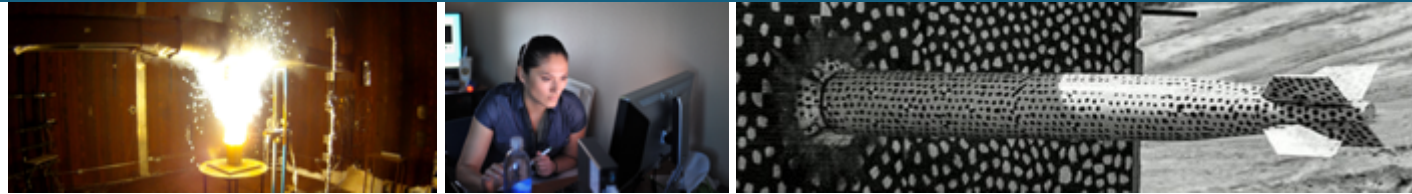




# Pseudo-Two-Dimensional Modeling of Lithium-Ion Conversion Cathode Materials



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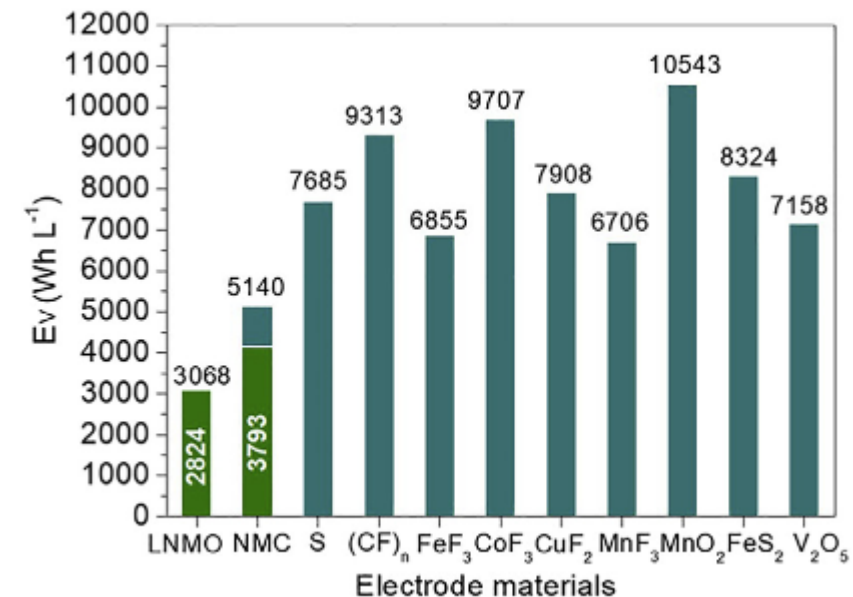
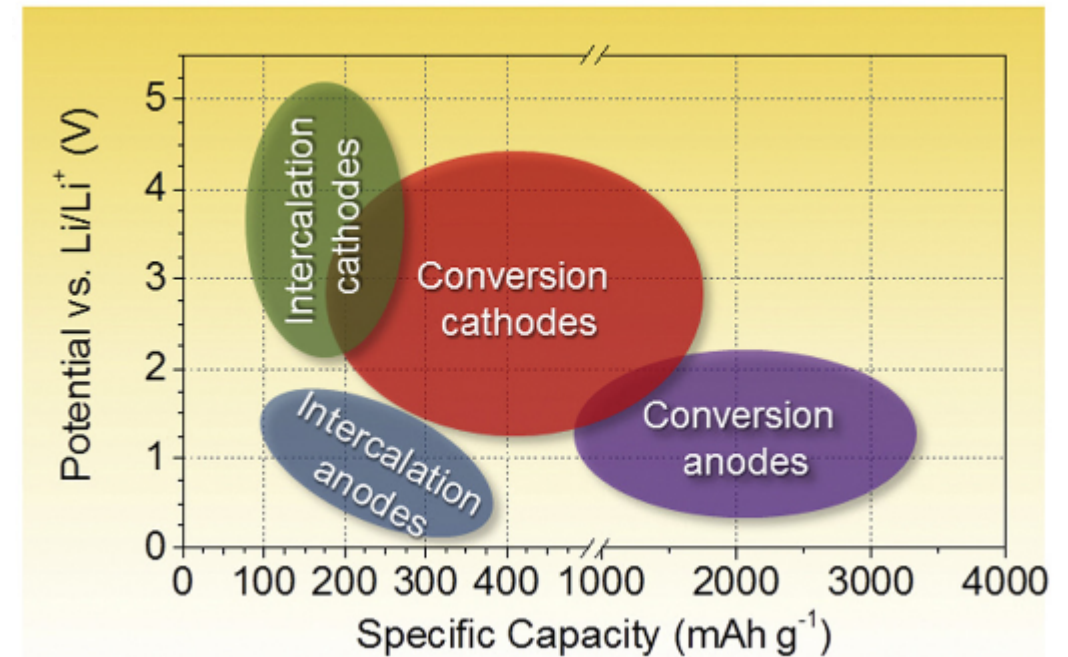
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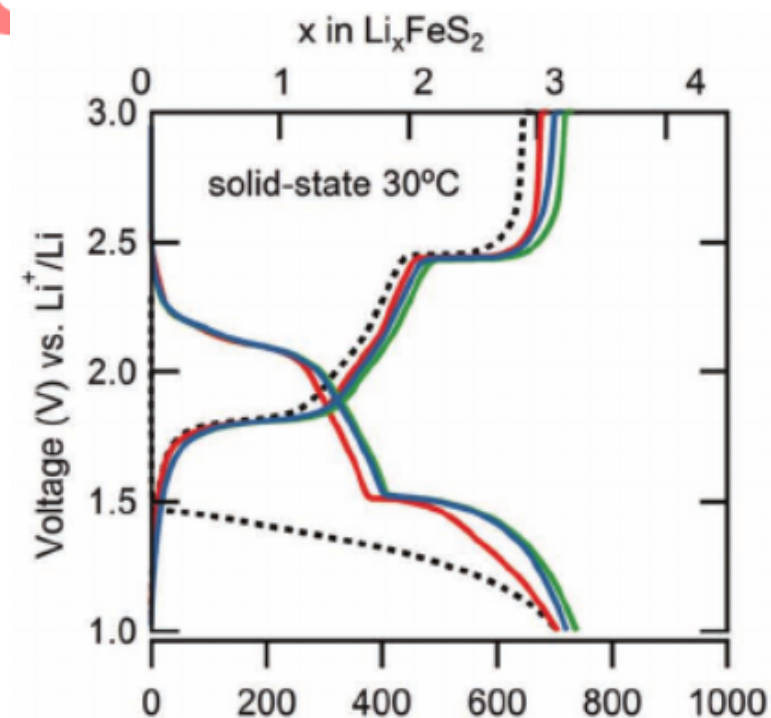
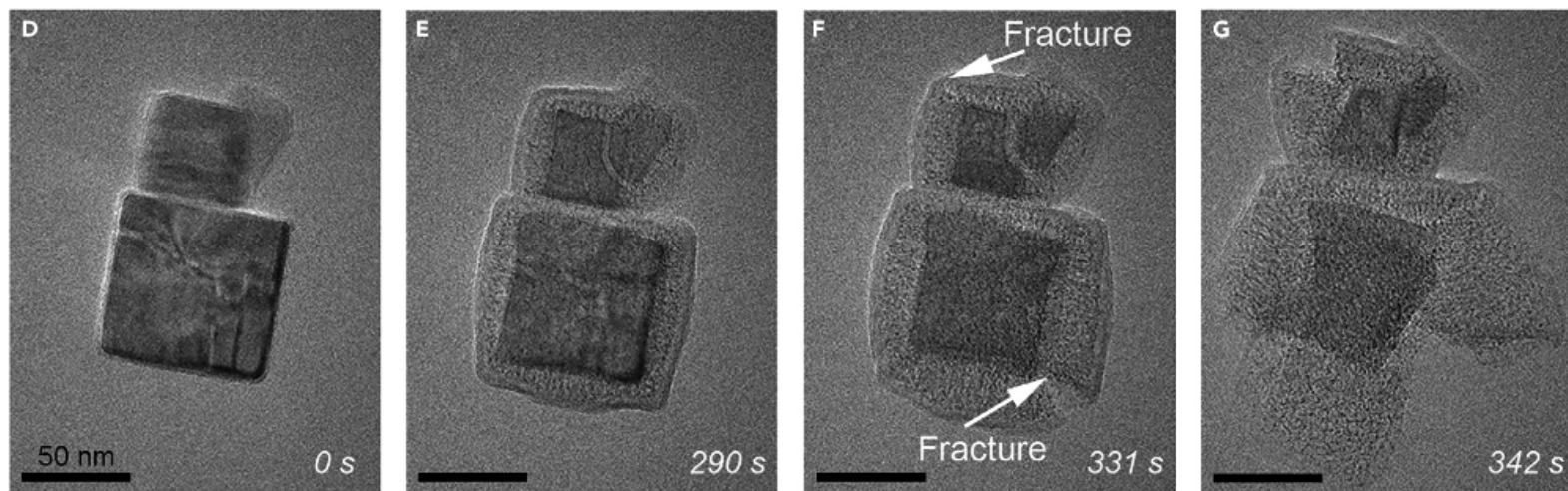
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# Conversion Cathode Materials

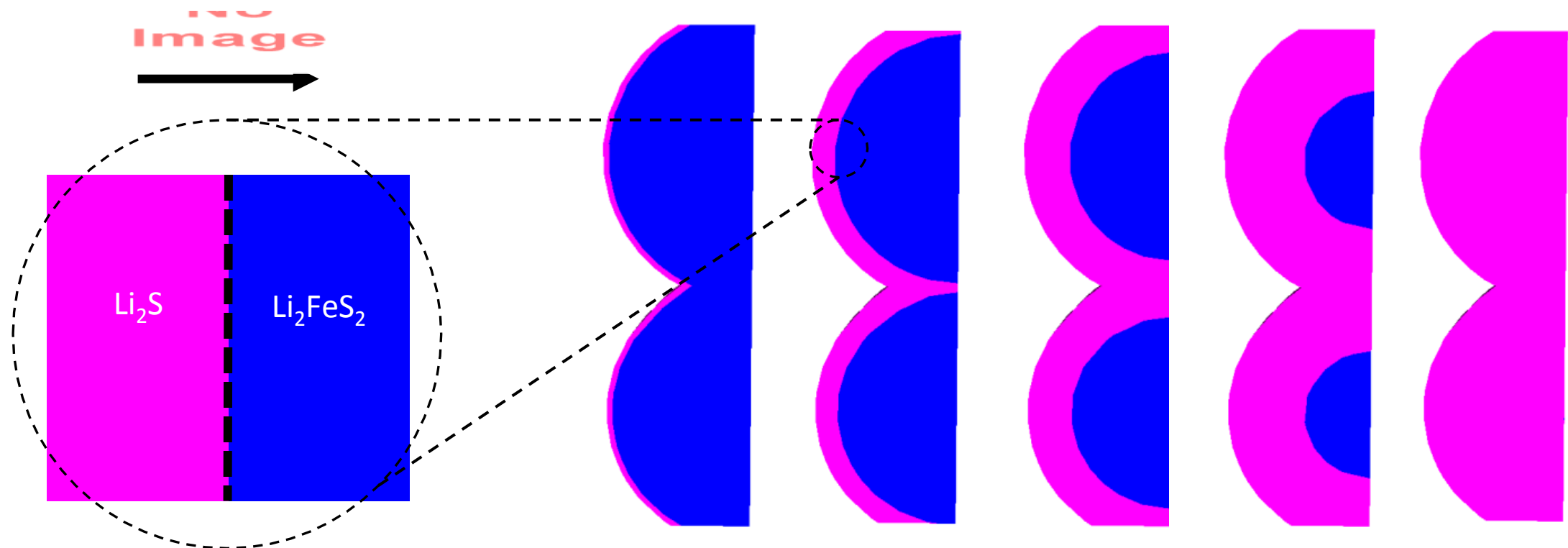
- Next-generation rechargeable batteries demand increased energy and power density
- Conversion cathode materials undergo a chemical reaction to produce new products
- Typically contain more abundant and safer materials
- Due to the complexity of the reactions, these materials are not fully understood



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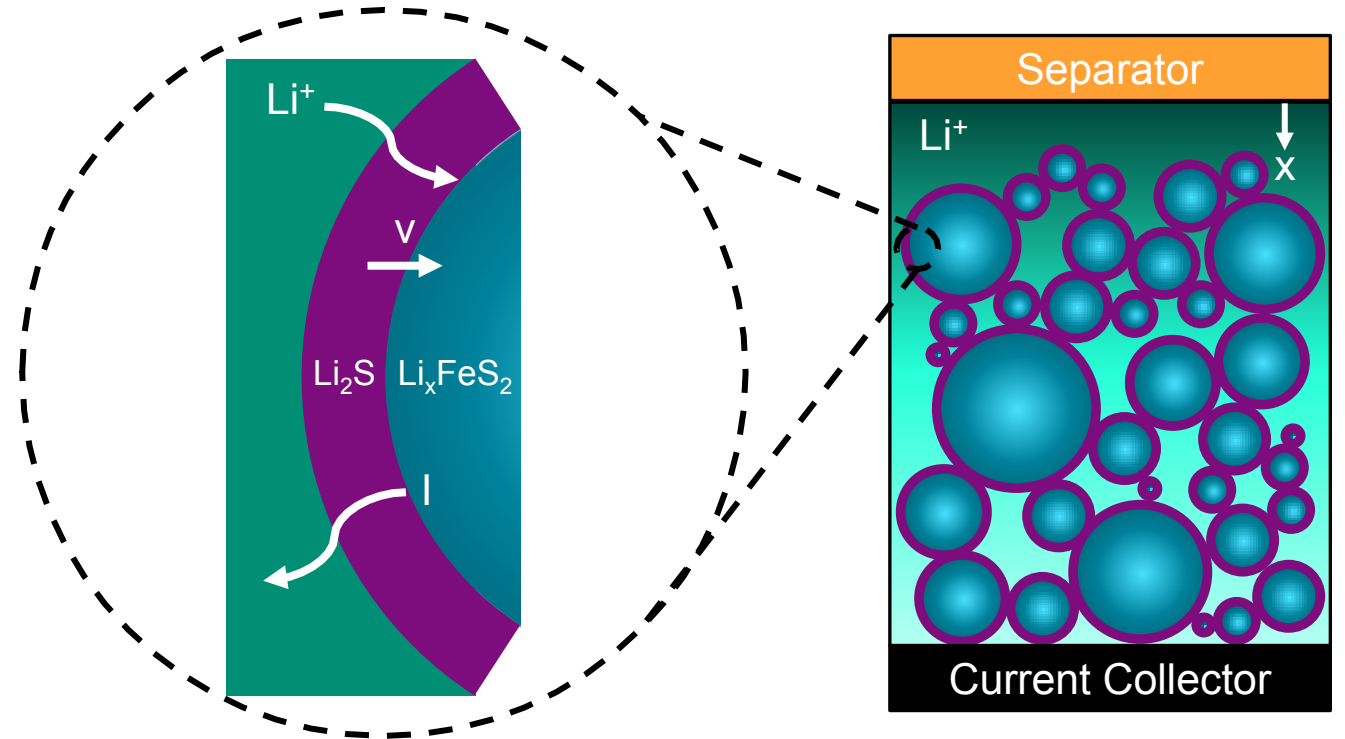
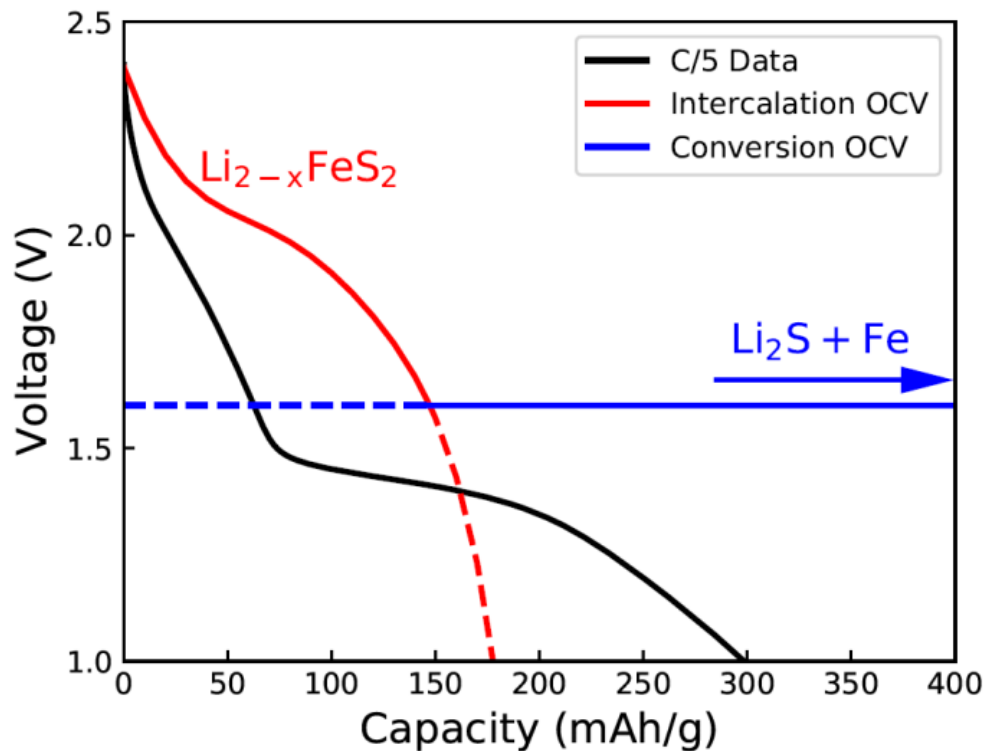




# Pseudo-Two-Dimensional (P2D) Model



- Large mesoscale simulations can be computationally expensive and difficult to run
- We can simplify the process through an adapted pseudo-two-dimensional approach which considers relevant transport both on the electrode and particle scales



# Model Equations and Variables



- Used adapted Doyle-Fuller-Newman (DFN) half-cell model with non-ideal transport for the intercalated lithium and an additional equation that tracks the shell thickness
- The presence of the shell affects the solid potential, electrolyte potential and lithium-ion concentration at the reaction surface as well as the overall electrode conductivity

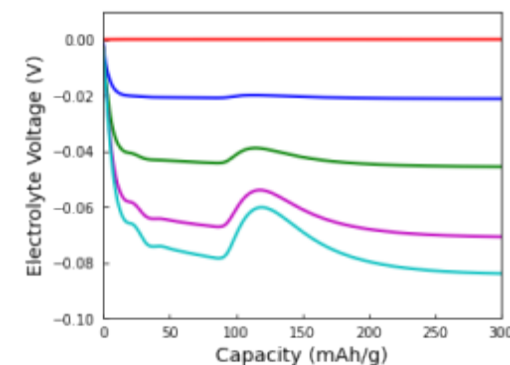
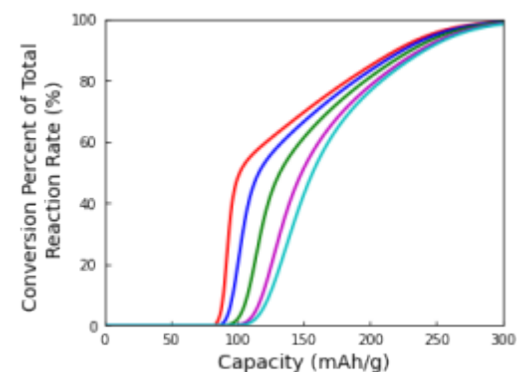
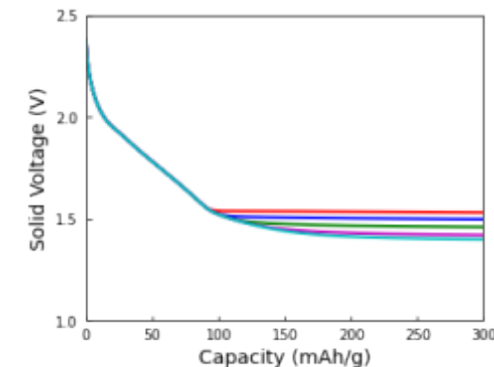
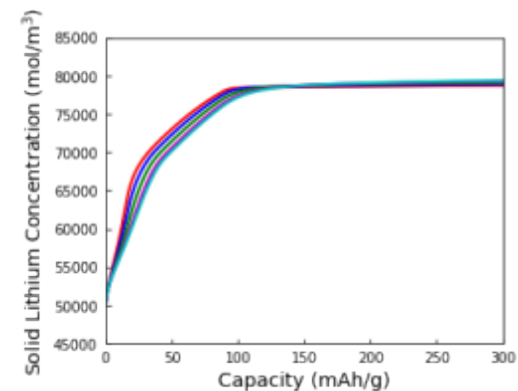
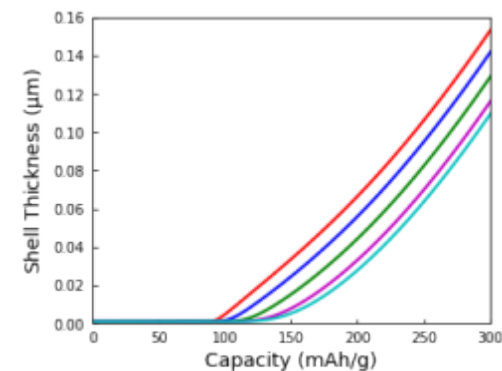
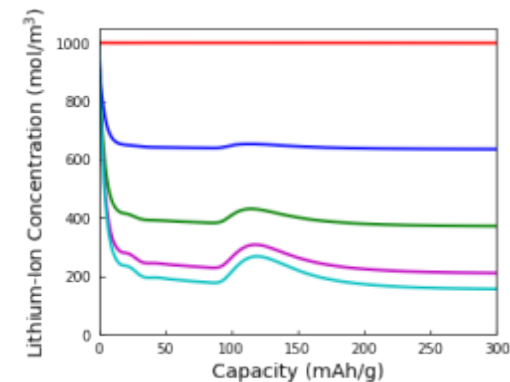
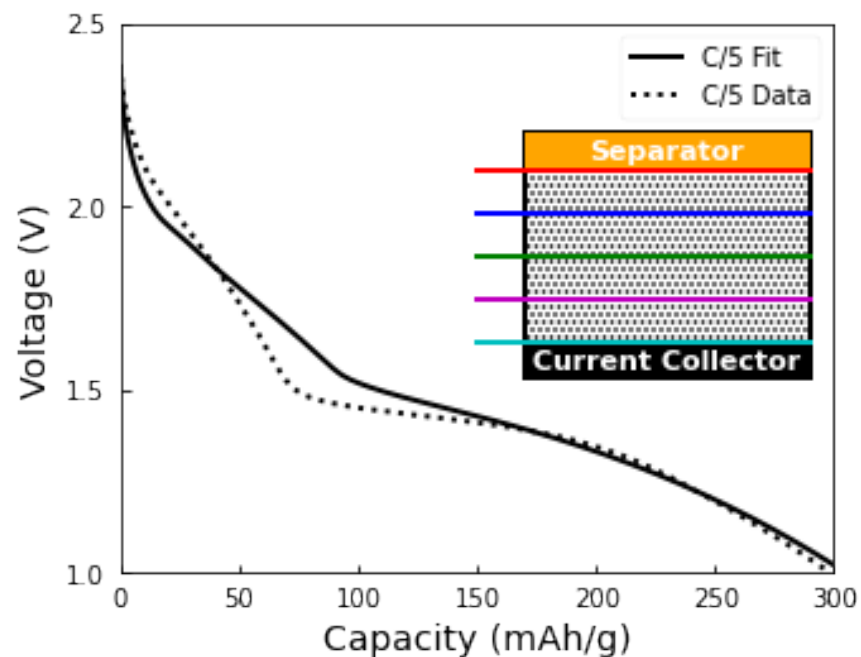
## Equations

## Variables

Electrode Potential:	$\frac{\partial}{\partial x} \left( (1 - \epsilon)^b \kappa_{eff} \frac{\partial V_s}{\partial x} \right) = aFj$	Effective Electrode Conductivity:	$0 = \sum_i \phi_i \frac{\kappa_i - \kappa_{eff}}{\kappa_i + 2\kappa_{eff}}$
Electrolyte Potential:	$\frac{\partial}{\partial x} \left[ \epsilon^b \kappa_l \left( \frac{\partial V_l}{\partial x} - (1 - t_+) \frac{2RT}{FC_{Li^+}} \frac{\partial C_{Li^+}}{\partial x} \right) \right] = -aFj$	Inner Solid Potential:	$V_{s,in} = V_{s,out} - \frac{jFR_c^2}{\kappa_{shell}} \left( \frac{1}{R_c} - \frac{1}{R_p} \right)$
Electrolyte Concentration:	$\epsilon \frac{\partial C_{Li^+}}{\partial t} = \frac{\partial}{\partial x} \left[ \epsilon^b D_{Li^+} \frac{\partial C_{Li^+}}{\partial x} \right] + a(1 - t_+)j$	Inner Electrolyte Potential:	$V_{l,in} = V_{l,out} + \ln \left( \frac{C_{Li^+,in}}{C_{Li^+,out}} \right) \frac{RT}{F}$
Solid Concentration:	$\frac{\partial C_{Li}}{\partial t} = -\frac{1}{r^2} \frac{\partial}{\partial r} \left( r^2 \frac{D_{Li} F C_{Li}}{RT} \frac{\partial V_{Eq}}{\partial r} \right)$	Inner Lithium-Ion Concentration:	$C_{Li^+,in} = C_{Li^+,out} + \frac{jR_c^2}{2D_{shell}} \left( \frac{1}{R_c} - \frac{1}{R_p} \right)$
Shell Thickness:	$\frac{\partial \delta}{\partial t} = -\frac{j_{conv} M}{\rho z \left( 2 - \frac{C_{Li}}{C_{max}} \right)}$	Overpotential:	$\eta = V_{s,in} - V_{l,in} - V_{Eq}$

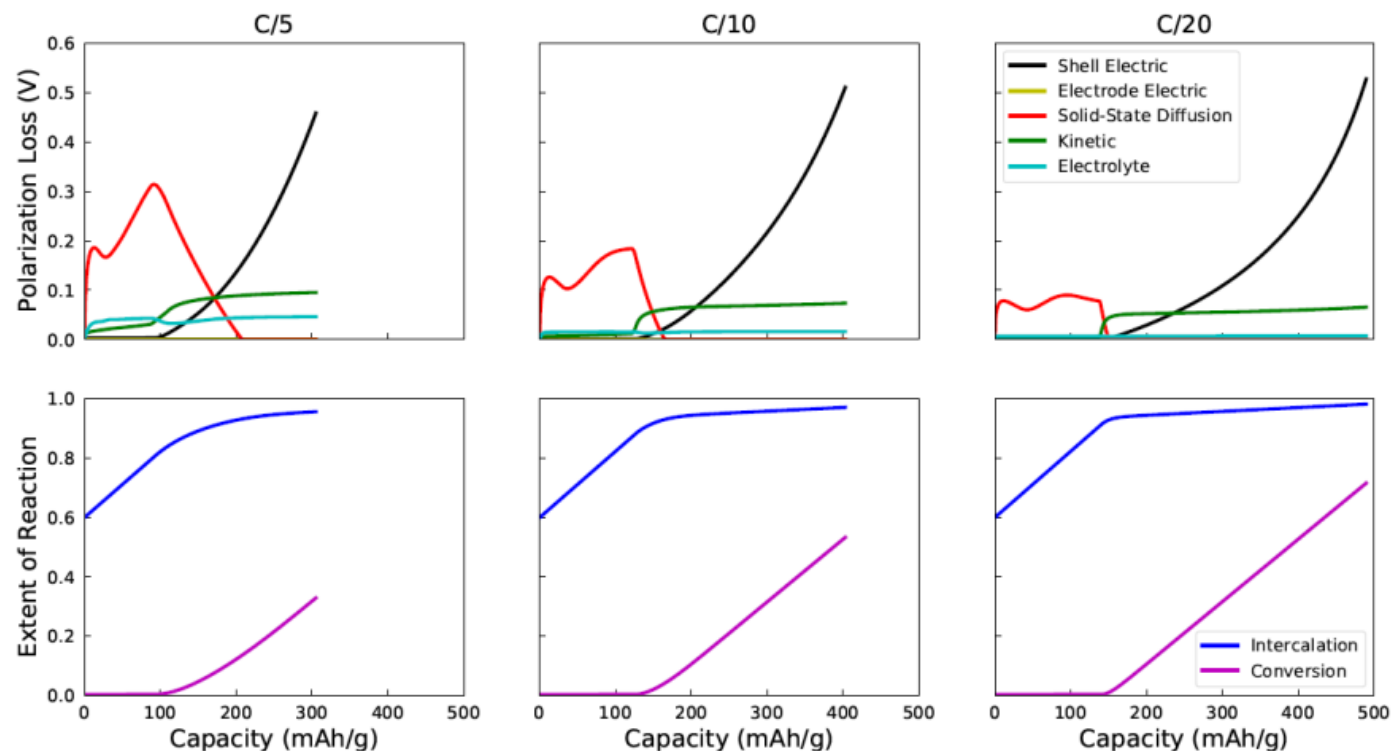
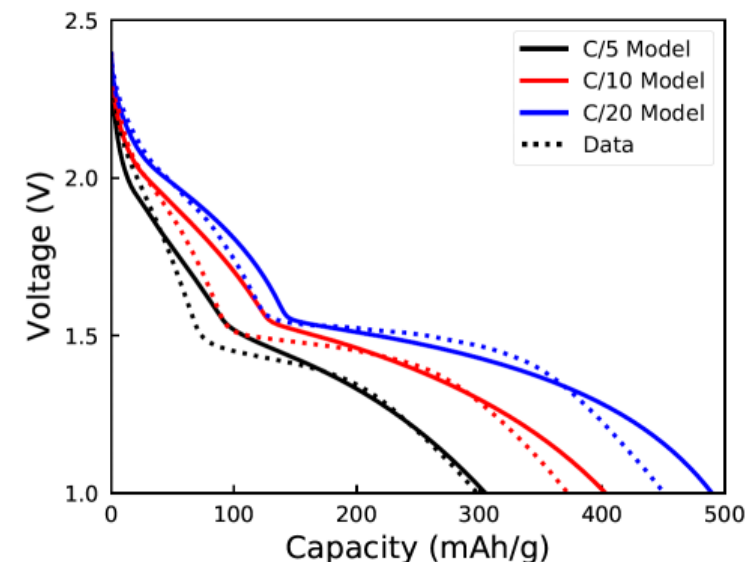
# P2D C/5 Model Results

- We fit the model to C/5 data to identify the remaining unknown transport parameters
- Quantities associated with the conversion reaction and the electrolyte exhibit polarization across the electrode



# Leading Loss Mechanisms

- The P2D model enables us to identify the leading loss mechanisms for the cell
- At slow c-rates, solid-state diffusion and shell electrical conductivity are the leading loss mechanisms
- At faster c-rates, additional losses including kinetic and electrical conductivity through the electrode become relevant

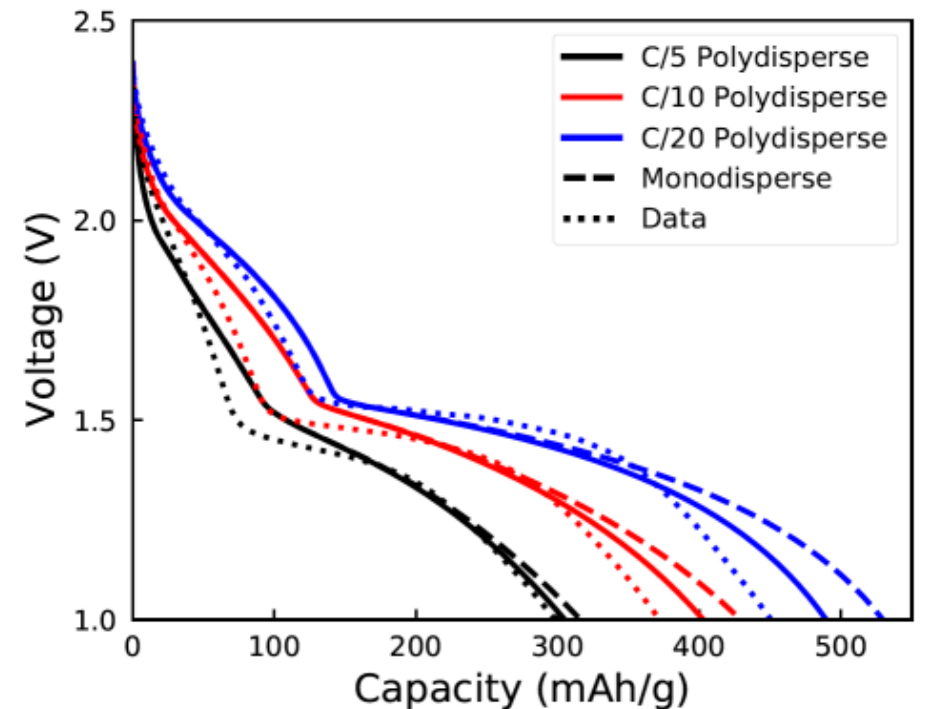
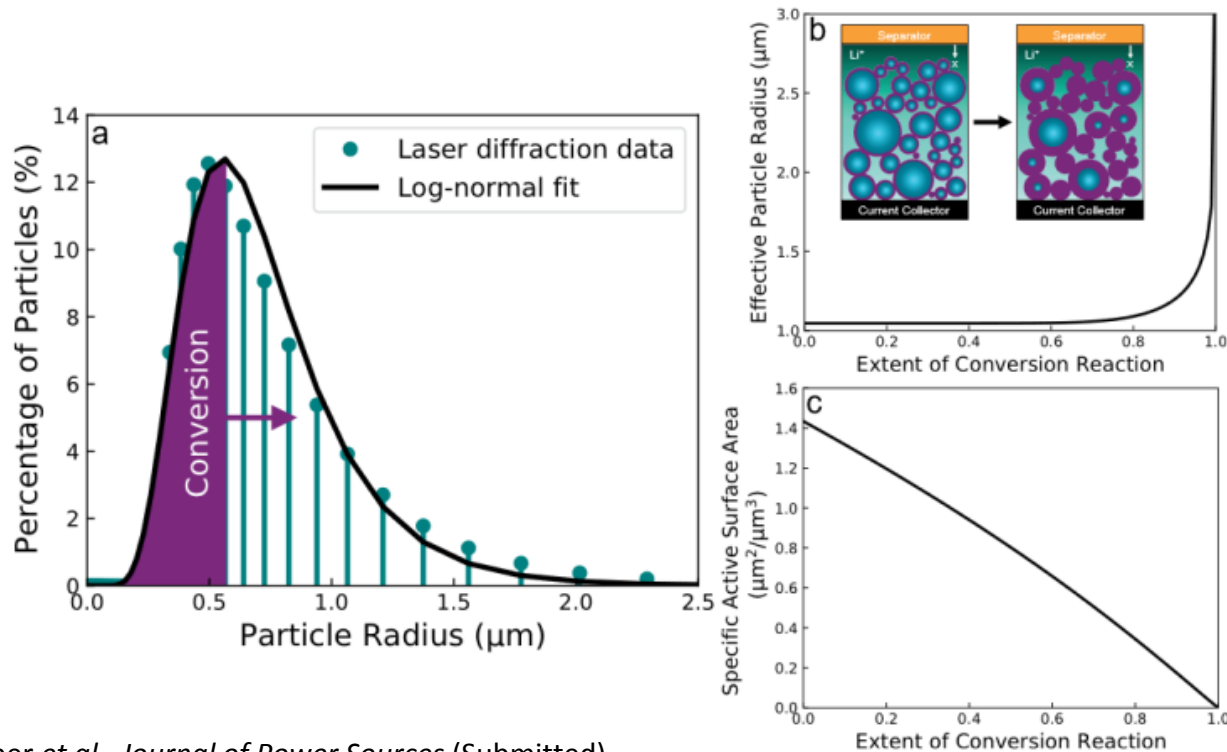




# P2D Model Polydispersity

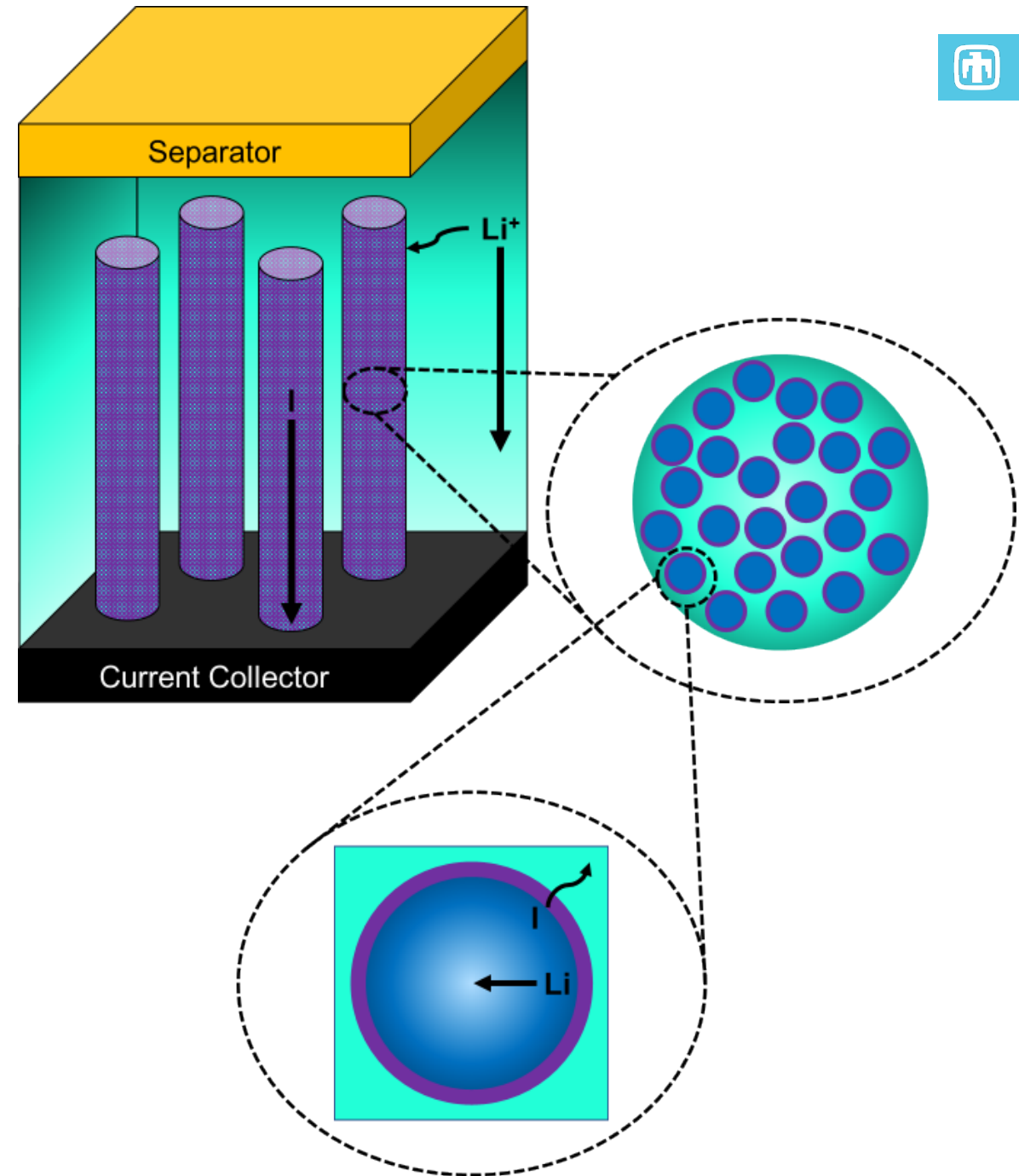
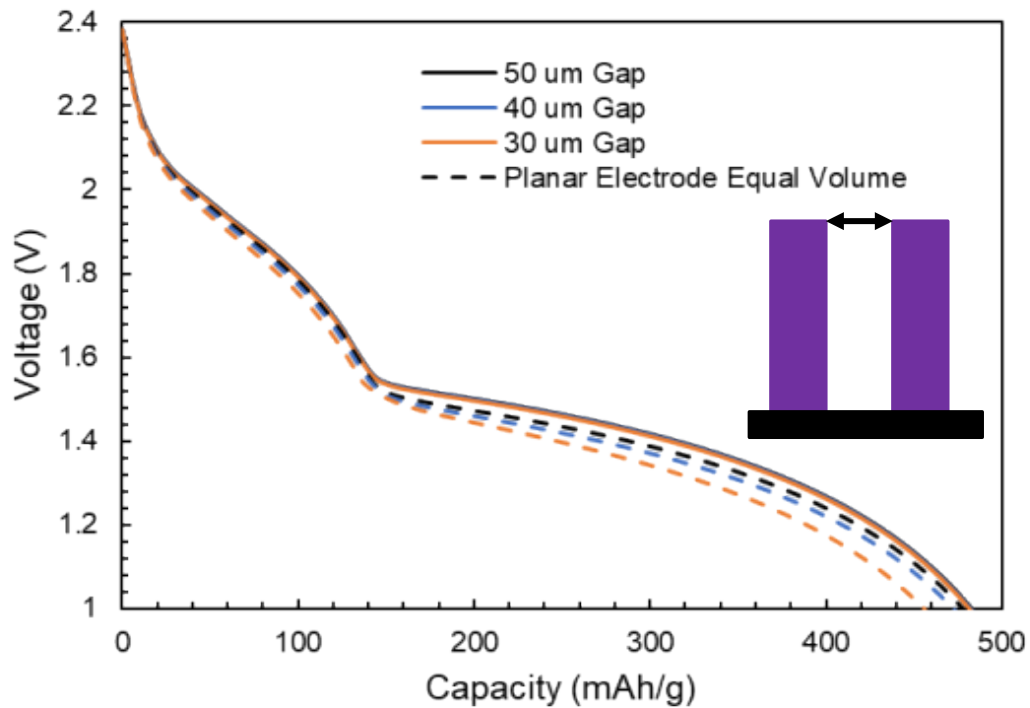


- We include polydispersity by introducing a variable effective particle radius and specific active surface area
- Inclusion of polydispersity results in a lower capacity in the conversion regime, particularly at slow c-rates, when compared to a single particle approach



# Three-Dimensional Electrodes

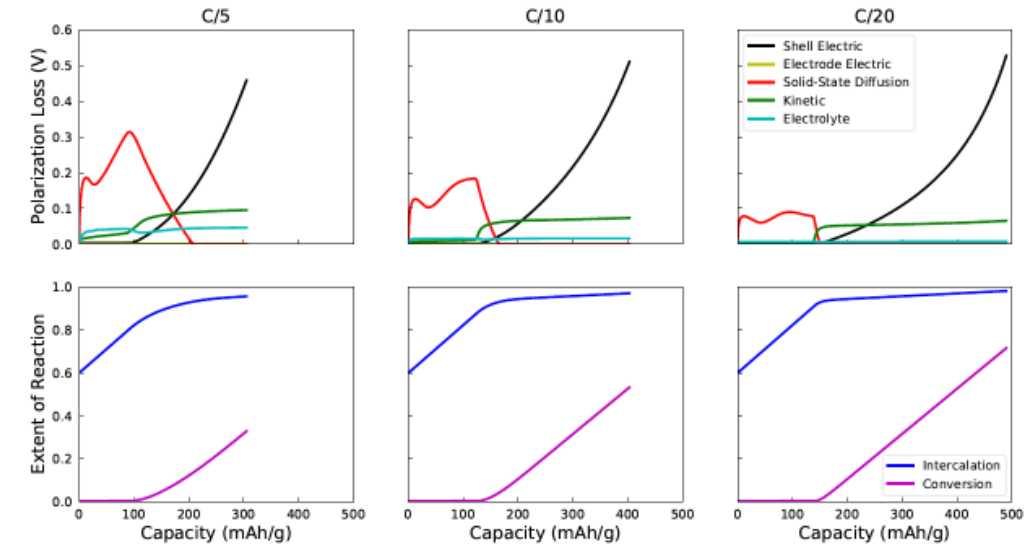
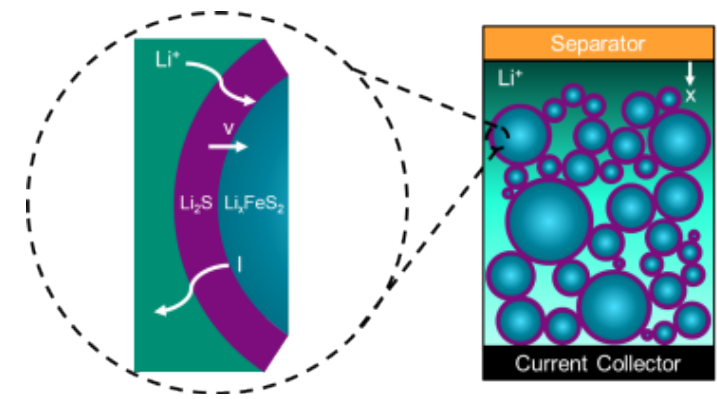
- Three-dimensional electrodes are intriguing due to their potential to outperform planar electrodes
- By extending the P2D approach to three-dimensional electrodes, we can validate this assertion for  $\text{FeS}_2$



# Conclusions and Acknowledgements

- We developed a polydisperse, P2D model to represent the full behavior of  $\text{FeS}_2$  during lithiation
- The model helped to identify solid-state diffusion and shell electrical conductivity as the leading loss mechanisms
- Incorporation of polydispersity led to decreased capacity in the conversion regime
- Thanks to:
  - Funding: Laboratory Directed Research and Development Program
  - David Ashby
  - Katharine Harrison
  - Ben Ng
  - Alec Talin

Horner et al., *Journal of Power Sources* (Submitted)



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