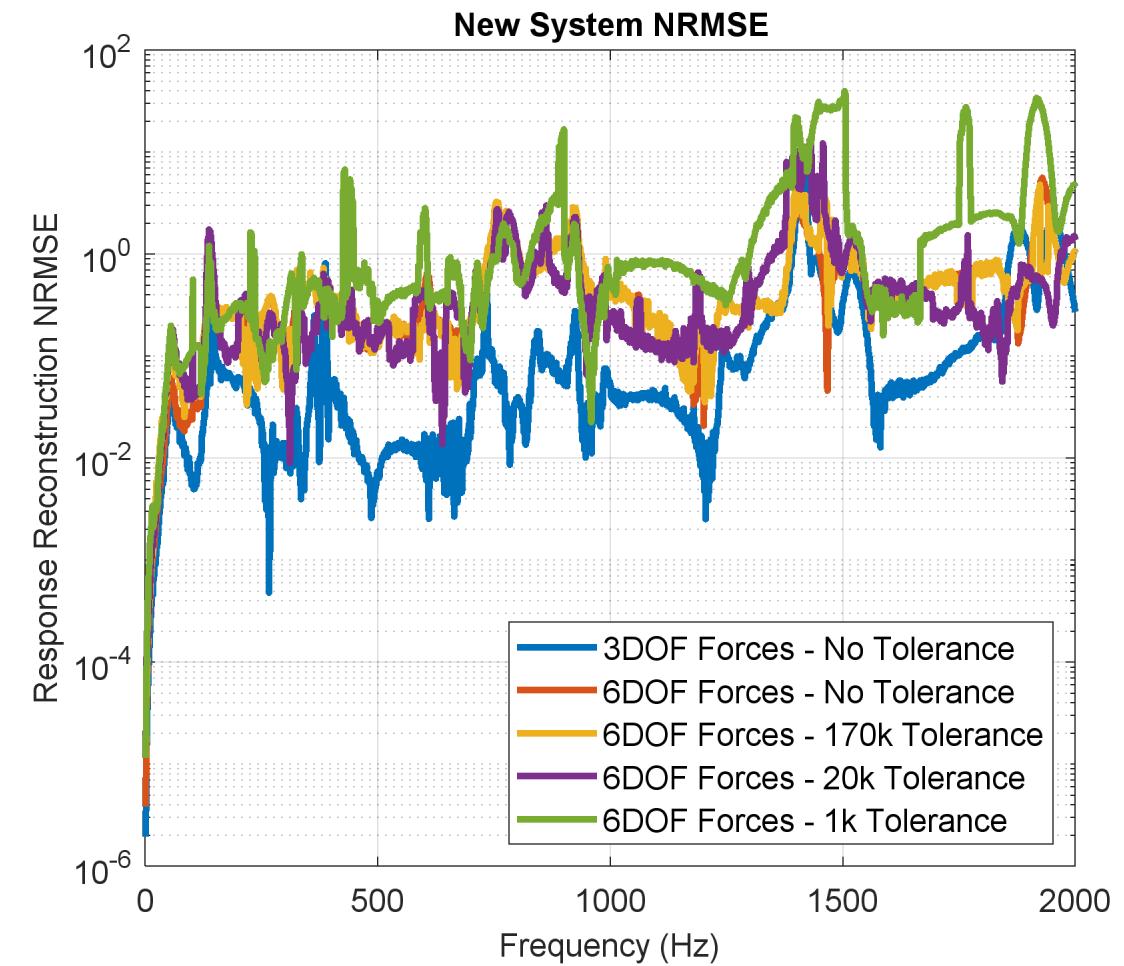
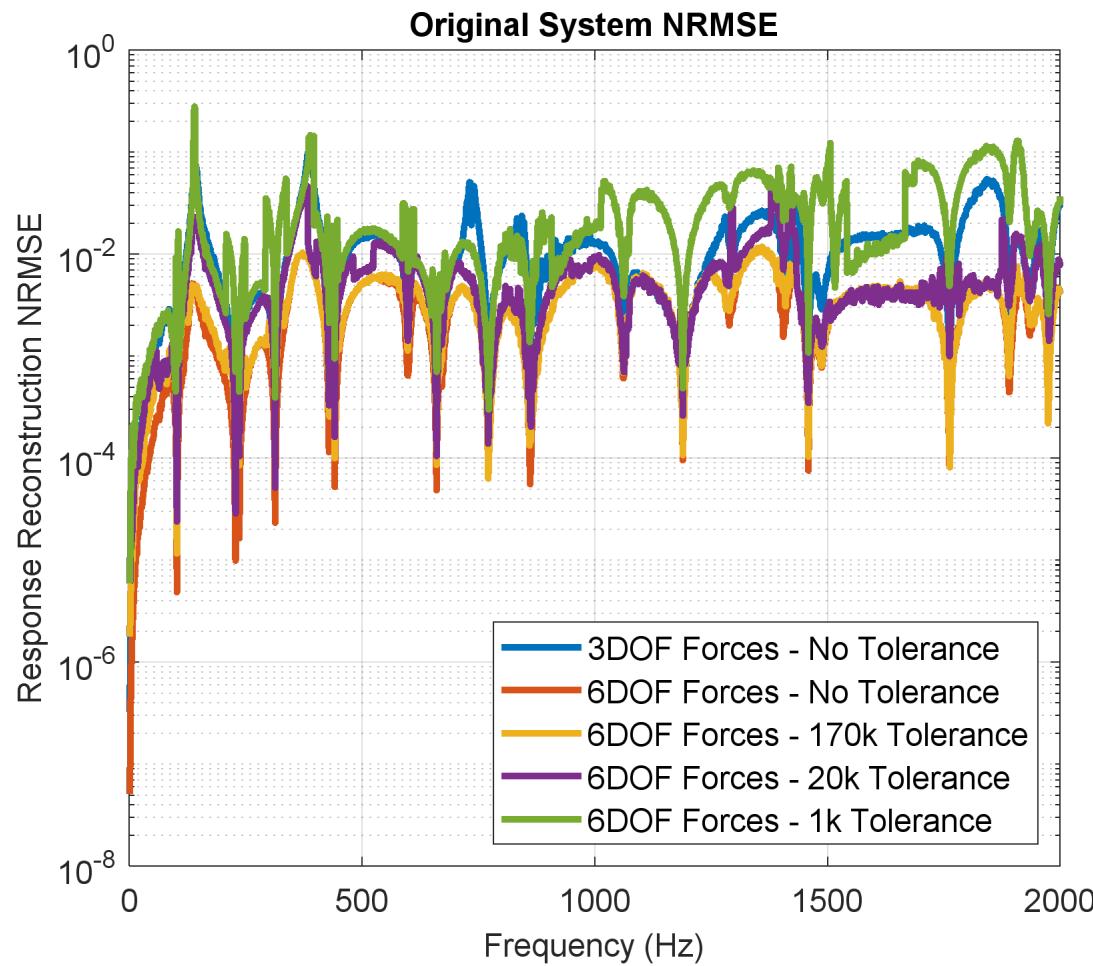
- *Response reconstruction error may be a misleading metric for the accuracy of estimated forces*
- *Unnecessary reference DOFs may lead to errors in inverse force estimation*



# Back-up

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# Results – Singular Value Rejection



# Results – Regularization

