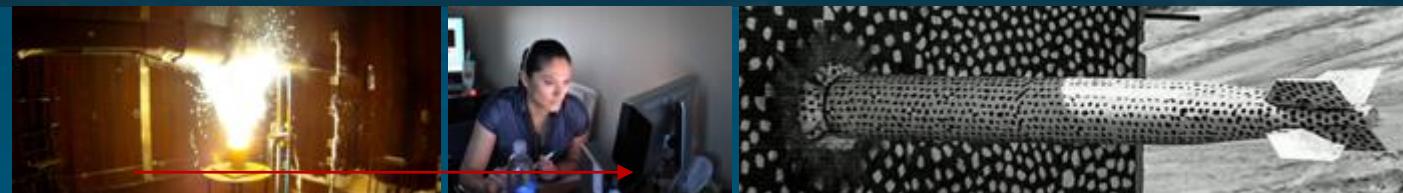




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# Peridynamic modeling of the dynamic failure of additively manufactured steel



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# Outline



- Spall phenomenology and testing.
- Peridynamics background.
- Crystal plasticity model.
- Spall kinetics model.
- Impact simulations and comparison with test data.

## Motivation

Can additively manufactured metals be substituted for conventional in applications involving shock waves?

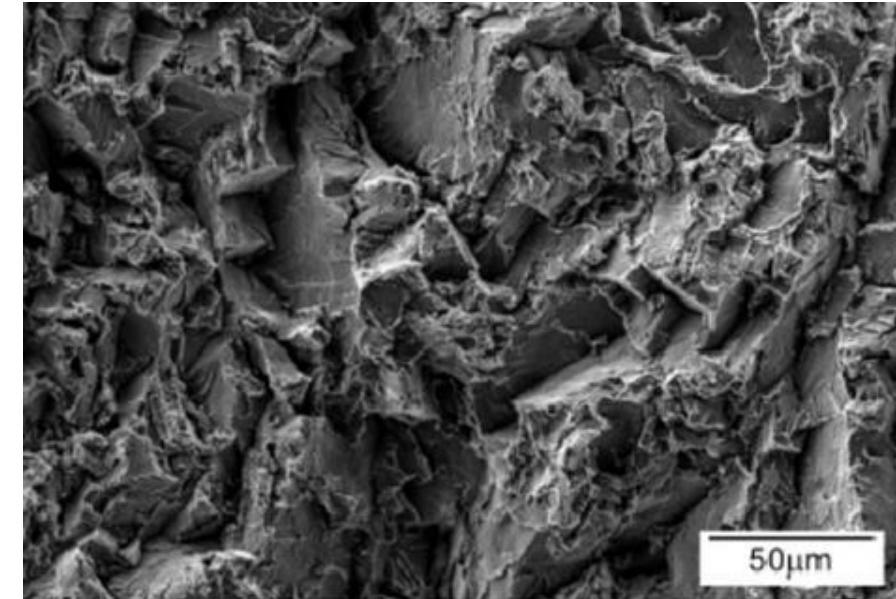
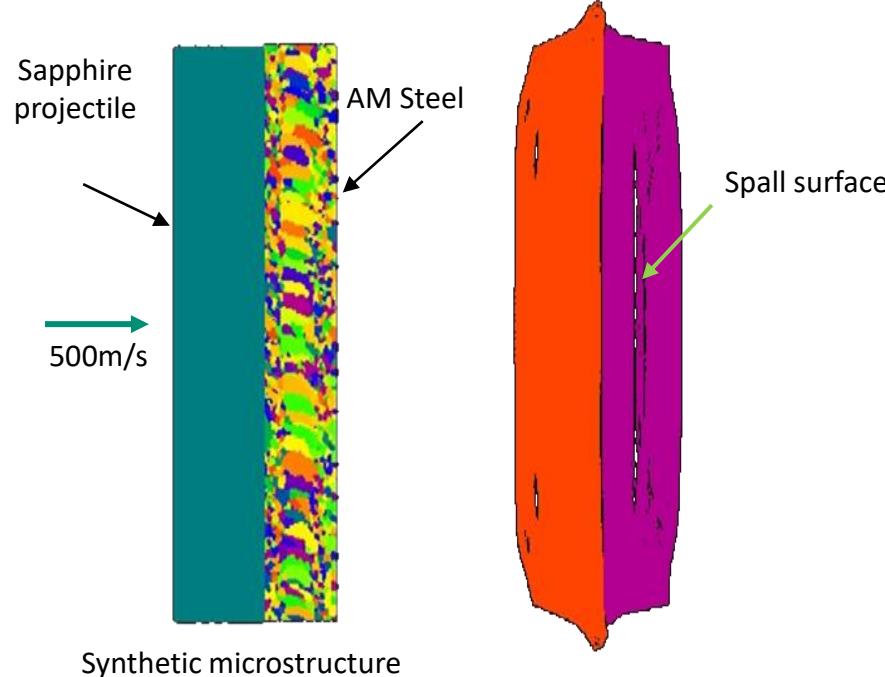
## Acknowledgments

Justin Brown, Nathan Brown, John Mitchell, Tim Ruggles, Paul Specht

# Failure of metals under impact loading

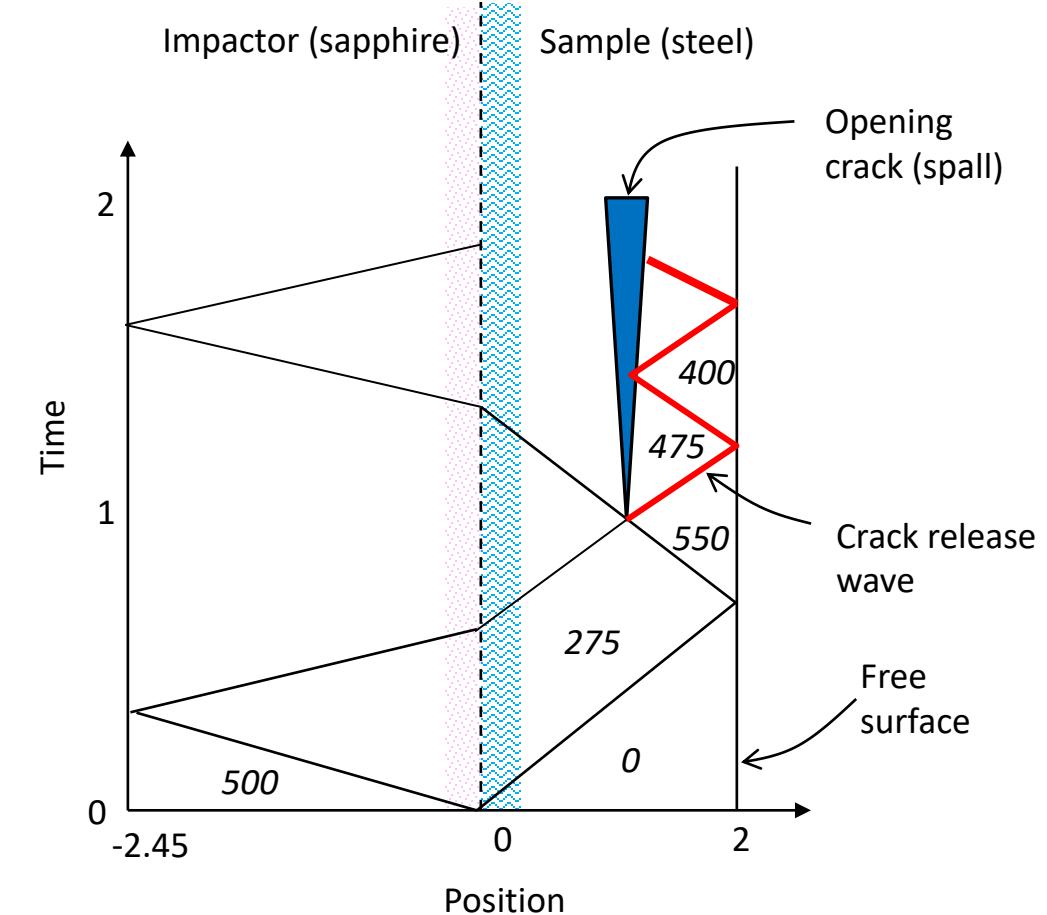
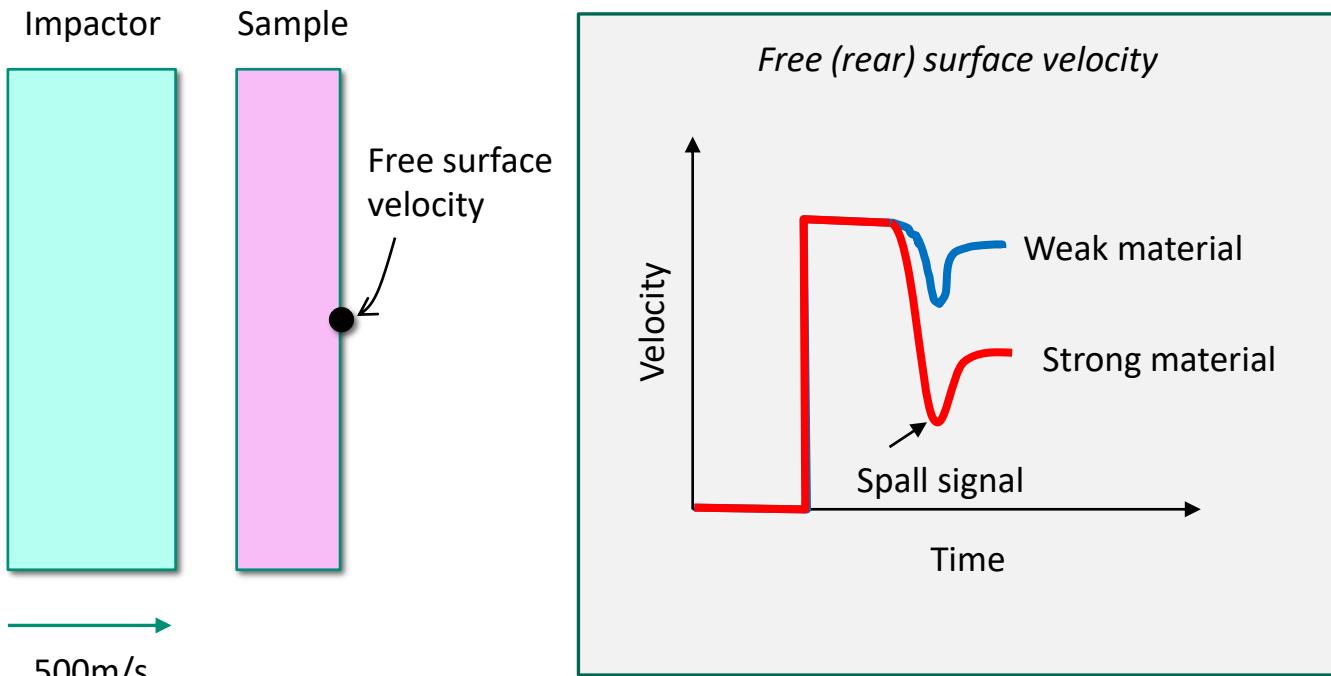


- Plate impact experiments are used in various configurations to measure dynamic material properties.
  - Equation of state data (Hugoniot and release).
  - Dynamic strength under high-rate tensile loading ( $\sim 10^5$  1/s)
  - Spall stress  $\gg$  quasi-static tensile strength (typically  $> 3$  GPa for steel).
- Basic test data is the free surface velocity.



Spall surfaces can be irregular\*

# Wave reflections lead to strong tension



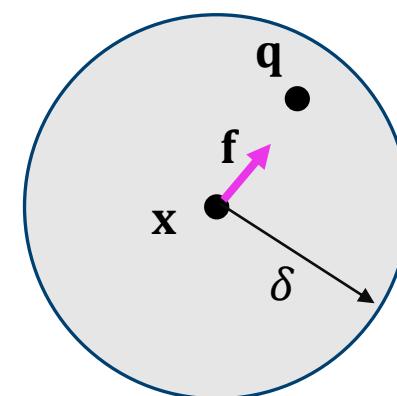
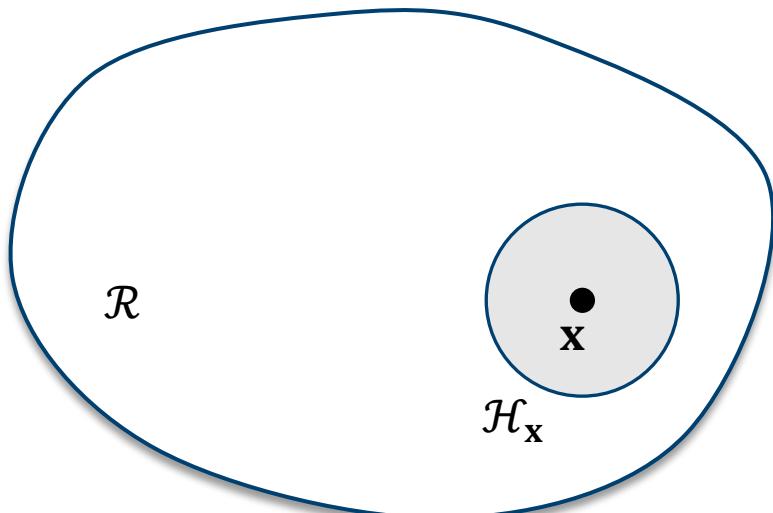
# Peridynamics background



- Peridynamic momentum balance in 3D:

$$\rho(\mathbf{x})\ddot{\mathbf{u}}(\mathbf{x}, t) = \int_{\mathcal{H}_x} \mathbf{f}(\mathbf{q}, \mathbf{x}, t) d\mathbf{q} + \mathbf{b}(\mathbf{x}, t) \quad \forall \mathbf{x} \in \mathcal{R}, t \geq 0.$$

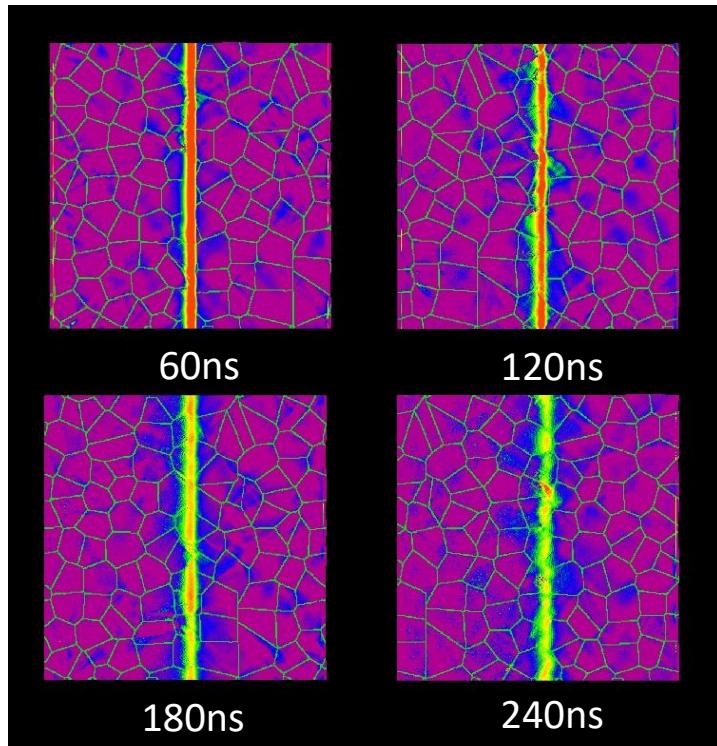
- $\mathbf{f}$  is the *pairwise bond force density* of the *bond* from  $\mathbf{q}$  to  $\mathbf{x}$ .
- $\mathcal{H}_x$  is the *family* of  $\mathbf{x}$ , which is a ball centered at  $\mathbf{x}$  with radius  $\delta$  (the *horizon*).



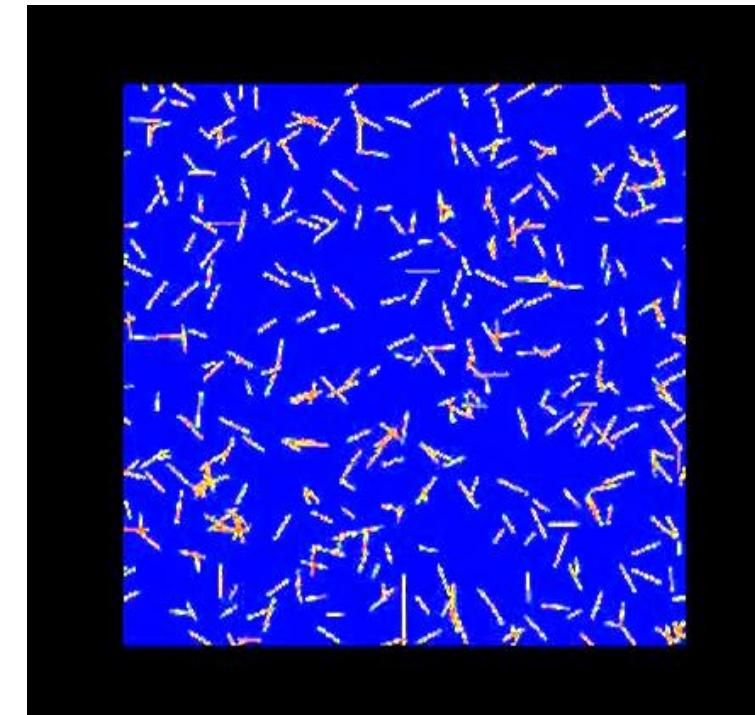
# Peridynamics allows fractures to appear spontaneously

- Integral equations: no need to try to differentiate on a singularity.
- Meshless discretization allows grains to be defined in any shape without a FE mesh.
- Bonds fail according to a damage criterion..
  - which in this case is supplied by the Spall Kinetics Model (more later).

Example of shock wave propagation  
Colors show strain rate

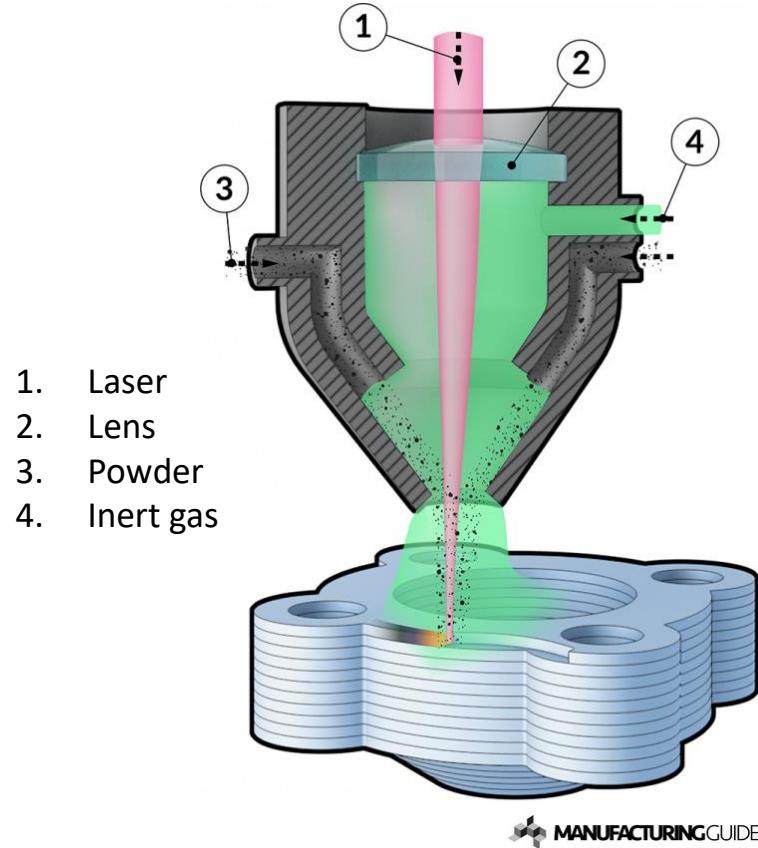


Example of macroscopic failure in a sample with defects  
[VIDEO](#)



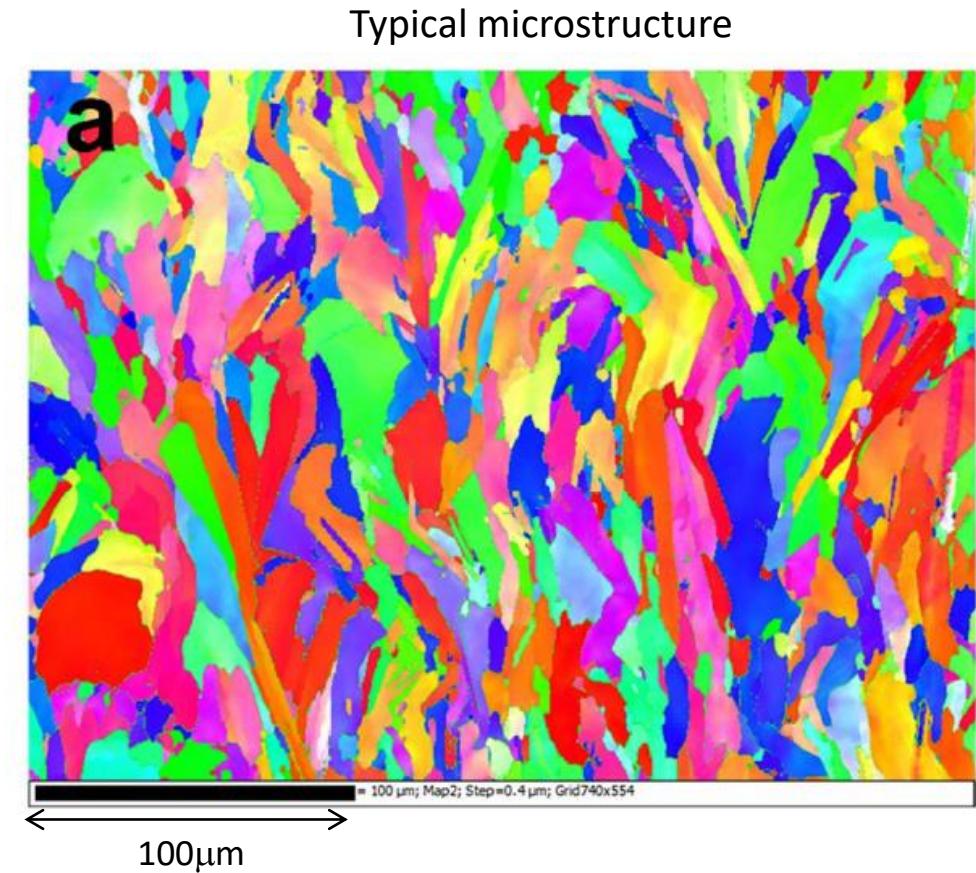
# LENS process

- Large, elongated grains are typically formed
- Nonuniform thermal history



Images:

- <https://www.manufacturingguide.com/en/laser-engineered-net-shaping-lens-0>
- S. Gorsse et al, *Science and Technology of Advanced Materials* (2017)



# Crystal plasticity model\*

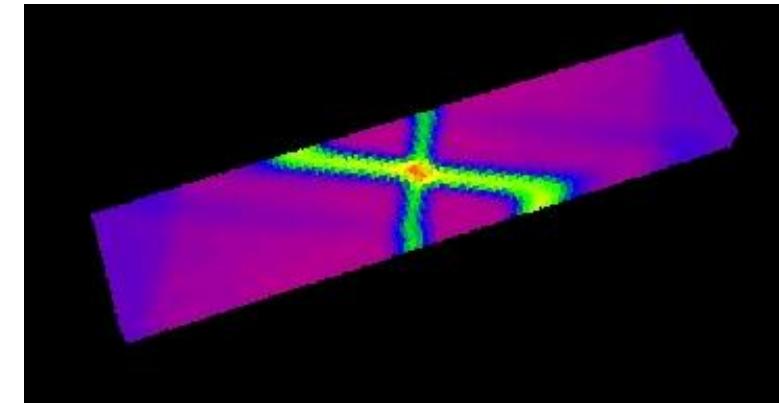
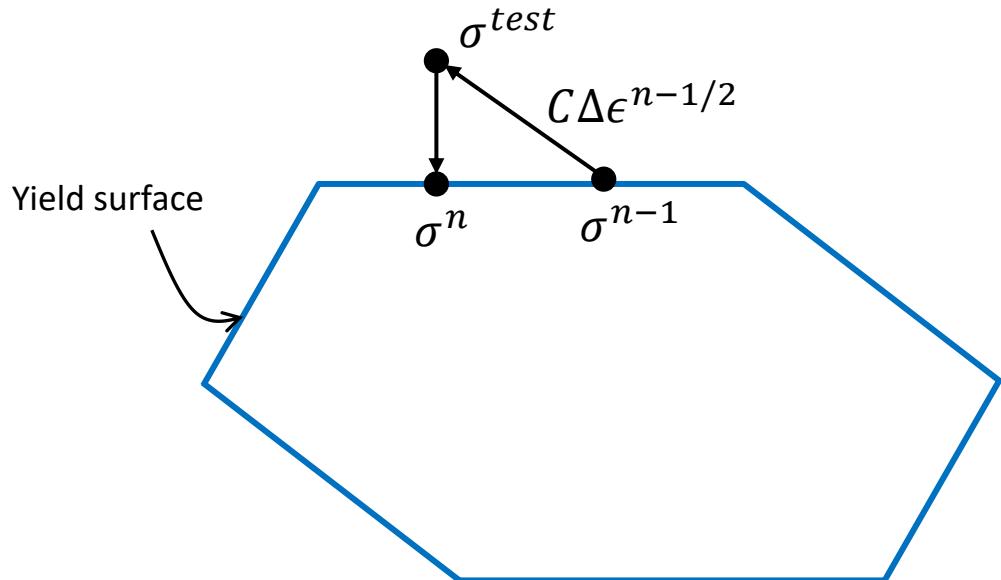


- Analogous to the radial return method
- The slip systems limit the deviatoric stress to a polyhedron in the space of deviatoric tensors.
- A test stress is found from the previous cycle stress and the current stress increment.

$$\sigma^{test} = \sigma^{n-1} + C\Delta\epsilon^{n-1/2}$$

where  $C$  is the anisotropic 4<sup>th</sup> order elasticity tensor.

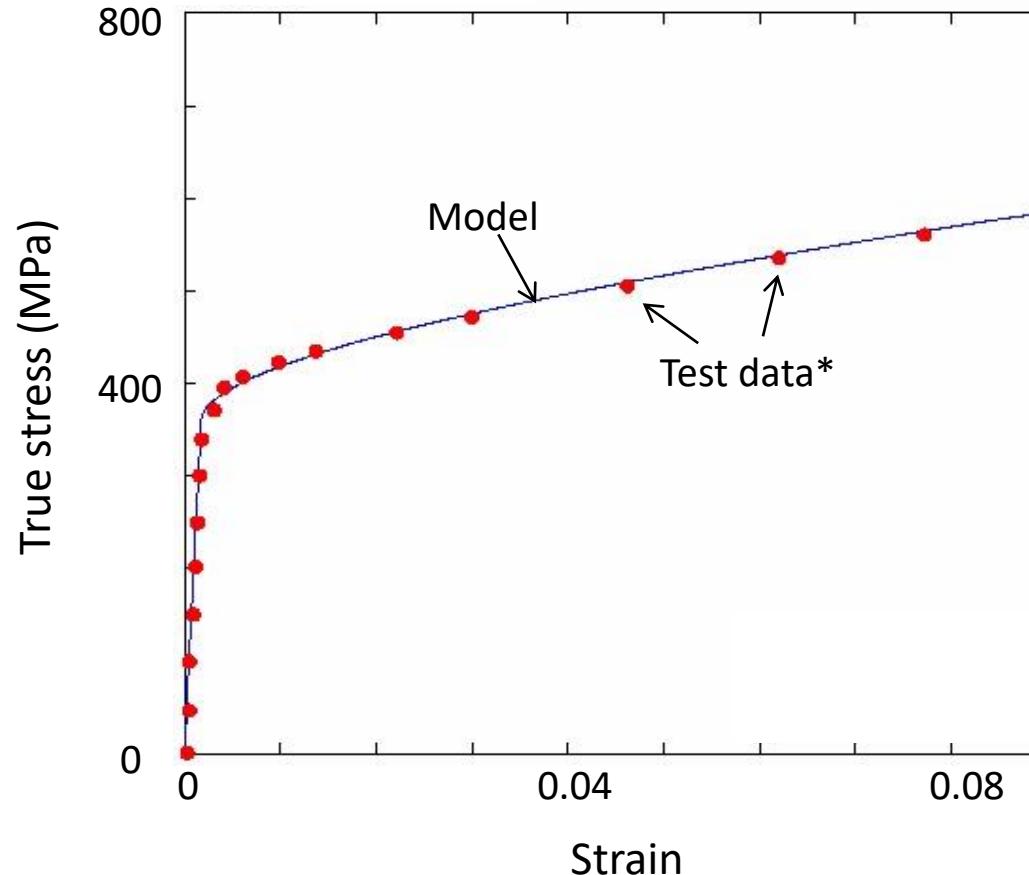
- The new stress  $\sigma^n$  is the point on the surface closest to the test stress.



Stretching of a bar with one slip system  
Colors show equivalent plastic strain

## Fit to quasi-static stress-strain data for AM 304L stainless steel

- Sample was additively manufactured with the Laser Engineered Net Shaping (LENS) process.
- The model also contains temperature and strain rate dependence.



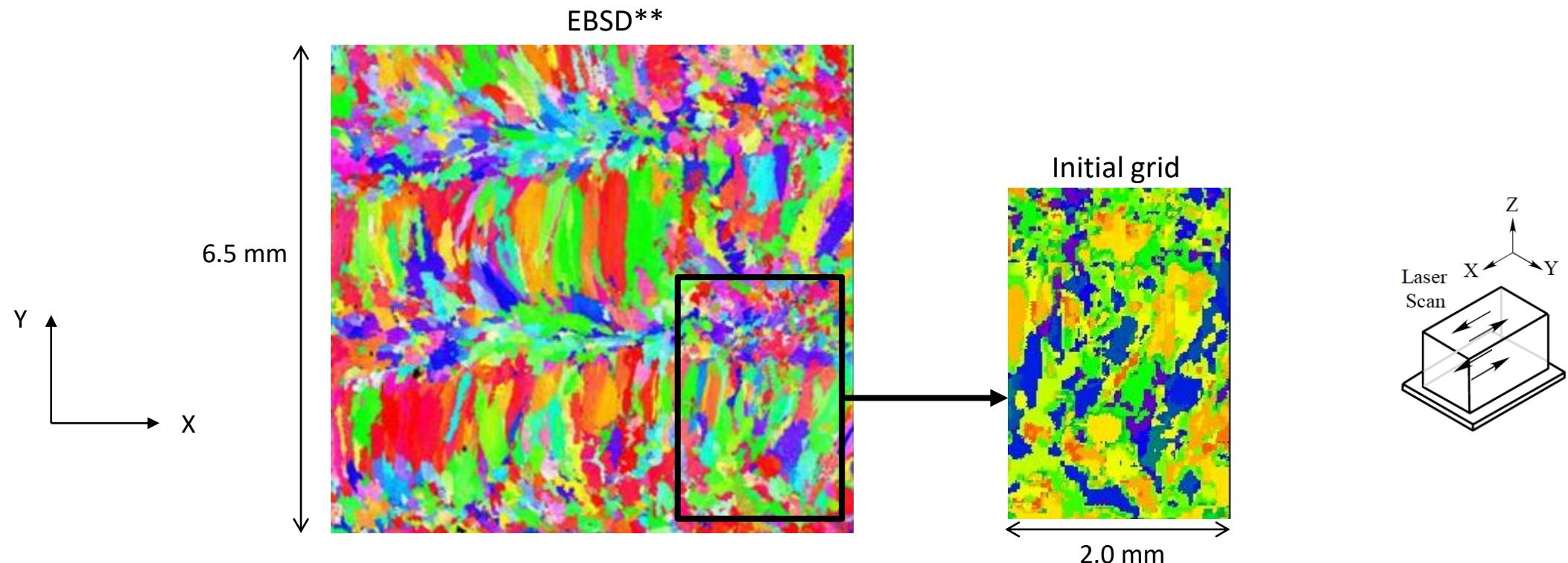
\* D. P. Adams et al., Sandia tech report SAND2019-7001 (2019)

# Assignment of lattice orientations



- Grains are imported into the model from electron backscatter diffraction (EBSD) images.
- Lattice orientations are assigned randomly using Euler angles.
- These are combined with published anisotropic crystal elasticity data\* for 304L SS to compute  $C$  for each grain.

$$C_{11} = 209 \text{ GPa} \quad C_{12} = 133 \text{ GPa} \quad C_{44} = 121 \text{ GPa}$$

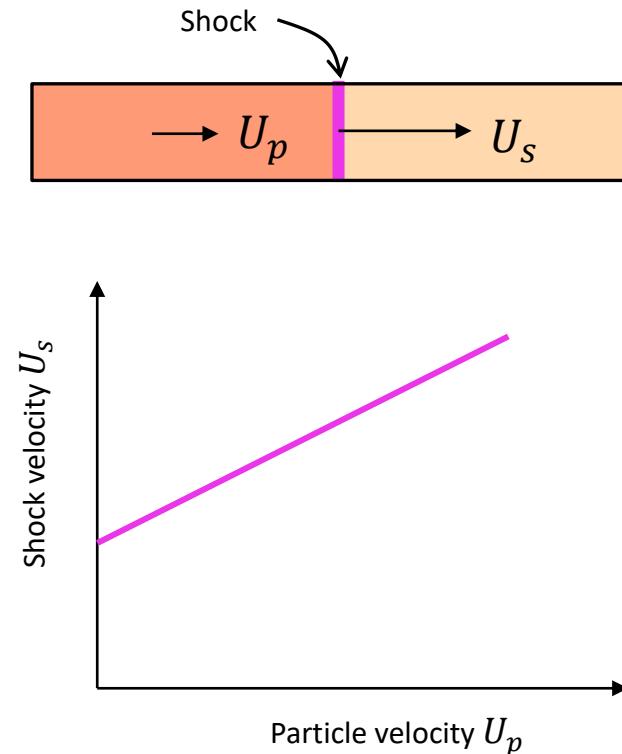
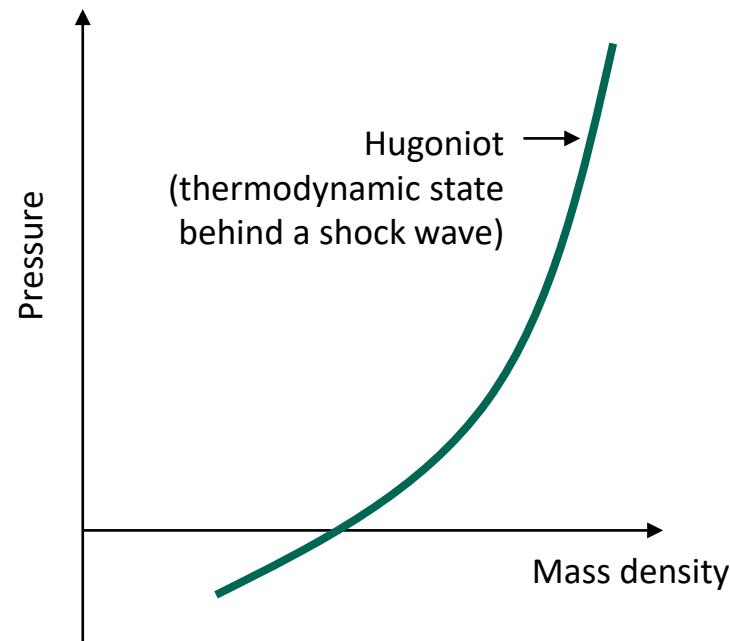


\*H. Ledbetter, *Physica B+C* (1985)

\*\*Image: T. Ruggles

# Equation of state

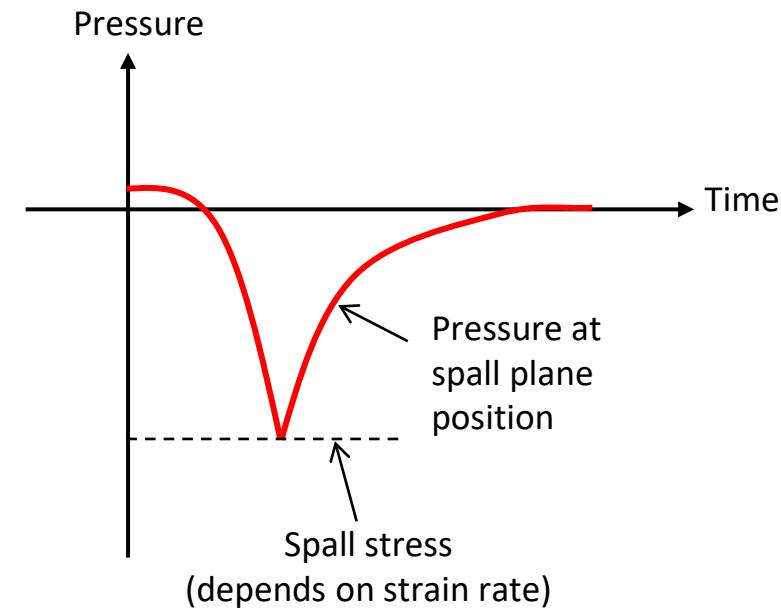
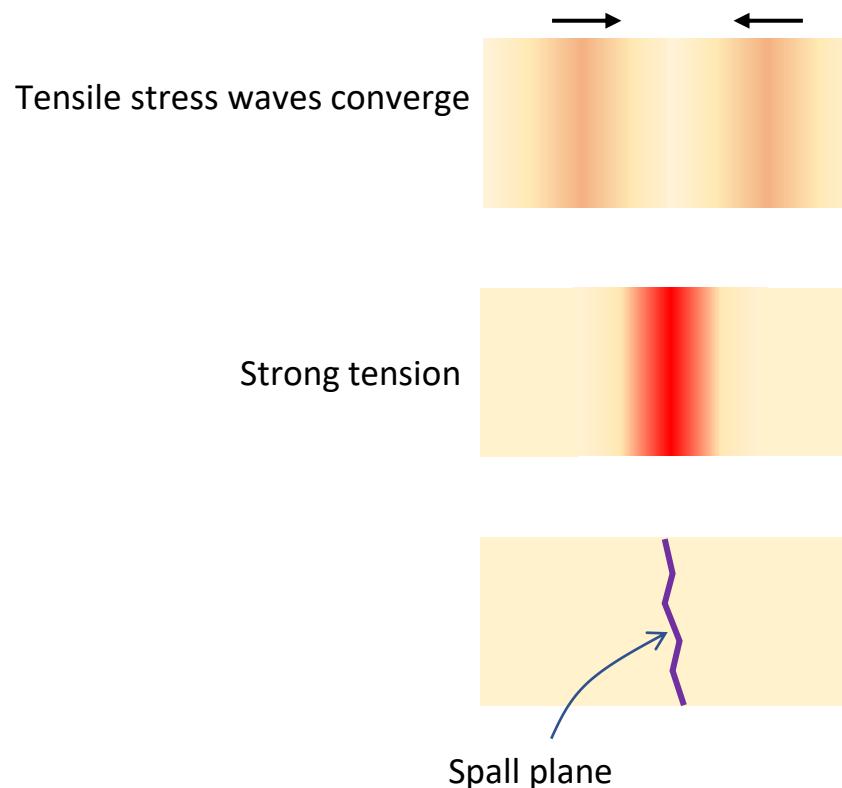
- Add a pressure term to the deviatoric stress found from the crystal plasticity model.
- Mie-Gruneisen EOS:
  - Input: Internal energy density, mass density
  - Output: Pressure, temperature
  - Shock velocity is a linear function of particle velocity behind the shock.
  - Same EOS for all grains



# Spall kinetics model



- Failure occurs over a finite period of time.
- The rate of failure depends on the peak tensile stress and strain rate.

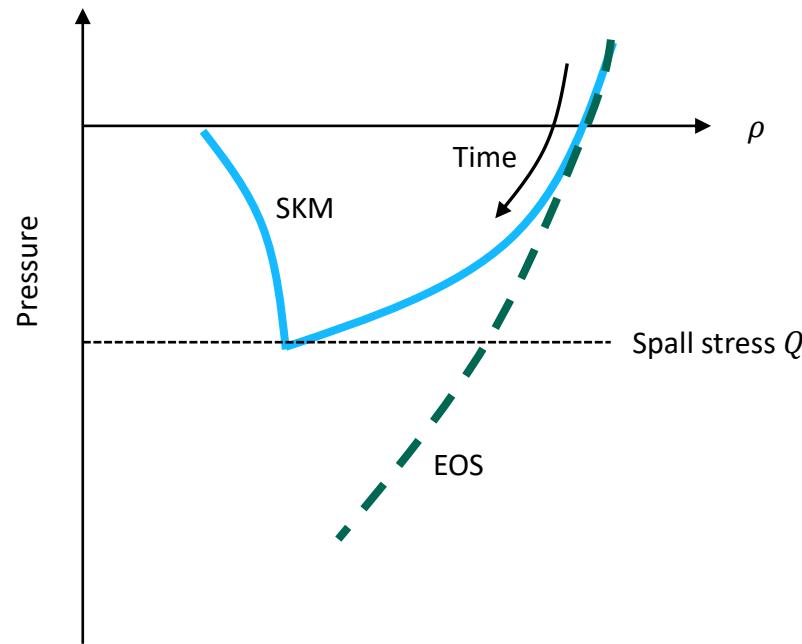


# Spall kinetics model: softening and variability

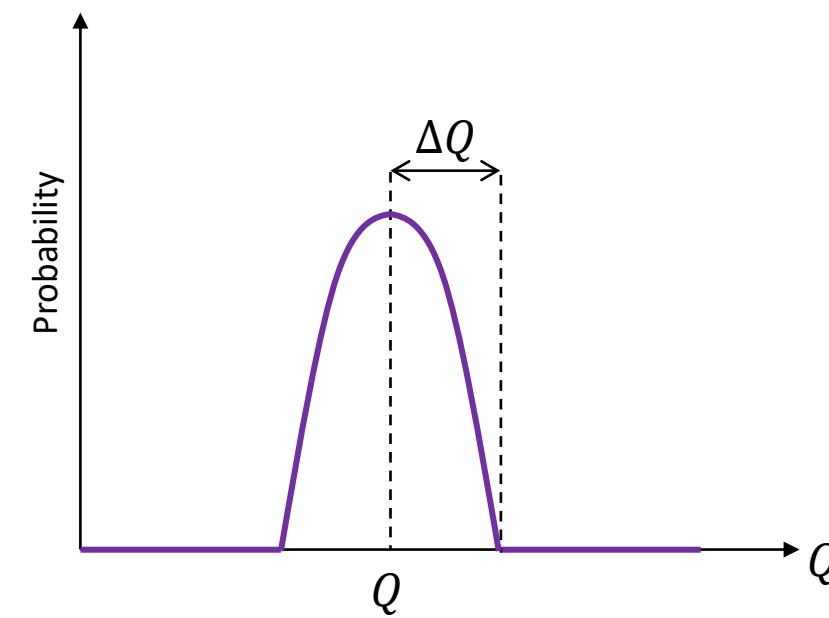


- The EOS is modified to include softening as the critical stress for failure is approached.
- Each grain (from EBSD) is randomly assigned a value of spall stress.

Softening and failure during expansion

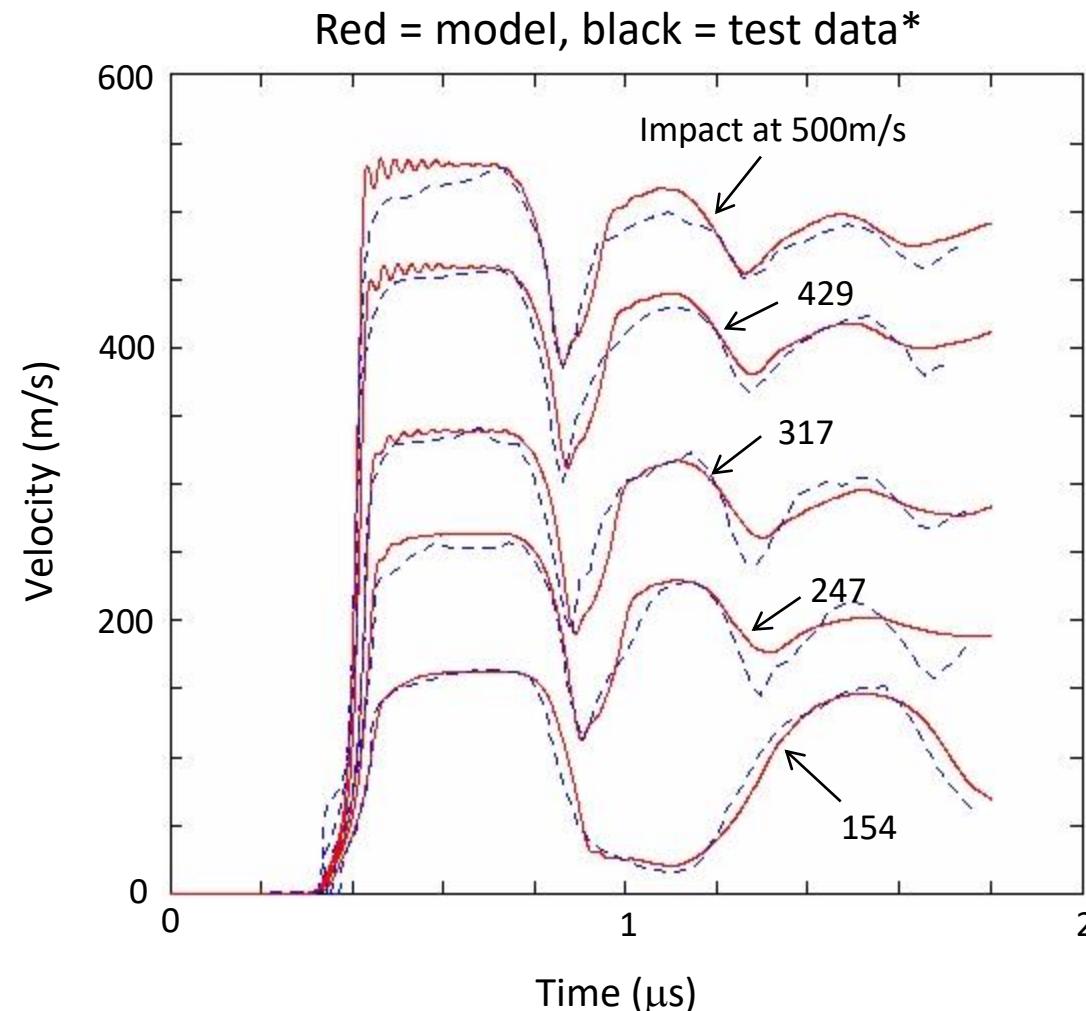
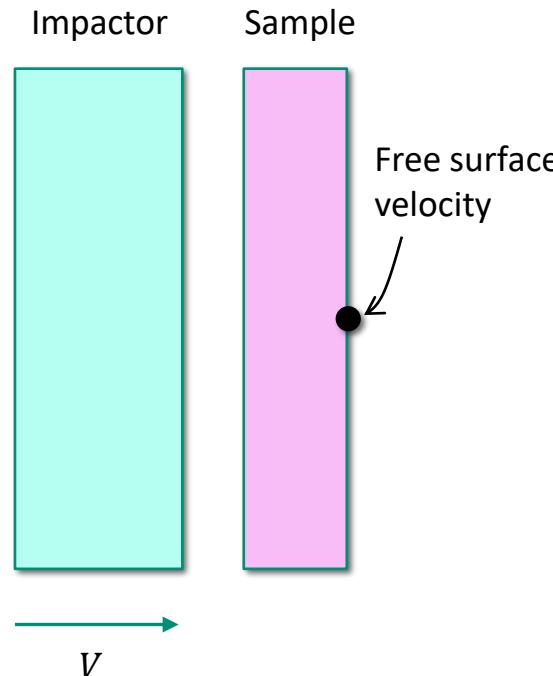


Grain-to-grain variability in spall stress



# Results: Free surface velocity

- Figure compares model results with test data.



\* J. L. Wise et al., AIP Conference Proceedings (2017)

P. E. Specht et al., Sandia tech report SAND2019-12275 (2019)

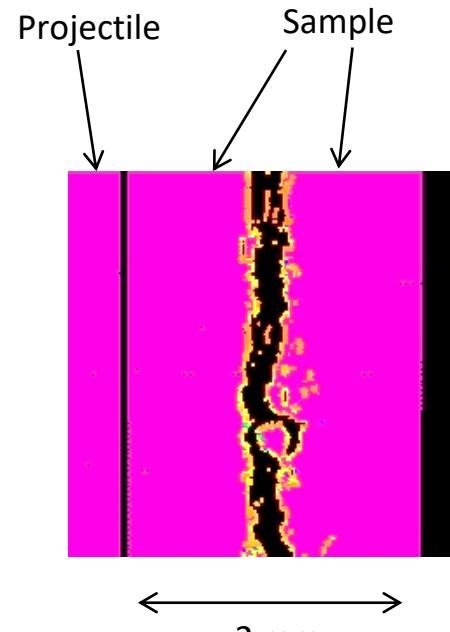
# Spall surface condition



$$V = 317 \text{ m/s}$$



Experiment\*



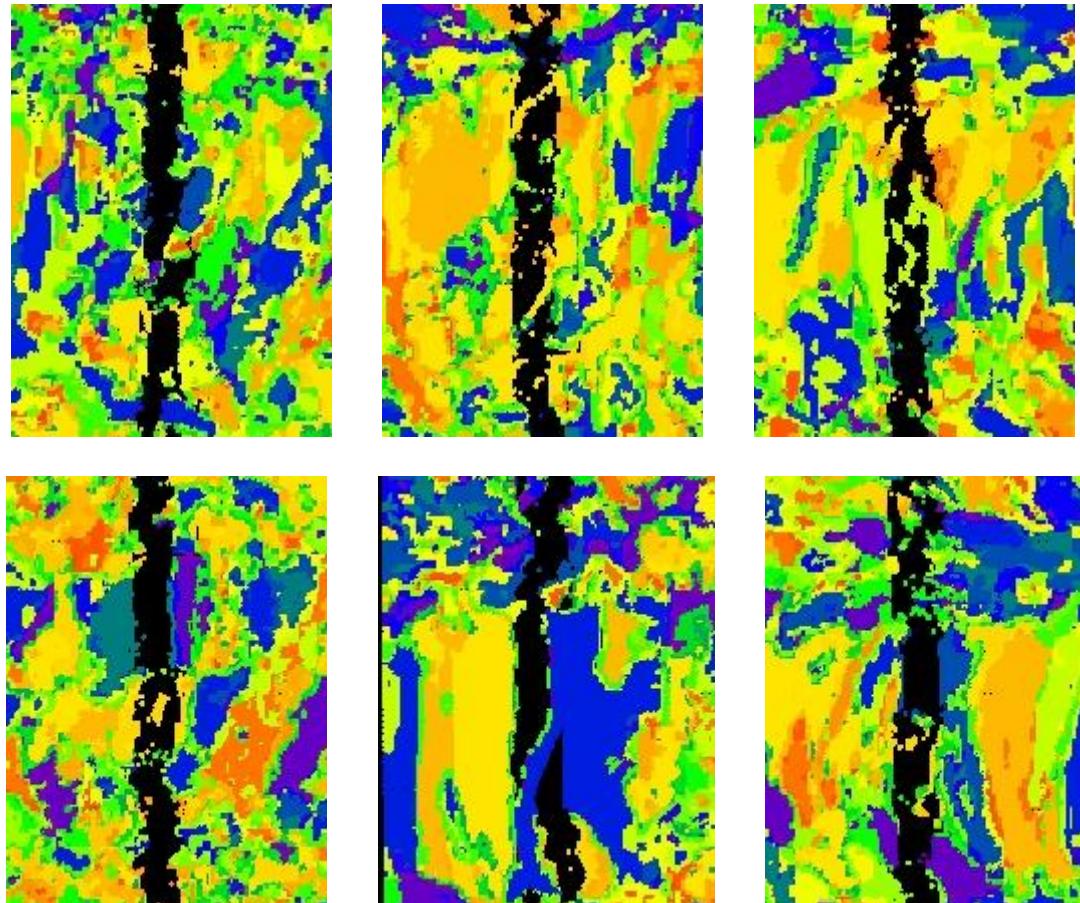
Model  
(Colors show damage)

\* D. P. Adams et al., Sandia tech report SAND2019-7001 (2019)

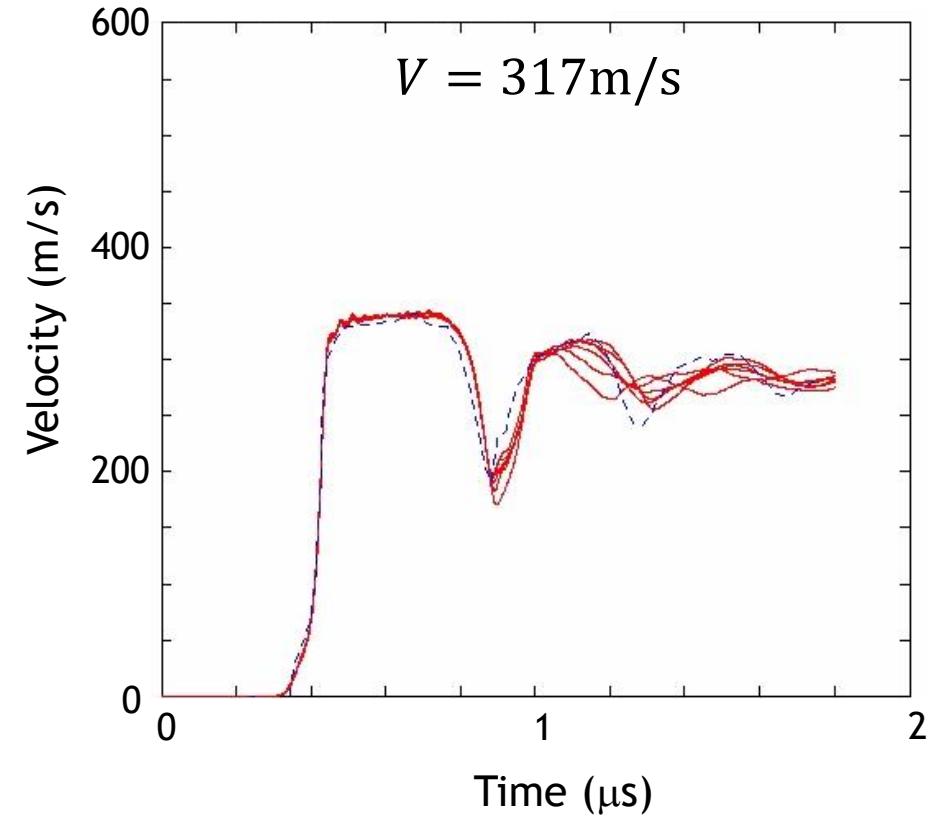
# Effect of microstructure



- What is the effect of extracting different samples from within the EBSD image?
- Makes some difference at intermediate impact velocities.



Free surface velocity for the 6 samples, all X-cut





- The large and distorted grain shapes with AM materials affect the dynamic failure properties.
- A number of new capabilities have been implemented in peridynamics:
  - Crystal plasticity
  - Importing microstructures
  - Spall kinetics model
  - Material variability
- The resulting model reproduces the main features of the test data over a range of impact velocities.