



# Assessment of Mix in MagLIF Experiments using an Analytic Hotspot Model



PRESENTED BY

Patrick F. Knapp

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## Thanks to my many colleagues and contributors



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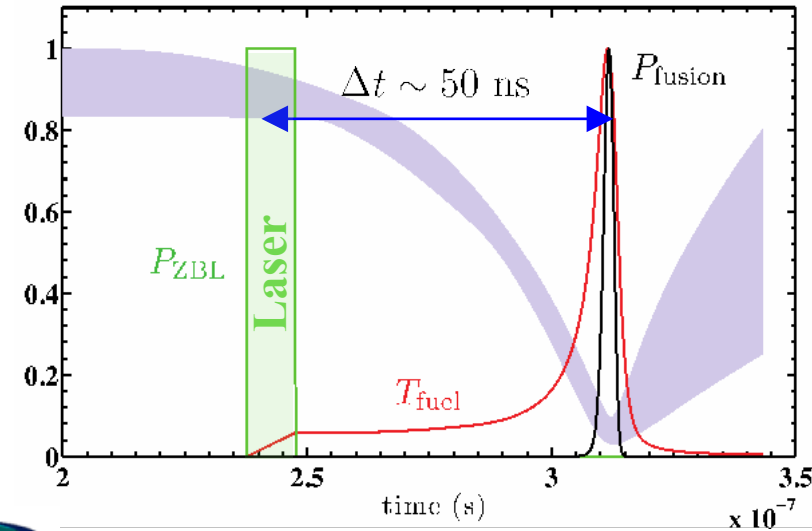
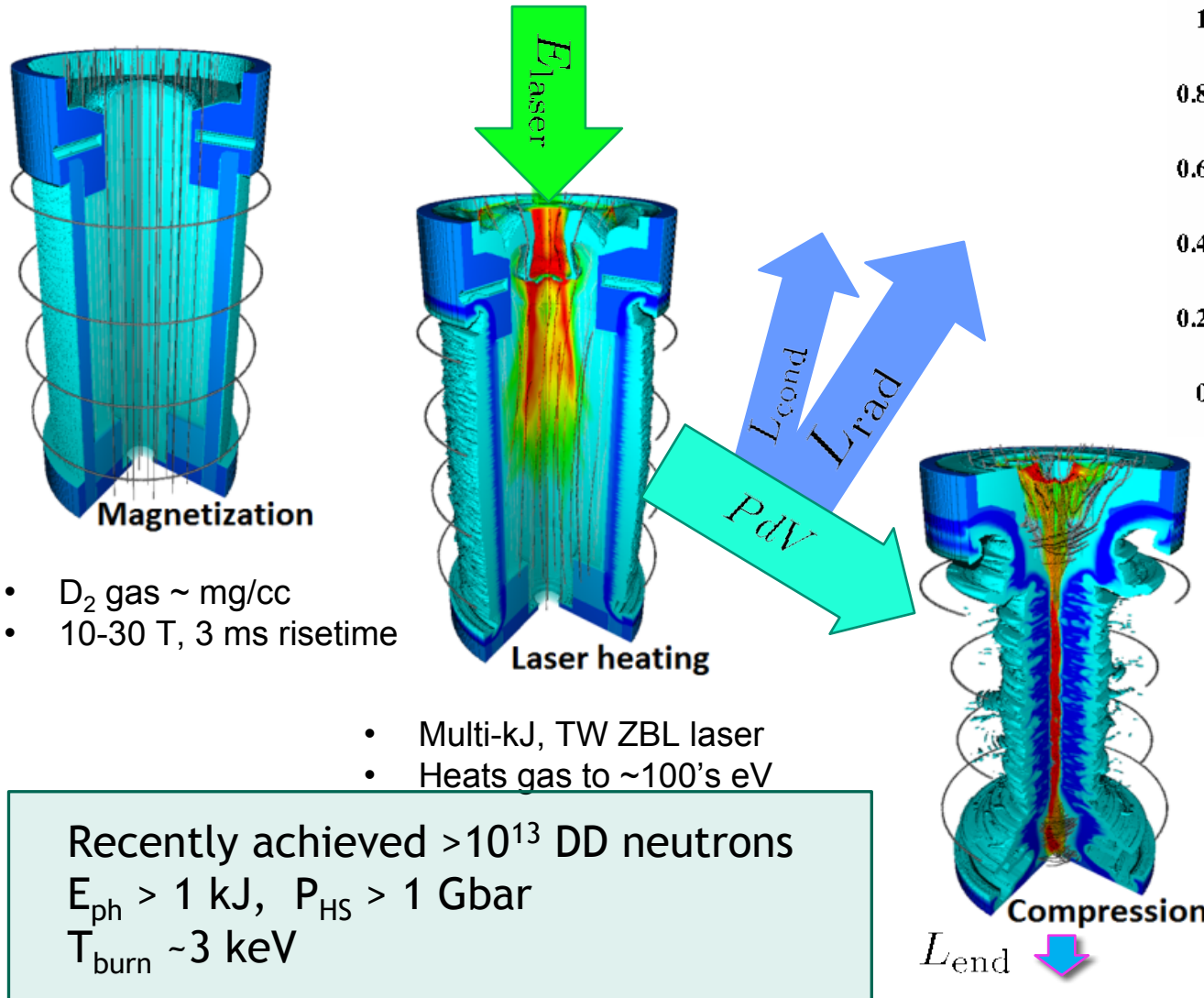
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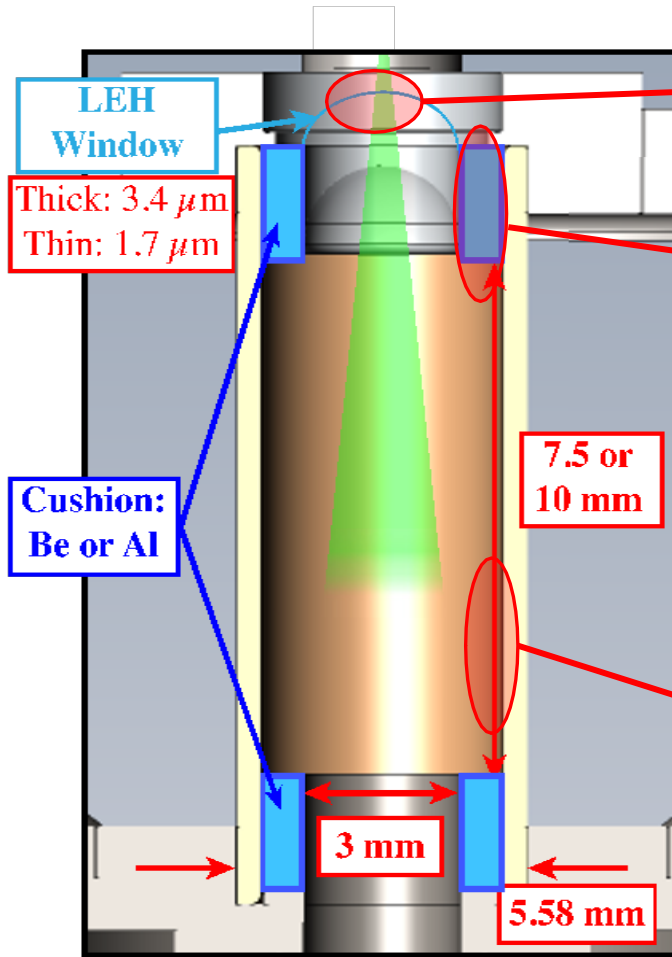
# MagLIF uses preheat, magnetic insulation and adiabatic compression to achieve high pressure



- Laser heating allows high pressures to be achieved with low implosion velocity ( $<100 \text{ km/s}$ )
- Preheat energy is contained during implosion via magnetic insulation
- Flux compression allows confinement of fusion products with low fuel  $\rho R$
- Long dwell time between preheat and stagnation makes us sensitive to early time mix

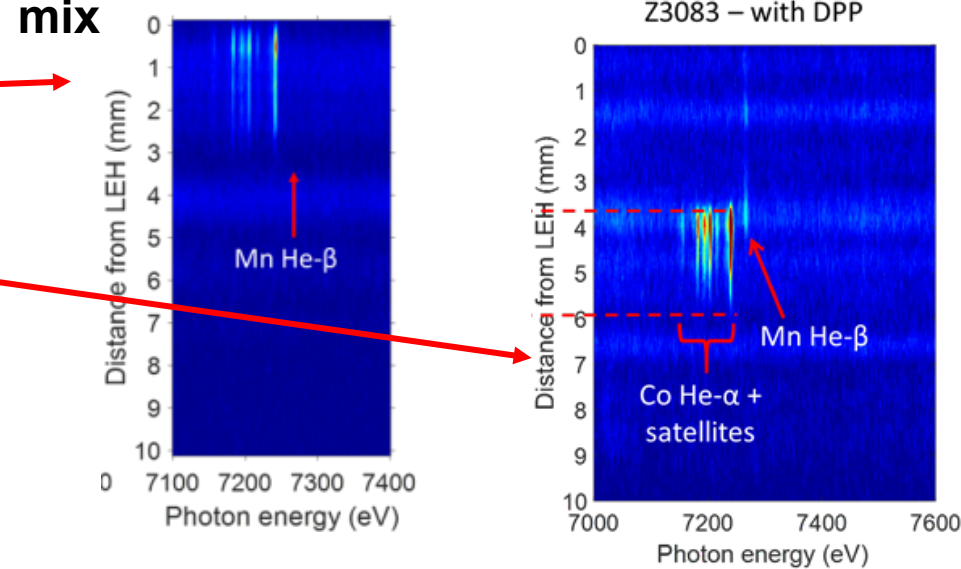


# Mix is known to occur, but the total amount and relative contributions from potential sources is poorly understood



See related presentations  
KI3.00002: Adam Harvey-Thompson  
GP11.00126: Matthias Geissel

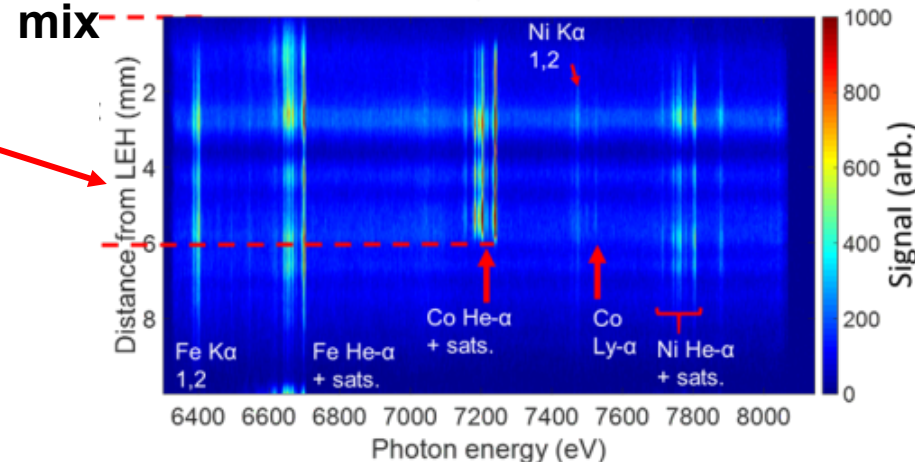
## Co coatings used to analyze window and cushion mix



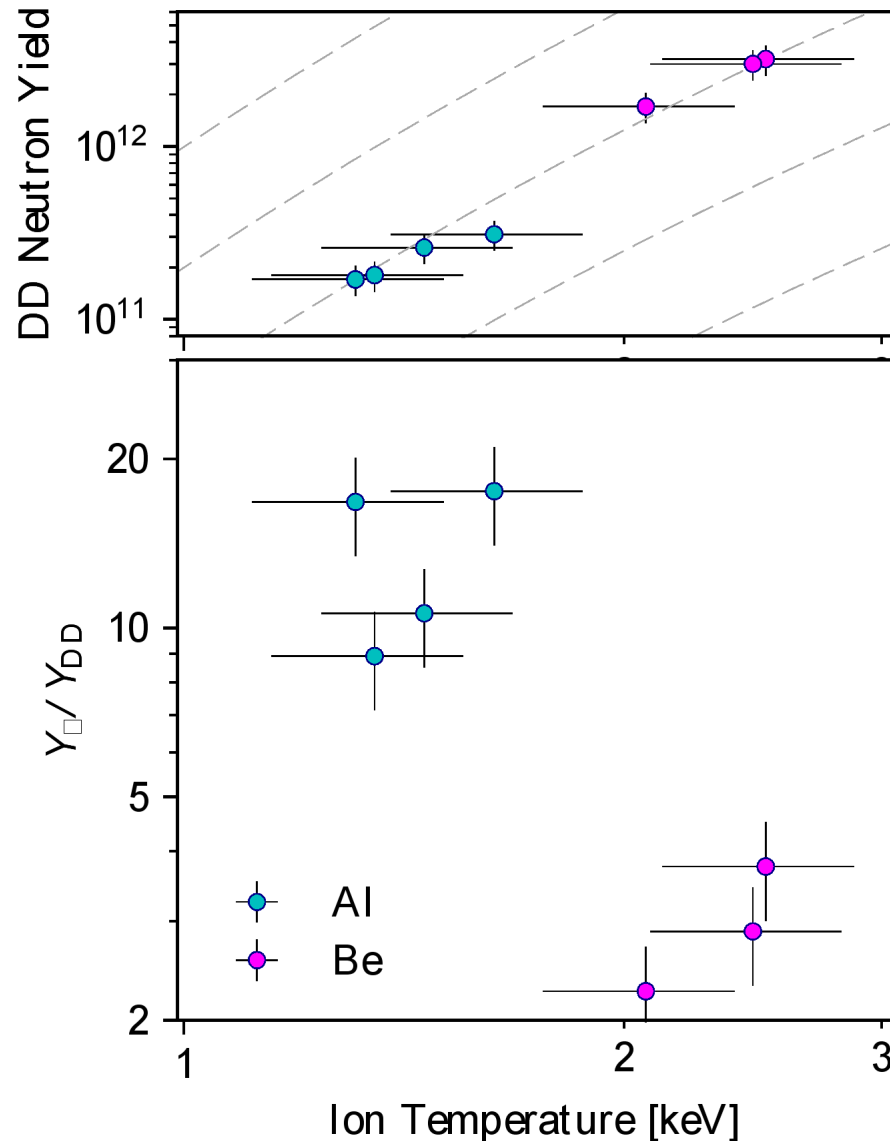
## Main Contributors to mix

- Preheat
  - Window
  - Cushion
- Implosion
  - Liner

## Fe impurity in Be used to analyze liner mix



# We have analyzed a series of experiments that isolate the effect of mix from the cushions

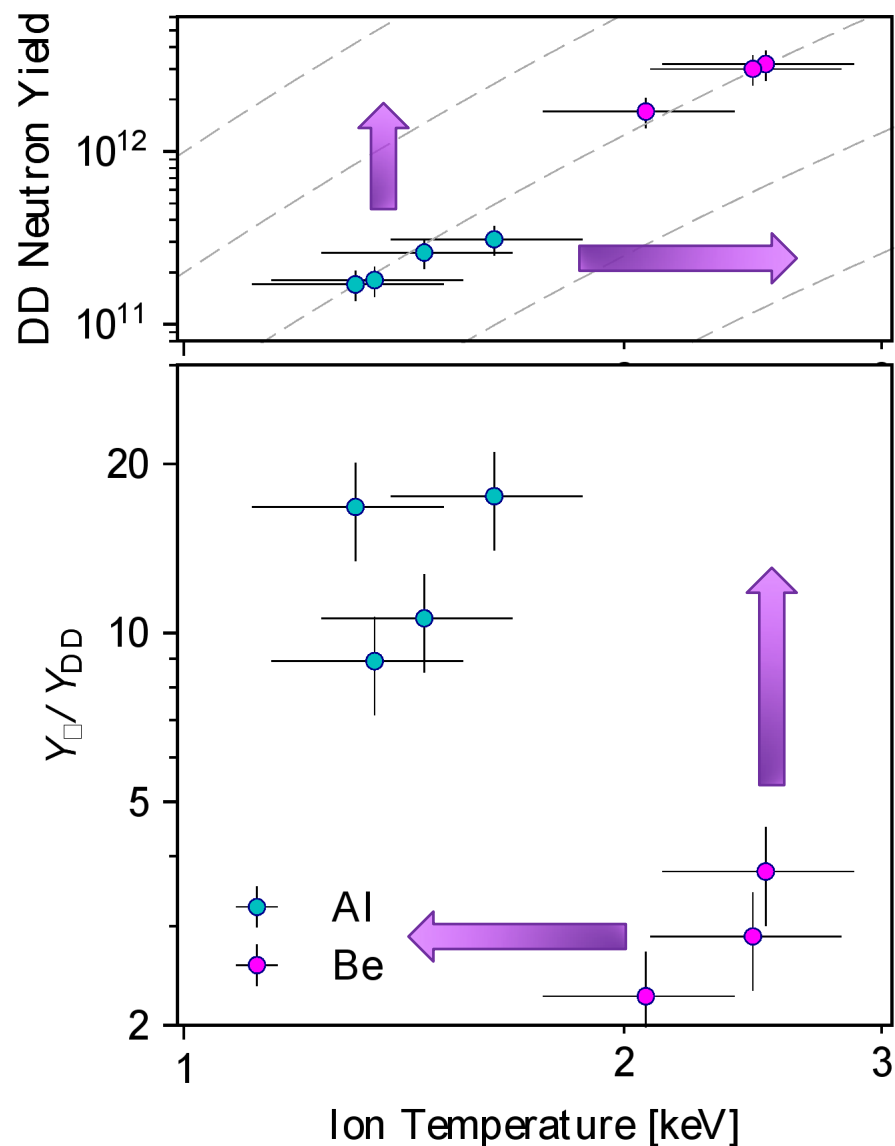


No DPP, 10 mm tall target, 1.7  $\mu\text{m}$  thick window 60 PSI  $\text{D}_2$  fill

Z Shot #	Cushion Material	$E_{PH}$ [kJ]	$Y_{DD}$ ( $\pm 20\%$ ) $\times 10^{12}$	$Y_\nu$ [J]	$T_i$ [keV]
z2707	Al	0.3+1.8	0.3	3.1	1.5
z2708	Al	0.4+2.3	0.2	3.2	1.3
z2758	Al	0.4+1.8	0.3	6.1	1.6
z2985	Al	0.6+2.1	0.2	1.8	1.4
z2839	Be	0.4+2.3	3.2	13.5	2.3
z2977	Be	0.4+2	3.0	9.7	2.5
z2979	Be	0.3+1.8	1.7	4.3	2.2

- Increased neutron yield is strongly correlated with higher temperatures
- Increased x-ray yield relative to neutron yield is strongly correlated with lower temperatures
- Be cushion experiments (magenta) are clustered in the higher yield, higher  $T_i$ , lower x-ray yield range
- Al cushion experiments are clustered in the opposite space
- All strongly suggests cushion mix in the Al case is a major contributor to the degraded performance

# In this configuration there is a significant difference in performance between the Al and Be cushion cases



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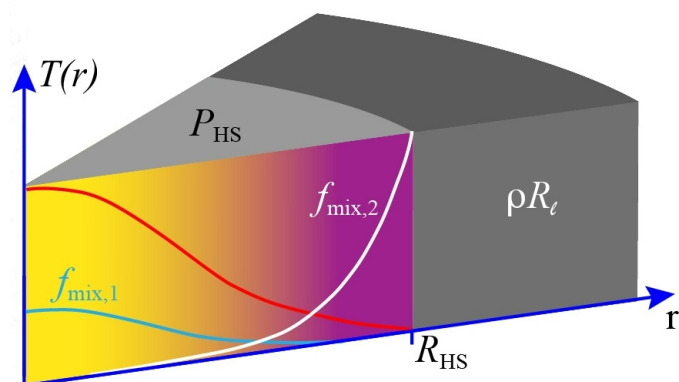
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# We have developed an analytic hotspot model to analyze and interpret these results



Model the stagnation as a 1D isobaric cylinder

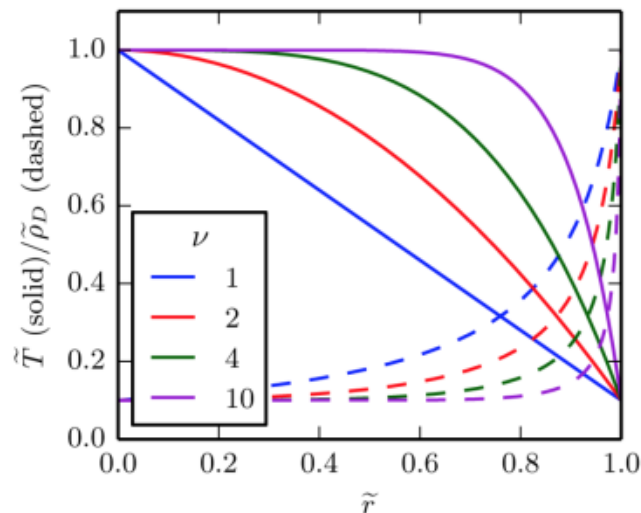


**Model Parameters**

$$\begin{aligned} &T_c \\ &P_{\text{HS}} \\ &V_{\text{HS}} \\ &f_{\text{mix}}; Z_{\text{mix}} \\ &\tau_\nu^\ell \\ &\tau_{\text{burn}} \end{aligned}$$

- In order to infer the stagnation parameters, we must account for the x-ray and neutron emission consistently
- By defining an isobaric cylinder with a prescribed (physically motivated) temperature profile ( $T_i = T_e$ ) we can calculate all of the required diagnostic outputs

Prescribed temperature profile



$$P_\nu = A_{ff} 4\pi P_{\text{HS}}^2 e^{-\tau_\nu^\ell} \int_{V_{\text{HS}}} \frac{\langle Z \rangle g_{\text{FF}}}{(1 + \langle Z \rangle)^2} \sum_i f_i \tilde{j}_i \frac{e^{-h\nu/T_e}}{T_e^{5/2}} dV$$

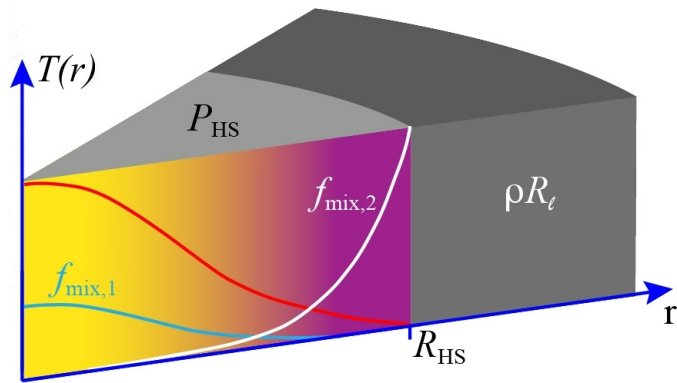
$$\tilde{j}_i \equiv j_i/j_D = Z_i^2 + (A_{fb}/A_{ff}) (Z_i^4/T_e) e^{Ry Z_i^2/T_e}$$

$$Y_{\text{DD}} = \frac{1}{2} P_{\text{HS}}^2 \tau_b \int_{V_{\text{HS}}} \frac{\langle \sigma v \rangle_{\text{DD}}}{(1 + \langle Z \rangle)^2 T_i^2} dV$$

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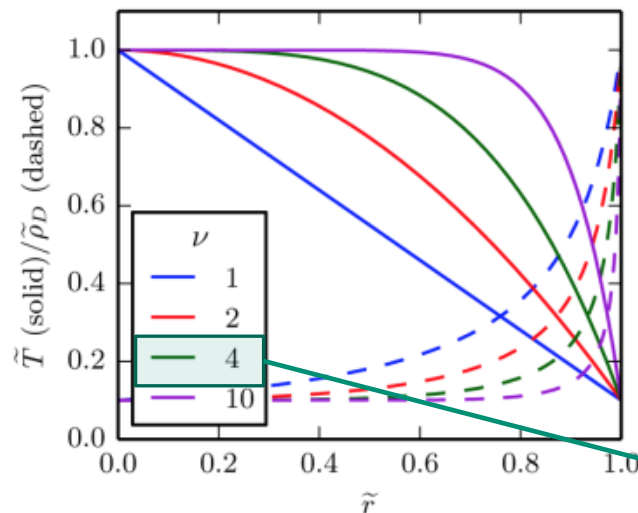


**Model Parameters**

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 $P_{HS}$   
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 $\tau_{burn}$

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Based on comparison with MHD simulations

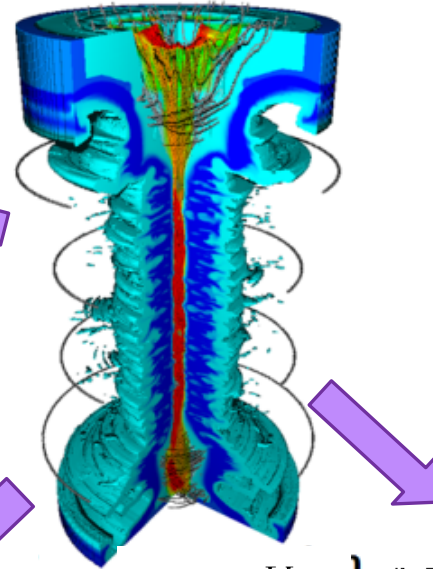
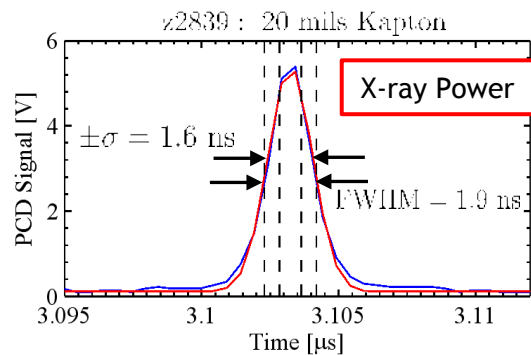
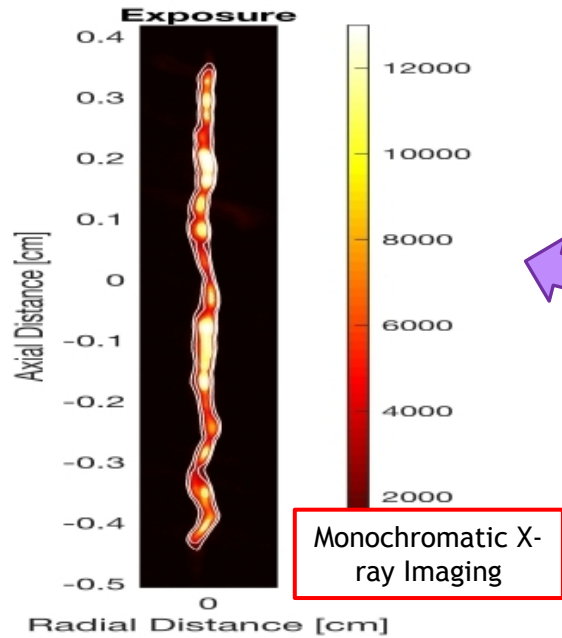
$$P_\nu = A_{ff} 4\pi P_{HS}^2 e^{-\tau_\nu^\ell} \int_{V_{HS}} \frac{\langle Z \rangle g_{FF}}{(1 + \langle Z \rangle)^2} \sum_i f_i \tilde{j}_i \frac{e^{-h\nu/T_e}}{T_e^{5/2}} dV$$

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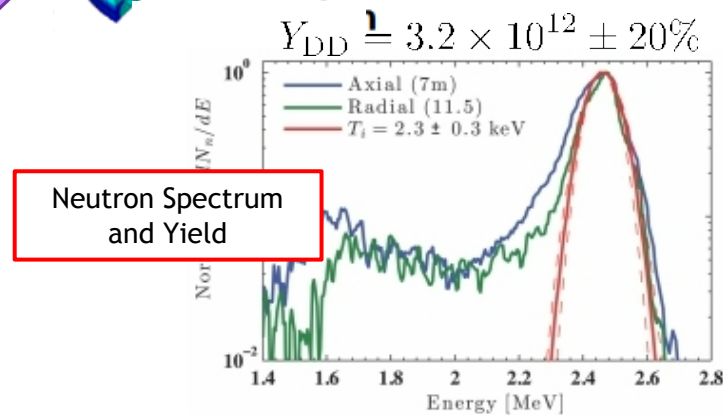
$$Y_{DD} = \frac{1}{2} P_{HS}^2 \tau_b \int_{V_{HS}} \frac{\langle \sigma v \rangle_{DD}}{(1 + \langle Z \rangle)^2 T_i^2} dV$$



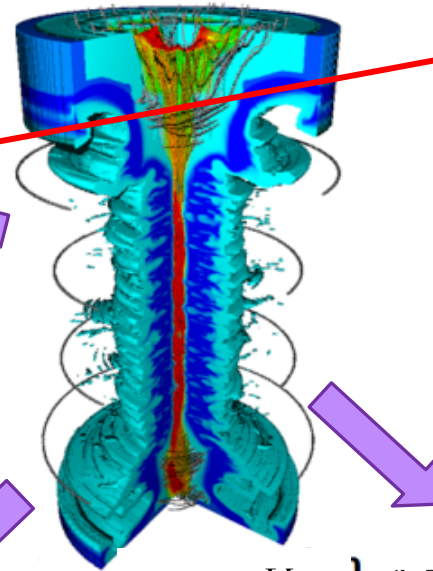
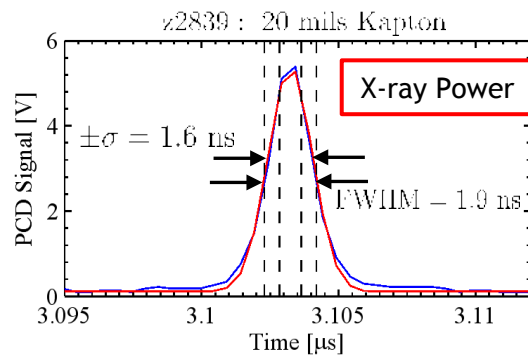
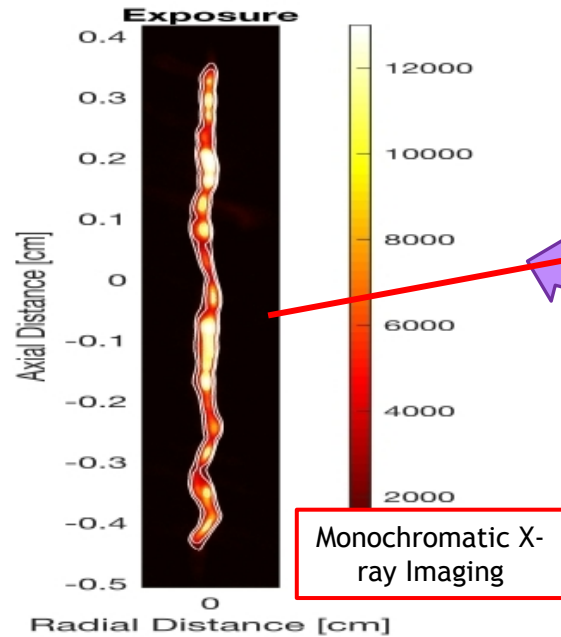
# Using the available data we can completely constrain the quantities required to infer *bulk* stagnation pressure and mix fraction



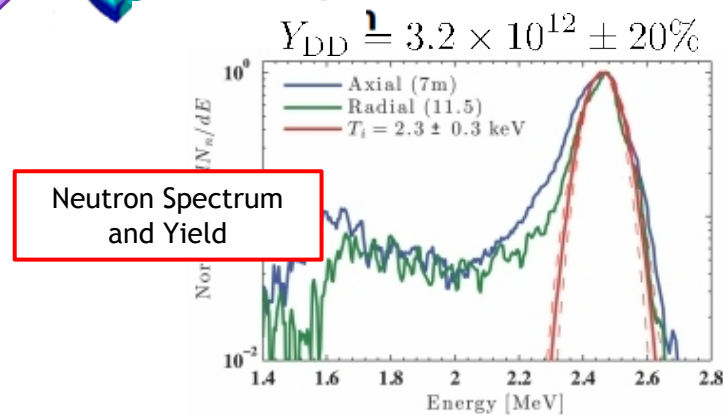
- Hotspot Volume:
- X-ray Yield:
- Burn Duration:
- Neutron Yield:
- Burn Temperature:



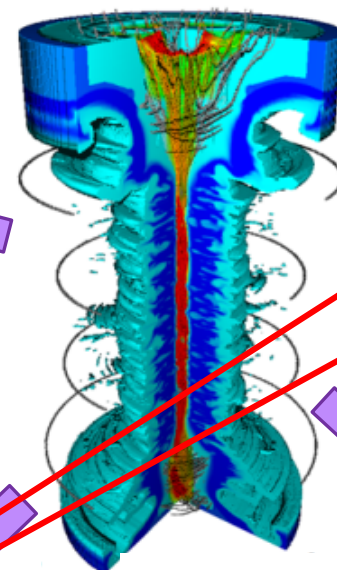
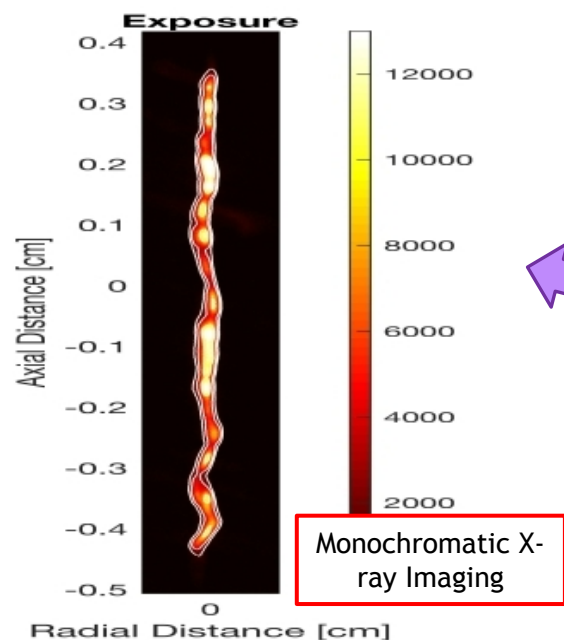
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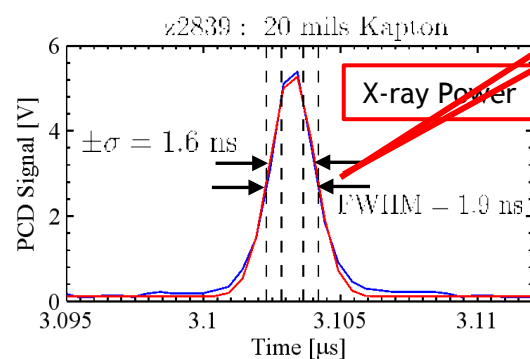
- Hotspot Volume:  $V_{\text{HS}} \pm \sigma_V$
- X-ray Yield:
- Burn Duration:
- Neutron Yield:
- Burn Temperature:



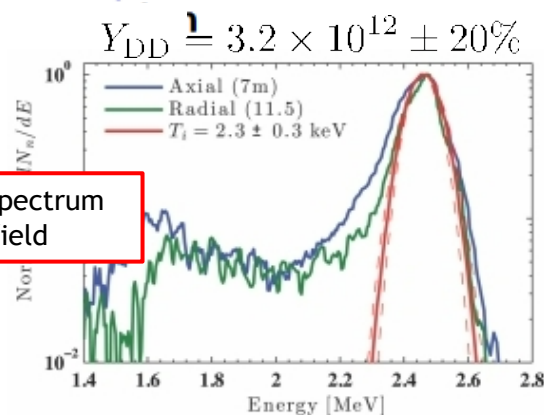
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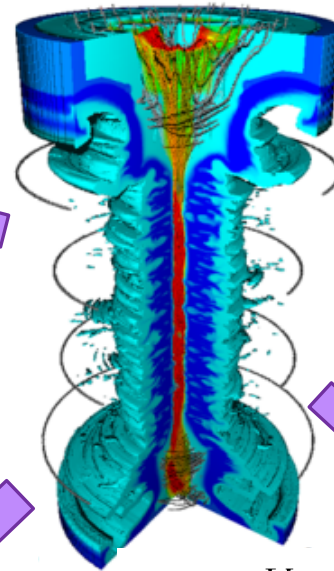
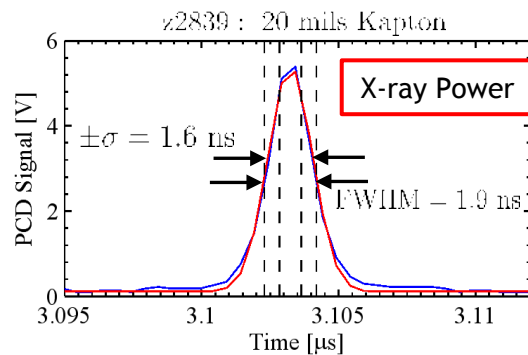
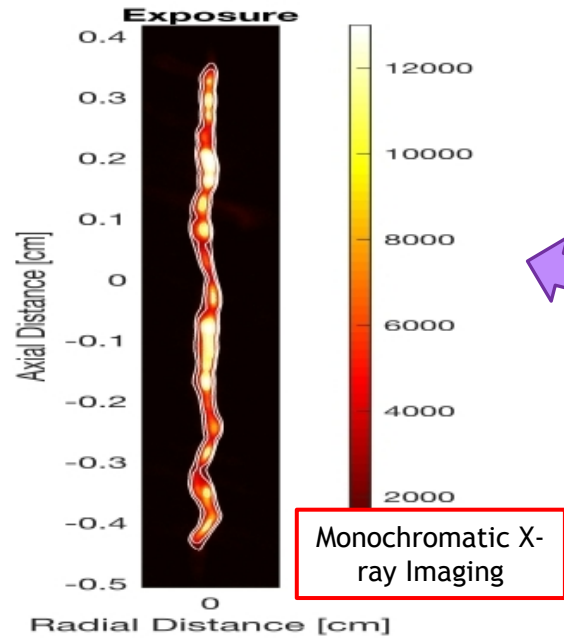
- Hotspot Volume:  $V_{HS} \pm \sigma_V$
- X-ray Yield:  $Y_{PCD}$
- Burn Duration:  $\tau_b \pm \sigma_\tau$
- Neutron Yield:
- Burn Temperature:



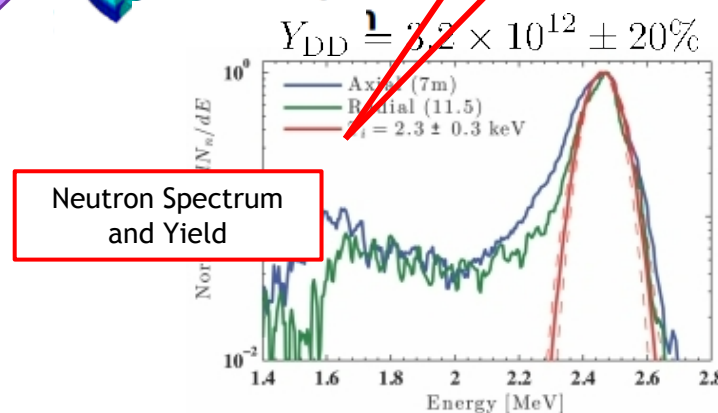
Neutron Spectrum and Yield



# Using the available data we can completely constrain the quantities required to infer *bulk* stagnation pressure and mix fraction

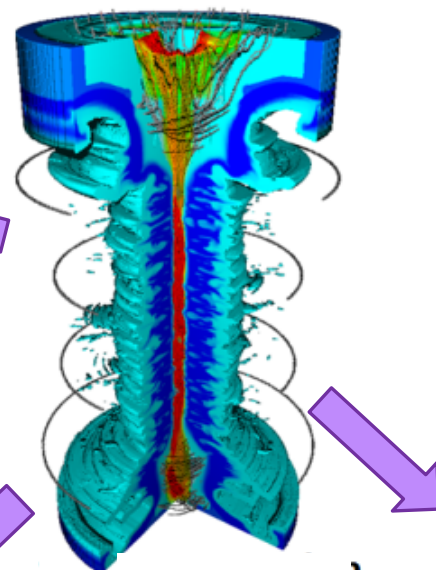
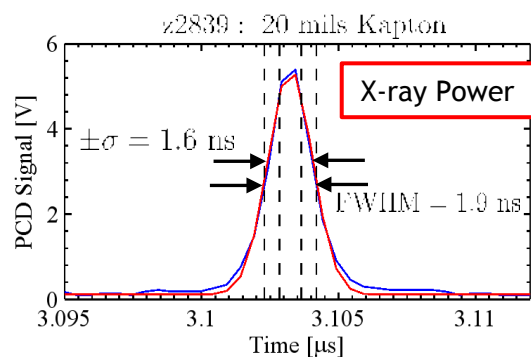
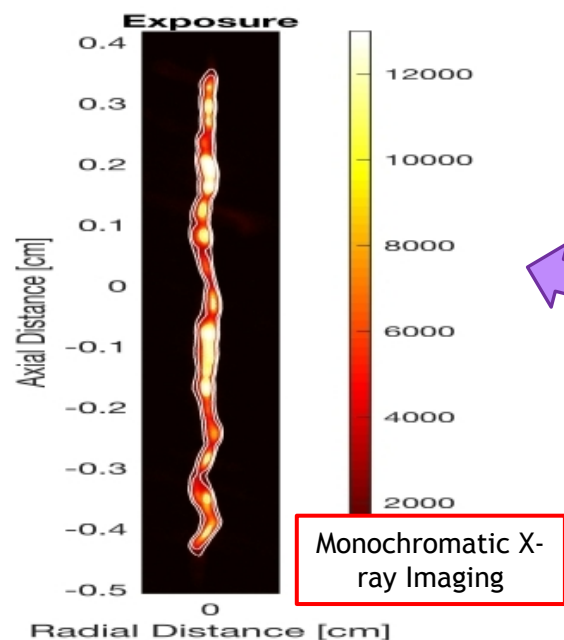


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- Neutron Yield:  $Y_{DD}$
- Burn Temperature:  $T_c \pm \sigma_T$

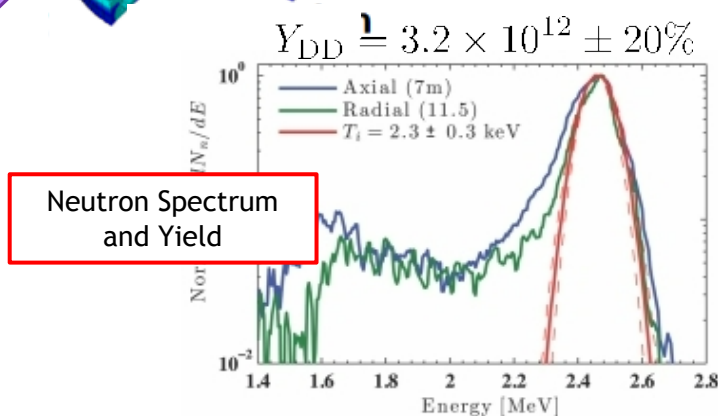




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- Burn Duration:  $\tau_b \pm \sigma_\tau$
- Neutron Yield:  $Y_{\text{DD}}$
- Burn Temperature:  $T_c \pm \sigma_T$



$$\rho R_\ell \pm \sigma_{\rho R}$$

Liner areal density taken as a nominal value from spectroscopic measurements\*

\*Hansen et al., Phys. Plasmas 22, 056313 (2015)

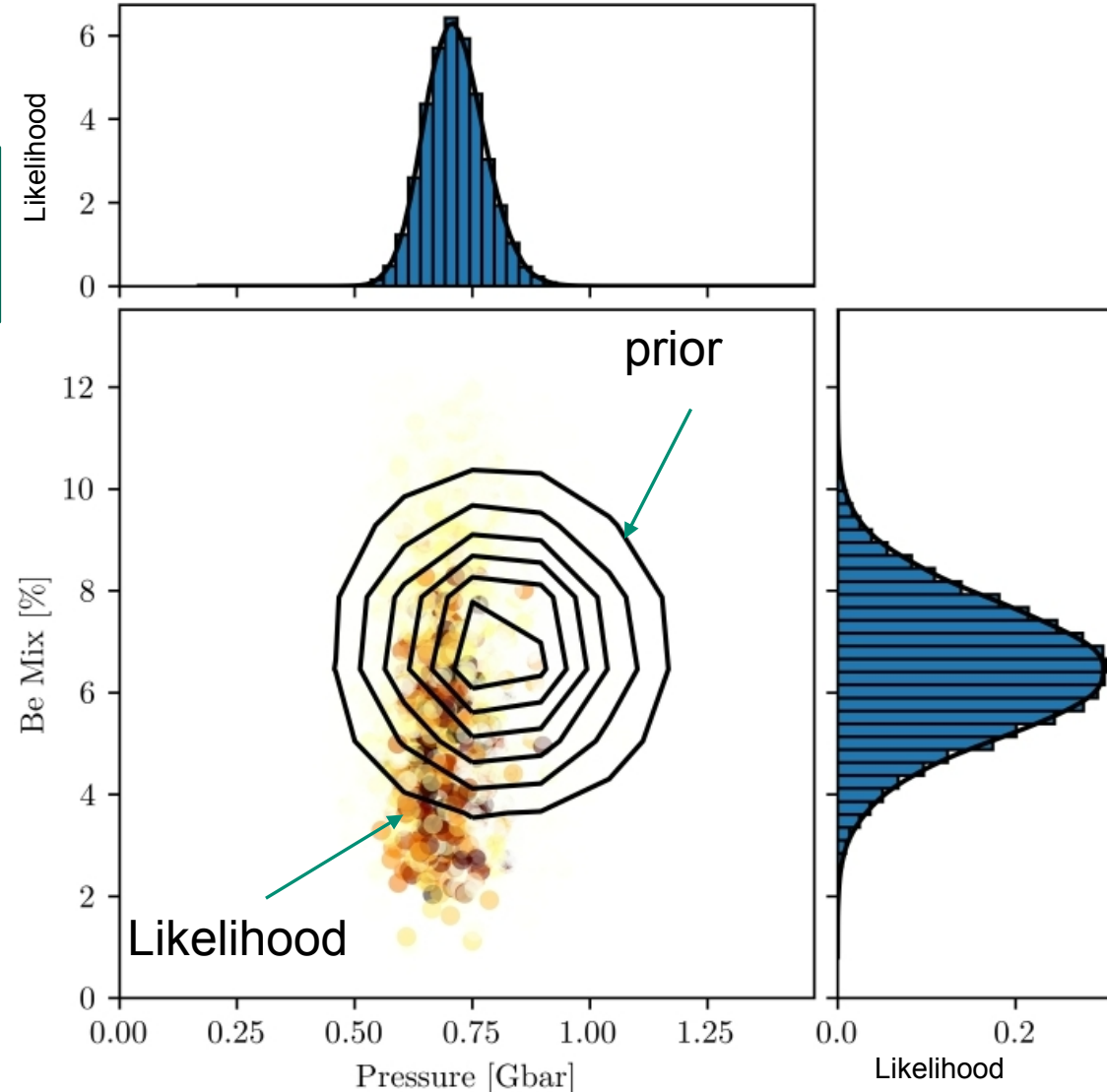
# By sampling the space of uncertain input parameters we determine the maximum likelihood solution for pressure and mix



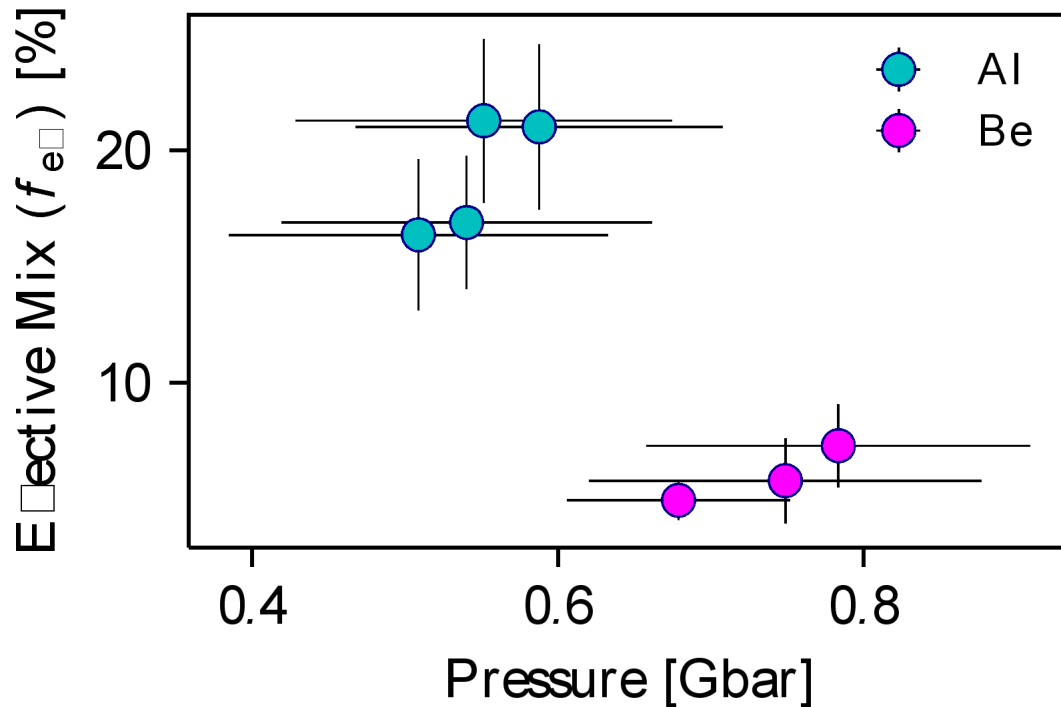
## Likelihood

$$\mathcal{P}(\bar{\mathbf{x}}|\bar{\mathbf{m}}, \mathcal{A}) = \exp \left( - \sum_i \frac{(\mathcal{F}_i(\bar{\mathbf{m}}) - x_i)^2}{2\sigma_i^2} \right)$$

- The likelihood is defined as the probability of observing the measurement given a particular set of model parameters and our prior knowledge of the system
- This method allows us to efficiently sample a wide range of parameter values, constrained by additional measurements
- Correlations are contained in the likelihood distribution



# This analysis shows that low mix is strongly correlated with high pressure and the Al and Be cushion shots are clustered



- This analysis determines the stagnation pressure and an *effective* mix fraction (assuming mix is 100% Be)
- The Be cushion shots have, on average
  - 3x less effective mix fraction
  - ~40% higher pressure
- The average hotspot energy is ~50% higher in the Be cushion experiments

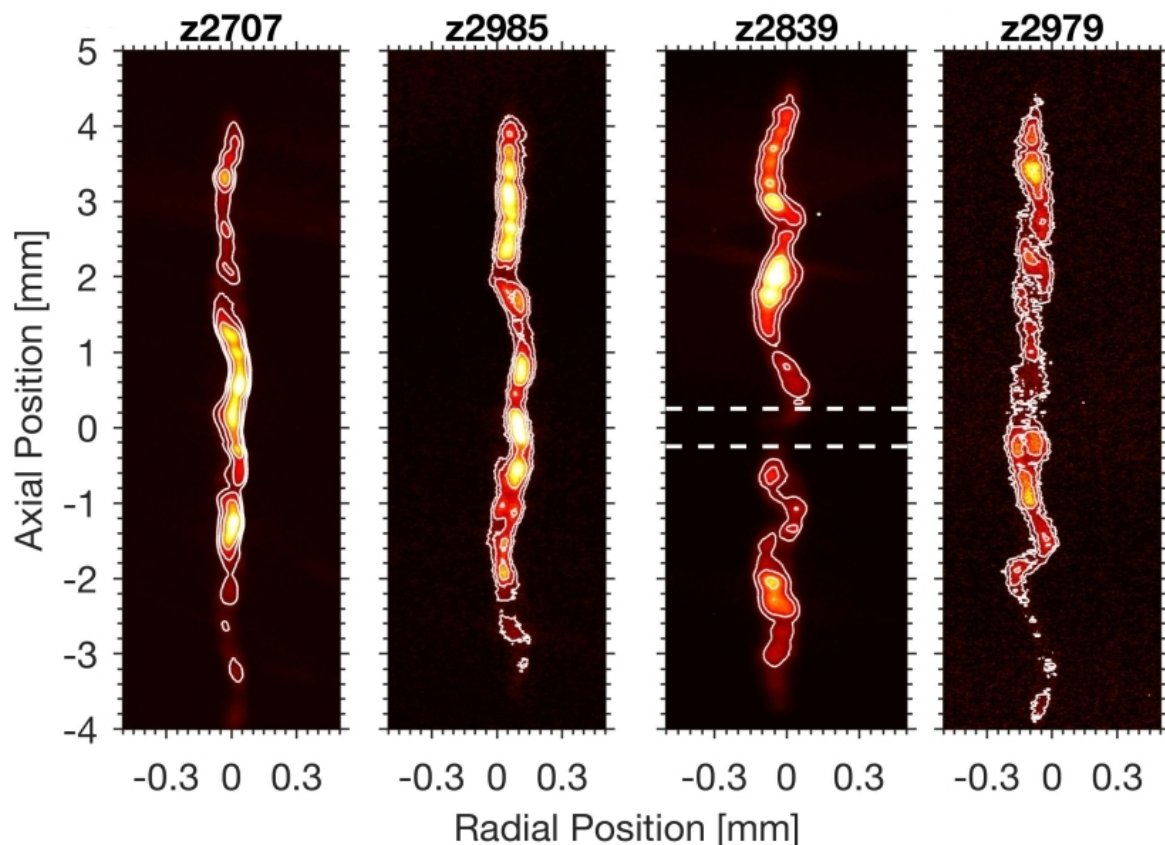
$$\langle E_{\text{HS}}^{\text{Al}} \rangle = \langle \frac{3}{2} P_{\text{HS}} V_{\text{HS}} \rangle \approx 7.6 \text{ kJ} \quad \langle E_{\text{HS}}^{\text{Be}} \rangle = \langle \frac{3}{2} P_{\text{HS}} V_{\text{HS}} \rangle \approx 11.4 \text{ kJ}$$

# We can use the similarities between the Al and Be experiments to deconvolve the mix sources from the integrated results



## Al Cushion

## Be Cushion



- The morphology and evolution of stagnation appear to be very similar between the high mix and low mix experiments
- Volumes are the same to +/- 20%
- $\tau_{\text{burn}}$  is the same to +/- 10% (measured with x-rays)
- Laser pulses and LEH windows are nominally identical
- Radiation losses are the only term significantly modified by mix



# Exploiting these similarities we can break the mix contribution into three sources and constrain each



$$N_W \approx (500 \mu\text{m})^2 * 1.77 \mu\text{m} * n_{\text{ion}} \approx 4 \times 10^{16}$$

Mix total: **Window** + **Cushion** + **Liner**

$$\begin{aligned} f_{\text{eff}}^{\text{Be}} Z_{\text{Be}}^3 &= \boxed{f_W \bar{Z}_{\text{poly}}^3} + \boxed{f_C^{\text{Be}} Z_{\text{Be}}^3} + \boxed{f_D Z_{\text{Be}}^3} && \text{Be Cushion} \\ f_{\text{eff}}^{\text{Al}} Z_{\text{Be}}^3 &= \boxed{f_W \bar{Z}_{\text{poly}}^3} + \boxed{f_C^{\text{Al}} Z_{\text{Al}}^3} + \boxed{f_D Z_{\text{Be}}^3} && \text{Al Cushion} \end{aligned}$$

$$N_{\text{fucl}} = \frac{P}{kT} \approx 8 \times 10^{18}$$

$$f_W = 0.5 \pm 0.2\%$$

- $f_W$  and  $f_D$  are assumed to be the same in the two cases
- 2 equations, four unknowns
  - Constrain  $f_W$  using the window thickness and laser spot size
  - Define a relationship between fractions of cushion mix in each case
- The system is fully defined and we can solve for each contribution using the ensemble averages for  $f_{\text{eff}}$

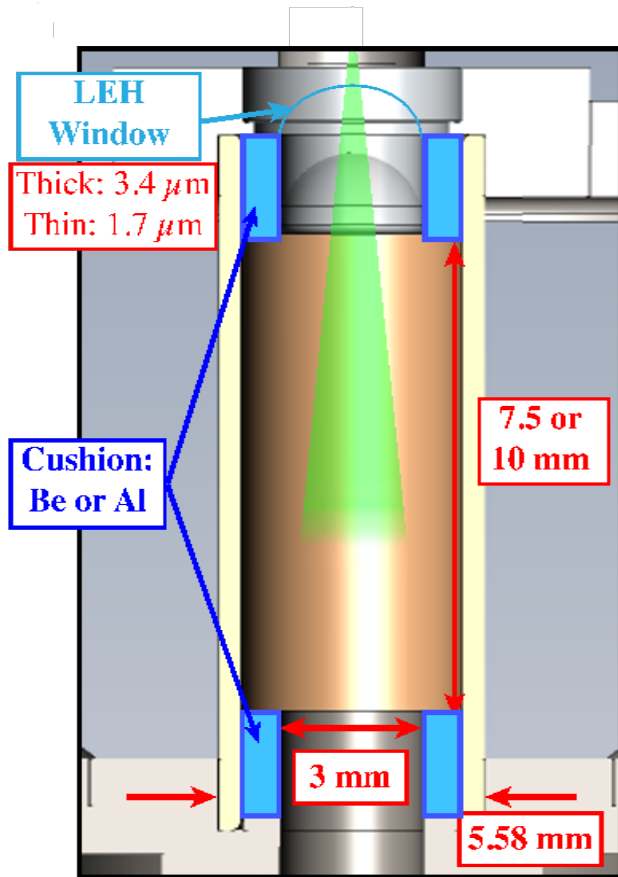
Equal cushion scrape-off mass

$$f_C^{\text{Al}} = \frac{1}{3} f_C^{\text{Be}}$$

Equal cushion scrape-off volume

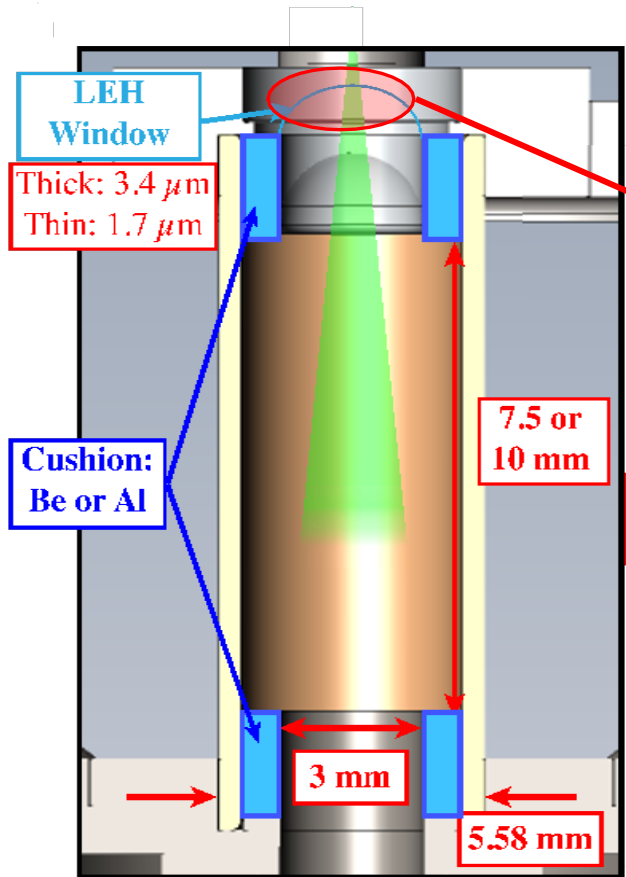
$$f_C^{\text{Al}} = \frac{1}{2} f_C^{\text{Be}}$$

# Summary of contributions from the three potential sources of mix



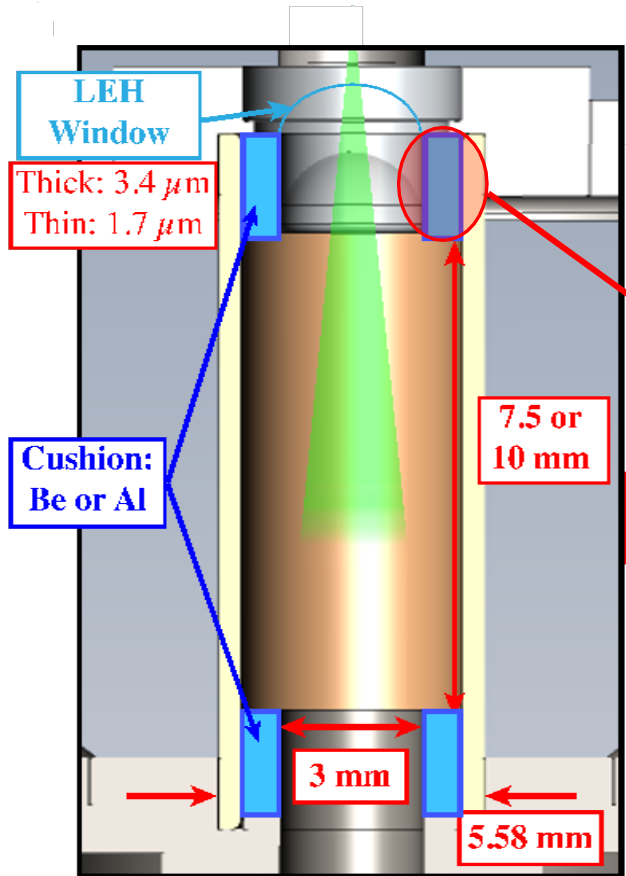
	Aluminum Cushion at %	Beryllium Cushion at %	mass %
Window	0.5 %	0.5 %	1.8 %
Cushion	0.57 %	1.5 %	6.7 %
Liner	2.6 %	2.6 %	12 %

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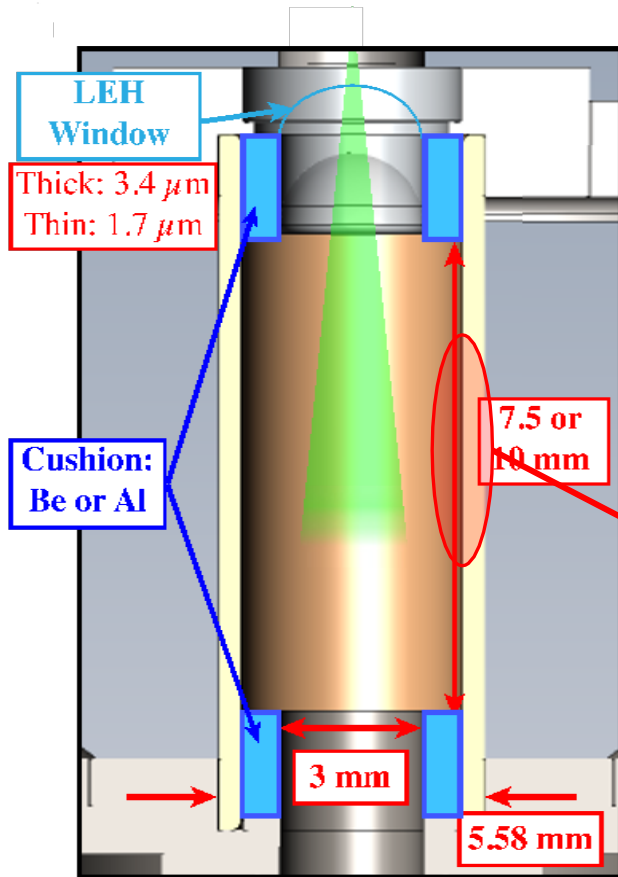
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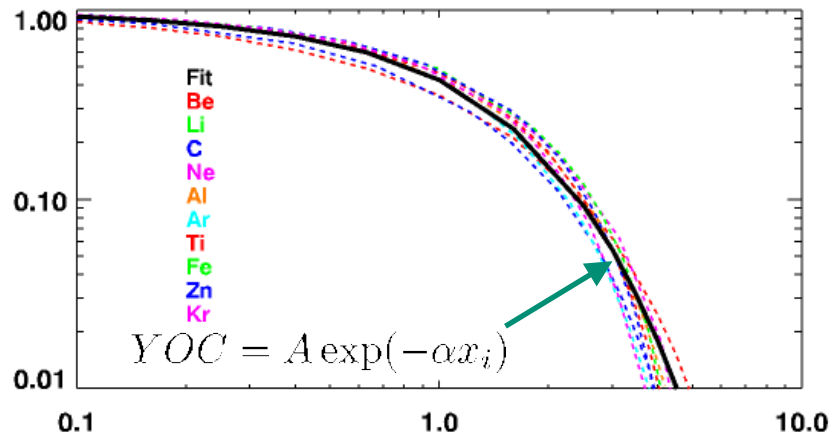
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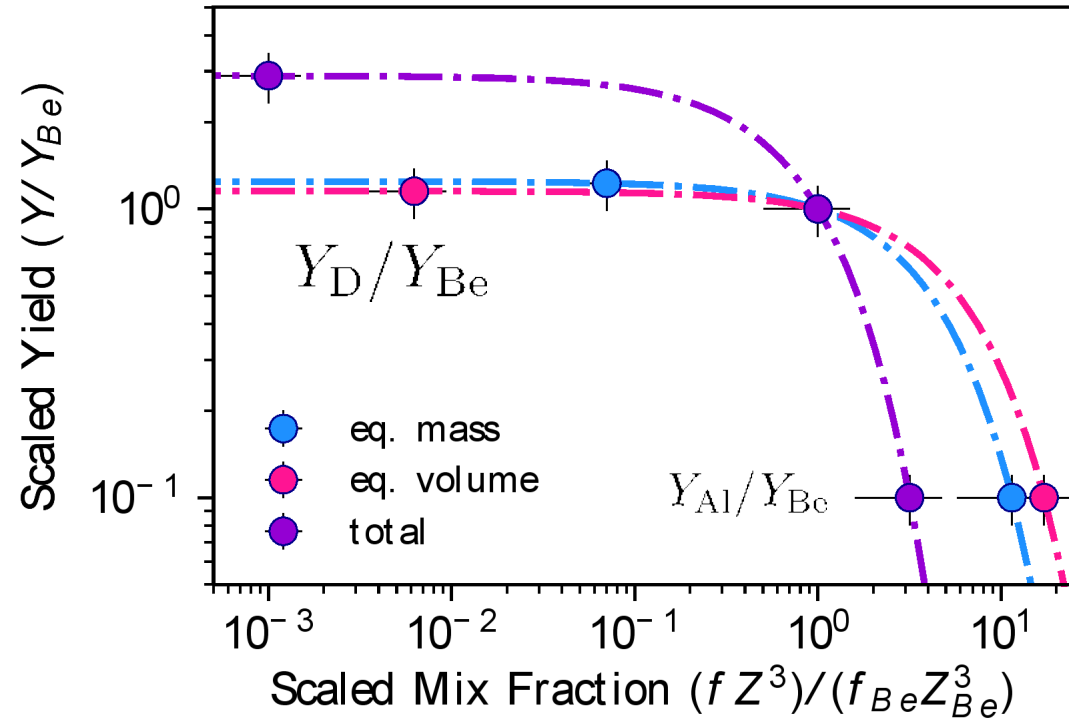
- When cushions are made of Al, they overwhelmingly dominate the degradation
- Liner accounts for >50% of the mix (by atom)
- Simple  $Z^3$  scaling suggests liner mix and window mix are comparable in terms of losses at stagnation
- Window mix is almost certainly worse than liner mix since it is introduced earlier

# How much impact does the observed mix fraction have on target performance?



$$x_i = (f_i Z_i^3) / (f_{Be} Z_{Be}^3)$$

$$Y_i / Y_{Be} = A \exp(-\alpha x_i)$$



- Using calculations for pre-mix YOC from Slutz et al. we back out the trend under various assumptions
- We find that replacing the inferred cushion mix with D gives only 15—25% increase in yield
- Removing the entire observed effective mix fraction gives ~3x increase in yield
- Suggests that Be cushion mix in thin window, tall target, unconditioned beam case is not severely limiting performance, but overall mix is

# Conclusions and Future work



- We find that mix is a significant factor in determining target performance
  - When the cushion is made of Be instead of Al yield was increased by ~10x, ion temperature by ~40% and pressure by ~40%
- Mix from the interaction with the laser (cushion + window) accounts for <50% of the observed total
- Here we have inferred bulk averaged quantities, but we know there is significant variation along the stagnation column
  - We are undertaking a detailed analysis of the data that attempts to account for 2D and 3D variations using the Bayesian Analysis\*
  - We are working on incorporating 1D neutron imaging into the analysis\*\*
  - A high fidelity nuclear burn history measurement would be a valuable addition
- We expect that mix from different sources will be distributed differently. We will address the *radial* and axial distributions of mix as part of the ongoing effort

\*NP11.00138: Patrick Knapp (Wednesday)  
\*\*GP11.00094 : Jeremy Vaughan (Tuesday)  
\*\*GP11.00132: Dave Ampleford (Tuesday)