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Non-intrusive coupling of multi-physics codes for Eulerian-Lagrangian solid-solid interaction using Immersed Finite Element Method

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- **Introduction**
- Review of modified Immersed Finite Element Method (mIFEM)
- Non-intrusive coupling of software
- Improvements in mIFEM algorithm
- Numerical test cases
- Summary and future work



Motivation



shock induced structural damage [1]

- **Simulation of hypervelocity impact and solid-solid interactions**
- **Applications:**
 - Ballistic penetration [2]
 - Geodynamics [3]
 - Spacecraft design [4]
- **Challenges:**
 - Non-linear wave propagation
 - Large plastic deformations, fragmentations

[1] https://commons.wikimedia.org/wiki/File:Shock_tube.JPG

[2] Shen Wei and Wu Cuisheng. Computer simulation for damage-failure process of composite plate under high-speed impact. *Engineering fracture mechanics*, 1992

[3] Francois E Heuz'e. An overview of projectile penetration into geological materials. In *International journal of rock mechanics and mining sciences & geomechanics abstracts*, Elsevier, 1990

[4] MV Silnikov, IV Guk, AF Nechunaev, and NN Smirnov. Numerical simulation of hypervelocity impact problem for spacecraft shielding elements. *Acta Astronautica*, 2018



Motivation

Hydrocode: codes used to simulate **highly dynamic events** involving shocks

Lagrangian Hydrocodes

- Nodes are attached to material points.
- Explicit material boundaries
- Easier to apply interface conditions.
- Mesh distortion
- Need re-meshing/ element deletion strategies
- DYNA [1], Camacho and Ortiz [2]

Eulerian Hydrocodes

- Materials are tracked across a fixed mesh.
- Fixed mesh, large plastic deformations.
- Interfaces are not tracked explicitly
- Benson [3], Udaykumar et. al. [4]

Coupled Lagrangian-Eulerian

- Projectile: Lagrangian description
- Target: Eulerian description
- Leverage advantages of both approaches
- Zapotec [5]

[1] JO Hallquist and RG Whirley. Dyna3d user manual, nonlinear dynamic analysis in three dimensions. Report UCID-19592, Rev, 5, 1989.

[2] GT Camacho and M Ortiz. Adaptive lagrangian modelling of ballistic penetration of metallic targets. Computer methods in applied mechanics and engineering, 1997

[3] DJ Benson. A multi-material eulerian formulation for the efficient solution of impact and penetration problems. Computational mechanics, 1995.

[4] HS Udaykumar, L Tran, DM Belk, and KJ Vanden. An eulerian method for computation of multimaterial impact with eno shock-capturing and sharp interfaces. Journal of Computational Physics, 2003

[5] Bessette et. al., Zapotec: A Coupled Euler-Lagrange Program for Modeling Earth Penetration (2002)



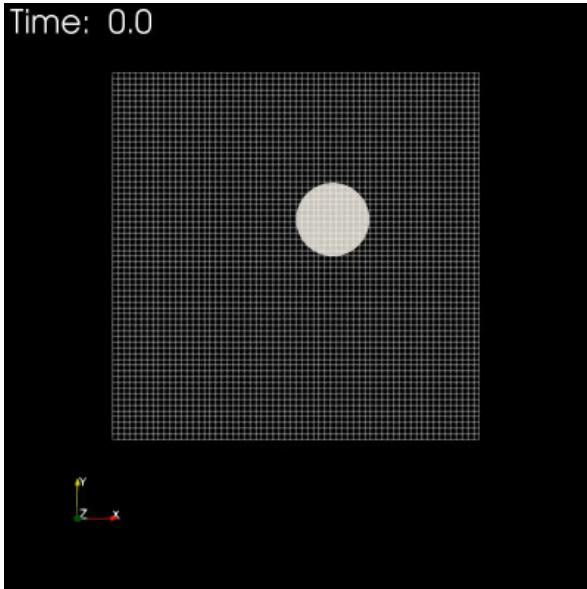
Overview

- Introduction
- **Review of modified Immersed Finite Element Method (mIFEM)**
- Non-intrusive coupling of software
- Improvements in mIFEM algorithm
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Background

Time: 0.0



- **Modified Immersed Finite Element Method (mIFEM) [1]**
 - Non-conforming mesh method, partitioned approach
 - Inspired from IB method [2]

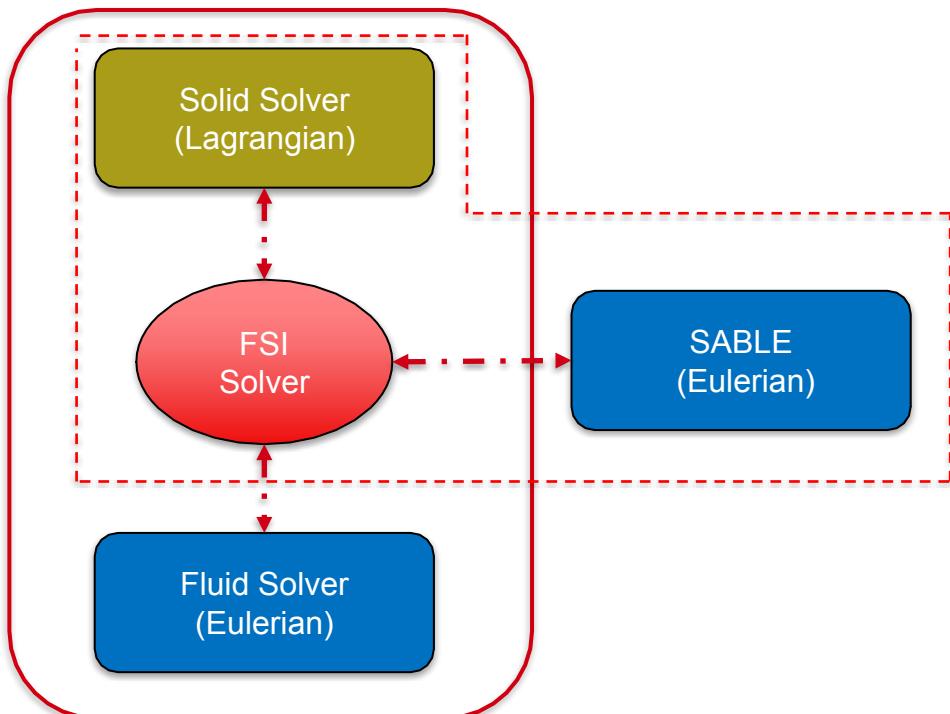
- **Comparison with classical IB:**
 - **Volume based** interpolation
 - **Solve solid dynamics** and enforce it on overlapping fluid
 - **Solid has constitutive relationship** and yields stress information

[1] Xingshi Wang and Lucy T. Zhang. Modified immersed finite element method. *Computer Methods in Applied Mechanics and Engineering*, 267:150–169, 2013.

[2] Charles S Peskin. The immersed boundary method. *Acta Numerica*, 11:479–517, 2002

Background

OpenIFEM



➤ OpenIFEM [1]:

- Opensource, C++
- Modular implementation of mIFEM

➤ Objectives:

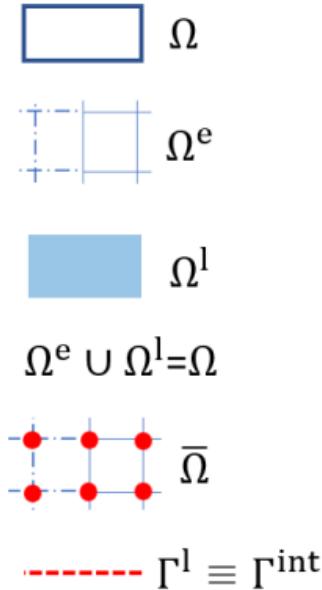
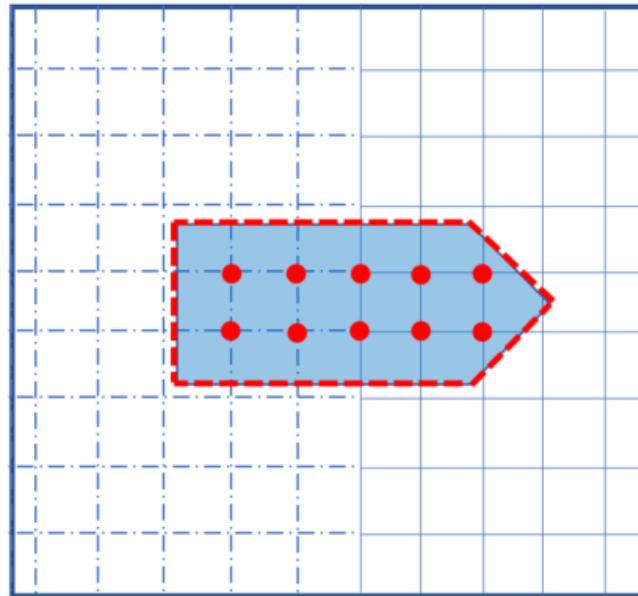
- Couple a multi-material Eulerian shock physics code **SABLE** [2] with **OpenIFEM** for simulation of solid-solid impacts.
- Couple OpenIFEM and SABLE non-intrusively.
- Provide framework for coupling two hydrocodes.

[1] <https://github.com/OpenIFEM>

[2] KM Hays et al. A users guide to sable 2.0: The sandia automated boolean logic evaluation software. Sandia National Lab. (1996)



mIFEM Algorithm: Domain decomposition



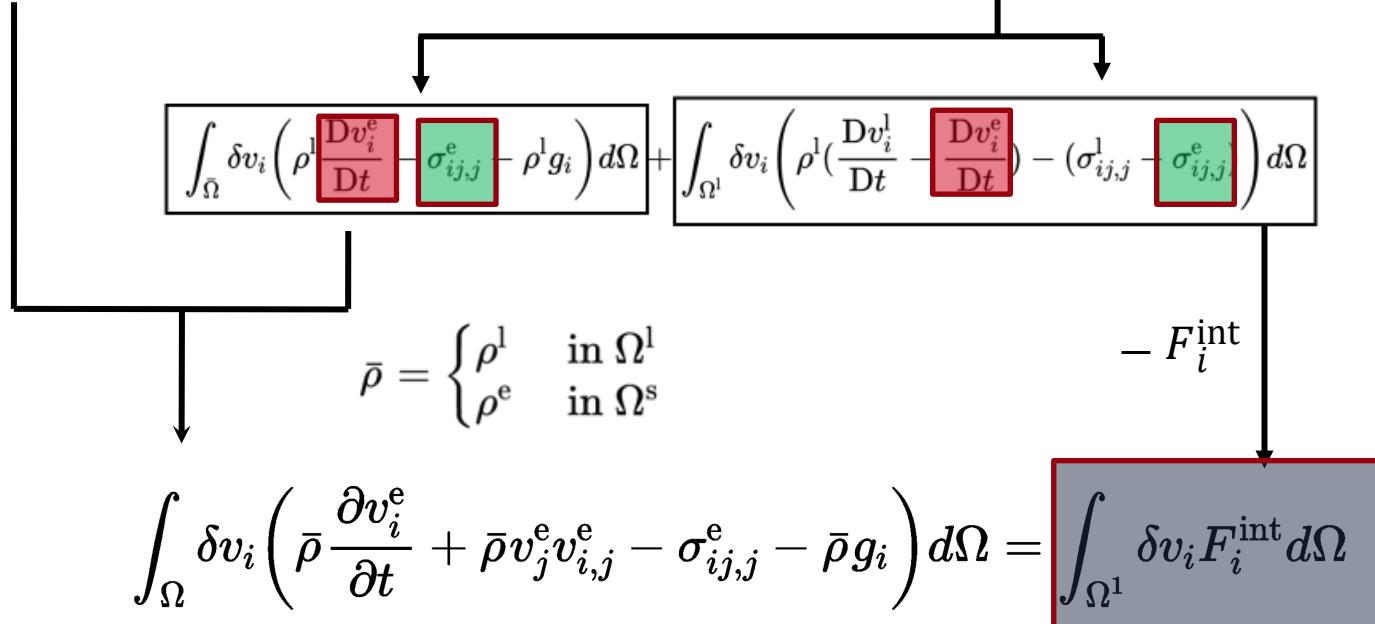
mIFEM Algorithm: Formulation

virtual work done by the Eulerian material

$$\int_{\Omega^e} \delta v_i \left(\rho^e \frac{Dv_i^e}{Dt} - \sigma_{ij,j}^e - \rho^e g_i \right) d\Omega + \int_{\Omega^l} \underline{\delta v_i \left(\rho^l \frac{Dv_i^l}{Dt} - \sigma_{ij,j}^l - \rho^l g_i \right) d\Omega} = 0$$

virtual work done by the Lagrangian material

$$\int_{\Omega^e} \delta v_i \left(\rho^e \frac{Dv_i^e}{Dt} - \sigma_{ij,j}^e - \rho^e g_i \right) d\Omega + \int_{\Omega^l} \underline{\delta v_i \left(\rho^l \frac{Dv_i^l}{Dt} - \sigma_{ij,j}^l - \rho^l g_i \right) d\Omega} = 0$$



mIFEM Algorithm: Governing Equations

$$\rho^l u_{,tt} = \sigma_{ij}^l \quad \text{in } \Omega^l$$

$$u_i = q_i = \hat{v}_i^e \quad \text{on } \Gamma^{\text{sq}}$$

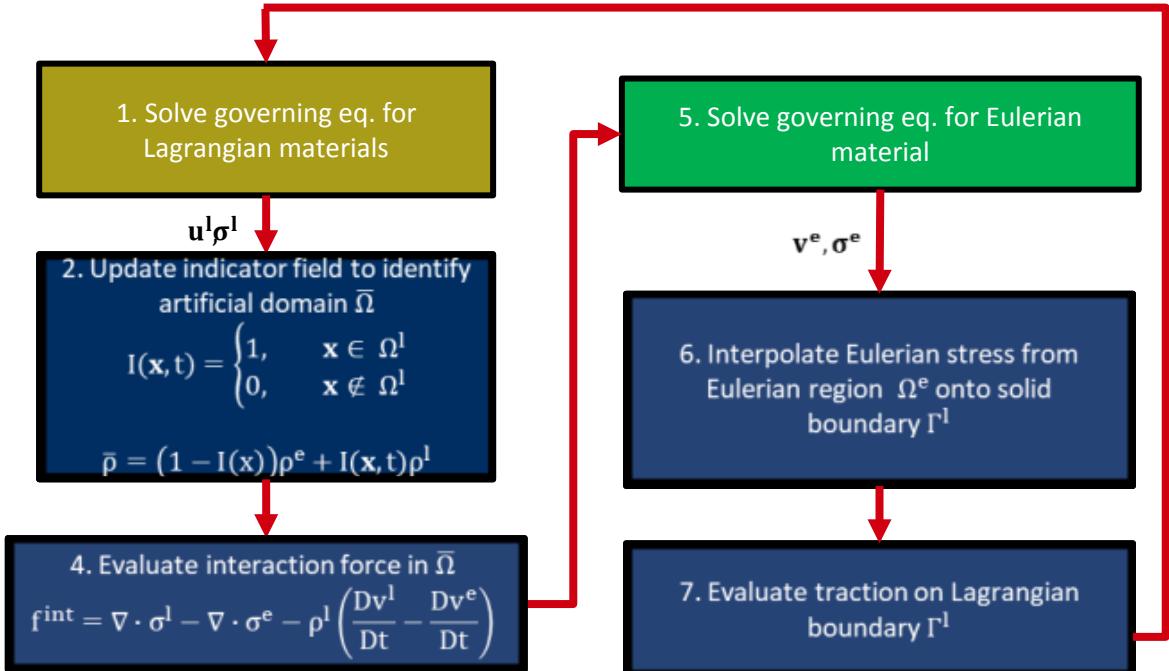
$$\sigma_{ij}^l n_j = h_i = -\sigma_{ij}^e n_j \quad \text{on } \Gamma^{\text{sh}}$$

$$\bar{\rho} \left(\frac{\partial v_i^e}{\partial t} + v_j^e v_{,j}^e \right) = \sigma_{ij,j} + F_i^{\text{int}}(\mathbf{x}, t)$$



mIFEM Algorithm

$$t^{n+1} = t^n + \Delta t$$



Modular Implementation



Cheng J et al., OpenIFEM: A high performance modular open-source software fluid-structure interactions. (2019)



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OpenIFEM-SABLE Coupling

- Coupling via information exchange using MPI protocols

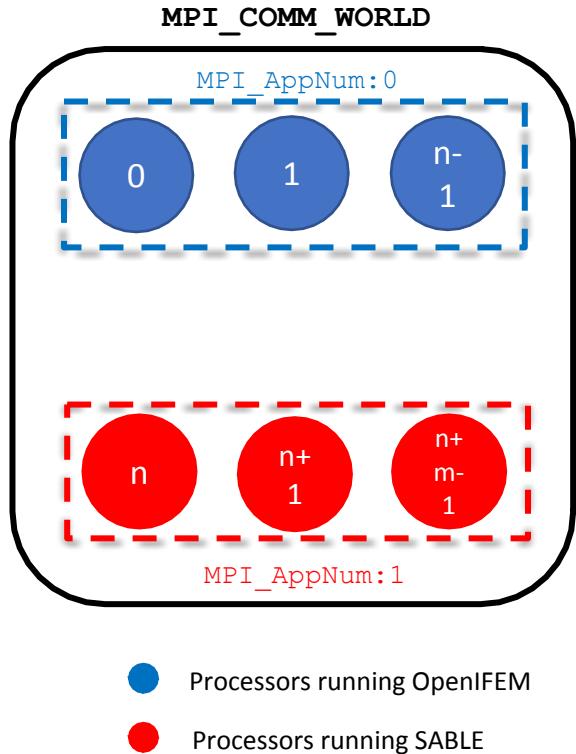
1. Launch OpenIFEM and SABLE:

- `mpirun -np n OpenIFEM : -np m SABLE`

2. Find total number of applications running simultaneously:

- Get `MPI_APPNUM` using the function

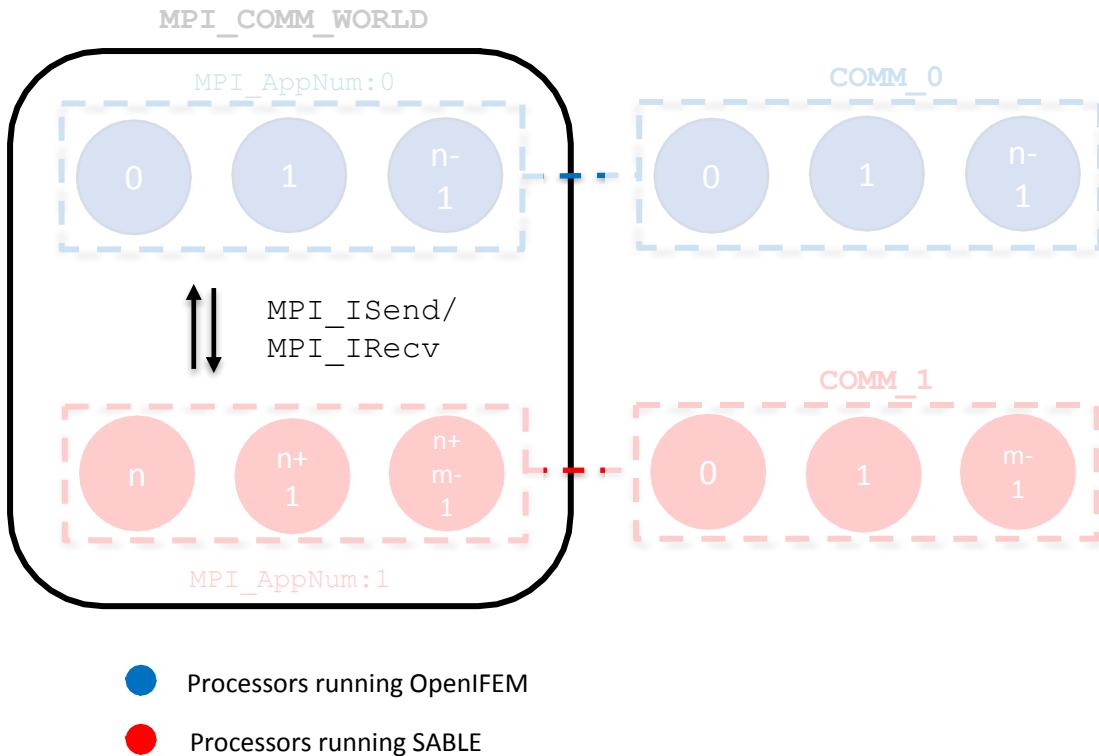
```
MPI_Comm_get_attr
```



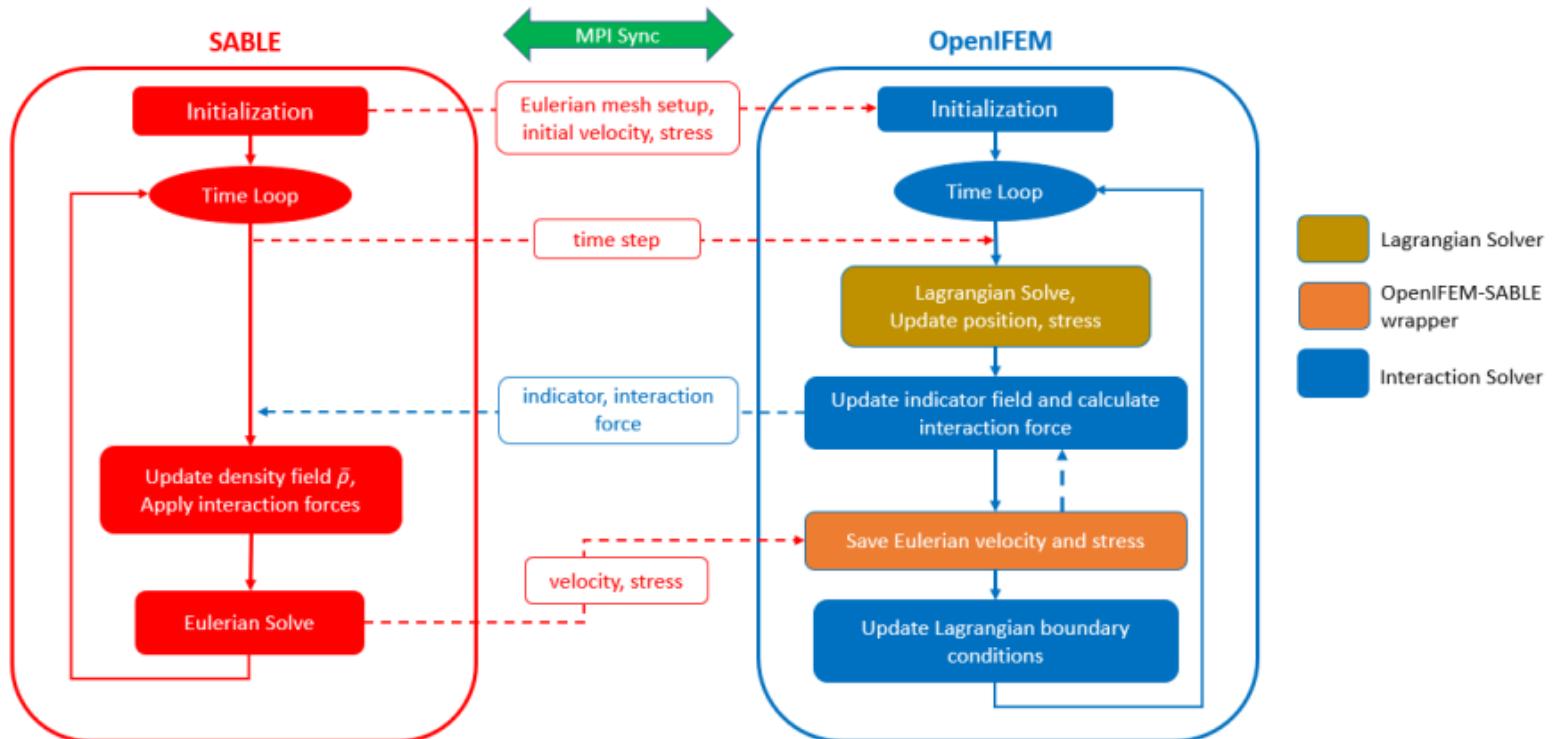
OpenIFEM-SABLE Coupling

3. Split `MPI_COMM_WORLD` into two communicators using function:
`MPI_COMM_split`

4. Switch to `MPI_COMM_WORLD` and exchange data using `MPI_ISend` and `MPI_IRecv`



OpenIFEM-SABLE Coupling

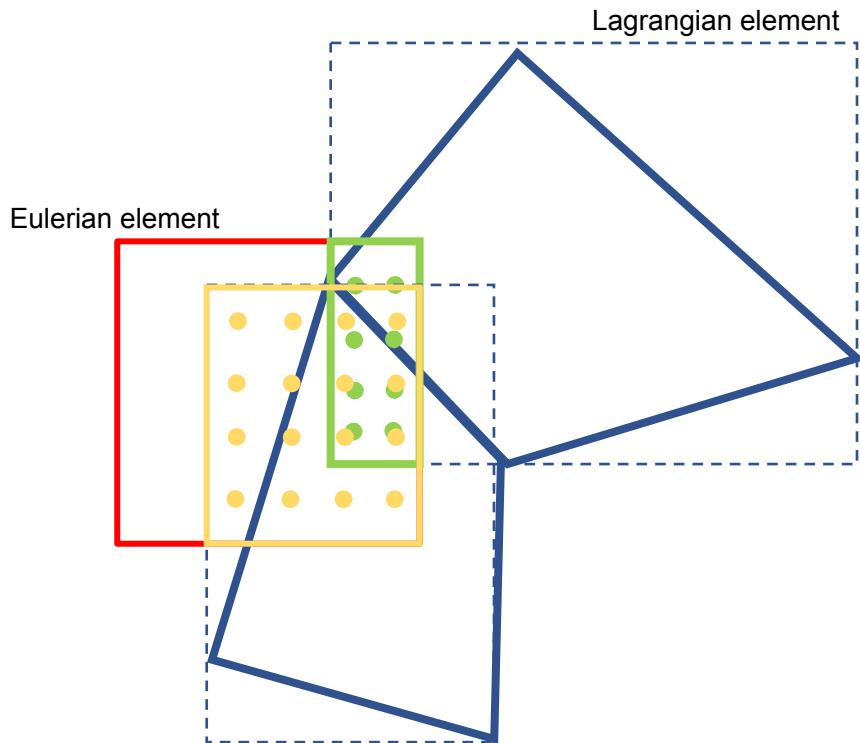


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Improvements in mIFEM for solid-solid coupling

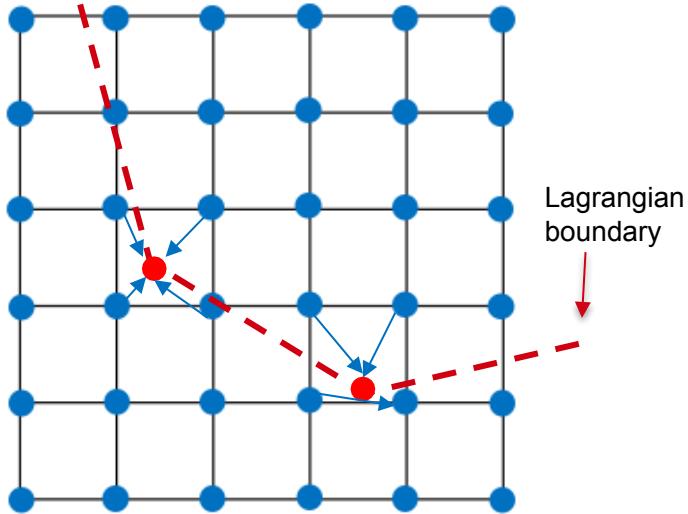


➤ Improved Interface

- Check intersection of each Lagrangian cell bounding box with Eulerian cell
- Sample points in bounding box.
- Check if the point is inside the selected element.
- Exact indicator from current Lagrangian cell
$$= \frac{\text{Area (intersection box)}}{\text{Area(cell)}} * \frac{\text{points inside solid cell}}{\text{total points sampled}}$$
- Repeat for all the elements.



Improvements in mIFEM for solid-solid coupling



➤ Added mass effect [1], [2]:

- Inertial effect of Eulerian solid
- Increase effective forces on Lagrangian solid
- Calculate lumped mass for Eulerian solid.
- Interpolate Eulerian nodal mass to Lagrangian boundary nodes

➤ Calculation of stable time step:

- SABLE: explicit hydrocode
- Stable time step $\Delta t = \alpha * f(h, C^E)$
- h : grid size, C^E : elastic wave speed for Eulerian material, $\alpha=0.85$
- Stable time step for coupled run:
 - $\beta = C^E/C^L$
 - $\Delta t = \beta * \alpha * f(h, C^E)$

[1] Panton, R.L., Incompressible Flow, JohnWiley and Sons (1984)

[2] Brown et. al. Coupled Eulerian–Lagrangian methods for earth penetrating weapon applications, Sandia National Laboratories (2002)

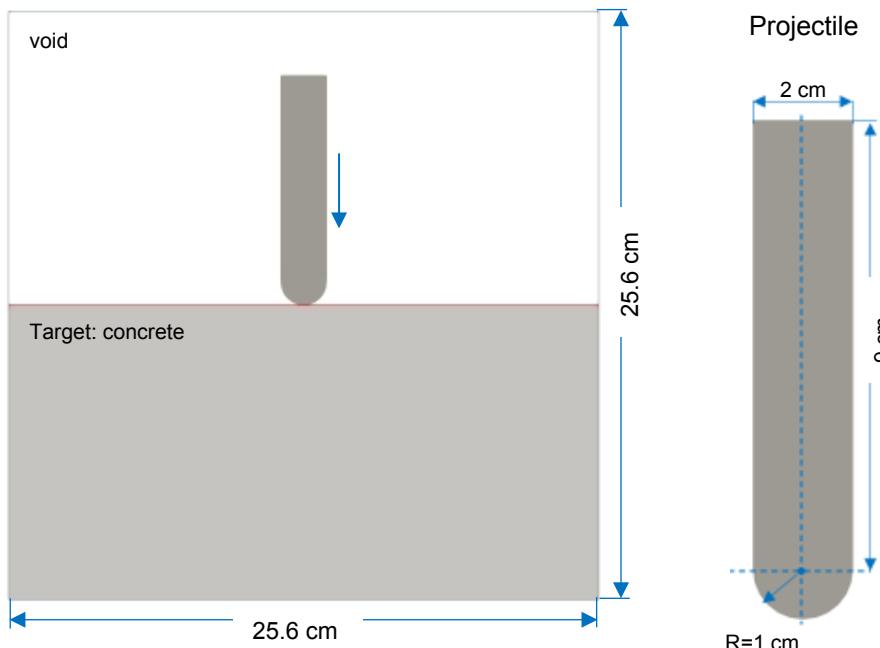


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Test Case 1: Setup



➤ Eulerian (target):

- Material: void + concrete
- Concrete:
 - Material mode: elastic-plastic
 - Compressive strength: 23 MPa
 - Density: 2.03 g/cm^3
- BCs: no displacement at all sides
- Mesh: $\text{dx}=\text{dy}=0.1\text{ cm}$

➤ Lagrangian (projectile):

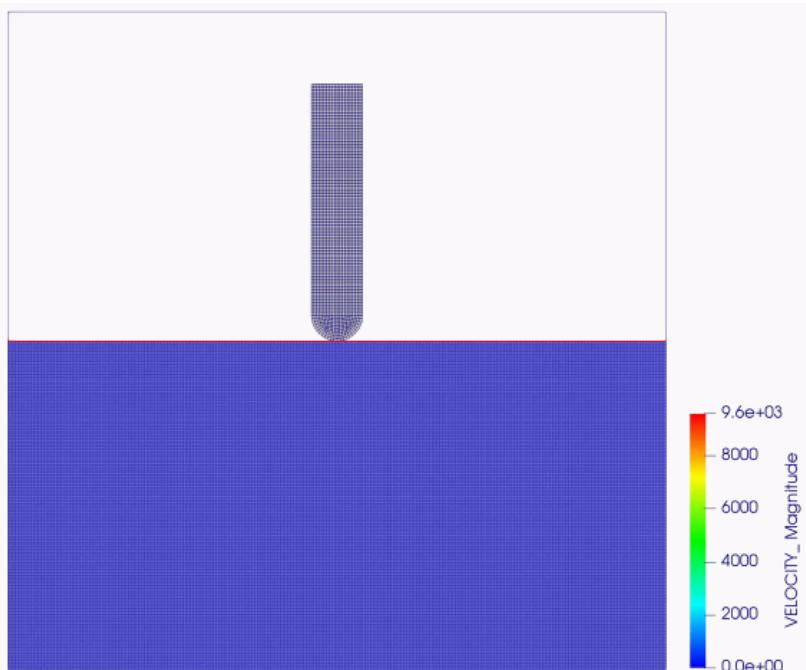
- Material: 4340 steel
- Material model: linear elastic
- $E: 20\text{ GPa}$ $\nu: 0.28$
- Density: 7.8 g/cm^3
- Mesh: $\text{dx}=\text{dy}=0.1\text{ cm}$
- Initial velocity: $-50,000\text{ cm/s}$

➤ Simulation time: 5e-4 s



Test Case 1: Results

Target velocity (cm/s)

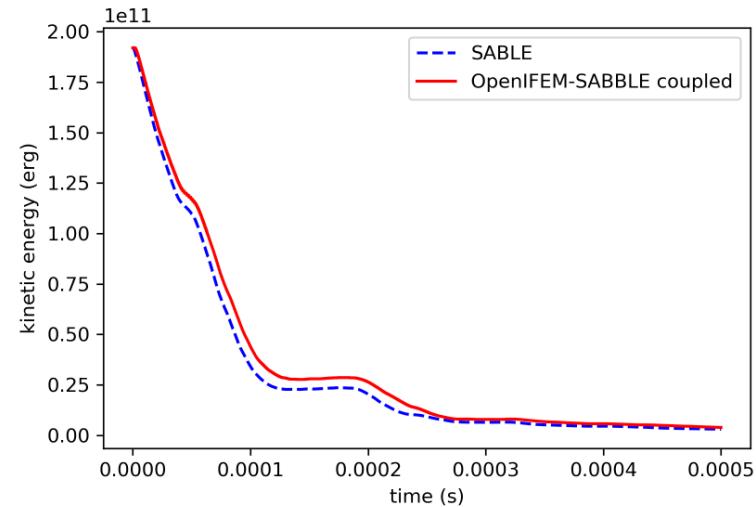
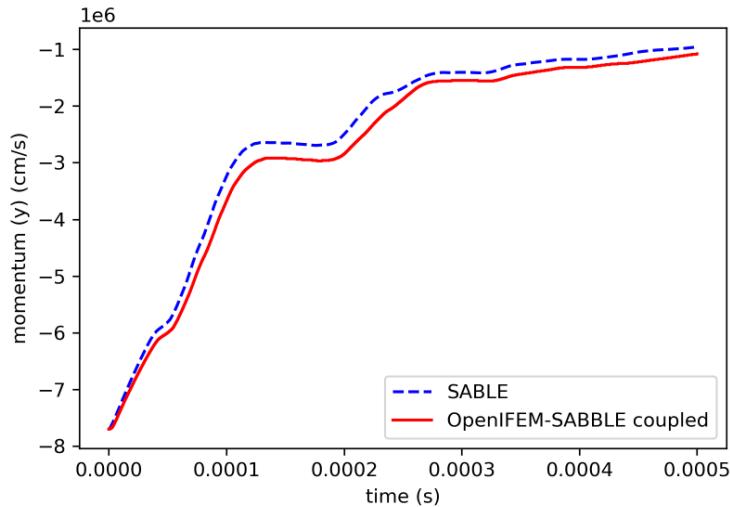


Target pressure (dyn/cm²) + Projectile velocity (cm/s)



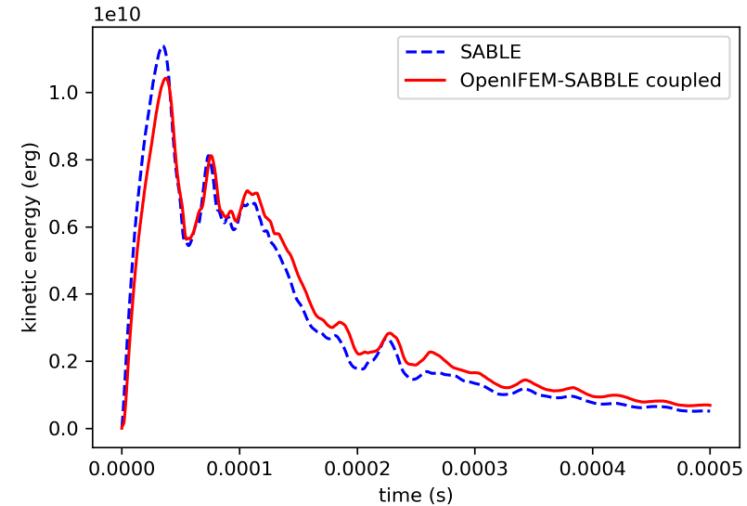
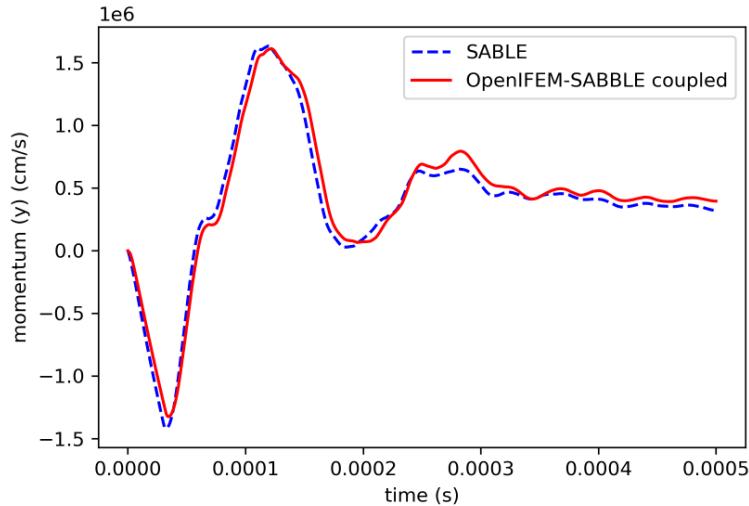
Test Case 1: Results

Projectile Results

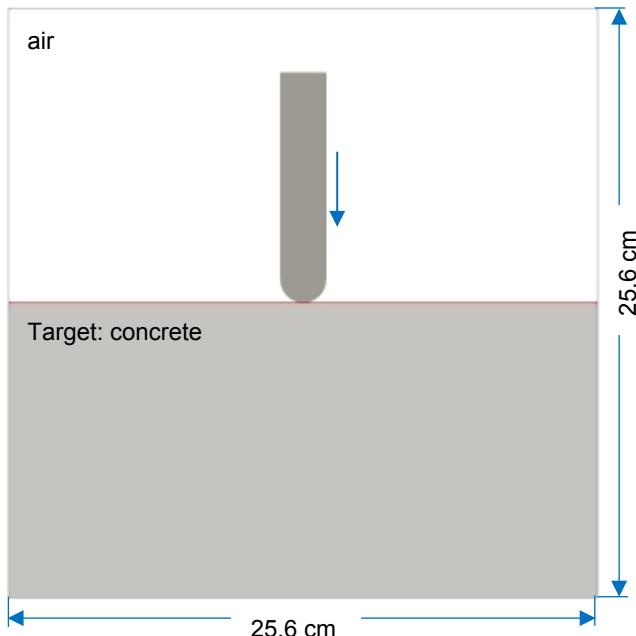


Test Case 1: Results

Target Results



Test Case 2: Setup



➤ Eulerian (target):

- Material: air + concrete
- Air:
 - Pressure: $1\text{e}6 \text{ dyn/cm}^2$
 - Density: $1.2\text{e}-3 \text{ g/cm}^3$
- Concrete:
 - Material mode: elastic-plastic
 - Compressive strength: 23 Mpa
 - Density: 2.03 g/cm^3
- BCs: no displacement at all sides
- Mesh: $\text{dx}=\text{dy}=0.1 \text{ cm}$

➤ Lagrangian (projectile):

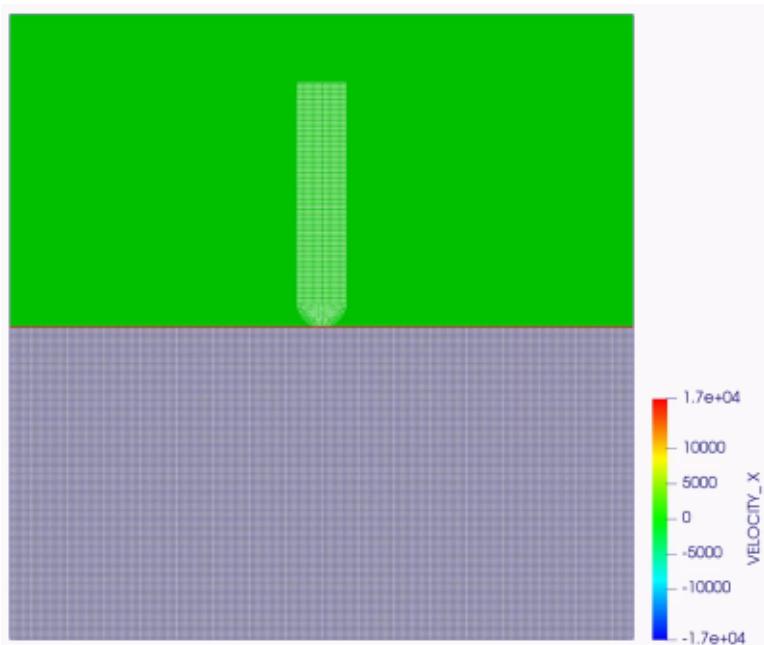
- Material: 4340 steel
 - Material model: linear elastic
 - $E: 20 \text{ GPa}$ $v: 0.28$
 - Density: 7.8 g/cm^3
- Mesh: $\text{dx}=\text{dy}=0.1 \text{ cm}$
- Initial velocity: **-50,000 cm/s**

➤ Simulation time: $5\text{e}-4 \text{ s}$

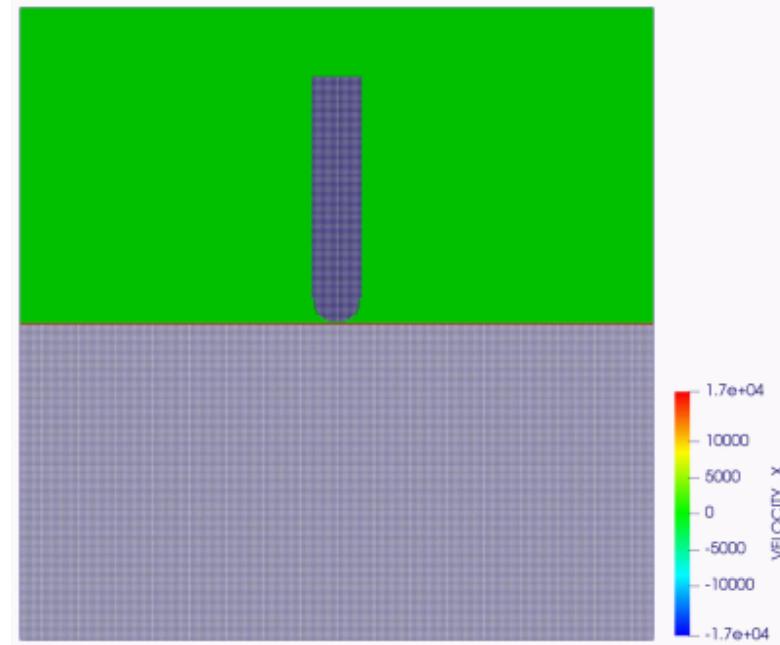


Test Case 2: Results

Air velocity x (cm/s): **OpenIFEM-SABLE coupled**

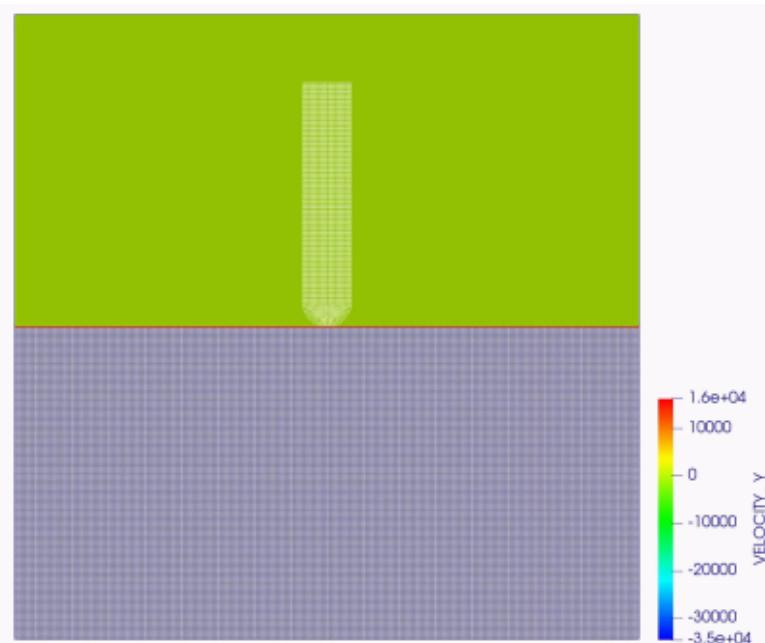


Air velocity x (cm/s): **SABLE**

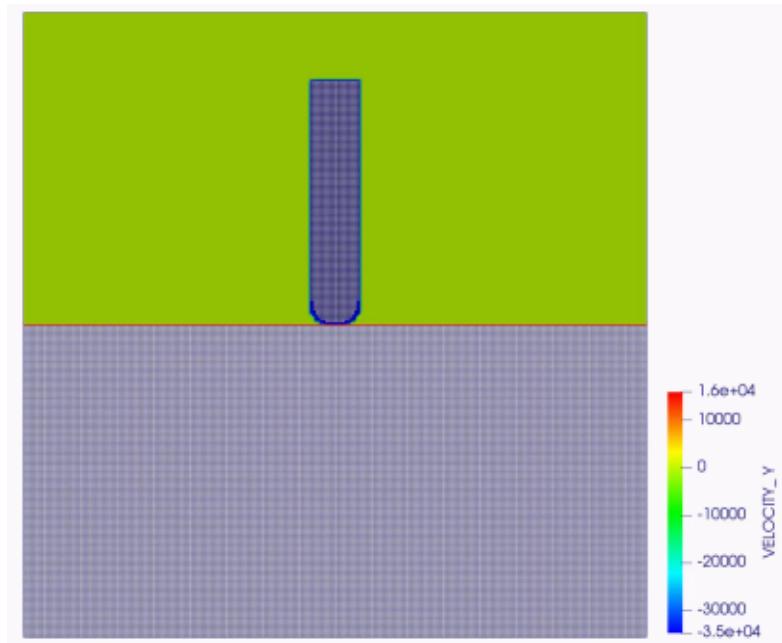


Test Case 2: Results

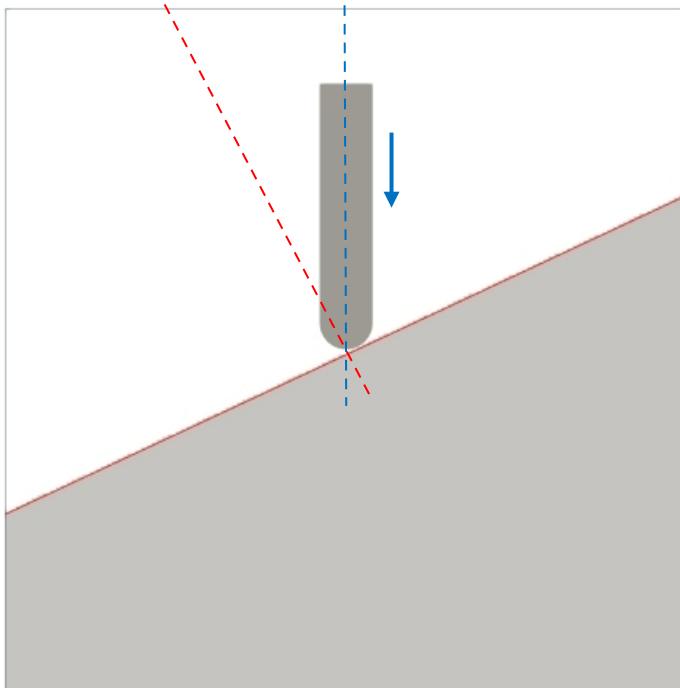
Air velocity y (cm/s): **OpenIFEM-SABLE coupled**



Air velocity y (cm/s): **SABLE**



Test Case 3: Setup

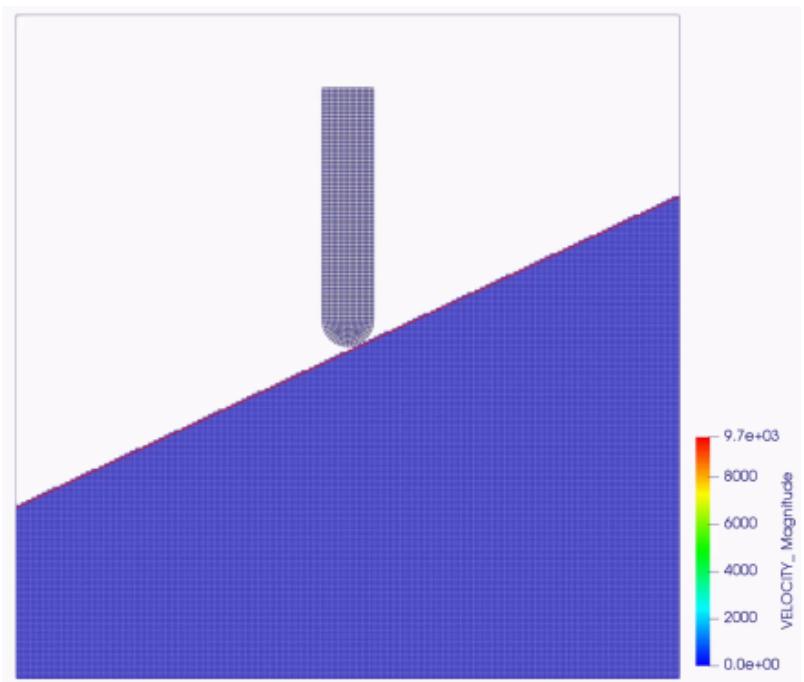


- **Oblique impact: $\theta = 25^0$**
- **Eulerian (target):**
 - Material: void + concrete
 - Concrete:
 - Material mode: elastic-plastic
 - Compressive strength: 23 MPa
 - Density: 2.03 g/cm³
 - BCs: no displacement at all sides
 - Mesh: dx=dy=0.1 cm
- **Lagrangian (projectile):**
 - Material: 4340 steel
 - Material model: linear elastic
 - E: 20 GPa ν : 0.28
 - Density: 7.8 g/cm³
 - Mesh: dx=dy=0.1 cm
 - Initial velocity: -50,000 cm/s
- **Simulation time: 5e-4 s**

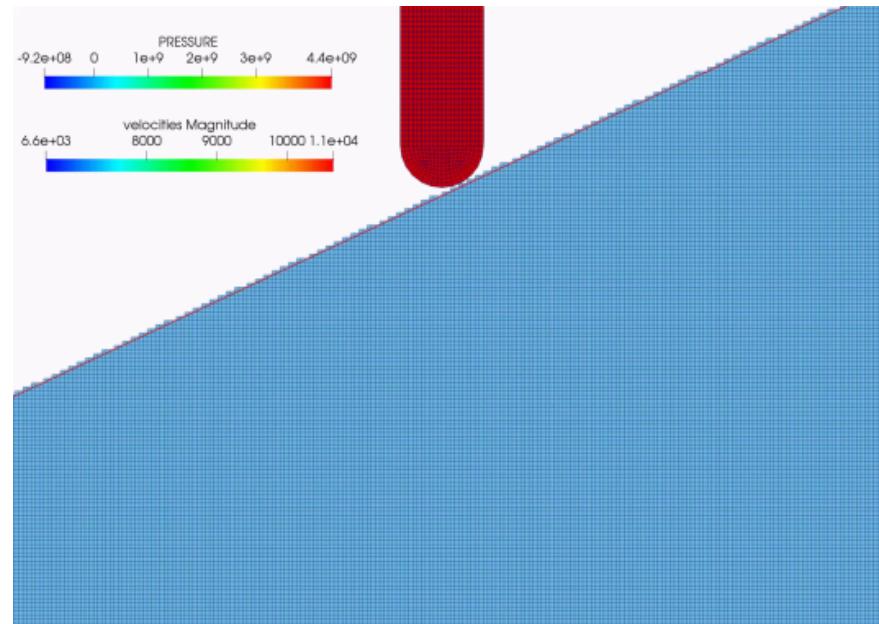


Test Case 3: Results

Target velocity (cm/s)

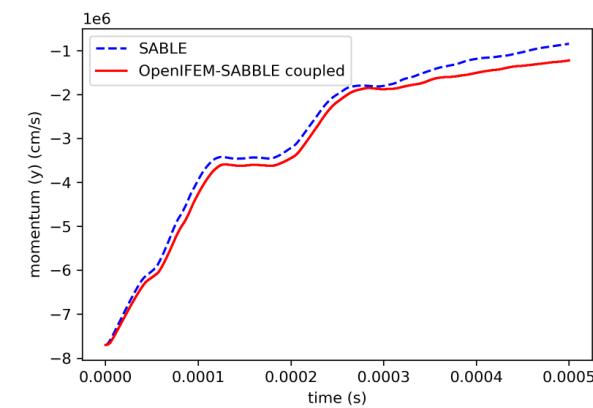


Target pressure (dyn/cm²) + Projectile velocity (cm/s)

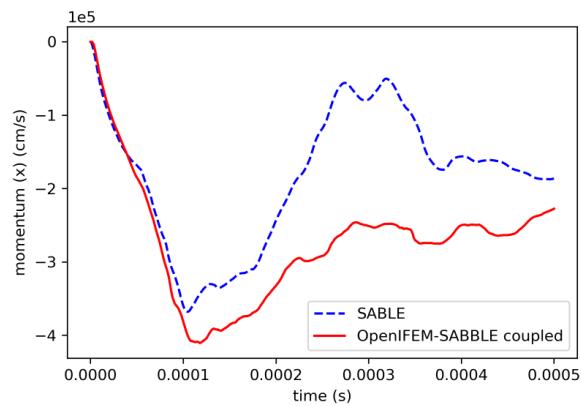


Test Case 3: Results

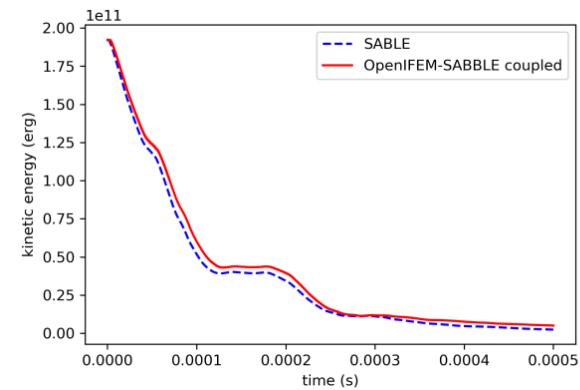
Projectile momentum (y)



Projectile momentum (x)

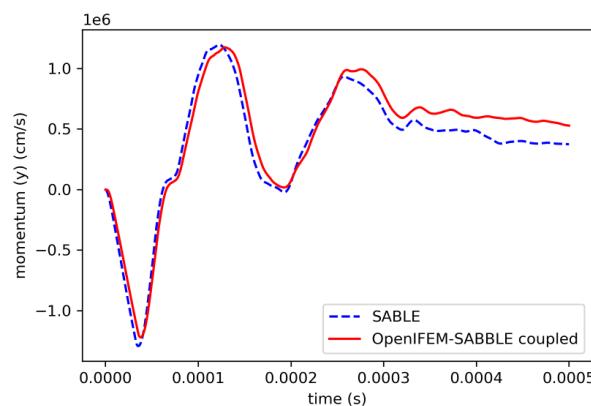


Projectile kinetic energy

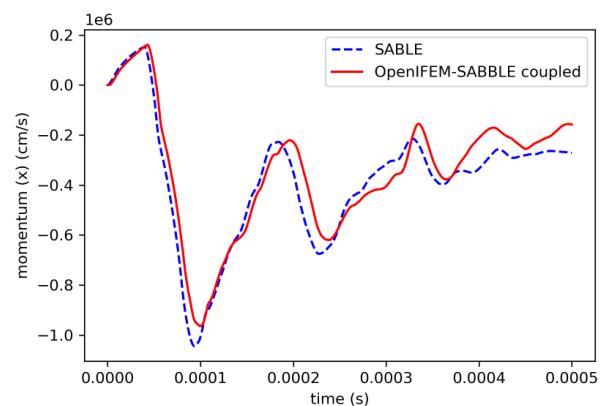


Test Case 3: Results

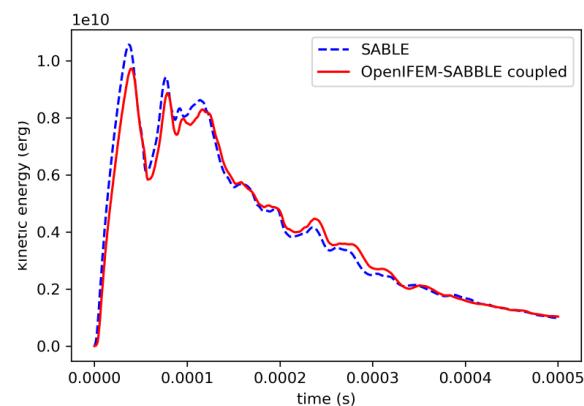
Target momentum (y)



Target momentum (x)

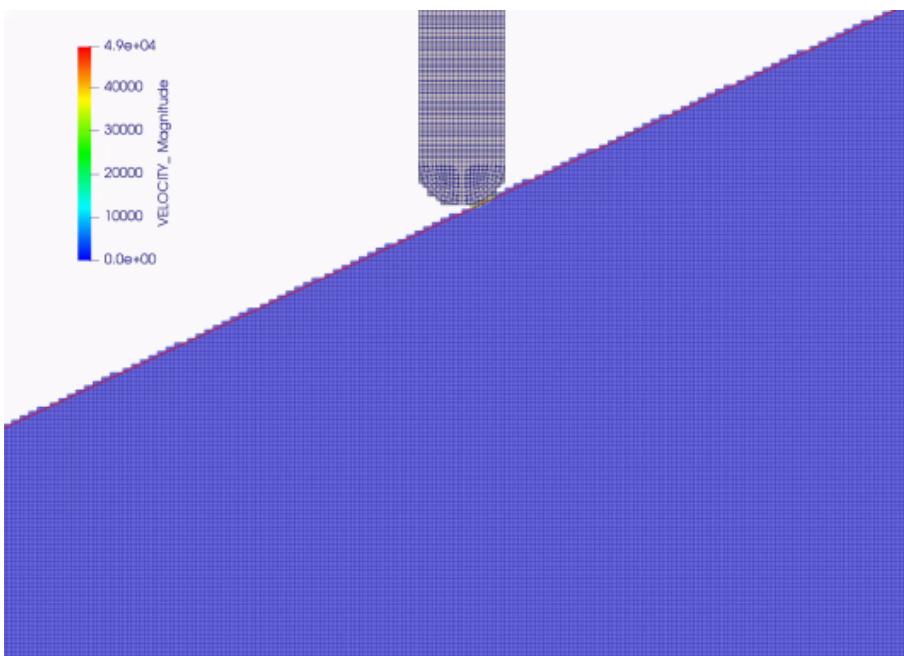


Target kinetic energy

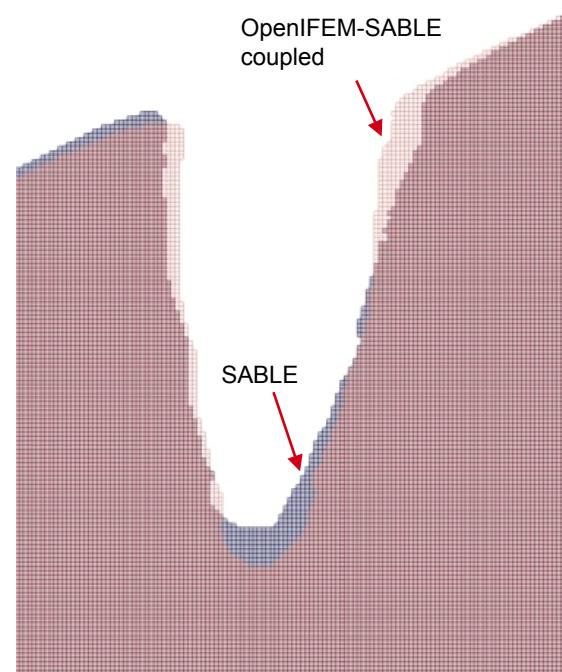


Test Case 3: Results

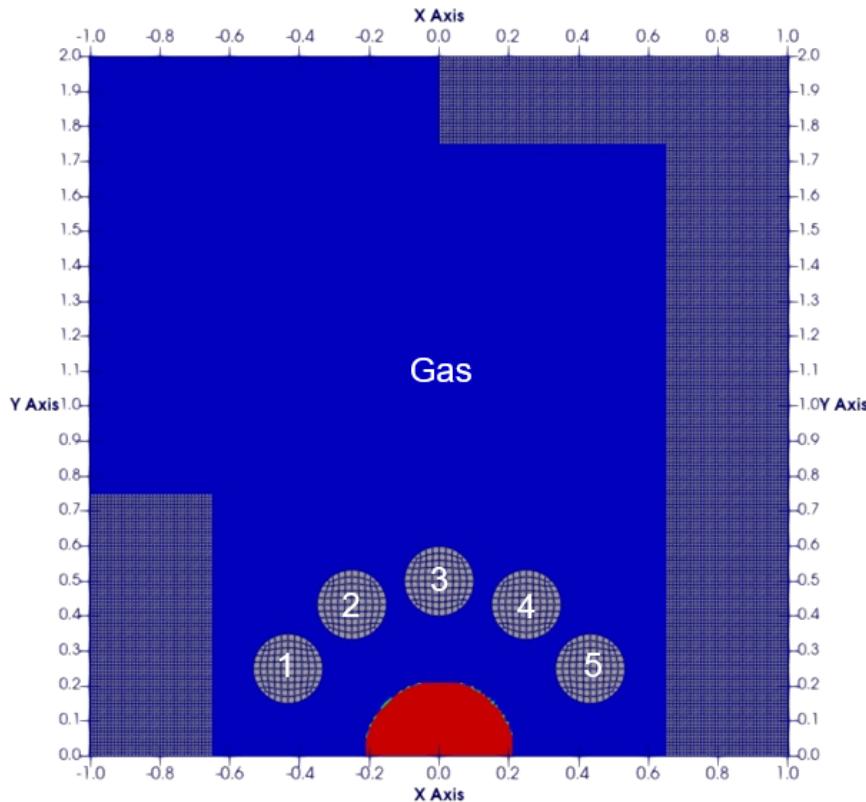
SABLE run: comparison with Lagrangian projectile



Target at $t=5\text{e-}4$ s



Test Case 4: Setup

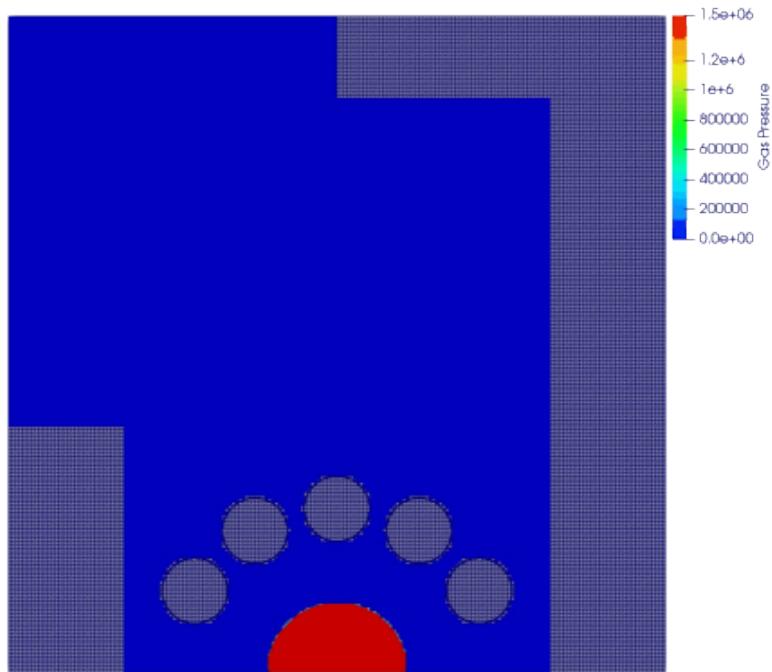


- **5 Plexiglass balls loaded by a high-pressure gas with moveable plexiglass walls**
- **Eulerian:**
 - **High-Pressure Gas Region**
 - $(x,y) = (0.0, 0.0)$, Radius = 0.3 cm
 - Initial Pressure: 10^8 dynes/cm²
 - **Low-Pressure Gas Region**
 - Initial Pressure: 10^{-5} dynes/cm²
 - Initial Density: 1 gm/cm³
- **Lagrangian:**
 - Plexiglass balls, Radius = 0.1 cm
 - Ball-1: $(x,y) = (-0.433, 0.2500)$
 - Ball-2: $(x,y) = (-0.2500, 0.4330)$
 - Ball-3: $(x,y) = (0.0000, 0.5000)$
 - Ball-4: $(x,y) = (0.2500, 0.4330)$
 - Ball-5: $(x,y) = (0.4330, 0.2500)$
 - Plexiglass properties
 - Hyperelastic Neo-Hookean material
 - $c1 = 4.85e11$ dynes/cm² $c2 = 1.35e12$ dynes/cm²
 - Density: 1.18 gm/cm³
- Simulation time: 6e-4 s

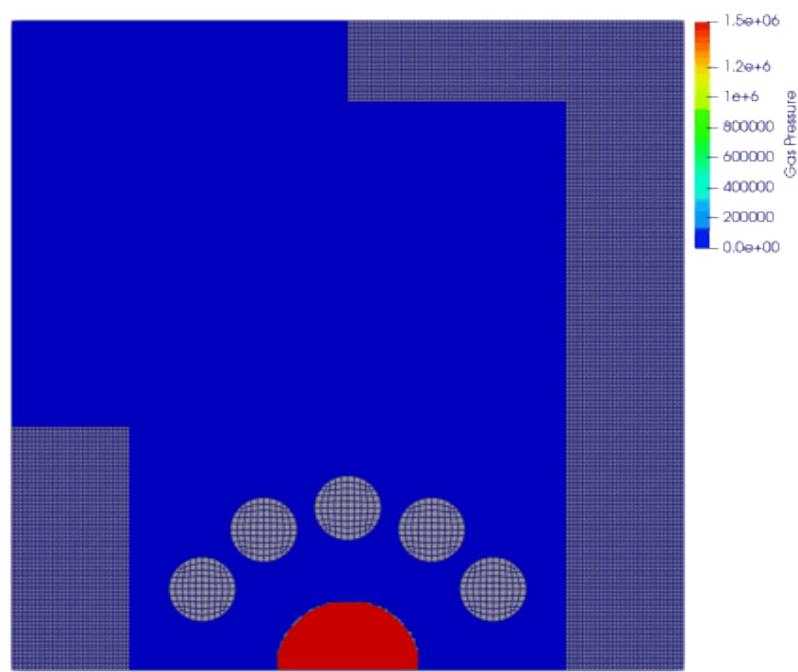


Test Case 4: Results

Gas pressure (dyn/cm²): **SABLE**

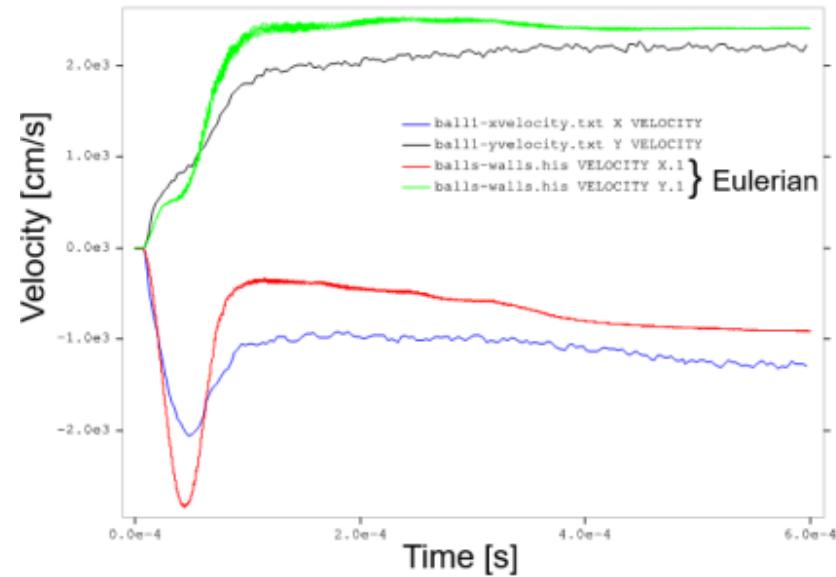
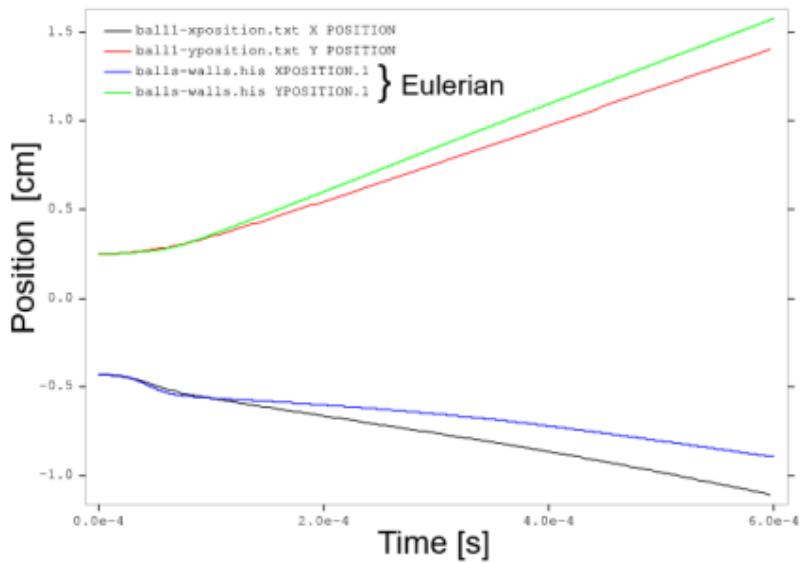


Gas pressure (dyn/cm²): **OpenIFEM-SABLE coupled**



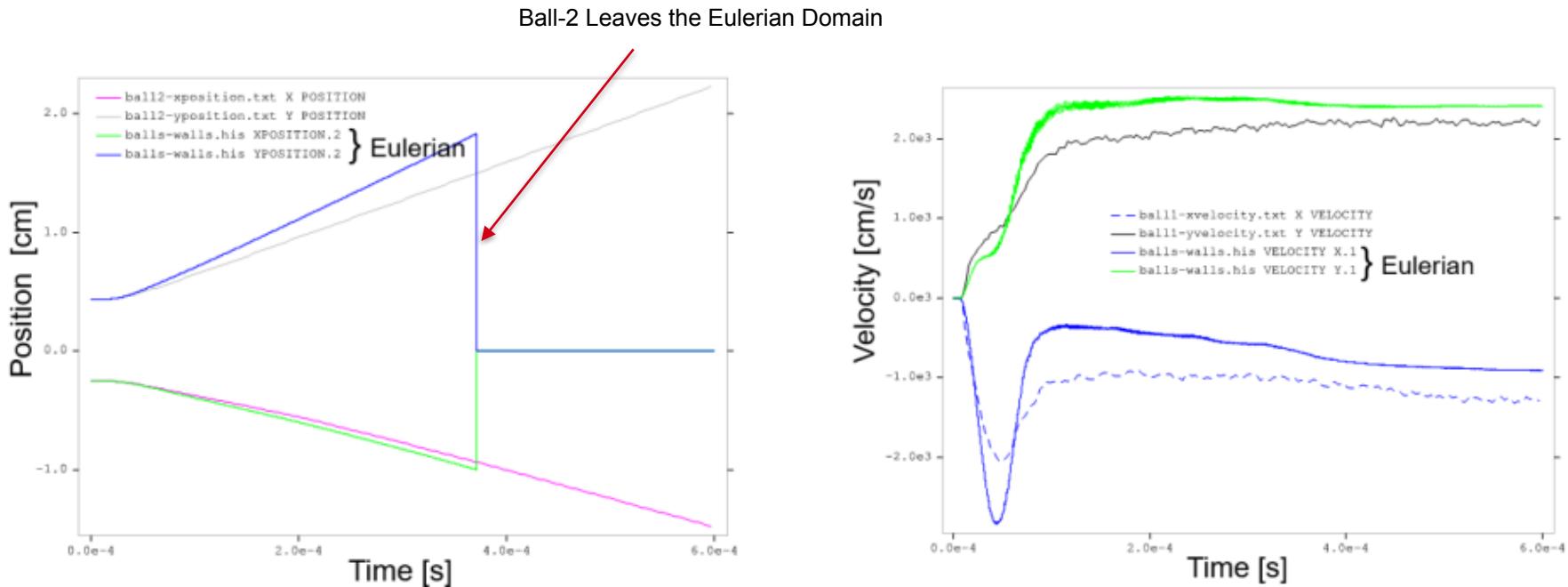
Test Case 4: Results

Ball-1:



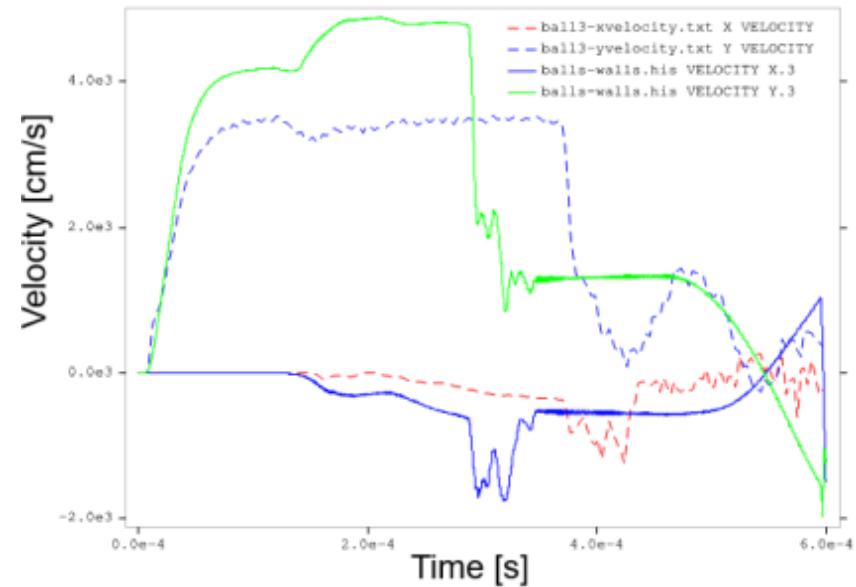
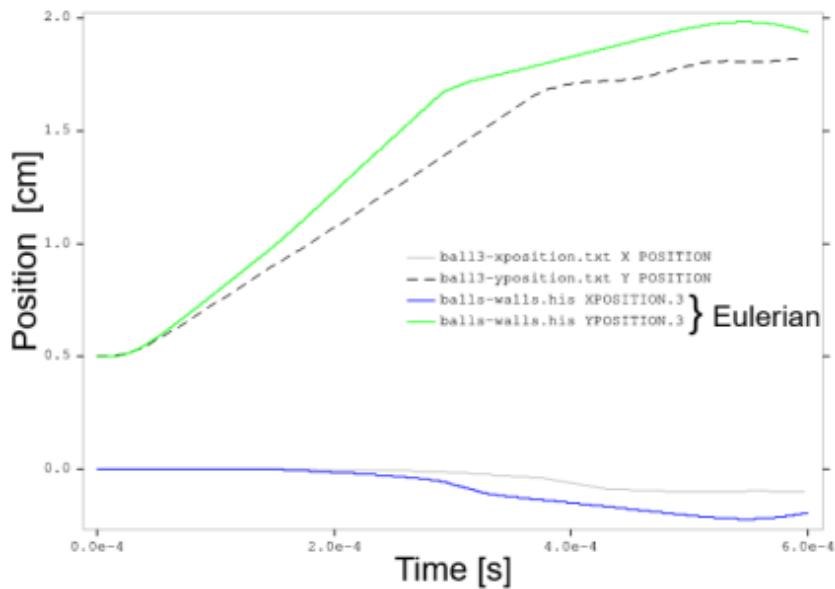
Test Case 4: Results

Ball-2:



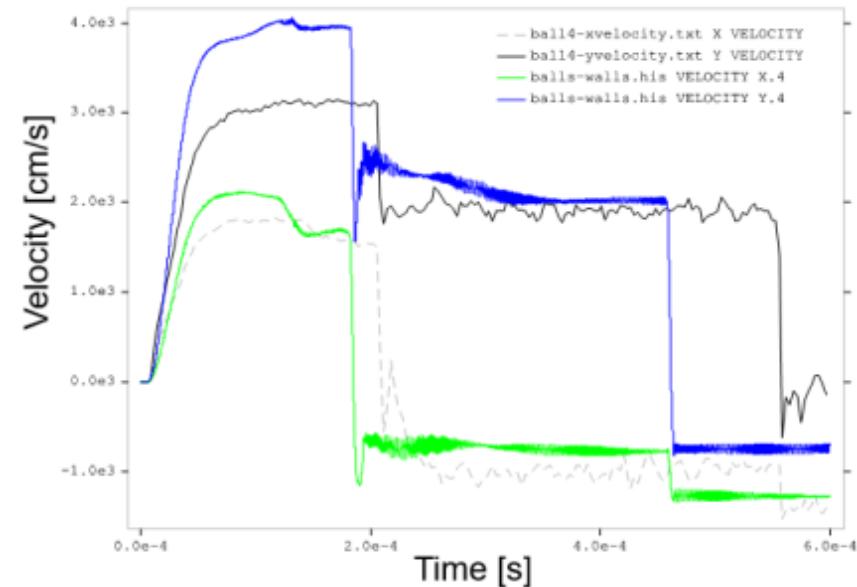
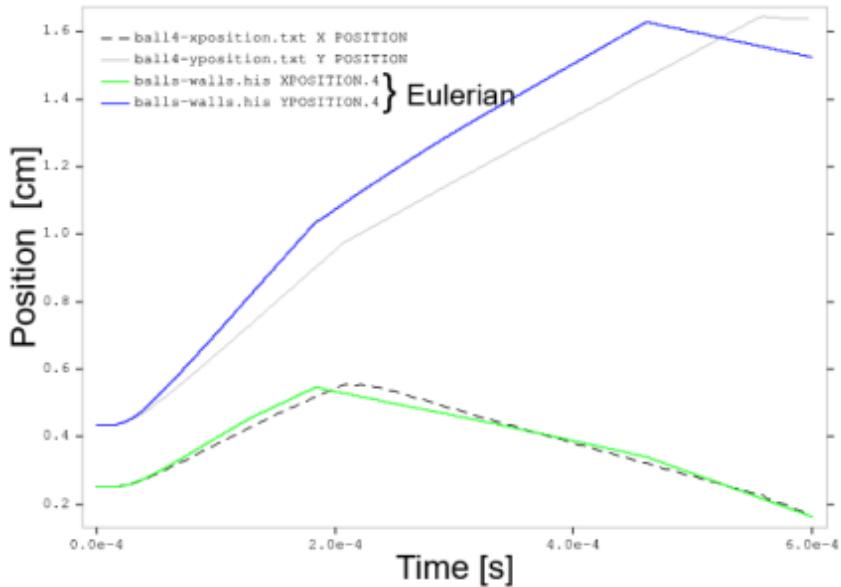
Test Case 4: Results

Ball-3:



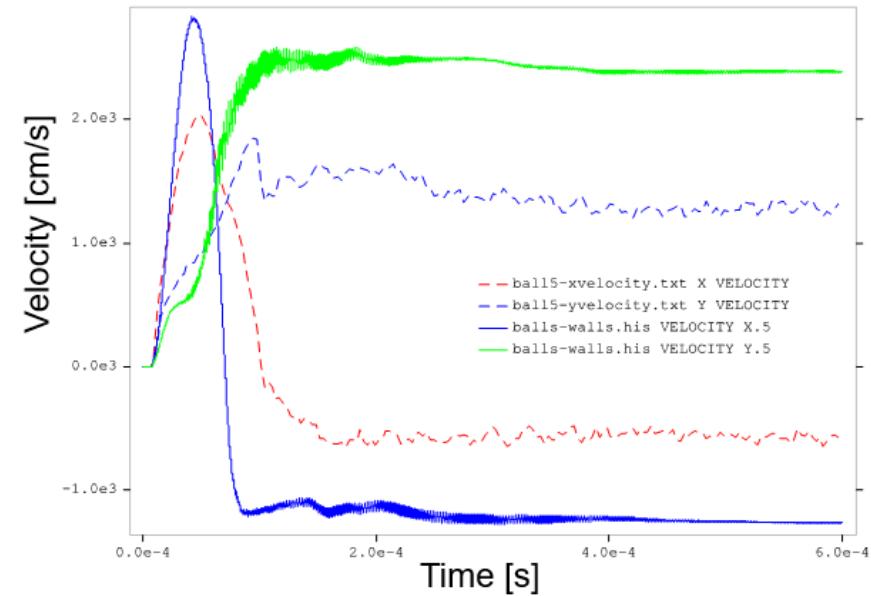
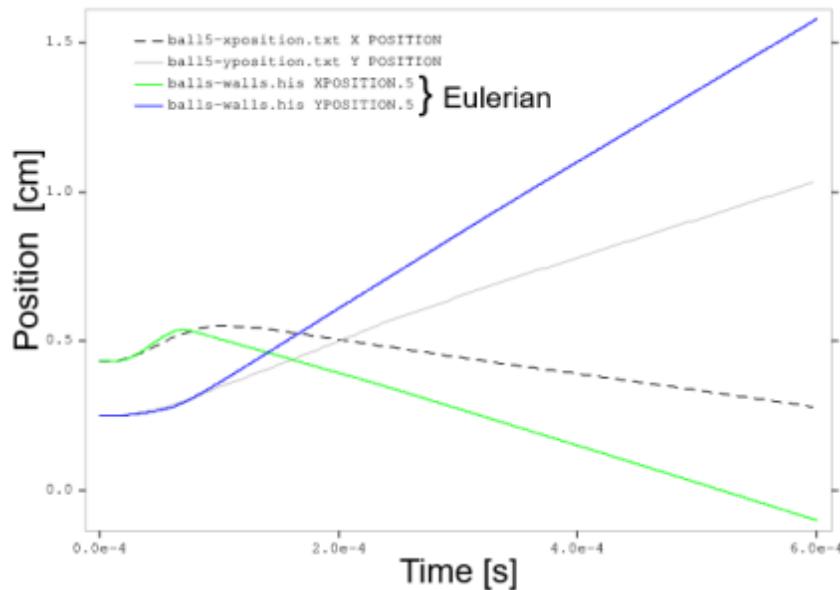
Test Case 4: Results

Ball-4:

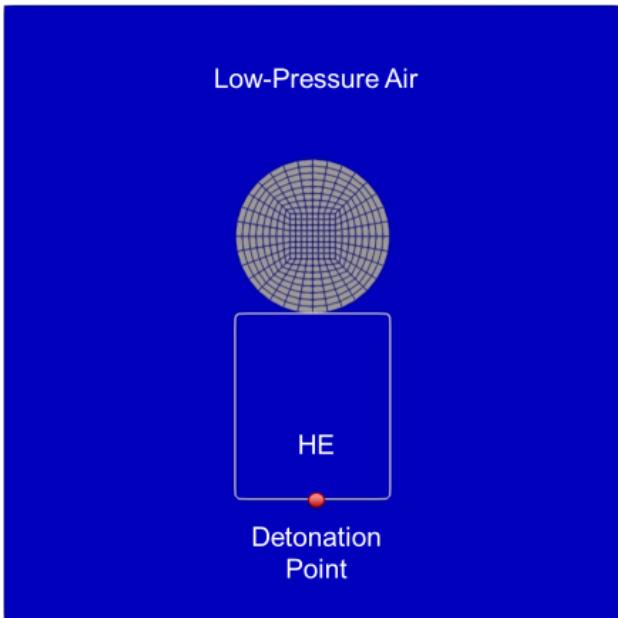


Test Case 4: Results

Ball-5:



Test Case 5: Setup



➤ **Eulerian Domain:**

- $(-5.0, 0.0) \leq (x, y) \leq (15.0, 20.0)$ [cm]
- Mesh size: $h = 0.1$ [cm]
- Low-Pressure Air: $P = 10^{-5}$ [dynes/cm²]
- High Explosive: $(2.5, 4.0) \leq (x, y) \leq (7.5, 10)$ [cm]
- Tracer Location: $(x, y) = (4.5, 12.5)$ [cm]

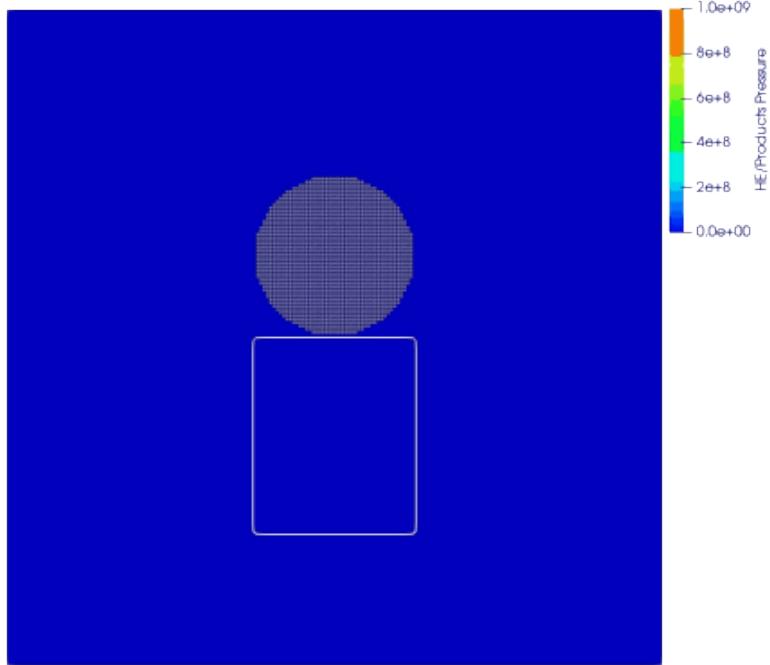
➤ **Lagrangian Solid:**

- Ball Position: $(x, y) = (4.5, 12.5)$
- Linear Elastic material
- Density: 7.8724 [g/cm³]
- Young's Modulus: $E = 200 \times 10^{10}$ [dynes/cm²]
- Poisson's ratio: $\nu = 0.28$
- Mie Gruenesien EOS for Eulerian simulation

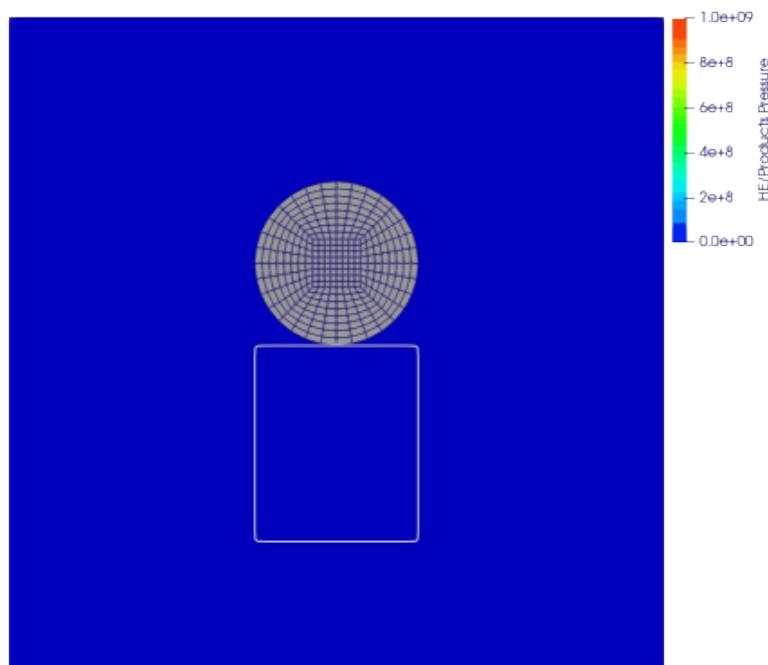


Test Case 5: Results

Gas pressure (dyn/cm²): **SABLE**



Gas pressure (dyn/cm²): **OpenFEM-SABLE coupled**



Summary

- Develop framework for **simulation solid-solid interaction** and impact using **modified Immersed Finite Element Method**.
- **Non-intrusively couple** OpenIFEM and SABLE.
- Penetrator: **Lagrangian** description, Target: **Eulerian** description
- Future Work:
 - Extend coupling for **3D simulations**.
 - Investigate application of a **contact model**.
 - Validate coupling with **literature reported test cases**.



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