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# Transformer Leakage Inductance Design Methodology

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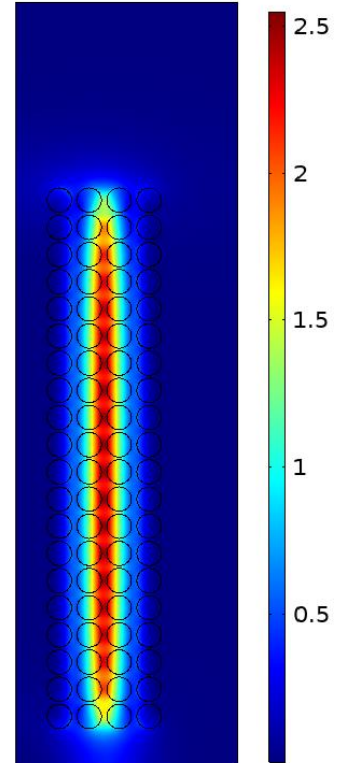
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Electrical and Computer Engineering

# Outline

- Transformer leakage inductance
- Magnetically-integrated transformers
- Motivation
- Design specifications
- General transformer design
- Leakage inductance design
- Results and discussion
- Conclusion

# Transformer Leakage Inductance ( $L_{lk}$ )

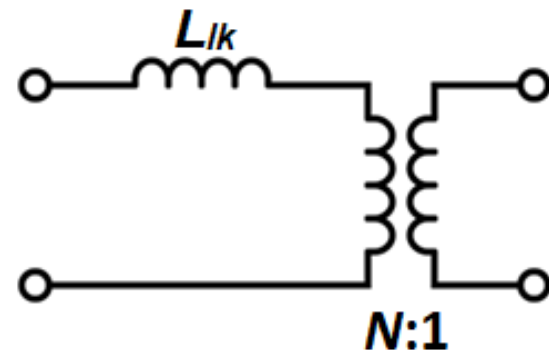
- Byproduct of stored magnetic energy
- Depends on the winding geometry
  - *winding structure*
    - number of layers, number of turns per layer
  - *interleaving configuration*
    - PPSS, PSSP, PSPS for 4 layers
  - *key design parameters:*
    - 1) inter-winding gap
    - 2) inter-layer gap
    - 3) inter-turn gap
    - 4) overlapping height of the two windings
- Infinite design possibilities



Magnetic energy density ( $\text{J/m}^3$ )

# Magnetically-integrated Transformers

- $L_{lk}$  can replace the series inductor in power converters
- Scope to reduce cost and footprint
- Requires precise  $L_{lk}$  design and tuning



## Two-step design process

Step 1	General transformer design	Outputs the required core size, number of turns, and wire gauge
Step 2	Leakage inductance design	Outputs the right winding structure, interleaving configuration and key design parameters

# Motivation

- Several methods exist for general transformer design, like Area Product Method,  $K_g$  (core geometry) method, etc.
- No emphasis on leakage inductance design
- Leads to inefficient design process—requires numerous trial-and-error iterations
- Only a handful of experienced magnetic engineers/designers know the tricks to tune the  $L_{lk}$

This paper attempts to make the design process of magnetically-integrated transformers simpler and more efficient.

# Design Specifications

**Target:** Naturally air-cooled 2-winding transformer for an isolated resonant dc-dc converter

Output power	1 kVA
Input voltage (rms)	340 V
Turns ratio	1:1
Operating frequency	220 kHz
Duty cycle	0.5
Maximum flux density	0.1 T
Maximum temperature rise	50° C

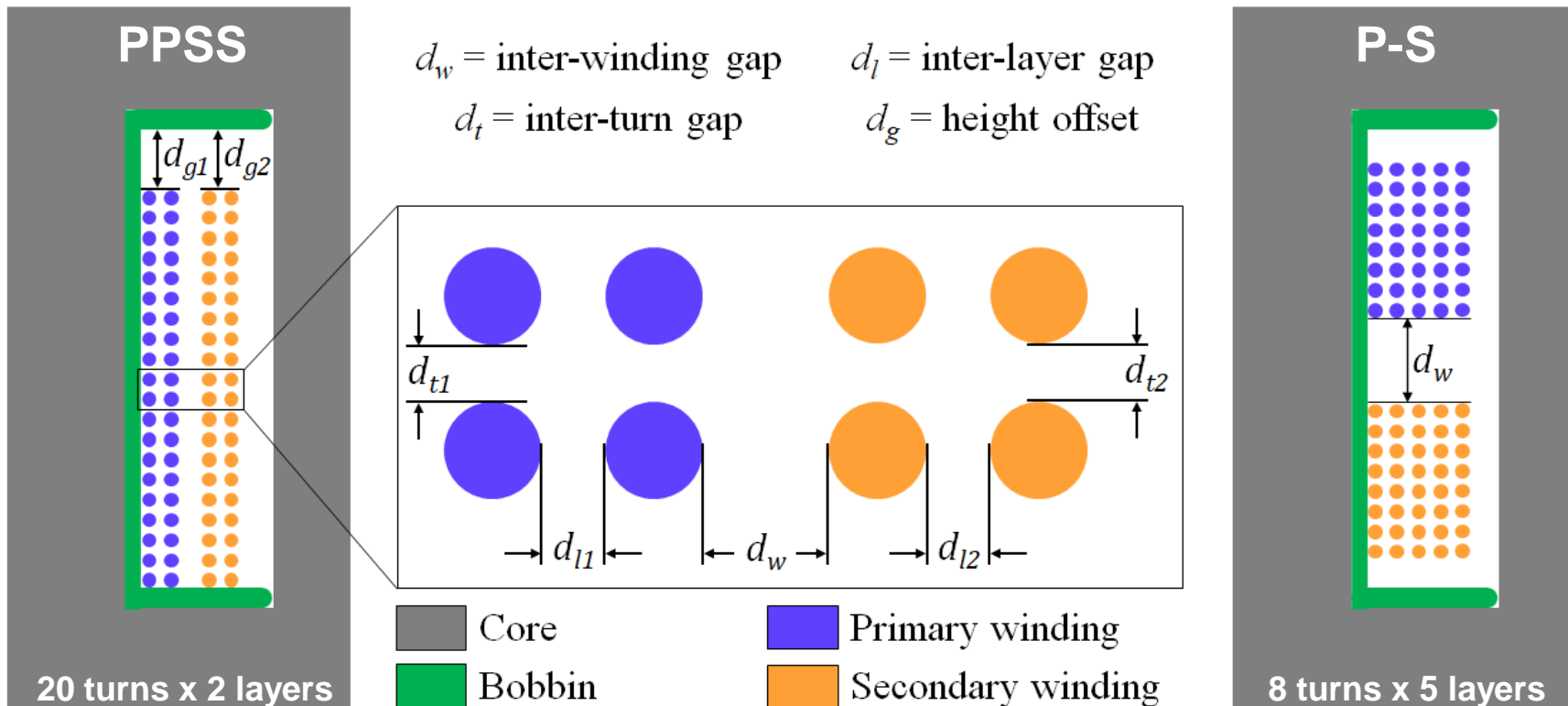
# General Transformer Design (contd.)

## Results of the *Area Product Method*

Minimum area product	1.65 cm <sup>4</sup>
Selected core	<b>ETD 39</b> ( $WaAc = 2.18 \text{ cm}^4$ )
Peak current density	484 A/cm <sup>2</sup>
Selected wire gauge	<b>AWG 19</b> ( $J = 450 \text{ A/cm}^2$ )
Primary/secondary turns	<b>40/40</b>
Core loss	1.27 W
DC copper loss	1.24 W
Temperature rise	34.9° C
DC efficiency	99.75 %

# Leakage Inductance Design

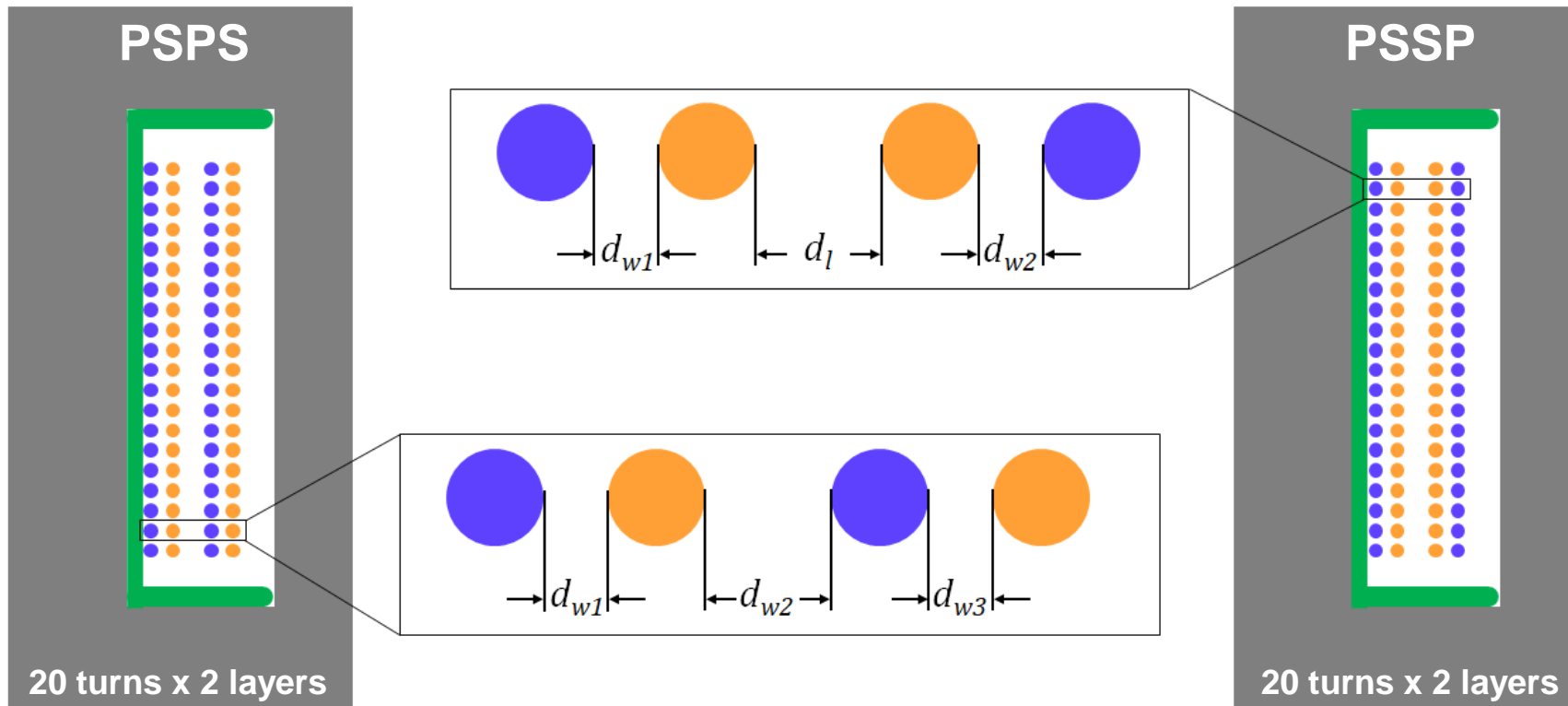
## 2 winding structures: **PPSS** and **P-S**





# Leakage Inductance Design (contd.)

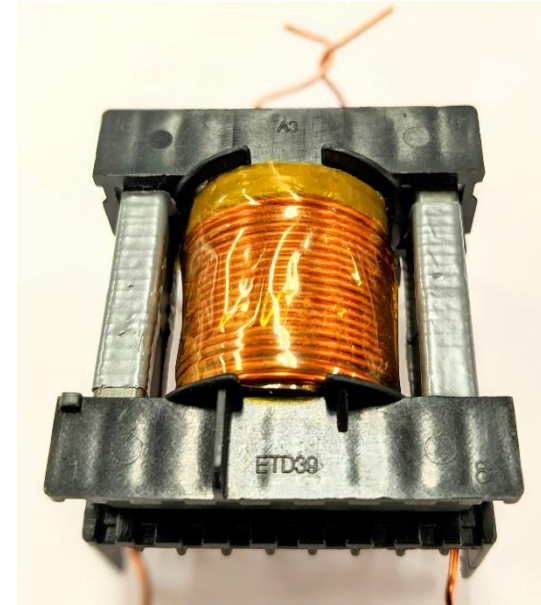
3 possible interleaving configurations: PPSS, **PSPS** and **PSSP**



# Results

Ideal values of different parameters  
and corresponding  $L_{lk}$

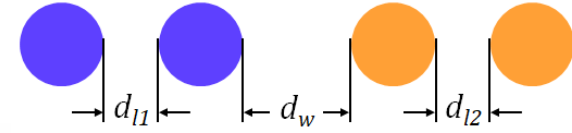
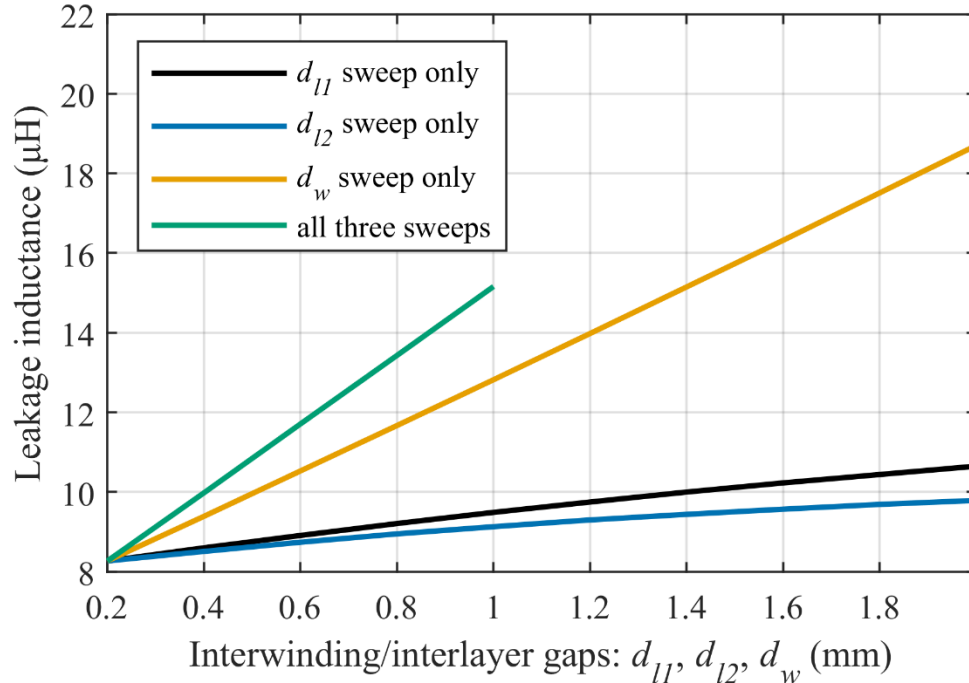
Parameter	Value			
	PPSS	PSPS	PSSP	P-S
$d_l$ (mm)	0.2	0.2	0.2	0.2
$d_w$ (mm)	0.2	0.2	0.2	0.3
$d_f$ (mm)	0.1	0.2	0.2	0.2
$d_g$ (mm)	0	1.8	1.8	0
$L_{lk}$ ( $\mu\text{H}$ )	<b>8.27</b>	<b>1.92</b>	<b>2.29</b>	<b>45.84</b>



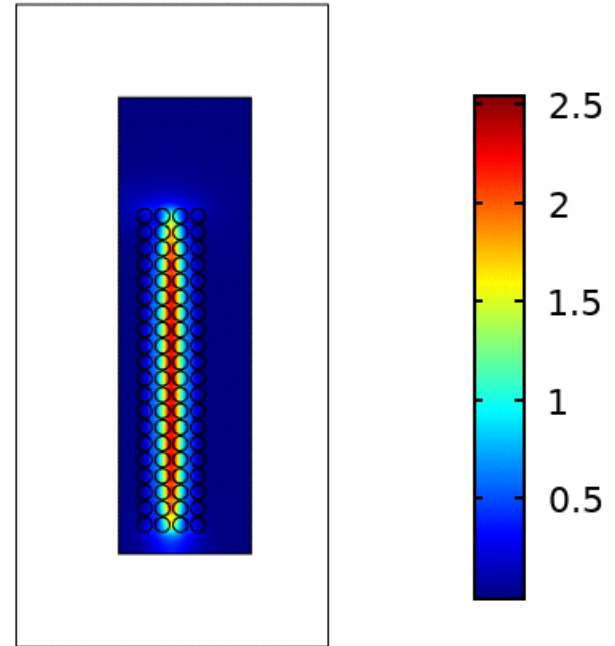
PPSS Structure  
Measured leakage  
inductance = 8.3  $\mu\text{H}$

# Results: PPSS structure

## Parametric sweep of interwinding and inter-layer gaps

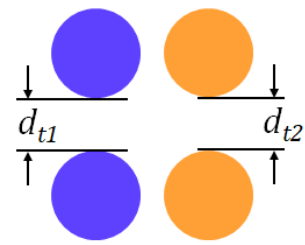


$d_{I1}=0.2$ ,  $d_{I2}=0.2$ ,  $d_w=0.2$  Time=1.2

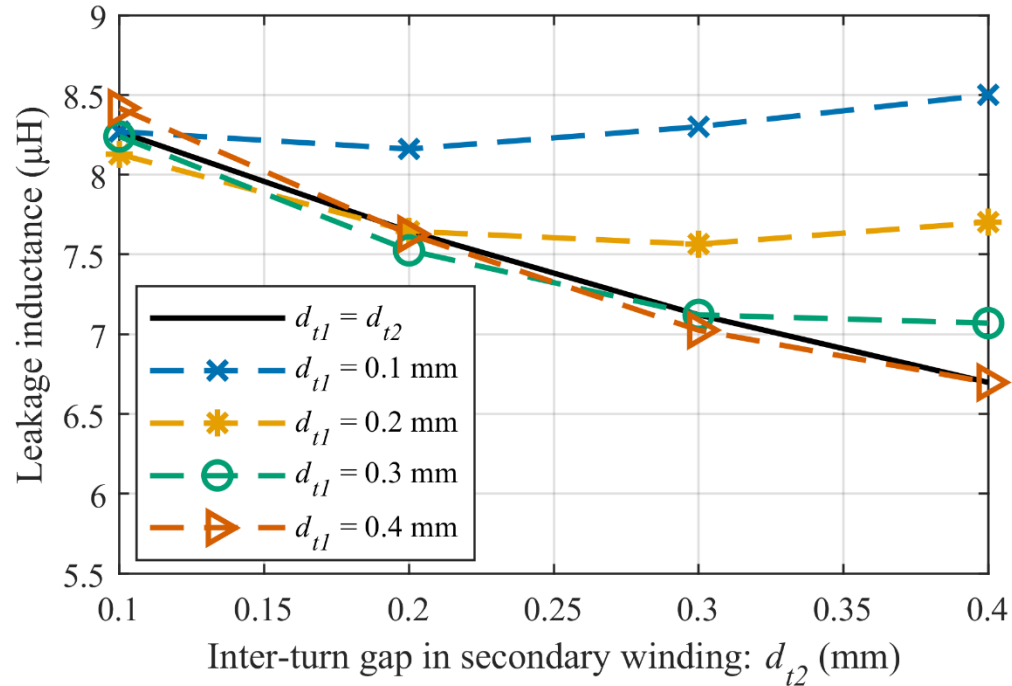


Magnetic energy density (J/m<sup>3</sup>)

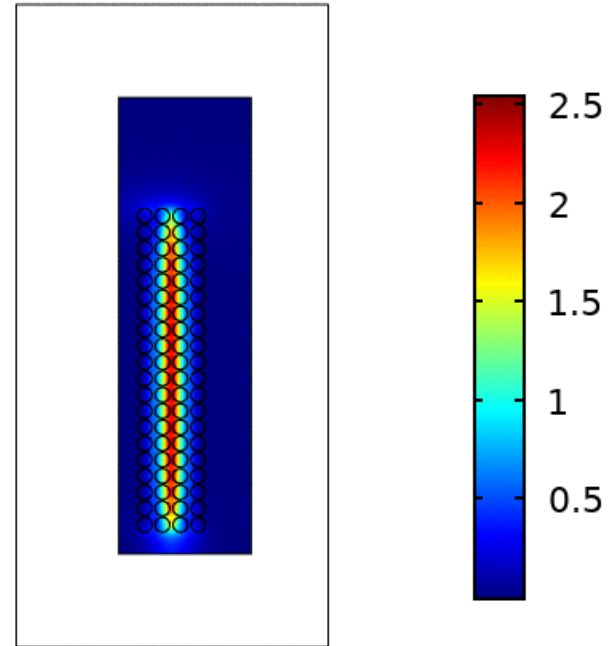
# Results: PPSS structure



## Parametric sweep of inter-turn gap

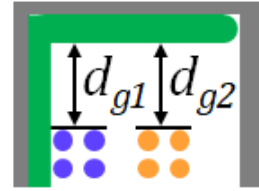


$d_{it1}=0.1, d_{it2}=0.1$  Time= $1.25\text{E-}4$  s

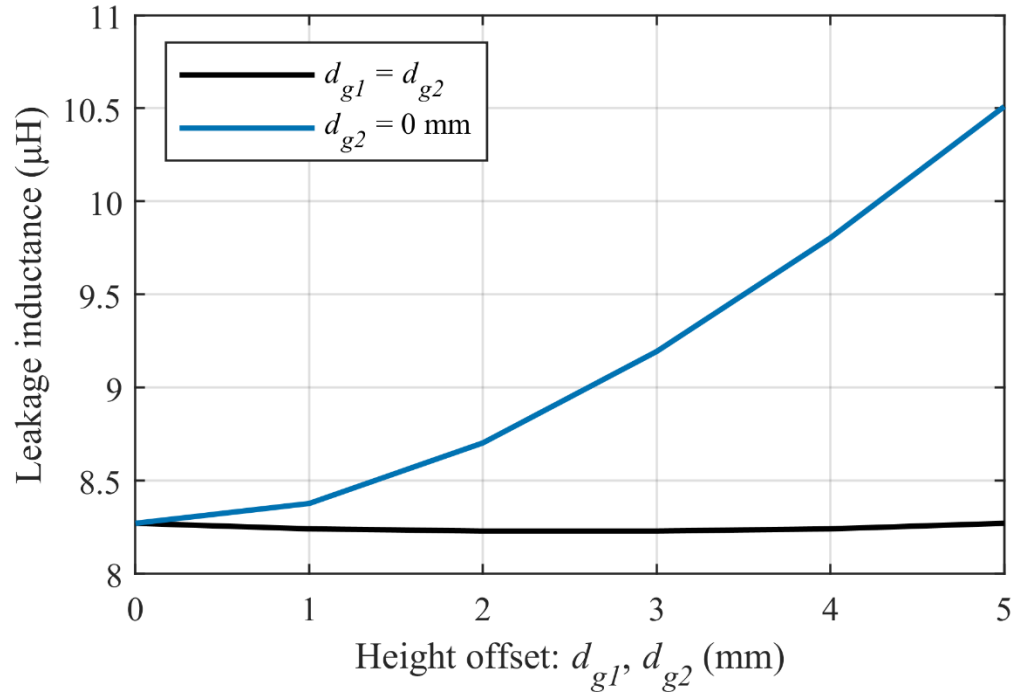


Magnetic energy density ( $\text{J/m}^3$ )

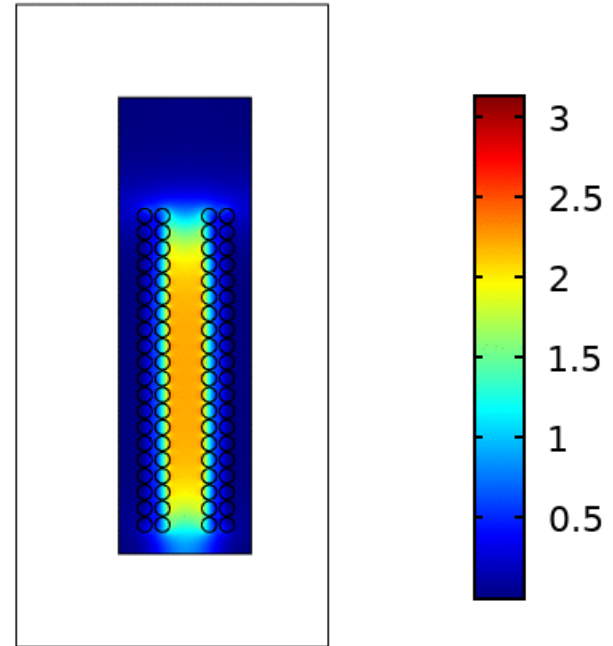
# Results: PPSS structure



Parametric sweep of the height offset



$g(1)=0$  mm Time= $1.25\text{E}-4$  s



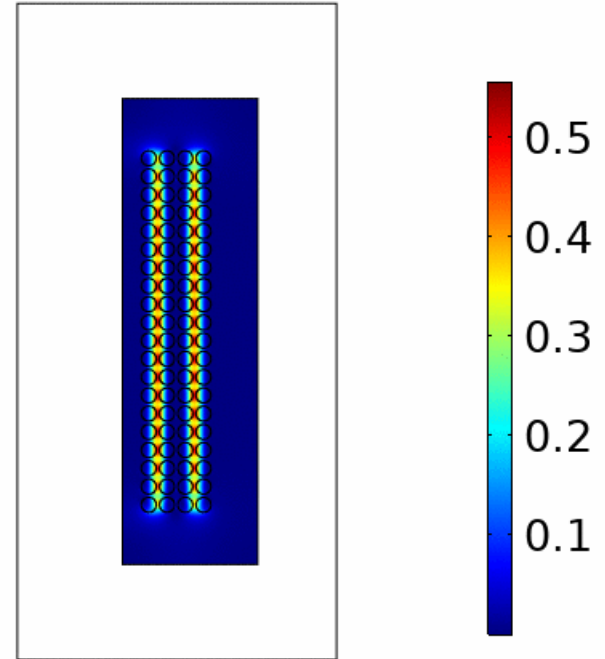
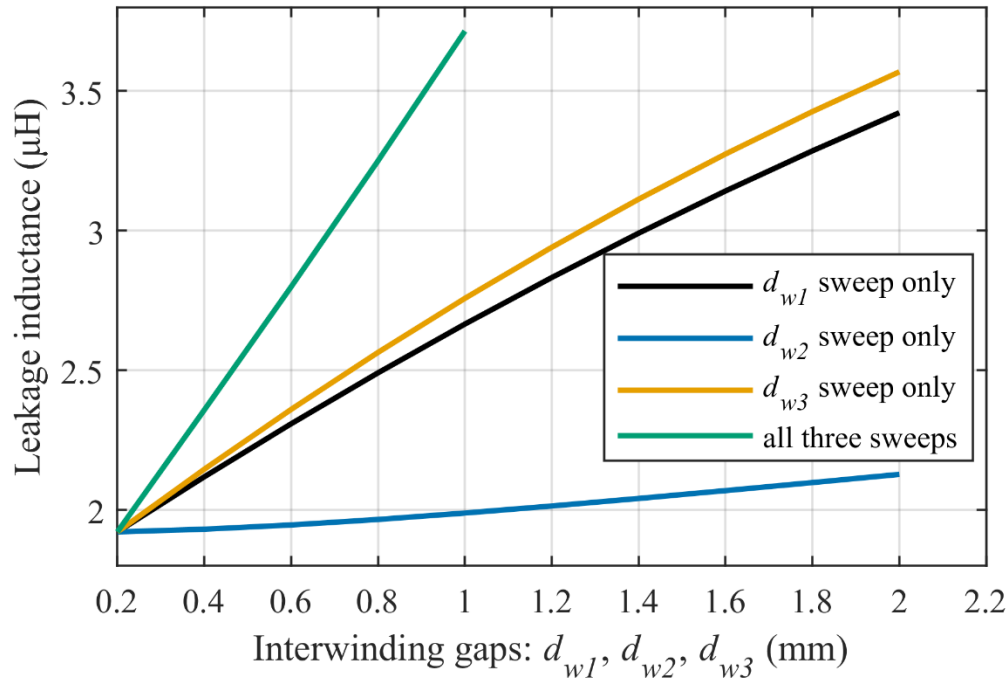
Magnetic energy density ( $\text{J}/\text{m}^3$ )

# Results: PSPS structure

Parametric sweep of inter-winding and inter-layer gaps



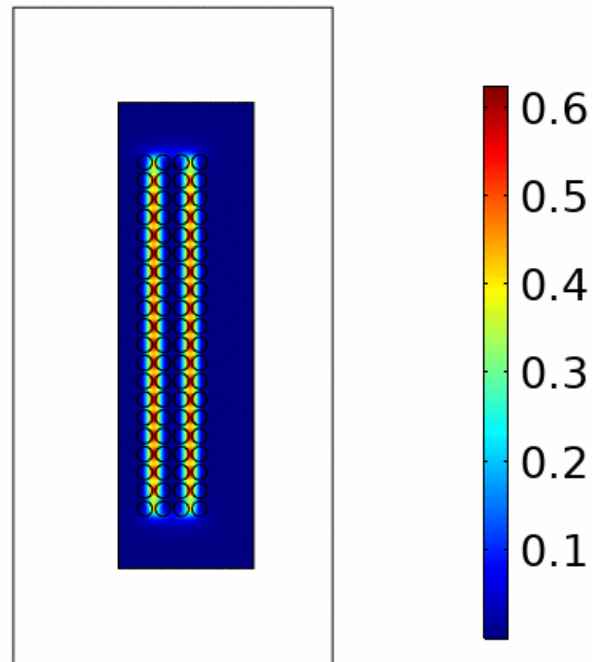
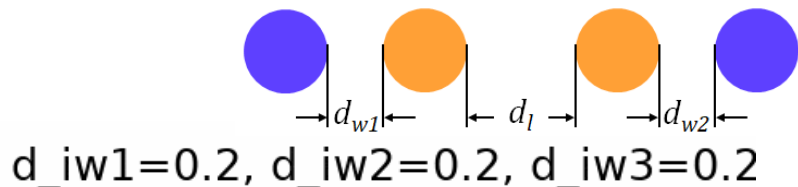
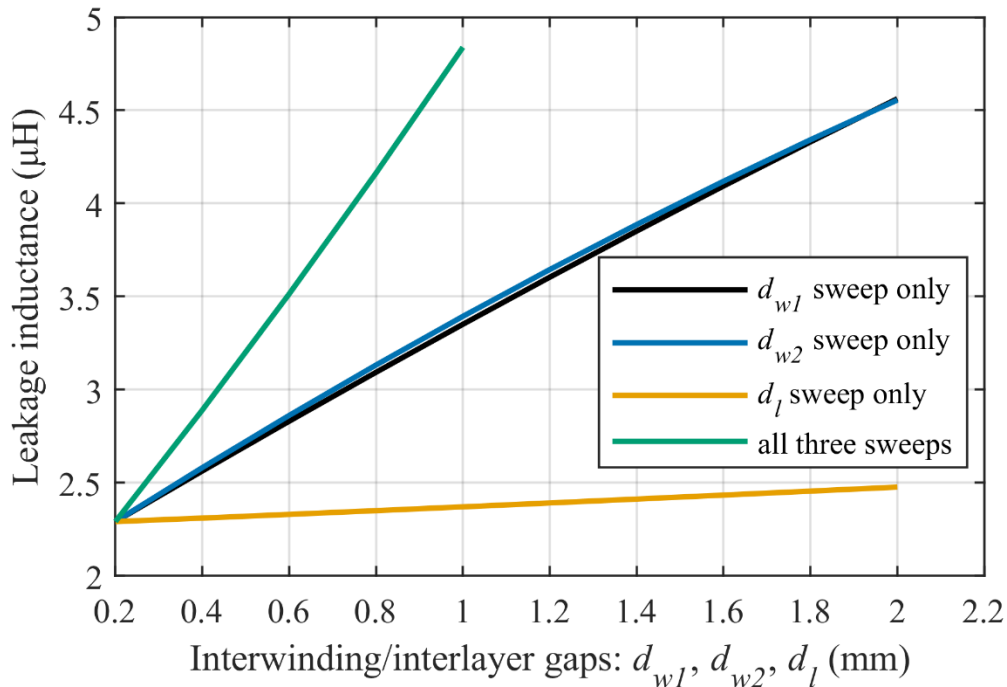
$d_{iw1}=0.2$ ,  $d_{iw2}=0.2$ ,  $d_{iw3}=0.2$



Magnetic energy density ( $\text{J/m}^3$ )

# Results: PSSP structure

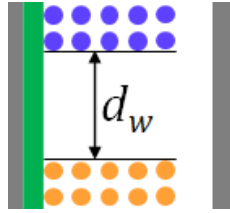
## Parametric sweep of inter-winding and inter-layer gaps



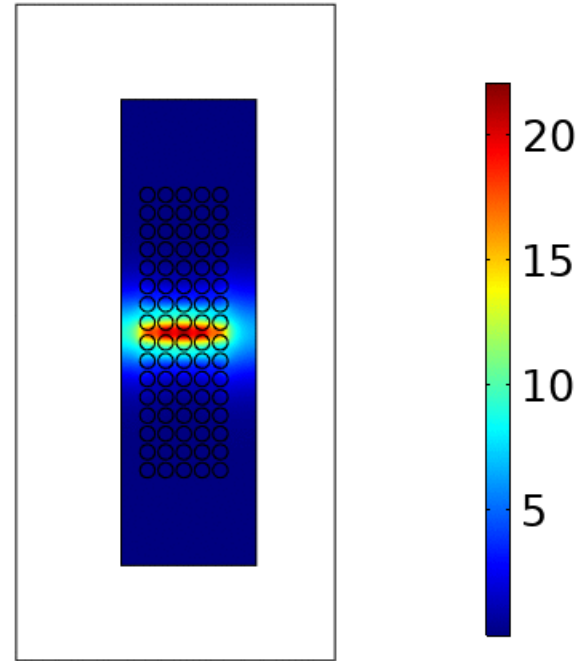
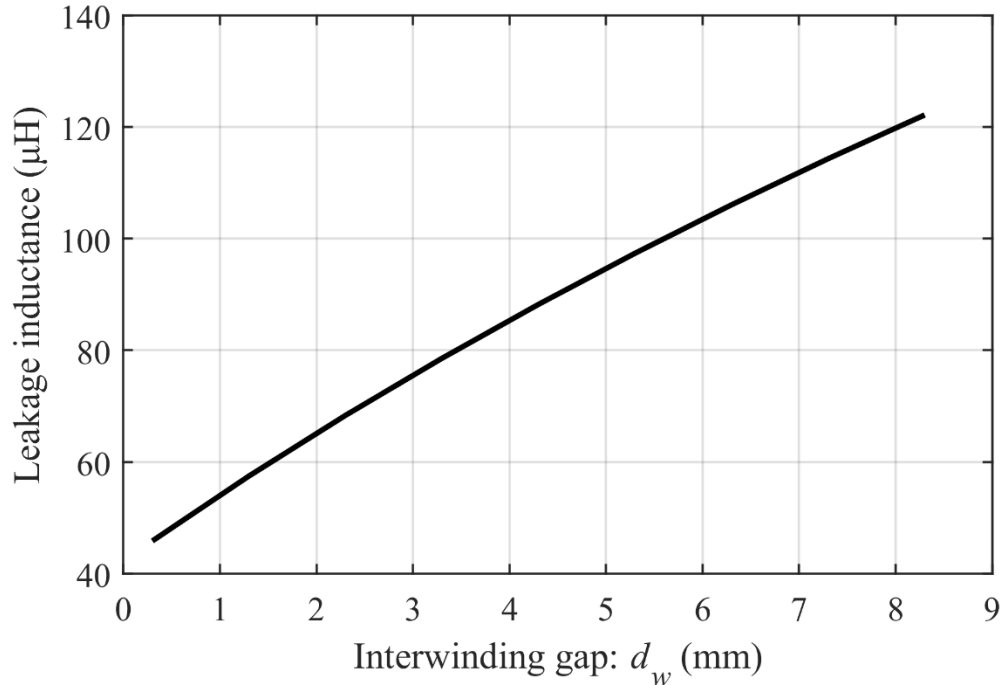
Magnetic energy density ( $J/m^3$ )

# Results: P-S structure

## Parametric sweep of inter-winding gap



$g(1)=0$  mm Time= $1.25E-4$  s



Magnetic energy density ( $\text{J}/\text{m}^3$ )



# Discussion

- 1) Interleaving of layers can reduce the effective  $L_{lk}$
- 2) Alternately arranged P and S layers give the smallest  $L_{lk}$
- 3) Most of the leakage energy is stored in  $d_w$
- 4) Varying  $d_w$  can help in making large adjustments
- 5) Varying  $d_l$  can help in making small adjustments
- 6) Offsetting the height of one of the windings can increase  $L_{lk}$

# Conclusion

Using the Area Product Method, a 1 kVA, 340/340 V, 220 kHz, 2-winding transformer is designed with two ETD 39 ferrite cores and 40 turns of enameled AWG 19 wires per winding.

2 winding structures and 3 interleaving configurations of one of the 2 structures are investigated

Trends in  $L_{lk}$  due to various parametric sweeps are recorded and further discussed

Results show that  $L_{lk}$  between 1.9 and 122.1  $\mu\text{H}$  is achievable

Observations made here can be helpful for future magnetic engineers/designers in realizing the desired  $L_{lk}$  with fewer trial-and-error iterations

# Reference

- 1) C. W. T. McLyman, *Transformer and inductor design handbook*. CRC press, 2004.
- 2) **A. Sharma and J. W. Kimball**, “Evaluation of transformer leakage inductance using magnetic image method,” *IEEE Transactions on Magnetics*, vol. 57, no. 11, pp. 1–12, 2021.
- 3) **A. Sharma and J. W. Kimball**, “Novel transformer with variable leakage and magnetizing inductances,” in *2021 IEEE Energy Conversion Congress and Exposition (ECCE)*. IEEE, 2021, pp. 2155–2161.
- 4) Z. Ouyang, O. C. Thomsen, and M. A. Andersen, “The analysis and comparison of leakage inductance in different winding arrangements for planar transformer,” in *2009 International Conference on Power Electronics and Drive Systems (PEDS)*. IEEE, 2009, pp. 1143–1148.

# Thanks

for your attention!

# Questions?

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