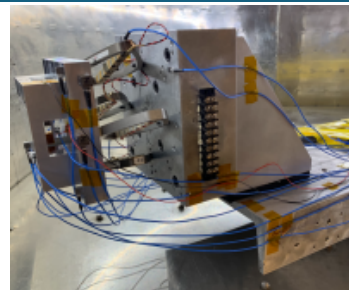
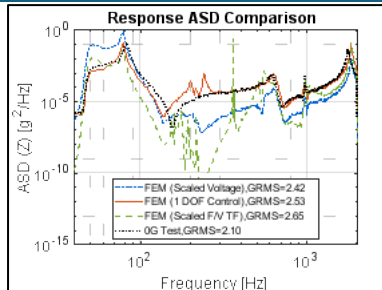
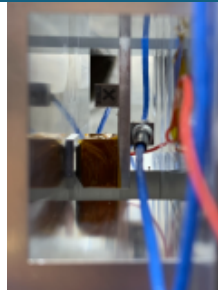
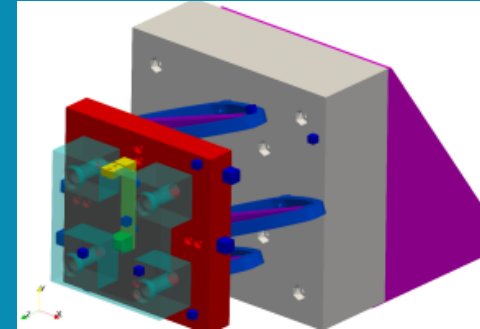




Model Validation for Combined Inertial Acceleration and Vibration Environments



Moheimin Khan, David M. Siler, Garrett K. Lopp,
Brian C. Owens

PRESENTED BY

Moheimin Khan

IMAC-XL

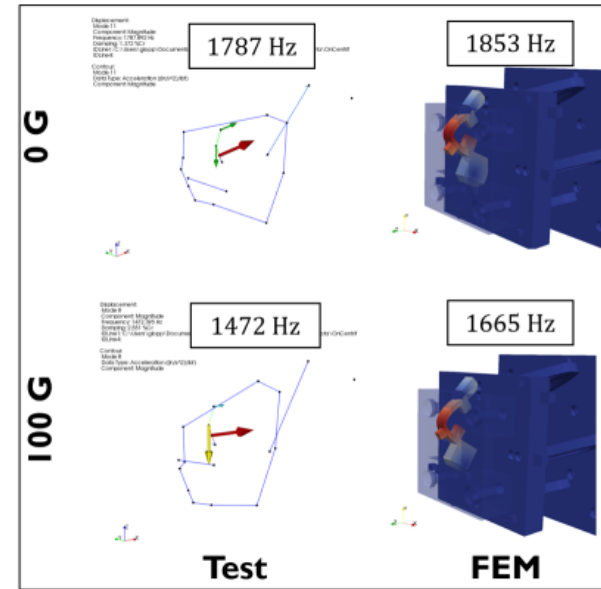
February 7-10, 2022

Submission # 12486

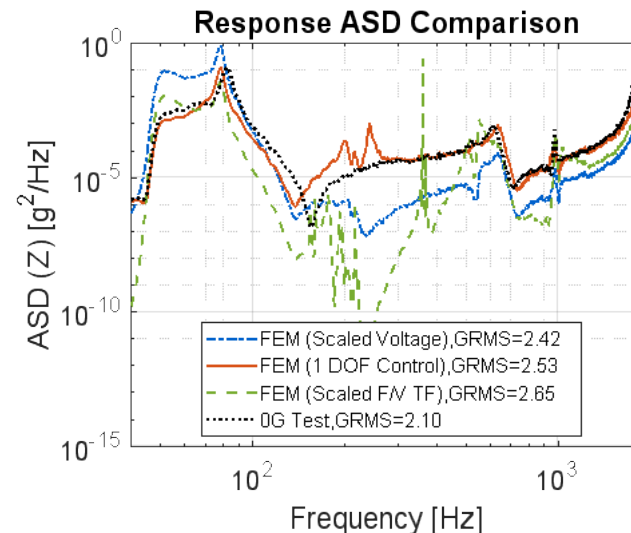


Summary

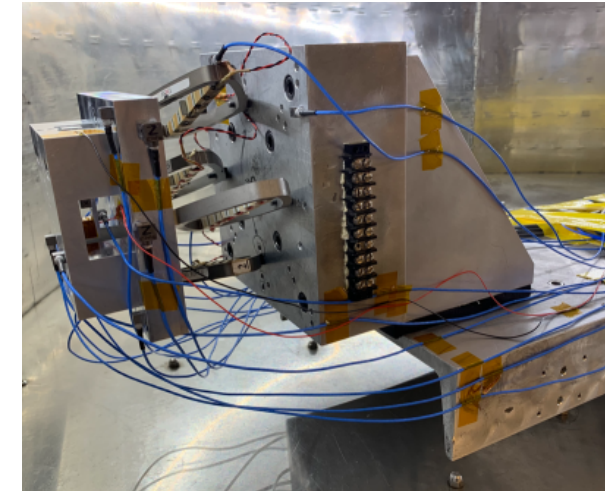
- Model validation was performed for a research structure subjected to combined inertial acceleration and vibration environments (vibrafuge)
- SIERRA coupled analysis was conducted to evaluate the effect of centrifuge acceleration combined with random vibration
 - Preloading the cantilever beam structure using SIERRA/SM
 - Updating the contact state, and evaluating the preloaded response using SIERRA/SD
- Results were validated with vibrafuge testing using piezoelectric actuators on a centrifuge
 - Comparisons to test data showed that the SM to SD handoff model was able to account for the updated dynamic response due to the inertial acceleration preload
 - Validation metrics were computed to quantify comparisons between model and test data
- This work demonstrates the development of an improved approach for combined mechanical environments analysis and model validation using SIERRA



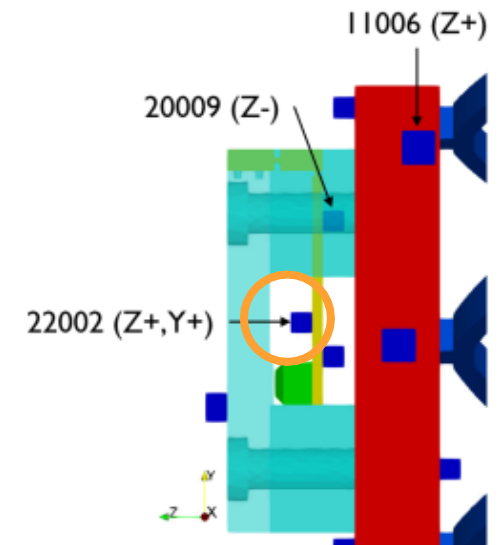
3rd Bending Mode- 0/100 G Comparison



Acceleration Response Results and Location



Test Article Vibrafuge Setup





- I. Introduction/Overview
 - A. Unit Description
 - B. Setup
- II. Experimental Characterization
 - A. Modal Testing
 - B. Vibrafuge Testing
- III. FE Modeling and Calibration
 - A. Modal Analysis
 - B. Code Coupling/Handoff Procedure
 - C. Random Vibration Analysis
- IV. Conclusion



I. Introduction/Overview

- A. Unit Description
- B. Setup

II. Experimental Characterization

- A. Modal Testing
- B. Vibrafuge Testing

III. FE Modeling and Calibration

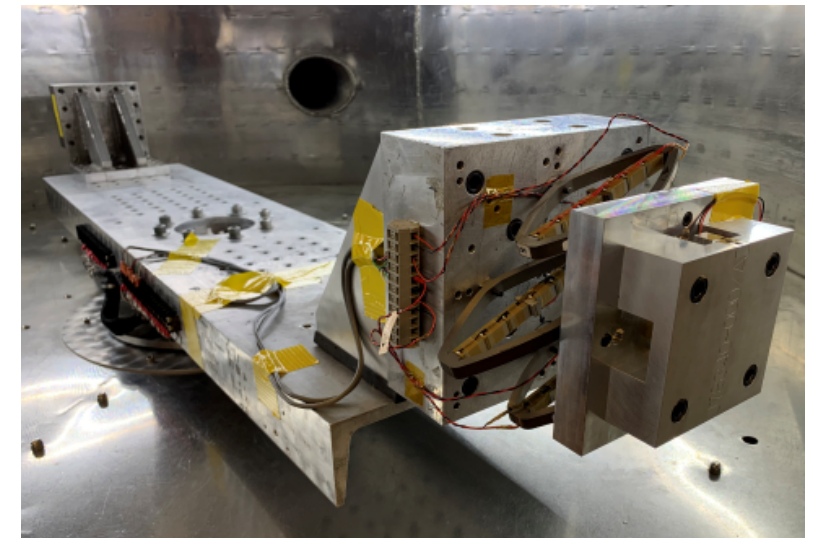
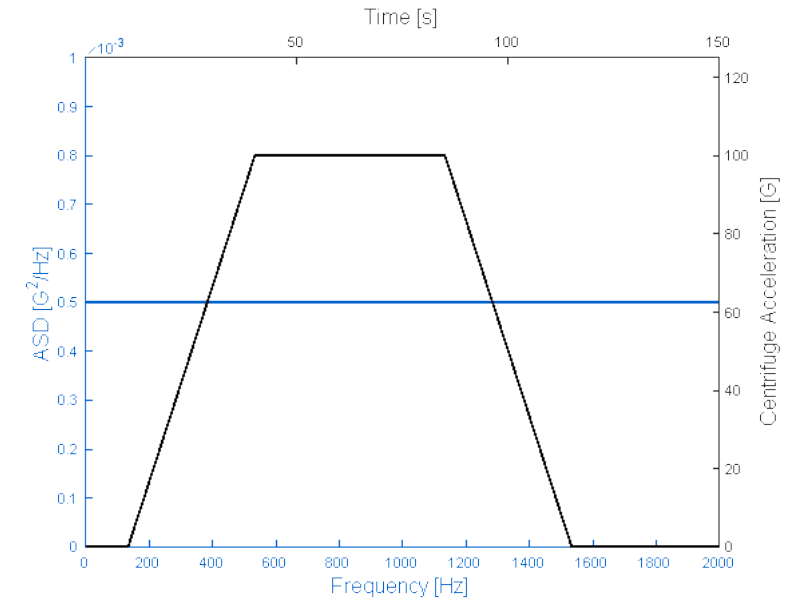
- A. Modal Analysis
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- C. Random Vibration Analysis

IV. Conclusion

Introduction

- Aerospace structures are often subjected to combined inertial acceleration and vibration environments during operation
- Traditional test approaches independently assess a system under a sequence of inertial and vibration environments
 - Incapable of addressing couplings in system response under combined environments
- Considering combined environments throughout the design and qualification of a system requires development of both analytical and experimental capabilities
- Recent ground testing efforts have improved the ability to replicate flight conditions and aid qualification by incorporating combined centrifuge acceleration and vibration environments in a **vibrafuge** test
 - Modeling these loading conditions involves the coupling of multiple physical phenomena to accurately capture dynamic behavior

Combined Acceleration and Vibration Environments



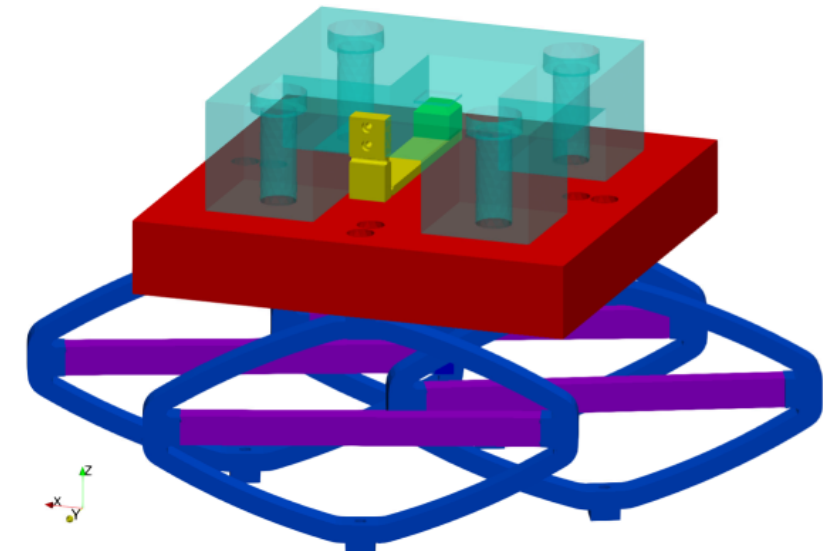
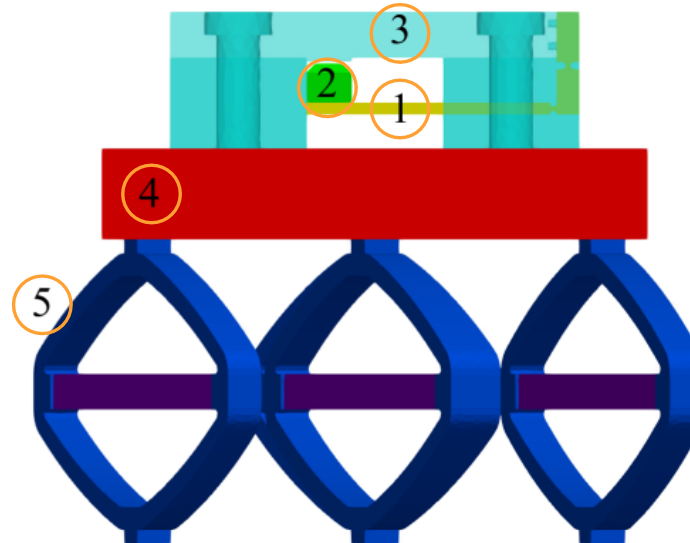
Vibrafuge Setup

Unit Description

- Vibrafuge capability demonstrated with research structure
 - Applied acceleration on centrifuge
 - Vibration using Cedrat Technologies APA230L amplified piezoelectric actuators (APA)
- Consists of an inverted cantilever beam
 - Functions as simple acceleration switch
 - Goal to study dynamics as tip contact state changes under vibrafuge environment
- Assembly consists of the following
 1. Aluminum beam
 2. Tungsten mass
 3. Aluminum support block
 4. Aluminum base block
 5. Piezoelectric actuators



Cantilever Beam Geometry

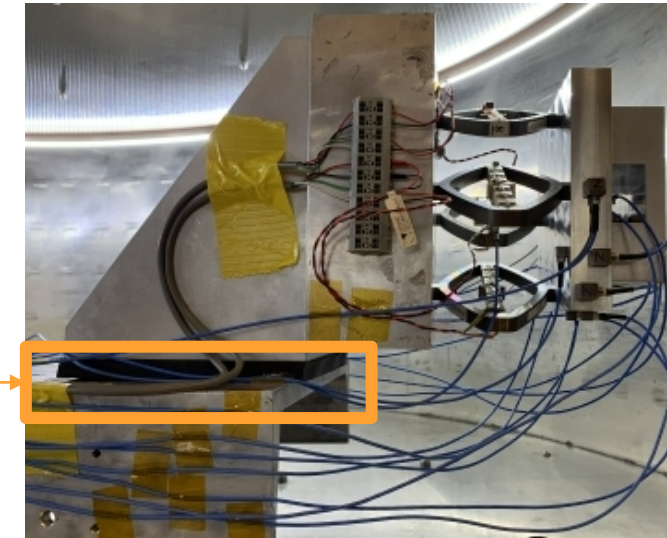
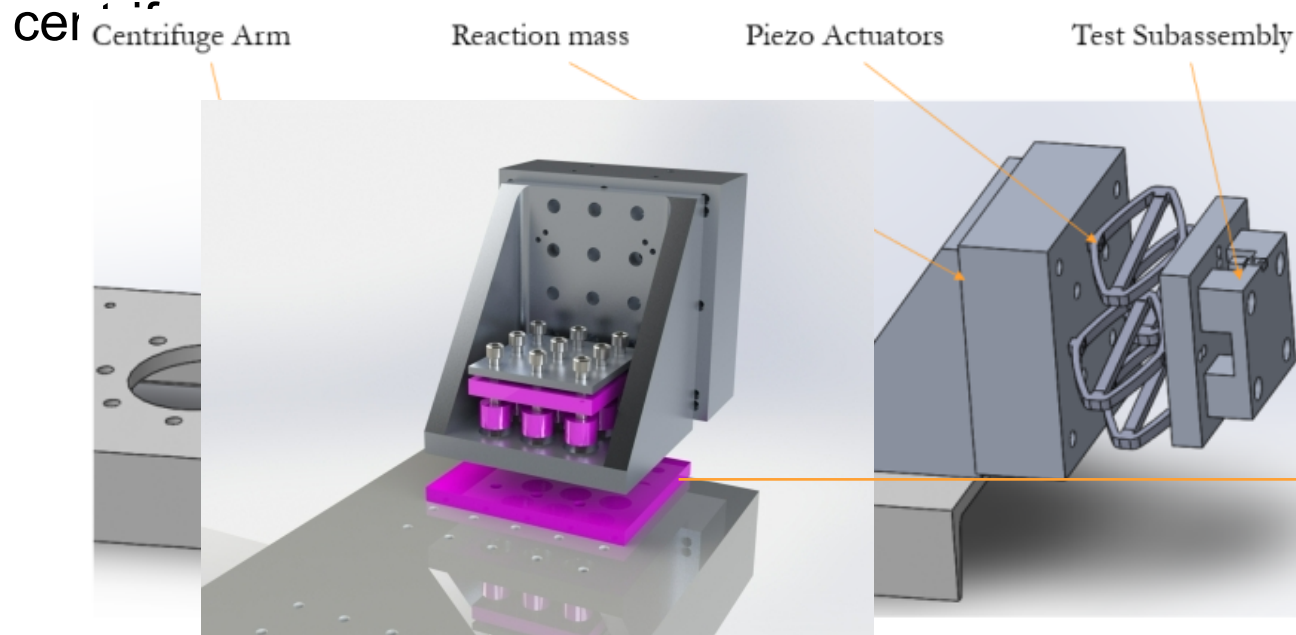


Test Subassembly

Vibrafuge Setup



- Combined inertial acceleration and vibration environments simulated using “vibrafuge” setup
 - Cantilever beam assembly and APA fixtured on centrifuge arm with reaction mass and angle bracket
- Test setup allows for dynamic characterization under simultaneous environments
 - Instrumentation set up through slip rings and routed to external controller and data acquisition
- Additional polyurethane rubber sheets and rounds used to isolate APA vibration to



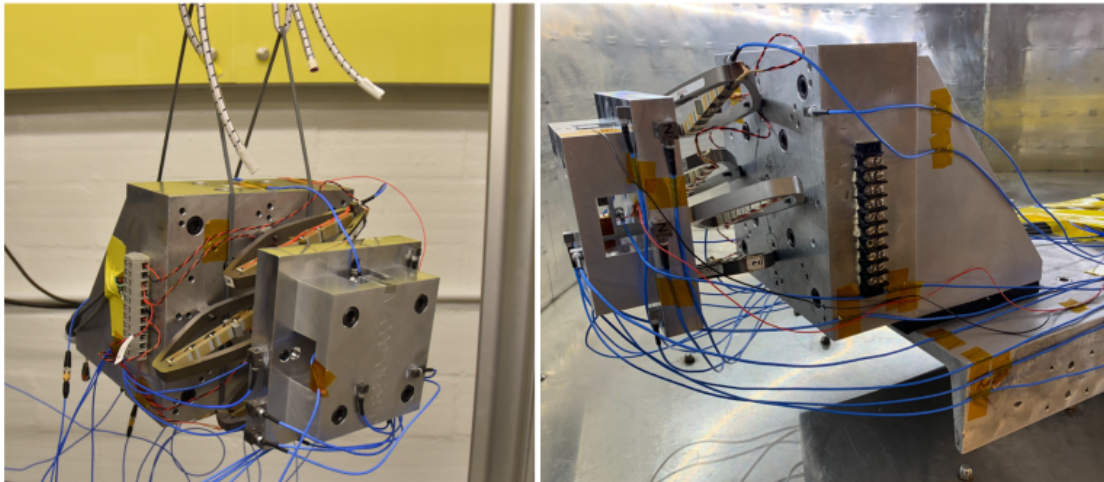
Vibrafuge Description and Test Setup



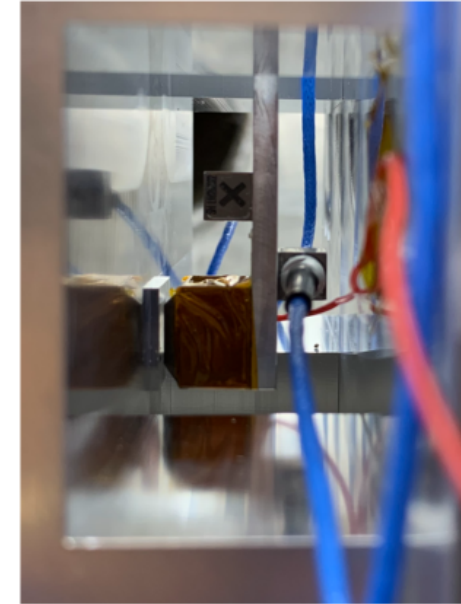
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Modal Testing

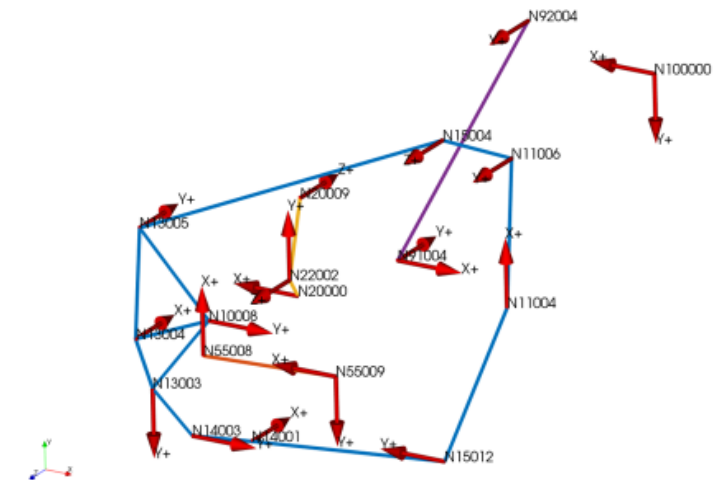
- Instrumentation designed to capture modes of interest
 - 18 accelerometers, 22 DOF total
- Modal testing performed in free-free and centrifuge boundary conditions
 - To evaluate effect of fixturing
- APAs also used to extract modal parameters during centrifuge testing
 - Modes and frequencies evaluated at various G-levels
 - Data used to later validate FE model



Modal Test Setup



Beam Tip Instrumentation Closeup



Instrumentation Layout

Modal Testing- Results



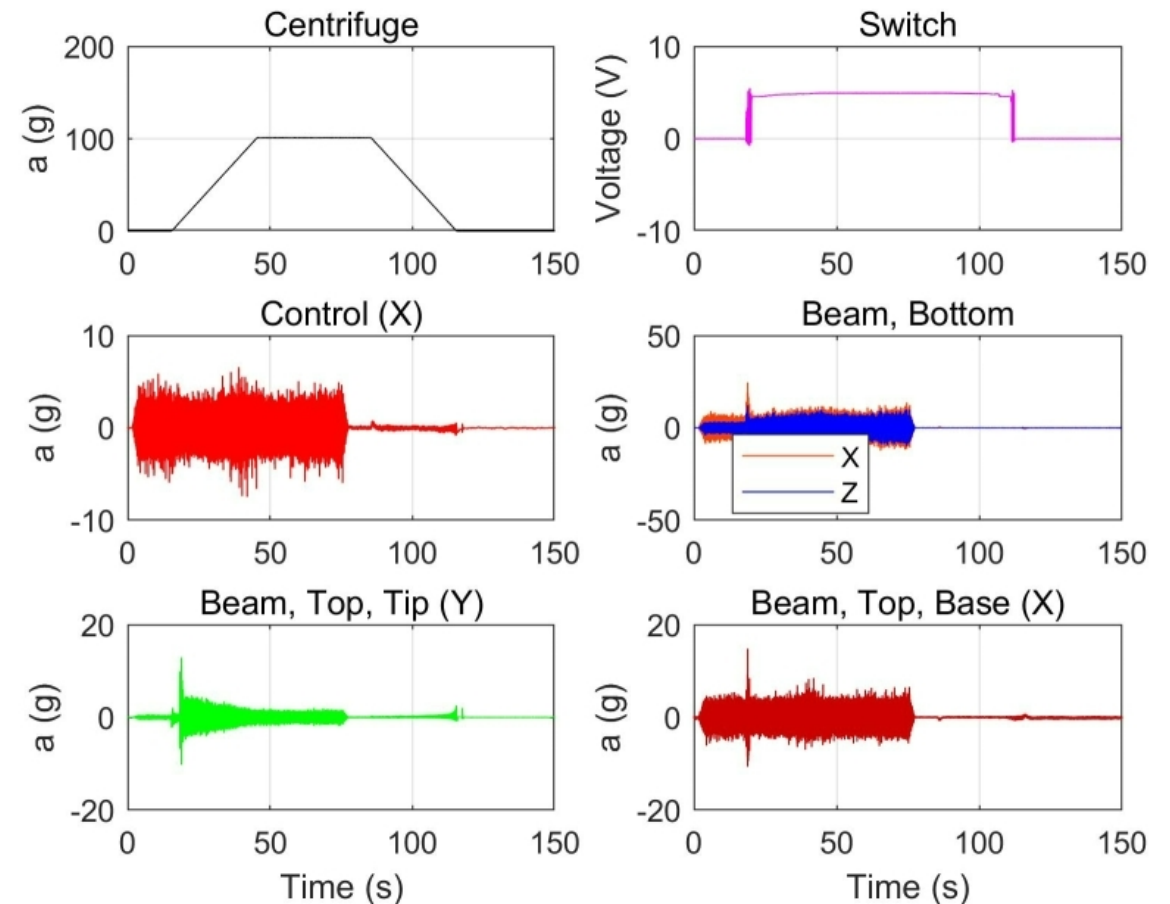
Test Mode	Description	Free-Free Modal Freq. (Hz)	Vibrafuge Modal 0G Freq. (Hz)	Vibrafuge APA 5G Freq. (Hz)	Vibrafuge APA 5G Freq. (Hz)	Free-Free Modal Damp (%)	Vibrafuge Modal 0G Damp. (%)	Vibrafuge APA 5G Damp. (%)	Vibrafuge APA 100G Damp. (%)
1	1 st Beam Vertical Bending	79	84	75.3	-	0.4	2.0	2.4	-
2	1 st Beam Lateral Bending	267	261	-	-	1.1	2.1	-	-
3	2 nd Beam Vertical Bending	616	623	623	-	2.1	3.3	3.2	-
4	3 rd Beam Vertical Bending	1784	1776	1788	1472.4	1.1	1.2	1.4	2.55

Frequency

Damping

Vibrafuge Testing

- Vibrafuge testing conducted with APA
 - 1 GRMS 50 to 2000 Hz
 - Range of acceleration from 5 to 100 G
- Vibration data measured at same accelerometers as modal testing
- Additional centrifuge acceleration profile
- Electrical contact measurement at beam tip
- Data used to validate FEM



100 G Vibrafuge Test Measurements

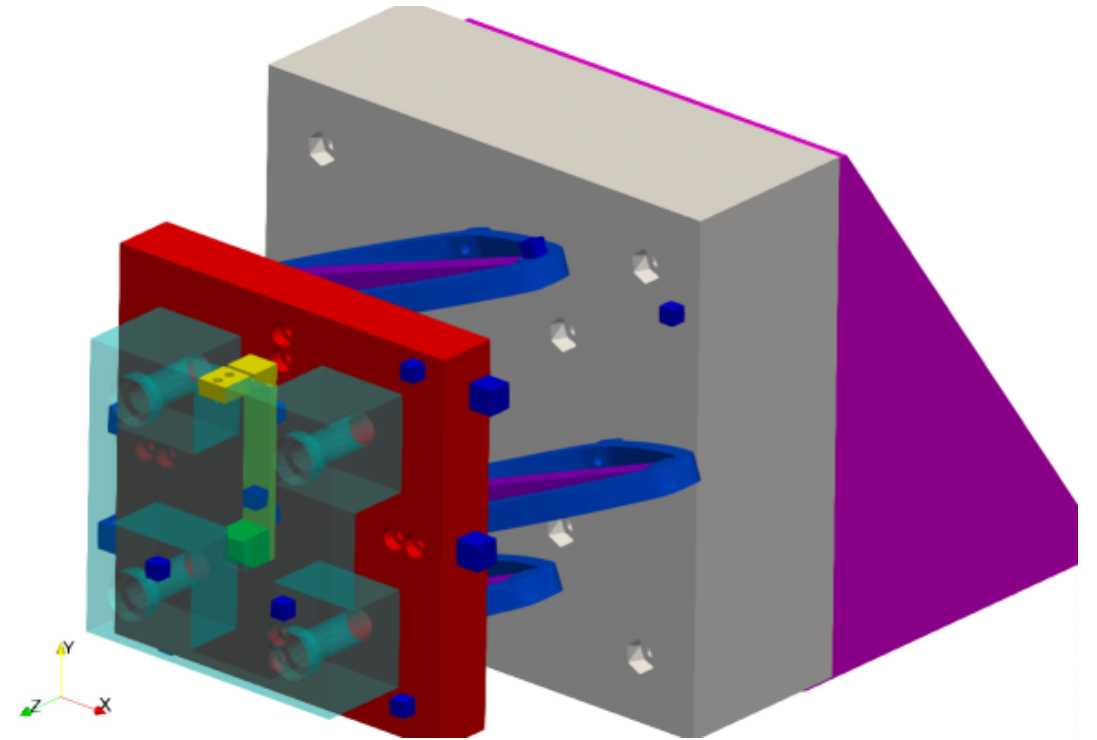


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Finite Element Analysis



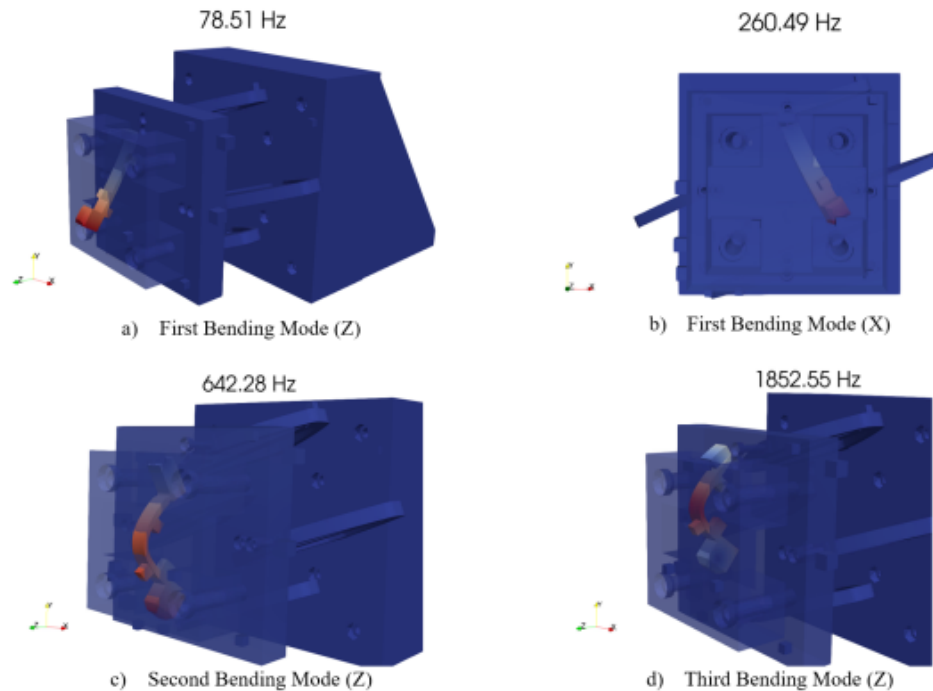
- FE modeling used to perform model calibration and validation
 - CUBIT meshing software and SIERRA codes
- Model assumptions
 - Elastic materials
 - Tied contact at joints/interfaces
 - Neglect rubber pads
- SIERRA Structural Dynamics used to perform initial calibration and updating to dial in modes and frequencies
- Followed by SIERRA Solid Mechanics preload analysis and handoff to SD
 - Coupled analysis used to pre-stress/stiffen cantilever beam and hand off state for a linearized modal analysis



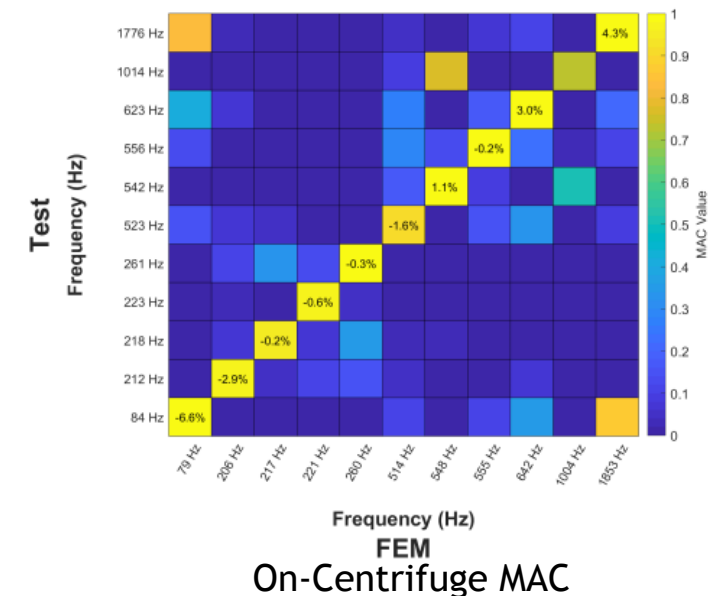
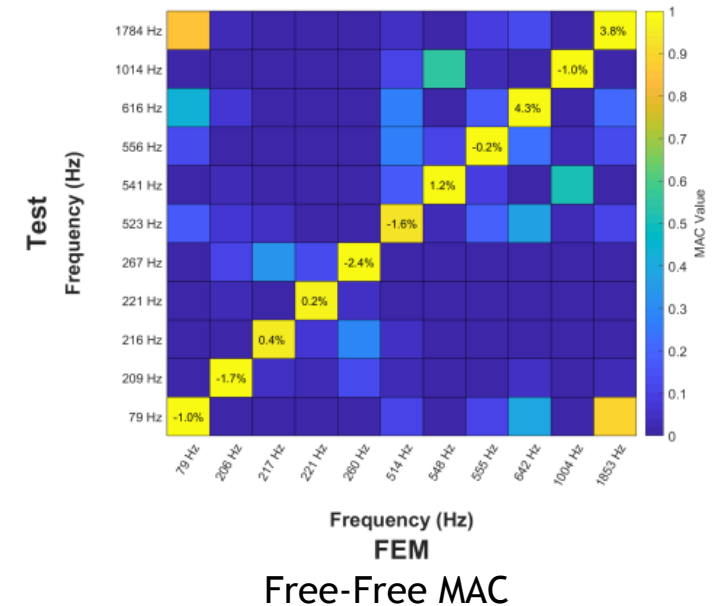
Vibrafuge Subassembly FEM

Modal Analysis

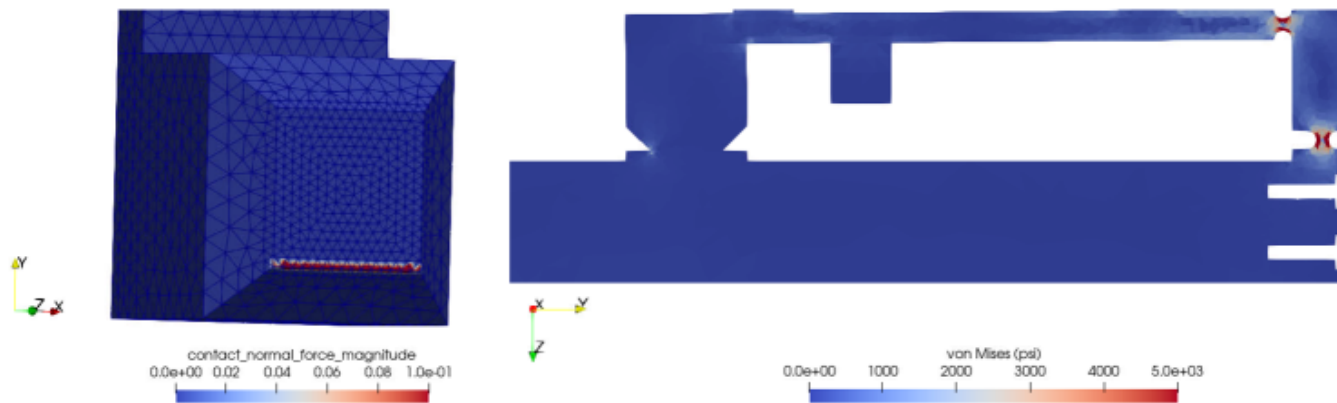
- Linear modal analysis using SIERRA/SD and model calibration with free-free test data
- Good match with frequency errors below 5% and MAC above 0.9
- Similar results for on-centrifuge (vibrafuge) data
 - Some discrepancies due to assumptions approximate boundary conditions



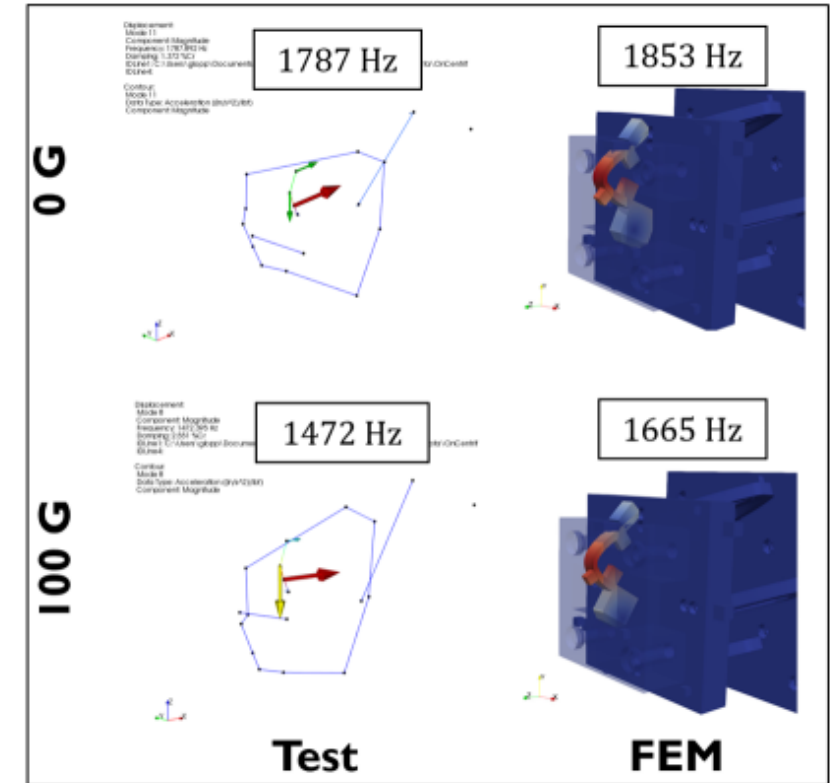
Free-Free Cantilever Beam Modes



- After initial model calibration, the handoff analysis was performed
- Preload analysis in SIERRA/SM to determine contact state and update element tangent stiffness matrices
- Automatic conversion to tied contact based on threshold for linear modal analysis in SIERRA/SD
- Handoff model able to account of updated contact state and effect on dynamics
 - Updated modes consistent with test data



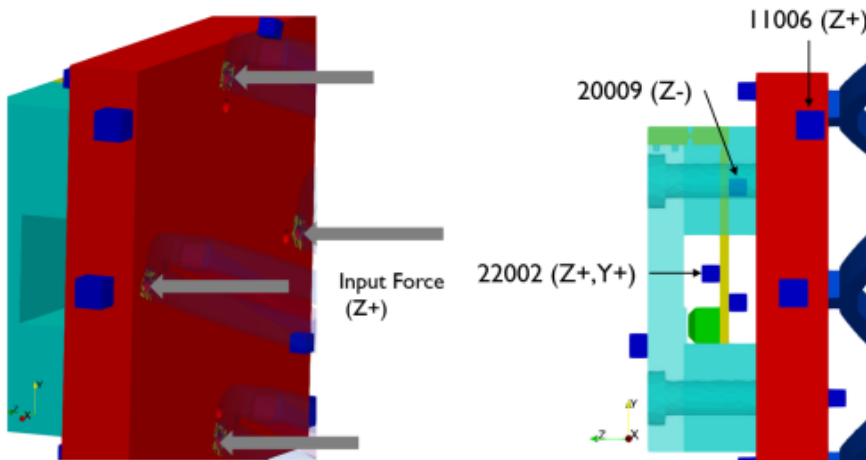
SIERRA/SM Preload Results



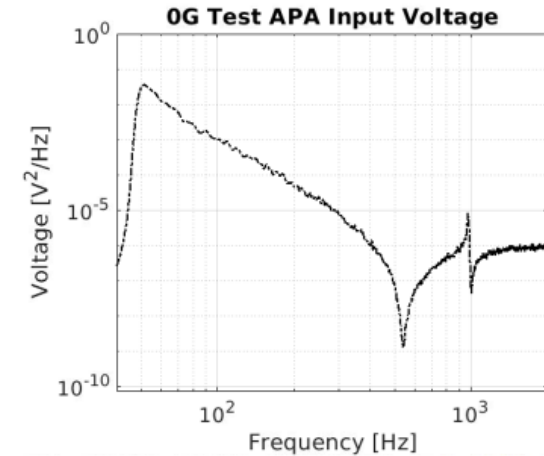
0 G and 100 G Comparison for 3rd Bending Mode

Random Vibration Analysis

- After model calibration and updated handoff model, random vibration analysis performed for same loading as testing
- Loading using input force at APAs
- Responses compared using 3 separate analysis approaches
 - Scale APA voltage
 - 1 DOF control
 - Estimate APA voltage transfer function
- These approaches highlight the discrepancies with test data and impact of modeling assumptions



Random vibration loading and response location



Method 1

$$S_{yy} = H_{yx} S_{xx} H_{yx}^H$$

Method 2

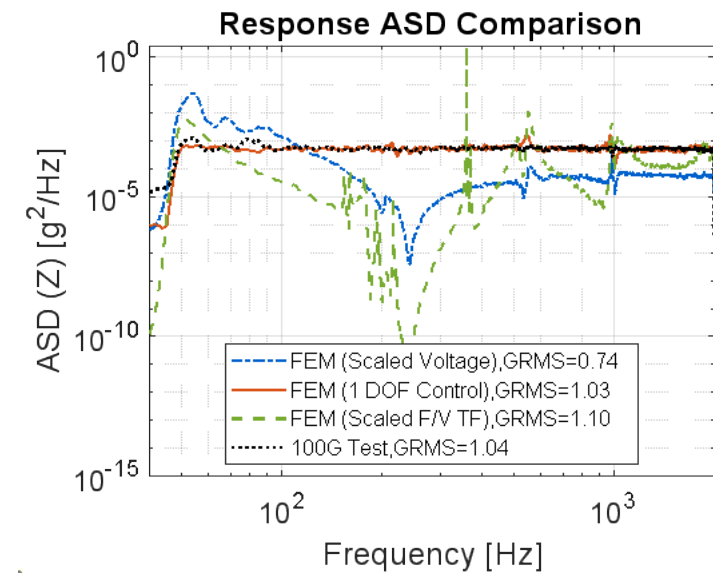
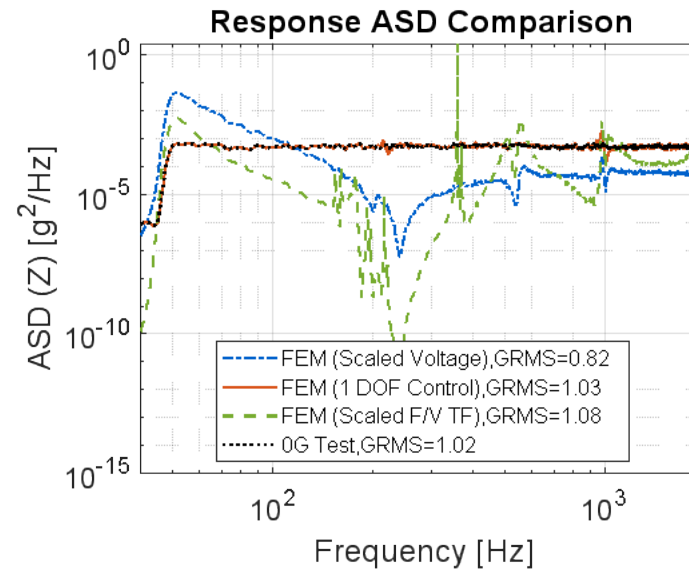
$$F_p = k_p^E (u_2 - u_1) - \alpha V$$

$$\alpha = nd_{33} k_p^E \quad k_p^E = \frac{Y_3^E A_p}{L_p} \quad \text{Method 3}$$

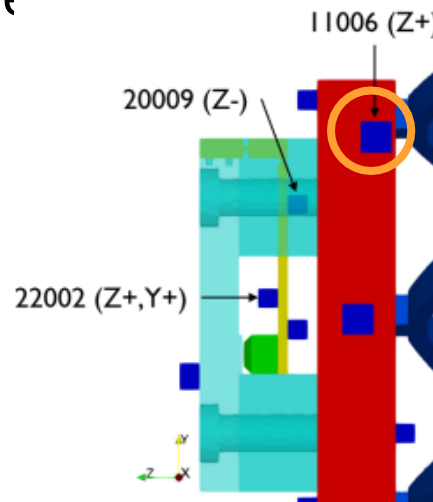
$$\frac{F_p}{V} = \frac{\alpha}{k_p^E \left(\frac{u_2}{F_p} - \frac{u_1}{F_p} \right) - 1}$$

Results- Control Accel

- 1 DOF Control (Method 2) matches control accelerometer exactly, as expected
- Computed APA FRF (Method 3) does better at some frequencies compared to scaled voltage (Method 1)
 - Still, both are poor matches
 - May be issues with FRF calculation causing discrepancies
- dB error high for methods 1 and 3 due to poor frequency match at certain bandwidths



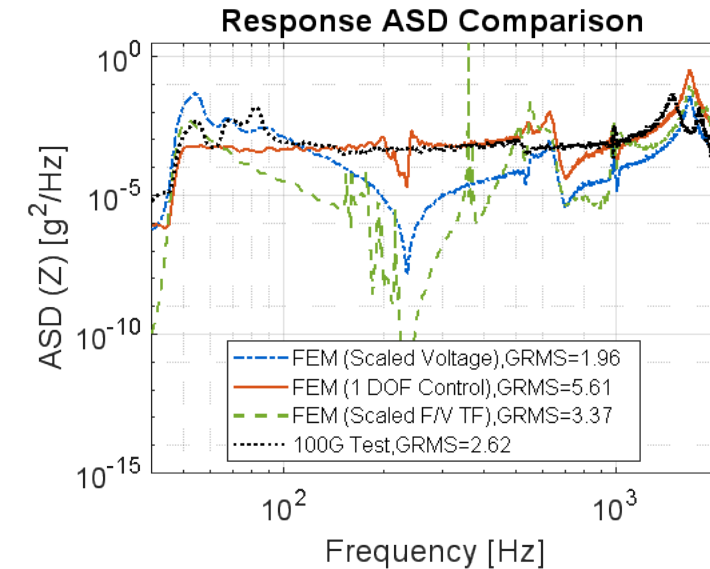
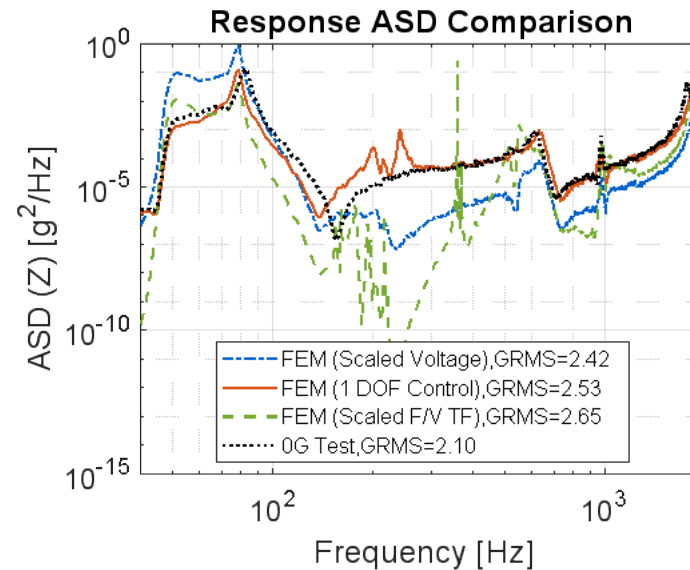
FEM/Test Comparison: Control Location 11006 (Z+)



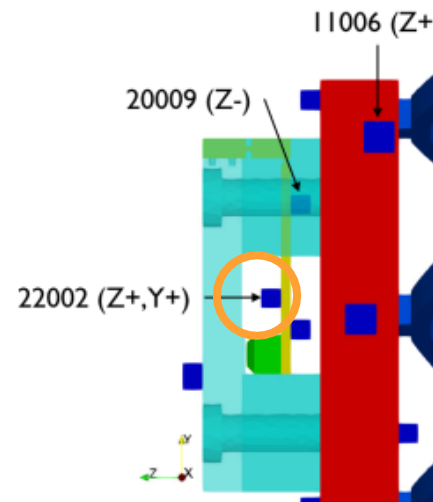
Case	Response GRMS	1/12 Oct Smoothed dB Error St. Dev.
0 G Test	1.02	-
0 G FEM Method 1	0.82	8.7
0 G FEM Method 2	1.03	0.2
0 G FEM Method 3	1.08	13.9
100 G Test	1.04	-
100 G FEM Method 1	0.74	8.3
100 G FEM Method 2	1.01	0.7
100 G FEM Method 3	1.10	13.9

Results- Mid-Beam

- 1 DOF Control (method 2) once again best match
 - General trends match, good GRMS
 - Able to capture mode shifting
- Again APA FRF (method3) does better at higher frequencies compared to scaled voltage (method 1) are quite different
- dB error high for methods 1 and 3 due to poor frequency match at certain bandwidths
- Ideally APA scaled transfer function would perform better since it incorporates additional physics
 - Assumptions and simplified equations may not be valid (neglected stack mass)
- Need to improve loads and BC, but this method is able to qualitatively match trends such as mode and



FEM/Test Comparison: Mid-Beam Location 22002 (Z+)

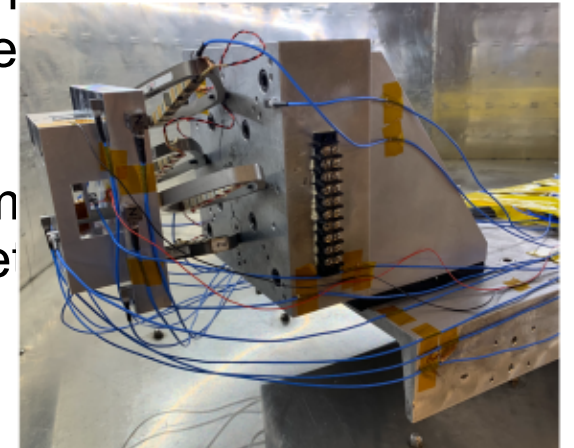


Case	Response GRMS	1/12 Oct Smoothed dB Error St. Dev.
0 G Test	2.10	-
0 G FEM Method 1	2.42	7.8
0 G FEM Method 2	2.53	3.6
0 G FEM Method 3	2.65	13.2
100 G Test	2.62	-
100 G FEM Method 1	1.96	8.0
100 G FEM Method 2	5.61	4.1
100 G FEM Method 3	3.37	14.5



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- Model validation was performed for a research structure subjected to combined inertial acceleration and vibration environments (vibrafuge)
 - SIERRA coupled analysis performed by preloading the structure, updating the contact state, and evaluating the altered structural response
 - Results validated with modal and vibrafuge testing using amplified piezoelectric actuators on a centrifuge
- Comparisons to test data showed that the handoff model accounts for the updated dynamic response
 - Mode frequency shift and elimination were observed under increased centrifuge acceleration
 - ASD trends consistent with test data, although the approximate BCs led to large errors in some frequency bands
- Modeling adjustments can improve the match to test data, but this work demonstrates the development of an improved approach for combined mechanical environment validation
- Future work can focus on improving model BC, adjusting the handoff parameters, further work on force-voltage TF, and inverse solution methods to obtain better input loading





- [1]D. Vangoethem, R. Jepsen, and E. Romero, "Vibrafuge: Re-entry and Launch Test Simulation in a Combined Linear Acceleration and Vibration Environment", 44th AIAA Aerospace Sciences Meeting and Exhibit. 9-12 January 2006, Reno, Nevada. DOI: 10.2514/6.2006-1318
- [2]B. C. Owens and J. M. Harvie, "Combined Mechanical Environments for Design and Qualification", IMAC XXXVI, 12-15 February 2018, Orlando, Florida. doi:10.1007/978-3-319-74700-2_16.
- [3]M. T. Merewether, N. K. Crane, G. J. de Frias, S. Le, D. J. Littlewood, M. D. Mosby, K. H. Pierson, V. L. Porter, T. Shelton, J. D. Thomas, M. R. Tupek, M. Veilleux, S. Gampert, P. G. Xavier, & J. A. Plews, "Sierra/Solid Mechanics 4.48 User's Guide", United States. <https://doi.org/10.2172/1433781>. SAND-2018-2961.
- [4]N. K. Crane, D. M. Day, S. Hardesty, P. Lindsay, and B. L. Stevens, "Sierra/SD - User's Manual - 4.56", United States: n. p., 2020. doi:10.2172/1673458. SAND2020-3828.
- [5]"Cedrat Technologies, Innovation in Mechatronics." Amplified Piezo Actuators, <https://cedrat-technologies.com/en/products/actuators/apa.html>.
- [6]G. K. Lopp, D. M. Siler, M. Khan, and B. C. Owens, "Modal Testing with Piezoelectric Stack Actuators", Paper to be presented at IMAC XL, 7-10 February 2022, Orlando, Florida.
- [7]CUBIT Development Team, CUBIT Geometry and Mesh Generation Toolkit 15.8 User Documentation, 2021, SAND2021-5152 W.



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