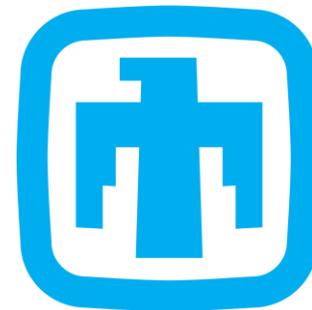
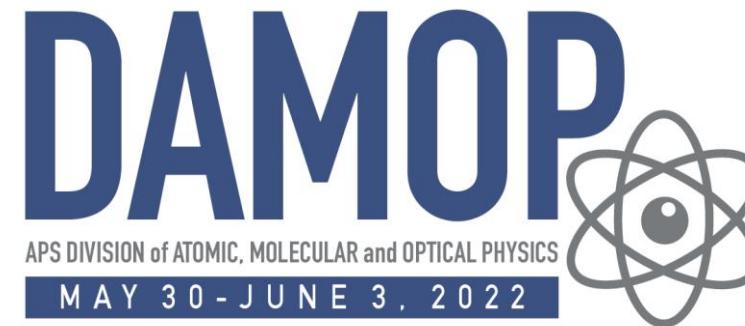


# Two-qubit Quantum Logic Gates for Neutral Atoms Based on the Spin-Flip Blockade



**Sandia  
National  
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**CQuIC**  
Center for Quantum  
Information and Control

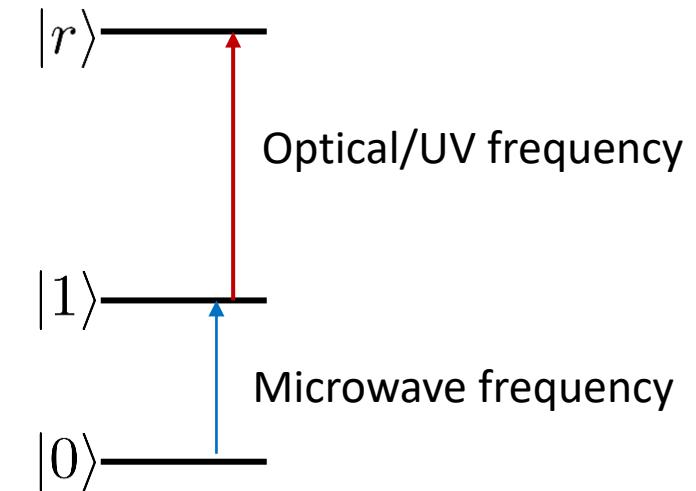
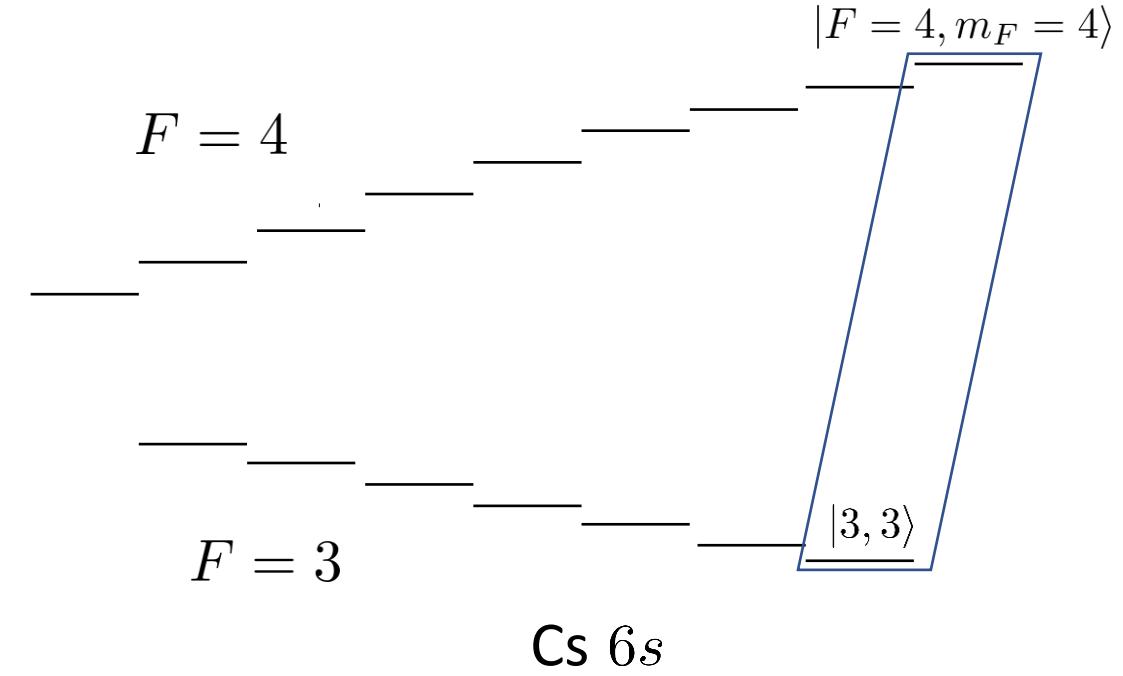
**Vikas Buchem mavari, Sivaprasad Omanakuttan,  
Yuan-Yu Jau, Ivan Deutsch**

# Cesium system

Motivation: Designing a high fidelity  
Entangling gate for Neutral atom qubits

Entanglement achieved via Rydberg  
states

$$H_{int} = V_{rr} |rr\rangle\langle rr|$$



—|rr⟩

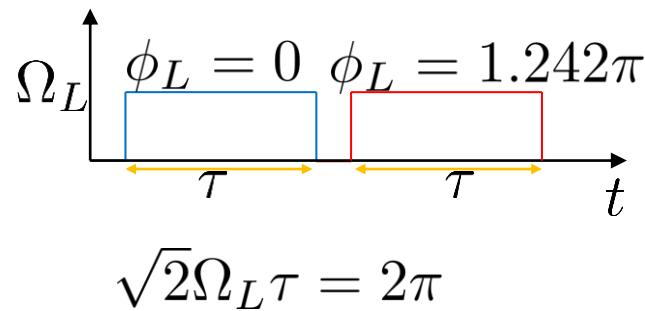
# Levine-Lukin gate – LL gate

—  
|00⟩

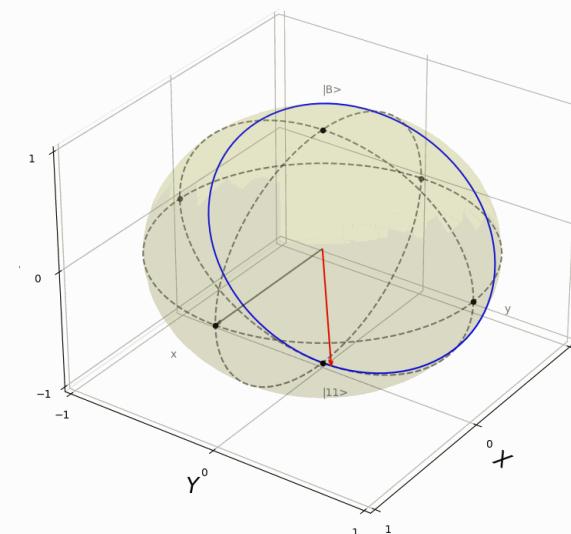
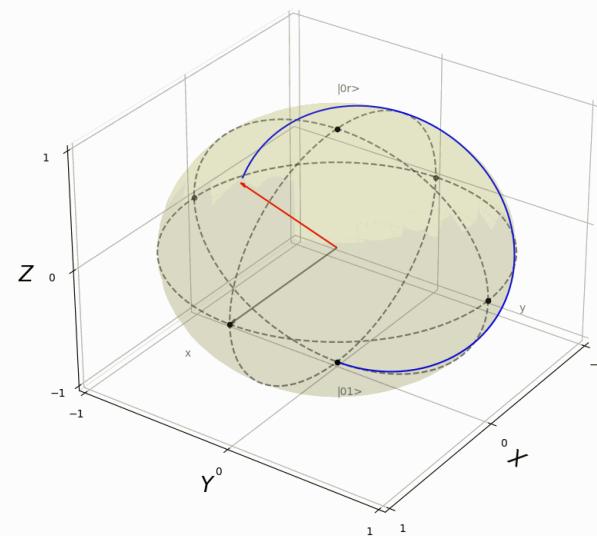
|0r⟩, |r0⟩  
—  
Δ<sub>L</sub>  
|01⟩, |10⟩  
Ω<sub>L</sub>, ϕ<sub>L</sub>

|B⟩ =  $\frac{|1r\rangle + |r1\rangle}{\sqrt{2}}$   
—  
Δ<sub>L</sub>  
|11⟩  
√2Ω<sub>L</sub>, ϕ<sub>L</sub>

|00⟩ → |00⟩  
|01⟩ →  $e^{i\alpha}|01\rangle$   
|10⟩ →  $e^{i\alpha}|10\rangle$   
|11⟩ →  $e^{i\beta}|11\rangle$

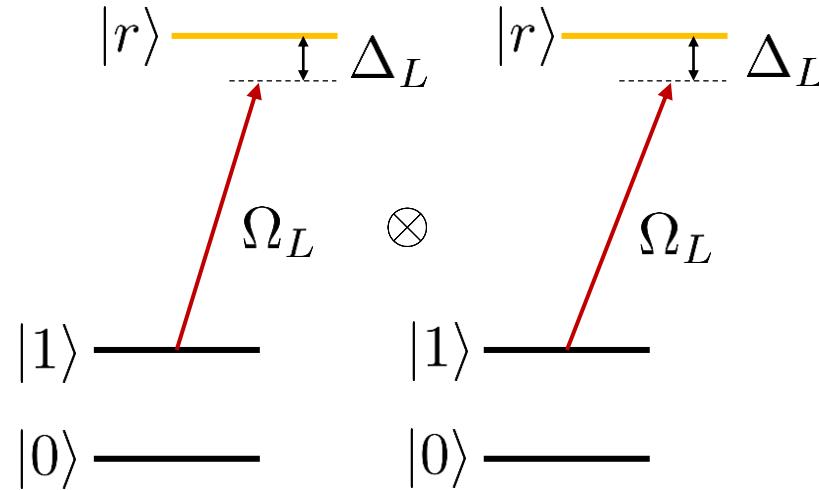


$$\Delta_L = 0.377\Omega_L \implies \beta - 2\alpha = \pi$$

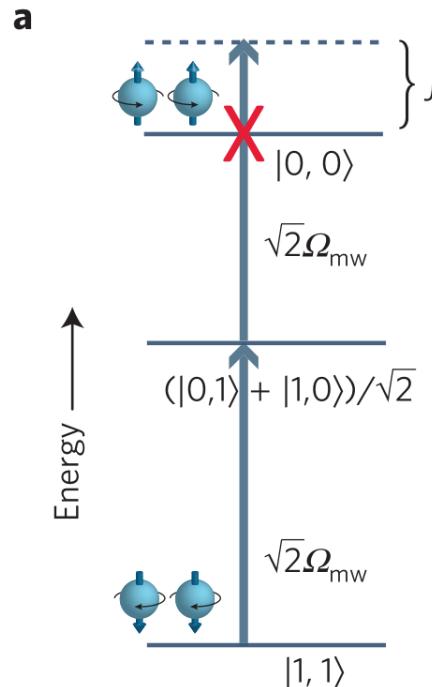
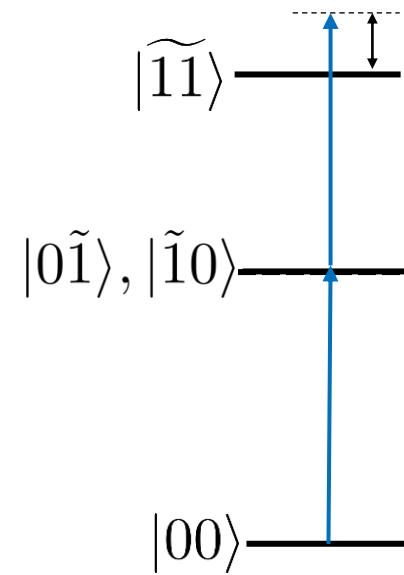


# Entangling atomic spins with a Rydberg-dressed spin-flip blockade

Y.-Y. Jau<sup>1,2</sup>, A. M. Hankin<sup>1,2</sup>, T. Keating<sup>1,2</sup>, I. H. Deutsch<sup>1,2</sup> and G. W. Biedermann<sup>1,2\*</sup>



$$\Rightarrow J = E_{LS}^2 - 2E_{LS}^1$$

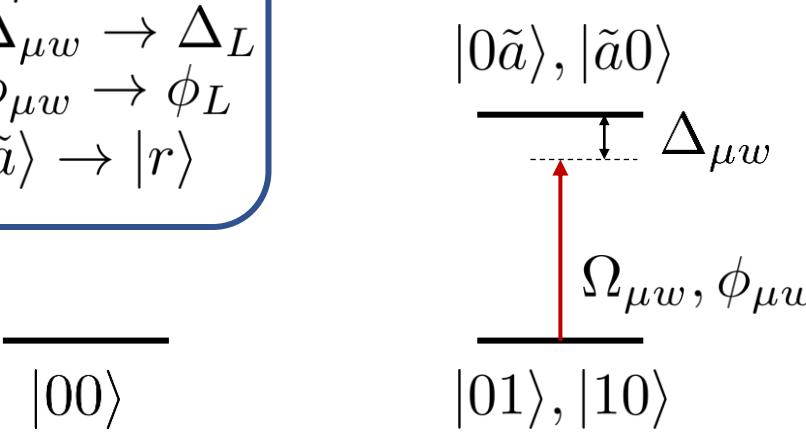


# LL gate in the hyperfine regime

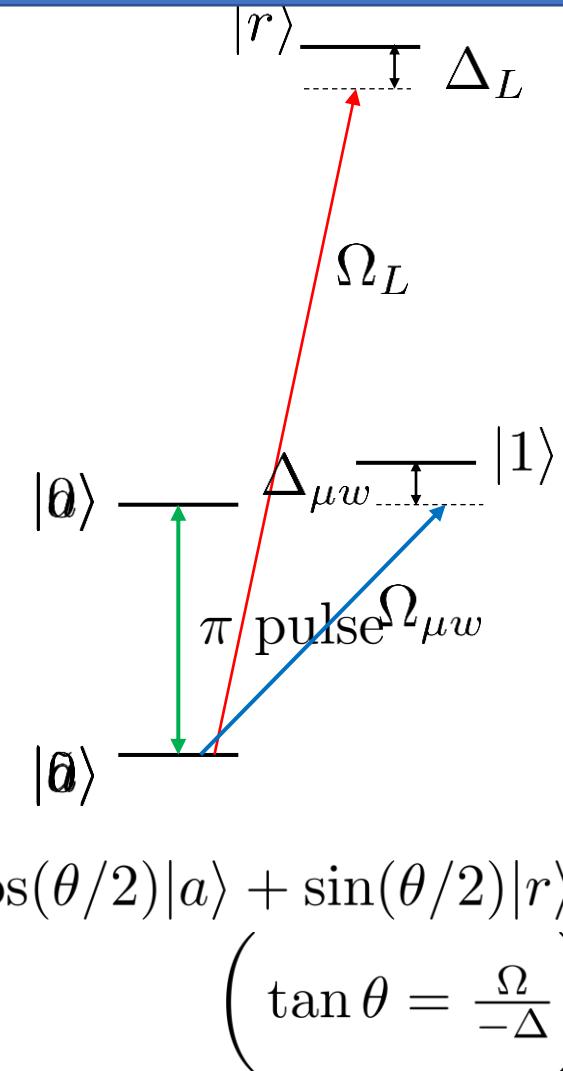
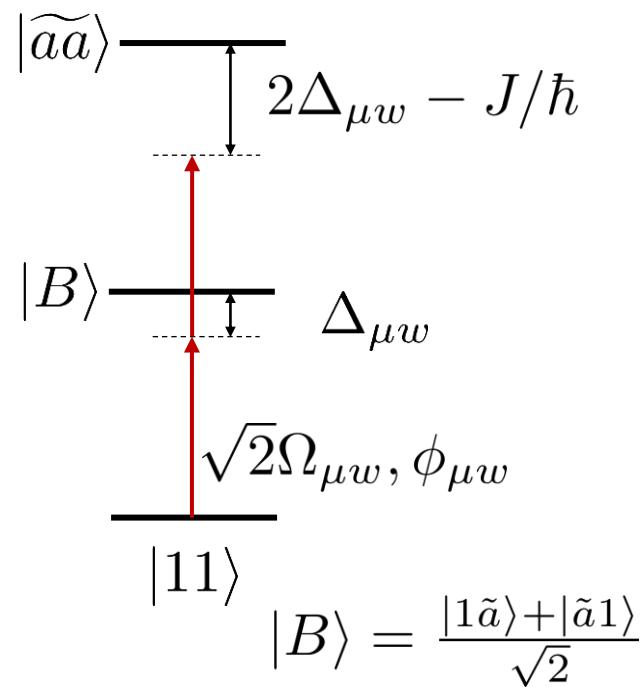
$$H_{hf}^1 = E_0|0\rangle\langle 0| + E_1|1\rangle\langle 1| + E_a|a\rangle\langle a|$$

$$H_{hf} = H_{hf}^1 \otimes \mathbf{1} + \mathbf{1} \otimes H_{hf}^1 + \textcolor{red}{J} |\widetilde{aa}\rangle\langle\widetilde{aa}|$$

$$\begin{aligned} J &\rightarrow V_{rr} \\ \Omega_{\mu w} &\rightarrow \Omega_L \\ \Delta_{\mu w} &\rightarrow \Delta_L \\ \phi_{\mu w} &\rightarrow \phi_L \\ |\tilde{a}\rangle &\rightarrow |r\rangle \end{aligned}$$



Jandura, Pupillo; arXiv:2202.00903 (2022)



$$\begin{aligned} J &\rightarrow V_{rr} \\ \Omega_{\mu w} &\rightarrow \Omega_L \\ \Delta_{\mu w} &\rightarrow \Delta_L \\ \phi_{\mu w} &\rightarrow \phi_L \\ |\tilde{a}\rangle &\rightarrow |r\rangle \end{aligned}$$

$J$  is much smaller than  $V$

If we aim for perfect blockade, our gates become much slower

Is there a way around this?

Yes! Quantum optimal control is the answer!

# Optimal Quantum control for the LL gate

We use Gradient Ascent Pulse Engineering (GRAPE)

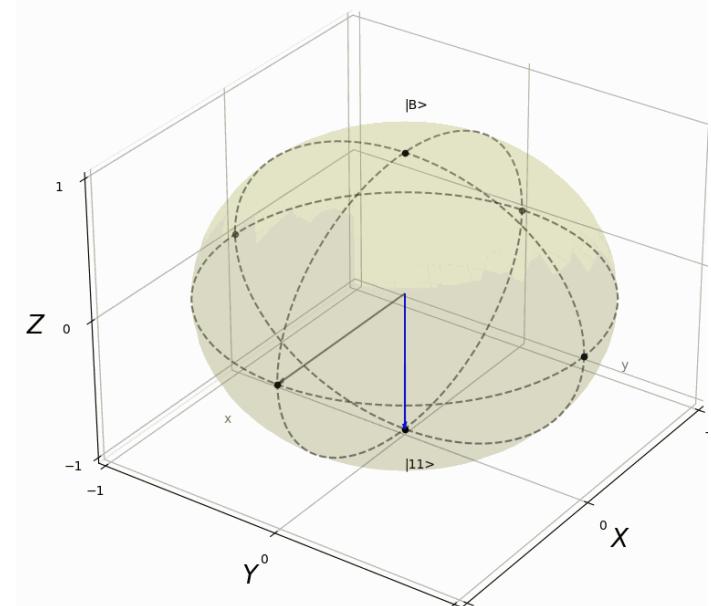
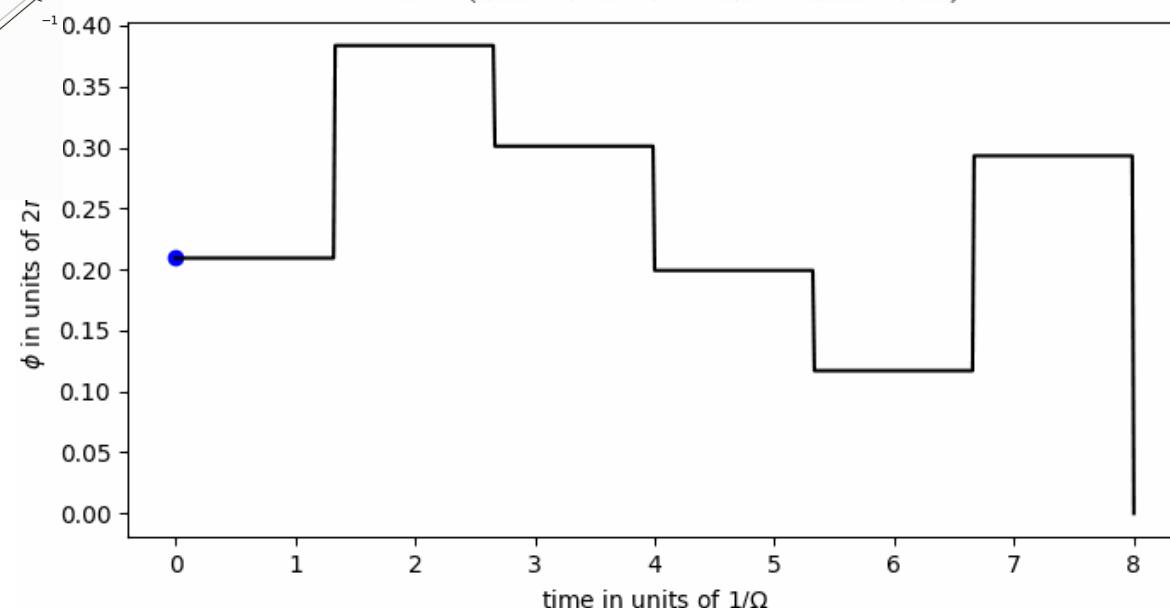
We maximize  $\mathcal{F}$  by using  $\vec{\nabla}_{\vec{\phi}} \mathcal{F}$ .

$$\mathcal{F} = \text{Tr}((\text{CZ})^\dagger U[\phi(t)])$$

$$\Delta_L = 0, \Omega_L = 1$$

$$\vec{\phi} = (\phi_1, \phi_2, \phi_3, \phi_4, \phi_5, \phi_6)$$

$$|01\rangle \rightarrow e^{i\phi_1} |01\rangle$$



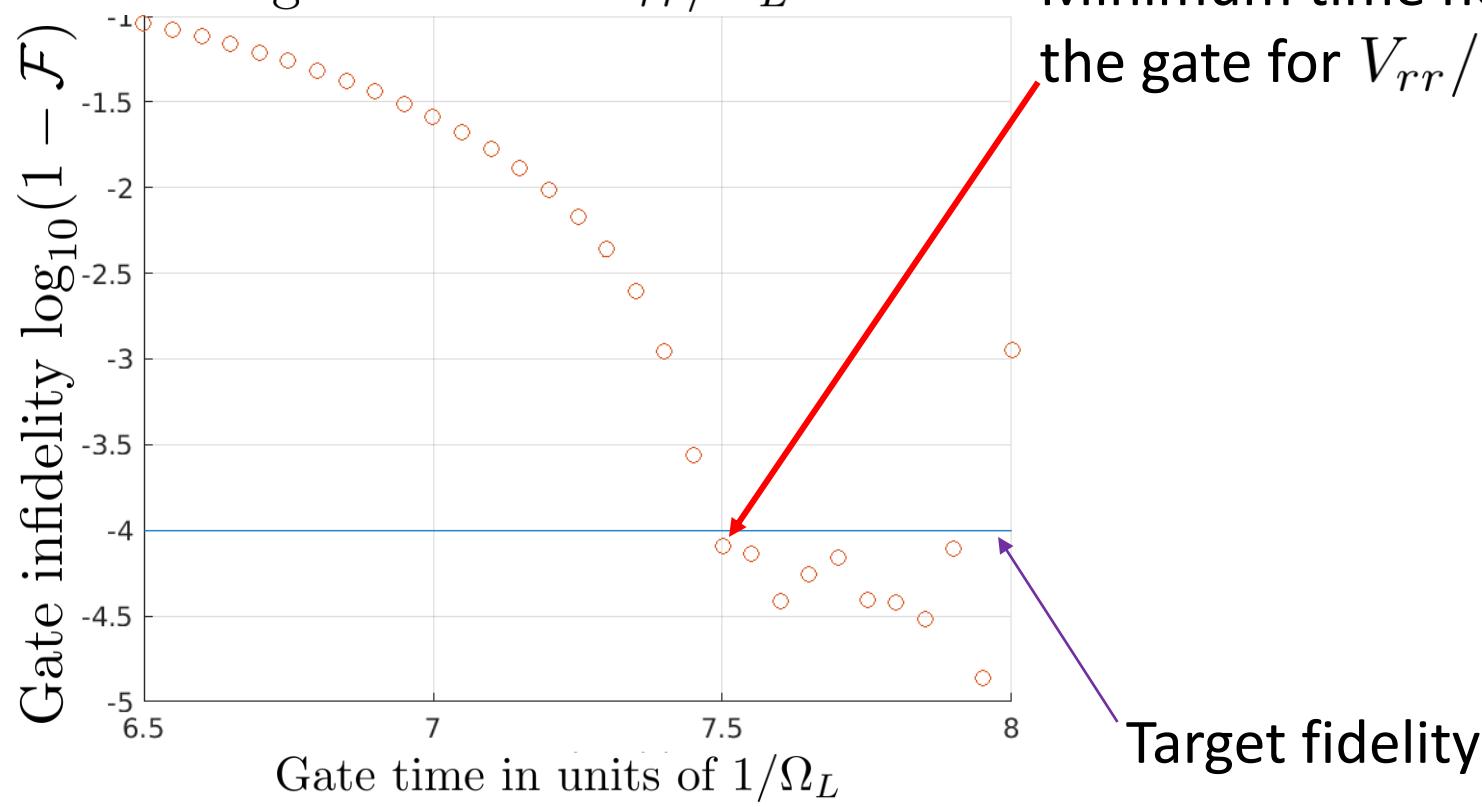
$$|11\rangle \rightarrow e^{i\phi_2} |11\rangle$$

$$\phi_2 - 2\phi_1 = \pi$$

# Quantum speed-limit

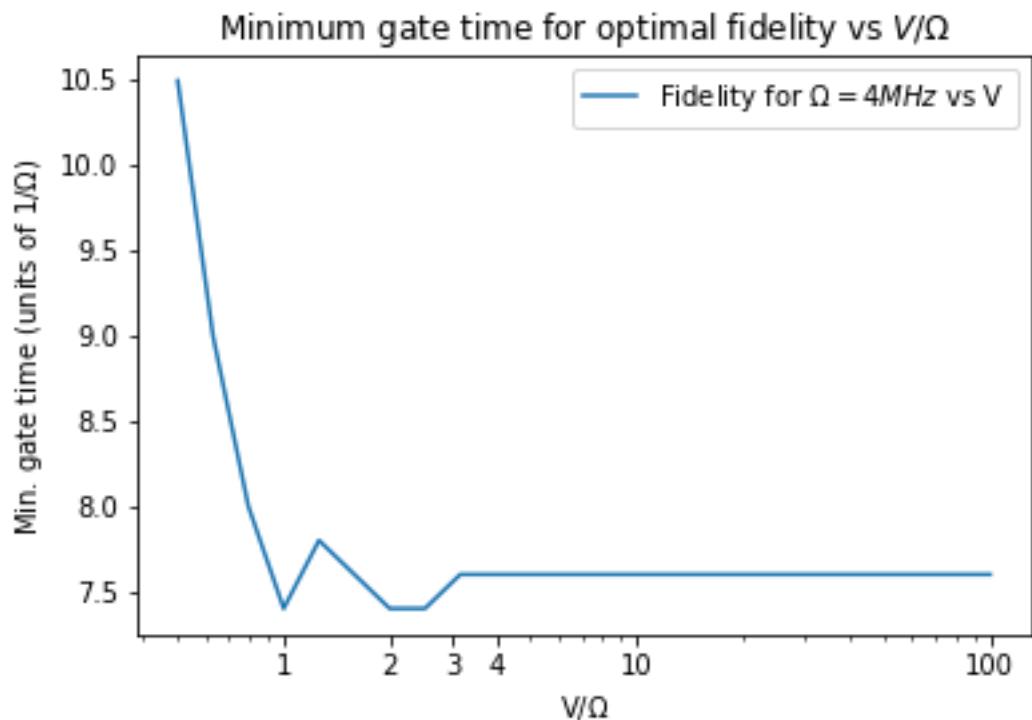
Infidelity of the Optimal control gate

vs gate time at  $V_{rr}/\Omega_L = 4$



Minimum time needed to implement  
the gate for  $V_{rr}/\Omega = 4$

# Some counterintuitive results!



Imperfect blockade doesn't slow down your gate too much! In fact, it can make it faster!

$$H = \frac{\Omega}{2}(\sigma_{\phi}^1 + \sigma_{\phi}^2) + \frac{V_{rr}}{2}(\sigma_z^1 \otimes \sigma_z^2 + \sigma_z^1 + \sigma_z^2)$$

Known result from Spin Quantum control!

$$J = \omega(J_x \cos \phi + J_y \sin \phi) + \kappa J_z^2$$

The fastest state preparation times arise when  $\kappa \sim \Omega$ .

-The cost: More population is pumped into  $|rr\rangle$

# Tunability of interaction strength

By changing our dressing parameters,  $\Delta_L, \Omega_L$

We can change  $J$  and the Rydberg character of the dressed states

$$P_{\tilde{a}} = |\langle r|\tilde{a}\rangle|^2$$

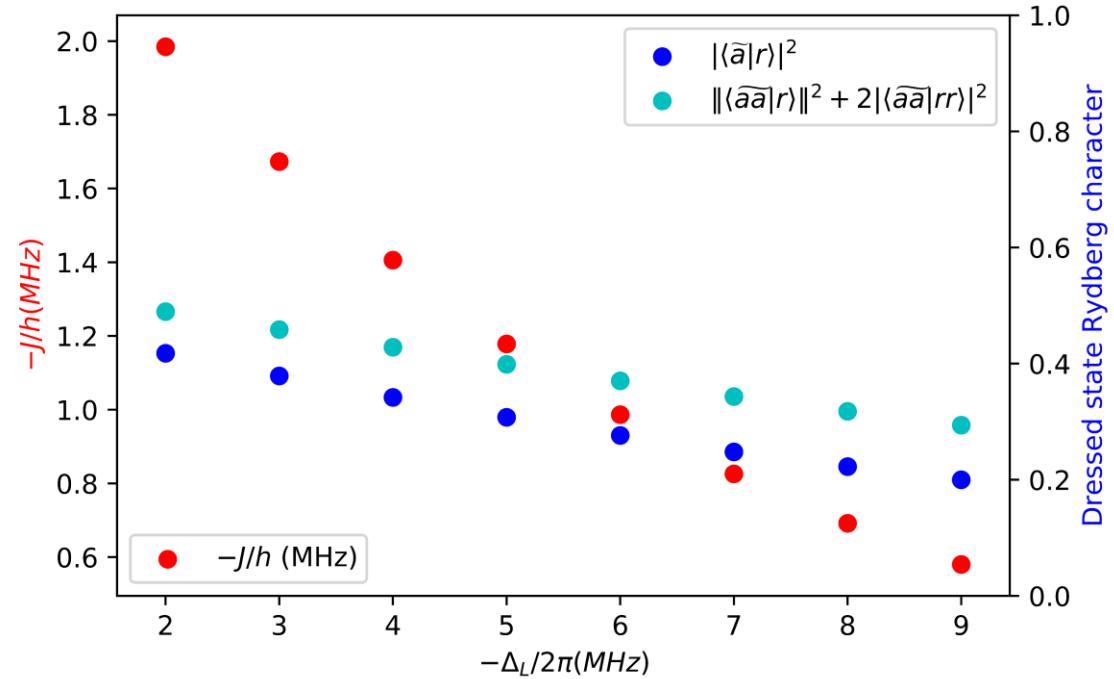
$$P_{\tilde{aa}} = \|\langle r|\tilde{aa}\rangle\|^2 + 2|\langle rr|\tilde{aa}\rangle|^2$$

$$\Gamma_{\tilde{a}} = P_{\tilde{a}}\Gamma_r$$

$$\Gamma_{\tilde{aa}} = P_{\tilde{aa}}\Gamma_r$$

We can choose between a stronger interaction strength vs a weaker decay!

$$\Omega_L/2\pi = 12\text{MHz}, V_{rr}/2\pi = -40\text{MHz}$$



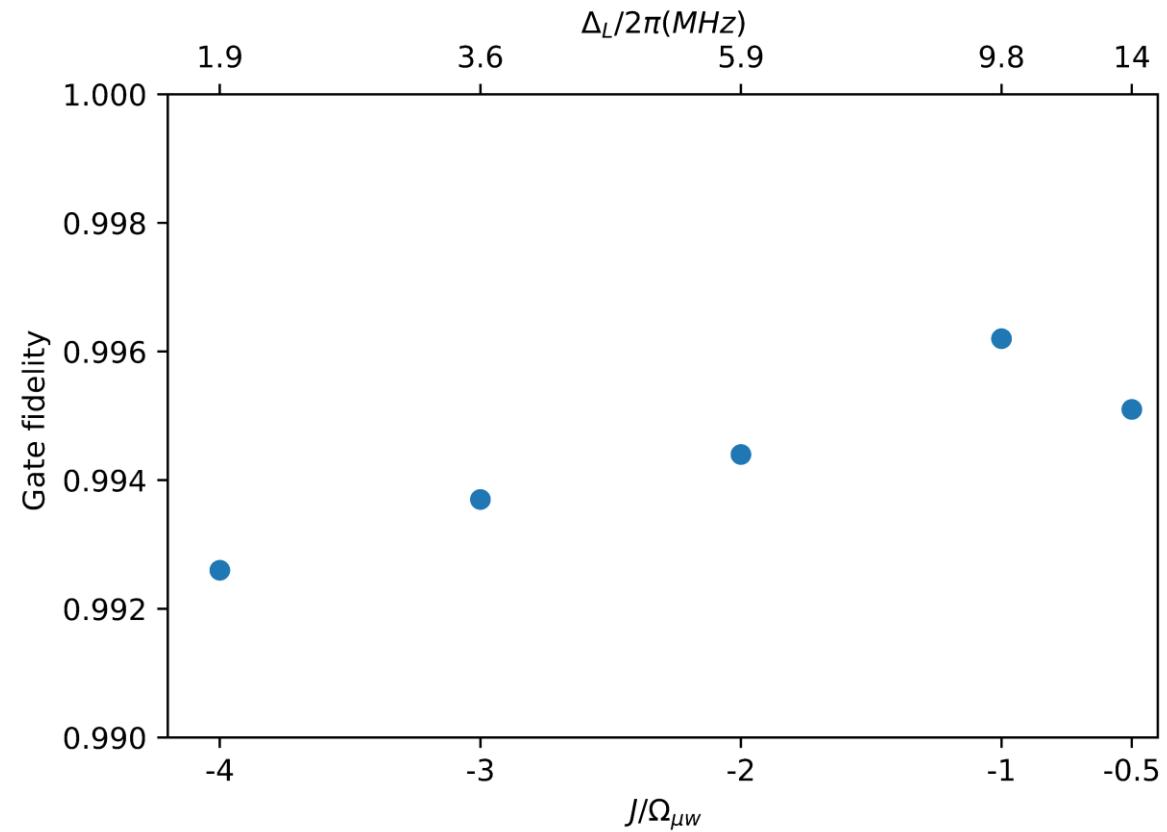
# Limitations and usefulness

- One big limitation here:  $J/2\pi \sim 1MHz$   $\Omega_L/2\pi = 12MHz, V_{rr}/2\pi = -40MHz$   
 $V_{rr}/2\pi \sim 20 - 100MHz$   $\Omega_{\mu w}/2\pi = 0.5MHz$

But hey, it's fine if  $J/\Omega_{\mu w}$  is small!

Also microwaves are slower than Lasers!

$$\Omega_{\mu w} < \Omega_L$$



# Summary and outlook

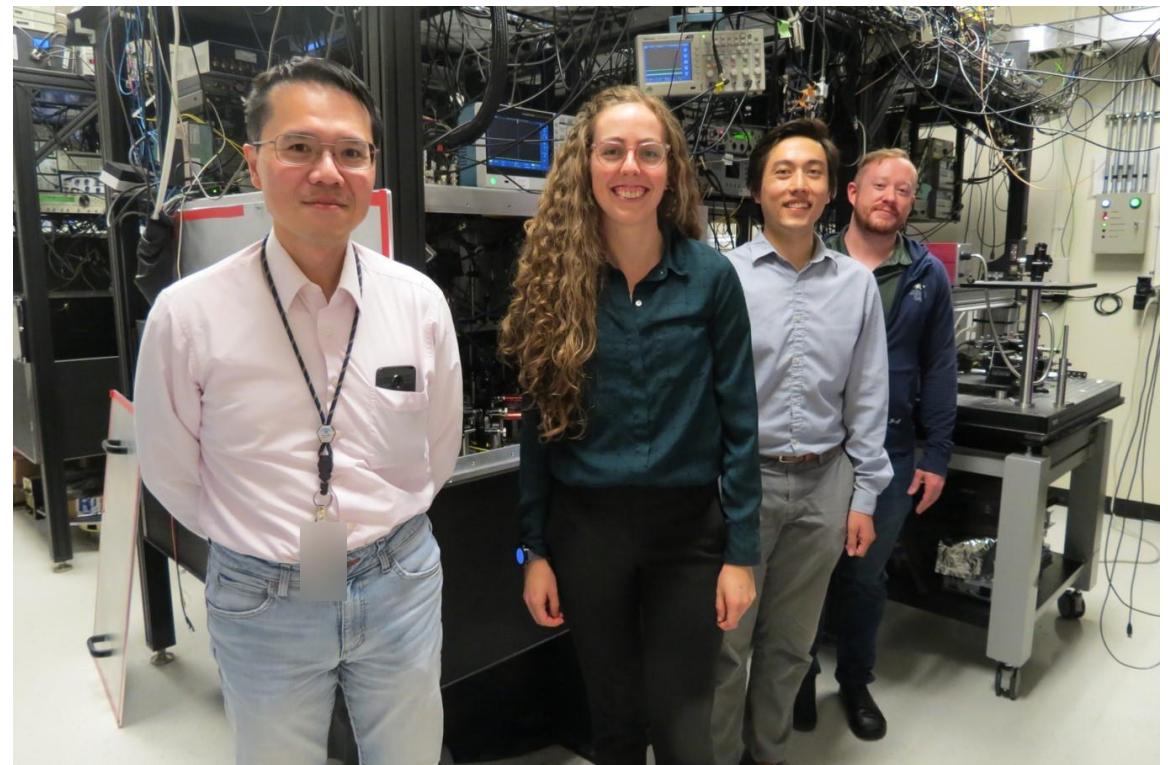
- Imperfect blockade is not a limitation, in fact it might be an advantage.
- Entangling protocols can be implemented in the microwave regime, and dressing can help fully exploit finite and weak blockades.

Other things I am not talking about here

- Adiabatic gates in the dressed regime
- Anti-blockade dressing for better fidelities

# Collaborators

- UNM: Sivaprasad Omanakuttan and Ivan Deutsch.
- Sandia Collaborators: Yuan-Yu Jau, Matt Chow, Bethany Little.



Thank you for your attention!