



# Molecular Dynamics of High Pressure Tin Phases I: Strength and deformation evaluations of empirical potentials

J Matthew D Lane<sup>1</sup>, Mary Alice Cusentino<sup>1</sup>, Ben Nebgen<sup>3</sup>,  
Kipton M Barros<sup>3</sup>, John D Shimanek<sup>2</sup>, Alice Allen<sup>3</sup>,  
Aidan P Thompson<sup>1</sup>, and Saryu J Fensin<sup>3</sup>

*Sandia National Labs, Albuquerque, NM  
Penn State University, University Park, PA  
Los Alamos National Lab, Los Alamos, NM*

July 14, 2022

Shock Compression of Condensed Matter Conference (SHOCK 2022)  
Anaheim, California



Sandia National Laboratories is a multimission laboratory managed and operated by National Technology & Engineering Solutions of Sandia, LLC, a wholly owned subsidiary of Honeywell International Inc., for the U.S.

Department of Energy's National Nuclear Security Administration under contract DE-NA0003525.

# Strength in materials, tri-lab effort



**Strength** is a measure of a material's ability to sustain an applied load without failure or irreversible deformation.

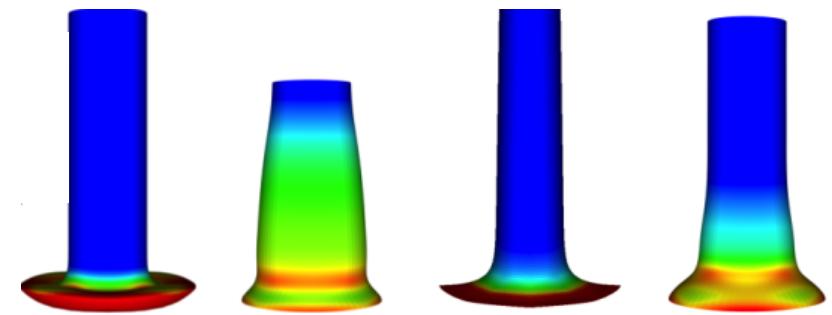
Strength response is "universal"  
but mechanisms are unique to each system.

In the hydro code world,  
EOS → controls volume compression  
strength → controls deformability

In the real world,  
Dislocation motion  
Dislocation generation  
Grain boundary motion  
Twinning and stacking faults  
Phase transition

**History and path dependence**  
**Microstructure**  
Grain size  
Grain orientation  
Grain boundary orientation

**Compressive plastic flow stress in textured polycrystalline metal (ignoring anisotropy)**



Why tantalum?

Tantalum, as a high-Z **body-center-cubic (bcc) metal** with **no experimentally observed high-pressure phase transitions** up to 350 GPa, has potential use as a standard for high-pressure studies. But, its properties depend on poorly understood elastic/plastic and dislocation dynamics. High melt temperature of 3290 K.

# Motivation: Multiphase multiplies the unknowns



Multi-phase problems have so many more unknowns, we'd like to have a tool to constrain some open questions related to microstructure and twin & dislocation behavior.

We want an atomistic scale perspective on aspects of strength.

DFT high accuracy, but expensive

**Classical MD allows scaling to address larger length and time scale behavior**

Continuum is broadly applicable to macroscopic experimental test scales

Some multi-scale questions accessible to atomistic study:

What lattice-specific behavior influences dislocation production/mobility and/or twinning?

Do the phase transformations wipe-out, modify or preserve grain size and orientation?

Does plastic strain reset at phase transition? If so under what conditions?

Tin is the material chosen for the effort

- Non-hazardous
- Multiple accessible solid phases at relatively low pressures

**J. McNaney**, J04.00001, "Overview and highlights of a tri-lab effort on multi-phase material strength," July 12<sup>th</sup>

**M. Prime**, L05.0001, "Multiphase Strength Coupled with Phase Change Kinetics in RMI Experiments on Tin Across the  $\beta$ - $\gamma$  Boundary," July 12<sup>th</sup>

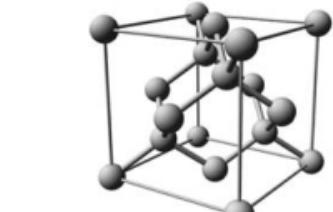
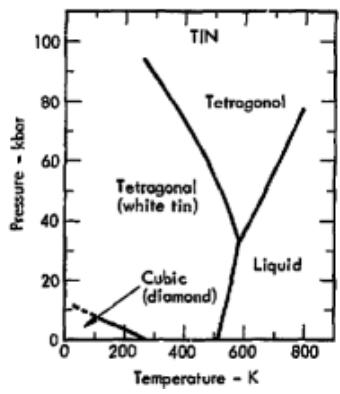
**W. Schill**, O03.0001, "Simultaneous Bayesian calibration of strength, kinetics, and phase boundaries," July 13<sup>th</sup>

**C. Battaile**, O05.0004, "Measuring the Strength of Metals by Extending the Richtmyer-Meshkov Instability to Shockless Loading," July 13<sup>th</sup>

# Tin phase diagrams from experiments and dft

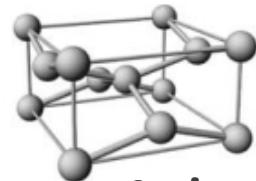


Young, LLNL (1975)



**$\alpha$ -tin**  
Diamond  
Below 300 K  
Non-conducting

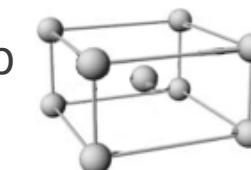
Diffusion-less



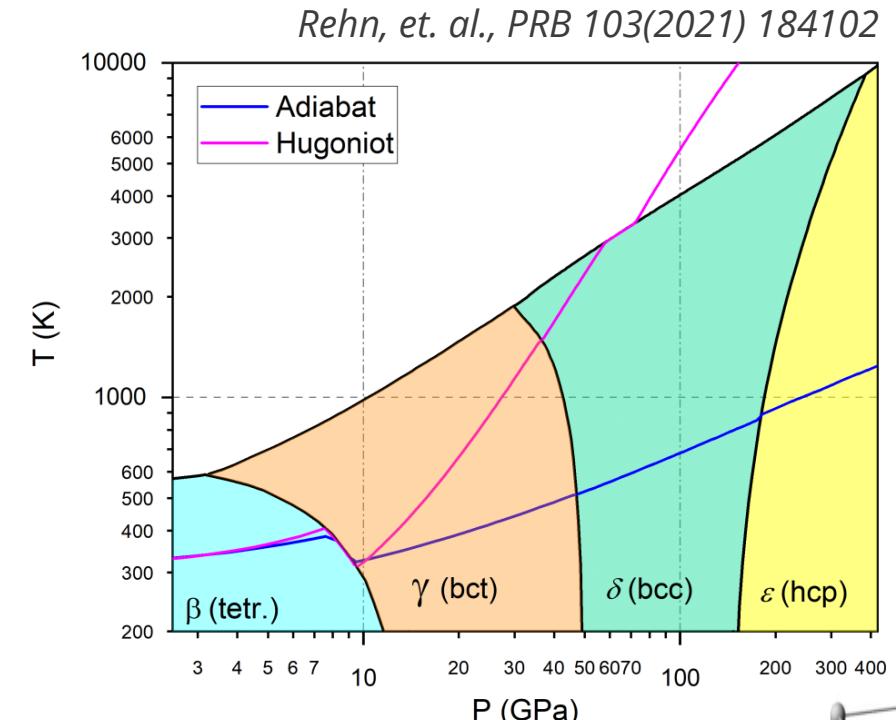
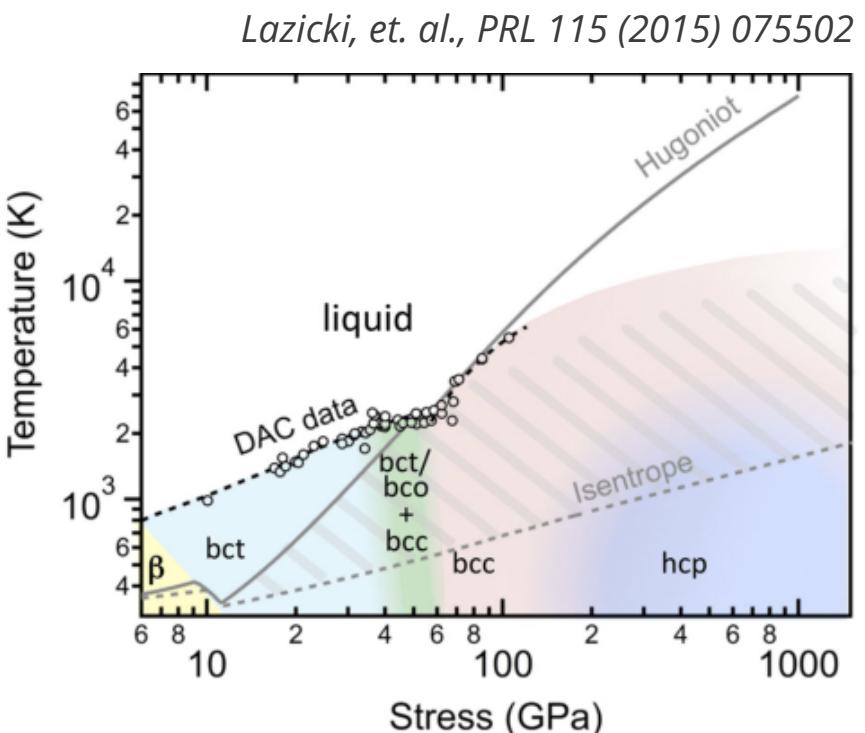
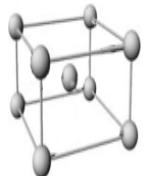
**$\beta$ -tin**  
Tetragonal  
0 to ~8 GPa  
Non-conducting  
27% volume change

Diffusion driven

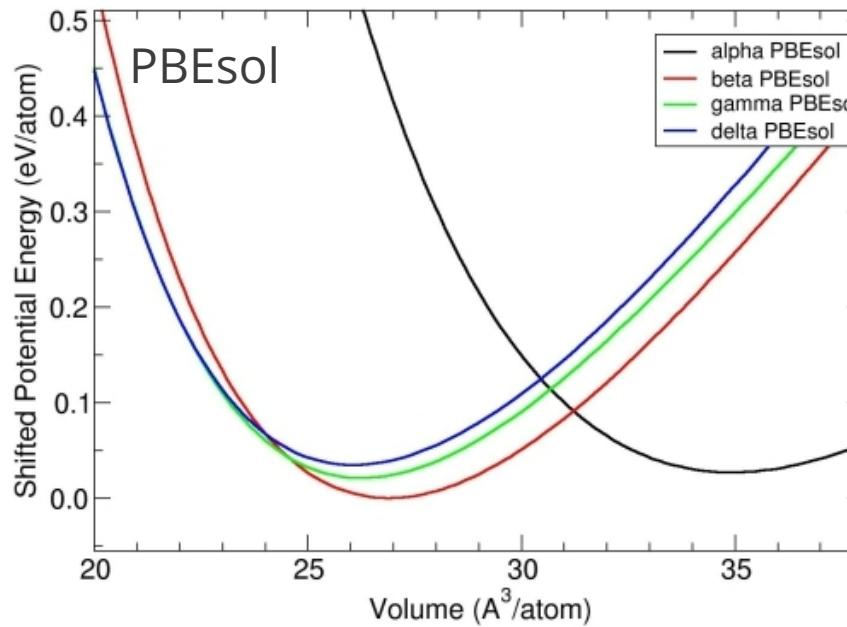
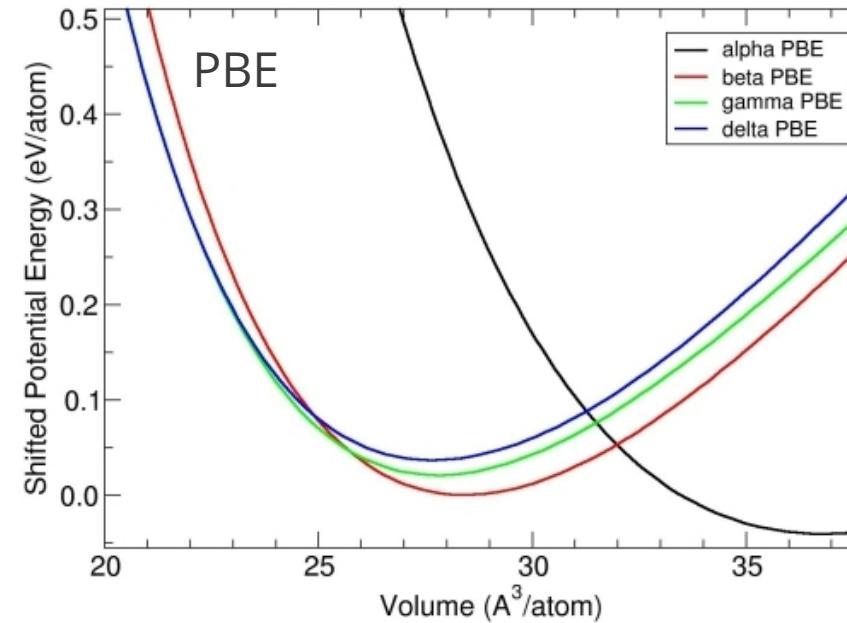
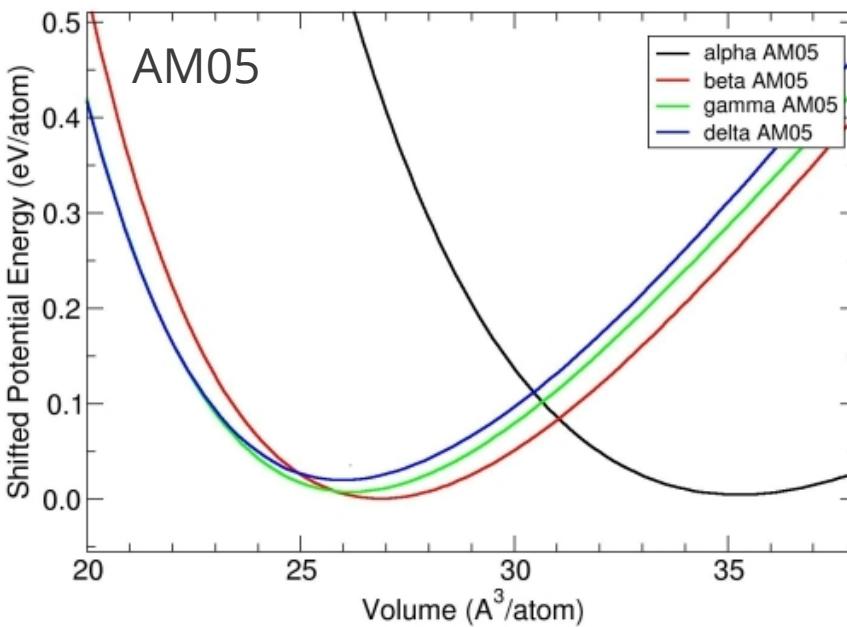
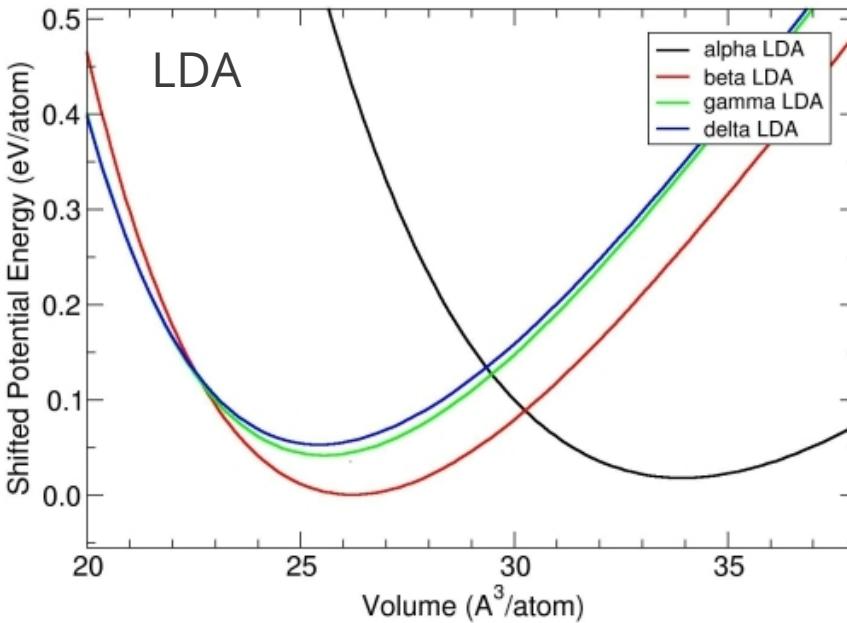
**$\gamma$ -tin**  
bct  
~8 to ~40 GPa  
Non-conducting  
3-5% volume drop



**$\delta$ -tin**  
bcc  
~40 to 150+ GPa  
Non-conducting  
No volume drop

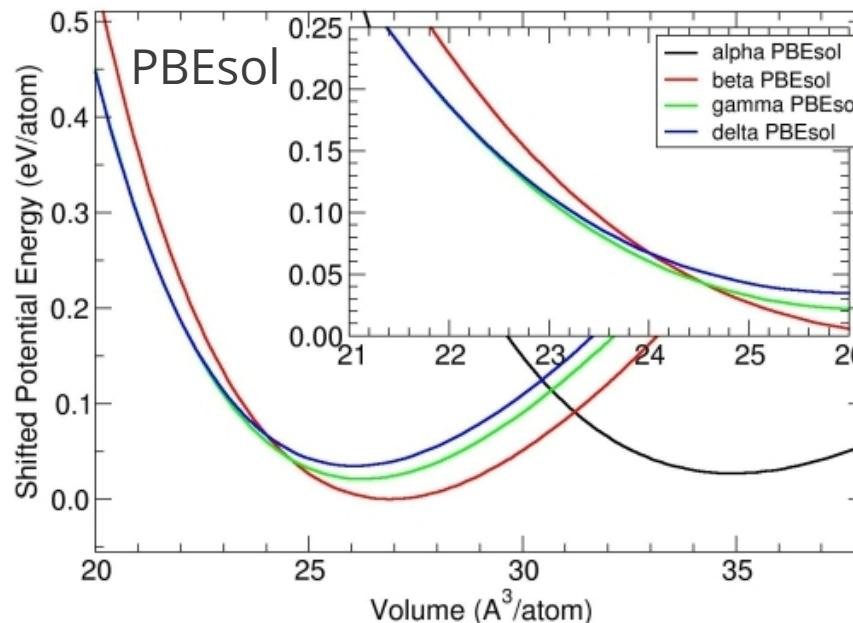
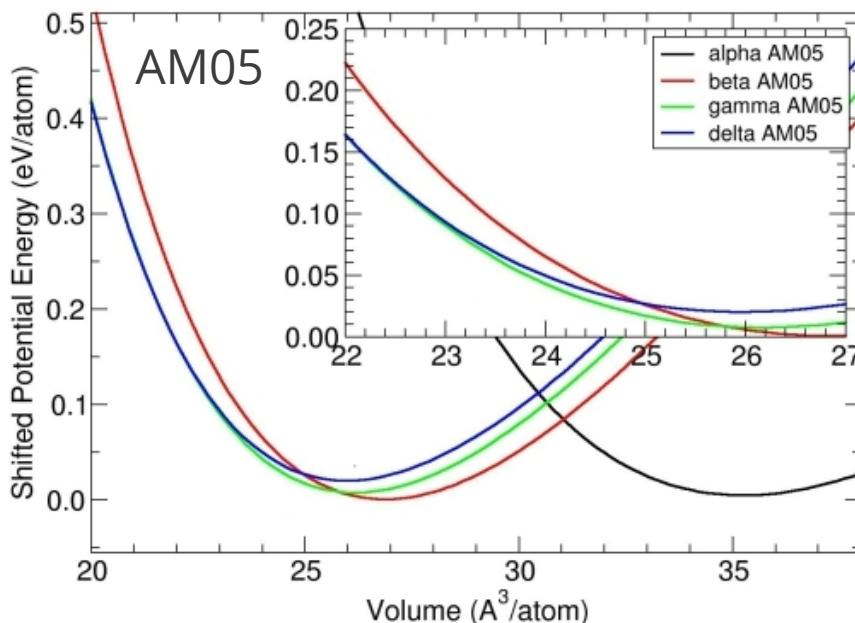
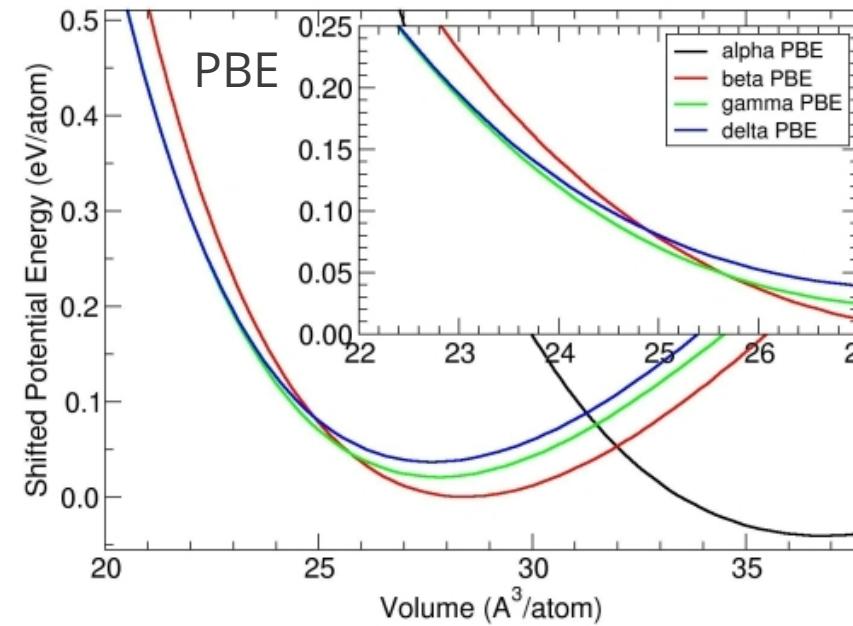
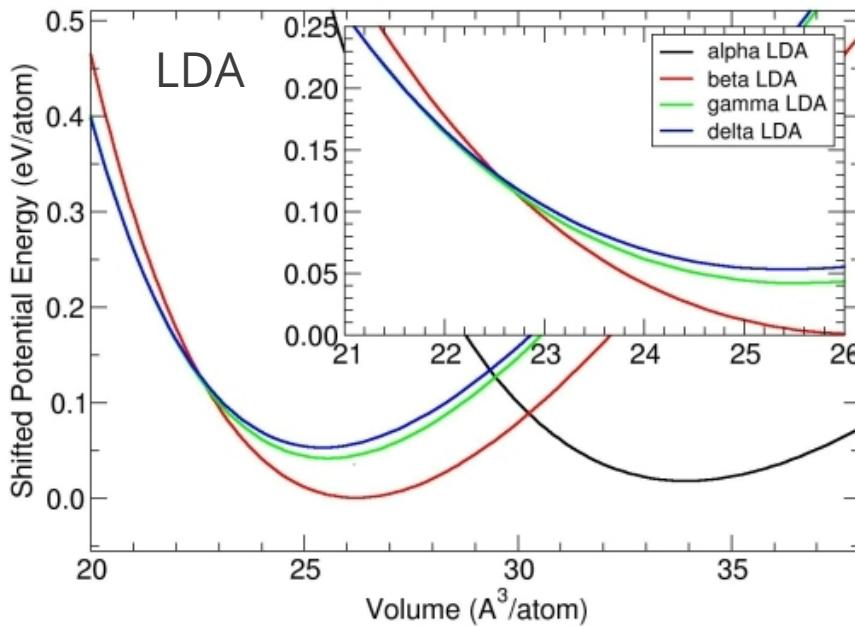


# DFT cold curves and uncertainty between functionals



- Energy-volume curves are highly dependent on exchange-correlation functional used
- Only PBE predicts the alpha phase to be lowest in energy at 0 K
- Beta, gamma, and delta curves are also very similar to each other

# DFT cold curves and uncertainty between functionals



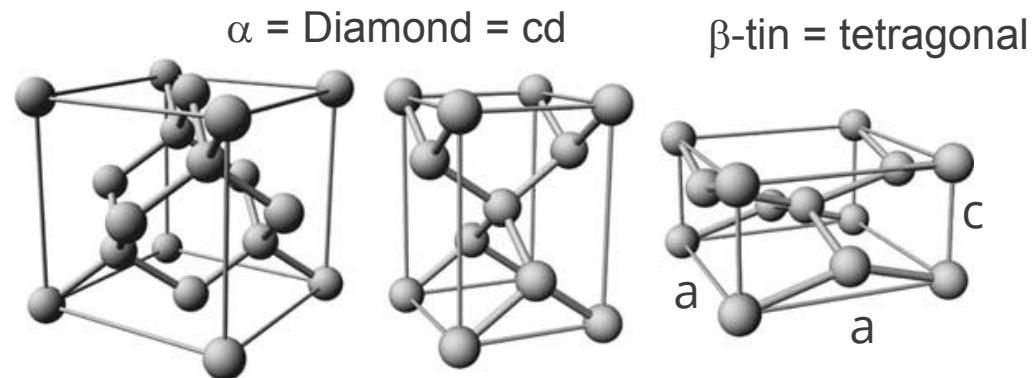
Transition order depends on subtle energy differences

P (GPa)	AM05	LDA	PBE	PBE sol	Expt.
$\alpha > \beta$	1.5	-5.4	-2.9	-2.5	1
$\beta > \gamma$	-2.1	-3.6	-0.5	-0.3	14
$\gamma > \delta$	36.7	4.8	12.3	36.7	50

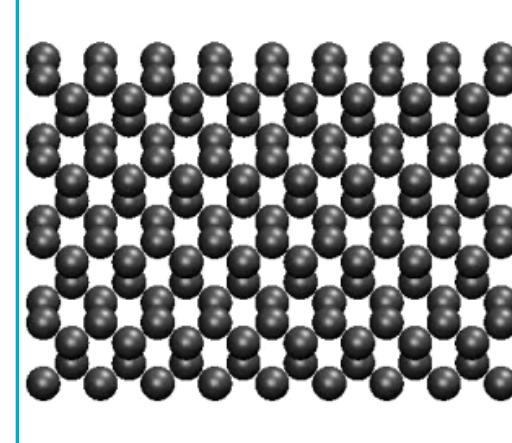
The issue is resolved with energy shifts in EOS models, but that's not an option here.

None of the functionals predict the experimental transition pressures

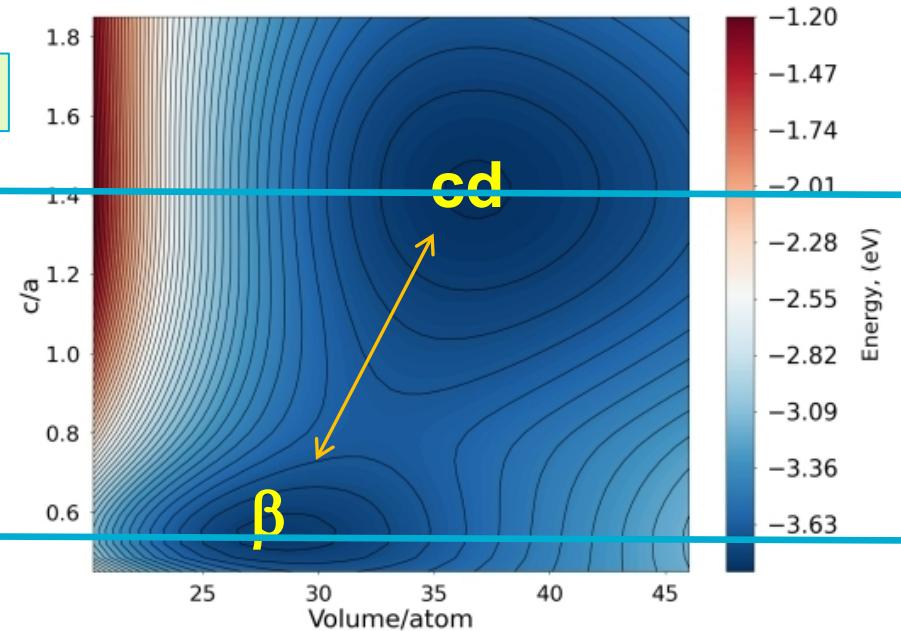
# Low Pressure phases of tin



Diffusion-less phase transition



DFT PBE



$\alpha$  - diam

$\beta$  - tetragonal

Tin is a ductile metal with signatures of ionic and covalently-bonded materials

MEAM, Tersoff, 3-body potentials

Low pressure states are open structures

# Empirical potentials

EAM and MEAM potentials have been successful

1998 Ravelo/Baskes MEAM

alpha, beta and liquid

2017 Vella & Chen MEAM

liquid

2018 Etesami MEAM

alpha, beta, liquid

2018 Ko 2NN MEAM

alpha, beta

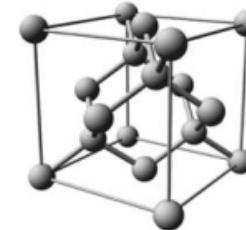
2006 Foiles EAM with Tersoff

liquid and gamma

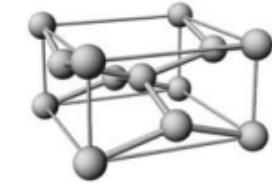
2014 Sapzhnikov EAM

gamma, delta and liquid

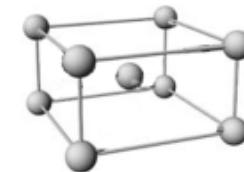
Alpha



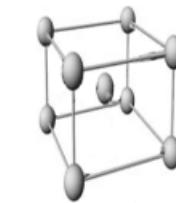
Beta



Gamma



Delta



Tin is a challenge because it exhibits open structures and close-packed structures.

As recently as 2020 and 2021, Ravelo MEAM potential has been the basis of numerous shock studies, which emphasize coarse Hugoniot response rather than structure details.

SNAP and ANI potentials could be quickly trained from DFT (See Talk II)

- Different DFT functionals give wide variety of transition pressures and even transition ordering
- The approach and any issues with fitting a multi-phase material like tin would generalize to other materials

# LAVA tool to evaluate behaviors in LAMMPS & VASP



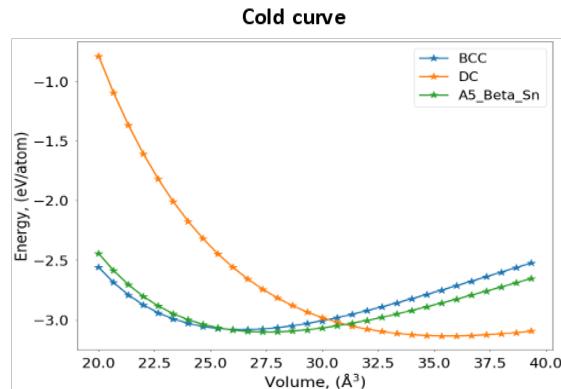
<https://github.com/lanl/LAVA>

The Lava Wrapper is a general-purpose calculator from LANL that provides a python interface to enable one-click calculation of the many common properties with lammps and vasp.

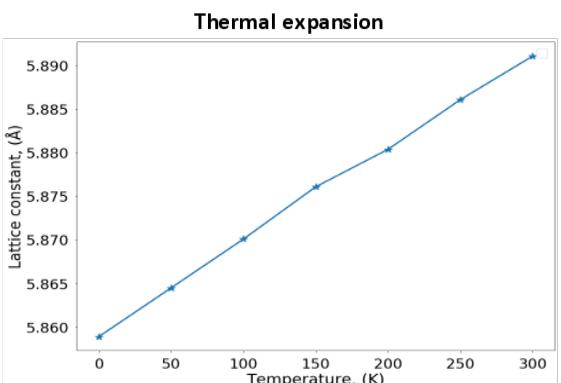
It provides a set of classes and functions to generate configs, run lammps/vasp calculation, retrieve the output, postprocess and plot the results.

## beta-Sn

<b>a (Å)</b>	<b>5.8589</b>
<b>c/a</b>	<b>0.5472</b>
<b>Ecoh (eV/atom)</b>	<b>-3.1019</b>
<b>C11 (GPa)</b>	<b>119.795</b>
<b>C12 (GPa)</b>	<b>16.611</b>
<b>C13 (GPa)</b>	<b>36.911</b>
<b>C33 (GPa)</b>	<b>93.694</b>
<b>C44 (GPa)</b>	<b>9.485</b>
<b>B (GPa)</b>	<b>51.006</b>
<b>Esuf_100 (mJ/m<sup>2</sup>)</b>	<b>345.025</b>
<b>Esuf_101 (mJ/m<sup>2</sup>)</b>	<b>366.551</b>



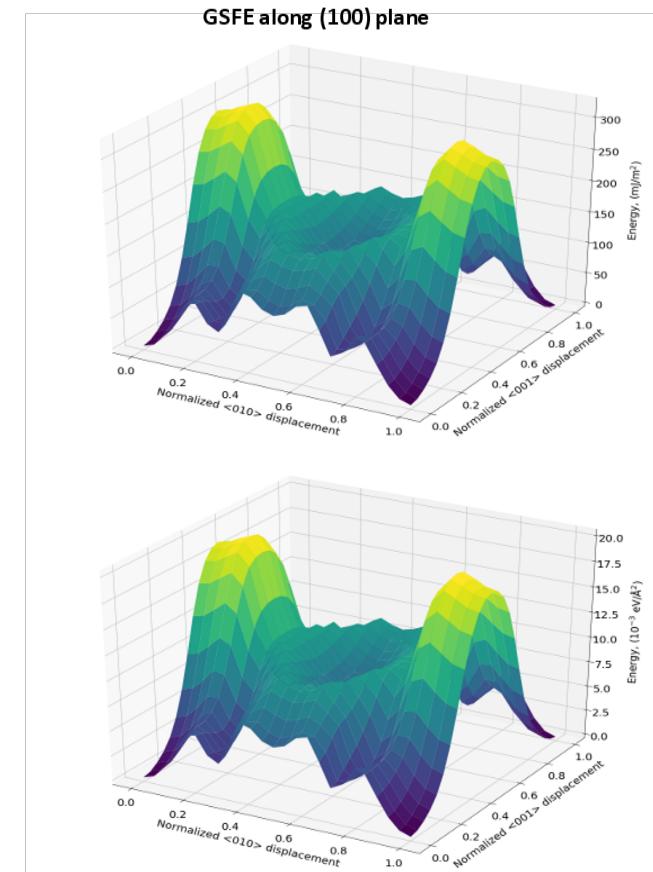
<b>Evac (eV)</b>	<b>0.855</b>
<b>Eint (eV)</b>	<b>1.715</b>



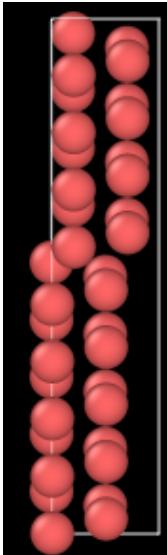
#Temp	average_lat		d_lat(%)
	0	5.8589	0.0006
50		5.8645	0.0964
100		5.8701	0.1918
150		5.8761	0.2934
200		5.8804	0.3667
250		5.8861	0.4637
300		5.8911	0.55

## Automatic Property Calculations:

- Minimum energy for lattice parameters a and c/a
- Cold curves (energy vs volume)
- Thermal expansion
- Elastic constants



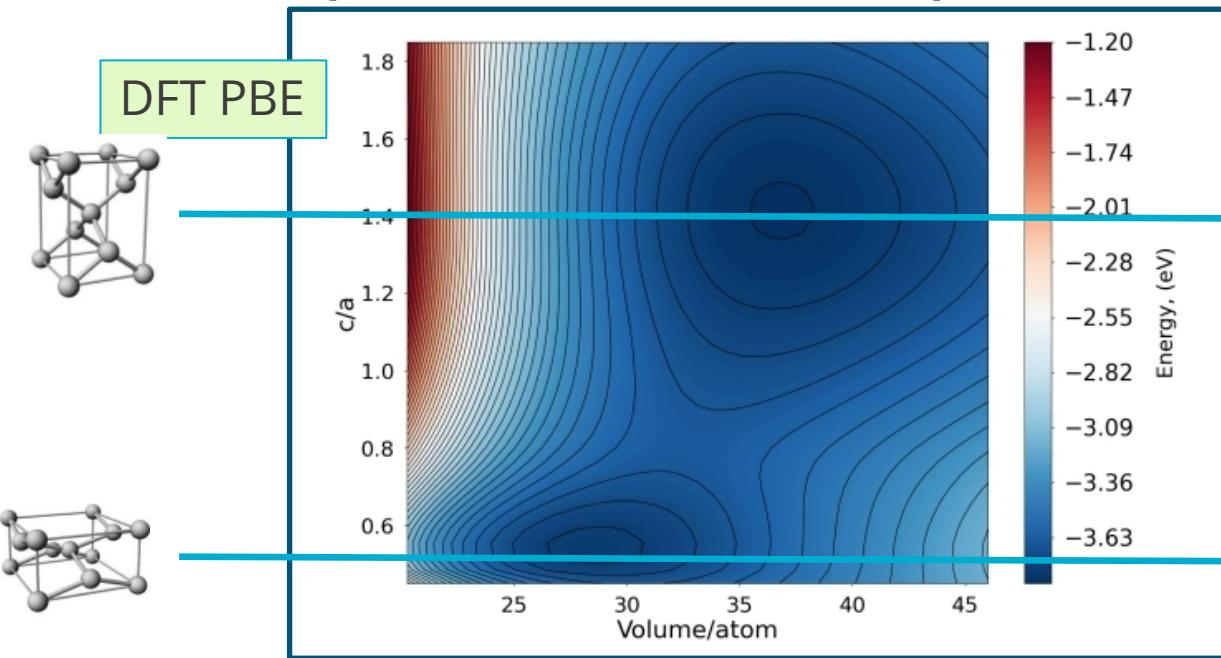
Example GSFE structure



- Cohesive energies
- Melt temperature
- Generalized stacking fault energies
- 2D Bain and Trigonal Paths

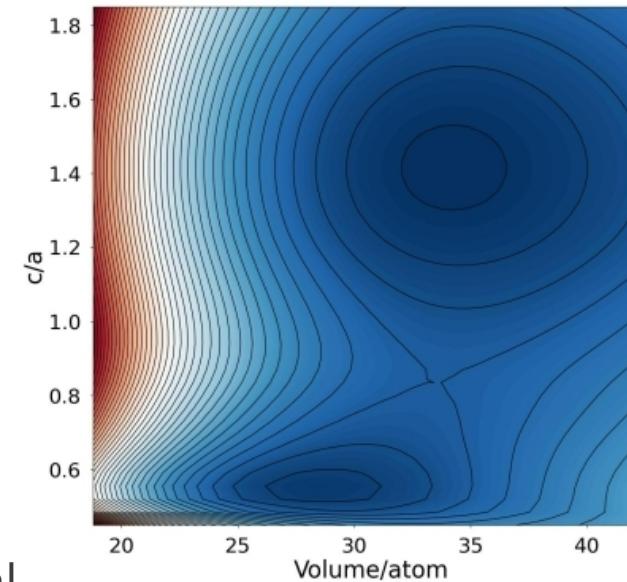
>> Dislocation core energies and slip systems

# MEAM potentials at low pressures: 2D Bain Paths

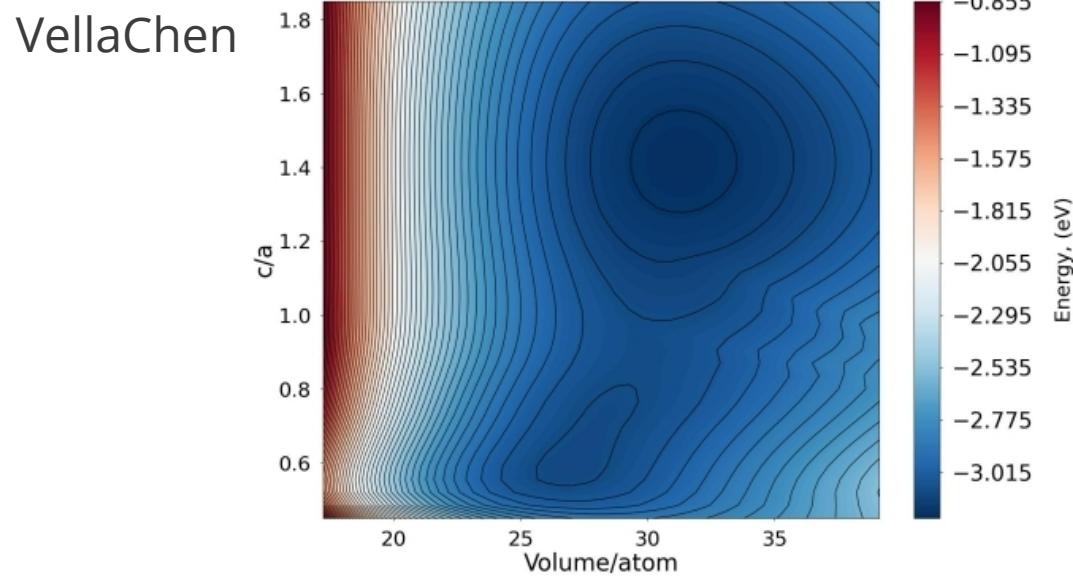


Ravelo

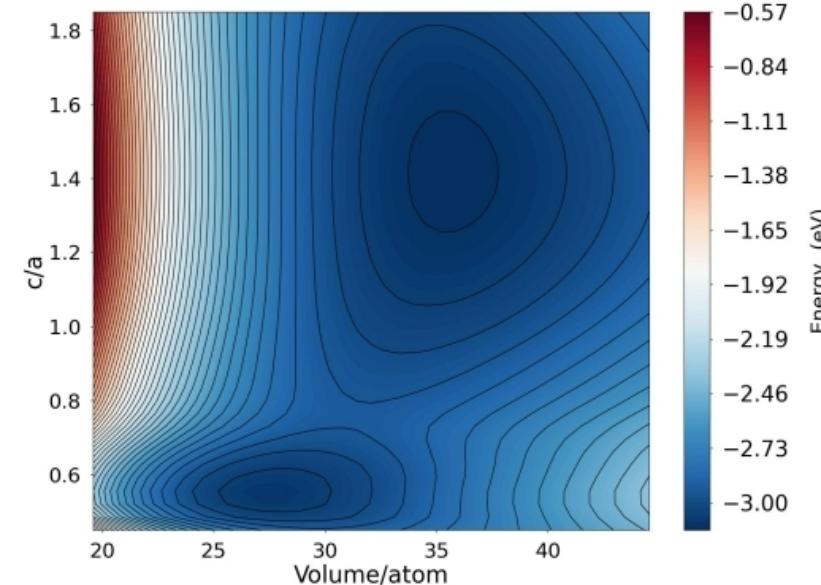
diam



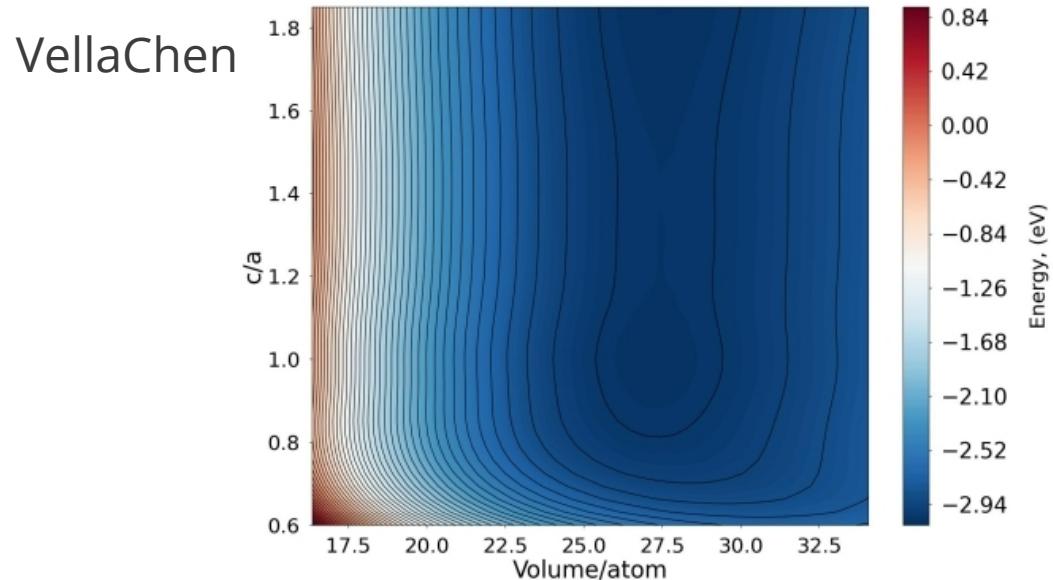
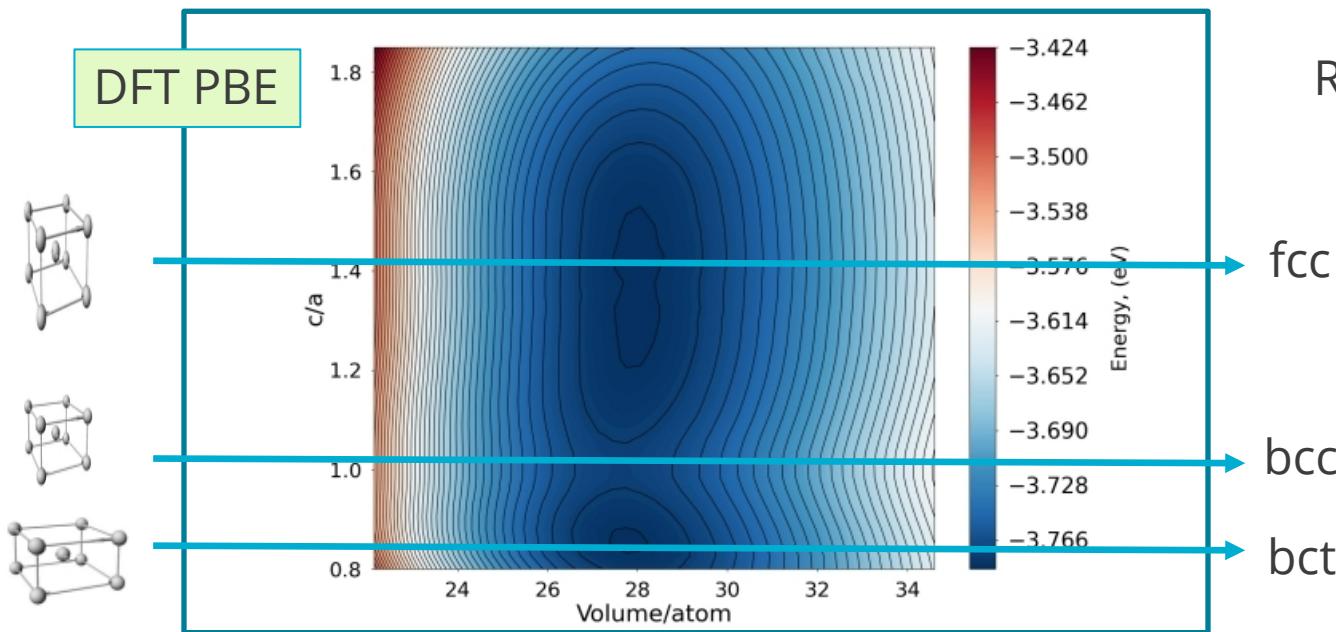
$\beta$ -tin  
tetragonal



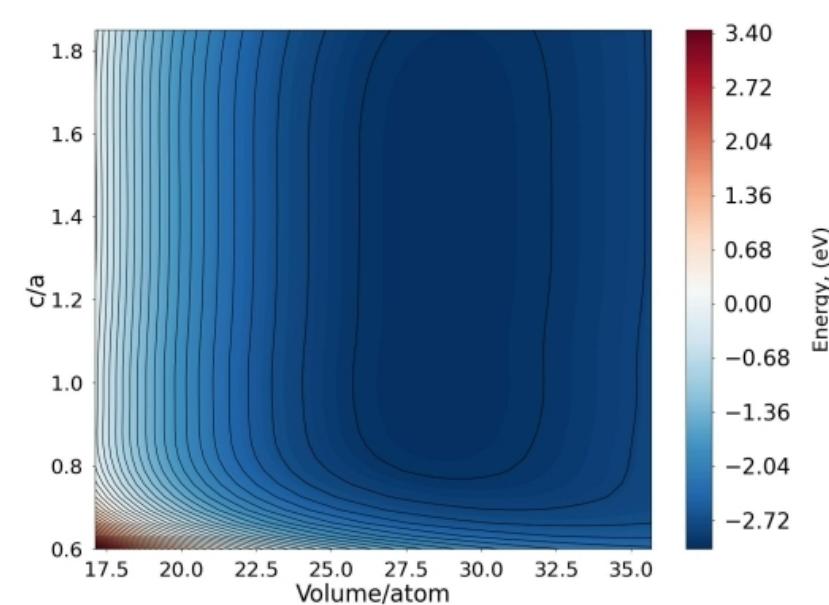
Ko



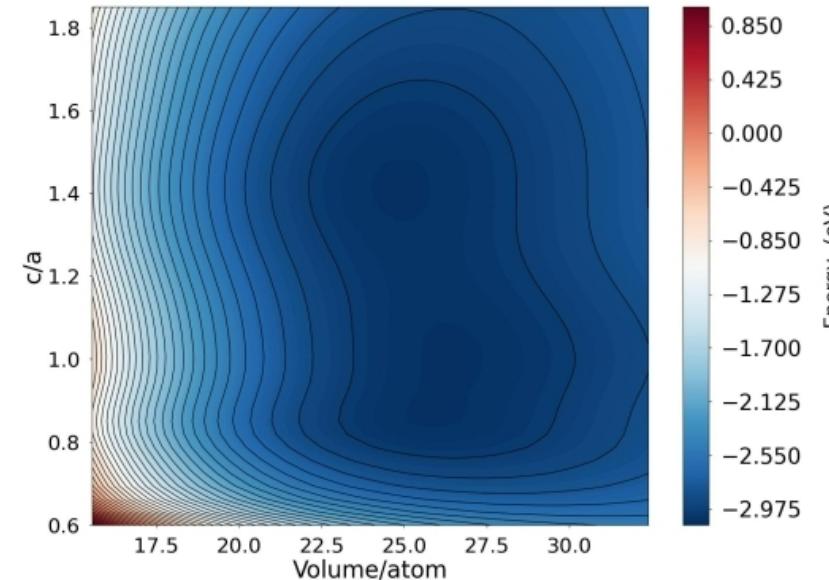
# MEAM potentials at high pressures : 2D Bain Paths



Ravelo



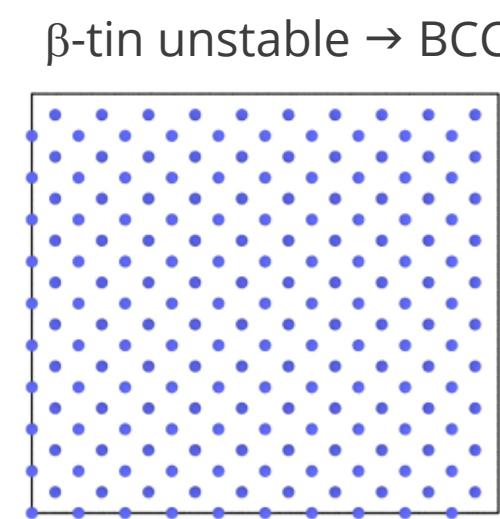
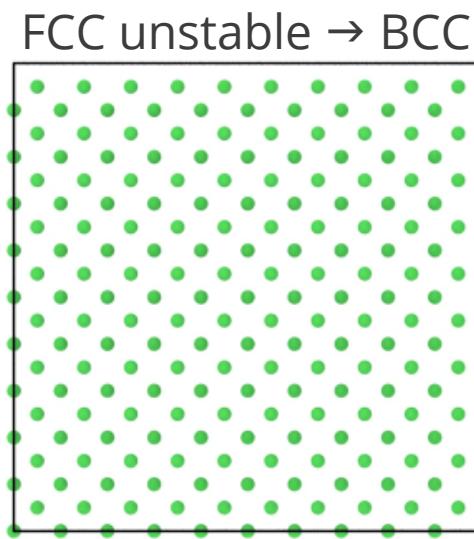
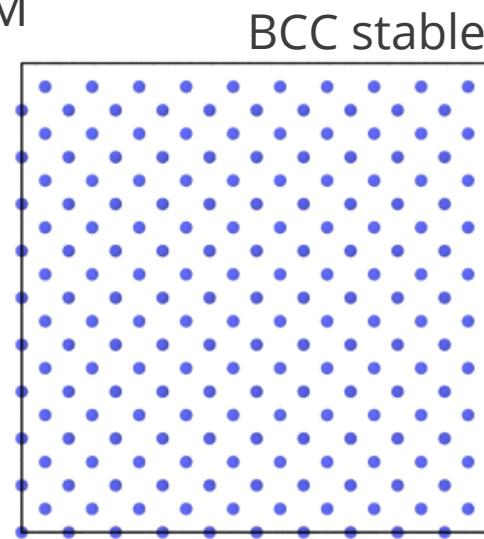
Ko



# Finite temperature results promising but ultimately fail



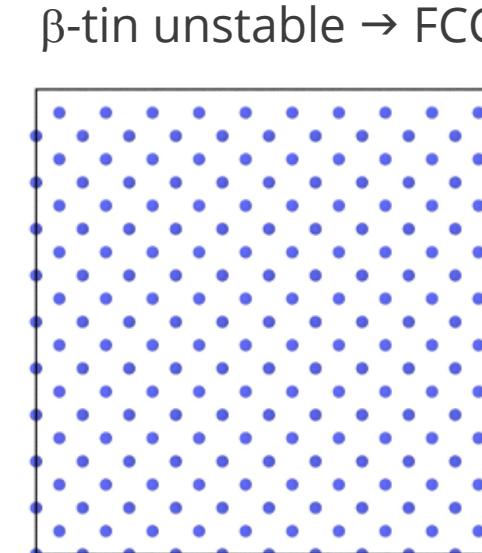
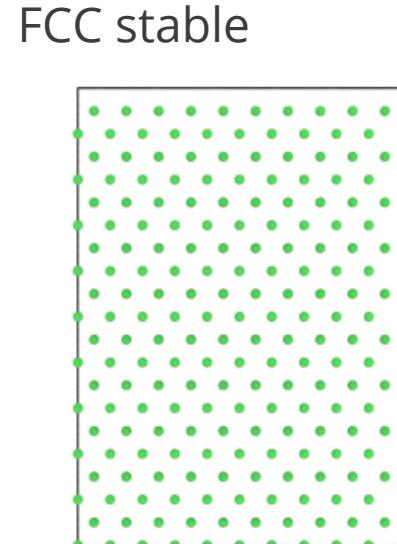
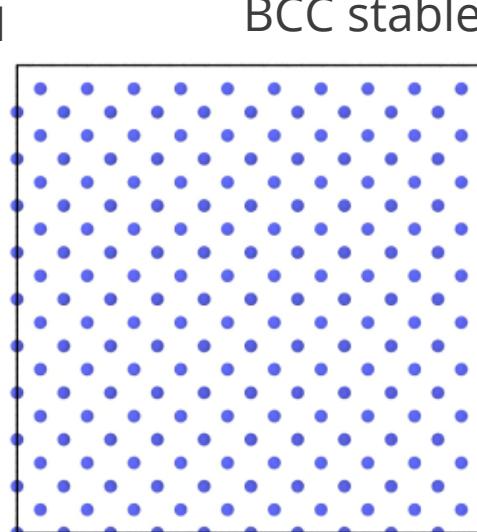
Ravelo MEAM



10 GPa  
300 K  
 $\beta$ -tin state

- BCC / BCT
- HCP
- FCC

Ko MEAM



# Conclusions: The good, the bad and the ugly



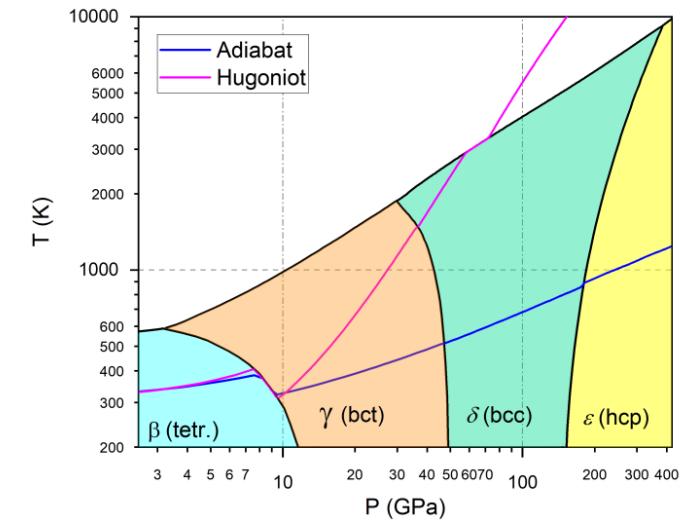
- The MEAM based Ravelo and the newer 2NN Ko interatomic potentials are very good for the covalent (open) structures of the alpha, beta phases and liquid.
  - Zero temperature calculations imply they may be capable of stabilizing the gamma and delta phases as well. They also do reasonably well with density pressure Hugoniot response
  - Unfortunately, they do not do well with predicted high pressure structure stability.
    - Ravelo offers a qualitative phenomenological tool for study of ramp into the delta (bcc) phase, only.
    - Ko predicts unphysical stability for the fcc phase

# Challenges for empirical models, ML potential



Two paths forward for atomistic modeling of high pressure tin:

- There may be hope for a potential which focuses exclusively on melt and the higher pressure phases. This approach has been attempted at Sandia by Steven Foiles and Jean-Paul Davis c. 2006.
- Clearly a machine learning based potential will be much less constrained by functional forms which limit the classical empirical potentials like EAM, MEAM and Tersoff.



Mary Alice Cusentino will explore this second approach next.