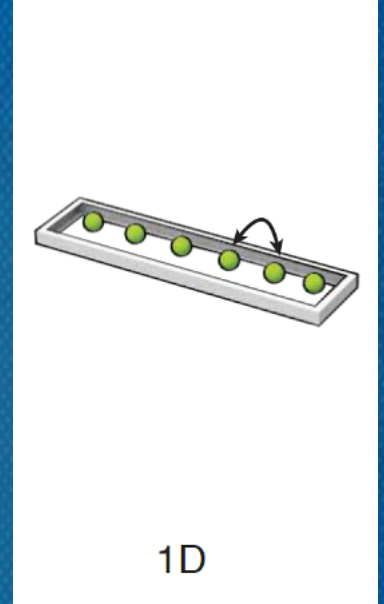
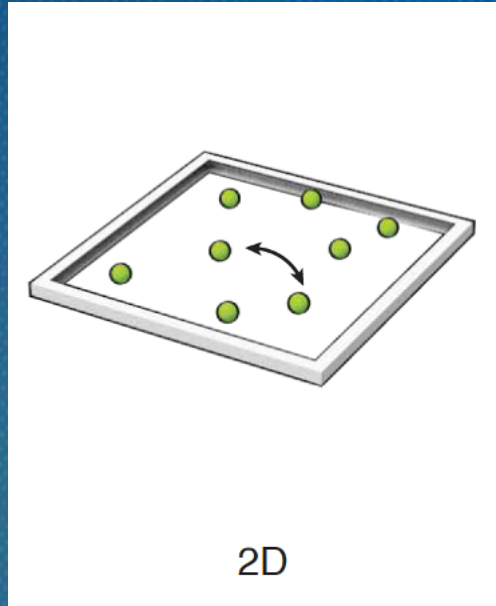
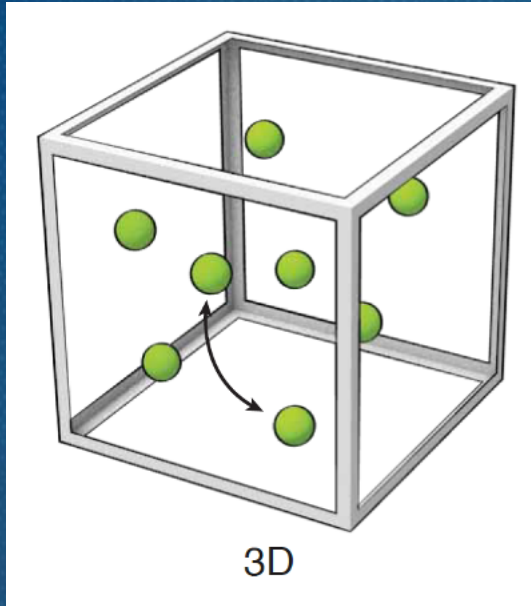


FABRICATION AND TRANSPORT PHENOMENON IN LOW -DIMENSIONAL SYSTEMS COUPLED AT THE NANOSCALE

Dominique Laroche

American Vacuum Society - Florida – Symposia
May 6th, Orlando, FL

Low-dimensional systems



Reduced scattering phase-space in low dimensional systems.



Increased interactions



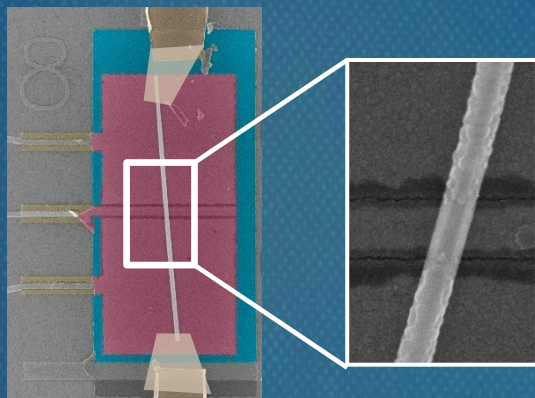
Novel and exciting
quantum phenomenon :

- Integer and Fractional quantum Hall effect
- Luttinger liquid physics
- Non-Fermi liquids
- Quantum dots/ quantum computing
- ETC.

Coupled low-dimensional systems

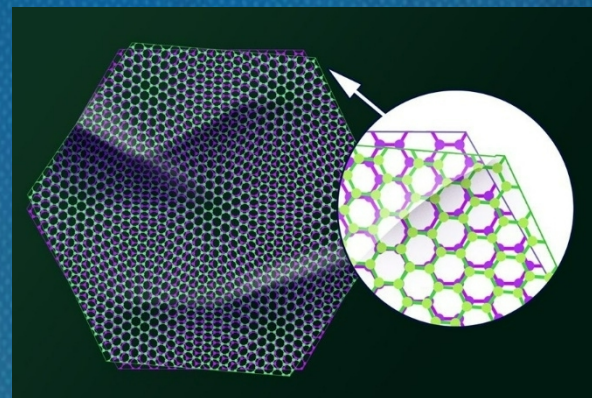
Additional properties to engineer novel quantum phenomena / phases

MBS signatures in hybrid SM-SC nanowires



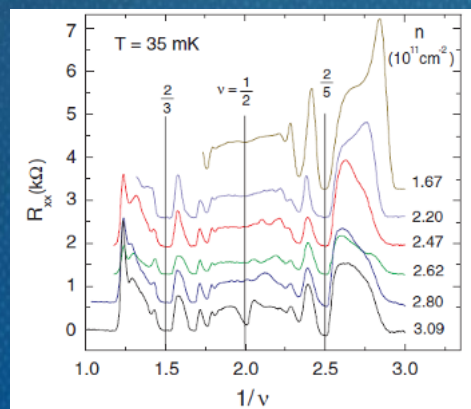
D. Laroche *et al.* Nature Comm. **10**, 245 (2019)

Superconductivity in graphene



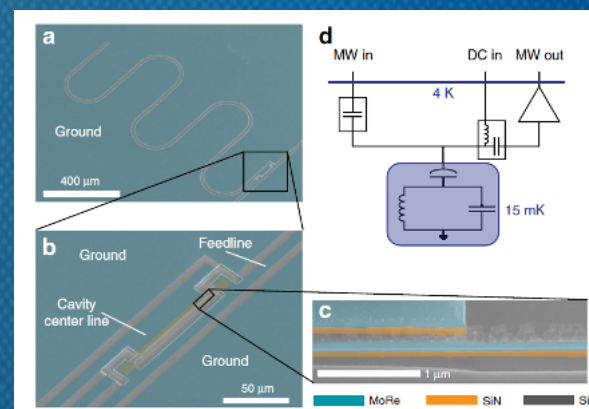
Y. Cao *et al.* Nature **556**, 43 (2018)

Exotic FQHE states



J. Shabani *et al.* PRL 103, 256802 (2009)

Electromechanics in the quantum limit



D. Bothner *et al.* Nature Comm. **11**, 1589 (2020)

- Introduction to low-dimensional systems
- Search for exciton condensation in Si quantum wells
 - Si/SiGe quantum wells
 - Exciton condensation
 - Device fabrication
 - Excitation gaps in the quantum Hall regime
- Coulomb drag between quantum wires
 - Luttinger liquids
 - Coulomb drag technique
 - Device fabrication
 - Coulomb drag measurements in laterally-coupled quantum wires

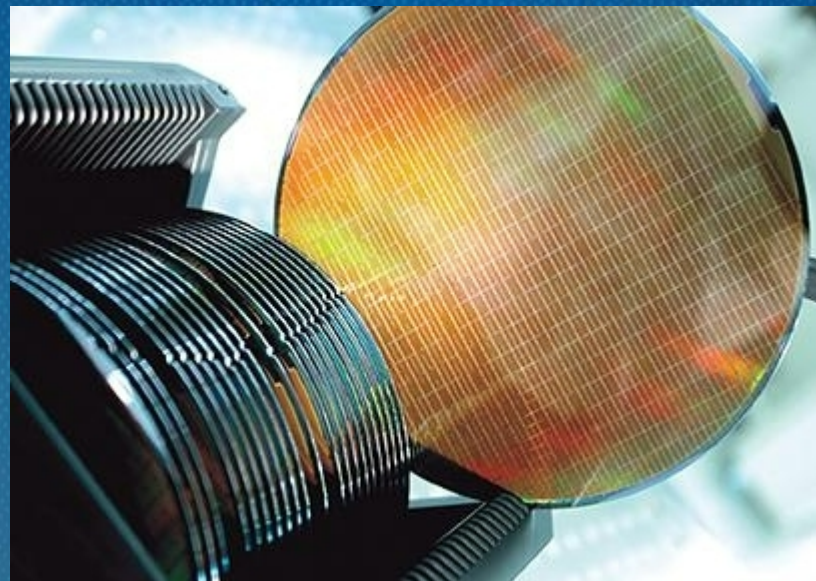
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 - Coulomb drag measurements in laterally-coupled quantum wires



Search for exciton condensation
in Si quantum wells

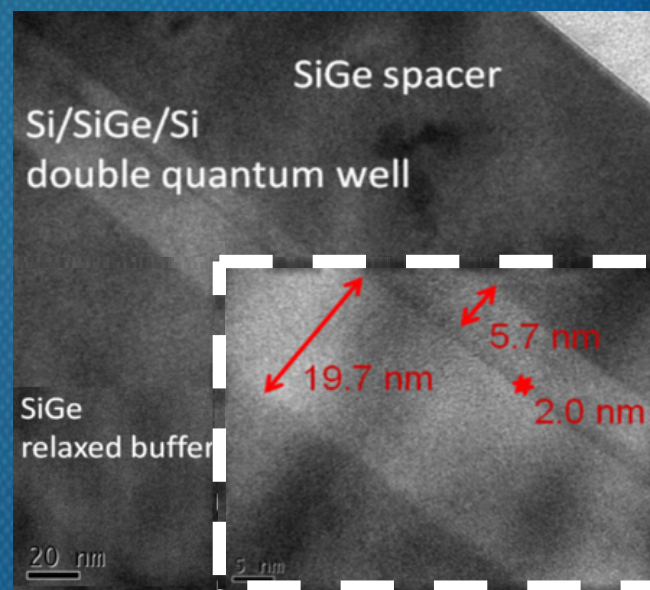
Why

- Low disorder system
- Scaling potential with CMOS foundries
Resistanceless devices
Quantum computing
- New degree of freedom : valley



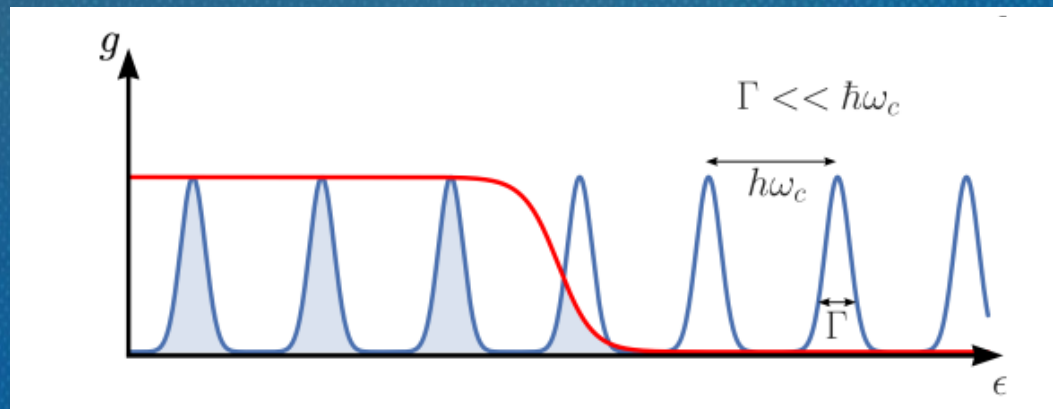
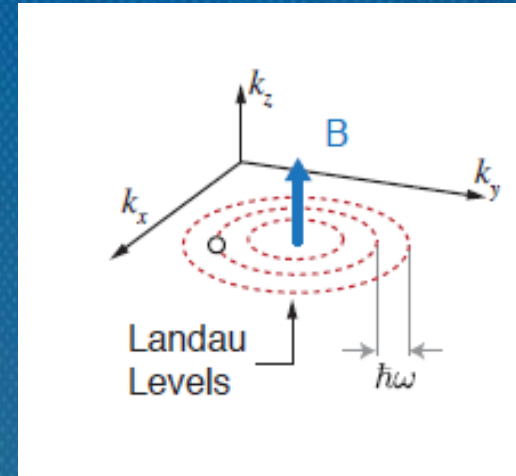
How

- UHVCVD growth;
Ultra High Vacuum Chemical Vapor Deposition



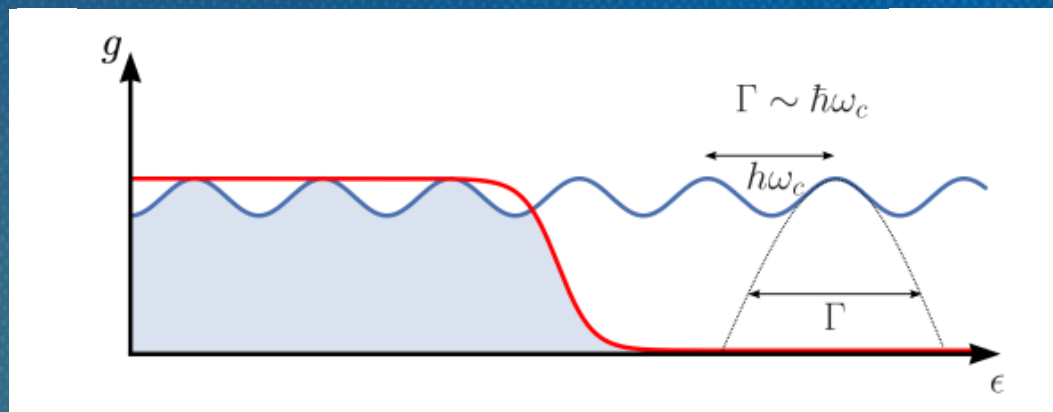
Quantum Hall effect

Electron motion of 2D electrons gets quantized in Landau levels with a magnetic field.

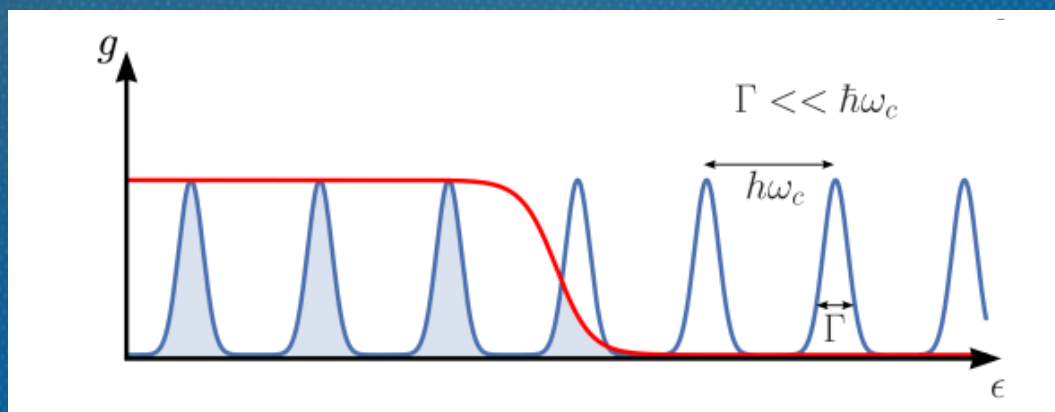


Large B, low T and disorder

Quantum Hall effect

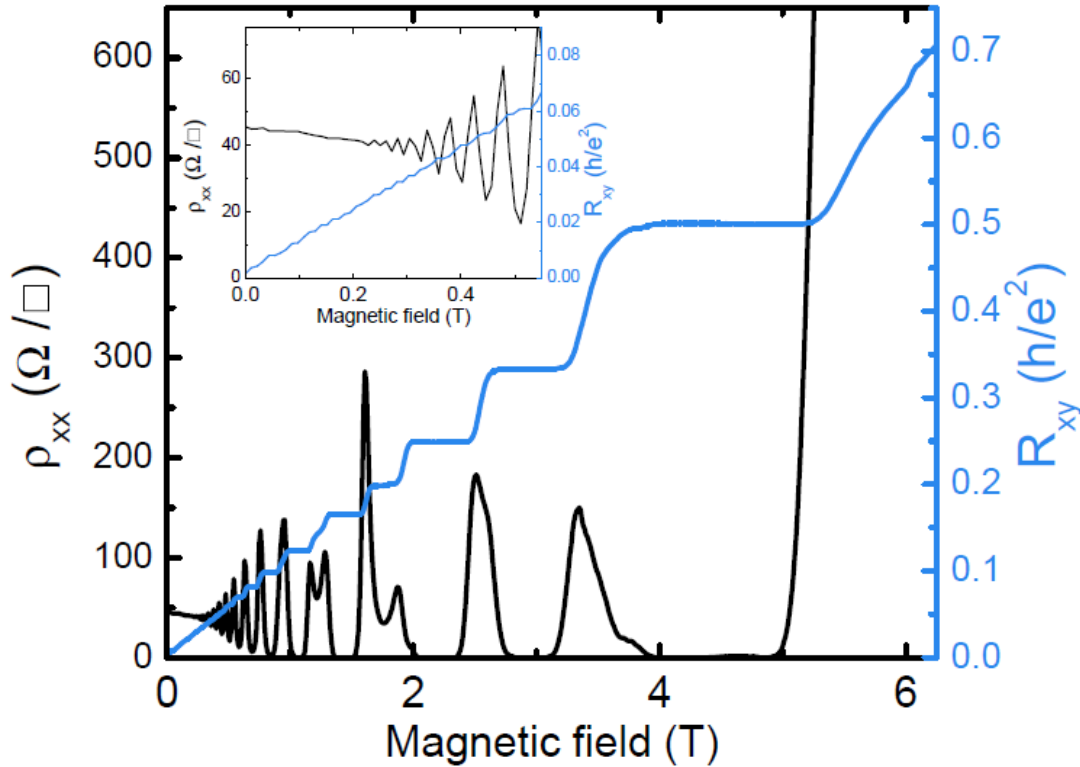


Low B, High T and disorder

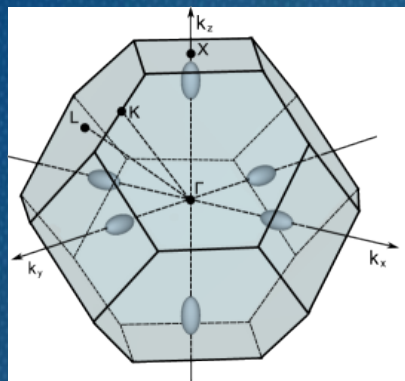


Large B, low T and disorder

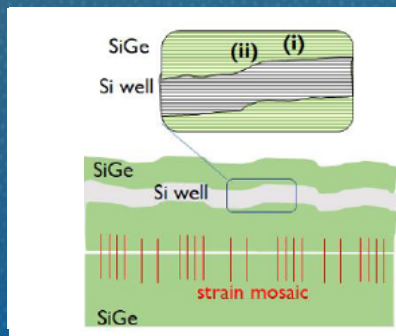
Quantum Hall effect



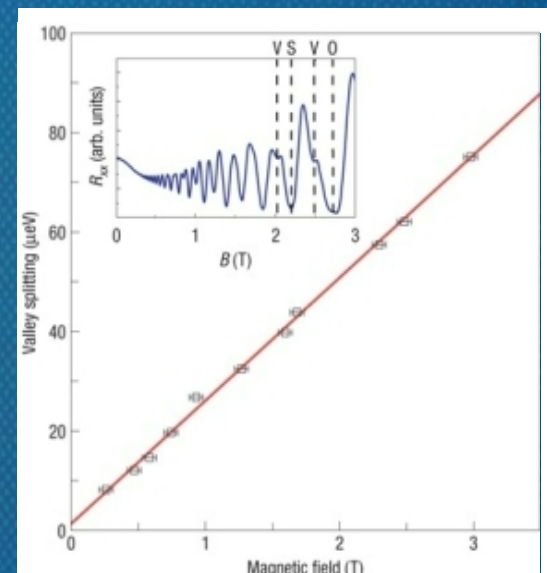
Si/SiGe : Valley splitting in single layer



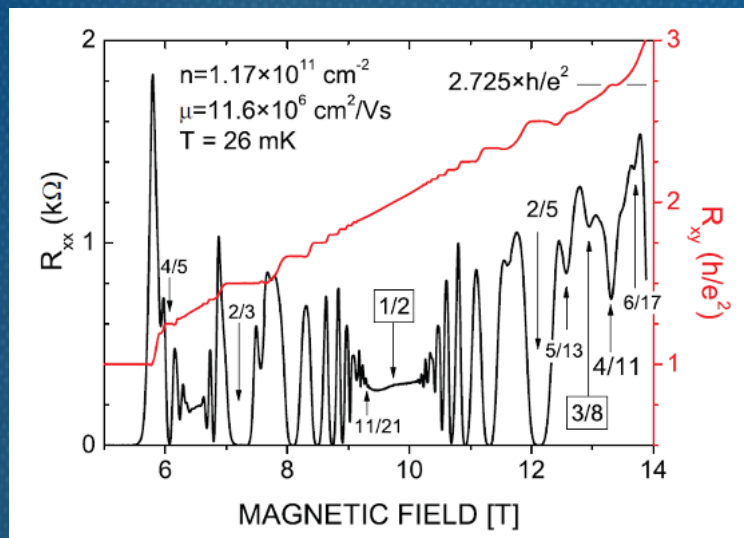
- Silicon has 6 degeneracies
- Vertical confinement + strain \rightarrow m_l (2x degenerate)
 m_t (4x degenerate)
- Sharp interface \rightarrow Lifts m_l degeneracy $\rightarrow \Delta v$
- Interface disorder \rightarrow Destructive interference
 \rightarrow lowers ΔE_v



Theory matches experiments :
 $\Delta E_v \sim C_v B + \Gamma$

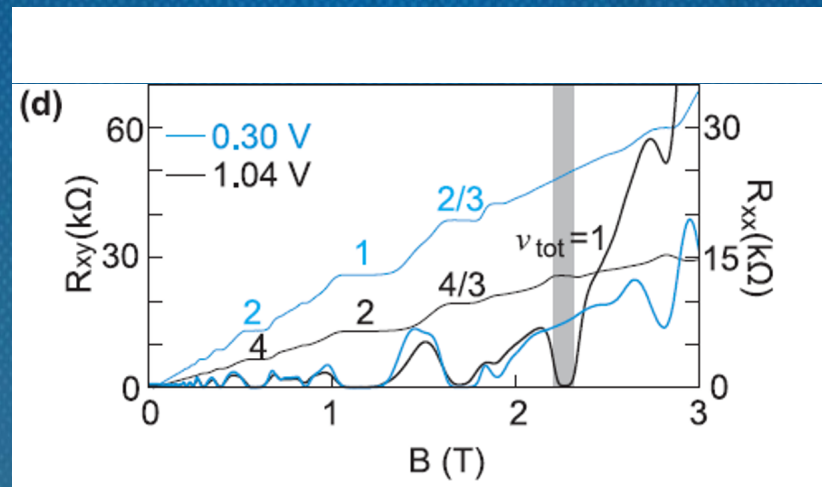


$\nu_{\text{tot}} = 1$ quantum Hall state



W. Pan *et al.* PRB **91**, 041301(R) (2015)

Single layers \rightarrow no $\nu = 1/2$ quantum Hall state.



D. Zhang *et al.* PRB **87**, 205304 (2013)

Two independent bilayers (matched density) :

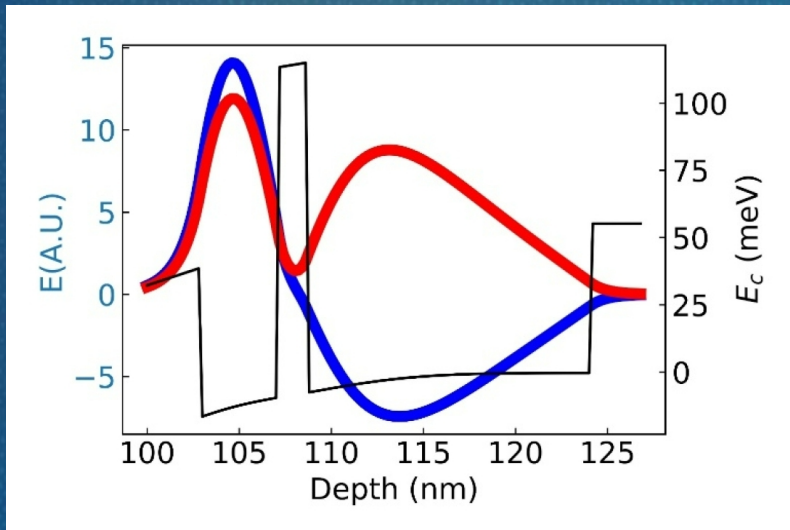
$\nu_{\text{tot}} = 1 \rightarrow \nu_{1/2} + \nu_{1/2} = \text{no quantum Hall state}$

At low density and small separation, a quantum Hall state at $\nu_{\text{tot}} = 1$ is observed!

$\nu_{\text{tot}} = 1$ quantum Hall state

Bilayers : new degree freedom
 \hookrightarrow Layer.

Leads to Δ_{SAS} between symmetric (S) and anti-symmetric (AS) states.

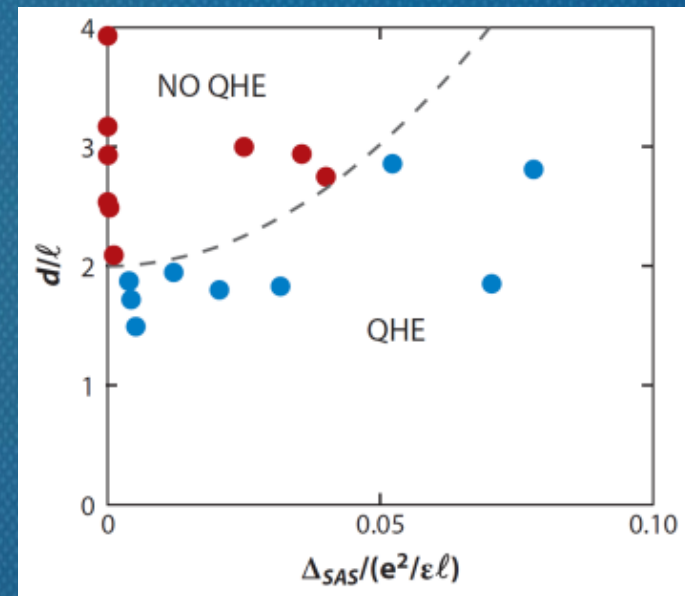


Easily captured through SP simulations

If intra- and inter-layer energies are comparable \rightarrow Spontaneous interlayer coherence.

Only visible for $d/l_b < 1.8$.

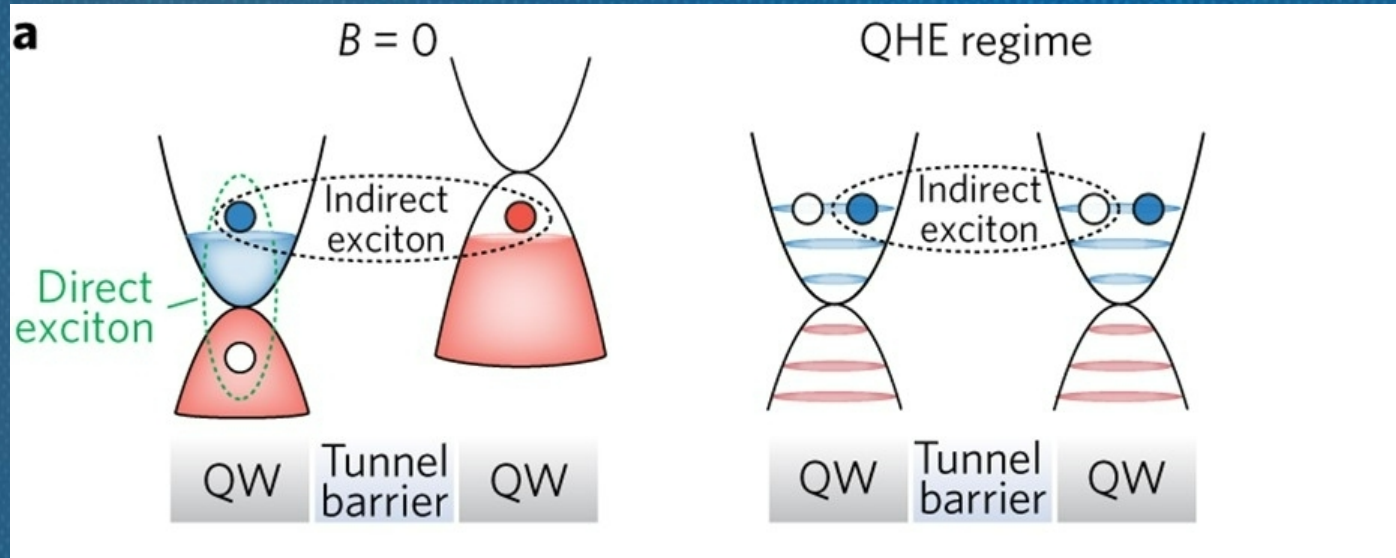
Occurs even for negligible tunneling.



Exciton condensation

Pairing of an electron and a hole \rightarrow Boson

Low-temperature \rightarrow Condensation to a phase-coherent ground state



Direct excitons : Photo-induced \rightarrow short lifetime \sim ps to fs

Indirect excitons : Separated electron-hole pairs \rightarrow longer lifetime \sim μ s to ns

$B = 0 \rightarrow$ Large interlayer voltage in undoped systems

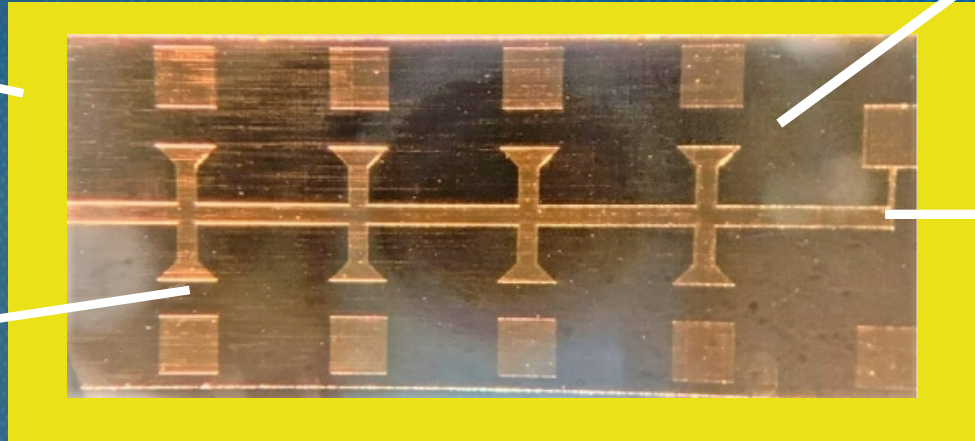
Instabilities / Leakage

QHE at half filling \rightarrow More robust platform

Si/SiGe bilayers

Fabrication

Back gate

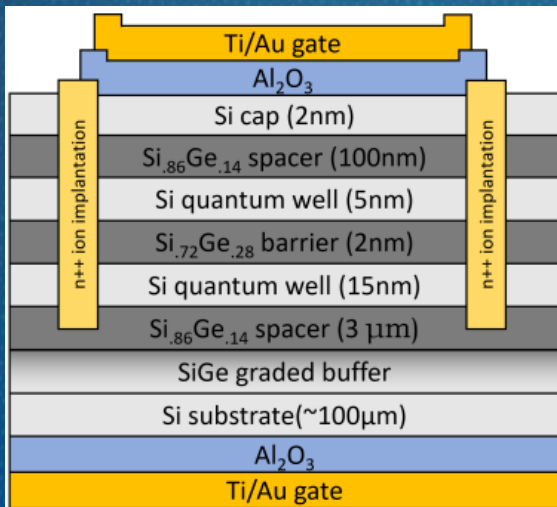


Al_2O_3 dielectric layer

Top gate

Ion implanted
contacts

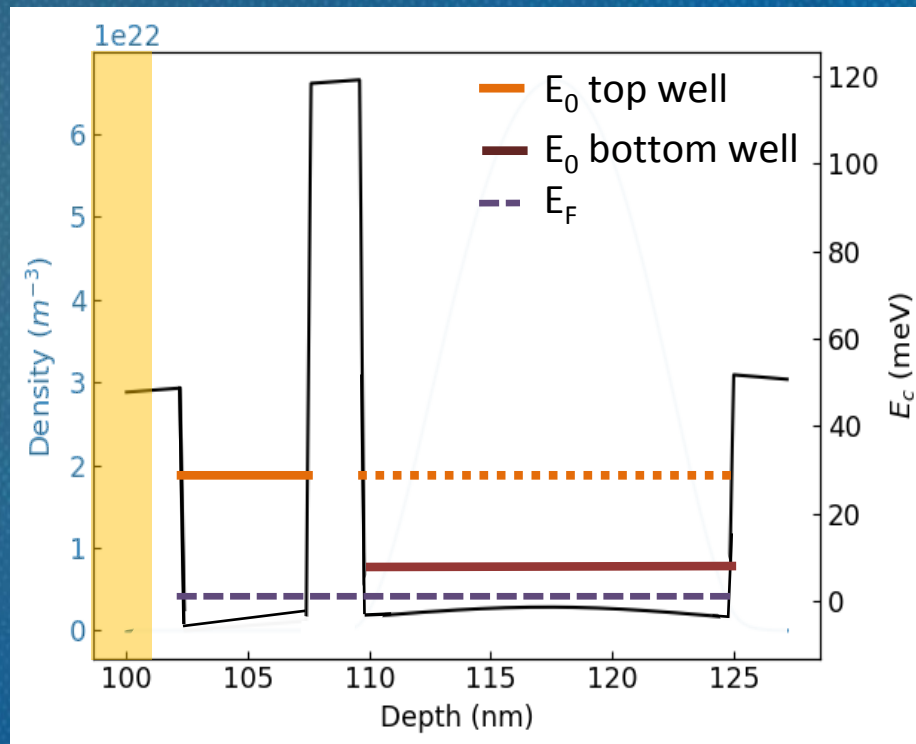
Device



- Front and back gate capabilities
- Hall densities from $5 \times 10^{10} \text{ cm}^{-2}$ to $3.4 \times 10^{11} \text{ cm}^{-2}$; Hall mobility up to $3.08 \times 10^5 \text{ cm}^2/(\text{V} \cdot \text{s})$

Asymmetric design

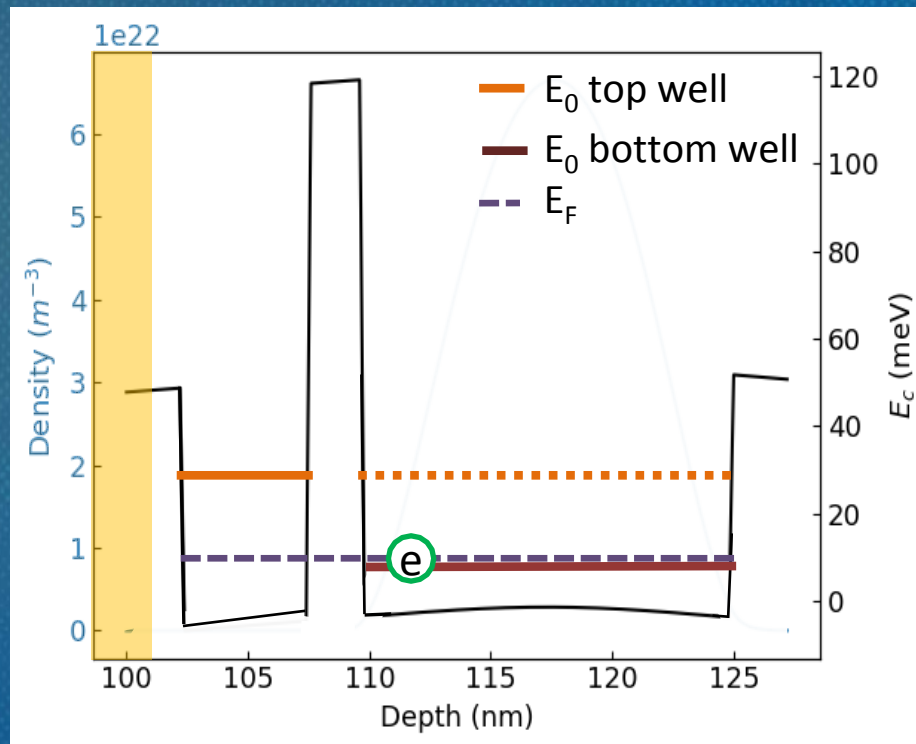
$$V < V_{th}$$



$$E = E_0 + \frac{\hbar^2}{2m^*} (k_x^2 + k_y^2)$$

Asymmetric design

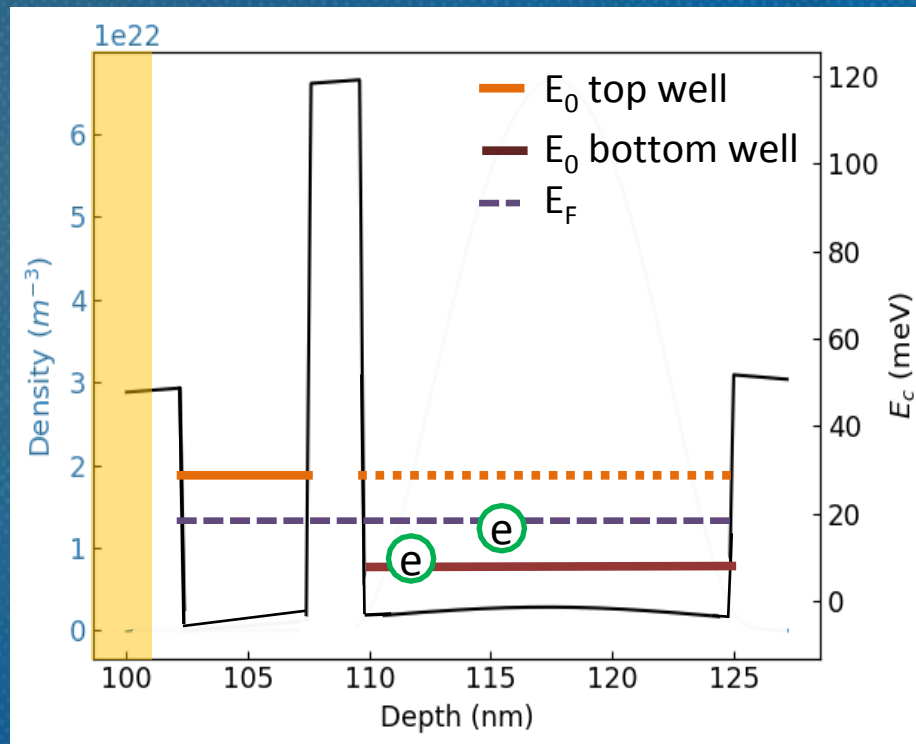
$$V < V_{th}$$



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Asymmetric design

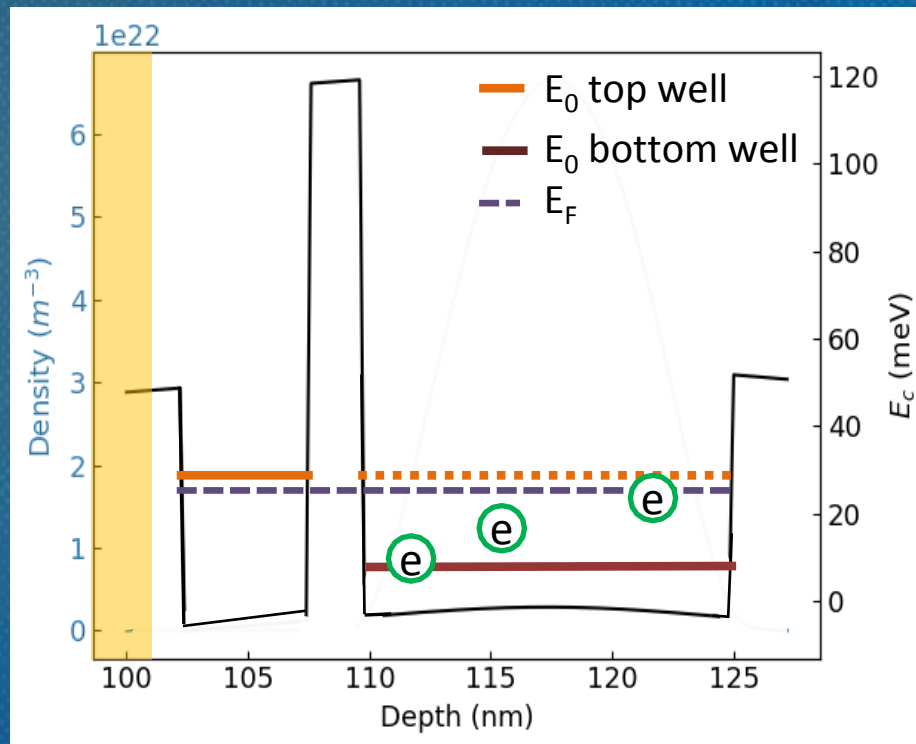
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Asymmetric design

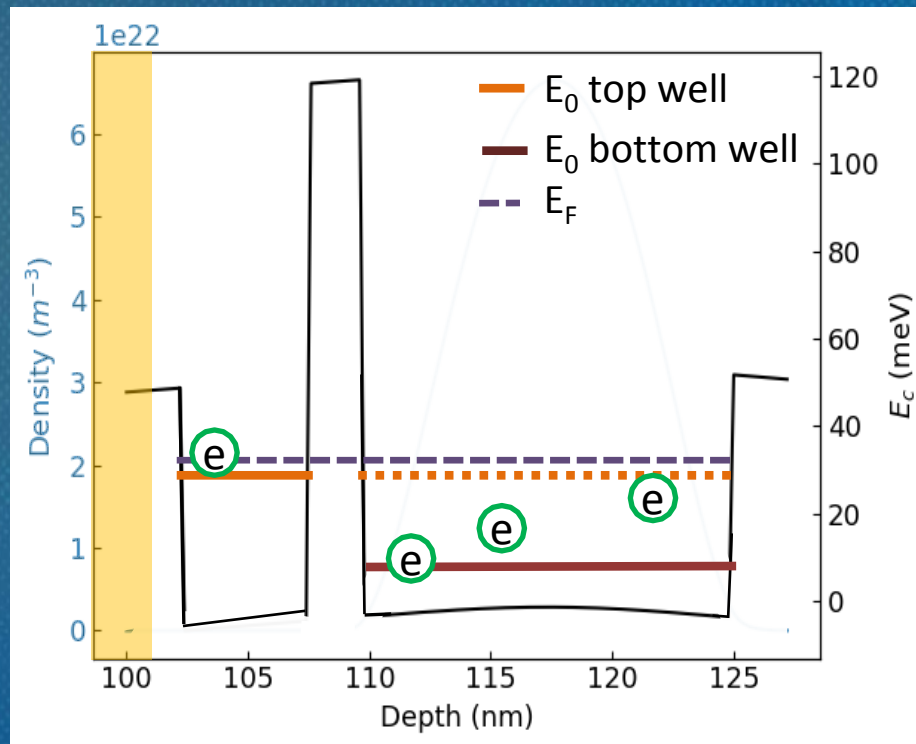
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Asymmetric design

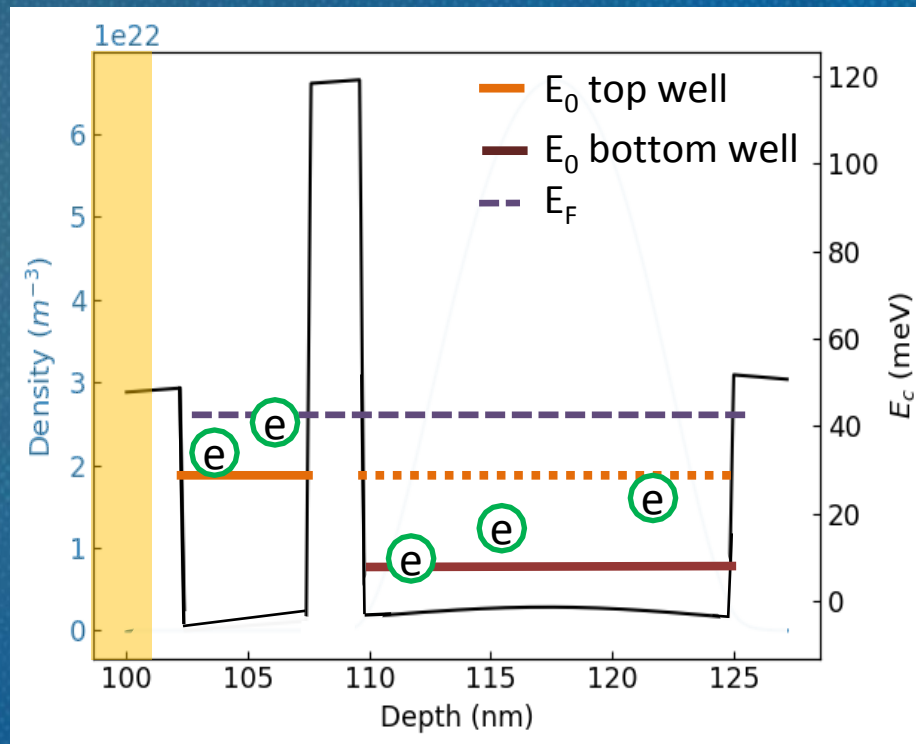
$$V > V_{th}$$



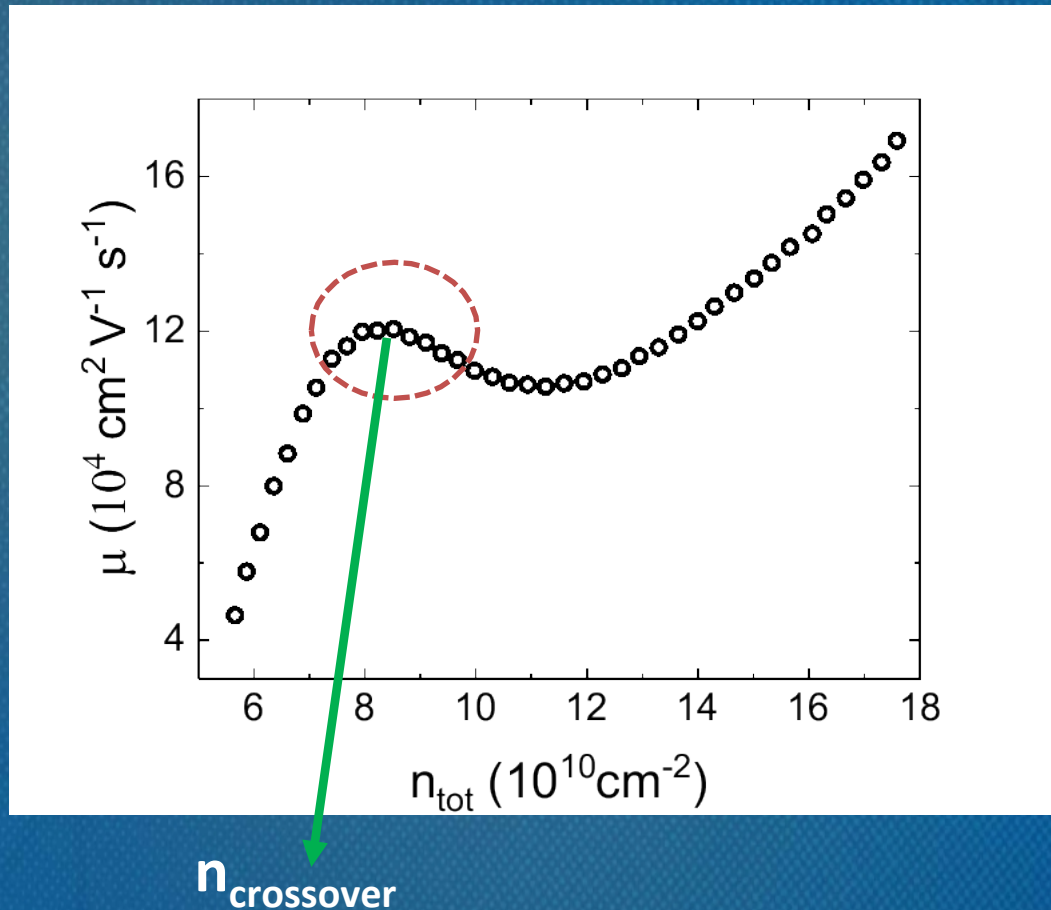
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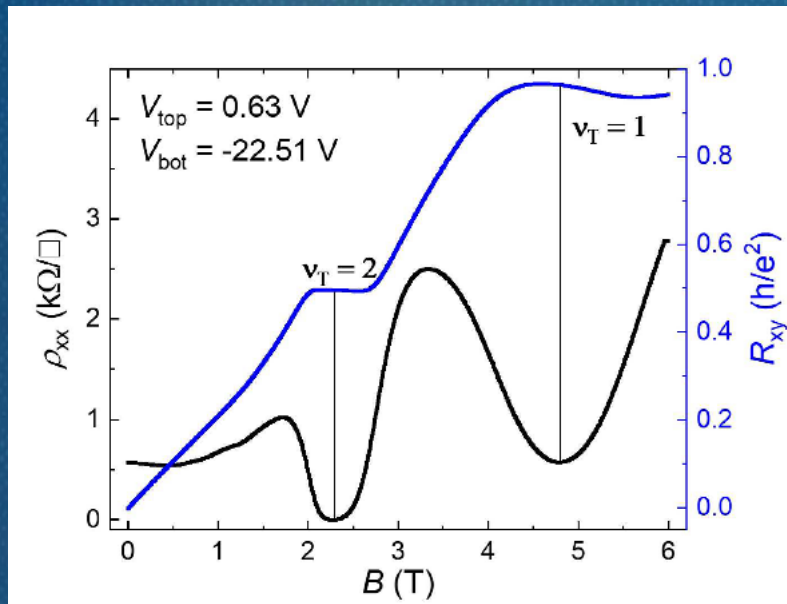


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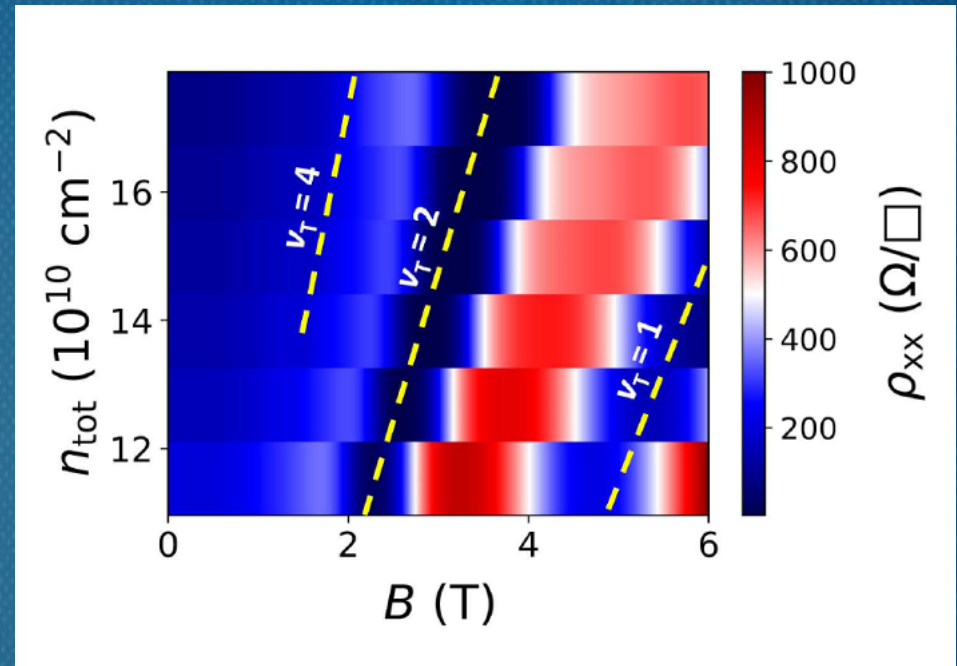
Bilayer behavior

Additional inter-subband scattering causes a mobility drop

Si/SiGe : quantum Hall states

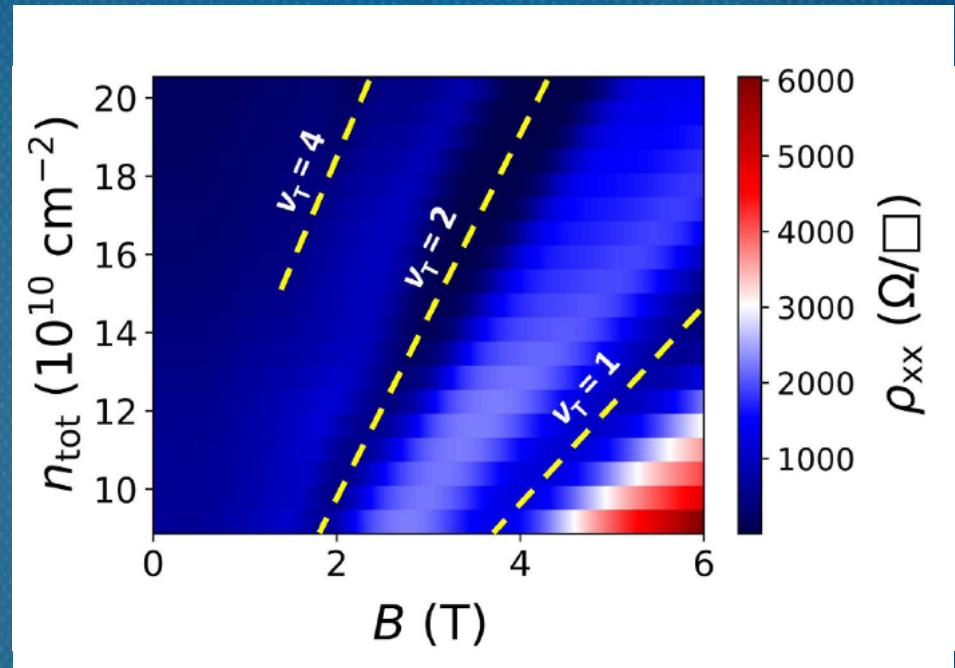
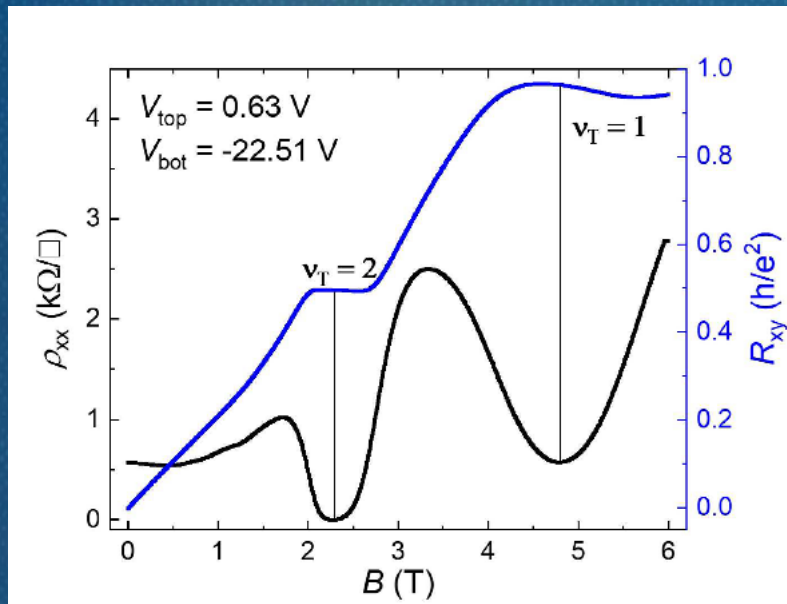


$$n_{tot} = 11.23 \times 10^{10} \text{ cm}^{-2}$$



Top and bottom gating (matched density)

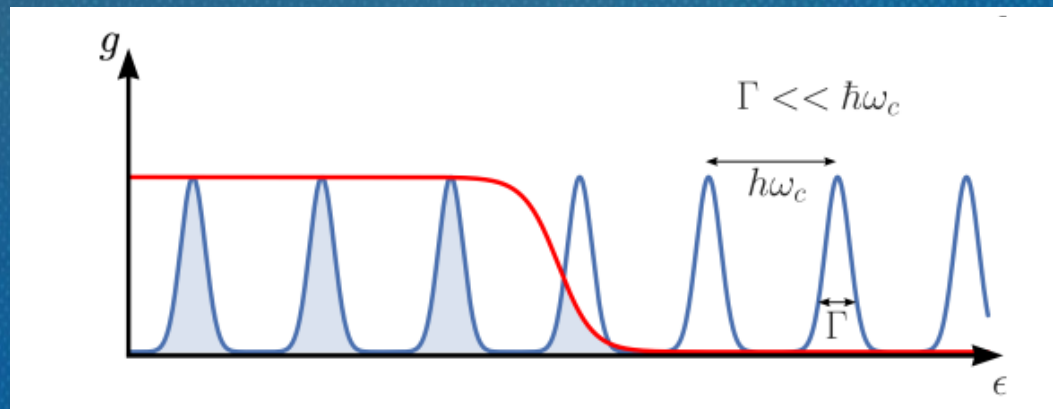
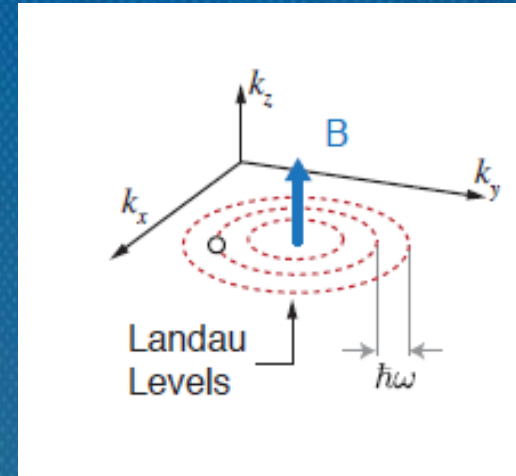
Si/SiGe : quantum Hall states



Top gating (variable density mismatch)

Quantum Hall effect

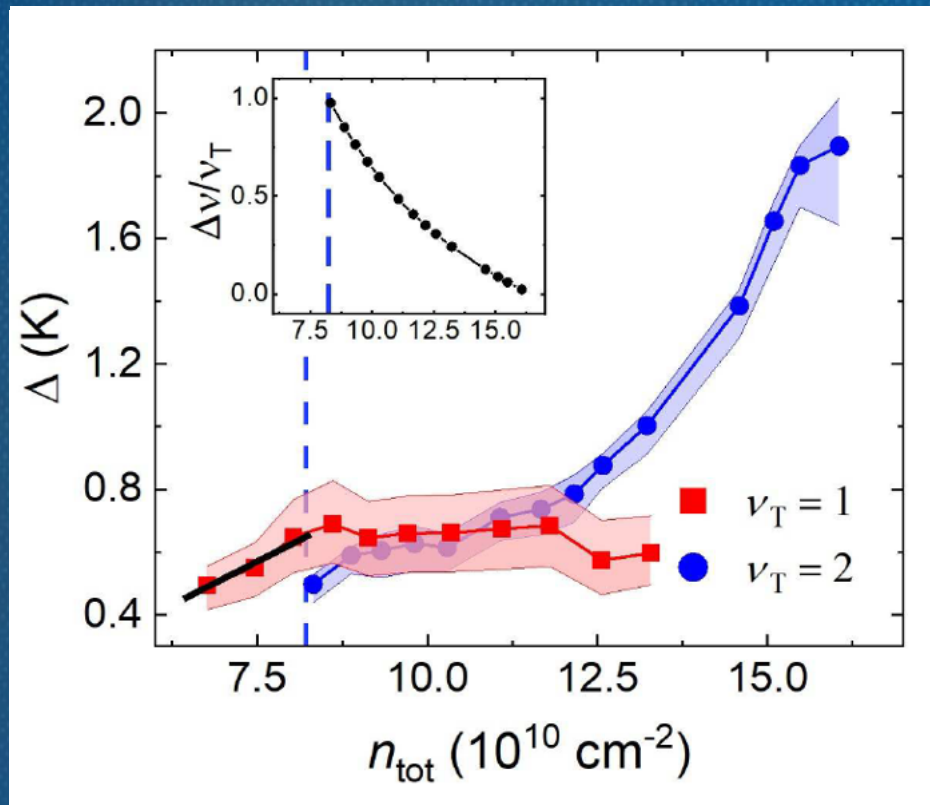
Electron motion of 2D electrons gets quantized in Landau levels with a magnetic field.



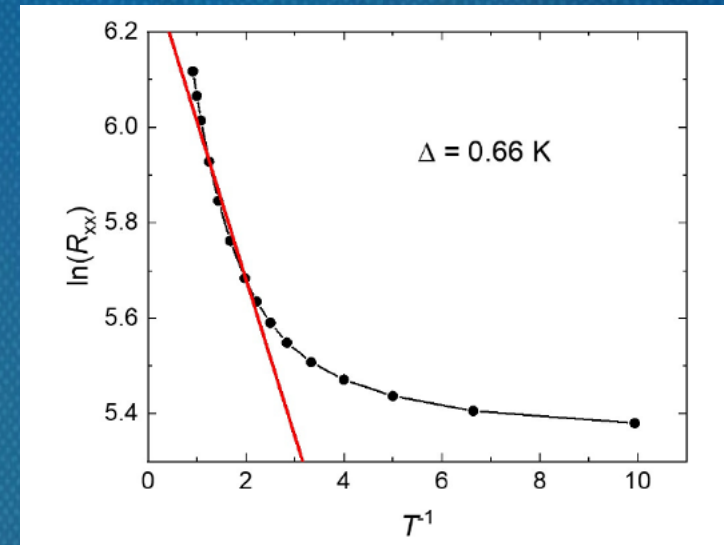
Large B, low T and disorder

Si/SiGe : Activation gaps

Variable density imbalance regime



Single layer regime $\rightarrow \Delta_1 = C_B B - \Gamma$
 $C_B = 0.29 \text{ K/T}$ $\Gamma = 0.327 \text{ K}$

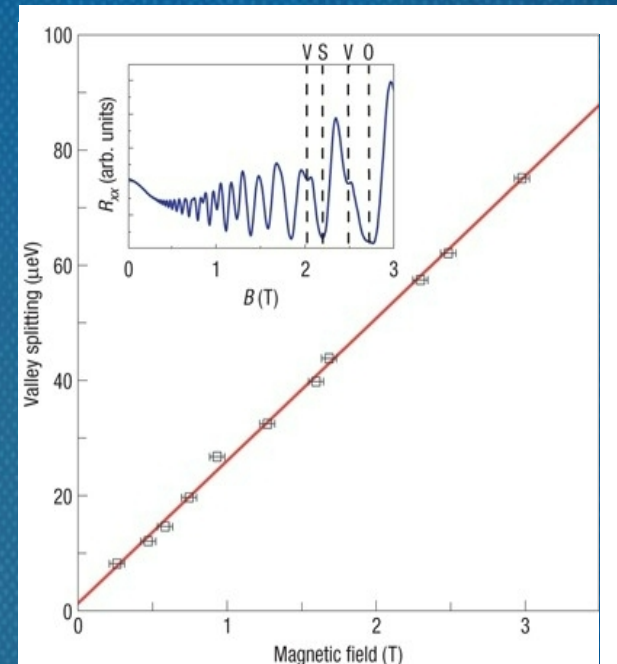
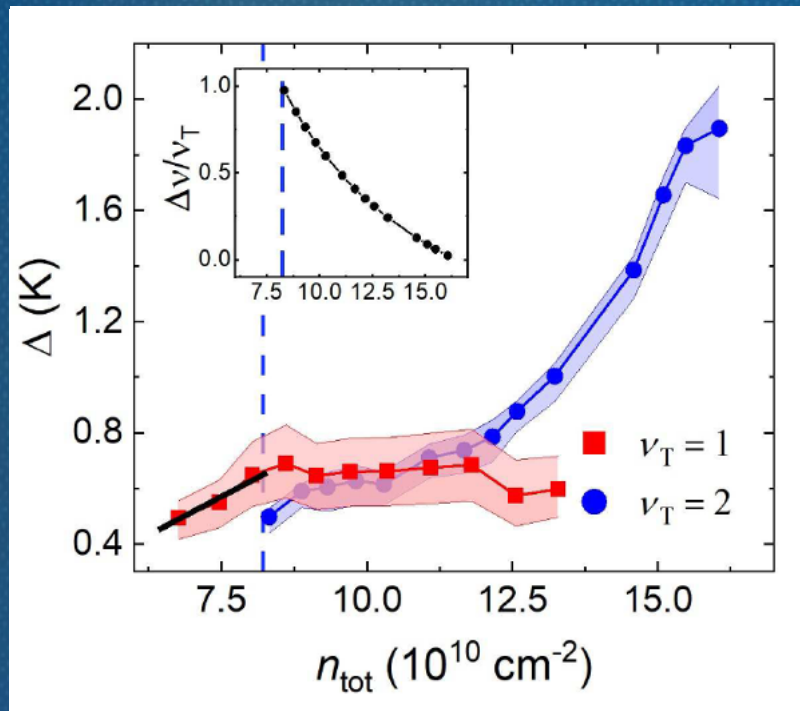


For a spin quantum Hall state,
 $C_B = g\mu_B = 1.3 \text{ K/T}$

Δ_1 is constant with a valley state

Si/SiGe : ν_1 activation gaps

Variable density imbalance regime



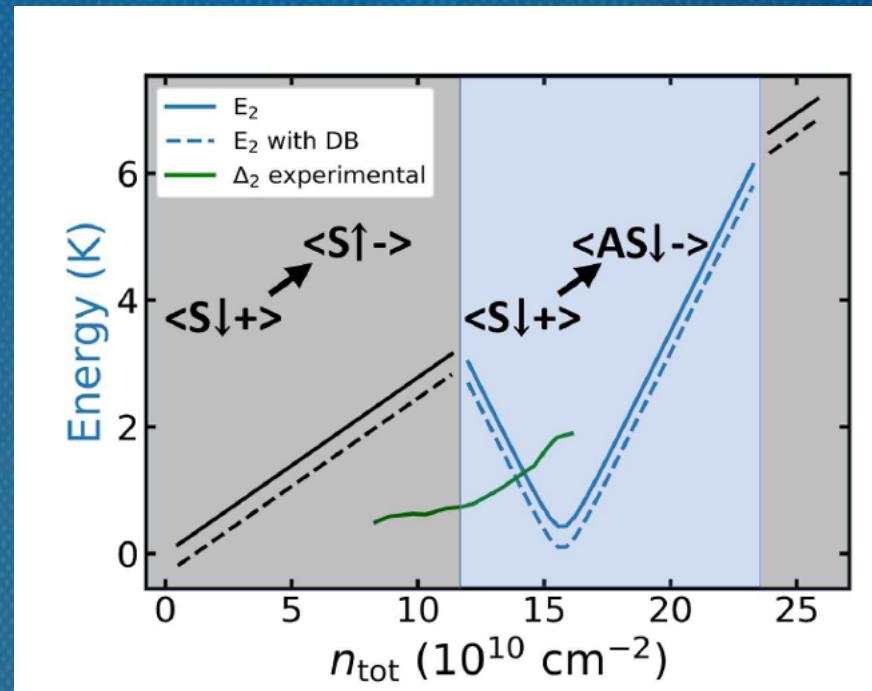
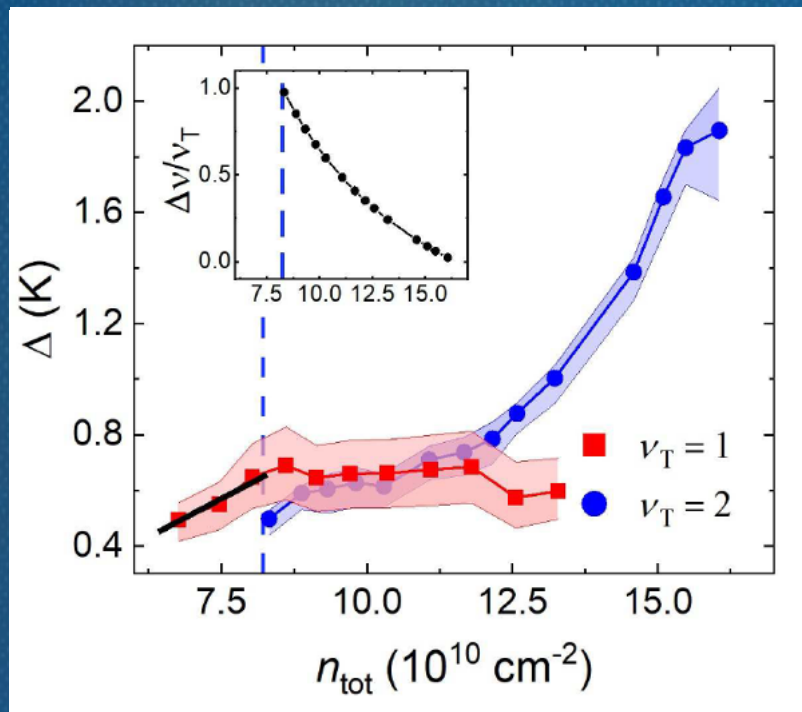
S. Goswami et al. Nature Phys. **3** 41, 2006

Valley splitting very different in bilayers and single layers!

- Different interference conditions?
- Ge content increases valley splitting?
- Consequence of exciton condensation?

Si/SiGe : ν_2 activation gaps

Variable density imbalance regime



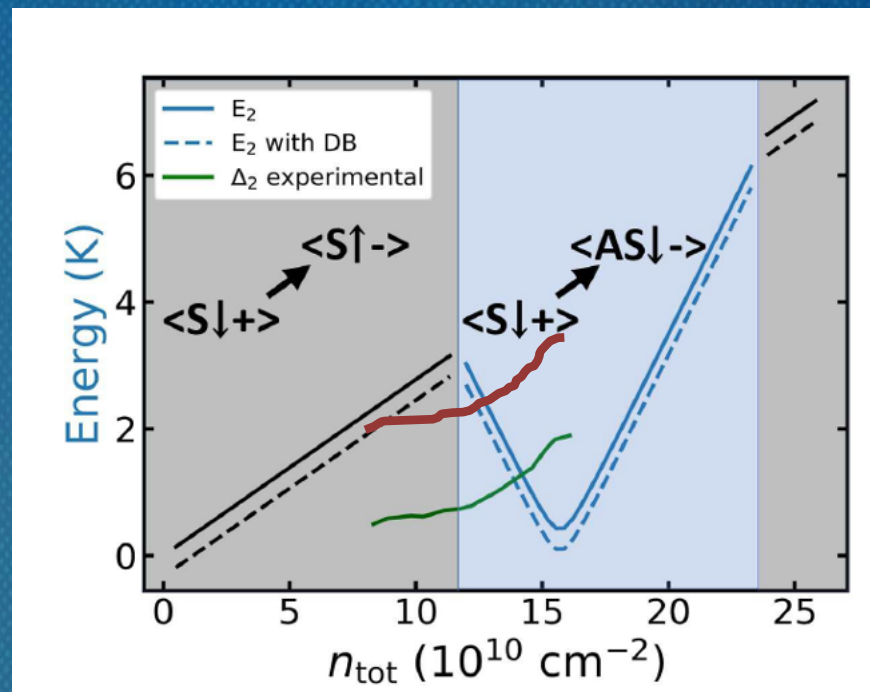
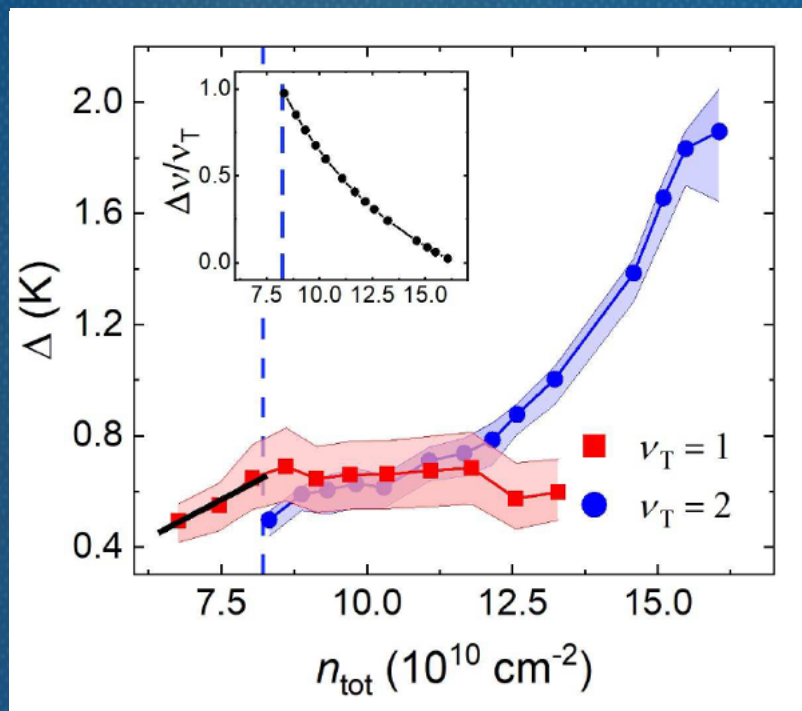
The SP simulation only produces E_2 .

$$\Delta_2 = E_{s/l} - E_v - \Gamma = E_{s/l} - \Delta_1 - 2\Gamma$$

Δ_2 is inconsistent with a spin or a S-AS quantum state \rightarrow consistent with exciton condensation*

Si/SiGe : ν_1 activation gaps

Variable density imbalance regime

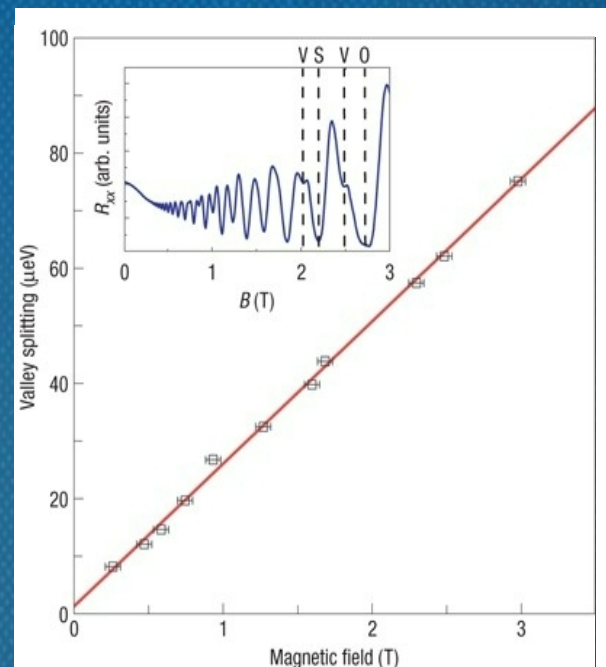
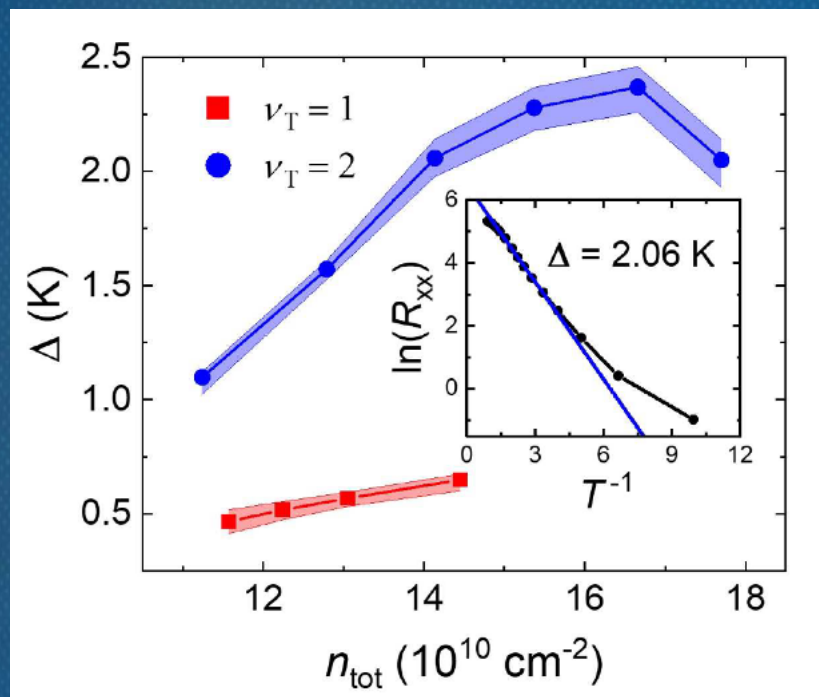


Δ_2 is nearly one order of magnitude larger than the expected value from Δ_{SAS}

From theory :

$\Delta_{\text{SIC}} \rightarrow$ decreases with magnetic field, tunneling

$\Delta_{\text{SIC}} \rightarrow$ increases with density imbalance

Density matched regime

S. Goswami et al. Nature Phys. **3** 41, 2006

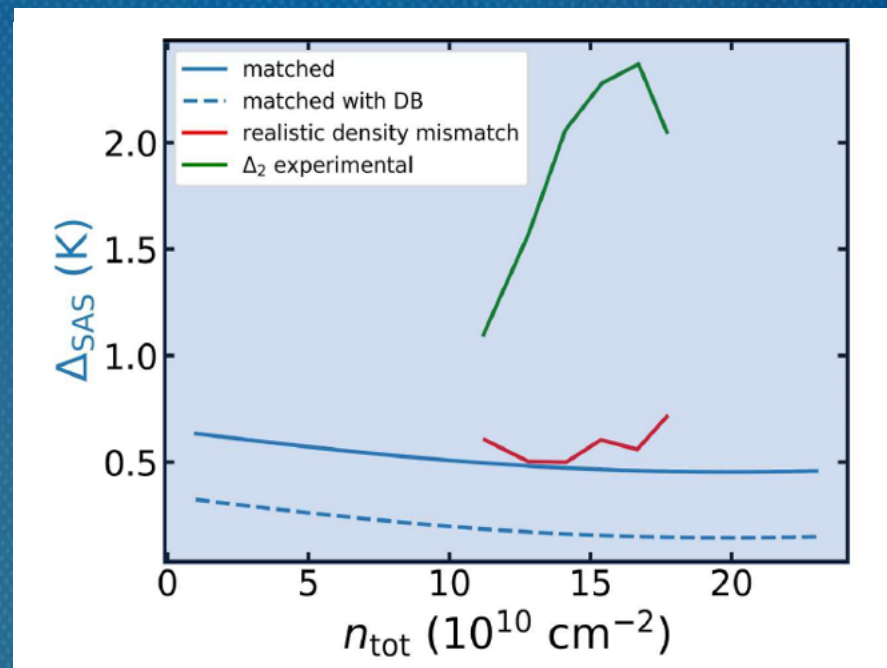
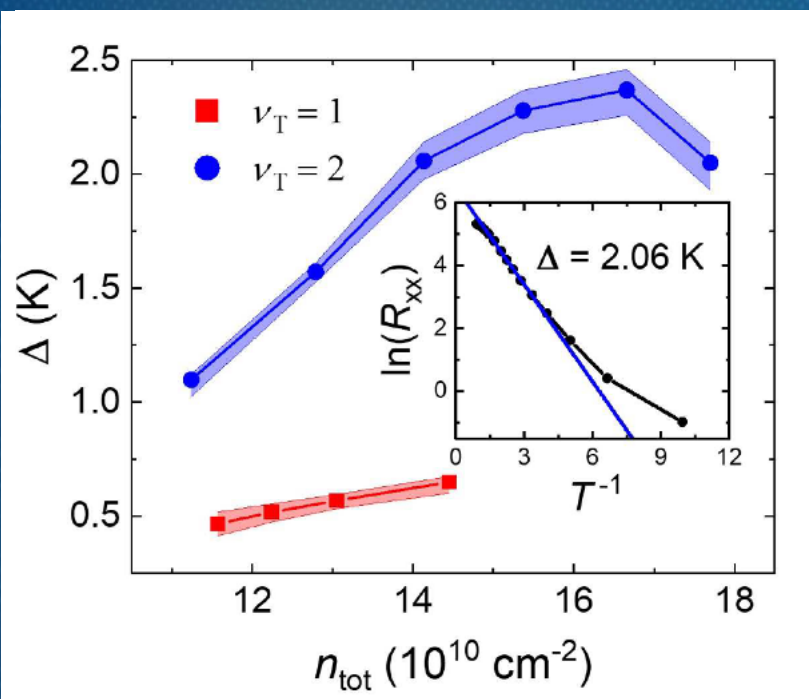
Valley splitting is linear in matched density bilayers

C_B reduced from 0.29 K/T to 0.15 K/T

Further work needed to understand valley splitting in bilayers

Si/SiGe : ν_2 activation gaps

Variable density imbalance regime



Δ_2 is nearly one order of magnitude larger than the expected value from Δ_{SAS}

Δ_2 has the opposite concavity from Δ_{SAS}

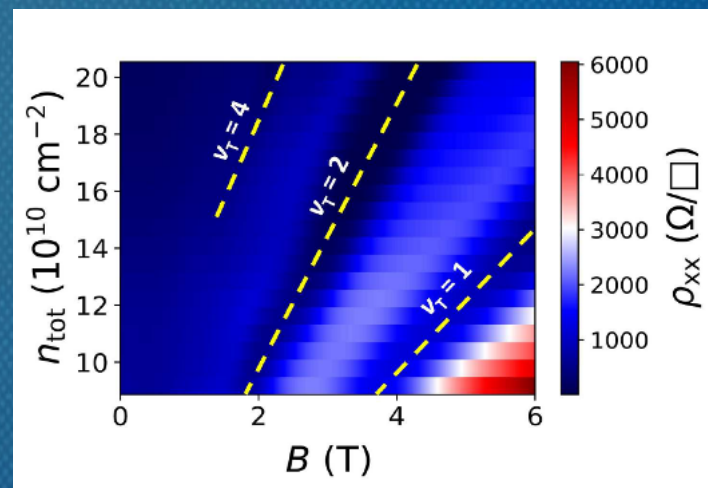
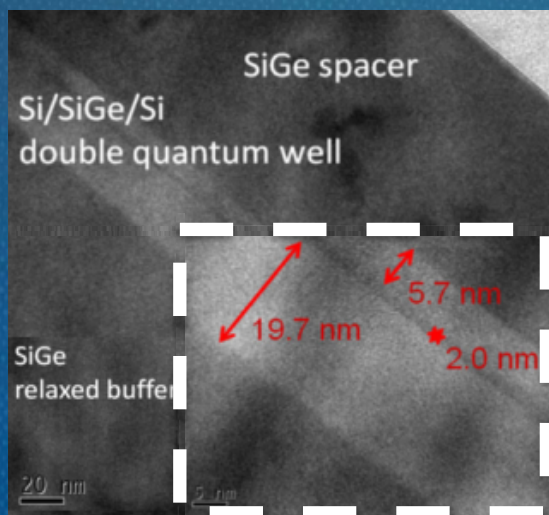
From theory :

$\Delta_{\text{SIC}} \rightarrow$ decreases with magnetic field, tunneling



$\Delta_{\text{SIC}} \rightarrow$ increases with density imbalance

Si/SiGe : Summary

- Observed bilayer effects in system \rightarrow Mobility dip and ν_1 quantum Hall state
- $\nu_{\text{tot}} = 1$ state is attributed to valley splitting
 - Behavior is clear departure from single layer valley splitting
 - Warrant further investigation!
- $\nu_{\text{tot}} = 2$ state is attributed to layer effects
 - Behavior inconsistent with Δ_{SAS}
 - Consistent with spontaneous interlayer coherence
- Next steps : independent contact to both layers \rightarrow Study tunneling, counterflow

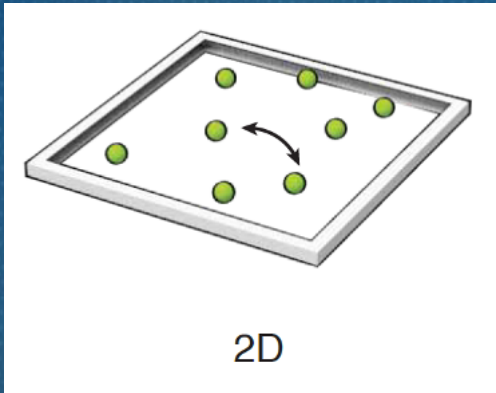


Outline

- Introduction to low-dimensional systems 
- Search for exciton condensation in Si quantum wells 
 - Introduction to Si/SiGe quantum wells
 - 2DEG
 - Growth
 - Valley splitting
 - Introduction to exciton condensation
 - Device fabrication
 - Excitation gaps in the quantum Hall regime
- Coulomb drag between quantum wires
 - Quantum wires
 - Introduction to Luttinger liquids
 - Coulomb drag technique
 - Device fabrication
 - Coulomb drag measurements in laterally-coupled quantum wires
- Future directions

2. Drag in Coupled GaAs quantum wires

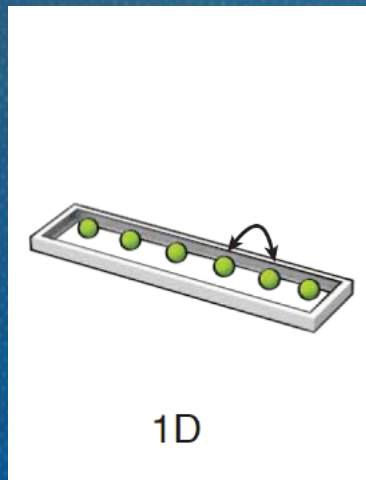
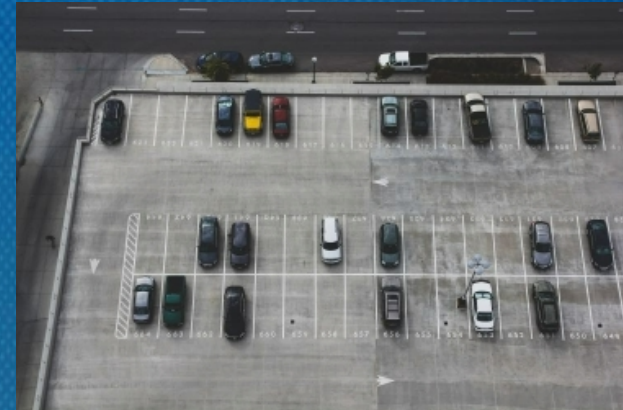
Luttinger liquid physics



Fermi liquid



Effective parameters



Luttinger liquid

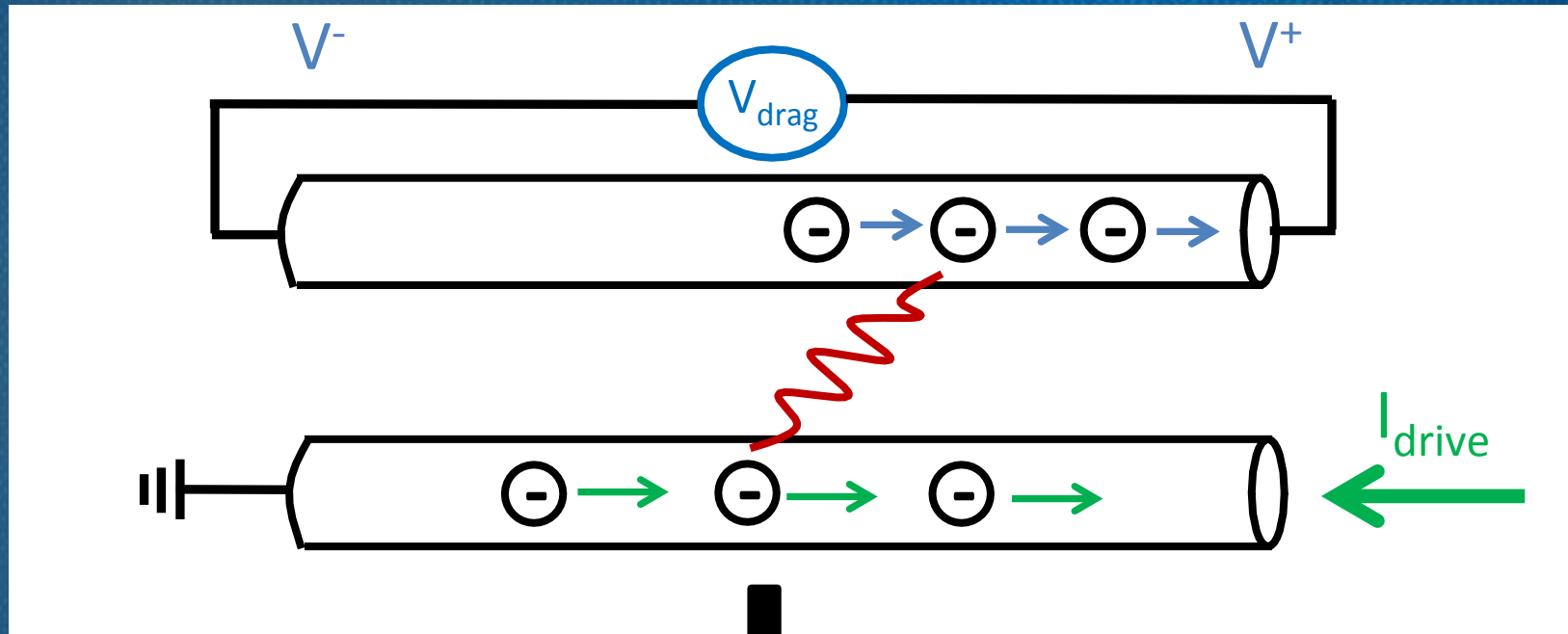


All motion is correlated
Strongly interacting system



Coulomb drag

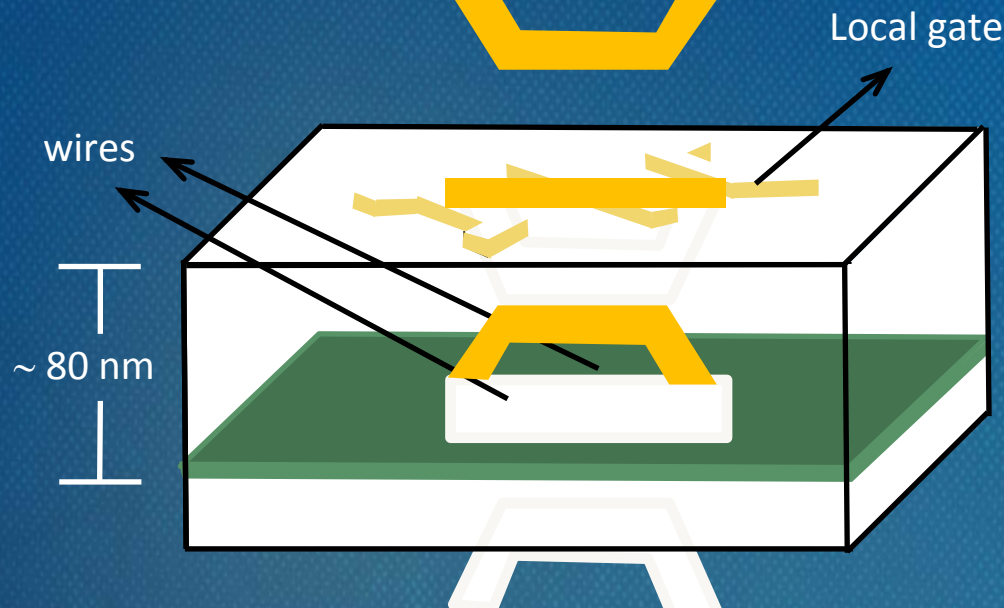
Momentum transfer models



$$R_D = \frac{-V_{\text{drag}}}{I_{\text{drive}}}$$

Magnitude of frictional resistance depends on $e^- - e^-$ interactions

Coupled quantum wires

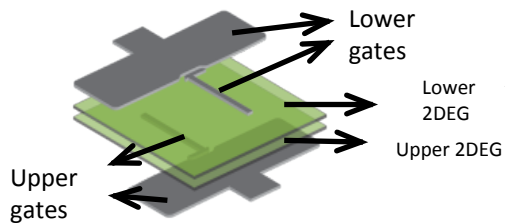


Laterally coupled quantum wires

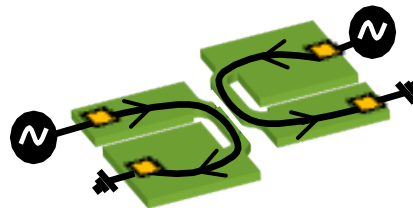
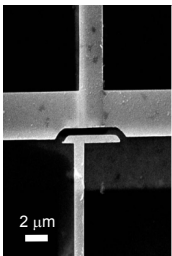
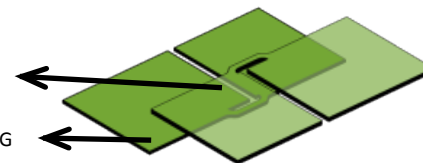
Ease of fabrication
Tunable interwire separation

Large interwire separation
Soft electrostatic barrier

Gates design



Gates activated

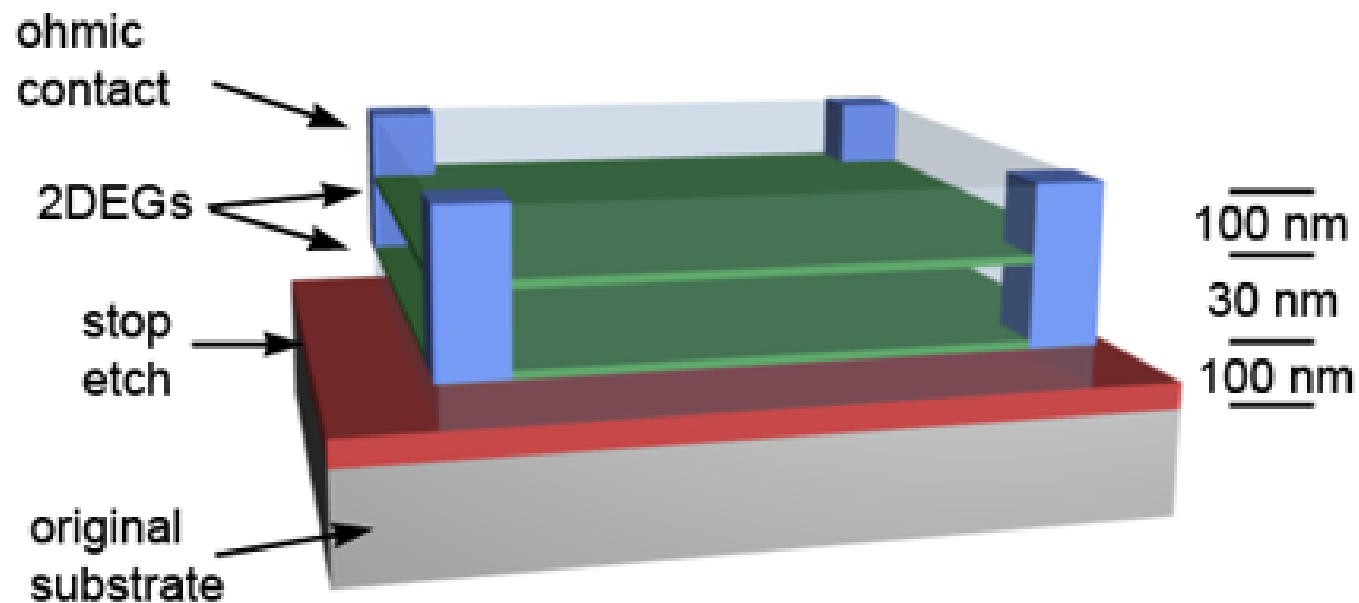


Vertically-coupled quantum wires

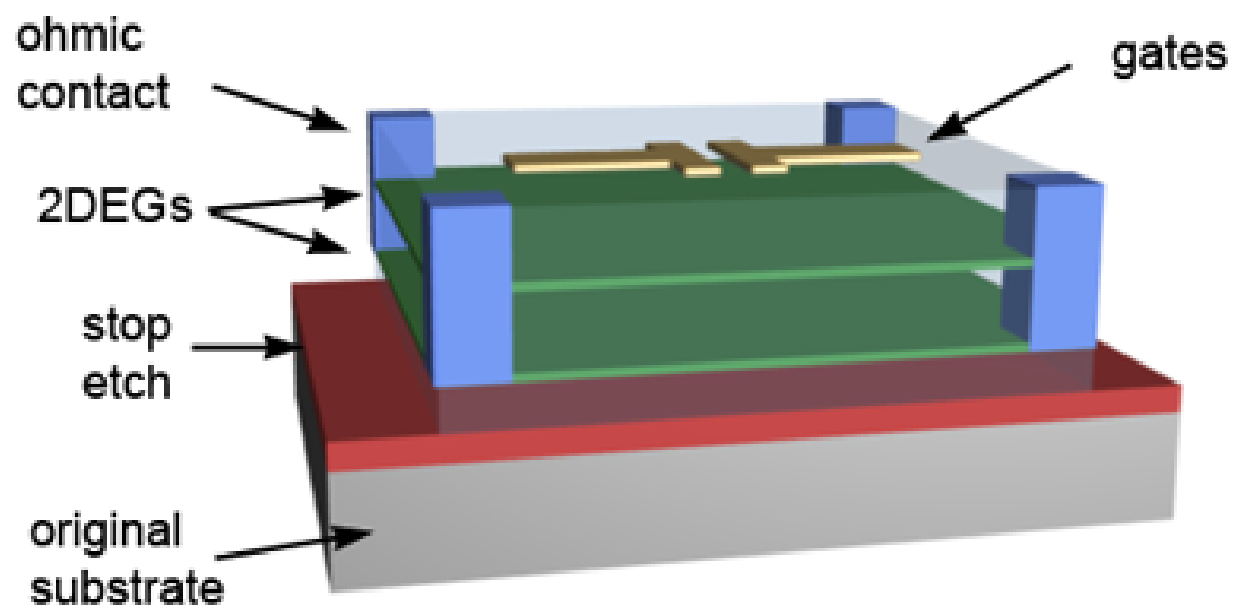
Small interwire separation
Hard dielectric barrier

Involved fabrication process

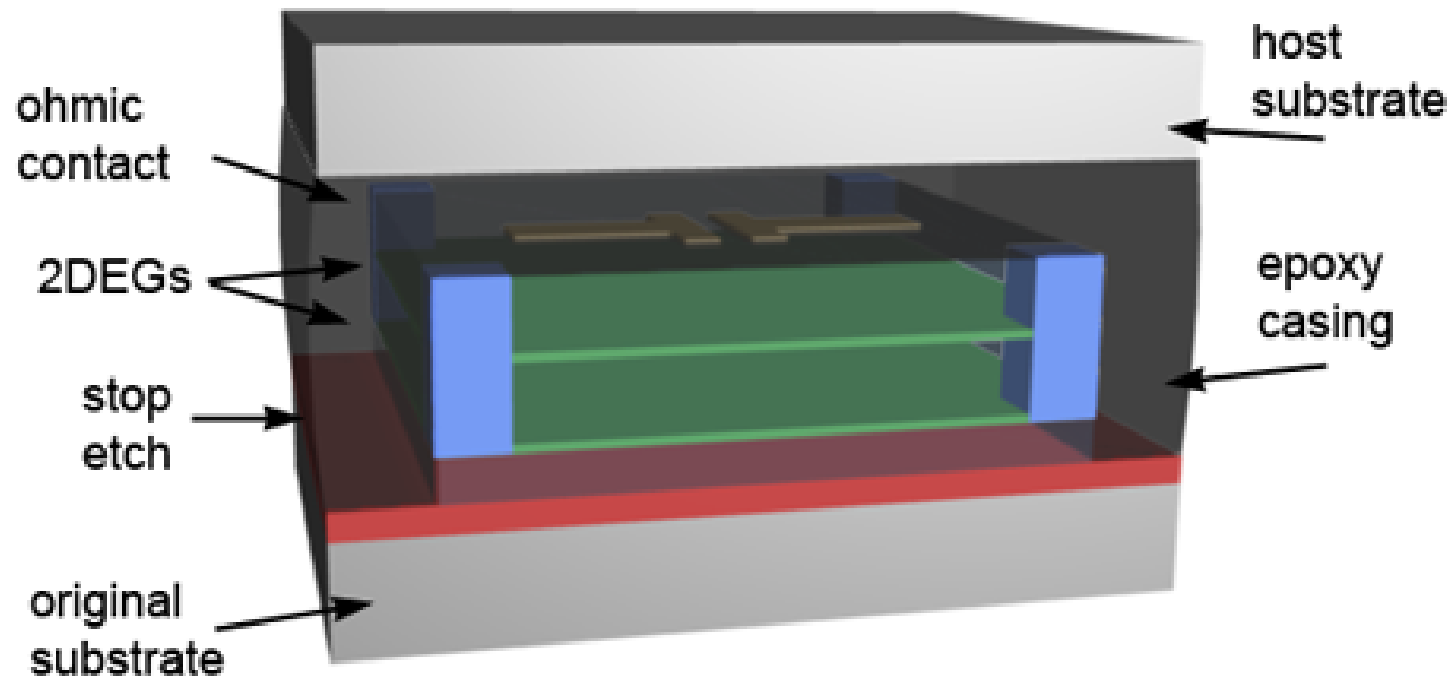
Vertically-coupled quantum wires



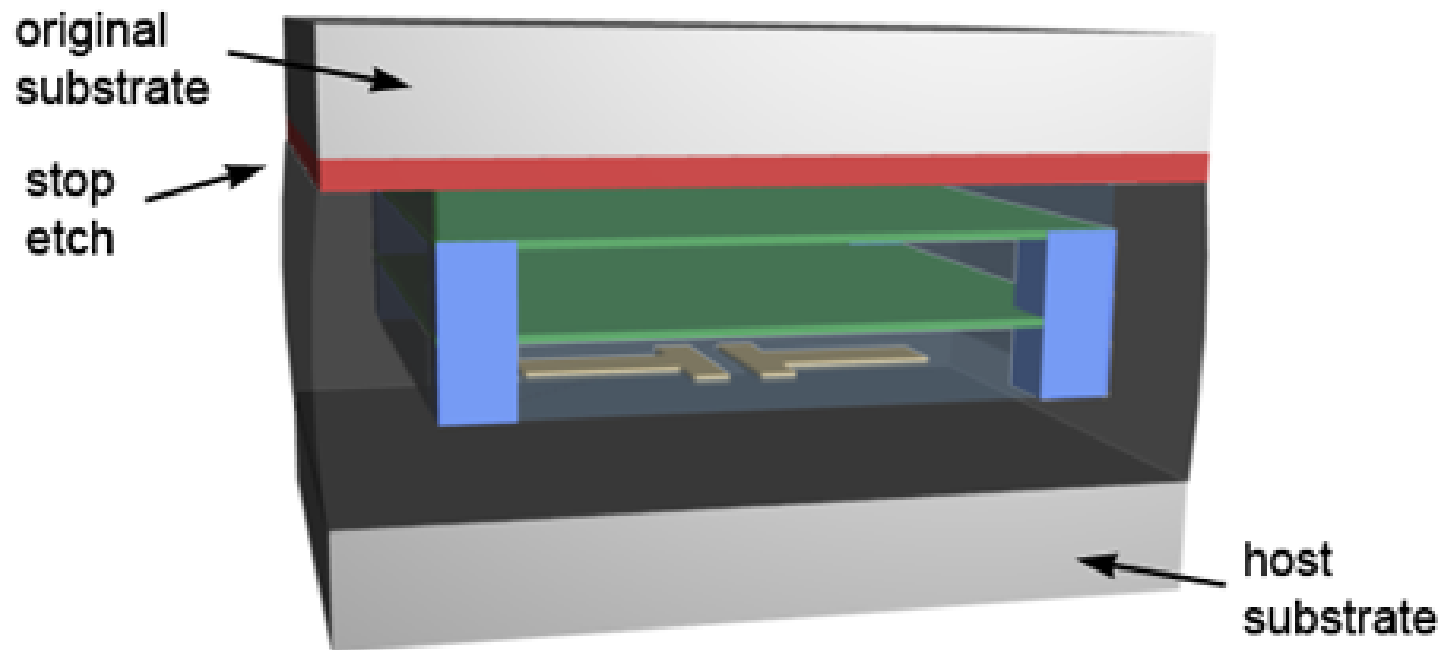
Vertically-coupled quantum wires



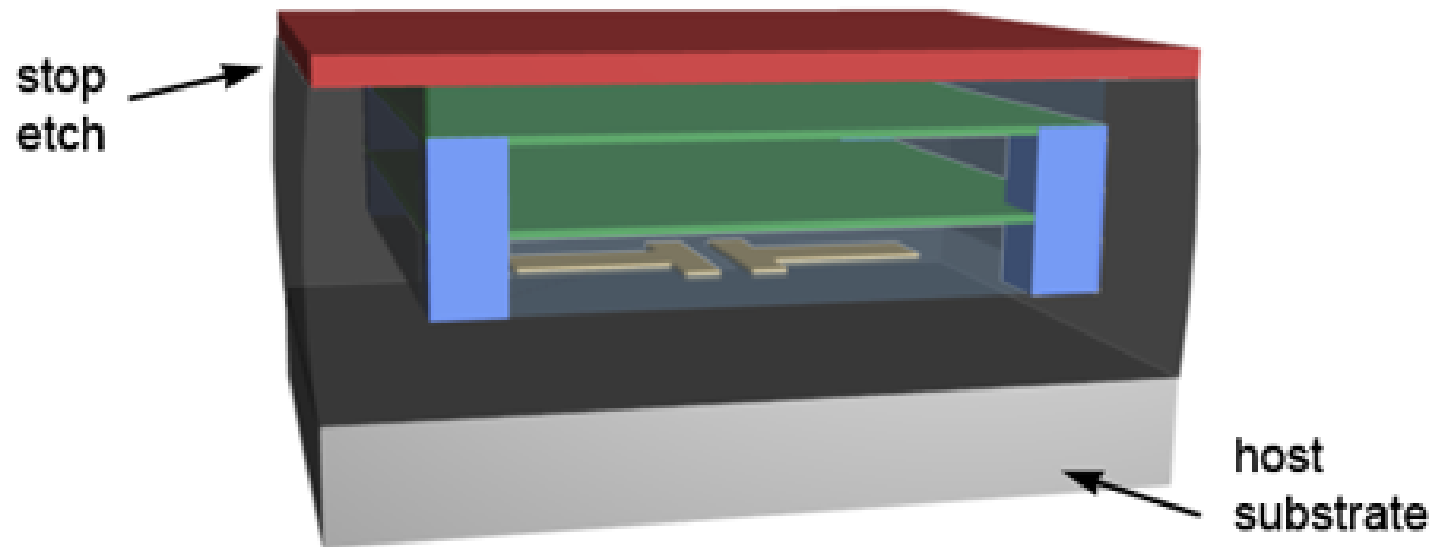
Vertically-coupled quantum wires



Vertically-coupled quantum wires

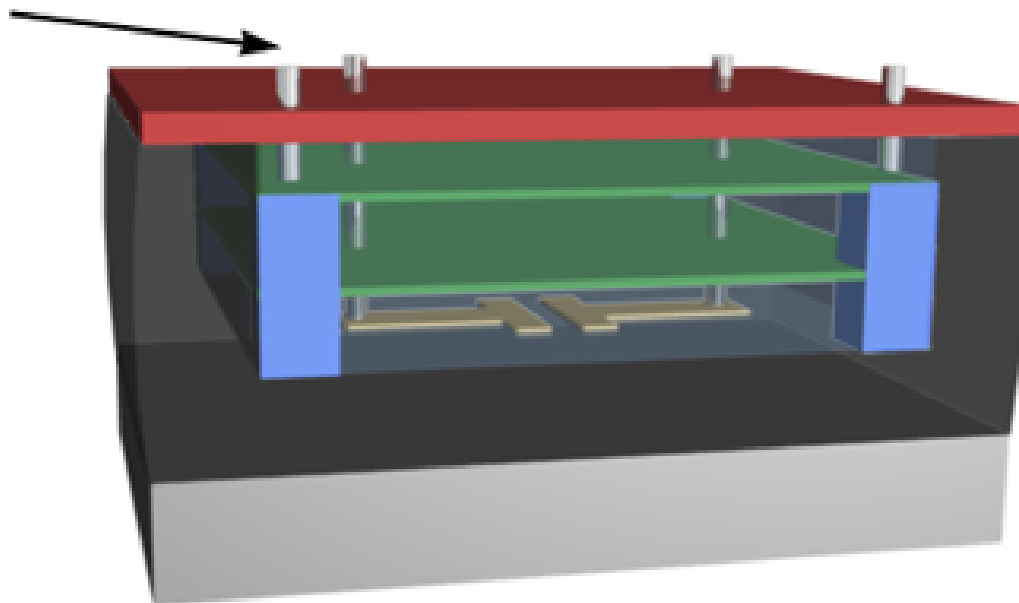


Vertically-coupled quantum wires

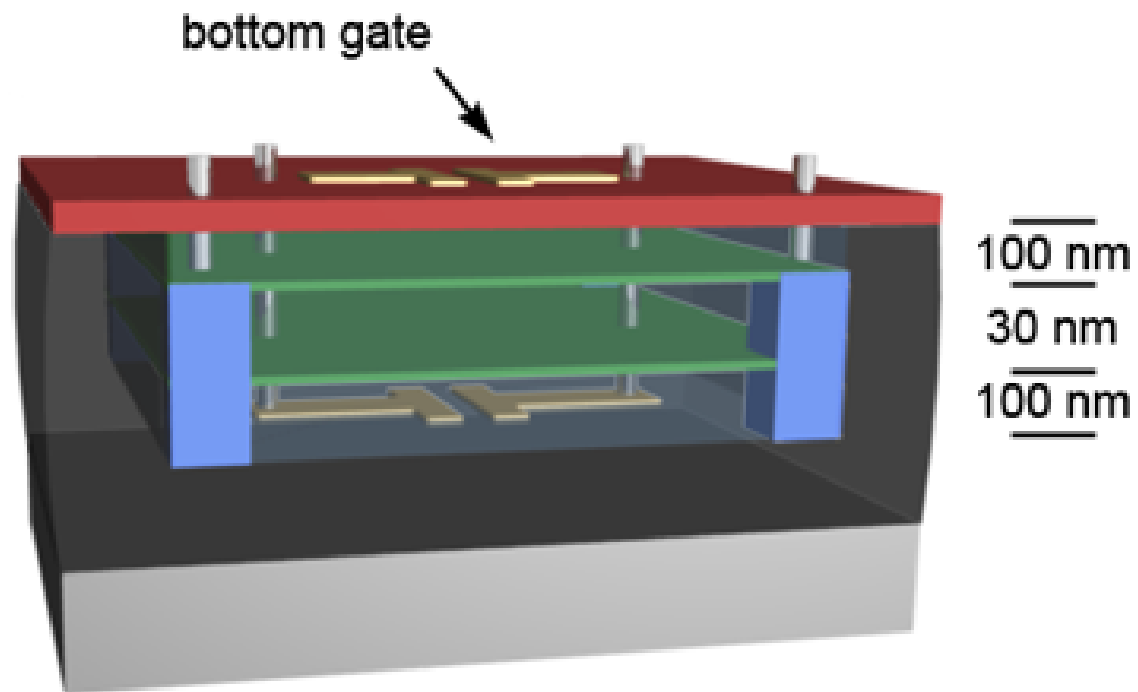


Vertically-coupled quantum wires

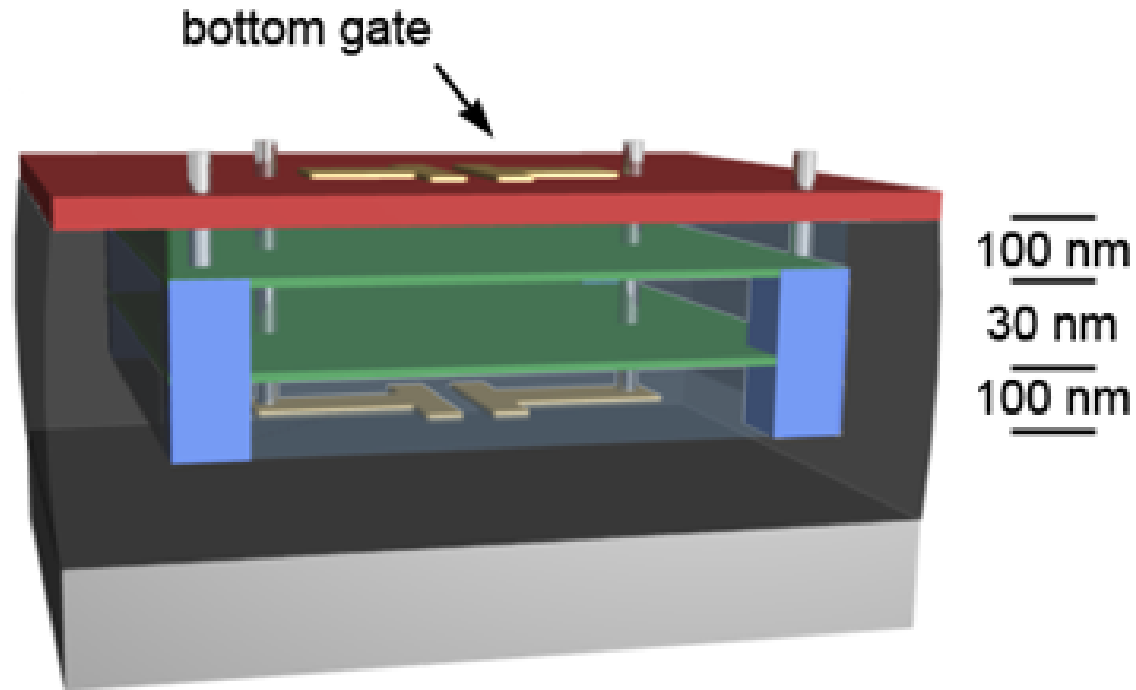
vias to
gates
and
ohmic
contact



Vertically-coupled quantum wires

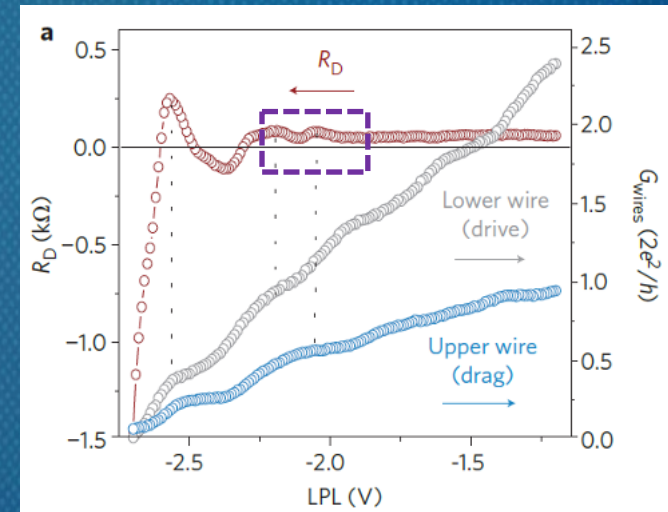
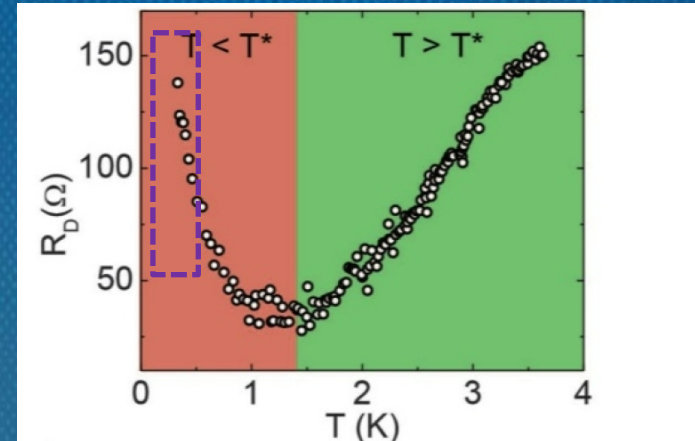


Vertically-coupled quantum wires

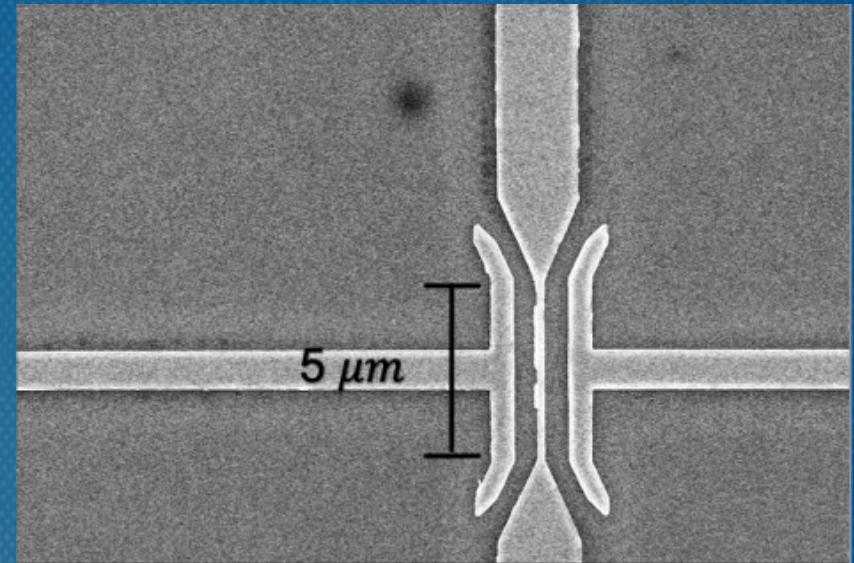
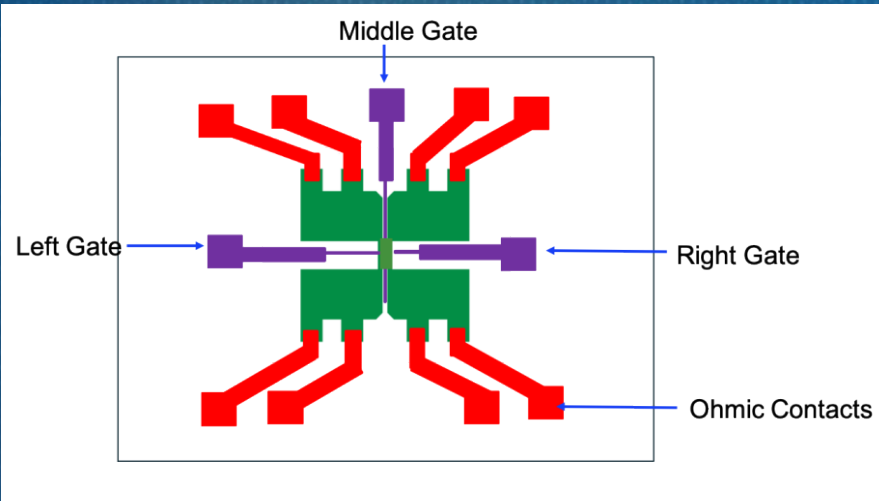


Objective : contrast the strength of electron-electron interactions
as a function of geometry/separation

- Drag in the multi-subband regime
- Dominant drag scattering mechanism
- Impact of wire length / interwire separation
- Coulomb drag in the $T=0$ limit
- Drag in the spin-polarized regime



Quasi-1D drag

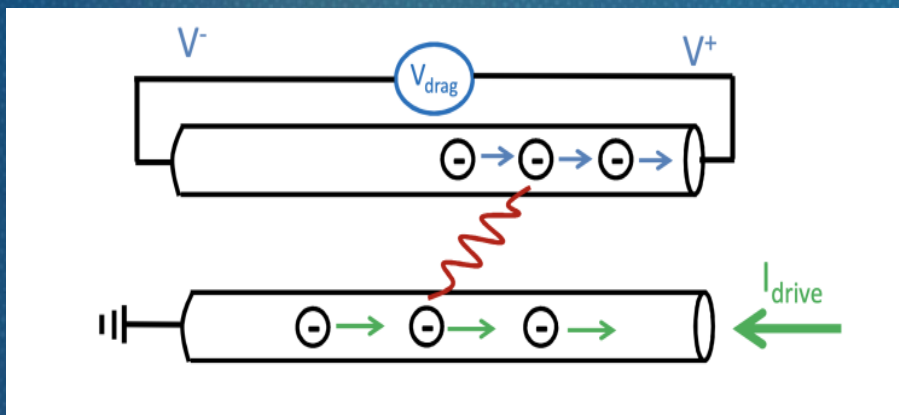


Lateral device
Barrier size : $\sim 150\ \text{nm}$
 $5\ \mu\text{m}$ long wires

Survey of drag-inducing mechanism

Momentum transfer Model

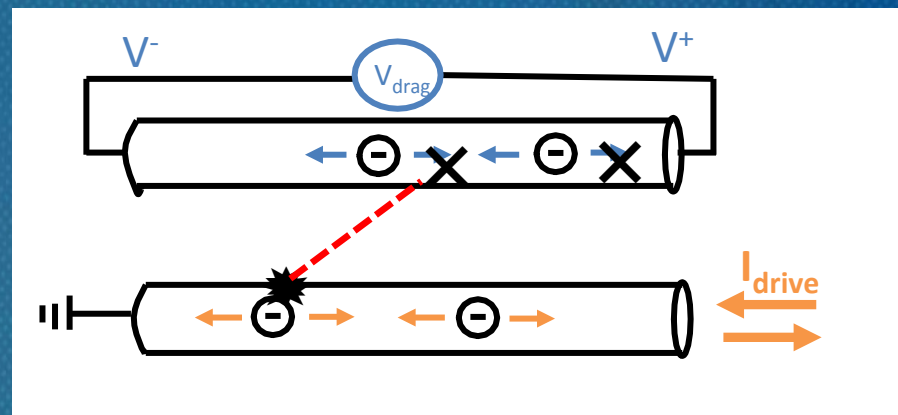
Drag current is induced through momentum transfer¹



¹Klesse, R. and Stern, A. Phys. Rev. B 62, 16912 (2000).

Charge-fluctuation Model

Arises from interlayer energy transfer²



²Levchenko, A. and Kamenev, A. Phys. Rev. Lett. 101, 216806 (2008).

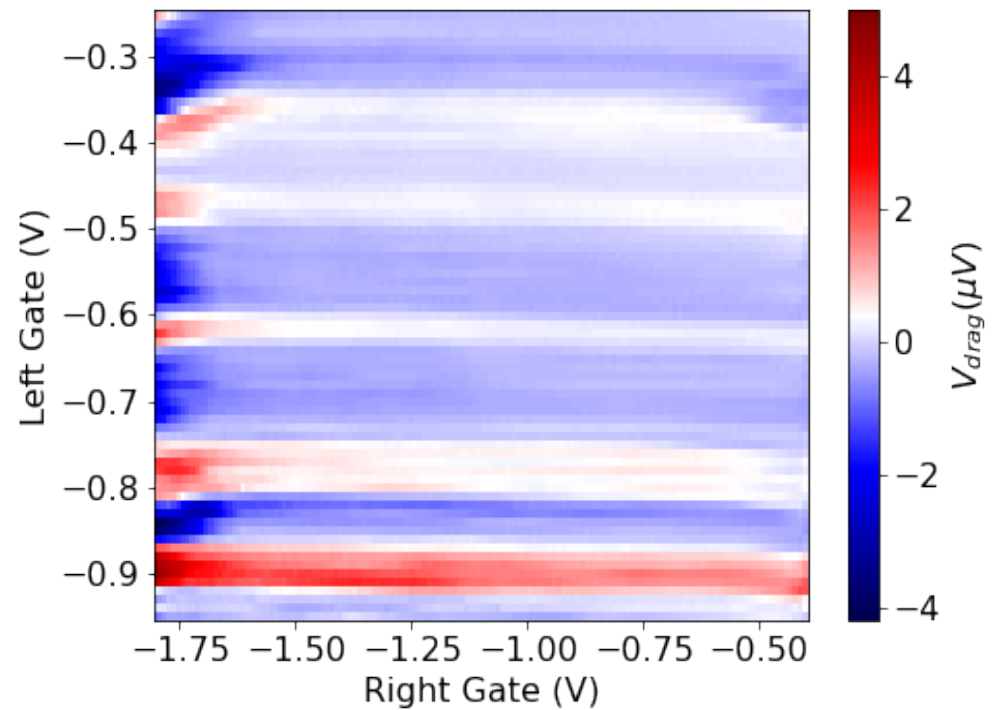
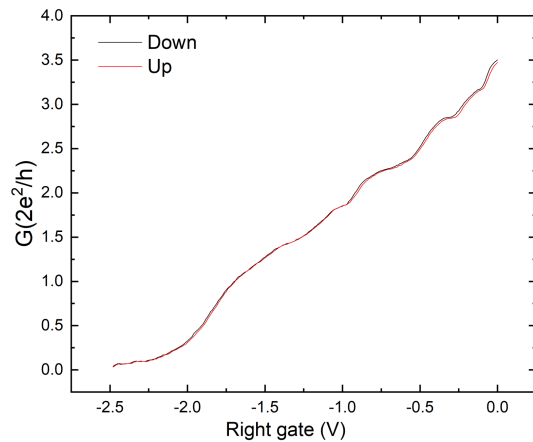
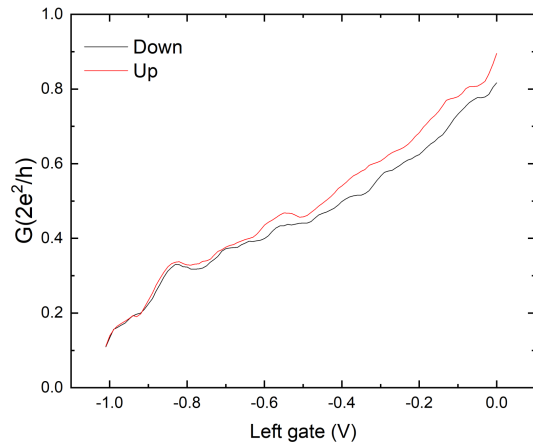
Expect positive drag resistance

Expect V_{drag} to have opposite sign of I_{drive}

Expect rectified drag signal

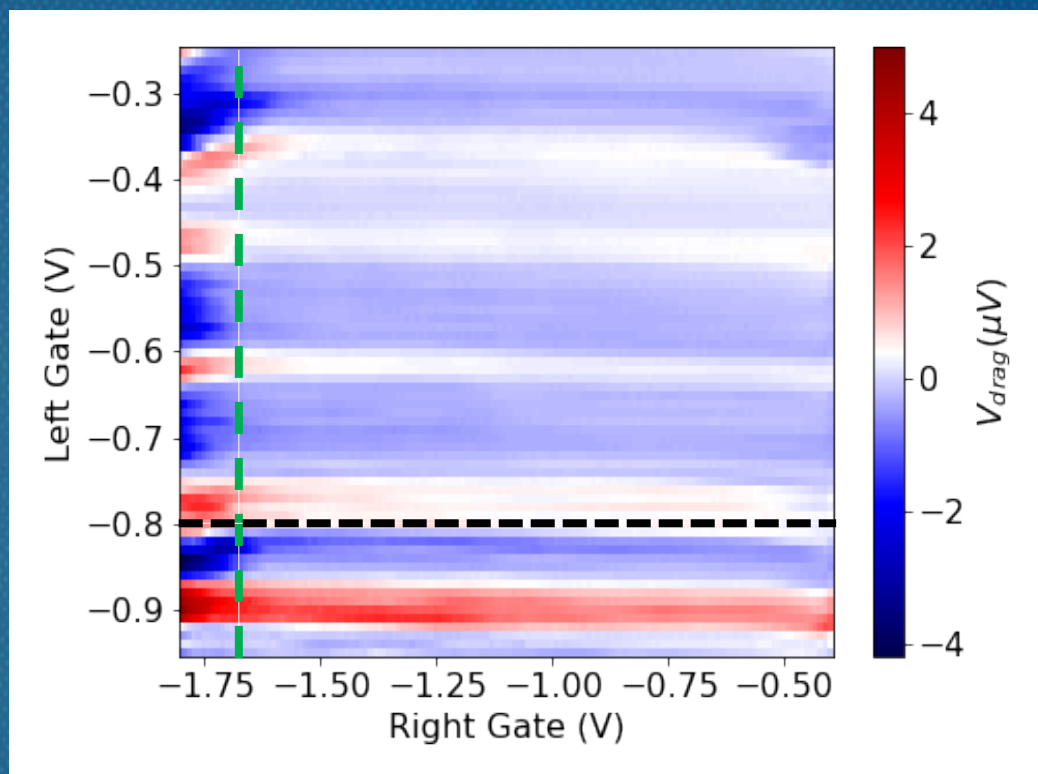
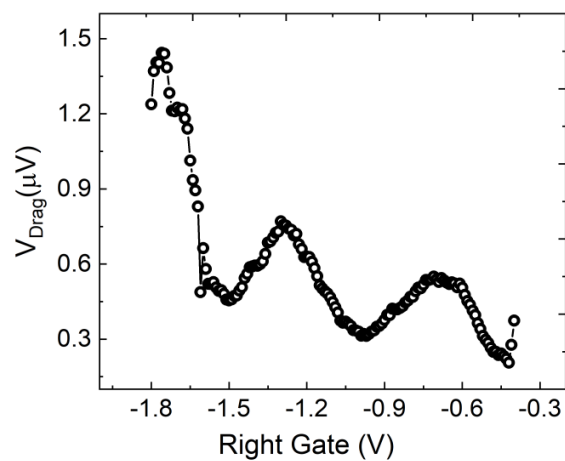
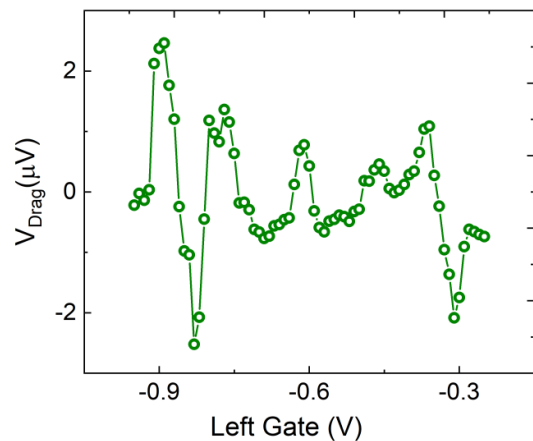
Expect V_{drag} to be independent of I_{drive} sign

Quasi-1D drag – AC data



Drag is principally modulated in the left wire direction.

Quasi-1D drag – AC data

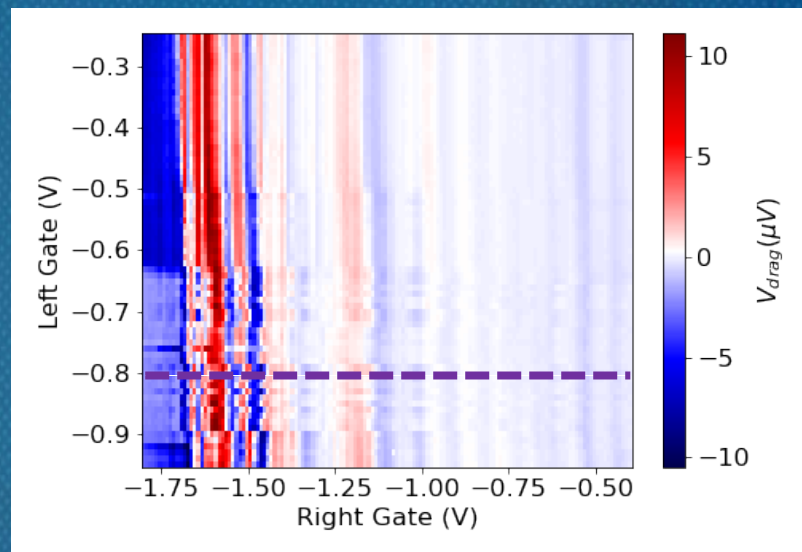
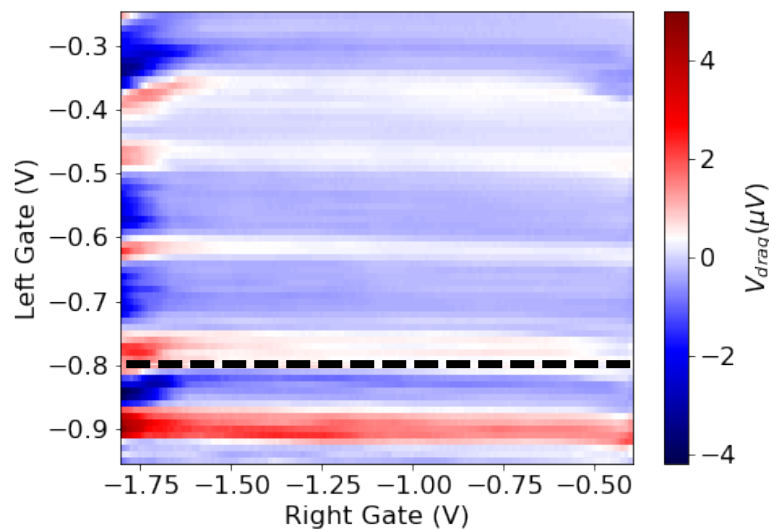


Standard drag tests

Onsager relations : drag is independent of drive/drag layer and current direction



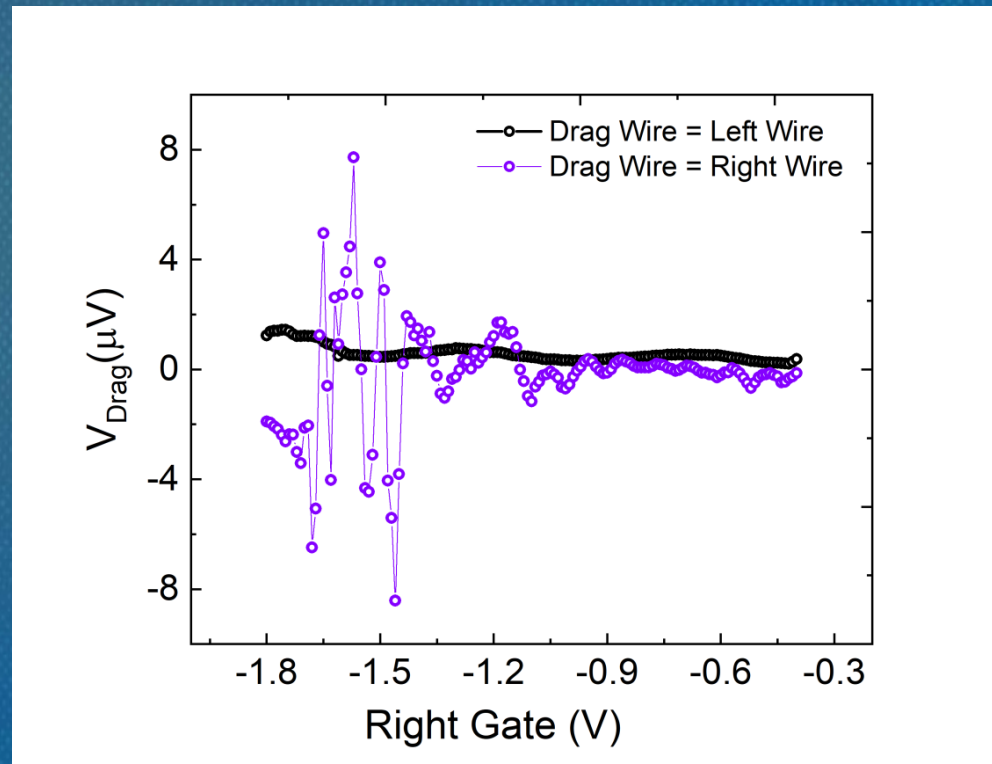
I_{drive}



Drag voltage is strongly modulated by the drag wire!

Standard drag tests

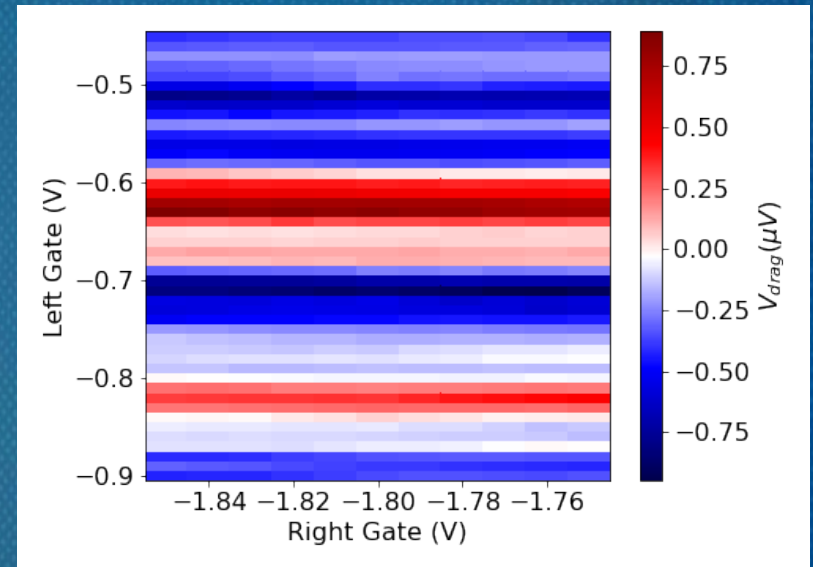
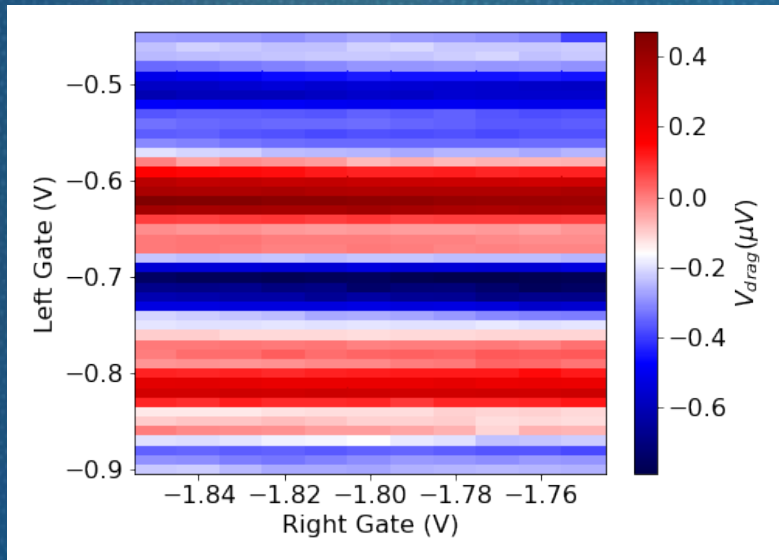
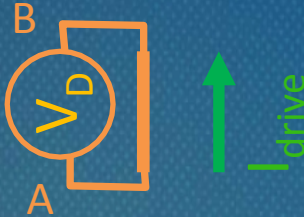
Onsager relations : drag is independent of drive/drag layer and current direction



Drag is strongly modulated by the drag wire!

Standard drag tests

Onsager relations : drag is independent of drive/drag layer and current direction



Drag voltage features polarity are independent of drag direction
Consistent with rectification!

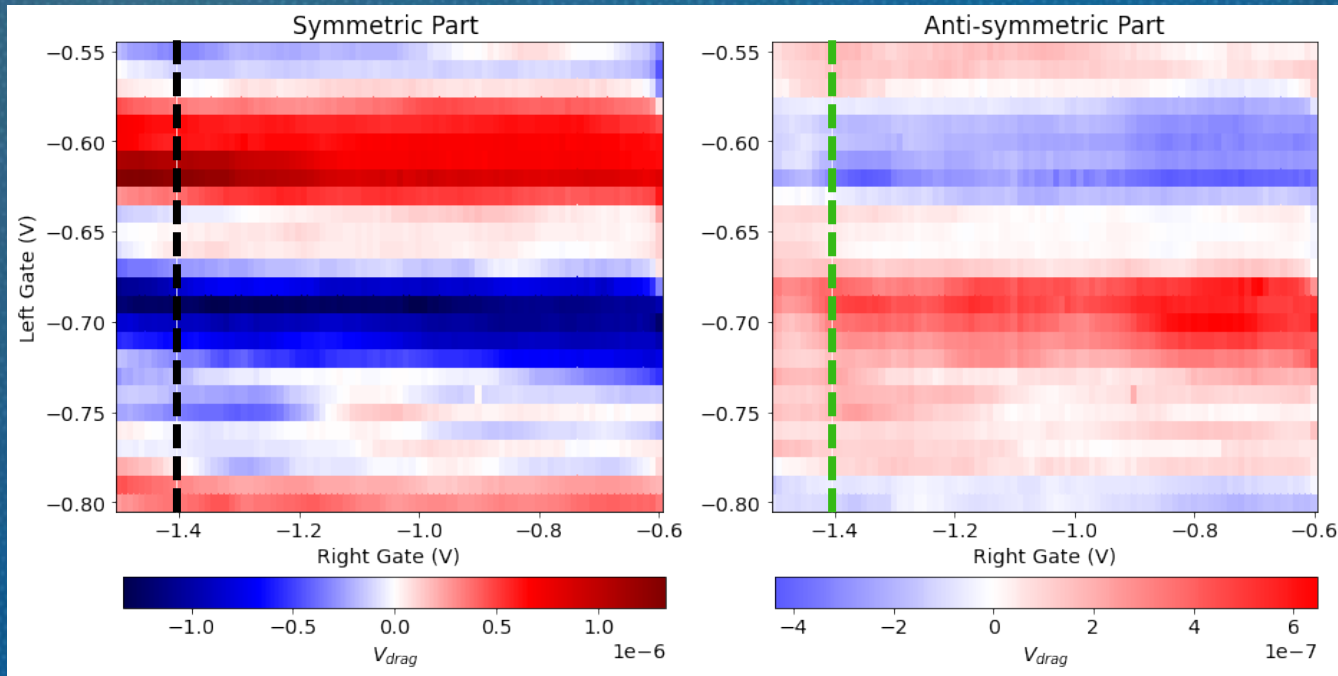
Symmetric and anti-symmetric contributions

Upon current reversal, the signal is not identical

Hypothesis : two contributions:

Symmetric : Rectification

Antisymmetric : Momentum- transfer



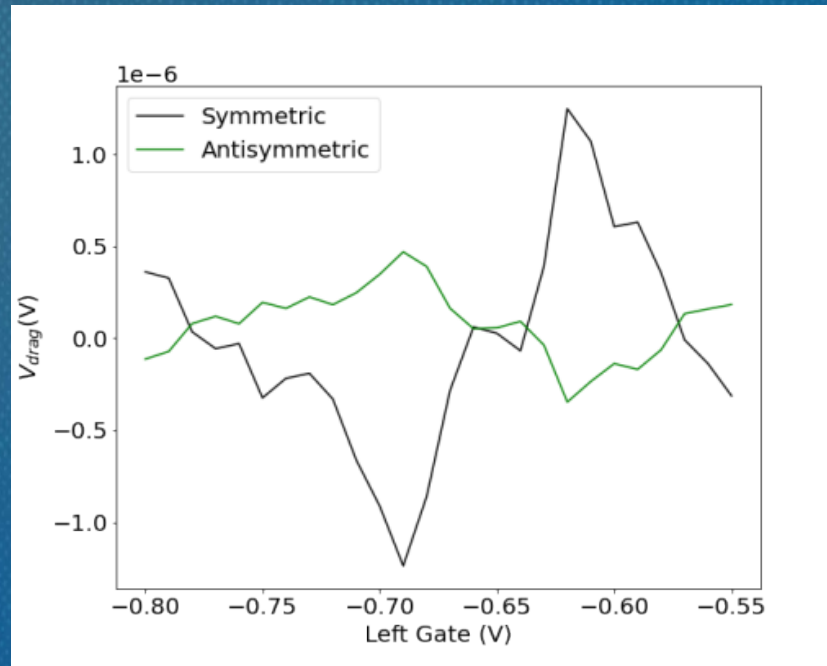
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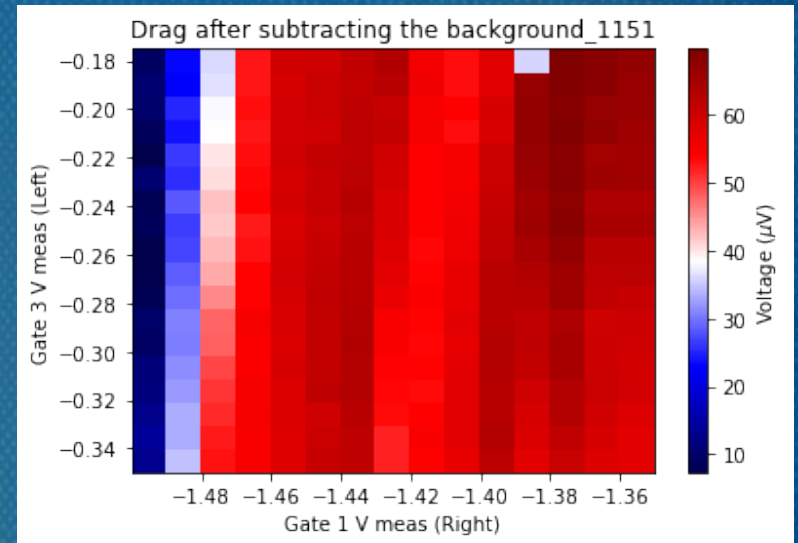
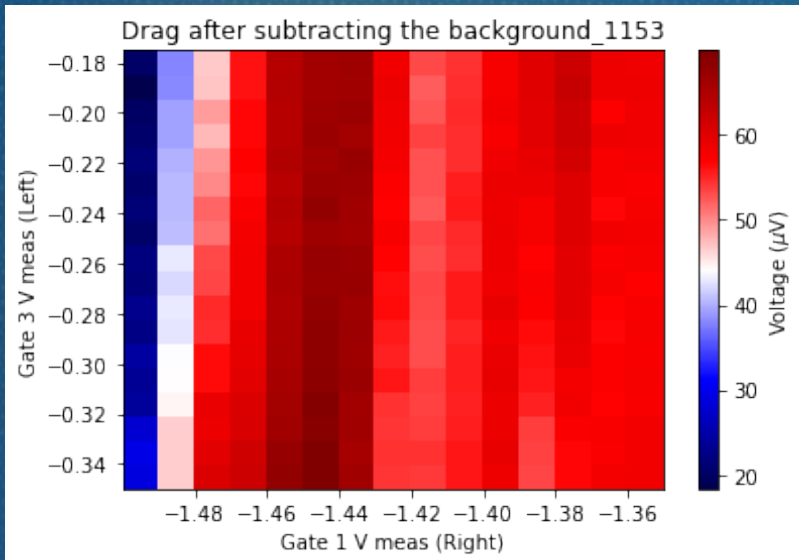
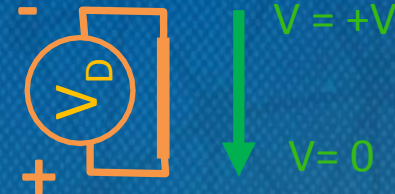
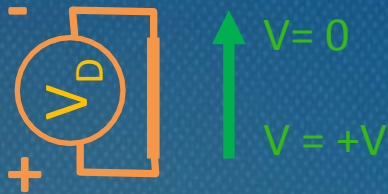
Symmetric : Rectification

Antisymmetric : Momentum- transfer



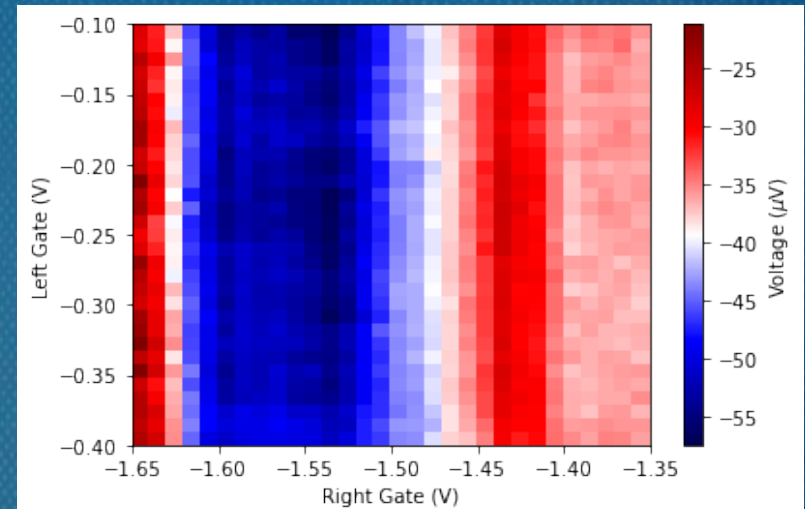
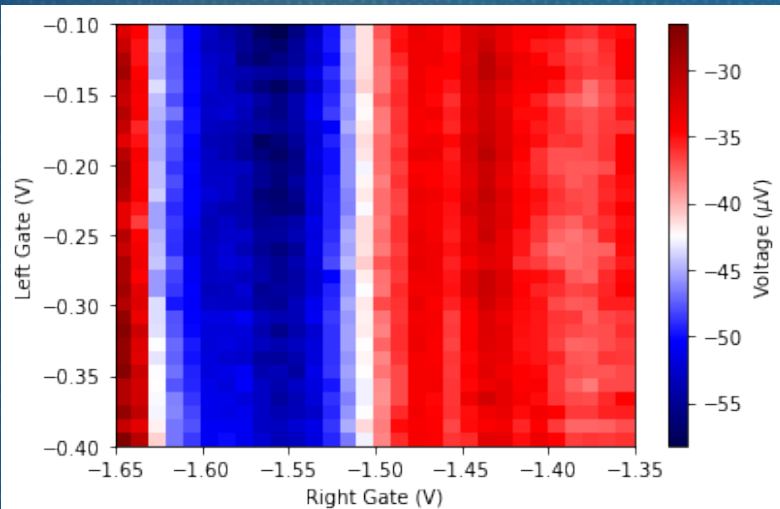
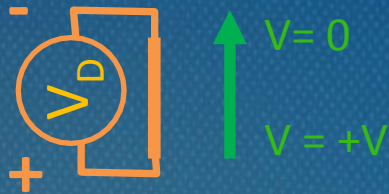
Symmetric part dominates

DC measurements



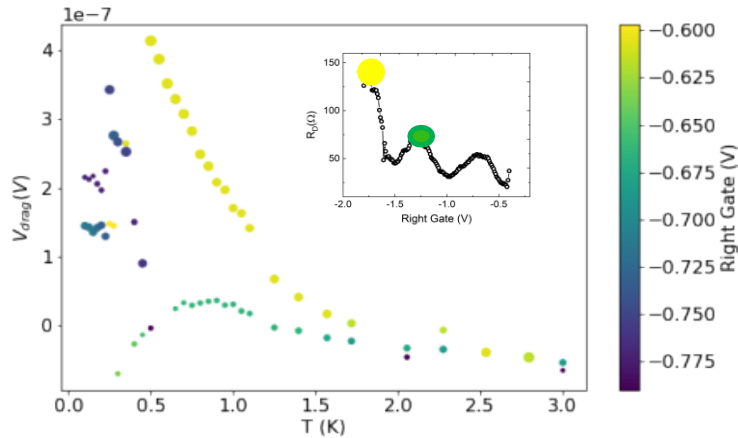
Signal is remains nearly identical
Consistent with charge fluctuations

DC measurements

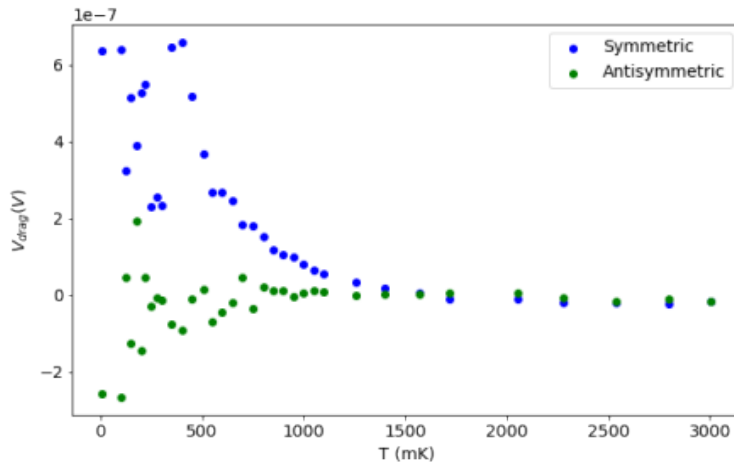


Similar rectification behavior
Currently analyzing current linearity and chemical
potential influence.

Temperature dependence overview



AC total contribution



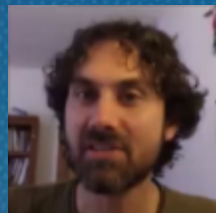
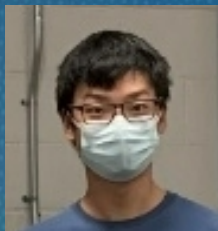
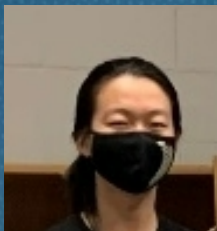
AC Symmetric vs antisymmetric contribution

Not a simple T^2 dependence

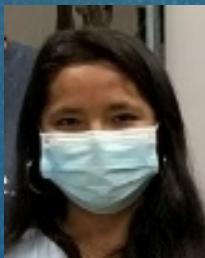
Collaborators/students

Si/SiGe exciton condensation

Growers at
National Taiwan
University



GaAs Coulomb drag



The National High Magnetic Field Laboratory is supported by the National Science Foundation through NSF/DMR-1644779 and the State of Florida.



Center for Integrated
Nanotechnologies



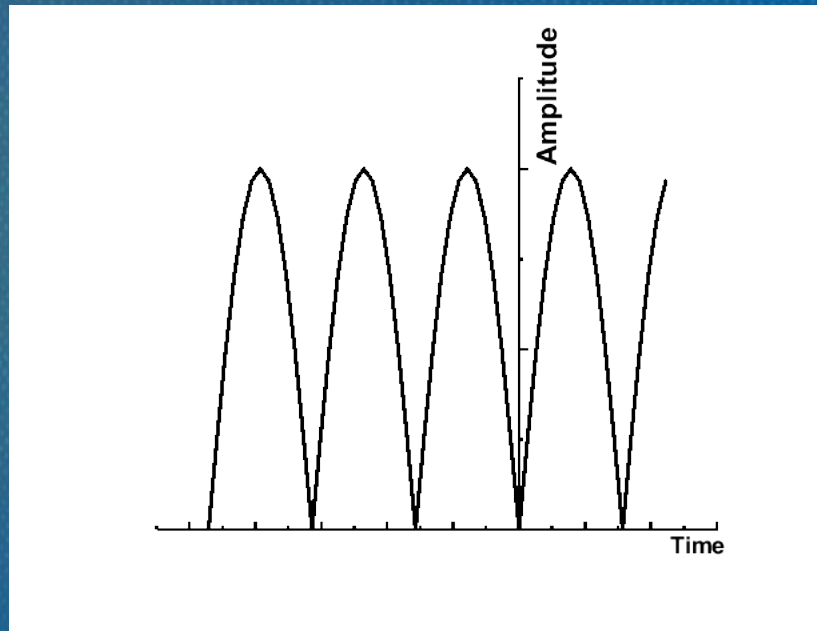
Sandia National Laboratories

Thank you for your attention

Questions?

Current rectification

Expectation

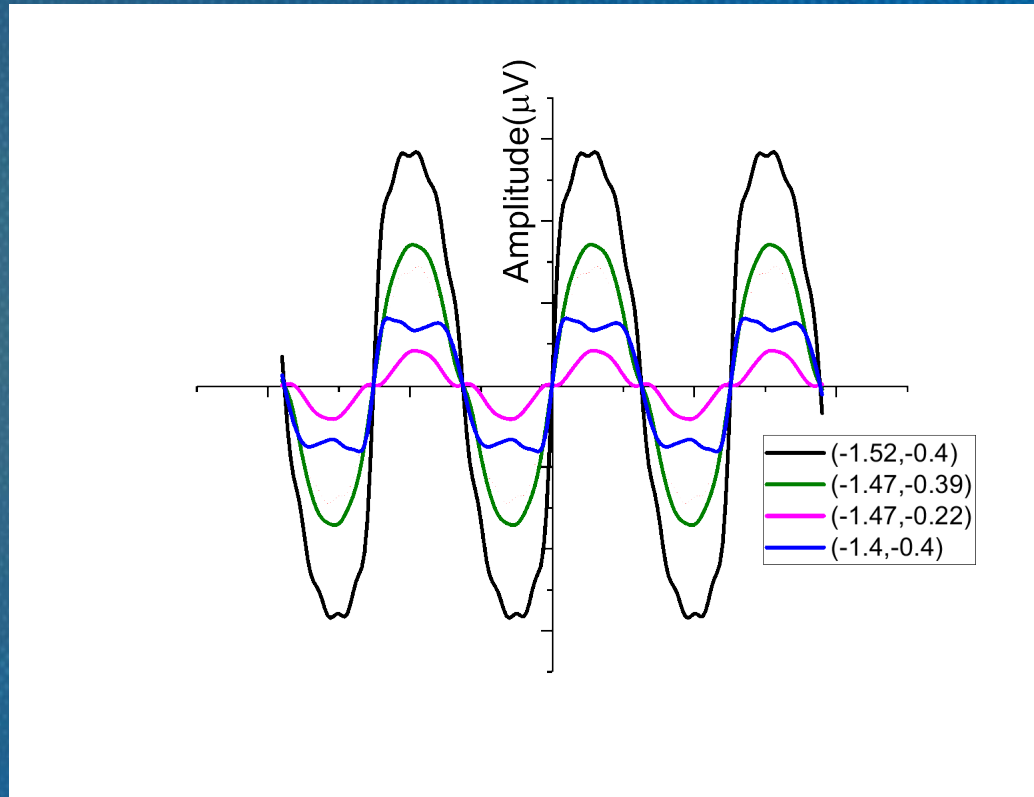


Sum of even sine terms

$$V_{\text{drag}} \sim |\sin(\omega t)|$$

Current rectification

Measured



Waveform depends on wires configuration

Cooling 1D electrons

- Coulomb drag in the $T=0$ limit → lowest electron value : 80 mK
- Drag in the spin-polarized regime → never attempted

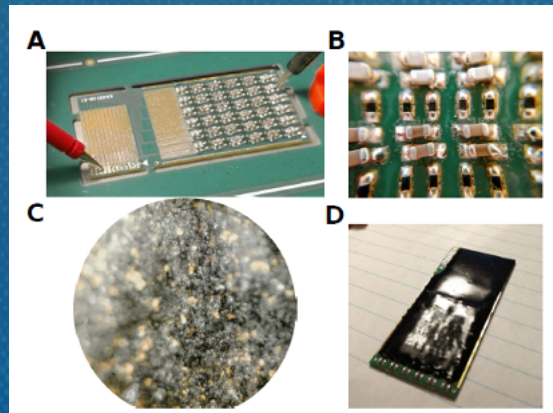
- 1- Samples lattice temperatures usually limited to ~ 20 mK
- 2 - Electron temperatures difficult to cool in low-dimensional systems



- 1 - Nuclear demagnetization → Lattice temperatures ~ 0.5 mK
- 2 – Sample in ^3He immersion cell
Electrical connections with silver sintered leads
5th order RC filter and continuous element filters at 30 mK



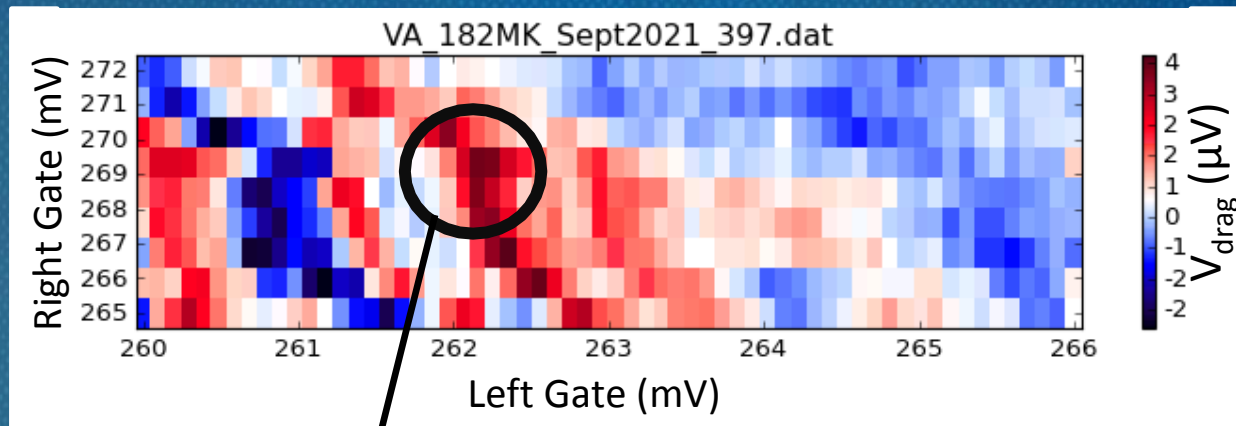
Microkelvin facilities



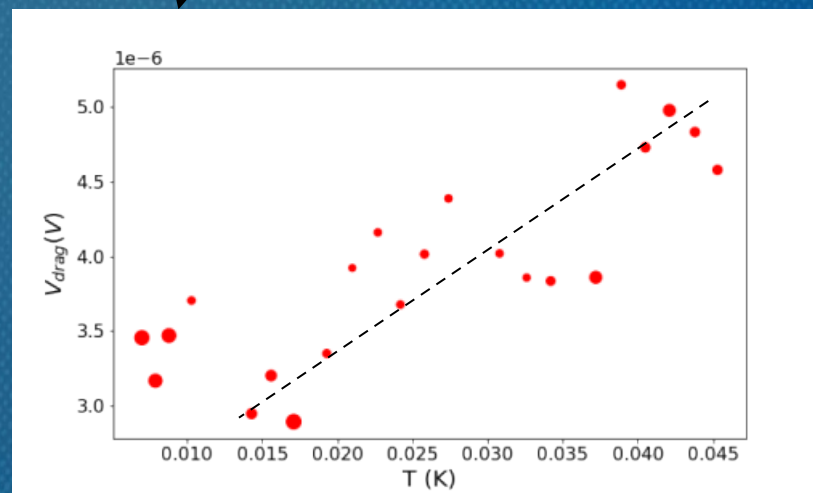
Ultra-low-temperature 1D drag

Preliminary results in laterally coupled quantum wires :

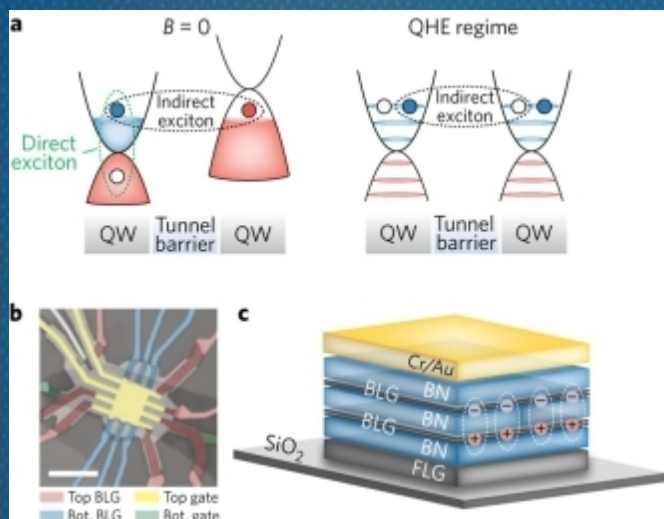
Coulomb drag is modulated with wire occupancy



A temperature dependence is observed down to ~ 10 -15 mK



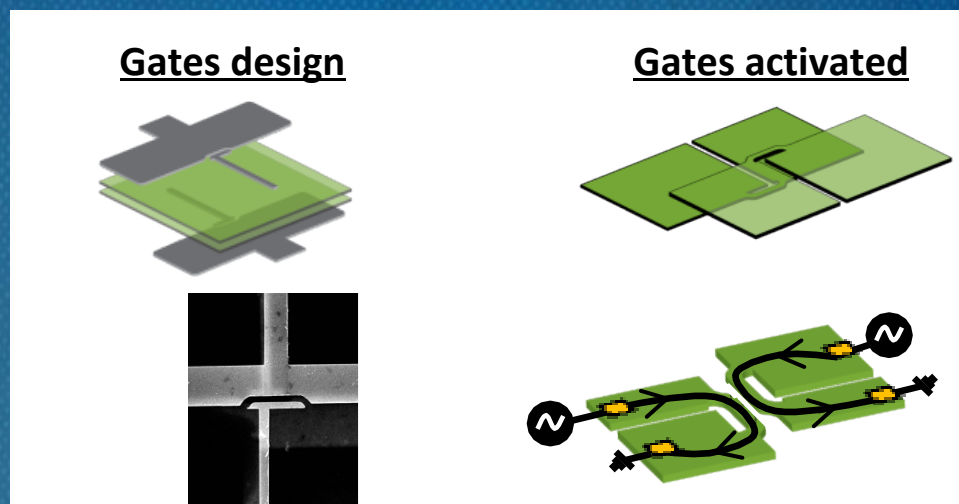
Exciton condensation in 2D bilayers



J. I. A. Li *et al.* Nature Phys. **13**, 751 (2017)

Material systems :
GaAs/AlGaAs bilayers
Graphene bilayers
Si/SiGe bilayers

Signatures of Luttinger liquids in quantum wires

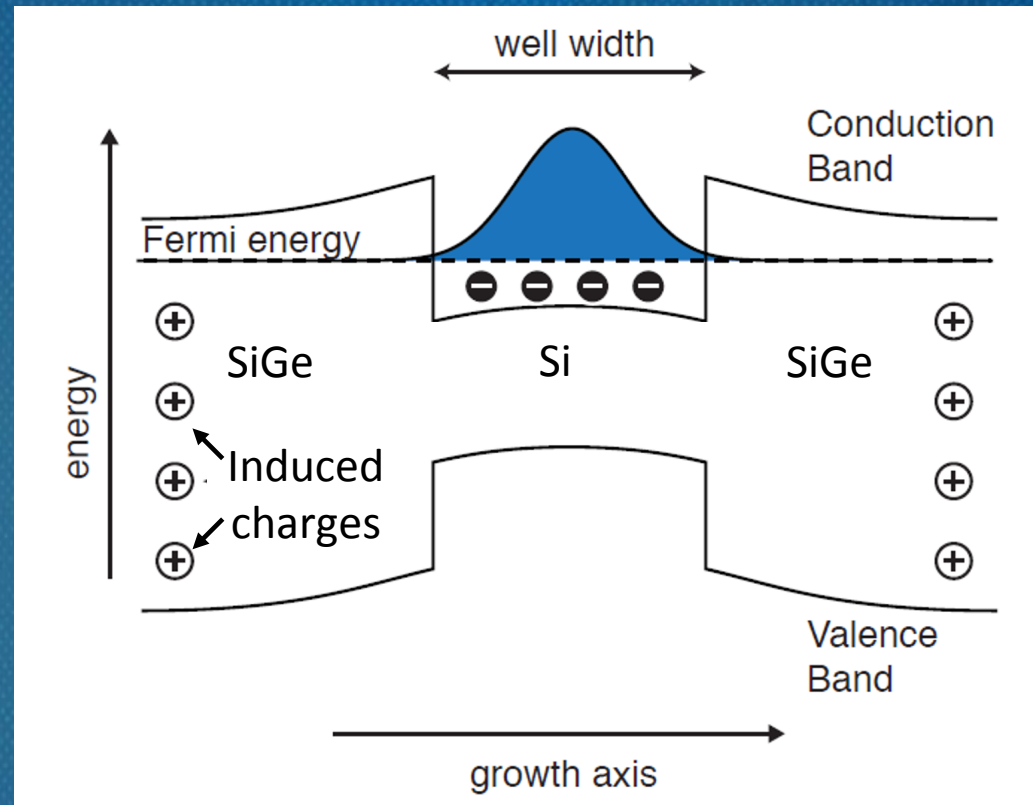


D. Laroche *et al.* Nature Nanotech. **6**, 793 (2011)

Techniques:
Universal conductance scaling
1D-1D and 1D-2D resonant tunneling
Coulomb drag

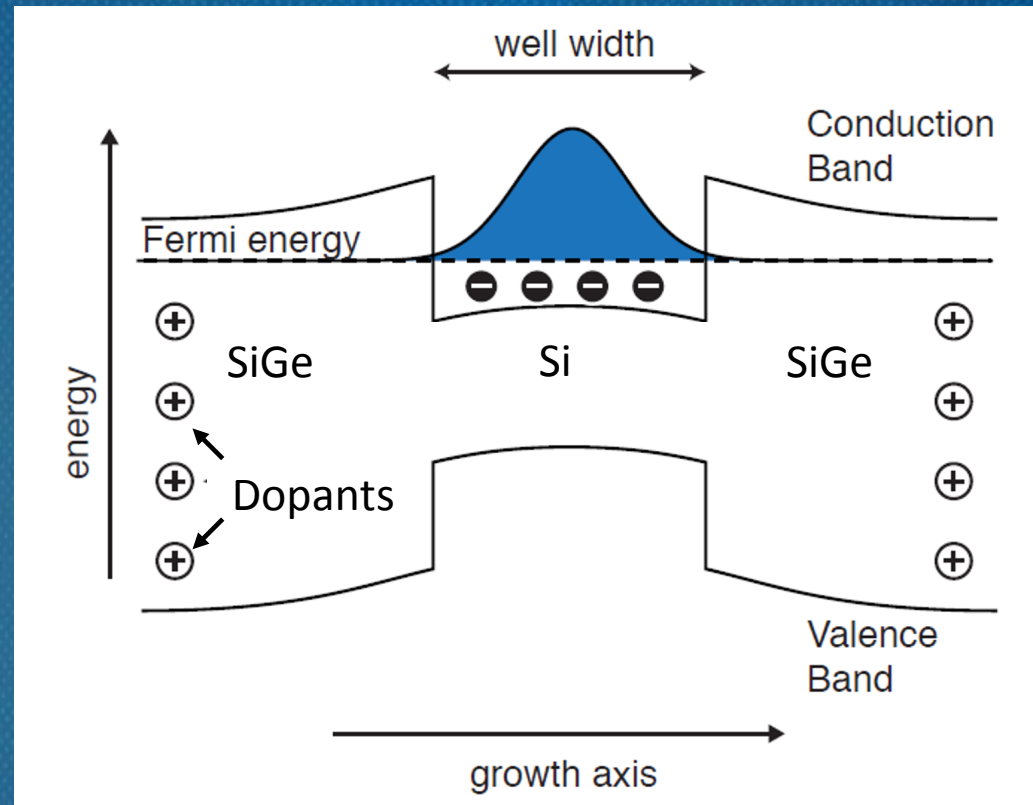
Quantum well

- Particle-in-a-box type of problem.
- A single 2D subband occupied at low-temperature
- Carriers induced by doping (intrinsic) or gating (extrinsic)
- Realized in GaAs/AlGaAs, graphene, InAs/InAlAs, SrTiO₃/LaAlO₃ and many others



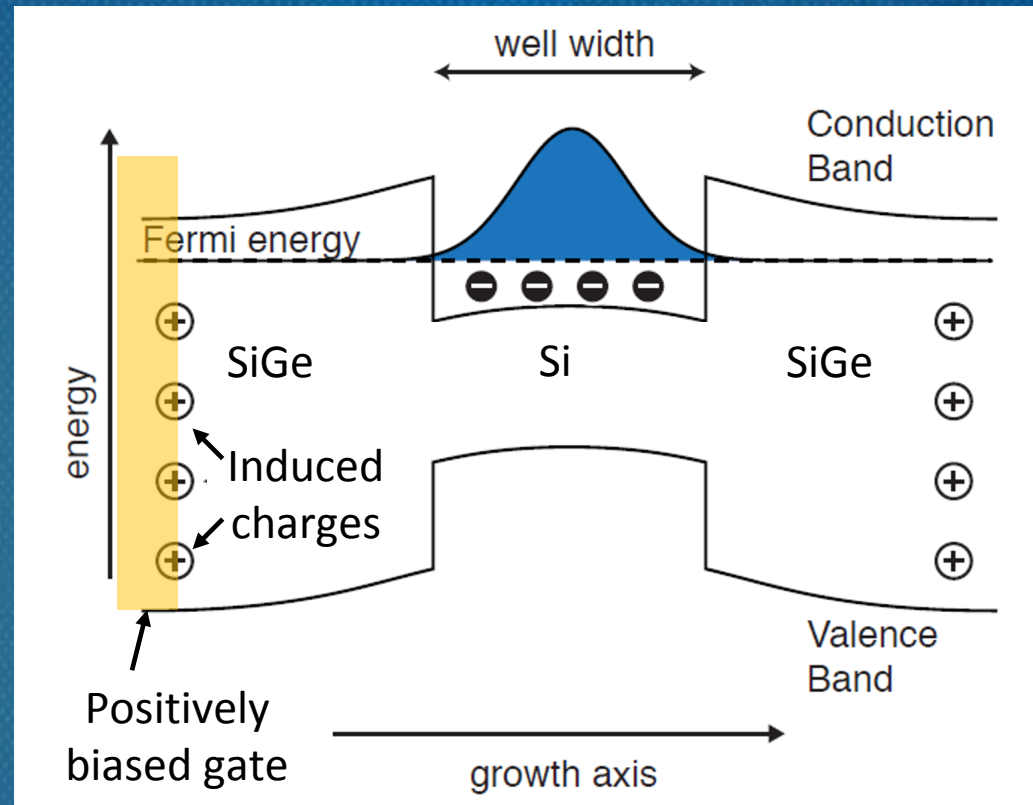
Quantum well

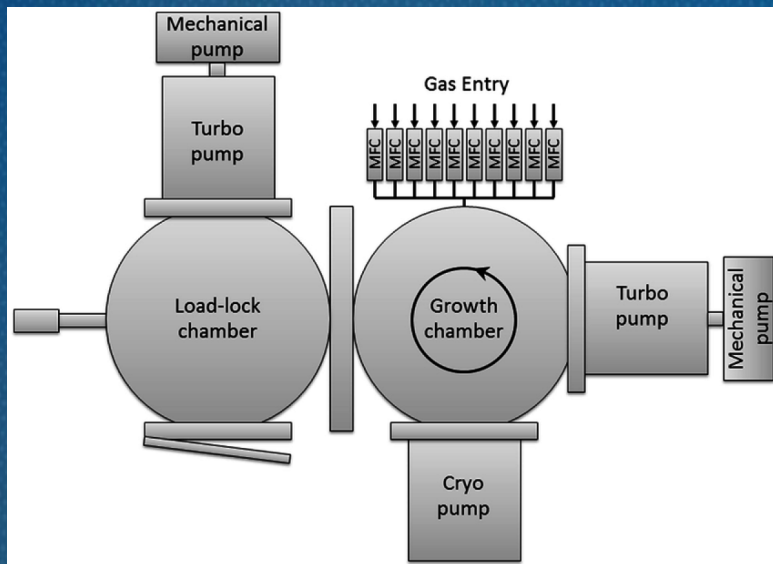
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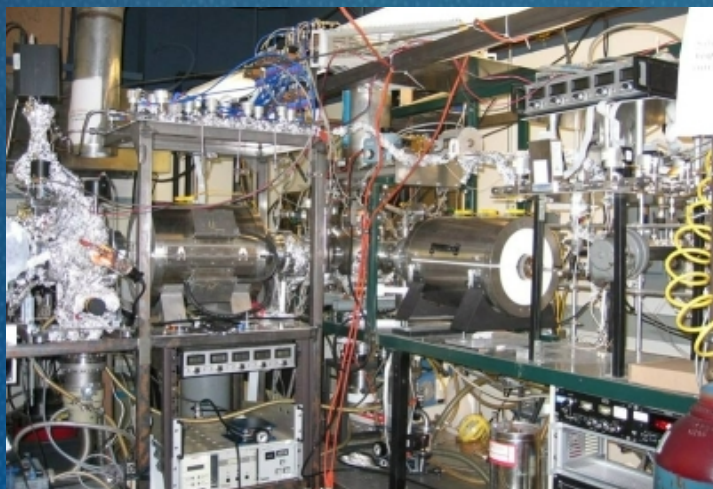
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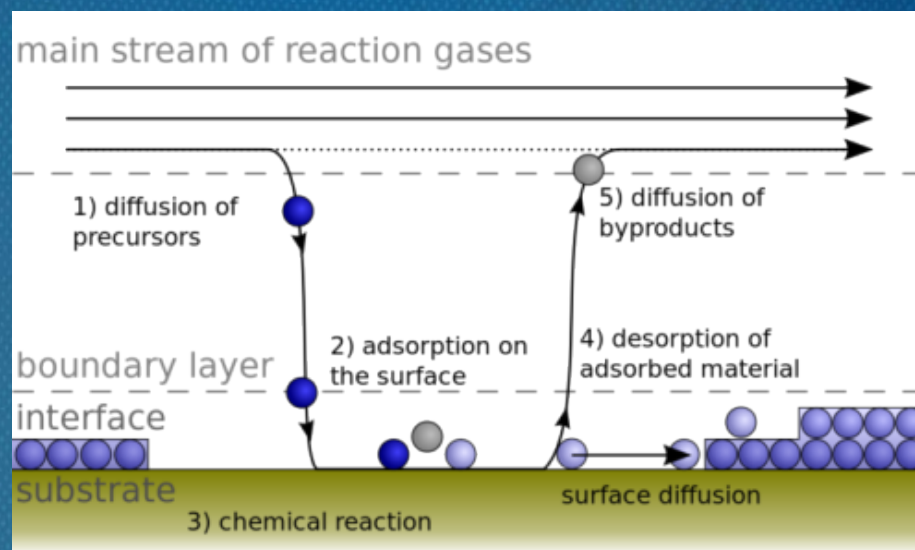




UHV-CVD machine schematics

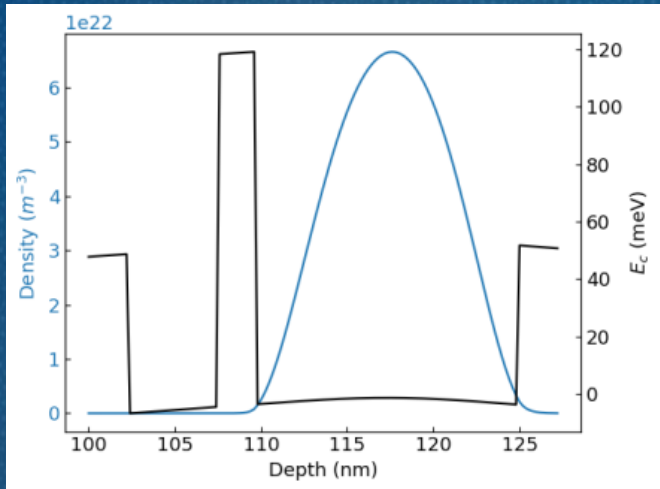


UHV-CVD from Kouvetakis group at ASU

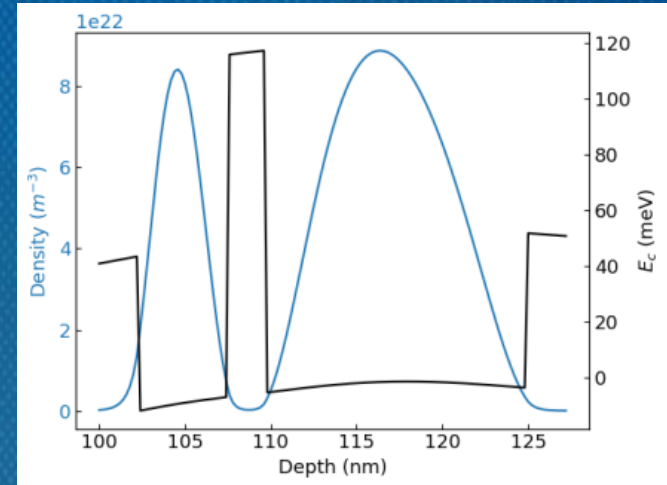


CVD process flow

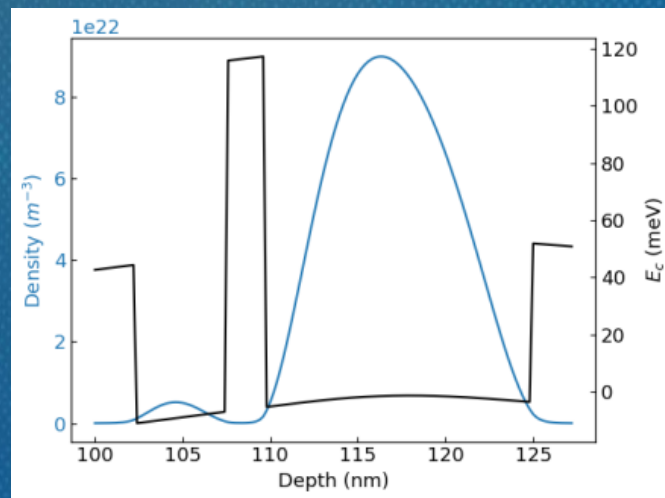
Asymmetric design - SP



$$n_{tot} = 6 \times 10^{10} \text{ cm}^{-2}$$

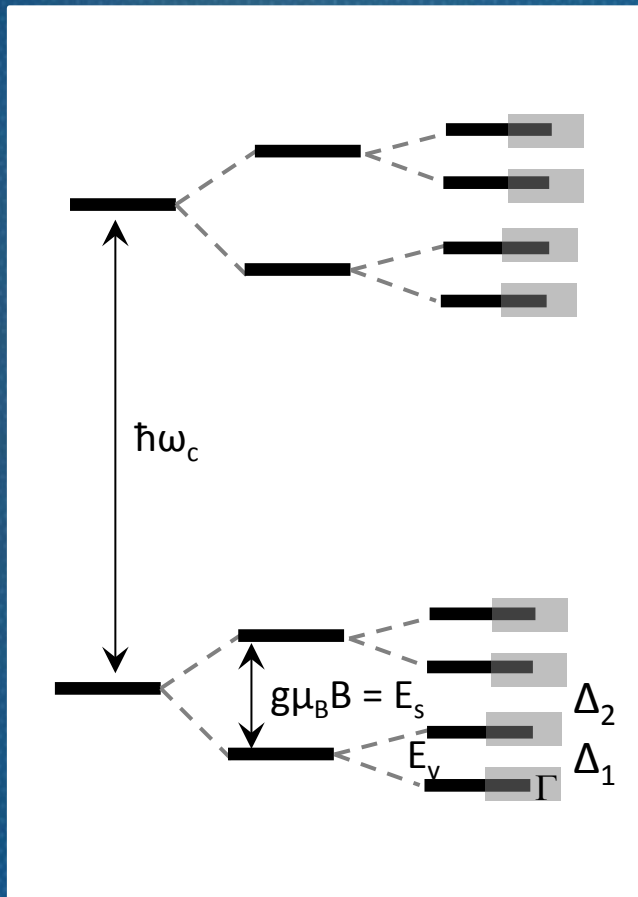


$$n_{tot} = 10.9 \times 10^{10} \text{ cm}^{-2}$$



$$n_{tot} = 8.39 \times 10^{10} \text{ cm}^{-2}$$

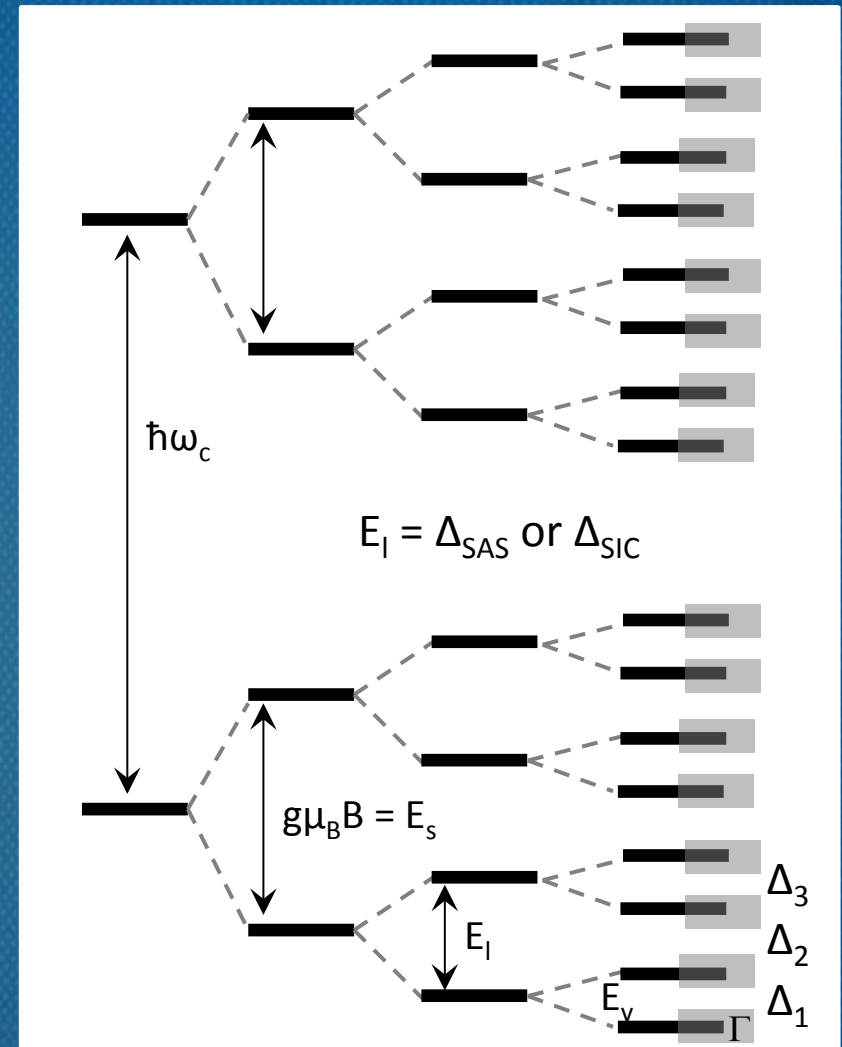
1 layer



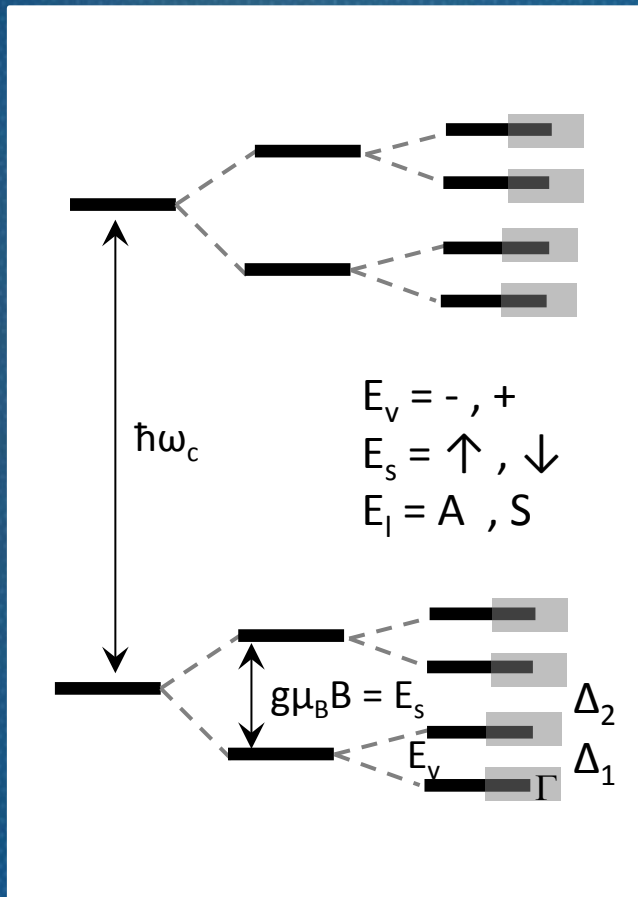
$$\Delta_1 = E_v - \Gamma$$

$$\Delta_2 = E_{s/l} - E_v - \Gamma = E_{s/l} - \Delta_1 - 2\Gamma$$

2 layers



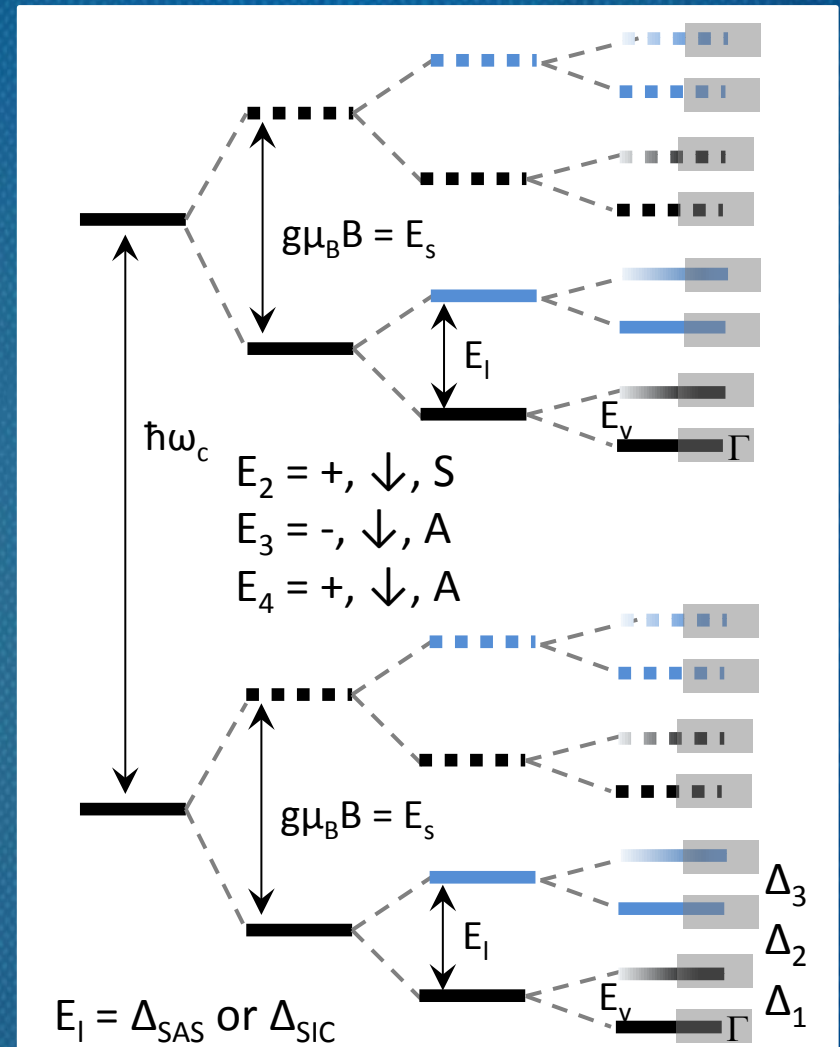
1 layer



$$\Delta_1 = E_v - \Gamma$$

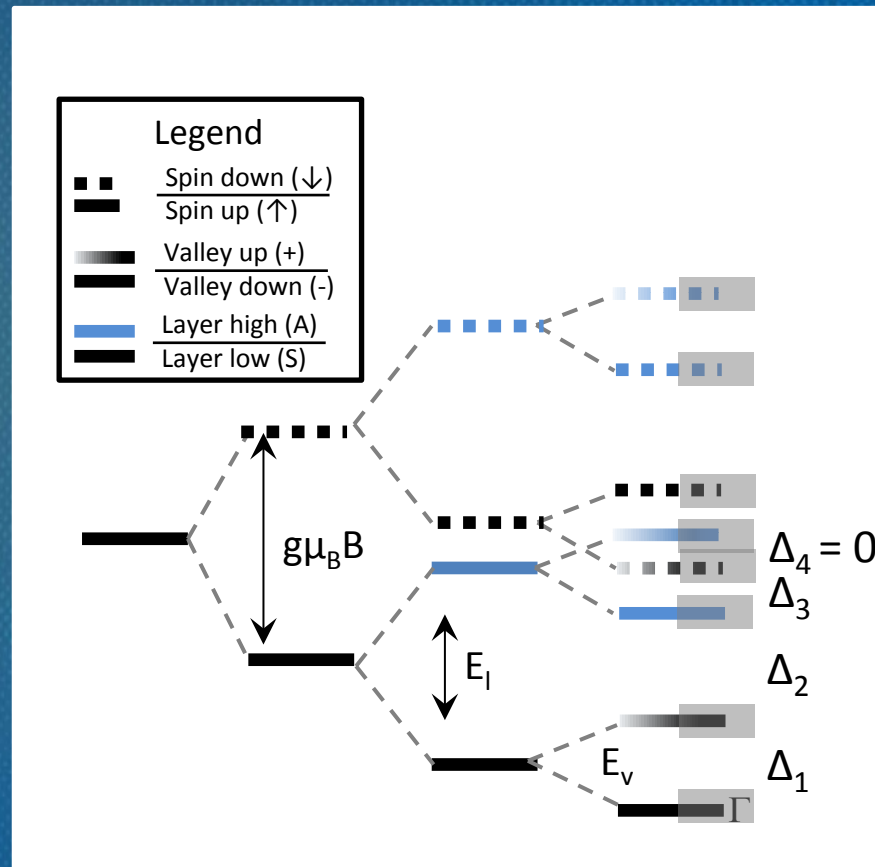
$$\Delta_2 = E_{s/l} - E_v - \Gamma = E_{s/l} - \Delta_1 - 2\Gamma$$

2 layers



Si/SiGe : theoretical fan diagram

Landau level crossings are possible



$$E_v = -, +$$

$$E_s = \uparrow, \downarrow$$

$$E_l = A, S$$

$$E_2 = +, \downarrow, S$$

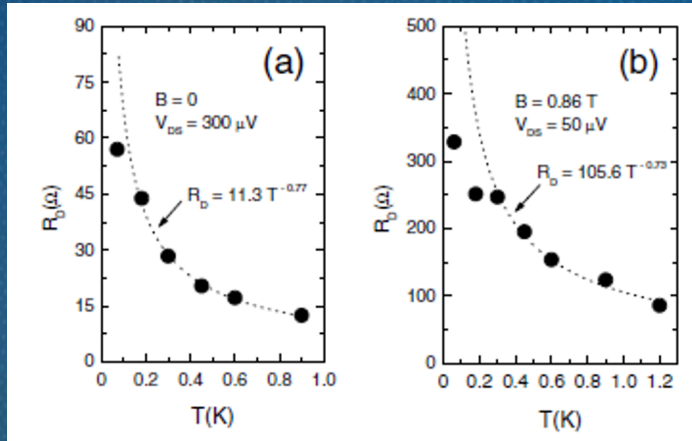
$$E_3 = -, \downarrow, A$$

$$E_4 = -, \uparrow, S$$

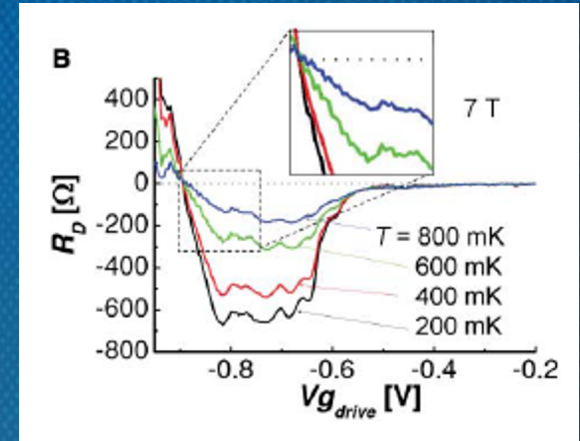
As 2 level cross, the quantum state is not observable experimentally

Previous drag studies

Laterally coupled quantum wires

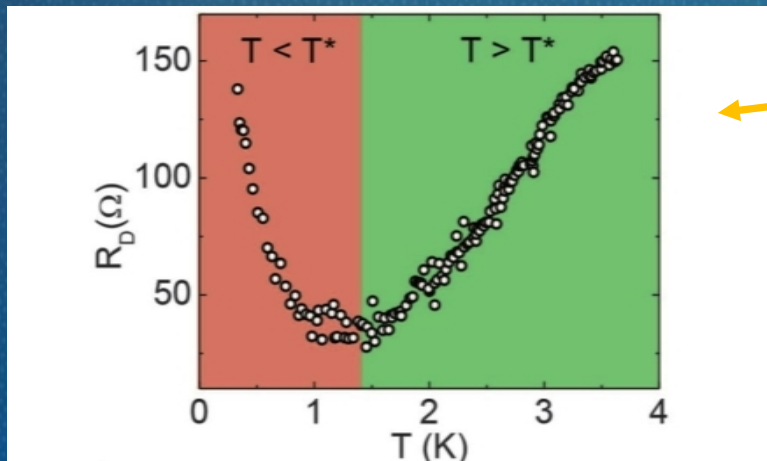


P. Debray *et al.* J. of Phys. Condes. Matter. **13**, 3389 (2001)

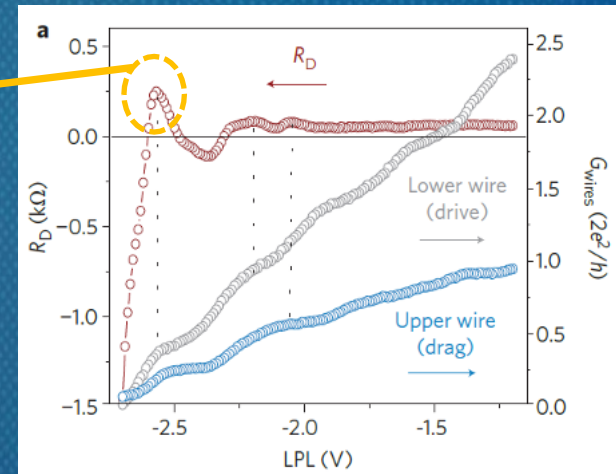


Yamamoto *et al.* Science **313**, 204 (2006)

Vertically-coupled quantum wires



D. Laroche *et al.* Science **343**, 631 (2014)



D. Laroche *et al.* Nature Nanotech. **6**, 793 (2011)

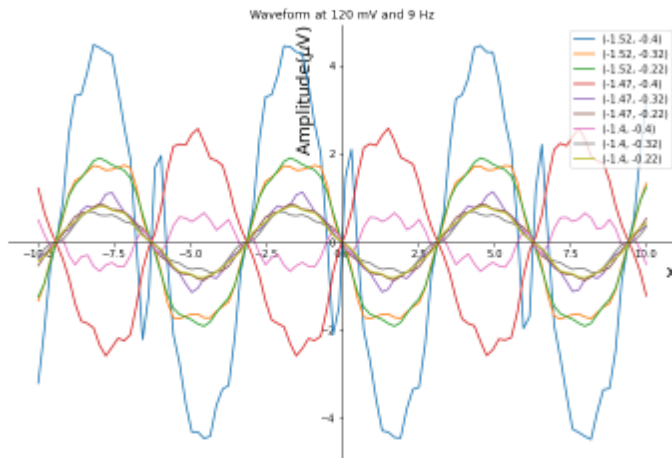
Survey of drag-inducing mechanism

Momentum-transfer models		Charge fluctuation models
$n_1 = n_2$	$n_1 \neq n_2$	Coupling through leads
<p>a Fermi liquid</p> <p>$R_D \sim T$</p> <p>$R_D \sim \cosh^4 x$ ($p^2 / 4 m^2 K_F T$)</p> <p>$eV \sim K_F T$</p>	<p>b Fermi liquid</p> <p>$R_D \sim e^{-W/T}$</p>	<p>h</p> <p>$R_D \sim T^2$</p>
<p>c Luttinger liquid – Backscattering</p> <p>$e^{(T^*/T)}$</p> <p>T^{2K-1}</p>	<p>d Luttinger liquid – Backscattering</p> <p>$e^{(T^* - W)/T}$</p> <p>$e^{(-Q/T)}$</p> <p>— $W < T^*$ — $W > T^*$</p>	
<p>e Luttinger liquid – forward and backscattering</p> <p>$e^{(T^*/T)}$</p> <p>T^2</p> <p>$T^{-3/2}$</p> <p>T^* T_0 E_F</p>	<p>f Luttinger liquid – forward and backscattering</p> <p>$(T/T_1)^3$</p> <p>$(T/T_1) e^{-T_1/T}$</p>	
<p>g Luttinger liquid – spin-incoherent</p> <p>$e^{(T^*/T)}$</p> <p>$T^{2K_p} e^{-cT/J}$</p> <p>$T^{(SK_p-3)}$</p> <p>T^* J</p>	<p>No change</p>	

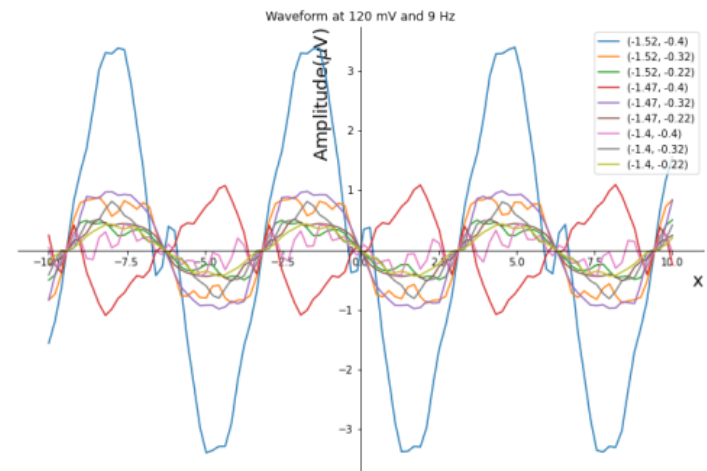
Symmetric and anti-symmetric contributions

Look at both contributions waveforms :

Symmetric



Anti-Symmetric



No clear cut waveform allowing identification of rectification or momentum transfer