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Assessing the Limits of Predictive Uncertainty in Seismic Event Discrimination Using Bayesian Neural Networks

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Traditional NNs are great at predicting



But not so much at **not** predicting

- Overconfident predictions makes it difficult to trust models
- Classification: Tuning of label threshold may help, but there is no other criteria to distinguish False Positives from True Positives.
- Regression: How can we establish if a prediction is wrong?
- **The goal of this is to determine how we can prevent irresponsible predictions?**

Bayesian NNs might provide an answer



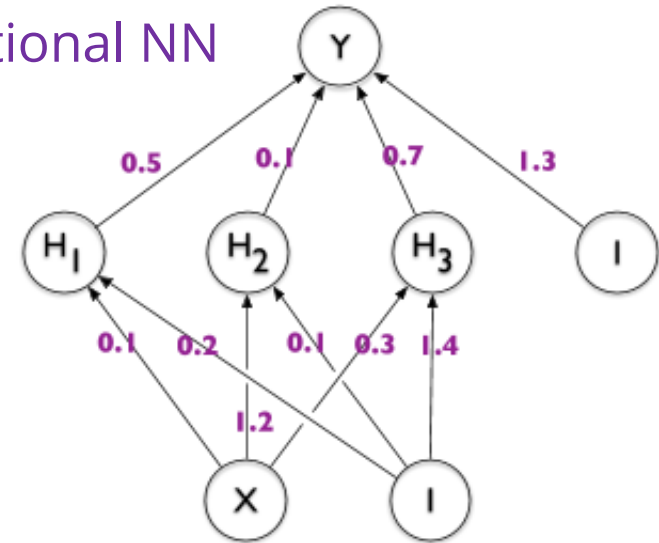
Obtain a distribution of weights

- Allows for sampling different models, resulting in varying predictions

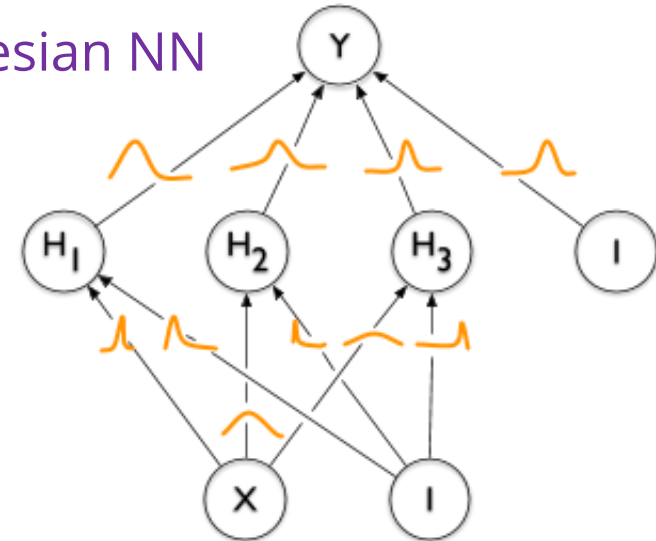
Therefore, obtain a distribution of predictions

- Standard deviation of prediction → confidence on prediction

Traditional NN



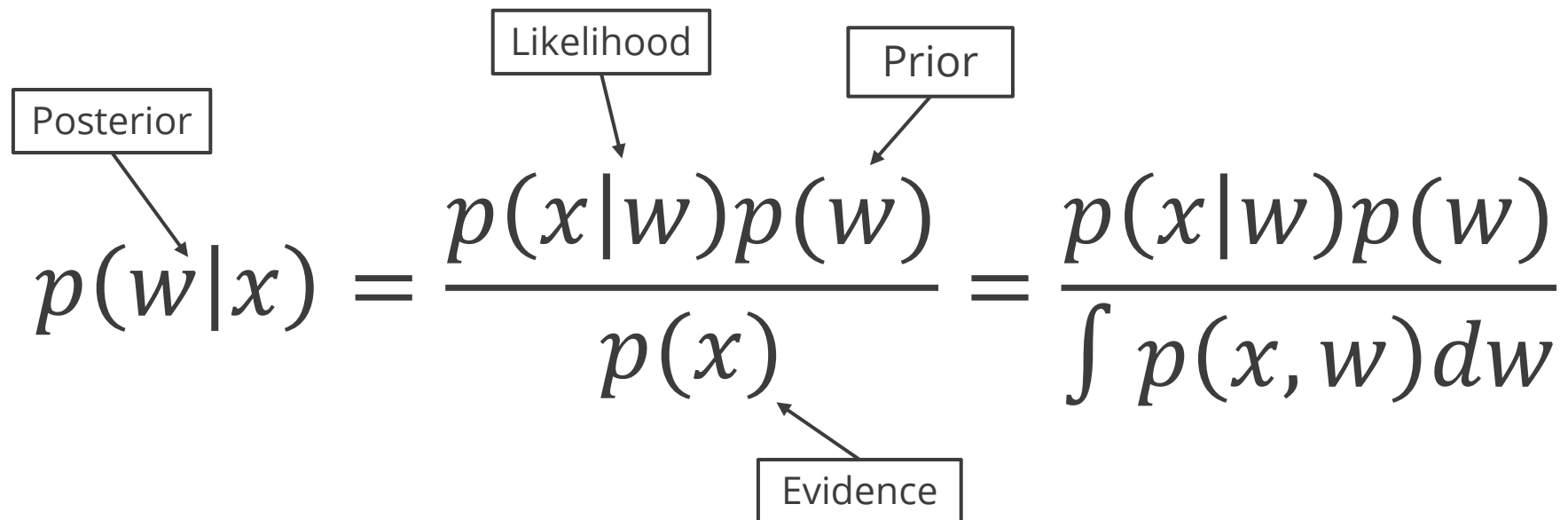
Bayesian NN



Suppose we want to find a model:

$$f(x_0, w) = x_1$$

Want to know what the parameters w are:



The diagram shows the equation for the posterior probability $p(w|x)$ with labels and arrows indicating the components:

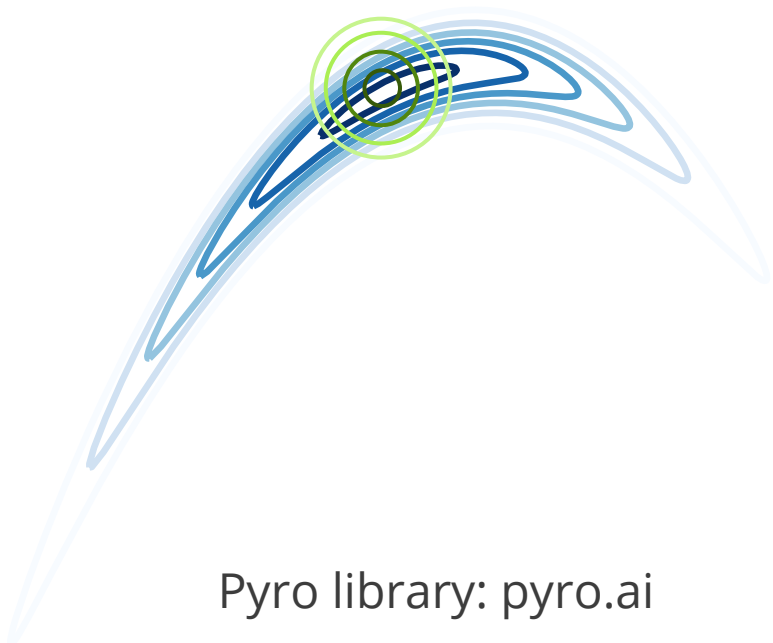
- Posterior**: A box with an arrow pointing to $p(w|x)$.
- Likelihood**: A box with an arrow pointing to $p(x|w)$ in the numerator of the first fraction.
- Prior**: A box with an arrow pointing to $p(w)$ in the numerator of the first fraction.
- Evidence**: A box with an arrow pointing to $p(x)$ in the denominator of the first fraction.

$$p(w|x) = \frac{p(x|w)p(w)}{p(x)} = \frac{p(x|w)p(w)}{\int p(x, w)dw}$$

Need posterior, but Evidence is hard to calculate in high dimensions

Variational Inference (VI)

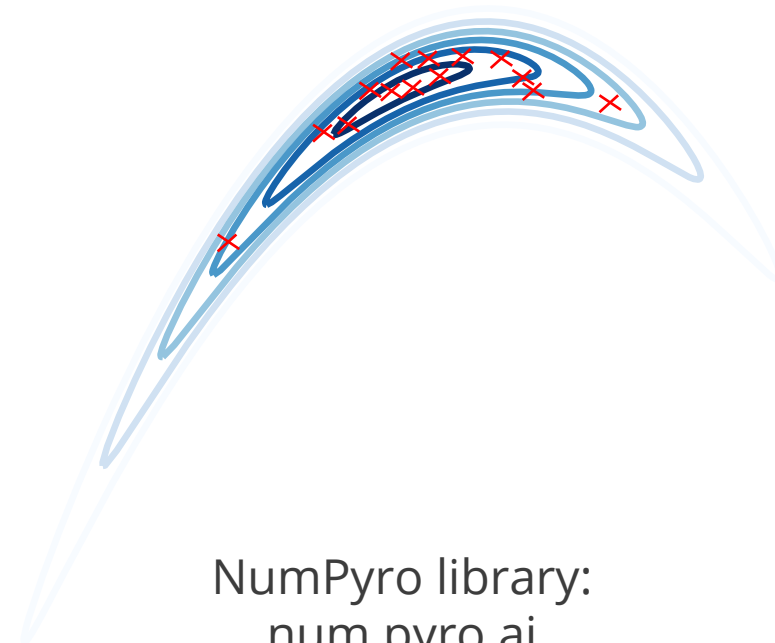
- Use a family of distributions $q(w)$ to find the one that best approximates the posterior $p(w|x)$



Pyro library: pyro.ai

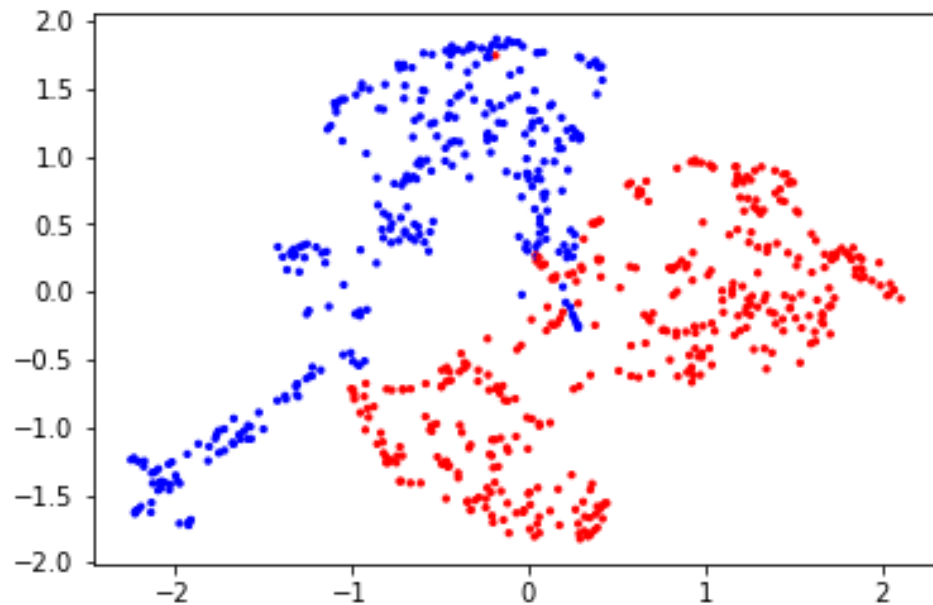
Markov Chain Monte Carlo (MCMC)

- Find the posterior $p(w|x)$ by drawing parameter samples and testing them against the data



NumPyro library:
num.pyro.ai

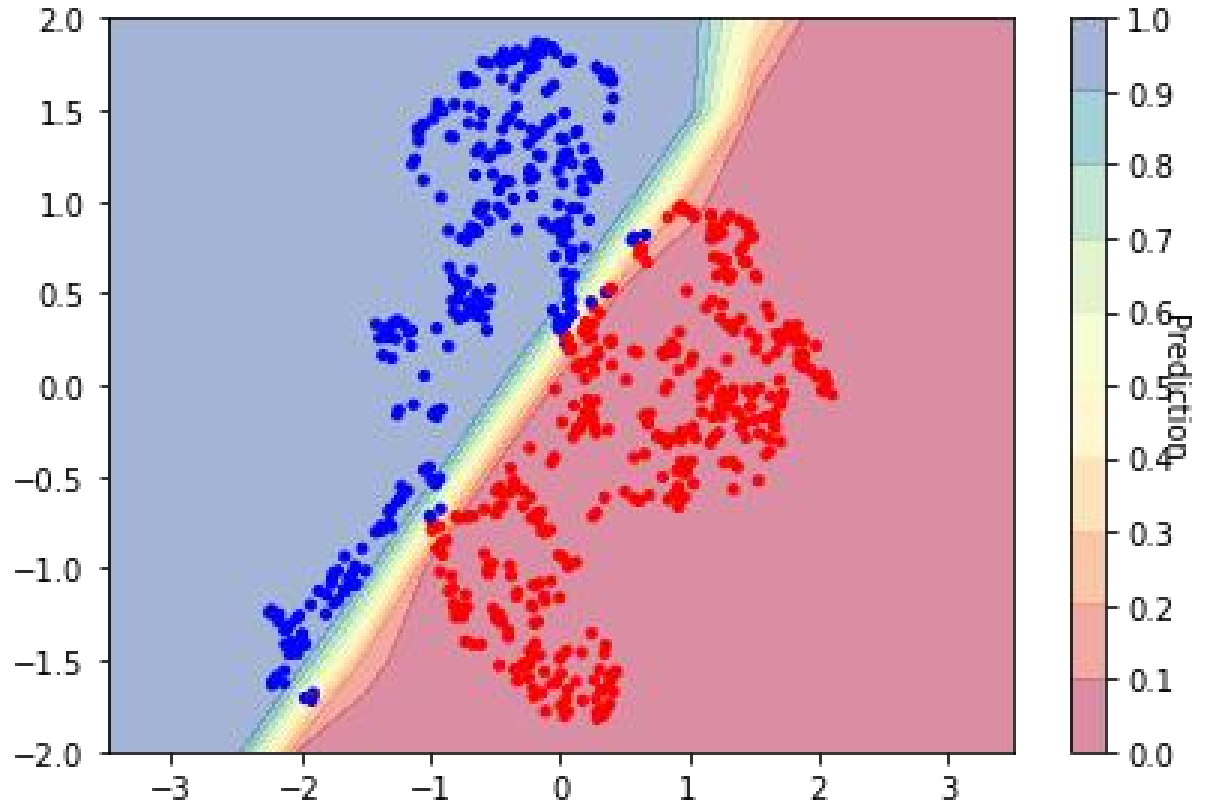
Dataset I: Exploratory Dataset



2D mapping of seismic data
(quarry blasts vs earthquakes)

Same architecture as used in previous SSL work we've done:

- Feedforward Network with 3 layers
- Tanh activations



95% acc

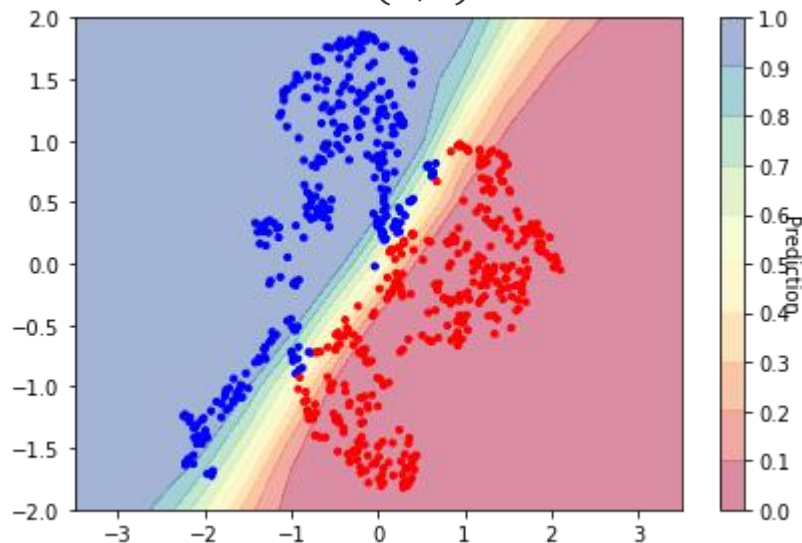
Fit a standard NN using gradient descent

- Naturally, easiest way to separate the data set is a line

VI: Quick to train, similar results, more info

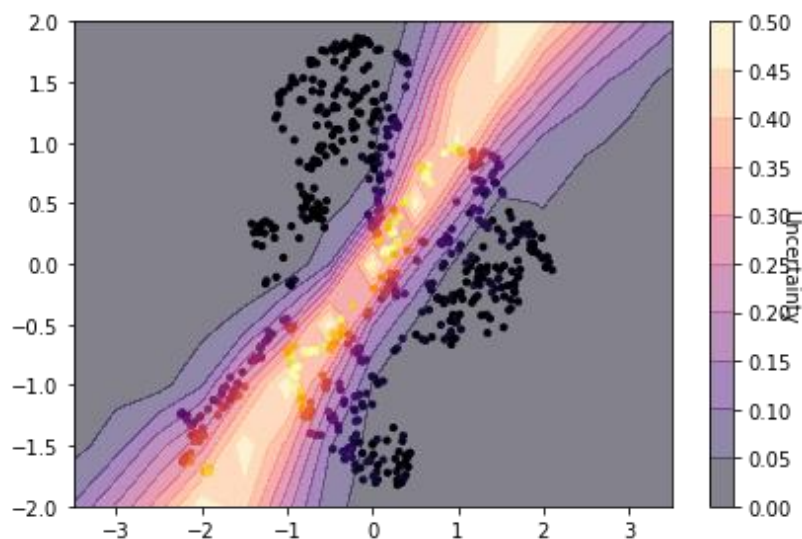
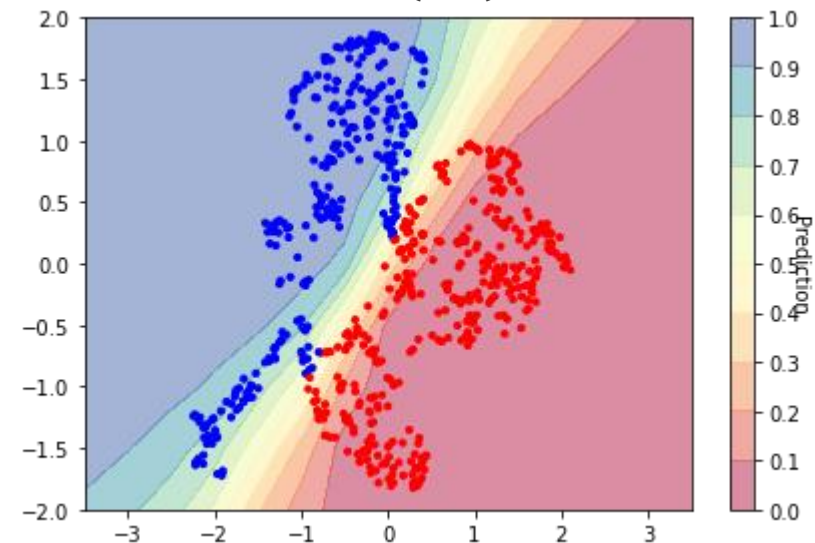


$\mathcal{N}(0,1)$



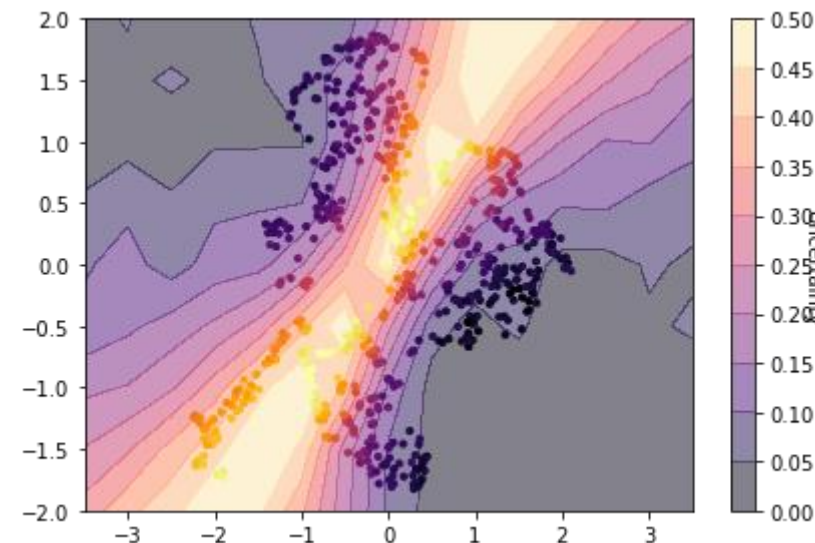
We can obtain a distribution of predictions for an input, allowing to obtain a mean prediction (upper) and a standard deviation (lower)

$\mathcal{N}(0,5)$



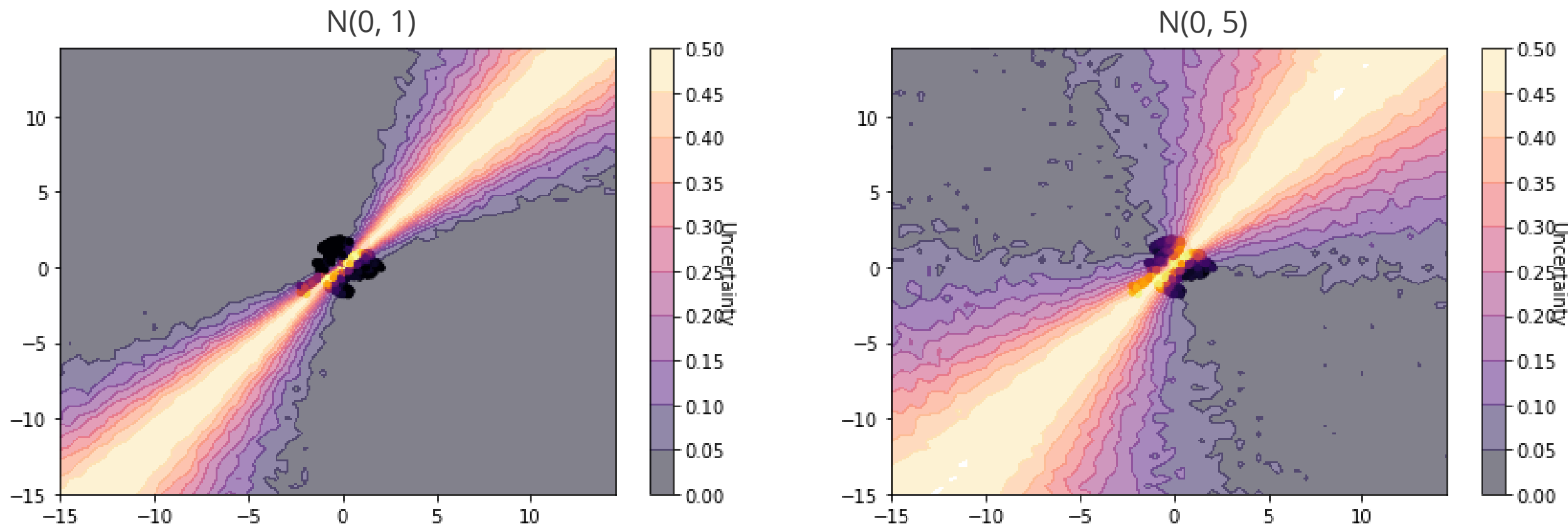
92% acc

Prior choice matters:
Larger variance explores a larger model space, resulting in a wider/less "steep" decision boundary



88% acc

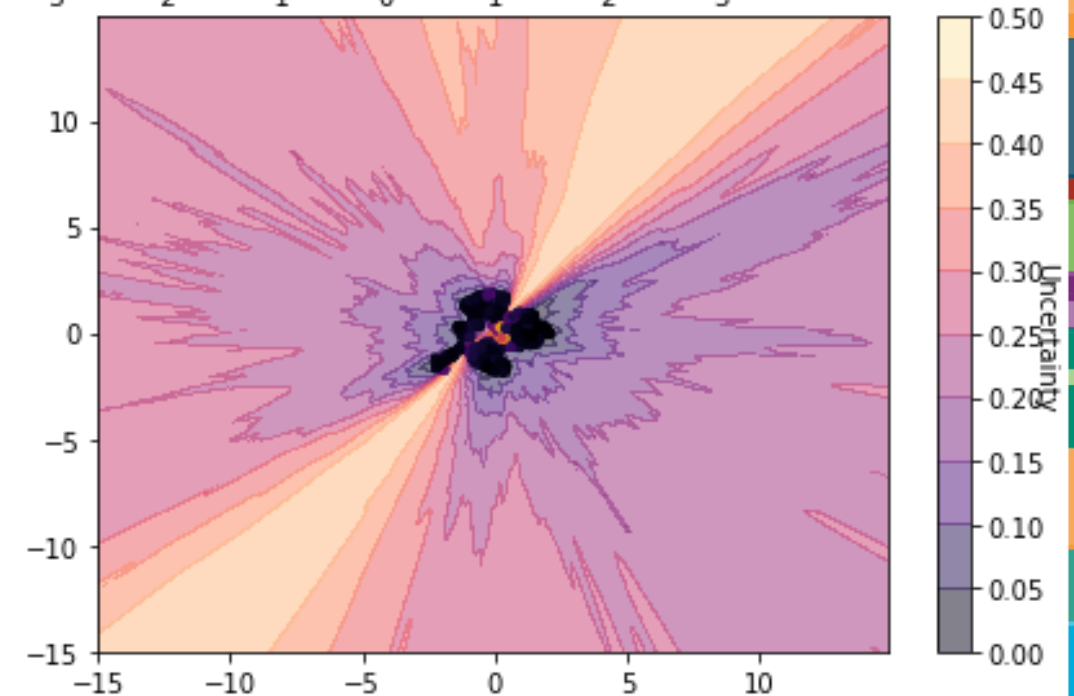
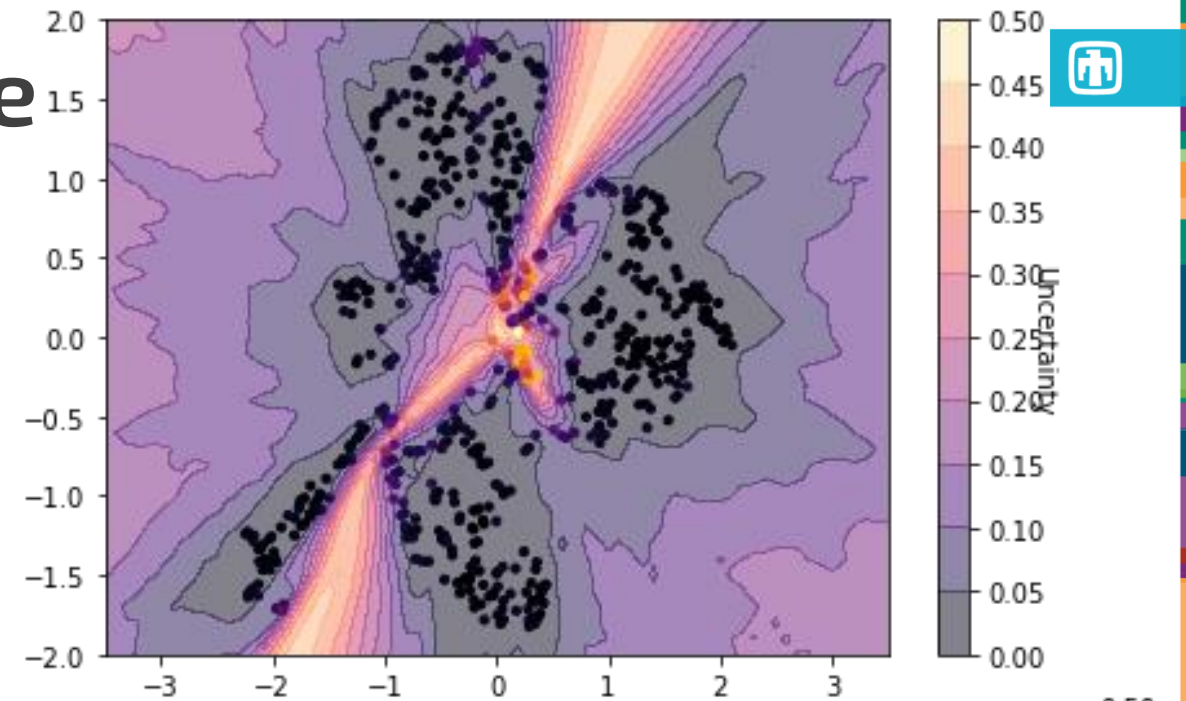
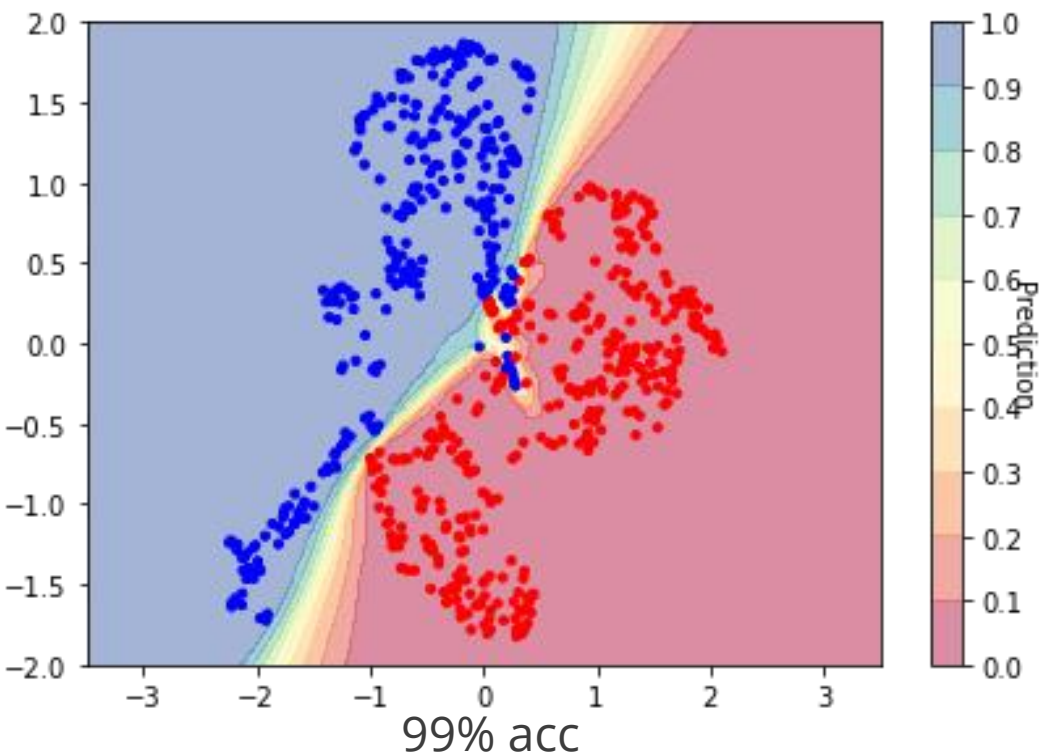
Models still seem overconfident though



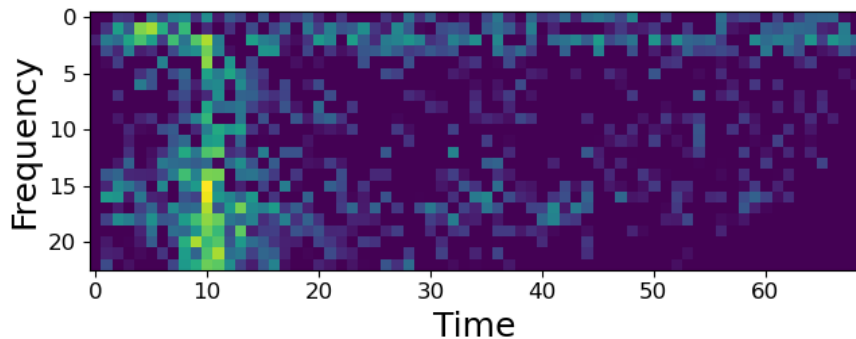
Notice the lack of uncertainty in data-absent regimes

MCMC: Great and sensible results, but costly

- Captures finer details of data distribution
- Only confident where data is existent
- Long training time: 6 hrs to train vs 1 hr for VI



Dataset II: Seismic Waveform Spectrogram Features



Conv Layers



4096-dim feature space



Feed Forward Layers



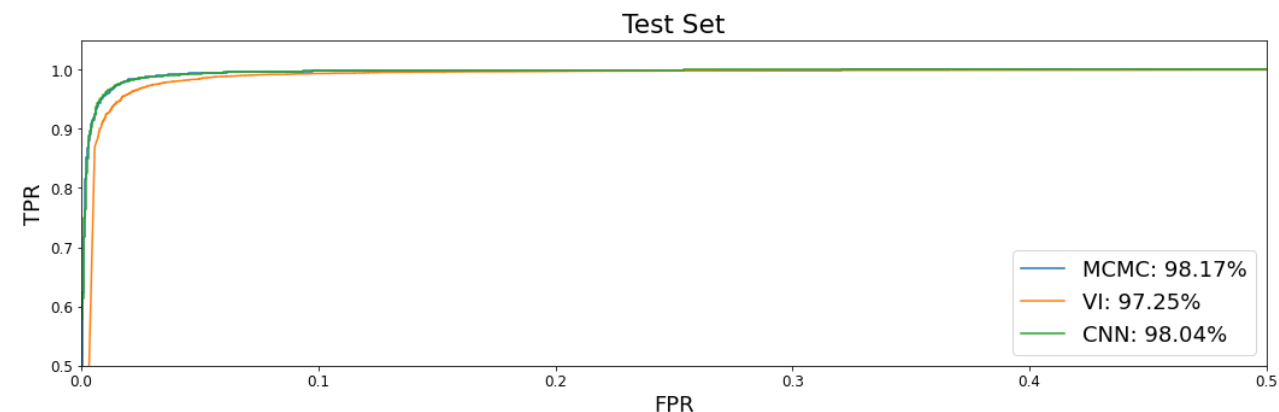
Output



Convert these
set weights into
a distribution

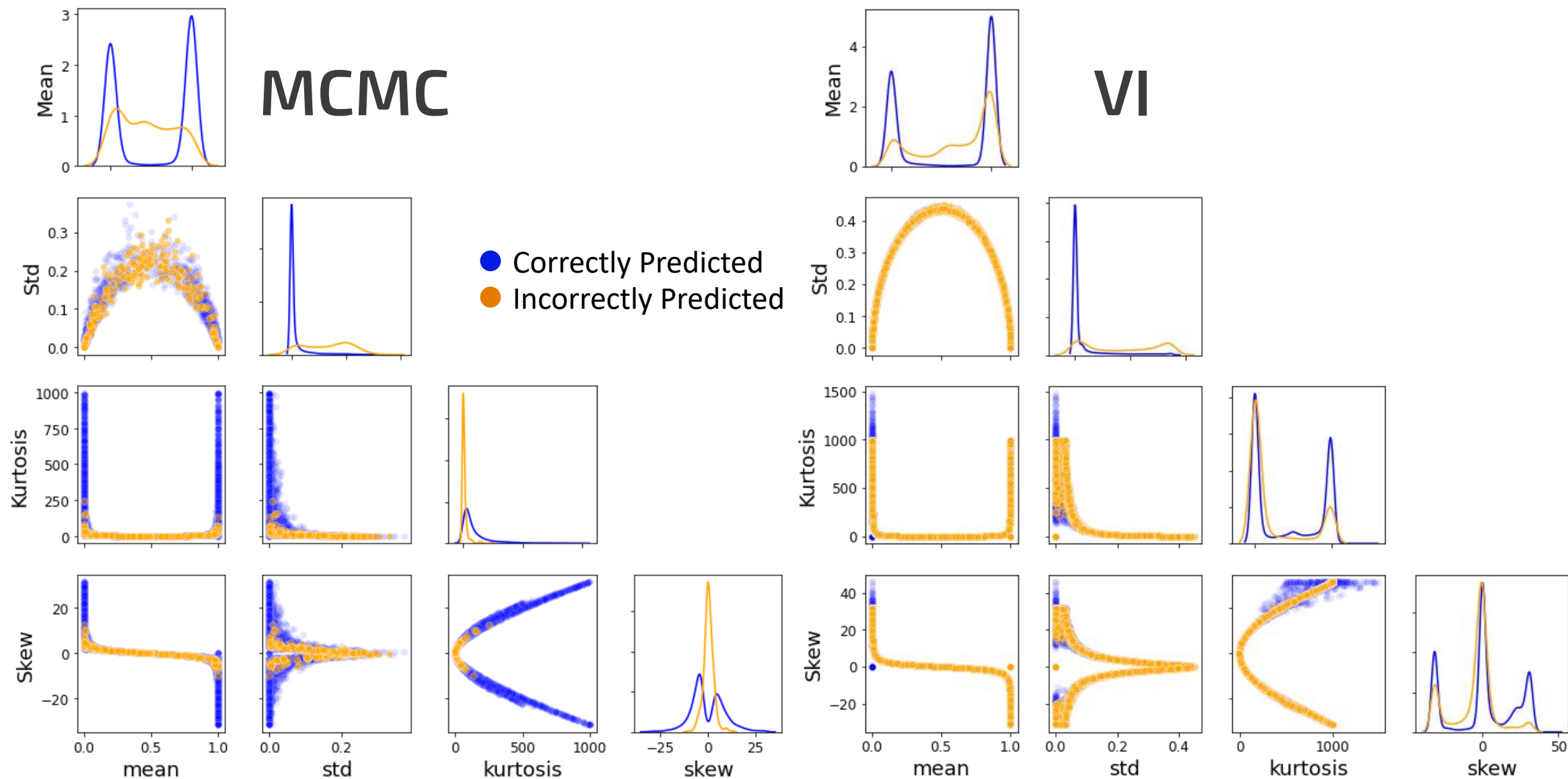
Architecture: VGG Conv NN

- Quarry blasts vs local earthquakes
- Training the whole network in a Bayesian framework would present computational and engineering complexities
- Use Bayesian Inference on only part of the network



- Model performance is still on-par with original baseline despite transferred feature space

Possibility for exploiting other distribution descriptors



Conclusion and Next Steps



- So far MCMC has generated more powerful models with more nuanced characterizations of uncertainty
 - The cost is in training time to generate the model (can make or break depending on model or data sample size)
- Currently developing a testbed to compare other methods which generate distributions of predictions
 - MCMC, VI, Bayesian Dropout and Ensemble Methods
- Evaluate performance under a variety of OOD cases
 - Simplest case: Artificial sinusoidal wave
 - More complexity: Seismic events of different nature (e.g. mining induced events, noise)