



Sandia
National
Laboratories

Probing Structural and Magnetic Phase Changes in the Shock Response of Iron with Molecular Dynamics

Svetoslav Nikolov, Julien Tranchida, Attila Cangi,
Kushal Ramakrishna, Mani Lokamani, Mitchell
Wood

APS March Meeting, 2022



Sandia National Laboratories is a multimission laboratory managed and operated by National Technology & Engineering Solutions of Sandia, LLC, a wholly owned subsidiary of Honeywell International Inc., for the U.S. Department of Energy's National Nuclear Security Administration under contract DE-NA0003525.

Background & Motivation

Behavior of metals under HED conditions is difficult to predict

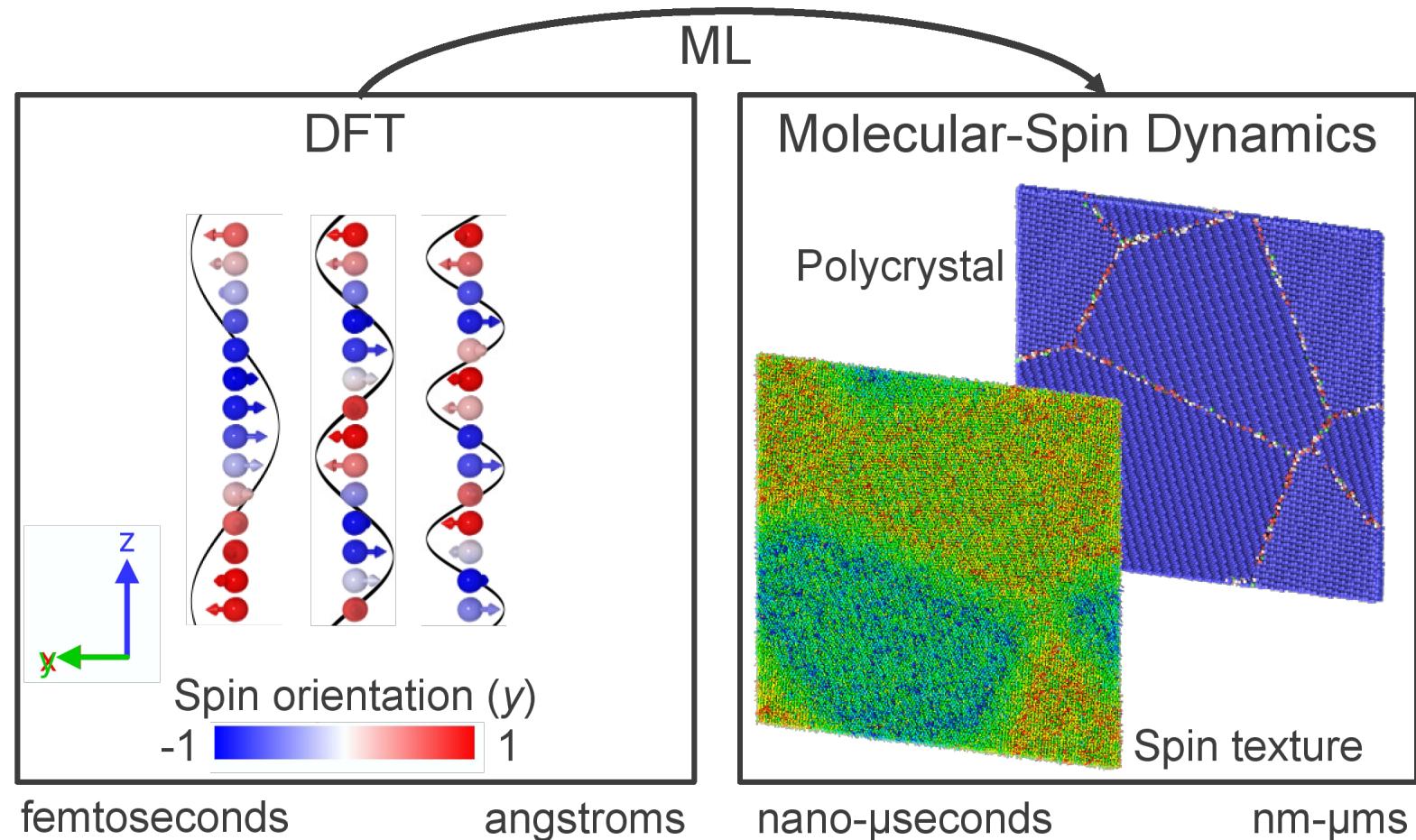
- Geophysics, fusion energy science, etc.
- Accounting for magnetic degrees of freedom is important

Ab-initio resolution of magnetic DOF is ideal

- Spatial and temporal restrictions

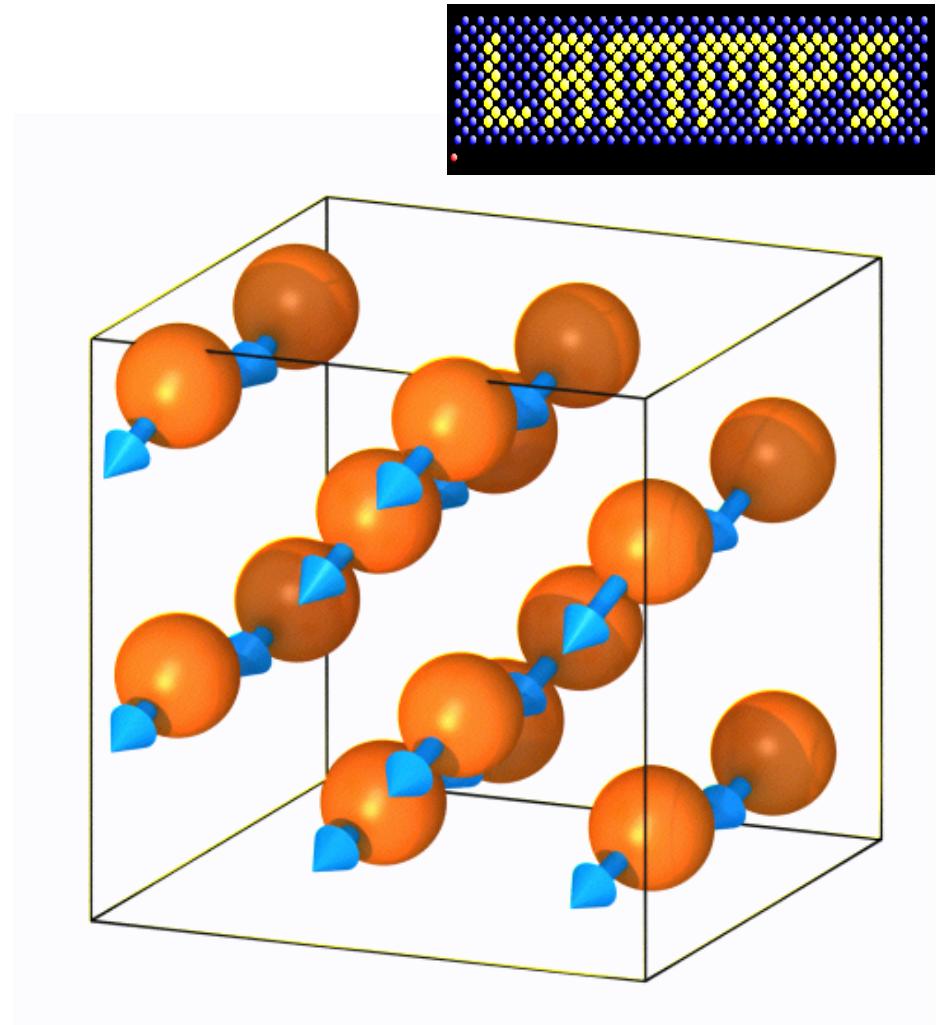
Molecular-Spin Dynamics models can be trained on DFT data

- Applied to study emergent material behavior



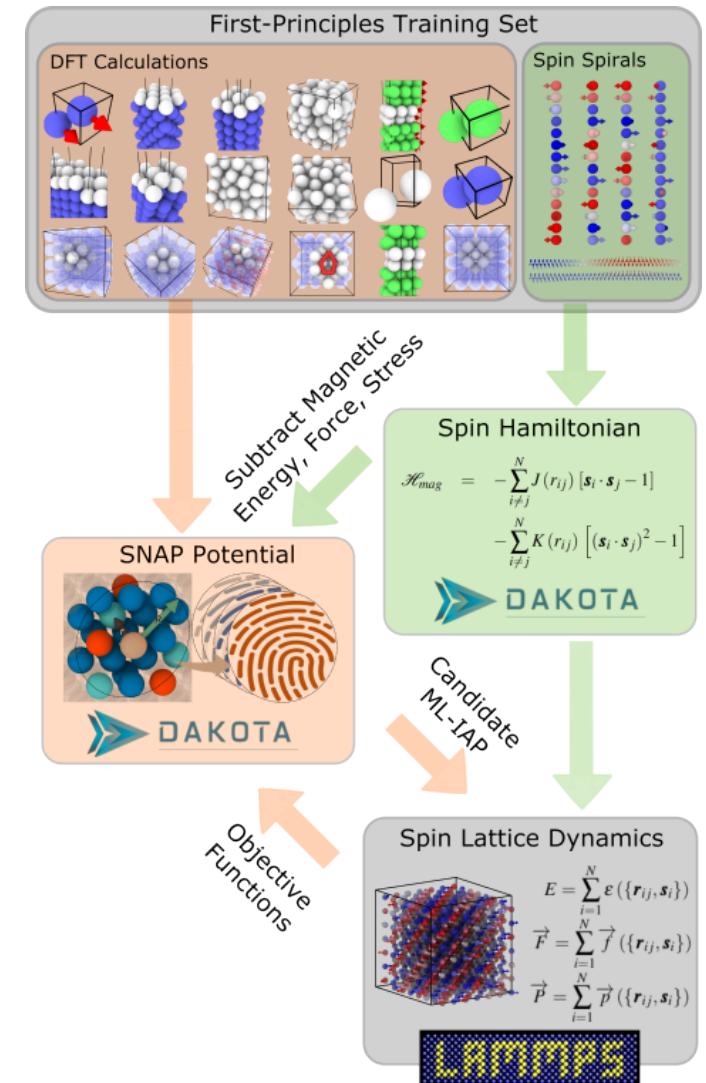
Molecular-Spin Dynamics

- Molecular Dynamics
 - Atoms interact via nonmagnetic interatomic potential, $U(\mathbf{R})$
 - $\mathcal{H}_{MD} = \sum_i \frac{\mathbf{p}_i^2}{2m} + U(\mathbf{R})$
- Spin Dynamics
 - Atoms interact via exchange function which conserves total angular momentum
 - $\mathcal{H}_s = -\sum_{i,j}^N J_{ij}(\mathbf{R})[\vec{s}_i \cdot \vec{s}_j - 1] - \sum_{i,j}^N K_{ij}(\mathbf{R})[(\vec{s}_i \cdot \vec{s}_j)^2 - 1]$
 - Additional physics can be easily incorporated
 - Magnetocrystalline anisotropies, external magnetic fields, longitudinal fluctuations, etc.
- Molecular-Spin Dynamics
 - $\mathcal{H}_{MSD} = \mathcal{H}_l + \mathcal{H}_s = \sum_i \frac{\mathbf{p}_i^2}{2m} + U(\mathbf{R}) - \sum_{i,j}^N J_{ij}(\mathbf{R})[\vec{s}_i \cdot \vec{s}_j - 1] - \sum_{i,j}^N K_{ij}(\mathbf{R})[(\vec{s}_i \cdot \vec{s}_j)^2 - 1]$ (Implemented in LAMMPS)



ML Framework for α -Fe

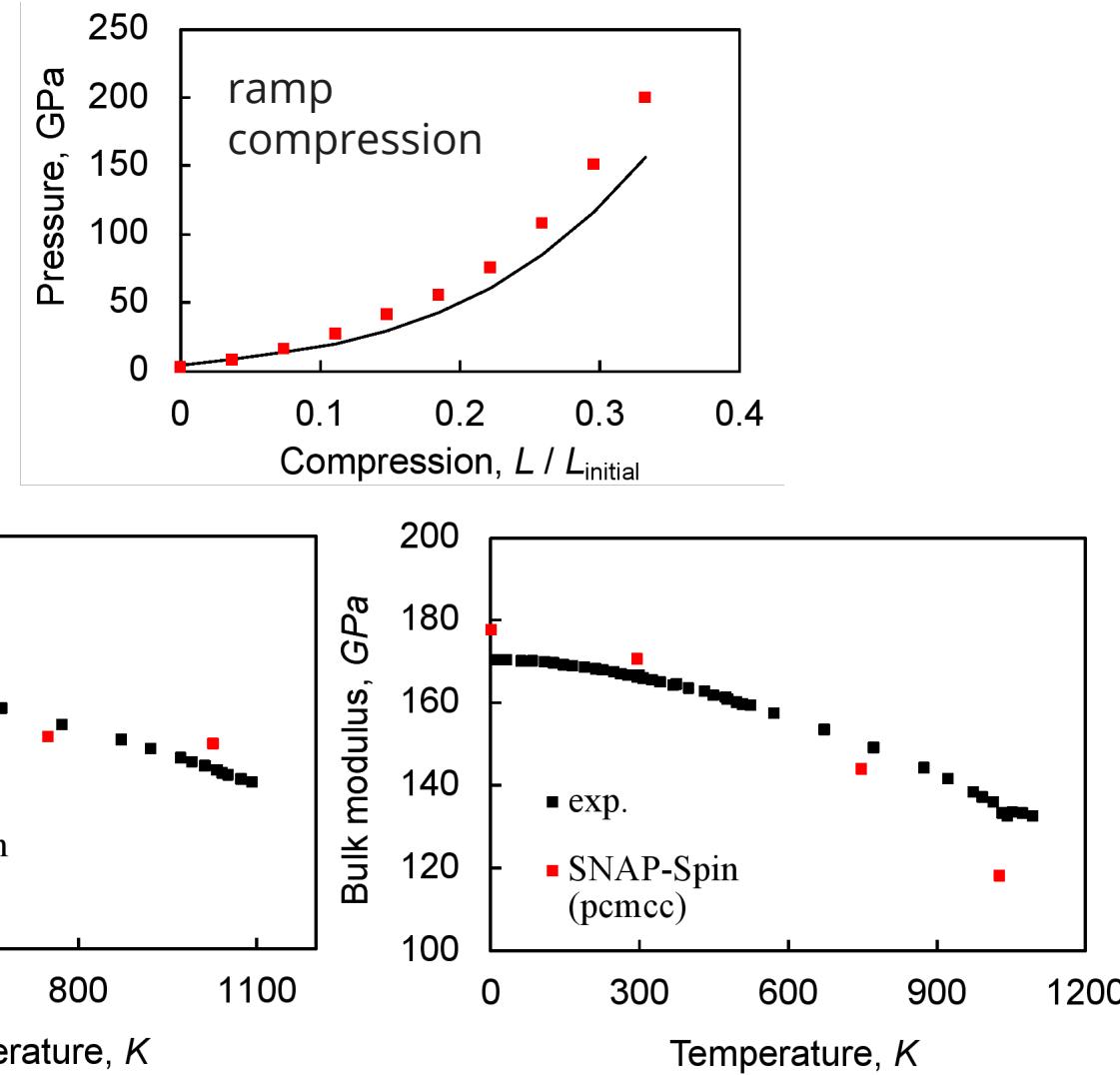
- 1) Generate ab-initio dataset for Fe (VASP)
 - Fe data generated for 0 - 1200K and 0 - 13 Gpa
 - Spin spiral data generated for different degrees of compression
- 2) Use genetic algorithm (GA) to parameterize spin Hamiltonian using spin spiral data
- 3) Subtract magnetic energies/forces/stress from DFT Fe data and train interatomic potential, $U(R)$, using GA
 - $U(R)$ built using spectral neighbor analysis potential (SNAP)
 - $E_{SNAP}^i = \beta_0 + \beta \cdot \mathbf{B}^i$ and $F_j^{SNAP} = -\beta \cdot \sum_{i=1}^N \frac{\partial \mathbf{B}_i}{\partial \mathbf{r}_j}$
- 4) Evaluate candidate on predetermined set of objective functions (OFs)
 - Using candidate SNAP potential and parameterized spin Hamiltonian
- 5) Continue GA until desired OFs accuracy is reached



Shock Response of MSD Model

- Trained SNAP-Spin model on high pressure / temperature data
- Includes bcc / fcc / hcp collinear spin DFT (VASP) data
 - Up to 400 GPa and 6500K

0 K Objective Functions				
	MSD	Exp/DFT	Units	Error
C_{11}	243.3	239.6	GPa	1.5%
C_{44}	111.3	120.8	GPa	7.9%
Bulk modulus	177.8	169.6	GPa	4.8%
$(C_{11} - C_{12}) / 2$	42.7	51.9	GPa	17.7%
Poisson ratio	0.389	0.36	-	8.1%
FCC trans. press.	25.644	19	GPa	35%
HCP trans. press.	15.487	13	GPa	19%



Shock Response of MSD Model

- Longitudinal changes in magnetic vector

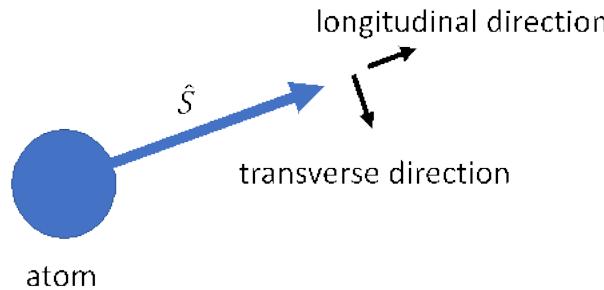
- $$\mathcal{H}_{Landau} = \sum_i (AS_i^2 + BS_i^4 + CS_i^6)$$

- \hat{S} → spin vector of atom

- $$\hat{S} = \frac{-\hat{M}}{g\mu_B} = S_x\hat{i} + S_y\hat{j} + S_z\hat{k}$$

- $$S_i = \|\hat{S}\| = \sqrt{(S_x)^2 + (S_y)^2 + (S_z)^2}$$

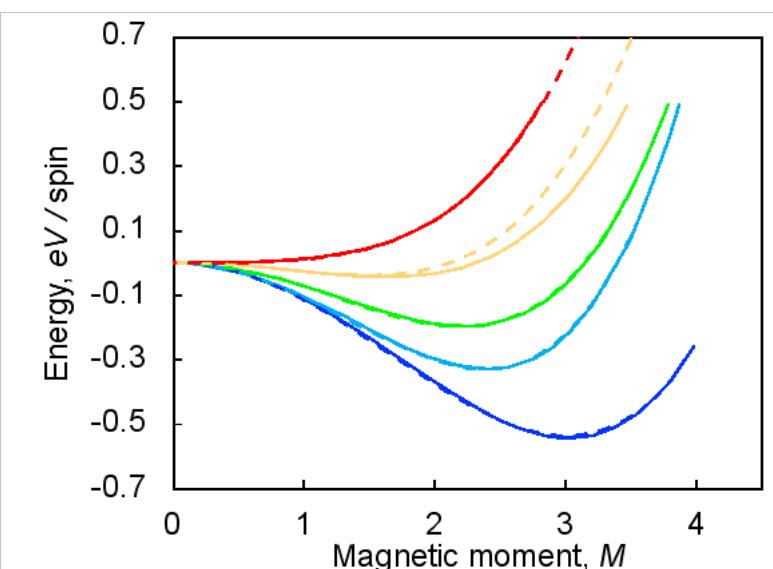
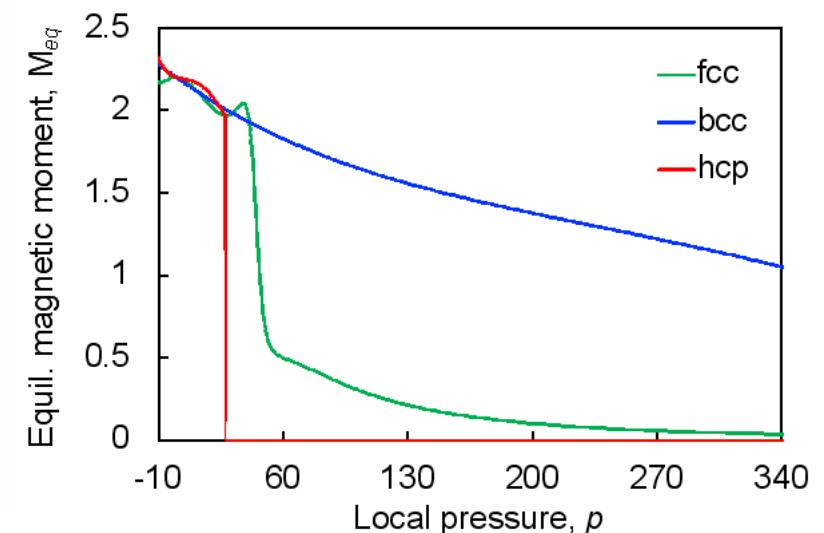
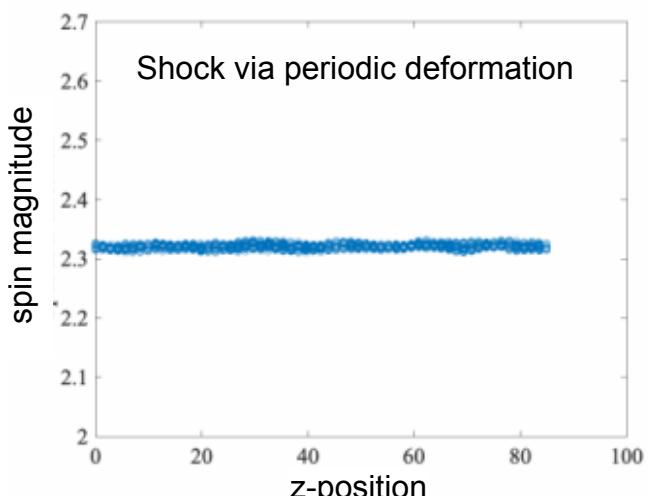
- $A(p), B(p),$ and $C(p)$ are fitted to noncollinear spin data for iron[†]



- Magnetic moment adjusted on the fly

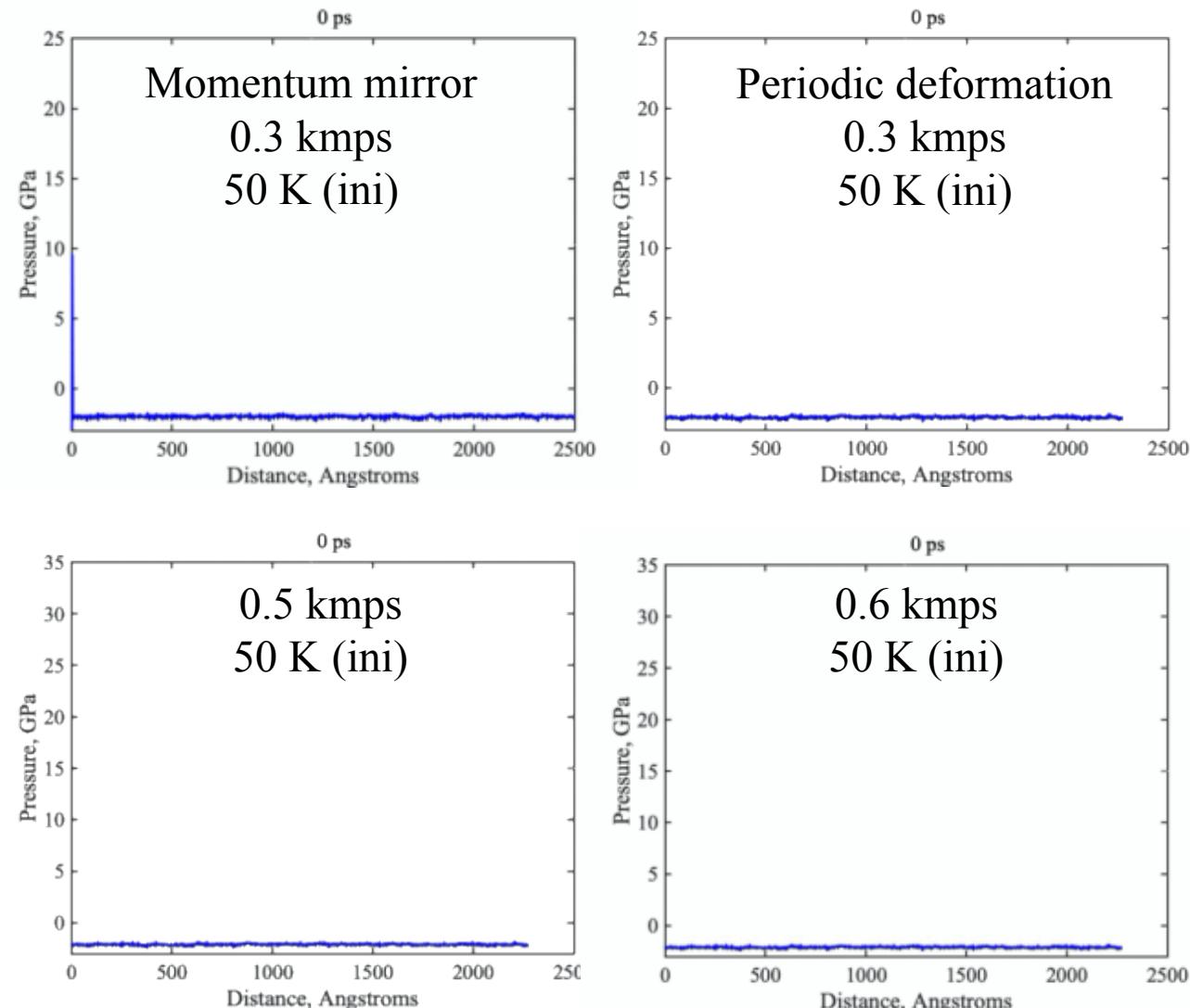
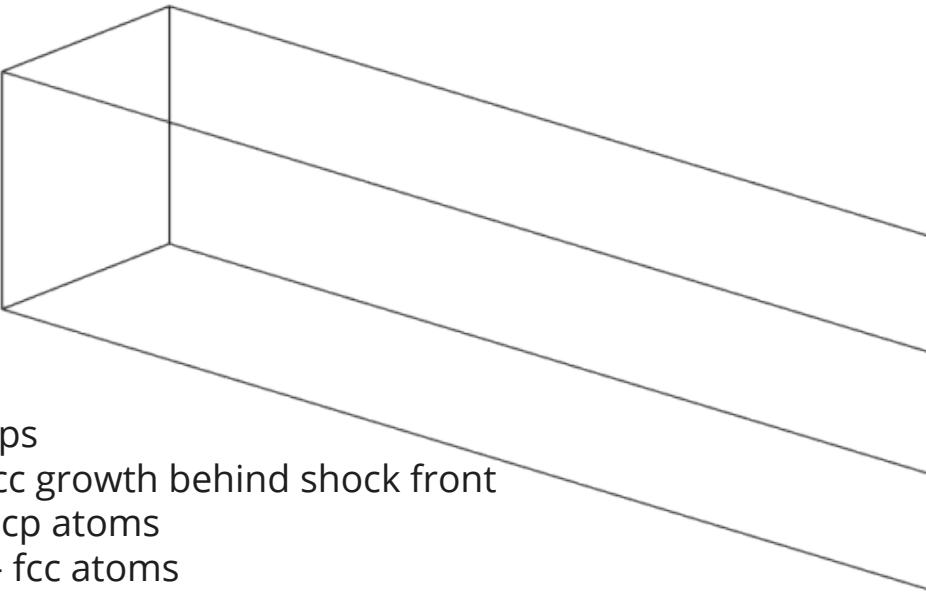
- Based on local pressure & phase

[†]Gambino, Davide, et al. "Longitudinal spin fluctuations in bcc and liquid Fe at high temperature and pressure calculated with a supercell approach." *Physical Review B* 102.1 (2020): 014402.



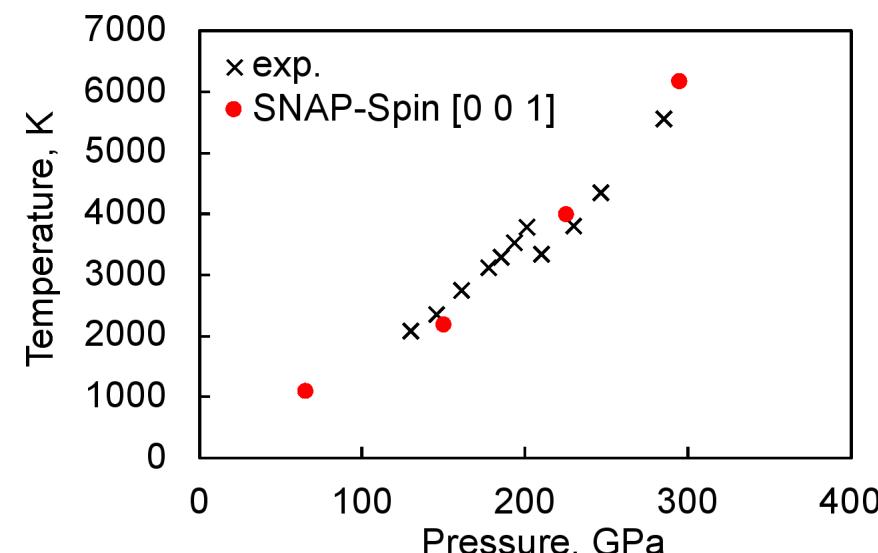
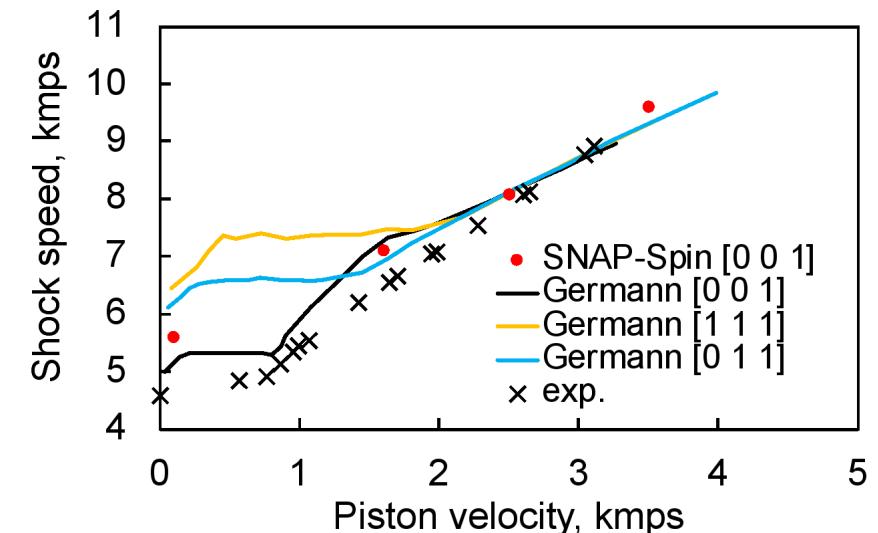
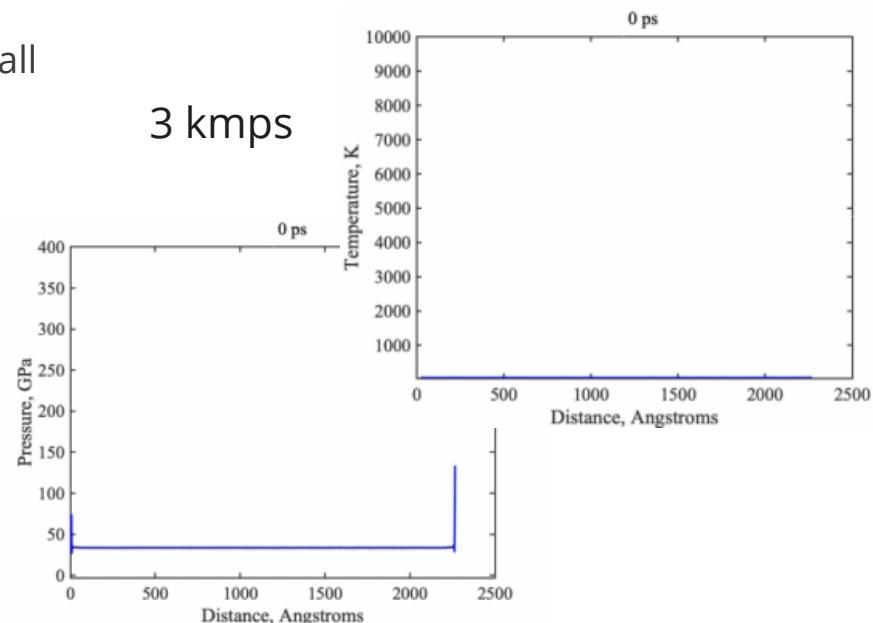
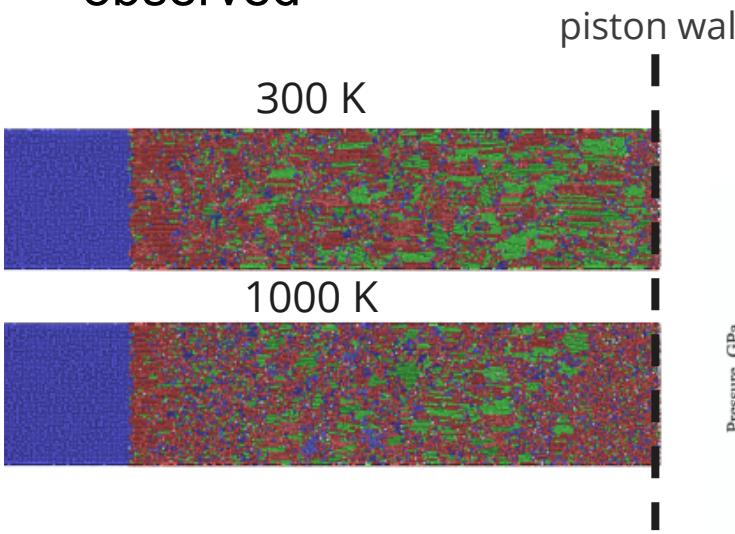
Shock Response of MSD Model

- Tested both two methods to generate shocks
 - Momentum-mirror
 - Uniaxial shrinking of periodic domain
- Response for shocks < 1 kmmps
 - Below 0.6 kmmps no phase transformations detected
 - Dual-wave profile observed for shocks above 0.6 kmmps



Shock Response of MSD Model

- Hugoniot curves for single crystal in good agreement with previous computational results and experiments
- Temperature / pressures in good agreement with experiments
- Potential was tested on 3-3.5 kmmps and good stability was observed



Conclusion

- Illustrated framework for building α -Fe molecular-spin dynamics model from ab-initio data
- Showed impact of different equilibration methods on mechanical response of α -Fe
- Analyzed phonon/magnon spectra and thermal conductivity at corresponding temperatures
 - Good agreement with experiments
 - Able to reproduce acoustic peak shift up to ~ 700 K
- Retrained potential for high temperature / pressure data
 - Good agreement for elastic properties / transition pressures / ramp curve
 - Dual-wave profile observed once bcc begins transforming into hcp phase

