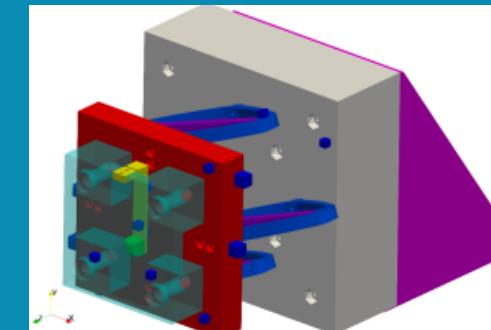
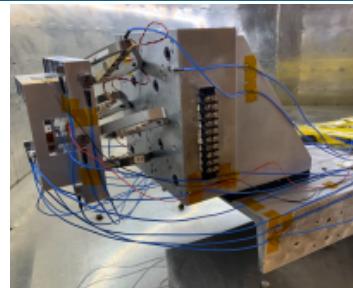
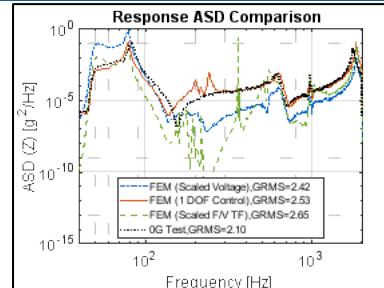
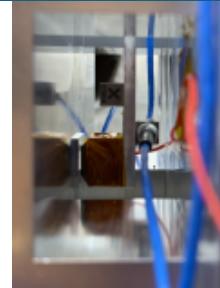




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# Model Validation for Combined Inertial Acceleration and Vibration Environments



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Brian C. Owens

*PRESENTED BY*

Moheimin Khan

IMAC-XL

February 7-10, 2022

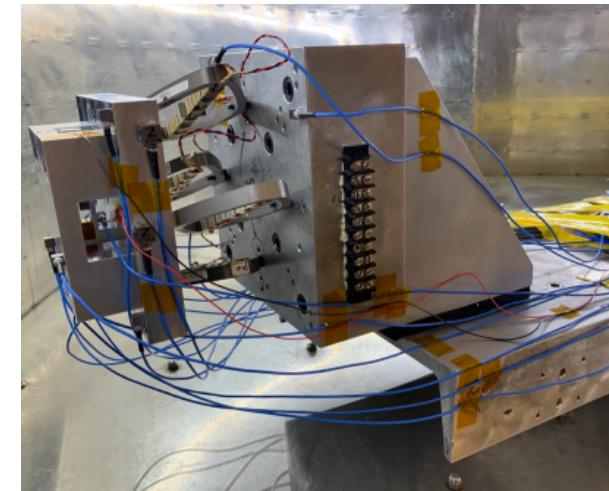
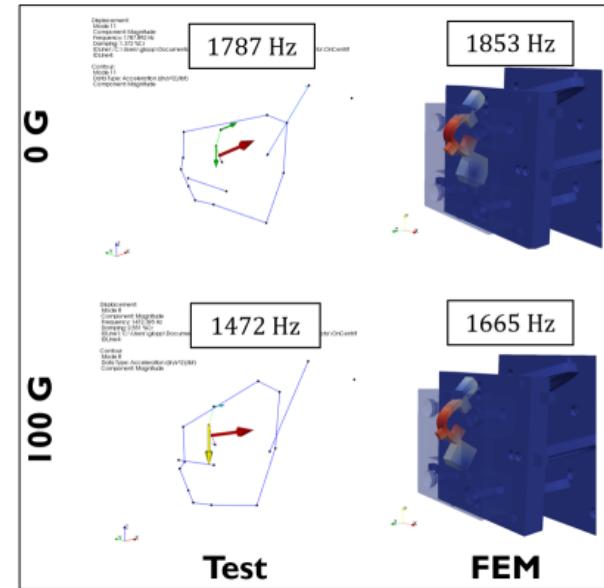
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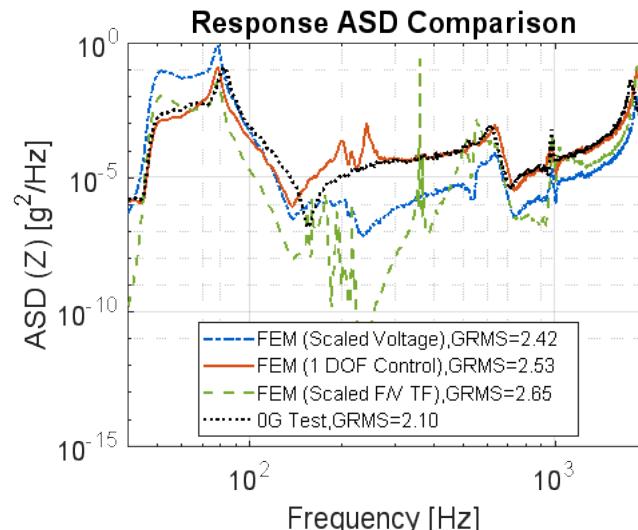
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# Summary

- Model validation was performed for a research structure subjected to combined inertial acceleration and vibration environments (vibrafuge)
- SIERRA coupled analysis was conducted to evaluate the effect of centrifuge acceleration combined with random vibration
  - Preloading the cantilever beam structure using SIERRA/SM
  - Updating the contact state, and evaluating the preloaded response using SIERRA/SD
- Results were validated with vibrafuge testing using piezoelectric actuators on a centrifuge
  - Comparisons to test data showed that the SM to SD handoff model was able to account for the updated dynamic response due to the inertial acceleration preload
  - Validation metrics were computed to quantify comparisons between model and test data
- This work demonstrates the development of an improved approach for combined mechanical environments analysis and model validation using SIERRA

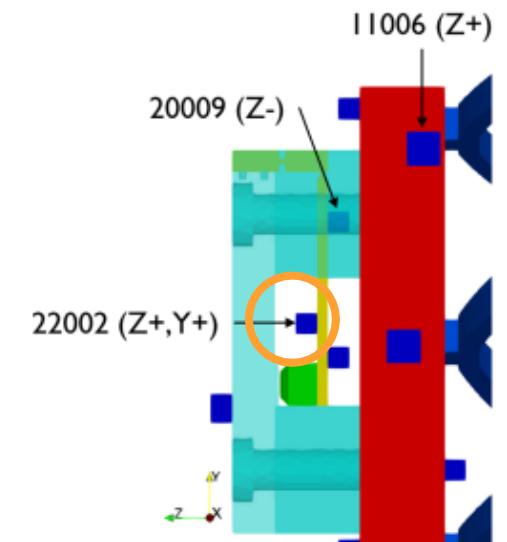


3rd Bending Mode- 0/100 G Comparison



Acceleration Response Results and Location

Test Article Vibrafuge Setup



# Outline



## I. Introduction/Overview

- A. Unit Description
- B. Setup

## II. Experimental Characterization

- A. Modal Testing
- B. Vibrafuge Testing

## III. FE Modeling and Calibration

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- C. Random Vibration Analysis

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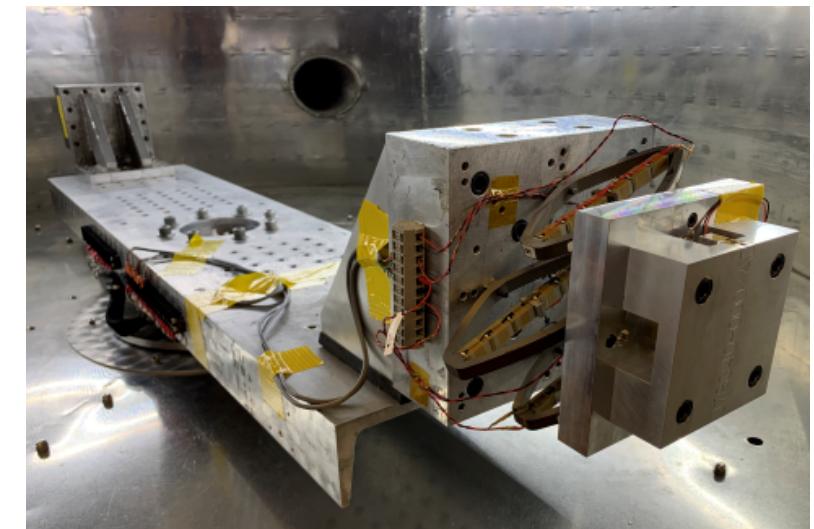
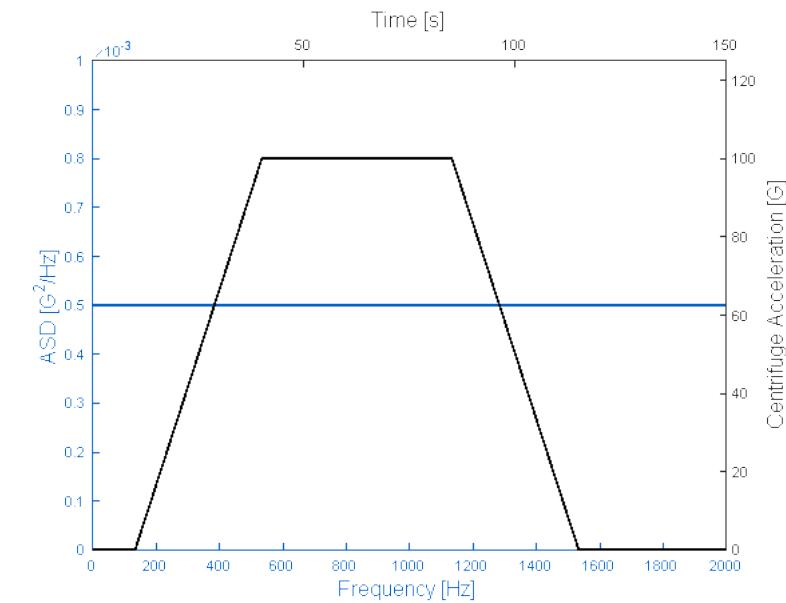
## IV. Conclusion

# Introduction



- Aerospace structures are often subjected to combined inertial acceleration and vibration environments during operation
- Traditional test approaches independently assess a system under a sequence of inertial and vibration environments
  - Incapable of addressing couplings in system response under combined environments
- Considering combined environments throughout the design and qualification of a system requires development of both analytical and experimental capabilities
- Recent ground testing efforts have improved the ability to replicate flight conditions and aid qualification by incorporating combined centrifuge acceleration and vibration environments in a **vibrafuge** test
  - Modeling these loading conditions involves the coupling of multiple physical phenomena to accurately capture dynamic behavior

Combined Acceleration and Vibration Environments



Vibrafuge Setup

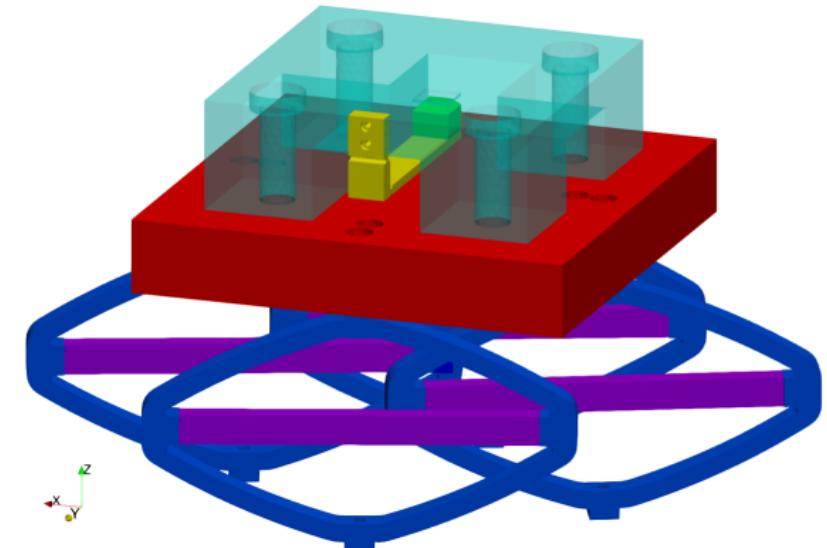
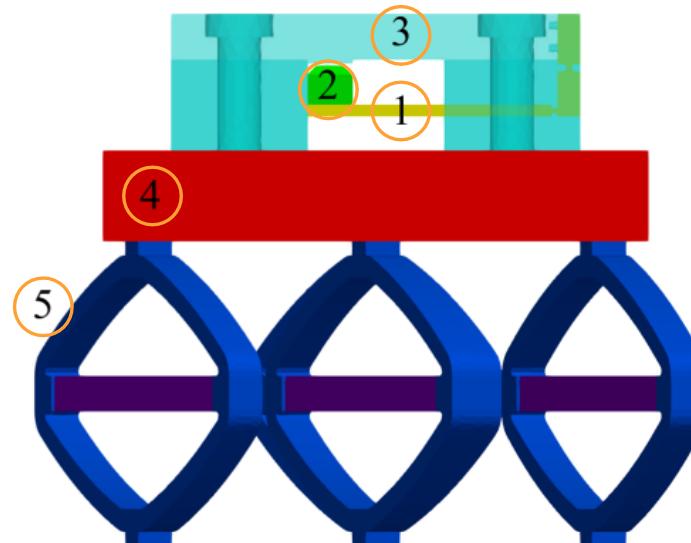
# Unit Description



- Vibrafuge capability demonstrated with research structure
  - Applied acceleration on centrifuge
  - Vibration using Cedrat Technologies APA230L amplified piezoelectric actuators (APA)
- Consists of an inverted cantilever beam
  - Functions as simple acceleration switch
  - Goal to study dynamics as tip contact state changes under vibrafuge environment
- Assembly consists of the following
  1. Aluminum beam
  2. Tungsten mass
  3. Aluminum support block
  4. Aluminum base block
  5. Piezoelectric actuators



Cantilever Beam Geometry

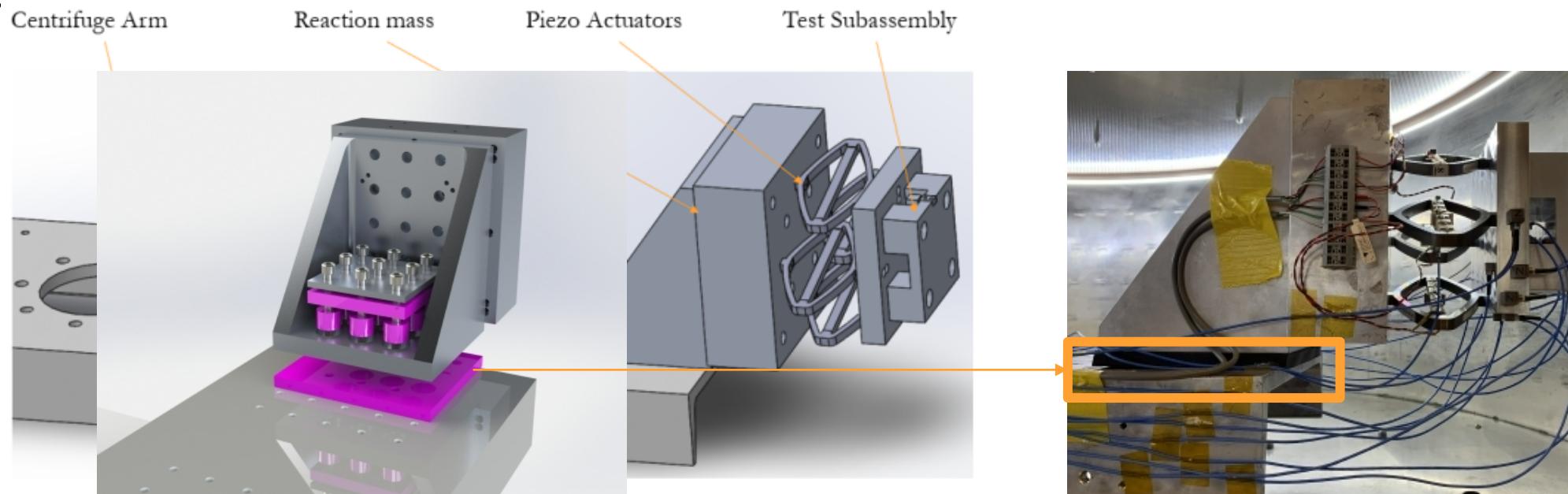


Test Subassembly

# Vibrafuge Setup



- Combined inertial acceleration and vibration environments simulated using “vibrafuge” setup
  - Cantilever beam assembly and APA fixtured on centrifuge arm with reaction mass and angle bracket
- Test setup allows for dynamic characterization under simultaneous environments
  - Instrumentation set up through slip rings and routed to external controller and data acquisition
- Additional polyurethane rubber sheets and rounds used to isolate APA vibration to



Vibrafuge Description and Test Setup

# Outline



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## III. FE Modeling and Calibration

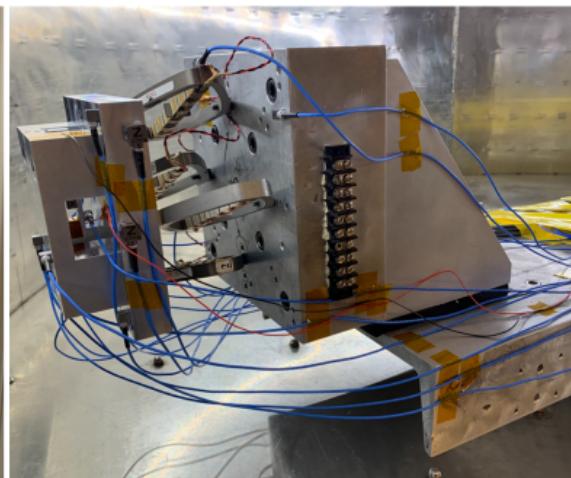
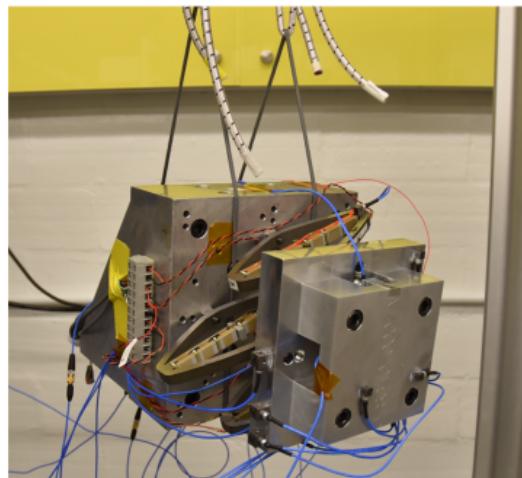
- A. Modal Analysis
- B. Code Coupling/Handoff Procedure
- C. Random Vibration Analysis

## IV. Conclusion

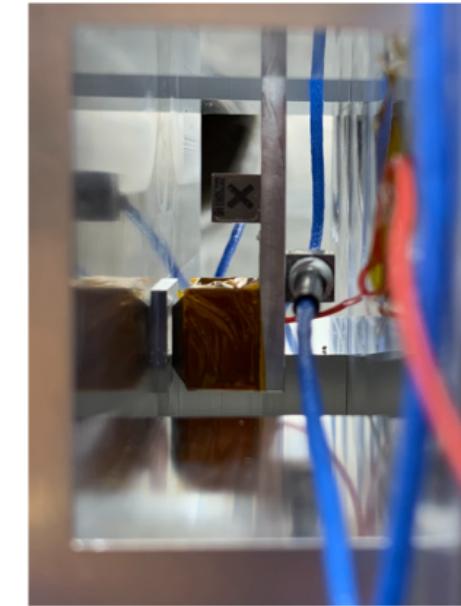
# 9 Modal Testing



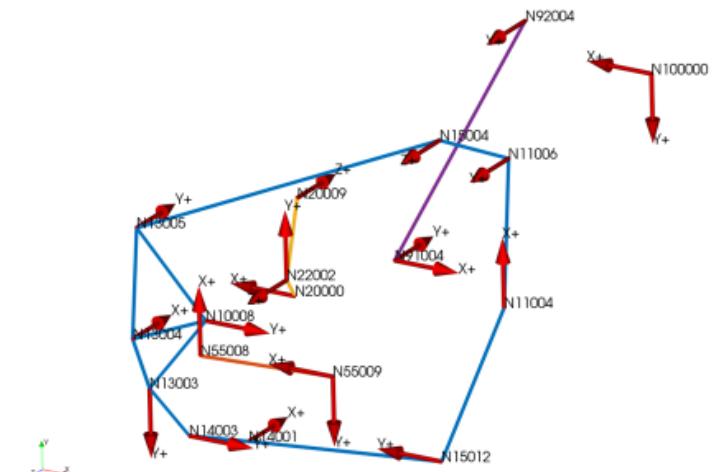
- Instrumentation designed to capture modes of interest
  - 18 accelerometers, 22 DOF total
- Modal testing performed in free-free and centrifuge boundary conditions
  - To evaluate effect of fixturing
- APAs also used to extract modal parameters during centrifuge testing
  - Modes and frequencies evaluated at various G-levels
  - Data used to later validate FE model



Modal Test Setup



Beam Tip Instrumentation Closeup



# Modal Testing- Results



Test Mode	Description	Free-Free Modal Freq. (Hz)	Vibrafuge Modal 0G Freq. (Hz)	Vibrafuge APA 5G Freq. (Hz)	Vibrafuge APA 5G Freq. (Hz)	Free-Free Modal Damp (%)	Vibrafuge Modal 0G Damp. (%)	Vibrafuge APA 5G Damp. (%)	Vibrafuge APA 100G Damp. (%)
1	1 <sup>st</sup> Beam Vertical Bending	79	84	75.3	-	0.4	2.0	2.4	-
2	1 <sup>st</sup> Beam Lateral Bending	267	261	-	-	1.1	2.1	-	-
3	2 <sup>nd</sup> Beam Vertical Bending	616	623	623	-	2.1	3.3	3.2	-
4	3 <sup>rd</sup> Beam Vertical Bending	1784	1776	1788	1472.4	1.1	1.2	1.4	2.55

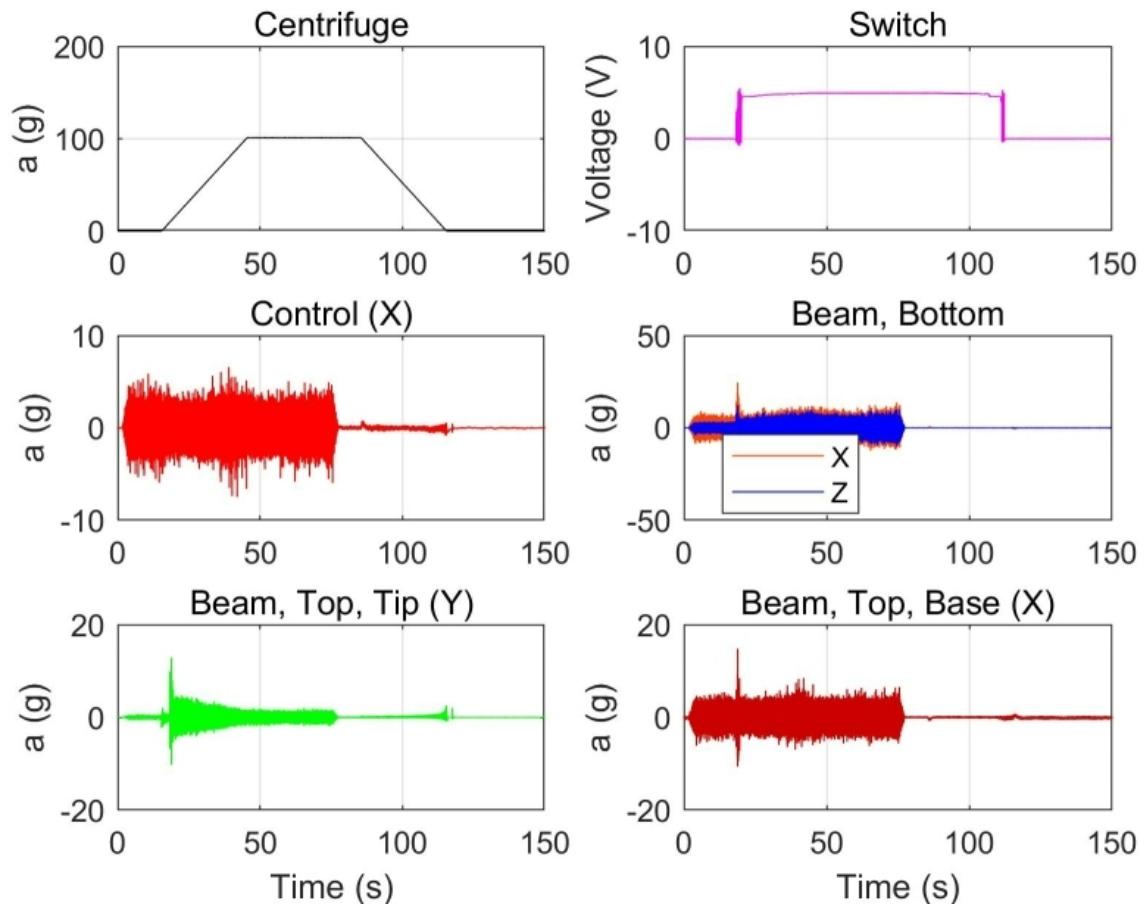
Frequency

Damping

# Vibrafuge Testing



- Vibrafuge testing conducted with APA
  - 1 GRMS 50 to 2000 Hz
  - Range of acceleration from 5 to 100 G
- Vibration data measured at same accelerometers as modal testing
- Additional centrifuge acceleration profile
- Electrical contact measurement at beam tip
- Data used to validate FEM



100 G Vibrafuge Test Measurements

# Outline

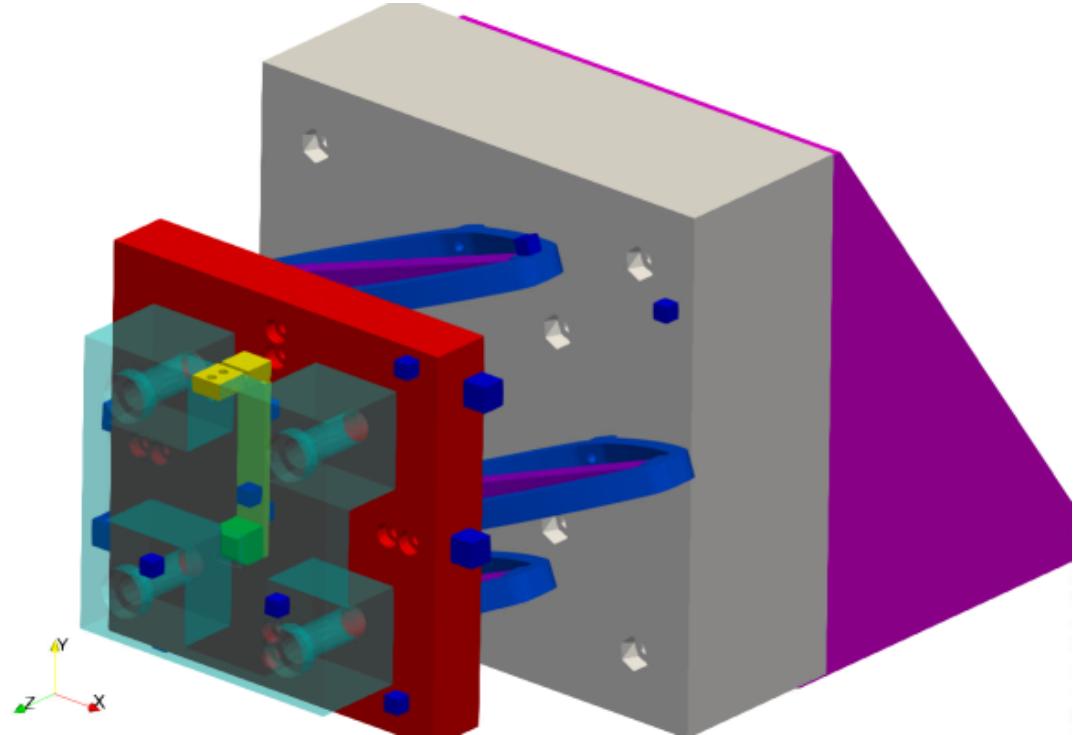


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# Finite Element Analysis



- FE modeling used to perform model calibration and validation
  - CUBIT meshing software and SIERRA codes
- Model assumptions
  - Elastic materials
  - Tied contact at joints/interfaces
  - Neglect rubber pads
- SIERRA Structural Dynamics used to perform initial calibration and updating to dial in modes and frequencies
- Followed by SIERRA Solid Mechanics preload analysis and handoff to SD
  - Coupled analysis used to pre-stress/stiffen cantilever beam and hand off state for a linearized modal analysis



Vibrafuge Subassembly FEM

- Linear modal analysis using SIERRA/SD and model calibration with free-free test data
- Good match with frequency errors below 5% and MAC above 0.9
- Similar results for on-centrifuge (vibrafuge) data

- Some conclusions

A 3D finite element model of a mechanical assembly, likely a mold or frame, shown in a blue color scheme. A red component is attached to the left side. A green coordinate system (x, y, z) is visible in the bottom left corner.

a) First Bending Mode (Z)

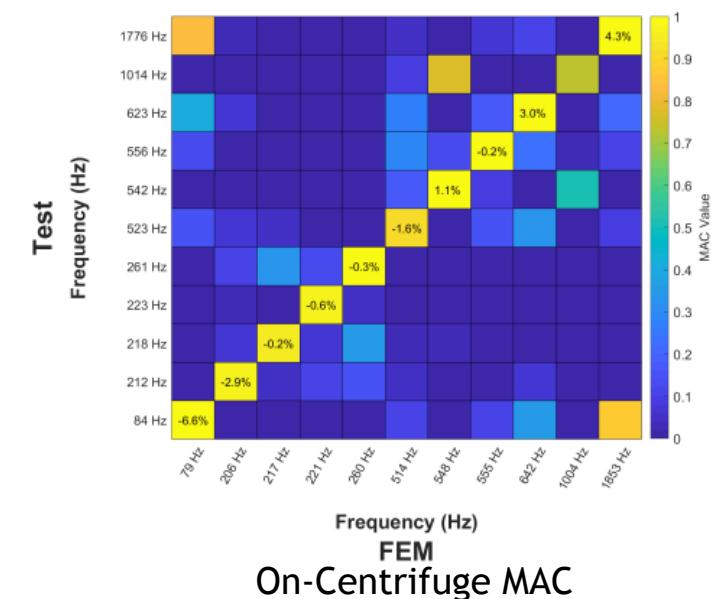
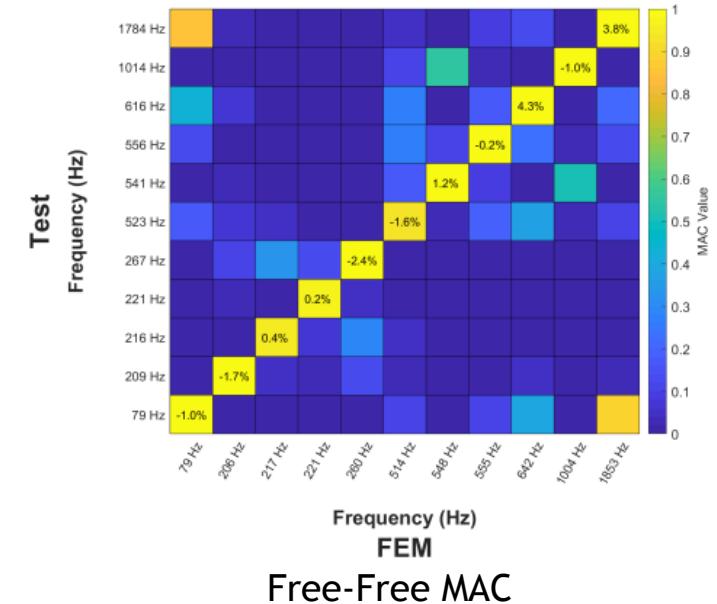
mate boundary

b) First Bending Mode (X)

c) Second Bending Mode (Z)

A 3D finite element model of a mechanical part, likely a bracket or frame, is shown in a dark blue color. A red arrow indicates a specific vibration mode or displacement direction within the model. A small coordinate system icon is visible in the bottom left corner.

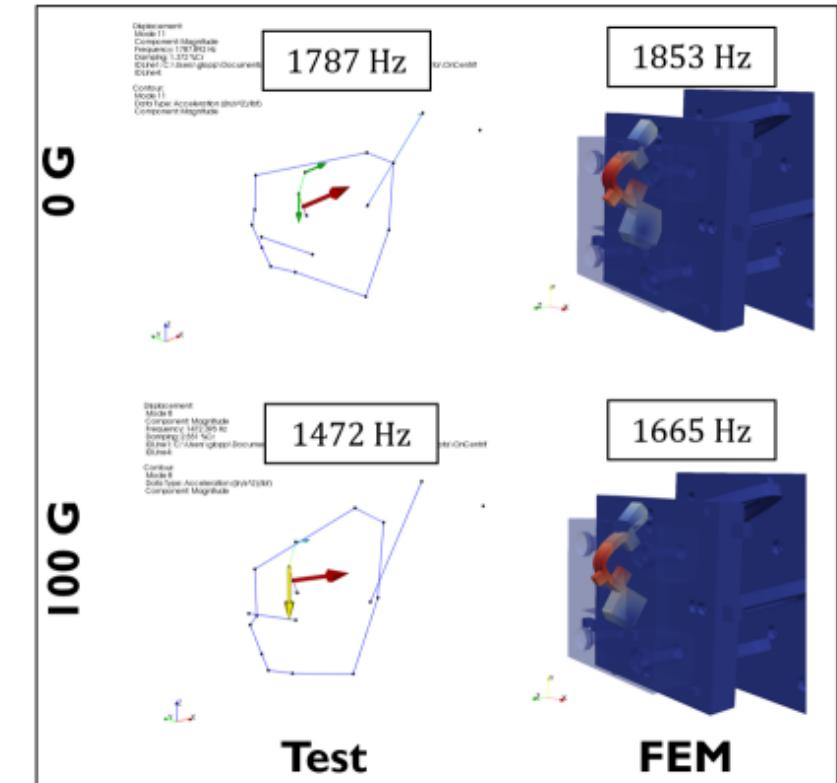
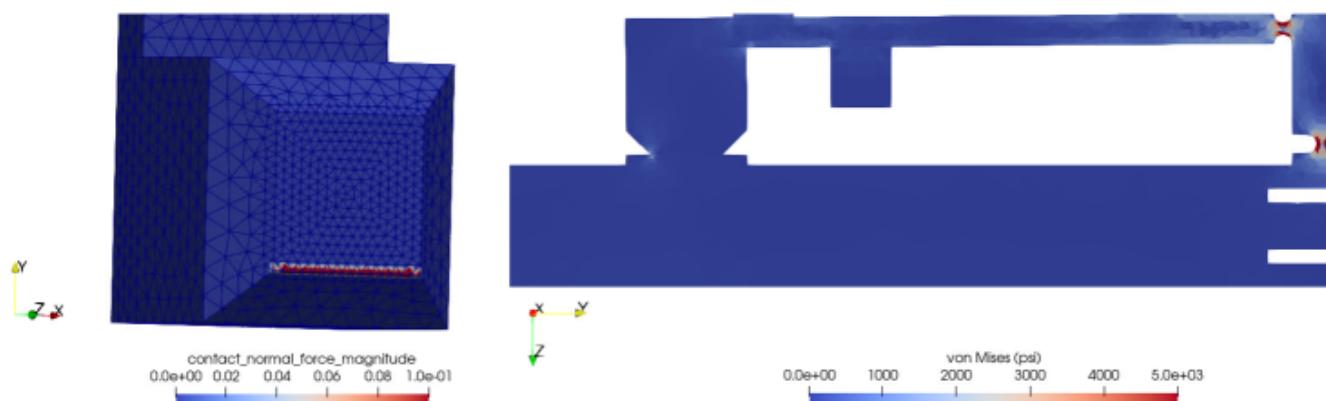
#### d) Third Bending



# Code Coupling / Handoff



- After initial model calibration, the handoff analysis was performed
- Preload analysis in SIERRA/SM to determine contact state and update element tangent stiffness matrices
- Automatic conversion to tied contact based on threshold for linear modal analysis in SIERRA/SD
- Handoff model able to account of updated contact state and effect on dynamics
  - Updated modes consistent with test data

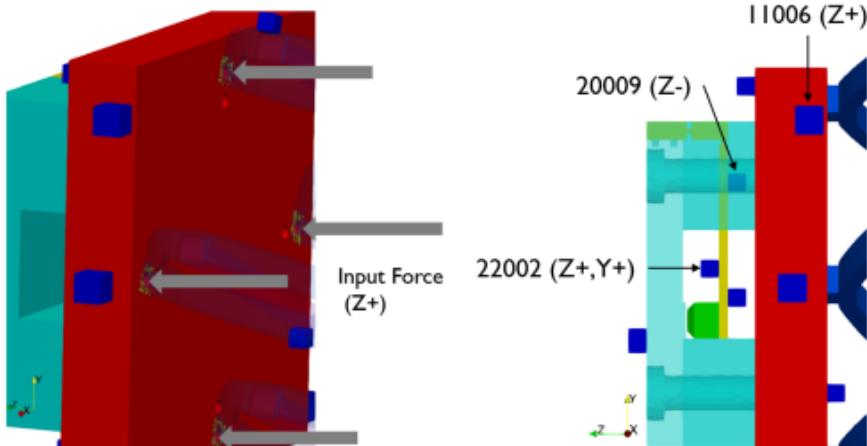


0 G and 100 G Comparison for 3rd Bending Mode

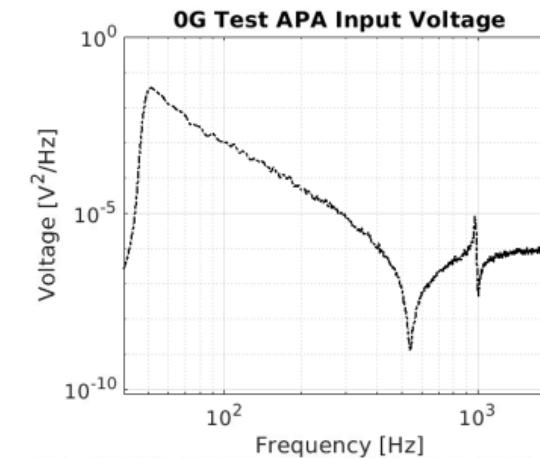
# Random Vibration Analysis



- After model calibration and updated handoff model, random vibration analysis performed for same loading as testing
- Loading using input force at APAs
- Responses compared using 3 separate analysis approaches
  - Scale APA voltage
  - 1 DOF control
  - Estimate APA voltage transfer function
- These approaches highlight the discrepancies with test data and impact of modeling assumptions



Random vibration loading and response location



Method 1

$$S_{yy} = H_{yx} S_{xx} H_{yx}^H$$

Method 2

$$F_p = k_p^E (u_2 - u_1) - \alpha V$$

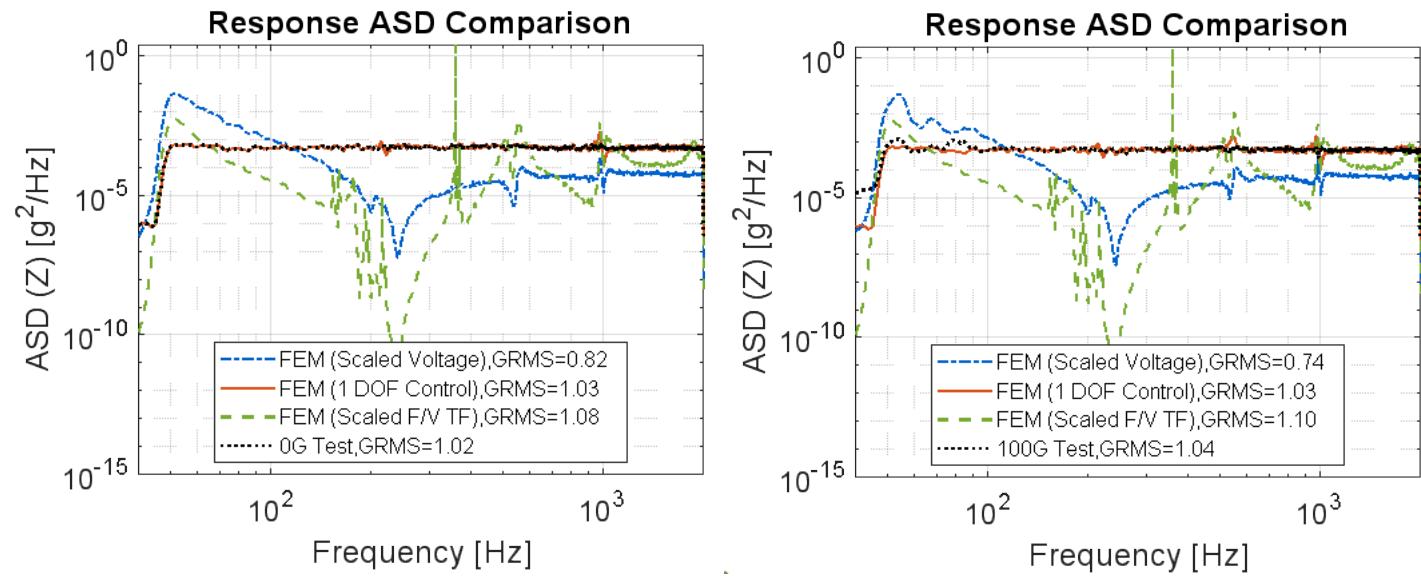
$$\alpha = n d_{33} k_p^E \quad k_p^E = \frac{Y_3^E A_p}{L_p} \quad \text{Method 3}$$

$$\frac{F_p}{V} = \frac{\alpha}{k_p^E \left( \frac{u_2}{F_p} - \frac{u_1}{F_p} \right) - 1}$$

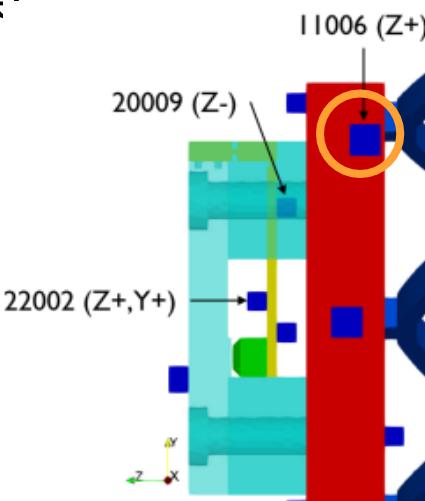
# Results- Control Accel



- 1 DOF Control (Method 2) matches control accelerometer exactly, as expected
- Computed APA FRF (Method 3) does better at some frequencies compared to scaled voltage (Method 1)
  - Still, both are poor matches
  - May be issues with FRF calculation causing discrepancies
- dB error high for methods 1 and 3 due to poor frequency match at certain bandwidths



FEM/Test Comparison: Control Location 11006 (Z+)

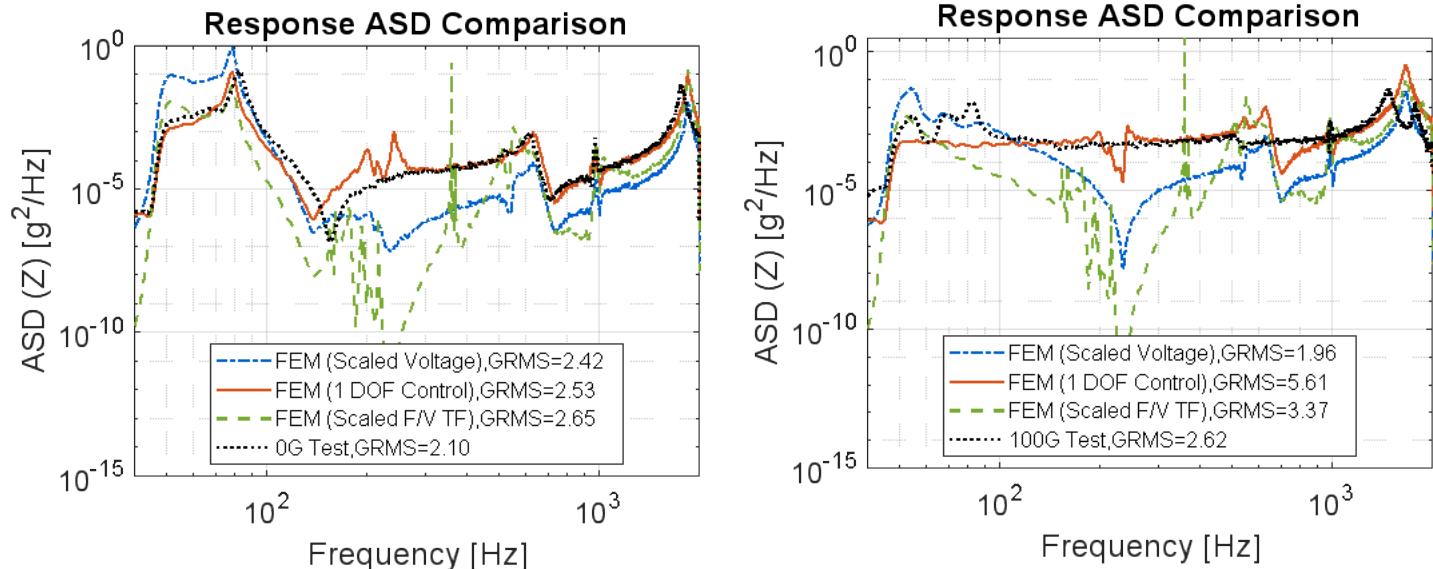


Case	Response GRMS	1/12 Oct Smoothed dB Error St. Dev.
0 G Test	1.02	-
0 G FEM Method 1	0.82	8.7
0 G FEM Method 2	1.03	0.2
0 G FEM Method 3	1.08	13.9
100 G Test	1.04	-
100 G FEM Method 1	0.74	8.3
100 G FEM Method 2	1.01	0.7
100 G FEM Method 3	1.10	13.9

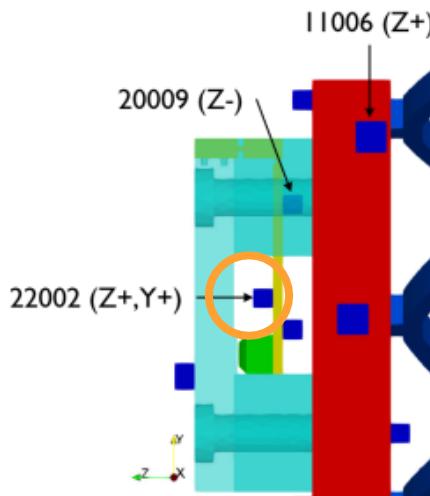
# Results- Mid-Beam



- 1 DOF Control (method 2) once again best match
  - General trends match, good GRMS
  - Able to capture mode shifting
- Again APA FRF (method3) does better at higher frequencies compared to scaled voltage (method 1) are quite different
- dB error high for methods 1 and 3 due to poor frequency match at certain bandwidths
- Ideally APA scaled transfer function would perform better since it incorporates additional physics
  - Assumptions and simplified equations may not be valid (neglected stack mass)
- Need to improve loads and BC, but this method is able to qualitatively match trends such as mode and



FEM/Test Comparison: Mid-Beam Location 22002 (Z+)



Case	Response GRMS	1/12 Oct Smoothed dB Error St. Dev.
0 G Test	2.10	-
0 G FEM Method 1	2.42	7.8
0 G FEM Method 2	2.53	3.6
0 G FEM Method 3	2.65	13.2
100 G Test	2.62	-
100 G FEM Method 1	1.96	8.0
100 G FEM Method 2	5.61	4.1
100 G FEM Method 3	3.37	14.5

# Outline

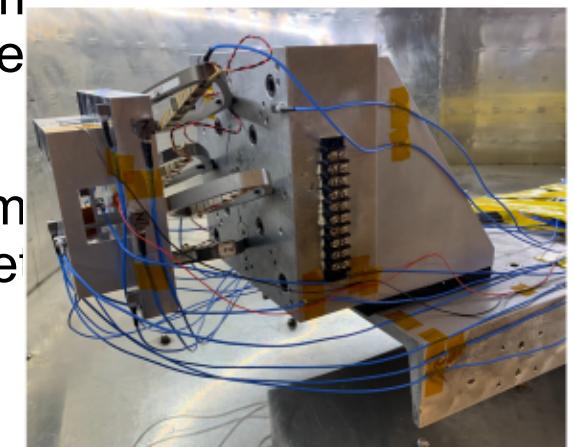


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# Conclusion



- Model validation was performed for a research structure subjected to combined inertial acceleration and vibration environments (vibrafuge)
  - SIERRA coupled analysis performed by preloading the structure, updating the contact state, and evaluating the altered structural response
  - Results validated with modal and vibrafuge testing using amplified piezoelectric actuators on a centrifuge
- Comparisons to test data showed that the handoff model accounts for the updated dynamic response
  - Mode frequency shift and elimination were observed under increased centrifuge acceleration
  - ASD trends consistent with test data, although the approximate BCs led to large errors in some frequency bands
- Modeling adjustments can improve the match to test data, but this work demonstrates the development of an improved approach for combined mechanical environment validation
- Future work can focus on improving model BC, adjusting the handoff parameters, further work on force-voltage TF, and inverse solution methods to obtain better input loading



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- [7] CUBIT Development Team, CUBIT Geometry and Mesh Generation Toolkit 15.8 User Documentation, 2021, SAND2021-5152 W.



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