



# Characterization of Memory Devices for Energy Efficient Analog In-Memory Neural Computing at the Edge

Matthew Marinella<sup>1</sup>, Tianyao Xiao<sup>2</sup>, Christopher Bennett<sup>2</sup>, William Wahby<sup>2</sup>, Robin Jacobs-Gedrim<sup>2</sup>, David Hughart<sup>2</sup>, Elliot Fuller<sup>3</sup>, A.A. Talin<sup>3</sup>, Sapan Agarwal<sup>3</sup>

1 – Electrical, Computer and Energy Engineering, Arizona State University, Tempe AZ

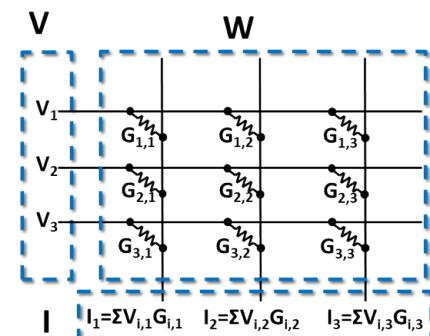
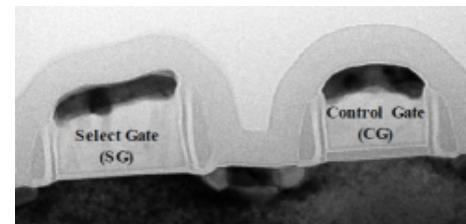
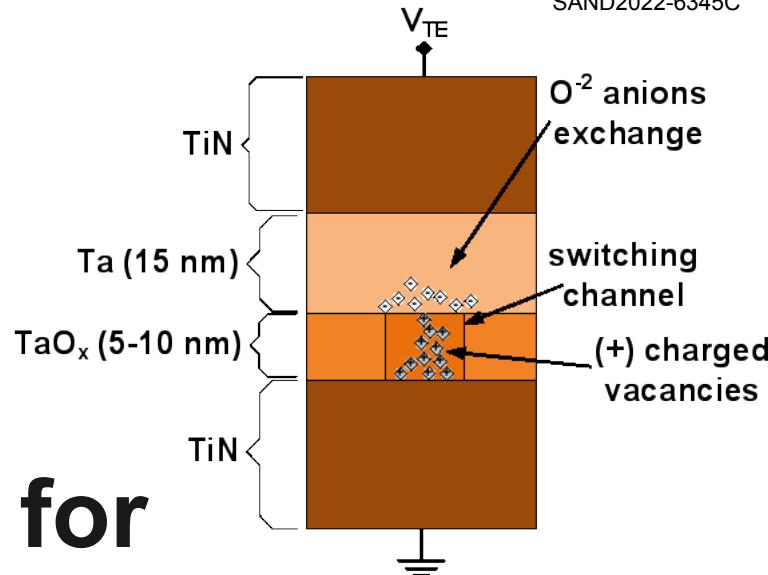
2 – Sandia National Laboratories, Albuquerque, NM

3 – Sandia National Laboratories, Livermore, CA

May 2, 2022



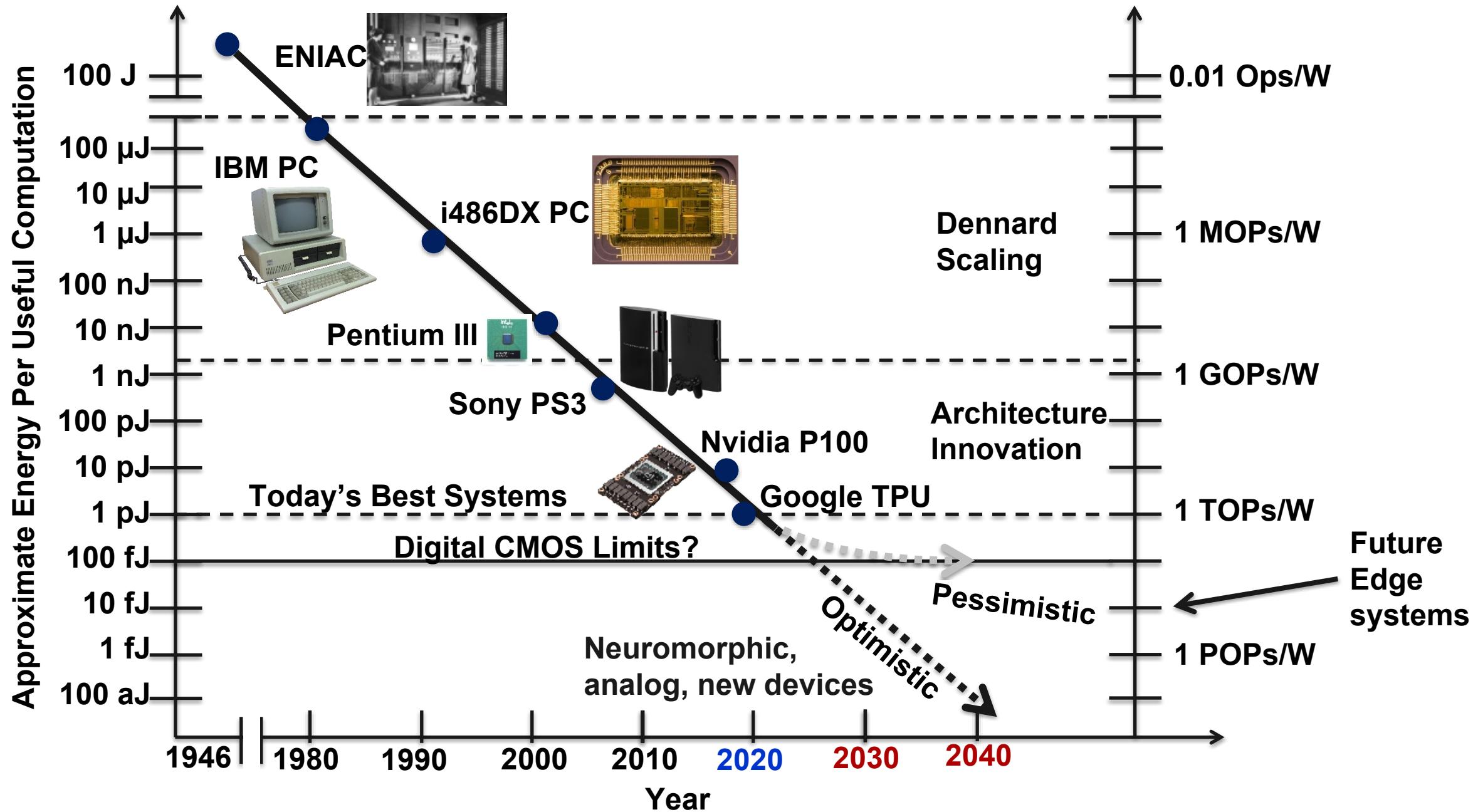
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# Outline

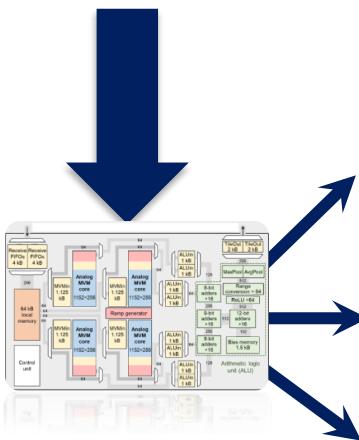
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- Motivation and Digital Limits
- Analog In-Memory Compute Energy & Latency
- Accurate Analog Inference
- Accurate Analog Training
- Conclusions



# Revolutionary Systems

- What do we want in the future?
- **10-100+ TOPS/W:**
- →*Supercomputing at the edge*
- Deep networks (100M+ parameters) execute and train in the field
- Lots of applications enabled and enhanced: Safe and fully autonomous navigation in ground, air and space vehicles, smart particle detectors
- Getting to this goal may require imperfect hardware...and this might be ok.

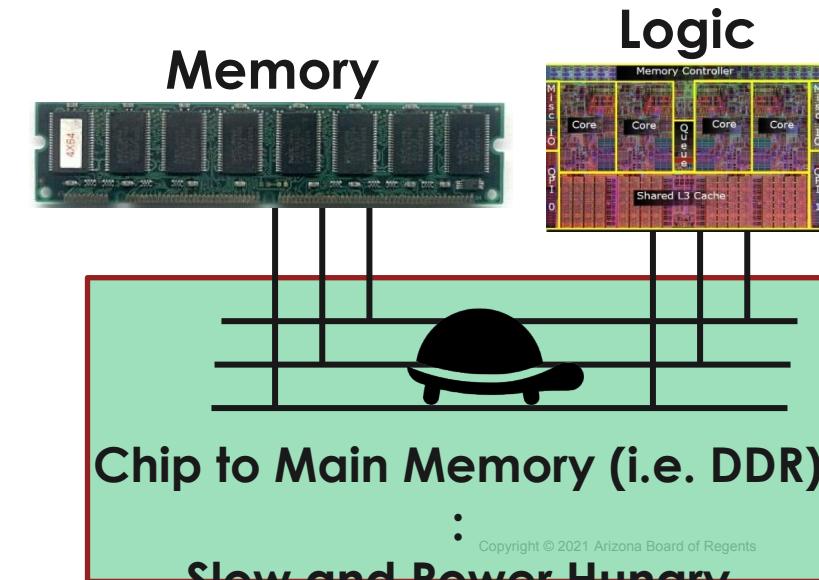


# Where are we now? Example: Apple A13

- Apple's iPhone 11 main SoC processor
- 7nm+ TSMC process
- Lightening AMX 8-core Neural Engine accelerator IP
- Apple spec: 5 TeraOps/s (TOPS) @ 8 bit precision
- Power is ~2.5-5W
- **State of the art smartphone chip Neural Accelerator:**
- ~ 1-2 TOPS/W or ~1pJ per 8 bit operation
- von Neumann architectures struggling to improve efficiency
- Especially difficult for off chip data movement
- CMOS research is continuing to push efficiency with low voltage, weight on chip designs – how much more possible?
- ***Where will the next orders of magnitude improvements in energy efficiency come from?***



apple.com, techinsights.com



# Outline

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# Keep Data in Memory & Exploit Physics for Computing

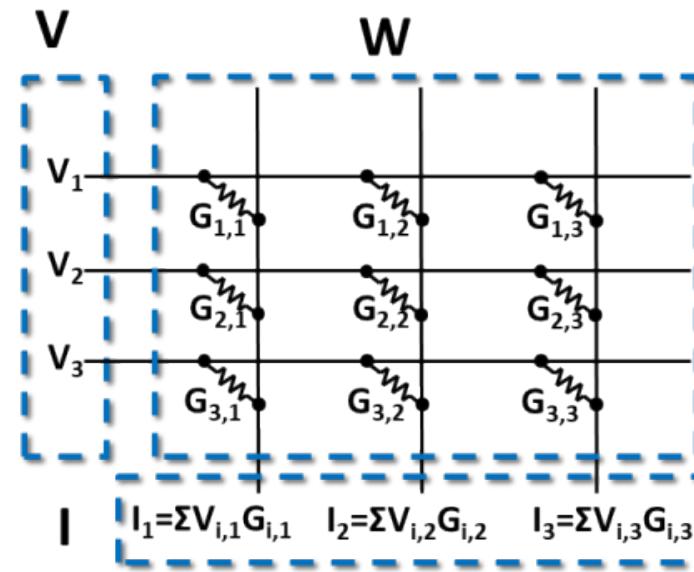
## Mathematical

$$V^T W = I$$

$$\begin{bmatrix} V_1 & V_2 & V_3 \end{bmatrix} \begin{bmatrix} W_{1,1} & W_{1,2} & W_{1,3} \\ W_{2,1} & W_{2,2} & W_{2,3} \\ W_{3,1} & W_{3,2} & W_{3,3} \end{bmatrix} =$$

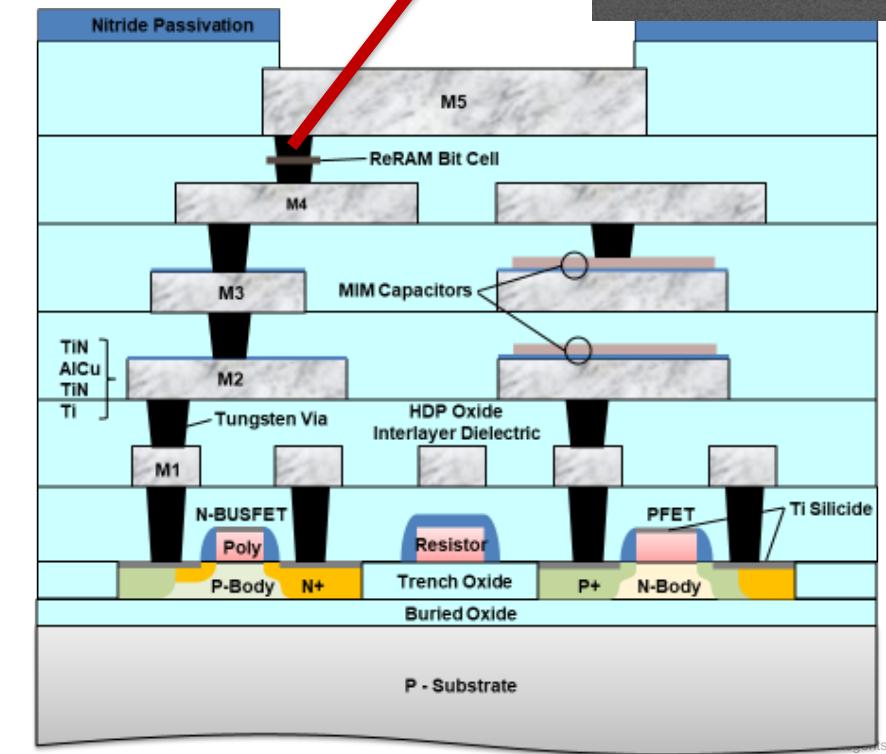
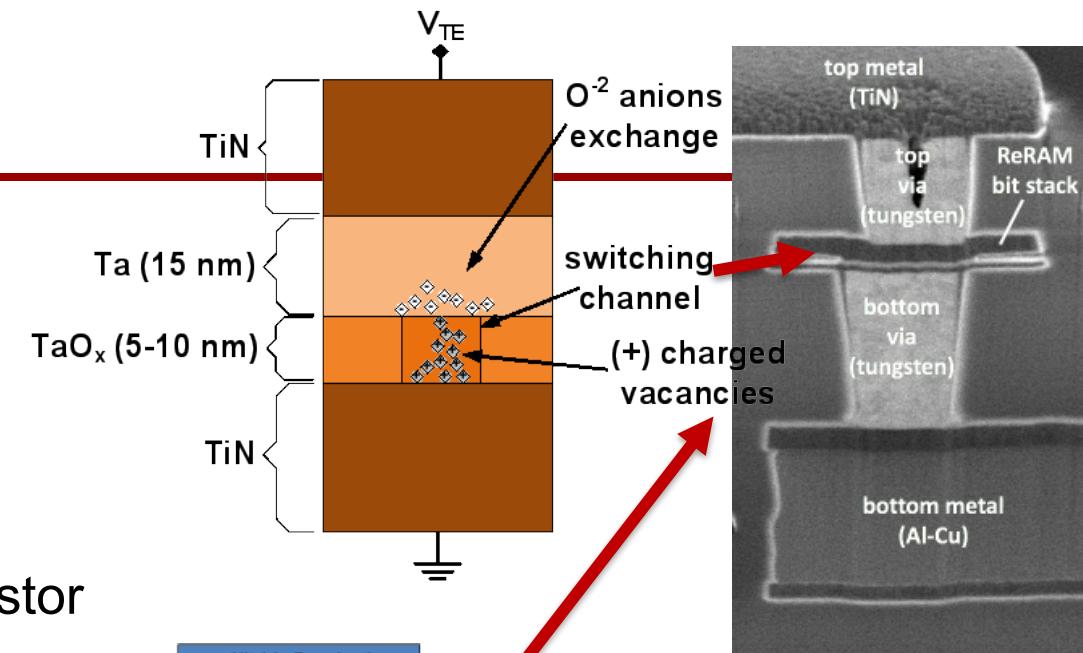
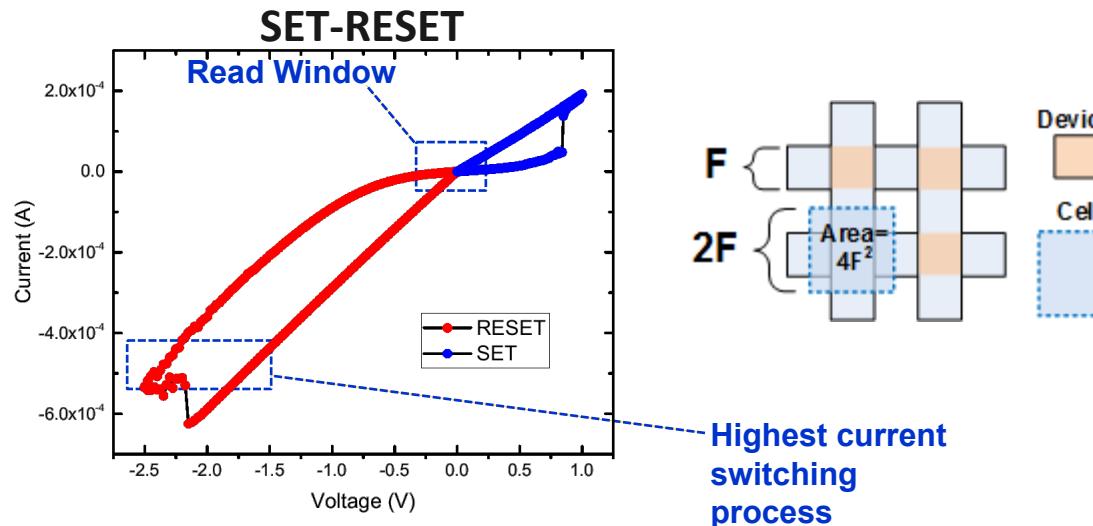
$$\begin{bmatrix} I_1 = \sum V_{i,1} W_{i,1} & I_2 = \sum V_{i,2} W_{i,2} & I_3 = \sum V_{i,3} W_{i,3} \end{bmatrix}$$

## Electrical



# Tunable Resistor: Oxide ReRAM

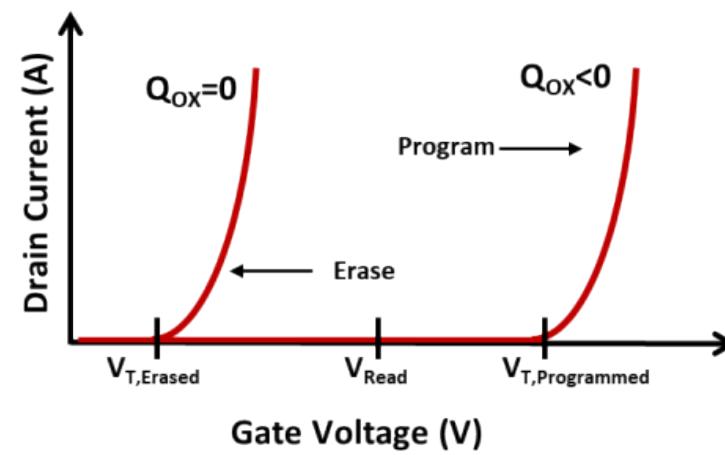
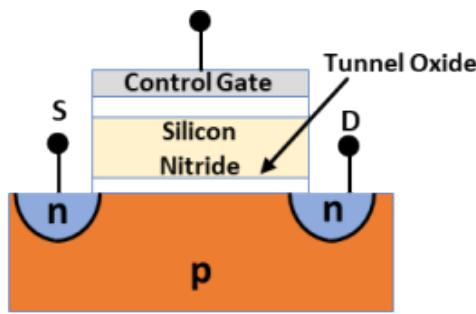
- Known as ReRAM, OxRAM, memristor
- Bipolar resistance modulation in metal-insulator-metal structure
- +V pulse, R decreases. -V pulse, R increases
- Fast, scalable, low switching energy, tunable resistor
- Potential for 100 Tbit of ReRAM on chip
- Analog In-Memory Compute weight



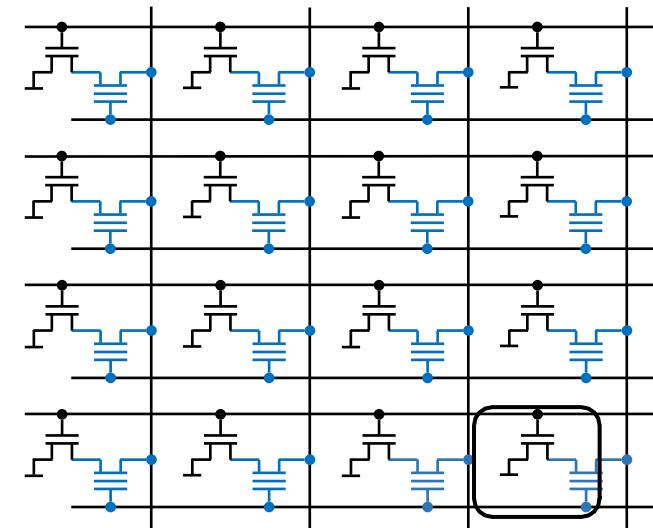
# Semiconductor-Oxide-Nitride-Oxide-Semiconductor (SONOS)

- Mature, commercial technology pioneered by Sandia in the 1980's
- Basis of modern SSD's (your iPhone uses a SONOS or a variant)
- Can be used as resistive array similar to ReRAM
- Commercial: Infineon 40nm SONOS

**SONOS Device**



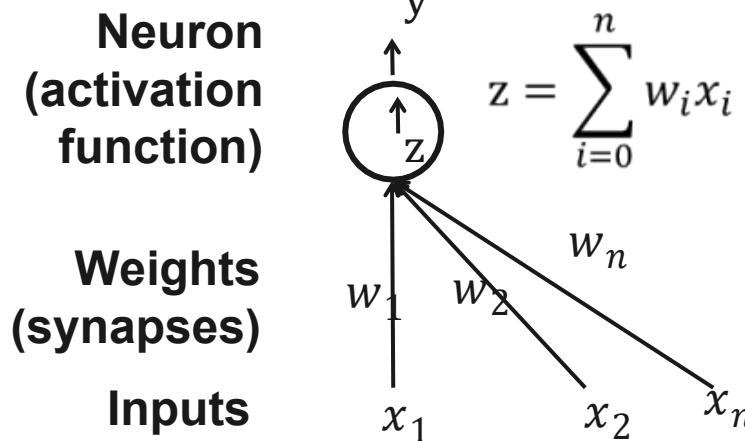
**SONOS Analog VMM Array Implementation**



# Neural Network Basics

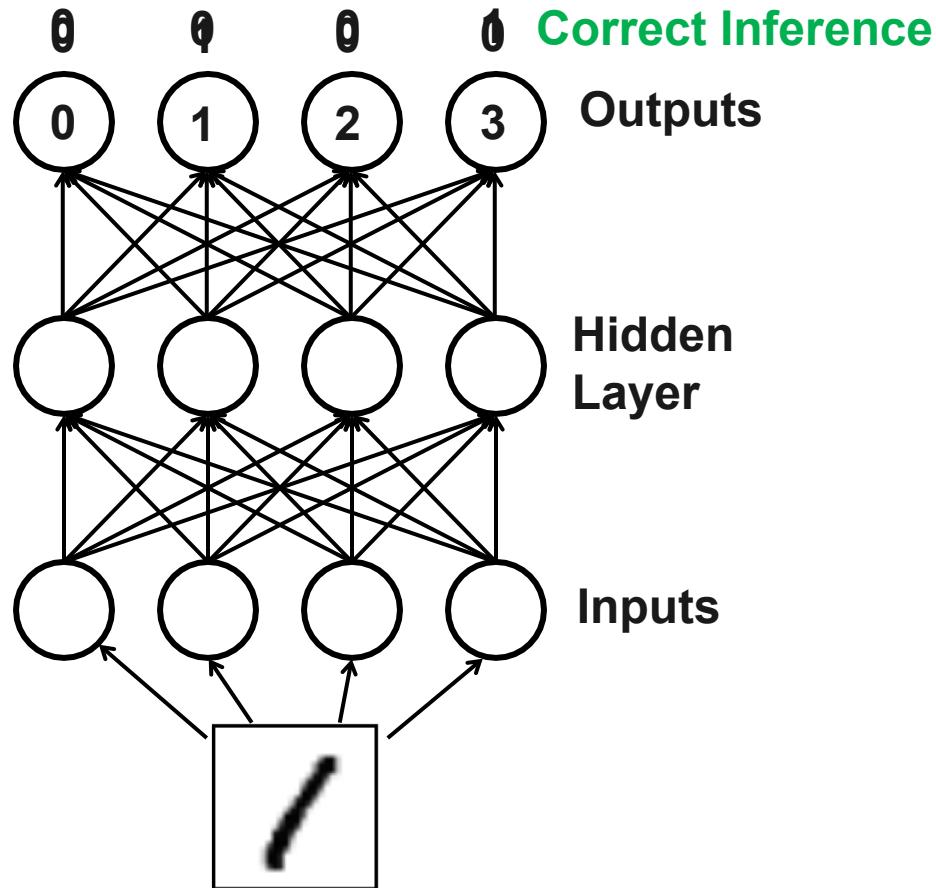
## Basic Building Block

$$y = \frac{1}{1 + e^{-z}}, \text{ReLU, etc.}$$

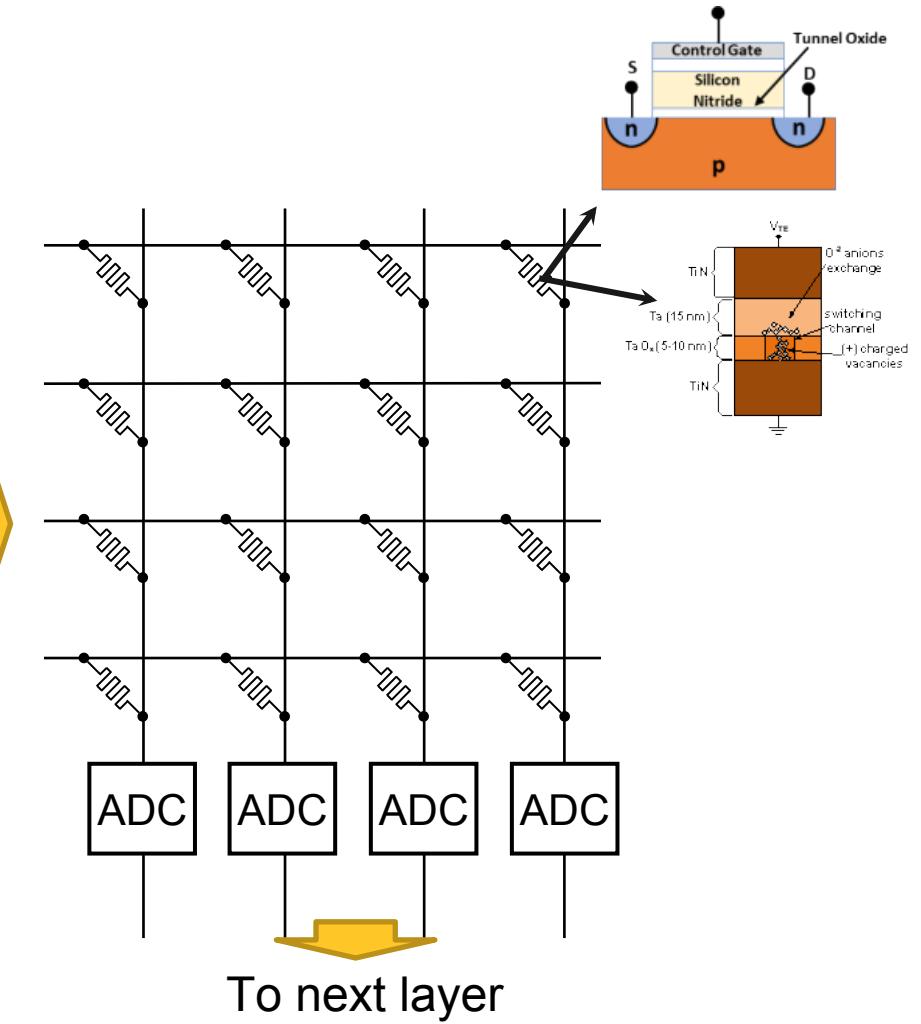
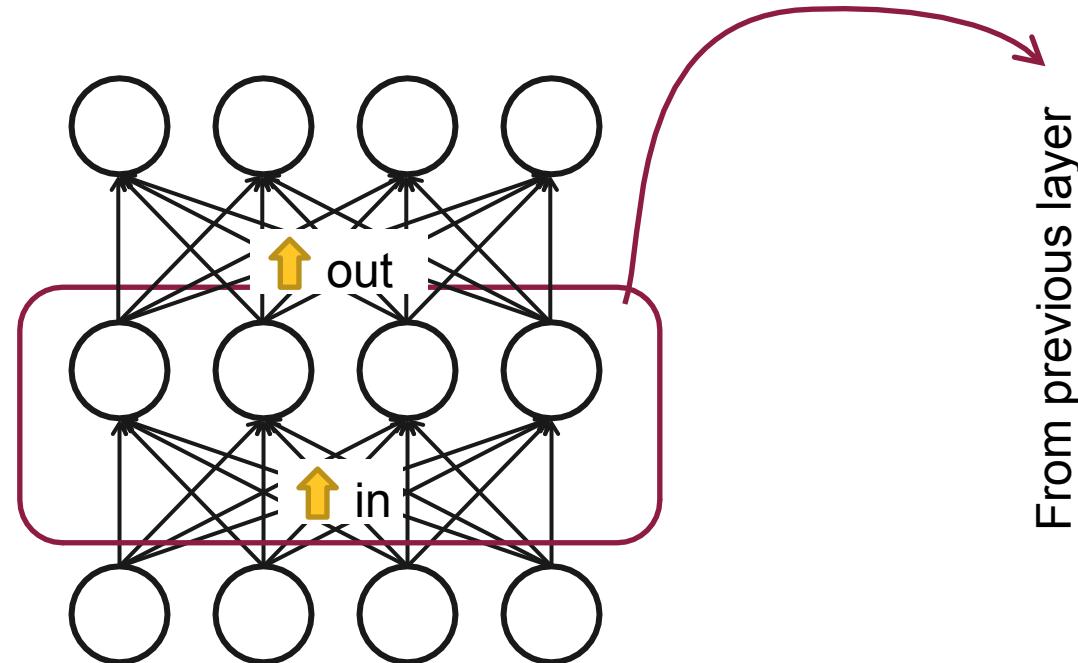


Incorrect –  
adjust if  
training

Simple Network:  
Inference & Training  
(Backpropagation)



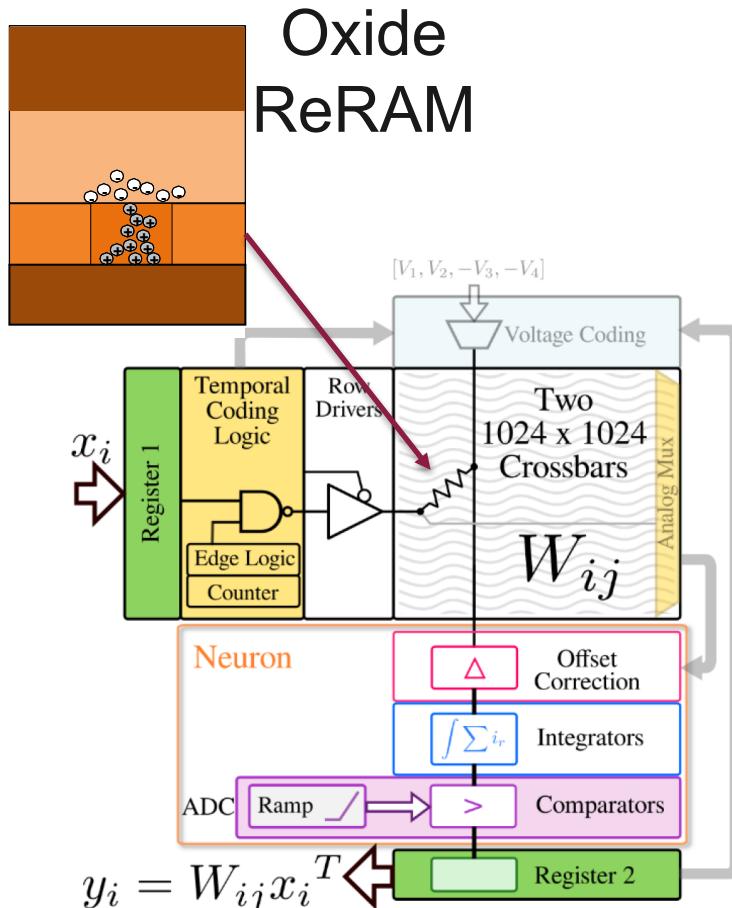
# Physically Mapping a Neural Network to Resistive Array



# How much computing needs to be done?

Metrics	LeNet 5	AlexNet	Overfeat fast	VGG 16	GoogLeNet v1	ResNet 50
<b>Top-5 error<sup>†</sup></b>	n/a	16.4	14.2	7.4	6.7	5.3
<b>Top-5 error (single crop)<sup>†</sup></b>	n/a	19.8	17.0	8.8	10.7	7.0
<b>Input Size</b>	28×28	227×227	231×231	224×224	224×224	224×224
<b># of CONV Layers</b>	2	5	5	13	57	53
<b>Depth in # of CONV Layers</b>	2	5	5	13	21	49
<b>Filter Sizes</b>	5	3,5,11	3,5,11	3	1,3,5,7	1,3,7
<b># of Channels</b>	1, 20	3-256	3-1024	3-512	3-832	3-2048
<b># of Filters</b>	20, 50	96-384	96-1024	64-512	16-384	64-2048
<b>Stride</b>	1	1,4	1,4	1	1,2	1,2
<b>Weights</b>	2.6k	2.3M	16M	14.7M	6.0M	23.5M
<b>MACs</b>	283k	666M	2.67G	15.3G	1.43G	3.86G
<b># of FC Layers</b>	2	3	3	3	1	1
<b>Filter Sizes</b>	1,4	1,6	1,6,12	1,7	1	1
<b># of Channels</b>	50, 500	256-4096	1024-4096	512-4096	1024	2048
<b># of Filters</b>	10, 500	1000-4096	1000-4096	1000-4096	1000	1000
<b>Weights</b>	58k	58.6M	130M	124M	1M	2M
<b>MACs</b>	58k	58.6M	130M	124M	1M	2M
<b>Total Weights</b>	60k	61M	146M	138M	7M	25.5M
<b>Total MACs</b>	341k	724M	2.8G	15.5G	1.43G	3.9G
<b>Pretrained Model Website</b>	[56] <sup>‡</sup>	[57, 58]	n/a	[57-59]	[57-59]	[57-59]

# VMM & Outer Product Update Tile Analysis with Ideal ReRAM

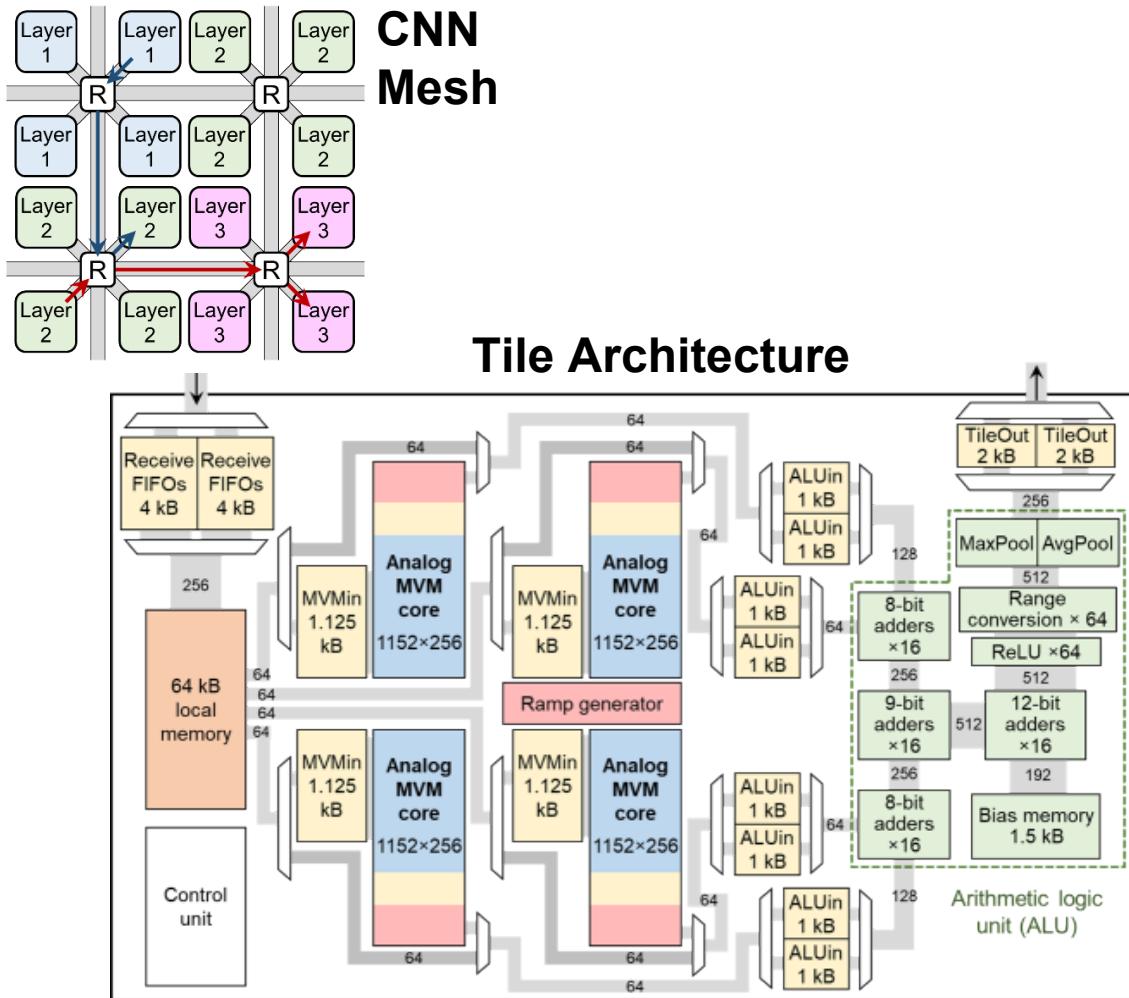


Component	Vector Matrix Multiply (8-bit, Inference)	Outer Product Update (8-bit, Training)
Energy/Op ReRAM (fJ)	12.2	2.1
Energy/Op Digital (fJ)	2718	4102
Array Latency ReRAM (μs)	0.38	0.51
Array Latency Digital (μs)	4	8

14nm PDK

Initial results: two orders of magnitude beyond digital!

# 78 TOPS/Watt 8-bit Inference using 40nm SONOS



ISAAC (2016)	Newton (2018)	This work
32 nm, ReRAM	32 nm, ReRAM	40 nm, SONOS
16 bits	16 bits	8 bits
0.63 TOPS/W (theoretical peak)	0.92 TOPS/W (theoretical peak)	21.8 TOPS/W (on ResNet-50) 55 TOPS/W (custom net, near peak)

- Based on 40nm SONOS devices from our commercial collaborator, Infineon

TOPS = TeraOperations / sec

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# Analog Accuracy Challenges

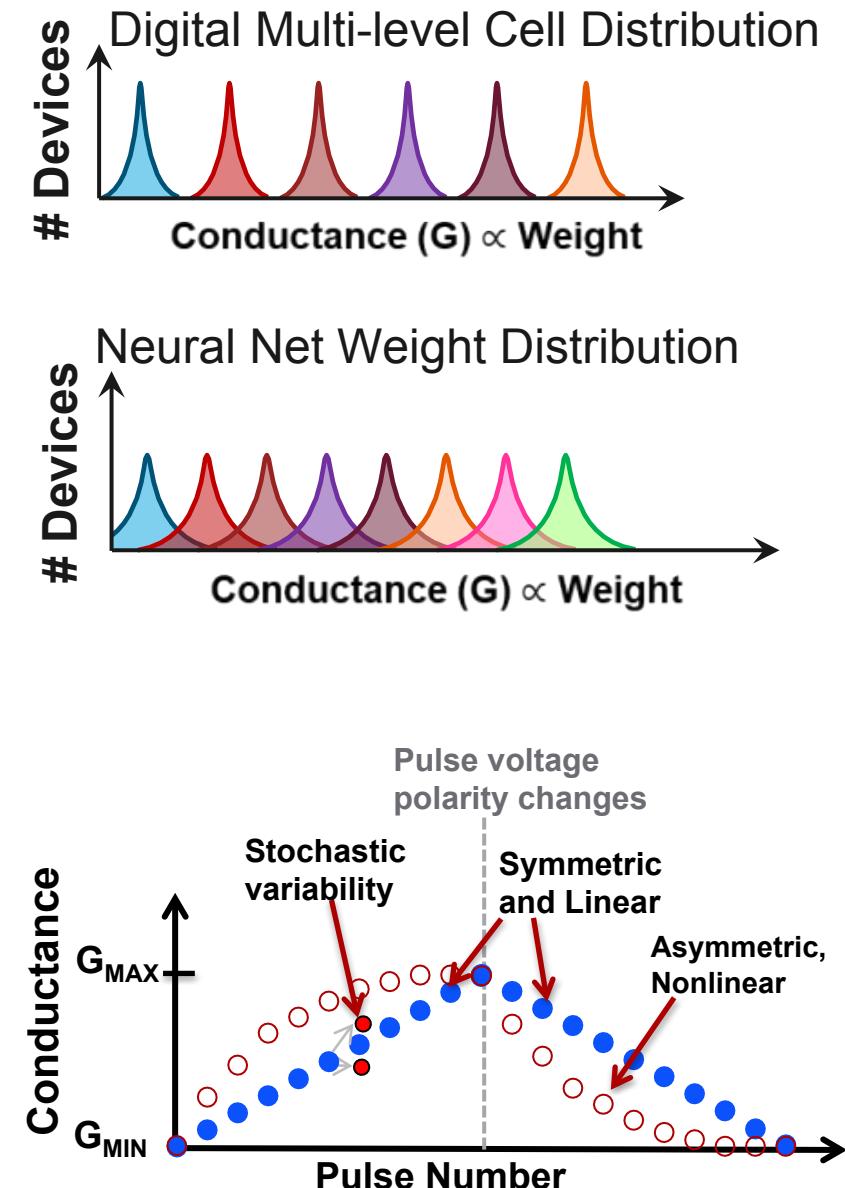
- Analog in memory compute offers great benefits...
- ...but comes with great challenges
- Digital: Deterministic results
- Analog: Device characteristics affect *algorithm accuracy*!
  - Research challenge: analog behavior cannot compromise final result

## Inference Accuracy Challenges

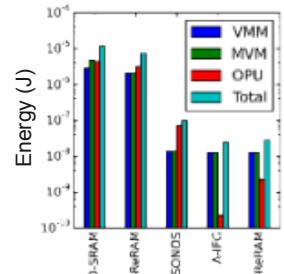
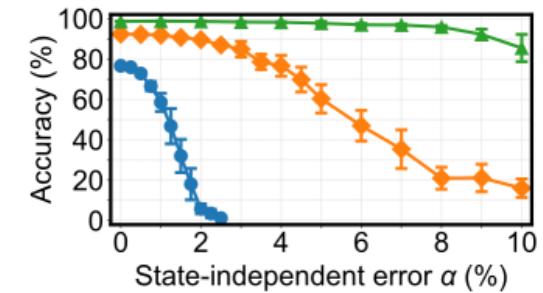
- Measured device conductance should be proportional to weight – but this is only approximately true
- Caused by **analog programming accuracy versus state, current drift, read noise**

## Training Accuracy Challenges

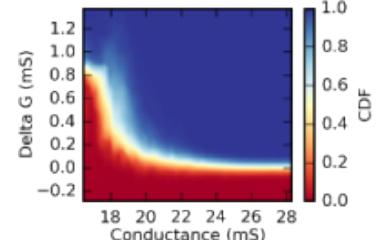
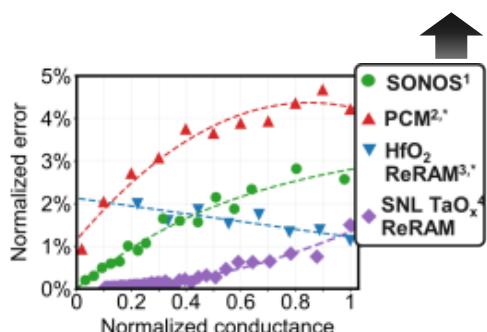
- Actual analog device state change does not match intended weight update
- Caused by **write nonlinearity, asymmetry, stochasticity**
- **Device to device variation**



# Multiscale CoDesign Framework Required for Device Accuracy Modeling

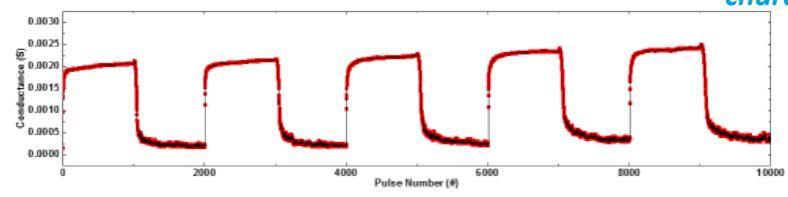


**Accuracy/Energy/Performance Model**  
Model accuracy, energy, and performance based on device attributes



**ROSS SIM**

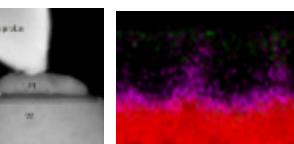
**Sandia Cross-Sim:**  
Translates device measurements and crossbar circuits to algorithm-level performance



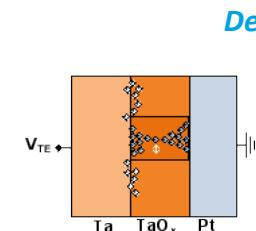
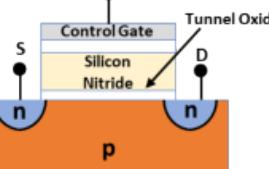
**Analog characterization**

**Devices**

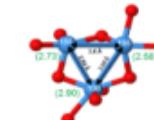
**In situ Characterization**



**Materials**



**Ab Initio Modeling**

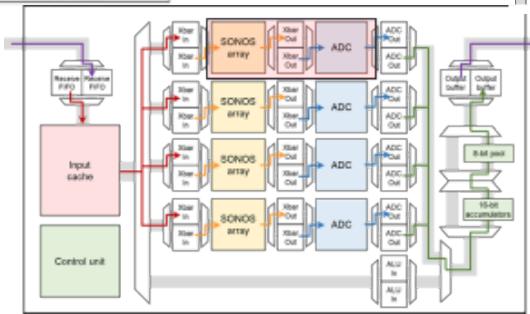
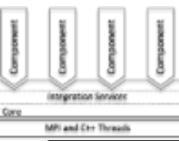


**Algorithms**

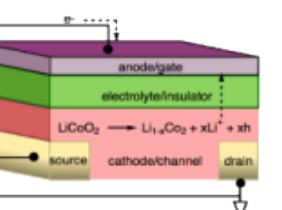
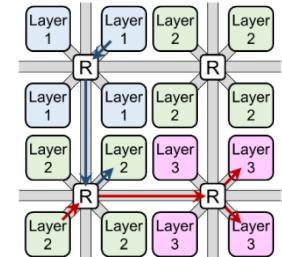
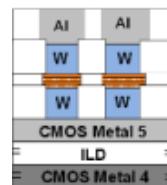
**Target Algorithms**

- Deep Convolutional Nets
- Sparse Coding
- Liquid State Machines

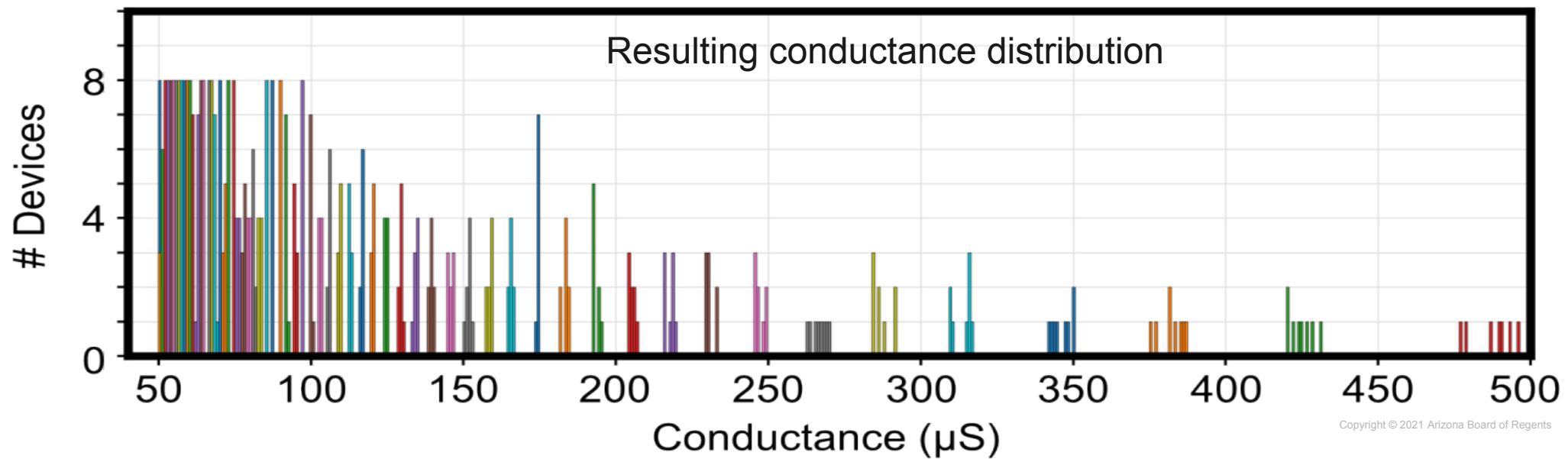
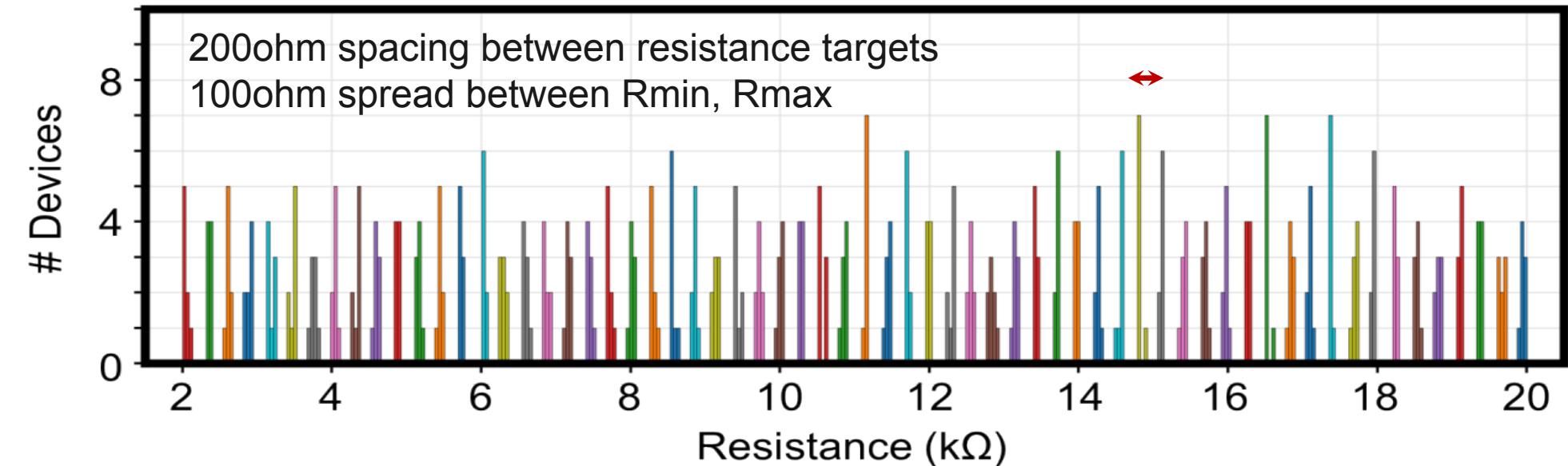
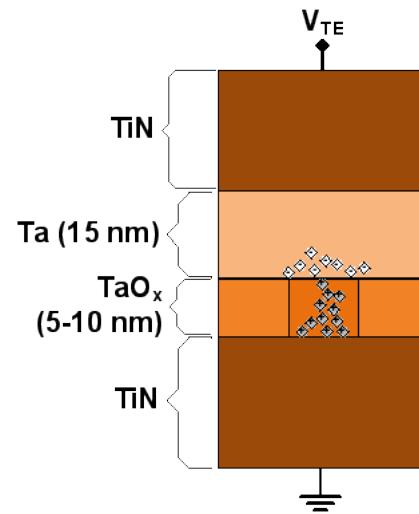
**Architecture Simulation**



**Device Models**

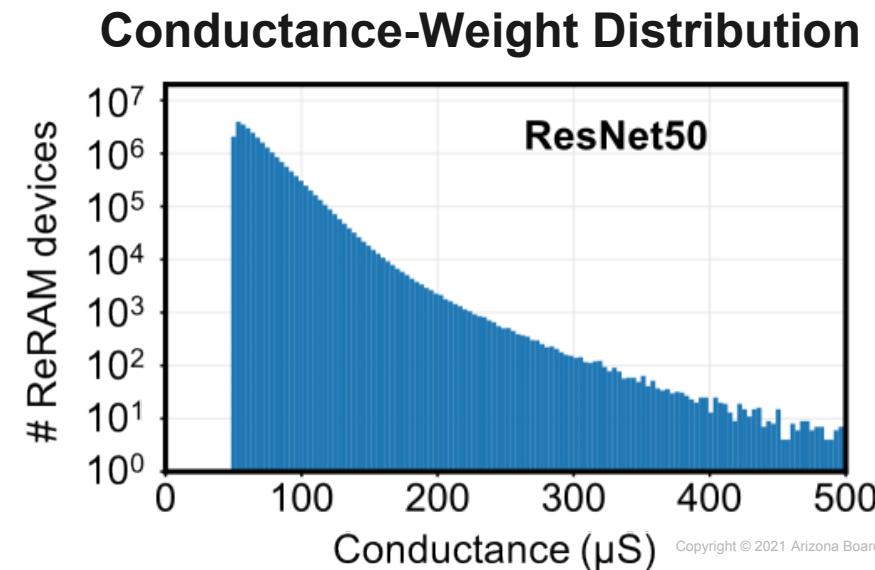
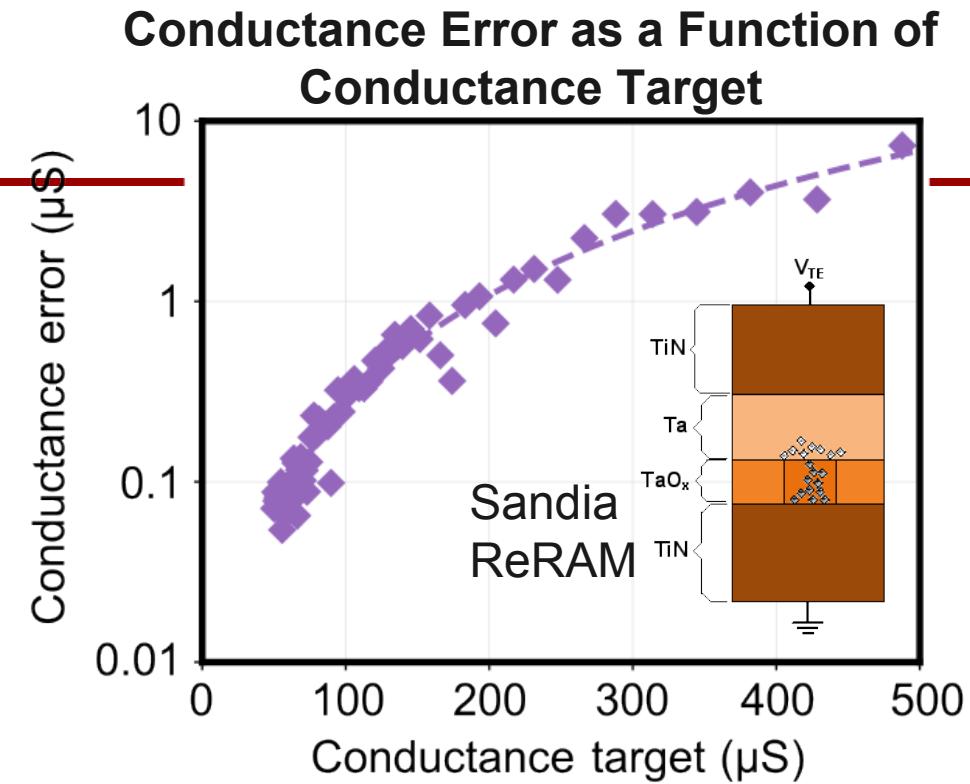


# Sandia TaOx ReRAM Inference Resistance Distributions



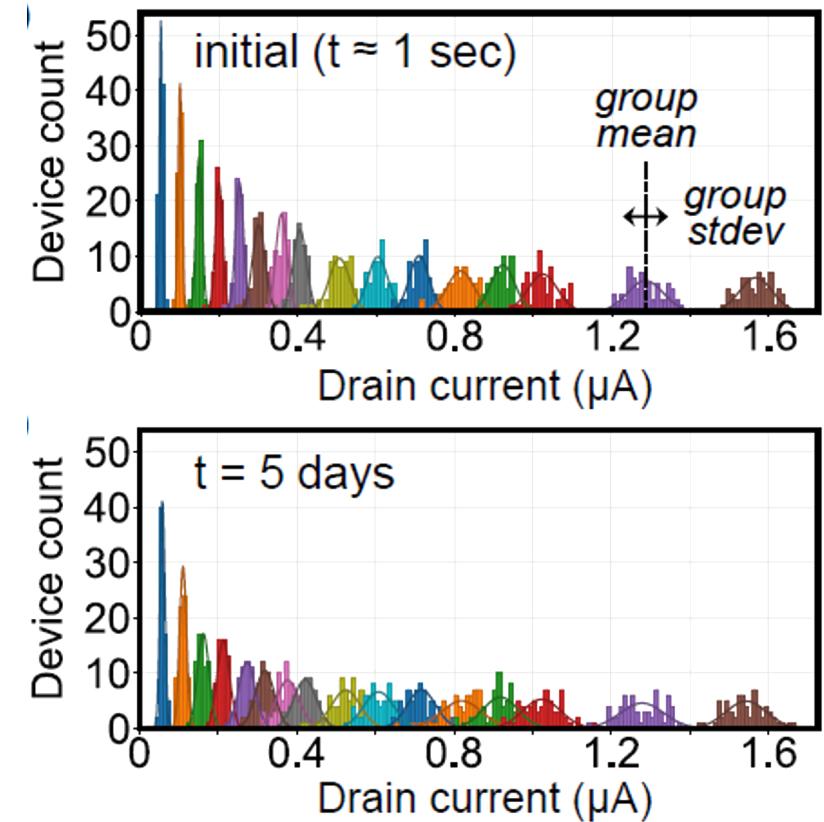
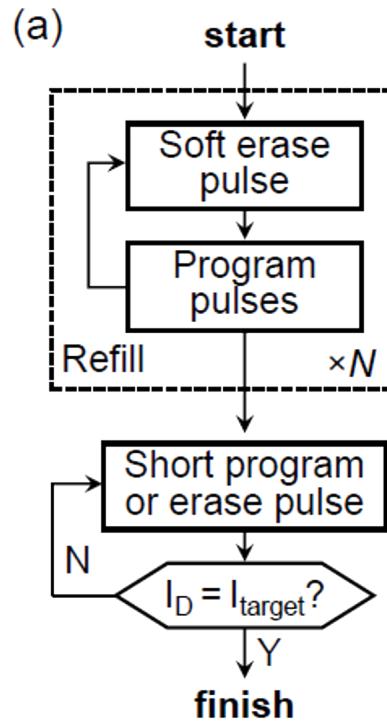
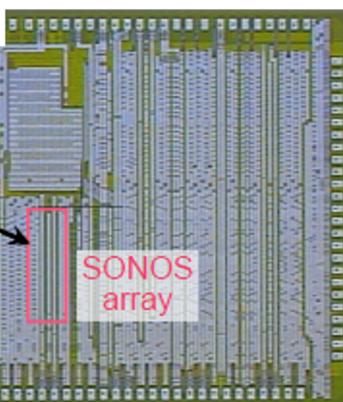
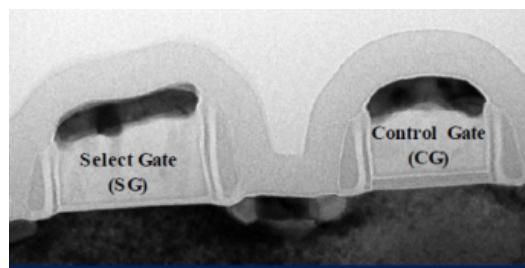
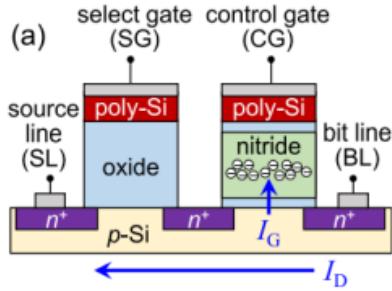
# TaOx ReRAM Error Model

- Conductance error approx parabolic with conductance target – this is ideal:
  - Lower conductances have lowest error and map to weights near zero.
  - Weights near zero hold most information, hence device error is minimized
- Modeled Accuracy in CrossSim Inference
  - ResNet50 CNN, ImageNet Dataset
  - 1000 image average
  - 8-bit ADC, 8-bit weight quant
  - Assume  $G_{ON}/G_{OFF} = 10$
- ReRAM accuracy on ImageNet:
  - Top-1 76.4%
  - Top-5 92.91%
- Compared to Digital (32 bit FP)
  - Top-1 77.18% (analog loss = 0.78%)
  - Top-5 93.06% (analog loss = 0.15%)
- Analog Inference predicted <1% loss!
  - Caveat: preliminary data – relaxation may degrade



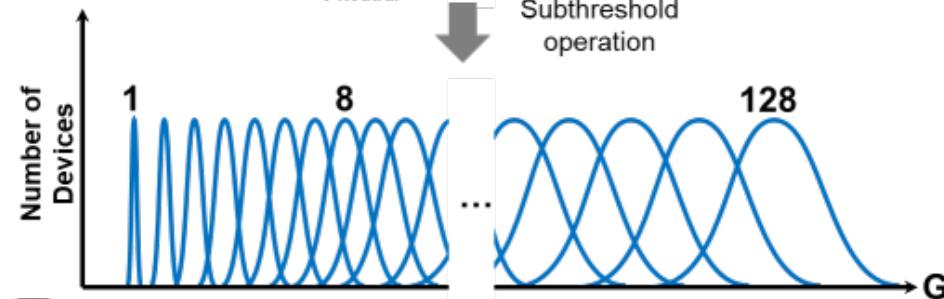
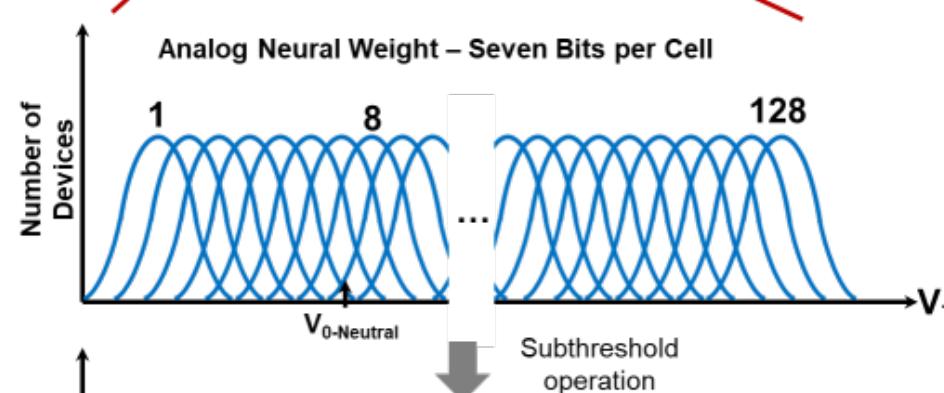
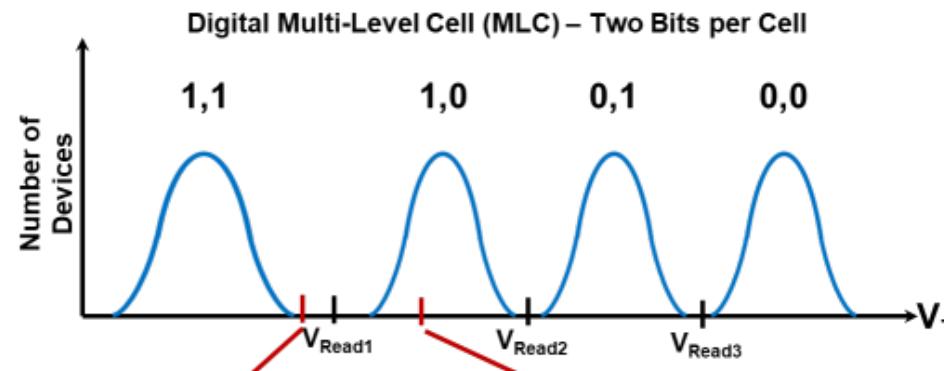
# 40nm SONOS Analog Inference Experimental Characterization

- Infineon 40nm SONOS Characterization Chip
- 1024x1024 test array
- Write verify routine programs all cells with analog values
- Experimental statistical assessment of analog programming error as a function of target drain current

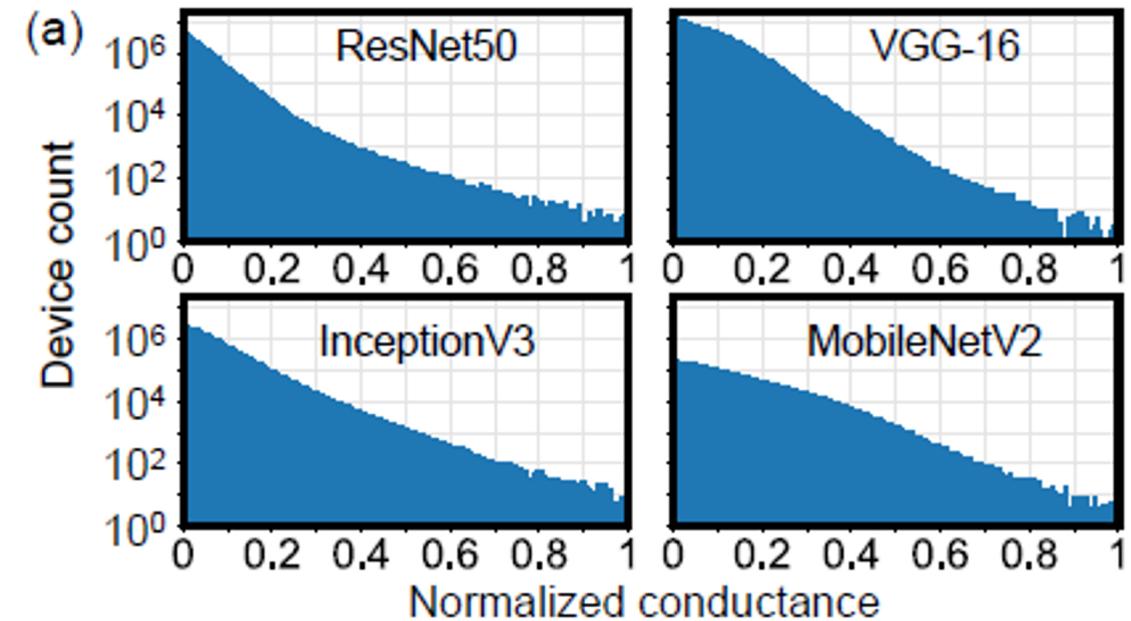
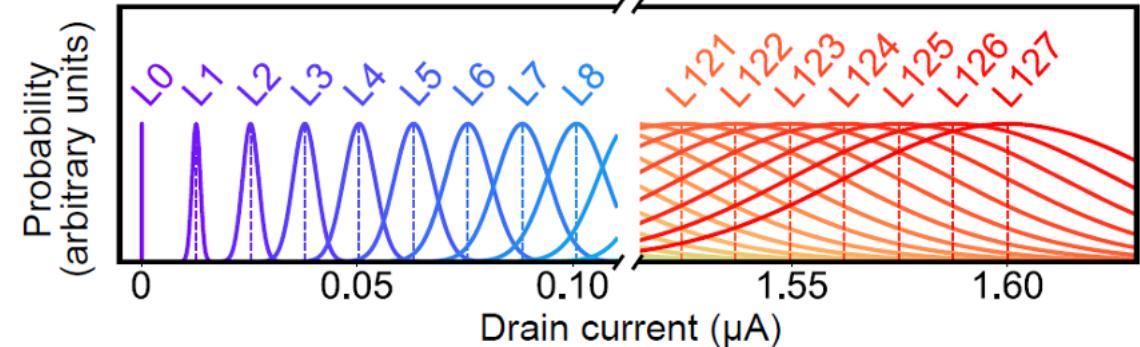


Agrawal et al, IEEE IMW 2020.  
T.P. Xiao et al, IEEE TCAS, 2022.

# SONOS Deep CNN Inference Modeling: State Overlap



## Modeled 7-bit Weight Distribution and Mapping

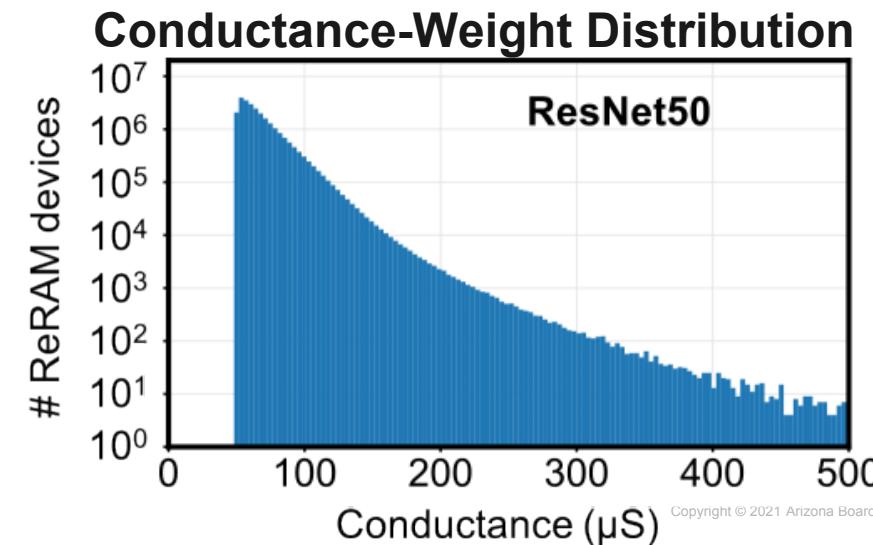
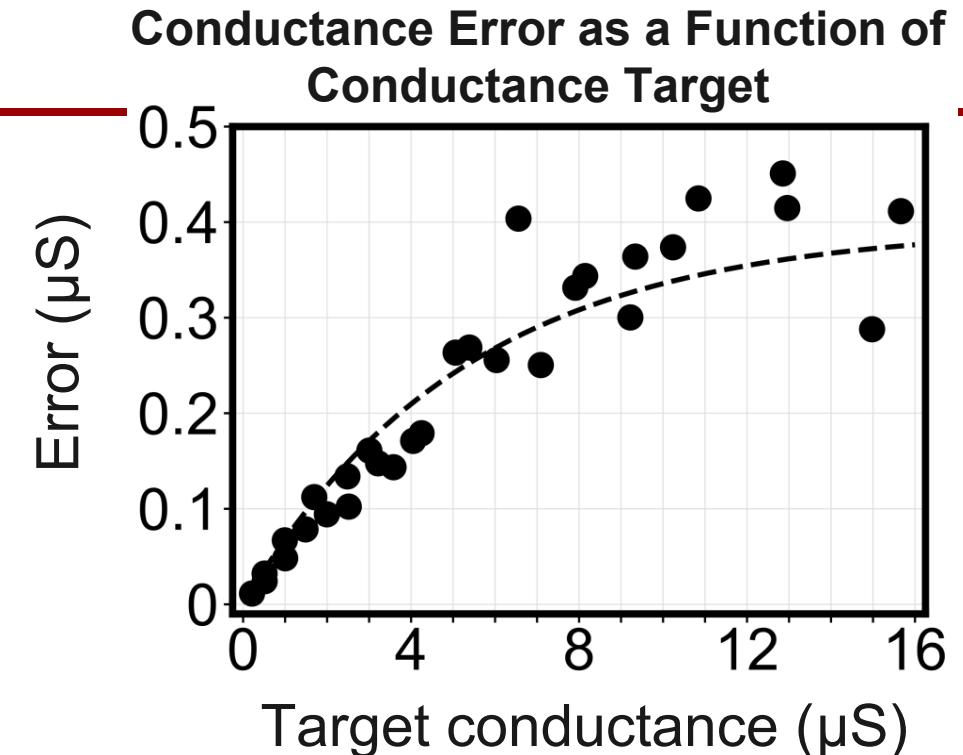


# SONOS Accuracy Model Results

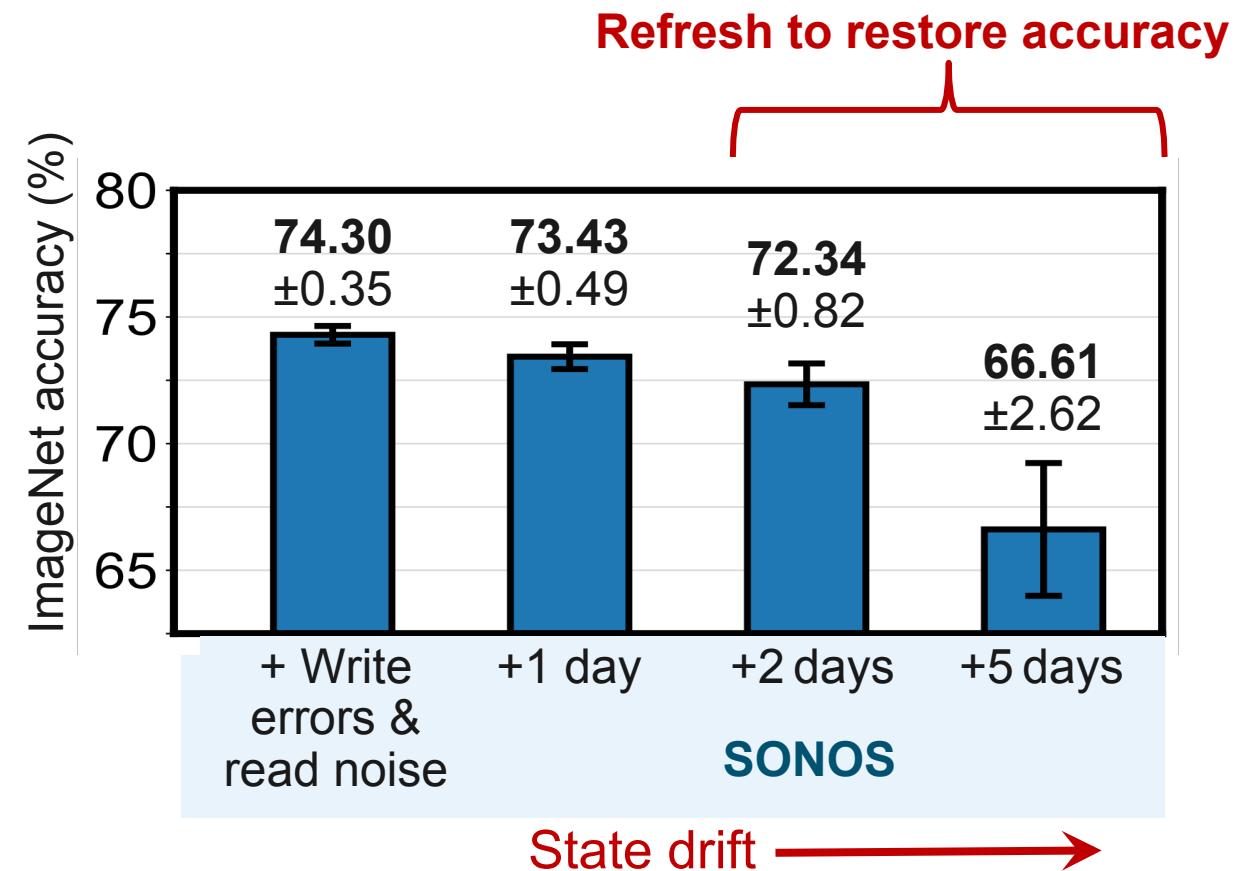
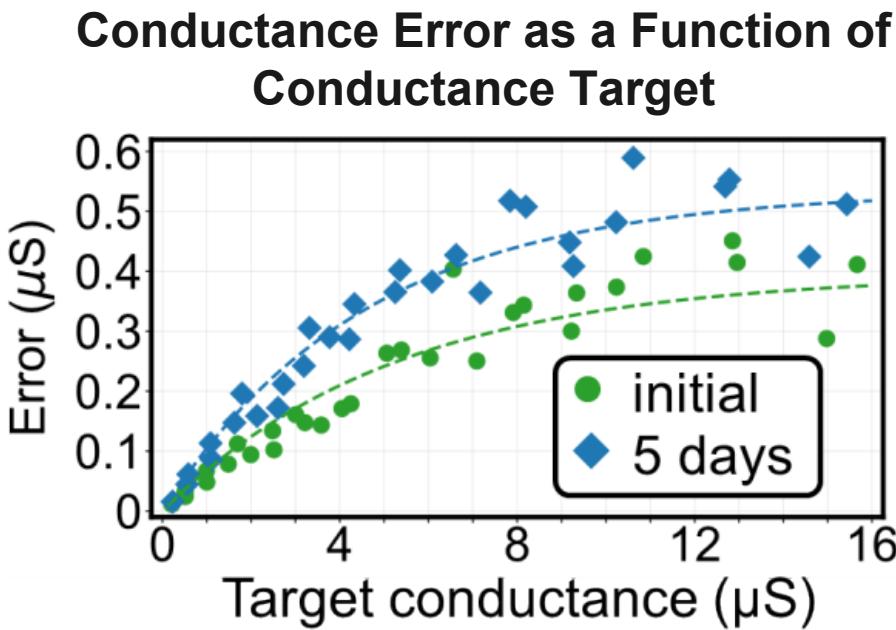
- Conductance error proportional to conductance target – this is ideal:
  - Lower conductances have lowest error and map to weights near zero.
  - Weights near zero are most common
  - Result: device-induced accuracy degradation minimized
- Modeled Accuracy in CrossSim Inference
  - ResNet50 CNN, ImageNet Dataset
  - 50,000 images
  - 8-bit ADC, 8-bit weight quantization

SONOS accuracy on ImageNet:

- Top-1 74.30%
- Top-5 91.97%
- Compare this to Ideal Digital (32 bit FP)
  - Top-1 76.46% (analog loss = 2.16%)
  - Top-5 93.00% (analog loss = 1.03%)
- **>10x Performance/Watt Improvement with only ~2% accuracy loss**
  - *Uses Commercial 40nm Technology*

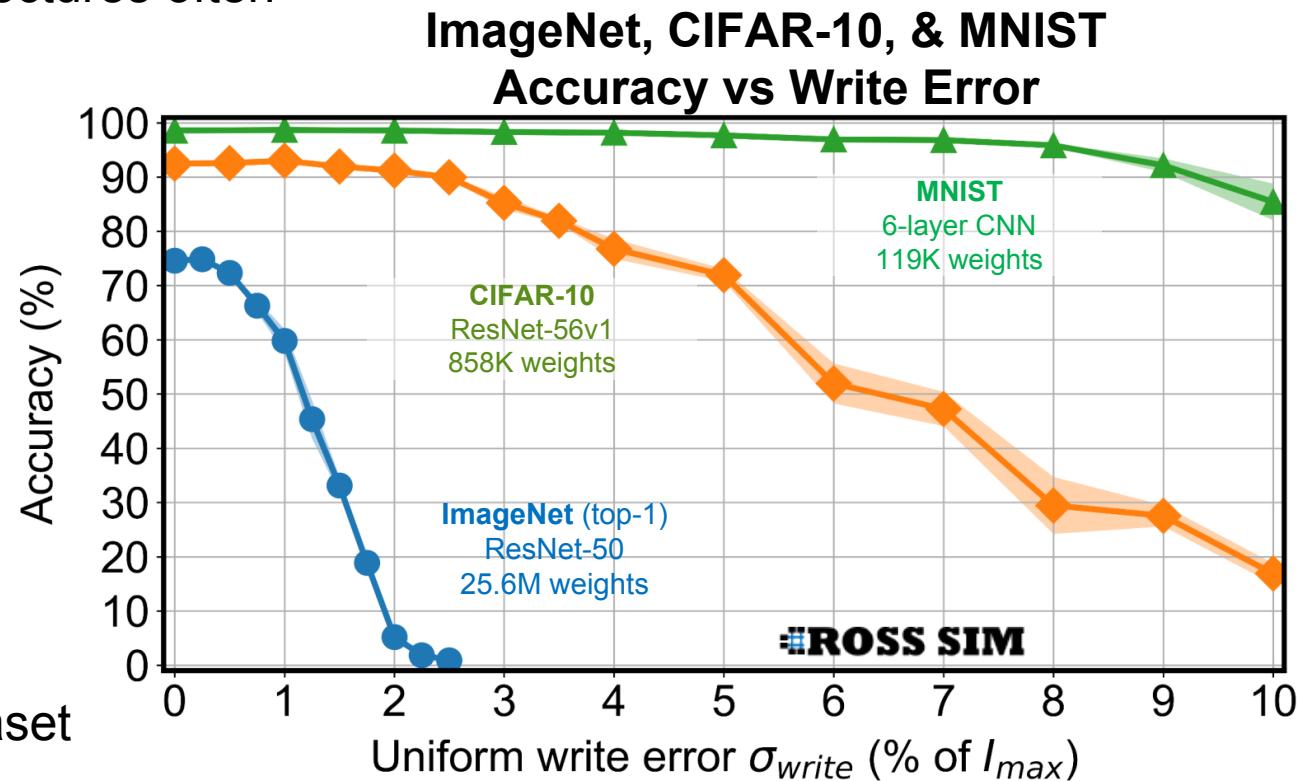


# Effect of SONOS State Drift on Inference Accuracy

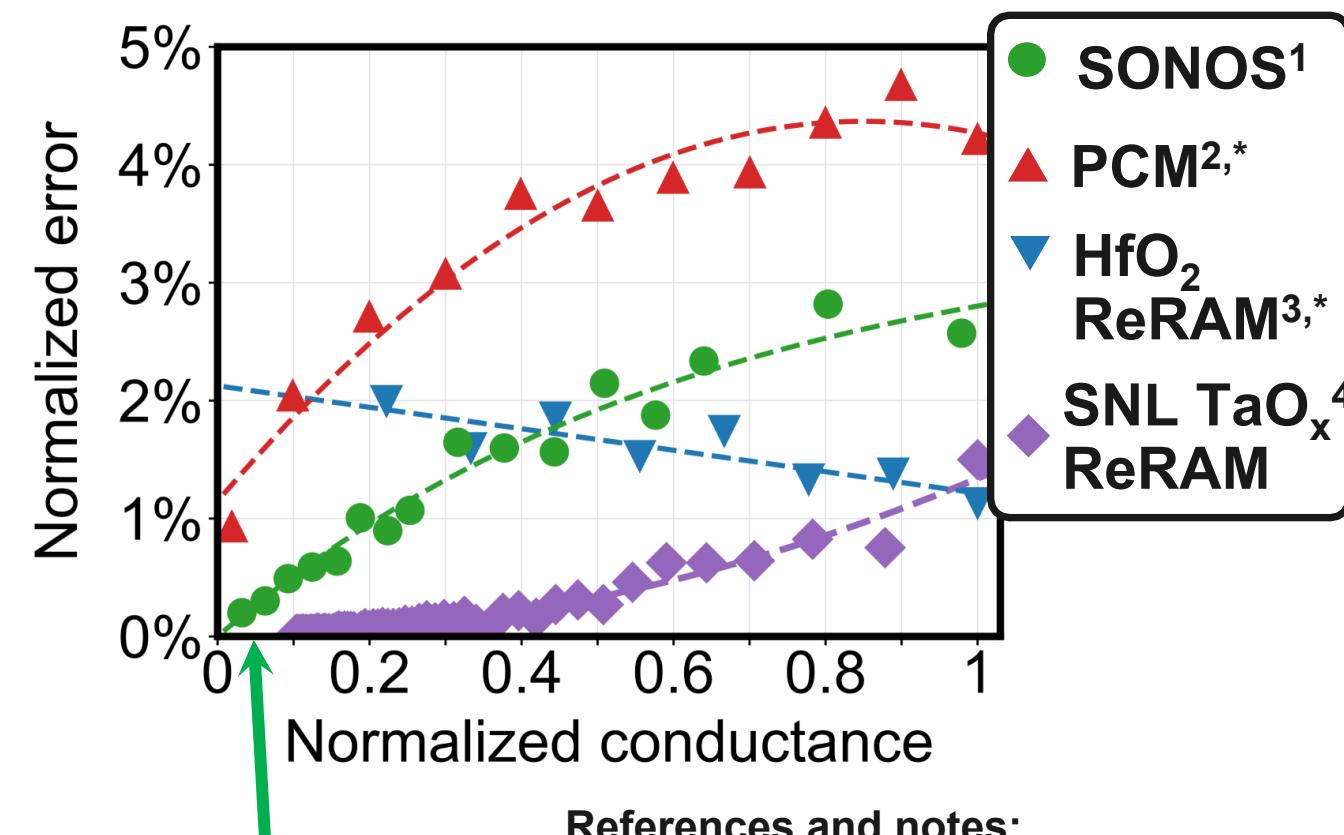


# Effect of Network and Dataset on Accuracy

- Different common datasets and CNN architectures often analyzed
- MNIST (simple CNN)
  - 28x28 pixel grayscale
  - 10 classes
  - 60k training images, 10k test images
  - ImageNet (requires large CNN arch.)
  - 224x224 pixel color
  - 1000 classes
  - 1.3M training images, 100k test images
  - ImageNet represents production-grade dataset
    - Sometimes smaller nets like MNIST are used due to computing constraints, esp for modeling training
- **Key Takeaway: Excellent accuracy on MNIST does not translate to excellent accuracy on ImageNet!**



# Error and Inference Accuracy Summary: SONOS, ReRAM, PCM



Low error @ low conductance:  
this is ideal

## References and notes:

<sup>1</sup>T.P. Xiao et al, IEEE TCAS, 2022.

<sup>2</sup>V. Joshi et al, Nat Comm. 11, 2020.

<sup>3</sup>Milo et al, IEEE IRPS, 2021.

<sup>4</sup>State drift/relaxation not yet measured, which may reduce accuracy.

<sup>\*</sup>All analog simulation also includes 8-bit weight quantization, 8-bit activations, and 8-bit ADCs

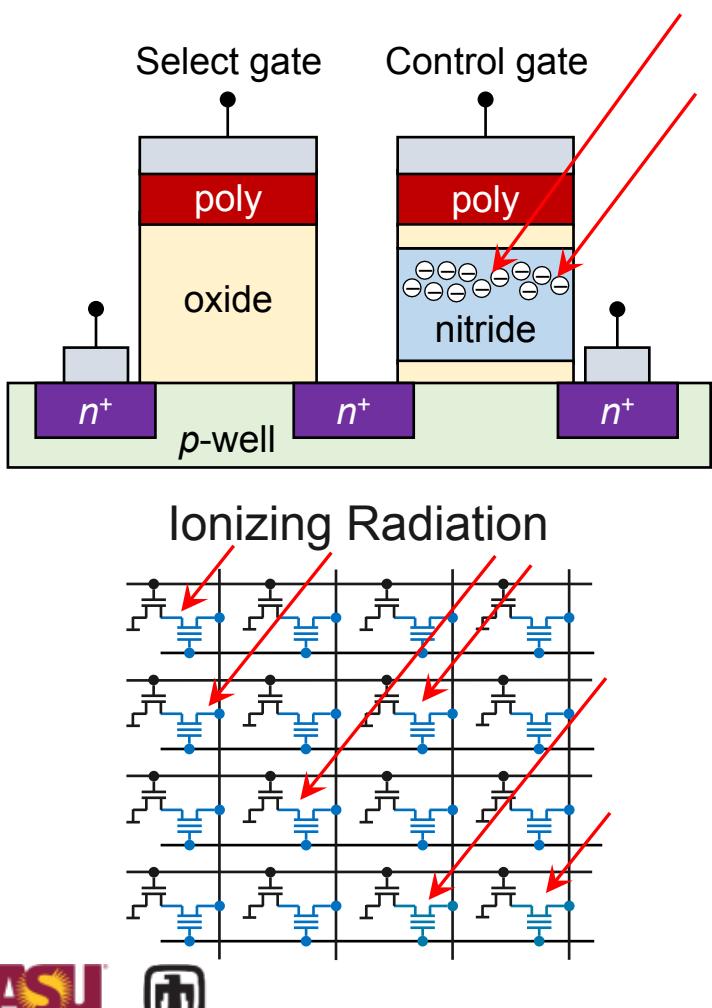
<sup>\*</sup>PCM and HfO<sub>2</sub> error are modeled entirely from data and programming used in publication only.

<sup>\*\*</sup>Based on 1000 ImageNet images

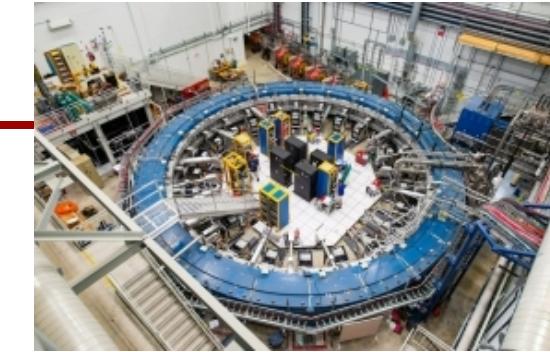
Technology <sup>+</sup>	Top-1 accuracy <sup>**</sup>	Top-5 accuracy <sup>**</sup>
Floating point digital (ideal)	77.5%	93.3%
SONOS <sup>1</sup>	74.0% $\pm$ 1.0%	92.5% $\pm$ 0.4%
SNL TaO <sub>x</sub> ReRAM <sup>4</sup>	76.4% $\pm$ 0.2%	93.3% $\pm$ 0.1%
PCM <sup>2</sup>	28.2% $\pm$ 6.4%	49.7% $\pm$ 7.8%

ROSS SIM

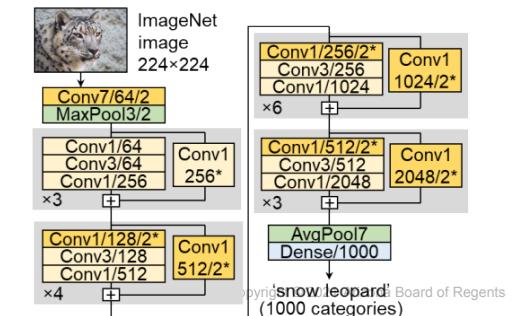
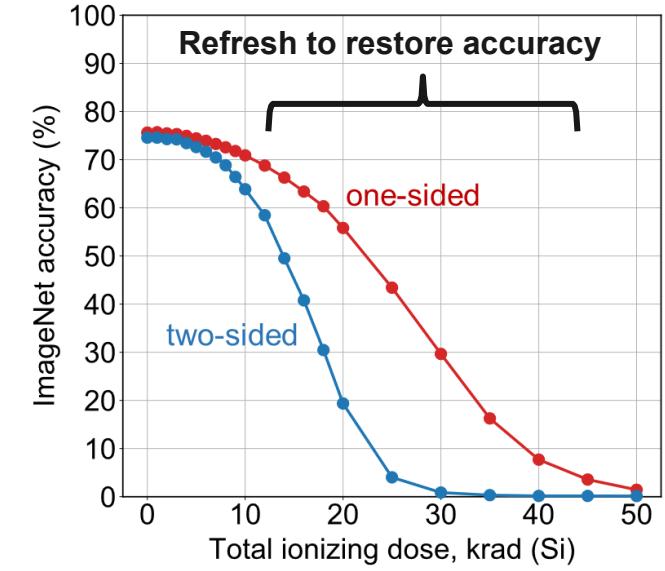
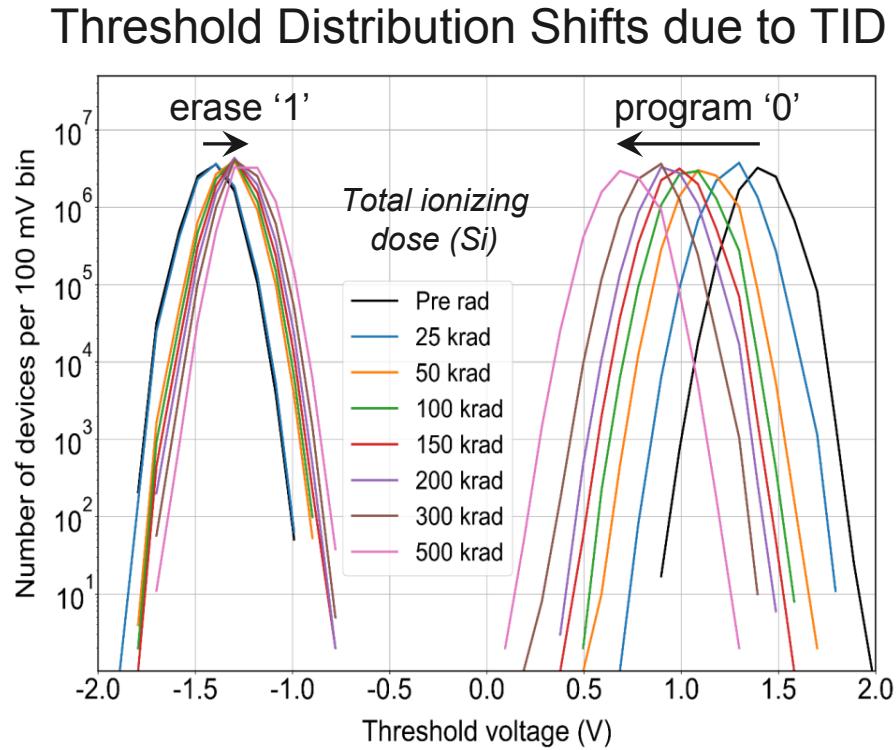
# Device-Level Radiation Impacts Algo Accuracy



How will the accuracy  
degrade in radiation  
environments ?



Algorithm Accuracy Degradation due to TID



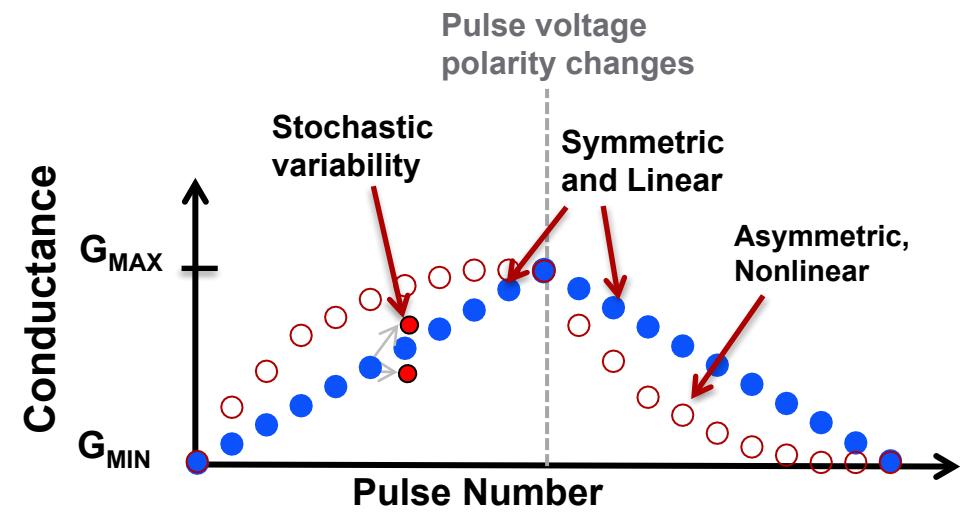
# Outline

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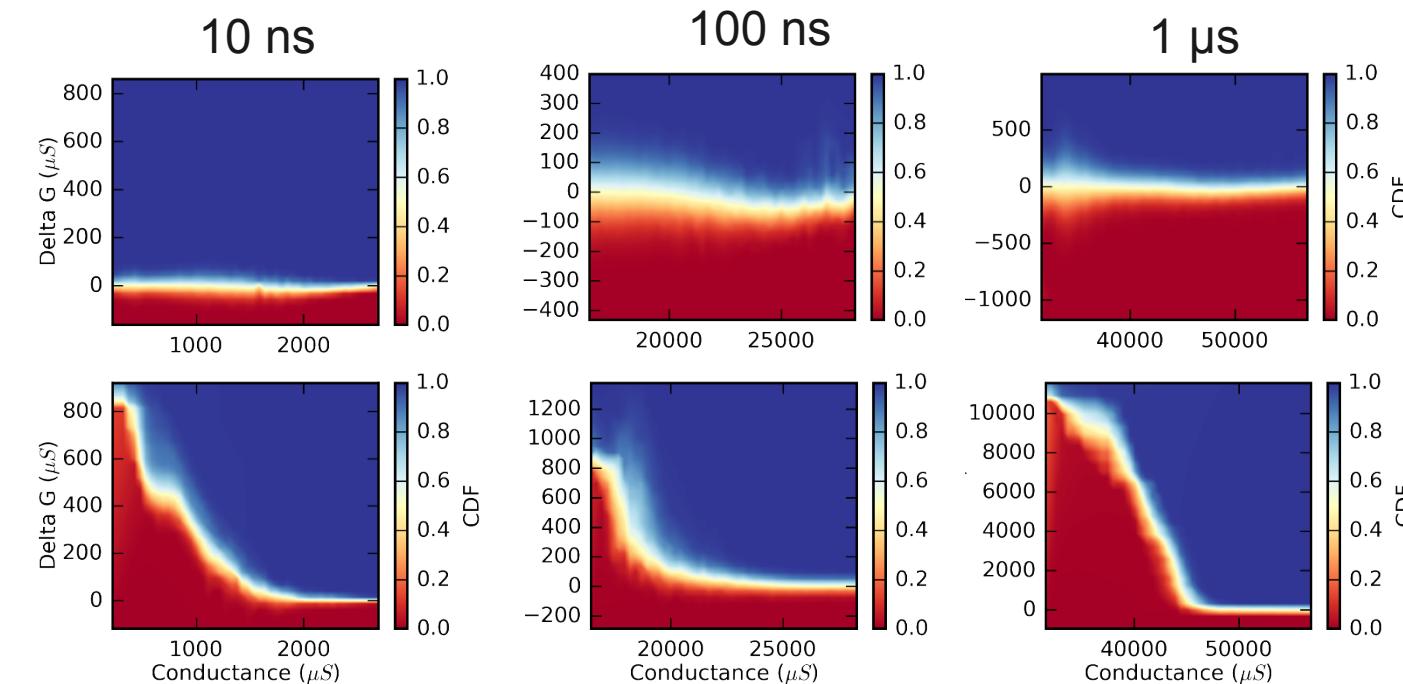
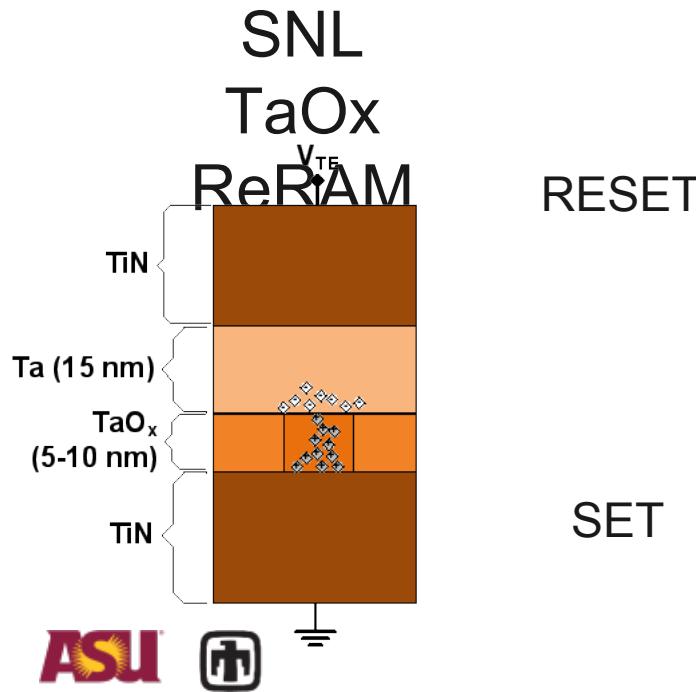
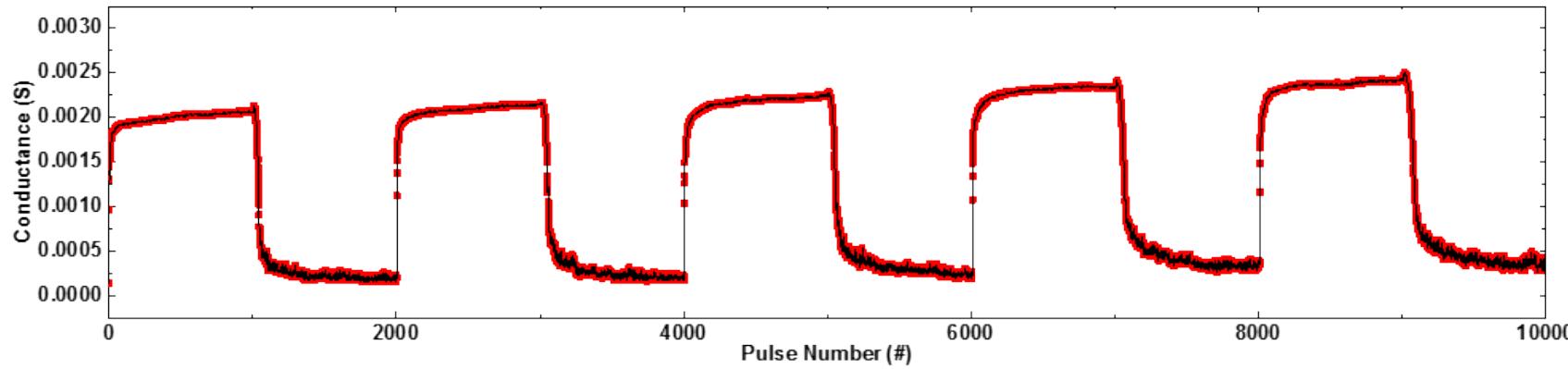
- Motivation and Digital Limits
- Analog In-Memory Compute Energy & Latency
- Accurate Analog Inference
- Accurate Analog Training
- Conclusions

# Device Challenges for Training

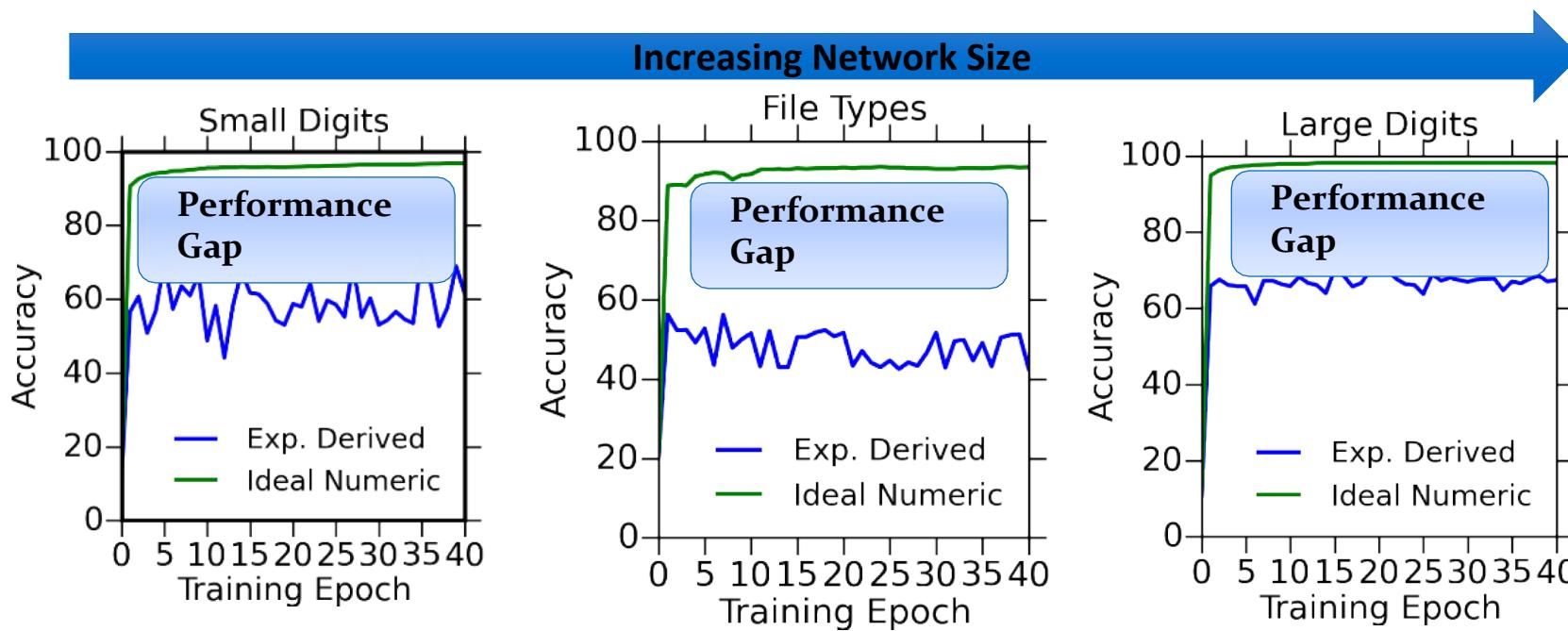
- Training has an overlapping set of challenges
- Ideally weight increases and decreases linearly proportional to learning rule result
- Issue for open loop nonvolatile memory: altered the relationship between intended and actual update
- Nonlinear and asymmetric state change
- Cycle to cycle random variability (write stochasticity)
- Device to device random variability
- Also: very high endurance ( $>10^{12}$ )



# Characterization for Training



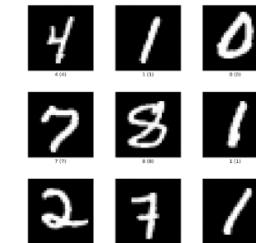
# Initial TaOx ReRAM Training Accuracy Modeling (MNIST)



#ROSS SIM

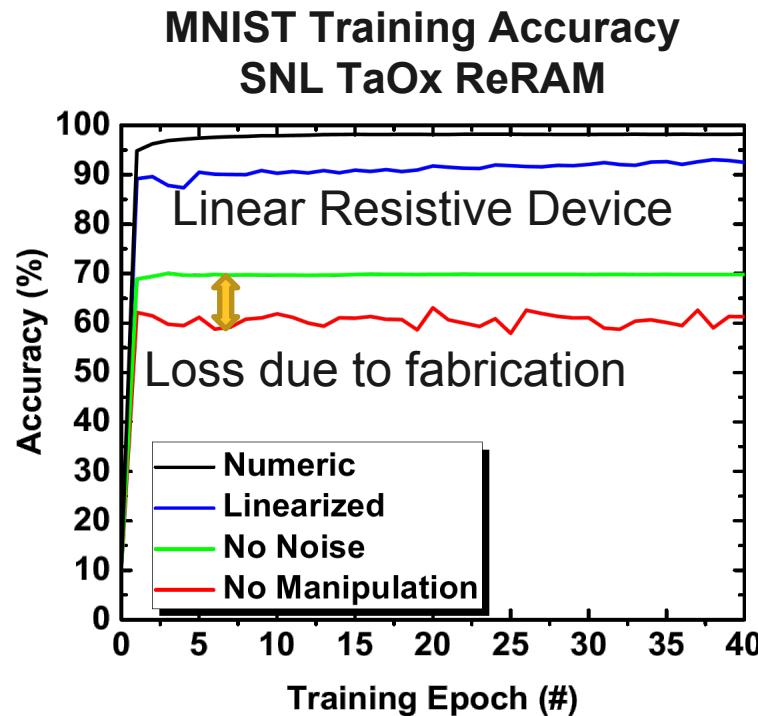


- TaOx ReRAM has challenges for open loop training...
- Why?



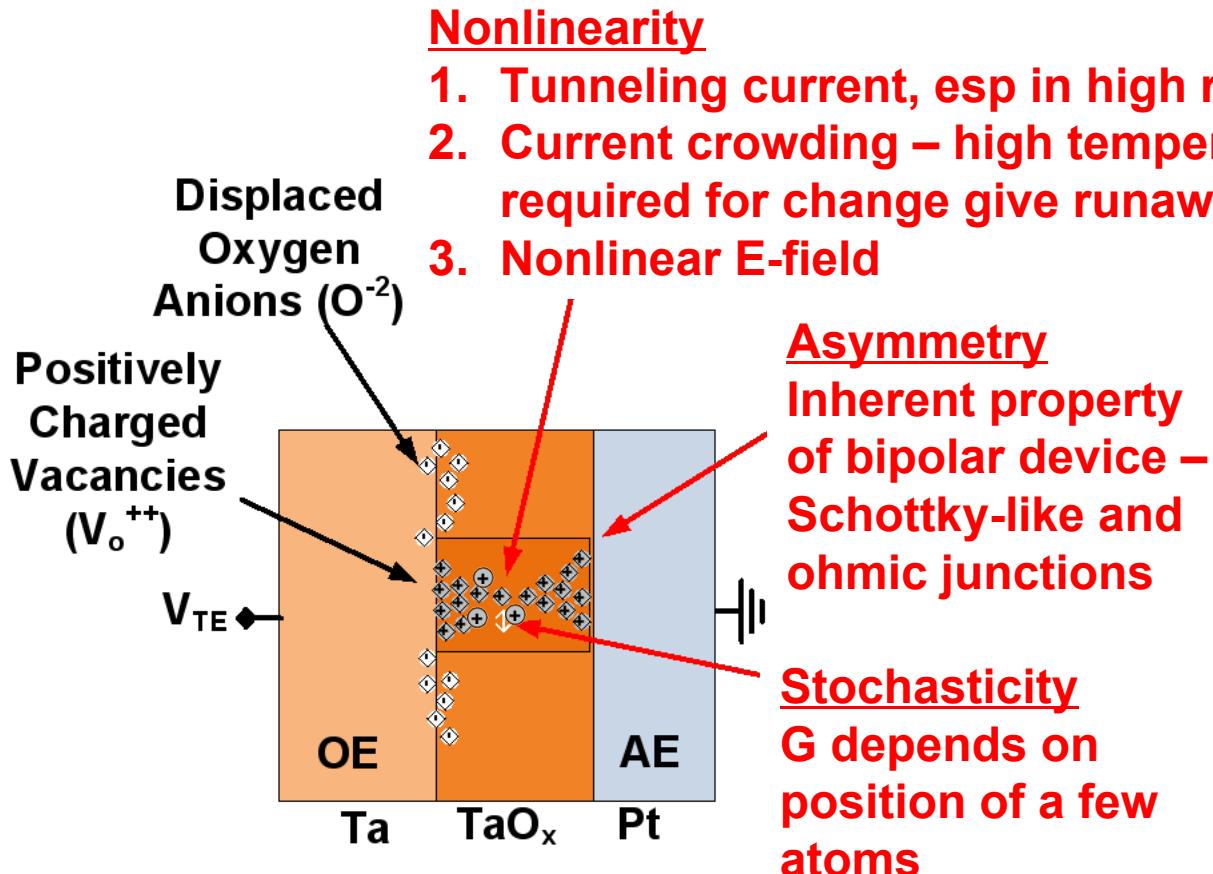
# Physical Insight from Multiscale Model - CrossSim

## Challenges using Filamentary ReRAM for Training



R. Jacobs-Gedrim et al, Proc. 2017 IEEE ICRC, 2017.

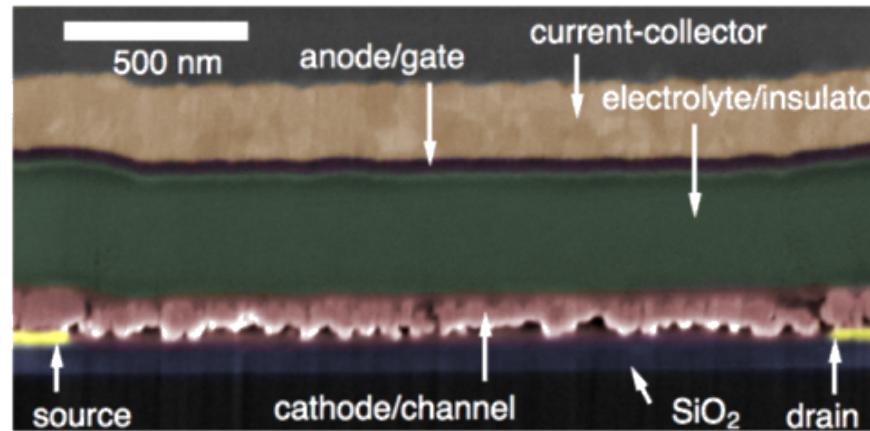
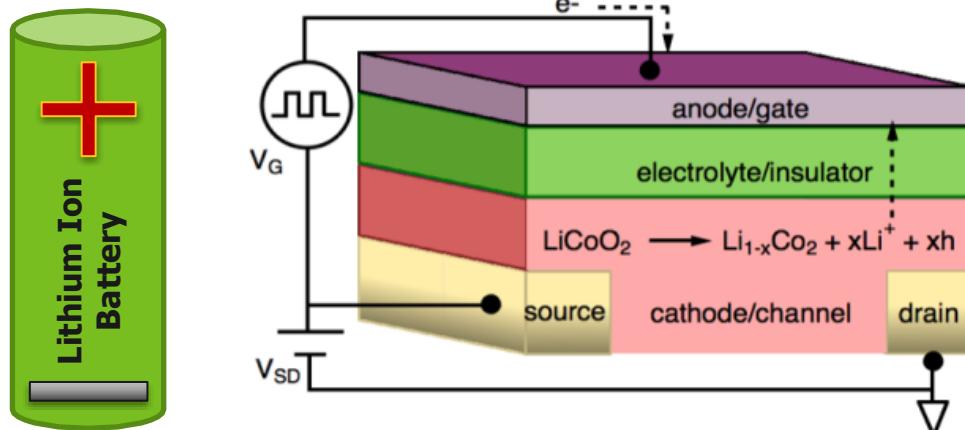
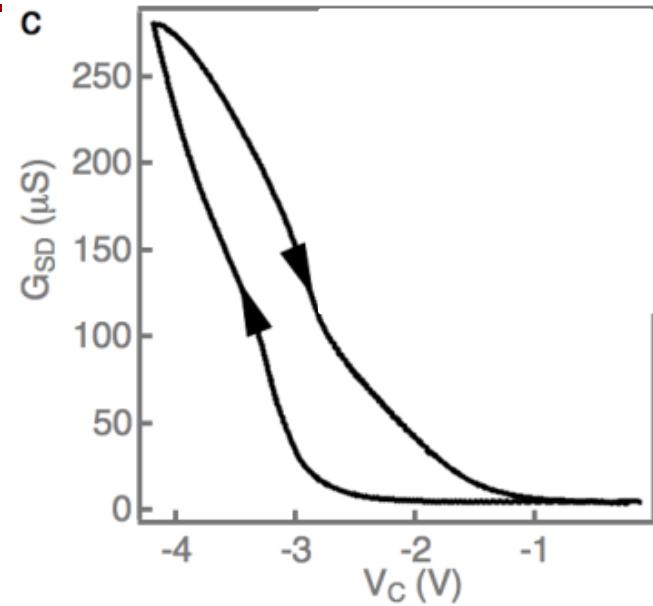
**CROSS SIM**



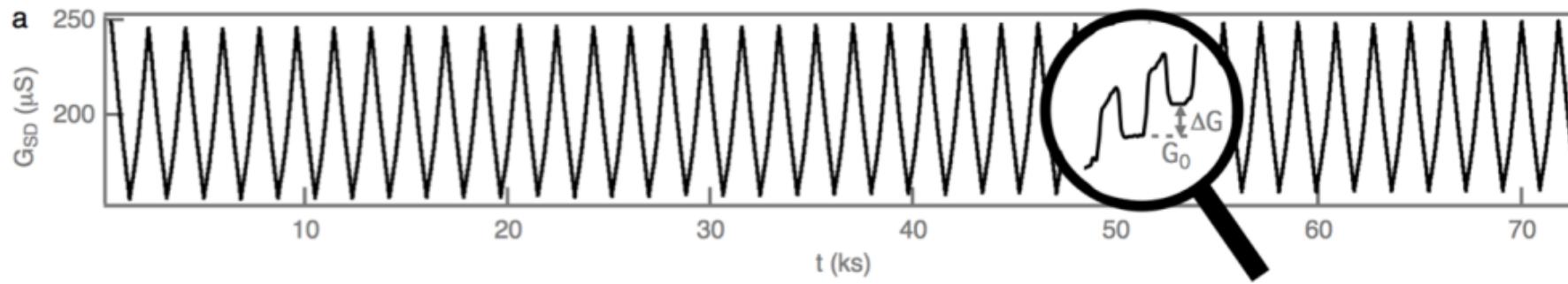
# Electrochemical RAM (ECRAM) Synapse

- Lithium acts as dopant in LCO cathode
- Resistivity across cathode changes linearly with Li insertion (battery charge/discharge)
- Functions as an analog nonvolatile transistor!
- Much smoother state change than filament devices

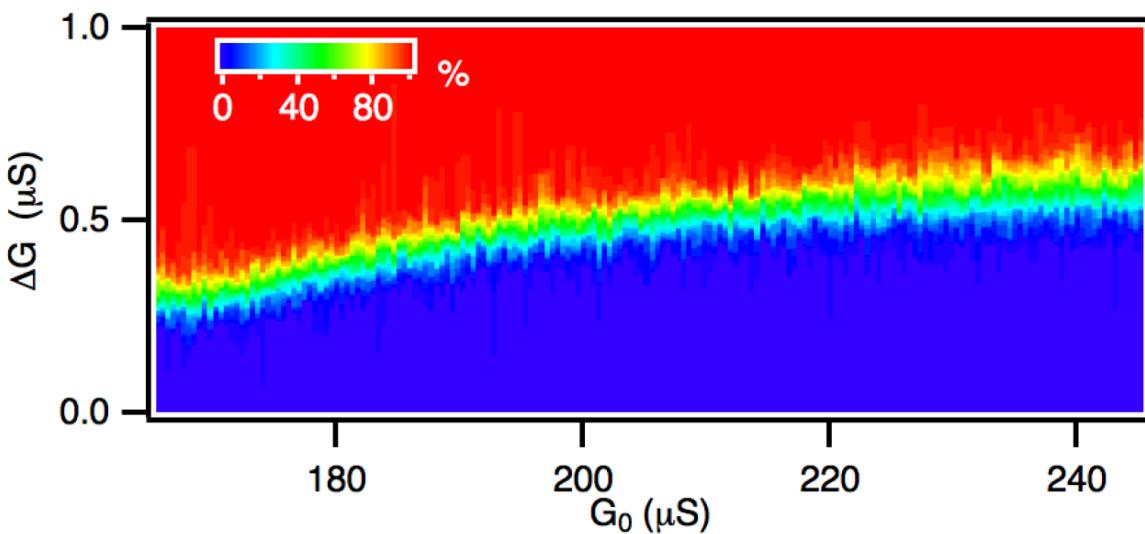
Conductance vs Voltage



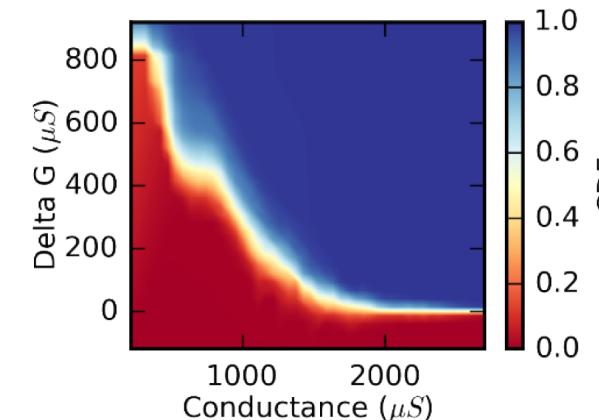
# ECRAM Characterization



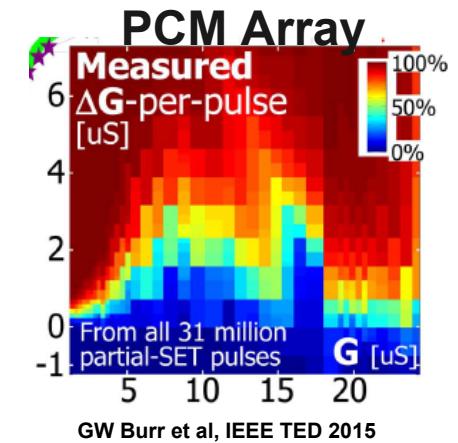
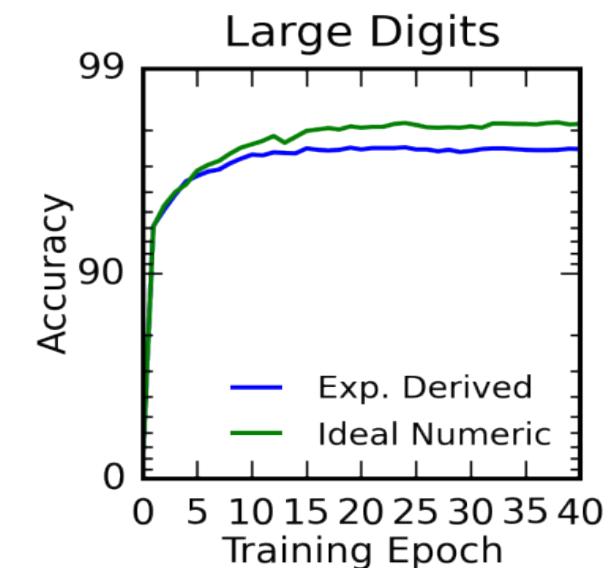
ECRAM



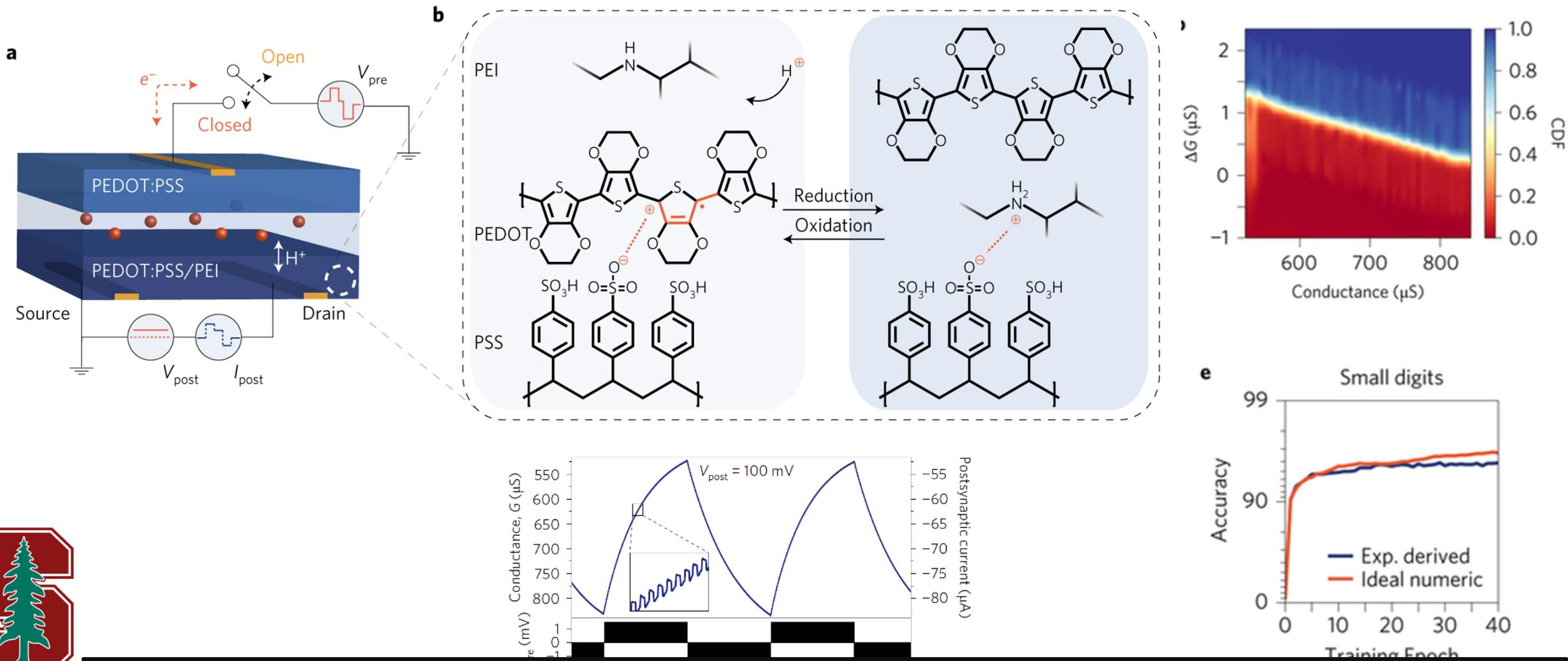
TaOx ReRAM



ECRAM-MNIST

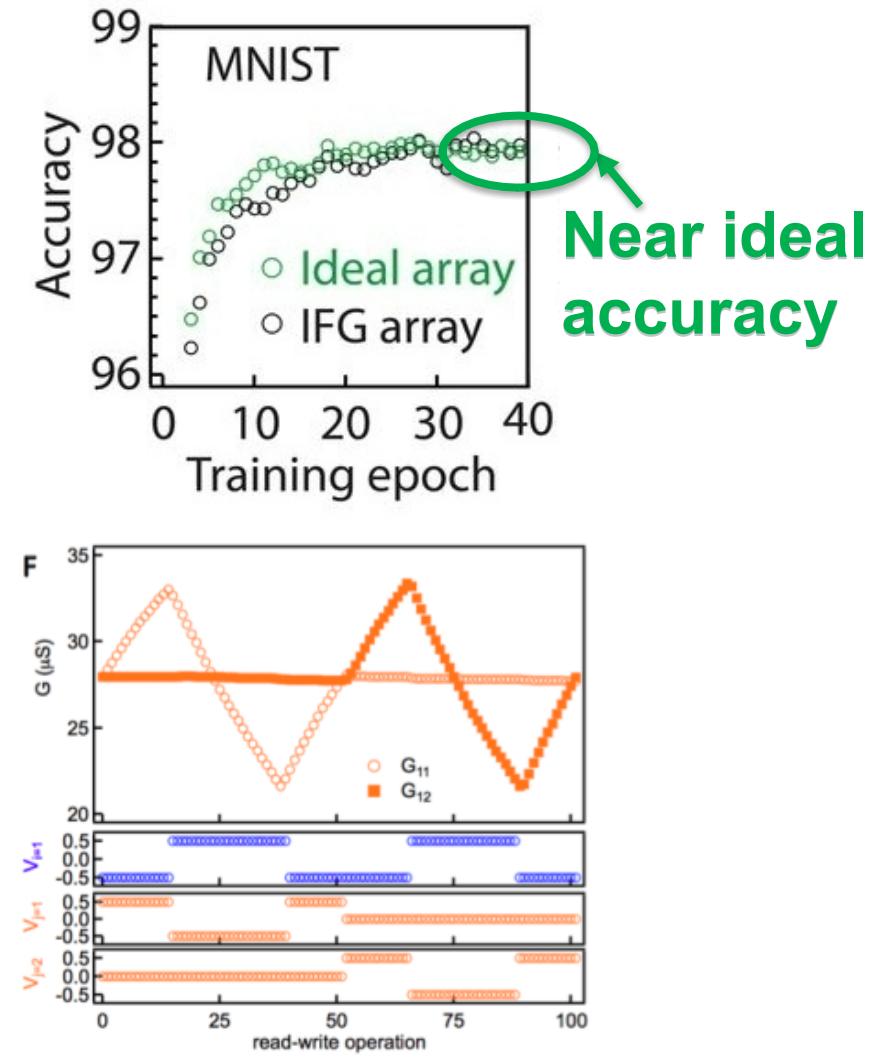
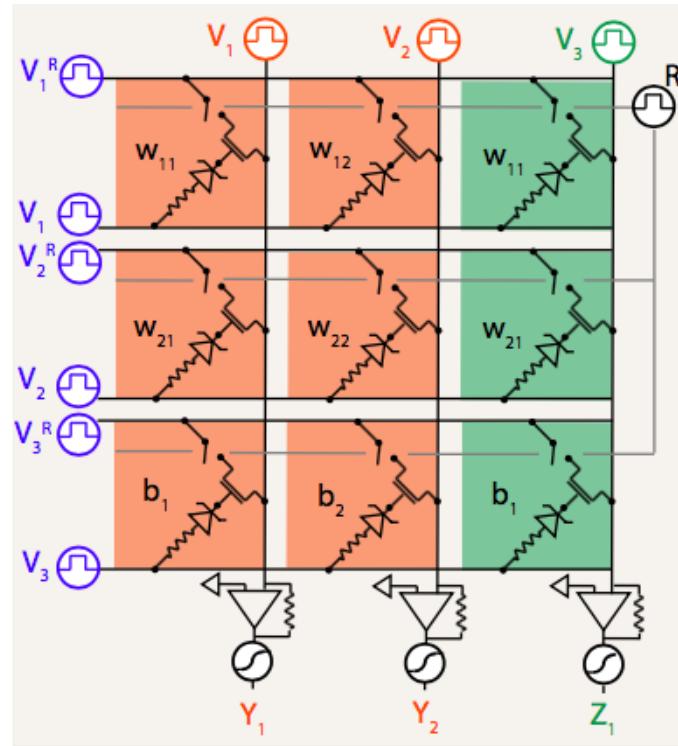
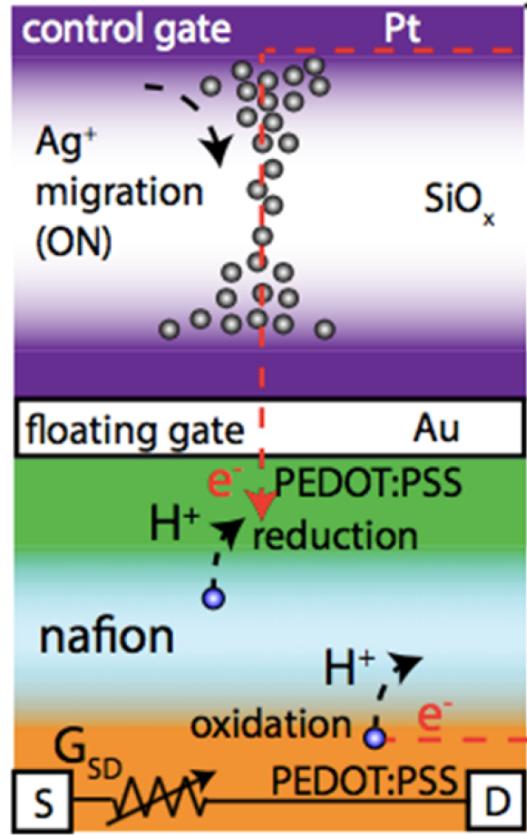


# Electrochemical Neuromorphic Organic Device (eNode)



Proton-based polymer ECRAM synapse: fast, better endurance

# ECRAMs Array Parallel Update Training Demonstration



# Outline

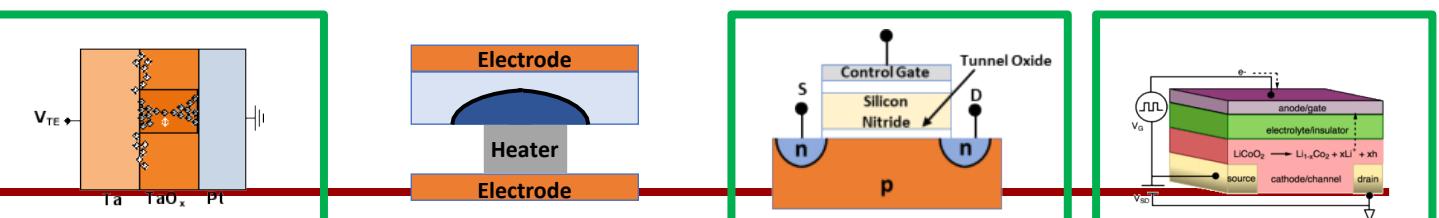
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- Motivation and Digital Limits
- Analog In-Memory Compute Energy & Latency
- Accurate Analog Inference
- Accurate Analog Training
- Conclusions

# Analog Device Requirements

Property	Inference	Training
Analog programing error (w/ write verify)	Critical	Less Important
Long term retention	Important	Less Important
Read noise	Important	Less Important
Conductance Range	Important	Important
Short term state drift	Important	Important
Device to device variability	Important	Important
Write stochasticity	Less Important	Important
Write speed	Less Important	Important
Write linearity	Less Important	Important
Write symmetry	Less Important	Critical
Endurance	Less Important	Critical

# Perspective: IMC Devices



Property	ReRAM	PCRAM	SONOS/FG	ECRAM
Analog programing error (w/ write verify)	😊	😐	😊	😊
Long term retention	😊	😊	😊	😐
Read noise	😊	😊	😊	😊
Conductance range	😐	😐	😊	😊
Short term state drift	😐	😐	😐	😐
Device to device variability	😐	😐	😊	😊
Write stochasticity	😢	😢	😊	😊
Write speed	😊	😊	😐	😐
Write linearity	😢	😢	😐	😊
Write symmetry	😢	😢	😊	😊
Endurance	😐	😐	😐	😐

# Final Thoughts

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- Traditional digital CMOS computing is hitting disruptive roadblocks for continuing energy efficiency (or equivalently, performance per watt)
- Analog In Memory Computing offers path to  $>10$  TOPS/W
  - Ideal for deep neural nets and deep convolutional nets
  - Analog In Memory Computing has significant new challenges
    - *Algorithm* accuracy depends on the *device*
    - This creates significant, new device electrical characterization requirements
    - Inference and training have distinct challenges, with some overlap.
    - Inference: high accuracy predicted with commercial SONOS and ReRAM
      - Inference challenge: write-verify with short term state drift
    - Training: is more challenging, but devices such as ECRAM and related nonfilamentary devices provide a path forward

# Acknowledgements

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- This work was funded by:
- DOE Office of Science Microelectronics Codesign Research Program, Supported ASCR, BES, HEP, and FES, Under the Abisko Project (Oak Ridge National Laboratories, Sandia National Labs), PM Robinson Pino, (ASCR).
- Sandia National Laboratories Laboratory Directed Research and Development (LDRD)
- Defense Threat Reduction Agency (PM, Jacob Calkins)



Office of  
Science



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## Sandia Contributors

Patrick Xiao  
Chris Bennett  
Will Wahby  
Sapan Agarwal  
Alec Talin  
Robin Jacobs-Gedrim  
David Hughart  
Elliot Fuller  
Ben Feinberg

  
**Hewlett Packard  
Enterprise**



## External Collaborators

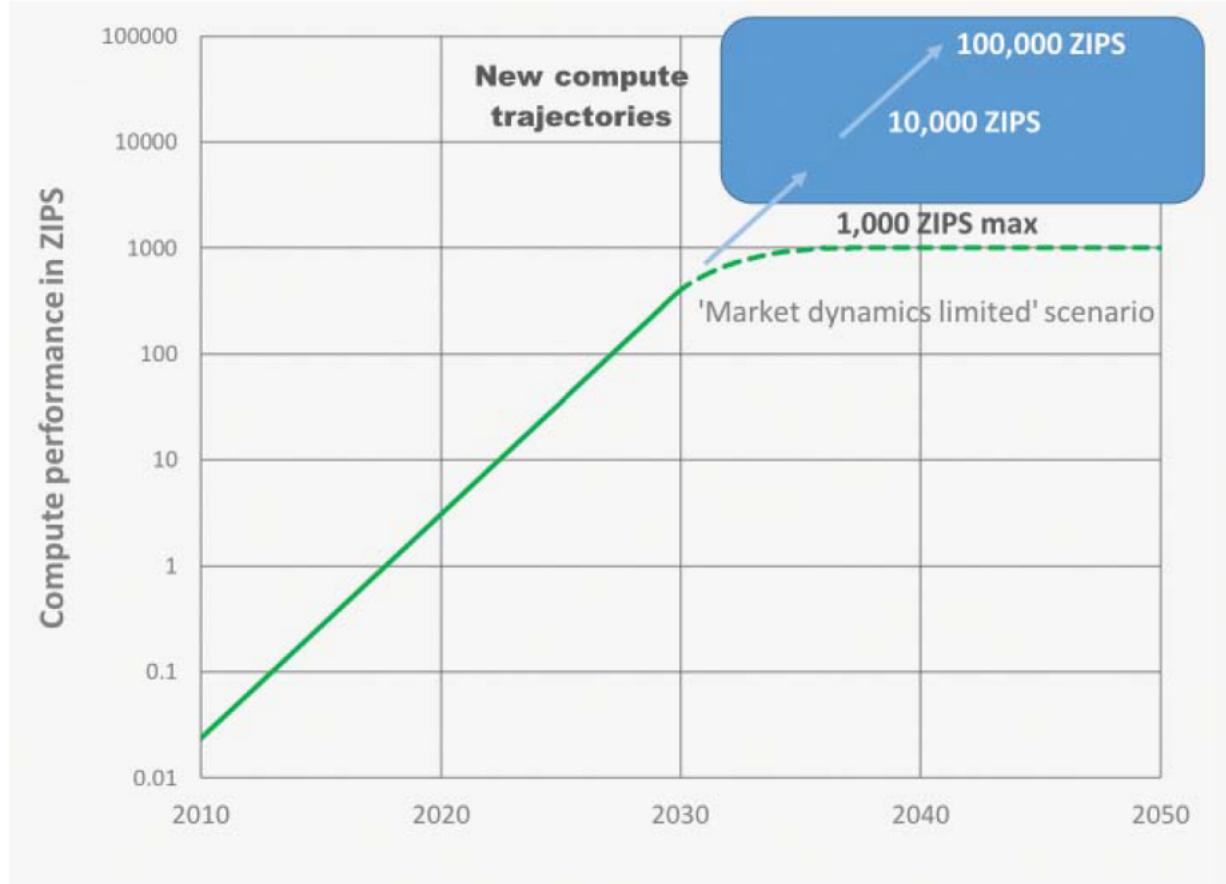
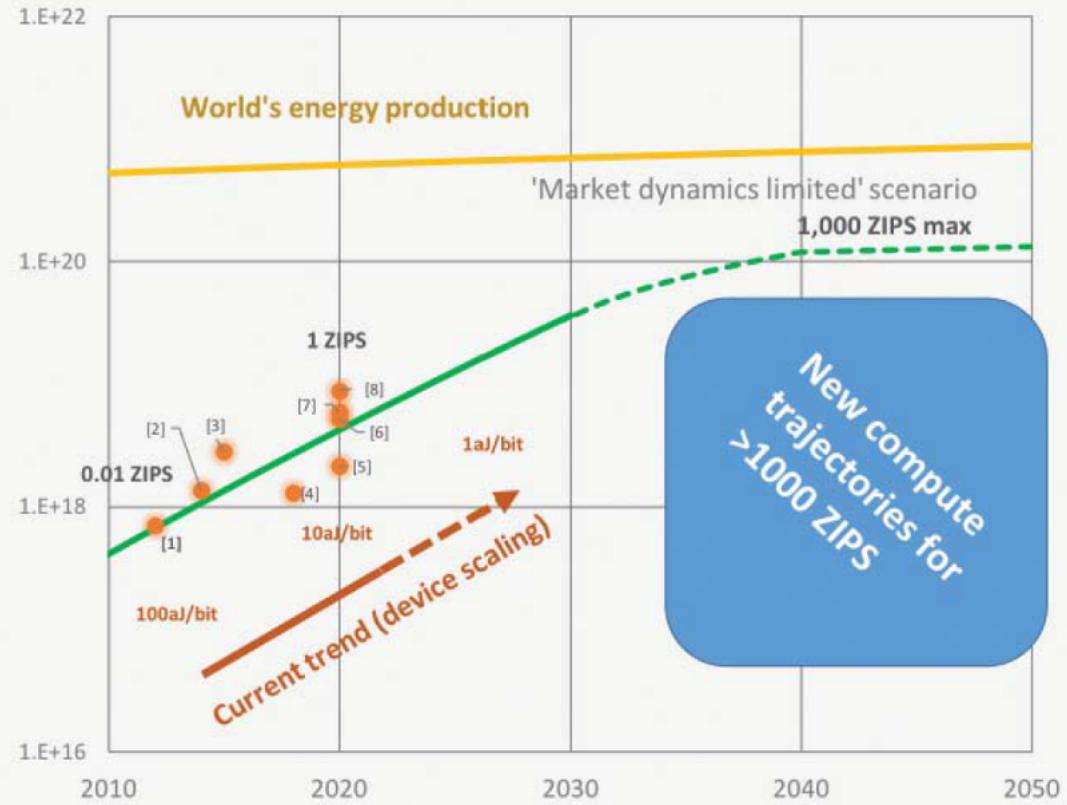
Helmut Puchner, Infineon  
Vineet Agarwal, Infineon  
Jean Anne Incovia, UT  
Stan Williams, TAMU  
Hugh Barnaby, ASU  
Jesse Mee, AFRL  
Yiyang Li, U Michigan  
John Paul Strachan, HPE  
Victor Zhirnov, SRC



# Thank You – Questions?

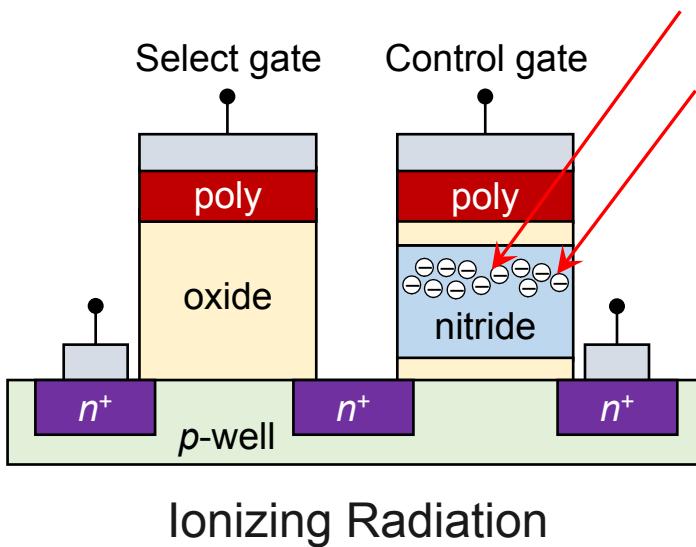
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# Microelectronics Grand Challenge

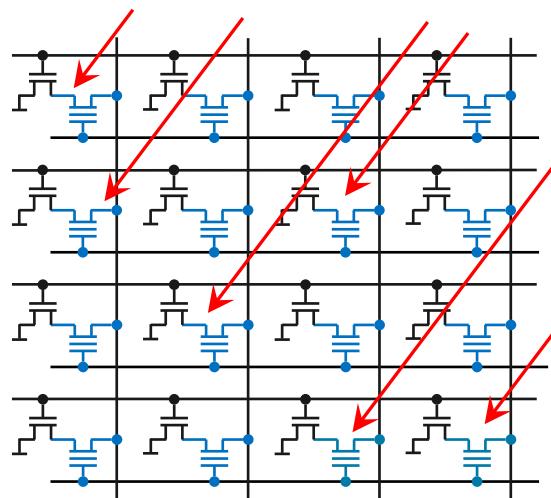


SRC Decadal Plan for Semiconductors, 2020

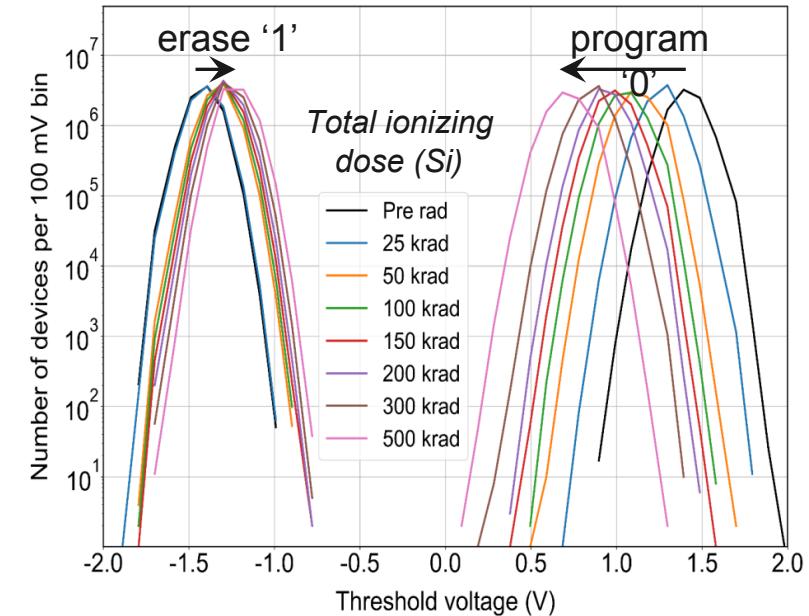
# Impact of Ionizing Radiation on Deep Net Accuracy



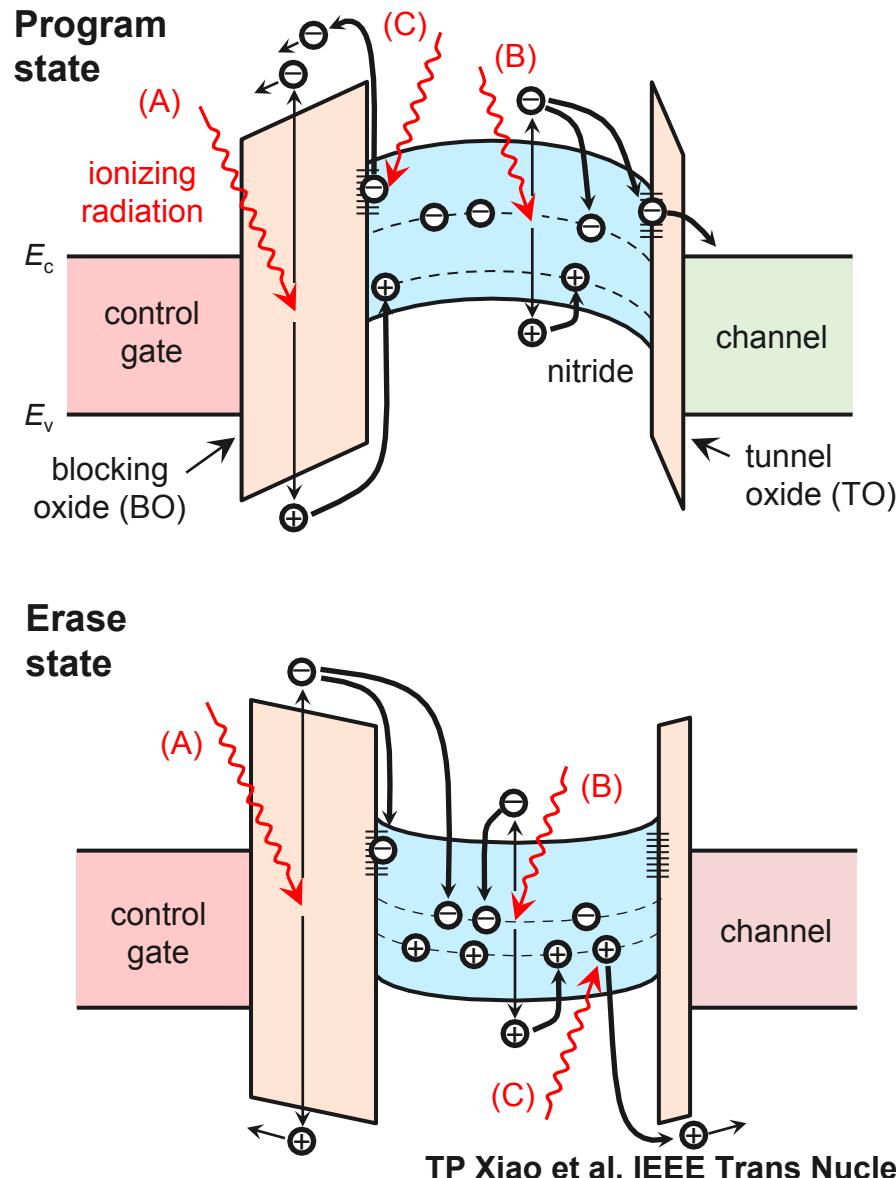
Uniform Gamma Irradiation



Threshold Distribution Shifts Across Array

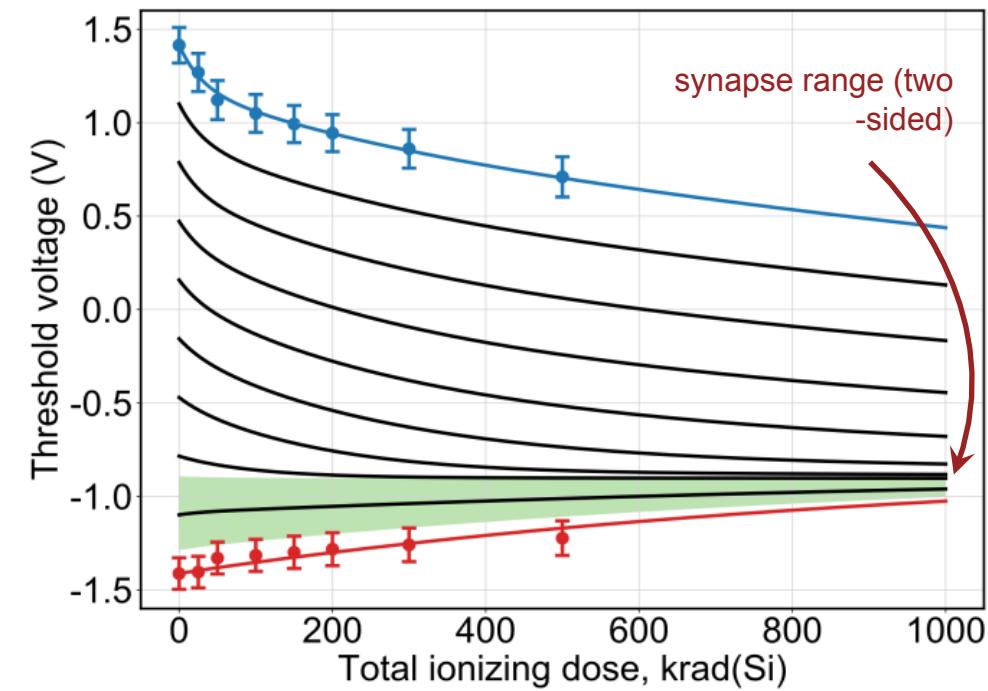


# Analog Neuromorphic SONOS In Space: Physics to Algorithm



TP Xiao et al, IEEE Trans Nuclear Sci, 2021 (in press).

$V_T$  versus Total Ionizing Dose: Model and Experiment

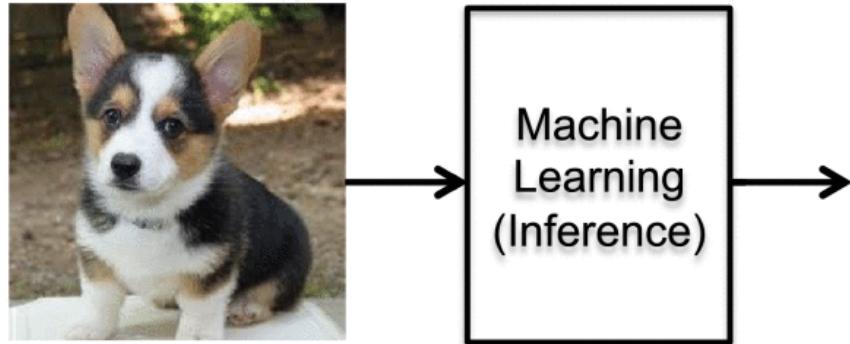


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# Neural Network Basics

## Inference

- Feed forward operation of the network to perform task, i.e. classification
- Ex: Image recognition
- Computationally requires single feed forward pass through network
- 

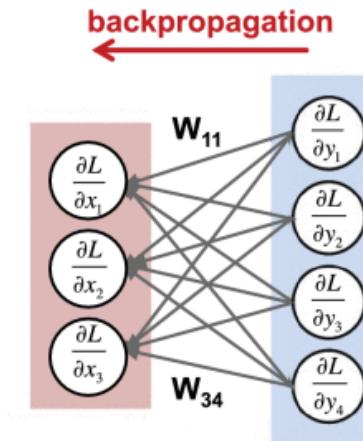


## Class Probabilities

Dog (0.7)  
Cat (0.1)  
Bike (0.02)  
Car (0.02)  
Plane (0.02)  
House (0.04)

## Training

- Adjusting the weights to reduce error and improve
- Typically done with backprop
- **Parallel update possible on crossbar architecture**



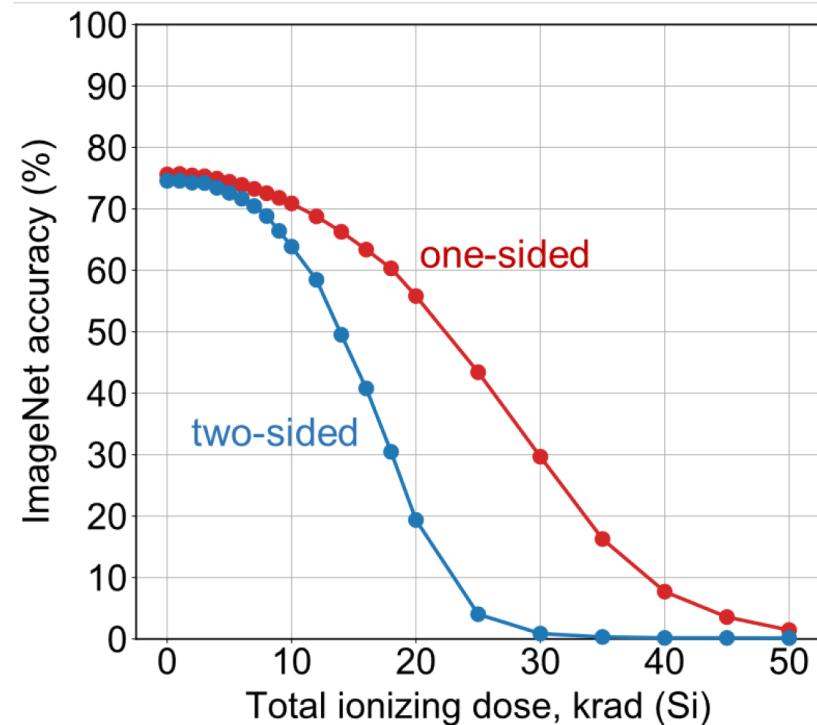
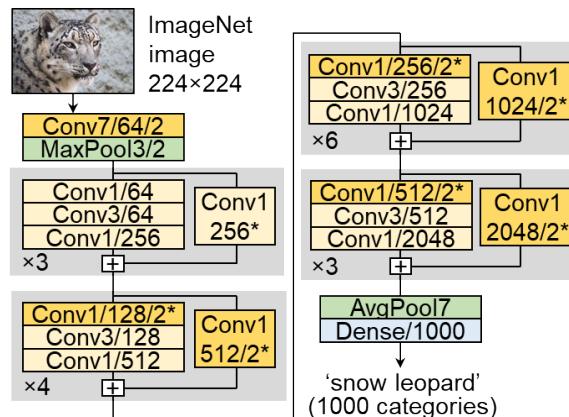
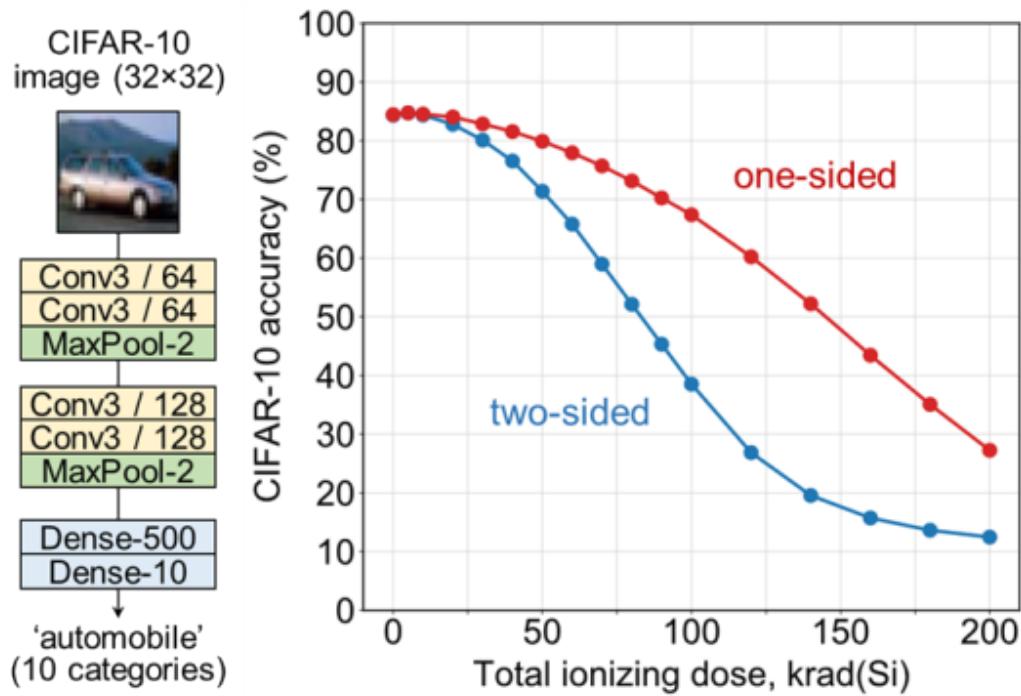
(b) Compute the gradient of the loss relative to the filter inputs

# Analog Neuromorphic SONOS In Space: Physics to Algorithm

How will the accuracy degrade in space?



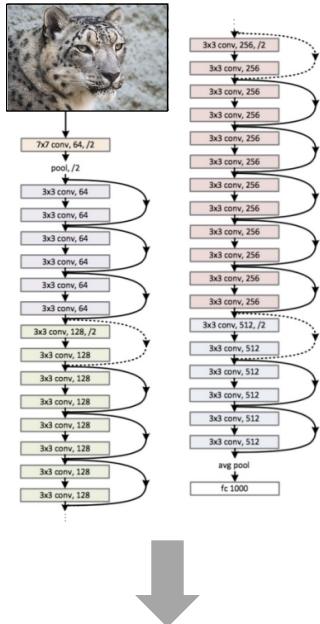
**6-layer CNN for CIFAR-10**  
4.36M weights, 100.4M ops



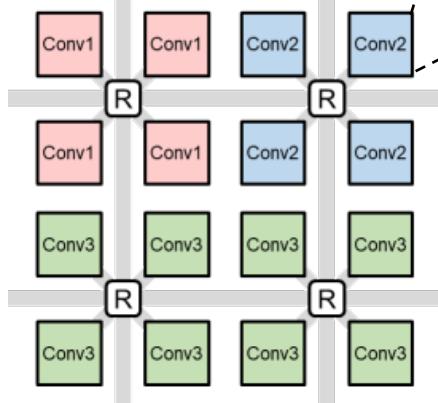
CoDesign provides insight for fielding neuromorphic devices

# Neural Network Inference Architecture

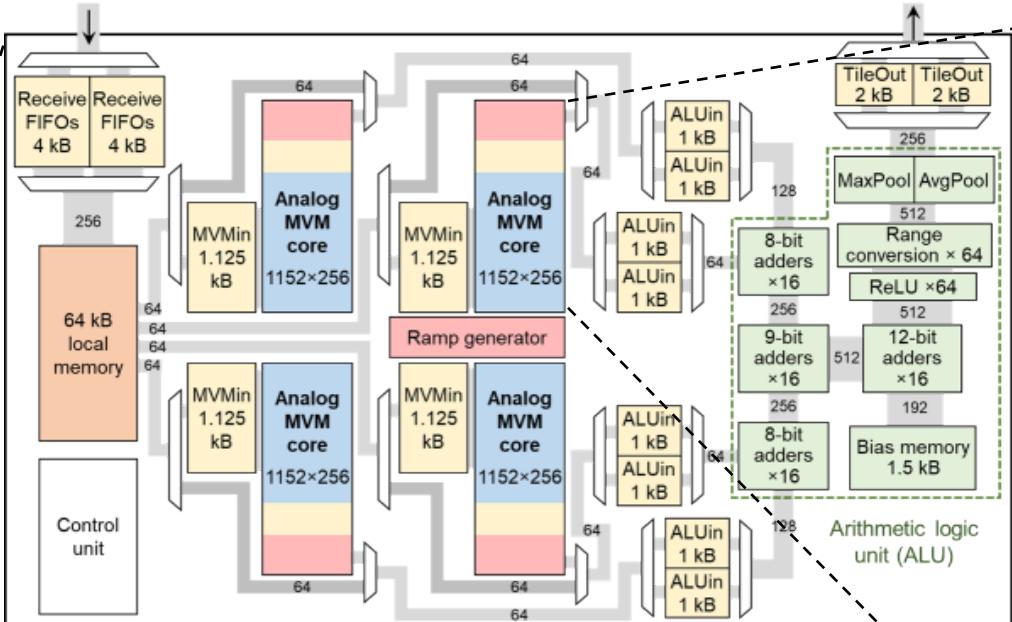
Neural network



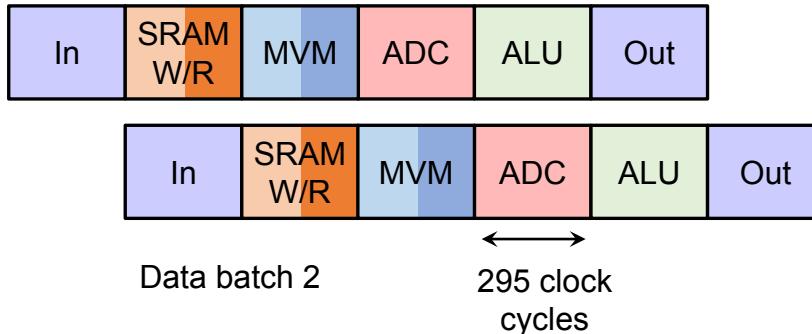
Mesh architecture



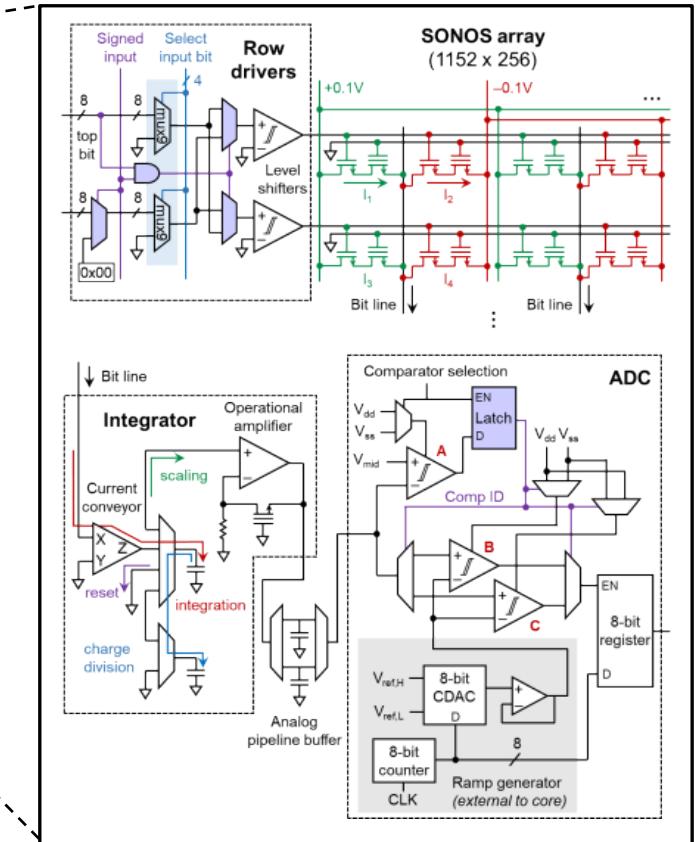
Pipelined MVM tile



Data batch 1



Analog MVM core



Circuits designed and simulated using commercial 40nm PDK

# Comparison of State of the Art Accelerators

TABLE II. Comparison of selected digital and mixed-signal neural network inference accelerators from industry and research.<sup>a</sup> TOPS: Tera-Operations per second. We have counted MACs as single operations where possible. Note that performance (TOPS) is measured at the specified level of weight and activation precision, which differs between accelerators. The results for NVIDIA T4, TPU, Goya, UNPU, and Ref. 122 are measured; others are simulated. TOPS/mm<sup>2</sup> values are based on the die area, where provided.

	NVIDIA T4 <sup>175</sup>	Google TPU v1 <sup>22,b</sup>	Habana Goya HL-1000 <sup>176</sup>	DaDianNao <sup>44</sup>	UNPU <sup>51</sup>	Reference 122 mixed-signal <sup>c</sup>
Process	12 nm	28 nm	16 nm	28 nm	65 nm	28 nm
Activation resolution	8-bit int	8-bit int	16-bit int	16-bit fixed-pt.	16 bits	1 bit
Weight resolution	8-bit int	8-bit int	16-bit int	16-bit fixed-pt.	1 bit <sup>d</sup>	1 bit
Clock speed	2.6 GHz	700 MHz	2.1 GHz (CPU)	606 MHz	200 MHz	10 MHz
Benchmarked workload	ResNet-50 <sup>177</sup> (batch = 128)	Mean of six MLPs, LSTMs, CNNs	ResNet-50 (batch = 10)	Peak performance	Peak performance	Co-designed binary CNN (CIFAR-10)
Throughput (TOPS)	22.2, 130 (peak)	21.4, 92 (peak)	63.1	5.58	7.37	0.478
Density (TOPS/mm <sup>2</sup> )	0.04, 0.24 (peak)	0.06, 0.28 (peak)	...	0.08	0.46	0.10
Efficiency (TOPS/W)	0.32	2.3 (peak)	0.61	0.35	50.6	532

<sup>a</sup>To enable performance comparisons across a uniform application space, we did not consider accelerators for spiking neural networks.

<sup>b</sup>The TPU v2 and v3 chips, which use 16-bit floating point arithmetic, are commercially available for both inference and training on the cloud. MLPerf inference benchmarking results for the Cloud TPU v3 are available,<sup>179</sup> but power and area information is undisclosed. The TPU v1 die area is taken to be the stated upper bound of 331 mm<sup>2</sup>; the listed TOPS/mm<sup>2</sup> values are therefore a lower bound.

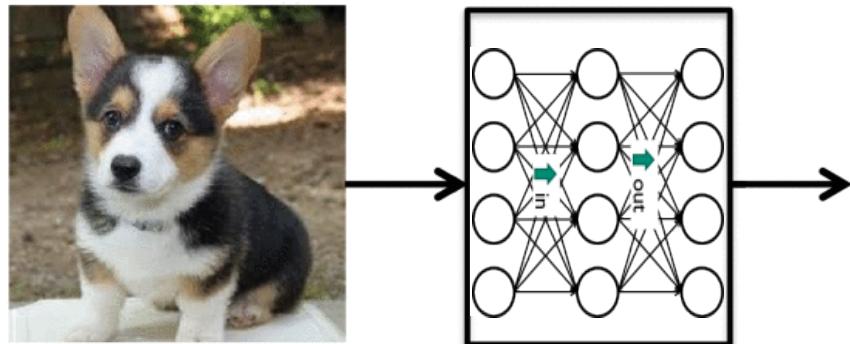
<sup>c</sup>The mixed-signal accelerator in Ref. 122 performs multiplication using digital logic and summation using analog switched-capacitor circuits.

<sup>d</sup>The UNPU architecture flexibly supports any weight precision from 1 to 16 bits. The results are listed for 1-bit weights.

# Neural Networks

## Inference

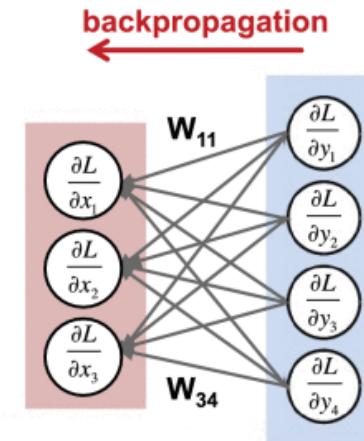
- Feed forward operation of the network to perform task, i.e. classification
- Ex: Image recognition
- Computationally requires single feed forward pass through network
- **Typical device update through write-verify**



## Class Probabilities

## Training

- Adjusting the weights to reduce error and improve
- Typically done with backprop
- **Parallel update possible on crossbar architecture**



(b) Compute the gradient of the loss relative to the filter inputs

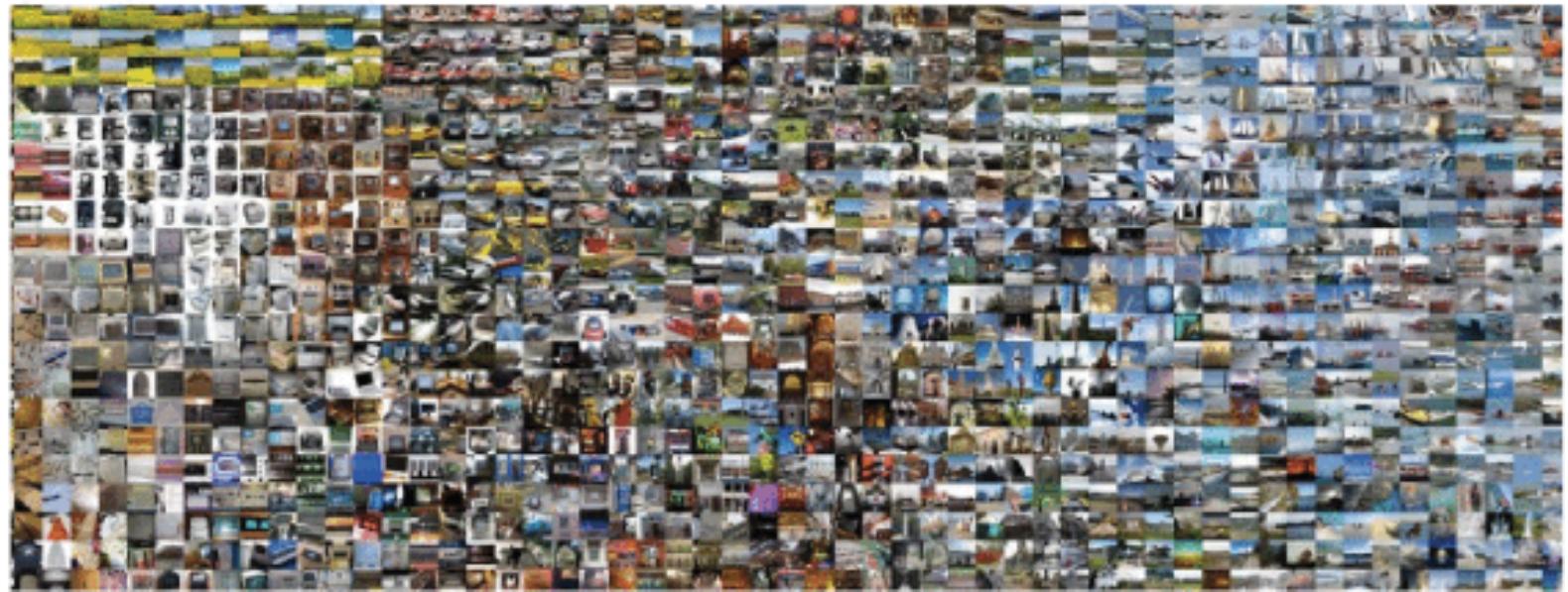
# Example Standard Visual Recognition Datasets

---

**MNIST**

3 6 8 1 7 9 6 6 9 1  
6 7 5 7 8 6 3 4 8 5  
2 1 7 9 7 1 2 8 4 6  
4 8 1 9 0 1 8 8 9 4  
7 6 1 8 6 4 1 5 6 0  
7 5 9 2 6 5 8 1 9 7  
1 2 2 2 2 3 4 4 8 0  
0 2 3 8 0 7 3 8 5 7  
0 1 4 6 4 6 0 2 4 3  
7 1 2 8 7 6 9 8 6 1

**ImageNet**

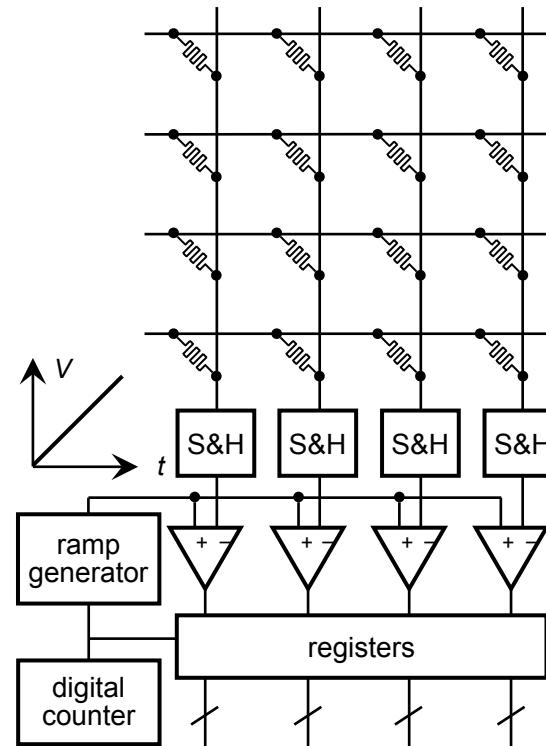
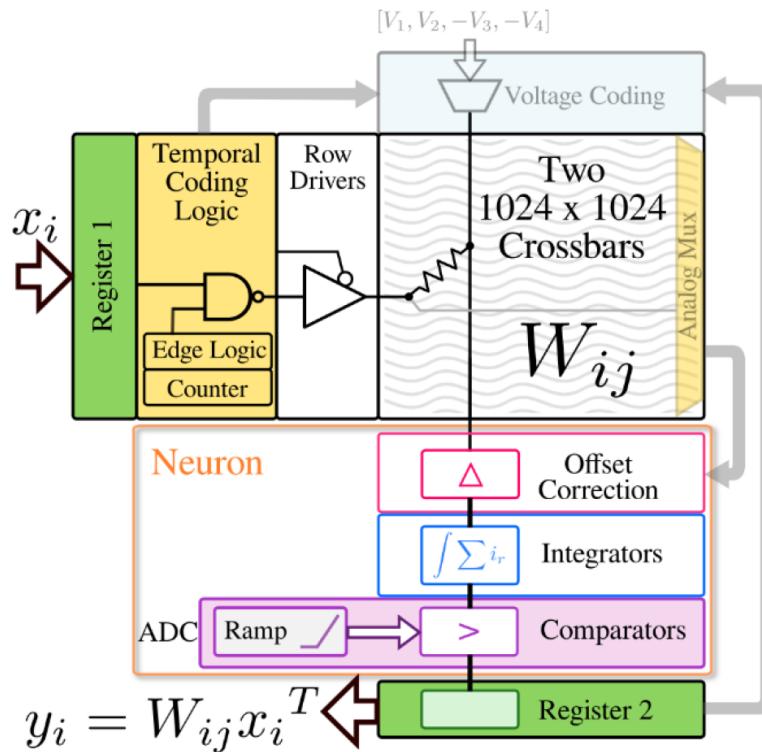


- 28x28 pixel grayscale
- 10 classes
- 60k training images
- 10k test images

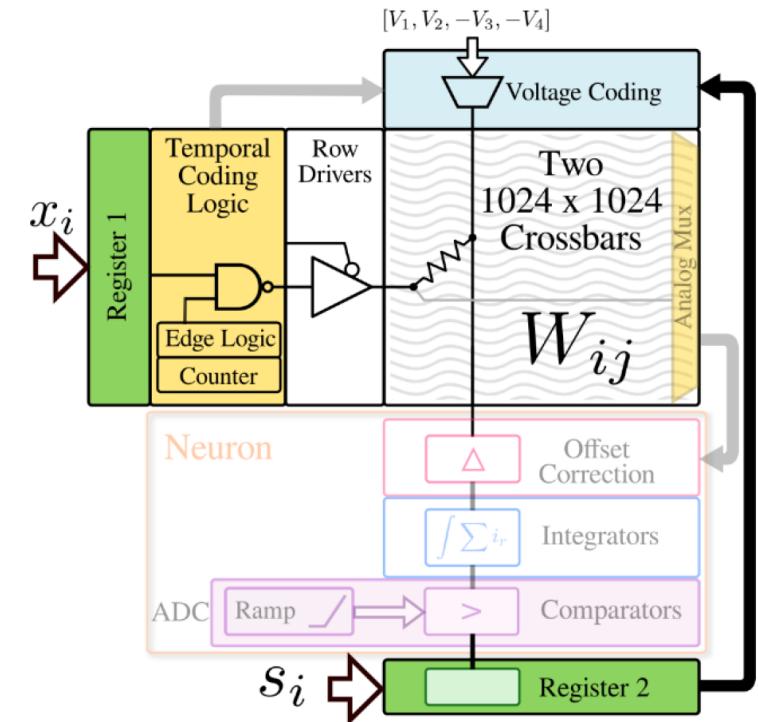
- 256x256 pixel color
- 1000 classes
- 1.3M training images
- 100k test images

# Key Circuit Block/Kernel Analysis

## Vector Matrix Multiply (Inference)

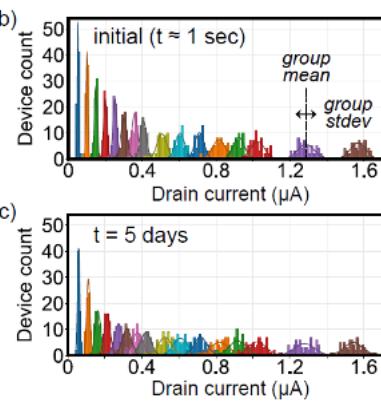
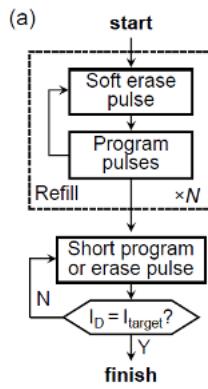
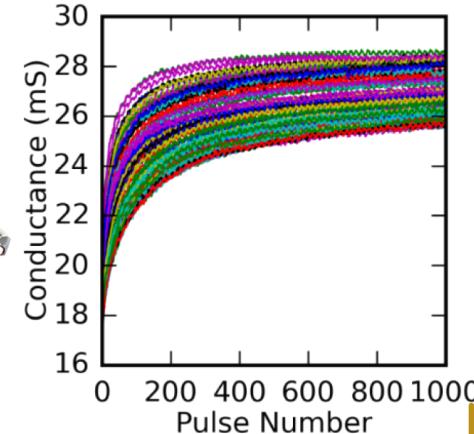
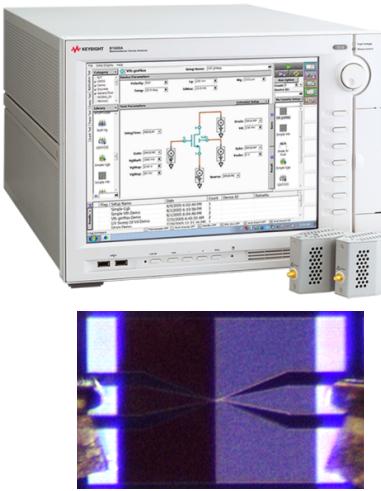


## Rank-1 Update (Training)



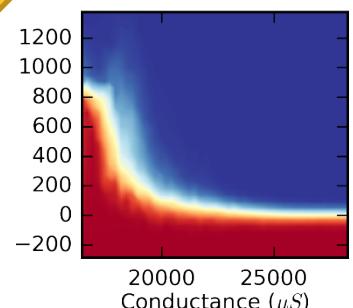
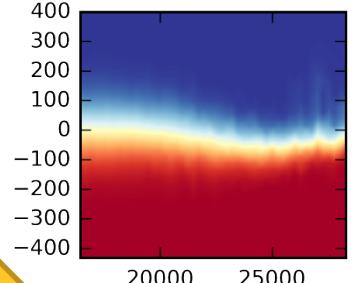
# Compact Modeling Dataset for Neural Accuracy Model

## Measure Devices



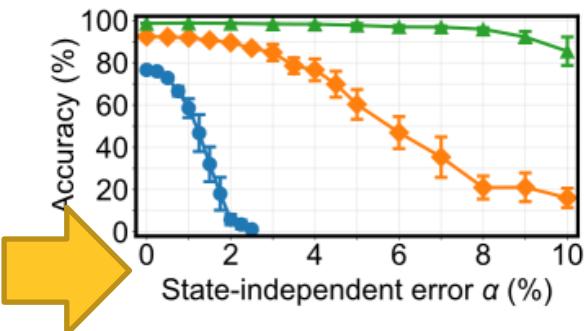
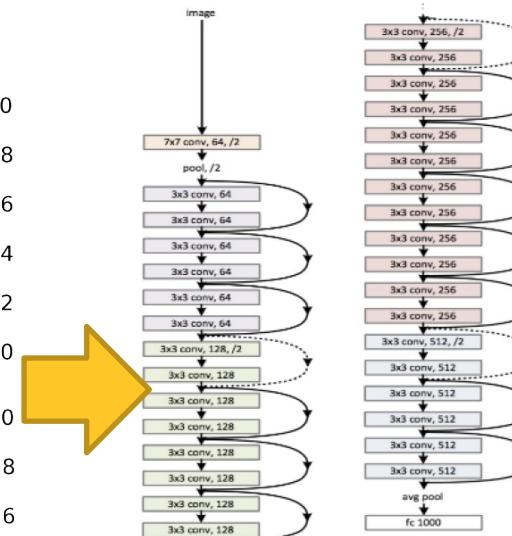
## Construct Lookup Tables

100 ns



#ROSS SIM

## Model Array Circuitry, Architecture, & Algorithms



Assess Neural  
Algorithm  
Accuracy,  
Efficiency,  
Performance,  
Radiation

Component VMM OPU

Energy/Op ReRAM (fJ)	12.2	2.1
Array Latency ReRAM (μs)	0.38	0.51

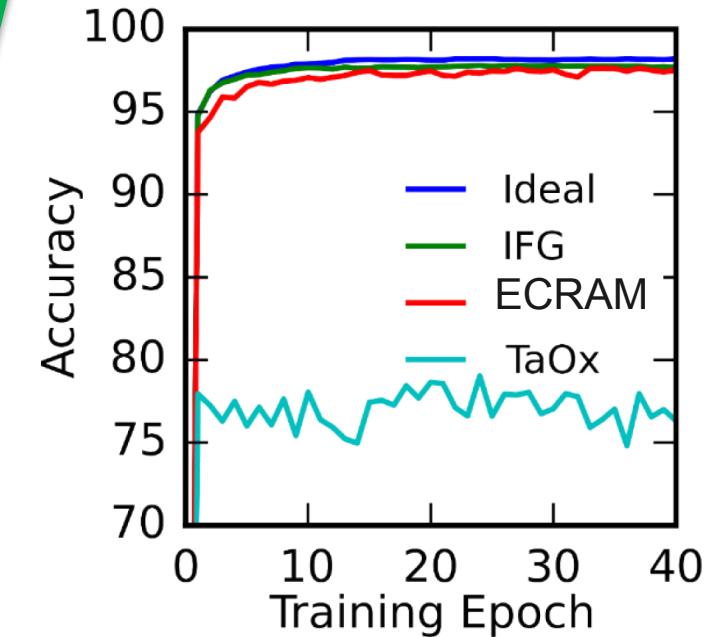
# Training Accuracy and Tile Energy/Summary

Codesign to Model Performance & Energy

Component	Vector Matrix Multiply	Matrix Vector Multiply	Outer Product Update
Energy/Op ECRAM (fJ)	11.9	11.9	0.2
Energy/Op ReRAM (fJ)	12.2	12.2	2.1
Energy/Op SONOS (fJ)	13.7	13.7	68.2
Energy/Op SRAM (fJ)	2718	4630	4102
Array Latency ECRAM (μs)	0.39	0.39	1.9
Array Latency ReRAM (μs)	0.38	0.38	0.51
Array Latency SONOS (μs)	0.40	0.40	20
Array Latency SRAM (μs)	4	32	8

**SONOS: While accuracy, program  
is slow: use for inference**

**ECRAM: Use for training  
& inference**



**ReRAM: Training is not  
accurate: better for  
inference**