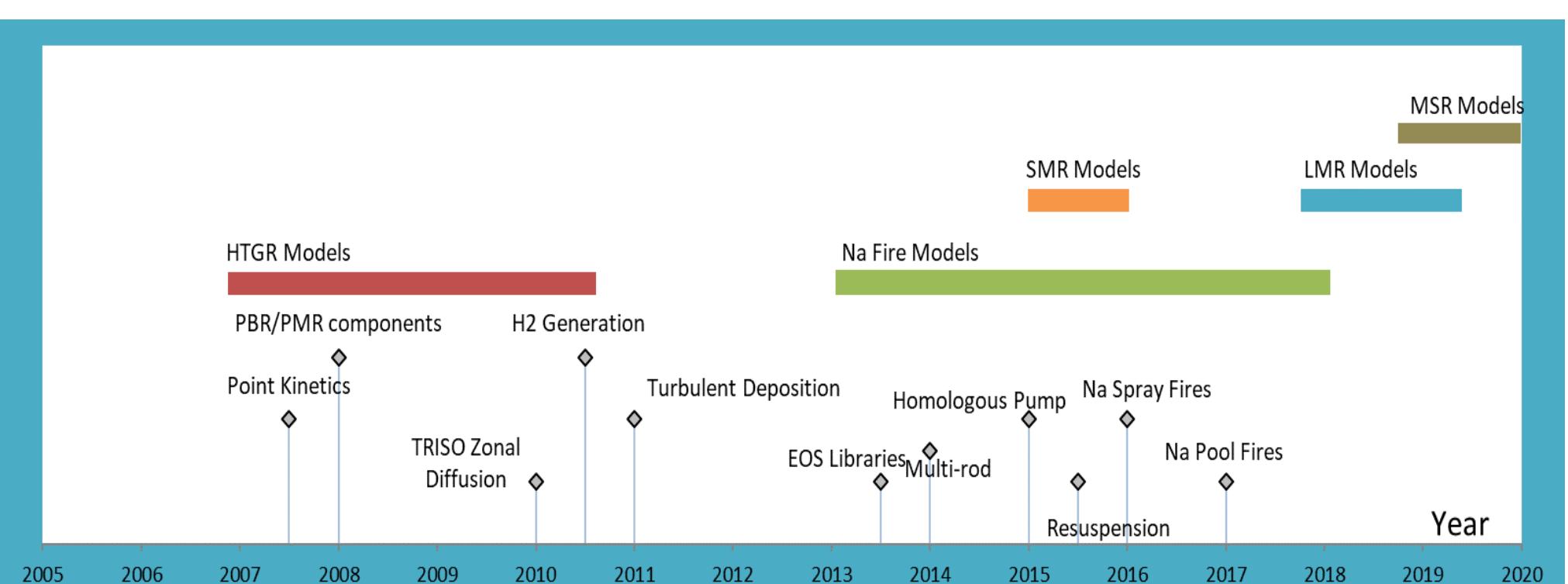
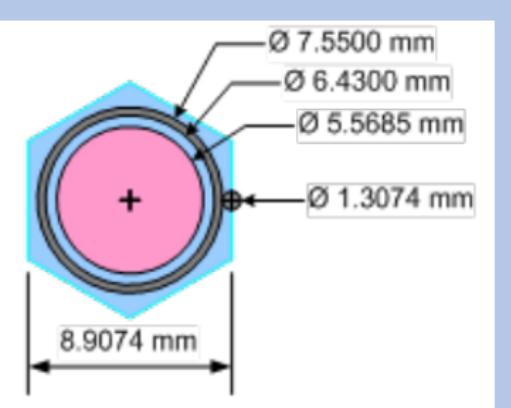


SFR Modeling



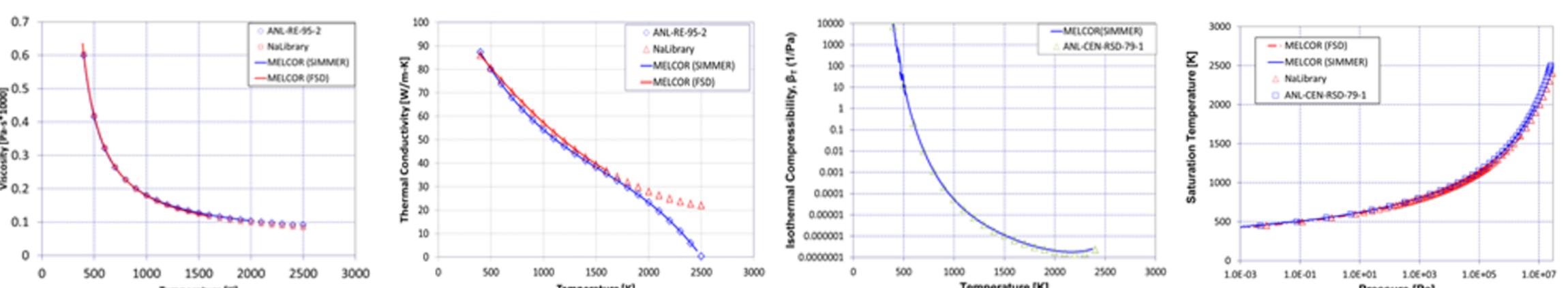
SFR Components (under development)

- SFR to use fuel, clad, cannister, and support/non-support structure
- Bond sodium gap not its own component as of now
 - Existing gap modeling capabilities
 - New models for gap closure, sodium migration to plenum, and attending FP transport
- Pin plenum not its own component as of now
 - Initialization
 - Volume accounting and ideal gas treatment
 - Attending FP transport
 - Pressure calculation
- Expect reflector component could factor into SFR designs
- May revise some intracell and intercell component-wise heat transfer models



Sodium Equation of State (EOS)

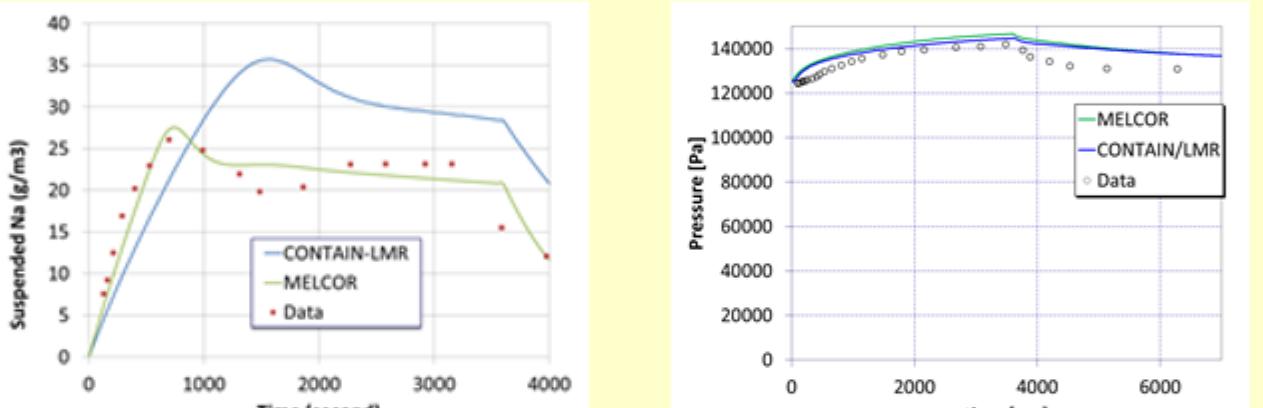
- Two alternatives: Fusion Safety Database (FSD) and SIMMER-III
 - FSD uses a soft-sphere EOS model fit to an experimental database
 - SIMMER-III supplemented with experimental data (Fink & Leibowitz)
- Verified EOS on a wide range of thermodynamic conditions
- Enthalpy, heat capacity, heat of fusion, vapor pressure, heat of vaporization, density, thermal conductivity, thermal diffusivity, and thermal expansion
- Demonstration calculations reproduce the experimental database



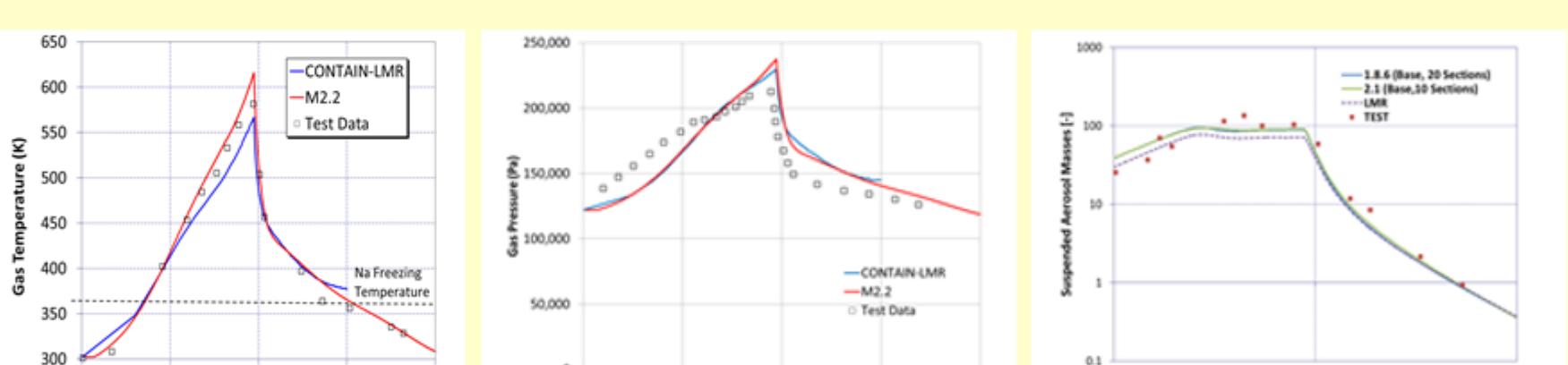
SFR Containment (Ex-Vessel) Models

- Spray and pool fire models from CONTAIN/LMR
- Pool fire
 - Pool fire model from SOFIRE-II based on pool fire tests
 - Predicts rate of oxygen and sodium consumption plus heat evolved from reaction
$$(1 + f_1) \cdot 2 \cdot \text{Na} + \text{O}_2 \rightarrow 2 \cdot f_1 \cdot \text{Na}_2\text{O} + (1 - f_1) \cdot \text{Na}_2\text{O}_2 + q(\text{reaction})$$
- Spray fire
 - Spray fire model from NACOM
 - Predict total burned sodium mass as function of droplet size and fall velocity
 - Integrate combustion rate over droplet fall height

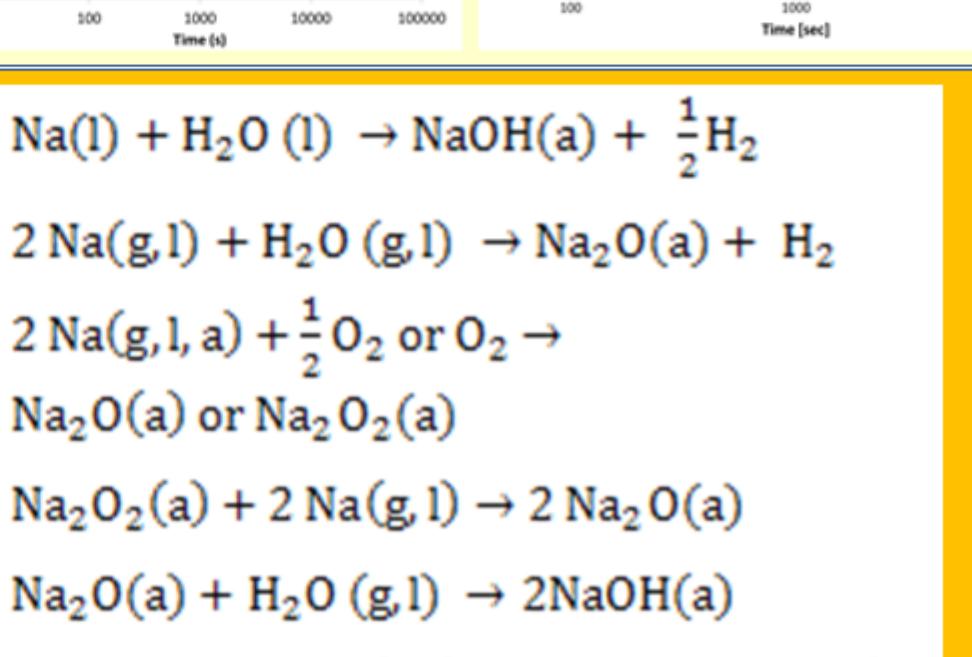
- Fire model validation – ABCOVE AB1/AB5
 - AB1 (pool)



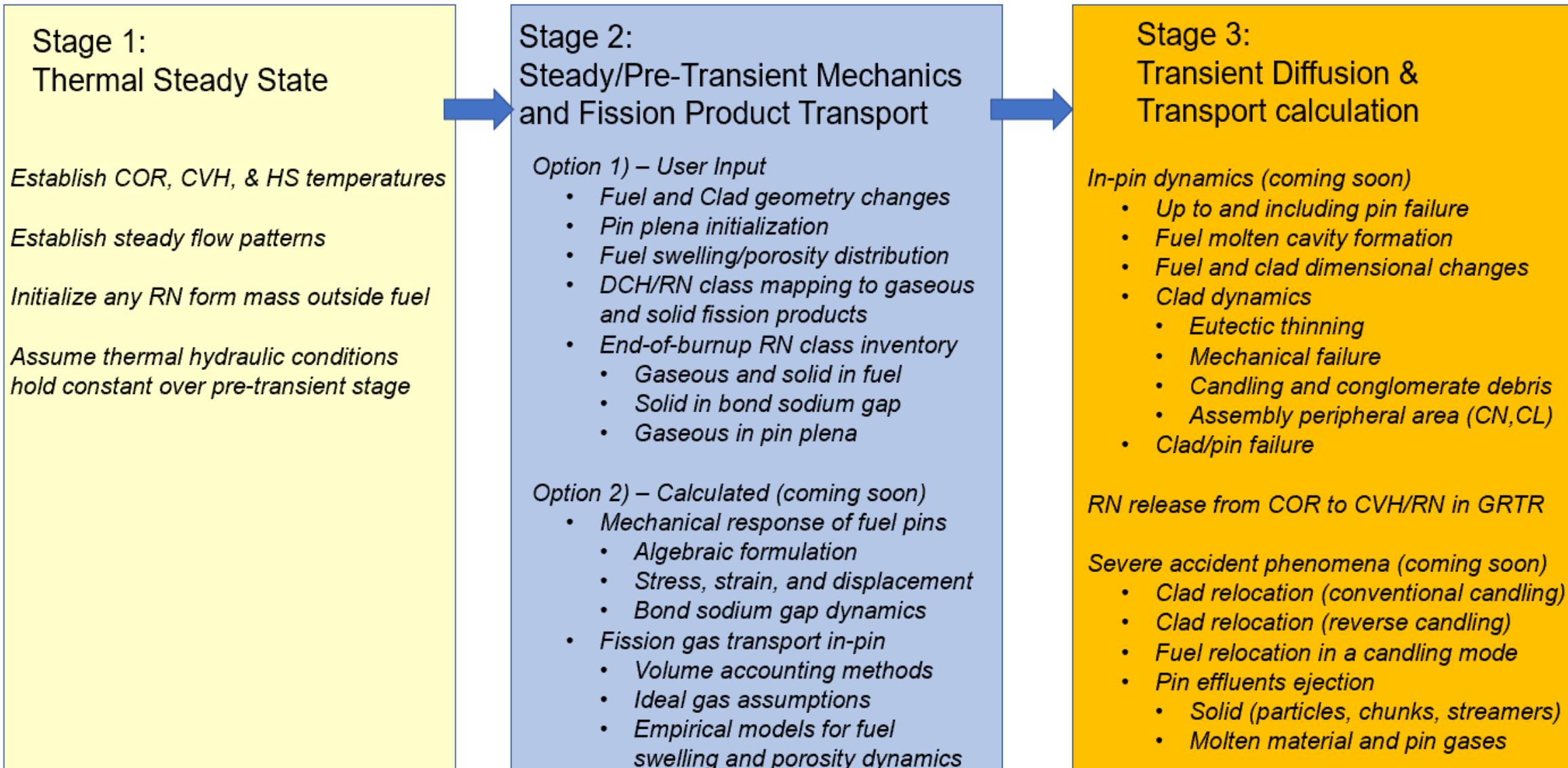
- AB5 (spray)



- Atmospheric chemistry
 - Aerosol/atmosphere
 - Aerosol on surfaces
 - Sodium/water in atmosphere
 - Reactions in hierarchical order
 - Affected through NAC package
 - New RN classes
 - New sensitivity coefficients



Transient/Accident Solution Methodology

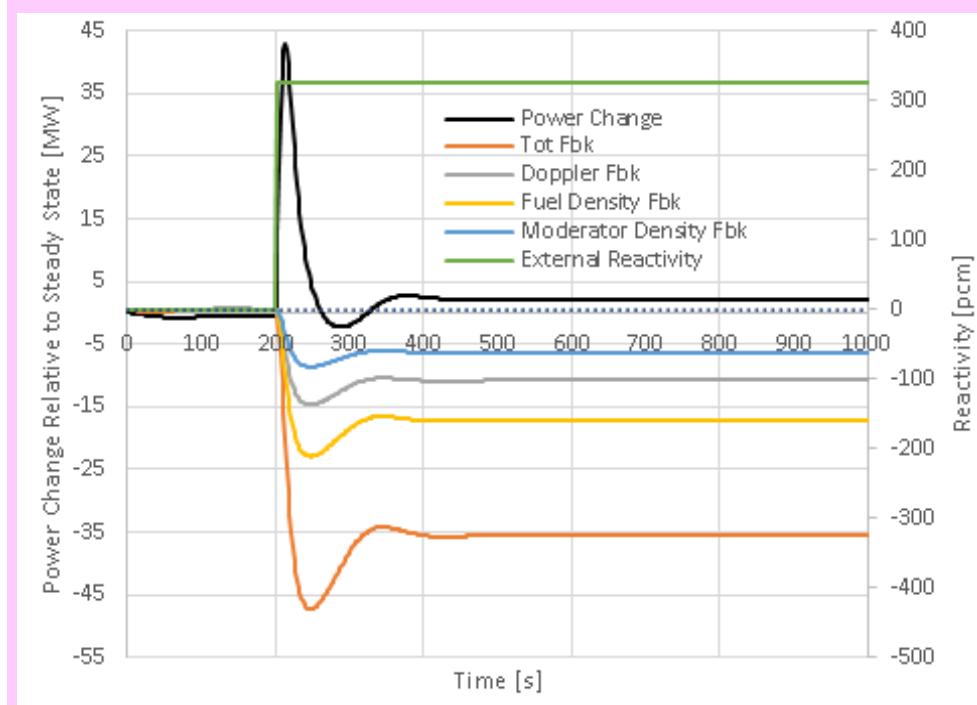


Standard Point Reactor Kinetics Equations

Standard 6 group treatment

$$\frac{dP}{dt} = \left(\frac{\rho - \beta}{\Lambda} \right) P + \sum_{i=1}^6 \lambda_i Y_i + S_0$$

$$\frac{dY_i}{dt} = \left(\frac{\beta_i}{\Lambda} \right) P - \lambda_i C_i, \quad \text{for } i = 1 \dots 6$$



Kinetics data accessible by sensitivity coefficients

Feedback models

- Control function-specified external
- Doppler
- Fuel and moderator density
- New for SFRs (under development)
 - Dimension changes and rod bowing
 - Molten fuel/clad
 - Sodium void

Define core cell ranges over which component average temperatures are taken to inform feedback models

SFR Expanded In-Vessel Modeling

Pin Mechanics

- Radial stress/strain/displacement
- Axial stress/strain
- Solve iteratively

Radial

Axial

$$\sigma_r = \frac{1}{2} \left(\sigma_x - v(\sigma_y + \sigma_z) \right) + \Delta(\sigma^r)$$

$$\sigma_x = \frac{1}{2} \left(\sigma_y - v(\sigma_x + \sigma_z) \right) + \Delta(\sigma^x)$$

$$\sigma_z = \frac{1}{2} \left(\sigma_z - v(\sigma_x + \sigma_y) \right) + \Delta(\sigma^z)$$

The result for fuel solid zone force is:

$$F_r = F_{ext} + F_{in} + F_r$$

A force balance on the axial segment can be written considering a few contributions:

$$\sigma_x = \frac{2\sigma_r}{1-v^2} \left[\frac{1}{1-v^2} \left(\sigma_r^2 - \sigma_y^2 - \sigma_z^2 \right) - \frac{E\Delta(\sigma^x)}{1-v^2} + E_{ext} \right]$$

The cavity and axial terms (F_{ext} and F_{in}) are computed from molten cavity and pin plenum pressure, while the clad term (F_r) is computed from a similar formulation to that of F_r for hot but with clad properties.

The state of the system is:

If the gap is open or free expansion is assumed, the clad force contribution is zero.

The axial force balance equation can be solved for the force on the cavity (based on thermal and force components) and written in terms of time-averages of inner and outer boundary conditions as well as cavity and plenum pressures. In the absence of a clad force contribution, for example, the thermal and force components of the axial force plane strain are:

$$A_{ext} = \frac{2\sigma_r}{1-v^2} \left(\sigma_r^2 - \sigma_y^2 - \sigma_z^2 \right)$$

$$A_{in} = \frac{2\sigma_r}{1-v^2} \left(\sigma_r^2 - \sigma_y^2 - \sigma_z^2 \right) - \frac{E\Delta(\sigma^x)}{1-v^2}$$

Miscellaneous models

- Fuel swelling
- Fuel molten cavity formation
- Pin pressurization
- Reactivity effects

Strain/displacement relations:

$$\epsilon_r = \frac{du}{dr}$$

$$\epsilon_x = u/r$$

$$\epsilon_z = z_0$$

Equilibrium:

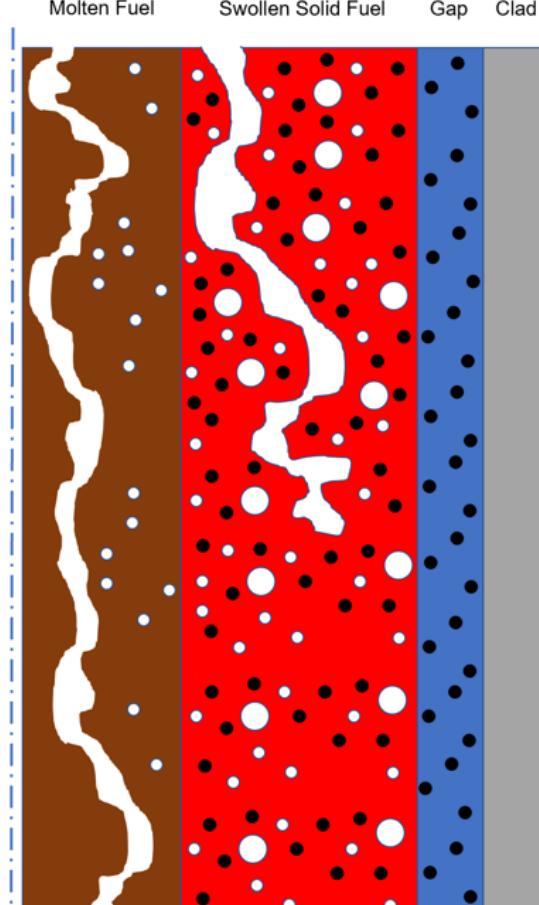
$$\frac{d\sigma_r}{dr} + (\sigma_r - \sigma_x)/r = 0$$

$$A_{ext} = \frac{2\sigma_r}{1-v^2} \left(\sigma_r^2 - \sigma_y^2 - \sigma_z^2 \right)$$

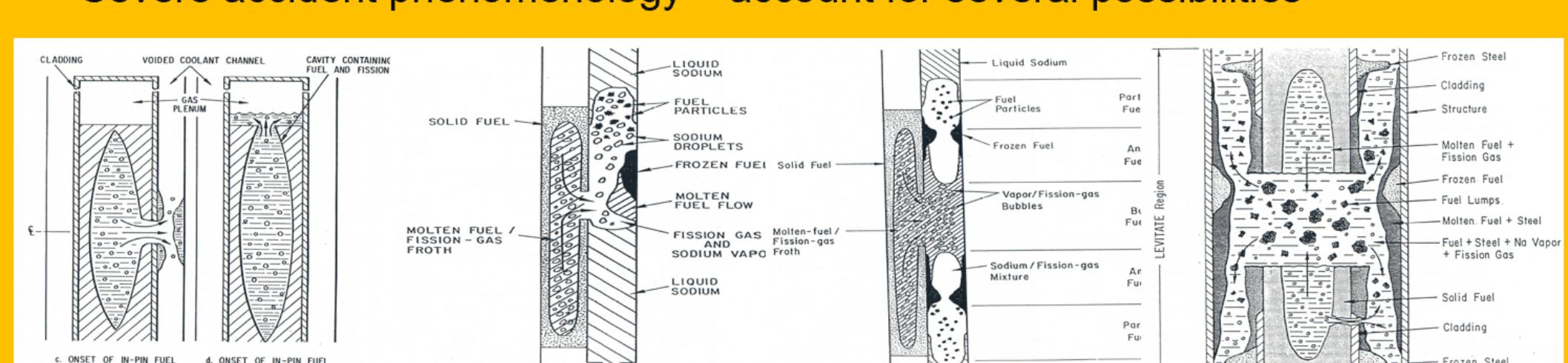
$$A_{in} = \frac{2\sigma_r}{1-v^2} \left(\sigma_r^2 - \sigma_y^2 - \sigma_z^2 \right) - \frac{E\Delta(\sigma^x)}{1-v^2}$$

Fission gas dynamics in-pin

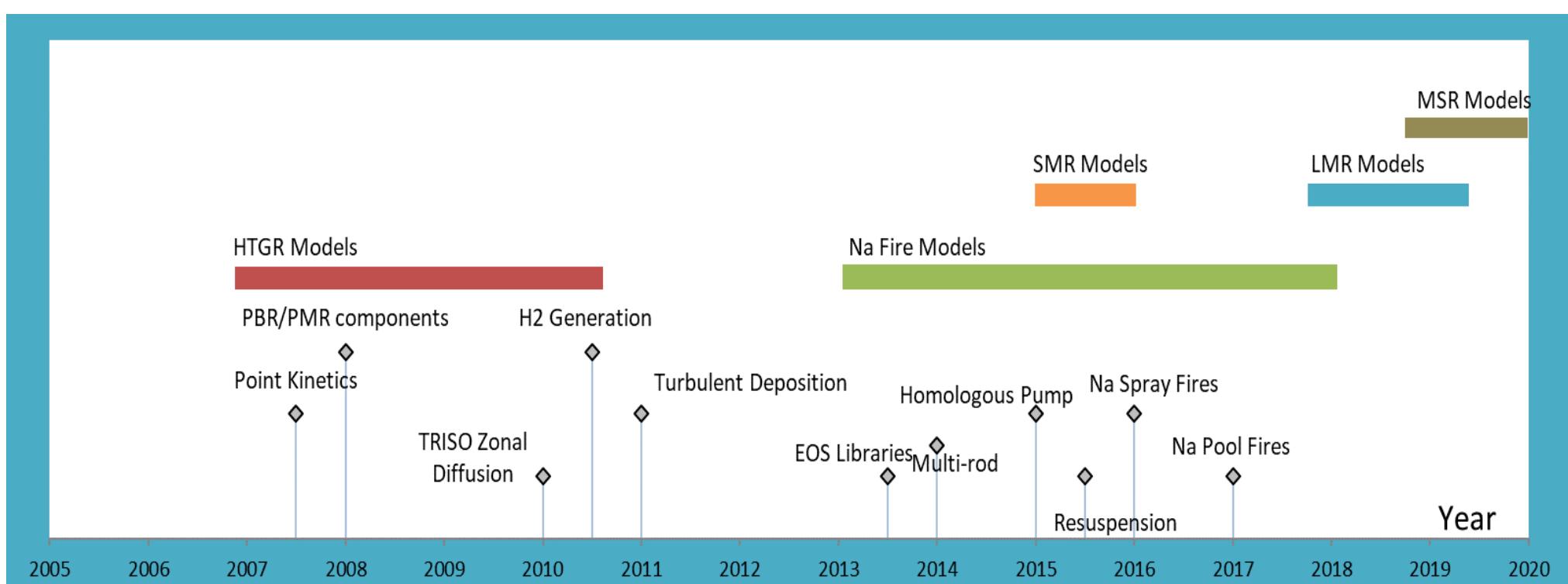
- Forms closed porosity in solid fuel
- Closed porosity grows
- Closed porosity "releases" – swelling
- Open/connected porosity
 - Forms from closed porosity release
 - A "free volume" in pin
 - Communicates with pin plenum
 - At pin plenum pressure
- Molten fuel
 - Forms as solid melts
 - Subsumes open/closed porosity
- RN class inventory migrates as volume



Severe accident phenomenology – account for several possibilities

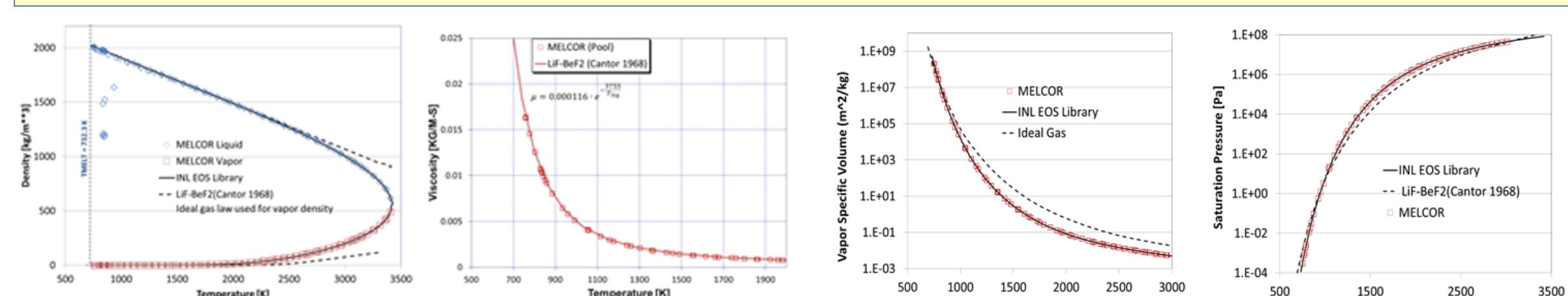


MSR Modeling

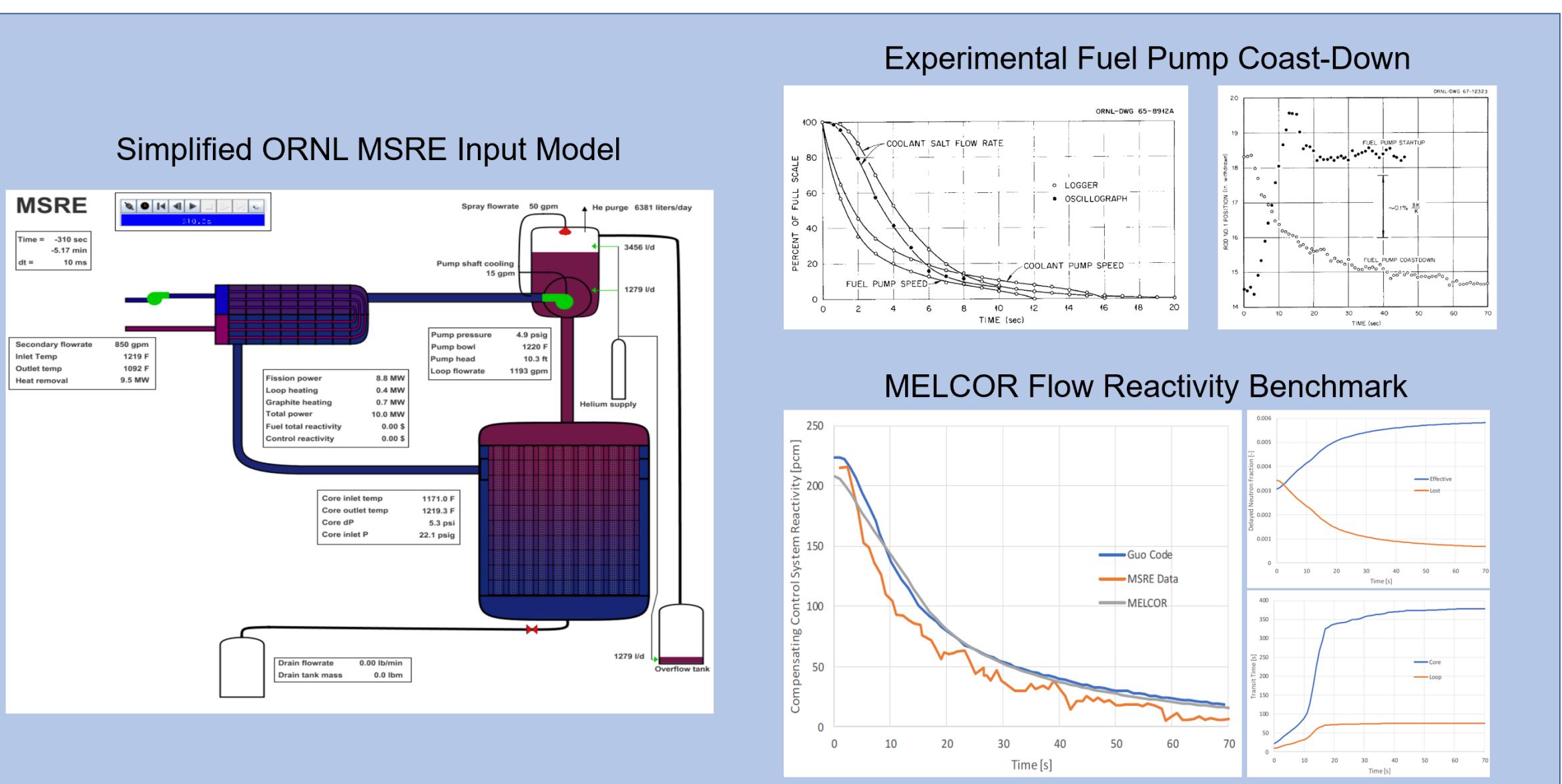


FLiBe Equation of State (EOS)

- Property database based on ORNL publication
- Verified EOS on a wide range of thermodynamic conditions
- Demonstration calculations reproduce the experimental database
- Provisions exist for salt freezing (solid phase) from liquid phase

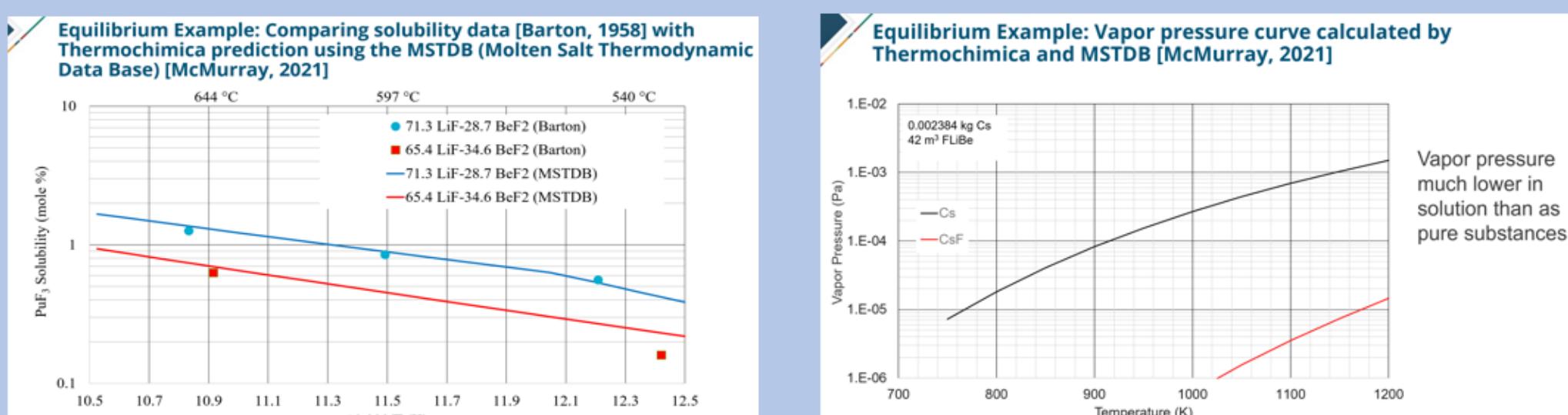


ORNL MSRE Zero-Power Flow Coast-Down Benchmark

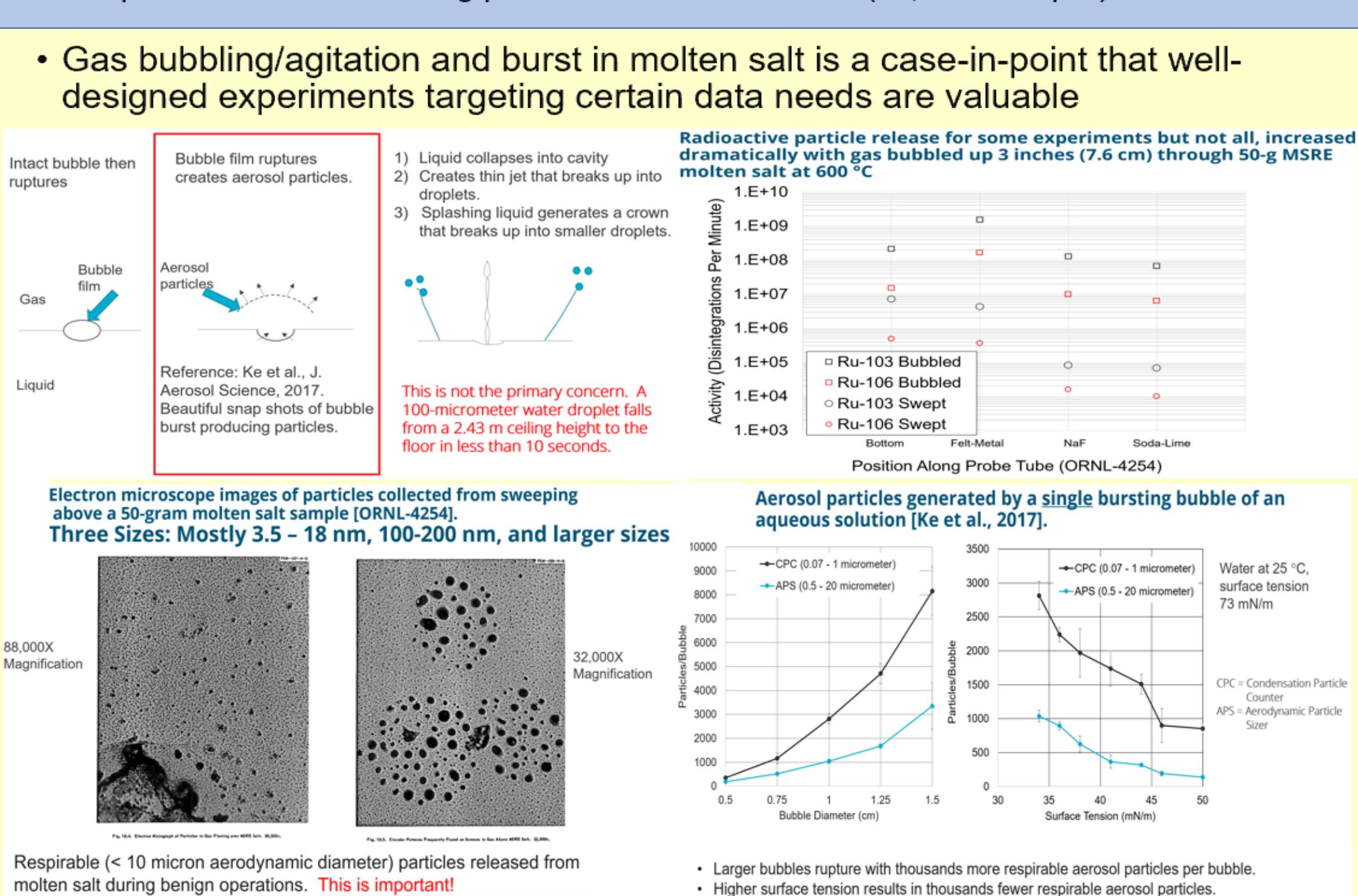


Thermochemistry and Data Needs

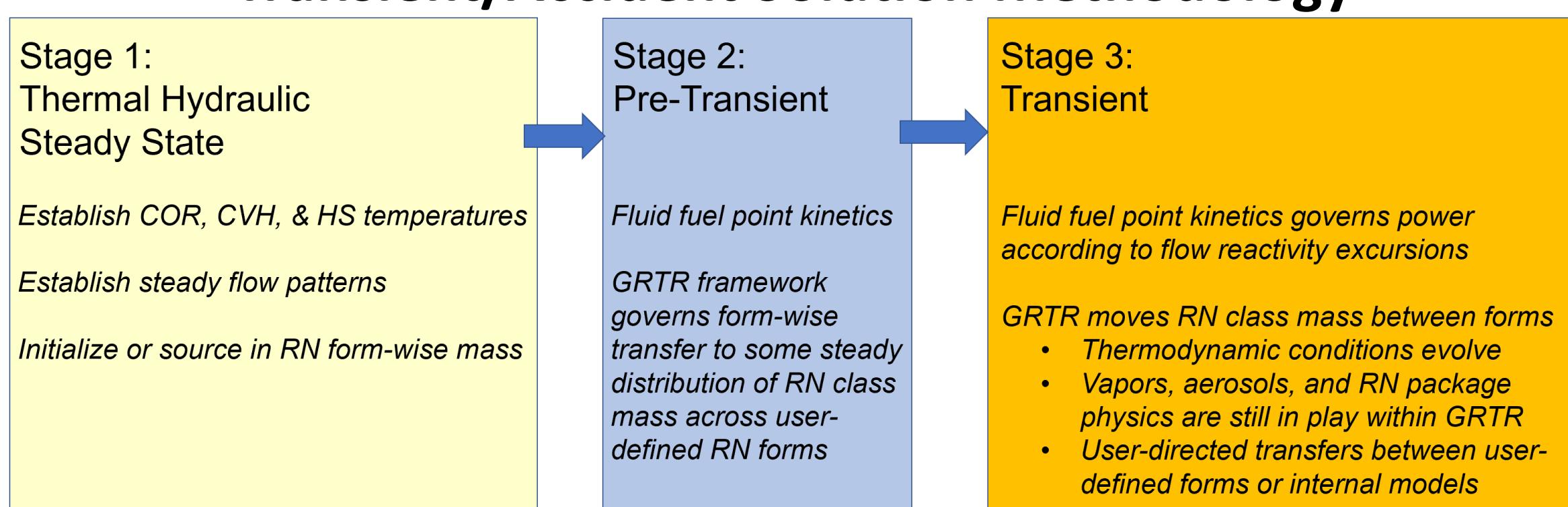
- MELCOR capabilities are in place to use data as available
- MELCOR can utilize Gibbs Energy Minimization type tools (e.g. [Thermochimica](#))



- Thermo databases available in FactSage format:
 - MSTDB w/ 2 systems:
 - Fluoride: Pu-U-Th-Nd-Ce-La-Cs-Rb-Ni-Ca-K-Na-F-Be-Li
 - Chloride: Pu-U-Ce-Cs-Rb-Ni-Fe-Cr-Ca-K-Cl-Al-Mg-Na-Li
 - JRC database: Pu-U-Th-Ce-La-Cs-I-Zr-Rb-Ca-K-Cl-Mg-Na-F-Be-Li
- Databases under active development, needs for severe accidents include:
 - High temperatures (beyond normal operating range)
 - Fission product elements in row 5 of periodic table (Sr, I, Ag, etc.)
 - Species introduced during possible severe accidents (air, water vapor)



Transient/Accident Solution Methodology



Fluid Fuel Point Reactor Kinetics Equations

Under these assumptions, the steady form of the FFPRK equations is:

$$\frac{dP(t)}{dt} = \left(\frac{\rho(t) - \bar{\beta}}{\Lambda} \right) P(t) + \sum_{i=1}^6 \lambda_i C_i^C + S_0$$

$$\frac{dC_i^C(t)}{dt} = \left(\frac{\beta_i}{\Lambda} \right) P(t) - (\lambda_i + 1/\tau_C) C_i^C(t) + \left(\frac{V_L}{\tau_L V_C} \right) C_i^L(t - \tau_L), \quad \text{for } i = 1 \dots 6$$

$$\frac{dC_i^L(t)}{dt} = \left(\frac{V_C}{\tau_C V_L} \right) C_i^C(t) - (\lambda_i + 1/\tau_L) C_i^L(t), \quad \text{for } i = 1 \dots 6$$

$$\bar{\beta} = \beta - \left(\frac{\Lambda}{P(t)} \right) \sum_{i=1}^6 \lambda_i C_i^L(t)$$

Where:

$P(t)$ = Thermal power due to fission 0

C_i^C = delayed neutron precursor group i inventory/concentration in-core

C_i^L = delayed neutron precursor group i inventory/concentration ex-core (in loop)

S_0 = Thermal power generation rate due to neutron source

$\rho(t) = \frac{k-1}{k}$ = Reactivity for k the effective multiplication factor

$\bar{\beta}$ = Effective delayed neutron fraction

β = Delayed neutron fraction (static, in absence of drift effects)

$\Lambda = 1/\nu V \Sigma_f$ = Neutron generation time

$\tau_{C/L} = \frac{M_{C/L}}{\dot{m}}$ = Residence time of precursors (core, loop, respectively)

$V_{C/L}$ = Fluid volume (core, loop, respectively)

λ_i = Decay constant of delayed neutron precursor group i

A – In-Vessel DNP gain by fission

B – In-Vessel DNP loss by decay, flow

C – In-Vessel DNP gain by Ex-Vessel DNP flow

D – Ex-Vessel DNP gain by In-Vessel DNP flow

E – Ex-Vessel DNP loss by decay, flow

Solving for DNP cohorts:

$$\frac{dP(0)}{dt} = 0 = \left(\frac{\Delta\rho_0 - \bar{\beta}(0)}{\Lambda} \right) P_0 + \sum_{i=1}^6 \lambda_i C_{i,0}^C = \left(\frac{\Delta\rho_0 - \beta + \beta_{lost}(0)}{\Lambda} \right) P_0 + \sum_{i=1}^6 \lambda_i C_{i,0}^C$$

$$\frac{dC_i^C(0)}{dt} = 0 = \left(\frac{\beta_i}{\Lambda} \right) P_0 - (\lambda_i + 2/\tau_C) C_{i,0}^C + \left(\frac{V_L}{V_C} \right) (\lambda_i + 2/\tau_L) C_{i,0}^L, \quad i = 1 \dots 6$$

$$\frac{dC_i^L(0)}{dt} = 0 = \left(\frac{V_C}{\tau_C V_L} \right) C_{i,0}^C - (\lambda_i + 1/\tau_L) C_{i,0}^L, \quad i = 1 \dots 6$$

Solving for the bias reactivity and the time-zero effective delayed neutron fraction:

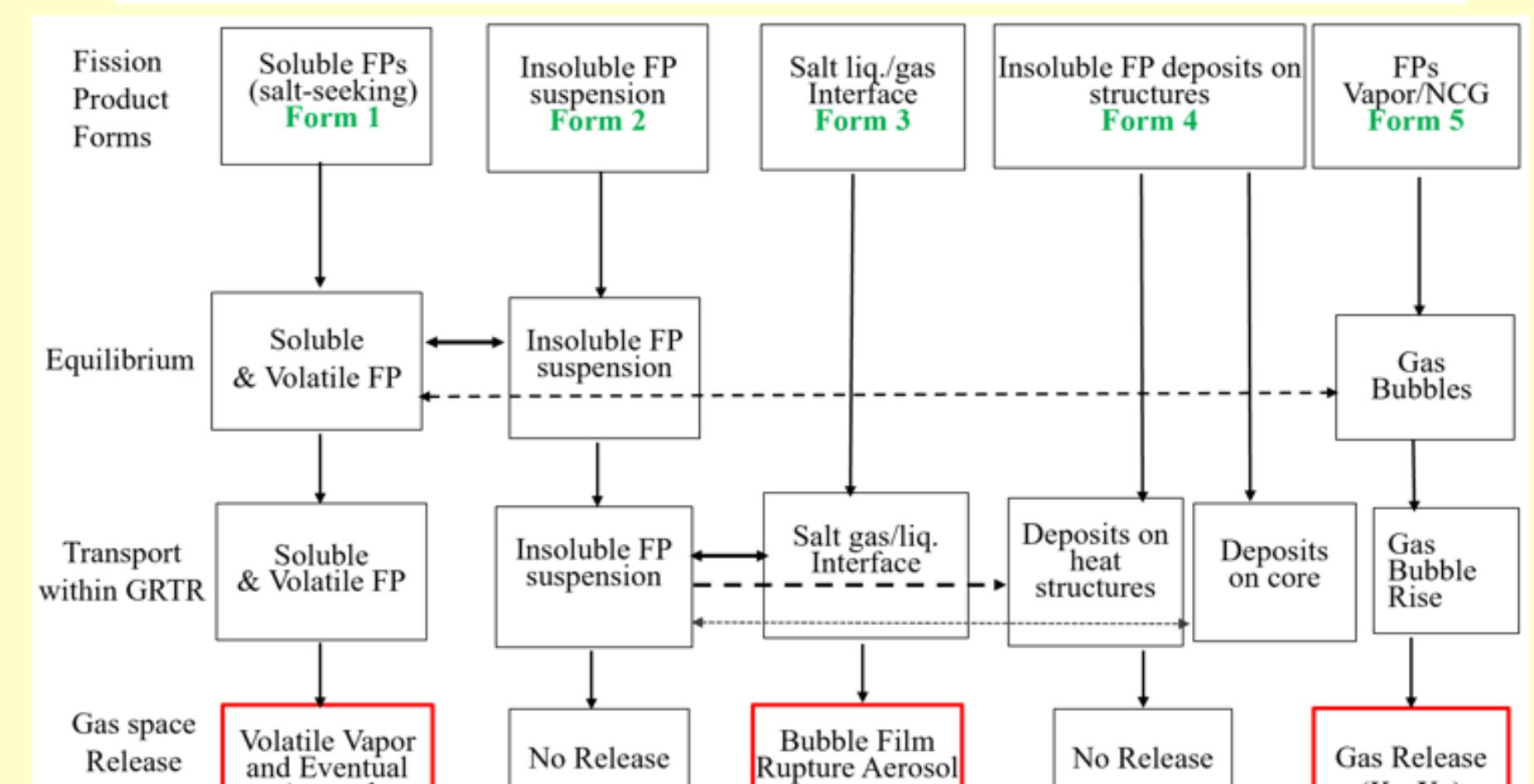
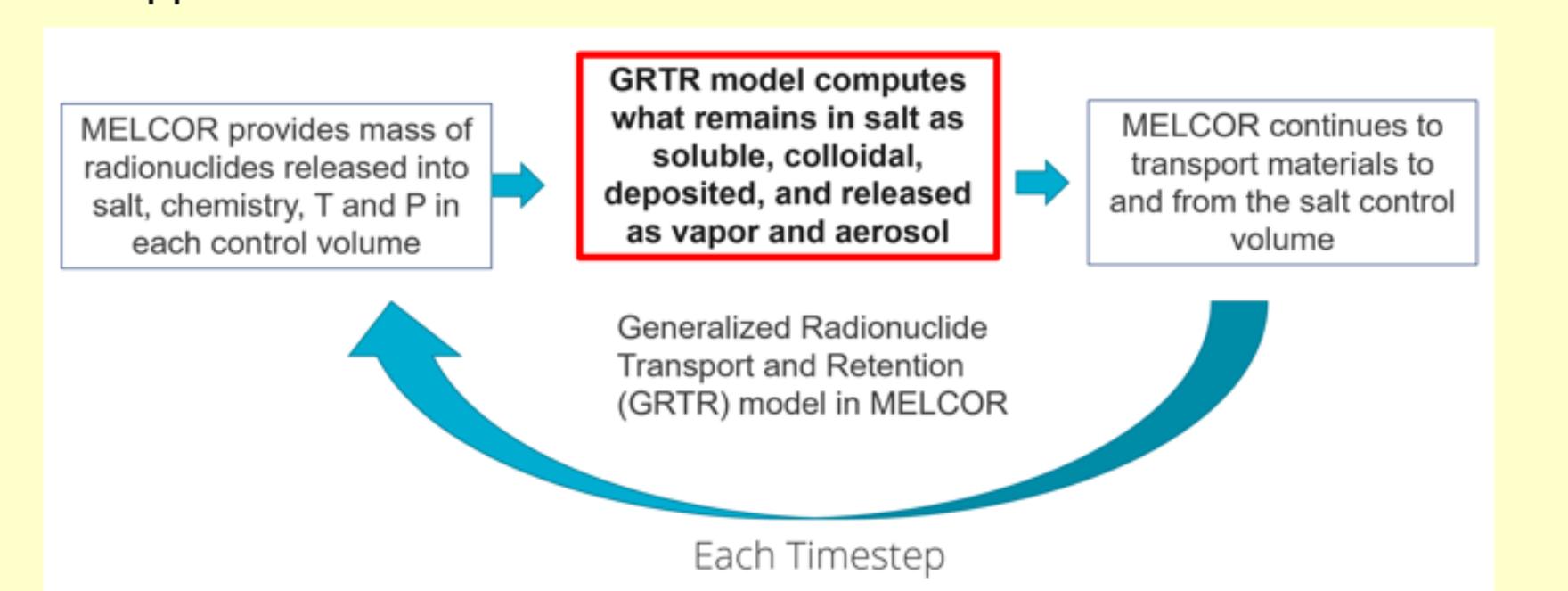
$$\Delta\rho_0 = \beta - \Lambda \sum_{i=1}^6 \lambda_i \alpha_i (1 + \gamma_i)$$

$$\bar{\beta}(0) = \beta - \beta_{lost}(0) = \beta - \Lambda \sum_{i=1}^6 \lambda_i \gamma_i \alpha_i$$

GRTR Modeling Framework

- GRTR affected through CVH and RN1
 - CVH input declares:
 - User-defined forms and their characteristics (sectionwise, nonsectionwise, HS deposition)
 - Transfers between user-defined forms and from user-defined forms to built-in forms
 - Control functions can direct transfers
 - Limited built-in form-wise transfer physics models
 - Limited ability to employ Gibbs Energy Minimization tools like Thermochimica
 - RN1 input declares:
 - Initial user-defined form-wise mass by class and control volume
 - Sources for user-defined form-wise mass by class and control volume
 - If COR package is active, require a mapping for user-defined form-wise release

- GRTR applied to MSRs



- In MSR context, GRTR can account for:
 - Dissolved mass and its coming out of solution
 - Colloidal (insoluble) mass and its transport
 - Generation of aerosol at a free surface as bubbles burst
 - Vaporization
 - Aerosol dynamics according to conventional MELCOR physics models
 - HS deposition of any of the above forms
 - Advection of any of the above with CVH/FL flows
 - Use of control functions or built-in models or Thermochemica for form-wise transfers