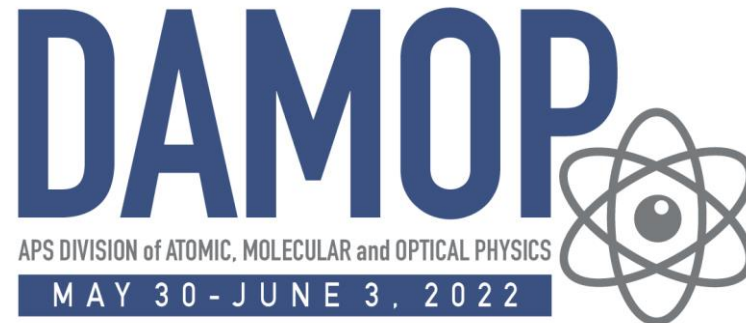


# Two-qubit Quantum Logic Gates for Neutral Atoms Based on the Spin-Flip Blockade



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**CQuIC**  
Center for Quantum  
Information and Control

**Vikas Buchemmavari, Sivaprasad Omanakuttan,**

**Yuan-Yu Jau, Ivan Deutsch**

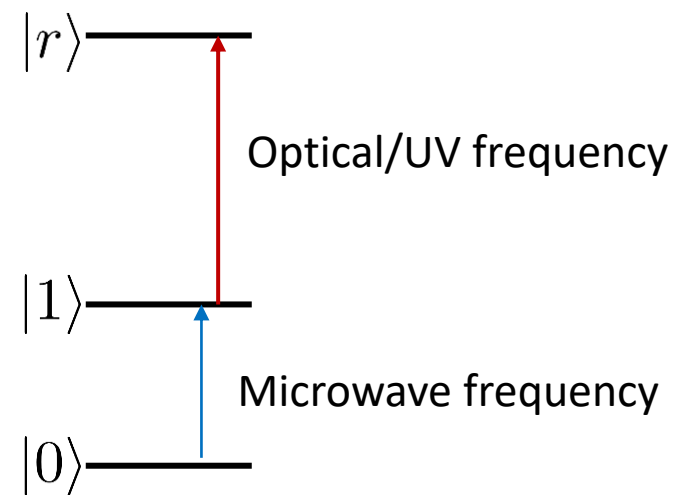
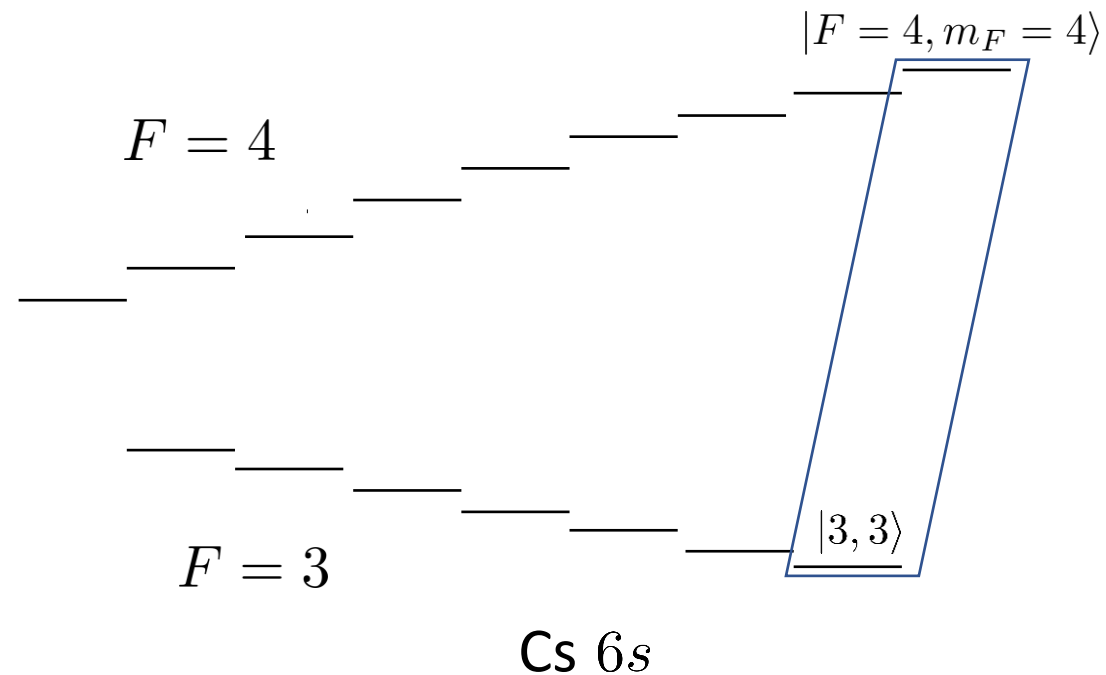
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# Cesium system

Motivation: Designing a high fidelity  
Entangling gate for Neutral atom qubits

Entanglement achieved via Rydberg  
states

$$H_{int} = V_{rr} |rr\rangle\langle rr|$$



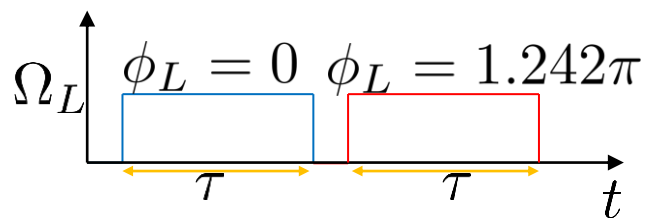
# Levine-Lukin gate – LL gate

$$\text{---} |00\rangle$$

$$\begin{array}{c} |0r\rangle, |r0\rangle \\ \text{---} \Delta_L \\ \uparrow \Omega_L, \phi_L \\ |01\rangle, |10\rangle \end{array}$$

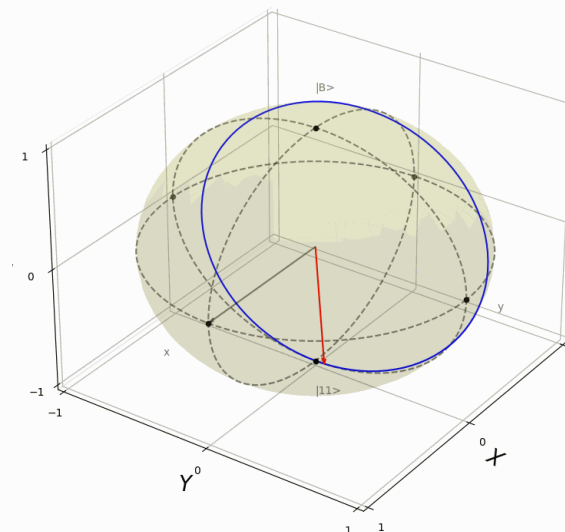
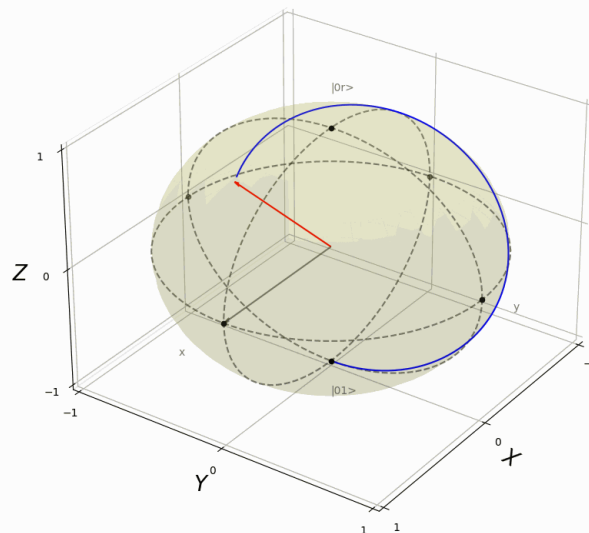
$$\begin{array}{c} |B\rangle = \frac{|1r\rangle + |r1\rangle}{\sqrt{2}} \\ \text{---} \Delta_L \\ \uparrow \sqrt{2}\Omega_L, \phi_L \\ |11\rangle \end{array}$$

$$\begin{aligned} |00\rangle &\rightarrow |00\rangle \\ |01\rangle &\rightarrow e^{i\alpha}|01\rangle \\ |10\rangle &\rightarrow e^{i\alpha}|10\rangle \\ |11\rangle &\rightarrow e^{i\beta}|11\rangle \end{aligned}$$



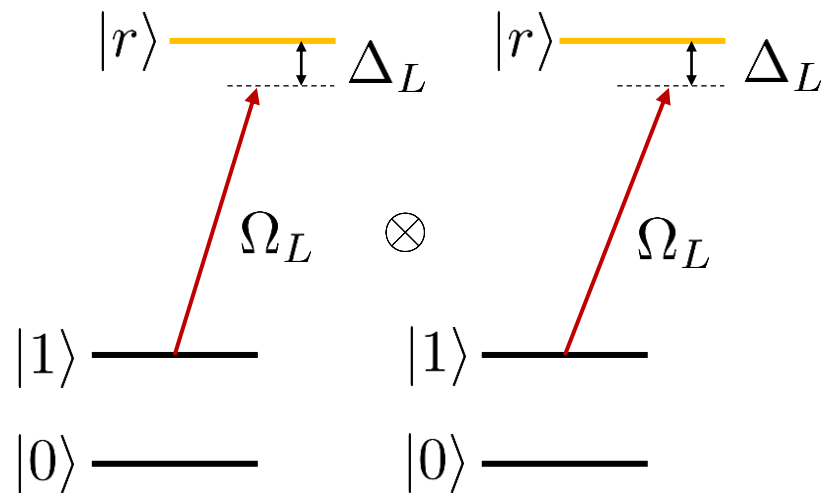
$$\sqrt{2}\Omega_L\tau = 2\pi$$

$$\Delta_L = 0.377\Omega_L \implies \beta - 2\alpha = \pi$$

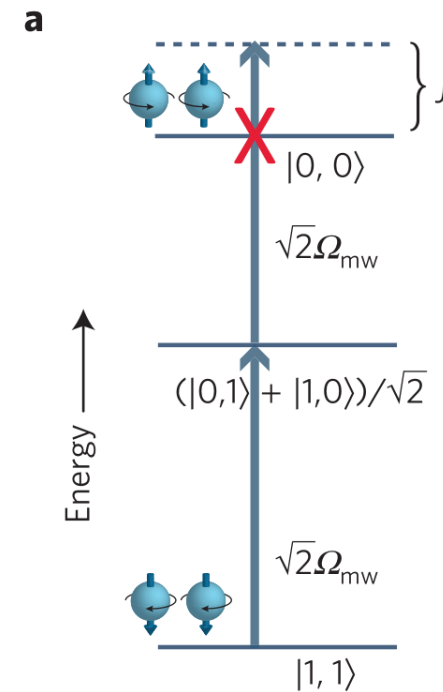
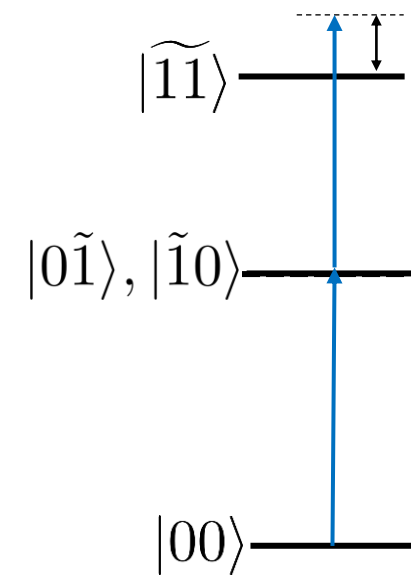


# Entangling atomic spins with a Rydberg-dressed spin-flip blockade

Y.-Y. Jau<sup>1,2</sup>, A. M. Hankin<sup>1,2</sup>, T. Keating<sup>1,2</sup>, I. H. Deutsch<sup>1,2</sup> and G. W. Biedermann<sup>1,2\*</sup>



$$\Rightarrow J = E_{LS}^2 - 2E_{LS}^1$$




# LL gate in the hyperfine regime

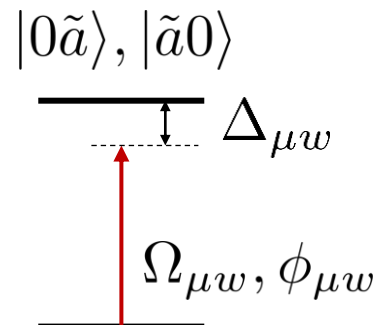
$$H_{hf}^1 = E_0|0\rangle\langle 0| + E_1|1\rangle\langle 1| + E_a|a\rangle\langle a|$$

$$H_{hf} = H_{hf}^1 \otimes \mathbf{1} + \mathbf{1} \otimes H_{hf}^1 + \textcolor{red}{J}|\widetilde{aa}\rangle\langle \widetilde{aa}|$$

$$\begin{aligned} J &\rightarrow V_{rr} \\ \Omega_{\mu w} &\rightarrow \Omega_L \\ \Delta_{\mu w} &\rightarrow \Delta_L \\ \phi_{\mu w} &\rightarrow \phi_L \\ |\tilde{a}\rangle &\rightarrow |r\rangle \end{aligned}$$



$$|00\rangle$$

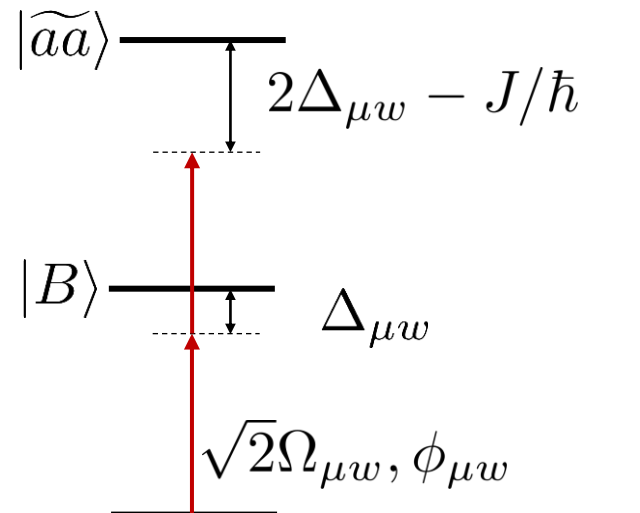


$$|0\tilde{a}\rangle, |\tilde{a}0\rangle$$

$$\Delta_{\mu w}$$

$$\Omega_{\mu w}, \phi_{\mu w}$$

$$|01\rangle, |10\rangle$$



$$|\widetilde{aa}\rangle$$

$$2\Delta_{\mu w} - J/\hbar$$

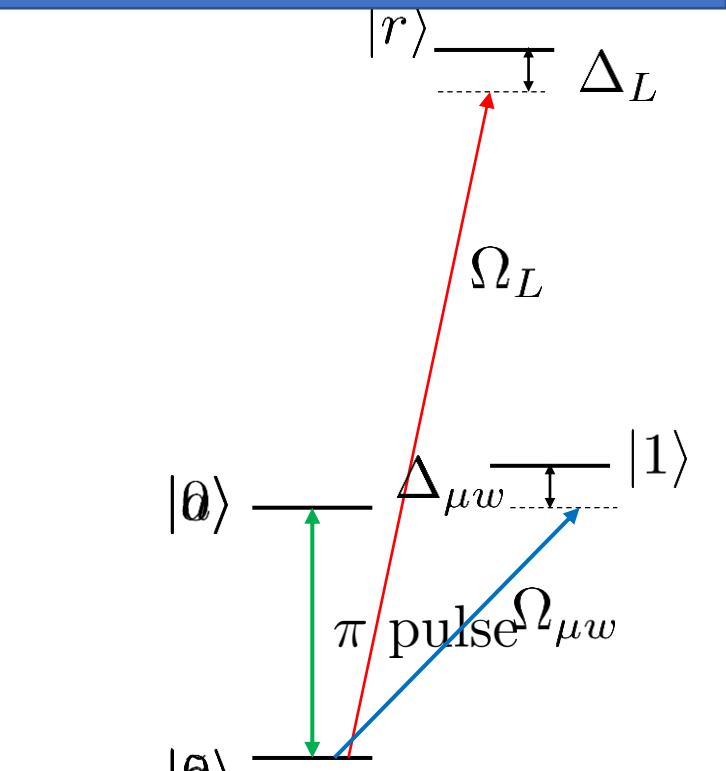
$$|B\rangle$$

$$\Delta_{\mu w}$$

$$\sqrt{2}\Omega_{\mu w}, \phi_{\mu w}$$

$$|11\rangle$$

$$|B\rangle = \frac{|1\tilde{a}\rangle + |\tilde{a}1\rangle}{\sqrt{2}}$$



$$|r\rangle$$

$$\Delta_L$$

$$\Omega_L$$

$$|a\rangle$$

$$\Delta_{\mu w}$$

$$|1\rangle$$

$$\pi \text{ pulse}$$

$$\Omega_{\mu w}$$

$$|a\rangle$$

$$= \cos(\theta/2)|a\rangle + \sin(\theta/2)|r\rangle$$

$$\left( \tan \theta = \frac{\Omega}{-\Delta} \right)$$

$$\begin{aligned} J &\rightarrow V_{rr} \\ \Omega_{\mu w} &\rightarrow \Omega_L \\ \Delta_{\mu w} &\rightarrow \Delta_L \\ \phi_{\mu w} &\rightarrow \phi_L \\ |\tilde{a}\rangle &\rightarrow |r\rangle \end{aligned}$$

J is much smaller than V

If we aim for perfect blockade, our gates become much slower

Is there a way around this?

Yes! Quantum optimal control is the answer!

# Optimal Quantum control for the LL gate

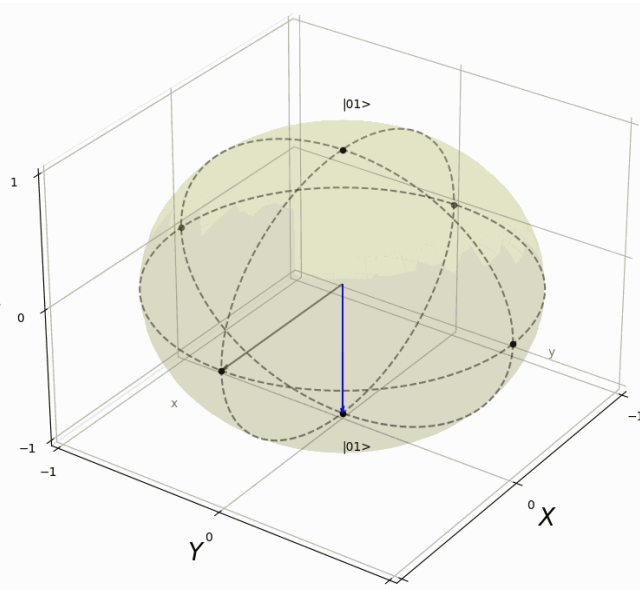
We use Gradient Ascent Pulse Engineering (GRAPE)

We maximize  $\mathcal{F}$  by using  $\vec{\nabla}_{\vec{\phi}} \mathcal{F}$ .

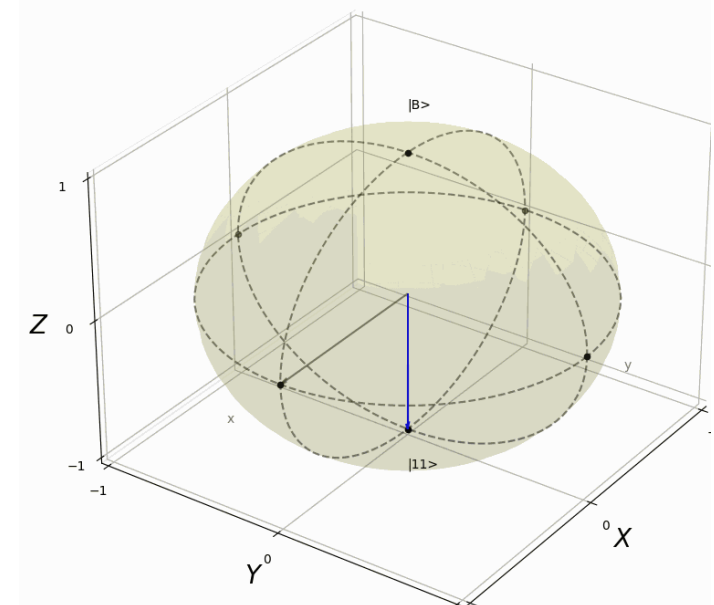
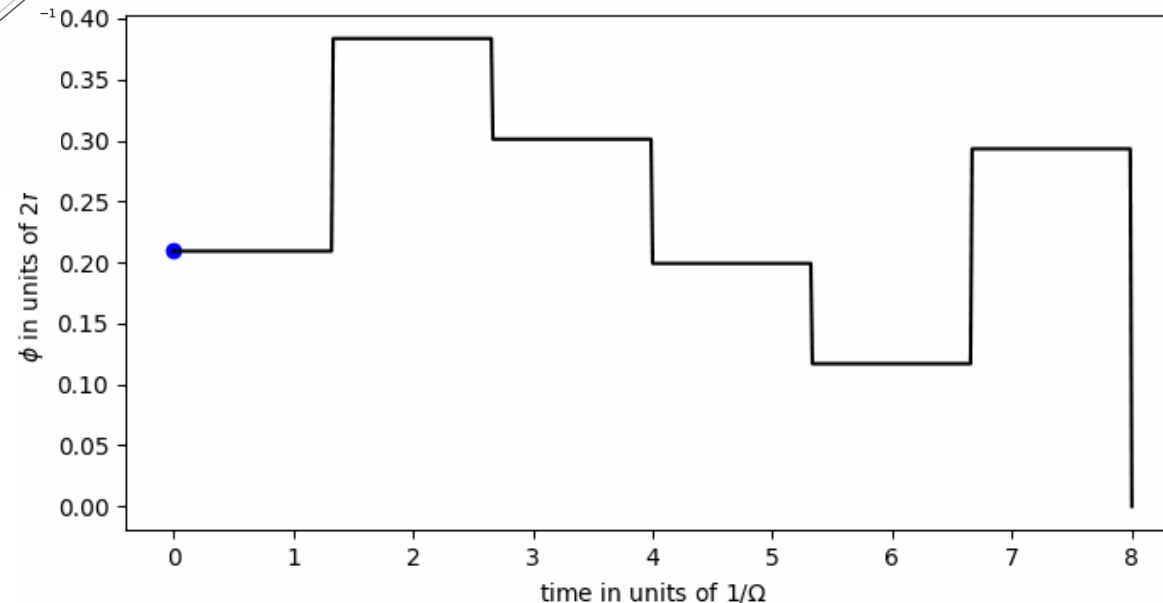
$$\mathcal{F} = \text{Tr}((CZ)^\dagger U[\phi(t)])$$

$$\Delta_L = 0, \Omega_L = 1$$

$$\vec{\phi} = (\phi_1, \phi_2, \phi_3, \phi_4, \phi_5, \phi_6)$$



$$|01\rangle \rightarrow e^{i\phi_1} |01\rangle$$

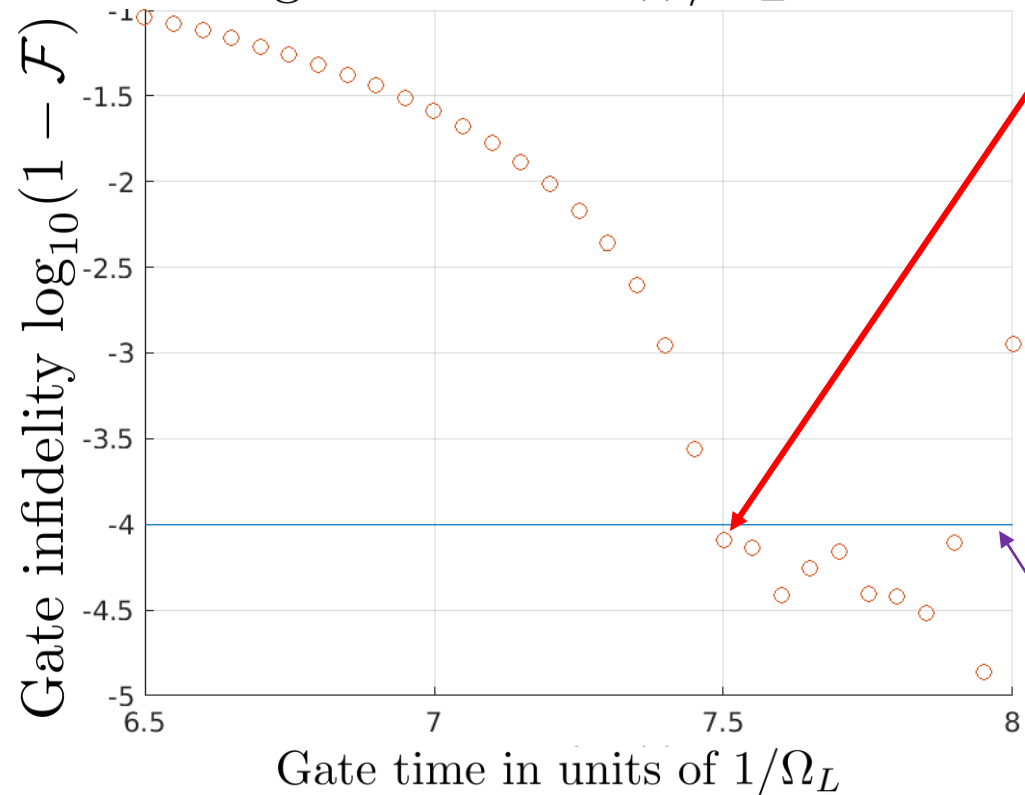


$$|11\rangle \rightarrow e^{i\phi_2} |11\rangle$$

$$\phi_2 - 2\phi_1 = \pi$$

# Quantum speed-limit

Infidelity of the Optimal control gate  
vs gate time at  $V_{rr}/\Omega_L = 4$

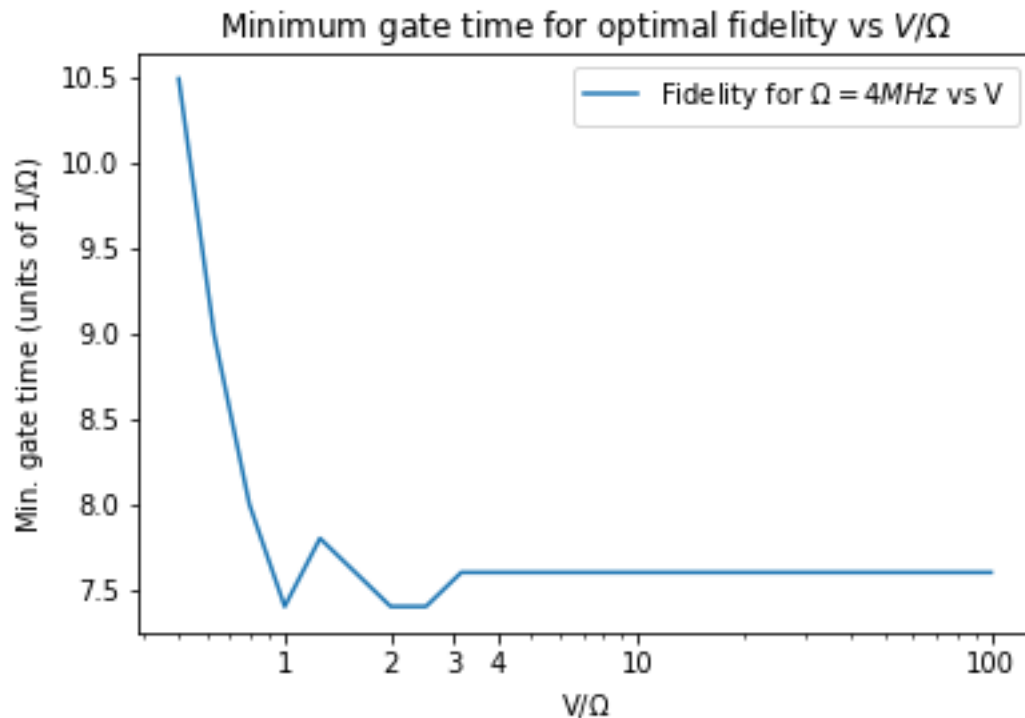


Minimum time needed to implement  
the gate for  $V_{rr}/\Omega = 4$

Target fidelity



# Some counterintuitive results!



Imperfect blockade doesn't slow down your gate too much! In fact, it can make it faster!

$$H = \frac{\Omega}{2} (\sigma_{\phi}^1 + \sigma_{\phi}^2) + \frac{V_{rr}}{2} (\sigma_z^1 \otimes \sigma_z^2 + \sigma_z^1 + \sigma_z^2)$$

Known result from Spin Quantum control!

$$J = \omega(J_x \cos \phi + J_y \sin \phi) + \kappa J_z^2$$

The fastest state preparation times arise when  $\kappa \sim \Omega$ .

-The cost: More population is pumped into  $|rr\rangle$

# Tunability of interaction strength

By changing our dressing parameters,  $\Delta_L, \Omega_L$   
We can change J and the Rydberg  
character of the dressed states

$$\Omega_L/2\pi = 12\text{MHz}, V_{rr}/2\pi = -40\text{MHz}$$

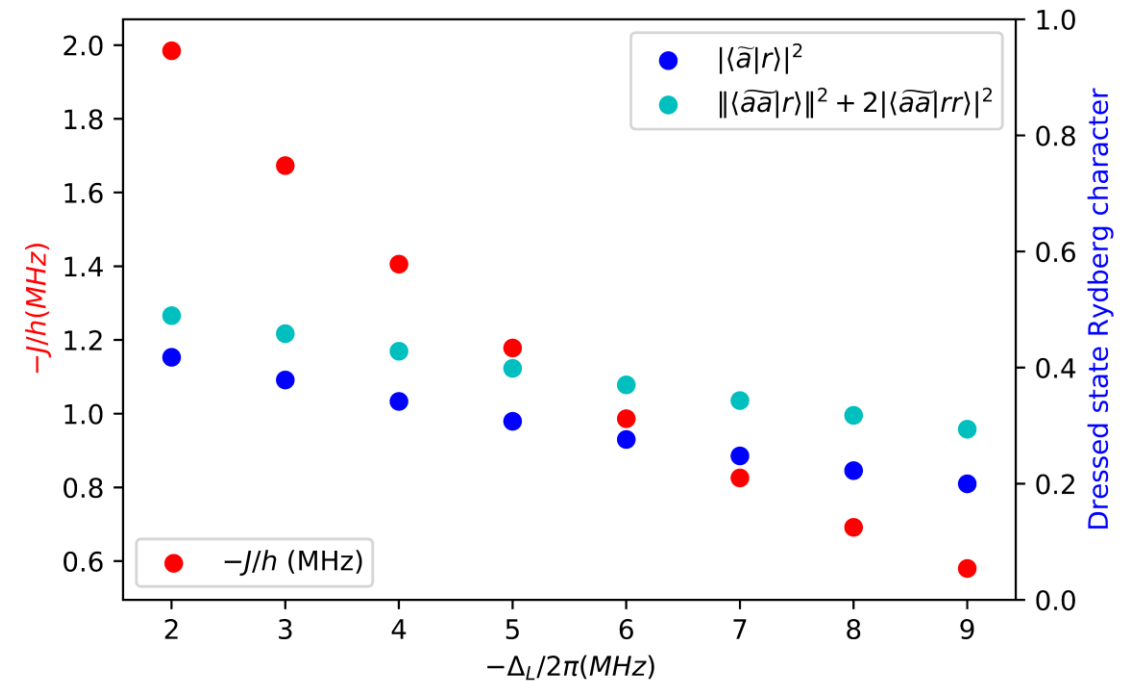
$$P_{\tilde{a}} = |\langle r|\tilde{a}\rangle|^2$$

$$P_{\tilde{a}\tilde{a}} = \|\langle r|\tilde{a}\tilde{a}\rangle\|^2 + 2|\langle rr|\tilde{a}\tilde{a}\rangle|^2$$

$$\Gamma_{\tilde{a}} = P_{\tilde{a}}\Gamma_r$$

$$\Gamma_{\tilde{a}\tilde{a}} = P_{\tilde{a}\tilde{a}}\Gamma_r$$

We can choose between a stronger  
interaction strength vs a weaker decay!



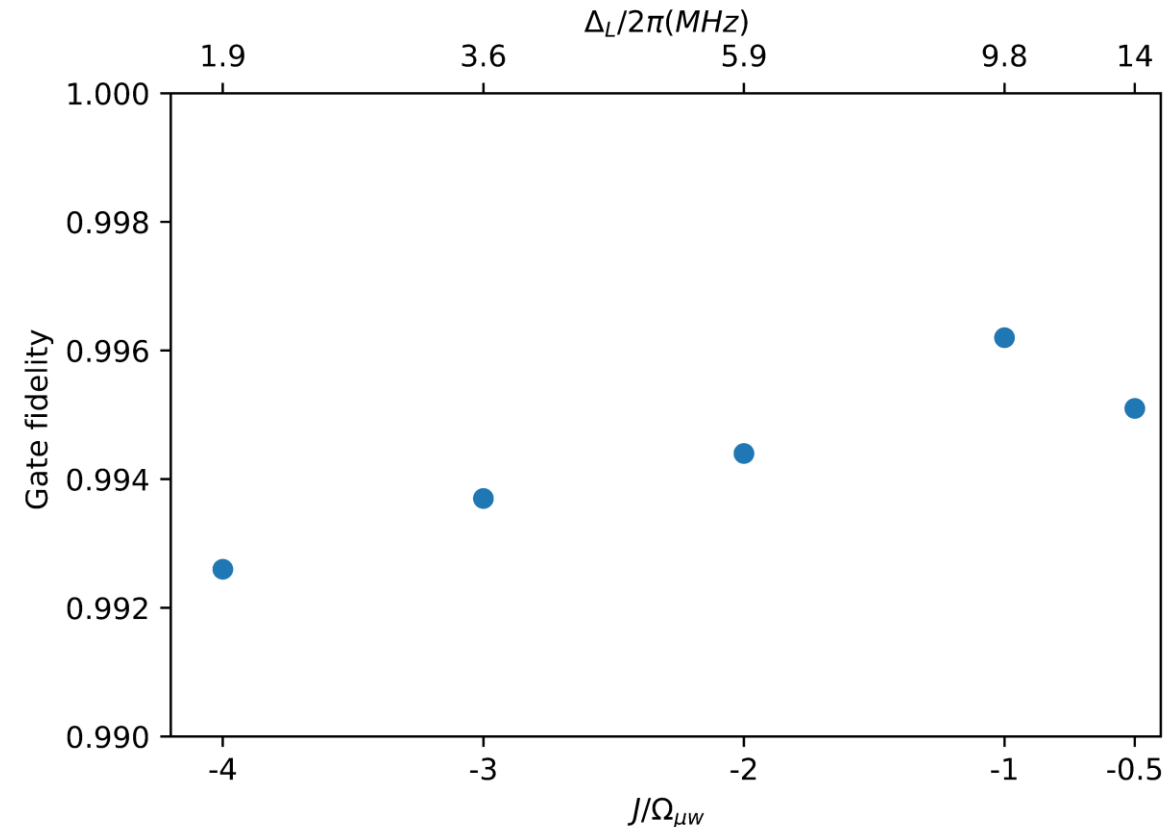
# Limitations and usefulness

- One big limitation here:  $J/2\pi \sim 1\text{MHz}$   
 $V_{rr}/2\pi \sim 20 - 100\text{MHz}$
- $\Omega_L/2\pi = 12\text{MHz}, V_{rr}/2\pi = -40\text{MHz}$   
 $\Omega_{\mu w}/2\pi = 0.5\text{MHz}$

But hey, it's fine if  $J/\Omega_{\mu w}$  is small!

Also microwaves are slower than Lasers!

$$\Omega_{\mu w} < \Omega_L$$



# Summary and outlook

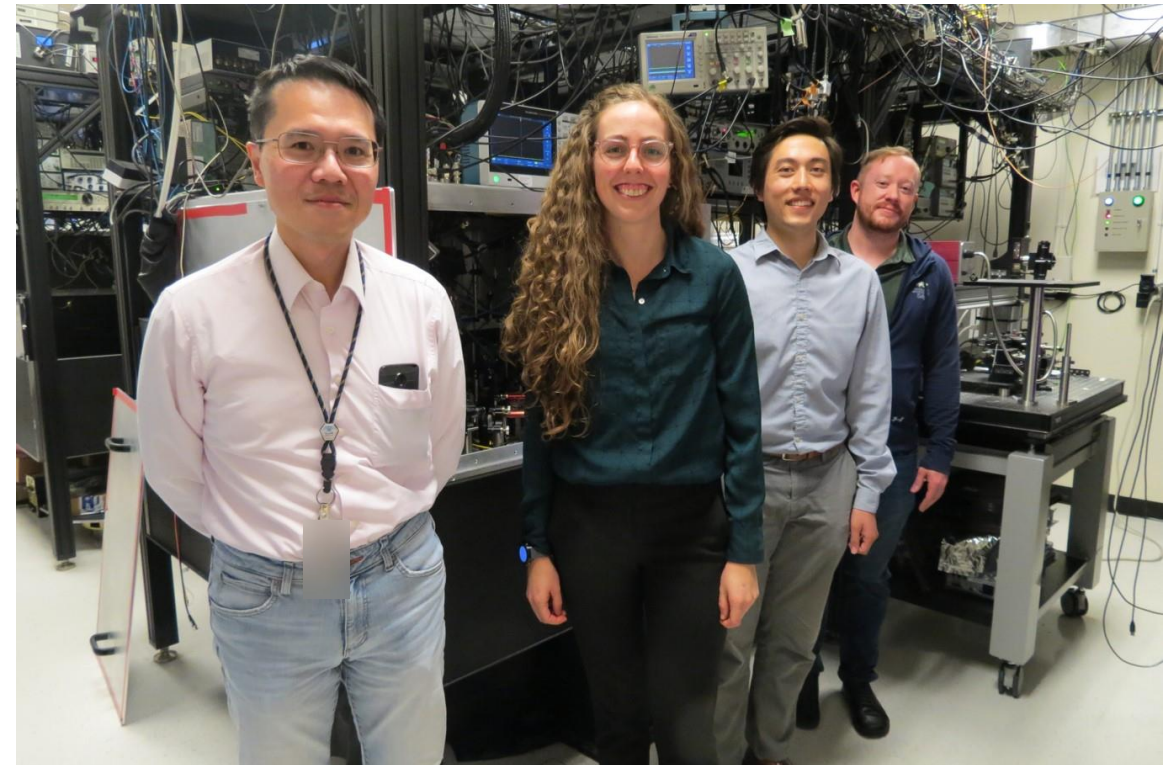
- Imperfect blockade is not a limitation, in fact it might be an advantage.
- Entangling protocols can be implemented in the microwave regime, and dressing can help fully exploit finite and weak blockades.

Other things I am not talking about here

- Adiabatic gates in the dressed regime
- Anti-blockade dressing for better fidelities

# Collaborators

- UNM: Sivaprasad Omanakuttan and Ivan Deutsch.
- Sandia Collaborators: Yuan-Yu Jau, Matt Chow, Bethany Little.



Thank you for your attention!