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# Overview of the latest features and capabilities in the Dakota software



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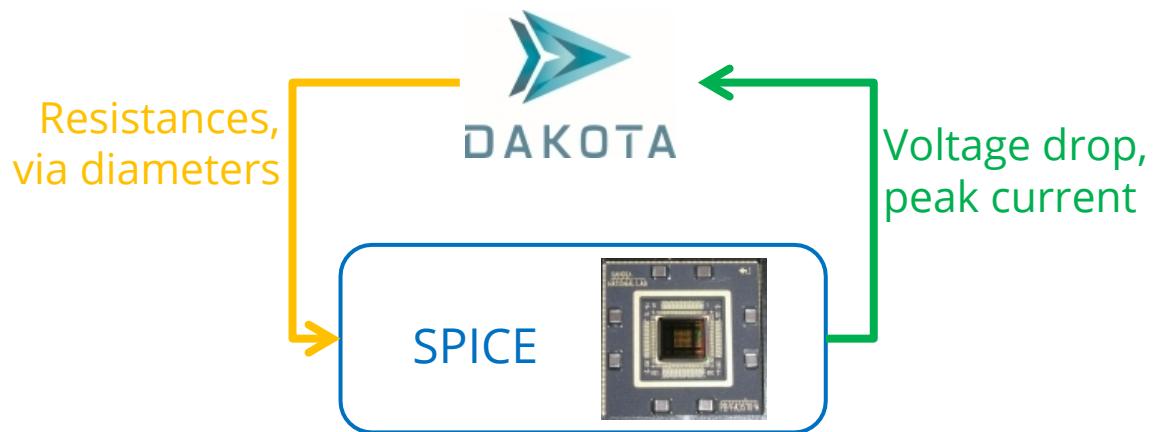
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# What is Dakota?



Open-source software for black-box, ensemble analysis of computational simulations

- Suite of iterative mathematical and statistical methods and a convenient means of interfacing with (just about) any simulation software
- Provides scientists, engineers, and decision makers greater insight into the predictions of their models via:
  - Global Sensitivity Analysis
  - Uncertainty Quantification
  - Optimization
  - Calibration
- Production and Research focus
- Works on desktops and HPCs and the major operating systems (\*nix, OS X, Windows)
- Command line interface, GUI, and API



# Capabilities



Common interface to established and cutting edge algorithms

## Sensitivity Analysis

- Designs: MC/LHS, DACE, sparse grid, one-at-a-time
- Analysis: correlations, scatter, Morris effects, Sobol indices

## Uncertainty Quantification

- MC/LHS/Adaptive Sampling
- MF/ML sampling and surrogates
- Reliability
- Stochastic expansions
- Epistemic methods

- Mixed aleatory/epistemic UQ
- Optimization under uncertainty

## Optimization

- Gradient-based local
- Derivative-free local
- Global/heuristics
- Surrogate-based

## Calibration

- Tailored gradient-based
- Use any optimizer
- Bayesian inference

- Parallel execution
- HDF5 Output
- Direct Python interface

Develop simulation driver once; use in different kinds of studies

# Multifidelity and Multilevel UQ Methods

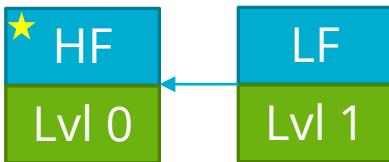


Exploit hierarchies of models to compute lower variance estimates of moments at lower cost

- Dakota 6.10 (May '19) included Control Variate Monte Carlo (CVMC), Multilevel (ML)MC, and MLCV MC.

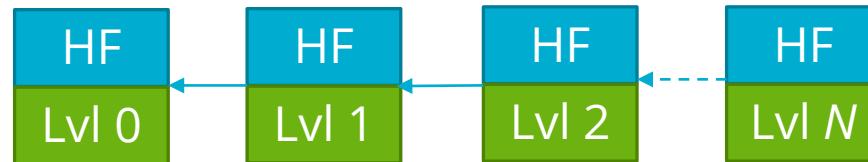
## Multifidelity Hierarchy

Predictions of lower fidelity models are biased, regardless of model resolution

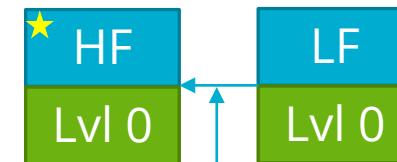


### CVMC

High and Low Fidelity  
(LF prediction is biased)



**MLMC**  
Multiple model resolutions  
(Prediction converges as  
resolution is improved)



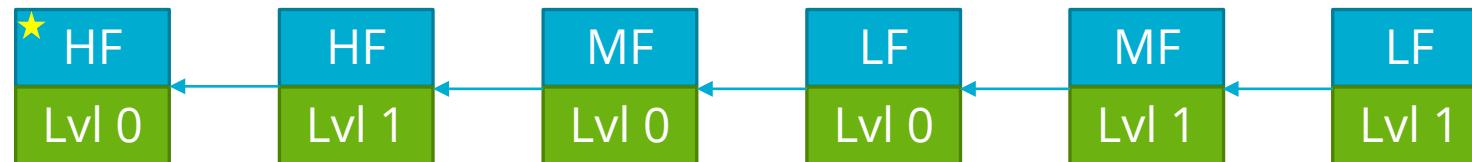
**MLCV MC**  
(2D hierarchy)

# Multifidelity and Multilevel UQ Methods



## Lifting Restrictions on Model Hierarchies

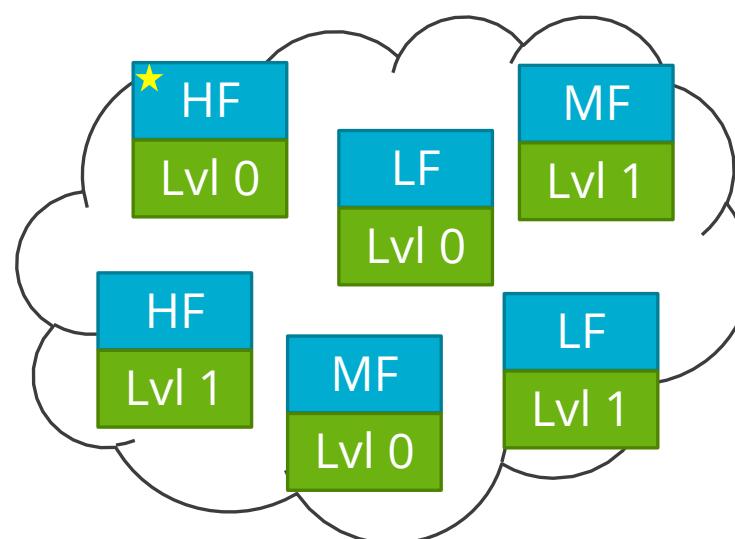
### Multifidelity Monte Carlo - 6.15 (Nov '21)



1D hierarchy of models of unlimited depth; convergence requirement lifted

### Approximate Control Variate – 6.15 (Nov '21)

- “Cloud” of models; no hierarchy assumed
- Recursion limit on variance reduction  $(1 - \rho^2)$  is lifted



# Multifidelity and Multilevel UQ Methods



## Other Recent Algorithmic and Usability Improvements

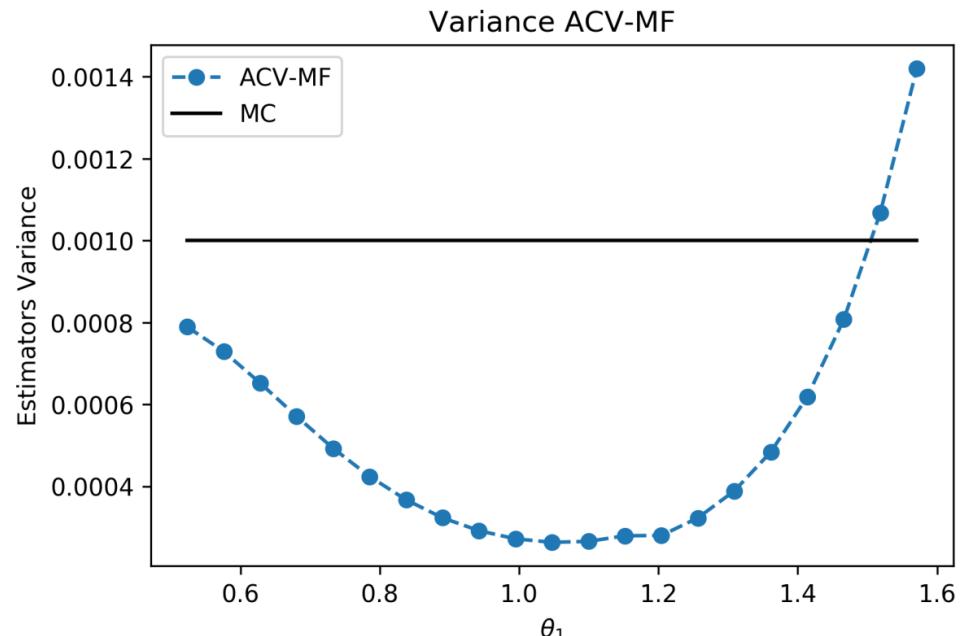
### Pilot Projection - 6.16 (May '22)

Which estimator (CVMC, MLMC, ACV, etc) provides the greatest variance reduction at the least cost?

Geraci/Reuter's talk: *Multifidelity UQ workflows with Dakota's graphical user interface*

### Model Tuning - 6.16 (May '22)

Tune solution level to achieve the best variance reduction and cost



Mike Eldred's talk: *Model tuning for multifidelity sampling in Dakota*

# Batch Parallel Efficient Global Optimization (EGO)



Efficiently use parallel computing resources to perform global optimization

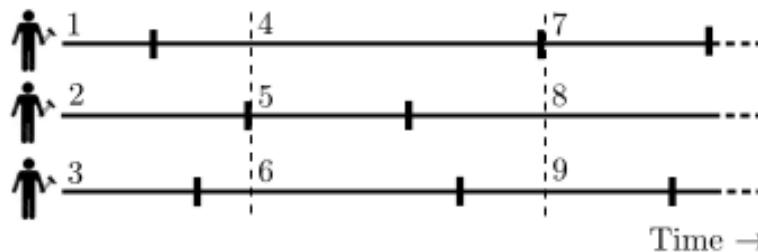
EGO uses the mean and variance prediction of a Gaussian process to balance exploration and exploitation

## Original EGO Algorithm

1. Train a GP on an initial set of samples.
2. Identify candidate:  $\underset{u}{\operatorname{argmax}} EI(\hat{G}(u))$ , where  $EI(\hat{G}(u)) \equiv \mathbb{E}[\max(\hat{G}(u^*) - \hat{G}(u), 0)]$
3. Evaluate candidate using the truth model; incorporate into the GP's training set
4. If not converged, go to 2.

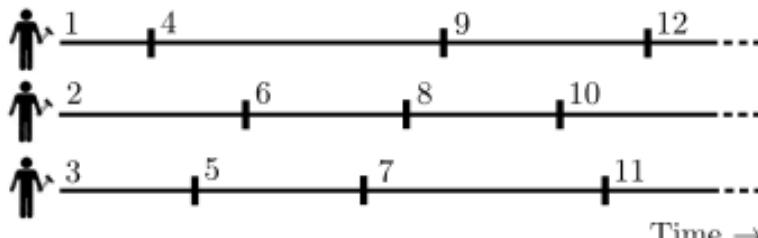
## Improvement 1 - 6.12 (May '20)

*Batch Sequential EGO.* Instead of a single point, batches are added. The additional points are based on *hallucination*.



## Improvement 2 - 6.14 (May '21)

*Batch Parallel EGO.* Evaluations and updates to the GP occur asynchronously.



# Surrogates Library



## Refresh and modularize Dakota's Surrogate Modeling Capabilities

Key Features of Dakota's new surrogate library:

- Export models from and import back into Dakota

```
model
  id_model = 'SurrogateModel'
  surrogate global
    dace_method_pointer = 'DesignMethod'
  experimental_gaussian_process
    export_model
      filename_prefix 'morris'
      formats binary_archive
    export_approx_variance = 'dak_gp_variances.dat'
```

- Python binding
- Rewritten Gaussian process and polynomial models

```
[4]: import dakota.surrogates as daksurr

nugget_opts = {"estimate nugget": True}
trend_opts = {
    "estimate trend": True,
    "Options": {"max degree": 2}
}

config_opts = {
    "kernel type": "squared exponential",
    "scaler name": "standardization",
    "Nugget": nugget_opts,
    "num restarts": 15,
    "Trend": trend_opts
}

gp = daksurr.GaussianProcess(xs, ys, config_opts)
gp_value = gp.value(ps)
gp_variance = gp.variance(ps)
gp_grad = gp.gradient(ps)
gp_hessian = [gp.hessian(p)[0, 0] for p in ps] >
```

# Examples Library



Dakota includes a large and growing collection of runnable examples

- Examples include
  - Dakota inputs
  - Drivers
  - Jupyter notebooks
  - Case studies
  - Tutorials
- Consistent Presentation
- Routinely Tested
- Included with Dakota downloads
- Soon to be a part of our unified documentation

## Summary

Import a Python module into Dakota to use a decorated function it contains as a driver

## Description

This example combines use of the Dakota direct python callback interface together with use of the `dakota.interfacing` Python module provided by Dakota to transparently convert from the incoming Python dictionary to Parameters and Response objects native to `dakota.interfacing`. This is done using an idiom supported in Python known as a decorator factory. More specific details for both the direct python callback in Dakota and the `dakota.interfacing` module can be found in the `linked` and `di` examples that are peers to this one.

## Driver

The main function of the direct Python callback driver `driver.py` is:

```
@di.python_interface()
def decorated_driver(params, results):

    textbook_input = pack_textbook_parameters(params, results)
    fns, grads, hessians = textbook_list(textbook_input)
    results = pack_dakota_results(fns, grads, hessians, results)

    return results
```

Prior to this snippet, the driver imports the `dakota.interfacing` module as `di`, and the actual function, gradient and hessian calculations are brought in from the `textbook` module.

The Python decorator is invoked by using the Python convention of the `@` followed by the



# On the horizon..

## Dakota's repositories will move to GitHub

- More easily explore and work with Dakota source
- Create and track feature requests and bug reports
- User support will move to GitHub Discussions



**GitHub**

## New Documentation System

**Rosenbrock Test Problem**

The Rosenbrock function is a common test problem for Dakota examples. This function has the form:

$$f(x_1, x_2) = 100(x_2 - x_1^2)^2 + (1 - x_1)^2$$

Shown below is a three-dimensional plot of this function, where both  $x_1$  and  $x_2$  range in value from  $-2$  to  $2$ ; also shown below is a contour plot for Rosenbrock's function.

