



Probing Structural and Magnetic Phase Changes in the Shock Response of Iron with Molecular Dynamics

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Background & Motivation



Behavior of metals under HED conditions is difficult to predict

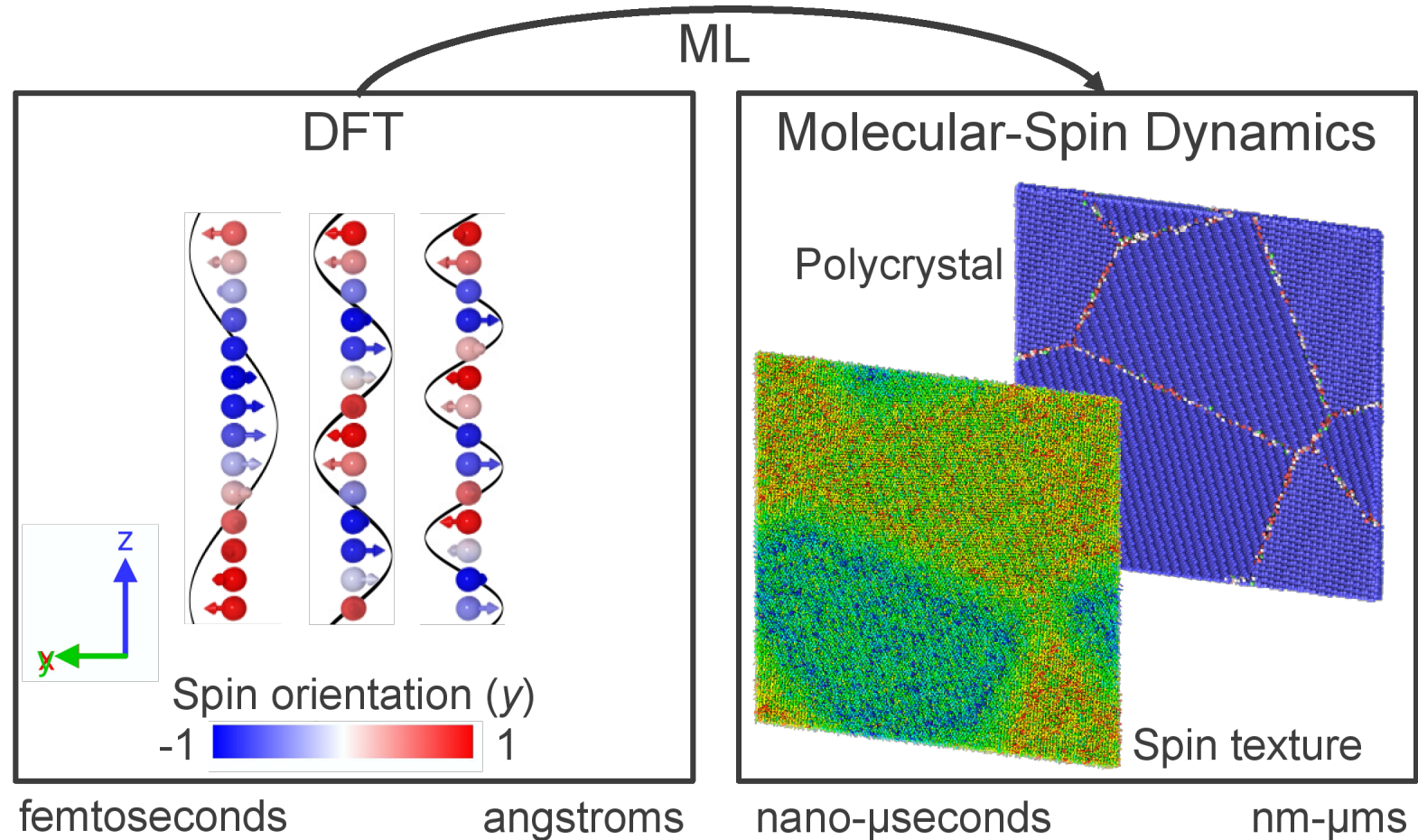
- Geophysics, fusion energy science, etc.
- Accounting for magnetic degrees of freedom is important

Ab-initio resolution of magnetic DOF is ideal

- Spatial and temporal restrictions

Molecular-Spin Dynamics models can be trained on DFT data

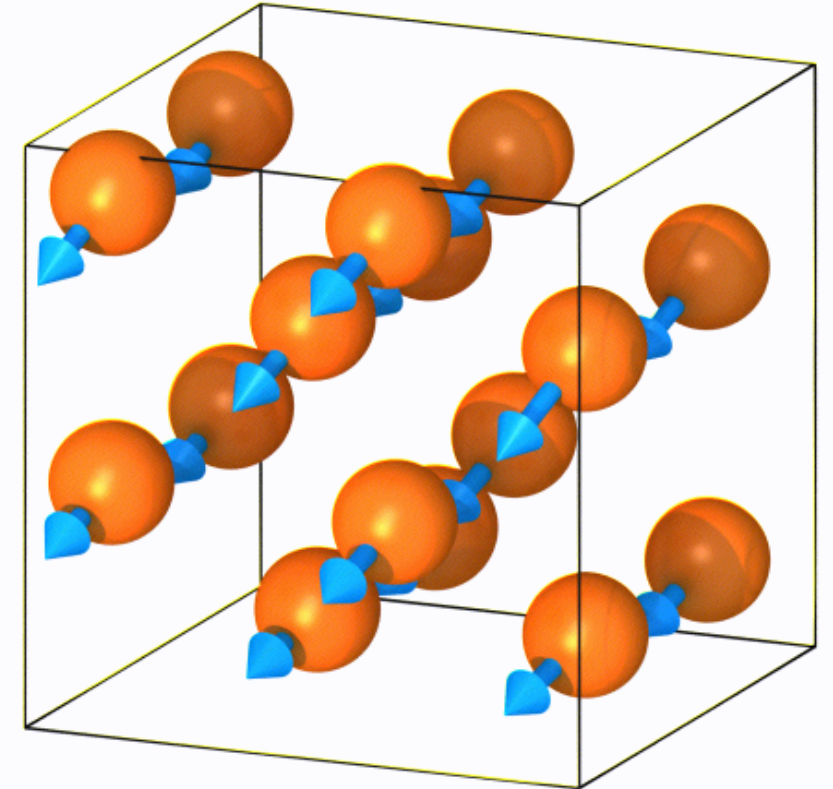
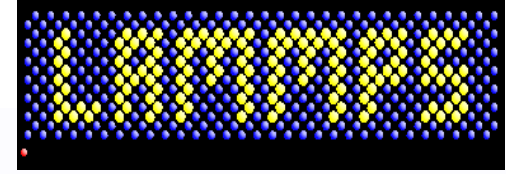
- Applied to study emergent material behavior



Molecular-Spin Dynamics

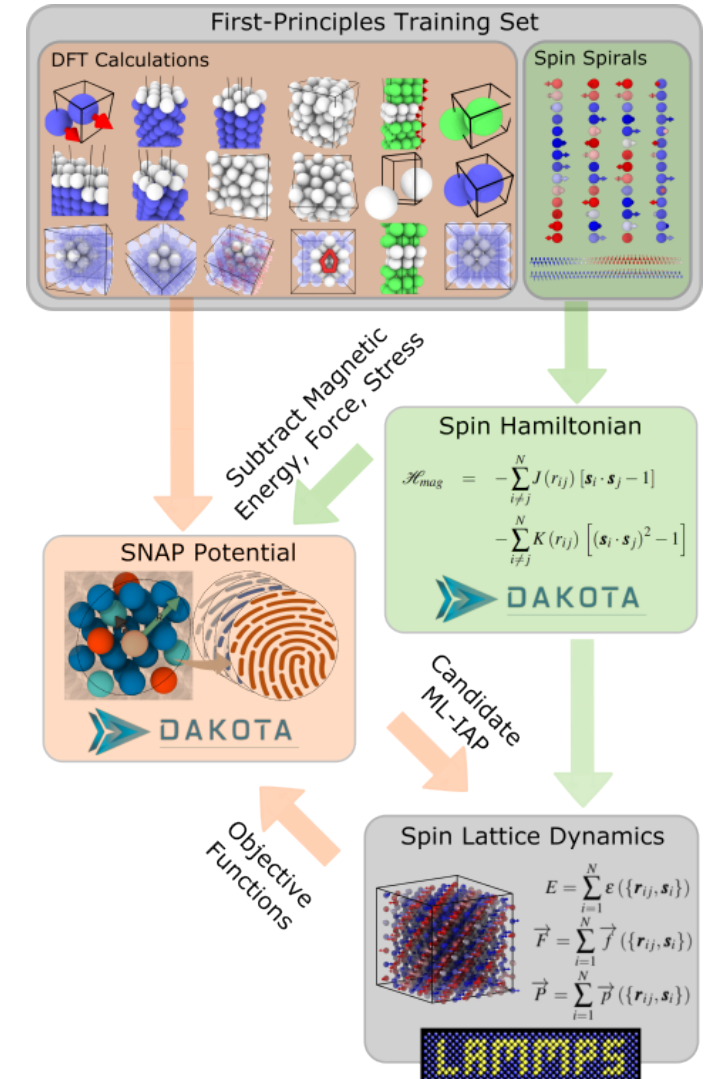


- Molecular Dynamics
 - Atoms interact via nonmagnetic interatomic potential, $U(\mathbf{R})$
 - $\mathcal{H}_{MD} = \sum_i \frac{\mathbf{p}_i^2}{2m} + U(\mathbf{R})$
- Spin Dynamics
 - Atoms interact via exchange function which conserves total angular momentum
 - $\mathcal{H}_s = -\sum_{i,j}^N J_{ij}(\mathbf{R}) [\vec{s}_i \cdot \vec{s}_j - 1] - \sum_{i,j}^N K_{ij}(\mathbf{R}) [(\vec{s}_i \cdot \vec{s}_j)^2 - 1]$
 - Additional physics can be easily incorporated
 - Magnetocrystalline anisotropies, external magnetic fields, longitudinal fluctuations, etc.
- Molecular-Spin Dynamics
 - $\mathcal{H}_{MSD} = \mathcal{H}_l + \mathcal{H}_s = \sum_i \frac{\mathbf{p}_i^2}{2m} + U(\mathbf{R}) - \sum_{i,j}^N J_{ij}(\mathbf{R}) [\vec{s}_i \cdot \vec{s}_j - 1] - \sum_{i,j}^N K_{ij}(\mathbf{R}) [(\vec{s}_i \cdot \vec{s}_j)^2 - 1]$ (Implemented in LAMMPS)



ML Framework for α -Fe

- 1) Generate ab-initio dataset for Fe (VASP)
 - Fe data generated for 0 - 1200K and 0 - 13 GPa
 - Spin spiral data generated for different degrees of compression
- 2) Use genetic algorithm (GA) to parameterize spin Hamiltonian using spin spiral data
- 3) Subtract magnetic energies/forces/stress from DFT Fe data and train interatomic potential, $U(R)$, using GA
 - $U(R)$ built using spectral neighbor analysis potential (SNAP)
 - $E_{SNAP}^i = \beta_0 + \boldsymbol{\beta} \cdot \mathbf{B}^i$ and $F_j^{SNAP} = -\boldsymbol{\beta} \cdot \sum_{i=1}^N \frac{\partial \mathbf{B}_i}{\partial \mathbf{r}_j}$
- 4) Evaluate candidate on predetermined set of objective functions (OFs)
 - Using candidate SNAP potential and parameterized spin Hamiltonian
- 5) Continue GA until desired OFs accuracy is reached

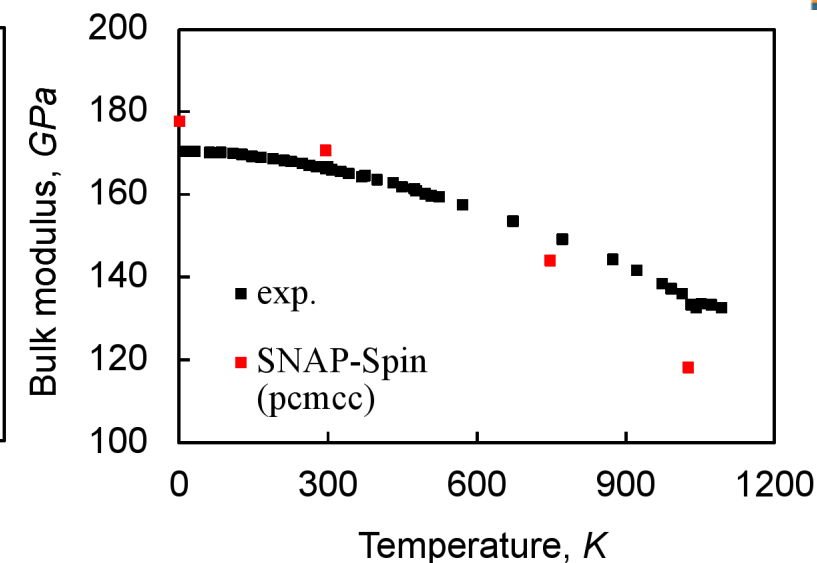
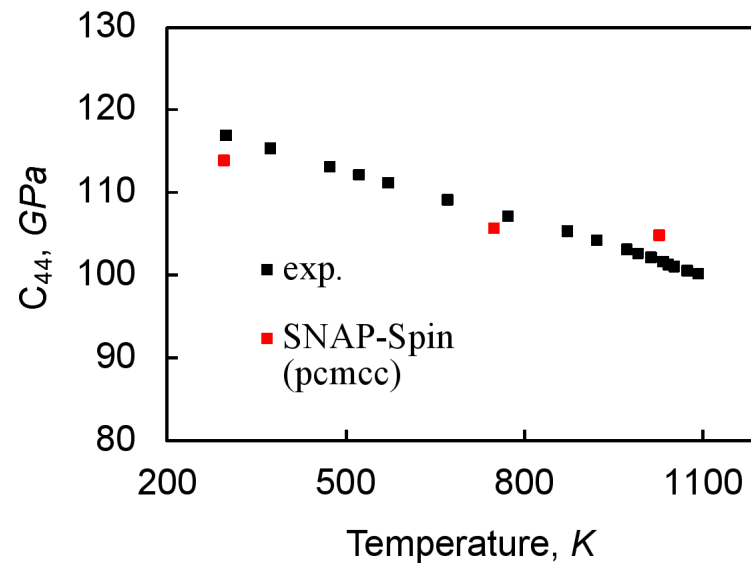
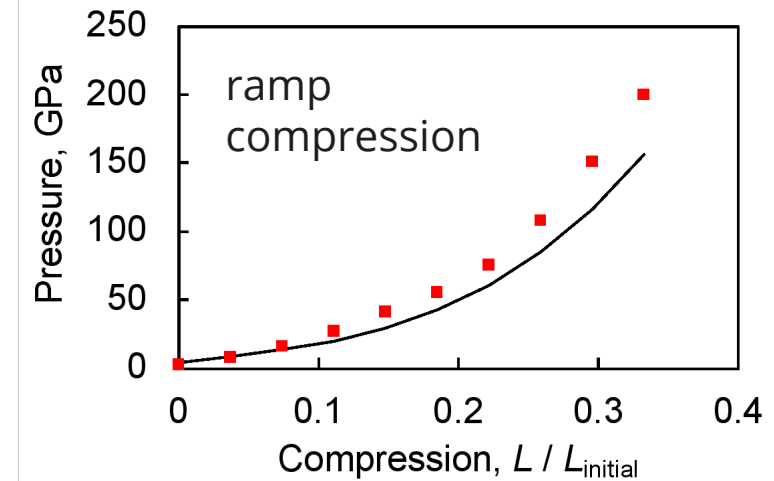


Shock Response of MSD Model

- Trained SNAP-Spin model on high pressure / temperature data
- Includes bcc / fcc / hcp collinear spin DFT (VASP) data
 - Up to 400 GPa and 6500K

0 K Objective Functions

	MSD	Exp/DFT	Units	Error
C_{11}	243.3	239.6	GPa	1.5%
C_{44}	111.3	120.8	GPa	7.9%
Bulk modulus	177.8	169.6	GPa	4.8%
$(C_{11} - C_{12}) / 2$	42.7	51.9	GPa	17.7%
Poisson ratio	0.389	0.36	-	8.1%
FCC trans. press.	25.644	19	GPa	35%
HCP trans. press.	15.487	13	GPa	19%



Shock Response of MSD Model

- Longitudinal changes in magnetic vector

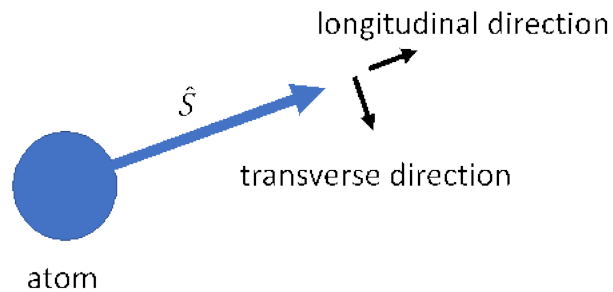
- $\mathcal{H}_{Landau} = \sum_i (AS_i^2 + BS_i^4 + CS_i^6)$

- $\hat{S} \rightarrow$ spin vector of atom

- $\hat{S} = \frac{-\hat{M}}{g\mu_B} = S_x\hat{i} + S_y\hat{j} + S_z\hat{k}$

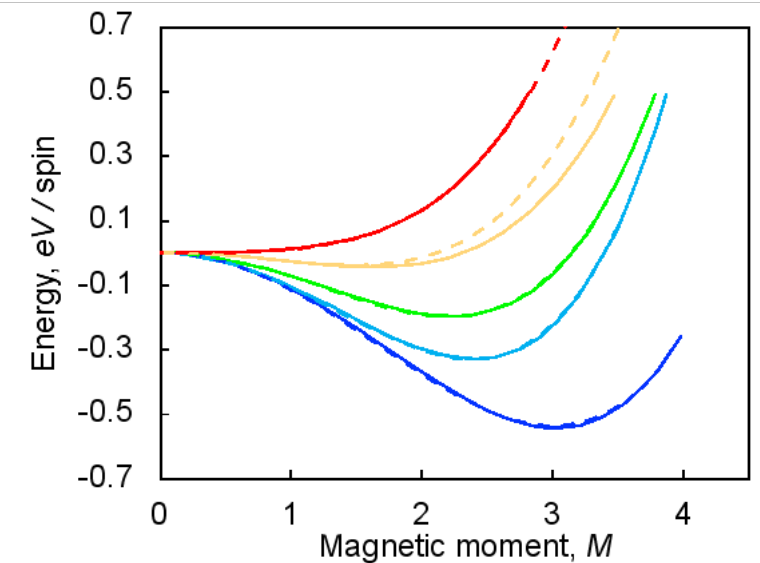
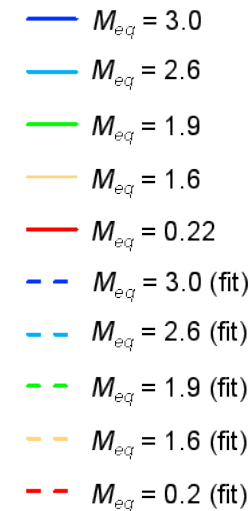
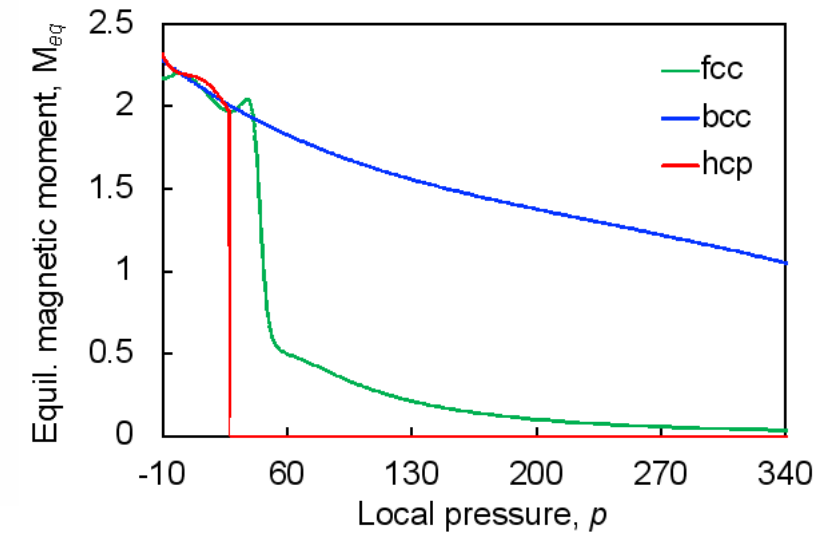
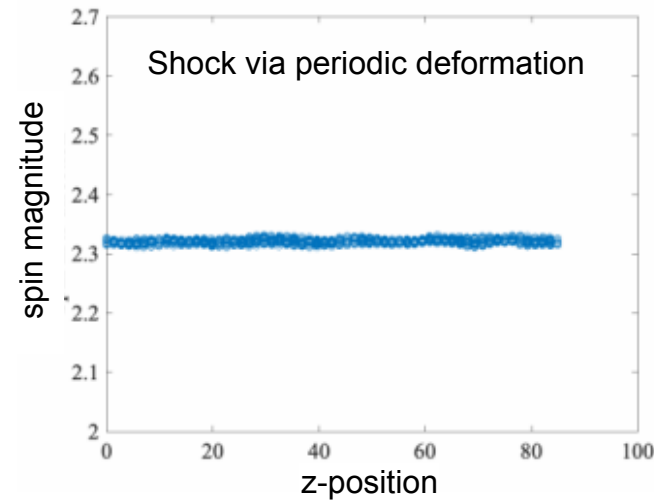
- $S_i = \|\hat{S}\| = \sqrt{(S_x)^2 + (S_y)^2 + (S_z)^2}$

- $A(p), B(p),$ and $C(p)$ are fitted to noncollinear spin data for iron[†]



- Magnetic moment adjusted on the fly

- Based on local pressure & phase

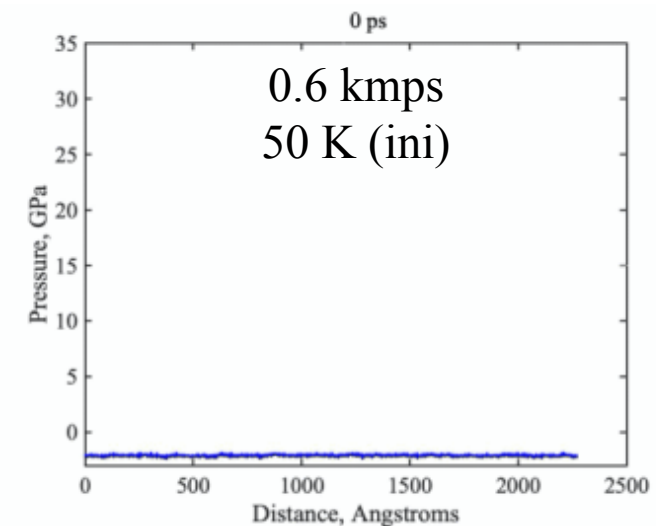
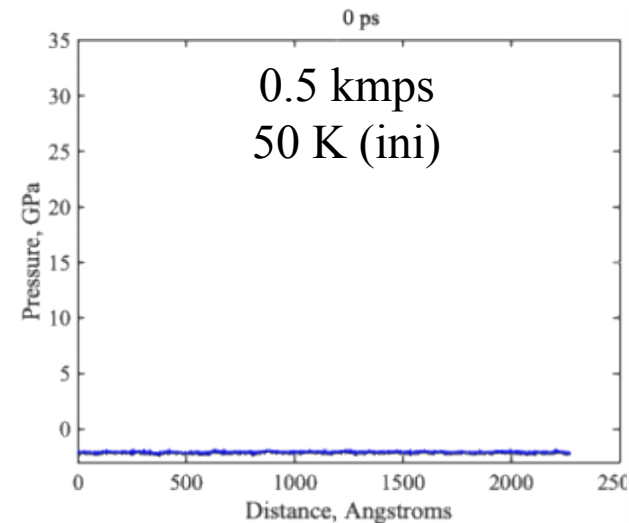
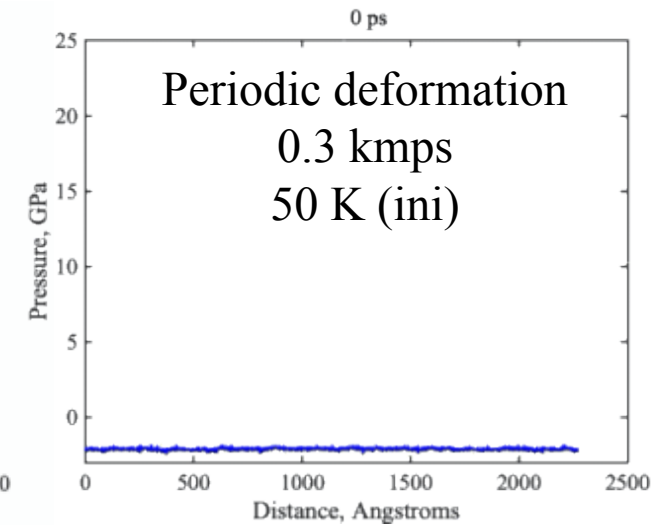
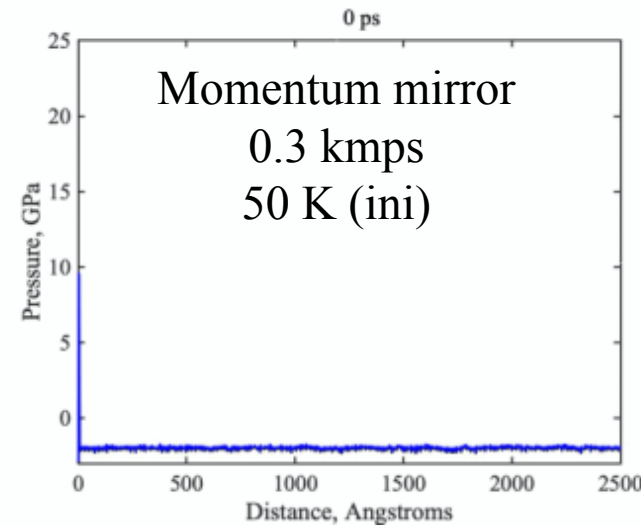
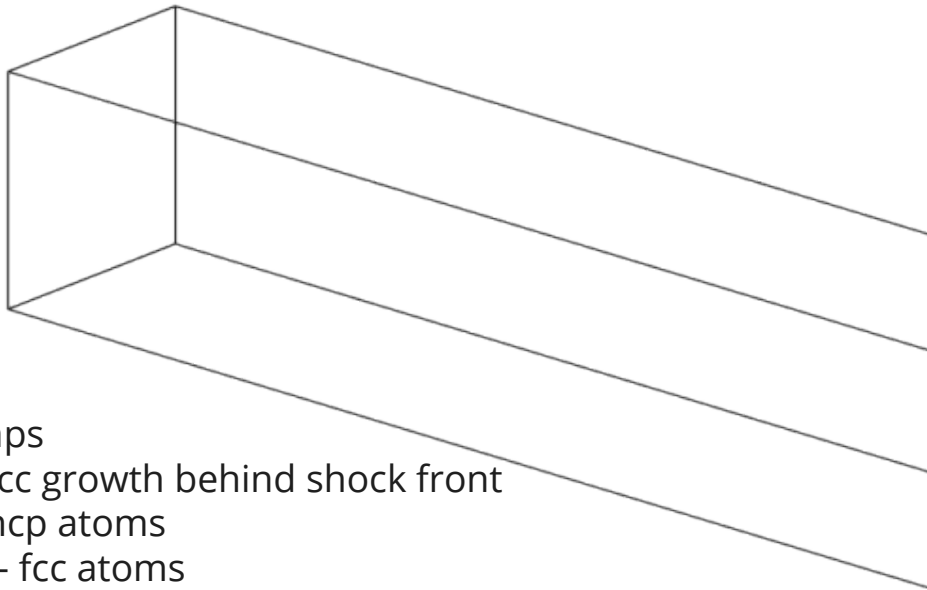


[†]Gambino, Davide, et al. "Longitudinal spin fluctuations in bcc and liquid Fe at high temperature and pressure calculated with a supercell approach." *Physical Review B* 102.1 (2020): 014402.

Shock Response of MSD Model



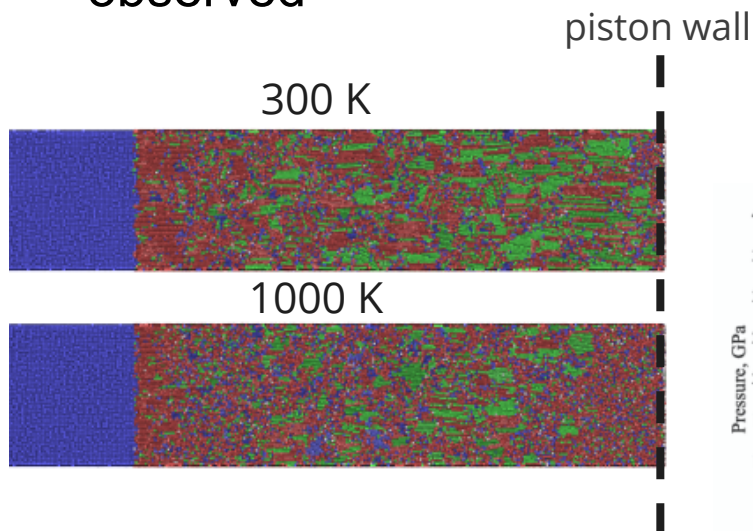
- Tested both two methods to generate shocks
 - Momentum-mirror
 - Uniaxial shrinking of periodic domain
- Response for shocks < 1 km/s
 - Below 0.6 km/s no phase transformations detected
 - Dual-wave profile observed for shocks above 0.6 km/s



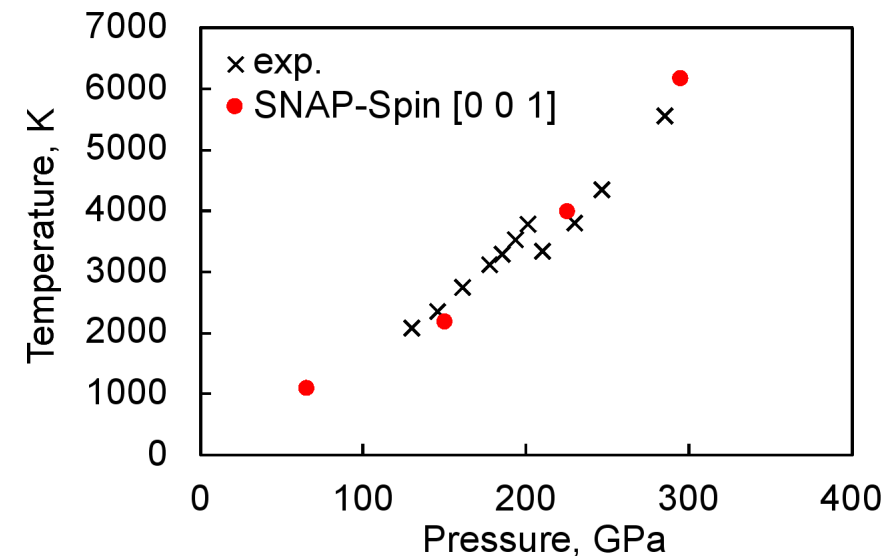
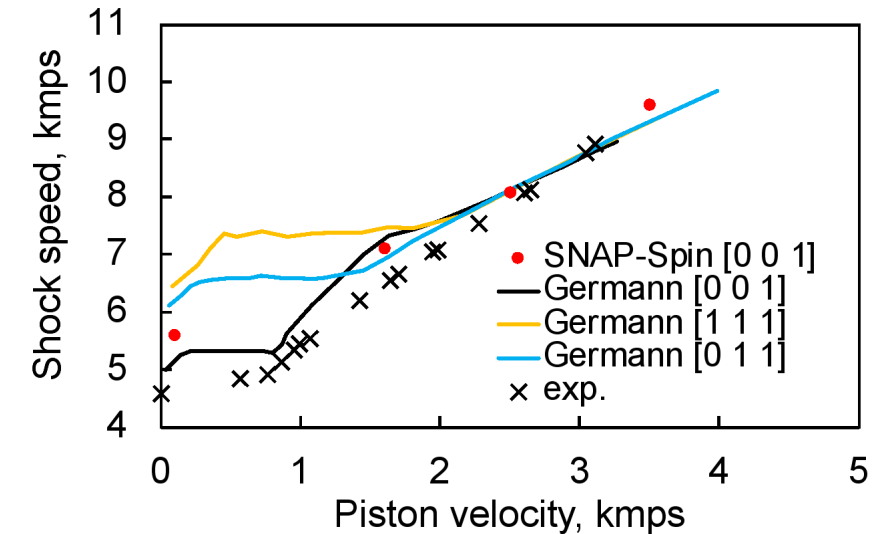
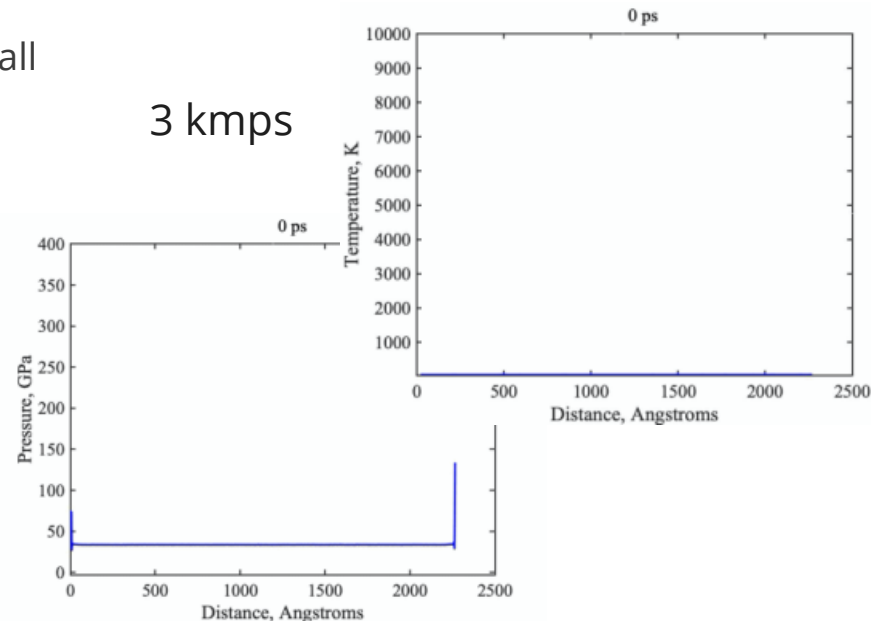
Shock Response of MSD Model



- Hugoniot curves for single crystal in good agreement with previous computational results and experiments
- Temperature / pressures in good agreement with experiments
- Potential was tested on 3-3.5 km/s and good stability was observed



blue – bcc atoms
red – hcp atoms
green – fcc atoms



Conclusion

- Illustrated framework for building α -Fe molecular-spin dynamics model from ab-initio data
- Showed impact of different equilibration methods on mechanical response of α -Fe
- Analyzed phonon/magnon spectra and thermal conductivity at corresponding temperatures
 - Good agreement with experiments
 - Able to reproduce acoustic peak shift up to $\sim 700\text{K}$
- Retrained potential for high temperature / pressure data
 - Good agreement for elastic properties / transition pressures / ramp curve
 - Dual-wave profile observed once bcc begins transforming into hcp phase

