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# Requirements for Interdependent Reserve Types Providing Primary Frequency Control

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## Reference

Garcia, Manuel, and Ross Baldick.  
"Requirements for interdependent reserve types providing primary frequency control." IEEE Transactions on Power Systems 37.1 (2021): 51-64.

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# Inverter-Based Resources & Primary Frequency Response

- Inverter-Based Resources (IBRs) have been detrimental to primary frequency control.
  - Do not provide inertia.
  - Traditionally do not provide frequency control.
- Difficulties in performing primary frequency control.
  - Low system-wide inertia levels makes it more difficult to arrest system-wide frequency decline.
  - Accommodating a large generator trip is difficult.
- Some regions have proposed new ancillary services for primary frequency control.
  - ERCOT [1], NEM [2], and National Grid [3] proposed new ancillary services for primary frequency control.
  - Western and Eastern interconnect have not proposed such ancillary services.

*Table 1: Yearly minimum inertia levels and largest contingencies in various regions.*

ISO/Region	US West [4]	US East [4]	(Texas) ERCOT [4]	(Australia) NEM [5]	(UK) National Grid [6], [7]
Yearly Minimum Inertia (GWs)	472	1281	134	4.4	129
Largest Contingency (MW)	2626	4500	2750	100	1260
Inertia/Contingency Ratio (s)	179	284	48	44	102

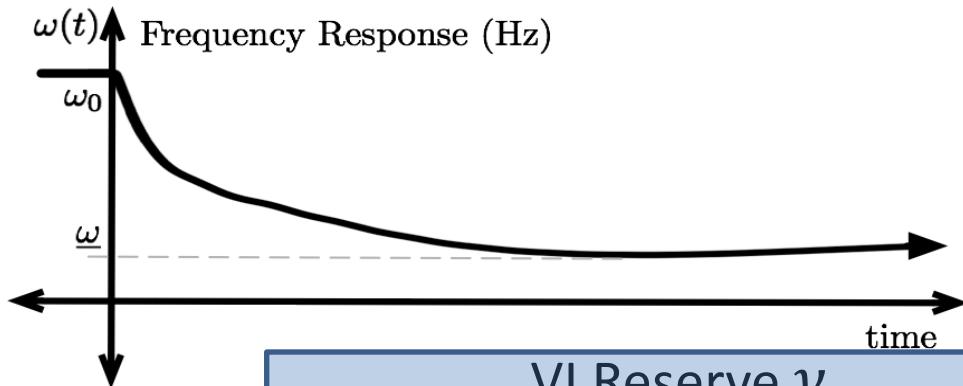
# Ancillary Services for Primary Frequency Control

## Inertia and the Swing Equation

Simple Swing Equation neglects damping.

System frequency is  $\omega(t)$ , nominal frequency is  $\omega_0$ , inertia from generator  $i$  is  $M_i$ , net-demand is  $e(t)$ .

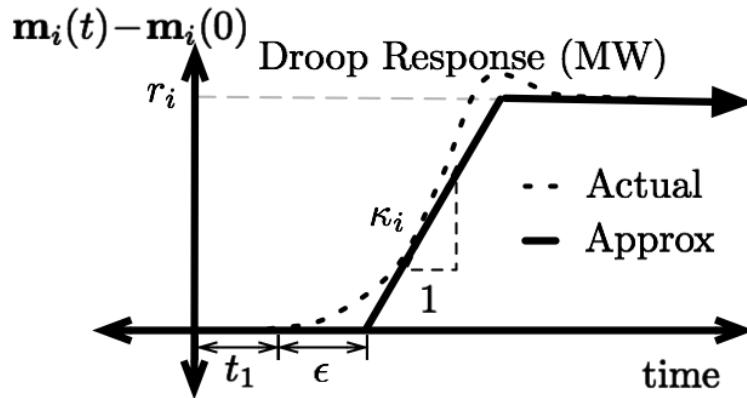
$$\frac{d\omega(t)}{dt} = \frac{\omega_0}{2(1^T M)} (1^T m(t) + 1^T p(t) + 1^T d(t) - e(t))$$



## PFR Reserve $b$

(Droop Control)

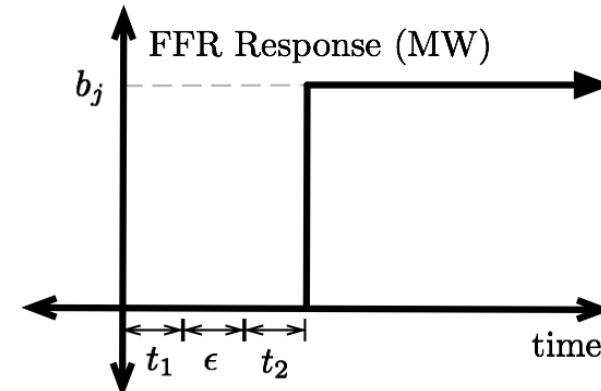
$m_i(t)$ : Ramp in mechanical power  
 $r_i$  : PFR reserve for generator  $i$



## FFR Reserve $b$

(Step Response)

$d_j(t)$ : Instantaneous jump in electric power  
 $b_j$ : FFR reserve for IBR  $j$



## VI Reserve $\nu$

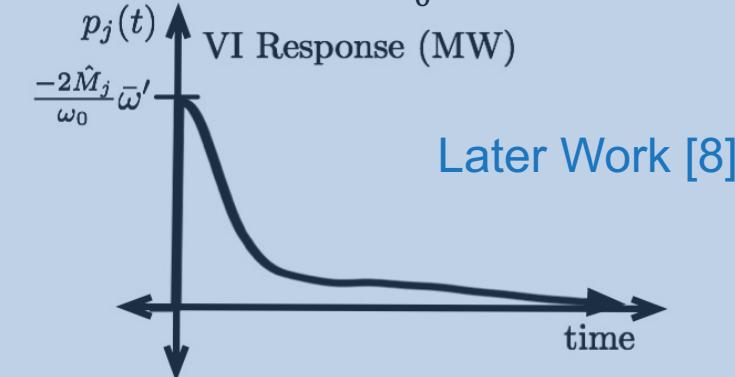
(Virtual Inertia)

$p_j(t)$ : Electric power proportional to  $\frac{d\omega(t)}{dt}$

$$\nu_j(t) = \frac{2 \hat{M}_j}{\omega_0} \bar{\omega}'$$

$\bar{\omega}'$ : VI reserve for IBR  $j$

$$p_j(t) = \frac{2 \hat{M}_j}{\omega_0} \frac{d\omega(t)}{dt}$$



Later Work [8]

# ERCOT's Equivalency Ratio Requirement

## Equivalency Ratio Requirement

Constraint from [9].

$$1^T R + \alpha(M) 1^T b \geq \nu(M)$$

## Summary

Determined through simulation.

Claims to ensure frequency remains above critical threshold.

## Intuition

Places lower bound  $\nu(M)$  on total freq. resp. reserve.

FFR reserve is more effective than PFR reserve by a factor of  $\alpha(M)$ .

*Table 2: Parameters appearing in the equivalency ratio reserve requirement from [9]. The equivalency ratio  $\alpha(M)$  and the frequency response reserve requirement  $\nu(M)$  are provided for different inertia levels.*

Inertia $M$ (GWs)	Equiv. Ratio $\alpha(M)$	Req. Amount $\nu(M)$ (MW)
120	2.2	5200
136	2.0	4700
152	1.5	3750
177	1.4	3370
202	1.3	3100
230	1.25	3040

Notation
• $R$ : Vector of nominal PFR reserve for generators
• $b$ : Vector of FFR reserve for resources
• $M$ : Total post-outage system inertia
• $\alpha(M)$ : Equivalency Ratio
• $\nu(M)$ : Requirement Quantity

## Important Observation

Often assigns more PFR reserve to generators than they can provide due to ramping limitations.

Makes up for this by over procuring total reserve.

Inertia $M$ (GWs)	Equiv. Ratio $\alpha(M)$	Req. Amount $\nu(M)$ (MW)
256	1.13	2640
278	1.08	2640
297	1	2240
316	1	2280
332	1	2140
350	1	2140

# Proposed Requirement Framework

## General Requirement

Sufficient reserve to cover an outage of arbitrary size  $L$ .  
Intuitive because the requirement quantity is the outage size considered.

$$L \leq 1^T r + 1^T b \quad (1)$$

Assuming all reserve can be delivered before  $\omega_{min}$  is reached, the frequency will be arrested before  $\omega_{min}$  is reached.

## Nominal PFR Reserve R

Head-room required to provide PFR.

$$G + R \leq \bar{G} \quad (2)$$

## PFR Reserve Limits

Not all nominal PFR reserve  $R$  may be available before  $\omega_{min}$  is reached.  
Limits on available PFR reserve  $r$  represent physical ramping limitations,

$$r_i \leq \ell_i(\cdot) \quad \text{for each generator } i \quad (4)$$

where  $\ell_i(\cdot)$  is a limit function that may depend on many system-wide values.

## Notation

- $r$ : Vector of available PFR reserve for generators
- $R$ : Vector of nominal PFR reserve for generators
- $b$ : Vector of FFR reserve for resources
- $M$ : Total post-outage system inertia
- $G$ : Vector of power output for generators
- $\bar{G}$ : Vector of generator capacities
- $\omega_{min}$ : Minimum frequency threshold

## Available PFR Reserve r

Available before  $\omega_{min}$  is reached.

$$r \leq R \quad (3)$$

# Proposed PFR Reserve Limits

## Empirically Derived PFR Reserve Limits

### Equivalency Ratio Requirements

Approximately the same as equivalency ratio requirement from [9]

$$r_i \leq \frac{1}{\alpha(M)} R_i \quad (5)$$

### Empirical PFR reserve limits

Similar method as used to determine equivalency ratios. (In progress)

$$r_i \leq \ell_i(M, 1^T b) \quad (6)$$

## Empirically Derived PFR Reserve Limits

### Rate-Based PFR Reserve Limits

Assumes fixed ramp rate  $\kappa_i$ .

Derives  $h(\cdot, \cdot)$  from first principles.

$$r_i \leq \kappa_i h(M, 1^T b) \quad (7)$$

### Proportional PFR Reserve Limits

Ramp rate  $\kappa_i$  is proportional to  $R_i$ .

Derives  $\alpha(M)$  from first principles.

$$r_i \leq \tau_i R_i h(M, 1^T b) \quad (8)$$

# Numerical Results: Texas 2000 Bus Test Case

## Texas 2000 Bus Test Case

- PFR generators: 50 largest natural gas
- FFR Reserve Capacity is  $\bar{b} = 600\text{MW}$ .

## Figure 2: Total PFR Reserve Allocation

- Rate-based PFR reserve limit assigns exactly enough PFR reserve to cover the contingency  $L-b=1900\text{ MW}$ .
- Equiv. ratio req. assigns more PFR reserve than necessary.
- Both requirements simultaneously allocates the same total PFR reserve as the equiv. ratio req.

## Figure 3: Largest PFR Reserve Allocation

- Equiv. Ratio Req. assigns too much nominal PFR reserve to a single generator.
  - Not all is available before frequency threshold is reached.
- Rate-based PFR reserve limit ensures all PFR reserve is available.
  - Limit increases with inertia
- Enforcing both req. allocates some extra headroom to generators.
  - Disperses PFR reserve among more generators.

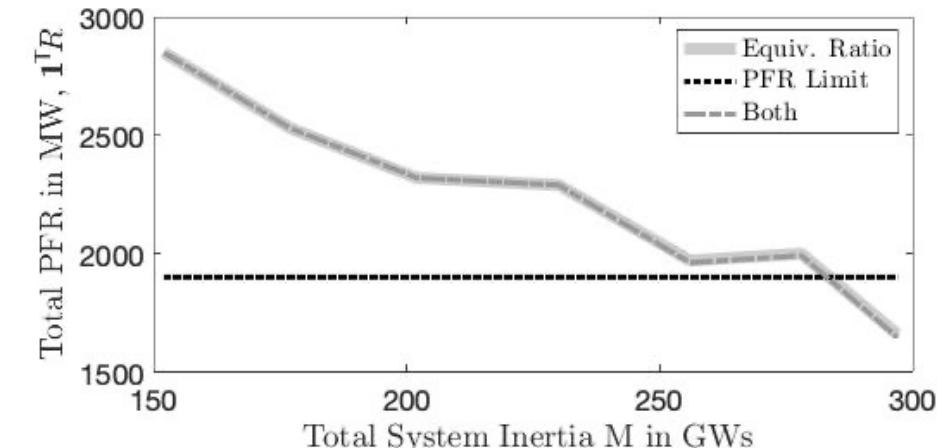


Figure 2: Total PFR reserve in the system as total system inertia varies. [3]

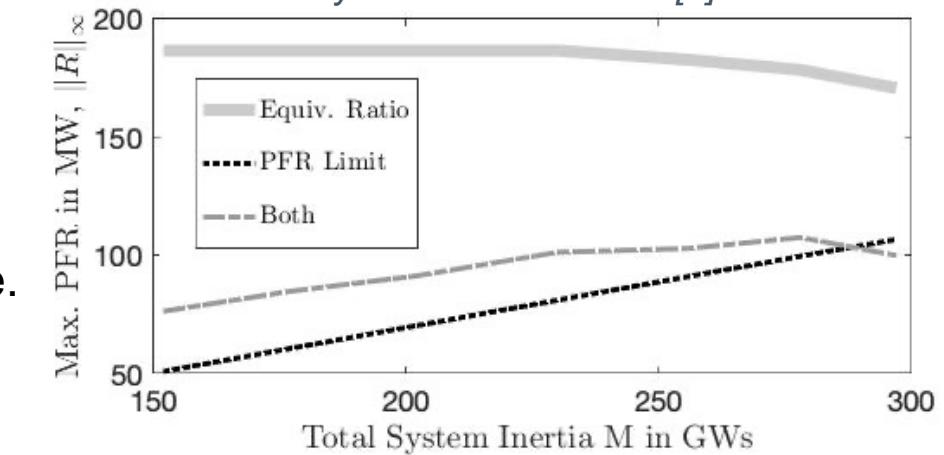


Figure 3: The infinity norm of the PFR reserve vector as total system inertia varies. [3]

# Conclusions/Recommendations

- Proposed introduction of new primary frequency response reserve products into wholesale electricity markets.
- Presented ERCOT's equivalency ratio requirement.
  - Derived equivalency ratios from first principles.
- Proposed more general reserve requirement framework in the form of *PFR reserve limits* to ensure sufficient frequency response.
  - Proposed four different PFR reserve limits.
  - Proposed one PFR Reserve limit that is approximately the same as the equivalency ratio requirement.
- Illustrated the differences between reserve requirements.
  - Rate-based PFR reserve limit spreads out PFR reserve allocation among more generators.
  - Equivalency ratio requirement allocates too much PFR reserve to a single generator and procures more total PFR reserve than is strictly necessary to cover the largest contingency.
  - Both limits can be enforced at the same time, making the requirement more conservative.

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